Ray Tracing

Ray Tracing 1

- Basic algorithm
- **■** Overview of pbrt
- Ray-surface intersection (triangles, ...)

Ray Tracing 2

- Problem: brute force = |Image| x |Objects|
- Acceleration data structures

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Primitives

pbrt primitive base class

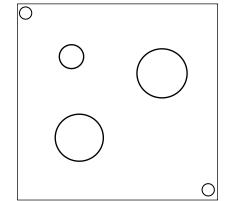
- Shape
- Material (reflection and emission)

Subclasses

- **■** Primitive instance
 - Transformation and pointer to a primitive
- Aggregate (collection)
 - Treat collections just like single primitives
 - Incorporate acceleration structures into collections
 - May nest accelerators of different types
 - Types: grid.cpp and kdtree.cpp

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Uniform Grids



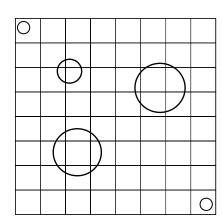
Preprocess scene

1. Find bounding box

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Uniform Grids



Preprocess scene

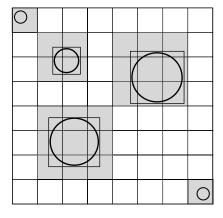
- 1. Find bounding box
- 2. Determine resolution

$$n_v = n_x n_y n_z \propto n_o$$

$$\max(n_x, n_y, n_z) = d\sqrt[3]{n_o}$$

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Uniform Grids



Preprocess scene

- 1. Find bounding box
- 2. Determine resolution

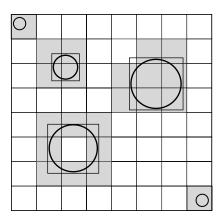
$$\max(n_x, n_y, n_z) = d\sqrt[3]{n_o}$$

3. Place object in cell, if object overlaps cell

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Uniform Grids



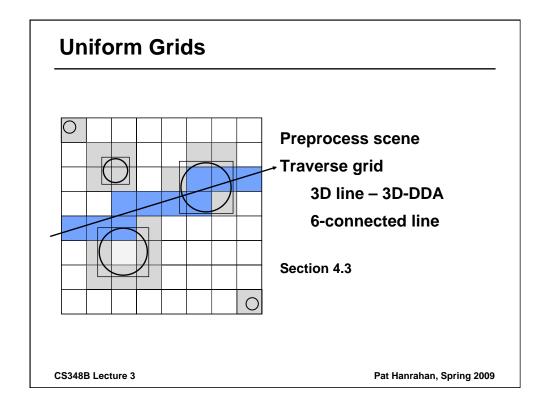
Preprocess scene

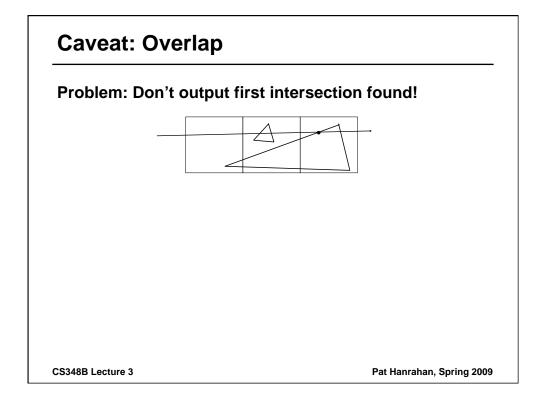
- 1. Find bounding box
- 2. Determine resolution

$$\max(n_x, n_y, n_z) = d\sqrt[3]{n_o}$$

- 3. Place object in cell, if object overlaps cell
- 4. Check that object's surface intersects cell

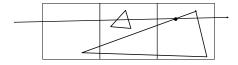
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Caveat: Overlap

Problem: Don't output first intersection found!



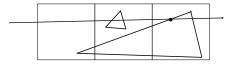
Problem: Redundant intersection tests

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Caveat: Overlap

Problem: Don't output first intersection found!



Problem: Redundant intersection tests

Solution: Mailboxes

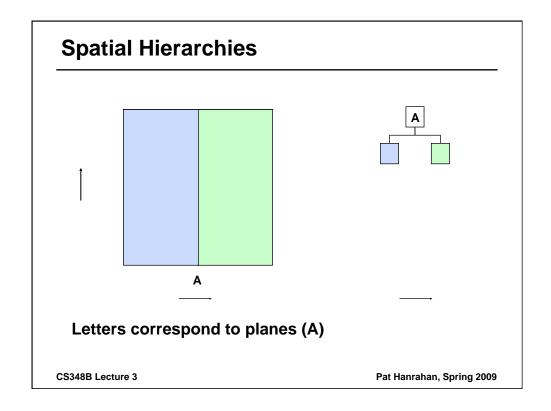
■ Assign each ray an increasing number

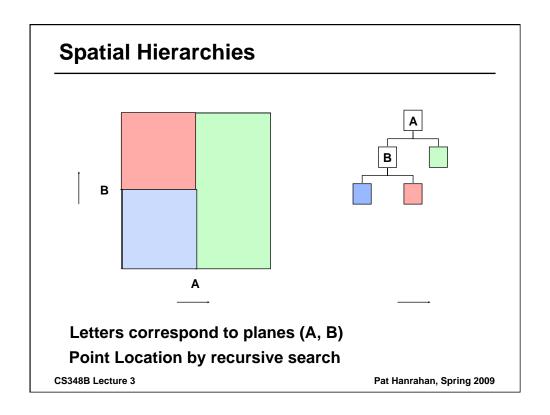
■ Primitive intersection cache (mailbox)

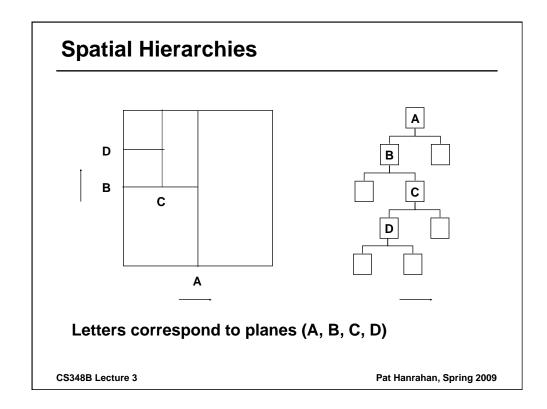
■ Store last ray number tested in mailbox

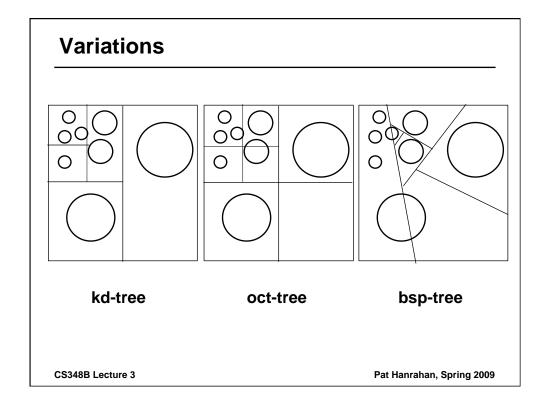
■ Only intersect if ray number is greater

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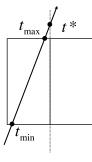


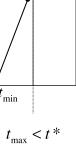
Ray Traversal Algorithms

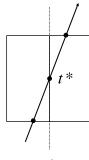
Recursive inorder traversal

[Kaplan, Arvo, Jansen]

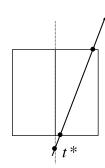
$$t^* = (S - \mathbf{O}[a]) / \mathbf{D}[a]$$







 $t_{\rm min} < t^* < t_{\rm max}$



 $t^* < t_{\min}$

Intersect(L,tmin,tmax)

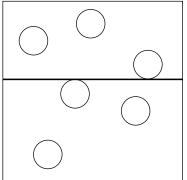
Intersect(L,tmin,t*) Intersect(R,t*,tmax)

Intersect(R,tmin,tmax)

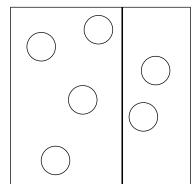
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How to Build the Hierarchy?

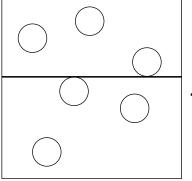


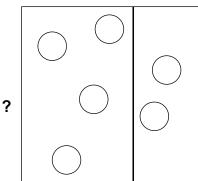
?



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Build Hierarchy Top-Down





Methods to choose axis and splitting plane

- Midpoint
- Median cut (balanced)
- Surface area heuristic

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Cost

What is the cost of tracing a ray through a node?

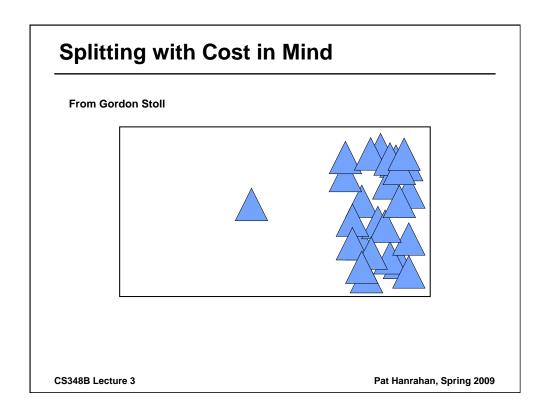
 $Cost(node) = C_{trav} + Prob(hit L) * Cost(L) + Prob(hit R) * Cost(R)$

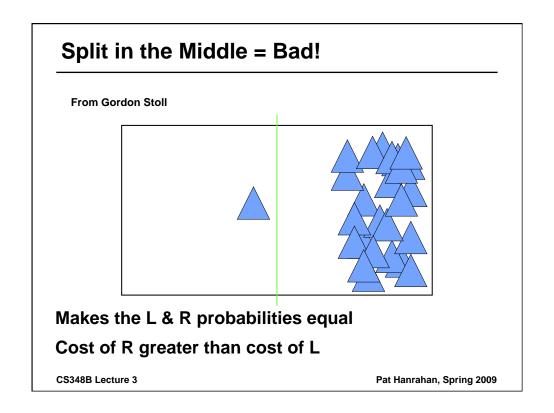
C_trav = cost of traversing a cell

Cost(L) = cost of traversing left child

Cost(R) = cost of traversing right child

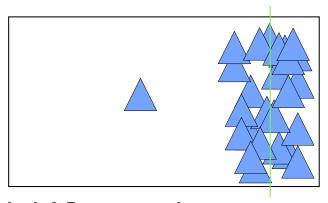
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From Gordon Stoll



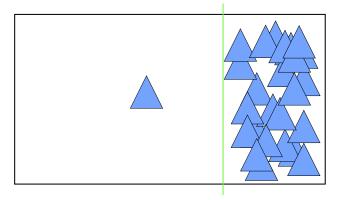
Makes the L & R costs equal Probability of hitting L greater than R

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Cost-Optimized Split = Good!

From Gordon Stoll



Cost(cell) = C_trav + Prob(hit L) * Cost(L) + Prob(hit R) * Cost(R)

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Cost

Need the probabilities

- Turns out to be proportional to surface area Need the child cell costs
 - Triangle count is a good approximation

 $Cost(cell) = C_{trav} + SA(L) * TriCount(L) + SA(R) * TriCount(R)$

C_trav is the ratio of the cost to traverse to the cost to intersect

 $C_{trav} = 1:80$ in pbrt

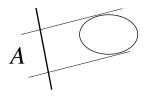
C_trav = 1:1.5 in a highly optimized version

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Projected Area and Ray Intersection

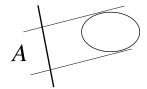
Number of rays in a given direction that hit an object is proportional to its projected area



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Projected Area and Surface Area

Number of rays in a given direction that hit an object is proportional to its projected area



The total number of rays hitting an object is $4\pi \overline{A}$ Crofton's Theorem:

For a convex body $\overline{A} = \frac{S}{4}$

For a sphere $\,S=4\pi r^2$ and $\,\overline{A}=A=\pi r^2$

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Surface Area and Ray Intersection

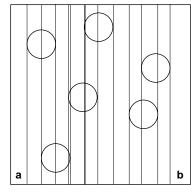
The probability of a ray hitting a convex shape enclosed by another convex shape is

$$S_c$$
 S_o

$$\Pr[r \cap S_o \middle| r \cap S_c] = \frac{S_o}{S_c}$$

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Sweep Build Algorithm



2n splits

$$p_a = \frac{S_a}{S}$$

$$N_a$$

$$p_b = \frac{S_b}{S}$$

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Basic Build Algorithm (Triangles)

- 1. Pick an axis, or optimize across all three
- 2. Build a set of "candidate" split locations

Note: Cost extrema must be at bbox vertices

- Vertices of triangle
- Vertices of triangle clipped to node bbox
- 3. Sort the triangles into intervals
- 4. Sweep to incrementally track L/R counts, cost
- 5. Output position of minimum cost split

Running time: $T(N) = N \log N + 2T(N/2)$

$$T(N) = N \log^2 N$$

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Termination Criteria

When should we stop splitting?

- Bad: depth limit, number of triangles
- Good: When split does not lower the cost

Threshold of cost improvement

- Stretch over multiple levels
- For example, if cost doesn't go down after three splits in a row, terminate

Threshold of cell size

■ Absolute probability SA(node)/SA(scene) small

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Best Reported Timings

Millions of Rays per Second

Framerate (FPS) @ 1024x1024 resolution scene # of triangles and shader (+/-)			OpenRT @ 2.5 GHz P4 1 thread	MLRTA @ 2.4 GHz P4 1 thread	MLRTA @ 3.2 GHz P4 with HT 2 threads
Erw6 804		– shader	7.1	70.2	109.8
		+ shader	2.3	37.8	50.7
Confe- rence 274K	K K Think &	– shader	4.55	11.2	19.5
		+ shader	1.93	9.5	15.6
Soda Hall 2195K		– shader	4.12	21.1	35.5
		+ shader	1.8	15.3	24.1

Reshetov, Soupikov, Hurley, SIGGRAPH 2005

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Superoptimizations

Lots of optimizations

- Carefully written inner loop (no recursion)
- Use vector instructions SSE2
- 64 bits per kd-tree node
 - 32 bit position
 - 32 bit pointer to pair of child nodes
 - 2 bits for split plane direction (x, y, or z)
- Trace packet of rays
 - 4 or more rays at a time
- Intersect beam at top of tree
- **■** Encourage empty nodes
- Special case axis-aligned triangles
- **...**

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Theoretical Nugget 1

Computational geometry of ray shooting

1. Triangles (Pellegrini)

■ Time: $O(\log n)$

■ Space: $O(n^{5+\varepsilon})$

2. Sphere (Guibas and Pellegrini)

Time: $O(\log^2 n)$

■ Space: $O(n^{5+\varepsilon})$

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Theoretical Nugget 2

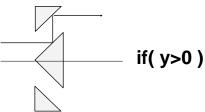
Optical computer = Turing machine

Reif, Tygar, Yoshida

Determining if a ray starting at y0 arrives at yn is undecidable







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