

SPRINT 4 DELIVERABLES

11/10/2020

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1). BULB PROBLEM

* EXPECTED LIFE TIME = 2,000 H $E[X] = 2,000$ H $\lambda = 1/2,000$

* $P(\text{THAT 2 BULBS SURVIVE MORE THAN 3,000 H})$

BULB 1 $\rightarrow P(X > 2,000 + 1,000 | X > 2,000)$

$$\rightarrow e^{-\lambda s} \Rightarrow e^{-1/2000 \cdot 1,000} \Rightarrow e^{-1/2} = 0.60653$$

$$= e^{-1/2} \Rightarrow 0.223130$$

• BECAUSE THE BULBS ARE INDEPENDENT, AND THE MEMORY-LESS PROPERTY

$$P(2 \text{ BULBS SURVIVE OVER } 3,000 \text{ H}) = P(\text{A BULB SURVIVES } 3,000)^2$$

$$P(X > 3,000 | X > 2,000) = 0.223130$$

$$(0.223130)^2 = 0.04978 \Rightarrow \underline{0.04978}$$

2). FIND PROBABILITY THAT BOTH BULBS REACH 3,000 HOURS

BULB 1 \rightarrow OPERATING FOR 1,000 H $\rightarrow P(X > t+s | P > t) \Rightarrow e^{-\lambda s}$

BULB 2 \rightarrow OPERATING FOR 2,500 H $\rightarrow P(X > t+s | P > t) \Rightarrow e^{-\lambda s}$

• $P(\text{BULB 1 REACHES } 3,000 \text{ H}) = e^{-(1/2000) \cdot 2,000} \leftarrow \text{REMAINING TIME TO REACH } 3,000 \text{ H}$

$$\hookrightarrow e^{-2,000/2,000} = e^{-1}$$

• $P(\text{BULB 2 REACHES } 3,000 \text{ H}) = e^{-(1/2,000) \cdot 500} \Rightarrow e^{-(5/20)}$

• $P(\text{BULB 1 AND BULB 2 REACH } 3,000 \text{ H}) = e^{-1} \cdot e^{-5/20}$

$$= e^{-1 + (-5/20)} = \underline{0.2865}$$

3) CHECK MY MATH:

GIVEN:

O AVERAGE TIME FOR DISK = 5ms

O AVERAGE NUMBER OF DISKS / JOB = 2

O NUMBER OF JOBS IN THE SYSTEM = 120

O AVERAGE RESIDENCE TIME = 1 SEC.

* WE HAVE TO TAKE INTO ACCOUNT THE ~~AVG~~ AVERAGE TIME IT TAKES TO ACCESS EACH DISK

→ AVERAGE JOB NEEDS TO ACCESS BOTH DISKS

$$\therefore 1 \text{ DISK ACCESS} = 0.05 \text{ s}$$

$$2 \text{ DISK ACCESS} = (0.05) \times 2 = 0.01$$

$$* \bar{N} = 120 \text{ JOBS } \lambda \Rightarrow \bar{R}/\bar{N} = 120 \text{ COST/SEC } \} \text{ PREVIOUS ASSUMPTION}$$

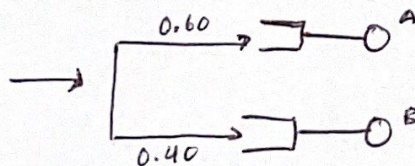
$$* U = \lambda \cdot \bar{S} = \lambda = 120 \quad \bar{S} = 0.01$$

$$* U = 120 \cdot 0.01$$

$$* U = 1.2$$

4) UNBALANCED SERVICE LOADS

GIVEN:

SERVER A $\rightarrow U = 80\%$ SERVER B $\rightarrow U = 60\%$, $\bar{S}_B = 250 \text{ ms}$

$$* \text{SERVER B} = U_B = \bar{S}_B \cdot \lambda_B \rightarrow \lambda_B = U_B / \bar{S}_B \rightarrow \lambda_B = 0.60 / 250 = 0.024 \text{ s}$$

$$\lambda_k = U_k \cdot \lambda \quad U_k = 0.25 \rightarrow \text{ARRIVAL RATE} = 2.5 / \text{MIN}$$

$$* \text{SERVER A} = U_A = \bar{S}_A \cdot \lambda_A \Rightarrow U_A / \lambda_A = \bar{S}_A = U_A / \lambda_A = \bar{S}_A =$$

* SERVER B RELIEVES 40%, SERVER A RELIEVES 60%

$$\therefore 0.60 / 0.40 = 1.5 \Rightarrow 1.5 \cdot \lambda_B = 0.036$$

$$U_A / \lambda_A = \bar{S}_A \Rightarrow 0.80 / 0.036 = 222$$

$$\bar{S}_A = 222 \text{ ms}$$

THE M/M/1 QUEUE

- $DEPARTURE\ TIME = EST[i] + st[i] \} DE$
- $RESIDENCE\ TIME = DE - AT$

- $EST \rightarrow ENTER\ SERVICE\ TIME$
- $DE \rightarrow DEPARTURE\ TIME$
- $AT \rightarrow ARRIVAL\ TIME$
- $RT \rightarrow RESIDENCE\ TIME$

ARRIVAL TIME	SERVICE TIME	ENTER SERVICE TIME	DE	RT
1 \rightarrow	3 \rightarrow	1 \rightarrow	4 \rightarrow	3
3 \rightarrow	2 \rightarrow	4 \rightarrow	6 \rightarrow	3
5 \rightarrow	4 \rightarrow	6 \rightarrow	10 \rightarrow	5
7 \rightarrow	1 \rightarrow	10 \rightarrow	11 \rightarrow	4
8 \rightarrow	1 \rightarrow	11 \rightarrow	12 \rightarrow	4
13 \rightarrow	2 \rightarrow	13 \rightarrow	15 \rightarrow	2
14 \rightarrow	1 \rightarrow	15 \rightarrow	16 \rightarrow	2
17 \rightarrow	3 \rightarrow	18 \rightarrow	20 \rightarrow	3