cp2021t-0.1.0.0: Trabalho para Calculo Proposicional da Universidade do Minho

Trabalho para Calculo Proposicional da Universidade do Minho

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BTree

module BTree (

```
cataBTree :: (Either () (b, (d, d)) \rightarrow d) \rightarrow BTree b \rightarrow d
anaBTree :: (a \rightarrow Either () (b, (a, a))) \rightarrow a \rightarrow BTree b
hyloBTree :: (Either () (b, (c, c)) -> c) -> (a -> Either () (b, (a, a))) -> a -> c
baseBTree :: (a1 -> b1) -> (a2 -> d) -> Either b2 (a1, (a2, a2)) -> Either b2 (b1, (d, d))
invBTree :: BTree b -> BTree b
countBTree :: BTree a -> Integer
inordt :: BTree a -> [a]
inord :: Either b (a, ([a], [a])) -> [a]
preordt :: BTree a -> [a]
preord :: Either b (a, ([a], [a])) -> [a]
postordt :: BTree a -> [a]
qSort :: Ord a => [a] -> [a]
qsep :: Ord a => [a] -> Either () (a, ([a], [a]))
part :: (a -> Bool) -> [a] -> ([a], [a])
traces :: Eq a => BTree a -> [[a]]
tunion :: Eq a => (a, ([[a]], [[a]])) -> [[a]]
hanoi :: (Bool, Integer) -> [(Integer, Bool)]
present :: Either b (a, ([a], [a])) -> [a]
strategy :: Integral b => (Bool, b) -> Either () ((b, Bool), ((Bool, b), (Bool, b)))
balBTree :: BTree a -> Bool
depthBTree :: BTree a -> Integer
baldepth :: BTree a -> (Bool, Integer)
tnat :: Monoid c \Rightarrow (a \rightarrow c) \rightarrow Either () (a, (c, c)) \rightarrow c
monBTree :: Monoid d \Rightarrow (a \rightarrow d) \rightarrow BTree a \rightarrow d
preordt' :: BTree a -> [a]
countBTree' :: BTree b -> Sum Integer
```

data Deriv a

Constructors

= Dr Bool a (BTree a)

type Zipper a = [Deriv a]

plug :: Zipper a -> BTree a -> BTree a

Ср

```
module Cp (
    split, (><), (!), p1, p2, i1, i2, (-|-), cond, ap, expn, p2p,
    grd, swap, assocr, assocl, undistr, undistl, flatr, flatl, br, bl,
    coswap, coassocr, coassocl, distl, distr, BiFunctor(bmap), (.!),
    mult, ap', singl, Strong(lstr, rstr), dstr, splitm, bang, dup,
    zero, one, nil, cons, add, mul, conc, true, nothing, false,
    inMaybe, Unzipable(unzp), DistL(lamb), aap, gather, cozip, tot
) where</pre>
```

```
split :: (a -> b) -> (a -> c) -> a -> (b, c)

(><) :: (a -> b) -> (c -> d) -> (a, c) -> (b, d)

(!) :: a -> ()

p1 :: (a, b) -> a

p2 :: (a, b) -> b

i1 :: a -> Either a b

i2 :: b -> Either a b

(-|-) :: (a -> b) -> (c -> d) -> Either a c -> Either b d

cond :: (b -> Bool) -> (b -> c) -> (b -> c) -> b -> c
```

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```
ap :: (a -> b, a) -> b
expn :: (b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow c
p2p :: (a, a) -> Bool -> a
grd :: (a -> Bool) -> a -> Either a a
swap :: (a, b) -> (b, a)
assocr :: ((a, b), c) \rightarrow (a, (b, c))
assocl :: (a, (b, c)) \rightarrow ((a, b), c)
undistr :: Either (a, b) (a, c) -> (a, Either b c)
undistl :: Either (b, c) (a, c) -> (Either b a, c)
flatr :: (a, (b, c)) -> (a, b, c)
flatl :: ((a, b), c) -> (a, b, c)
br :: a -> (a, ())
bl :: a -> ((), a)
coswap :: Either a b -> Either b a
coassocr :: Either (Either a b) c -> Either a (Either b c)
coassocl :: Either b (Either a c) -> Either (Either b a) c
distl :: (Either c a, b) \rightarrow Either (c, b) (a, b)
distr :: (b, Either c a) -> Either (b, c) (b, a)
class BiFunctor f where
      Methods
     bmap :: (a \rightarrow b) \rightarrow (c \rightarrow d) \rightarrow f a c \rightarrow f b d
instance BiFunctor Either
instance BiFunctor (,)
(.!) :: Monad a => (b -> a c) -> (d -> a b) -> d -> a c
mult :: Monad m => m (m b) -> m b
ap' :: Monad m => (a -> m b, m a) -> m b
```

```
singl :: a -> [a]
class (Functor f, Monad f) => Strong f where
     Methods
     rstr :: (f a, b) -> f (a, b)
     lstr :: (b, f a) -> f (b, a)
instance Strong []
instance Strong Maybe
instance Strong IO
instance Strong LTree
dstr :: Strong m \Rightarrow (m a, m b) \rightarrow m (a, b)
splitm :: Strong ff => ff (a -> b) -> a -> ff b
bang :: a -> ()
dup :: c -> (c, c)
zero :: b -> Integer
one :: b -> Integer
nil :: b -> [a]
cons :: (a, [a]) -> [a]
add :: (Integer, Integer) -> Integer
mul :: (Integer, Integer) -> Integer
conc :: ([a], [a]) -> [a]
true :: b -> Bool
nothing :: b -> Maybe a
false :: b -> Bool
inMaybe :: Either () a -> Maybe a
class Functor f => Unzipable f where
     Methods
```

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```
unzp :: f (a, b) \rightarrow (f a, f b) class Functor g \Rightarrow DistL g where
```

lamb :: Monad $m \Rightarrow g (m a) \rightarrow m (g a)$

instance DistL []
instance DistL Maybe

Methods

 $aap :: Monad m \Rightarrow m (a \rightarrow b) \rightarrow m a \rightarrow m b$

gather :: [a -> b] -> a -> [b]

 $\texttt{cozip} \ :: \ \ \texttt{Functor} \ \ \texttt{f} \ \ \texttt{=>} \ \ \texttt{Either} \ \ (\texttt{f} \ \ \texttt{a}) \ \ (\texttt{f} \ \ \texttt{b}) \ \ \ \ \texttt{->} \ \ \texttt{f} \ \ (\texttt{Either} \ \ \texttt{a} \ \ \texttt{b})$

tot :: (a -> b) -> (a -> Bool) -> a -> Maybe b

LTree

```
module LTree (
   LTree(Fork, Leaf), inLTree, outLTree, recLTree, baseLTree,
   cataLTree, anaLTree, hyloLTree, invLTree, countLTree, tips, dfac,
   dfacd, dsq', dsq, fib, fibd, mSort, merge, lsplit, dmap, dmap1, mu,
   tnat, monLTree, tips', countLTree', dlLTree, Deriv(Dr), Zipper,
   plug
  ) where
data LTree a
     Constructors
     = Leaf a
     | Fork (LTree a, LTree a)
instance Monad LTree
instance Functor LTree
instance Applicative LTree
instance Strong LTree
instance Eq a => Eq (LTree a)
instance Show a => Show (LTree a)
inLTree :: Either a (LTree a, LTree a) -> LTree a
outLTree :: LTree a -> Either a (LTree a, LTree a)
```

```
recLTree :: (a \rightarrow d) \rightarrow Either b (a, a) \rightarrow Either b (d, d)
baseLTree :: (a1 -> b) -> (a2 -> d) -> Either a1 (a2, a2) -> Either b (d, d)
cataLTree :: (Either b (d, d) \rightarrow d) \rightarrow LTree b \rightarrow d
anaLTree :: (a1 -> Either a2 (a1, a1)) -> a1 -> LTree a2
hyloLTree :: (Either b (c, c) \rightarrow c) \rightarrow (a \rightarrow Either b (a, a)) \rightarrow a \rightarrow c
invLTree :: LTree a -> LTree a
countLTree :: LTree b -> Integer
tips :: LTree a -> [a]
dfac :: Integral p => p -> p
dfacd :: Integral b \Rightarrow (b, b) \rightarrow Either b ((b, b), (b, b))
dsq':: Integer -> Integer
dsq :: Integer -> Integer
fib :: Integer -> Integer
fibd :: (Ord b, Num b) \Rightarrow b \Rightarrow Either () (b, b)
mSort :: Ord a => [a] -> [a]
merge :: Ord a => ([a], [a]) -> [a]
lsplit :: [a] -> Either a ([a], [a])
dmap :: (b -> a) -> [b] -> [a]
dmap1 :: (b -> a) -> [b] -> [a]
mu :: LTree (LTree a) -> LTree a
tnat :: Monoid c \Rightarrow (a \rightarrow c) \rightarrow Either a (c, c) \rightarrow c
monLTree :: Monoid d \Rightarrow (a \rightarrow d) \rightarrow LTree a \rightarrow d
tips' :: LTree a -> [a]
countLTree' :: LTree b -> Sum Integer
dlLTree :: Strong f => LTree (f a) -> f (LTree a)
```

data Deriv a

Constructors

= Dr Bool (LTree a)

type Zipper a = [Deriv a]

plug :: Zipper a -> LTree a -> LTree a

List

```
module List (
    inList, outList, cataList, recList, anaList, hyloList,
    baseList, eval, invl, look, iSort, take', fac, algMul, nats, fac',
    sq, summing, odds, sq', prefixes, suffixes, diff, nest, myfoldr,
    myfoldl, nr, ccat, mmap, lam, mcataList, dl, stream, join, sep
) where

inList :: Either b (a, [a]) -> [a]

outList :: [a] -> Either () (a, [a])

cataList :: (Either () (b, d) -> d) -> [b] -> d

recList :: (c -> d) -> Either b1 (b2, c) -> Either b1 (b2, d)

anaList :: (c -> Either b (a, c)) -> c -> [a]

hyloList :: (Either () (b1, c1) -> c1) -> (c2 -> Either b2 (b1, c2)) -> c2 -> c1

baseList :: (a -> b1) -> (c -> d) -> Either b2 (a, c) -> Either b2 (b1, d)

eval :: Integer -> [Integer] -> Integer
invl :: [a] -> [a]
```

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```
look :: Eq a \Rightarrow a \Rightarrow [(a, b)] \Rightarrow Maybe b
iSort :: Ord a => [a] -> [a]
take' :: Integer -> [a] -> [a]
fac :: Integer -> Integer
algMul :: Either b (Integer, Integer) -> Integer
nats :: Integer -> Either () (Integer, Integer)
fac' :: Integer -> Integer
sq :: Integer -> Integer
summing :: Either b (Integer, Integer) -> Integer
odds :: Integer -> Either () (Integer, Integer)
sq' :: Integer -> Integer
prefixes :: Eq a => [a] -> [[a]]
suffixes :: [a] -> [[a]]
diff :: Eq a \Rightarrow [a] \Rightarrow [a] \Rightarrow [a]
nest :: Eq a => Int -> [a] -> [[a]]
 myfoldr :: (a \rightarrow b \rightarrow b) \rightarrow b \rightarrow [a] \rightarrow b 
myfoldl :: (a \rightarrow b \rightarrow a) \rightarrow a \rightarrow [b] \rightarrow a
nr :: Eq a => [a] -> Bool
ccat :: [a] -> [a] -> [a]
mmap :: Strong m => (a1 -> m a2) -> [a1] -> m [a2]
lam :: Strong m => [m a] -> m [a]
mcataList :: Strong ff \Rightarrow (Either () (b, c) \rightarrow ff c) \rightarrow [b] \rightarrow ff c
dl :: Strong m => Either () (b, m a) -> m (Either () (b, a))
stream :: (t1 \rightarrow Maybe (a, t1)) \rightarrow (t1 \rightarrow t2 \rightarrow t1) \rightarrow t1 \rightarrow [t2] \rightarrow [a]
join :: ([a], [b]) -> [Either a b]
sep :: [Either a1 a2] -> ([a1], [a2])
```

Main

```
module Main (
   ExpAr(Un, N, X, Bin), BinOp(Product, Sum), UnOp(Negate, E),
   inExpAr, baseExpAr, prop_in_out_idExpAr, prop_out_in_idExpAr,
   prop_sum_idr, prop_sum_idl, prop_product_idr, prop_product_idl,
   prop_e_id, prop_negate_id, prop_double_negate,
   prop_optimize_respects_semantics, prop_const_rule, prop_var_rule,
   prop_sum_rule, prop_product_rule, prop_e_rule, prop_negate_rule,
   prop_congruent, fib', f', prop_cat, linear1d, NPoint, OverTime,
   prop_calcLine_def, prop_bezier_sym, prop_avg, e', OutExpAr, expd,
   catdef, oracle, bezier2d, World(World, points, time), initW, tick,
   actions, scaleTime, bezier2dAtTime, bezier2dAt, thicCirc, ps,
   picture, animateBezier, runBezier, runBezierSym, main, run,
   (.=?=.), (.==>.), (.<==), (.<=.), (.&&&.), cataExpAr,
   anaExpAr, hyloExpAr, eval_exp, optmize_eval, sd, ad, outExpAr,
   recExpAr, g_eval_exp, clean, gopt, sd_gen, ad_gen, loop, inic, prj,
   cat, calcLine, deCasteljau, hyloAlgForm, avg, avg_aux, avgLTree
  ) where
```

```
data ExpAr a
```

Constructors

```
= X
| N a
| Bin BinOp (ExpAr a) (ExpAr a)
| Un UnOp (ExpAr a)
```

```
instance Eq a => Eq (ExpAr a)
instance Show a => Show (ExpAr a)
instance Arbitrary a => Arbitrary (ExpAr a)
data BinOp
     Constructors
        Sum
     | Product
instance Eq BinOp
instance Show BinOp
instance Arbitrary BinOp
data UnOp
     Constructors \\
     = Negate
     | E
instance Eq UnOp
instance Show UnOp
instance Arbitrary UnOp
inExpAr :: Either b (Either a (Either (BinOp, (ExpAr a, ExpAr a)) (UnOp, ExpAr a)))
           -> ExpAr a
baseExpAr :: (a1 -> b1)
             -> (a2 -> b2)
                -> (a3 -> b3)
                   -> (a4 -> b4)
                      -> (c1 -> d1)
                         -> (a5 -> b5)
                            -> (c2 -> d2)
                               -> Either a1 (Either a2 (Either (a3, (a4, c1)) (a5, c2)))
                                  -> Either b1 (Either b2 (Either (b3, (b4, d1)) (b5, d2)))
prop_in_out_idExpAr :: Eq a => ExpAr a -> Bool
prop_out_in_idExpAr :: Eq a => OutExpAr a -> Bool
prop_sum_idr :: (Floating a, Real a) => a -> ExpAr a -> Bool
prop_sum_idl :: (Floating a, Real a) => a -> ExpAr a -> Bool
prop_product_idr :: (Floating a, Real a) => a -> ExpAr a -> Bool
```

```
prop_product_idl :: (Floating a, Real a) => a -> ExpAr a -> Bool
prop_e_id :: (Floating a, Real a) => a -> Bool
prop_negate_id :: (Floating a, Real a) => a -> Bool
prop_double_negate :: (Floating a, Real a) => a -> ExpAr a -> Bool
prop_optimize_respects_semantics :: (Floating a, Real a) => a -> ExpAr a -> Bool
prop_const_rule :: (Real a, Floating a) => a -> Bool
prop_var_rule :: Bool
prop_sum_rule :: (Real a, Floating a) => ExpAr a -> ExpAr a -> Bool
prop_product_rule :: (Real a, Floating a) => ExpAr a -> ExpAr a -> Bool
prop_e_rule :: (Real a, Floating a) => ExpAr a -> Bool
prop_negate_rule :: (Real a, Floating a) => ExpAr a -> Bool
prop_congruent :: (Floating a, Real a) => a -> ExpAr a -> Bool
fib' :: Integer -> Integer
f' :: (Integral c, Num b) => b -> b -> c -> b
prop_cat :: Integer -> Property
linear1d :: Rational -> Rational -> OverTime Rational
type NPoint = [Rational]
type OverTime a = Float -> a
prop_calcLine_def :: NPoint -> NPoint -> Float -> Bool
prop_bezier_sym :: [[Rational]] -> Gen Bool
prop_avg :: [Double] -> Property
e' :: (Fractional c1, Integral c2) \Rightarrow c1 \Rightarrow c2 \Rightarrow c1
type OutExpAr a = Either () (Either a (Either (BinOp, (ExpAr a, ExpAr a)) (UnOp, ExpAr a)))
expd :: Floating a => a -> a
```

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```
catdef :: Integer -> Integer
oracle :: [Integer]
bezier2d :: [NPoint] -> OverTime (Float, Float)
data World
     Constructors
     = World
             { points :: [NPoint]
             , time :: Float
initW :: World
tick :: Float -> World -> World
actions :: Event -> World -> World
scaleTime :: World -> Float
bezier2dAtTime :: World -> (Float, Float)
bezier2dAt :: World -> OverTime (Float, Float)
thicCirc :: Picture
ps :: [Float]
picture :: World -> Picture
animateBezier :: Float -> [NPoint] -> Picture
runBezier :: IO ()
runBezierSym :: IO ()
main :: IO ()
run :: IO ExitCode
(.=?=.) :: Real a => a -> a -> Bool
(.==>.) :: Testable prop => (a -> Bool) -> (a -> prop) -> a -> Property
(.<==>.) :: (a -> Bool) -> (a -> Bool) -> a -> Property
(.==.) :: Eq b => (a \rightarrow b) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow Bool
(.<=.) :: Ord b => (a -> b) -> (a -> b) -> a -> Bool
```

```
(.&&&.) :: (a -> Bool) -> (a -> Bool) -> a -> Bool
cataExpAr :: (b \rightarrow c) \rightarrow a \rightarrow c
anaExpAr :: (a1 \rightarrow b) \rightarrow a1 \rightarrow ExpAr a2
hyloExpAr :: (b1 \rightarrow c) \rightarrow (a \rightarrow b2) \rightarrow a \rightarrow c
eval_exp :: Floating a => a -> ExpAr a -> a
optmize_eval :: (Floating a, Eq a) => a -> ExpAr a -> a
sd :: Floating a => ExpAr a -> ExpAr a
ad :: Floating a => a -> ExpAr a -> a
outExpAr :: a
recExpAr :: a
g_eval_exp :: a
clean :: a
gopt :: a
sd_gen :: Floating a =>
          Either () (Either a (Either (BinOp, ((ExpAr a, ExpAr a), (ExpAr a, ExpAr a))) (UnOp, (ExpAr a, Ex
          -> (ExpAr a, ExpAr a)
ad_gen :: a
loop :: a
inic :: a
prj :: a
cat :: Integer -> c
calcLine :: NPoint -> NPoint -> OverTime NPoint
     Spec
          calcLine :: NPoint -> (NPoint -> OverTime NPoint)
          calcLine [] = const nil
          calcLine (p : x) = curry g p (calcLine x)
            g :: (, NPoint -> OverTime NPoint) -> (NPoint -> OverTime NPoint)
            g(d, f) l = case l of
               [] -> nil
               (x : xs) -> concat . sequenceA [singl . linear1d d x, f xs]
```

CHAPTER 5. MAIN

Nat

```
module Nat (
    inNat, outNat, cataNat, recNat, anaNat, hyloNat, for, somar,
    multip, exp, sq, sq', sq'', fac, facfor, idiv, aux, bSort, while,
    mfor
  ) where
inNat :: Either b Integer -> Integer
outNat :: Integral b => b -> Either () b
cataNat :: Integral c => (Either () d -> d) -> c -> d
recNat :: (c -> d) -> Either b c -> Either b d
anaNat :: (c -> Either b c) -> c -> Integer
hyloNat :: (Either () c1 \rightarrow c1) \rightarrow (c2 \rightarrow Either b c2) \rightarrow c2 \rightarrow c1
for :: Integral c \Rightarrow (b \rightarrow b) \rightarrow b \rightarrow c \rightarrow b
somar :: (Integral c, Enum d) \Rightarrow d \Rightarrow c \Rightarrow d
multip :: (Integral c, Num d) \Rightarrow d \Rightarrow c \Rightarrow d
exp :: (Integral c, Num d) \Rightarrow d \Rightarrow c \Rightarrow d
sq :: Integral p \Rightarrow p \rightarrow p
```

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```
sq' :: Integer -> Integer
sq'' :: (Integral c, Num b) => c -> b
fac :: Integer -> Integer
facfor :: Integer -> (Integer, Integer)
idiv :: Integer -> Integer -> Integer
aux :: (Ord c, Num c) => c -> c -> Integer
bSort :: Ord a => [a] -> [a]
while :: (a -> Bool) -> (a -> a) -> a -> a
mfor :: forall t1 m t2. (Monad m, Integral t1) => (t2 -> m t2) -> t2 -> t1 -> m t2
```