## Project 2

## SF2568 Program construction in C++ for Scientific Computing

## October 5, 2018

In this project you will implement a general class for matrices. The final aim is to provide all necessary functionality for computing elementary functions of matrices. You will learn details about the construction of classes in C++.

The exponential function has the series representation

$$e^{x} = \sum_{n=0}^{\infty} \frac{x^{n}}{n!}.$$

This series converges for all  $x \in \mathbb{R}$ . Therefore, an exponential for square matrices  $A \in \mathbb{R}^{m \times m}$  can be defined by

$$\exp(A) = \sum_{n=0}^{\infty} \frac{A^n}{n!}.$$

**Task 1** Implement the evaluation of the exponential for real numbers! The calling sequence should be

The parameter tol indicates the required accuracy.

Validate your routine by checking it against the exponential function from the standard library!

**Task 2** Now we are interested in computing the matrix exponential. The idea consist of using the series for that. Therefore, you must construct a matrix class according to the following skeleton:

```
class Matrix {
public:
   Matrix(int m);
   Matrix(const& Matrix);
   Matrix& operator=(const Matrix&);
   Matrix& operator+=(const Matrix&);
   Matrix& operator*=(const Matrix&);
   Matrix& operator*=(const double);
   double norm() const;
   void printMatrix() const;
   void fillMatrix(....);
   ...
};
```

Add members as needed and convenient for the problem. For the implementation of the arrays you may use either C-style arrays or corresponding classes from the C++ standard library.

In order to check your computations, a C++ routine for computing the matrix exponential, r8mat\_expm1.cpp, is provided. The latter implements Matlab's algorithm for expm. Show using a number of freely choosen matrices how accurate your matrix exponential is!

Note: The provided routines consist of two source files and two header files. The calling sequence is:

```
double* r8mat_expm1(int m, double a[])
```

Here, m is the dimension of the matrix and a denotes a C-style array where the matrix is stored in Fortran-style (column wise). The return result is a pointer to a C-style array holding the matrix exponential. Note: The header file r8lib.h assume that the namespace std has been opened. So do the following in your code:

```
using namespace std;
#include "r8lib.h"
```

Note: I recommend to have a look at the following paper: Cleve Moler, Charles Van Loan: *Nineteen dubious ways to compute the exponential of a matrix, twenty-five years later.* SIAM Review **45**(2003)1, 3–49

The programming exercises should be done individually, or in groups of two. Hand in a report containing:

- Comments and explanations that you think are necessary for understanding your program.
- Results as indicated in the tasks. Don't forget to draw conclusions!
- Printout of your source code.
- E-mail the source code to hanke@nada.kth.se.