SOLUCIONARIOMateria Resistencia de materiales

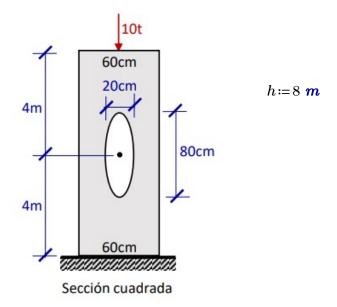
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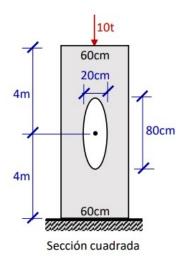
Ejercicio Nº6

Para los elementos del siguiente sistema, obtener:

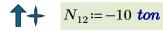
- a) Diagrama de esfuerzo normal
- b) Diagrama de Tensión Axial



Paso 1: Calculo de la Normal



$$\Sigma F_V = 0$$

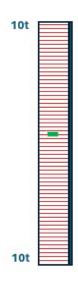


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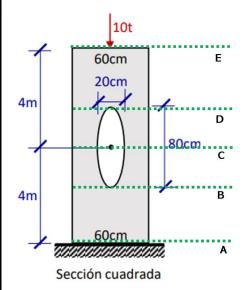
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Paso 2: Diagramar las normales



Paso 3: Calcular las diferencias de áreas



Analizamos la sección

A) tramo A-B

$$A_{AB} \coloneqq 60 \ cm \cdot 60 \ cm$$

$$A_{AB}$$
 = 3600 cm^2

- B) tramo B-C
- A) tramo C-D
- A) tramo D-E

$$A_{DE} \coloneqq 60 \ cm \cdot 60 \ cm$$

$$A_{DE}$$
 = 3600 cm^2



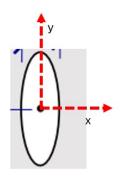
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Usamos las ecuación de la elipse

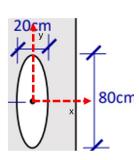


VERTICAL	
$\frac{x^2}{b^2} + \frac{y^2}{a^2} = 1$	FORMA CANÓNICA ELIPSE CON CENTRO EN ORIGEN (0,0)

$$\frac{x^2}{b^2} + \frac{y^2}{a^2} = 1 \qquad a = 0.4 \ m \qquad b = 0.1 \ m$$

$$a = 0.4 m$$

$$b = 0.1 \ m$$



$$\frac{x^2}{0.1^2} + \frac{y^2}{0.4^2} = 1$$

$$\frac{x^{2}}{0.1^{2}} + \frac{y^{2}}{0.4^{2}} = 1$$

$$\frac{x^{2}}{0.1^{2}} + \frac{y^{2}}{0.4^{2}} = 1 \xrightarrow{solve, x} \begin{bmatrix} 0.01 \cdot (-625.0 \cdot y^{2} + 100.0)^{0.5} \\ -0.01 \cdot (-625.0 \cdot y^{2} + 100.0)^{0.5} \end{bmatrix}$$
80cm

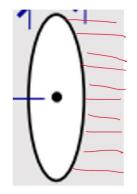
$$x := (0.01 \cdot (-625.0 \cdot \mathbf{d}^2 + 100.0)^{0.5}) \cdot 2$$

$$d_{BC} \coloneqq \begin{bmatrix} 0 \\ -0.1 \\ -0.2 \\ -0.3 \\ -0.4 \end{bmatrix} \qquad x \coloneqq \left(0.01 \cdot \left(-625.0 \cdot d_{BC}^{2} + 100.0\right)^{0.5}\right) \cdot 2 \cdot \boldsymbol{m} = \begin{bmatrix} 0.2 \\ 0.194 \\ 0.173 \\ 0.132 \\ 0 \end{bmatrix} \boldsymbol{m}$$

$$d_{CD} \coloneqq \begin{bmatrix} 0.4 \\ 0.3 \\ 0.2 \\ 0.1 \\ 0 \end{bmatrix} \qquad \varnothing \coloneqq \left(0.01 \cdot \left(-625.0 \cdot d_{CD}^{2} + 100.0 \right)^{0.5} \right) \cdot 2 \cdot \boldsymbol{m} = \begin{bmatrix} 0 \\ 0.132 \\ 0.173 \\ 0.194 \\ 0.2 \end{bmatrix} \boldsymbol{m}$$

 $D_T \coloneqq \begin{bmatrix} 0.6 \\ 0.6 \\ 0.6 \\ 0.6 \end{bmatrix} \boldsymbol{m}$ Calculamos la área

$$D_{BC} \coloneqq - \begin{bmatrix} 0.2 \\ 0.194 \\ 0.173 \\ 0.132 \\ 0 \end{bmatrix} \boldsymbol{m} + D_T = \begin{bmatrix} 0.4 \\ 0.406 \\ 0.427 \\ 0.468 \\ 0.6 \end{bmatrix} \boldsymbol{m}$$



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$$D_{CB} \coloneqq -\begin{bmatrix} 0 \\ 0.132 \\ 0.173 \\ 0.194 \\ 0.2 \end{bmatrix} \boldsymbol{m} + D_{T} = \begin{bmatrix} 0.6 \\ 0.468 \\ 0.427 \\ 0.406 \\ 0.4 \end{bmatrix} \boldsymbol{m}$$

$$CC \coloneqq \begin{bmatrix} 0.4 \\ 0.406 \\ 0.427 \\ 0.468 \\ 0.6 \end{bmatrix} \qquad A_{BC} \coloneqq 0.6 \cdot CC \cdot \boldsymbol{m}^2 = \begin{bmatrix} 0.24 \\ 0.244 \\ 0.256 \\ 0.281 \\ 0.36 \end{bmatrix} \boldsymbol{m}^2$$

$$AL \coloneqq egin{bmatrix} 0.6 \\ 0.468 \\ 0.427 \\ 0.406 \\ 0.4 \end{bmatrix} \qquad A_{CD} \coloneqq 0.6 \boldsymbol{\cdot} AL \boldsymbol{\cdot} m{m}^2 = egin{bmatrix} 0.36 \\ 0.281 \\ 0.256 \\ 0.244 \\ 0.24 \end{bmatrix} m{m}^2$$

Paso 3: Calcular las tensiones

a) Tensión en la sección

$$T_{12} \coloneqq \frac{N_{12}}{\boxed{A}} \hspace{1cm} \begin{array}{c} \text{T : tensión} \\ \text{A : Área} \\ \text{N : Normal} \end{array}$$

A) Tramo A-B

$$T_{AB} \coloneqq \frac{N_{12}}{A_{AB}} = -27.778 \frac{\textbf{ton}}{\textbf{m}^2}$$

B) Tramo B-C

$$T_{BC} \coloneqq rac{N_{12}}{A_{BC}} = egin{bmatrix} -41.667 \ -41.051 \ -39.032 \ -35.613 \ -27.778 \ \end{bmatrix} rac{ton}{m^2}$$

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C) Tramo C-D

$$T_{CD} \coloneqq \frac{N_{12}}{A_{CD}} = \begin{bmatrix} -27.778 \\ -35.613 \\ -39.032 \\ -41.051 \\ -41.667 \end{bmatrix} \frac{\textit{ton}}{\textit{m}^2}$$

C) Tramo D-E

$$T_{DE} \coloneqq \frac{N_{12}}{A_{DE}} = -27.778 \; \frac{\textit{ton}}{\textit{m}^2}$$