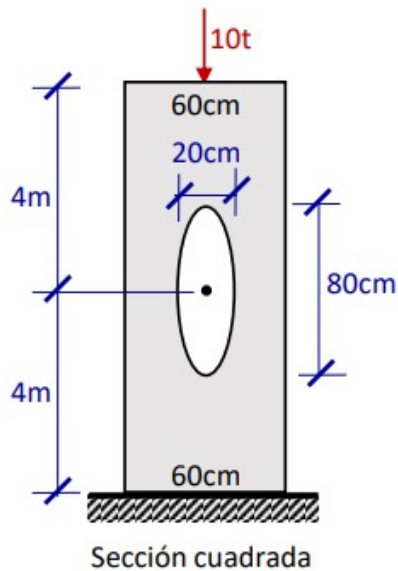


### Ejercicio N°6

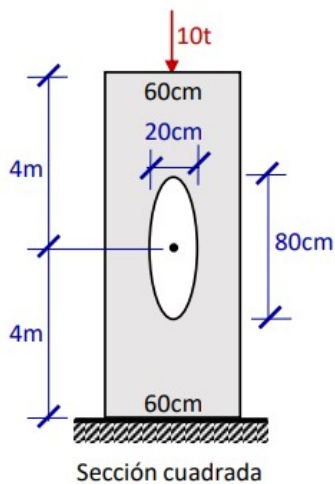
Para los elementos del siguiente sistema, obtener:

- a) Diagrama de esfuerzo normal
- b) Diagrama de Tensión Axial



$$h := 8 \text{ m}$$

Paso 1: Calculo de la Normal

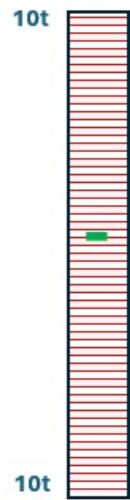


$$\Sigma F_V = 0$$

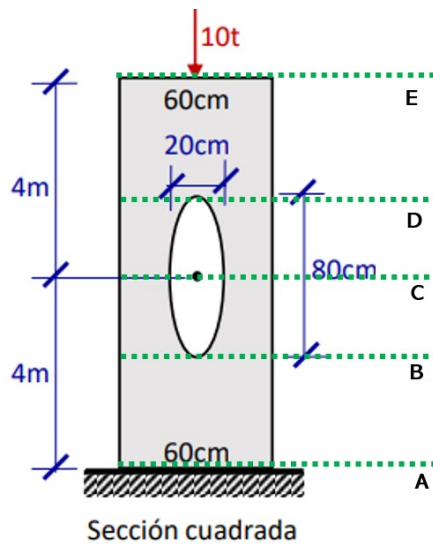


$$N_{12} := -10 \text{ ton}$$

Paso 2: Diagramar las normales



Paso 3: Calcular las diferencias de áreas



Analizamos la sección

A) tramo A-B

$$A_{AB} := 60 \text{ cm} \cdot 60 \text{ cm}$$

$$A_{AB} = 3600 \text{ cm}^2$$

B) tramo B-C

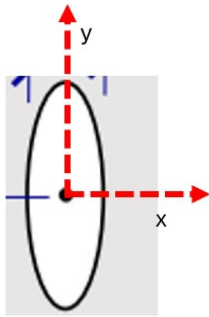
A) tramo C-D

A) tramo D-E

$$A_{DE} := 60 \text{ cm} \cdot 60 \text{ cm}$$

$$A_{DE} = 3600 \text{ cm}^2$$

Usamos la ecuación de la elipse



VERTICAL

$$\frac{x^2}{b^2} + \frac{y^2}{a^2} = 1$$

FORMA CANÓNICA  
ELIPSE CON  
CENTRO EN ORIGEN  
(0,0)

$$\frac{x^2}{b^2} + \frac{y^2}{a^2} = 1 \quad a = 0.4 \text{ m} \quad b = 0.1 \text{ m}$$

$$\frac{x^2}{0.1^2} + \frac{y^2}{0.4^2} = 1$$

$$\frac{x^2}{0.1^2} + \frac{y^2}{0.4^2} = 1 \xrightarrow{\text{solve, } x} \left[ \begin{array}{l} 0.01 \cdot (-625.0 \cdot y^2 + 100.0)^{0.5} \\ -0.01 \cdot (-625.0 \cdot y^2 + 100.0)^{0.5} \end{array} \right]$$

$$x := (0.01 \cdot (-625.0 \cdot d^2 + 100.0)^{0.5}) \cdot 2$$

$$d_{BC} := \begin{bmatrix} 0 \\ -0.1 \\ -0.2 \\ -0.3 \\ -0.4 \end{bmatrix}$$

$$x := (0.01 \cdot (-625.0 \cdot d_{BC}^2 + 100.0)^{0.5}) \cdot 2 \cdot m = \begin{bmatrix} 0.2 \\ 0.194 \\ 0.173 \\ 0.132 \\ 0 \end{bmatrix} m$$

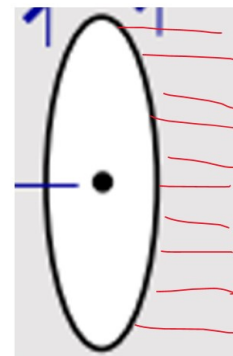
$$d_{CD} := \begin{bmatrix} 0.4 \\ 0.3 \\ 0.2 \\ 0.1 \\ 0 \end{bmatrix}$$

$$x := (0.01 \cdot (-625.0 \cdot d_{CD}^2 + 100.0)^{0.5}) \cdot 2 \cdot m = \begin{bmatrix} 0 \\ 0.132 \\ 0.173 \\ 0.194 \\ 0.2 \end{bmatrix} m$$

Calculamos la área

$$D_T := \begin{bmatrix} 0.6 \\ 0.6 \\ 0.6 \\ 0.6 \\ 0.6 \end{bmatrix} m$$

$$D_{BC} := - \begin{bmatrix} 0.2 \\ 0.194 \\ 0.173 \\ 0.132 \\ 0 \end{bmatrix} m + D_T = \begin{bmatrix} 0.4 \\ 0.406 \\ 0.427 \\ 0.468 \\ 0.6 \end{bmatrix} m$$





$$D_{CB} := - \begin{bmatrix} 0 \\ 0.132 \\ 0.173 \\ 0.194 \\ 0.2 \end{bmatrix} \text{ m} + D_T = \begin{bmatrix} 0.6 \\ 0.468 \\ 0.427 \\ 0.406 \\ 0.4 \end{bmatrix} \text{ m}$$

$$CC := \begin{bmatrix} 0.4 \\ 0.406 \\ 0.427 \\ 0.468 \\ 0.6 \end{bmatrix} \quad A_{BC} := 0.6 \cdot CC \cdot \text{m}^2 = \begin{bmatrix} 0.24 \\ 0.244 \\ 0.256 \\ 0.281 \\ 0.36 \end{bmatrix} \text{ m}^2$$

$$AL := \begin{bmatrix} 0.6 \\ 0.468 \\ 0.427 \\ 0.406 \\ 0.4 \end{bmatrix} \quad A_{CD} := 0.6 \cdot AL \cdot \text{m}^2 = \begin{bmatrix} 0.36 \\ 0.281 \\ 0.256 \\ 0.244 \\ 0.24 \end{bmatrix} \text{ m}^2$$

### Paso 3: Calcular las tensiones

#### a) Tensión en la sección

$$T_{12} := \frac{N_{12}}{A}$$

T : tensión

A : Área

N : Normal

#### A) Tramo A-B

$$T_{AB} := \frac{N_{12}}{A_{AB}} = -27.778 \frac{\text{ton}}{\text{m}^2}$$

#### B) Tramo B-C

$$T_{BC} := \frac{N_{12}}{A_{BC}} = \begin{bmatrix} -41.667 \\ -41.051 \\ -39.032 \\ -35.613 \\ -27.778 \end{bmatrix} \frac{\text{ton}}{\text{m}^2}$$



C) Tramo C-D

$$T_{CD} := \frac{N_{12}}{A_{CD}} = \begin{bmatrix} -27.778 \\ -35.613 \\ -39.032 \\ -41.051 \\ -41.667 \end{bmatrix} \frac{\text{ton}}{\text{m}^2}$$

C) Tramo D-E

$$T_{DE} := \frac{N_{12}}{A_{DE}} = -27.778 \frac{\text{ton}}{\text{m}^2}$$