

CS 162 Programming languages

Lecture 14: Environment and Closure

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Variables and bindings

```
#let x = 2+2;  
val x : int = 4
```

```
let x = e;;
```

“Bind the value of expression e to the variable x”

Variables and bindings

```
# let x = 2+2;;  
val x : int = 4  
# let y = x * x * x;;  
val y : int = 64  
# let z = [x;y;x+y];;  
val z : int list = [4;64;68]
```

Most recent “bound” value used for evaluation

Sounds like C/Java? **No!**

Environment and evaluation

ML begins in a “top-level” environment

```
let x = e;;
```

ML program = **Sequence of variable bindings**

Program evaluated by evaluating bindings in order

1. Evaluate expr e in current env to get value v
2. Extend env to bind x to v
3. Repeat with next binding

Example

```
# let x = 2+2;;  
val x : int = 4
```

```
# let y = x * x * x;;  
val y : int = 64
```

```
# let z = [x;y;x+y];;  
val z : int list = [4;64;68]
```

```
# let x = x + x ;;  
val x : int = 8
```

...	...
-----	-----

...	...
x	4:int

...	...
x	4:int
y	64:int

...	...
x	4:int
y	64:int
z	[4;64;68] : int list

...	...
x	4:int
y	64:int
z	[4;64;68] : int list
x	8:int

New binding! →

Environments

1. Evaluate: Use most recent bound value of var
2. Extend: Add new binding at end

How is this different from C/Java's “store” ?

```
# let x = 2+2;;  
val x : int = 4
```

```
# let f = fun y -> x + y;  
val f : int -> int = fn
```

```
# let x = x + x ;  
val x : int = 8
```

```
# f 0;  
val it : int = 4
```

...	...
x	4:int

...	...
x	4:int
f	fn <code, *>: int->int

New binding:

- No change or mutation
- Old binding frozen in **f**

Environments

1. Evaluate: Use most recent bound value of var
2. Extend: Add new binding at end

How is this different from C/Java's “store” ?

```
# let x = 2+2;;  
val x : int = 4
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```
# let f = fun y -> x + y;  
val f : int -> int = fn
```

```
# let x = x + x ;  
val x : int = 8
```

```
# f 0;  
val it : int = 4
```

...	...
x	4:int

...	...
x	4:int
f	fn <code, *>: int->int

...	...
x	4:int
f	fn <code, *>: int->int
x	8:int

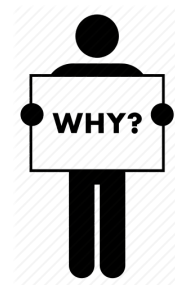
Cannot change the world

Cannot “assign” to variables

- Can extend the env by adding a fresh binding
- Does not affect previous uses of variable

Environment at fun declaration frozen inside fun “value”

- Frozen env used to evaluate application (f ...)



Why is this a good thing?

```
# let x = 2+2;;  
val x : int = 4  
# let f = fun y -> x + y;  
val f : int -> int = fn  
# let x = x + x ;  
val x : int = 8  
# f 0;  
val it : int = 4
```

...	...
x	4:int
f	fn <code, *>: int->int
x	8:int

Cannot change the world

Function behavior frozen at declaration

Q: Why is this a good thing?

- Nothing entered afterwards affects function
- Same inputs always produce same outputs
 - Localizes debugging
 - Localizes reasoning about the program
 - No “sharing” means no evil aliasing

Functions

Type `f : T1 -> T2`

f takes a value of type T1
and returns a value of type T2

Value of function: Closure

- “Body” expression not evaluated until application
 - but type-checking takes place at compile time
 - i.e. when function is defined
- Function value =
 - (code + environment at definition)
 - “closure”

```
# let x = 2+2;;  
val x : int = 4  
# let f = fun y -> x + y;  
val f : int -> int = fn  
# let x = x + x ;  
val x : int = 8  
# f 0;  
val it : int = 4
```

...	...
x	4:int
f	fn <code, *>: int->int
x	8:int

Values of function application

Application: function call or β -reduction

$(e_1 \ e_2)$

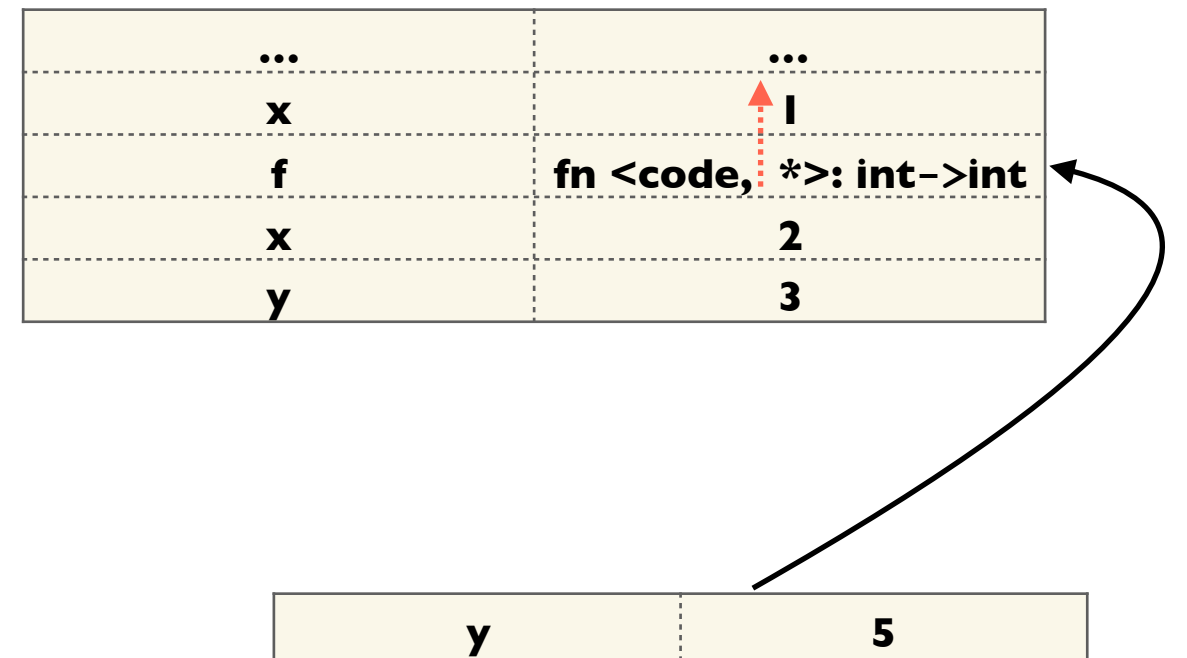
Apply argument e_2 to function e_1

Application Value:

1. Evaluate e_1 in current env to get (function) v_1
 - v_1 is code + env
 - code is (formal x + body e) , env is E
2. Evaluate e_2 in current env to get (argument) v_2
3. Evaluate body e in env E extended by binding x to v_2

Example 1

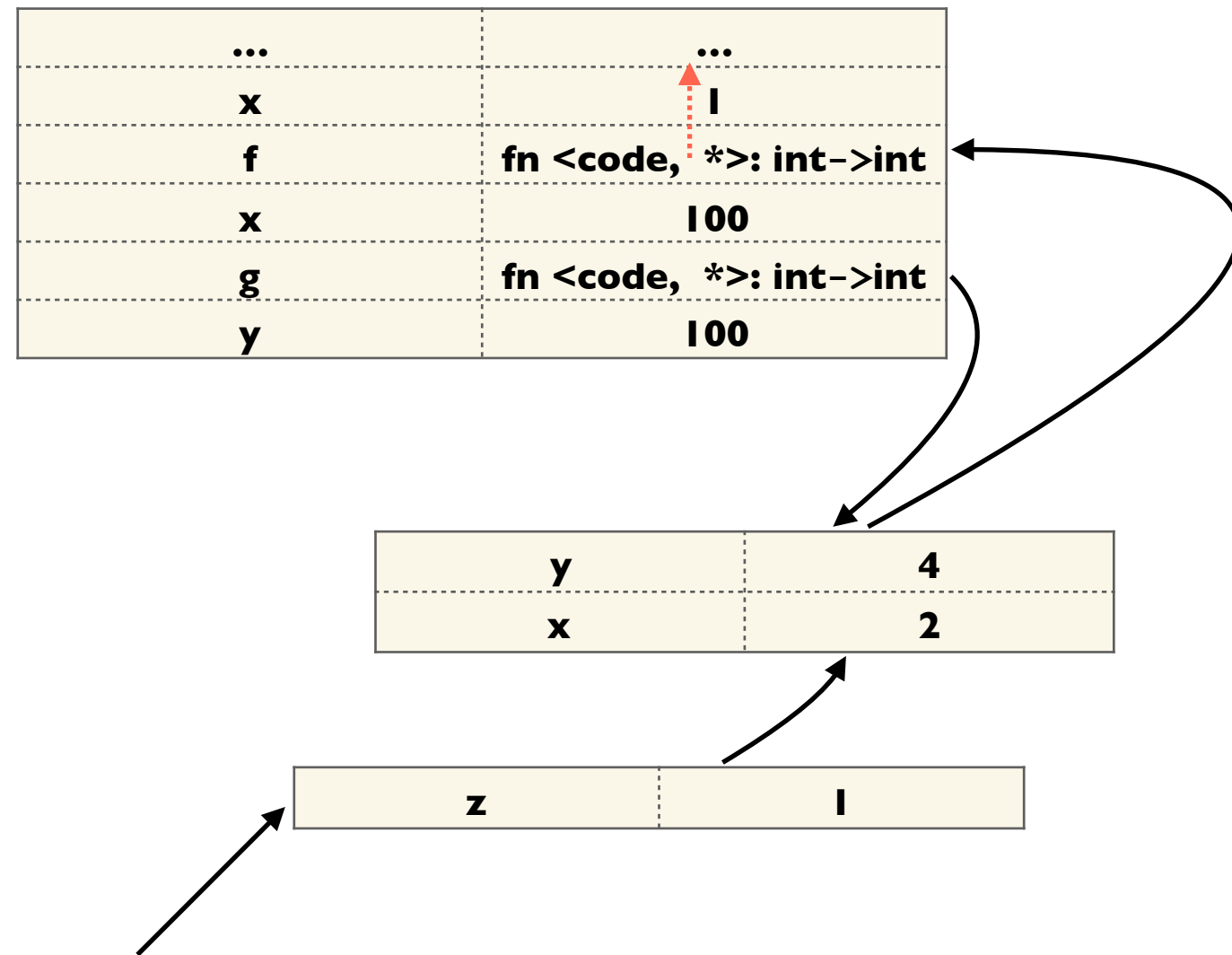
```
let x = 1;;  
let f y = x + y;;  
let x = 2;;  
let y = 3;;  
f (x + y);;
```



Evaluate body of f in this Env

Example 2

```
let x = 1;;  
let f y =  
  let x = 2 in  
  fun z -> x + y + z  
;;  
  
let x = 100;;  
let g = (f 4);;  
let y = 100;;  
(g 1);;
```



Evaluate x+y+z