ELECTROESTÁTICA E

CONSERVATIVO

LEY DE GAUSS

$$\oint \vec{E} \cdot d\vec{s} = \frac{\sum q_{int}}{\epsilon_o}$$

(superficie cerrada)

$$\oint \vec{B} \cdot d\vec{s} = 0 \quad (sup \ u mada)$$

LEY DE AMPÈRE

$$\oint_{\Gamma} \vec{B} d\vec{r} = M_0 \sum_{\text{int}} I_{\text{int}}$$
(dinea cerrada)

Escojo como línea (p) una circunferencia centrada en el hilo.

BÍDI = Mo. I = B

BZTTR = Mo I = $B = \frac{\mu_0}{2\pi R}$.

BOBINA, SOLENOIDE, INDUCTANCIAS



$$\Rightarrow \int \vec{\beta} \vec{B} \cdot d\vec{r} = B.\ell$$

$$\int_{\Gamma} \vec{B} d\vec{r} = \int_{A}^{B} \vec{B} d\vec{r}$$

$$\int_{B} \overrightarrow{B} d\vec{r} = \int_{A}^{B} \overrightarrow{B} d\vec{r}$$

$$\vec{B} \int_{A}^{B} d\vec{r} = B. \ell$$

$$B = \frac{\ell}{\mu \circ N I}$$

L = A-B

N= Nueltas = Nespiras

$$B = \frac{\mu_0 I}{2R}$$
 radio de la espira

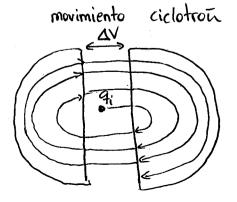
FUERZA SOBRE UNA CARGA PUNTUAL QUE SE MUEVE EN UNA REGIÓN EN LA QUE JB.

Fuerzas centripetas:
$$F = \frac{mv^2}{r}$$

$$F_m = qvB$$

$$\Rightarrow QVB = \frac{mV^2}{R} \Rightarrow \Gamma = \frac{mV}{4B}$$

$$T = \frac{2\pi r}{V} = \frac{2\pi m}{9B}$$



Fuerza magnética sobre corrientes eléctricas

$$\vec{F} = \vec{q} \vec{v} \times \vec{B}; \quad \vec{V} = \frac{d\vec{\ell}}{dt} \Rightarrow \vec{d} \vec{F} = dq \frac{d\vec{\ell}}{dt} \times \vec{B} = \vec{I} \cdot d\vec{\ell} \times \vec{B}$$

$$\int_{dF} \vec{F} = \vec{F} \cdot \vec{F} = \vec{I} \cdot d\vec{\ell} \times \vec{B} = \vec{I} \cdot d\vec{\ell} \times \vec{B}$$

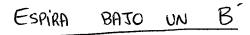
Fuerza magnética sobre un cable de longitud l con I bajo Buniforme

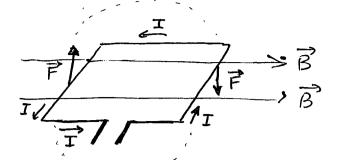
Fuerza magnética sobre un cable de longitud
$$\ell$$
 con I bajo f
 $\vec{B} \cdot \vec{B} \cdot \vec{B} = I \int_{\Gamma} (0,d\ell,0) \times (0,0,B) = I \int_{\Gamma} B d\ell \, \hat{\lambda} = I B \int_{\Gamma} d\ell \,$

FUERRA TOTAL: F= IBL = IB

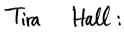
FUERTAS ENTRE DOS CORRIENTES PARALELAS

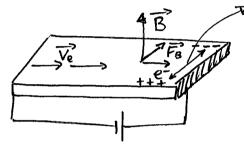
| F₁₂ sobre I₄ | F₁₃ sobre I₂ | I₄ crea B₄ | I₂ "siente" B₂ |
| I₄ | B₁ |
$$B_1$$
 | B_2 | B_1 | B_2 | B_1 | B_2 | B_1 | B_2 | B_1 | B_2 | B_3 | B_4 |





EFECTO HALL





 E_{Hall} $F_{B} = F_{e}$ cargas despl.

qvxB = q EHall

AVB = & EHall = D | EHALL = VB

VHall = E.d = VB.d

CAMPOS ELECTROMAGNÉTICOS

el tiempo ___ crea B E variable en B variable en el hiempo -> crea E

RECORDAR: FLUJO

LEY DE FARADAY

$$fem = \mathcal{E} = \Delta V = \frac{-d\phi_m}{dt}$$

Ejemplo

Un B uniforme forma un $\theta=30^{\circ}$ con el eje de la bobina N=300 y R=40 El B varia a razon de 85 Ts. Determinar la ε inducida en la bobina.

$$| f_{e,m} = \mathcal{E} - \Delta V = -\frac{d\phi_m}{dt}$$

 $\oint_{\mathbf{m}} = \int_{\mathbf{S}} \vec{B} \cdot d\vec{s}' = \left| B. ds. \cos \Theta \right| = B \cos \Theta \left| ds \right| = B \cos \Theta \cdot (\pi R^2) N$

$$\varepsilon = -\frac{d\Phi_m}{dt} = -\frac{d(B\cos\theta \pi R^2 N)}{dt} = -\pi R^2 N\cos\theta \cdot \frac{dB}{dt} = \frac{\sin\theta}{\theta}$$

=
$$- \pi R^2 \cos \theta$$
. $85 \pi / s = - \pi (0'04)^2$. $300. \cos 30^\circ$. $85 = -111 \sqrt{}$

$$\varepsilon = -\frac{d\Phi_m}{dt}$$

en mi circuito!

$$\Phi_{m} = \int_{S} \vec{B}' . d\vec{s}' = \int_{S} \vec{B} ds \cos\theta = B \cos\theta \int_{1}^{\infty} ds = B \cdot \hat{a}rea = B \cdot \hat{c} \cdot x$$

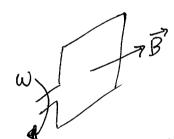
$$\mathcal{E} = -\frac{d\Phi_{m}}{dt} = -\frac{d(B.\ell.x)}{dt} = -B.\ell.x$$

$$I = \frac{E}{R} = \frac{B.l.v}{R}$$
 sentido antihorario

APLICACIÓN DE LA LEY DE FARADAY

▶ Generador de corriente alterna

V

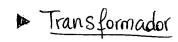


planina Pespira (a egira gira veloudadlar 1 0 = wt + 00 ángulo inicial

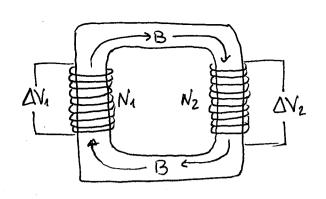
$$\phi_{m} = \int \vec{B} \cdot d\vec{s} = BS \cos\theta = BS \cos(\omega t + \theta_{0})$$

$$\mathcal{E} = -\frac{d\Omega_m}{dt} = -\frac{d}{dt} \left(BS \cos(\omega t + \theta_0) \right) = -B.S. \frac{d}{dt} \left(\cos(\omega t + \theta_0) \right) = D$$

$$= D \left[\mathcal{E} = B.S. \omega \operatorname{sen}(\omega.t + \theta_0) \right]$$







flujo El material magnético nos asegura que:

Nor espira 1
$$\Rightarrow \varphi_{e_1} = \varphi_{e_2} \leftarrow \frac{\text{flujo por}}{\text{espira 2}} \Delta V_1 = -\frac{\text{d}\varphi_{b_1}}{\text{d}t} = -N_1 \cdot \frac{\text{d}\varphi_e}{\text{d}t}$$

flujo

bohina 1 $\Rightarrow \varphi_{b_1} = N_1 \cdot \varphi_e$

$$\Delta V_2 = \frac{-\text{d}\varphi_{b_2}}{\text{d}t} = -N_2 \cdot \frac{\text{d}\varphi_e}{\text{d}t}$$
 (2)

flujo
behina 1
$$\rightarrow \Phi_{b_1} = N_1 \cdot \Phi_{e}$$

 $\Phi_{b_2} = N_2 \cdot \Phi_{e}$

$$\Delta V_A = -\frac{\partial \phi_{bA}}{\partial t} = -N_A \cdot \frac{\partial \phi_e}{\partial t} \quad (1)$$

$$\Delta V_2 = \frac{-d\phi_{b2}}{dt} = -N_2 \cdot \frac{d\phi_e}{dt}$$
 (2)

$$(1) \rightarrow \frac{-d\Phi_e}{dt} = \frac{\Delta V_A}{M_A}$$

$$(2) \rightarrow \frac{-d\Phi_e}{dt} = \frac{\Delta V_2}{N_2}$$

$$(1) \rightarrow \frac{-d\Phi_e}{dt} = \frac{\Delta V_A}{N_A}$$

$$(2) \rightarrow \frac{-d\Phi_e}{dt} = \frac{\Delta V_2}{N_2}$$

$$\Rightarrow \frac{\Delta V_A}{N_A} = \frac{\Delta V_2}{N_2}$$

$$\Rightarrow \frac{\Delta V_A}{N_A} = \frac{\Delta V_2}{N_2}$$

INDUCCION MUTUA

Sean dos circuitos Co y Cz corriente que de pen de del tiempo.

$$B_{2}(t)$$
 $B_{2}(t)$
 E_{4}

y por uno circula una

Paz = Maz Iz/

$$\varepsilon_1 = -M_{12} \frac{dI_2}{dt} = \frac{-d\phi_{12}}{dt}$$
 produce sobre 1.

$$S.I[M_{12}] = \frac{T.m^2}{A} = H \text{ (henrio)}$$

HUTOINDUCCION

COEFICIENTE DE AUTOINDUCCIÓN

Analogamente
$$\phi_{12} = M_{12}I_2$$

$$\phi = LI$$

$$L = \frac{\phi}{I}$$

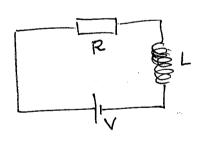
COEFICIENTE INDUCTANCIA

Coeficiente de autoinducción de una bobina

$$L = \frac{\phi}{T} = \mu_0 n N \pi r^2 = \mu_0 \frac{N^2}{e} \pi r^2$$

BOBINAS EN CIRCUITOS

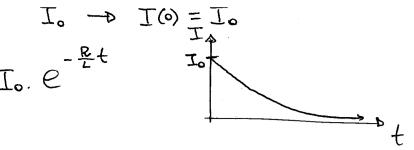
INDUCTANCIAS



$$I(t) = \frac{1}{R} \left(1 - e^{-\frac{R}{L} \cdot t} \right) = \frac{1}{R} \left(1 - e^{-\frac{R}{L} \cdot t} \right)$$

$$I(t) = \frac{1}{R} \left(1 - e^{-\frac{R}{L} \cdot t} \right) = \frac{1}{R} \left(1 - e^{-\frac{R}{L} \cdot t} \right)$$

$$\Rightarrow I = I_0 \cdot e^{-\frac{R}{L}t}$$



Energía almacenada en una bobina: $|U_m = \frac{1}{2} \cdot L \cdot I^2$

en t=0 cerramos el interruptor

a) I para
$$t \rightarrow \infty$$

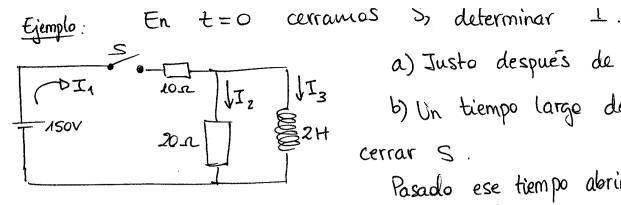
c) ¿ Cuanto tiempo (medido en m Ts) hasta que la I alcanta el 99% de su valo final?

d) c'Energía almacenada en la bobina?

a)
$$I_F = \frac{V}{R} = \frac{12}{15} = \frac{0.8 \text{ A}}{15}$$

b)
$$T = \frac{L}{R} = \frac{5.10^{-3}}{1.5} = \frac{3^{1}33.10^{-4}}{1.5}$$

d)
$$U_m = \frac{1}{2} \cdot L \cdot I^2 = 16.10^{-3} J$$



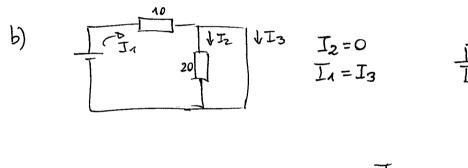
- a) Justo después de cerrar S
- VI2 VI3 b) Un tiempo largo después de cerrar S.

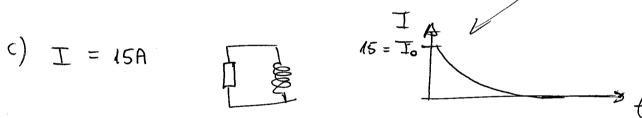
Pasado ese tiempo abrimos S.

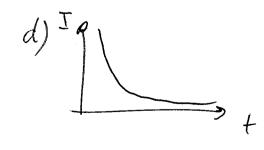
c) I justo después de abrirlo.

d) that desgrette I un t largo después de abrir

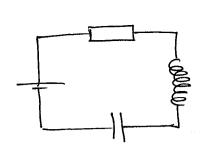
a)
$$I_3 = 0$$
 $I_4 = I_2$







 $I_1 = I_2 = I_3 = 0$ después de un tiempo largo la intensidad tiende a cero.



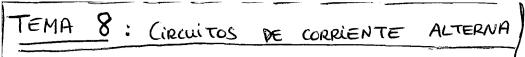
Hmplitud de bobina

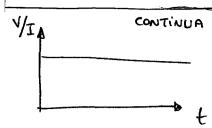
Condensador

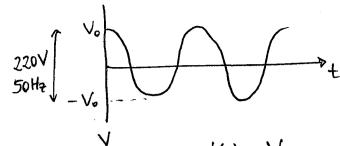
Frecuencia

RES-BAJA

RES-ALTA







$$V(t) = V_o \cdot sen(\omega t)$$

$$V(t) = V_0.\cos(\omega t + \frac{\pi}{2})$$

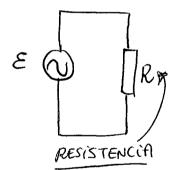
$$V_0 \simeq V_{\text{max}} = \frac{V_{\text{pp}}}{2}$$

EFICACES VALORES

definición general

$$Veff = \frac{V_0}{VZ}$$

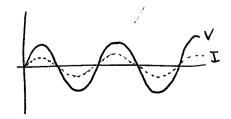
Veff =
$$\frac{V_0}{\sqrt{2}}$$
; $I_{eff} = \frac{I_0}{\sqrt{2}}$



$$\mathcal{E} = \mathcal{E}_{max} \operatorname{sen}(\omega t + \mathcal{U})$$

$$V_R = I.R \rightarrow I = \frac{V}{R} = \frac{E}{R} = \frac{E_{\text{max}} \text{ sen}(\text{wt + U})}{R}$$

$$\begin{cases} \mathcal{E} = \mathcal{E}_{\text{max}} \cdot \text{sen}(\omega t + Q) \\ I = \frac{\mathcal{E}_{\text{max}} \cdot \text{sen}(\omega t + Q)}{\mathcal{R}} \end{cases}$$

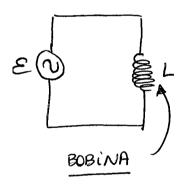


$$I = \frac{dQ}{dt} = C. \, \mathcal{E}_{\text{max}} . \, \omega. \, \cos(\omega t + \mathcal{U})$$

$$\int \mathcal{E} = \mathcal{E}_{\text{max}} \cdot \text{seu}(\omega t + \psi)$$

$$I = C \cdot \mathcal{E}_{\text{max}} \cdot \omega \cdot \text{sen}(\omega t + \psi + \frac{\pi}{2})$$

$$\chi_{c} = \frac{s}{c.\omega}$$
 reactancia capacitiva o capacitancia



Fuente de V
$$\mathcal{E} = \mathcal{E}_{\text{max}} \cdot \text{Sen}(\text{wt} + \mathcal{U})$$

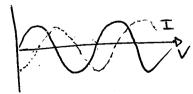
$$V_{L} = V_{\mathcal{E}} = L \cdot \frac{dI}{dt}$$

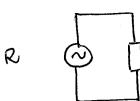
$$\frac{dI}{dt} = \frac{\varepsilon}{L} \implies I = \int \frac{\varepsilon}{L} dt = \int \frac{\varepsilon_{\text{max}}}{L} \cdot \text{Sen}(\omega t + \ell \ell) dt = \int \frac{\varepsilon}{L} dt = \int \frac{\varepsilon_{\text{max}}}{L} \cdot \text{Sen}(\omega t + \ell \ell) dt = \int \frac{\varepsilon}{L} dt = \int \frac{\varepsilon_{\text{max}}}{L} \cdot \text{Sen}(\omega t + \ell \ell) dt = \int \frac{\varepsilon}{L} dt = \int \frac{\varepsilon_{\text{max}}}{L} \cdot \text{Sen}(\omega t + \ell \ell) dt = \int \frac{\varepsilon}{L} dt = \int \frac{\varepsilon_{\text{max}}}{L} \cdot \text{Sen}(\omega t + \ell \ell) dt = \int \frac{\varepsilon}{L} dt = \int \frac{\varepsilon_{\text{max}}}{L} \cdot \text{Sen}(\omega t + \ell \ell) dt = \int \frac{\varepsilon}{L} dt =$$

$$= \frac{-\mathcal{E}_{\text{max}}}{\omega L} \cos(\omega t + U)$$

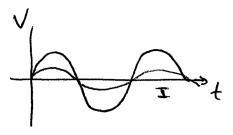
$$I = \frac{\varepsilon_{\text{max}}}{\omega \cdot L}$$
. Sen $\left(\omega t + \mathcal{U} - \frac{\pi}{2}\right)$

$$\begin{cases} \mathcal{E} = \mathcal{E}_{\text{max}} \cdot \text{sen}(\omega t + \mathcal{U}) \\ I = \frac{\mathcal{E}_{\text{max}}}{(\mathcal{V})} \cdot \text{sen}(\omega t + \mathcal{U} - \frac{\mathbb{T}}{2}) \end{cases}$$





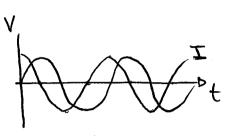
$$I = \frac{\varepsilon_{\text{max}}}{R} \cdot \text{sen}(\omega t + U)$$

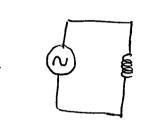


$$= I = \frac{\mathcal{E}_{\text{max}}}{[7/\omega.c]} \cdot \text{sen}(\omega + 1/2)$$

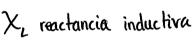
$$= \chi_{\text{c}} \cdot \text{reactancia capacitiva}$$

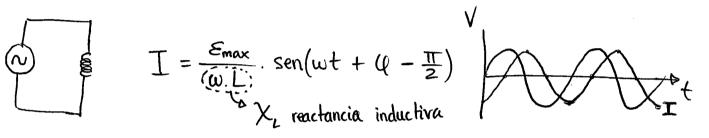






$$I = \frac{\varepsilon_{\text{max}}}{(\hat{\omega}.\hat{L})} \cdot \text{sen}(\omega t + (1 - \frac{\pi}{2}))$$



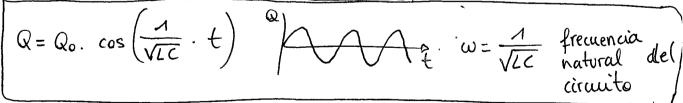


CIRCUITO LC SIN GENERADOR

$$C + V_L$$

$$\Rightarrow \left[\frac{d^2Q}{dt} + \frac{Q}{C} = 0 \right]$$

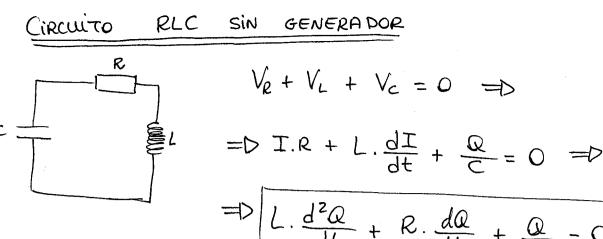
$$Q = Q_0$$
. $cos\left(\frac{1}{\sqrt{LC}} \cdot t\right)$



$$I = Io. Sen(\frac{1}{\sqrt{LC}} \cdot t)$$
; $\omega = \frac{1}{\sqrt{LC}}$

Corriente oscilante en el tiempo con una frecuencia de $\omega = \frac{1}{\sqrt{1 - \epsilon}}$

@Esto seria en un mundo ideal, en el que los cables, condensar y bobina No tenga resistencia.



$$\Rightarrow \left[L \cdot \frac{d^2Q}{dt} + R \cdot \frac{dQ}{dt} + \frac{Q}{C} = 0 \right]$$

$$Q(t) = Q_0 \cdot e^{-8t} \operatorname{sen}(\omega_{am} \cdot t + (I_0)) \qquad \delta = \frac{R}{2L}$$

$$\omega_{am}^2 = 0$$

$$\omega_{am}^2 = 0$$

$$\omega_{am}^2 = 0$$

Circuito RLC GENERADOR CON

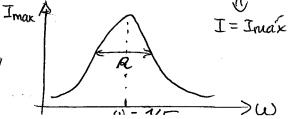
donde
$$U = \frac{\chi_L - \chi_c}{R}$$

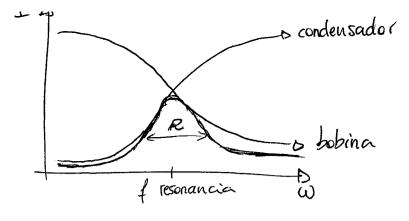
I max =
$$\frac{V_{\text{max}}}{\sqrt[3]{R^2 + (\chi_L - \chi_c)^2}}$$
 $7 = \sqrt{R^2 + (\chi_L - \chi_c)^2}$ impedancia total del circuito

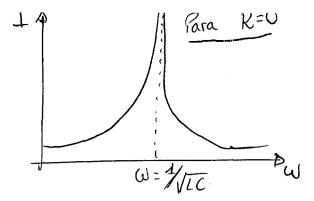
T será máx cuando z es mínimo => z es mínimo cuando (X1-Xc)?

T sera max cuando
$$\varepsilon$$
 cos mentros ε cos max cuando ε cos max cuando ε cos max cuando ε cos ε

$$\int_{\mathbb{R}^{2}} \mathbb{R} I = \frac{\varepsilon_{\text{max}}}{\sqrt{R^{2} + (\chi_{\iota} - \chi_{c})^{2}}} \cdot \text{Sen}(\omega t - u)$$





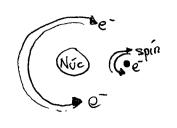


Potencia disipada en RLC?

Pdisipada_media = Ieff² · R

Observación

Propiedades magnéticas de la materia



paramagnéticos $\chi_m>0$ pequeña $\mu>$ ferromagnéticos $\chi_m>>>0$ $\mu>>>1$ diamagnéticos $\chi_m<0$ $\mu<1$

Xm>0 pequeña M>1

ermeabilidad nagnética ! medio

Xm - susceptibilidad magn. M - permeabilidad magn.
del medio

MATERIAL FERROMAGNÉTICO



orientar en dos direcciones dependiendo de la del campo magnético que le aplicamos. los podemos orientación

