

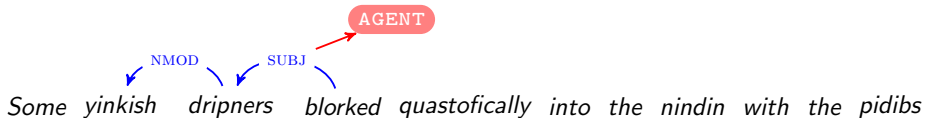
# L90: Overview of Natural Language Processing

## Lecture 9: Compositional Semantics

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Michaelmas 2020/21



syntax provides scaffolding for semantic composition

## Lecture 9: Compositional Semantics

1. Being able to transform
2. Semantic composition
3. Graph-based meaning representations
4. Inference and RTE

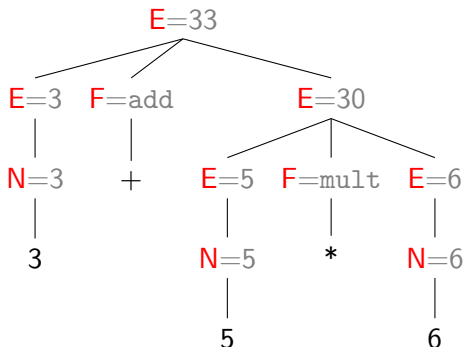
many slides  
are from  
Ann Copestake

Principle: Being Able to Transform

# Programming language interpreter

What is meaning of  $3 + 5 * 6$ ?

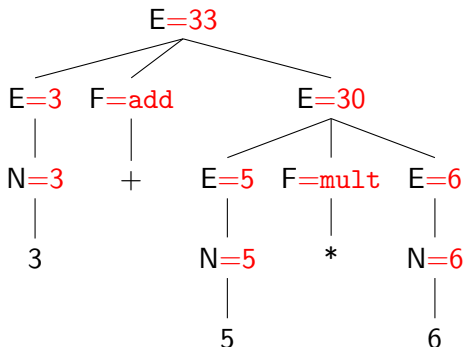
- First parse it into  $3 + (5 * 6)$
- Now give a meaning to each node in the tree (bottom-up)



# Programming language interpreter

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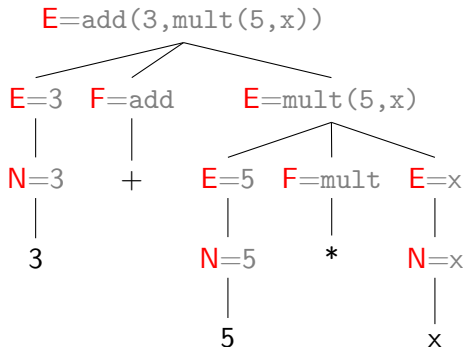
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# Interpreting in an environment

How about  $3 + 5 * x$ ?

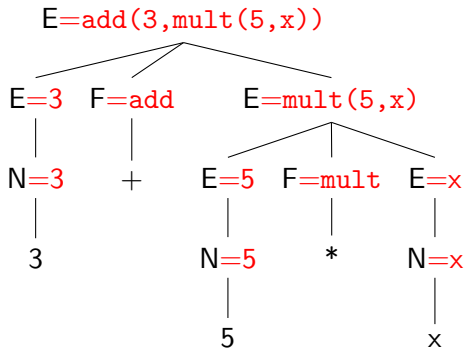
- Don't know  $x$  at compile time
- *Meaning* at a node is a piece of code, not a number



# Interpreting in an environment

How about  $3 + 5 * x$ ?

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*There is in my opinion no important theoretical difference between natural languages and the artificial languages of logicians; indeed, I consider it possible to comprehend the syntax and semantics of both kinds of languages within a single natural and mathematically precise theory.*

*Richard Montague, 1930–1971*



# What counts as understanding?

Characterizing what we mean by *meaning* is a difficult philosophical issue.

a compiler is a translator  
(formal language to formal language)

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Natural Language Understanding ▷ being able to translate

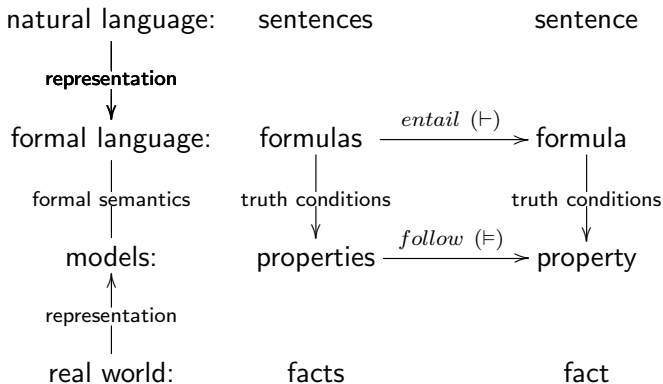
Natural language to natural language?

- Reasonable. Sometimes requires deeper understanding

Natural language to formal language (defined by logic)?

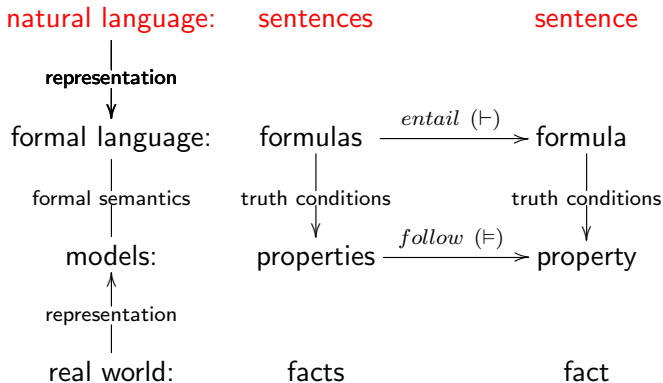
- Popular in NLP.

# The general picture



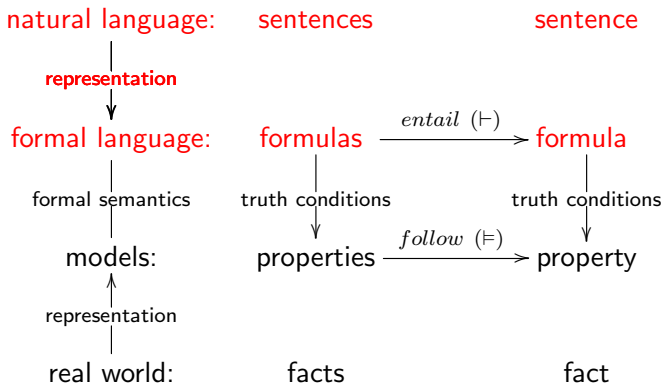
from Yanjing Wang

# The general picture



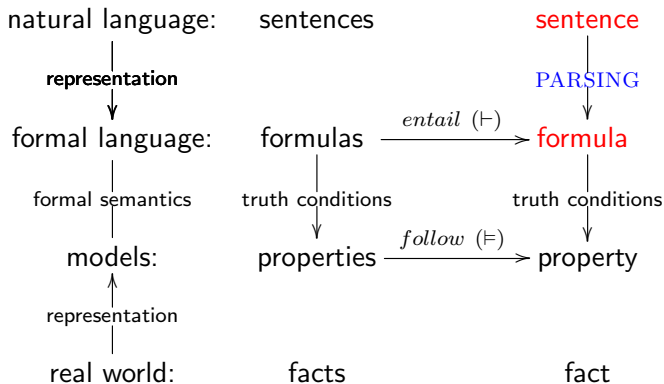
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# The general picture



from Yanjing Wang

# The general picture

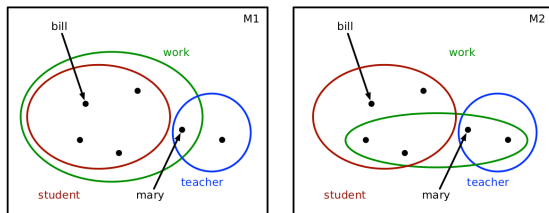


from Yanjing Wang

# Logic as a formal language

## Example

- $\llbracket \text{every student works} \rrbracket = \text{true}$  iff.  $\underline{\text{student}} \subseteq \underline{\text{work}}$
- $\text{every student works} \Rightarrow \forall x(\text{stud}'(x) \rightarrow \text{work}'(x))$



- Logic supports **precise**, **consistent** and **controlled** meaning representation via truth-conditional interpretation.
- Logic provides deduction systems to model **inference processes**, controlled through a formal entailment concept.
- Logic supports uniform modelling of the semantic **composition process**.

# Semantic Composition

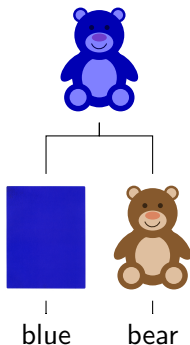


# Modeling syntactico-semantic composition

## The Principle of Compositionality

*The meaning of an expression is a function of **the meanings of its parts** and of **the way they are syntactically combined**.*

*B. Partee*

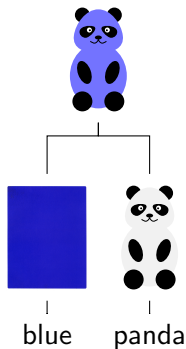


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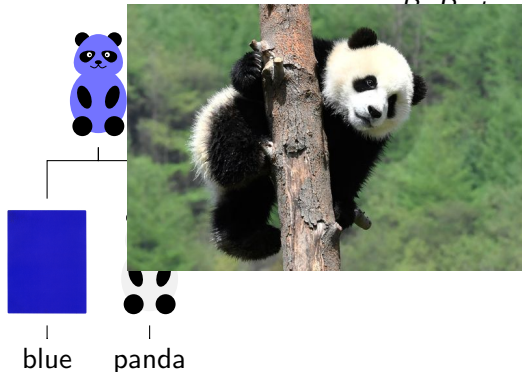
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# Modeling syntactico-semantic composition

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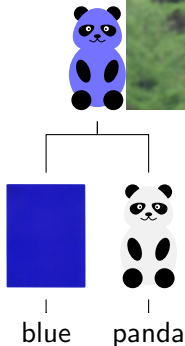
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# Modeling syntactico-semantic composition

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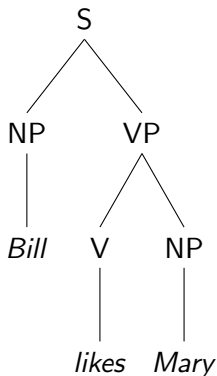
# Rule-to-rule translation

Syntactic parsing + Lexical interpretation



Meaning representation

## Example



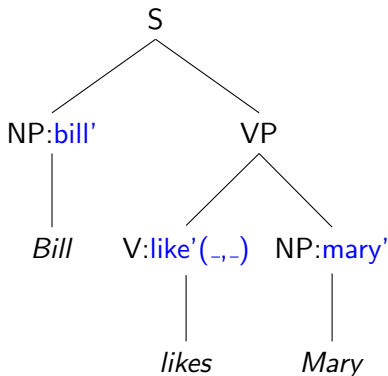
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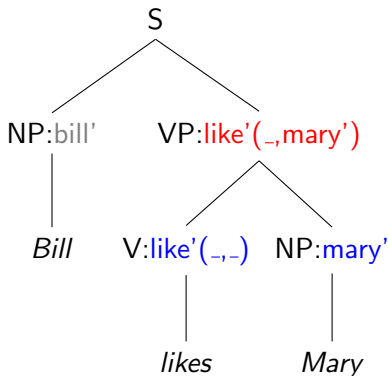
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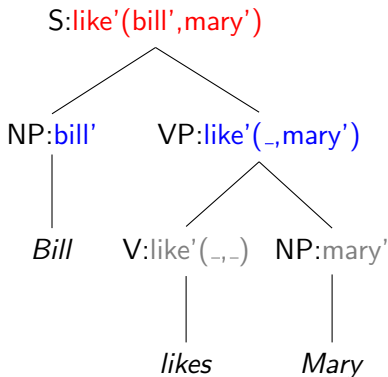
# Rule-to-rule translation

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Meaning representation

## Example





# Using $\lambda$ 's

- **Church** defined an idealized programming language called the  *$\lambda$ -calculus*.
- A formal system in mathematical logic. A model of computation.
- $\lambda$ -reduction:
  - $\lambda x[\text{sleep}'(x)](\text{john}')$  becomes  $\text{sleep}'(\text{john}')$
  - $\lambda y[\lambda x.\text{love}'(x, y)](\text{pizza}')$  becomes  $\lambda x[\text{love}'(x, \text{pizza}')]$
  - $\lambda x[\text{love}'(x, \text{pizza}')](\text{john}')$  becomes  $\text{love}'(\text{john}', \text{pizza}')$

## Example

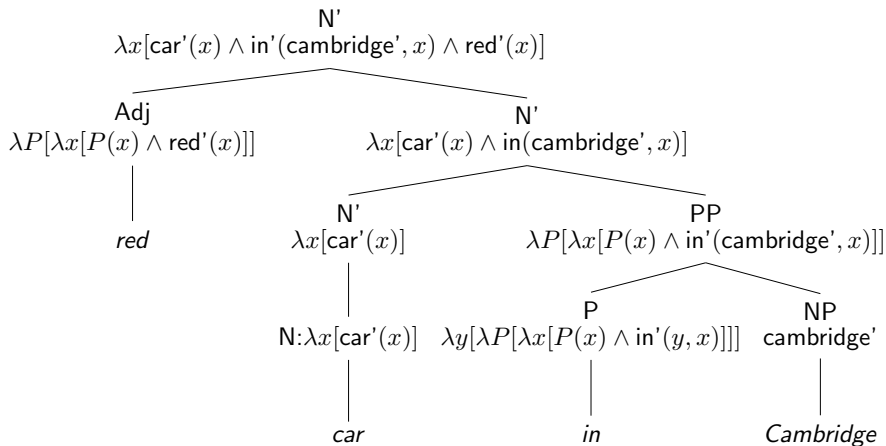
- $f(x) = x^2$   $\lambda x[x^2]$
- $f(5) = 25$   $\lambda x[x^2](5) = 25$
- $g(x, y) = x^2 + y^2$   $\lambda x[\lambda y[x^2 + y^2]]$
- $g(2, 1) = 5$   $(\lambda x[\lambda y[x^2 + y^2]](2))(1) = 5$

# Rule-to-rule translation

Syntactic parsing + Lexical interpretation



Meaning representation

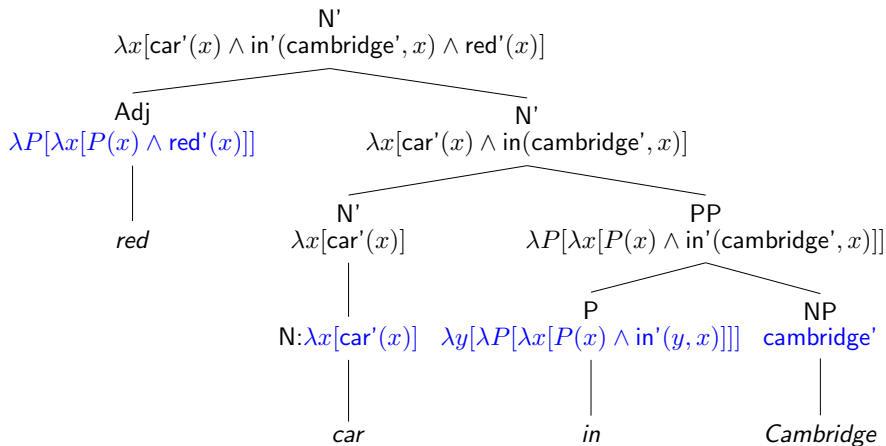


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Meaning representation

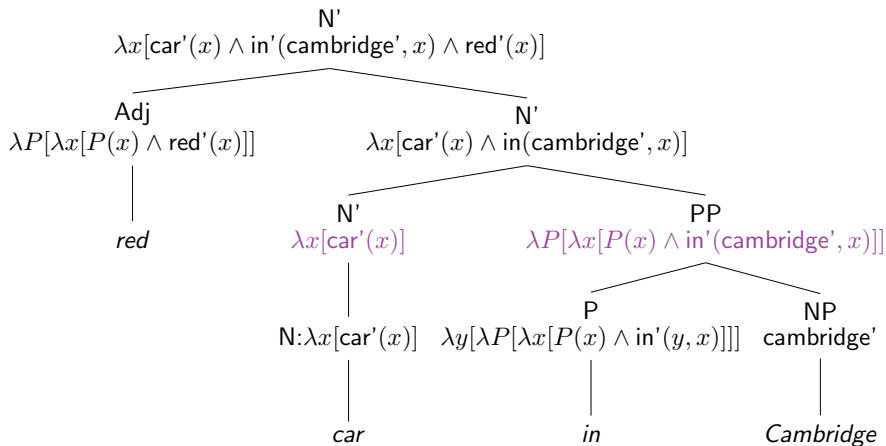


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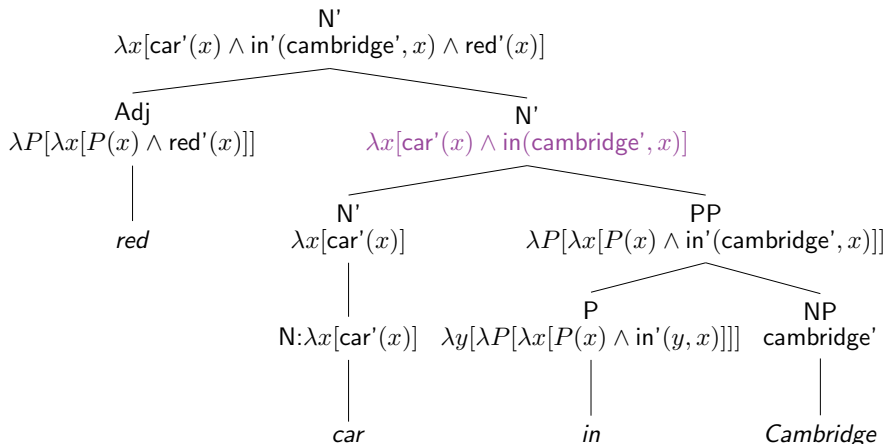


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Meaning representation

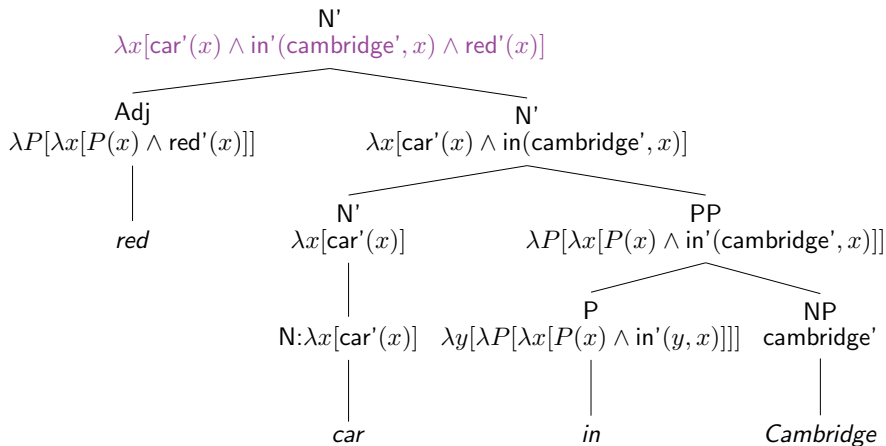


# Rule-to-rule translation

Syntactic parsing + Lexical interpretation



Meaning representation



# Semantic composition rules are non-trivial

Ordinary pronouns contribute to the semantics:

- (1) a. *It barked.*  
b.  $\exists x[\text{bark}'(x) \wedge \text{PRON}(x)]$

Pleonastic pronouns don't:

- (2) a. *It rained.*  
b. *rain'*

Similar syntactic structures may have different meanings. Different syntactic structures may have the same meaning:

- (3) a. *Kim seems to sleep.*  
b. *It seems that Kim sleeps.*

Differences in presentation but not in truth conditions.

## Beyond toy examples ...

Use first order logic where possible (e.g., event variables, next slide).

However, First Order Predicate Calculus (FOPC) is sometimes inadequate:  
e.g., *most*, *may*, *believe*.

Quantifier scoping multiplies analyses:

(4) a. *Every cat chased some dog*

b.  $\forall x[\text{cat}'(x) \rightarrow \exists y[\text{dog}'(y) \wedge \text{chase}'(x, y)]]$

c.  $\exists y[\text{dog}'(y) \wedge \forall x[\text{cat}'(x) \rightarrow \text{chase}'(x, y)]]$

Often no straightforward logical analysis e.g., Bare plurals such as *Ducks lay eggs*.

Non-compositional phrases (multiword expressions): e.g., *red tape* meaning bureaucracy.



## Event variables

Allow first order treatment of adverbs and PPs modifying verbs by *reifying* the event.

(5) a. *Rover barked*

b.  $\text{bark}'(r)$

c.  $\exists e[\text{bark}'(e, r)]$

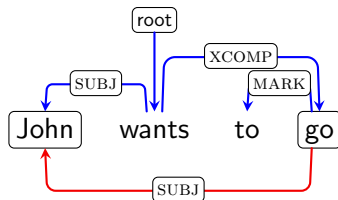
(6) a. *Rover barked loudly*

b.  $\exists e[\text{bark}'(e, r) \wedge \text{loud}'(e)]$

There was an event of Rover barking and that event was loud.

# Graph-Based Meaning Representations

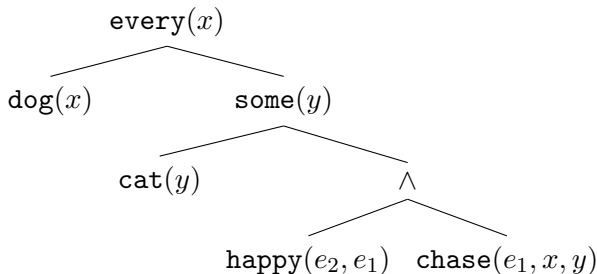
# Non-tree dependency structures



# Logical expression and semantic graph

- Every dog chases some cats.
- $\exists y(\text{cat}(y) \wedge \forall x(\text{dog}(x) \rightarrow \text{chase}(e, x, y)))$
- $\text{some}(y, \text{cat}(y), \text{every}(x, \text{dog}(x), \text{chase}(e, x, y)))$
- $\forall x(\text{dog}(x) \rightarrow \exists y(\text{cat}(y) \wedge \text{chase}(e, x, y)))$
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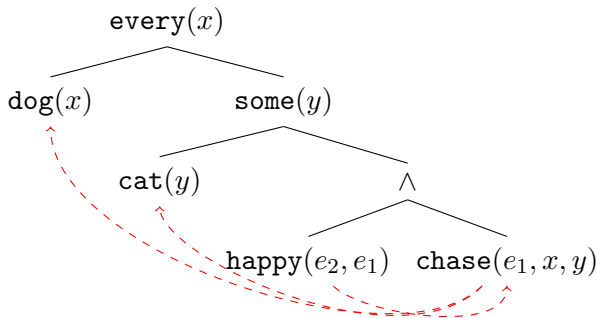
bracketing  $\Rightarrow$  tree



# Logical expression and semantic graph

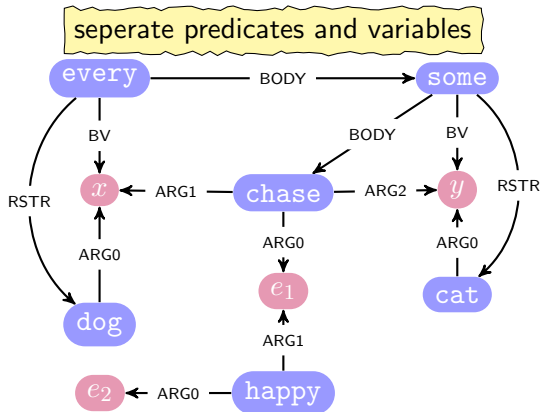
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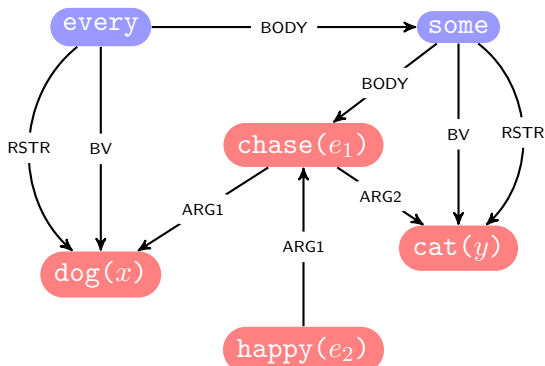
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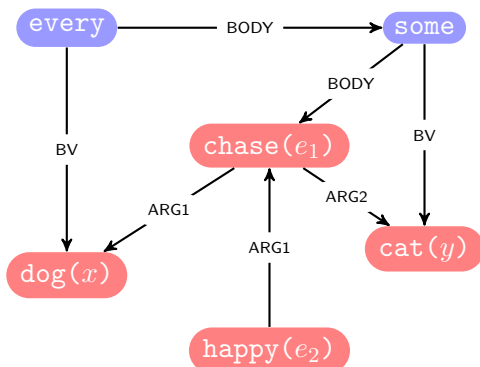
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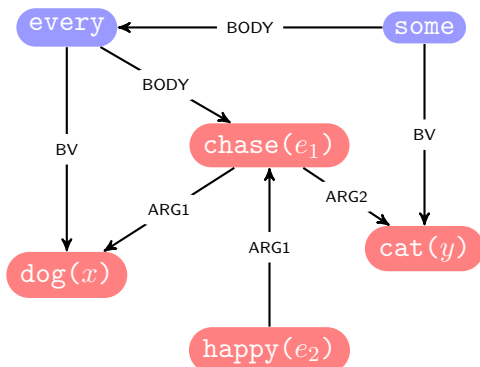
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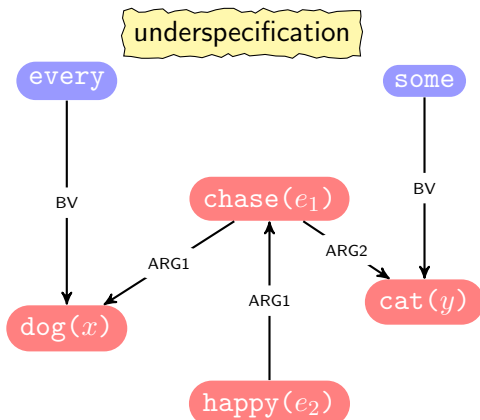
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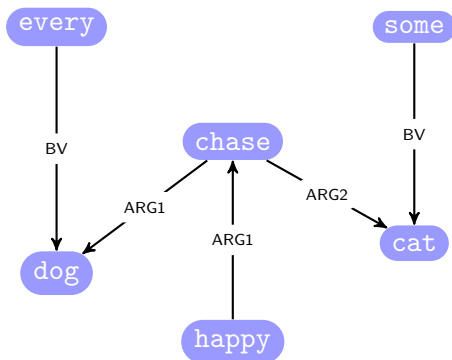
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# Inference and RTE

# Natural language inference

**Inference on a knowledge base:** convert natural language expression to KB expression, valid inference according to KB.

- 😊 Precise
- 😊 Formally verifiable
- 😊 Disambiguation using KB state
- 😞 Limited domain, requires KB to be formally encodable

**Language-based inference:** does one utterance follow from another?

- 😊 Unlimited domain
- 😊/😞 Human judgement
- 😞/😊 Approximate/imprecise

Both approaches may use logical form of utterance.

# Lexical meaning and meaning postulates

- Some inferences validated on logical representation directly, most require lexical meaning. What makes soup, soup?
- meaning postulates: e.g.,

$$\forall x[bachelor'(x) \rightarrow man'(x) \wedge unmarried'(x)]$$

- usable with compositional semantics and theorem provers, e.g.

*Kim is a bachelor*

$\Downarrow$

$bachelor'(kim')$

$\Downarrow$

$unmarried'(kim')$

- Problematic in general, OK for narrow domains or micro-worlds

# Recognising Textual Entailment (RTE) shared tasks

*T* The girl was found in Drummondville earlier this month.

*H* The girl was discovered in Drummondville.

- *Data*: pairs of text ( $T$ ) and hypothesis ( $H$ ).  $H$  may or may not follow from  $T$ .
- *Task*: label true (if follows) or false (if doesn't follow), according to human judgements.

## RTE using logical forms

- $T$  sentence has logical form  $T'$ ,  $H$  sentence has logical form  $H'$
- If  $T' \Rightarrow H'$  conclude true, otherwise conclude false.

$T$  The girl was found in Drummondville earlier this month.

$T'$   $\exists x, u, e[\text{girl}'(x) \wedge \text{find}'(e, u, x) \wedge \text{in}'(e, \text{drummondville}') \wedge \text{earlier-this-month}'(e)]$

$H$  The girl was discovered in Drummondville.

$H'$   $\exists x, u, e[\text{girl}'(x) \wedge \text{discover}'(e, u, x) \wedge \text{in}'(e, \text{drummondville}')] ]$

MP  $\text{find}'(x, y, z) \Rightarrow \text{discover}'(x, y, z)$

- So  $T' \Rightarrow H'$  and we conclude true



## More complex examples

- T Four Venezuelan firefighters who were traveling to a training course in Texas were killed when their sport utility vehicle drifted onto the shoulder of a highway and struck a parked truck.
- H Four firefighters were killed in a car accident.

Systems using logical inference are not robust to missing information: simpler techniques can be effective (partly because of choice of hypotheses in RTE).

## More examples

*T* Clinton's book is not a big seller here.

*H* Clinton's book is a big seller.

*T* After the war the city was briefly occupied by the Allies and then was returned to the Dutch.

*H* After the war, the city was returned to the Dutch.

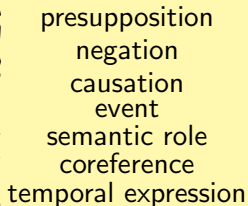
*T* Lyon is actually the gastronomic capital of France.

*H* Lyon is the capital of France.

## An example from a linguist

*T* The Commissioner doesn't regret that the President failed to make him leave Athens before May 2.

*H* The Commissioner was in Athens on May 2.



presupposition  
negation  
causation  
event  
semantic role  
coreference  
temporal expression

# Reading

- Ann's lecture notes.
- ACL tutorial on graph-based meaning representations  
<https://github.com/cfmrp/tutorial>