

## KRONECKER PRODUCT :

A is MATRIX  $m \times m$

B is MATRIX  $p \times q$

$A \otimes B$  is MATRIX  $mp \times mq$

$$A \otimes B = \begin{bmatrix} a_{11}B & \dots & a_{1m}B \\ \vdots & \ddots & \vdots \\ a_{m1}B & \dots & a_{mm}B \end{bmatrix}$$

FOR  $A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}$  AND  $B = \begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix}$

WE HAVE

$$A \otimes B = \begin{bmatrix} a_{11}b_{11} & a_{11}b_{12} & a_{12}b_{11} & a_{12}b_{12} \\ a_{11}b_{21} & a_{11}b_{22} & a_{12}b_{21} & a_{12}b_{22} \\ a_{21}b_{11} & a_{21}b_{12} & a_{22}b_{11} & a_{22}b_{12} \\ a_{21}b_{21} & a_{21}b_{22} & a_{22}b_{21} & a_{22}b_{22} \end{bmatrix}$$

## GEOMETRIC SERIES :

$$\sum_{n=0}^{\infty} \lambda^n A_x^n = 1 + \lambda A_x \sum_{n=0}^{\infty} \lambda^n A_x^n \Rightarrow \sum_{n=0}^{\infty} \lambda^n A_x^n = [I - \lambda A_x]^{-1}$$