b)
$$p(d=6|c=t) = \frac{1}{6}$$
 $p(th) = p(c=t) = \frac{1}{2}$
 $p(d=6|c=h) = \frac{5}{36}$ $[(1,5), (5,1), (3,3), (4,2), (2,4)]$

$$\frac{p(k=h) d=6)}{p(c=h) p(d=6|c=h)} + \frac{p(c=h) p(d=6|c=h)}{p(c=h) p(d=6|c=h)}$$

$$=\frac{5/36}{5/36+1/6}=\frac{5}{11}$$

a)
$$\lambda_{ML} = a_{3} max$$
 $P(\xi t_{n} \xi_{n=1}^{N} | \lambda) = a_{3} max$ $t_{3} p(\xi t_{n} \xi_{n=1}^{N} | \lambda)$ where

$$P(\xi t_{\lambda} \beta_{\lambda=1}^{N} | \lambda) = \frac{1}{\lambda^{N}} P(t_{\lambda} | \lambda) = \frac{1}{\lambda^{N}} exp(-\xi t_{\lambda} | \lambda)$$

b)
$$\frac{d}{d\lambda} \left[-N \log \lambda - \frac{1}{2} \int_{\lambda=\lambda_{mL}}^{\infty} d\lambda \right] = 0$$

$$-\frac{N}{\lambda_{\text{NL}}} + \frac{1}{\lambda_{\text{NL}}^2} \sum_{n=1}^{N} t_n = 0$$

=)
$$\lambda_{NL} = \frac{1}{N} \sum_{n=1}^{N} t_n$$

let
$$\sum_{N}^{(N)} = \frac{1}{N} \sum_{n=1}^{N} t_n = \frac{1}{N} S_N = \frac{N-1}{N} J_{NL} + \frac{1}{N} t_N$$

b)
$$\frac{d}{d\mu} \left[log pinton^2 \right] + log piytu] = 0$$

$$\frac{d}{d\mu} \left[-\frac{1}{20\mu^{2}} \mu^{2} + -\frac{1}{2} (y - \mu)^{2} \right] = 0$$

$$=)$$
 $MMAP = \frac{y}{1+1/5^2}$

a)
$$p(y, | X, w) = \frac{1}{1+e^{-wx+b}}$$

$$u = -10$$

b)
$$y_2 = y_1 (\xi \sigma_1 + \mu_1 + c_1 x) + (1-y_1)(\xi \sigma_2 + \mu_2 + c_2 x)$$

$$\sigma_1 = \frac{1}{2} \qquad \mu_1 = 2 \qquad \text{for } c_1 = 4 \qquad \text{approximate values}$$

$$\sigma_2 = \frac{1}{10} \qquad \mu_2 = -2 \qquad c_2 = -2 \qquad \text{are fine live}$$

P(y2/y,,x) = y, N(y2; C1x+M1, 0,2) + (1-y.) N(y2; C2x+M2, 0,2)

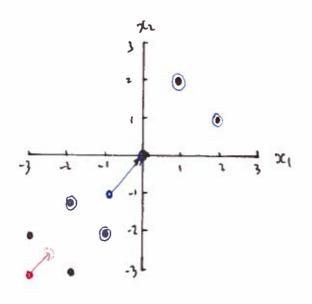
Assignment step

Sn = ary min 1 xn - MKI

(assign each data point in to rewest cluster k*)

Update Step

mean (xn sn=k) (update cluster centres mk to be wear of data points assigned to that chistor)



initial (-1,-1) (-3,-3) (0,0) (-2.5,-2.5) update 1 update 2 (1.5,1.5) (-2,-2)

a) $\alpha = 0.1$ as the KL divergence is minimized when $\alpha = P$

$$\frac{dKL}{d\alpha} = \left(-\frac{P_1}{\lambda} + \frac{2P_2}{1-2\alpha} - \frac{P_3}{\lambda} \right) = 0$$

$$=) \qquad \left(P_1 + P_3\right) \left(1 - 2\lambda^2\right) = 2P_2 x^*$$

$$\frac{P_1 + P_3}{2} = \alpha^{\vee}$$

$$=) \quad \angle^* = \underbrace{0.6 + 0.2}_{2} = 0.4$$

$$\frac{d^{2}}{d\lambda^{2}} = \frac{0.6}{(\chi^{*})^{2}} + \frac{0.4}{(1-2\lambda^{*})^{2}} + \frac{6.2}{(\chi^{*})^{2}} > 0 =) minim$$

a)
$$p(x_1, x_2) = p(x_1) p(x_2|x_1)$$

$$P(X_1=0, X_2=0) = 4/10 = 2/5$$

$$P(X_1=1, X_2=0) = 1/10$$

$$P(X_1=1, X_2=1) = 1/10$$

$$P(X_1=1, X_2=1) = 4/10 = 2/5$$

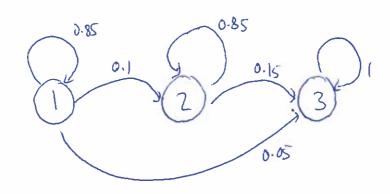
b)
$$p(y_1,y_2) = \sum_{x_1,x_2} p(x_1,x_2) p(y_1|x_1) p(y_2|x_2)$$

$$= \frac{2}{5} \cdot N(\begin{bmatrix} 31 \\ 32 \end{bmatrix}) \begin{bmatrix} -1 \\ -1 \end{bmatrix} + \frac{1}{10} \cdot N(\begin{bmatrix} 31 \\ 32 \end{bmatrix}) \begin{bmatrix} -1 \\ -1 \end{bmatrix} \underbrace{I} + \frac{2}{5} \cdot N(\begin{bmatrix} 31 \\ 32 \end{bmatrix}) \underbrace{I} \underbrace{I}$$

c) plg (17) is a mixture of Gaussians with 2T components each weighted by the probability of the latent segmence pixit) that produced them.

Q8

a



b) every the ends up in state 3
$$\begin{cases} p(Sm=1) \\ p(Sm=2) \end{cases} = \begin{cases} 0 \\ 0 \\ 1 \end{cases}$$