

# Caminata aleatoria

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## Informacion de contacto

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```
## Loading required package: zoo
```

```
##
```

```
## Attaching package: 'zoo'
```

```
## The following objects are masked from 'package:base':
```

```
##
```

```
##      as.Date, as.Date.numeric
```

# Caminata aleatoria

## Descripcion

Veamos el proceso:

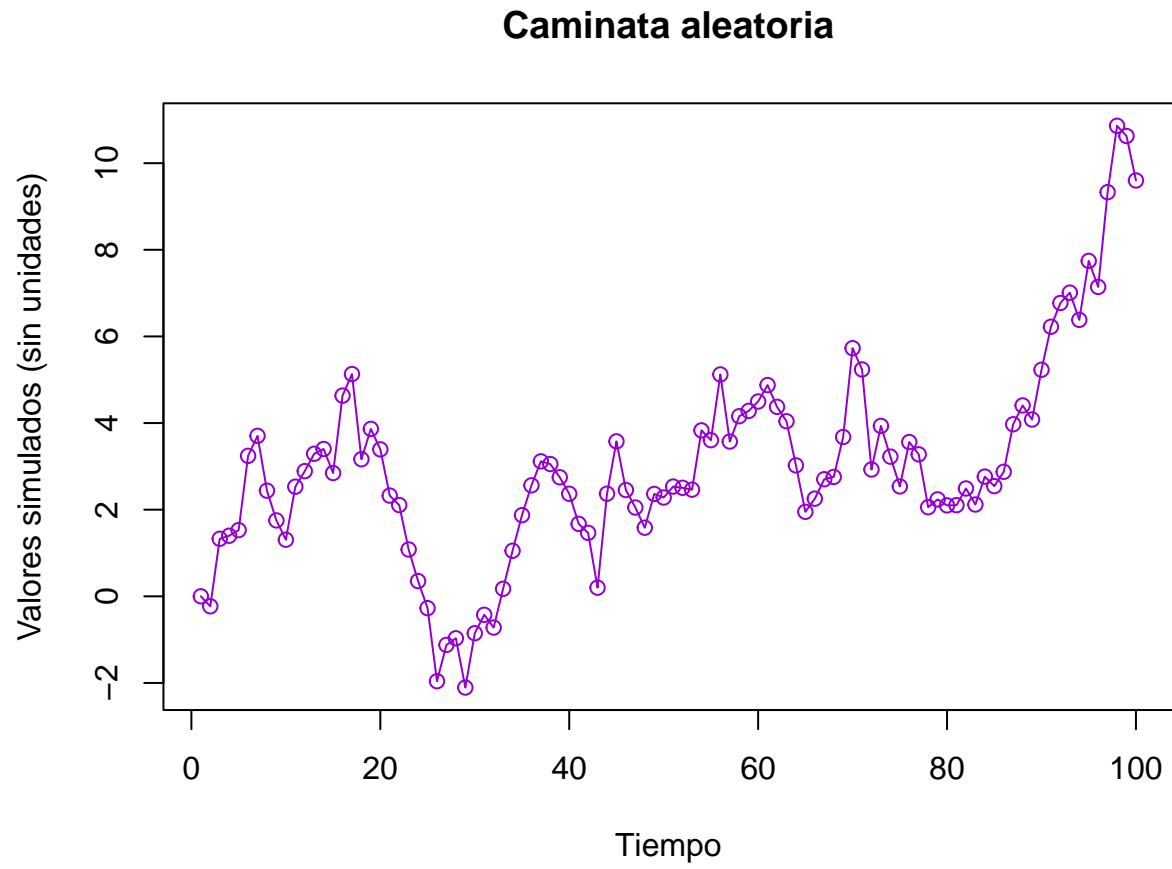
$$\begin{aligned}x_t &= x_{t-1} + Z_t \\Z_t &\sim N(0, 1) \\i &= 1, 2, \dots, 100\end{aligned}$$

Desplegando los valores de la serie que se simulara, creando funciones propias

```
## Time Series:
## Start = 1
## End = 100
## Frequency = 1
## [1] 0.0000000 -0.2301775 1.3285308 1.3990392 1.5283270 3.2433919
## [7] 3.7043081 2.4392469 1.7523941 1.3067321 2.5308139 2.8906277
## [13] 3.2913992 3.4020819 2.8462407 4.6331539 5.1310044 3.1643872
## [19] 3.8657431 3.3929517 2.3251280 2.1071531 1.0811486 0.3522574
## [25] -0.2727819 -1.9594752 -1.1216881 -0.9683150 -2.1064520 -0.8526370
## [31] -0.4261728 -0.7212443 0.1738814 1.0520149 1.8735959 2.5622362
## [37] 3.1161538 3.0542421 2.7482795 2.3678085 1.6731015 1.4651842
## [43] 0.1997879 2.3687438 3.5767058 2.4535972 2.0507124 1.5840570
## [49] 2.3640222 2.2806531 2.5339716 2.5054249 2.4625544 3.8311567
## [55] 3.6053857 5.1218563 3.5731035 4.1577173 4.2815715 4.4975131
## [61] 4.8771525 4.3748291 4.0416217 3.0230463 1.9512551 2.2547837
## [67] 2.7029935 2.7559977 3.6782652 5.7283499 5.2373187 2.9281499
## [73] 3.9338884 3.2246876 2.5366790 3.5622504 3.2774774 2.0567597
## [79] 2.2380631 2.0991718 2.1049360 2.4902164 2.1195563 2.7639329
## [85] 2.5434463 2.8752283 3.9720673 4.4072488 4.0813172 5.2301248
## [91] 6.2236287 6.7720256 7.0107574 6.3828513 7.7435037 7.1432442
## [97] 9.3305771 10.8631878 10.6274874 9.6010665
```

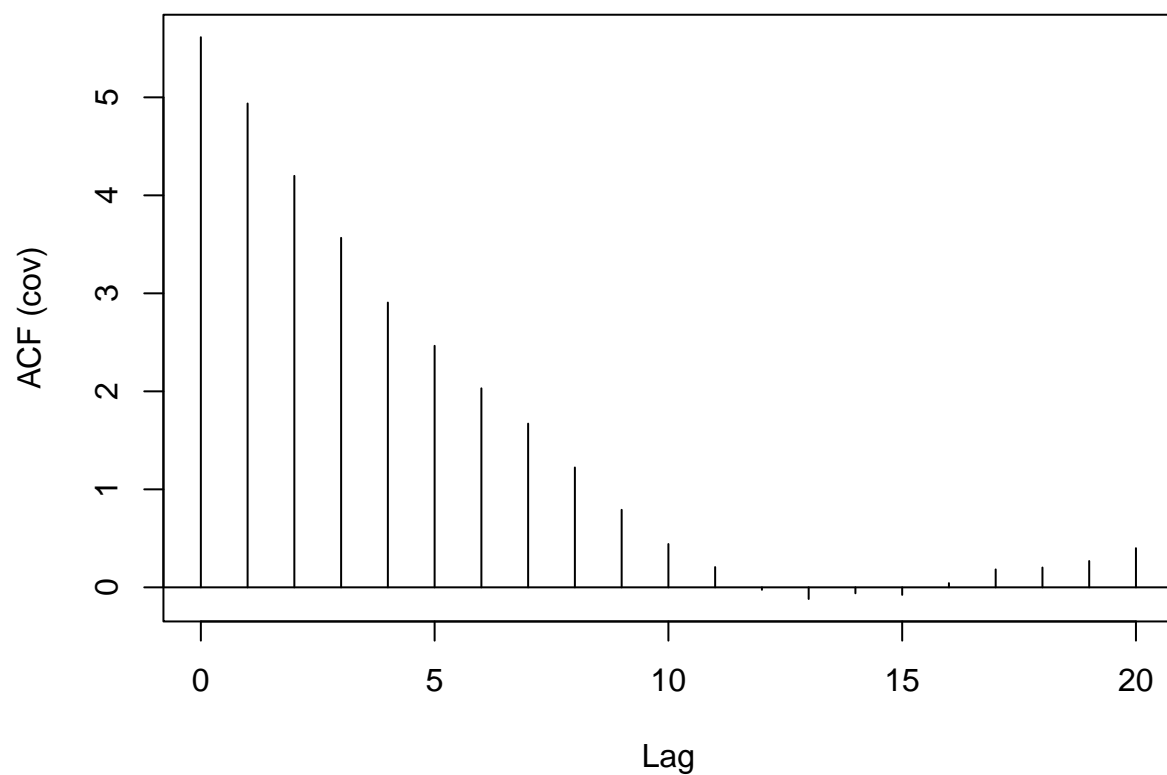
## Visualizacion de la caminata aleatoria

Viendo el grafico correspondiente



Funcion de autocovarianza (linea de comando)

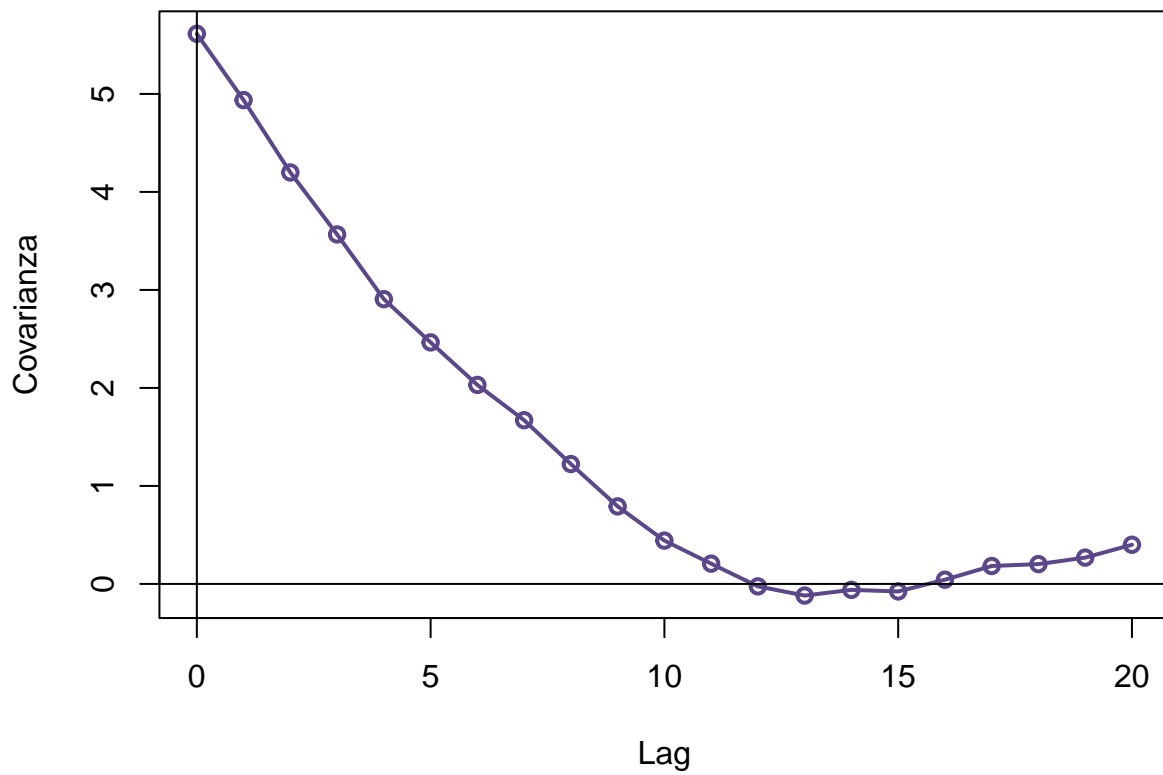
## Covarianza



```
##
## Autocovariances of series 'random_walk', by lag
##
##      0      1      2      3      4      5      6      7      8      9
## 5.6136 4.9370 4.1987 3.5662 2.9057 2.4643 2.0308 1.6704 1.2231 0.7908
##     10     11     12     13     14     15     16     17     18     19
## 0.4418 0.2066 -0.0252 -0.1188 -0.0607 -0.0768 0.0428 0.1828 0.2021 0.2686
##     20
## 0.3996
```

## Funcion de autocovarianza ACF (funcion propia)

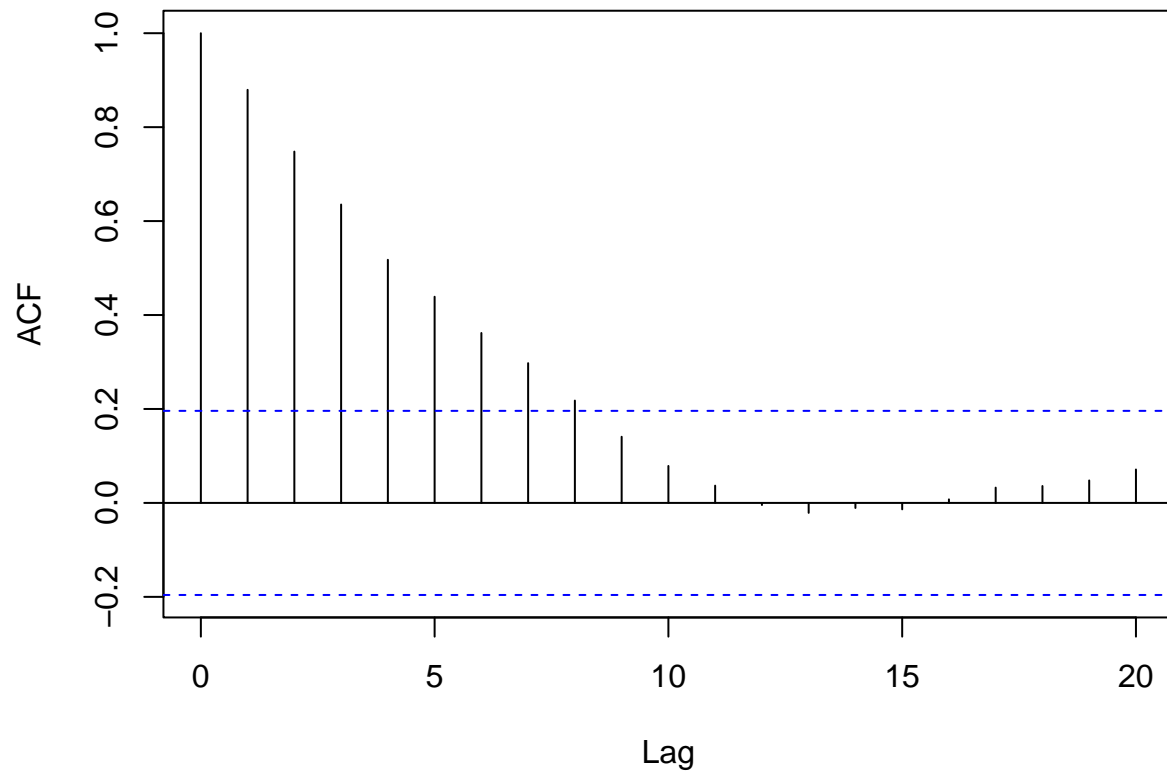
Programando la funcion de autocovarianza para comparar



```
## [1] 5.61361604 4.93697857 4.19866360 3.56615358 2.90565953 2.46426507
## [7] 2.03076975 1.67041840 1.22313850 0.79080219 0.44176616 0.20656990
## [13] -0.02517372 -0.11882969 -0.06065415 -0.07679099 0.04284598 0.18280084
## [19] 0.20212641 0.26855131 0.39964020
```

Funcion de autocorrelacion (linea de comando)

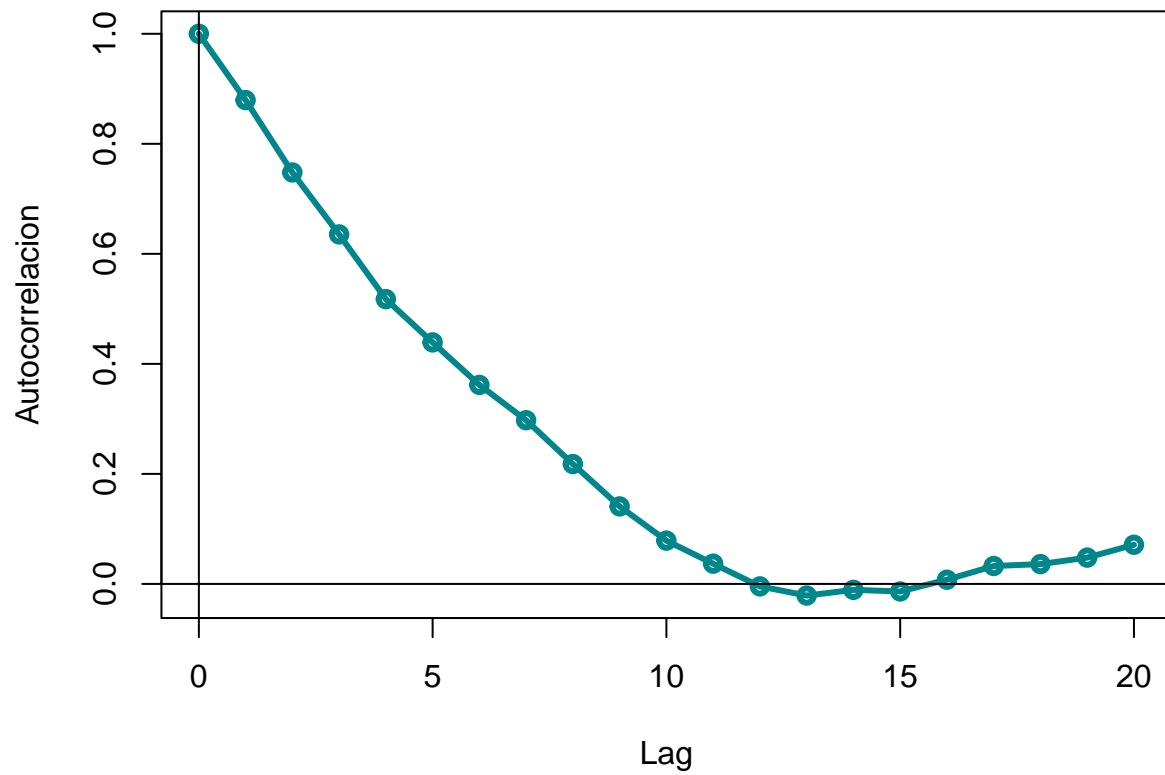
## Autocorrelacion



```
##
## Autocorrelations of series 'random_walk', by lag
##
##      0      1      2      3      4      5      6      7      8      9     10
## 1.000 0.879 0.748 0.635 0.518 0.439 0.362 0.298 0.218 0.141 0.079
##     11     12     13     14     15     16     17     18     19     20
## 0.037 -0.004 -0.021 -0.011 -0.014 0.008 0.033 0.036 0.048 0.071
```

## Funcion de autocorrelacion (funcion propia)

Programando la funcion de autocorrelacion para comparar

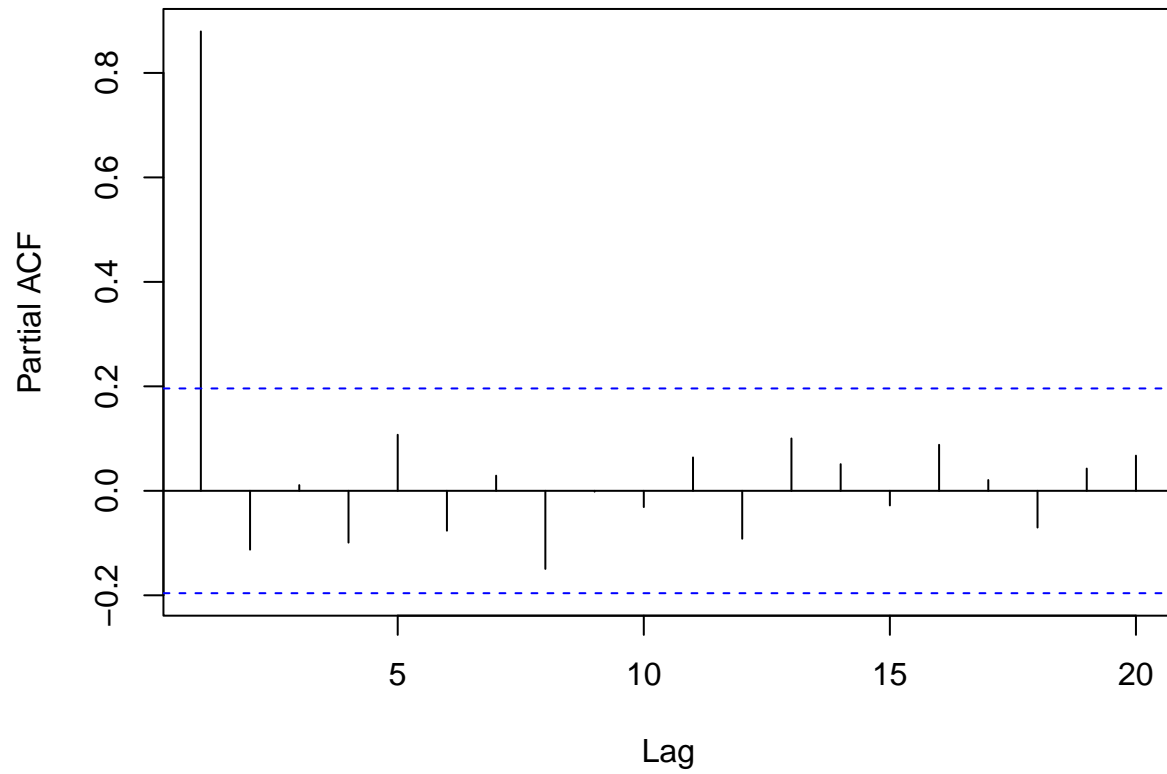


```
## [1] 1.000000000 0.879464954 0.747942783 0.635268525 0.517609239
## [6] 0.438979983 0.361757865 0.297565488 0.217887808 0.140872155
## [11] 0.078695471 0.036798010 -0.004484403 -0.021168118 -0.010804827
## [16] -0.013679416 0.007632509 0.032563830 0.036006455 0.047839274
## [21] 0.071191225
```



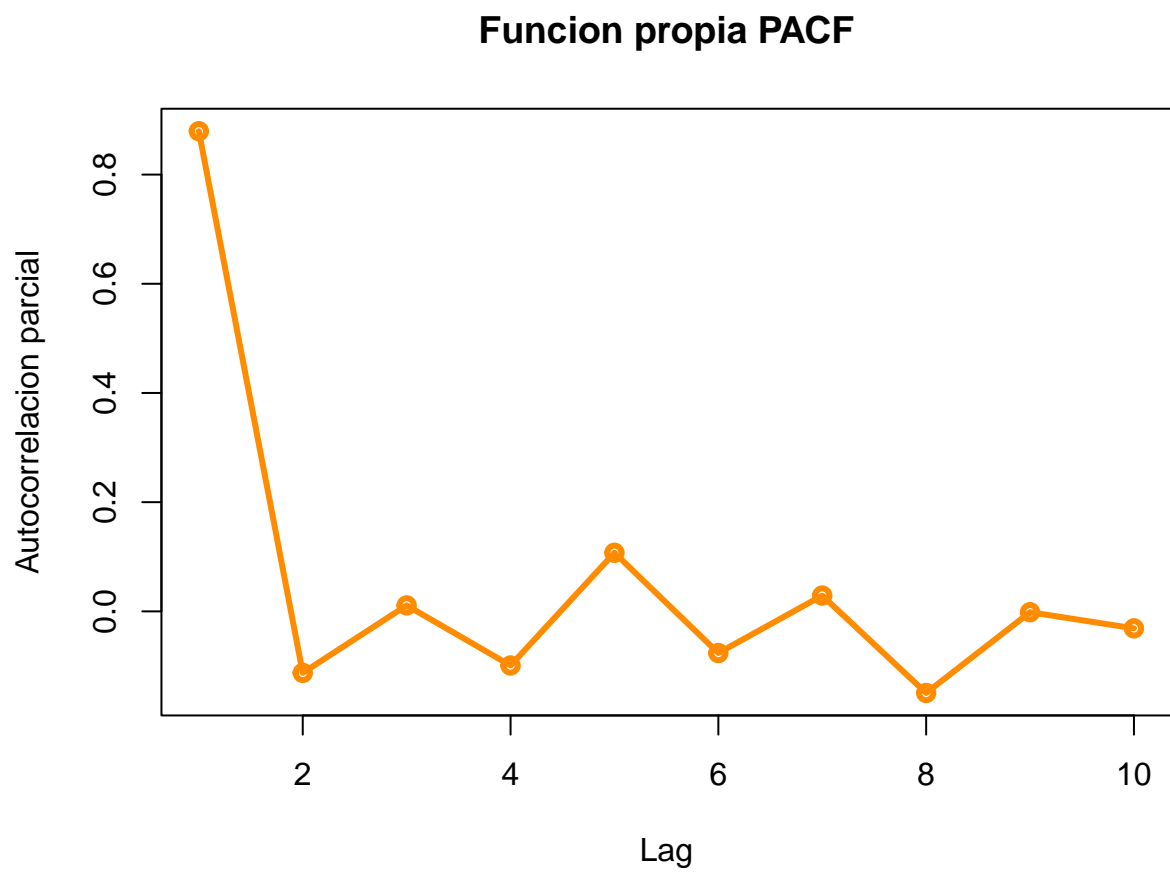
PACF por linea de comando

## Autocorrelacion



```
##
## Partial autocorrelations of series 'random_walk', by lag
##
##      1      2      3      4      5      6      7      8      9     10     11
## 0.879 -0.113  0.011 -0.099  0.107 -0.076  0.029 -0.149 -0.002 -0.031  0.064
##     12     13     14     15     16     17     18     19     20
## -0.092  0.100  0.051 -0.028  0.088  0.021 -0.070  0.043  0.067
```

PACF de forma manual (primeros 10 rezagos)



```
## [1] 0.879464954 -0.112632048 0.010939561 -0.099128816 0.107318297
## [6] -0.076334919 0.028978460 -0.149474449 -0.001520482 -0.031108977
```

## Quitando tendencia

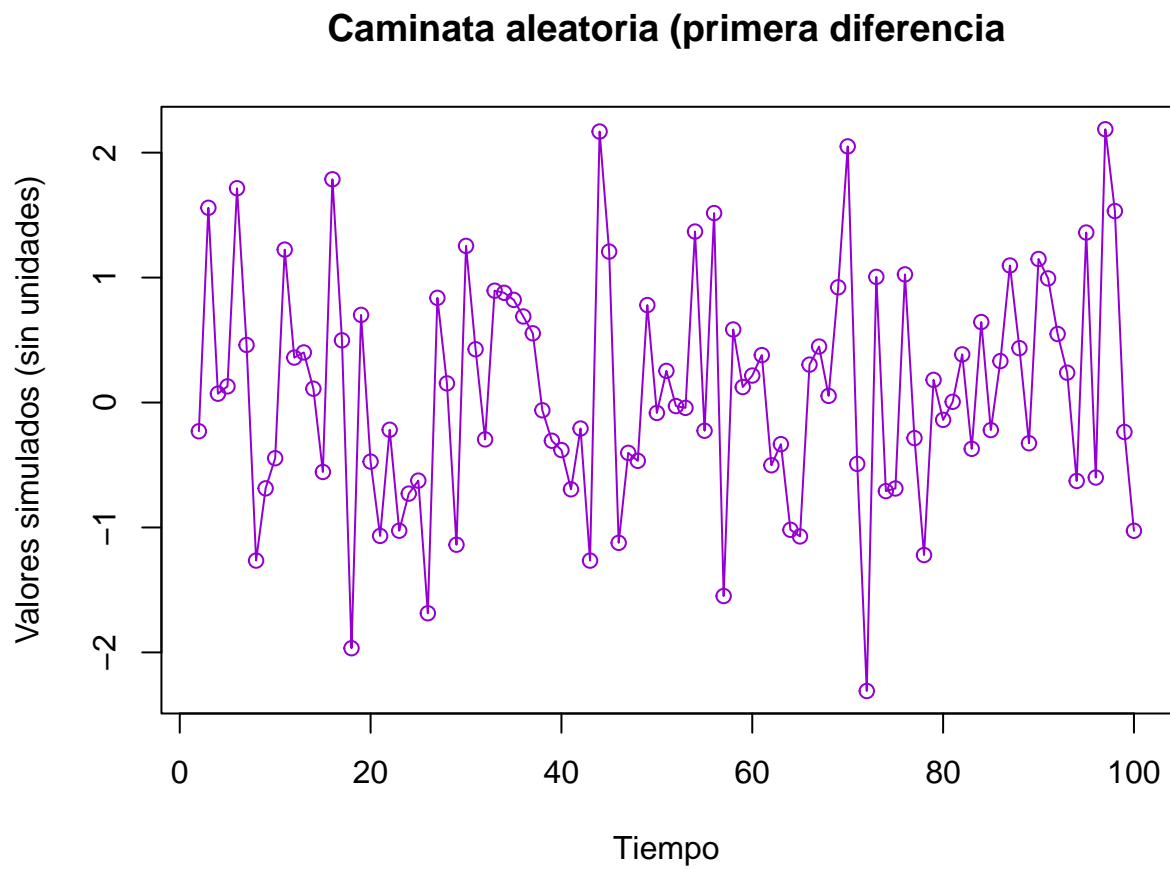
### Descripcion

Del proceso anterior:

$$\begin{aligned}x_t &= x_{t-1} + Z_t \\x_t - x_{t-1} &= Z_t \\ \nabla x_t &= Z_t \\ Z_t &\sim N(0, 1)\end{aligned}$$

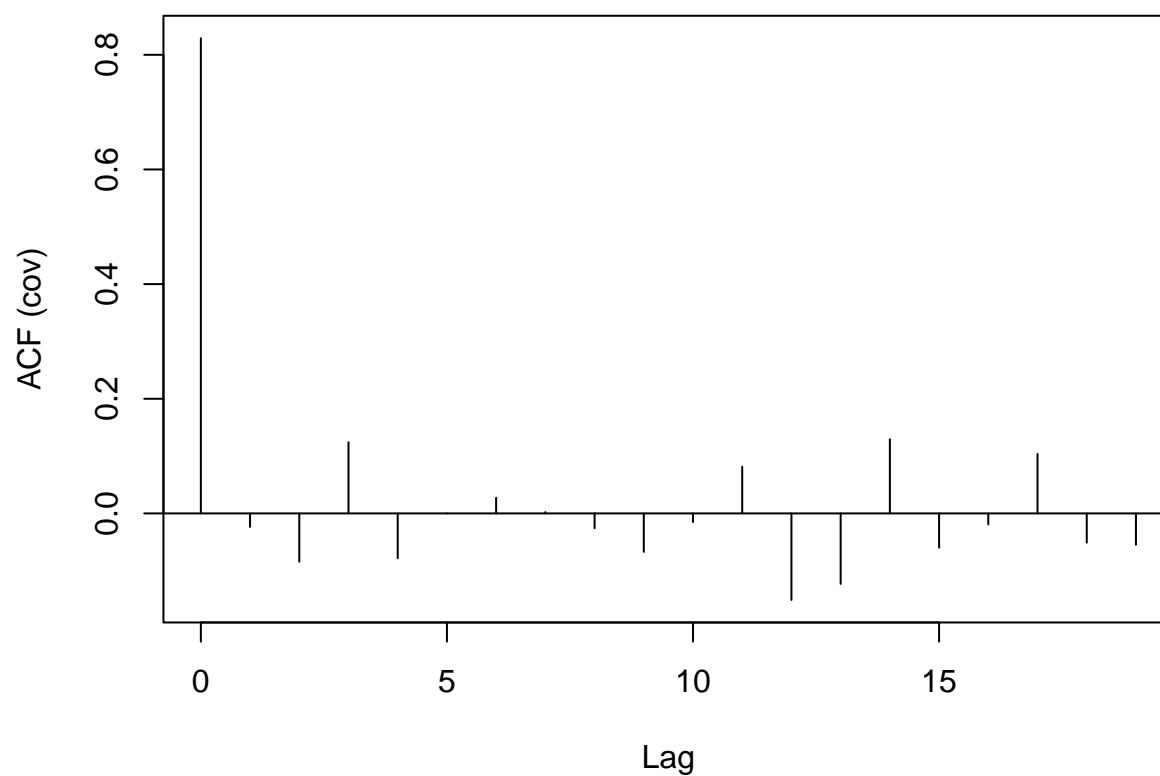
### Visualización del operador diferencia

De tal forma nuestro nuevo grafico seria



## Funcion de autocovarianza

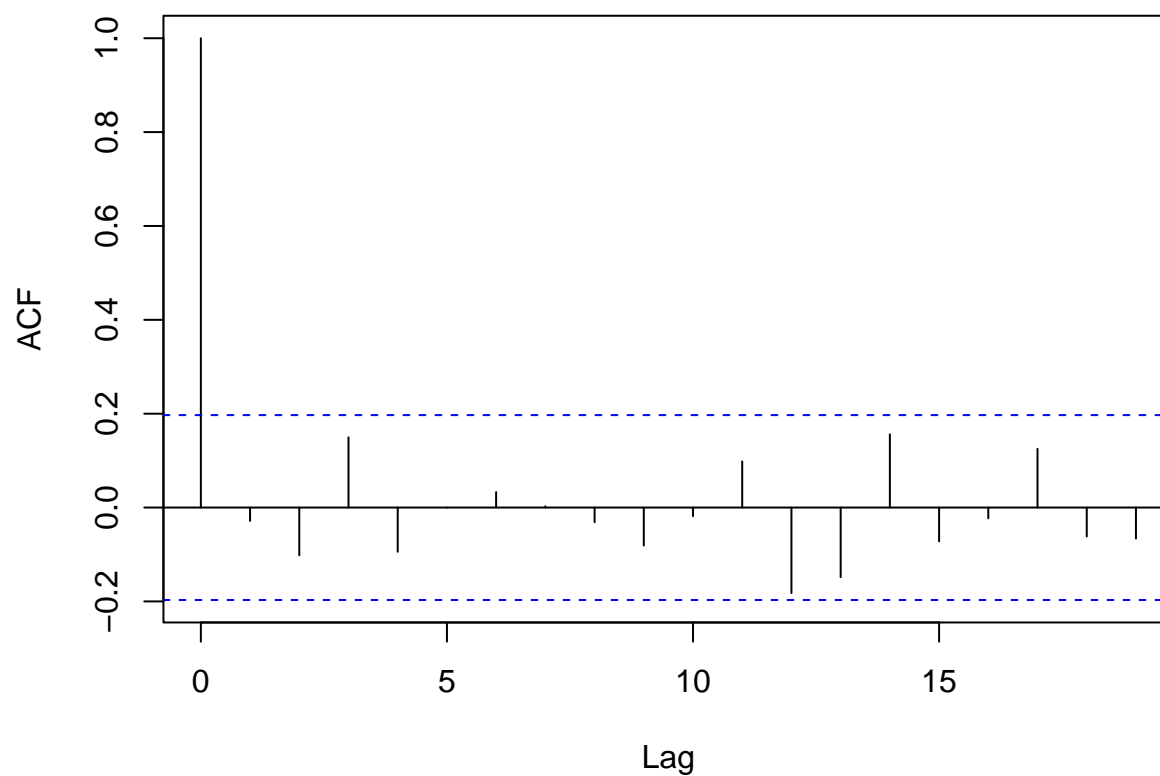
### Covarianza de primera diferencia



```
##
## Autocovariances of series 'random_walk_diff', by lag
##
##      0      1      2      3      4      5      6      7
## 0.828910 -0.023575 -0.084277 0.124043 -0.078128 -0.000128 0.027310 0.002245
##      8      9     10     11     12     13     14     15
## -0.025982 -0.067090 -0.015168 0.081536 -0.151057 -0.122898 0.129434 -0.059758
##     16     17     18     19
## -0.019096 0.103741 -0.051035 -0.054789
```

## Funcion de autocorrelacion

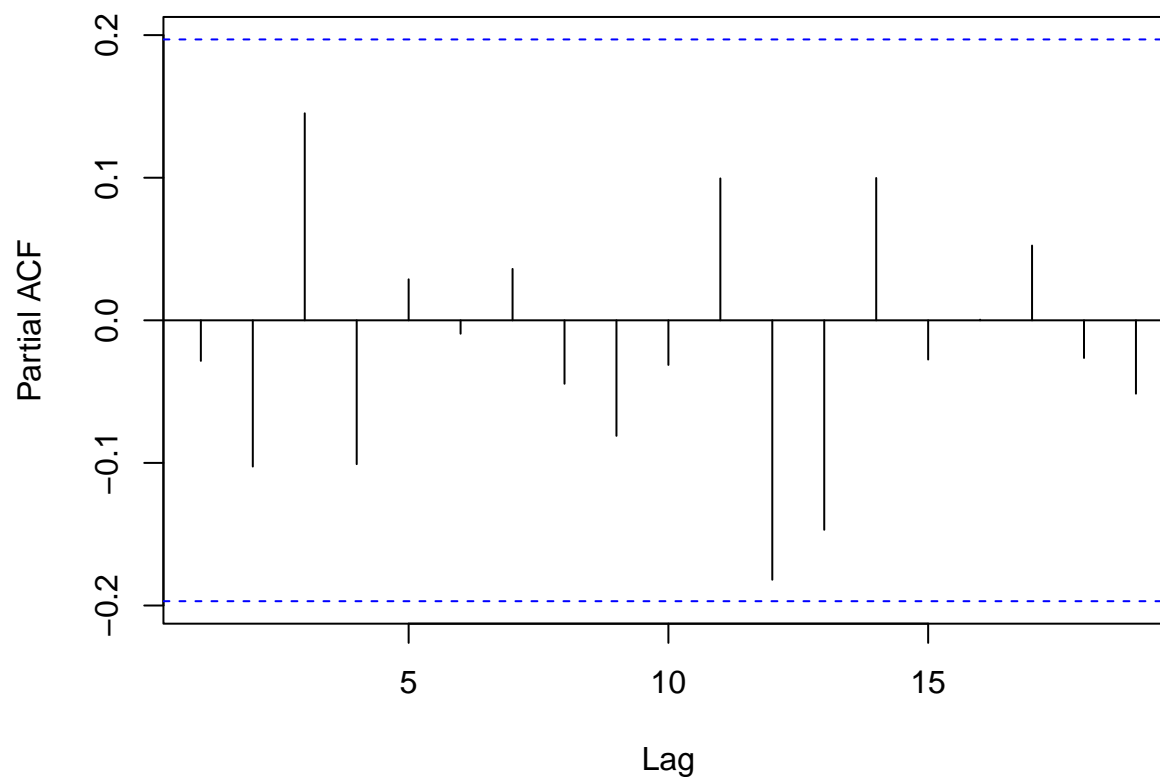
### Autocorrelacion de primera diferencia



```
##
## Autocorrelations of series 'random_walk_diff', by lag
##
##      0      1      2      3      4      5      6      7      8      9     10
## 1.000 -0.028 -0.102  0.150 -0.094  0.000  0.033  0.003 -0.031 -0.081 -0.018
##      11     12     13     14     15     16     17     18     19
## 0.098 -0.182 -0.148  0.156 -0.072 -0.023  0.125 -0.062 -0.066
```

## Funcion de autocorrelacion parcial

### Autocorrelacion parcial de primera diferencia



```
##
## Partial autocorrelations of series 'random_walk_diff', by lag
##
##      1      2      3      4      5      6      7      8      9     10     11
## -0.028 -0.103  0.145 -0.101  0.029 -0.009  0.036 -0.044 -0.081 -0.031  0.100
##      12     13     14     15     16     17     18     19
## -0.182 -0.147  0.100 -0.028  0.000  0.052 -0.026 -0.051
```