

Q. 2.36 CONT

Now Prove  $L$  passes pumping Lemma

$$S = a^i b^j c^k d^m \text{ with } i \neq 2 \text{ and } i+j+k+m \geq 2$$

Case 1. Let  $u=v=x=\epsilon$ ,  $y$  is the first symbol and  $z$  is the remainder symbols.  $u v^n x y^n z$  will either be ( $i=0$  or  $i=1$  and  $n=0$ ) or more than one  $a$  followed by a string in form  $b^j c^k d^m$ , so this case passes pumping Lemma.

Case 2.

$$S = a^i b^j c^k d^m \in L \text{ for some } j, k, m \geq 0$$

$$|S| \geq 2. \text{ Let } u=v=x=\epsilon, y=a^2 \text{ and}$$

$$z = b^j c^k d^m$$

$$x y^i z = a^{j+(i-1)} b^j c^k d^m \in L$$

Both cases hold, therefore  $L$  is context free in the pumping lemma