

Q. 2.30

d.  $\{ t, \# t_2 \dots \# t_k \mid k \geq 2, t_i \in \{a, b\}^* \text{ and } t_i = t_j \text{ for } i \neq j \}$

Assume  $L = \text{Context Free}$

$$s = a^p b^p \# a^p b^p \in L$$

Let  $vxy$  fall on one side of  $\#$

then pumping once  $uv^2xy^2z$  results in a string where  $t_1 \neq t_2$ , so  $uv^2xy^2z$  is not in  $L$ .

Let  $\#$  be contained in  $vxy$ . We can pump down to  $uv^0xy^0z$ , the  $s$  will not have  $\#$  and will not be in  $L$ .

Let  $x$  contain  $\#$ ,  $v$  contains  $b^p$ ,  $y$  contains  $a^p$ . Pumping down to  $uv^0xy^0z$  reduces the number of  $b$ 's in  $t_1$  and  $a$ 's in  $t_2$ . Now  $t_1 \neq t_2$ , therefore not in  $L$ .

All case contradict therefore  $L$  is context free