Assignment 3

due May 27

- (1) Consider a classical electron in a two-dimensional harmonic oscillator and in thermal equilibrium with a heat bath at temperature T.
 - (a) calculate analytically the thermal average of the energy E(T), as a function of T.
 - (b) design and run a Monte Carlo simulation to determine E(T)
 - (C) If $\mathcal{E}_2(T)$ designates the thermal average of E^2 calculate this function with your Monde Carlo simulation

Notation and hints:

$$E = \frac{\vec{p}^{2}}{2m} + V(r) \qquad \vec{p} (r_{1}, r_{2})$$

$$\frac{1}{2}m\omega^{2}r^{2} \quad \vec{r} (x_{1}, x_{2})$$

$$P(E(\vec{p},\vec{r})) = \frac{E(\vec{p},\vec{r})}{Z}$$

$$Probability \qquad Boltzman factor$$

$$Porklim function $Z = \int e^{-\frac{1}{k_B}T} E(\vec{p},\vec{r}) d^2p d^2r$$$

$$\mathcal{E}(T) = \frac{\int E(\vec{p},\vec{r}) e^{-\frac{1}{k_B T}} E(\vec{p},\vec{r})}{Z} d\vec{p} d\vec{r}$$

- (a) the sheare tical calculation only needs Gaussian type integrals
- (b) use your convenient units kg, m, w for the MC simulation
- (c) When you calculate $E_2(T)$ replace $E_2(T)$ replace $E_2(T)$ replace $E_2(T)$ replace

- Consider a quantum electron in a one-dimensional harmonic oscillator and in Hermal equilibrium with a heat bath at temperature T.
 - (a) calculate analytically the thermal average of the energy E(T), as a function of T.
 - (b) design and run a Monte Carlo simulation to determine E(T)
 - (C) If $\mathcal{E}_2(T)$ designates the thermal average of E^2 calculate this function with your Monde Carlo simulation

Notation and hints:

$$E_{h} = (n + \frac{1}{2}) t \omega \quad n = 0,1,2,...$$

energy levels from Schrödinger eg. is accepted

calculate the specific heat and its classical and gruanhum limit

$$\frac{P_n}{Z} = \frac{e^{-\frac{1}{8gT}} E_n}{Z}$$
Bolfzman probabilities
$$\frac{E_n}{R_{gT}} = \frac{E_n}{R_{gT}}$$

$$\mathcal{E}(T) = \sum_{n} E_{n} \cdot P_{n}$$

- (a) the sheare tical calculation subj needs geometric summation
- (b) use your convenient units for the MC simulation
- (c) When you calculate $E_2(T)$ replace $E_2(T)$ replace $E_2(T)$ replace
- (d) quantum dehavior only kicks in at low temperatures