HW 10

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R Markdown

```
df_chineseRCs<-read.table("chinese_meta_analysis.txt",header=TRUE)</pre>
head(df_chineseRCs)
     study.id
                           study
                                        У
## 1
                  Hsiao et al 03
            1
                                  50.000 25.00
## 2
            2
                 Gibson et al 13 -120.000 48.00
## 3
           3 Vas. et al 13, E1 148.500 50.90
           4 Vas. et al 13, E2
                                   82.600 41.20
            5 Vas. et al 13, E3 -109.400 54.80
## 5
            6 Jaeg. et al 15, E1
                                   55.617 65.14
#install.packages("metafor")
library(metafor)
## Loading required package: Matrix
## Loading required package: metadat
## Warning: package 'metadat' was built under R version 4.1.2
## Loading required package: numDeriv
##
## Loading the 'metafor' package (version 4.4-0). For an
## introduction to the package please type: help(metafor)
## run the meta-analysis:
m <- rma(yi=y,</pre>
         vi=se^2,
         method = "REML",
         slab = paste(study.id, study, sep = "_"),
         data = df_chineseRCs)
summary(m)
##
## Random-Effects Model (k = 13; tau^2 estimator: REML)
##
     logLik deviance
                            AIC
                                      BIC
                                                AICc
## -70.7258 141.4517 145.4517 146.4215 146.7850
## tau^2 (estimated amount of total heterogeneity): 5520.9801 (SE = 2950.7285)
## tau (square root of estimated tau^2 value):
                                                     74.3033
## I^2 (total heterogeneity / total variability):
                                                     82.09%
## H^2 (total variability / sampling variability): 5.58
```

```
##
## Test for Heterogeneity:
## Q(df = 12) = 53.5603, p-val < .0001
##
## Model Results:
##
## estimate
                              zval
                                        pval
                                                   ci.lb
                                                               ci.ub
                      se
    17.4296 23.7222 0.7347 0.4625
                                              -29.0651 63.9243
##
##
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
forest(m,xlab="Subject - Object RC reading time (ms)")
  1 Hsiao et al 03
                                                                            50.00 [
                                                                                       1.00, 99.00]
     Gibson et al 13
                                                                     –120.00 [–214.08, –25.92
                                                                     -120.00 [-∠14.08, -∠5.9∠]

-148,50 [ 48.74, 248.26]

- 82.60 [ 1.85, 163.35]

-109.40 [-216.81, -1.99]

--55.62 [ -72.06, 183.29]

-- 81.92 [ 10.87, 152.97]

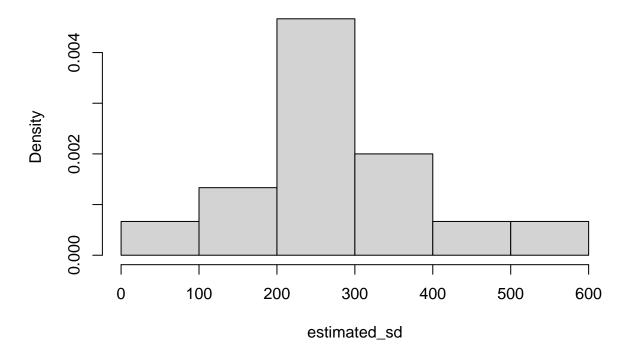
50.00 [ 4.92, 95.08]

-70.00 [-152.32, 12.32]
    Vas. et al 13, E1
 4_Vas. et al 13, E2
5_Vas. et al 13, E3
6_Jaeg. et al 15, E1
 7_Jaeg. et al 15, E2
8_Wu 09
 9_Qiao et al 11, E1
  10_Qiao et al 11, E2
                                                                            6.19^{-}[-32.81, 45.19]
  11_Lin & Garn. 11, E1
                                                                     -100.00 [-158.80, -41.20<sup>°</sup>
                                                                        75.00 [ 5.42, 144.58]
<del>100.0</del>0 [ –56.80, 256.80]
  12_Chen et al 08
  13 C Lin & Bev. 06
 RE Model
                                                                          17.43 [ -29.07, 63.92]
                                -300
                                                -100
                                                                100
                                                                       200
                                                          0
                                                                               300
                                  Subject – Object RC reading time (ms)
SEs<-c(48, 54.8, 30, 42, 44.63,19.9, 25, 40.74,23, 65.14,
        35.5,36.25,41.2, 80, 50.9)
n_subj<- c(37,40,48,32,40,24,35,48,40,49,39,49,61,48,60)
chinese_SE_n<-data.frame(SEs,n_subj)</pre>
chinese_SE_n
##
          SEs n_subj
## 1
       48.00
                    37
## 2
       54.80
                    40
       30.00
## 3
                    48
## 4
       42.00
                    32
       44.63
## 5
                    40
## 6
       19.90
                    24
## 7
       25.00
                    35
## 8
       40.74
                    48
## 9
       23.00
                    40
## 10 65.14
                    49
## 11 35.50
                    39
## 12 36.25
                    49
## 13 41.20
                    61
## 14 80.00
                    48
```

```
## 15 50.90 60
estimated_sd<-SEs*sqrt(n_subj)
summary(estimated_sd)

## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 97.49 214.77 282.25 282.74 334.18 554.26
hist(estimated_sd, freq=FALSE)</pre>
```

Histogram of estimated_sd



Exercise 1

Given that the effect size based on the published data is 17 ms, and assuming that the standard deviation can range from 100 to 560 ms, find out what the sample size (the number of subjects) you would need to have 80% statistical power. Show power calculations for a one-sample t-test assuming a range of standard deviations. For example, do a series of power analyses with $sd=100,170,180,\ldots,560$:

```
SDs<-seq(100,560,by=10)

# Load the pwr package
#install.packages("pwr")
library(pwr)

# Set the effect size (Cohen's d)
effect_size <- 17 / sd(c(100, 560))

# Set the desired power
desired_power <- 0.8

# Perform the power analysis
sample_size <- pwr.t.test(d = effect_size, sig.level = 0.05, power = desired_power, type = "two.sample"</pre>
```

```
# Print the result
cat("The required sample size is:", round(sample_size))
## The required sample size is: 5748
library(pwr)
# Create a sequence of standard deviations
SDs \leftarrow seq(100, 560, by = 10)
# Calculate the number of standard deviations
n_SD <- length(SDs)</pre>
# Create an empty data frame to store the results
results <- data.frame(SDs, n_subjects_needed = rep(NA, n_SD))
# Perform power analysis for each standard deviation
for (i in 1:n_SD) {
  sd_value <- SDs[i]</pre>
  effect_size <- 17 / sd_value
  # Perform the power analysis
  power_result <- pwr.t.test(d = effect_size, sig.level = 0.05, power = 0.8, type = "one.sample")</pre>
  # Store the sample size needed for 80% power
 results$n_subjects_needed[i] <- power_result$n</pre>
}
# Print the results
print(results)
      SDs n_subjects_needed
## 1 100
                   273.5138
## 2 110
                   330.5460
## 3 120
                   393.0101
## 4 130
                   460.9062
## 5 140
                   534.2342
## 6 150
                   612.9940
## 7 160
                   697.1856
## 8 170
                   786.8089
## 9 180
                   881.8641
## 10 190
                   982.3511
## 11 200
                  1088.2698
## 12 210
                  1199.6202
## 13 220
                  1316.4025
## 14 230
                  1438.6165
## 15 240
                  1566.2622
## 16 250
                  1699.3397
## 17 260
                  1837.8489
## 18 270
                  1981.7899
## 19 280
                  2131.1626
## 20 290
                  2285.9670
## 21 300
                  2446.2032
## 22 310
                  2611.8712
```

```
## 23 320
                   2782.9709
## 24 330
                   2959.5023
## 25 340
                   3141.4655
## 26 350
                   3328.8604
## 27 360
                   3521.6870
                   3719.9454
## 28 370
## 29 380
                   3923.6356
## 30 390
                   4132.7574
## 31 400
                   4347.3110
## 32 410
                   4567.2964
## 33 420
                   4792.7135
                   5023.5623
## 34 430
## 35 440
                   5259.8428
## 36 450
                   5501.5551
## 37 460
                   5748.6992
## 38 470
                   6001.2749
## 39 480
                   6259.2824
## 40 490
                   6522.7217
                   6791.5927
## 41 500
## 42 510
                   7065.8954
## 43 520
                   7345.6299
## 44 530
                   7630.7961
                   7921.3940
## 45 540
## 46 550
                   8217.4237
## 47 560
                   8518.8851
```

Exercise 2

The meta-analysis estimate actually comes with some uncertainty about the effect size. The estimate is 17 ms with an estimated standard error of 24 ms (look at Model Results below):

```
summary(m)
```

```
##
## Random-Effects Model (k = 13; tau^2 estimator: REML)
##
##
     logLik deviance
                            AIC
                                      BIC
                                                AICc
                                           146.7850
## -70.7258
             141.4517
                       145.4517
                                 146.4215
##
## tau^2 (estimated amount of total heterogeneity): 5520.9801 (SE = 2950.7285)
  tau (square root of estimated tau^2 value):
                                                     74.3033
## I^2 (total heterogeneity / total variability):
                                                     82.09%
## H^2 (total variability / sampling variability):
##
## Test for Heterogeneity:
## Q(df = 12) = 53.5603, p-val < .0001
##
## Model Results:
##
## estimate
                                         ci.lb
                                                   ci.ub
                  se
                        zval
                                pval
             23.7222
                      0.7347
                              0.4625
                                      -29.0651
##
   17.4296
                                                63.9243
##
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
library(pwr)
# Create a sequence of standard deviations
SDs \leftarrow seq(100, 560, by = 10)
# Calculate the number of standard deviations
n_SD <- length(SDs)</pre>
# Create an empty data frame to store the results
results <- data.frame(SDs, n_subjects_needed = rep(NA, n_SD))
# Perform power analysis for each standard deviation
for (i in 1:n_SD) {
  sd_value <- SDs[i]
  effect_size <- 35 / sd_value
  # Perform the power analysis
  power_result <- pwr.t.test(d = effect_size, sig.level = 0.05, power = 0.8, type = "one.sample")</pre>
  \# Store the sample size needed for 80% power
  results$n_subjects_needed[i] <- power_result$n</pre>
# Print the results
print(results)
##
      SDs n_subjects_needed
## 1 100
                   66.01882
## 2 110
                   79.46965
## 3 120
                  94.20294
## 4 130
                  110.21839
## 5 140
                  127.51583
## 6 150
                  146.09511
## 7 160
                  165.95614
## 8 170
                  187.09885
## 9 180
                  209.52319
## 10 190
                  233.22913
## 11 200
                  258.21663
## 12 210
                  284.48568
## 13 220
                  312.03626
## 14 230
                  340.86835
## 15 240
                  370.98194
## 16 250
                  402.37703
## 17 260
                  435.05359
## 18 270
                  469.01164
## 19 280
                  504.25118
## 20 290
                  540.77217
## 21 300
                  578.57464
## 22 310
                  617.65858
## 23 320
                  658.02399
## 24 330
                  699.67084
## 25 340
                  742.59916
## 26 350
                  786.80894
## 27 360
                  832.30018
```

```
## 28 370
                  879.07287
## 29 380
                  927.12702
## 30 390
                  976.46262
                 1027.07967
## 31 400
## 32 410
                 1078.97818
## 33 420
                 1132.15814
## 34 430
                 1186.61956
## 35 440
                 1242.36242
## 36 450
                 1299.38671
## 37 460
                 1357.69250
## 38 470
                 1417.27971
## 39 480
                 1478.14838
## 40 490
                 1540.29849
## 41 500
                 1603.73004
## 42 510
                 1668.44307
## 43 520
                 1734.43753
## 44 530
                 1801.71344
## 45 540
                 1870.27080
## 46 550
                 1940.10962
## 47 560
                 2011.22988
```

Exercise 3

A researcher carries out an experiment on Chinese relative clauses. Here are the data:

```
df_gibsonwu2<-read.table("chineseRCstudy.txt",header=TRUE)
head(df_gibsonwu2)</pre>
```

```
##
      subj item condition pos
                                rt
                                       region
## 9
       1m1
             15
                  obj-ext
                            8 832 head noun
## 20
      1m1
              8
                 subj-ext
                             8 2131 head noun
## 33 1m1
                  obj-ext
                             8 553 head noun
             11
## 46
       1m1
             10
                 subj-ext
                             8 1091 head noun
## 62
       1m1
             16
                 subj-ext
                             8 598 head noun
## 75
     1m1
             14
                 subj-ext
                             8 645 head noun
means<-round(with(df_gibsonwu2, tapply(rt, IND=condition, mean)))</pre>
bysubj <- aggregate(rt~subj+condition,mean,data=df_gibsonwu2)
means
```

```
## obj-ext subj-ext
## 447 555
bysubj
```

```
##
      subj condition
                            rt
                      547.0000
## 1
       1m1
             obj-ext
## 2
     1m10
             obj-ext
                      310.1667
## 3
     1m11
             obj-ext
                      309.5000
## 4
     1m12
             obj-ext
                      556.5714
## 5
     1m13
             obj-ext
                      524.7500
## 6 1m14
             obj-ext
                      534.5714
## 7 1m15
             obj-ext
                      369.2500
## 8
     1m16
             obj-ext
                      231.6667
## 9
     1m17
             obj-ext
                      285.8571
## 10 1m18
             obj-ext 642.8571
```

```
## 11
       1m2
             obj-ext
                       405.1429
## 12
       1m3
             obj-ext
                       456.6250
## 13
       1m4
             obj-ext
                       388.8571
## 14
             obj-ext
                       410.2500
       1m5
## 15
       1m6
             obj-ext
                       351.4286
## 16
                       300.0000
       1m7
             obj-ext
## 17
                       358.0000
       1m8
             obj-ext
                       509.2500
## 18
       1m9
             obj-ext
## 19
       2m1
             obj-ext
                       311.0000
## 20 2m10
             obj-ext
                       600.0000
## 21 2m11
             obj-ext
                       884.7500
## 22 2m12
                       260.6667
             obj-ext
## 23 2m13
             obj-ext
                       925.1250
## 24 2m14
             obj-ext
                       277.8571
## 25 2m15
                       339.7500
             obj-ext
## 26 2m16
             obj-ext
                       381.5714
## 27 2m17
             obj-ext
                       260.2500
## 28 2m18
             obj-ext
                       435.7143
## 29 2m19
             obj-ext
                       545.6250
## 30
       2m2
             obj-ext
                       565.1429
## 31 2m20
             obj-ext
                       377.2857
## 32 2m21
             obj-ext
                       706.5000
## 33 2m22
                       442.8571
             obj-ext
## 34
       2m3
             obj-ext
                       732.7500
## 35
       2m4
             obj-ext
                       261.2857
                       383.3750
## 36
       2m5
             obj-ext
## 37
       2m6
             obj-ext
                       473.5714
## 38
                       253.5000
       2m7
             obj-ext
## 39
       2m8
                       312.8571
             obj-ext
## 40
       2m9
             obj-ext
                       469.0000
## 41
       1m1
            subj-ext
                       847.2857
## 42 1m10
            subj-ext
                       233.7143
## 43 1m11
            subj-ext
                       524.1429
                       472.1250
## 44 1m12
            subj-ext
## 45 1m13
            subj-ext
                       426.7143
## 46 1m14
                       347.7500
            subj-ext
## 47 1m15
            subj-ext
                       531.0000
## 48 1m16
            subj-ext
                       395.8750
## 49 1m17
            subj-ext 1886.2857
## 50 1m18
            subj-ext 1611.2500
            subj-ext
                       475.2500
## 51
       1m2
## 52
            subj-ext
                       698.0000
       1m3
                       371.1250
## 53
       1m4
            subj-ext
## 54
       1m5
            subj-ext
                       726.4286
## 55
                       520.2500
       1m6
            subj-ext
## 56
            subj-ext
                       336.0000
       1m7
## 57
       1m8
            subj-ext
                       317.1250
## 58
       1m9
            subj-ext
                       566.0000
## 59
       2m1
            subj-ext
                       325.5714
## 60 2m10
            subj-ext
                       433.1250
## 61 2m11
                       320.2857
            subj-ext
## 62 2m12
            subj-ext
                       609.2500
## 63 2m13
            subj-ext
                       993.1429
## 64 2m14 subj-ext
                       272.2500
```

```
## 65 2m15 subj-ext 429.5714
## 66 2m16 subj-ext 363.7500
## 67 2m17 subj-ext 338.5714
## 68 2m18 subj-ext 424.5000
## 69 2m19 subj-ext 1034.1429
## 70 2m2 subj-ext 432.1250
## 71 2m20 subj-ext 518.6250
## 72 2m21 subj-ext 614.5714
## 73 2m22 subj-ext 621.2500
## 74 2m3 subj-ext 718.0000
## 75 2m4 subj-ext 262.6250
## 76 2m5 subj-ext 432.5714
## 77 2m6 subj-ext 790.7500
## 78 2m7 subj-ext 306.4286
## 79 2m8 subj-ext 390.0000
## 80 2m9 subj-ext 394.8571
# one-sample t-test
result <- t.test(rt~condition,paired=TRUE,bysubj)$statistic
print(result)
##
## -2.191819
new_ttest<-t.test(rt~condition,bysubj,mu=17, paired=TRUE)</pre>
new_ttest
##
## Paired t-test
##
## data: rt by condition
## t = -2.5144, df = 39, p-value = 0.01616
## alternative hypothesis: true difference in means is not equal to 17
## 95 percent confidence interval:
## -222.092796
                 -8.912561
## sample estimates:
## mean of the differences
##
                 -115.5027
df<-39
abs_critical_t<-abs(qt(0.025,df))
abs_critical_t
## [1] 2.022691
SE<-90/sqrt(40)
SE
## [1] 14.23025
x_bar<-mean(df_gibsonwu2$rt)</pre>
x_bar
## [1] 501.0017
observed_t<-(x_bar-0)/SE
observed_t
## [1] 35.20681
```

in this case i suppose that we can reject the null hypothesis. Regarding the plausibility of the effect estimate from this study compared to the meta-analysis estimate. Several reasons could contribute to this difference: Methodological differences, Sample characteristics, Contextual factors.