

# Package ‘fdakmapp’

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**Title** Functional Data Analysis : K-mean and K-medoid with Alignemnt

**Version** 2.1

**Type** Package

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## Description

The fdakmapp package provides the kmap function that jointly performs clustering and alignment of a functional dataset (multidimensional or unidimensional). The centers can be computed by mean and medoid center methods. Many options are available as parallal version.

**License** GPL-3

**Encoding** UTF-8

**LazyData** true

**Import** Rcpp (>= 0.12.11)

**LinkingTo** Rcpp , RcppArmadillo

**SystemRequirements** C++11

**RoxygenNote** 6.0.1

**Suggests** testthat

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aneurisk65

*Data for Examples.***Description**

A dataset containing 65 multidimensional curves from aneurisk project. The curves represent the first derivatives of the 65 ICA centerlines.

**Usage**

aneurisk65

**Format**

A list with abscissas x and values y:

**x** matrix 65 x 1380

**y** array 65 x1380 x 3

fdakmapp

*Functional Data Analysis Plus: K-Mean/Medoid Alignment:***Description**

Fdakmapp is a package that allows to jointly perform clustering and alignment of a functional dataset (multidimensional or unidimensional functions).

**References**

- Sangalli, L.M., Secchi, P., Vantini, S., Vitelli, V., 2010. "*K-mean alignment for curve clustering*". Computational Statistics and Data Analysis, 54, 1219-1233.
- Sangalli, L.M., Secchi, P., Vantini, S., 2014. "*Analysis of AneuRisk65 data: K-mean Alignment*". Electronic Journal of Statistics, Special Section on "Statistics of Time Warpings and Phase Variations", Vol. 8, No. 2, 1891-1904.

**See Also**

[kmap](#).

**Examples**

```
##### EXE #####
res<-kmap(x=aneurisk65$x, y=aneurisk65$y, n_clust=2,seeds=c(32,64))

##### OUTPUT#####
kmap_show_results(res,TRUE,TRUE)
```

kmap

*K-mean algorithm for clustering and alignment of functional data***Description**

kmap jointly performs clustering and alignment of a functional dataset (multidimensional or unidimensional functions). To run kmap function with different numbers of clusters and/or different alignment methods see the input options.

**Usage**

```
res<-kmap( x, y, y1, n_clust, warping_method, center_method, similarity_method,
optim_method, seeds, span, delta, d_max, s_max, n_out, toll, fence,
iter_max, show_iter, check_total_similarity)
```

**Arguments**

- |                |  |
|----------------|--|
| x              | numeric matrix [ <i>n.func</i> X <i>grid.size</i> ] or vector [ <i>grid.size</i> ]: the abscissa values where each function is evaluated. <i>n.func</i> : number of functions in the dataset. <i>grid.size</i> : maximal number of abscissa values where each function is evaluated. The abscissa points may be unevenly spaced and they may differ from function to function. x can also be a vector of length <i>grid.size</i> . In this case, x will be used as abscissa grid for all functions. Furthermore if the grid's size differs from one function to another the matrix must be completed with NA values. The parameter x must be provided. |
| y              | numeric matrix [ <i>n.func</i> X <i>grid.size</i> ] or array [ <i>n.func</i> X <i>grid.size</i> X <i>d</i> ]: evaluations of the set of original functions on the abscissa grid x. <i>n.func</i> : number of functions in the dataset. <i>grid.size</i> : maximal number of abscissa values where each function is evaluated. <i>d</i> : (only if the sample is multidimensional) number of function components, i.e. each function is a <i>d</i> -dimensional curve. The parameter y must be provided.  |
| seeds          | numeric vector [n.clust] indexes of the functions to be used as initial centers. In the case where the values of seeds are not provided, they are randomly chosen among the <i>n.func</i> original functions. If seeds=NULL all the centers are randomly chosen. Default value of seeds is NULL.   |
| n_clust        | scalar: required number of clusters. Default value is 1. Note that if n.clust=1 kma performs only alignment without clustering.  |
| warping_method | character: type of alignment required. The implemented options are: "affine", "dialation", "shift" and "noalign". If warping.method='noalign' kma performs only clustering (without alignment). If warping.method='affine' kma performs alignment (and possibly clustering) of functions using linear affine transformation as warping functions, i.e., $x_{final} = dilation * x + shift$ . If warping.method='shift' kma allows only shift, i.e., $x_{final} = x + shift$ . If warping.method='dilation' kma allows only dilation, i.e., $x_{final} = dilation * x$ . Default value is 'affine'.   |
| center_method  | character: type of clustering method to be used. Possible choices are: 'mean', 'medoid' and 'pseudomedoid'. Default value is 'mean'.   |

similarity_method	character: required similarity measure. Possible choices are: 'pearson','l2'. Default value is 'pearson'.
optim_method	character: optimization method chosen to solve the minimization problems at each iteration. Possible choices are: 'bobyqa'. Default method is 'bobyqa'
warping_opt	numeric vector. The parameters depend on the warping_method chosen. If warping_method='affine' warping_opt <- c( max_dilation , max_shift). If warping_method <- 'dilation' warping_opt <- c(max_dilation). If warping_method <- 'shift' warping_opt <- c(max_shift). If warping_method <- 'noalign' warping_opt <- as.numeric(). Default value is warping_opt<-c(0.15,0.15).
center_opt	numeric vector. The parameters depend on the center_method chosen. If center_method='mean' center_opt <- c(span, delta). If center_method='medoid' center_opt <- as.numeric(). If center_method='pseudomedoid' center_opt <- as.numeric(). Default value is center_opt<-c(0.01,0.1).
out_opt	numeric vector. The parameters to set are (n_out , tolerance, max_iteration). n_out is the size of the grid where the centers will be computed. tolerance is a stop condition parameter. max_iteration is a stop condition parameter. The default value is out_opt <- c(100 , 0.001 , 100).
fence	boolean: if fence=TRUE a control is activated at the end of each iteration. The aim of the control is to avoid warping outliers with respect to their computed distributions. If fence=TRUE the running time can increase considerably. Default value of fence is FALSE.
check_total_similarity	boolean: if check.total.similarity=TRUE at each iteration the algorithm checks if the total similarity is improving and stops if it's not true. In this case the results obtained in the penultimate iteration are returned. Default value is TRUE.
show_iter	boolean: if show.iter=TRUE kmap shows the current iteration of the algorithm. Default value is TRUE.
comp_original_center	boolean: if comp_original_center=TRUE the initial center with relative dissimilarities is computed otherwise this step is skipped. It can be computationally expensive. Default value is FALSE.
par_opt	numeric vector: Parallel options. The parameters to set are (num_threads, parallel_version) parallel_version available are 0 and 1 : 0 is a trivial parallelization in which each thread compute the center of a cluster; 1 is a more efficient parallelization in which all the threads compute the centers sequentially (available only with center_method = 'medoid').

## Value

The function output is a list containing the following elements:

x                      as input.

<code>y</code>	as input.
<code>seeds</code>	vector with the indeces used in the algorithm.
<code>warping.method</code>	as input.
<code>similarity.method</code>	as input.
<code>center.method</code>	as input.
<code>iterations</code>	scalar: total number of iterations performed by kma function.
<code>n.clust</code>	as input.
<code>x.center.orig</code>	numeric vector $n_{out}$ : abscissa of the center computed if <code>comp_original_center=TRUE</code> .
<code>y.center.orig</code>	numeric vector $n_{out}$ or matrix $n_{out} \times n_{dim}$ : value of the center computed if <code>comp_original_center=TRUE</code> .
<code>similarity.origin</code>	numeric vector $n_{obs}$ dissimilarity, similarity or distance of the original center respect the obserbations computed if <code>comp_original_center=TRUE</code> .
<code>x.final</code>	matrix [ $n_{func} \times \text{grid.size}$ ]: aligned abscissas.
<code>n.clust.final</code>	scalar: final number of clusters. Note that <code>n.clust.final</code> may differ from initial number of clusters (i.e., from <code>n.clust</code> ) if some clusters are found to be empty.
<code>x.centers.final</code>	matrix [ $n_{clust.final} \times \text{grid.size}$ ]: abscissas of the final function centers.
<code>y.centers.final</code>	matrix [ $n_{clust.final} \times n_{out}$ ] or array [ $n_{clust.final} \times n_{out} \times n_{dim}$ ], contain the evaluations of the final functions centers.
<code>templates_vec</code>	list iteration : each element of the list contain centers of that iteration.
<code>x_out_vec</code>	list iteration : each element of the list contain the abscissa of the centers of that iteration.
<code>labels</code>	vector $n_{obs}$ : cluster assignments.
<code>similarity.final</code>	vector [ $n_{obs}$ ]: similarities, dissimilarities or distance between each function and the center of the cluster the function is assigned to.
<code>parameters.list</code>	list [ <code>iterations</code> ]: warping parameters at each iteration.
<code>parameters</code>	matrix [ $n_{par} \times n_{obs}$ ]: warping parameters applied to the original abscissas <code>x</code> to obtain the aligned abscissas <code>x.final</code> .
<code>timer</code>	vector: time of execution by step.

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kmap_show_results	<i>plot results kmap</i>
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**Description**

Show results of the clustering with alignment of functional data

**Usage**

kma\_show\_results <-function (Result, bp\_sim,wr\_fun)

**Arguments**

- |        |  |
|--------|--|
| Result | output of kmap.  |
| bp_sim | boolean: if TRUE dissimilarity,similarity or distance boxplot are plotted. Default value is FALSE. |
| wr_fun | boolean: if TRUE the warping functions applied to x are plotted. Default value is FALSE.           |

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simulated30	<i>Data for Examples.</i>
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**Description**

A dataset containing 30 simulated unidimensional curves.

**Usage**

simulated30

**Format**

A list with abscissas x and values y:

- x** matrix 30 x 200  
**y** array 30 x 200 x 1

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