

**CS151 Spring 2017**

**Prep for Final: Birdseye View**

**Final Exam:**

**Comprehensive**

**Wednesday, 1-3pm, LC A1**

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**UNIT-1: Logic**

Material:

Chapter-3 of the MIT Reader

Additional Resources:

Chapters 12 and 14 of Stanford Text:

<http://i.stanford.edu/~ullman/focs.html>

Homeworks: 1 and 2

Exam-1

Some Key Concepts:

- Propositions and Propositional formulas
  - Logical Equivalence
  - Implication
  - DeMorgan's Laws
  - Tautologies ("valid" formulas)
  - The Satisfiability Problem (remember Zebras?)
  - Quantifiers
  - Writing and understanding quantified propositional formulas.
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**UNIT-2: Sets, relations and functions**

Material:

Chapter-4 and section 7.1 of MIT Reader

Chapters 7 and 8 of Stanford Text

Homeworks 3 and 4

Exam-2

Some Key Concepts:

- Finite vs. Infinite Sets
- Power Sets
- Subsets, membership, etc.
- Binary relations (and properties they may or may not have)
- Functions: one-to-one (injective); onto (surjective);  
bijections
- Countability

### UNIT-3: Sequences, recursive definitions and Induction

Material:

Chapter 5 of MIT Reader

Chapter 2 of Stanford Text

Homework 5

Exam-3

Some Key Concepts:

- Sigma notation
- Nested Sigma Notation
- Understanding Recursively Defined Functions
- Induction:
  - Structure
  - Why it works!
  - Strong vs. weak
  - Pitfalls

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### UNIT-4: Basics of Combinatorics ("Counting")

(More like a half-unit)

Material:

Chapter 14 of MIT Text

Chapter 4 of Stanford Text

Homework-6

Some Key Concepts:

- Counting as a sequence of choices
  - "Choice-trees"
- Ordered Selection
  - Example: GOLD, SILVER, BRONZE medals
- Unordered Selection
  - Examples:
    - forming a committee
    - Counting subsets of fixed size
- Symmetry of n-choose-k
- Relation to power-sets
- Pascal's recurrence / triangle
- Pitfalls/tricks:
  - OVERCOUNTING (and correcting it)
  - Turning a counting problem into a **string counting** problem (when possible). Example: distributing jelly beans to children
  - Indirect counting: e.g., compute the size of the complement of a set to determine the size of the set itself.

**General Advice: Work Problems!**

**Revisit Exams 1-3**

**Revisit Discussion Section Exercises**

**Revisit Homeworks**

**Make up sample problems and share with your friends!**

**Work Posted Sample Exam**

**Comprehension >> Memorization**