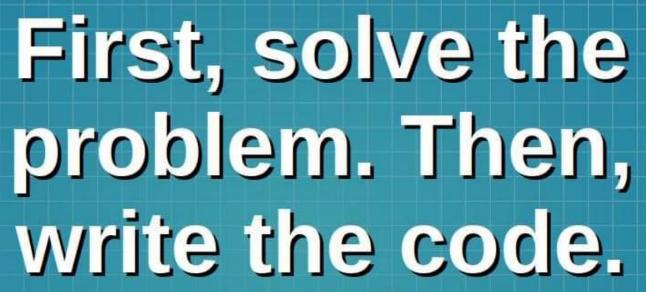
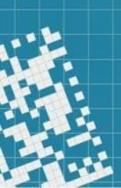
Automata and machines

Paolo Burgio paolo.burgio@unimore.it





- John Johnson





Industrial embedded systems

What they do

- Monitor physical properties of the system/plant (via sensors)
- > Might perform some control, or part of, control algos
- > Via actuators

Control can be

- > Continuous in time
- > Discrete in time
- → Control theory



Industrial controls in a nutshell



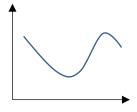
In their generic form,

$$F: \{S, I\} \rightarrow \{0\}$$

computed ...when?

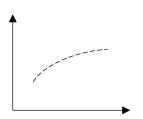
If continuous

- > Physical properties and actuators are continuous in time
- \rightarrow F(t) continuous
- > Combinatorial logic/analogic systems



If discrete

- > Computed at pre-determined instance in time
- > Event-driven (e.g., timeout, interrupt)
- > Sequential logics/digital systems





Finite state automations for discrete controls

E.g., an elevator, reacts to multiple events

- > Typically in idle state
- > If you are <u>press</u> the button, the door opens
- > You select the floor, doors close
- > Then, it <u>reaches</u> the floor (feat. velocity control)
- > Then, it opens the door, which subsequently closes after X seconds

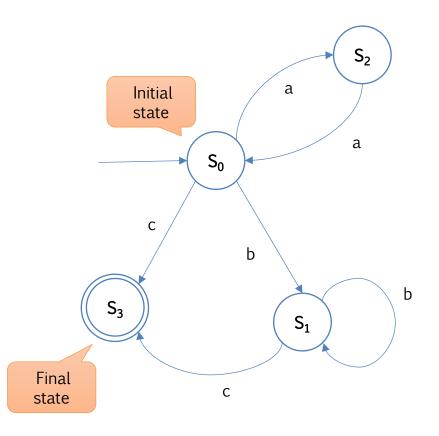
This behavior is controlled by a **finite state automations/machine**



Finite State Automations/Machines

Problem

> Identify even sequences of a (even empty), followed by one, or more, or no, b, ended by c



Given an alphabet 1/,

...that identifies a language (we'll see)..

define FSA as

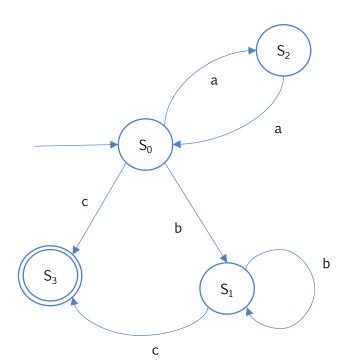
- \rightarrow S: a non-empty states set
- $> s_0 \in S$: initial state
- $\rightarrow S_f \subseteq S$: final states set
- \rightarrow t: $S \times V \rightarrow S$: states transaction func



FSMs and languages

Let $V^* = \{v, w, ...\}$ contain all the combinations of words using V symbols

- > Including the empty word arepsilon
- > For instance, ac, aabbc, abbabbbc belong to V*
- > (note that, we can associate words in be to inputs, or combination of them)



A language L is a subset of V*

(abbabbbc does not belong to L, as previously defined)

"Identify even sequences of a (even empty), followed by one, or more, or no, b, ended by c"



State transaction function

$$t(s_0, b) = s_1 | s_0 \rightarrow s_1$$

$$t: S \times V \rightarrow S$$

- \rightarrow s_v is <u>reachable</u> by s_x if there exists a path from s_x to s_v
 - a combination of alpabet symbols I (letters in our case), aka: token

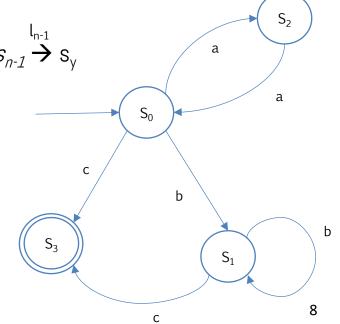
$$\rightarrow$$
: $S \times V^ \times S$: $s_x \stackrel{w^*}{\rightarrow} s_y$
iff

$$w = I_1 I_2 ... I_n$$

$$w = l_1 l_2 ... l_n$$
 $\exists s_{t, s_{u, ..., s_n}} : s_x \xrightarrow{l_1} s_t \xrightarrow{l_2} s_u ... s_{n-1} \xrightarrow{l_{n-1}} s_y$

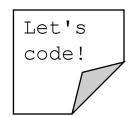


$$w = aaab$$
 $\exists s_1, s_2, ..., s_n : s_2 \xrightarrow{a} s_0 \xrightarrow{a} s_2 \xrightarrow{a} s_0 \xrightarrow{b} s_1$





Exercise



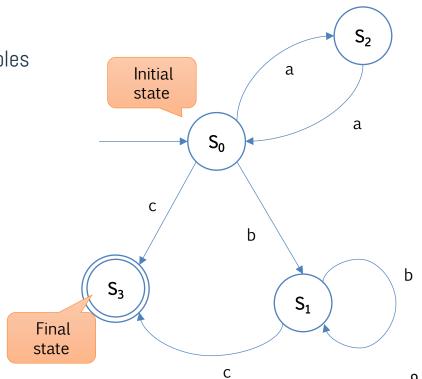
Implement the automata that understands whether a words is from L

"Identify even sequences of a (even empty), followed by one, or more, or no, b, ended by c"

Use the language that you want

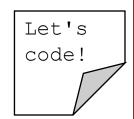
- You just need IFs, CASE-SWITCH, recursion, tables
- Receive the target word from stdin
- Hint: start simple...

What's missing?





Exercise



Implement the automata that understands whether a words is from L

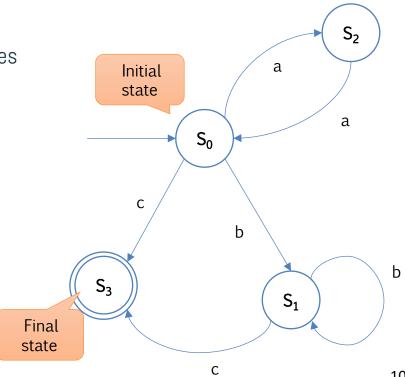
"Identify even sequences of a (even empty), followed by one, or more, or no, b, ended by c"

Use the language that you want

- You just need IFs, CASE-SWITCH, recursion, tables
- Receive the target word from stdin
- Hint: start simple...

What's missing?

- In case of error => default error state
- Typically implicit in state diagrams





Grammars

> A standard way of representing languages (Noam Chomsky, 1950)

$$G = \langle VT, VN, P, S \rangle$$

- > VT : terminal symbols ⊆ V
- \rightarrow VN : non-terminal symbols \subseteq V (aka: syntax categories)
- \rightarrow P: production rules $P \subseteq VN \times (VN \cup VT)$
- \rightarrow S \in VN: initial symbol

VT and VN disjoint $VT \cap VN = \emptyset$

VT and VN are VVT U VN = V

A language L_G generated by grammar G is the set of V* elements derived by start symbol S through productions in P



Backus-Naur Form

> Productions rules have form

$$\alpha ::= \beta$$
, $\alpha \in VN \beta \in V$

- $x \in VN$ have the form < name>
- > specifies an option



Another example

> Natural numbers

> Challenge: extend it with sign (+, -)!



Another example: solution

> Natural numbers

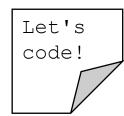
> Challenge: extend it with sign (+, -)!



In reality...

> We only give production rules: VN, VT, S are implicitly defined...

```
P = {
    <frase> ::= <soggetto> <verbo> <compl-ogg>
    <soggetto> ::= <articolo> <nome>
        <articolo> ::= il
        <nome> ::= gatto | topo | sasso
        <verbo> ::= mangia | beve
        <compl-ogg> ::= <articolo> <nome>
}
```



Want to try?

- > Implement a machine that recognizes whether a sentence (aka: a word of the Language L) is legal for that language
- > ("our" words are symbols of L)



Hierarchy of machine types

- > Base (combinatorial) machine
- > Finite state machines FSM
- > FSM with stack (PDA)
- > Turing machine



Base combinatorial machine

- > E.g., Logical ports, gates
- > Suitable for continuous control
- Non suitable if you need state/memory
 - Need to model all possible cases!

I: (finite) set of Input symbolsO: (finite) set of output symbols

 $mfn: I \rightarrow O$ machine function



$$I = \{ \{0,1\} \times \{0,1\} \}$$

$$0 = \{0,1\}$$

mfn defined by a table

	0	1
0	0	0
1	0	1



Finite state machine

< I, O, S, mfn, sfn >

- > Partly already seen
- > Has memory
- > Memory is a limitation

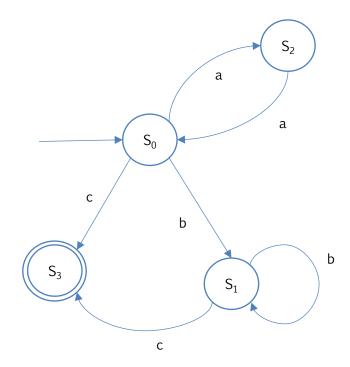
I: (finite) set of Input symbols

O: (finite) set of output symbols

S: (finite) set of states

 $mfn: I \times S \rightarrow O$ machine function

 $sfn: I \times S \rightarrow S$ state function





Finite state machine with stack

< I, O, A, S, mfn, sfn >

I: (finite) set of Input symbols

A: (finite) set of stack alphabet symbols

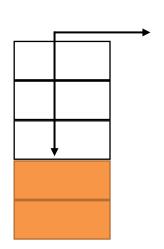
O: (finite) set of output symbols

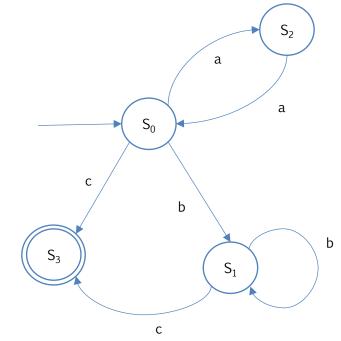
S: (finite) set of states

mfn: I x S x A \rightarrow O machine function

sfn: I x S x A \rightarrow S state function

- > Also known as Push-Down Automata (PDA)
- > Uses a stack
- > We'll see them...







Turing machine

< A, S, mfn, sfn, dfn >

A: (finite) set of in/out symbols

S: (finite) set of states

mfn: A x S → A machine function

sfn: A x S → S state function (inc. HALT)

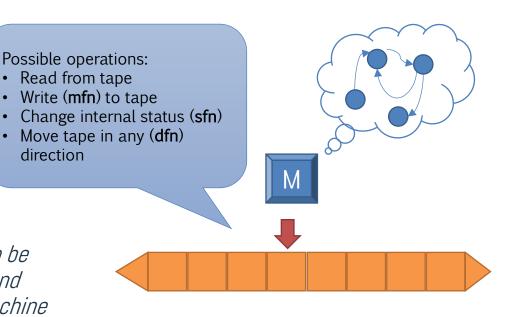
dfn: A x S → { left, right, none }

direction function

> Unlimited memory

Church-Turing thesis

A function on the natural numbers can be calculated by an effective method if and only if it is computable by a Turing machine





A Universal Turing Machine

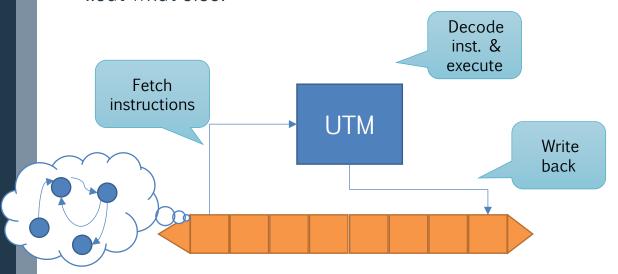
> In TM, the algorithm is inside the machine M, we write results in the tape

What if instruction as well is <u>in</u> the tape?

- > We have a programmable machine, with a memory
- >does this remind something?

Which are the catch? What do we miss?

- > Ok, the infinite tape makes it infeasible
- > ..but what else?

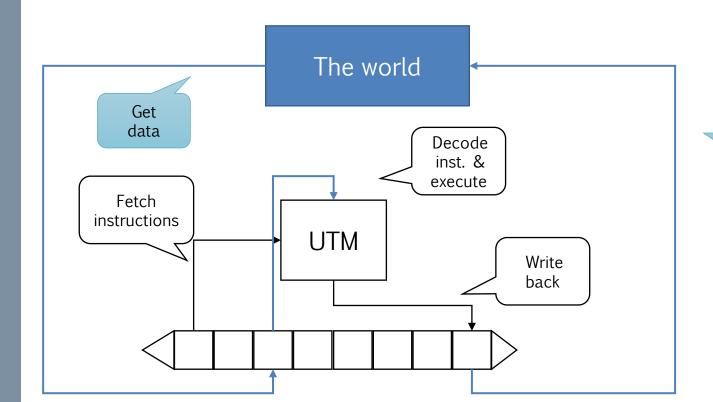




The Van Neumann Machine

We also need to model the interaction with the environment!

- Aka: I/O (HD/SSD is also I/O)
- Where data comes from!
- It is a real machine: we can build it



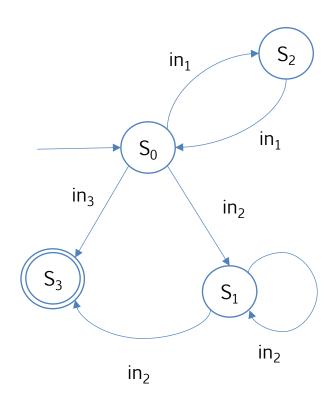
Store data

How to implement a FSM



A generic FSM

- > Till now, we only saw machines that can recognize a word from a language
 - I say "word", you might want to understand "sentence"
- > Let's now see how a machine can actually **produce** an output





The Machine of Mealy

> When crossing an edge, produce an output

< I, O, S, mfn, sfn >

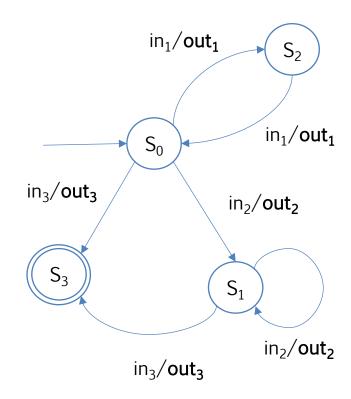
I: (finite) set of Input symbols

O: (finite) set of output symbols

S: (finite) set of states (s_0 initial state)

 $mfn: I \times S \rightarrow O$ machine/output function

 $sfn: I \times S \rightarrow S$ state transition function





The Machine of Moore

> When in a state an edge, produce an output

< I, O, S, mfn, sfn >

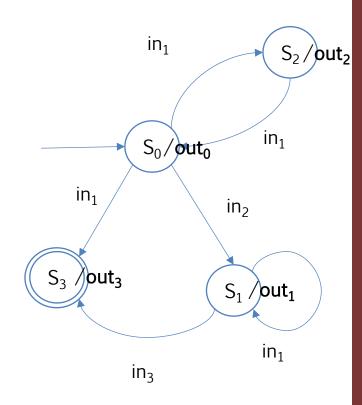
I: (finite) set of Input symbols

O: (finite) set of output symbols

S: (finite) set of states (s_0 initial state)

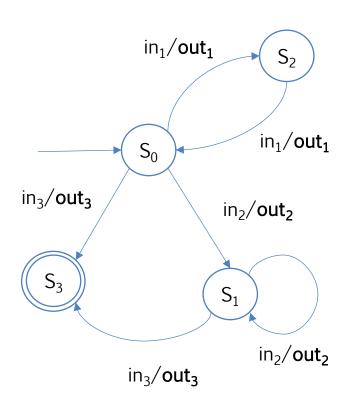
mfn: S → O machine/output function

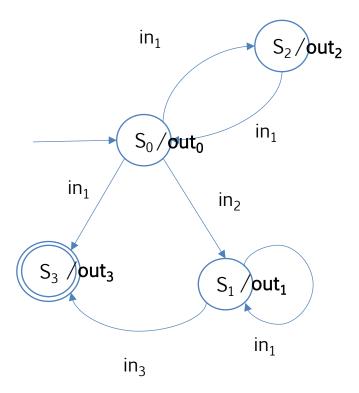
 $sfn: I \times S \rightarrow S$ state transition function





What's the difference?







What's the difference?

Mathematically equivalent

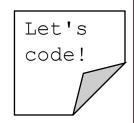
> One can be transformed in another

..but..

- Mealy can potentially have different outs, to different inputs/transitions
 - Less states, if output depends on inputs one can add an edge to the machine
- > Moore potentially keeps the output stable for all the state
 - Moore requires more states, in case out depends on input and not only on state



Exercise



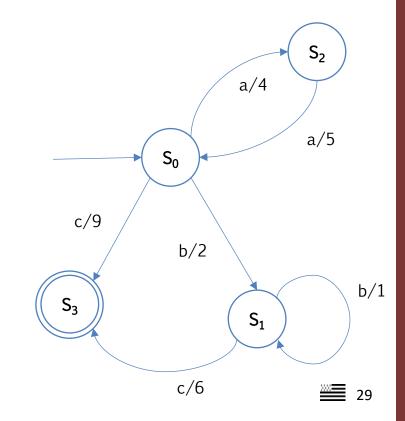
> Implement the automata that understands whether a words is from L

"Identify even sequences of a (even empty), followed by one, or more, or no, b, ended by c"

- ..and writes the corresponding number (I choose them <u>randomly</u>)
- > Mealy? Moore? You choose
 - Here, I show Mealy

Hint

If not already done, use tables for state/output transactions





What else?

Several tools to support the design

> Matlab Stateflow, UML

Several grammar interpreters to rely the burden of writing FSM code

- > FSF's GNU Bison Included in GCC
- > YACC Yet Another Compiler-Compiler



GNU Bison



Converts a context-free grammar into a deterministic LR parser (but not only) in C

- > Recognizes correct sentences from a grammar
- https://www.gnu.org/software/bison/



Input format: Bison grammar files

```
%{
   Prologue
%}

Bison declarations
%%
Grammar rules
%%
Epilogue
```



Bison prologue



C-style code that will be appended at the beginning of the generated file

- > Useful for defining macros, includes, headers...
- > ptypes.h contains Bison internal data structures: trees, tokens...

```
응 {
 #define GNU SOURCE
 #include <stdio.h>
 #include "ptypes.h"
응 }
%union {
 long n;
 tree t; /* tree is defined in ptypes.h. */
응 {
  static void print token (yytoken_kind_t token, YYSTYPE val);
응 }
```



Grammar rules

- > Like-BNF syntax
- > Can also include (C) language-specific rules

```
// results => non-terminal;
// components => any
result: components...;
// C statement
{C statements}
// Multiple rules
result:
  rule1-components...
| rule2-components...
// recursive rule
expseq1:
  exp
| expseq1 ',' exp
```



Example - Reverse-polish notation calculator

```
rpcalc.y
      /* empty */
input:
       | input line
     '\n'
line:
        | \exp ' \mid  { printf ("\t%.10g\n", $1); }
exp:
       NUM
                       \{ \$\$ = \$1;
        | \exp \exp '+'  { $$ = $1 + $2;
        | \exp \exp '-'  { $$ = $1 - $2;
        | \exp \exp '*'  { $$ = $1 * $2;
        | \exp \exp '/'  { $$ = $1 / $2;
      /* Exponentiation */
        | \exp \exp '^{\prime} | \{ \$\$ = pow (\$1, \$2); \}
      /* Unary minus */
       | \exp 'n'  { $$ = -$1;
응응
```



Example - Reverse-polish notation calculator

```
"A complete input is either an empty
                                                            rpcalc.y
                               string, or a complete input followed by
         /* empty */
input:
                                       an input line"
         | input line
          '\n'
line:
         | \exp ' n' | \{ printf ("\t%.10g\n", $1); \}
                             \{ $$ = $1;
exp:
           NUM
         | exp exp '+'
                             \{ \$\$ = \$1 + \$2;
                        \{ \$\$ = \$1 - \$2;
           exp exp '-'
           \exp \exp '*' { $$ = $1 * $2;
         | exp exp '/'
                        \{ $$ = $1 / $2;
       /* Exponentiation */
         | exp exp '^'
                         \{ \$\$ = pow (\$1, \$2); \}
       /* Unary minus
                          \{ \$\$ = -\$1;
         exp 'n'
응응
```



응응

Example - Reverse-polish notation calculator

```
rpcalc.y
input:
             /* empty */
             input line
             '\n'
line:
             exp '\n' { printf ("\t%.10g\n", $1); }
exp:
             NUM
                                        "Can be either a newline, or an expression followed
             exp exp '+'
                                        by a newline"
             exp exp '-'
             exp exp
                                        Also, speficies an action that prints this value (exp.
             exp exp '/'
                                        indicated by $1)
           Exponentiation */
                                        Note: we use language-specific features and
           exp exp '^'
                                        libraries, such as printf (in prologue, I included
            Unary minus
                                        stdio.h)
             exp 'n'
```



Example - Reverse-polish notation calculator

rpcalc.y

```
Multi-rules expression ("pure" numbers + six arithm operators)
Actions specify how to translate it in C
   $$ => result
   1, 2 =  operators
  (remember to #include math.h ☺)
                              \{ $$ = $1;
           NUM
exp:
         | \exp \exp '+'  { $$ = $1 + $2;
           \exp \exp '-'  { $$ = $1 - $2;
           \exp \exp '*' { $$ = $1 * $2;
           \exp \exp '/'  { $$ = $1 / $2;
       /* Exponentiation */
         | \exp \exp '^{\prime} | \{ \$\$ = pow (\$1, \$2); \}
       /* Unary minus */
         | exp 'n'  { $$ = -$1;
응응
```



Exercise (optional)

Let's code!

Write a parser for the following grammar using Bison

Event driven Systems



Event driven systems

A system that reacts from external stimula

- > Instantly?
- > Aka: Cyber-Physical Systems (CPS)

Can be

- > Synchronous
- Asynchronous



Synchronous (Active polling)

Infinite loop

```
char c;
while (c != EXIT_VALUE)
  c = readC();

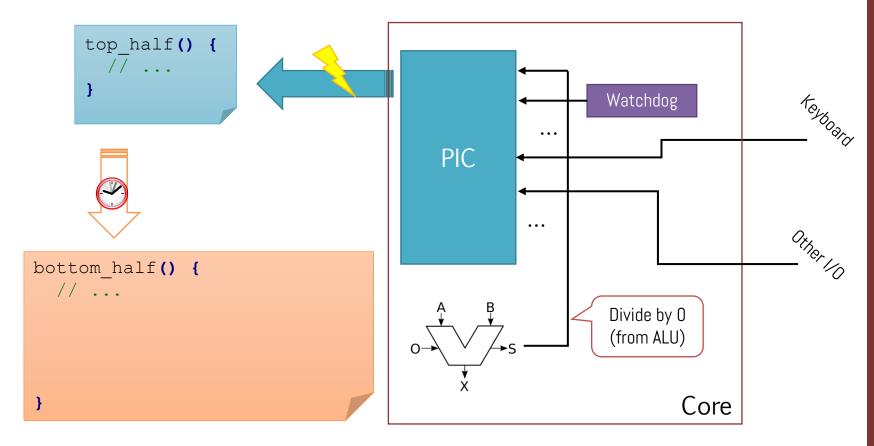
// We can go, now
```

- > Pros: extremely fast and reactive
- > Cons: waste of resources as one core is busy
 - Possible workaround: insert a sleep



Asynchronous (Interrupt Service Routine)

> Programmable interrupt controller (hierarchy)



- > Pros: "pay-as-you-go"
- Cons: takes more time to issue a ISP



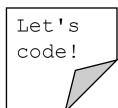
...a mix of the two

Keyboard management in a General-Purpose system

- > GNU/Linux
- > ISP with bottom-half and top-half @ kernel space
- Synchronous, language-specific library API @ user space0 kernel space user space Core top half() { char c; cin >> c; // Blocking bottom_half() { Unlock // Blocked // ... istream &operator>>(istream &, char &); 43 iostream.h



How to run the examples



> Find them in Code/ folder from the course website

For C++: compile

> \$ gcc code.cpp -o code -Wall -lstdc++

Run (Unix/Linux)

\$./code

Run (Win/Cygwin)

\$./code.exe



References



Course website

http://hipert.unimore.it/people/paolob/pub/Industrial_Informatics/index.html

My contacts

- > paolo.burgio@unimore.it
- http://hipert.mat.unimore.it/people/paolob/

Resources

- > Alessandro Fantechi, «Informatica Industriale», Città Studi Edizioni
- > For interrupts
 - Robert Love, «Linux kernel development», Pearson
- For GNU Bison
 - http://dinosaur.compilertools.net/bison/bison_5.html
- A "small blog"
 - http://www.google.com