Artificial Intelligence 18. Heuristic Search How to Avoid Having to Look at a Gazillion States

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Autumn Term

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Agenda

Introduction

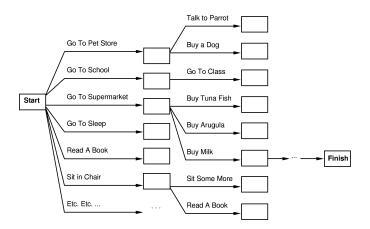
- Introduction
- What Are Heuristic Functions?
- Mow to Use Heuristic Functions?
- 4 How to Obtain Heuristic Functions?
- Conclusion

References

Fill in (some) details on these choices:

- Search space: Progression vs. regression.
- ightarrow Previous Chapter
- Search algorithm: Uninformed vs. heuristic; systematic vs. local.
 - \rightarrow This Chapter
- Search control: Heuristic functions and pruning methods.
 - \rightarrow Chapters 19–20

Looking at a Gazillion States?



 \rightarrow Use heuristic function to guide the search towards the goal!

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Introduction

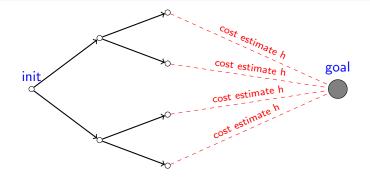
Artificial Intelligence

Chapter 18: Heuristic Search

What's a Heuristic? How to Use it? How to Obtain it? Conclusion References

Heuristic Search

Introduction



 \rightarrow Heuristic function h estimates the cost of an optimal path from a state s to the goal; search prefers to expand states s with small h(s).

Live Demo:

http://qiao.github.io/PathFinding.js/visual/

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Sara Bernardini Artificial Intelligence Chapter 18: Heuristic Search

Our Agenda for This Chapter

- What Are Heuristic Functions? Gives the basic definition and introduces a number of important properties that we will be considering throughout the course.
- How to Use Heuristic Functions? Recaps the basic heuristic search algorithms from Chapter 4 and adds a few new ones. Gives a few planning-specific algorithms and explanations.
- **4 How to Obtain Heuristic Functions?** A basic explanation how heuristic functions are derived in practice.

Introduction

References

Heuristic Functions

Definition (Heuristic Function). Let Π be a planning task with state space $\Theta_{\Pi} = (S, L, c, T, I, S^G)$. A heuristic function, short heuristic, for Π is a function $h: S \mapsto \mathbb{R}_0^+ \cup \{\infty\}$. Its value h(s) for a state s is referred to as the state's heuristic value, or h value.

Definition (Remaining Cost, h^*). Let Π be a planning task with state space $\Theta_{\Pi} = (S, L, c, T, I, S^G)$. For a state $s \in S$, the state's remaining cost is the cost of an optimal plan for s, or ∞ if there exists no plan for s. The perfect heuristic for Π , written h^* , assigns every $s \in S$ its remaining cost as the heuristic value.

- \rightarrow Heuristic functions h estimate remaining cost h^* .
- \rightarrow These definitions apply to both STRIPS and FDR.

Heuristic Functions: The Eternal Trade-Off

What does it mean "estimate remaining cost"?

- In principle, the "estimate" is an arbitrary function. In practice, we want it to be accurate (aka: informative), i.e., close to the actual remaining cost.
- ullet We also want it to be fast, i.e., a small overhead for computing h.
- These two wishes are in contradiction! Extreme cases?
 - $\rightarrow h = 0$: No overhead at all, completely un-informative.
 - $\rightarrow h = h^*$: Perfectly accurate, overhead=solving the problem in the first place.
- ightarrow We need to trade off the accuracy of h against the overhead of computing it.
- → What exactly is "accuracy"? How does it affect search performance? Interesting and challenging subject!

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References

| 9 | 2 | 12 | 6 |
|----|----|----|----|
| 5 | 7 | 14 | 13 |
| 3 | 4 | 1 | 11 |
| 15 | 10 | 8 | |

| 1 | 2 | 3 | 4 |
|----|----|----|----|
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | |

- ullet Problem Π : Move tiles to transform left state into right state.
- Relaxed Problem Π' : Allow to move each tile to *any cell* in a single move, regardless of the situation.
- Heuristic function h: Number of misplaced tiles. Here: 13.

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Chapter 18: Heuristic Search

Heuristic Functions: Example 2

What's a Heuristic?

| 9 | 2 | 12 | 6 |
|----|----|----|----|
| 5 | 7 | 14 | 13 |
| 3 | 4 | 1 | 11 |
| 15 | 10 | 8 | |

| 1 | 2 | 3 | 4 |
|----|----|----|----|
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | |

- ullet Problem Π : Move tiles to transform left state into right state.
- ullet Relaxed Problem Π' : Allow to move each tile to any neighbor cell, regardless of the situation.
- Heuristic function h: Manhattan distance. Here: 36.

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Properties of Individual Heuristic Functions

Definition (Safe/Goal-Aware/Admissible/Consistent). Let Π be a planning task with state space $\Theta_{\Pi} = (S, L, c, T, I, S^G)$, and let h be a heuristic for Π . The heuristic is called:

- safe if, for all $s \in S$, $h(s) = \infty$ implies $h^*(s) = \infty$;
- goal-aware if h(s) = 0 for all goal states $s \in S^G$;
- admissible if $h(s) \le h^*(s)$ for all $s \in S$;
- consistent if $h(s) \le h(s') + c(a)$ for all transitions $s \xrightarrow{a} s'$.

\rightarrow Relationships:

Proposition. Let Π be a planning task, and let h be a heuristic for Π . If h is admissible, then h is goal-aware. If h is admissible, then h is safe. If h is consistent and goal-aware, then h is admissible. No other implications of this form hold.

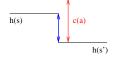
Proof. First two claims: Easy. Third claim: Next slide.

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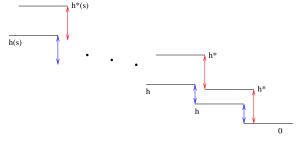
Consistency: Illustration

Introduction

Consistency = "heuristic value decreases by at most c(a)":



Consistent and goal-aware implies admissible: Let s be a state. $h^*(s)$ is the cost of an optimal solution path for s. Induction over that path, backwards from the goal: (on an optimal path, h^* decreases by exactly c(a) in each step)



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Chapter 18: Heuristic Search

Properties of Individual Heuristic Functions, ctd.

Examples:

- Is h = Manhattan distance in the 15-Puzzle safe/goal-aware/admissible/consistent? All yes. Easy for goal-aware and safe (h is never ∞). Consistency: Moving a tile can't decrease h by more than 1.
- Is h =straight line distance safe/goal-aware/admissible/consistent? All yes. Easy for goal-aware and safe (h is never ∞). Consistency: If you drive 100km, then straight line distance can't decrease by more than 100km.
- An admissible but inconsistent heuristic: To-Paris with h(London) = 100, h(Brighton) = 120.
- \rightarrow In practice, most heuristics are safe and goal-aware, and admissible heuristics are typically consistent.

What about inadmissible heuristics?

• Inadmissible heuristics typically arise as approximations of admissible heuristics that are too costly to compute. (Examples: Chapter 20)

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Domination Between Heuristic Functions

Definition (Domination). Let Π be a planning task, and let h and h' be admissible heuristics for Π . We say that h' dominates h if h < h', i.e., for all states s in Π we have $h(s) \leq h'(s)$.

 $\rightarrow h'$ dominates h = h' provides a lower bound at least as good as h''.

Remarks:

- Example: h' = Manhattan Distance vs. h = Misplaced Tiles in 15-Puzzle: Each misplaced tile accounts for at least 1 (typically, more) in h'.
- h* dominates every other admissible heuristic.
- Modulo tie-breaking, the search space of A^* under h' can only be smaller than that under h (see [Holte (2010)] for details).
- It is possible to consider much more powerful concepts, comparing entire families of heuristic functions.

Additivity of Heuristic Functions

What's a Heuristic?

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Definition (Additivity). Let Π be a planning task, and let h_1, \ldots, h_n be admissible heuristics for Π . We say that h_1, \ldots, h_n are additive if $h_1 + \cdots + h_n$ is admissible, i.e., for all states s in Π we have $h_1(s) + \cdots + h_n(s) \leq h^*(s)$.

 \rightarrow An ensemble of heuristics is additive if its sum is admissible.

Remarks:

- Example: h_1 considers only tiles $1 \dots 7$, and h_2 considers only tiles $8 \dots 15$, in the 15-Puzzle: The two estimates are then, intuitively, "independent".
 - $(h_1 \text{ and } h_2 \text{ are orthogonal projections})$
- We can always combine h_1, \ldots, h_n admissibly by taking the max. Taking \sum is *much* stronger; in particular, \sum dominates max.
- If we have time, we will devise a third, strictly more general, technique to admissibly combine heuristic functions.

What Works Where in Planning?

Blind (no h) vs. heuristic:

- For satisficing planning, heuristic search vastly outperforms blind algorithms pretty much everywhwere.
- For optimal planning, heuristic search also is better (but the difference is not as huge).

Systematic (maintain all options) vs. local (maintain only a few):

- For satisficing planning, there are successful instances of each.
- For optimal planning, systematic algorithms are required.
- → Here, we briefly cover the search algorithms most successful in planning. For more details (in particular, for blind search), refer to Chapter 3 & 4

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Reminder: Greedy Best-First Search and A*

For simplicity, duplicate elimination omitted:

```
function Greedy Best-First Search [A*] (problem) returns a solution, or failure
  node \leftarrow a \text{ node } n \text{ with } n.state = problem.InitialState
  frontier \leftarrow a priority queue ordered by ascending h [g+h], only element n
  loop do
       if Empty?(frontier) then return failure
       n \leftarrow \mathsf{Pop}(\mathsf{frontier})
       if problem.GoalTest(n.State) then return Solution(n)
       for each action a in problem. Actions (n.State) do
          n' \leftarrow ChildNode(problem, n, a)
           Insert(n', h(n')) [a(n') + h(n')], frontier)
```

 \rightarrow Greedy best-first search explores states by increasing heuristic value h. A^* explores states by increasing plan-cost estimate g+h.

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Chapter 18: Heuristic Search

Greedy Best-First Search: Remarks

Properties:

- Complete? Yes, with duplicate elimination. (If $h(s) = \infty$ states are pruned, h needs to be safe.)
- Optimal? No. (Even for perfect heuristics! E.g., say the start state has two transitions to goal states, one of which costs a million bucks while the other one is for free. Nothing keeps Greedy Best-First Search from choosing the bad one.)

Technicalities:

• Duplicate elimination: Insert child node n' only if n'. State is not already contained in *explored* \cup States(*frontier*).

Bottom line: Fast but not optimal \implies satisficing planning.

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References

A*: Remarks

Introduction

Properties:

- Complete? Yes. (Even without duplicate detection; if $h(s) = \infty$ states are pruned, h needs to be safe.)
- Optimal? Yes, for admissible heuristics.

Technicalities:

- "Plan-cost estimate" g(s) + h(s) known as f-value f(s) of s.
 - \to If g(s) is taken from a cheapest path to s, then f(s) is a lower bound on the cost of a plan through s.
- Duplicate elimination: If n'.State $\not\in explored \cup States(frontier)$, then insert n'; else, insert n' only if the new path is cheaper than the old one, and if so remove the old path.

Bottom line: Optimal for admissible $h \implies$ optimal planning, with such h.

References

Weighted A*

Introduction

For simplicity, duplicate elimination omitted:

```
function Weighted A*(problem) returns a solution, or failure
  node \leftarrow a \text{ node } n \text{ with } n.state = problem.InitialState
  frontier \leftarrow a priority queue ordered by ascending q + W * h, only element n
  loop do
       if Empty?(frontier) then return failure
       n \leftarrow Pop(frontier)
       if problem.GoalTest(n.State) then return Solution(n)
       for each action a in problem.Actions(n.State) do
          n' \leftarrow ChildNode(problem, n, a)
          Insert(n', [q(n') + W*h(n'), frontier)
```

 \rightarrow Weighted A* explores states by increasing weighted-plan-cost estimate q + W * h.

Weighted A*: Remarks

The weight $W \in \mathbb{R}_0^+$ is an algorithm parameter:

- For W = 0, weighted A* behaves like? Uniform-cost search, i.e., "cheapest-first on path costs g".
- For W=1, weighted A^* behaves like? A^* .
- For $W=10^{100}$, weighted A^* behaves like? Greedy best-first search (i.e., if W is large enough, the "g" in "g+W*h" doesn't matter anymore.)

Properties:

- For W > 1, weighted A^* is bounded suboptimal.
 - ightarrow If h is admissible, then the solutions returned are at most a factor W more costly than the optimal ones.

Bottom line: Allows to interpolate between greedy best-first search and A^{\ast} , trading off plan quality against computational effort.

References

Hill-Climbing

Introduction

Remarks:

- Is this complete or optimal? No.
- Can easily get stuck in local minima where immediate improvements of h(n) are not possible.
- Many variations: tie-breaking strategies, restarts, . . .

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```
function Enforced Hill-Climbing returns a solution node \leftarrow \text{a node } n \text{ with } n.state = problem.InitialState} \textbf{loop do} \textbf{if } problem.GoalTest(n.State) \textbf{ then return } Solution(n) \textbf{Perform breadth-first search for a node } n' \text{ s.t. } h(n') < h(n) n \leftarrow n'
```

Remarks:

- Is this optimal? No.
- Is this complete? See next slide.

Questionnaire

Introduction

```
function Enforced Hill-Climbing returns a solution node \leftarrow \text{a node } n \text{ with } n.state = problem.InitialState \\ \textbf{loop do} \\ \textbf{if } problem.GoalTest(n.State) \textbf{ then return } Solution(n) \\ \textbf{Perform breadth-first search for a node } n' \text{ s.t. } h(n') < h(n) \\ n \leftarrow n' \\ \end{cases}
```

Question!

Assume that h(s)=0 if and only if s is a goal state. Is Enforced Hill-Climbing complete?

- ightarrow Only when restricting the input to planning tasks that do not contain any reachable unrecognized dead-end states:
 - If there is a reachable unrecognized dead-end state, then the current node n may at some point end up containing that state, in which case the algorithm will not find a solution.
 - Say there are no reachable unrecognized dead-end states. Say the current node n contains the non-goal state s. Then h(s)>0, a goal state s' is reachable from s, and 0=h(s')< h(s). So breadth-first search will terminate with success.

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References

nat's a Heuristic? How to Use it? How to Obtain it? Conclusion References

Heuristic Functions from Relaxed Problems

Introduction



Problem Π : Find a route from Saarbruecken To Edinburgh.

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References

Heuristic Functions from Relaxed Problems

Introduction



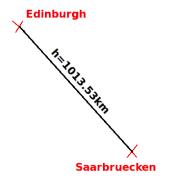


Relaxed Problem Π' : Throw away the map.

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Heuristic Functions from Relaxed Problems

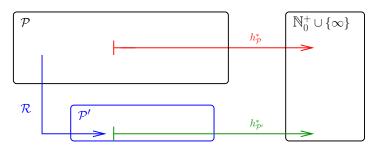
Introduction



Heuristic function h: Straight line distance.

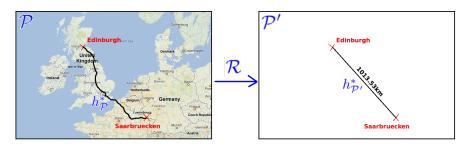
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- You have a class \mathcal{P} of problems, whose perfect heuristic $h_{\mathcal{P}}^*$ you wish to estimate.
- You define a class \mathcal{P}' of simpler problems, whose perfect heuristic $h_{\mathcal{D}'}^*$ can be used to estimate $h_{\mathcal{D}}^*$.
- You define a transformation the relaxation mapping R that maps instances $\Pi \in \mathcal{P}$ into instances $\Pi' \in \mathcal{P}'$.
- Given $\Pi \in \mathcal{P}$, you let $\Pi' := \mathcal{R}(\Pi)$, and estimate $h_{\mathcal{D}}^*(\Pi)$ by $h_{\mathcal{D}'}^*(\Pi')$.

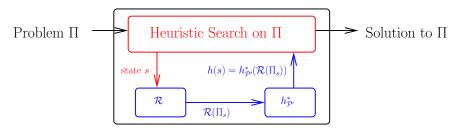
Relaxation in Route-Finding



- Problem class \mathcal{P} : Route finding.
- Perfect heuristic $h_{\mathcal{D}}^*$ for \mathcal{P} : Length of a shortest route.
- Simpler problem class \mathcal{P}' : Route finding on an empty map.
- Perfect heuristic $h_{\mathcal{D}'}^*$ for \mathcal{P}' : Straight-line distance.
- Transformation \mathcal{R} : Throw away the map.

How to Relax During Search: Overview

Attention! Search uses the real (un-relaxed) Π . The relaxation is applied **only** within the call to h(s)!!!



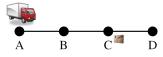
- Here, Π_s is Π with initial state replaced by s, i.e., $\Pi = (P, A, I, G)$ changed to (P, A, s, G): The task of finding a plan for search state s.
- A common student mistake is to instead apply the relaxation once to the whole problem, then doing the whole search "within the relaxation".
- Next slides illustrate the correct search process in detail.

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How to Relax in Planning?

Example: "Logistics"

Introduction

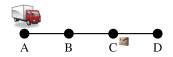


- Facts P: $\{truck(x) \mid x \in \{A, B, C, D\}\} \cup \{pack(x) \mid x \in \{A, B, C, D, T\}\}.$
- Initial state I: $\{truck(A), pack(C)\}$.
- Goal G: $\{truck(A), pack(D)\}$.
- Actions A: (Notated as "precondition ⇒ adds, ¬ deletes")
 - drive(x, y), where x, y have a road: " $truck(x) \Rightarrow truck(y), \neg truck(x)$ ".
 - load(x): " $truck(x), pack(x) \Rightarrow pack(T), \neg pack(x)$ ".
 - unload(x): " $truck(x), pack(T) \Rightarrow pack(x), \neg pack(T)$ ".

Example "Only-Adds" Relaxation: Drop the preconditions and deletes.

"drive(x, y): $\Rightarrow truck(y)$ "; "load(x): $\Rightarrow pack(T)$ "; "unload(x): $\Rightarrow pack(x)$ ".

 \rightarrow Say we want to use this for generating a heuristic function.



Real problem:

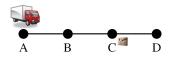
- Initial state *I*: *AC*; goal *G*: *AD*.
- Actions A: pre, add, del.
- \bullet drXY, loX, ulX.

Greedy best-first search:

Introduction



How to Relax During Search: Only-Adds



Relaxed problem:

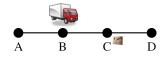
- State s: AC; goal G: AD.
- Actions A: add.
- $h^{\mathcal{R}}(s) = 1$: $\langle ulD \rangle$.

Greedy best-first search:

Introduction



How to Relax During Search: Only-Adds

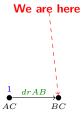


Real problem:

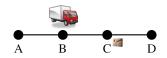
- State s: BC; goal G: AD.
- Actions A: pre, add, del.
- $AC \xrightarrow{drAB} BC$

Greedy best-first search:

Introduction



How to Relax During Search: Only-Adds



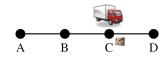
Relaxed problem:

- State s: BC; goal G: AD.
- Actions A: add.
- $h^{\mathcal{R}}(s) = 2$: $\langle drBA, ulD \rangle$.

Greedy best-first search:

Introduction





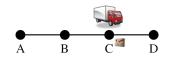
Real problem:

- State s: CC; goal G: AD.
- Actions A: pre, add, del.
- $BC \xrightarrow{drBC} CC$.

Greedy best-first search:

Introduction





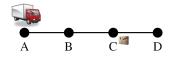
Relaxed problem:

- State s: CC; goal G: AD.
- Actions A: add.
- $h^{\mathcal{R}}(s) = 2$: $\langle drBA, ulD \rangle$.

Greedy best-first search:

Introduction



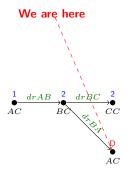


Real problem:

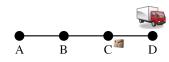
- State s: AC; goal G: AD.
- Actions A: pre, add, del.
- Duplicate state, prune.

Greedy best-first search: (tie-breaking: alphabetic)

Introduction



References

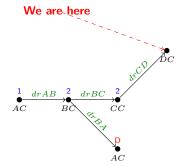


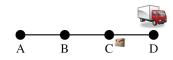
Real problem:

- State s: DC; goal G: AD.
- Actions A: pre, add, del.
- $CC \xrightarrow{drCD} DC$.

Greedy best-first search:

Introduction



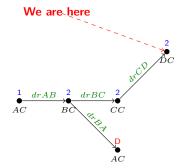


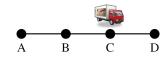
Relaxed problem:

- State s: DC; goal G: AD.
- Actions A: add.
- $h^{\mathcal{R}}(s) = 2$: $\langle drBA, ulD \rangle$.

Greedy best-first search:

Introduction



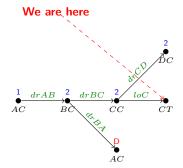


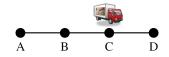
Real problem:

- State s: CT; goal G: AD.
- Actions A: pre, add, del.
- $CC \xrightarrow{loC} CT$.

Greedy best-first search:

Introduction

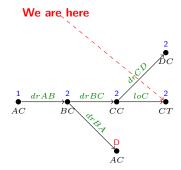


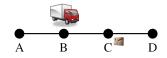


Relaxed problem:

- State s: CT; goal G: AD.
- Actions A: add.
- $h^{\mathcal{R}}(s) = 2$: $\langle drBA, ulD \rangle$.

Greedy best-first search:

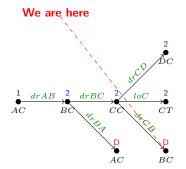


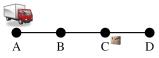


Real problem:

- State s: BC; goal G: AD.
- Actions A: pre, add, del.
- Duplicate state, prune.

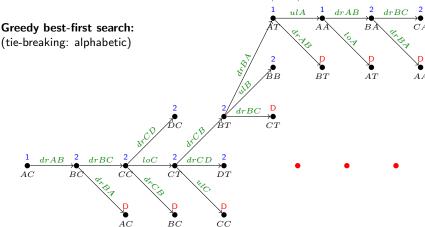
Greedy best-first search: (tie-breaking: alphabetic)





Real problem:

- Initial state I: AC; goal G: AD.
- Actions A: pre, add, del.
- \bullet drXY, loX, ulX.



References

Questionnaire

Question!

Introduction

Does Only-Adds yield a "good heuristic" (accurate goal distance estimates) in ...

(A): Freecell? (B): SAT? (#unsatisfied clauses)

(C): Blocksworld? (D): Path Planning?

- \rightarrow (A): No: The heuristic value does take into account how many cards are already "home", but it is completely independent of the placement of all the other cards. In particular, dead-end avoidance is essential in Freecell, but the heuristic is completely unable to detect any dead ends.
- \rightarrow (B): No: Typically, it is easy to satisfy many clauses, but then satisfying the remaining ones involves re-doing the entire assignment. (Nevertheless, this heuristic is being used in local search for SAT!)
- \rightarrow (C): No: e.g., if a single block A still needs to move elsewhere, but there are 100 blocks on top of A, then the heuristic value is 1.
- \rightarrow (D): No! The heuristic remains constantly 1 until we reach the actual goal state.

Remarks

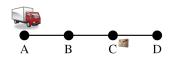
Introduction

The goal-counting approximation h = "count the number of goals currently not true" is a very uninformative heuristic function:

- Range of heuristic values is small (0...|G|).
- Ignores almost all structure: Heuristic value does not depend on the actions at all!
- ightarrow By the way, is h safe/goal-aware/admissible/consistent? Only safe and goal-aware.
- \rightarrow We will see in \rightarrow the next chapters how to compute **much** better heuristic functions.

Introduction

How to Relax During Search: Ignoring Deletes



Real problem:

- Initial state I: AC; goal G: AD.
- Actions A: pre, add, del.

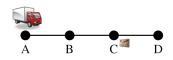
How to Obtain it?

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 \bullet drXY, loX, ulX.

Greedy best-first search:



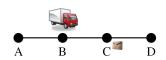


Relaxed problem:

- State s: AC; goal G: AD.
- Actions A: pre, add.
- $h^+(s) = 5$: e.g. $\langle drAB, drBC, drCD, loC, ulD \rangle$.

Greedy best-first search: (tie-breaking: alphabetic)





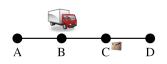
Real problem:

- State s: BC; goal G: AD.
- Actions A: pre, add, del.
- $AC \xrightarrow{drAB} BC$.

Greedy best-first search:

Introduction



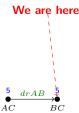


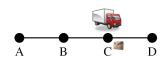
What's a Heuristic?

Relaxed problem:

- State s: BC; goal G: AD.
- Actions A: pre, add.
- $h^+(s) = 5$: e.g. $\langle drBA, drBC, drCD, loC, ulD \rangle$.

Greedy best-first search: (tie-breaking: alphabetic)





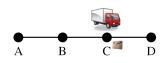
Real problem:

- State s: CC; goal G: AD.
- Actions A: pre, add, del.
- $BC \xrightarrow{drBC} CC$.

Greedy best-first search:

Introduction



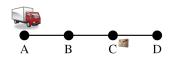


Relaxed problem:

- State s: CC; goal G: AD.
- Actions A: pre, add.
- $h^+(s) = 5$: e.g. $\langle drCB, drBA, drCD, loC, ulD \rangle$.

Greedy best-first search: (tie-breaking: alphabetic)

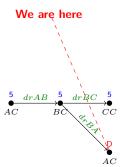


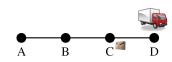


Real problem:

- State s: AC; goal G: AD.
- Actions A: pre, add, del.
- Duplicate state, prune.

Greedy best-first search: (tie-breaking: alphabetic)





Real problem:

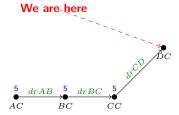
- State s: DC; goal G: AD.
- Actions A: pre, add, del.

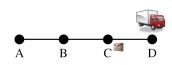
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• $CC \xrightarrow{drCD} DC$

Greedy best-first search:

Introduction

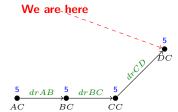


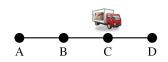


Relaxed problem:

- State s: DC; goal G: AD.
 - Actions A: pre, add.
- $h^+(s) = 5$: e.g. $\langle drDC, drCB, drBA, loC, ulD \rangle$.

Greedy best-first search: (tie-breaking: alphabetic)



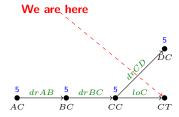


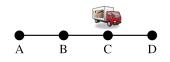
Real problem:

- State s: CT; goal G: AD.
- Actions A: pre, add, del.
- $CC \xrightarrow{loC} CT$.

Greedy best-first search:

Introduction

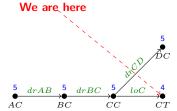


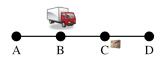


Relaxed problem:

- State s: CT; goal G: AD.
- Actions A: pre, add.
- $h^+(s) = 4$: e.g. $\langle drCB, drBA, drCD, ulD \rangle$.

Greedy best-first search: (tie-breaking: alphabetic)



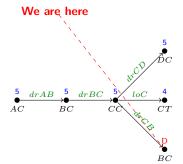


Real problem:

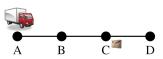
- State s: BC; goal G: AD.
- Actions A: pre, add, del.
- Duplicate state, prune.

Greedy best-first search: (tie-breaking: alphabetic)

Introduction

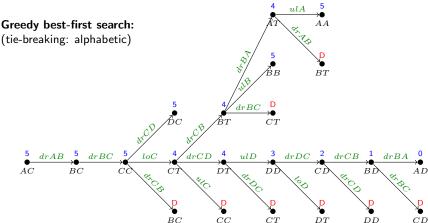


References



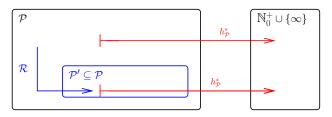
Real problem:

- Initial state *I*: *AC*; goal *G*: *AD*.
- Actions A: pre, add, del.
- \bullet drXY, loX, ulX.



Only-Adds and Ignoring Deletes are "Native" Relaxations

Native Relaxations: Confusing special case where $\mathcal{P}' \subseteq \mathcal{P}$.



- Problem class P: STRIPS planning tasks.
- Perfect heuristic $h_{\mathcal{P}}^*$ for \mathcal{P} : Length h^* of a shortest plan.
- ullet Transformation \mathcal{R} : Drop the (preconditions and) delete lists.
- Simpler problem class \mathcal{P}' is a special case of \mathcal{P} , $\mathcal{P}' \subseteq P$: STRIPS planning tasks with empty (preconditions and) delete lists.
- Perfect heuristic for \mathcal{P}' : Shortest plan for only-adds respectively delete-free STRIPS task.

hat's a Heuristic? How to Use it? How to Obtain it? Conclusion

Summary

Introduction

- Heuristic functions h map states to estimates of remaining cost. A heuristic
 can be safe, goal-aware, admissible, and/or consistent. A heuristic may
 dominate another heuristic, and an ensemble of heuristics may be additive.
- Greedy best-first search can be used for satisficing planning, A^* can be used for optimal planning provided h is admissible. Weighted A^* interpolates between the two.
- Relaxation is a method to compute heuristic functions. Given a problem \mathcal{P} we want to solve, we define a relaxed problem \mathcal{P}' . We derive the heuristic by mapping into \mathcal{P}' and taking the solution to this simpler problem as the heuristic estimate.
- During search, the relaxation is used *only inside* the computation of h(s) on each state s; the relaxation does not affect anything else.

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References

Reading

Introduction

- Al'18 Chapters 4 and 5.
- A word of caution regarding Artificial Intelligence: A Modern Approach (Third Edition) [Russell and Norvig (2010)], Sections 3.6.2 and 3.6.3.

Content: These little sections are aimed at describing basically what I call "How to Relax" here. They do serve to get some intuitions. However, strictly speaking, they're a bit misleading. Formally, a pattern database (Section 3.6.3) is what is called a "relaxation" in Section 3.6.2: pattern databases are abstract transition systems that have more transitions than the original state space. On the other hand, not every relaxation can be usefully described this way; e.g., critical-path heuristics (\rightarrow Chapter 9) and ignoring-deletes heuristics (\rightarrow Chapter 10) are associated with very different state spaces.

References

What's a Heuristic? How to Use it? How to Obtain it? Conclusion References

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- Jörg Hoffmann and Bernhard Nebel. The FF planning system: Fast plan generation through heuristic search. *Journal of Artificial Intelligence Research*, 14:253–302, 2001.
- Robert C. Holte. Common misconceptions concerning heuristic search. In Ariel Felner and Nathan R. Sturtevant, editors, *Proceedings of the 3rd Annual Symposium on Combinatorial Search (SOCS'10)*, pages 46–51, Stone Mountain, Atlanta, GA, July 2010. AAAI Press.
- Stuart Russell and Peter Norvig. Artificial Intelligence: A Modern Approach (Third Edition). Prentice-Hall, Englewood Cliffs, NJ, 2010.