

$$\sum m_\nu =$$

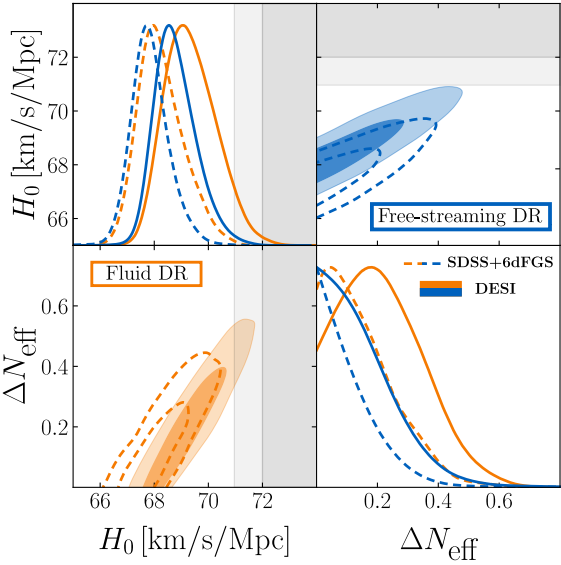
[†] notari@fqa.ub.edu
[‡] frompineve@ifae.es

MontePython;

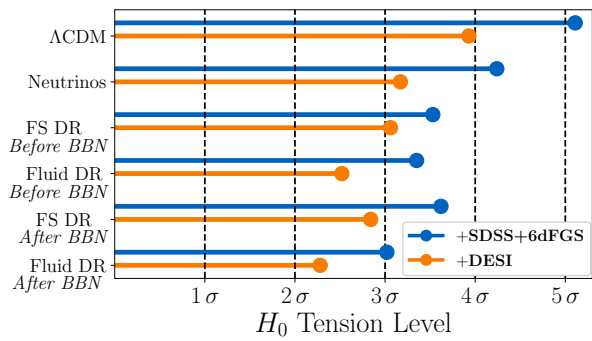
Σ

Σ

ΔN_{eff}		< 0.386	$0.221^{+0.088}_{-0.18}$	0.06		
			69.35		$68.62^{+0.53}_{-0.76}$	$68.97^{+0.65}_{-0.93}$
H_0 GT		3.53σ	2.81σ	3.43σ	3.79σ	3.31σ
H_0 IT		3.06σ	2.52σ	3.24σ	3.4σ	2.93σ



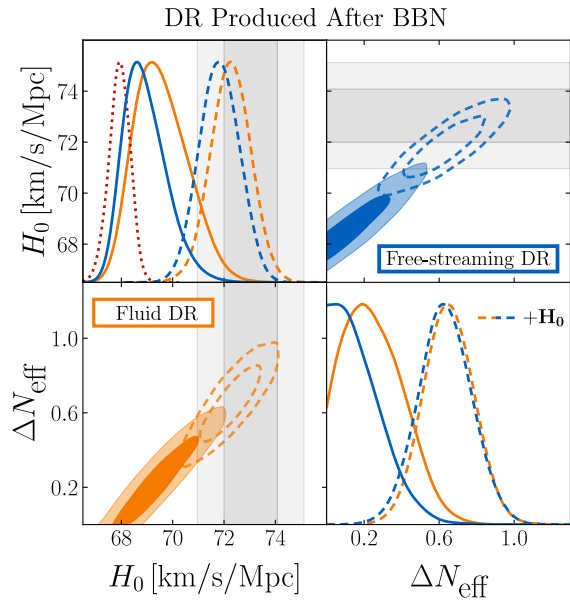
Σ



√

e.g. [66].

ΔN_{eff}	< 0.435	$0.26 \text{ (0.34)}^{+0.11}_{-0.21}$ $69.56 \text{ (69.82)}^{+0.85}_{-1.2}$	$0.63 \text{ (0.56)} \pm 0.14$ $71.82 \text{ (71.65)}^{+0.78}_{-0.77}$	$0.65 \text{ (0.73)} \pm 0.13$ $72.26 \text{ (73.0)}^{+0.77}_{-0.78}$
H_0 GT	3.37σ	2.59σ	0.94σ	0.6σ
H_0 IT	2.84σ	2.28σ	0.94σ	0.6σ
$\Delta\chi^2$	~ 0	-0.4	-20.5	-24.7
ΔAIC	$+2.0$	$+1.6$	-18.5	-22.7



Remarkably, our findings also suggest that the

Acknowledgments

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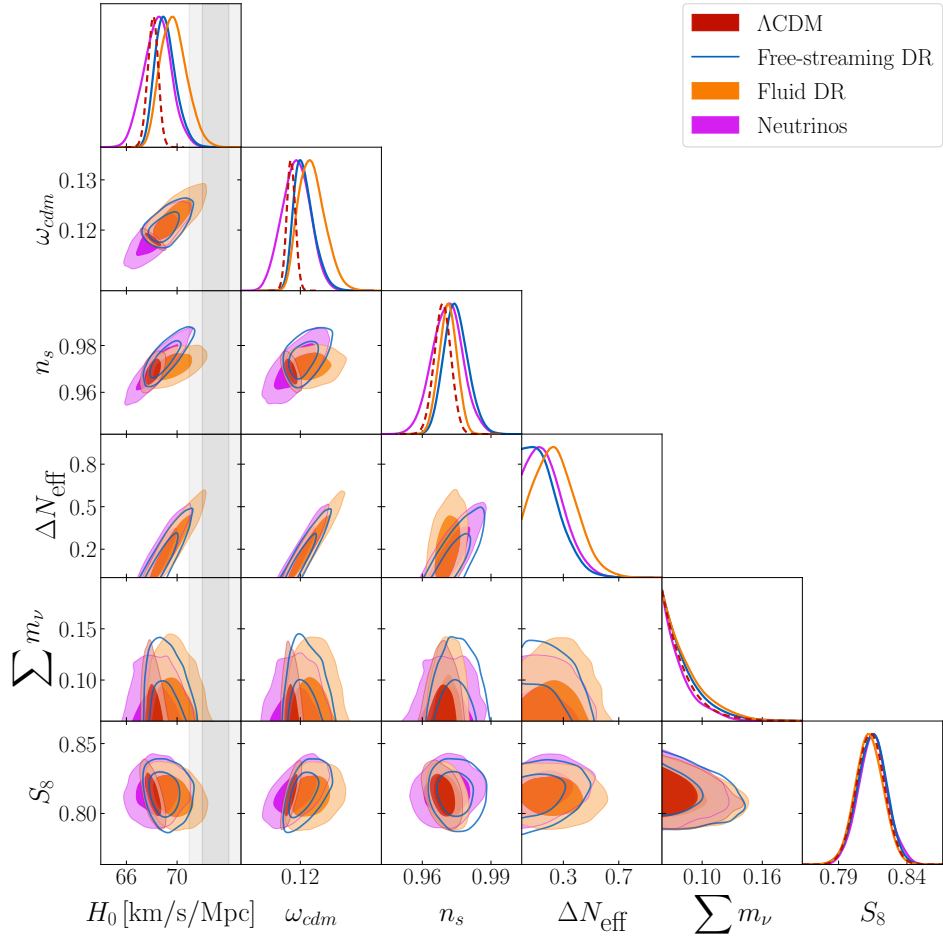
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$$\sqrt{\sigma_m^2 + \sigma_{\text{MC}}^2}$$

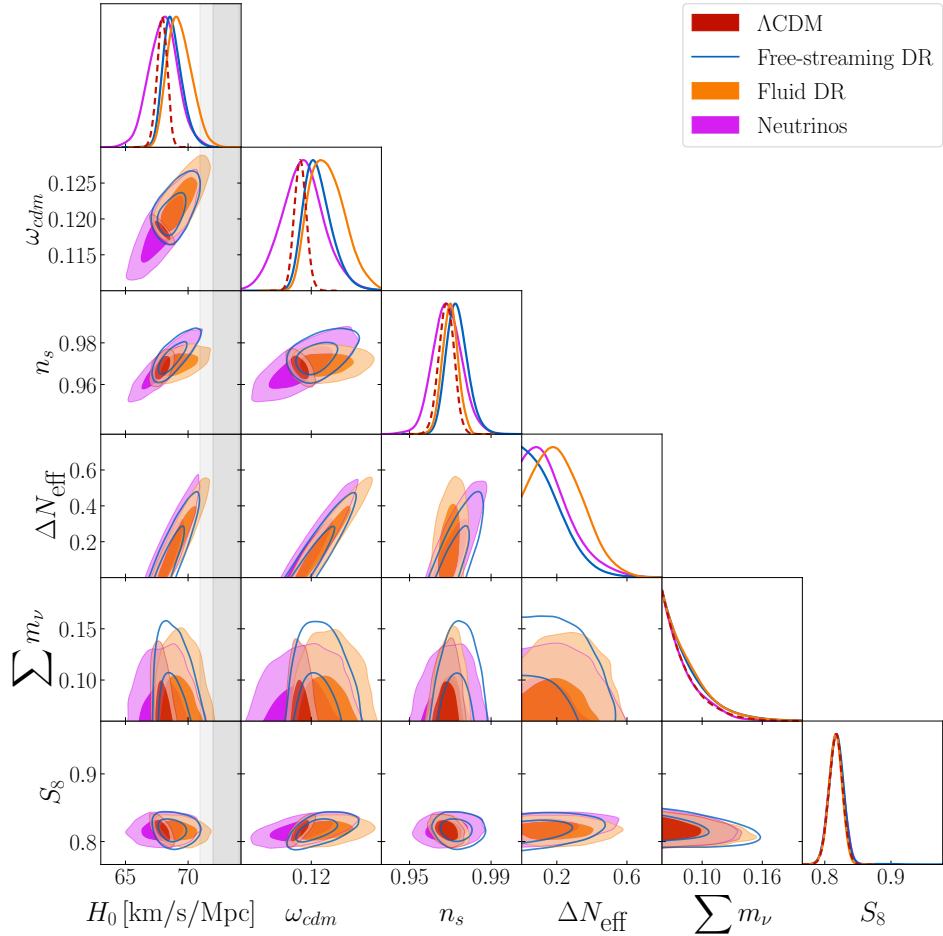
$$\int_{-\infty}^{\infty} \exp\left(-\frac{\left(h-\mu_m\right)^2}{2\sigma_m^2}\right) \int_{-\infty}^{\infty} x^2 dx \tag{A2}$$

$100\omega_b$	$2.249 (2.248)^{+0.013}_{-0.013}$	$2.262 (2.264)^{+0.016}_{-0.016}$	$2.272 (2.274)^{+0.017}_{-0.019}$	$2.256 (2.25)^{+0.019}_{-0.017}$
ω_{cdm}	$0.11811 (0.11823)^{+0.00087}_{-0.00086}$	$0.1208 (0.1212)^{+0.0015}_{-0.0024}$	$0.1224 (0.1205)^{+0.0021}_{-0.0031}$	$0.1193 (0.1176)^{+0.0024}_{-0.0028}$
$\ln 10^{10} A_s$	$3.054 (3.057)^{+0.014}_{-0.016}$	$3.062 (3.055)^{+0.015}_{-0.017}$	$3.052 (3.041)^{+0.015}_{-0.016}$	$3.058 (3.057)^{+0.015}_{-0.018}$
n_s	$0.9689 (0.9689)^{+0.0036}_{-0.0036}$	$0.9748 (0.9742)^{+0.0047}_{-0.0057}$	$0.9712 (0.9678)^{+0.0039}_{-0.0039}$	$0.9713 (0.9715)^{+0.0064}_{-0.0065}$
τ_{reio}	$0.0608 (0.0608)^{+0.0070}_{-0.0081}$	$0.0614 (0.0595)^{+0.0072}_{-0.0083}$	$0.0619 (0.053)^{+0.0072}_{-0.0084}$	$0.0615 (0.0641)^{+0.0067}_{-0.0087}$
ΔN_{eff}	—	< 0.395	$0.25 (0.13)^{+0.11}_{-0.13}$	$0.12 (0.062)^{+0.16}_{-0.16}$
H_0 [km/s/Mpc]	$68.09 (68.18)^{+0.43}_{-0.40}$	$69.10 (68.91)^{+0.66}_{-0.95}$	$69.75 (69.19)^{+0.87}_{-1.2}$	$68.5 (68.4)^{+1.1}_{-0.99}$
S_8	$0.813 (0.818)^{+0.010}_{-0.010}$	$0.814 (2.483)^{+0.011}_{-0.011}$	$0.812 (0.809)^{+0.010}_{-0.010}$	$0.816 (0.807)^{+0.011}_{-0.010}$
H_0 GT	4.4σ	3.2σ	2.43σ	3.0σ
H_0 IT	4.12σ	2.81σ	2.17σ	3.08σ



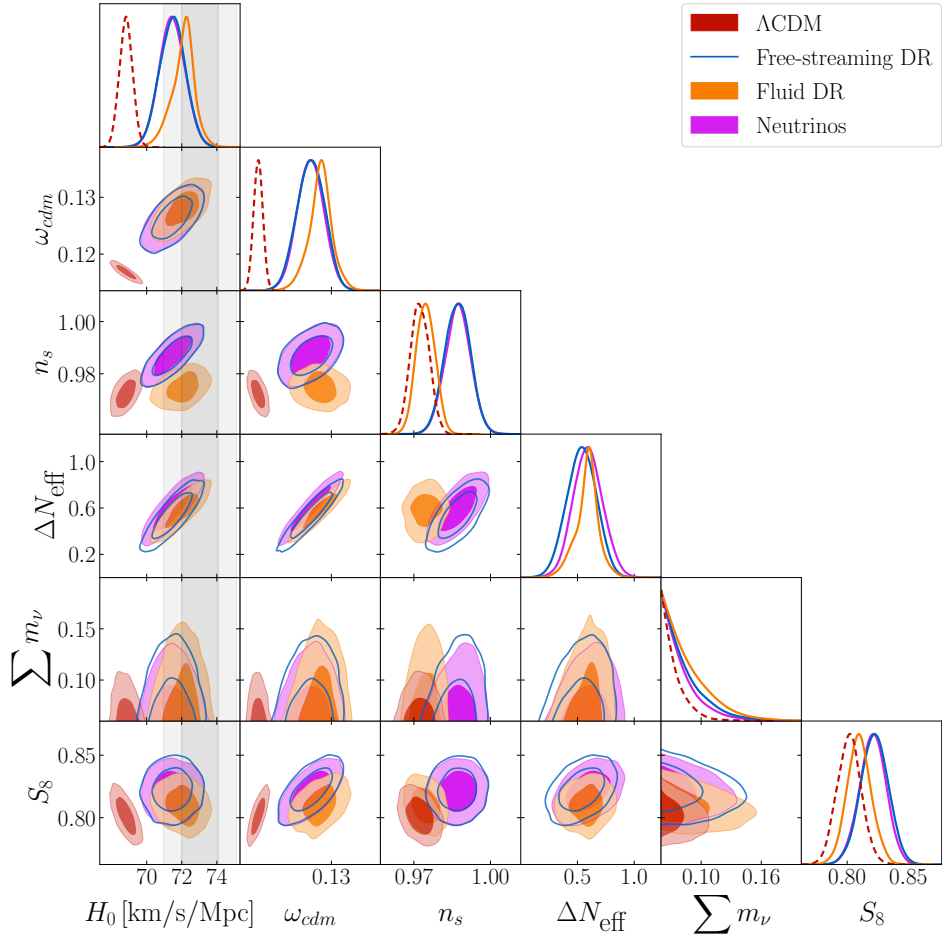
2. P18+DESI+Pantheon_Plus

$100\omega_b$	2.247 (2.251) $^{+0.013}_{-0.013}$	2.258 (2.246) $^{+0.015}_{-0.016}$	2.265 (2.257) $^{+0.017}_{-0.019}$	2.248 (2.256) $^{+0.019}_{-0.018}$
ω_{cdm}	0.11844 (0.11856) $^{+0.00084}_{-0.00086}$	0.1211 (0.1192) $^{+0.0014}_{-0.0025}$	0.1223 (0.1212) $^{+0.0020}_{-0.0030}$	0.1186 (0.1191) $^{+0.0028}_{-0.0031}$
$\ln 10^{10} A_s$	3.054 (3.061) $^{+0.015}_{-0.016}$	3.061 (3.039) $^{+0.014}_{-0.017}$	3.050 (3.055) $^{+0.015}_{-0.015}$	3.054 (3.052) $^{+0.017}_{-0.018}$
n_s	0.9681 (0.9679) $^{+0.0039}_{-0.0036}$	0.9734 (0.9689) $^{+0.0045}_{-0.0058}$	0.9699 (0.9667) $^{+0.0037}_{-0.0039}$	0.9685 (0.9759) $^{+0.0068}_{-0.0069}$
τ_{reio}	0.0602 (0.0636) $^{+0.0074}_{-0.0083}$	0.0606 (0.0537) $^{+0.0071}_{-0.0082}$	0.0605 (0.0619) $^{+0.0072}_{-0.0080}$	0.0601 (0.0608) $^{+0.0071}_{-0.0086}$
ΔN_{eff}	—	< 0.386	0.221 (0.128) $^{+0.088}_{-0.100}$	0.06 (0.143) $^{+0.17}_{-0.19}$
H_0 [km/s/Mpc]	67.93 (68.07) $^{+0.44}_{-0.38}$	68.79 (67.99) $^{+0.60}_{-0.89}$	69.35 (68.72) $^{+0.81}_{-1.1}$	68.0 (67.14) $^{+0.97}_{-1.2}$
S_8	0.817 (0.822) $^{+0.010}_{-0.010}$	0.818 (0.436) $^{+0.010}_{-0.011}$	0.8161 (0.825) $^{+0.0099}_{-0.0099}$	0.817 (0.821) $^{+0.011}_{-0.011}$
M_b	-19.424 (-19.421) $^{+0.013}_{-0.011}$	-19.396 (-19.426) $^{+0.017}_{-0.028}$	-19.381 (-19.4) $^{+0.024}_{-0.033}$	-19.422 (-19.448) $^{+0.030}_{-0.036}$
H_0 GT	4.53 σ	3.53 σ	2.81 σ	3.54 σ
H_0 IT	3.93 σ	3.06 σ	2.52 σ	3.22 σ



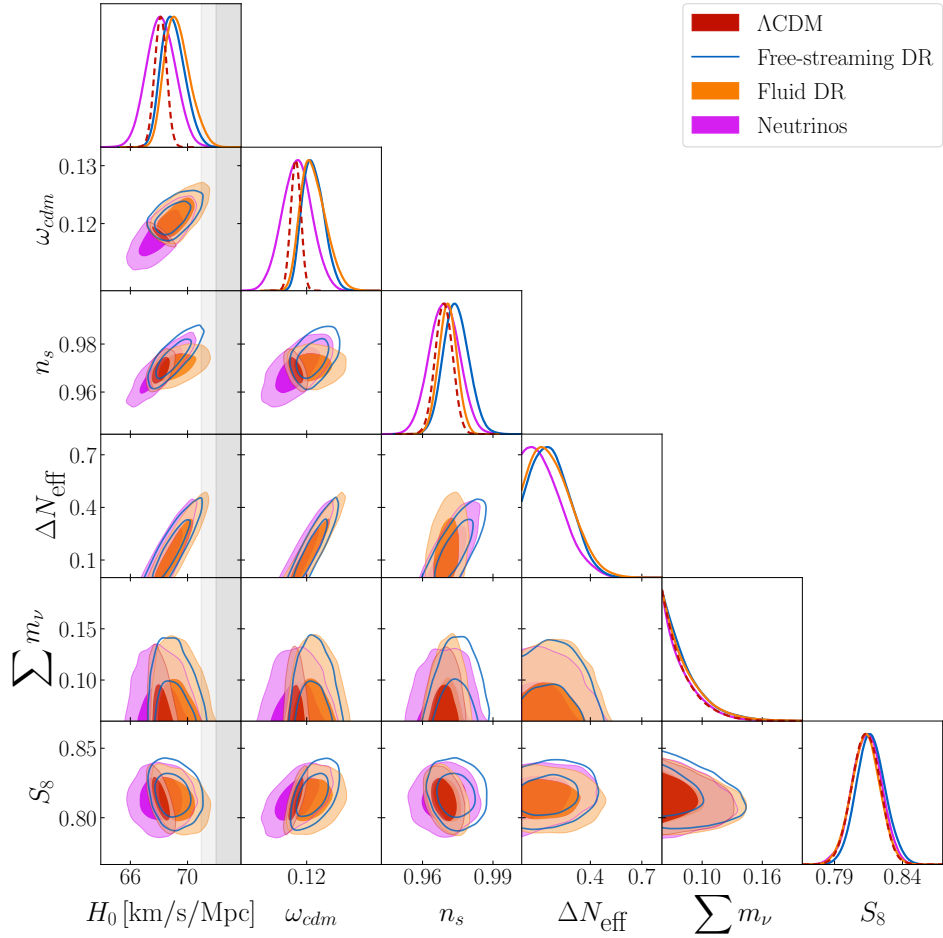
3. P18+DESI+Pantheon_Plus+H₀

$100\omega_b$	$2.264 (2.275)^{+0.013}_{-0.013}$	$2.290 (2.289)^{+0.015}_{-0.015}$	$2.304 (2.307)^{+0.015}_{-0.015}$	$2.291 (2.285)^{+0.014}_{-0.014}$
ω_{cdm}	$0.11682 (0.11669)^{+0.00083}_{-0.00083}$	$0.1263 (0.126)^{+0.0025}_{-0.0025}$	$0.1281 (0.1286)^{+0.0019}_{-0.0016}$	$0.1263 (0.1268)^{+0.0024}_{-0.0024}$
$\ln 10^{10} A_s$	$3.061 (3.07)^{+0.015}_{-0.016}$	$3.078 (3.079)^{+0.015}_{-0.017}$	$3.048 (3.042)^{+0.015}_{-0.016}$	$3.078 (3.065)^{+0.016}_{-0.016}$
n_s	$0.9723 (0.9732)^{+0.0037}_{-0.0036}$	$0.9871 (0.9867)^{+0.0049}_{-0.0050}$	$0.9746 (0.972)^{+0.0036}_{-0.0039}$	$0.9872 (0.9873)^{+0.0049}_{-0.0050}$
τ_{reio}	$0.0651 (0.0666)^{+0.0074}_{-0.0085}$	$0.0634 (0.0636)^{+0.0072}_{-0.0086}$	$0.0633 (0.0588)^{+0.0074}_{-0.0077}$	$0.0633 (0.0567)^{+0.0073}_{-0.0084}$
ΔN_{eff}	—	$0.54 (0.52)^{+0.13}_{-0.13}$	$0.592 (0.611)^{+0.091}_{-0.091}$	$0.59 (0.619)^{+0.12}_{-0.13}$
H_0 [km/s/Mpc]	$68.82 (68.98)^{+0.37}_{-0.39}$	$71.47 (71.39)^{+0.73}_{-0.76}$	$72.13 (72.25)^{+0.61}_{-0.41}$	$71.46 (71.79)^{+0.73}_{-0.73}$
S_8	$0.8017 (0.8045)^{+0.0096}_{-0.010}$	$0.822 (0.824)^{+0.011}_{-0.011}$	$0.8095 (0.8086)^{+0.0097}_{-0.010}$	$0.821 (0.819)^{+0.011}_{-0.011}$
M_b	$-19.398 (-19.392)^{+0.011}_{-0.011}$	$-19.320 (-19.319)^{+0.021}_{-0.021}$	$-19.301 (-19.295)^{+0.017}_{-0.011}$	$-19.320 (-19.311)^{+0.021}_{-0.021}$
H_0 GT	3.82σ	1.23σ	0.75σ	1.24σ
H_0 IT	3.8σ	1.23σ	0.76σ	1.24σ
$\Delta\chi^2$	—	-19.1	-23.8	-17.5
ΔAIC	—	-17.1	-21.8	-15.5



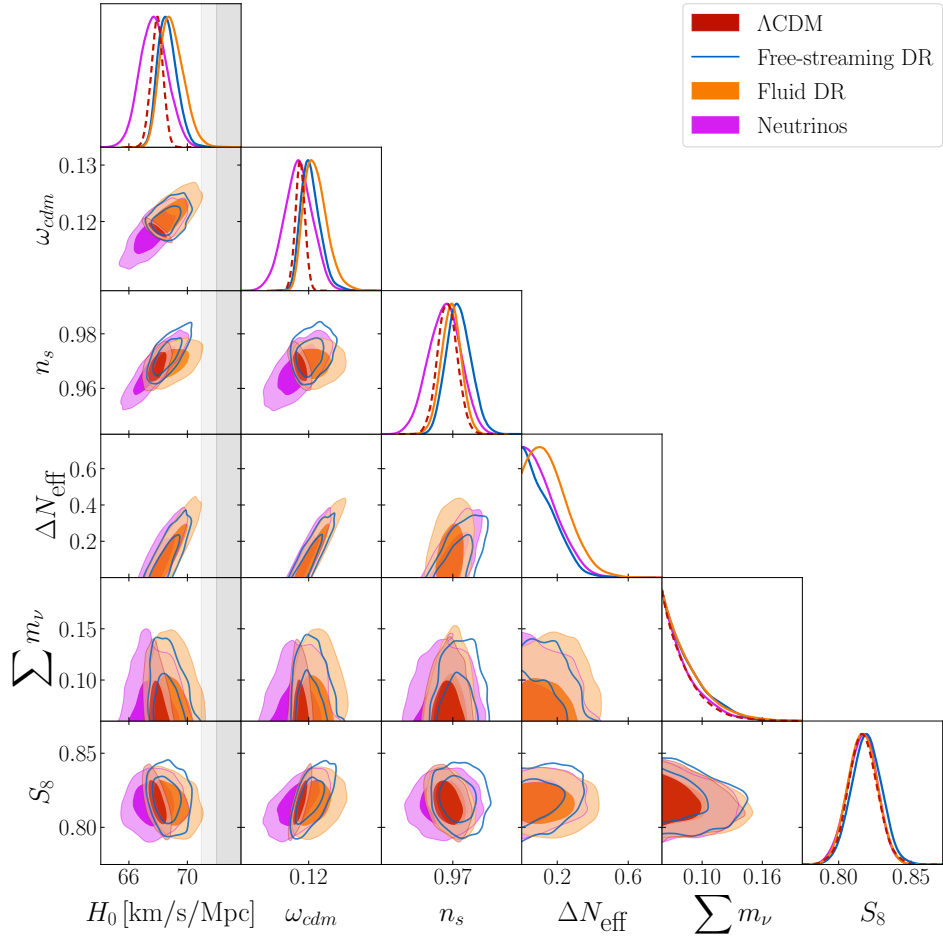
4. P18+DESI+Y_{He}, D/H

$100\omega_b$	$2.249 (2.24)^{+0.013}_{-0.013}$	$2.254 (2.25)^{+0.015}_{-0.017}$	$2.266 (2.271)^{+0.016}_{-0.018}$	$2.250 (2.23)^{+0.017}_{-0.018}$
ω_{cdm}	$0.11812 (0.11808)^{+0.00089}_{-0.00087}$	$0.1212 (0.1206)^{+0.0016}_{-0.0021}$	$0.1212 (0.1205)^{+0.0018}_{-0.0026}$	$0.1183 (0.1166)^{+0.0026}_{-0.0026}$
$\ln 10^{10} A_s$	$3.055 (3.051)^{+0.015}_{-0.015}$	$3.061 (3.06)^{+0.015}_{-0.017}$	$3.053 (3.061)^{+0.015}_{-0.016}$	$3.055 (3.058)^{+0.016}_{-0.016}$
n_s	$0.9689 (0.9676)^{+0.0036}_{-0.0035}$	$0.9743 (0.9754)^{+0.0050}_{-0.0057}$	$0.9707 (0.9723)^{+0.0039}_{-0.0039}$	$0.9693 (0.9629)^{+0.0064}_{-0.0062}$
τ_{reio}	$0.0610 (0.0587)^{+0.0071}_{-0.0082}$	$0.0605 (0.061)^{+0.0072}_{-0.0083}$	$0.0619 (0.0642)^{+0.0074}_{-0.0083}$	$0.0611 (0.0655)^{+0.0071}_{-0.0083}$
ΔN_{eff}	—	$0.179 (0.136)^{+0.073}_{-0.077}$	$0.182 (0.148)^{+0.061}_{-0.077}$	$0.06 (-0.078)^{+0.16}_{-0.16}$
H_0 [km/s/Mpc]	$68.09 (68.17)^{+0.42}_{-0.41}$	$69.00 (68.86)^{+0.69}_{-0.93}$	$69.30 (69.39)^{+0.71}_{-1.0}$	$68.2 (67.2)^{+1.0}_{-0.011}$
S_8	$0.814 (0.814)^{+0.010}_{-0.010}$	$0.817 (1.829)^{+0.010}_{-0.011}$	$0.813 (0.816)^{+0.011}_{-0.010}$	$0.814 (0.822)^{+0.011}_{-0.011}$
H_0 GT	4.42σ	3.23σ	2.97σ	3.37σ
H_0 IT	3.95σ	2.99σ	2.66σ	3.31σ



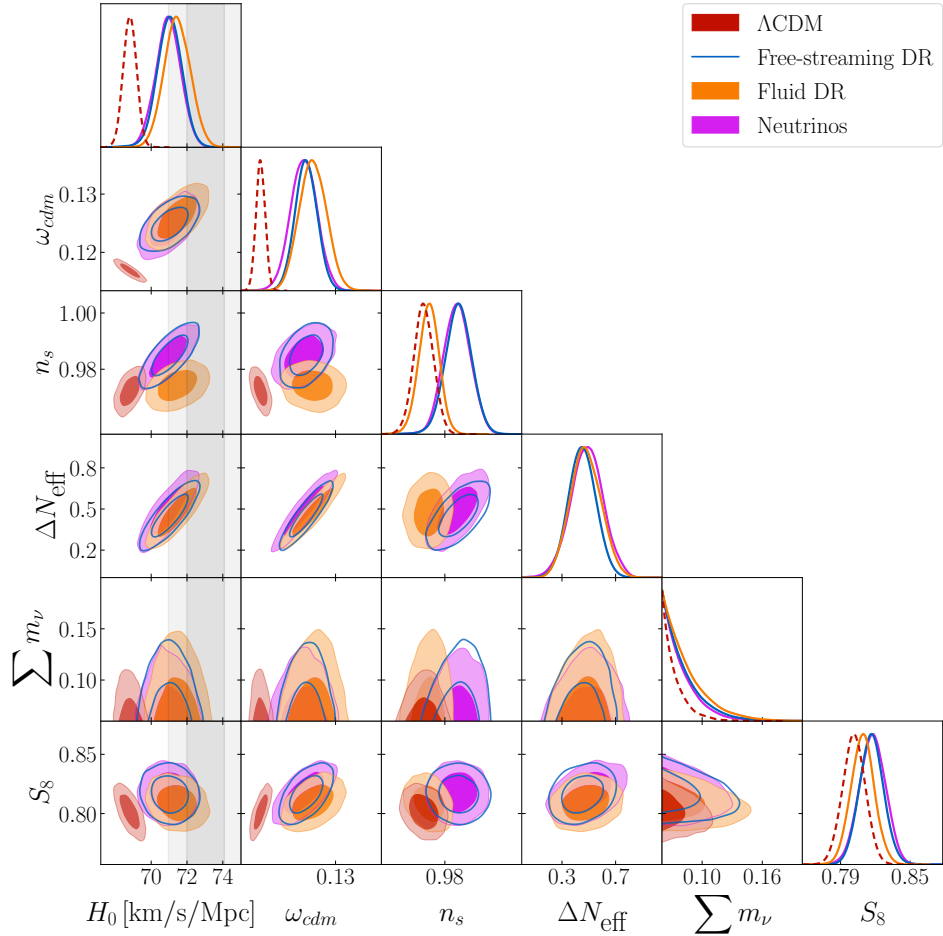
5. P18+DESI+Y_{He}, D/H+Pantheon_Plus

$100\omega_b$	$2.247 (2.251)^{+0.014}_{-0.014}$	$2.254 (2.255)^{+0.014}_{-0.014}$	$2.260 (2.242)^{+0.016}_{-0.016}$	$2.249 (2.238)^{+0.015}_{-0.015}$
ω_{cdm}	$0.11845 (0.11833)^{+0.00084}_{-0.00084}$	$0.1203 (0.1196)^{+0.0013}_{-0.0020}$	$0.1213 (0.1187)^{+0.0016}_{-0.0024}$	$0.1191 (0.1183)^{+0.0015}_{-0.0025}$
$\ln 10^{10} A_s$	$3.053 (3.055)^{+0.014}_{-0.016}$	$3.059 (3.061)^{+0.015}_{-0.017}$	$3.052 (3.045)^{+0.015}_{-0.015}$	$3.055 (3.034)^{+0.015}_{-0.017}$
n_s	$0.9680 (0.9677)^{+0.0035}_{-0.0038}$	$0.9721 (0.9728)^{+0.0043}_{-0.0049}$	$0.9694 (0.9694)^{+0.0037}_{-0.0037}$	$0.9695 (0.9662)^{+0.0050}_{-0.0065}$
τ_{reio}	$0.0602 (0.0606)^{+0.0069}_{-0.0081}$	$0.0607 (0.0625)^{+0.0071}_{-0.0084}$	$0.0608 (0.058)^{+0.0071}_{-0.0082}$	$0.0599 (0.0519)^{+0.0070}_{-0.0082}$
ΔN_{eff}	—	< 0.295	< 0.365	$0.087 (-0.007)^{+0.076}_{-0.15}$
H_0 [km/s/Mpc]	$67.92 (68.09)^{+0.41}_{-0.41}$	$68.58 (68.89)^{+0.55}_{-0.69}$	$68.97 (68.0)^{+0.65}_{-0.93}$	$68.13 (67.53)^{+0.68}_{-0.96}$
S_8	$0.817 (0.817)^{+0.010}_{-0.0098}$	$0.819 (0.816)^{+0.010}_{-0.011}$	$0.816 (0.819)^{+0.010}_{-0.010}$	$0.817 (0.818)^{+0.010}_{-0.0097}$
M_b	$-19.424 (-19.421)^{+0.012}_{-0.012}$	$-19.404 (-19.393)^{+0.016}_{-0.021}$	$-19.392 (-19.423)^{+0.020}_{-0.028}$	$-19.418 (-19.436)^{+0.020}_{-0.029}$
H_0 GT	4.58σ	3.8σ	3.31σ	3.96σ
H_0 IT	3.79σ	3.42σ	2.93σ	3.68σ



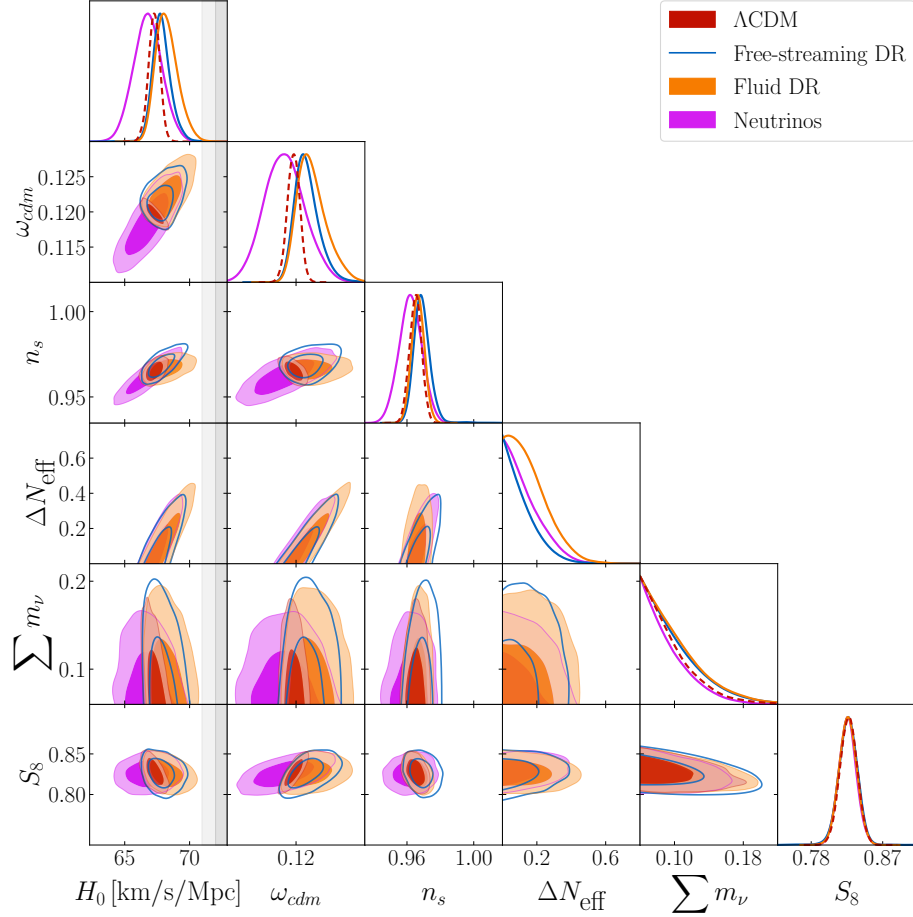
6. P18+DESI+Y_{He}, D/H+Pantheon_Plus+H₀

$100\omega_b$	$2.264 (2.273)^{+0.013}_{-0.013}$	$2.285 (2.28)^{+0.014}_{-0.014}$	$2.295 (2.296)^{+0.015}_{-0.015}$	$2.287 (2.284)^{+0.015}_{-0.014}$
ω_{cdm}	$0.11685 (0.11643)^{+0.00081}_{-0.00081}$	$0.1248 (0.1238)^{+0.0019}_{-0.0019}$	$0.1260 (0.1256)^{+0.0024}_{-0.0024}$	$0.1244 (0.1229)^{+0.0023}_{-0.0023}$
$\ln 10^{10} A_s$	$3.060 (3.068)^{+0.015}_{-0.017}$	$3.076 (3.057)^{+0.015}_{-0.017}$	$3.051 (3.042)^{+0.015}_{-0.017}$	$3.075 (3.063)^{+0.016}_{-0.017}$
n_s	$0.9723 (0.9721)^{+0.0035}_{-0.0036}$	$0.9849 (0.9825)^{+0.0048}_{-0.0047}$	$0.9742 (0.9747)^{+0.0037}_{-0.0037}$	$0.9844 (0.9832)^{+0.0050}_{-0.0049}$
τ_{reio}	$0.0647 (0.0677)^{+0.0073}_{-0.0084}$	$0.0635 (0.0557)^{+0.0071}_{-0.0087}$	$0.0636 (0.0604)^{+0.0070}_{-0.0087}$	$0.0639 (0.0615)^{+0.0074}_{-0.0084}$
ΔN_{eff}	—	$0.45 (0.38)^{+0.10}_{-0.10}$	$0.48 (0.48)^{+0.11}_{-0.11}$	$0.49 (0.431)^{+0.12}_{-0.12}$
H_0 [km/s/Mpc]	$68.81 (69.12)^{+0.37}_{-0.37}$	$71.02 (70.59)^{+0.69}_{-0.67}$	$71.46 (71.78)^{+0.74}_{-0.72}$	$70.95 (71.06)^{+0.70}_{-0.70}$
S_8	$0.8015 (0.8005)^{+0.0098}_{-0.0098}$	$0.817 (2.701)^{+0.010}_{-0.010}$	$0.8090 (0.8007)^{+0.0099}_{-0.010}$	$0.817 (0.807)^{+0.011}_{-0.011}$
M_b	$-19.398 (-19.387)^{+0.011}_{-0.011}$	$-19.332 (-19.341)^{+0.019}_{-0.020}$	$-19.321 (-19.31)^{+0.021}_{-0.021}$	$-19.335 (-19.332)^{+0.020}_{-0.020}$
H_0 GT	3.83σ	1.62σ	1.24σ	1.67σ
H_0 IT	3.84σ	1.62σ	1.24σ	1.67σ
$\Delta\chi^2$	—	-12.7	-17.7	-10.5
ΔAIC	—	-10.7	-15.7	-8.5



7. P18+SDSS+6dFGS+Pantheon_Plus

$100\omega_b$	$2.238 (2.253)^{+0.013}_{-0.013}$	$2.246 (2.248)^{+0.015}_{-0.015}$	$2.251 (2.252)^{+0.016}_{-0.018}$	$2.232 (2.23)^{+0.018}_{-0.018}$
ω_{cdm}	$0.11964 (0.11931)^{+0.00090}_{-0.00089}$	$0.1217 (0.1202)^{+0.0012}_{-0.0022}$	$0.1223 (0.1204)^{+0.0015}_{-0.0025}$	$0.1183 (0.1177)^{+0.0028}_{-0.0031}$
$\ln 10^{10} A_s$	$3.049 (3.053)^{+0.013}_{-0.015}$	$3.055 (3.049)^{+0.014}_{-0.016}$	$3.048 (3.048)^{+0.014}_{-0.016}$	$3.045 (3.051)^{+0.016}_{-0.016}$
n_s	$0.9652 (0.9653)^{+0.0036}_{-0.0037}$	$0.9691 (0.9698)^{+0.0039}_{-0.0053}$	$0.9666 (0.9656)^{+0.0038}_{-0.0038}$	$0.9621 (0.9615)^{+0.0069}_{-0.0068}$
τ_{reio}	$0.0572 (0.0578)^{+0.0067}_{-0.0075}$	$0.0570 (0.0563)^{+0.0069}_{-0.0078}$	$0.0577 (0.056)^{+0.0068}_{-0.0080}$	$0.0568 (0.0597)^{+0.0067}_{-0.0075}$
ΔN_{eff}	—	< 0.312	< 0.285	$-0.04 (-0.061)^{+0.18}_{-0.18}$
$\sum m_\nu$	< 0.152	< 0.174	< 0.169	< 0.146
H_0 [km/s/Mpc]	$67.27 (67.78)^{+0.43}_{-0.43}$	$67.84 (67.79)^{+0.58}_{-0.75}$	$68.25 (67.83)^{+0.69}_{-0.98}$	$66.8 (66.9)^{+1.1}_{-1.1}$
S_8	$0.827 (0.826)^{+0.011}_{-0.011}$	$0.826 (5.249)^{+0.012}_{-0.012}$	$0.826 (0.828)^{+0.011}_{-0.011}$	$0.826 (0.826)^{+0.011}_{-0.011}$
M_b	$-19.443 (-19.43)^{+0.013}_{-0.013}$	$-19.421 (-19.426)^{+0.015}_{-0.026}$	$-19.412 (-19.427)^{+0.021}_{-0.030}$	$-19.458 (-19.455)^{+0.034}_{-0.035}$
H_0 GT	5.12σ	4.37σ	3.83σ	4.19σ
H_0 IT	5.11σ	3.53σ	3.35σ	4.24σ



Parameter	P18+SDSS+6dFGS+Pantheon_Plus	P18+DESI+Pantheon_Plus	P18+DESI+Pantheon_Plus+H₀
$100\omega_b$	2.251 (2.241) $^{+0.015}_{-0.017}$	2.266 (2.263) $^{+0.015}_{-0.019}$	2.299 (2.305) $^{+0.015}_{-0.015}$
ω_{cdm}	0.1228 (0.1219) $^{+0.0018}_{-0.0028}$	0.1229 (0.1254) $^{+0.0023}_{-0.0034}$	0.1291 (0.1303) $^{+0.0028}_{-0.0028}$
$\ln 10^{10} A_s$	3.047 (3.049) $^{+0.015}_{-0.015}$	3.049 (3.041) $^{+0.015}_{-0.015}$	3.045 (3.053) $^{+0.016}_{-0.016}$
τ_{reio}	0.9658 (0.9652) $^{+0.0038}_{-0.0037}$	0.9689 (0.9666) $^{+0.0037}_{-0.0037}$	0.9716 (0.9759) $^{+0.0035}_{-0.0035}$
ΔN_{eff}	0.0575 (0.057) $^{+0.0069}_{-0.0075}$	0.0607 (0.057) $^{+0.0071}_{-0.0081}$	0.0627 (0.0679) $^{+0.0073}_{-0.0083}$
$\sum m_\nu$	< 0.433 < 0.166	< 0.137	0.65 (0.73) $^{+0.13}_{-0.14}$ < 0.149
H_0 [km/s/Mpc]	68.39 (67.94) $^{+0.71}_{-1.1}$	69.56 (69.82) $^{+0.85}_{-1.2}$	72.25 (73.0) $^{+0.79}_{-0.79}$
S_8	0.826 (0.834) $^{+0.011}_{-0.011}$	0.815 (0.825) $^{+0.010}_{-0.011}$	0.809 (0.812) $^{+0.011}_{-0.011}$
M_b	-19.408 (-19.42) $^{+0.022}_{-0.033}$	-19.374 (-19.365) $^{+0.026}_{-0.037}$	-19.298 (-19.276) $^{+0.024}_{-0.021}$
H_0 GT	3.69σ		0.6σ
H_0 IT	3.02σ		0.6σ
$\Delta\chi^2$	~ 0	-0.4	-24.7
ΔAIC	+2.0	+1.6	-22.7

TABLE X: Marginalized posteriors for various model parameters for the Fluid DR model where the **P18+DESI+Pantheon_Plus**, and **P18+DESI+Pantheon_Plus+H₀**. All upper bounds are reported at 95% C.L., for any case where the 1σ lower bound is overlapping with our priors.

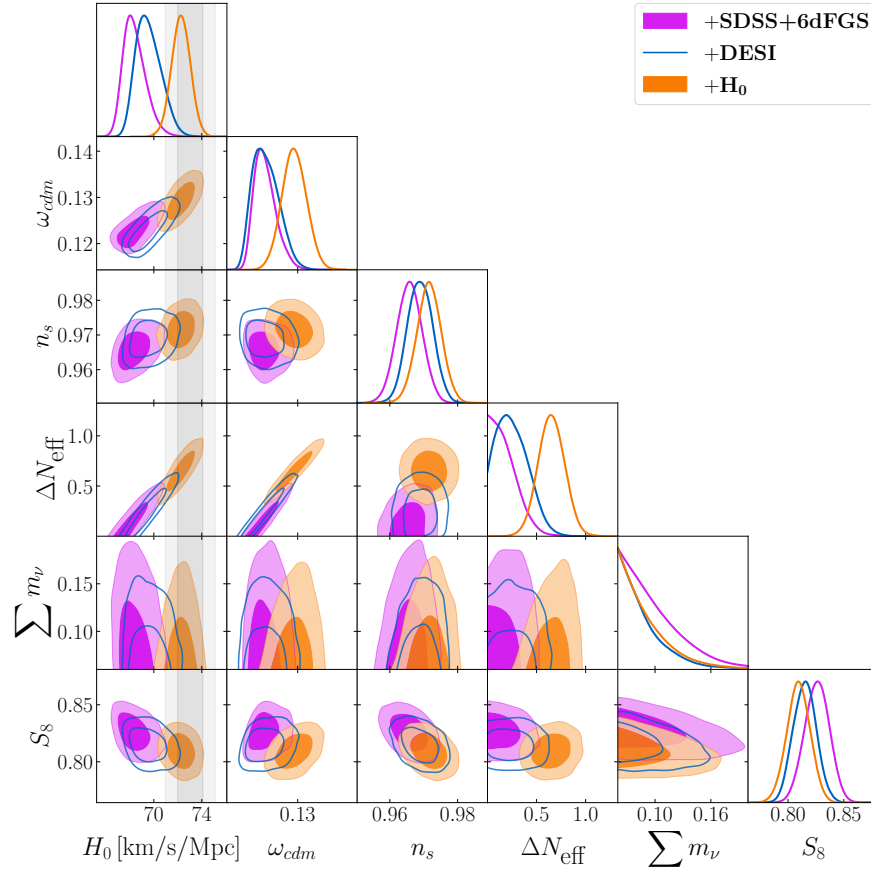
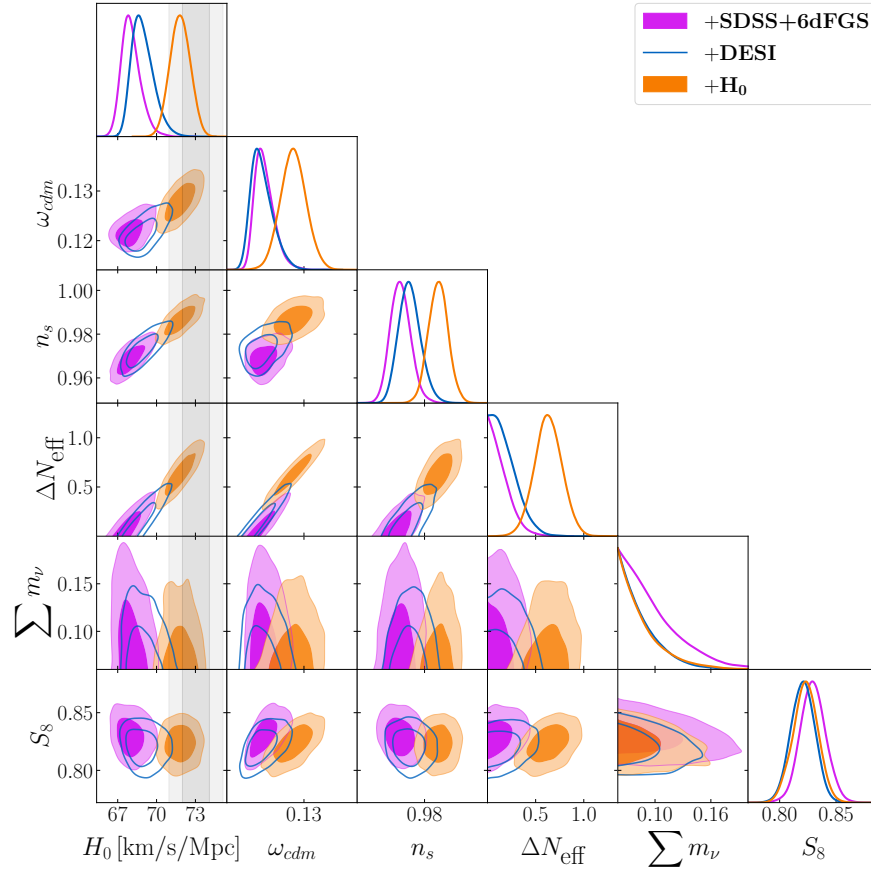


FIG. 11: One and two-dimensional posterior distributions for various model parameters for the Fluid DR model **P18+DESI+Pantheon_Plus**, and **P18+DESI+Pantheon_Plus+H₀**.

Parameter	P18+SDSS+6dFGS+Pantheon_Plus	P18+DESI+Pantheon_Plus	P18+DESI+Pantheon_Plus+H ₀
$100\omega_b$	2.245 (2.24) ^{+0.015} _{-0.014}	2.257 (2.254) ^{+0.015} _{-0.016}	2.288 (2.278) ^{+0.014} _{-0.014}
ω_{cdm}	0.1219 (0.1218) ^{+0.0014} _{-0.0024}	0.1214 (0.1193) ^{+0.0016} _{-0.0027}	0.1278 (0.1287) ^{+0.0026} _{-0.0026}
$\ln 10^{10} A_s$	3.054 (3.041) ^{+0.015} _{-0.016}	3.060 (3.059) ^{+0.014} _{-0.017}	3.077 (3.071) ^{+0.014} _{-0.017}
τ_{reio}	0.9688 (0.9676) ^{+0.0043} _{-0.0050}	0.9731 (0.9732) ^{+0.0045} _{-0.0055}	0.9864 (0.987) ^{+0.0044} _{-0.0047}
ΔN_{eff}	0.0568 (0.0493) ^{+0.0068} _{-0.0079}	0.0602 (0.0623) ^{+0.0071} _{-0.0081}	0.0622 (0.0584) ^{+0.0069} _{-0.0084}
$\sum m_\nu$	< 0.353	< 0.435	0.63 (0.65) ^{+0.14} _{-0.14}
H_0 [km/s/Mpc]	< 0.161	< 0.129	< 0.137
H_0 GT	68.03 (68.17) ^{+0.57} _{-0.84}	68.94 (68.41) ^{+0.63} _{-0.99}	71.82 (71.65) ^{+0.78} _{-0.77}
S_8	0.830 (0.826) ^{+0.011} _{-0.011}	0.821 (0.822) ^{+0.011} _{-0.011}	0.823 (0.83) ^{+0.011} _{-0.011}
M_b	-19.419 (-19.414) ^{+0.017} _{-0.026}	-19.393 (-19.41) ^{+0.019} _{-0.030}	-19.310 (-19.311) ^{+0.022} _{-0.022}
H_0 IT	4.22 σ		0.94 σ
H_0 IT	3.62 σ		0.94 σ
$\Delta\chi^2$	~ 0	+0.4	-20.5
ΔAIC	+2.0	+2.4	-18.5



P18+DESI+Pantheon_Plus+H₀.