

# Positronium

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## 1 Aims

- Measure the ratio between the two and three photons decay of the Positronium;
- Measure the lifetime of the Positronium through the time distribution of the decays.

## 2 Experimental setup

The experimental setup consist in 4 inorganic scintillators; three coplanar (DET. 1,2,3) and a fourth (DET. 4) perpendicular to the plane.

The first three detectors are placed on a circumference in the center of which lies a  $^{22}\text{Na}$  source, with an activity of around 380kBq. These detectors are free to move around the circumference; in this session, two different configurations have been explored. To observe the two-photons decay, the detectors #1 and #2 have been aligned; instead, to observe the three-photons decay, the three coplanar detectors have been positioned at the vertices of an equilateral triangle.

Data are collected from the detectors through a electronic chain: a fan-in-fan-out quad module reply the signal of each detectors and produce four copies of it; then, through a CFD, a trigger signal is produced. The CFD trigger threshold has been set so that the background noise is discarded, while the interesting signals produce an output. As can be seen from fig. 1, the signals corresponding to the detection of the 511keV and 1275keV photons are clearly visible.

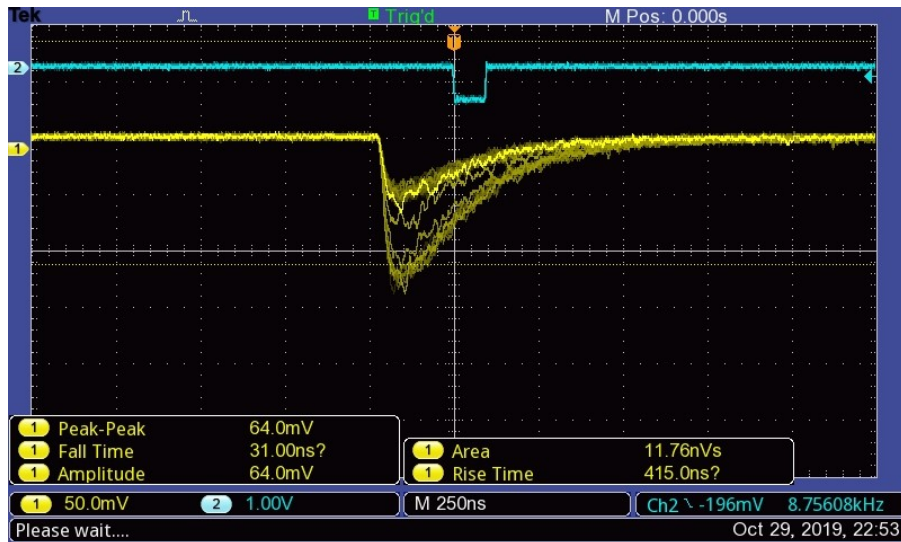


Figure 1: Signal from the detector #2 (yellow), triggering on the CFD (blue). The two different types of peaks, respectively for the 511keV( $\sim 50\text{mV}$ ) and 1275keV( $\sim 125\text{mV}$ ) photons

Between the second and the third day, a technical problem required the substitution of the high voltage power supply; due to this, all thresholds have been re-set; moreover, in the middle of the day

3 the high voltage power supply burned; it has been replaced and the thresholds had to be re-set once again. While in the first two days all the detectors saw the two peaks around an amplitude of respectively 100 and 250mV (and therefore the threshold had been set at about 75mV), in the third day the detectors #1 and #3 saw the two peaks around an amplitude of respectively 50 and 125mV (and therefore the thresholds have been set at about 35mV). For the detector #4, finally, the threshold has been set to about 200mV, such that only the higher energetic photons produce a trigger.

The CFD is provided of two sets of microswitches, to adjust delay and width of the output signal. As verified thanks to the oscilloscope, the delay microswitches allow to adjust the time between the triggering of the system and the start of the logic signal, while the width microswitches can be used to adjust the time length of the logic signal.

### 3 Apparatus calibration

Due to the various problem, the apparatus calibration has been done many times; only the first calibration is here reported, having for the other followed the same procedure.

The positions of the two peaks are known with very high precision:

<sup>22</sup> Na Gamma radiations
511.0 keV
1274.537 keV

Table 1: Gamma radiation for <sup>22</sup>Na from NuDat, <https://www.nndc.bnl.gov/nudat2/decaysearchdirect.jsp?nuc=22NA&unc=nds>

Acquiring the energy spectra with the digitizer, the two peaks are clearly visible; by computing their centroids the horizontal axis can be linearly rescaled to be calibrated in energy. To fit the peaks, observing the variation of background before and after each peak, a gaussian plus a linear noise is used:

$$f(x) = \underbrace{a + bx}_{\text{noise}} + \epsilon e^{-(x-\mu)^2/2\sigma^2}$$

The following result are found:

Det.	$\mu$	$\sigma$	$\chi^2/dof$
#1	$4345.0 \pm 0.1$	$142.7 \pm 0.8$	107/80
	$10589 \pm 2$	$233 \pm 2$	137/149
#2	$4679.4 \pm 0.6$	$143 \pm 1$	150/80
	$11362 \pm 2$	$249 \pm 2$	140/159
#3	$3304.3 \pm 0.5$	$112.3 \pm 0.7$	66/61
	$8021 \pm 1$	$205 \pm 3$	118/108
#4	$3303.0 \pm 0.4$	$112.4 \pm 0.5$	102/67
	$8021 \pm 1$	$205 \pm 3$	118/108

Table 2: Interpolation results

The similarity between the chi-squared value and the number of degree of freedom for all the fits, combined with the observation of the fit plots, guarantee the reliability of the interpolations. For each detector the rescaling factor are computed and thus the resolution  $r$ .

$$E = a \cdot \text{channel} + b$$

$$r = \frac{\text{FWHM}_E}{\mu_E} = 2\sqrt{2 \ln 2} \frac{\sigma_E}{\mu_E} = 2\sqrt{2 \ln 2} \frac{a \cdot \sigma_c}{a \cdot \mu_c + b} = 2\sqrt{2 \ln 2} \frac{\sigma_c}{\mu_c + b/a}$$

Det.	$a[\text{keV}]$	$b[\text{keV}]$	$r_1$	$r_2$
#1	$0.12228 \pm 0.00004$	$-20.3 \pm 0.2$	$8.03 \pm 0.05$	$5.25 \pm 0.05$
#2	$0.11426 \pm 0.00004$	$-23.7 \pm 0.2$	$7.54 \pm 0.05$	$5.25 \pm 0.05$
#3	$0.16188 \pm 0.00004$	$-23.9 \pm 0.2$	$8.38 \pm 0.05$	$6.12 \pm 0.09$
#4	$0.16183 \pm 0.00004$	$-23.5 \pm 0.2$	$8.38 \pm 0.05$	$6.12 \pm 0.09$

Table 3: Calibration result,  $r_1$  and  $r_2$  are the resolutions of the 511[keV] and 1275[keV] peaks respectively.

The resolutions for the peaks are similar between the four detectors.

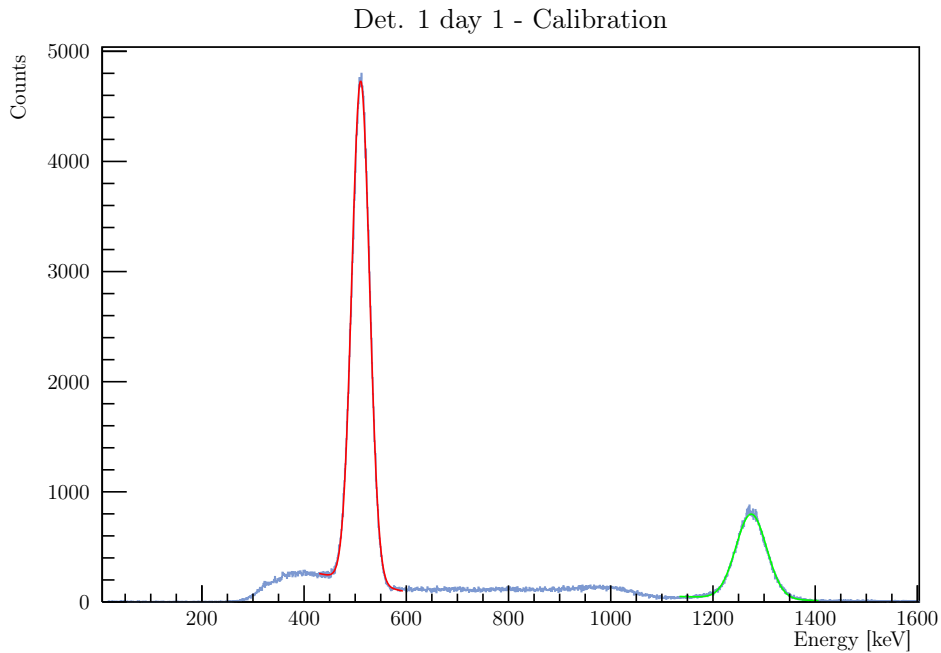


Figure 2: Calibration of detector 1: in blue the histogram of the detected signals, in red and green the peaks fits used for the calibration. Note the x axis properly calibrated in energy.

Finally, even the TAC must be calibrated. This module returns a voltage signal whose amplitude is proportional to the time difference between the triggering of the *start* and the *stop* channels. To calibrate it, the two channels are connected to the same signal; moreover, between the signal and the stop a delay module is inserted. Some measures are made with different delay, obtaining the following histograms (fig. 3).

Neglecting the zero-delay data (too close to the border of the histogram to efficiently find a centroid), centroids for the other peaks have been computed as the average of the registered values, with an associated error corresponding to the standard deviation of the data: a fit or a more precise statistic is meaningless due to the low number of channels in which data are spread on. Having no *zero* point, i.e. even if the *start* and the *stop* signal are the same, cables and other electronic device can introduce a delay between them, only difference can be meaningful defined. The calibration must be done separately for the  $2\gamma$  and the  $3\gamma$  detector, because the range of the TAC used in the two detection has been chosen different, to optimize the data collecting. A linear fit on the centroids returns the following results:

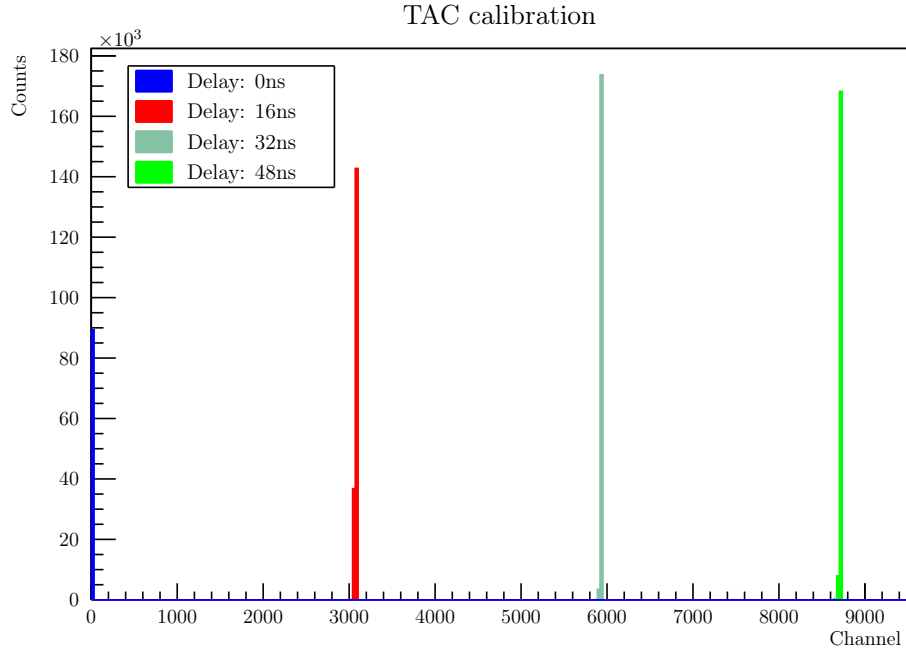


Figure 3: Measure collected from the TAC, with different delay, in about 1min of acquisition in day #2.

$$\Delta \text{channel} = m \cdot \Delta t$$

$$m_{2\gamma} = (117 \pm 1) \text{ns}^{-1}$$

$$m_{3\gamma} = (87.4 \pm 0.4) \text{ns}^{-1}$$

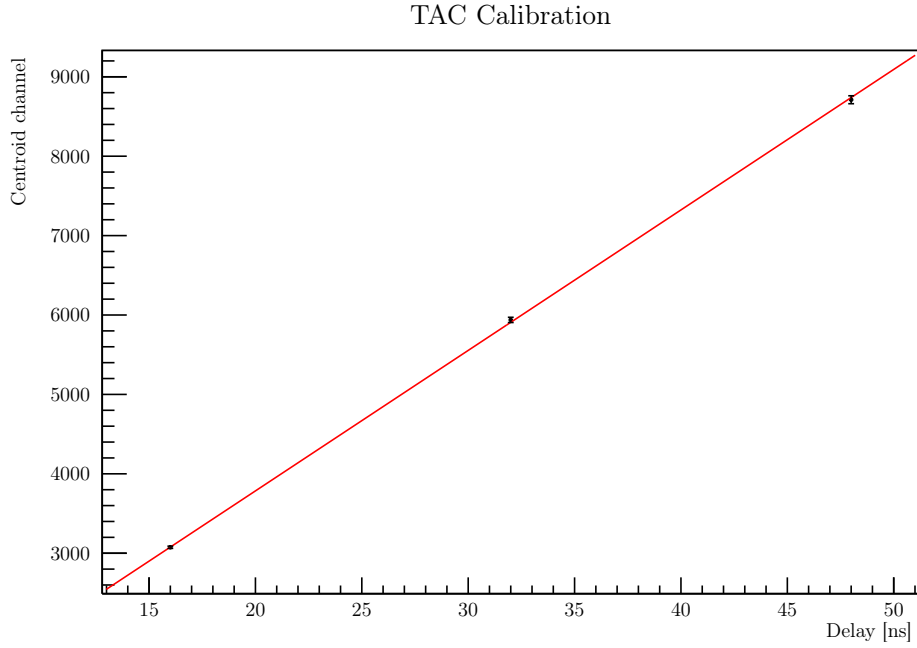


Figure 4: TAC calibration fit, for the  $2\gamma$  setup.

## 4 Digitizer dead time

The digitizer has a dead time, i.e. when it is triggered, it takes some time to scan over all channel and register data. To estimate the dead time, during the three experimental days multiple test have been done, measuring the frequency of different signals with both the digitizer (counting the number of registered events over the acquisition time) and a scaler module, which has a negligible dead time. The result found are summarized in table 4.

Event		Real rate [Hz] (scaler)	Measured rate [Hz] (digit.)
Det. #1	day 1	$9211 \pm 80$	$6543 \pm 10$
Det. #2	day 1	$12248 \pm 80$	$5997 \pm 10$
Det. #1&#2	day 2	$3687 \pm 10$	$3683 \pm 1$
Det. #1&#2&#4	day 2	$44 \pm 1$	$43.9 \pm 0.2$
Det. #1	day 3	$12610 \pm 70$	$7084 \pm 11$
Det. #2	day 3	$12460 \pm 40$	$6001 \pm 10$
Det. #1&#2&#4	day 3	$60 \pm 3$	$59.8 \pm 0.1$

Table 4: Event rate

The PDF of the time between two consecutive decays follows an exponential distribution:

$$p(t) = \nu e^{-\nu t} \quad \rightarrow \quad \langle t \rangle = \int_0^\infty t p(t) dt = \frac{1}{\nu}$$

where  $\nu$  is the event frequency. If the system has a dead time  $\tau$ , two event are both picked only if they differ of a time larger than  $\tau$ ; the measured frequency is therefore:

$$\frac{1}{\nu^*} = \frac{\int_\tau^\infty t p(t) dt}{\int_\tau^\infty p(t) dt} = \frac{\nu \tau + 1}{\nu}$$

Plotting the data in table 4, we obtain the plot in fig. 5

As can be seen from the graphs in fig 5, the dead time isn't constant, but is the result of a stochastic process and can vary at different rates. However, a coarse trend can be estimated (fit in fig. 5a) computing the order of magnitude of dead time:

$$\tau \sim 6 \cdot 10^{-5} \text{s}$$

## 5 Two photons events

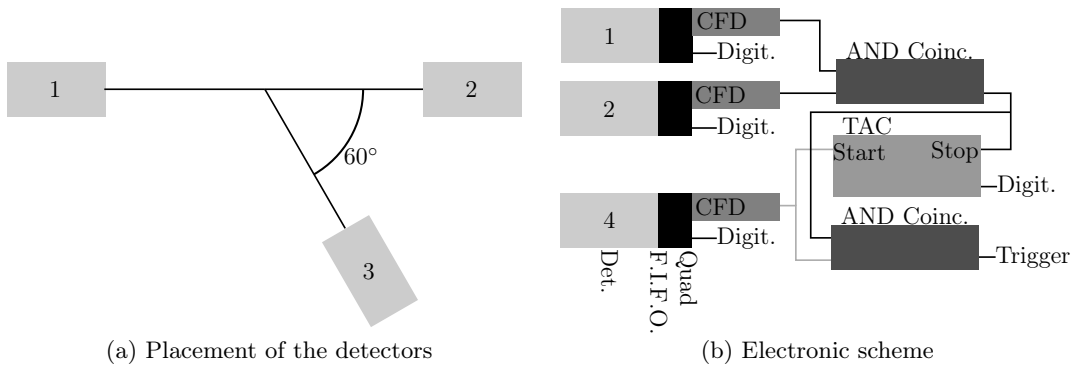
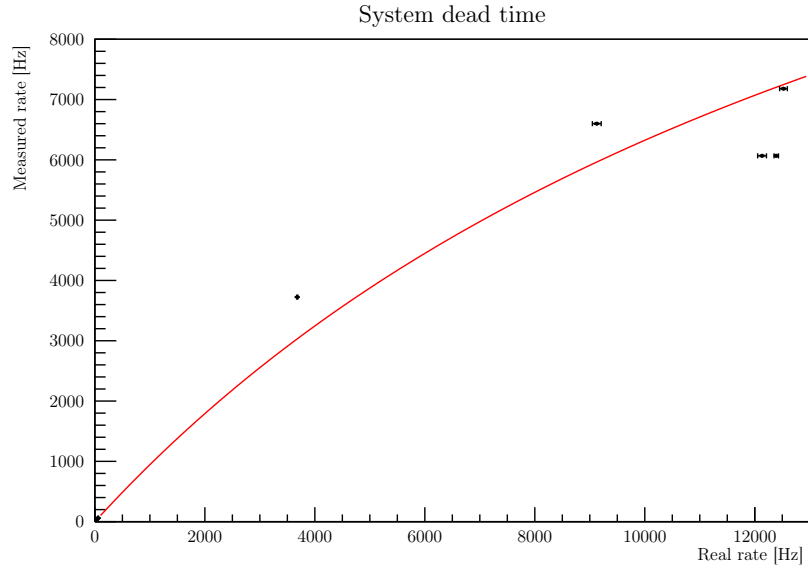
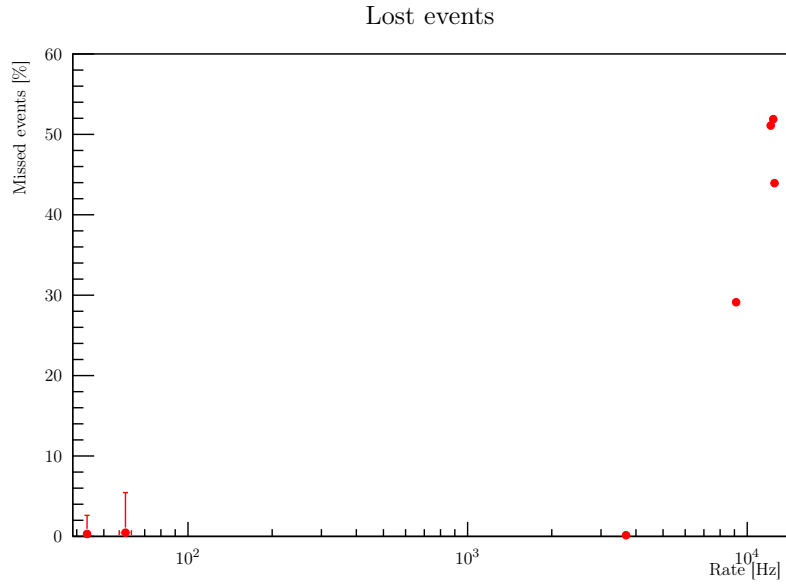


Figure 6: Two photons revelation.

To detect the two-photon events, the detectors have been placed as in fig. 6a. The electronics have been set to be triggered with the coincidente between det. #1, #2 and #4. However, we expect the



(a) Correlation between real and measured rate, and trend.



(b) Ratio of lost events.

Figure 5: Dead time effects.

detector #4 to observe the photons shortly before the other two detectors, because of the lifetime of the positronium. To prevent *false negative*, the width of the CFD of the detector #4 has been set to a high value to produce a long logic signal.

Moreover, the system has been set to measure via the TAC the time difference between the signal from det. #1&#2 and from det. #4.

After the acquisition, a data filtering has been implemented; the events whose sum of the energies of detector #1 and #2 differs from 1022keV for more than 10% (i.e. about two time the resolution) are discarded. The spectra with and without the filter are showed in fig. 7 and the following.

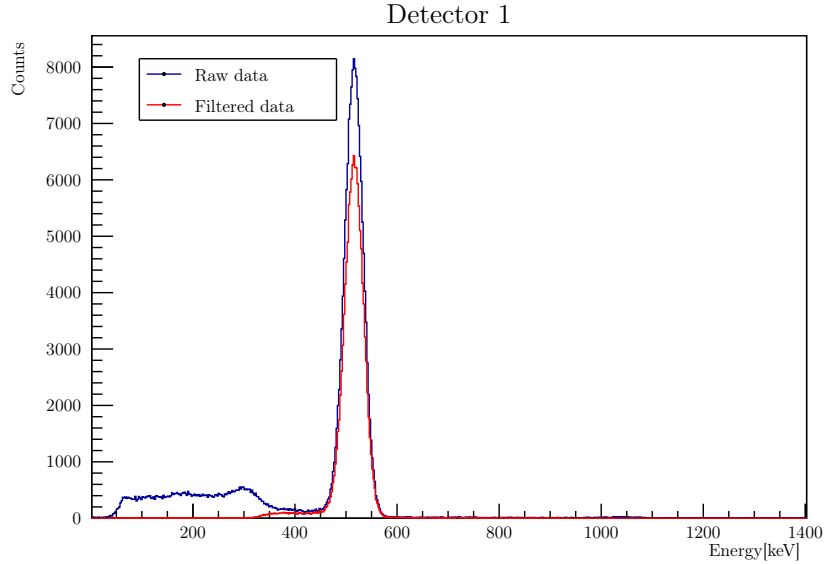


Figure 7: Detector 1. Note the absence of the 1275keV peak.

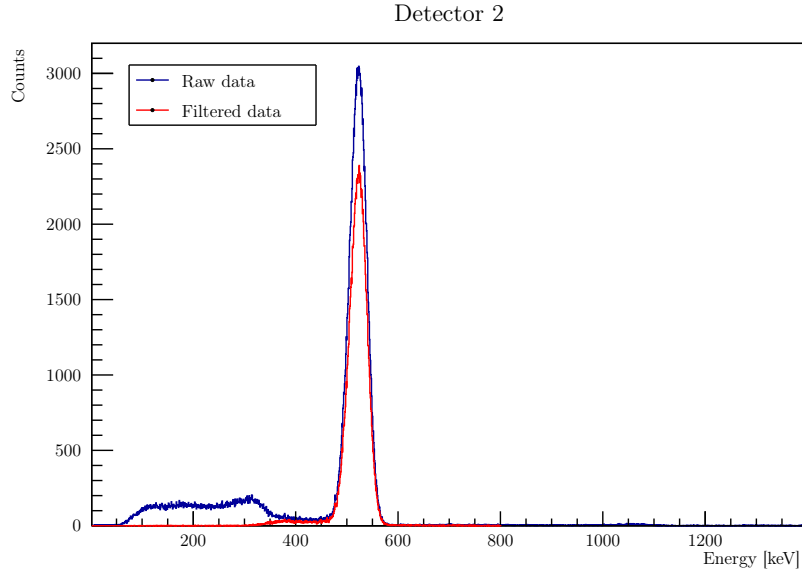


Figure 8: Detector 2. Note the absence of the 1275keV peak.

See fig 9. Should we filter also 1275keV peak to avoid events generated without the emission of the gamma?

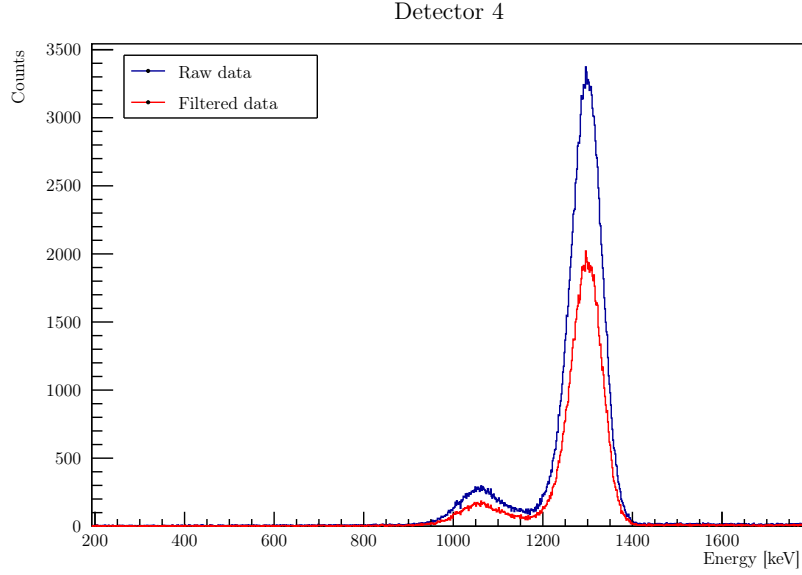


Figure 9: Detector 4. Note the absence of the 511keV peak.

Acquiring the time with TAC, what we obtain is the convolution of the decay law with the statistical gaussian error. At the end, what we see is a peaks centered in an arbitrary value (determined by the electronic configuration of the apparatus, the cable used and the delay introduced) which on its left tail shows a gaussian trend, while on the right the gaussian contribute is negligible and the exponential trend is visible. Fitting the right tail with an exponential is possible to find the parameters of the decay law, in particular the mean lifetime.

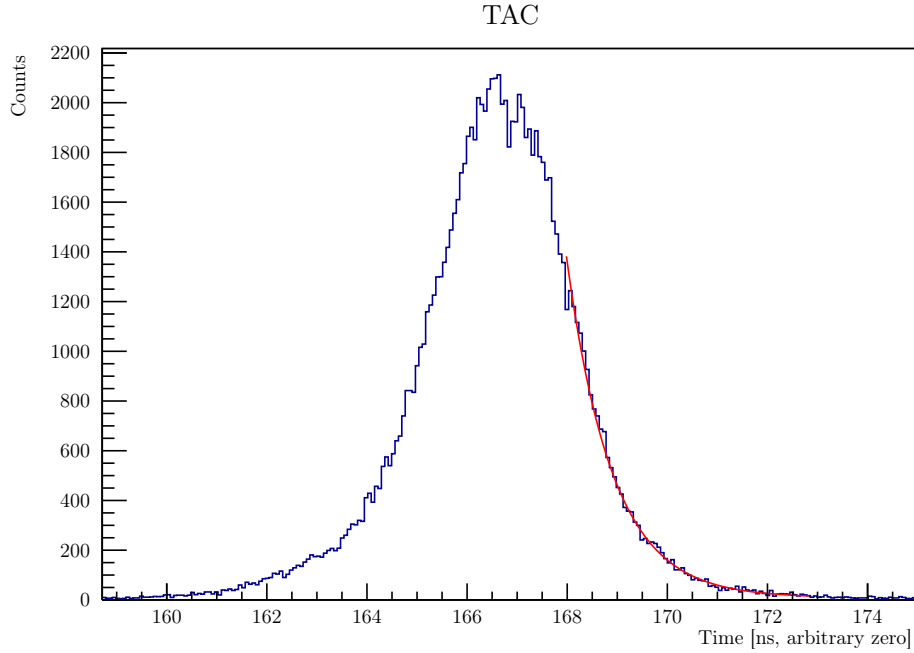


Figure 10: TAC for the  $2\gamma$  decay, with the exponential fit.

Fitting the right wing of the peaks, an estimation of the mean life can be found:

$$\tau = (0.91 \pm 0.01)\text{ns} \quad (1)$$

Is it coherent with the theory?



## 6 Three photons events

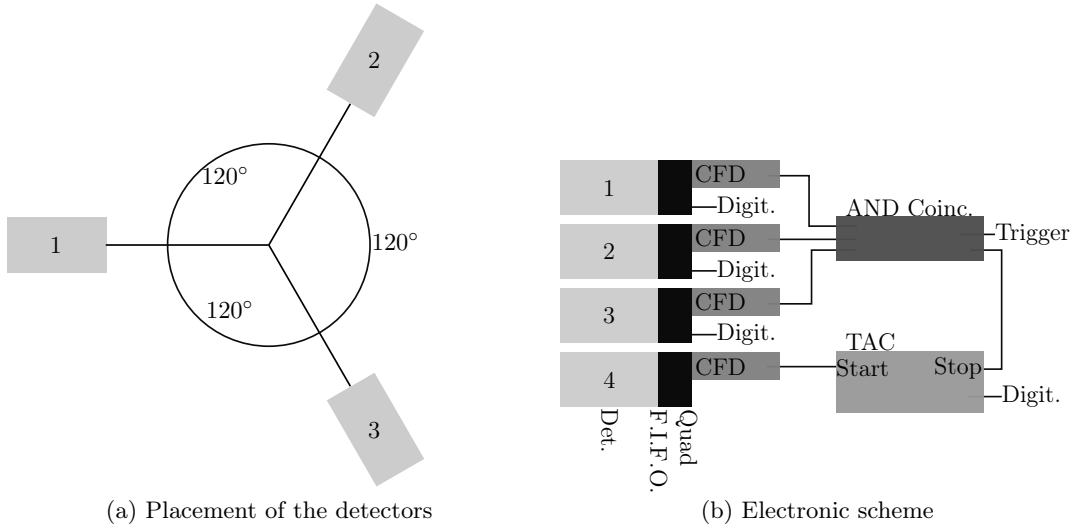


Figure 11: Three photons revelation.

To detect the three-photon events, the detectors have been placed as in fig. 11a. The optimal configurations would provide a triggering on the coincidences between all the four detectors. However, the three-photon events are very rare, and triggering on all the detectors would produce a too-low number of data to make a meaningful statistic, even with a full-night acquisition. Therefore the triggering has been set to the coincidences between the det. #1, #2 and #3, making an a-posteriori coincidence with the detector 4 only for the timing studies.

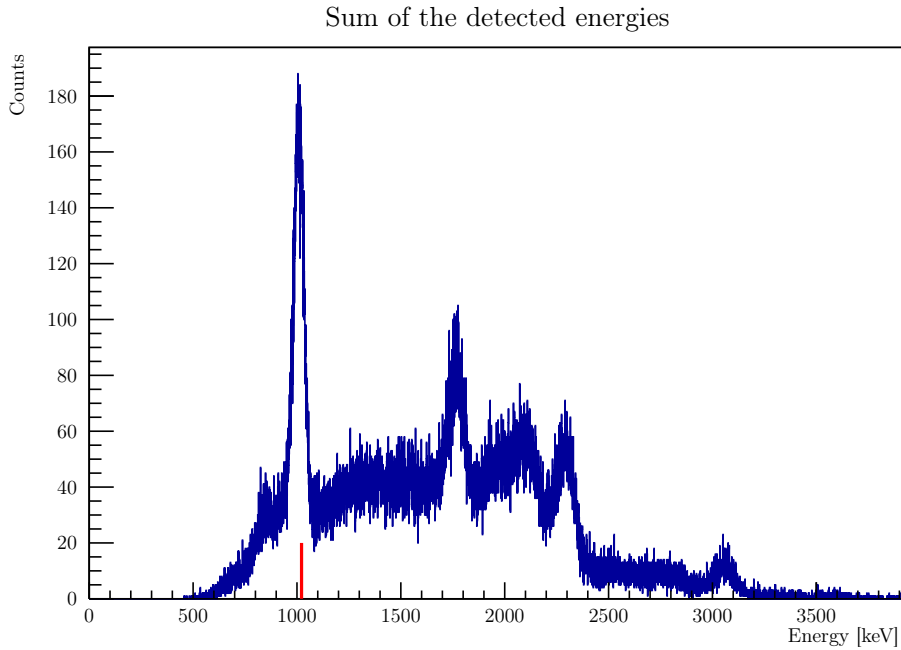


Figure 12: Sum of the energies observed from each detector

Observing fig. 12 we see the peak we're interested in, at 1022keV. All around this peak a lot of noise is present, given mainly by the way-more-probable 2-photons events. To select only the events we're interested in, a filter is applied: each event that violate one or more of the following conditions is discarded.

- The sum of the energies from the three detectors must be 1022keV, with a 10% tolerance (about

$3\sigma$ );

- Each detector must detect an energy around 340keV, with a 10% tolerance.

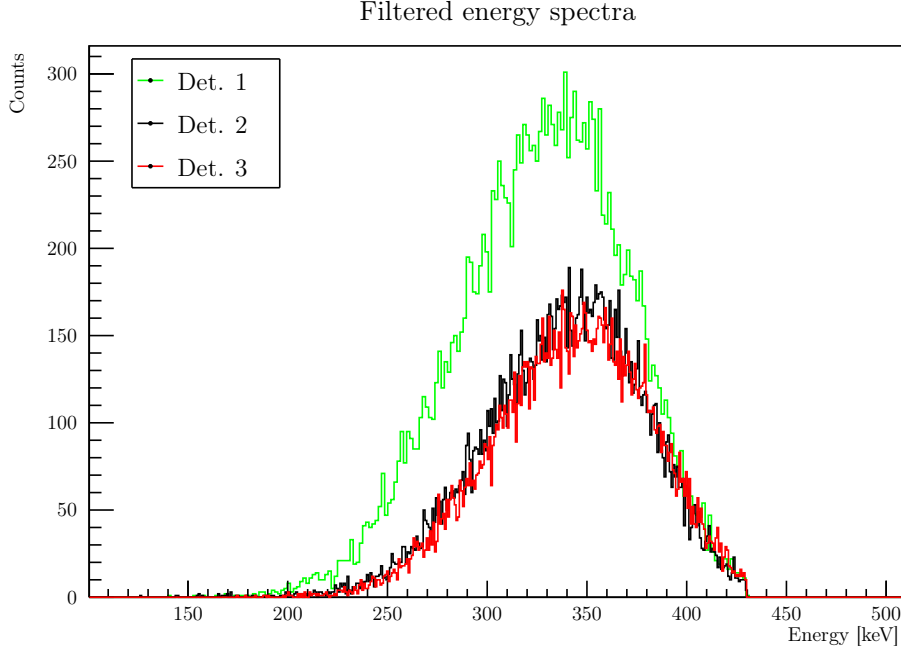


Figure 13: Filtered energy spectra of the detectors. The different bin heights is due to different binning width, itself due to different calibration parameters.

As can be seen from fig. 13, all the detectors show a peak around 340keV, as expected; their spectra are similar so the symmetry is respected.

Finally, the TAC spectrum is computed. During the acquisition no constraint on coincidences with #4 has been imposed, so most of the recorded events lack of TAC start triggering. Excluding the first and the last bin, containing the not-started and the not-stopped events, a filtered TAC spectrum can be computed.

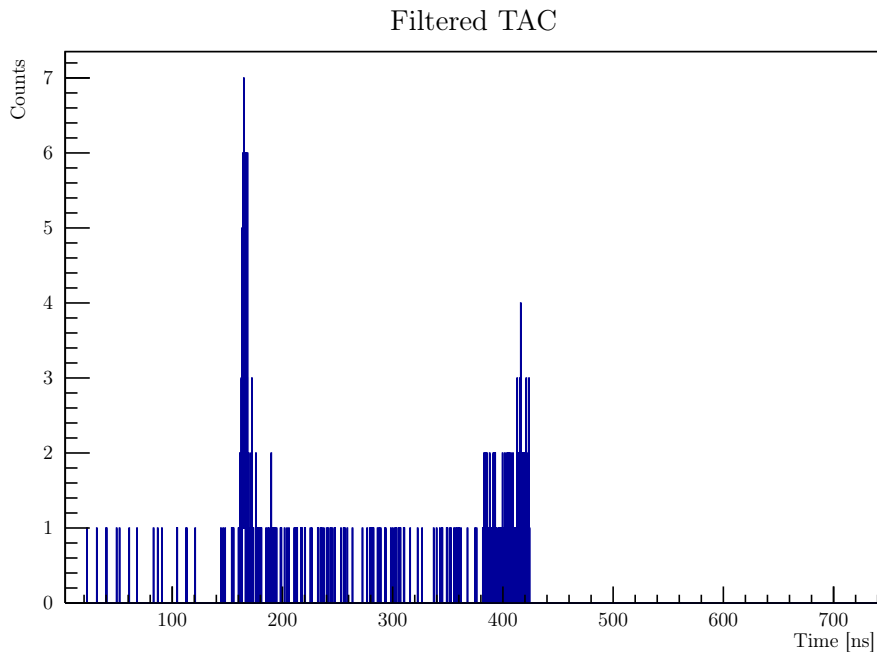


Figure 14: TAC for the three photons decay.

This spectrum has a too low statistic to allow any meaningful analysis. The three-photons decay it's a very rare event and only with a very long acquisition time plus a powerful filter to discard two-photons noise some results can be obtained.

Maybe write explicitly that we didn't obtain useful data although our acquisition was 23 hours long.

## 7 Rate

Applying the filter to the two photons and the three photons spectra (using the spectra recorded without the det. #4 coincidence), the obtained frequency are:

$$f_{2\gamma} = (2709 \pm 1)\text{Hz} \quad f_{3\gamma} = (0.259 \pm 0.002)\text{Hz} \quad (2)$$

where the errors are computed assuming a Poissonian distribution. The two acquisition have, before the filtering, a frequency of respectively  $(3674 \pm 1)\text{Hz}$  and  $(2.325 \pm 0.006)\text{Hz}$ : this means that for both the acquisition the dead time effect on the computed frequencies can be neglected. To estimate the ratio between the two decays, even the geometry of the system must be considered.

A first rough estimation can be done with a simple model: given  $r$  the detector radius ( $r \sim 5\text{cm}$ ) and  $d$  the distance of the detector from the source ( $d \sim 18\text{cm}$ ), we can roughly estimate that:

- For the two photons decay:
  - The first photons is detected only if it enters in one of the two detectors, so with a probability of  $2\pi r^2/4\pi d^2$ ;
  - For momentum conservation law, if the first enters a detector, the second must enter the other one;
- For the three photons decay:
  - As in the two photons case, the first photon is detected with a probability of  $3\pi r^2/4\pi d^2$ ;
  - This time even the second photon is free, so the detection probability is  $2\pi r^2/4\pi d^2$ ;
  - The third photon is constrained in the plane of the detectors (in a section of the plane, but let's consider on average half the plane): its probability it's something like  $2r/2\cdot 2\pi d$ ;

The correction factor is therefore about:

$$c_f \sim \frac{\frac{2\pi r^2}{4\pi d^2}}{\frac{3\pi r^2}{4\pi d^2} \cdot \frac{2\pi r^2}{4\pi d^2} \cdot \frac{2r}{2\cdot 2\pi d}} = \frac{8\pi d^3}{3r^3} \sim 390 \quad (3)$$

which lead to a ratio of about

$$R = \frac{f_{2\gamma}}{f_{3\gamma}} \frac{1}{c_f} \sim 27 \quad (4)$$

### 7.1 Simulations

The correction factor is better estimated through a Montecarlo simulation. If we denote as  $E$  the total energy of the three photons, we randomly divided the segment  $[0, E]$  into three parts  $E_1, E_2, E_3$ .

Discarding triplets that doesn't allow momentum conservation, we obtain a uniform distribution on all the possible energy triplets. Simulating also the three detectors and triggering on the triple coincidences, the ratio of observed events results:

$$c_{3\gamma} := \frac{\text{detected events}}{\text{total events}} \sim 5 \cdot 10^{-4}$$

Should we say that our simulation's results are coherent with published paper?

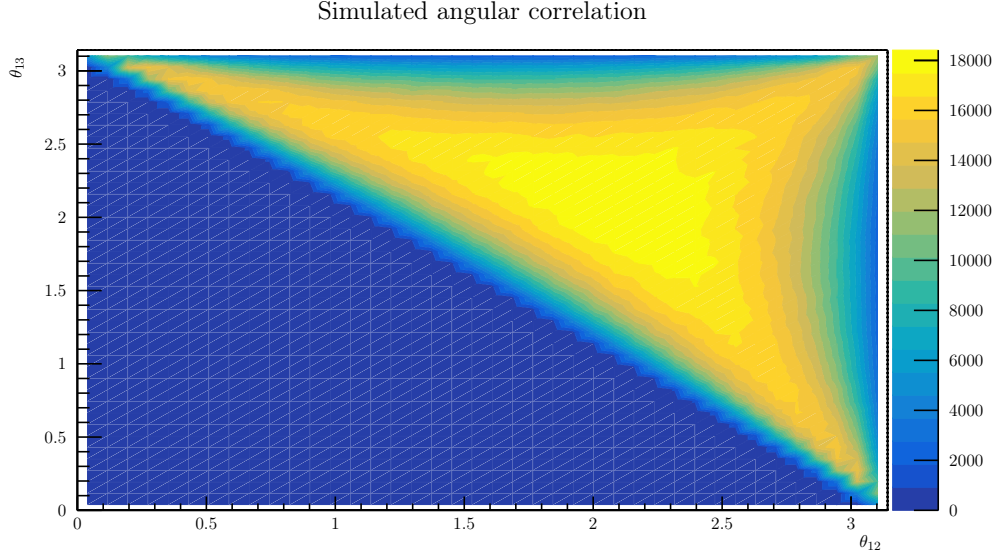


Figure 15: Correlation of the angles between first and second (x axis) and first and third (y axis) simulated photon.

With a similar calculation the ratio of observed events for the two-photons decay can be obtained:

$$c_{2\gamma} \sim 3.7 \cdot 10^{-2}$$

Therefore the correction factor results:

$$c_f = \frac{c_{2\gamma}}{c_{3\gamma}} 71 \quad (5)$$

From the simulation we can also assert that the dependence on  $d$  can be neglected in our rough results:  $c_f$  varies less than 10% for a  $d$  variation of 3%.

This lead to a ratio of about:

$$R = 387 \quad (6)$$

## 8 Conclusions

We succeeded in computing the ratio between the ortho and para positronium obtaining a result that matches what we expected from the theory ( $R_{th} = 373$ ) We instead failed in computing the lifetime of the two possible states of the positronium: for the parapositronium the lifetime was too small to be observed with our detector, and the  $\tau$  we obtained by fitting the right tail of the TAC peak is actually due to the electronics. Instead for the orthopositronium we didn't even had a right tail to fit :(

And we were also pretty unlucky with the HV module

This section  
is not very  
serious