

$$(B^T A^T)_{pq} = (\text{row}_p \text{ of } B^T) \times (\text{column}_q \text{ of } A^T) = (\text{column}_p \text{ of } B) \times (\text{row}_q \text{ of } A)$$