$$if v_0 = \alpha_0 \underline{u} \in S$$