

Summary of course

Main topics

- o Discretization + errors (truncation and round-off, loss of precision)
- o Num. differentiation
- o Linear algebra
 - Solve eq. $A\bar{x} = \bar{b}$ $\left\{ \begin{array}{l} \bullet \text{ Gauss elim} \\ \bullet \text{ LU decomp} \\ \bullet \text{ Iterative} \end{array} \right.$ special focus on tri-diag. matrices
 - Solve eigenval/eigenvect probs: $A\bar{x} = \lambda\bar{x}$
 - Matrix operations (diagonalization, LU decomp, ...)
- o Ordinary differential eqs (ODEs)
 - Boundary value problems $\begin{cases} \rightarrow \text{Solve matrix eqs (Proj 1)} \\ \rightarrow \text{Solve eigenvalue probs (Proj 2)} \end{cases}$
 - Initial value problems $\rightarrow \left\{ \begin{array}{l} \text{Euler's forward method} \\ \text{Euler-Cromer} \\ \text{verlet} \\ \text{Leapfrog} \\ \text{predictor-corrector} \\ \text{RK 4} \rightarrow \text{Proj 3} \end{array} \right.$
- o Probability, random numbers, Monte Carlo methods
 - Meaning
 - pdfs
 - Random numbers
 - Sampling from pdfs \rightarrow Markov Chain \rightarrow Proj. 4 (Ising model)
Monte Carlo
- o Numerical integration
 - Deterministic algos for low dim. problems
 - MC integration for high dim. problems
- o Partial differential eqs (PDEs)
 - Explicit (F.D.)
 - Implicit (B.D. and Crank-Nicolson) \rightarrow Proj 5 (Simulate double-slit)

- Writing proper reports in TeX
- Basic git
- Basic C++
- Parallelization w/ OpenMP

Potentially four
points on your CV!

• C++

- Compilation and linking
- Program structure
- Classes
- Using external libraries (here: Armadillo)

Things I would have liked to cover

- Eigenvalue problems: Householder's method for tridiagonalization, QR algorithm for finding eigenvalues
- C++:
 - Pointers (incl. function pointers!)
 - Dynamic memory allocation
 - Polymorphism / inheritance
 - Parallelization w/ MPI
- More git
- Numerical optimization
- A useful library: The GNU Scientific Library (GSL)