

# CE394M Advanced Analysis in Geotechnical Engineering: FEM

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1 Introduction to the Finite Element Analysis

2 Strong form

# Finite Element Analysis

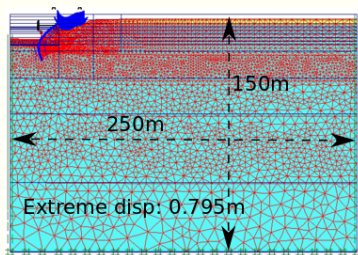


Fig. FE Mesh

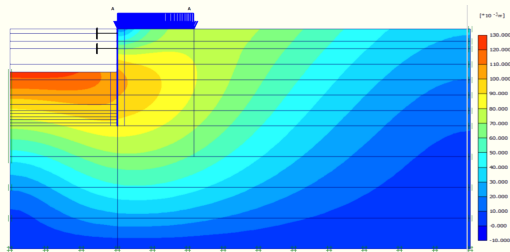


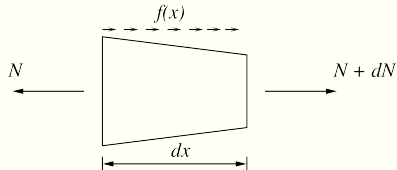
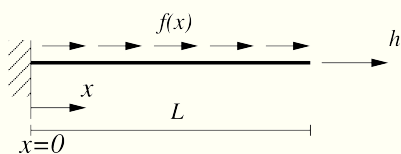
Fig. Displacement profile

Singapore Nicoll highway excavation FE analysis

# Galerkin: Ritz method

# Finite Element Approximations

# Strong form of the equilibrium equation for a 1-D bar



where  $f$  is a distributed force and  $h$  as a force applied at the end of the bar

The equilibrium equation can be derived by considering an infinitesimal bar:

where  $N$  is the normal force in the bar and  $f$  is the distributed force along the bar.

# Boundary value problem of a 1-D bar

For linear elasticity

where  $A(x)$  is the area of the bar,  $E(x)$  is Young's modulus  $u$  is the displacement and  $\varepsilon = du/dx$  is the strain.

which is a second-order differential equation. BCs: