CE394M: Stress-strain-strength relationship of clay

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Overview

1 Stress-strain-strength relationship

Simple shear

L-soil v D-soil

L-soils:

- yield at sub-critical stress ratios
- looser than their critical density at their projected yield stress
- lightly over-consolidated at yield
- contractile when sheared slowly
- "wet" when sheared quickly
- tend to strain-harden to a critical state if sheared beyond yield point

D-soils:

- fail at super-critical stress ratios
- denser than their critical density at their projected yield stress
- heavily over-consolidated at yield
- dilatant when sheared slowly
- "dry" when sheared quickly
- tend to strain-soften to a critical state if sheared beyond yield point

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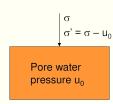
a dilatant when sheared slowly

· "dry" when sheared quickly

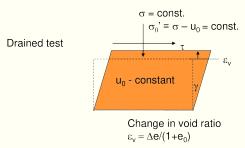
. tend to strain-soften to a critical state if sheared beyond yield point

The terms "wet" and "dry" come from the idea of working a specimen of soil by hand. On the wet side of critical state the soil skeleton is too loosely compacted to support pressure stress—such stress, if applied (such as by squeezing the soil by hand) passes immediately into the pore water and thus causes this water to bleed out of the specimen and wet the hands. The opposite effect occurs when the soil is on the dry side of critical state.

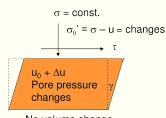
Simple shear



Initial consolidation Void ratio e₀

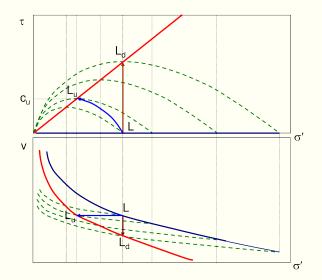


Undrained test



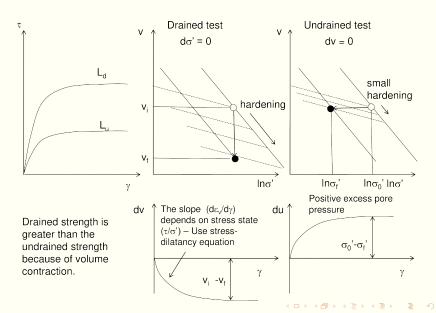
No volume change

Simple shear: Normally Consolidated Clay - L-soil



Drained shear: $L \to L_d$ and $\delta u = 0$. Undrained shear: $L \to L_u$ and $\delta v = 0$.

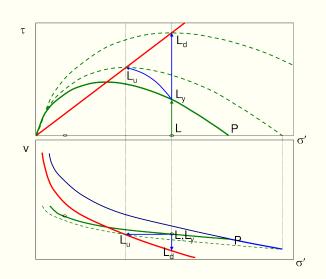
NCL: L-soil (drained v undrained)

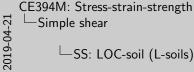


Note that the stack of κ -lines with their associated Cam Clay yield surfaces creates a 3D boundary surface in (τ, σ', v) space. State paths starting inside the boundary surface begin as elastic until they

hit the surface. Then they are forced to follow the boundary surface, obeying whatever test constraint is imposed (undrained v = const, or drained $\sigma' = \text{const}$) until the path reaches the critical state line. Then the soil shears at constant (τ, σ', v) state.

SS: LOC-soil (L-soils)





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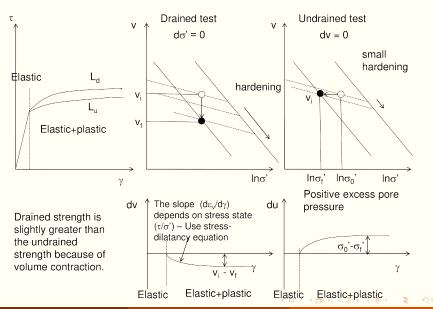
In undrained conditions, the effective stress path will be $d\sigma'=0$ during elastic response.

$$d\sigma' = (vp'/\kappa)d\varepsilon_v.$$

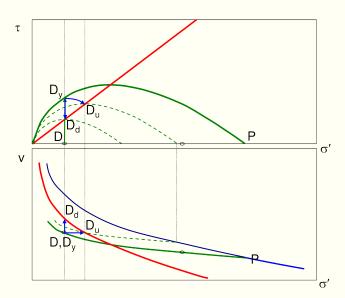
 $d\varepsilon_v = 0$ hence $d\sigma' = 0.$

-Simple shear

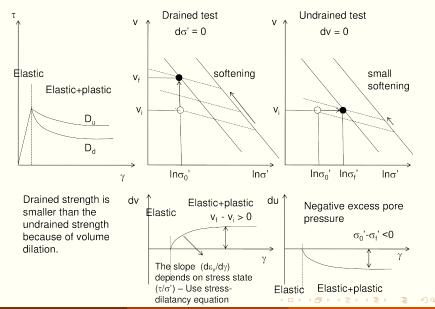
SS: LOC-soil (L-soils) (drained v undrained)



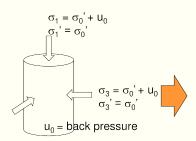
SS: HOC-soil (D-soils)



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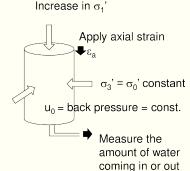


TXC: Drained strength and volume at failure using CS



Initial consolidation condition

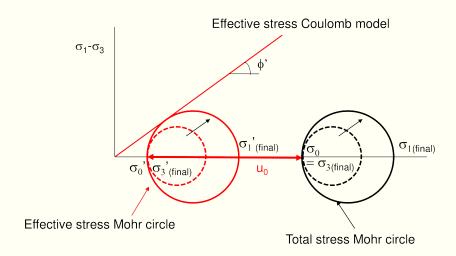
$$e_0 = Gsw_0$$



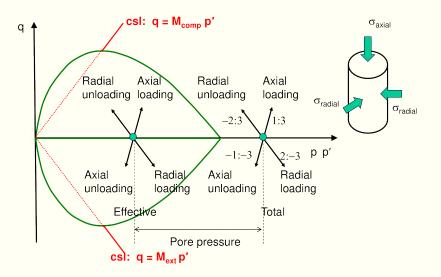
Changes in void ratio $\varepsilon_{\rm v} = {\rm de}/(1 + {\rm e}_0)$

 ε_{v}

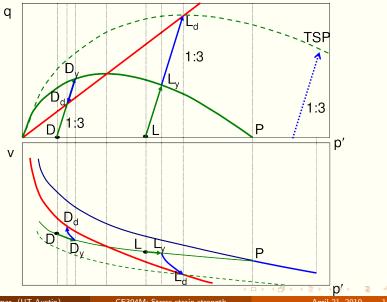
TXC: Drained (Mohr-Coulomb ESA)

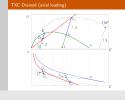


TXC: Drained Cam-Clay yield and failure



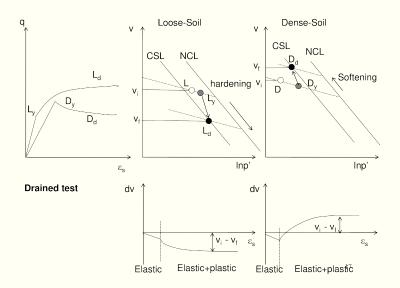
TXC Drained (axial loading)



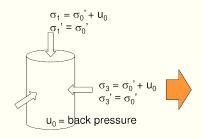


The total stress path of triaxial compression has a slope of 1:3. In drained test, the pore pressure is kept constant. Hence, the effective stress path will have a slope of 1:3.

TXC Drained (axial loading)



TXC: Undrained strength and excess PWP at failure



Increase in σ_1 and σ_1 '= σ_1 -u



Measure pore pressure (u) by a pressure transducer

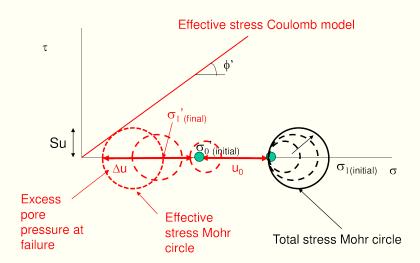
Excess pore pressure $\Delta u = u - u_0$

e₀ or w₀ is kept constant

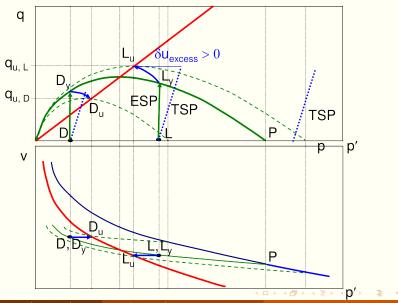
Initial consolidation condition

$$e_0 = Gsw_0$$

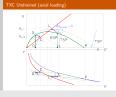
TXC: Undrained (Mohr-Coulomb ESA)



TXC Undrained (axial loading)



☐TXC Undrained (axial loading)



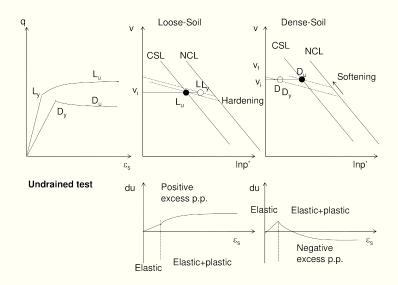
Elastic deformation: $dp' = Kd\varepsilon_v$ and $dq = 3Gd\varepsilon_s$.

$$K = rac{vp'}{\kappa}$$
 $G = rac{3K(1-2
u)}{2(1+
u)}$

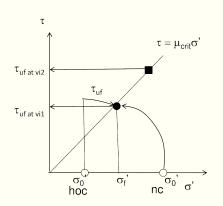
In undrained conditions, the effective stress path will be dp'=0 during elastic response.

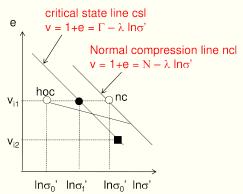
$$d\varepsilon_v = 0$$
 $dp' = 0$

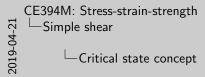
TXC Undrained (axial loading)



Critical state concept









The critical state concept shows that undrained shear strength is purely a function of initial void ratio (or water content).

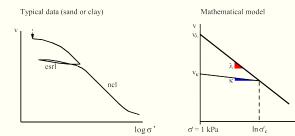
Critical state concept

Interchangeable parameters for stress at yield and $d\varepsilon^p$.

System	Effective normal stress	Plastic normal strain	Effective shear stress	Plastic shear strain	Critical stress ratio	Plastic normal stress	Critical normal stress
General	σ*	ε*	τ*	γ*	μ* _{crit}	σ* _c	σ* _{crit}
SSA	σ΄	3	τ	γ	tan ø _{crit}	σ΄,	σ'_{crit}
BA-PS	s'	$\epsilon_{\rm v}$	t	ϵ_{γ}	sin φ _{crit}	s′ c	s' crit
TA-AS	p'	$\epsilon_{\rm v}$	q	$\epsilon_{\rm s}$	M	p' c	p' _{crit}

Plastic work and dissipation: $\sigma^*\partial \varepsilon^* + \tau^*\partial \gamma^* = \mu^*_{crit}\sigma^*\partial \gamma^*$. General yield surface: $\frac{\tau^*}{\sigma^*} = \mu^* = \mu^*_{crit} \ln \left[\frac{\sigma^*_c}{\sigma}\right]$

Critical state concept: 1D compression



Plastic compression stress σ_c' is taken as the larger of the initial aggregate crushing stress and the historic maximum effective vertical stress. Clay muds are taken to begin with $\sigma_c'=1$ kPa.

Plastic compression (normal compression line): $v = v_l ambda - \lambda \ln \sigma'$ for $\sigma' = \sigma'_c$.

Elastic swelling and recompression line $(\kappa$ -line): $v = v_c + \kappa(\ln \sigma'_c - \ln \sigma'_v)$.

lnσ

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Equivalent parameters for log 10 stress scale:

Terzaghi's compression index: $C_c = \lambda \log e = \lambda \times 2.3026$ Terzaghi's swelling index: $C_s/C_r = \kappa \log e = \kappa \times 2.3026$