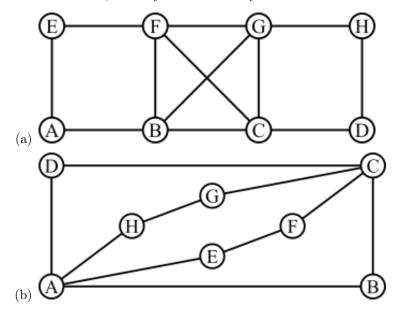
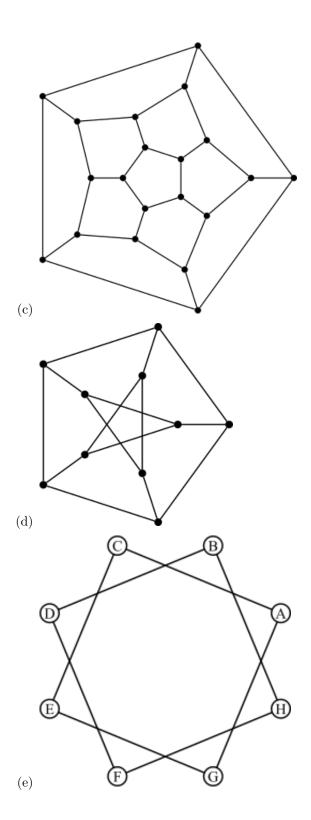
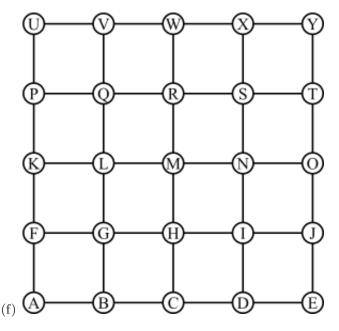
Exercises: Eulerian and Hamiltonian Graphs

Exercises

1. For each of the following graphs, decide if it is (i) Eulerian, semi-Eulerian, or non-Eulerian, and (ii) Hamiltonian, semi-Hamiltonian, or non-Hamiltonian. Find paths or cycles where appropriate to support your answers. If it is not Hamiltonian, then try to describe why this is.







- 2. You are asked to draw nine different graphs. Each must be connected and each must have exactly eight vertices. Use the table below as a guide to draw an appropriate graph according to the labels in the corresponding row and column. Pay attention to the following:
 - In the column labelled **Semi-Hamiltonian**, make sure that none of the graphs are actually **Hamiltonian**.
 - In the row labelled **Semi-Eulerian**, make sure that none of the graphs are actually **Eulerian**.
 - In the column labelled **Neither**, make sure that graphs are not **Hamiltonian** and not **Semi-Hamiltonian**.
 - In the row labelled **Neither**, make sure that graphs are not **Eulerian** and not **Semi-Eulerian**.
- 3. Find how many different trees there are with each of 1, 2, 3, 4, 5, and 6 vertices, and draw them. (Hint: There are 8 with 5 vertices or fewer.)

Solutions

- 1. (a) Eulerian and Hamiltonian
 - (b) Eulerian but not Hamiltonian nor semi-Hamiltonian
 - (c) Not Eulerian nor semi-Eulerian but it is Hamiltonian
 - (d) Not Eulerian nor semi-Eulerian but it is semi-Hamiltonian
 - (e) Not connected, so can't be either
 - (f) Not Eulerian nor semi-Eulerian but it is semi-Hamiltonian

	Hamiltonian	Semi-Hamiltonian	Neither
Eulerian			
Semi-Eulerian			
Neither			

- 2. You should be able to check your answers for this. Use the theorems to check whether the graph is Eulirian or semi-Eulerian. For those that are Hamiltonian or semi-Hamiltonian, provide an example cycle or path. For those which are not Hamiltonian or semi-Hamiltonian, try to provide an argument as to why.
- 3. There are 1, 1, 1, 2, 3, and 6 for trees with 1, 2, 3, 4, 5, and 6 nodes, respectively. See this sequence of numbers. This exercise is not quite the same, but is related to, the problem in Good Will Hunting. **Video** Visit

the URL below to view a video: https://www.youtube.com/embed/iW_LkYiuTKE