

Exercises: Vigenère Cipher and Kasiski Attacks

Spreadsheet Exercise: Vigenère

To begin with, download the Excel spreadsheet: `02a-vigenere_kasiski.xlsx`. We will use some functions from last week to create an encryption tool for the Vigenère cipher and later use a premade tool to aid Kasiski attacks on encrypted text.

1. Make sure you are in the worksheet named 'Vigenere Cipher'.
2. In Cell B1, enter a plaintext string in **lower case** and **without spaces** or leave the text in that is already there.
3. In Cell B2 there is a passage of plaintext. Leave this for now.
4. In Row 4 we will use the MID function as before to split the plaintext characters out one by one. Enter `'=MID(B1,B3,1)'` into Cell B4 to retrieve the first letter. Then copy or drag this formula across to the end of the row. (Remember that copying the formula and then holding **Ctrl-Shift-Right Arrow** will highlight the rest of the row before pasting.)
5. (Optional) Row 5 was already prefilled. Can you see what the formula from Cell C5 onwards is doing?
6. In Row 6 use the MID function again to split out the characters of the key using the positions in Row 5 above it. Remember to copy this to the end of the row so that it repeats the key word enough times.
7. We will use the CODE function to turn the letters in Row 4 and 6 into numbers. Since `=CODE("a")=97` we will need to adjust things a bit here. Enter `'=CODE(B4)-97'` into Cell B7 and copy this across the row. Do the same for the key letters in Cell B8 and copy this across too.
8. In the 'Shifted' row, Row 9, we will use modular arithmetic to shift the plaintext letters by each key letter value. In Cell B9 enter `'=MOD(B7+B8,26)+97'`, remembering that we need the +97 to shift the value back into the right range.

9. We'll now turn our numbers back into ciphertext letters using the UPPER and CHAR functions. Enter `'=IFERROR(UPPER(CHAR(B9)), "")'` in Cell B10. The UPPER function forces our ciphertext to be upper case.
10. Use the CONCAT function to stick the ciphertext letters together in Cell B11.
11. Check that your spreadsheet works by seeing if the plaintext message 'introductionto cybersecurity mathematics and cryptography' with key 'shannon' encrypts to 'AUTEB RHUAI BAHBU FBREG RUBRV GMZSA HRZOG AJSNA RPJFP GBUES WHL' (without spaces).
12. (Optional) What would happen if somebody entered the plaintext or the keyword with upper case letters? Can you use the LOWER function to account for this?

Exercises

1. Within the spreadsheet linked above there is a second worksheet called 'Kasiski Analysis'.
2. You do not need to create anything in this spreadsheet and can just use it as a tool.
3. There is an encrypted message in Cell B1, the full ciphertext is copied below. Inspect the rest of the spreadsheet to try and get an idea of what it will do.

FUIKBYMACFPJSLGSTGBUEKHRFPGUIHKCBVRGAUHCJTJEWKFKTVIDGHZEMIEIW
FYGLCQKARGMVOPWRCFKGFXIPIJJWFGVHVHWJSVATVHZAVIKQUUTRVFHMGTY
CHAHCDSGHLETSKQDASVAIVSVURAEFTDUPGKJSTQKZPHGTJEWKFWPNATGHZEX
OCWAWSVRLEYLHGBRTFWDIRRVSSNFFVNZGPGNFPHZEJERTHZIPTYGRTARGLZIVL
IHIYCRFOVCRWUZTCGCKAHSGOWVWOREEKBYWQRUUWFTJEJGQGNFATVWKHQUCF
BWVGRYCJWFKNZUVWDKTSWHSSKSKQCHEFTFRWUKKTLRAQAEJDSUAOEIKJWTGD
KQHZEQPVPDSSGAEFKATJATMGFVEITCJOTPTVTVSPUIKYOKOHJFAGGPQIXPOFT
VHRVWVUHFVTSVIPMGFGQNGRMGWKNCTTJSVTJEKJWFGQUKQTLHGCFZKAPDTTS
HTUHRMWFGVODAPWDTOFKZETEZTSSDKTRPRJETERFWLAPDNGDLAPDCCYHGD
PRLRGMSNSVWKTYCVGRTOIYVACJAKVWEEUJUOALUMVASLTJIKGLHGTYKBYTJ
AKVFGUDLVUAWFQRZEOFNQWQFYEVCRITQGSWYGFBNATMGLATSYCBIPTYGVW
AXEEUKZETEKJSKHCDFYGGFOEEUHZOWGYVGDEPGKJSFIPTYGOXTGREQCFWJEEV
VWTYIEUIFSUIEMWFTQTYGZSKGOWJODICNUOMEIPDNKZDBGAIHCJEXEIVVWMGM
FTMGFVHVRDLKDDCGCIRRRAUGDYICNQMRUEKJSORKTVTOKTJENTWLETHRUQMR
UEUVVWWQRCFKATJTYKGTECUKKTMLUTLRSFDQUJEFWAVIFPHWRTISNSANKTJUW
EPNITKHQITRVUWKTBCGWFIVSKTILHCWFTZVWJITJBGWVRVOPDEUBVHCJEVHV
MWFKNPZDOYWYGBLHGFIBUHIOMGFFMGNKUSAZGDKJSLRCNJNOLEFCFRWWSY
HZEZAFJLUHSRTIMGRANRAIKGDOPDFPCXCQUIUSTEEADGSSGGRKQFWAFIKKHA
SYECNYFOYNYQKLHGBFQYKPTERFZAKGAEBXEETZQIKDKSVCGWFTODEWLYVOTK
HQFTODECFTKNVPHLOEOEVWFEPSTCFJEFOLVVWRGCFPTASEAKGRLHGRVFSFOWN
TGRTYRRVUGSNFPLNDATEEEUIJEFEMGBTYVHVOCKTCDMCBUEFOWNWLETAIAOFA
TCYKGLSPOUGTANKTVRFANEIGNSKHCDSGSFVKOCCHWDKNKJCKEYITMSVPCGVUB
GDQCKTWFERRFIDGCTVFBGCQNMKQLIQNJQILRCGVFWLCQUCFBGTDEAWRYEFBP
CBQKPONPGLAPDRTRQEVACVVGUIHZVKSSCCBPCOLGDXGRLHCTKJSKURRVOSFOV

EFHOJTJAUDSWNUTIWQCIPTYGYANIEASDLQWRNZXENTKJOLHWMRPBSTWRVECM
 LFNFPVWATTYGLRCIEPCJTRZXSGNYOIFGANYHZEVLHGEJUSFCGOWRIJEUTGQ
 WKOPLLTYWDVHVXSJYDAECZATAAEFWFNQCV PQWOHTYGTARUTREHGNNYRNZGWGD
 KJSTLQWKQTSLNAWVSJWCRUYWLHOOIGOOFWLVHTWCV

- When you have had a look around the sheet, use the following table to start implementing a Kasiski attack on the ciphertext.

sequence	interval	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
TJEW	126	X	X			X	X		X					X			
KZET	168	X	X	X		X	X	X				X		X			
IPTY	434		X				X										
QMRU	28	X		X			X							X			
EWKF	126	X	X			X	X		X					X			
WFGV	406	X					X							X			

- First guess what the most probable key length is from studying the table (it is no bigger than 10). Enter your guess in Cell C2. You should find that the spreadsheet splits the ciphertext out into as many groups as your key length guess.
- Starting in Cell A18, the frequency of the letters in each group are counted and compared with the standard frequencies. This first group of letters is shifted by a Caesar cipher. When you think you have guessed how far the group is shifted, enter this guess in Cell AC22. For the first two groups there are bar charts to help you spot the patterns, and also a chart for the standard frequencies. Remember that if you think that shifts are one out from what you expect, so if C is the most common letter in this group, then the shift is 2, not 3. There is a reference for the shift values in Row 17.
- Continue to do this for each of the groups. As you enter guesses for how each group is shifted, the spreadsheet will update below Row 88. Keep an eye on this to see if your guesses start to reveal anything sensible.
- Repeat the task for the ciphertext below, using the table to help start building a Kasiski attack. Downloading this as a text file makes this easier as it gives you the text without any spaces. (This turns out to be much harder if you copy the text below with spaces in it, as it throws off the frequencies of each letter.)

ZRPSLTZRNAZHYMTVKHCINFPASMYSZTZRQSIIOAROB EYHJSRVJSISIQRLROHYL
 MAHRROGHFZSFWICCYXIBTWSCKBHKIYPBFVASMYSZRZHQ SURPEEZPRLTCWEKDY
 QVRWRCGVVVPGNAVEEECDZRREFCWZQRCEIRIAHCCCECDZRRVNDGMYKNHDCNLN
 ASICHCIXTWFCDIGMFWKSCMZIKXPVRRKEATVBXEEQLQYEXFRFUSZVBBCCELVG
 RRORBHYMYKZCIILLQWJXTRPHCCTVRAVQMI EWKALWVBKLPFYSROOIPSDFPVNB
 ILGUGVTLVNVHJMAUVQMIEKISFKUHZXDKUCJXFTBBKLPJYCFVPETSI PJMJWJL
 PHGVVQZVECNZLMAZPMSEQGFYRLGHFFZVECNJCSZAPFZSXGJYCGROJIZJFCIVZ
 AFCIVZASCIYSIYCJXWIACIIQSEHYICEESRROVNRZEYXZOHPRJVFQELROEKPP
 FBRQPPRBFVPRNAVPPWFVVPJBFVZPVZCII LRQHYIDMYVRDEQIEGPVGZRCYF
 HCMYKBTVENLCIITWIP IIXLMAHYVTPYSUQPJVZC IOQRKZXSJNBKEDXVQKICVBF

JRPZRFWIWXOSWSCIFCKLLXACNXZWGWCPELRPVEEMAUFJXCUSRVEMFHFISOVRDV
EEMAUKMDWBAVZTWVHFVPRGFVEEMAUVREVNBTILXZMTLLQOSIHZSEGFQPPNHVZ
TWVHFVPRGFVEEMAUVREVNBTILXZMTLLQOSIHZSEHYMDMGWJEYHACKLRTAFVP
TESJIYXYMDCDSHZXVPAFHISYKRFYIDMGOKMYKGVVRYSYCEKPVFWIWLQMWFVXE
QODXCYYMPSFVSCIKTZRBVWDMVAGPZVRPLXELRTRGEMFWNEDRNDGMYKNBUWZKR
BKPJCBITEXIEOGTTRTOEHDSOZREPLMFYNEZSKEATVBXXLTCWEKLXZMTLLQOS
IHZSEHYEEMFQRVNIJOJWFVRWYILVQMFYSIESZSAIASUATHRHYIOSBFUECOASJ
WELRFVEYHACKLRTAFVPHRSGMYXBHYEEHNFBRPWFVDVICMAUCSYKVGKSZHGUVV
PABBUICMAUWILVVBXHZYOHZRRHESRQTRTRIILQFBFQZVGOCIGIERRVPHGCUVP
EZPVJZVRPLXELRGZPPRPSNEDYAPISVIAOEHRELKGMWPASJWREISESESXSEEYH
GVVSYPLKFVOXUSIIDTBYVRHEFHYYIHLVGGICIQKFVOPRBFVPXUWJMHVLGGICIQ
OEHLRRQYSXYEALVPHOOTELRKFOVRBFVPQRFVPJXUWJEYHACKLRTAFVFPNQ
BMYXBHYINLNASICXHFEMYKNZCQJWBICATXUWEQPFHFEMYKCFRLKNWEMSINFU
EEEDZRRWBABASEGZFYOIEHYEYFRTFVPWHFVPJWNWUMDYESCCELNHZWSZSKL
TRTOKQJAVBUSHPNHKMNIYSKQPWRSKLPRJVRXELRFVEEMFOEHELVGDCDXRFP
TYCIIWIGAPLPEEHSIDVZCEXSZSEXLRQHMYMDQLGKICRCLGPZVRHZWELRKZROE
ARESELVBXQZVRGCIYLRVFMQPHBXSIFVLXEIEKYIYAVHYQLRLOWPTVGOEHQPH
HKICMAHYICIFHVTAIQOJXLXRZPVLZRBFLJELRGRMYXYMUEJWBTPSCIACKXSIYS
RWESOSZWLRSDEOIUSESEEZWEYEIFHFTAIQCIWEELSULPFHHNMELZWVRZJYCI
HZVYOUCAIEQYIOEOMIXCPVRQMIERFSCTRTFTLPHHDFRLFHGKSQTNZCEDNHGKE
MSISDCNLNASICHBCITPVPVHLRQGRXLRQBFXSMAUDSCIGVVRELGVFZRLPZVO
FRULMWMAUDCDEQTRRNCVBKSDQVZZRRFLHYIRVNJVEYHFHVYHRQFVFBTKLPG
BIEXPRNBTITXJCIIELBIXLELLQIIDXOSJLZVAOEHDNLJRELBIZWLMQOIXDYE
SESNVNJVRRLNGKPJKEWDEYHNBMTMPRGFRZPRJOEHPVVBXJCSZHYIYMTVKPJWUC
IIIEIYZDIHLNHLJPBFUPJRNAVMDSAHYIYMTVKWAPHHFRTEAGYSCIDIFXSXUSI
EGIAVZPVZCIIIXYPVZQLVISCPHGVZWFRTOZRWCSNPESUSRVOMFQFYCWRGFT
WEVBCCELBIXLTXFOEWHIEZZXEPRAVEYMAUCMEXYSIIWIIOEGJFBFVJZVJSTEY
RBHYIWTNUIIPMAUKLLXACCMGMAUYXEAAPVMYKRJVJVGKRWMPRGJIOAVHYWPI
VBXFTVQOSSGIUWJGSEZPVVOSBFSMCHBFSILWIGISYXUSJGFPCHLVPHOIJXLFB
JVLTPVVRQMIERFSCAVHYWFGUBRQPEFBVZPVZCIIMYGHYICEISEWTXGWEKWSAS
CCZRGVVWTWEPWUFFWGGGSVIBBCCELNHFRPABFUEDMSVZWSHZZRELNHFRPABFU
LPHVRFYETBIIRZXUWEKQEEHYICXUSELPYGHVVPHACKEQINHYICXUSELPJYIKX
PVRKMWVPVGTCEGRZPQZVRHYEYQHKKICIQCKLPVSFZFYHFRZPJYCNRMISCIIZ
RGVQZVECNLPAVZCPPEISDILWZMYSAIFVRZPJYCNRMISCIIELRBKLPVFVUWLM
QBVPVZVZCIIIXNFKPPHNLKLPWGWCPYIFGSVZORBSCCICZPWZECHCCDTBYVROSH
PKPPWFGRMOMJVRXTXHHKICWVGZXSAPWESPYPYRROWGCIINEHUYXQVBAJSXIH
YEATLARWEIEKYSXYAAVNMMSICTWNGKICJBZCSHIQTRWEEARWSWPBKVHQEFHV
VEMYZYMDWBBXWZRRPLVOIAPFVPXVZCXSIQWIKPWBTYMDLBDVXSEGAUPLRPVFP
JFHFUIYFBFVSQRRJVYIIISIQZVRPLXELRFRZPRFHZPWFRULMWMAURPWQLTRN
CVBKSQVZRRWGFRMRLGWNLPISUENYFVZSYIQGVEEMATISYXBTSMCHNBUFFW
GOEHOSBFLPRHDFRELJVPGIGGZRVMAUZFPXBCBQJWRZWXZPVBBMYKSOEGJYA
HFJLRPMKLTRXWEKHLNHLTWBAZRYFPZVOSSMFVPAUOKXSMFUIMXYAURMYPLU
YEDXYMXEFRGOEHZQVBFYDFVFUSQCBFVQPEAHZRNVBOMYKASMICQBFVXSFWJ
EEIAURKPHVBXYPWFWEKMYGBFWJPYOSPPKDIIDWVBXXZXUSWSHPJVFVPJVSIC
PCRGESHFHFEIOMAHFQJFBGFQDGBFVXSMFOEHXSESZWLXQWMMYMAUNMELZMYIL
HNHVEDIESTPTRVBXSXYUSTYDLVCEWGIYJVXWMAWEKELNHLPPNAGPTKUHPXZE
GSUSPVOIKASSFSMIWZRHMMZPRHCMYMAUNMELGVVPLQCZZKSXTZFEEMAUFICWU
SJLLPYDIIDWNVEIGIEAFVPXUSEQPXUCLKSXGVVETVTFVAQIAGVVAIETLQPHSF
FQLRHBVIPRPSEWPVFKLRRFLGVVLTUWDASSFSWSXSOCPDVBBPBBKLPXHTK
IOJYCFVHVRHTLTGEWVHELLUFHSEGVCIIYXGVVIMCGVVWPEAUVPLRVRXSWRBKX

SIRFVWAMGSIIDTVHVEYHASGIYXUSWVZQGVPQPQBFZIDSSZVRZVRELEQJBVHYL
JSHYMDOVBURPTRBKLPEARWSCKRHKLWYCJXWIACTIBYBHYXSIEOMIYRRJVVS
ESGVZTUSKWLmqwklTRTCWIGMYDISALRHJXTPYWFTVQCIHPZVZNLXPUSIXPQC
HVVDIAHFVHLRHYICXRAGIDXGCJWPHGVVISIESRWSSUESUIDSYOKIJIGOCFPRQO
LREIQCEXSMFRVWPVGZRROIAQYEXRRFRELVGYSXIOMYSCVBFYEFRGSUXPPYAV
XCYYMZMXTYCIITWGVVPMFHYICIOOCQTRTWCILHGSCPXIGSCPXIVWDTWSESHY
ZXUHYICEISERPZRFDSCICFFTSIGGRMOMGVZRRSSMMWTECGLPXFHZPVMSPZVO
SERVZTPOMKLLXUSRZPRGVRXMIARJEMSISLWMCGRXRSQKVZFZXUOUSCIGSCPEL
VGJSFPJWKLDSEFFAWEQSEMqAVHYMYXUSUMDXNBKETHRBEMEUOCNPNGGEDEV
BKIOQNWUIYAUCDXSINBXIWWAODIWIACIINPNGGECEESRROVNRZEYXZOZHPRJV
FQELROEKPPFBRQPPRBFVPUHCKLELRFRZPRASMICQBFVFPXUOKAZVQCLVDMTBF
JAEHZZRRFVFUSCJVSEHTWUFZIVIQIGWEEHZZRRKRHKLPIDOTOTRGCKLPXRAGI
DXNBUXSIAWXLWCZLXZRVOEWSSCILZRBFFWEPYGPFRQOJEESXSESXUOKPT
IGVPWZYYVRXSWCCBIYPROMIXCYCEIWMASJWFROFFOPRDIZXELRPLWEEOCMIXC
QCFVEEXSKLJFROBJCSZCLXXCUSRVEEARKEVIGVPJZVZTISXSSTDCOSBFHYZXU
HYICEISERPZRFDSCINBUXSIEOMIYRRJVVPVHKMYKFHWPWMFGZXEMAUXJTPYW
JWTXGWEKZRGVVTLPYWUFFWGCWTLPYOJNFWGOSSGIZMTLLQOSIHZSEOEHSMFSP
IDLNJVEWPGVWPJZWEKZJNRVQZRFHYEEMFRIILQVBXEYHGVVPLQCZZKSXBSIL
TQFHIILQVBXXSVBKJLTWVVRHZABBKLPJYCFVLRQAPWZYYTISXSHHKLXVVRHZ
AGVRXWMRGWPZEGWEKZRGVVJWSBFJLLPYPVPTJGSURPZRFDSCI

sequence	interval	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
ASMY	72	X	X	X		X		X	X			X					
ECDZ	24																
ZVEC	24																
FCIV	6																
VEEM	24																
EEMA	48																