qpp

0.1

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## **Contents**

1	Nam	nespace	Index							1
	1.1	Names	space List		 	 	 	 	 	1
2	Hier	archica	Index							3
	2.1	Class I	Hierarchy		 	 	 	 	 	3
3	Clas	ss Index								5
	3.1	Class I	List		 	 	 	 	 	5
4	File	Index								7
	4.1	File Lis	st		 	 	 	 	 	7
5	Nam	nespace	Documer	tion						9
	5.1	qpp Na	amespace	eference	 	 	 	 	 	9
		5.1.1	Function	ocumentation .	 	 	 	 	 	14
			5.1.1.1	bsm	 	 	 	 	 	14
			5.1.1.2	djoint	 	 	 	 	 	15
			5.1.1.3	nticomm	 	 	 	 	 	15
			5.1.1.4	hannel	 	 	 	 	 	16
			5.1.1.5	hannel	 	 	 	 	 	17
			5.1.1.6	hoi	 	 	 	 	 	17
			5.1.1.7	hoi2kraus	 	 	 	 	 	18
			5.1.1.8	omm	 	 	 	 	 	18
			5.1.1.9	ompperm	 	 	 	 	 	19
			5.1.1.10	onjugate	 	 	 	 	 	20
			5.1.1.11	osm	 	 	 	 	 	20
			5.1.1.12	wise	 	 	 	 	 	21
			5.1.1.13	et	 	 	 	 	 	21
			5.1.1.14	isp	 	 	 	 	 	22
			5.1.1.15	isp	 	 	 	 	 	22
			5.1.1.16	isp	 	 	 	 	 	22
			5.1.1.17	isp	 	 	 	 	 	22
			5 1 1 18	ienIn						23

iv CONTENTS

5.1.1.19	displn	23
5.1.1.20	displn	23
5.1.1.21	displn	24
5.1.1.22	entanglement	24
5.1.1.23	evals	24
5.1.1.24	evects	25
5.1.1.25	expandout	25
5.1.1.26	expm	26
5.1.1.27	funm	27
5.1.1.28	gconcurrence	28
5.1.1.29	grams	28
5.1.1.30	grams	28
5.1.1.31	grams	29
5.1.1.32	hevals	29
5.1.1.33	hevects	30
5.1.1.34	inverse	30
5.1.1.35	invperm	31
5.1.1.36	kron	31
5.1.1.37	kron	32
5.1.1.38	kron	32
5.1.1.39	kron	33
5.1.1.40	kronpow	33
5.1.1.41	load	34
5.1.1.42	loadMATLABmatrix	34
5.1.1.43	loadMATLABmatrix	34
5.1.1.44	loadMATLABmatrix	34
5.1.1.45	logdet	34
5.1.1.46	logm	35
5.1.1.47	mket	35
5.1.1.48	mket	36
5.1.1.49	mket	36
5.1.1.50	multiidx2n	37
5.1.1.51	n2multiidx	37
5.1.1.52	norm	38
5.1.1.53	operator""""_i	38
5.1.1.54	operator""""_i	38
5.1.1.55	powm	38
5.1.1.56	prj	39
5.1.1.57	ptrace	40
5.1.1.58	ptrace1	40

CONTENTS

5.1.1.59	ptrace2	41
5.1.1.60	ptranspose	42
5.1.1.61	qmutualinfo	44
5.1.1.62	rand	44
5.1.1.63	rand	44
5.1.1.64	rand	45
5.1.1.65	rand	45
5.1.1.66	randH	45
5.1.1.67	randint	45
5.1.1.68	randket	46
5.1.1.69	randkraus	46
5.1.1.70	randn	46
5.1.1.71	randn	46
5.1.1.72	randn	47
5.1.1.73	randn	47
5.1.1.74	randperm	47
5.1.1.75	randrho	48
5.1.1.76	randU	48
5.1.1.77	randV	48
5.1.1.78	renyi	48
5.1.1.79	renyi_inf	49
5.1.1.80	reshape	49
5.1.1.81	save	49
5.1.1.82	saveMATLABmatrix	49
5.1.1.83	saveMATLABmatrix	50
5.1.1.84	saveMATLABmatrix	50
5.1.1.85	schmidtcoeff	50
5.1.1.86	schmidtprob	51
5.1.1.87	schmidtU	51
5.1.1.88	schmidtV	52
5.1.1.89	shannon	52
5.1.1.90	sinm	52
5.1.1.91	spectralpowm	53
5.1.1.92	sqrtm	54
5.1.1.93	sum	55
5.1.1.94	super	56
5.1.1.95	syspermute	56
5.1.1.96	trace	57
5.1.1.97	transpose	58
5.1.1.98	tsallis	59

vi CONTENTS

	5.1.2	Variable	Documentation	59
		5.1.2.1	gt	59
		5.1.2.2	rdevs	59
		5.1.2.3	st	59
5.2	qpp::ct	Namespa	ce Reference	59
	5.2.1	Function	Documentation	59
		5.2.1.1	omega	59
	5.2.2	Variable	Documentation	59
		5.2.2.1	chop	59
		5.2.2.2	ee	59
		5.2.2.3	eps	59
		5.2.2.4	maxn	60
		5.2.2.5	pi	60
5.3	qpp::in	ternal Nan	nespace Reference	60
	5.3.1	Function	Documentation	60
		5.3.1.1	_check_col_vector	60
		5.3.1.2	_check_dims	60
		5.3.1.3	_check_dims_match_cvect	60
		5.3.1.4	_check_dims_match_mat	60
		5.3.1.5	_check_dims_match_rvect	61
		5.3.1.6	_check_eq_dims	61
		5.3.1.7	_check_nonzero_size	61
		5.3.1.8	_check_perm	61
		5.3.1.9	_check_row_vector	61
		5.3.1.10	_check_square_mat	61
		5.3.1.11	_check_subsys_match_dims	61
		5.3.1.12	_check_vector	61
		5.3.1.13	_kron2	61
		5.3.1.14	_multiidx2n	61
		5.3.1.15	_n2multiidx	61
		5.3.1.16	variadic_vector_emplace	61
		5.3.1.17	variadic_vector_emplace	61
5.4	qpp::ty	pes Name	space Reference	62
	5.4.1	Typedef I	Documentation	62
		5.4.1.1	bra	62
		5.4.1.2	cmat	62
		5.4.1.3	cplx	62
		5.4.1.4	dmat	62
		5.4.1.5	DynMat	62
		5.4.1.6	ket	62

CONTENTS vii

6	Clas	s Docu	mentation 6	3
	6.1	qpp::D	iscreteDistribution Class Reference	3
		6.1.1	Constructor & Destructor Documentation	3
			6.1.1.1 Discrete Distribution	3
			6.1.1.2 Discrete Distribution	3
			6.1.1.3 Discrete Distribution	3
		6.1.2	Member Function Documentation	3
			6.1.2.1 probabilities	3
			6.1.2.2 sample	4
		6.1.3	Member Data Documentation	4
			6.1.3.1 _d	4
	6.2	qpp::D	iscreteDistributionAbsSquare Class Reference	4
		6.2.1	Constructor & Destructor Documentation	5
			6.2.1.1 DiscreteDistributionAbsSquare	5
			6.2.1.2 DiscreteDistributionAbsSquare	5
			6.2.1.3 DiscreteDistributionAbsSquare	5
			6.2.1.4 DiscreteDistributionAbsSquare	5
		6.2.2	Member Function Documentation	5
			6.2.2.1 cplx2weights	5
			6.2.2.2 probabilities	5
			6.2.2.3 sample	5
		6.2.3	Member Data Documentation	5
			6.2.3.1 _d	5
	6.3	qpp::E	xception Class Reference	5
		6.3.1	Member Enumeration Documentation	7
			6.3.1.1 Type	7
		6.3.2	Constructor & Destructor Documentation	8
			6.3.2.1 Exception	8
			6.3.2.2 Exception	8
		6.3.3	Member Function Documentation	8
			6.3.3.1 _construct_exception_msg	8
			6.3.3.2 what	8
		6.3.4	Member Data Documentation	8
			6.3.4.1 _custom	8
			6.3.4.2 _msg	
			6.3.4.3 _type	
			6.3.4.4 _where	
	6.4		ates Class Reference	
		6.4.1	Constructor & Destructor Documentation	
			6.4.1.1 Gates	0

viii CONTENTS

	6.4.2	Member Function Documentation	70
		6.4.2.1 apply	71
		6.4.2.2 applyCTRL	71
		6.4.2.3 CTRL	72
		6.4.2.4 Fd	72
		6.4.2.5 ld	72
		6.4.2.6 Rn	72
		6.4.2.7 Xd	73
		6.4.2.8 Zd	73
	6.4.3	Friends And Related Function Documentation	73
		6.4.3.1 Singleton < const Gates >	73
	6.4.4	Member Data Documentation	73
		6.4.4.1 CNOTab	73
		6.4.4.2 CNOTba	73
		6.4.4.3 CZ	73
		6.4.4.4 FRED	73
		6.4.4.5 H	73
		6.4.4.6 ld2	73
		6.4.4.7 S	73
		6.4.4.8 SWAP	73
		6.4.4.9 T	73
		6.4.4.10 TOF	74
		6.4.4.11 X	74
		6.4.4.12 Y	74
		6.4.4.13 Z	74
6.5	qpp::No	rmalDistribution Class Reference	74
	6.5.1	Constructor & Destructor Documentation	74
		6.5.1.1 NormalDistribution	74
	6.5.2	Member Function Documentation	74
		6.5.2.1 sample	74
	6.5.3	Member Data Documentation	74
		6.5.3.1 _d	74
6.6	qpp::Qı	dit Class Reference	75
	6.6.1	Constructor & Destructor Documentation	75
		6.6.1.1 Qudit	75
	6.6.2	Member Function Documentation	75
		6.6.2.1 getD	75
		6.6.2.2 getRho	75
		6.6.2.3 measure	76
		6.6.2.4 measure	76

CONTENTS

	6.6.3	Member Data Documentation
		6.6.3.1 _D
		6.6.3.2 _rho
6.7	qpp::R	andomDevices Class Reference
	6.7.1	Constructor & Destructor Documentation
		6.7.1.1 RandomDevices
	6.7.2	Friends And Related Function Documentation
		6.7.2.1 Singleton < const RandomDevices >
	6.7.3	Member Data Documentation
		6.7.3.1 _rd
		6.7.3.2 _rng
6.8	qpp::Si	ingleton < T > Class Template Reference
	6.8.1	Constructor & Destructor Documentation
		6.8.1.1 Singleton
		6.8.1.2 ~Singleton
		6.8.1.3 Singleton
	6.8.2	Member Function Documentation
		6.8.2.1 get_instance
		6.8.2.2 operator=
6.9	qpp::St	tates Class Reference
	6.9.1	Constructor & Destructor Documentation
		6.9.1.1 States
	6.9.2	Friends And Related Function Documentation
		6.9.2.1 Singleton < const States >
	6.9.3	Member Data Documentation
		6.9.3.1 b00
		6.9.3.2 b01
		6.9.3.3 b10
		6.9.3.4 b11
		6.9.3.5 GHZ
		6.9.3.6 pb00
		6.9.3.7 pb01
		6.9.3.8 pb10
		6.9.3.9 pb11
		6.9.3.10 pGHZ
		6.9.3.11 pW
		6.9.3.12 px0
		6.9.3.13 px1
		6.9.3.14 py0
		6.9.3.15 py1

CONTENTS

		6.9.3.16 pz0	81
		6.9.3.17 pz1	81
		6.9.3.18 W	81
		6.9.3.19 x0	81
		6.9.3.20 x1	81
		6.9.3.21 y0	81
		6.9.3.22 y1	81
		6.9.3.23 z0	81
		6.9.3.24 z1	81
6.10	qpp::Ti	mer Class Reference	81
	6.10.1	Constructor & Destructor Documentation	82
		6.10.1.1 Timer	82
	6.10.2	Member Function Documentation	82
		6.10.2.1 seconds	82
		6.10.2.2 tic	82
		6.10.2.3 toc	82
	6.10.3	Friends And Related Function Documentation	82
		6.10.3.1 operator<<	82
	6.10.4	Member Data Documentation	82
		_	82
		6.10.4.2 _start	82
6.11	qpp::Ur	niformIntDistribution Class Reference	82
	6.11.1		83
			83
	6.11.2		83
		•	83
	6.11.3		83
			83
6.12			83
	6.12.1		83
			83
	6.12.2		83
			84
	6.12.3		84
		6.12.3.1 _d	84
File	Docume	entation	85
7.1	include	/channels.h File Reference	85
7.2	include	/classes/exception.h File Reference	86
7.3	include	/classes/gates.h File Reference	86

7

CONTENTS xi

7.4	4	include	e/classes/	qudit.h File	e Refere	nce .			 	 	 	 	 			87
7.	5	include	e/classes/i	randevs.h	File Refe	erence			 	 	 	 	 			87
7.0	6	include	e/classes/s	singleton.l	n File Re	ferenc	e		 	 	 	 	 			88
		7.6.1	Macro D	efinition D	ocumen	tation			 	 	 	 	 			88
			7.6.1.1	CLASS	_CONST	_SINC	GLETC	N	 	 	 	 	 			88
			7.6.1.2	CLASS	SINGLE	TON			 	 	 	 	 			88
7.	7	include	e/classes/s	stat.h File	Referen	ce			 	 	 	 	 			89
7.8	8	include	e/classes/s	states.h Fi	ile Refere	ence .			 	 	 	 	 			89
7.9	9	include	e/classes/t	timer.h File	e Refere	nce .			 	 	 	 	 			90
7.	10	include	e/constant	s.h File R	eference				 	 	 	 	 			90
7.	11	include	e/entangle	ment.h Fi	le Refere	nce .			 	 	 	 	 			91
7.	12	include	e/entropies	s.h File Re	eference				 	 	 	 	 			92
7.	13	include	e/functions	s.h File Re	ference				 	 	 	 	 			93
7.	14	include	e/internal.l	n File Refe	erence				 	 	 	 	 			96
7.	15	include	e/io.h File	Reference					 	 	 	 	 			98
7.	16	include	e/matlab.h	File Refe	rence.				 	 	 	 	 			98
7.	17	include	e/qpp.h Fil	e Referen	ce				 	 	 	 	 			100
7.	18	include	e/random.l	h File Refe	erence				 	 	 	 	 			101
7.	19	include	e/types.h F	File Refere	ence .				 	 	 	 	 	 		102
Index																103

# Chapter 1

# Namespace Index

### 1.1 Namespace List

Here is a list of all namespaces with brief descriptions:

qpp	
qpp::ct	
qpp::internal	60
<pre>qpp::types</pre>	62

2 Namespace Index

## **Chapter 2**

## **Hierarchical Index**

### 2.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

qpp::DiscreteDistribution	63
qpp::DiscreteDistributionAbsSquare	64
exception	
qpp::Exception	65
qpp::NormalDistribution	74
qpp::Qudit	75
qpp::Singleton< T >	78
qpp::Gates	68
qpp::RandomDevices	77
qpp::Singleton < const Gates >	78
qpp::Singleton < const RandomDevices >	78
qpp::Singleton < const States >	78
qpp::States	79
qpp::Timer	81
qpp::UniformIntDistribution	82
gpp::UniformRealDistribution	83

**Hierarchical Index** 

# **Chapter 3**

## **Class Index**

### 3.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

o::DiscreteDistribution	63
p::DiscreteDistributionAbsSquare	64
p::Exception	65
o::Gates	68
p::NormalDistribution	74
p::Qudit	75
p::RandomDevices	77
o::Singleton $<$ T $>$ $\dots$	78
o::States	79
o::Timer	81
p::UniformIntDistribution	82
p::UniformRealDistribution	83

6 Class Index

# Chapter 4

## File Index

### 4.1 File List

Here is a list of all files with brief descriptions:

include/channels.h
include/constants.h
include/entanglement.h
include/entropies.h
include/functions.h
include/internal.h
include/io.h
include/matlab.h
include/qpp.h
include/random.h
include/types.h
include/classes/exception.h
include/classes/gates.h
include/classes/qudit.h
include/classes/randevs.h
include/classes/singleton.h
include/classes/stat.h
include/classes/states.h
include/classes/timer.h

8 File Index

### **Chapter 5**

## **Namespace Documentation**

#### 5.1 qpp Namespace Reference

#### **Namespaces**

- ct
- internal
- types

#### Classes

- · class Discrete Distribution
- · class DiscreteDistributionAbsSquare
- class Exception
- · class Gates
- · class NormalDistribution
- class Qudit
- class RandomDevices
- class Singleton
- · class States
- class Timer
- · class UniformIntDistribution
- · class UniformRealDistribution

#### **Functions**

- types::cmat super (const std::vector< types::cmat > &Ks)
- types::cmat choi (const std::vector< types::cmat > &Ks)
- std::vector< types::cmat > choi2kraus (const types::cmat &A)
- template<typename Derived >
   types::cmat channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< types::cmat > &Ks)
- template<typename Derived >
   types::cmat channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< types::cmat > &Ks,
   const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- constexpr std::complex< double > operator""\_i (unsigned long long int x)
- constexpr std::complex< double > operator""\_i (long double x)
- template<typename Derived >
   types::cmat schmidtcoeff (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)

Eigenvalues.

```
• template<typename Derived >
  types::cmat schmidtU (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &dims)
• template<typename Derived >
  types::cmat schmidtV (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)

    template<typename Derived >

  types::cmat schmidtprob (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)
• template<typename Derived >
  double entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)

    template<typename Derived >

  double gconcurrence (const Eigen::MatrixBase< Derived > &A)

    template<typename Derived >

  double shannon (const Eigen::MatrixBase< Derived > &A)

    template<typename Derived >

  double renyi (const double alpha, const Eigen::MatrixBase< Derived > &A)
• template<typename Derived >
  double renyi_inf (const Eigen::MatrixBase< Derived > &A)
• template<typename Derived >
  double tsallis (const double alpha, const Eigen::MatrixBase< Derived > &A)

    template<typename Derived >

  double gmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &subsys,
  const std::vector< std::size t > &dims)

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > transpose (const Eigen::MatrixBase < Derived > &A)
     Transpose.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > conjugate (const Eigen::MatrixBase < Derived > &A)
     Complex conjugate.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > adjoint (const Eigen::MatrixBase < Derived > &A)
     Adjoint.
template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > inverse (const Eigen::MatrixBase < Derived > &A)

    template<typename Derived >

  Derived::Scalar trace (const Eigen::MatrixBase< Derived > &A)

    template<typename Derived >

  Derived::Scalar det (const Eigen::MatrixBase< Derived > &A)
     Determinant

    template<typename Derived >

  Derived::Scalar logdet (const Eigen::MatrixBase< Derived > &A)
     Logarithm of the determinant.

    template<typename Derived >

  Derived::Scalar sum (const Eigen::MatrixBase< Derived > &A)
     Element-wise sum.

    template<typename Derived >

  double norm (const Eigen::MatrixBase< Derived > &A)
     Trace norm.

    template<typename Derived >

  types::cmat evals (const Eigen::MatrixBase< Derived > &A)
```

```
• template<typename Derived >
  types::cmat evects (const Eigen::MatrixBase< Derived > &A)
     Eigenvectors.

    template<typename Derived >

  types::dmat hevals (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvalues.

    template<typename Derived >

  types::cmat hevects (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvectors.

    template<typename Derived >

  types::cmat funm (const Eigen::MatrixBase< Derived > &A, types::cplx(*f)(const types::cplx &))
     Functional calculus f(A)

    template<typename Derived >

  types::cmat sqrtm (const Eigen::MatrixBase< Derived > &A)
     Matrix square root.

    template<typename Derived >

  types::cmat absm (const Eigen::MatrixBase< Derived > &A)
     Matrix absolut value.

    template<typename Derived >

  types::cmat expm (const Eigen::MatrixBase< Derived > &A)
     Matrix exponential.
template<typename Derived >
  types::cmat logm (const Eigen::MatrixBase< Derived > &A)
     Matrix logarithm.

    template<typename Derived >

  types::cmat sinm (const Eigen::MatrixBase< Derived > &A)
• template<typename Derived >
  types::cmat cosm (const Eigen::MatrixBase< Derived > &A)
     Matrix cos.

    template<typename Derived >

  types::cmat spectralpowm (const Eigen::MatrixBase< Derived > &A, const types::cplx z)
     Matrix power.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > powm (const Eigen::MatrixBase< Derived > &A, std::size_t n)
     Matrix power.
• template<typename OutputScalar , typename Derived >
  types::DynMat< OutputScalar > cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const
  typename Derived::Scalar &))
     Functor.
• template<typename T >
  types::DynMat< typename T::Scalar > kron (const T &head)
     Kronecker product (variadic overload)
• template<typename T , typename... Args>
  types::DynMat< typename T::Scalar > kron (const T &head, const Args &...tail)
     Kronecker product (variadic overload)
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > kron (const std::vector < Derived > &As)
     Kronecker product (std::vector overload)
template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > kron (const std::initializer_list< Derived > &As)
```

Kronecker product (std::initializer\_list overload) • template<typename Derived > types::DynMat< typename Derived::Scalar > kronpow (const Eigen::MatrixBase< Derived > &A, std::size\_t n) Kronecker power. template<typename Derived > types::DynMat< typename Derived::Scalar > reshape (const Eigen::MatrixBase< Derived > &A, std::size t rows, std::size t cols) Reshape. template<typename Derived > types::DynMat< typename Derived::Scalar > syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &perm, const std::vector< std::size t > &dims) System permutation. • template<typename Derived > types::DynMat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &dims) Partial trace. template<typename Derived > types::DynMat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims) Partial trace. template<typename Derived > types::DynMat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &subsys, const std::vector< std::size\_t > &dims) Partial trace. template<typename Derived > types::DynMat< typename Derived::Scalar > ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims) Partial transpose. template<typename Derived1 , typename Derived2 > types::DynMat< typename Derived1::Scalar > comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B) Commutator. template<typename Derived1 , typename Derived2 > types::DynMat< typename Derived1::Scalar > anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B) Anti-commutator. template<typename Derived > types::DynMat< typename Derived::Scalar > prj (const Eigen::MatrixBase < Derived > &V) Projector. template<typename Derived > types::DynMat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, std::size\_t pos, const std::vector< std::size\_t > &dims) Expand out. template<typename Derived > types::DynMat< typename Derived::Scalar > grams (const std::vector < Derived > &Vs) Gram-Schmidt orthogonalization (std::vector overload)

```
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > grams (const std::initializer_list< Derived > &Vs)
     Gram-Schmidt orthogonalization (std::initializer_list overload)

    template<typename Derived >

  types::DynMat< typename
  {\tt Derived::Scalar} > {\tt grams} \; ({\tt const} \; {\tt Eigen::MatrixBase} < {\tt Derived} > \& {\tt A})
      Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)

    std::vector< std::size t > n2multiidx (std::size t n, const std::vector< std::size t > &dims)

     Non-negative integer index to multi-index.

    std::size_t multiidx2n (const std::vector< std::size_t > &midx, const std::vector< std::size_t > &dims)

     Multi-index to non-negative integer index.

    types::ket mket (const std::vector< std::size t > &mask)

     Multi-partite qubit ket.

    types::ket mket (const std::vector< std::size_t > &mask, const std::vector< std::size_t > &dims)

     Multi-partite qudit ket (different dimensions overload)

    types::ket mket (const std::vector< std::size t > &mask, std::size t d)

     Multi-partite qudit ket (same dimensions overload)

    std::vector< std::size_t > invperm (const std::vector< std::size_t > &perm)

     Inverse permutation.
• std::vector< std::size t > compperm (const std::vector< std::size t > &perm, const std::vector< std::size t
  > &sigma)
     Compose permutations.
• template<typename T >
  void disp (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]",
  std::ostream &os=std::cout)
template<typename T >
  void displn (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]",
  std::ostream &os=std::cout)

    template<typename T >

  void disp (const T *x, const std::size t n, const std::string &separator, const std::string &start="[", const std
  ::string &end="]", std::ostream &os=std::cout)
• template<typename T >
  void displn (const T *x, const std::size_t n, const std::string &separator, const std::string &start="[", const
  std::string &end="]", std::ostream &os=std::cout)

    template<typename Derived >

  void disp (const Eigen::MatrixBase < Derived > &A, double chop=ct::chop, std::ostream &os=std::cout)

    template<typename Derived >

  void displn (const Eigen::MatrixBase < Derived > &A, double chop=ct::chop, std::ostream &os=std::cout)

    void disp (const types::cplx c, double chop=ct::chop, std::ostream &os=std::cout)

• void displn (const types::cplx c, double chop=ct::chop, std::ostream &os=std::cout)

    template<typename Derived >

  void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > load (const std::string &fname)

    template<typename Derived >

  Derived loadMATLABmatrix (const std::string &mat file, const std::string &var name)
template<>
  types::dmat loadMATLABmatrix (const std::string &mat file, const std::string &var name)
• template<>
  types::cmat loadMATLABmatrix (const std::string &mat file, const std::string &var name)

    template<typename Derived >

  void saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std↔
```

::string &var\_name, const std::string &mode)

- template<>
   void saveMATLABmatrix (const Eigen::MatrixBase< types::dmat > &A, const std::string &mat\_file, const std::string &var name, const std::string &mode)
- template<>
   void saveMATLABmatrix (const Eigen::MatrixBase< typename types::cmat > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)
- template<typename Derived >
   Derived rand (std::size\_t rows, std::size\_t cols, double a=0, double b=1)
- template<>
  types::dmat rand (std::size t rows, std::size t cols, double a, double b)
- template<>
   types::cmat rand (std::size\_t rows, std::size\_t cols, double a, double b)
- double rand (double a=0, double b=1)
- long long randint (long long a, long long b)
- template<typename Derived >
   Derived randn (std::size t rows, std::size t cols, double mean=0, double sigma=1)
- template<>
   types::dmat randn (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- template<>
   types::cmat randn (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- double randn (double mean=0, double sigma=1)
- types::cmat randU (std::size\_t D)
- types::cmat randV (std::size\_t Din, std::size\_t Dout)
- std::vector< types::cmat > randkraus (std::size\_t n, std::size\_t D)
- types::cmat randH (std::size t D)
- types::ket randket (std::size\_t D)
- types::cmat randrho (std::size\_t D)
- std::vector< std::size\_t > randperm (std::size\_t n)

#### **Variables**

- const RandomDevices & rdevs = RandomDevices::get\_instance()
- const Gates & gt = Gates::get\_instance()
- const States & st = States::get\_instance()

#### **5.1.1 Function Documentation**

5.1.1.1 template<typename Derived > types::cmat qpp::absm ( const Eigen::MatrixBase< Derived > & A )

Matrix absolut value.

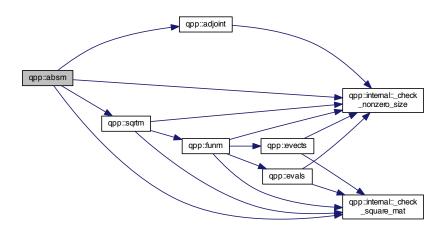
Parameters

A | Eigen expression

Returns

Matrix absolut value of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.2 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::adjoint ( const Eigen::MatrixBase< Derived > &  $\it A$  )

Adjoint.

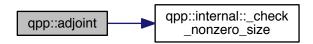
**Parameters** 

Α	Eigen expression

Returns

Adjoint (Hermitian conjugate) of A, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.3 template<typename Derived1 , typename Derived2 > types::DynMat<typename Derived1::Scalar> qpp::anticomm ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )

Anti-commutator.

Anti-commutator  $\{A,B\} = AB + BA$ 

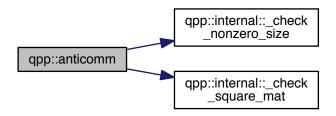
Both A and B must be Eigen expressions over the same scalar field

Α	Eigen expression
В	Eigen expression

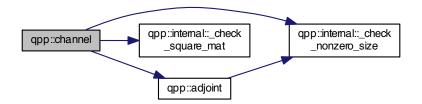
#### Returns

Anti-commutator AB + BA, as a dynamic matrix over the same scalar field

Here is the call graph for this function:

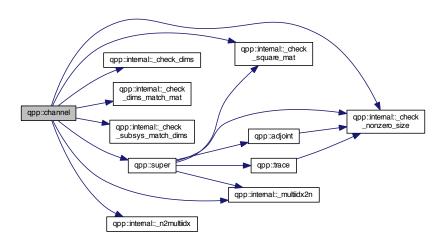


5.1.1.4 template<typename Derived > types::cmat qpp::channel ( const Eigen::MatrixBase< Derived > & rho, const std::vector< types::cmat > & Ks )

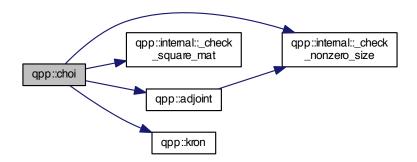


5.1.1.5 template < typename Derived > types::cmat qpp::channel ( const Eigen::MatrixBase < Derived > & rho, const std::vector < types::cmat > & Ks, const std::vector < std::size\_t > & subsys, const std::vector < std::size\_t > & dims 
)

Here is the call graph for this function:

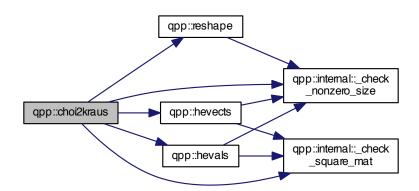


5.1.1.6 types::cmat qpp::choi ( const std::vector< types::cmat > &  $\mathit{Ks}$  )



5.1.1.7 std::vector<types::cmat> qpp::choi2kraus ( const types::cmat & A )

Here is the call graph for this function:



5.1.1.8 template<typename Derived1 , typename Derived2 > types::DynMat<typename Derived1::Scalar> qpp::comm ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )

#### Commutator.

Commutator [A,B] = AB - BA

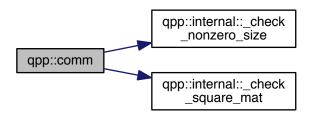
Both A and B must be Eigen expressions over the same scalar field

#### **Parameters**

Α	Eigen expression
В	Eigen expression

#### Returns

Commutator AB - BA, as a dynamic matrix over the same scalar field



5.1.1.9 std::vector < std::size\_t > & perm, const std::vector < std::size\_t > & perm, const std::vector < std::size\_t > & sigma )

Compose permutations.

perm	Permutation
sigma	Permutation

#### Returns

Composition of the permutations *perm* o *sigma* = perm(sigma)

Here is the call graph for this function:



5.1.1.10 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::conjugate ( const Eigen::MatrixBase< Derived > & A )

Complex conjugate.

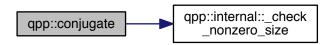
#### **Parameters**

A Ligen expression
--------------------

#### Returns

Complex conjugate of A, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



 $5.1.1.11 \quad template < typename \ Derived > types::cmat \ qpp::cosm \ ( \ const \ Eigen::Matrix Base < Derived > \& \ \textit{A} \ )$ 

Matrix cos.

Α	Eigen expression
---	------------------

#### Returns

Matrix cosine of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.12 template < typename OutputScalar , typename Derived > types::DynMat < OutputScalar > qpp::cwise ( const Eigen::MatrixBase < Derived > & A, OutputScalar(\*)(const typename Derived::Scalar &) f)

#### Functor.

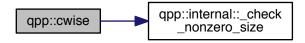
#### **Parameters**

Α	Eigen expression
f	Pointer-to-function from scalars of A to OutputScalar

#### Returns

Component-wise f(A), as a dynamic matrix over the *OutputScalar* scalar field

Here is the call graph for this function:



5.1.1.13 template<typename Derived > Derived::Scalar qpp::det ( const Eigen::MatrixBase< Derived > & A )

Determinant.

Α	Eigen expression	

#### Returns

Determinant of A, as a dynamic matrix over the same scalar field Returns  $\pm\infty$  when the determinant overflows/underflows

Here is the call graph for this function:



- 5.1.1.14 template<typename T > void qpp::disp ( const T & x, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )
- 5.1.1.15 template < typename T > void qpp::disp ( const T \* x, const std::size\_t n, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )
- 5.1.1.16 template < typename Derived > void qpp::disp ( const Eigen::MatrixBase < Derived > & A, double chop = ct::chop, std::ostream & os = std::cout )
- 5.1.1.17 void qpp::disp ( const types::cplx c, double chop = ct : :chop, std::ostream & os = std::cout )



5.1.1.18 template<typename T > void qpp::displn ( const T & x, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )

Here is the call graph for this function:



5.1.1.19 template<typename T > void qpp::displn ( const T \* x, const std::size\_t n, const std::string & separator, const std::string & std::string & end = "]", std::ostream & os = std::cout)

Here is the call graph for this function:



5.1.1.20 template < typename Derived > void qpp::displn ( const Eigen::MatrixBase < Derived > & A, double chop = ct::chop, std::ostream & os = std::cout )



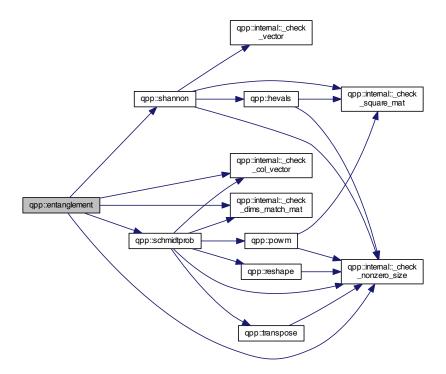
5.1.1.21 void qpp::displn ( const types::cplx c, double chop = ct : :chop, std::ostream & os = std::cout )

Here is the call graph for this function:



5.1.1.22 template < typename Derived > double qpp::entanglement ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

Here is the call graph for this function:



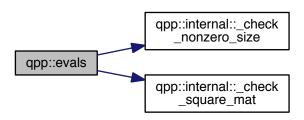
5.1.1.23 template<typename Derived > types::cmat qpp::evals ( const Eigen::MatrixBase< Derived > & A )

Eigenvalues.

A	Eigen expression
/ ·	Ligen expression

## Returns

Eigenvalues of *A*, as a diagonal dynamic matrix over the complex field, with eigenvalues on the diagonal Here is the call graph for this function:



5.1.1.24 template < typename Derived > types::cmat qpp::evects ( const Eigen::MatrixBase < Derived > & A )

## Eigenvectors.

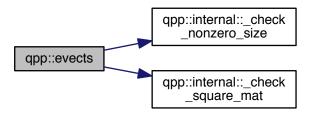
#### **Parameters**

```
A Eigen expression
```

#### Returns

Eigenvectors of A, as columns of a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.25 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::expandout ( const Eigen::MatrixBase< Derived > & A, std::size\_t pos, const std::vector< std::size\_t > & dims )

# Expand out.

Expand out A as a matrix in a multi-partite system Faster than using <a href="mailto:qpp::kron(I, I, ..., I, A, I, ..., I">qpp::kron(I, I, ..., I, A, I, ..., I)</a>

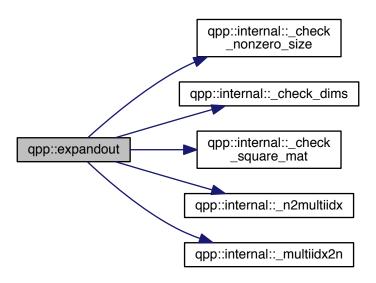
#### **Parameters**

Α	Eigen expression
pos	Position
dims	Dimensions of the multi-partite system

## Returns

Tensor product  $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$ , with A on position pos, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



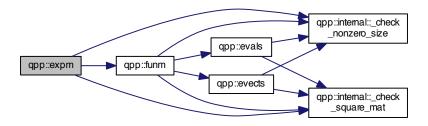
5.1.1.26 template<typename Derived > types::cmat qpp::expm ( const Eigen::MatrixBase< Derived > & A )

Matrix exponential.

Α	Eigen expression

Matrix exponential of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.27 template < typename Derived > types::cmat qpp::funm ( const Eigen::MatrixBase < Derived > & A, types::cplx(\*)(const types::cplx &) f )

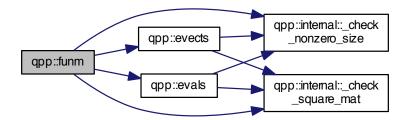
# Functional calculus f(A)

## **Parameters**

Α	Eigen expression
f	Pointer-to-function from complex to complex

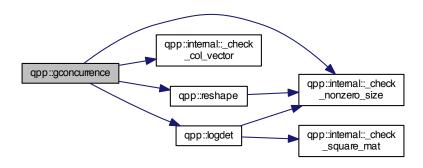
# Returns

f(A), as a dynamic matrix over the complex field



5.1.1.28 template < typename Derived > double qpp::gconcurrence ( const Eigen::MatrixBase < Derived > & A )

Here is the call graph for this function:



5.1.1.29 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::grams ( const std::vector< Derived > & Vs )

Gram-Schmidt orthogonalization (std::vector overload)

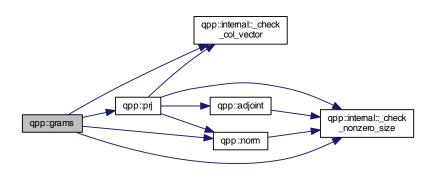
**Parameters** 

Vs	std::vector of Eigen expressions as column vectors
----	--

## Returns

Gram-Schmidt vectors of Vs as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.30 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::grams ( const std::initializer\_list< Derived > & Vs )

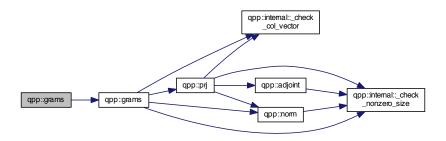
Gram-Schmidt orthogonalization (std::initializer list overload)

Vs	std::initializer_list of Eigen expressions as column vectors
• • • • • • • • • • • • • • • • • • • •	otalinitianzor_not or Eigon expressions as solution vestors

## Returns

Gram-Schmidt vectors of Vs as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.31 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::grams ( const Eigen::MatrixBase< Derived > & A )

Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)

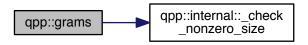
# **Parameters**

Α	Eigen expression, the input vectors are the columns of A

## Returns

Gram-Schmidt vectors of the columns of A, as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



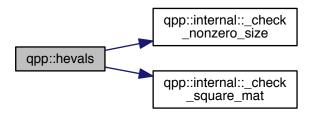
5.1.1.32 template < typename Derived > types::dmat qpp::hevals ( const Eigen::MatrixBase < Derived > & A )

Hermitian eigenvalues.

Α	Eigen expression
---	------------------

## Returns

Eigenvalues of Hermitian *A*, as a diagonal dynamic matrix over the real field, with eigenvalues on the diagonal Here is the call graph for this function:



5.1.1.33 template < typename Derived > types::cmat qpp::hevects ( const Eigen::MatrixBase < Derived > & A )

Hermitian eigenvectors.

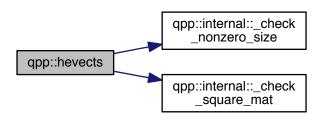
### **Parameters**

Α	Eigen expression

## Returns

Eigenvectors of Hermitian A, as columns of a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.34 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::inverse ( const Eigen::MatrixBase < Derived > & A )

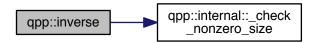
Inverse.

Α	Eigen expression

## Returns

Inverse of A, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.35 std::vector<std::size\_t> qpp::invperm ( const std::vector< std::size\_t> & perm )

Inverse permutation.

#### **Parameters**

perm	Permutation

## Returns

Inverse of the permutation perm

Here is the call graph for this function:



5.1.1.36 template < typename T > types::DynMat < typename T::Scalar > qpp::kron ( const T & head )

Kronecker product (variadic overload)

Used to stop the recursion for the variadic template version of *qpp::kron*(...)

head	Eigen expression

Its argument head

5.1.1.37 template < typename T , typename... Args > types::DynMat < typename T::Scalar > qpp::kron ( const T & head, const Args &... tail )

Kronecker product (variadic overload)

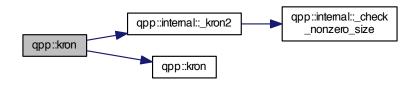
## **Parameters**

head	Eigen expression
tail	Variadic Eigen expression (zero or more parameters)

#### Returns

Kronecker product of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.38 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::kron ( const std::vector< Derived > & As )

Kronecker product (std::vector overload)

As	std::vector of Eigen expressions

Kronecker product of all elements in As, evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.39 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::kron ( const std::initializer\_list < Derived > & As)

Kronecker product (std::initializer\_list overload)

#### **Parameters**

As	std::initializer list of Eigen expressions, such as {A1, A2,, Ak}
AS	stdinitializer_list of Ligeri expressions, such as {A1, A2, ,Ak}

# Returns

Kronecker product of all elements in As, evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



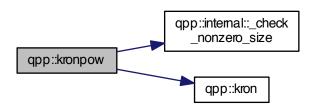
5.1.1.40 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::kronpow ( const Eigen::MatrixBase< Derived > &  $A_r$ , std::size\_t n)

Kronecker power.

Α	Eigen expression
n	Non-negative integer

Kronecker product of A with itself n times  $A^{\otimes n}$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



- $5.1.1.41 \quad template < typename \ Derived > types:: DynMat < typename \ Derived:: Scalar > qpp:: load ( \ const \ std:: string \ \& \ \textit{fname}$  )
- 5.1.1.42 template < typename Derived > Derived qpp::loadMATLABmatrix ( const std::string &  $mat\_file$ , const std::string &  $var\_name$  )
- 5.1.1.43 template <> types::dmat qpp::loadMATLABmatrix ( const std::string & mat\_file, const std::string & var\_name )
- 5.1.1.44 template<> types::cmat qpp::loadMATLABmatrix ( const std::string & mat\_file, const std::string & var\_name )
- 5.1.1.45 template<typename Derived > Derived::Scalar qpp::logdet ( const Eigen::MatrixBase< Derived > & A )

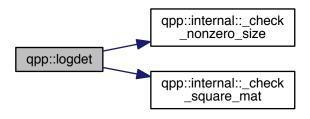
Logarithm of the determinant.

Especially useful when the determinant overflows/underflows

Α	Eigen expression
---	------------------

Logarithm of the determinant of A, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.46 template < typename Derived > types::cmat qpp::logm ( const Eigen::MatrixBase < Derived > & A )

Matrix logarithm.

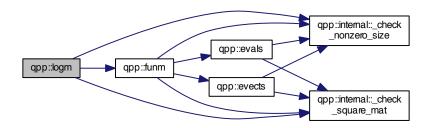
#### **Parameters**

Α	Eigen expression

## Returns

Matrix logarithm of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



# 5.1.1.47 types::ket qpp::mket ( const std::vector< std::size\_t > & mask )

Multi-partite qubit ket.

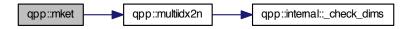
Constructs the multi-partite qubit ket  $|mask\rangle$ , where mask is a std::vector of 0's and 1's

mask	std::vector of 0's and 1's

## Returns

Multi-partite qubit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



5.1.1.48 types::ket qpp::mket ( const std::vector < std::size\_t > & mask, const std::vector < std::size\_t > & dims )

Multi-partite qudit ket (different dimensions overload)

Constructs the multi-partite qudit ket  $|mask\rangle$ , where mask is a std::vector of non-negative integers Each element in mask has to be smaller than the corresponding element in dims

#### **Parameters**

mask	std::vector of non-negative integers

# Returns

Multi-partite qudit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



5.1.1.49 types::ket qpp::mket ( const std::vector < std::size\_t > & mask, std::size\_t d )

Multi-partite qudit ket (same dimensions overload)

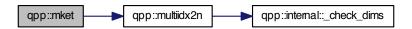
Constructs the multi-partite qudit ket  $|mask\rangle$  in a multi-partite system, all subsystem having equal dimension d mask is a std::vector of non-negative integers, and each element in mask has to be strictly smaller than d

mask	std::vector of non-negative integers
d	Subsystems' dimension

## Returns

Multi-partite qudit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



5.1.1.50 std::size\_t qpp::multiidx2n ( const std::vector < std::size\_t > & midx, const std::vector < std::size\_t > & dims )

Multi-index to non-negative integer index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

#### **Parameters**

midx	Multi-index
dims	Dimensions of the multi-partite system

# Returns

Non-negative integer index

Here is the call graph for this function:



5.1.1.51 std::vector<std::size\_t> qpp::n2multiidx ( std::size\_t n, const std::vector< std::size\_t> & dims )

Non-negative integer index to multi-index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

n	Non-negative integer index
dims	Dimensions of the multi-partite system

# Returns

Multi-index of the same size as dims

Here is the call graph for this function:



5.1.1.52 template<typename Derived > double qpp::norm ( const Eigen::MatrixBase< Derived > & A )

Trace norm.

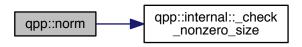
**Parameters** 

Α	Eigen expression

## Returns

Trace norm (Frobenius norm) of A, as a real number

Here is the call graph for this function:



- 5.1.1.53 constexpr std::complex<double> qpp::operator""\_i ( unsigned long long int x )
- 5.1.1.54 constexpr std::complex<double> qpp::operator""\_i ( long double x )
- 5.1.1.55 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::powm ( const Eigen::MatrixBase < Derived > & A, std::size\_t n)

Matrix power.

By convention  $A^0 = I$ 

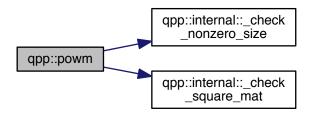
Explicitly multiplies the matrix A with itself n times

Α	Eigen expression
n	Non-negative integer

## Returns

Matrix power  $A^n$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.56 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::prj ( const Eigen::MatrixBase< Derived > & V )

# Projector.

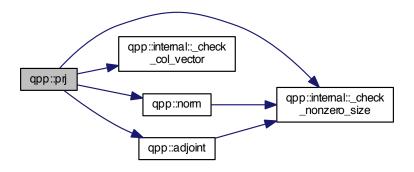
Normalized projector onto state vector

# **Parameters**

V Eigen expression
--------------------

## Returns

Projector onto the state vector V, or the matrix Zero if V has norm zero (i.e. smaller than qpp::ct::eps), as a dynamic matrix over the same scalar field



5.1.1.57 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::ptrace ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & subsys, const std::vector < std::size\_t > & dims )

Partial trace.

Partial trace of the multi-partite density matrix over a list of subsystems

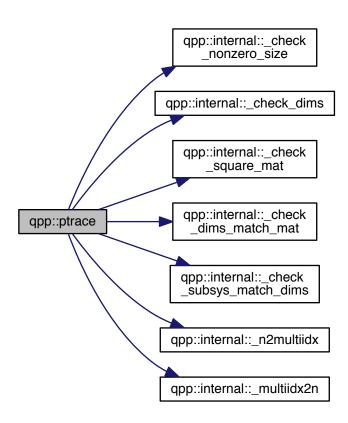
#### **Parameters**

Α	Eigen expression
subsys	Subsystems' indexes
dims	Dimensions of the multi-partite system

#### Returns

Partial trace  $Tr_{subsys}(\cdot)$  over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.58 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::ptrace1 ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & dims )

Partial trace.

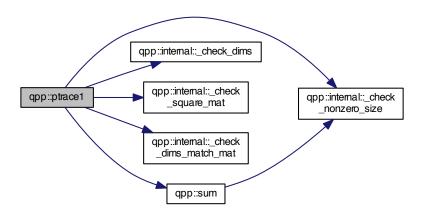
Partial trace of density matrix over the first subsystem in a bi-partite system

Α	Eigen expression
dims	Dimensions of bi-partite system (must be a std::vector with 2 elements)

# Returns

Partial trace  $Tr_A(\cdot)$  over the first subsytem A in a bi-partite system  $A\otimes B$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.59 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::ptrace2 ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & dims )

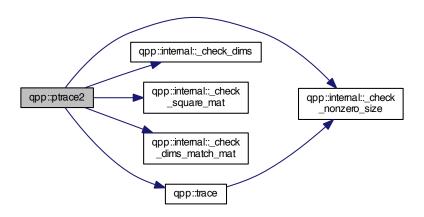
# Partial trace.

Partial trace of density matrix over the second subsystem in a bi-partite system

Α	Eigen expression
dims	Dimensions of bi-partite system (must be a std::vector with 2 elements)

Partial trace  $Tr_B(\cdot)$  over the second subsytem B in a bi-partite system  $A\otimes B$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



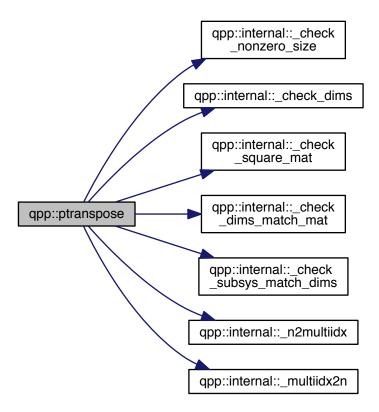
5.1.1.60 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::ptranspose ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & subsys, const std::vector< std::size\_t > & dims )

# Partial transpose.

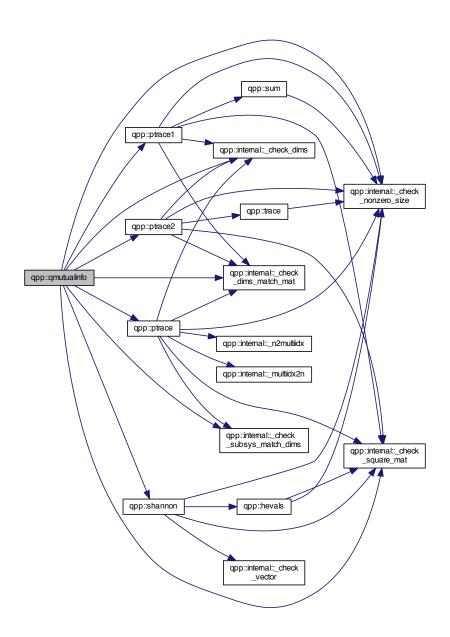
Partial transpose of the multi-partite density matrix over a list of subsystems

Α	Eigen expression
subsys	Subsystems' indexes
dims	Dimensions of the multi-partite system

Partial transpose  $(\cdot)^{T_{subsys}}$  over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field



5.1.1.61 template<typename Derived > double qpp::qmutualinfo ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & subsys, const std::vector< std::size\_t > & dims )



- 5.1.1.62 template < typename Derived > Derived qpp::rand ( std::size\_t rows, std::size\_t cols, double a = 0, double b = 1 )
- 5.1.1.63 template <> types::dmat qpp::rand ( std::size\_t rows, std::size\_t cols, double a, double b )

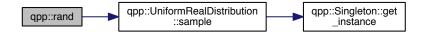
5.1.1.64 template<> types::cmat qpp::rand ( std::size\_t rows, std::size\_t cols, double a, double b )

Here is the call graph for this function:



5.1.1.65 double qpp::rand ( double a = 0, double b = 1 )

Here is the call graph for this function:



5.1.1.66 types::cmat qpp::randH ( std::size\_t D )

Here is the call graph for this function:

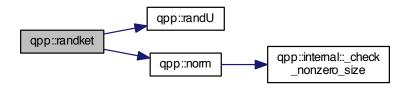


5.1.1.67 long long qpp::randint ( long long a, long long b )



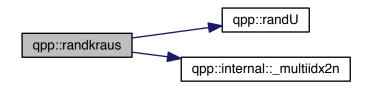
## 5.1.1.68 types::ket qpp::randket ( std::size\_t D )

Here is the call graph for this function:



## 5.1.1.69 std::vector<types::cmat> qpp::randkraus ( std::size\_t n, std::size\_t D )

Here is the call graph for this function:



- 5.1.1.70 template<typename Derived > Derived qpp::randn ( std::size\_t rows, std::size\_t cols, double mean = 0, double sigma = 1 )
- 5.1.1.71 template<> types::dmat qpp::randn ( std::size\_t rows, std::size\_t cols, double mean, double sigma )



5.1.1.72 template<> types::cmat qpp::randn ( std::size\_t rows, std::size\_t cols, double mean, double sigma )

Here is the call graph for this function:



5.1.1.73 double qpp::randn ( double mean = 0, double sigma = 1 )

Here is the call graph for this function:

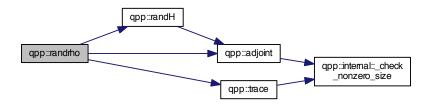


5.1.1.74 std::vector<std::size\_t> qpp::randperm ( std::size\_t n )



## 5.1.1.75 types::cmat qpp::randrho ( std::size\_t D )

Here is the call graph for this function:



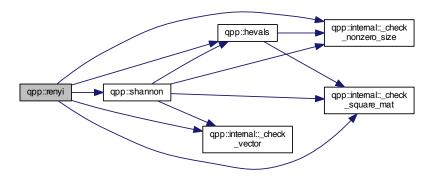
## 5.1.1.76 types::cmat qpp::randU ( std::size\_t D )

# 5.1.1.77 types::cmat qpp::randV ( std::size\_t Din, std::size\_t Dout )

Here is the call graph for this function:

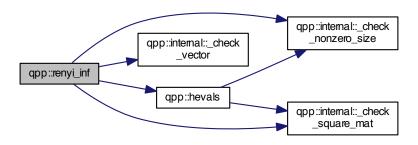


# 5.1.1.78 template < typename Derived > double qpp::renyi ( const double alpha, const Eigen::MatrixBase < Derived > & A )



5.1.1.79 template < typename Derived > double qpp::renyi\_inf ( const Eigen::MatrixBase < Derived > & A )

Here is the call graph for this function:



5.1.1.80 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::reshape ( const Eigen::MatrixBase< Derived > & A, std::size\_t rows, std::size\_t cols )

## Reshape.

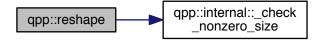
Uses column-major order when reshaping (same as MATLAB)

#### **Parameters**

Α	Eigen expression
rows	Number of rows of the reshaped matrix
cols	Number of columns of the reshaped matrix

## Returns

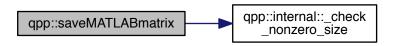
Reshaped matrix with rows rows and cols columns, as a dynamic matrix over the same scalar field



- 5.1.1.81 template < typename Derived > void qpp::save ( const Eigen::MatrixBase < Derived > & A, const std::string & fname )
- 5.1.1.82 template < typename Derived > void qpp::saveMATLABmatrix ( const Eigen::MatrixBase < Derived > & A, const std::string & mat\_file, const std::string & mode )

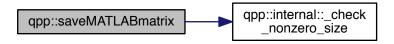
5.1.1.83 template<> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< types::dmat > & A, const std::string & mat\_file, const std::string & var\_name, const std::string & mode )

Here is the call graph for this function:

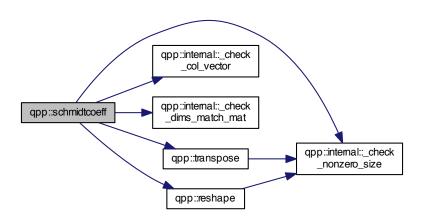


5.1.1.84 template<> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< typename types::cmat > & A, const std::string & mat\_file, const std::string & var\_name, const std::string & mode )

Here is the call graph for this function:

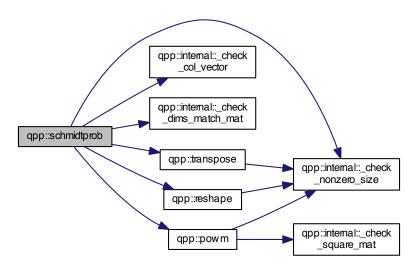


5.1.1.85 template < typename Derived > types::cmat qpp::schmidtcoeff ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

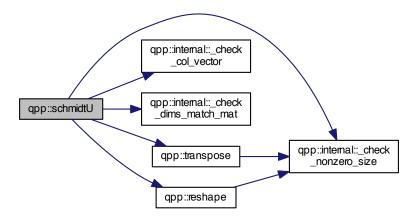


5.1.1.86 template < typename Derived > types::cmat qpp::schmidtprob ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

Here is the call graph for this function:

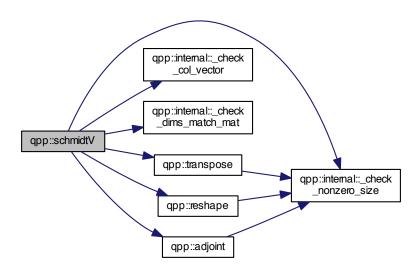


5.1.1.87 template < typename Derived > types::cmat qpp::schmidtU ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )



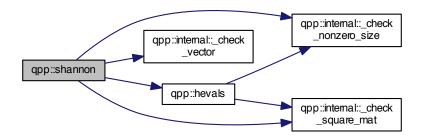
5.1.1.88 template < typename Derived > types::cmat qpp::schmidtV ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

Here is the call graph for this function:



5.1.1.89 template<typename Derived > double qpp::shannon ( const Eigen::MatrixBase< Derived > & A )

Here is the call graph for this function:



5.1.1.90 template < typename Derived > types::cmat qpp::sinm ( const Eigen::MatrixBase < Derived > & A )

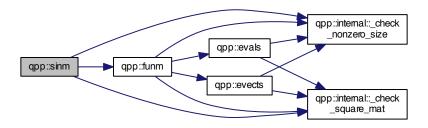
Matrix sin.

Α	Eigen expression
---	------------------

## Returns

Matrix sine of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.91 template<typename Derived > types::cmat qpp::spectralpowm ( const Eigen::MatrixBase< Derived > & A, const types::cplx z )

Matrix power.

By convention  $A^0 = I$ 

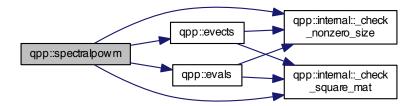
Uses the spectral decomposition of A to compute the matrix power

## **Parameters**

Α	Eigen expression
Z	Complex number

# Returns

Matrix power  $A^z$ , as a dynamic matrix over the complex field



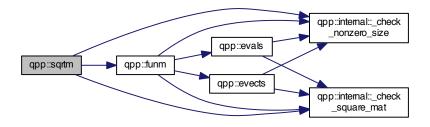
 $\label{topological constraints} \textbf{5.1.1.92} \quad \textbf{template} < \textbf{typename Derived} > \textbf{types::cmat qpp::sqrtm ( const Eigen::MatrixBase} < \textbf{Derived} > \textbf{\& A ) }$  Matrix square root.

Α	Eigen expression

## Returns

Matrix square root of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



 $5.1.1.93 \quad template < typename \ Derived > Derived :: Scalar \ qpp::sum \ ( \ const \ Eigen:: Matrix Base < Derived > \& \ A \ )$ 

Element-wise sum.

**Parameters** 

Α	Eigen expression

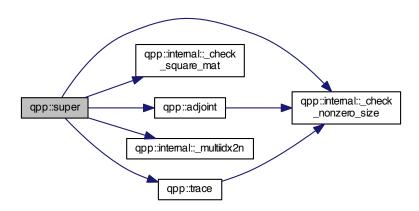
# Returns

Element-wise sum of A, as a dynamic matrix over the same scalar field



5.1.1.94 types::cmat qpp::super ( const std::vector< types::cmat > & Ks )

Here is the call graph for this function:



5.1.1.95 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::syspermute ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & perm, const std::vector < std::size\_t > & dims )

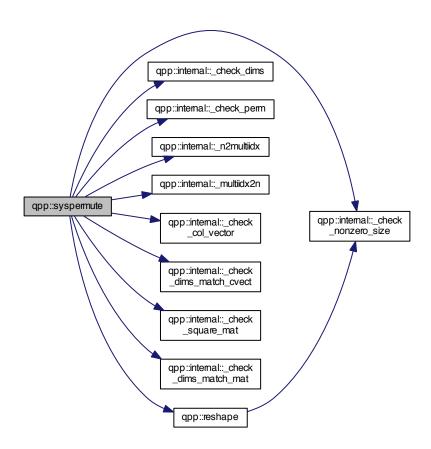
System permutation.

Permutes the subsystems in a state vector or density matrix The qubit perm[i] is permuted to the location i

Α	Eigen expression
perm	Permutation
dims	Subsystems' dimensions

Permuted system, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.96 template<typename Derived > Derived::Scalar qpp::trace ( const Eigen::MatrixBase< Derived > & A )

Trace.

Α	Eigen expression

Trace of A, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.97 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::transpose ( const Eigen::MatrixBase < Derived > & A )

# Transpose.

## **Parameters**

```
A | Eigen expression
```

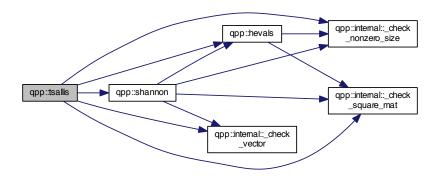
## Returns

Transpose of A, as a dynamic matrix over the same scalar field



5.1.1.98 template<typename Derived > double qpp::tsallis ( const double alpha, const Eigen::MatrixBase< Derived > & A )

Here is the call graph for this function:



#### 5.1.2 Variable Documentation

- 5.1.2.1 const Gates& gpp::gt = Gates::get instance()
- 5.1.2.2 const RandomDevices& gpp::rdevs = RandomDevices::get\_instance()
- 5.1.2.3 const States& qpp::st = States::get\_instance()

# 5.2 qpp::ct Namespace Reference

# **Functions**

std::complex< double > omega (std::size\_t D)

## **Variables**

- constexpr double chop = 1e-10
- constexpr double eps = 1e-12
- constexpr std::size\_t maxn = 64
- constexpr double pi = 3.141592653589793238462643383279502884
- constexpr double ee = 2.718281828459045235360287471352662497

## 5.2.1 Function Documentation

- 5.2.1.1 std::complex < double > qpp::ct::omega ( std::size\_t D )
- 5.2.2 Variable Documentation
- 5.2.2.1 constexpr double qpp::ct::chop = 1e-10
- 5.2.2.2 constexpr double qpp::ct::ee = 2.718281828459045235360287471352662497
- 5.2.2.3 constexpr double qpp::ct::eps = 1e-12

- 5.2.2.4 constexpr std::size\_t qpp::ct::maxn = 64
- 5.2.2.5 constexpr double qpp::ct::pi = 3.141592653589793238462643383279502884

# 5.3 qpp::internal Namespace Reference

#### **Functions**

- void n2multiidx (std::size t n, std::size t numdims, const std::size t \*dims, std::size t \*result)
- std::size\_t \_multiidx2n (const std::size\_t \*midx, std::size\_t numdims, const std::size\_t \*dims)
- template<typename Derived >

```
bool\_check\_square\_mat~(const~Eigen::MatrixBase < Derived > \&A)
```

• template<typename Derived >

bool <u>\_check\_vector</u> (const Eigen::MatrixBase< Derived > &A)

template<typename Derived >

```
bool <u>_check_row_vector</u> (const Eigen::MatrixBase< Derived > &A)
```

• template<typename Derived >

```
bool <u>_check_col_vector</u> (const Eigen::MatrixBase< Derived > &A)
```

• template<typename T >

bool check nonzero size (const T &x)

- bool <u>\_check\_dims</u> (const std::vector < std::size\_t > &dims)
- template<typename Derived >

```
bool _check_dims_match_mat (const std::vector< std::size_t > &dims, const Eigen::MatrixBase< Derived > &A)
```

template<typename Derived >

```
bool <u>_check_dims_match_cvect</u> (const std::vector< std::size_t > &dims, const Eigen::MatrixBase< Derived > &V)
```

 $\bullet \ \ \text{template}{<} \text{typename Derived} >$ 

 $\label{local_bool_check_dims_match_rvect} \mbox{ (const std::vector} < \mbox{ std::size\_t} > \& \mbox{dims, const Eigen::MatrixBase} < \mbox{ Derived} > \& \mbox{V})$ 

- bool <u>\_check\_eq\_dims</u> (const std::vector< std::size\_t > &dims, std::size\_t dim)
- bool \_check\_subsys\_match\_dims (const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- bool \_check\_perm (const std::vector< std::size\_t > &perm)
- template<typename Derived1 , typename Derived2 >

```
types::DynMat< typename
```

Derived1::Scalar > \_kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)

template<typename T >

```
void variadic vector emplace (std::vector< T > &)
```

template<typename T, typename First, typename... Args>
 void variadic\_vector\_emplace (std::vector< T > &v, First &&first, Args &&...args)

## 5.3.1 Function Documentation

- 5.3.1.1 template < typename Derived > bool qpp::internal::\_check\_col\_vector ( const Eigen::MatrixBase < Derived > & A )
- 5.3.1.2 bool qpp::internal::\_check\_dims ( const std::vector< std::size\_t > & dims )
- 5.3.1.3 template<typename Derived > bool qpp::internal::\_check\_dims\_match\_cvect ( const std::vector< std::size\_t > & dims, const Eigen::MatrixBase< Derived > & V)
- 5.3.1.4 template<typename Derived > bool qpp::internal::\_check\_dims\_match\_mat ( const std::vector< std::size\_t > & dims, const Eigen::MatrixBase< Derived > & A )

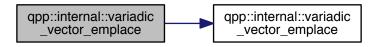
- 5.3.1.5 template<typename Derived > bool qpp::internal::\_check\_dims\_match\_rvect ( const std::vector< std::size\_t > & dims, const Eigen::MatrixBase< Derived > & V )
- 5.3.1.6 bool qpp::internal::\_check\_eq\_dims ( const std::vector < std::size\_t > & dims, std::size\_t dim )
- 5.3.1.7 template < typename T > bool qpp::internal::\_check\_nonzero\_size ( const T & x )
- 5.3.1.8 bool qpp::internal::\_check\_perm ( const std::vector< std::size\_t > & perm )
- 5.3.1.9 template < typename Derived > bool qpp::internal::\_check\_row\_vector ( const Eigen::MatrixBase < Derived > & A )
- 5.3.1.10 template < typename Derived > bool qpp::internal::\_check\_square\_mat ( const Eigen::MatrixBase < Derived > & A )
- 5.3.1.11 bool qpp::internal::\_check\_subsys\_match\_dims ( const std::vector< std::size\_t > & subsys, const std::vector< std::size\_t > & dims )
- 5.3.1.12 template < typename Derived > bool qpp::internal::\_check\_vector ( const Eigen::MatrixBase < Derived > & A )
- 5.3.1.13 template<typename Derived1 , typename Derived2 > types::DynMat<typename Derived1::Scalar> qpp::internal::\_kron2 ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )

Here is the call graph for this function:



- 5.3.1.14 std::size t qpp::internal:: multiidx2n ( const std::size t \* midx, std::size t numdims, const std::size t \* dims )
- 5.3.1.15 void qpp::internal::\_n2multiidx ( std::size\_t n, std::size\_t numdims, const std::size\_t \* dims, std::size\_t \* result )
- 5.3.1.16 template < typename T > void qpp::internal::variadic\_vector\_emplace ( std::vector < T > & )
- 5.3.1.17 template < typename T , typename First , typename... Args > void qpp::internal::variadic\_vector\_emplace ( std::vector < T > & v, First && first, Args &&... args )

Here is the call graph for this function:



## 5.4 qpp::types Namespace Reference

### **Typedefs**

```
using cplx = std::complex< double >
using cmat = Eigen::MatrixXcd
using dmat = Eigen::MatrixXd
using ket = Eigen::Matrix< cplx, Eigen::Dynamic, 1 >
using bra = Eigen::Matrix< cplx, 1, Eigen::Dynamic >
template<typename Scalar >
using DynMat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >
```

### 5.4.1 Typedef Documentation

```
5.4.1.1 using qpp::types::bra = typedef Eigen::Matrix<cplx, 1, Eigen::Dynamic>
```

- 5.4.1.2 using qpp::types::cmat = typedef Eigen::MatrixXcd
- 5.4.1.3 using qpp::types::cplx = typedef std::complex < double >
- 5.4.1.4 using qpp::types::dmat = typedef Eigen::MatrixXd
- 5.4.1.5 template<typename Scalar > using qpp::types::DynMat = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>
- 5.4.1.6 using qpp::types::ket = typedef Eigen::Matrix<cplx, Eigen::Dynamic, 1>

## **Chapter 6**

## **Class Documentation**

## 6.1 qpp::DiscreteDistribution Class Reference

```
#include <stat.h>
```

### **Public Member Functions**

- template<typename InputIterator >
   DiscreteDistribution (InputIterator first, InputIterator last)
- Discrete Distribution (std::initializer\_list< double > weights)
- Discrete Distribution (std::vector< double > weights)
- std::size\_t sample ()
- std::vector< double > probabilities () const

### **Protected Attributes**

```
std::discrete_distributionstd::size_t > _d
```

### 6.1.1 Constructor & Destructor Documentation

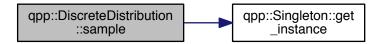
- 6.1.1.1 template < typename InputIterator > qpp::DiscreteDistribution::DiscreteDistribution ( InputIterator first, InputIterator last ) [inline]
- **6.1.1.2** qpp::DiscreteDistribution::DiscreteDistribution ( std::initializer\_list< double > weights ) [inline]
- 6.1.1.3 qpp::DiscreteDistribution::DiscreteDistribution ( std::vector< double > weights ) [inline]

### 6.1.2 Member Function Documentation

**6.1.2.1** std::vector<double> qpp::DiscreteDistribution::probabilities ( ) const [inline]

6.1.2.2 std::size\_t qpp::DiscreteDistribution::sample() [inline]

Here is the call graph for this function:



### 6.1.3 Member Data Documentation

**6.1.3.1 std::discrete\_distribution<std::size\_t> qpp::DiscreteDistribution::\_d** [protected]

The documentation for this class was generated from the following file:

· include/classes/stat.h

## 6.2 qpp::DiscreteDistributionAbsSquare Class Reference

#include <stat.h>

### **Public Member Functions**

- template<typename InputIterator >
   DiscreteDistributionAbsSquare (InputIterator first, InputIterator last)
- DiscreteDistributionAbsSquare (std::initializer\_list< types::cplx > amplitudes)
- DiscreteDistributionAbsSquare (std::vector< types::cplx > amplitudes)
- template<typename Derived >
   DiscreteDistributionAbsSquare (const Eigen::MatrixBase< Derived > &V)
- std::size\_t sample ()
- std::vector< double > probabilities () const

### **Protected Member Functions**

template<typename InputIterator >
 std::vector< double > cplx2weights (InputIterator first, InputIterator last) const

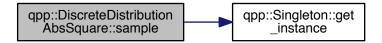
### **Protected Attributes**

std::discrete\_distributionstd::size\_t > \_d

### 6.2.1 Constructor & Destructor Documentation

- 6.2.1.1 template<typename InputIterator > qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare (InputIterator *first*, InputIterator *last* ) [inline]
- 6.2.1.2 qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare ( std::initializer\_list< types::cplx > amplitudes ) [inline]
- $\textbf{6.2.1.3} \quad \textbf{qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare ( \ \textbf{std::vector} < \textbf{types::cplx} > \textit{amplitudes} \ \textbf{)} \\ [\texttt{inline}]$
- 6.2.1.4 template<typename Derived > qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare ( const Eigen::MatrixBase< Derived > & V ) [inline]
- 6.2.2 Member Function Documentation
- 6.2.2.1 template<typename InputIterator > std::vector<double> qpp::DiscreteDistributionAbsSquare::cplx2weights ( InputIterator first, InputIterator last ) const [inline], [protected]
- **6.2.2.2** std::vector<double> qpp::DiscreteDistributionAbsSquare::probabilities ( ) const [inline]
- **6.2.2.3** std::size\_t qpp::DiscreteDistributionAbsSquare::sample() [inline]

Here is the call graph for this function:



### 6.2.3 Member Data Documentation

**6.2.3.1** std::discrete\_distribution<std::size\_t> qpp::DiscreteDistributionAbsSquare::\_d [protected]

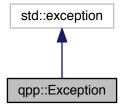
The documentation for this class was generated from the following file:

• include/classes/stat.h

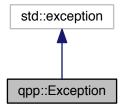
### 6.3 qpp::Exception Class Reference

#include <exception.h>

Inheritance diagram for qpp::Exception:



Collaboration diagram for qpp::Exception:



### **Public Types**

• enum Type {

Type::UNKNOWN\_EXCEPTION = 1, Type::ZERO\_SIZE, Type::MATRIX\_NOT\_SQUARE, Type::MATRIX\_← NOT\_CVECTOR,

Type::MATRIX\_NOT\_RVECTOR, Type::MATRIX\_NOT\_VECTOR, Type::MATRIX\_NOT\_SQUARE\_OR\_C↔ VECTOR, Type::MATRIX\_NOT\_SQUARE\_OR\_RVECTOR,

Type::MATRIX\_NOT\_SQUARE\_OR\_VECTOR, Type::DIMS\_INVALID, Type::DIMS\_NOT\_EQUAL, Type::D↔ IMS\_MISMATCH\_MATRIX,

 $\label{type::DIMS_MISMATCH_CVECTOR} Type::DIMS\_MISMATCH\_RVECTOR, Type::DIMS\_MISMATCH\_VE \leftarrow CTOR, Type::SUBSYS\_MISMATCH\_DIMS,$ 

Type::PERM\_INVALID, Type::NOT\_QUBIT\_GATE, Type::NOT\_QUBIT\_SUBSYS, Type::NOT\_BIPARTITE, Type::OUT\_OF\_RANGE, Type::TYPE\_MISMATCH, Type::UNDEFINED\_TYPE, Type::CUSTOM\_EXCEPT → ION }

### **Public Member Functions**

- Exception (const std::string &where, const Type &type)
- Exception (const std::string &where, const std::string &custom)
- virtual const char \* what () const noexceptoverride

### **Private Member Functions**

• std::string \_construct\_exception\_msg ()

### **Private Attributes**

- std::string \_where
- std::string \_msg
- Type \_type
- std::string \_custom

### 6.3.1 Member Enumeration Documentation

**6.3.1.1 enum qpp::Exception::Type** [strong]

### **Enumerator**

UNKNOWN\_EXCEPTION

ZERO\_SIZE

MATRIX\_NOT\_SQUARE

MATRIX\_NOT\_CVECTOR

MATRIX\_NOT\_RVECTOR

MATRIX\_NOT\_VECTOR

MATRIX\_NOT\_SQUARE\_OR\_CVECTOR

MATRIX\_NOT\_SQUARE\_OR\_RVECTOR

MATRIX\_NOT\_SQUARE\_OR\_VECTOR

DIMS\_INVALID

DIMS\_NOT\_EQUAL

DIMS\_MISMATCH\_MATRIX

DIMS\_MISMATCH\_CVECTOR

DIMS\_MISMATCH\_RVECTOR

DIMS\_MISMATCH\_VECTOR

SUBSYS\_MISMATCH\_DIMS

PERM\_INVALID

NOT\_QUBIT\_GATE

NOT\_QUBIT\_SUBSYS

NOT\_BIPARTITE

OUT\_OF\_RANGE

TYPE\_MISMATCH

UNDEFINED\_TYPE

CUSTOM\_EXCEPTION

### 6.3.2 Constructor & Destructor Documentation

6.3.2.1 qpp::Exception::Exception ( const std::string & where, const Type & type ) [inline]

Here is the call graph for this function:



6.3.2.2 qpp::Exception::Exception ( const std::string & where, const std::string & custom ) [inline]

Here is the call graph for this function:



### 6.3.3 Member Function Documentation

- **6.3.3.1** std::string qpp::Exception::\_construct\_exception\_msg( ) [inline], [private]
- **6.3.3.2 virtual const char\* qpp::Exception::what ( ) const** [inline], [override], [virtual], [noexcept]
- 6.3.4 Member Data Documentation
- **6.3.4.1 std::string qpp::Exception::\_custom** [private]
- **6.3.4.2 std::string qpp::Exception::\_msg** [private]
- **6.3.4.3 Type qpp::Exception::\_type** [private]
- **6.3.4.4 std::string qpp::Exception::\_where** [private]

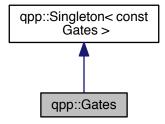
The documentation for this class was generated from the following file:

• include/classes/exception.h

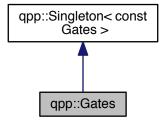
## 6.4 qpp::Gates Class Reference

#include <gates.h>

Inheritance diagram for qpp::Gates:



Collaboration diagram for qpp::Gates:



### **Public Member Functions**

- types::cmat Rn (double theta, std::vector< double > n) const
- types::cmat Zd (std::size\_t D) const
- types::cmat Fd (std::size\_t D) const
- types::cmat Xd (std::size\_t D) const
- template<typename Derived = Eigen::MatrixXcd>
   Derived Id (std::Size\_t D) const
- template<typename Derived1 , typename Derived2 >

types::DynMat< typename

Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size\_t > &ctrl, const std::vector< std::size\_t > &subsys, std::size\_t n, std::size\_t d=2) const

• template<typename Derived1 , typename Derived2 >

types::DynMat< typename

 $\label{lem:decomposition} Derived 1 :: Scalar > \underset{\mbox{\sc onst Eigen::MatrixBase} < \mbox{\sc Derived 1} > \underset{\mbox{\sc onst Eigen::MatrixBase} < \mbox{\sc Derived 2} > \underset{\mbox{\sc onst std::vector} < \mbox{\sc std::size\_t} > \underset{\mbox{\sc onst std::vector} < \mbox{\sc std::size\_t} > \underset{\mbox{\sc onst Std::vector} < \mbox{\sc onst std::vector} < \mbox{\sc onst std::vector} > \underset{\mbox{\sc onst Std::vector} < \mbox{\sc onst std::vector} < \mbox{\sc onst std::vector} > \underset{\mbox{\sc onst Std::vector} < \mbox{\sc onst std::vector} < \mbox{\sc onst std::vector} > \underset{\mbox{\sc onst Std::vector} < \mbox{\sc onst std::vector} < \mbox{\sc onst std::vector} > \underset{\mbox{\sc onst Std::vector$ 

 $\bullet \ \ \text{template}{<} \text{typename Derived} >$ 

types::DynMat< typename

 $\label{lem:decomposition} Derived::Scalar > CTRL \ (const \ Eigen::MatrixBase < Derived > \&A, \ const \ std::vector < std::size_t > \&ctrl, \ const \ std::vector < std::size_t > \&subsys, \ std::size_t \ n, \ std::size_t \ d=2) \ const$ 

### **Public Attributes**

```
types::cmat Id2 { types::cmat::Identity(2, 2) }
types::cmat H { types::cmat::Zero(2, 2) }
types::cmat X { types::cmat::Zero(2, 2) }
types::cmat Y { types::cmat::Zero(2, 2) }
types::cmat Z { types::cmat::Zero(2, 2) }
types::cmat S { types::cmat::Zero(2, 2) }
types::cmat T { types::cmat::Zero(2, 2) }
types::cmat CNOTab { types::cmat::Identity(4, 4) }
types::cmat CNOTba { types::cmat::Zero(4, 4) }
types::cmat SWAP { types::cmat::Identity(4, 4) }
types::cmat TOF { types::cmat::Identity(8, 8) }
types::cmat FRED { types::cmat::Identity(8, 8) }
```

### **Private Member Functions**

• Gates ()

### **Friends**

class Singleton < const Gates >

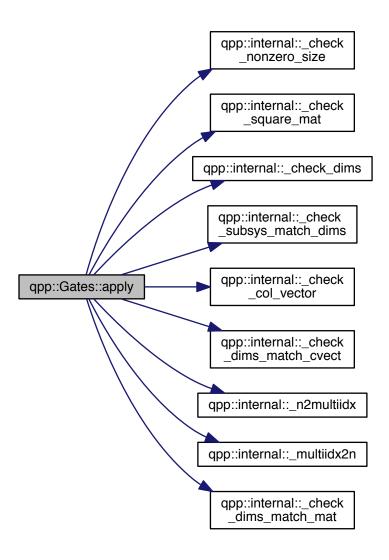
### **Additional Inherited Members**

### 6.4.1 Constructor & Destructor Documentation

```
6.4.1.1 qpp::Gates::Gates() [inline], [private]
```

### 6.4.2 Member Function Documentation

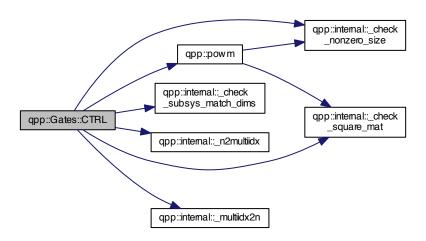
Here is the call graph for this function:



6.4.2.2 template < typename Derived1 , typename Derived2 > types::DynMat < typename Derived1::Scalar > qpp::Gates::applyCTRL ( const Eigen::MatrixBase < Derived1 > & state, const Eigen::MatrixBase < Derived2 > & A, const std::vector < std::size\_t > & subsys, std::size\_t n, std::size\_t d = 2 ) const [inline]

6.4.2.3 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::Gates::CTRL ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & ctrl, const std::vector< std::size\_t > & subsys, std::size\_t n, std::size\_t d = 2 ) const [inline]

Here is the call graph for this function:



6.4.2.4 types::cmat qpp::Gates::Fd ( std::size\_t D ) const [inline]

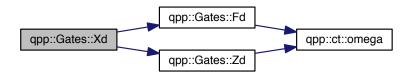
Here is the call graph for this function:



- 6.4.2.5 template<typename Derived = Eigen::MatrixXcd> Derived qpp::Gates::Id ( std::size\_t D ) const [inline]
- 6.4.2.6 types::cmat qpp::Gates::Rn ( double theta, std::vector < double > n ) const [inline]

6.4.2.7 types::cmat qpp::Gates::Xd ( std::size\_t D ) const [inline]

Here is the call graph for this function:



6.4.2.8 types::cmat qpp::Gates::Zd(std::size\_t D) const [inline]

Here is the call graph for this function:



- 6.4.3 Friends And Related Function Documentation
- **6.4.3.1 friend class Singleton**< const Gates > [friend]
- 6.4.4 Member Data Documentation
- 6.4.4.1 types::cmat qpp::Gates::CNOTab { types::cmat::Identity(4, 4) }
- 6.4.4.2 types::cmat qpp::Gates::CNOTba { types::cmat::Zero(4, 4) }
- 6.4.4.3 types::cmat qpp::Gates::CZ { types::cmat::Identity(4, 4) }
- 6.4.4.4 types::cmat qpp::Gates::FRED { types::cmat::Identity(8, 8) }
- 6.4.4.5 types::cmat qpp::Gates::H { types::cmat::Zero(2, 2) }
- 6.4.4.6 types::cmat qpp::Gates::ld2 { types::cmat::ldentity(2, 2) }
- 6.4.4.7 types::cmat qpp::Gates::S { types::cmat::Zero(2, 2) }
- 6.4.4.8 types::cmat qpp::Gates::SWAP { types::cmat::Identity(4, 4) }
- 6.4.4.9 types::cmat qpp::Gates::T { types::cmat::Zero(2, 2) }

```
6.4.4.10 types::cmat qpp::Gates::TOF { types::cmat::Identity(8, 8) }
6.4.4.11 types::cmat qpp::Gates::X { types::cmat::Zero(2, 2) }
6.4.4.12 types::cmat qpp::Gates::Y { types::cmat::Zero(2, 2) }
6.4.4.13 types::cmat qpp::Gates::Z { types::cmat::Zero(2, 2) }
```

The documentation for this class was generated from the following file:

• include/classes/gates.h

## 6.5 qpp::NormalDistribution Class Reference

```
#include <stat.h>
```

### **Public Member Functions**

- NormalDistribution (double mean=0, double sigma=1)
- double sample ()

### **Protected Attributes**

· std::normal\_distribution\_d

### 6.5.1 Constructor & Destructor Documentation

6.5.1.1 qpp::NormalDistribution::NormalDistribution ( double mean = 0, double sigma = 1 ) [inline]

### 6.5.2 Member Function Documentation

**6.5.2.1** double qpp::NormalDistribution::sample() [inline]

Here is the call graph for this function:



### 6.5.3 Member Data Documentation

**6.5.3.1** std::normal\_distribution qpp::NormalDistribution::\_d [protected]

The documentation for this class was generated from the following file:

• include/classes/stat.h

## 6.6 qpp::Qudit Class Reference

```
#include <qudit.h>
```

### **Public Member Functions**

- Qudit (const types::cmat &rho=States::get\_instance().pz0)
- std::size\_t measure (const types::cmat &U, bool destructive=false)
- std::size\_t measure (bool destructive=false)
- types::cmat getRho () const
- std::size\_t getD () const

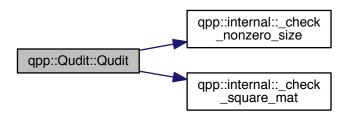
### **Private Attributes**

- · types::cmat \_rho
- std::size\_t \_D

### 6.6.1 Constructor & Destructor Documentation

6.6.1.1 qpp::Qudit::Qudit ( const types::cmat & rho = States::get\_instance() .pz0 ) [inline]

Here is the call graph for this function:

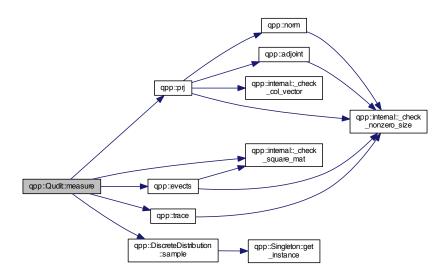


### 6.6.2 Member Function Documentation

- 6.6.2.1 std::size\_t qpp::Qudit::getD() const [inline]
- 6.6.2.2 types::cmat qpp::Qudit::getRho() const [inline]

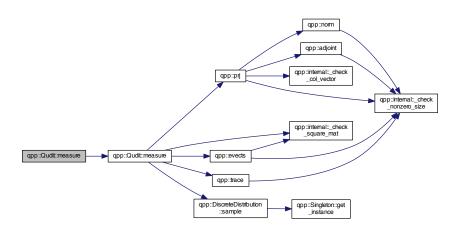
6.6.2.3 std::size\_t qpp::Qudit::measure ( const types::cmat & U, bool destructive = false ) [inline]

Here is the call graph for this function:



6.6.2.4 std::size\_t qpp::Qudit::measure ( bool destructive = false ) [inline]

Here is the call graph for this function:



### 6.6.3 Member Data Documentation

6.6.3.1 std::size\_t qpp::Qudit::\_D [private]

**6.6.3.2 types::cmat qpp::Qudit::\_rho** [private]

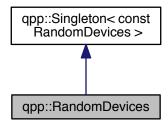
The documentation for this class was generated from the following file:

• include/classes/qudit.h

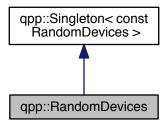
## 6.7 qpp::RandomDevices Class Reference

#include <randevs.h>

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



### **Public Attributes**

- std::random\_device \_rd
- std::mt19937 \_rng

### **Private Member Functions**

• RandomDevices ()

### **Friends**

class Singleton < const RandomDevices >

### **Additional Inherited Members**

### 6.7.1 Constructor & Destructor Documentation

- **6.7.1.1 qpp::RandomDevices::RandomDevices()** [inline], [private]
- 6.7.2 Friends And Related Function Documentation
- **6.7.2.1 friend class Singleton** < **const RandomDevices** > [friend]
- 6.7.3 Member Data Documentation
- 6.7.3.1 std::random\_device qpp::RandomDevices::\_rd
- **6.7.3.2** std::mt19937 qpp::RandomDevices::\_rng [mutable]

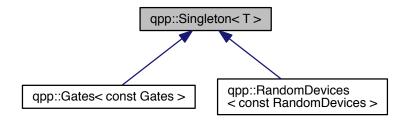
The documentation for this class was generated from the following file:

• include/classes/randevs.h

## 6.8 qpp::Singleton < T > Class Template Reference

#include <singleton.h>

Inheritance diagram for qpp::Singleton < T >:



### **Static Public Member Functions**

static T & get\_instance ()

### **Protected Member Functions**

- Singleton ()=default
- virtual ∼Singleton ()
- Singleton (const Singleton &)=delete
- Singleton & operator= (const Singleton &)=delete

### 6.8.1 Constructor & Destructor Documentation

**6.8.1.1** template<typename T> qpp::Singleton<T>::Singleton( ) [protected], [default]

- 6.8.1.2 template<typename T> virtual qpp::Singleton< T>:: $\sim$ Singleton( ) [inline], [protected], [virtual]
- 6.8.2 Member Function Documentation
- 6.8.2.1 template<typename T> static T& qpp::Singleton< T>::get\_instance( ) [inline], [static]
- 6.8.2.2 template<typename T> Singleton& qpp::Singleton< T>::operator= ( const Singleton< T> & ) [protected], [delete]

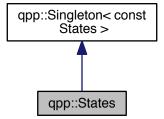
The documentation for this class was generated from the following file:

• include/classes/singleton.h

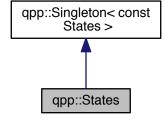
## 6.9 qpp::States Class Reference

#include <states.h>

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



### **Public Attributes**

```
types::ket x0 { types::ket::Zero(2) }
types::ket x1 { types::ket::Zero(2) }
types::ket y0 { types::ket::Zero(2) }
types::ket y1 { types::ket::Zero(2) }
types::ket z0 { types::ket::Zero(2) }
types::ket z1 { types::ket::Zero(2) }
types::cmat px0 { types::cmat::Zero(2, 2) }
types::cmat px1 { types::cmat::Zero(2, 2) }
types::cmat py0 { types::cmat::Zero(2, 2) }
types::cmat py1 { types::cmat::Zero(2, 2) }
types::cmat pz0 { types::cmat::Zero(2, 2) }
types::cmat pz1 { types::cmat::Zero(2, 2) }
types::ket b00 { types::ket::Zero(4) }
types::ket b01 { types::ket::Zero(4) }
types::ket b10 { types::ket::Zero(4) }
types::ket b11 { types::ket::Zero(4) }
types::cmat pb00 { types::cmat::Zero(4, 4) }
types::cmat pb01 { types::cmat::Zero(4, 4) }
types::cmat pb10 { types::cmat::Zero(4, 4) }
types::cmat pb11 { types::cmat::Zero(4, 4) }
types::ket GHZ { types::ket::Zero(8) }
types::ket W { types::ket::Zero(8) }
types::cmat pGHZ { types::cmat::Zero(8, 8) }
types::cmat pW { types::cmat::Zero(8, 8) }
```

### **Private Member Functions**

• States ()

### **Friends**

class Singleton < const States >

### **Additional Inherited Members**

```
6.9.1 Constructor & Destructor Documentation
6.9.1.1 qpp::States::States() [inline], [private]
6.9.2 Friends And Related Function Documentation
6.9.2.1 friend class Singleton < const States > [friend]
6.9.3 Member Data Documentation
6.9.3.1 types::ket qpp::States::b00 { types::ket::Zero(4) }
6.9.3.2 types::ket qpp::States::b01 { types::ket::Zero(4) }
6.9.3.3 types::ket qpp::States::b10 { types::ket::Zero(4) }
```

```
6.9.3.4 types::ket qpp::States::b11 { types::ket::Zero(4) }
6.9.3.5 types::ket qpp::States::GHZ { types::ket::Zero(8) }
6.9.3.6 types::cmat qpp::States::pb00 { types::cmat::Zero(4, 4) }
6.9.3.7 types::cmat qpp::States::pb01 { types::cmat::Zero(4, 4) }
6.9.3.8
        types::cmat qpp::States::pb10 { types::cmat::Zero(4, 4) }
6.9.3.9 types::cmat qpp::States::pb11 { types::cmat::Zero(4, 4) }
6.9.3.10 types::cmat qpp::States::pGHZ { types::cmat::Zero(8, 8) }
6.9.3.11 types::cmat qpp::States::pW { types::cmat::Zero(8, 8) }
6.9.3.12 types::cmat qpp::States::px0 { types::cmat::Zero(2, 2) }
6.9.3.13 types::cmat qpp::States::px1 { types::cmat::Zero(2, 2) }
6.9.3.14 types::cmat qpp::States::py0 { types::cmat::Zero(2, 2) }
6.9.3.15 types::cmat qpp::States::py1 { types::cmat::Zero(2, 2) }
6.9.3.16 types::cmat qpp::States::pz0 { types::cmat::Zero(2, 2) }
6.9.3.17 types::cmat qpp::States::pz1 { types::cmat::Zero(2, 2) }
6.9.3.18 types::ket qpp::States::W { types::ket::Zero(8) }
6.9.3.19 types::ket qpp::States::x0 { types::ket::Zero(2) }
6.9.3.20 types::ket qpp::States::x1 { types::ket::Zero(2) }
6.9.3.21 types::ket qpp::States::y0 { types::ket::Zero(2) }
6.9.3.22 types::ket qpp::States::y1 { types::ket::Zero(2) }
6.9.3.23 types::ket qpp::States::z0 { types::ket::Zero(2) }
6.9.3.24 types::ket qpp::States::z1 { types::ket::Zero(2) }
```

The documentation for this class was generated from the following file:

• include/classes/states.h

## 6.10 qpp::Timer Class Reference

```
#include <timer.h>
```

### **Public Member Functions**

- Timer ()
- void tic ()

- void toc ()
- double seconds () const

### **Protected Attributes**

- std::chrono::steady clock::time point start
- std::chrono::steady\_clock::time\_point \_end

### **Friends**

• std::ostream & operator<< (std::ostream &os, const Timer &rhs)

### 6.10.1 Constructor & Destructor Documentation

```
6.10.1.1 qpp::Timer::Timer( ) [inline]
```

### 6.10.2 Member Function Documentation

```
6.10.2.1 double qpp::Timer::seconds ( ) const [inline]
```

```
6.10.2.2 void qpp::Timer::tic( ) [inline]
```

6.10.2.3 void qpp::Timer::toc( ) [inline]

### 6.10.3 Friends And Related Function Documentation

```
6.10.3.1 std::ostream & os, const Timer & rhs ) [friend]
```

### 6.10.4 Member Data Documentation

```
6.10.4.1 std::chrono::steady_clock::time_point qpp::Timer::_end [protected]
```

```
6.10.4.2 std::chrono::steady_clock::time_point qpp::Timer::_start [protected]
```

The documentation for this class was generated from the following file:

• include/classes/timer.h

## 6.11 qpp::UniformIntDistribution Class Reference

```
#include <stat.h>
```

### **Public Member Functions**

- UniformIntDistribution (int a=0, int b=1)
- int sample ()

## **Protected Attributes**

std::uniform\_int\_distribution \_d

### 6.11.1 Constructor & Destructor Documentation

**6.11.1.1** qpp::UniformIntDistribution::UniformIntDistribution (int a = 0, int b = 1) [inline]

### 6.11.2 Member Function Documentation

**6.11.2.1** int qpp::UniformIntDistribution::sample() [inline]

Here is the call graph for this function:



### 6.11.3 Member Data Documentation

**6.11.3.1 std::uniform\_int\_distribution qpp::UniformIntDistribution::\_d** [protected]

The documentation for this class was generated from the following file:

• include/classes/stat.h

## 6.12 qpp::UniformRealDistribution Class Reference

```
#include <stat.h>
```

### **Public Member Functions**

- UniformRealDistribution (double a=0, double b=1)
- double sample ()

### **Protected Attributes**

std::uniform\_real\_distribution\_d

### 6.12.1 Constructor & Destructor Documentation

**6.12.1.1** qpp::UniformRealDistribution::UniformRealDistribution ( double a = 0, double b = 1 ) [inline]

### 6.12.2 Member Function Documentation

**6.12.2.1** double qpp::UniformRealDistribution::sample ( ) [inline]

Here is the call graph for this function:



### 6.12.3 Member Data Documentation

**6.12.3.1** std::uniform\_real\_distribution qpp::UniformRealDistribution::\_d [protected]

The documentation for this class was generated from the following file:

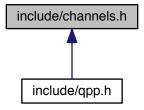
• include/classes/stat.h

## **Chapter 7**

## **File Documentation**

## 7.1 include/channels.h File Reference

This graph shows which files directly or indirectly include this file:



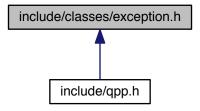
### **Namespaces**

qpp

- types::cmat qpp::super (const std::vector< types::cmat > &Ks)
- types::cmat qpp::choi (const std::vector< types::cmat > &Ks)
- std::vector< types::cmat > qpp::choi2kraus (const types::cmat &A)
- template<typename Derived >
   types::cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< types::cmat > &Ks)
- template<typename Derived >
   types::cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< types::cmat > &Ks,
   const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)

## 7.2 include/classes/exception.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

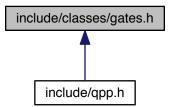
· class qpp::Exception

## **Namespaces**

• qpp

## 7.3 include/classes/gates.h File Reference

This graph shows which files directly or indirectly include this file:



## Classes

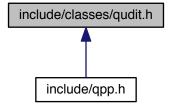
class qpp::Gates

### **Namespaces**

qpp

## 7.4 include/classes/qudit.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

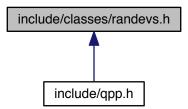
· class qpp::Qudit

## **Namespaces**

• qpp

## 7.5 include/classes/randevs.h File Reference

This graph shows which files directly or indirectly include this file:



## Classes

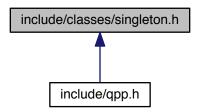
• class qpp::RandomDevices

## Namespaces

qpp

## 7.6 include/classes/singleton.h File Reference

This graph shows which files directly or indirectly include this file:



### **Classes**

class qpp::Singleton< T >

### **Namespaces**

qpp

### Macros

- #define CLASS\_SINGLETON(Foo)
- #define CLASS\_CONST\_SINGLETON(Foo)

### 7.6.1 Macro Definition Documentation

## 7.6.1.1 #define CLASS\_CONST\_SINGLETON( Foo )

### Value:

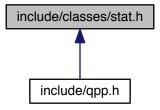
```
class Foo: public Singleton<const Foo>\
{\
          friend class Singleton<const Foo>;
```

### 7.6.1.2 #define CLASS\_SINGLETON( Foo )

### Value:

## 7.7 include/classes/stat.h File Reference

This graph shows which files directly or indirectly include this file:



### **Classes**

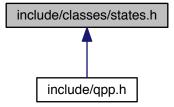
- class qpp::NormalDistribution
- class qpp::UniformRealDistribution
- class qpp::UniformIntDistribution
- class qpp::DiscreteDistribution
- class qpp::DiscreteDistributionAbsSquare

### **Namespaces**

qpp

## 7.8 include/classes/states.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

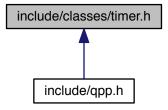
• class qpp::States

## **Namespaces**

• qpp

## 7.9 include/classes/timer.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

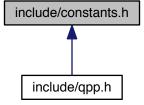
• class qpp::Timer

## **Namespaces**

qpp

## 7.10 include/constants.h File Reference

This graph shows which files directly or indirectly include this file:



## **Namespaces**

qpp

· qpp::ct

### **Functions**

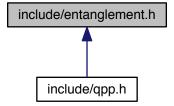
- constexpr std::complex< double > qpp::operator""\_i (unsigned long long int x)
- constexpr std::complex< double > qpp::operator""\_i (long double x)
- std::complex < double > qpp::ct::omega (std::size\_t D)

### **Variables**

- constexpr double qpp::ct::chop = 1e-10
- constexpr double <a href="mailto:qpp::ct::eps">qpp::ct::eps</a> = 1e-12
- constexpr std::size t qpp::ct::maxn = 64
- constexpr double qpp::ct::pi = 3.141592653589793238462643383279502884
- constexpr double <a href="mailto:qpp::ct::ee">qpp::ct::ee</a> = 2.718281828459045235360287471352662497

## 7.11 include/entanglement.h File Reference

This graph shows which files directly or indirectly include this file:



### **Namespaces**

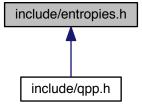
• qpp

- template<typename Derived >
   types::cmat qpp::schmidtcoeff (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t >
   &dims)
- template<typename Derived >
   types::cmat qpp::schmidtU (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- template<typename Derived >
   types::cmat qpp::schmidtV (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- template<typename Derived >
   types::cmat qpp::schmidtprob (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t >
   &dims)
- template<typename Derived >
   double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)

 template<typename Derived > double qpp::gconcurrence (const Eigen::MatrixBase< Derived > &A)

## 7.12 include/entropies.h File Reference

This graph shows which files directly or indirectly include this file:



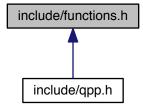
## **Namespaces**

qpp

- template<typename Derived >
   double qpp::shannon (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   double qpp::renyi (const double alpha, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   double qpp::renyi\_inf (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   double qpp::tsallis (const double alpha, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &subsys,
   const std::vector< std::size\_t > &dims)

### 7.13 include/functions.h File Reference

This graph shows which files directly or indirectly include this file:



### **Namespaces**

• qpp

```
    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > qpp::transpose (const Eigen::MatrixBase < Derived > &A)
      Transpose.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::conjugate (const Eigen::MatrixBase < Derived > &A)
      Complex conjugate.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::adjoint (const Eigen::MatrixBase < Derived > &A)
      Adjoint.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::inverse (const Eigen::MatrixBase < Derived > &A)
      Inverse.
• template<typename Derived >
  Derived::Scalar <a href="mailto:qpp::trace">qpp::trace</a> (const Eigen::MatrixBase</a> Derived > &A)
• template<typename Derived >
  Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > &A)
      Determinant.
• template<typename Derived >
  Derived::Scalar <a href="mailto:qpp::logdet">qpp::logdet</a> (const Eigen::MatrixBase</a> Derived > &A)
      Logarithm of the determinant.

    template<typename Derived >

  Derived::Scalar <a href="mailto:qpp::sum">qpp::sum</a> (const Eigen::MatrixBase</a> Derived > &A)
      Element-wise sum.
```

```
• template<typename Derived >
  double qpp::norm (const Eigen::MatrixBase< Derived > &A)
      Trace norm.

    template<typename Derived >

  types::cmat qpp::evals (const Eigen::MatrixBase< Derived > &A)
     Eigenvalues.

    template<typename Derived >

  types::cmat qpp::evects (const Eigen::MatrixBase< Derived > &A)
      Eigenvectors.

    template<typename Derived >

  types::dmat qpp::hevals (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvalues.

    template<typename Derived >

  types::cmat qpp::hevects (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvectors.
• template<typename Derived >
  types::cmat qpp::funm (const Eigen::MatrixBase< Derived > &A, types::cplx(*f)(const types::cplx &))
     Functional calculus f(A)

    template<typename Derived >

  types::cmat qpp::sqrtm (const Eigen::MatrixBase< Derived > &A)
     Matrix square root.

    template<typename Derived >

  types::cmat qpp::absm (const Eigen::MatrixBase< Derived > &A)
     Matrix absolut value.

    template<typename Derived >

  types::cmat qpp::expm (const Eigen::MatrixBase< Derived > &A)
     Matrix exponential.

    template<typename Derived >

  types::cmat <a href="mailto:qpp::logm">qpp::logm</a> (const Eigen::MatrixBase</a> Derived > &A)
     Matrix logarithm.

    template<typename Derived >

  types::cmat qpp::sinm (const Eigen::MatrixBase< Derived > &A)
     Matrix sin.

    template<typename Derived >

  types::cmat qpp::cosm (const Eigen::MatrixBase< Derived > &A)
     Matrix cos.

    template<typename Derived >

  types::cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived > &A, const types::cplx z)
     Matrix power.
\bullet \ \ \text{template}{<} \text{typename Derived} >
  types::DynMat< typename
  Derived::Scalar > qpp::powm (const Eigen::MatrixBase< Derived > &A, std::size t n)
     Matrix power.

    template<typename OutputScalar , typename Derived >

  types::DynMat< OutputScalar > qpp::cwise (const Eigen::MatrixBase< Derived > &A, Output↔
  Scalar(*f)(const typename Derived::Scalar &))
     Functor.
template<typename T >
  types::DynMat< typename T::Scalar > qpp::kron (const T &head)
     Kronecker product (variadic overload)
template<typename T, typename... Args>
  types::DynMat< typename T::Scalar > qpp::kron (const T &head, const Args &...tail)
     Kronecker product (variadic overload)
```

```
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::kron (const std::vector< Derived > &As)
     Kronecker product (std::vector overload)

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > qpp::kron (const std::initializer_list< Derived > &As)
     Kronecker product (std::initializer_list overload)
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::kronpow (const Eigen::MatrixBase< Derived > &A, std::size t n)
     Kronecker power.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::reshape (const Eigen::MatrixBase < Derived > &A, std::size_t rows, std::size_t cols)
     Reshape.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t
  > &perm, const std::vector< std::size t > &dims)
     System permutation.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t >
  &dims)
     Partial trace.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t >
  &dims)
     Partial trace.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t >
  &subsys, const std::vector< std::size_t > &dims)
     Partial trace.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t
  > &subsys, const std::vector< std::size_t > &dims)
     Partial transpose.
• template<typename Derived1 , typename Derived2 >
  types::DynMat< typename
  Derived1::Scalar > qpp::comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< De-
  rived2 > &B)
     Commutator.
• template<typename Derived1 , typename Derived2 >
  types::DynMat< typename
  Derived1::Scalar > qpp::anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase<
  Derived 2 > B
     Anti-commutator.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > qpp::prj (const Eigen::MatrixBase< Derived > &V)
     Projector.
```

• template<typename Derived > types::DynMat< typename Derived::Scalar > qpp::expandout (const Eigen::MatrixBase< Derived > &A, std::size\_t pos, const std↔ ::vector< std::size\_t > &dims) Expand out. • template<typename Derived > types::DynMat< typename Derived::Scalar > qpp::grams (const std::vector< Derived > &Vs) Gram-Schmidt orthogonalization (std::vector overload) • template<typename Derived > types::DynMat< typename Derived::Scalar > qpp::grams (const std::initializer\_list< Derived > &Vs) Gram-Schmidt orthogonalization (std::initializer\_list overload) • template<typename Derived > types::DynMat< typename Derived::Scalar > qpp::grams (const Eigen::MatrixBase < Derived > &A) Gram-Schmidt orthogonalization (Eigen expression (matrix) overload) std::vector< std::size\_t > qpp::n2multiidx (std::size\_t n, const std::vector< std::size\_t > &dims) Non-negative integer index to multi-index.

std::size\_t qpp::multiidx2n (const std::vector < std::size\_t > &midx, const std::vector < std::size\_t > &dims)
 Multi-index to non-negative integer index.

types::ket qpp::mket (const std::vector< std::size\_t > &mask)

Multi-partite qubit ket.

types::ket qpp::mket (const std::vector < std::size\_t > &mask, const std::vector < std::size\_t > &dims)

Multi-partite qudit ket (different dimensions overload)

types::ket qpp::mket (const std::vector< std::size\_t > &mask, std::size\_t d)

Multi-partite qudit ket (same dimensions overload)

std::vector< std::size\_t > qpp::invperm (const std::vector< std::size\_t > &perm)

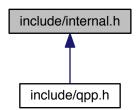
Inverse permutation.

std::vector< std::size\_t > app::compperm (const std::vector< std::size\_t > aperm, const std::vector< std::size\_t

Compose permutations.

### 7.14 include/internal.h File Reference

This graph shows which files directly or indirectly include this file:



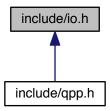
### **Namespaces**

- qpp
- · qpp::internal

- void qpp::internal:: n2multiidx (std::size t n, std::size t numdims, const std::size t \*dims, std::size t \*result)
- std::size\_t app::internal::\_multiidx2n (const std::size\_t \*midx, std::size\_t numdims, const std::size\_t \*dims)
- template<typename Derived >
   bool qpp::internal::\_check\_square\_mat (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_row\_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_col\_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename T >
   bool qpp::internal::\_check\_nonzero\_size (const T &x)
- bool qpp::internal::\_check\_dims (const std::vector< std::size\_t > &dims)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_mat (const std::vector< std::size\_t > &dims, const Eigen::Matrix
   Base< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_cvect (const std::vector< std::size\_t > &dims, const Eigen::Matrix
   Base< Derived > &V)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_rvect (const std::vector< std::size\_t > &dims, const Eigen::Matrix
   Base< Derived > &V)
- bool qpp::internal::\_check\_eq\_dims (const std::vector < std::size\_t > &dims, std::size\_t dim)
- bool qpp::internal::\_check\_subsys\_match\_dims (const std::vector< std::size\_t > &subsys, const std
   ::vector< std::size\_t > &dims)
- bool qpp::internal::\_check\_perm (const std::vector< std::size\_t > &perm)
- template<typename Derived1 , typename Derived2 >
   types::DynMat< typename
   Derived1::Scalar > qpp::internal::\_kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::Matrix
   Base< Derived2 > &B)
- template<typename T >
   void qpp::internal::variadic\_vector\_emplace (std::vector< T > &)
- template<typename T, typename First, typename... Args>
   void qpp::internal::variadic\_vector\_emplace (std::vector< T > &v, First &&first, Args &&...args)

### 7.15 include/io.h File Reference

This graph shows which files directly or indirectly include this file:



### **Namespaces**

• qpp

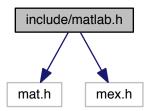
### **Functions**

- template<typename T >
   void qpp::disp (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]",
   std::ostream &os=std::cout)
- template<typename T >
   void qpp::displn (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)
- template<typename T >
   void qpp::disp (const T \*x, const std::size\_t n, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)
- template<typename T >
   void qpp::displn (const T \*x, const std::size\_t n, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)
- template<typename Derived >
   void qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=ct::chop, std::ostream &os=std::cout)
- template<typename Derived >
   void qpp::displn (const Eigen::MatrixBase< Derived > &A, double chop=ct::chop, std::ostream &os=std
   ::cout)
- void qpp::disp (const types::cplx c, double chop=ct::chop, std::ostream &os=std::cout)
- void qpp::displn (const types::cplx c, double chop=ct::chop, std::ostream &os=std::cout)
- template<typename Derived > void qpp::save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)
   template
- template<typename Derived >
   types::DynMat< typename
   Derived::Scalar > qpp::load (const std::string &fname)

### 7.16 include/matlab.h File Reference

```
#include "mat.h"
#include "mex.h"
```

Include dependency graph for matlab.h:



### **Namespaces**

qpp

- template<typename Derived >
   Derived qpp::loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)
- template<>
   types::dmat qpp::loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)
- template<>
  types::cmat qpp::loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)
- template<typename Derived >
   void qpp::saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat\_file, const std::string &var name, const std::string &mode)
- template<>
   void qpp::saveMATLABmatrix (const Eigen::MatrixBase< types::dmat > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)
- template<>
   void qpp::saveMATLABmatrix (const Eigen::MatrixBase< typename types::cmat > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)

## 7.17 include/qpp.h File Reference

```
#include <algorithm>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <exception>
#include <fstream>
#include <functional>
#include <iomanip>
#include <iostream>
#include <iterator>
#include <numeric>
#include <ostream>
#include <random>
#include <stdexcept>
#include <string>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "constants.h"
#include "types.h"
#include "classes/exception.h"
#include "classes/singleton.h"
#include "classes/states.h"
#include "classes/randevs.h"
#include "internal.h"
#include "functions.h"
#include "classes/gates.h"
#include "classes/stat.h"
#include "entropies.h"
#include "entanglement.h"
#include "channels.h"
#include "io.h"
#include "random.h"
#include "classes/qudit.h"
#include "classes/timer.h"
Include dependency graph for qpp.h:
```

### **Namespaces**

• qpp

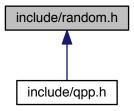
### **Variables**

const RandomDevices & qpp::rdevs = RandomDevices::get\_instance()

- const Gates & qpp::gt = Gates::get\_instance()
- const States & qpp::st = States::get\_instance()

### 7.18 include/random.h File Reference

This graph shows which files directly or indirectly include this file:



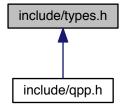
### **Namespaces**

qpp

- template<typename Derived >
   Derived qpp::rand (std::size\_t rows, std::size\_t cols, double a=0, double b=1)
- template<>
   types::dmat qpp::rand (std::size\_t rows, std::size\_t cols, double a, double b)
- template<>
  types::cmat qpp::rand (std::size\_t rows, std::size\_t cols, double a, double b)
- double qpp::rand (double a=0, double b=1)
- long long <a href="mailto:qpp::randint">qpp::randint</a> (long long a, long long b)
- template<typename Derived >
   Derived qpp::randn (std::size\_t rows, std::size\_t cols, double mean=0, double sigma=1)
- template<>
   types::dmat qpp::randn (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- template<>
   types::cmat qpp::randn (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- double <a href="mailto:qpp::randn">qpp::randn</a> (double mean=0, double sigma=1)
- types::cmat qpp::randU (std::size\_t D)
- types::cmat qpp::randV (std::size\_t Din, std::size\_t Dout)
- std::vector< types::cmat > qpp::randkraus (std::size\_t n, std::size\_t D)
- types::cmat qpp::randH (std::size\_t D)
- types::ket qpp::randket (std::size\_t D)
- types::cmat qpp::randrho (std::size\_t D)
- std::vector< std::size\_t > qpp::randperm (std::size\_t n)

## 7.19 include/types.h File Reference

This graph shows which files directly or indirectly include this file:



## **Namespaces**

- qpp
- qpp::types

## **Typedefs**

- using qpp::types::cplx = std::complex< double >
- using qpp::types::cmat = Eigen::MatrixXcd
- using qpp::types::dmat = Eigen::MatrixXd
- using qpp::types::ket = Eigen::Matrix< cplx, Eigen::Dynamic, 1 >
- using qpp::types::bra = Eigen::Matrix< cplx, 1, Eigen::Dynamic >
- template<typename Scalar >
   using qpp::types::DynMat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >

# Index

aham	ann 25
absm	qpp, 25
qpp, 14	expandout
adjoint	qpp, 25
qpp, 15	expm
anticomm	qpp, 26
qpp, 15	funm
OLIOTOM EVOERTION	
CUSTOM_EXCEPTION	qpp, 27
qpp::Exception, 67	aconcurrence
channel	gconcurrence qpp, 27
qpp, 16	
choi	grams
qpp, 17	qpp, 28, 29
choi2kraus	gt
qpp, 17	qpp, 59
comm	hevals
qpp, 18	
compperm	qpp, 29
qpp, 18	hevects
conjugate	qpp, 30
qpp, 20	invorce
cosm	inverse
qpp, 20	qpp, 30
cwise	invperm
qpp, 21	qpp, 31
	kron
DIMS_INVALID	
DIMS_INVALID  qpp::Exception, 67	qpp, 31–33
<del>-</del>	qpp, 31–33 kronpow
qpp::Exception, 67	qpp, 31–33
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR qpp::Exception, 67	qpp, 31–33 kronpow qpp, 33
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR qpp::Exception, 67 DIMS_MISMATCH_MATRIX	qpp, 31–33 kronpow qpp, 33
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33 load qpp, 34 logdet
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35  MATRIX_NOT_CVECTOR
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35  MATRIX_NOT_CVECTOR qpp::Exception, 67 MATRIX_NOT_RVECTOR
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35  MATRIX_NOT_CVECTOR qpp::Exception, 67  MATRIX_NOT_RVECTOR qpp::Exception, 67
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35  MATRIX_NOT_CVECTOR qpp::Exception, 67 MATRIX_NOT_RVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE
app::Exception, 67 DIMS_MISMATCH_CVECTOR app::Exception, 67 DIMS_MISMATCH_MATRIX app::Exception, 67 DIMS_MISMATCH_RVECTOR app::Exception, 67 DIMS_MISMATCH_VECTOR app::Exception, 67 DIMS_NOT_EQUAL app::Exception, 67 det app, 21 disp app, 22 dispIn	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35  MATRIX_NOT_CVECTOR qpp::Exception, 67 MATRIX_NOT_RVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE qpp::Exception, 67
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35  MATRIX_NOT_CVECTOR qpp::Exception, 67 MATRIX_NOT_RVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE qpp::Exception, 67 MATRIX_NOT_SQUARE qpp::Exception, 67 MATRIX_NOT_SQUARE qpp::Exception, 67
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35  MATRIX_NOT_CVECTOR qpp::Exception, 67  MATRIX_NOT_RVECTOR qpp::Exception, 67  MATRIX_NOT_SQUARE qpp::Exception, 67  MATRIX_NOT_SQUARE_OR_CVECTOR qpp::Exception, 67
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35  MATRIX_NOT_CVECTOR qpp::Exception, 67 MATRIX_NOT_RVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_CVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_CVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_RVECTOR
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35  MATRIX_NOT_CVECTOR qpp::Exception, 67 MATRIX_NOT_RVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_CVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_CVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_RVECTOR qpp::Exception, 67
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35  MATRIX_NOT_CVECTOR qpp::Exception, 67 MATRIX_NOT_RVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_CVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_RVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_RVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_VECTOR
qpp::Exception, 67 DIMS_MISMATCH_CVECTOR	qpp, 31–33 kronpow qpp, 33  load qpp, 34 logdet qpp, 34 logm qpp, 35  MATRIX_NOT_CVECTOR qpp::Exception, 67 MATRIX_NOT_RVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_CVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_CVECTOR qpp::Exception, 67 MATRIX_NOT_SQUARE_OR_RVECTOR qpp::Exception, 67

104 INDEX

F 0-	
qpp::Exception, 67	grams, 28, 29
mket	gt, 59
qpp, 35, 36 multiidx2n	hevals, 29 hevects, 30
qpp, 37	inverse, 30
<b>Ч</b> рр, <b>υ</b>	invperm, 31
n2multiidx	kron, 31–33
qpp, 37	kronpow, 33
NOT_BIPARTITE	load, 34
qpp::Exception, 67	logdet, 34
NOT_QUBIT_GATE	logm, 35
qpp::Exception, 67	mket, 35, 36
NOT_QUBIT_SUBSYS	multiidx2n, 37
qpp::Exception, 67	n2multiidx, 37
norm	norm, 38
qpp, 38	powm, 38
OUT OF PANOE	prj, 39
OUT_OF_RANGE	ptrace, 40
qpp::Exception, 67	ptrace1, 40
PERM INVALID	ptrace2, 41
qpp::Exception, 67	ptranspose, 42
powm	qmutualinfo, 43
qpp, 38	rand, 44, 45
prj	randint, 45
qpp, 39	randket, 45
ptrace	randkraus, 46
qpp, 40	randn, 46, 47
ptrace1	randperm, 47
qpp, 40	randrho, 47
ptrace2	rdevs, 59
qpp, 41	renyi, 48
ptranspose	reshape, 49
qpp, 42	save, 49
	schmidtcoeff, 50
qmutualinfo	schmidtprob, 51
qpp, 43	shannon, 52
qpp, 9	sinm, 52
absm, 14	spectralpowm, 53 sqrtm, 53
adjoint, 15	st, 59
anticomm, 15	sum, 55
channel, 16	super, 55
choi, 17	syspermute, 56
choi2kraus, 17 comm, 18	trace, 57
compperm, 18	transpose, 58
conjugate, 20	tsallis, 58
cosm, 20	qpp::Exception
cwise, 21	CUSTOM EXCEPTION, 67
det, 21	DIMS_INVALID, 67
disp, 22	DIMS MISMATCH CVECTOR, 67
displn, 22, 23	DIMS_MISMATCH_MATRIX, 67
entanglement, 24	DIMS_MISMATCH_RVECTOR, 67
evals, 24	DIMS_MISMATCH_VECTOR, 67
evects, 25	DIMS_NOT_EQUAL, 67
expandout, 25	MATRIX_NOT_CVECTOR, 67
expm, 26	MATRIX_NOT_RVECTOR, 67
funm, 27	MATRIX_NOT_SQUARE, 67
gconcurrence, 27	MATRIX_NOT_SQUARE_OR_CVECTOR, 67

MATRIX_NOT_SQUARE_OR_RVECTOR, 67 MATRIX_NOT_SQUARE_OR_VECTOR, 67 MATRIX_NOT_VECTOR, 67 NOT_BIPARTITE, 67 NOT_QUBIT_GATE, 67 NOT_QUBIT_SUBSYS, 67 OUT_OF_RANGE, 67 PERM_INVALID, 67 SUBSYS_MISMATCH_DIMS, 67 TYPE_MISMATCH, 67 UNDEFINED_TYPE, 67 UNKNOWN_EXCEPTION, 67 ZERO_SIZE, 67	TYPE_MISMATCH
rand	ZERO_SIZE
qpp, 44, 45	qpp::Exception, 67
randint	
qpp, 45	
randket	
qpp, 45	
randkraus	
qpp, 46	
randn	
qpp, 46, 47	
randperm	
qpp, 47	
randrho	
qpp, 47	
rdevs	
qpp, 59	
renyi	
qpp, 48	
reshape qpp, 49	
<b>Чрр</b> , то	
SUBSYS_MISMATCH_DIMS	
qpp::Exception, 67	
save	
qpp, 49	
schmidtcoeff	
qpp, 50	
schmidtprob	
qpp, 51	
shannon	
qpp, 52	
sinm	
qpp, 52 spectralpowm	
qpp, 53	
sqrtm	
qpp, 53	
st st	
qpp, 59	
sum	
qpp, 55	
super	
qpp, 55	
syspermute	
qpp, 56	