Quantum++

v1.0-rc2

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Contents

Chapter 1

Quantum++

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Build status: Master Devel

Quantum++ is a modern C++11 general purpose quantum computing library, composed solely of template header files. Quantum++ is written in standard C++11 and has very low external dependencies, using only the `Eigen 3` linear algebra header-only template library and, if available, the `OpenMP` multi-processing library.

Quantum++ is not restricted to qubit systems or specific quantum information processing tasks, being capable of simulating arbitrary quantum processes. The main design factors taken in consideration were the ease of use, high portability, and high performance. The library's simulation capabilities are only restricted by the amount of available physical memory. On a typical machine (Intel i5 8Gb RAM) Quantum++ can successfully simulate the evolution of 25 qubits in a pure state or of 12 qubits in a mixed state reasonably fast.

To report any bugs or ask for additional features/enhancements, please `submit an issue` with an appropriate label.

If you are interesting in contributing to this project, feel free to contact me. Alternatively, create a custom branch, add your contribution, then finally create a pull request. If I accept the pull request, I will merge your custom branch with the latest development branch. The latter will eventually be merged into a future release version. To contribute, you need to have a solid knowledge of C++ (preferably C++11), including templates and the standard library, a basic knowledge of quantum computing and linear algebra, and working experience with `Eigen 3`.

For additional `Eigen 3` documentation see `http://eigen.tuxfamily.org/dox/`. For a simple `Eigen 3` quick ASCII reference see `http://eigen.tuxfamily.org/dox/AsciiQuickReference.txt`.

Building instructions for POSIX-compliant platforms

Configuration

- Compiler: `g++` version 4.8.2 or later (for good C++11 support)
- `Eigen 3` linear algebra library. I assume here that the library is installed in `$HOME/eigen`, although the location may vary, e.g. if the libary was installed using a package manager.
- Quantum++ library located in `$HOME/qpp`

Optional

- `CMake` version 3.0 or later, highly recommended
- `MATLAB` compiler include header files: `/Applications/MATLAB_R2016a.app/extern/include`
- `MATLAB` compiler shared library files: `/Applications/MATLAB_R2016a.app/bin/maci64`

Building using `CMake` (version 3.0 or later)

The current version of the repository has a `./CMakeLists.txt` configuration file for building examples using `CMake`. To build an example using `CMake`, I recommend an out-of-source build, i.e., from the root of the project (where `./include` is located), type

```
mkdir ./build
cd ./build
cmake ..
make
```

The commands above build the release version (default) executable `qpp`, from the source file `./examples/minimal.cpp`, without `MATLAB` support (default), inside the directory `./build`.

If the location of `Eigen 3` is not detected automatically by the `CMake` build script, then the build script will fail (with an error message). In this case the location of `Eigen 3` needs to be specified manually in the `CMake` build command line by passing the `-DEIGEN3_INCLUDE_DIR=path_to_eigen3` flag, e.g.

```
cmake .. -DEIGEN3_INCLUDE_DIR=/usr/local/eigen3
```

To build a different configuration, e.g. the debug version with `MATLAB` support, type from the root of the project

```
cd ./build
rm -rf *
cmake -DCMAKE_BUILD_TYPE=Debug -DWITH_MATLAB=ON ..
make
```

Or, to disable `OpenMP` support (enabled by default), type

```
cd ./build
rm -rf *
cmake -DWITH_OPENMP=OFF ..
make
```

To change the name of the example file or the location of `MATLAB` installation, edit the `./CMakeLists.txt` file. Inspect also `./CMakeLists.txt` for additional fine-tuning options. Do not forget to clean the `./build` directory before a fresh build!

Building without an automatic build system

- Example file: `$HOME/qpp/examples/minimal.cpp`
- Output executable: `$HOME/qpp/examples/minimal`
- You must run the commands below from inside the directory `$HOME/qpp/examples`

Release version (without MATLAB support)

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
     -O3 -DNDEBUG -DEIGEN_NO_DEBUG \
     -isystem $HOME/eigen -I $HOME/qpp/include \
     minimal.cpp -o minimal
```

Debug version (without MATLAB support)

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
     -g3 -DDEBUG \
     -isystem $HOME/eigen -I $HOME/qpp/include \
      minimal.cpp -o minimal
```

Release version (with MATLAB support)

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
     -O3 -DNDEBUG -DEIGEN_NO_DEBUG \
     -isystem $HOME/eigen -I $HOME/qpp/include \
     -I/Applications/MATLAB_R2016a.app/extern/include \
     -L/Applications/MATLAB_R2016a.app/bin/maci64 \
     -lmx -lmat minimal.cpp -o minimal
```

Debug version (with MATLAB support)

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
     -g3 -DDEBUG \
     -isystem $HOME/eigen -I $HOME/qpp/include \
     -I /Applications/MATLAB_R2016a.app/extern/include \
     -L /Applications/MATLAB_R2016a.app/bin/maci64 \
     -lmx -lmat minimal.cpp -o minimal
```

Additional building instructions for particular platforms

Windows via Cygwin

- Some earlier versions of Cygwin had a bug related to lack of support for some C++11 math functions, see http://stackoverflow.com/questions/28997206/cygwin-support-for-c11-in-g4-9-2 for more details. Quick fix: patch the standard library header file `<cmath>` using the provided patch `./cmath_cygwin.patch`. Latest Cygwin (as of Nov. 11, 2016) seem to have fixed the issue.

Windows via Visual Studio

- Visual Studio versions preceeding version 2015 do not have full C++11 support. If you decide to use Visual Studio make sure you install version 2015 or later.
- Visual Studio 2015 only supports OpenMP 2.0. Quantum++ uses features from OpenMP 3.↩
  0, hence Quantum++ will not compile on Visual Studio 2015 if you enable OpenMP (disabled by default) in

  ```
  *Project/Properties/Configuration Properties/C_C++/Language/Open MP Support*
  ```

and `#define WITH_OPENMP_` in your source file.

- To create a Visual Studio 2015 or later console solution, start by creating a *Win32 Console Application*

  ```
  *File/New/Project.../Installed/Templates/Visual C++/Win32/Win32 Console Application*

  Click *Next* then select *Console Application* as *Application Type*.
  Click *Finish* to create the solution. Next select

  *Project/Properties*

  from the main menu. The *Property Pages* configuration window will open.
  From the latter select *All configurations* from the top left
  *Configuration* drop box. Next select

  *Configuration Properties/C_C++/General*

  and add to the field *Additional Include Directories* the location of
  Quantum++ `./include` folder as well as the location of
  [Eigen 3](http://eigen.tuxfamily.org). It should look similar to

  **C:\Users\User\Downloads\eigen;C:\Users\User\Downloads\qpp\include;%(AdditionalIncludeDirectories)**

  Finally select

  *Configuration Properties/C_C++/Advanced*

  and add to the field *Disable Specific Warnings* the values **4503;4996**.
  Click *Ok* to save the settings and close the *Property Pages* window.
  You are now ready to go.
  ```

OS X/macOS

- If you want to compile with clang++ version 3.7 or later, I highly recommend to install it via macports.
- If you run the program with MATLAB support, make sure that the environment variable DYLD_LIBRARY_↩
  PATH is set to point to the MATLAB compiler library location, see the run_mac_MATLAB script. Otherwise, you get a runtime error similar to

  ```
  > dyld: Library not loaded: @rpath/libmat.dylib.
  ```

  – I recommend running via a script, as otherwise setting the DYLD_LIBRARY_PATH globally may interfere with macports' CMake installation (in case you use CMake from macports). If you use a script, then the environment variable is local to the script and does not interfere with the rest of the system.
  – Example of script, assumed to be located in the root directory of Quantum++

  ```
  #!/bin/sh

  MATLAB=/Applications/MATLAB_R2016a.app
  export DYLD_LIBRARY_PATH=$DYLD_LIBRARY_PATH:$MATLAB/bin/maci64

  ./build/qpp
  ```

- If you build a debug version with g++ and use gdb to step inside template functions you may want to add -fno-weak compiler flag. See http://stackoverflow.com/questions/23330641/gnu-gdb-can-not-st for more details about this problem.

Unit testing

Quantum++ was extensively tested under multiple flavours of Linux, OS X/macOS, Windows XP/7/10, Solaris 11.x via a suite of unit tests constructed with Google Test 1.8.0 (included with the project in ./unit_tests/lib/gtest-1.8.0). The source code of the unit tests is provided under ./unit_↩ tests/tests. To build and run the unit tests, I strongly recommend to use CMake version 3.0 or later. Assuming you do use CMake, switch to the ./unit_tests directory, create a build directory inside it, then from the newly created ./unit_tests/build type

```
cmake ..
make
```

The commands above build ./unit_tests/build/tests/qpp_testing, which you then may run. Note that qpp::Timer tests or tests related to random functions such as qpp::rand() may sometime (very rarely) fail, due to timing imprecision or statistical errors. Such behaviour is perfectly normal.

Note

The CMake configuration file ./unit_tests/CMakeLists.txt defines the same building options and default choices as the main ./CMakeLists.txt of Quantum++. Therefore you can use the same flags as the ones mentioned at the beginning of this document when customizing the build. You should modify ./unit_↩ tests/CMakeLists.txt accordingly in case your Eigen 3 library or MATLAB include/library files are in a different location than the one assumed in this document.

Additional remarks

- If you use clang++ version 3.7 or later and want to use OpenMP (enabled by default), make sure to modify CLANG_LIBOMP and CLANG_LIBOMP_INCLUDE in CMakeLists.txt so they point to the correct location of the OpenMP library, as otherwise clang++ will not find <omp.h> and the libomp shared library.

Chapter 2

Namespace Index

2.1 Namespace List

Here is a list of all namespaces with brief descriptions:

Chapter 3

Hierarchical Index

3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

Chapter 4

Class Index

4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

Chapter 5

File Index

5.1 File List

Here is a list of all files with brief descriptions:

Chapter 6

Namespace Documentation

6.1 qpp Namespace Reference

Quantum++ main namespace.

Namespaces

- exception

  Quantum++ exception hierarchy namespace.
- experimental

  Experimental/test functions/classes, do not use or modify.
- internal

  Internal utility functions, do not use them directly or modify them.

Classes

- class Codes

  const Singleton class that defines quantum error correcting codes
- class Gates

  const Singleton class that implements most commonly used gates
- class IDisplay

  Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.
- class Init

  const Singleton class that performs additional initializations/cleanups
- struct is_complex

  Checks whether the type is a complex type.
- struct is_complex< std::complex< T > >

  Checks whether the type is a complex number type, specialization for complex types.
- struct is_iterable

  Checks whether T is compatible with an STL-like iterable container.
- struct is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >

  Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.
- struct is_matrix_expression

Checks whether the type is an Eigen matrix expression.

- struct make_void

  Helper for qpp::to_void<> alias template.
- class RandomDevices

  Singleton class that manages the source of randomness in the library.
- class States

  const Singleton class that implements most commonly used states
- class Timer

  Chronometer.

Typedefs

- template<typename... Ts>
  using to_void = typename make_void< Ts... >::type

  Alias template that implements the proposal for void_t.
- using idx = std::size_t

  Non-negative integer index.
- using bigint = long long int

  Big integer.
- using cplx = std::complex< double >

  Complex number in double precision.
- using ket = Eigen::VectorXcd

  Complex (double precision) dynamic Eigen column vector.
- using bra = Eigen::RowVectorXcd

  Complex (double precision) dynamic Eigen row vector.
- using cmat = Eigen::MatrixXcd

  Complex (double precision) dynamic Eigen matrix.
- using dmat = Eigen::MatrixXd

  Real (double precision) dynamic Eigen matrix.
- template<typename Scalar >
  using dyn_mat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >

  Dynamic Eigen matrix over the field specified by Scalar.
- template<typename Scalar >
  using dyn_col_vect = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >

  Dynamic Eigen column vector over the field specified by Scalar.
- template<typename Scalar >
  using dyn_row_vect = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >

  Dynamic Eigen row vector over the field specified by Scalar.

Functions

- constexpr cplx operator"" _i (unsigned long long int x) noexcept

  User-defined literal for complex $i = \sqrt{-1}$ (integer overload)
- constexpr cplx operator"" _i (long double x) noexcept

  User-defined literal for complex $i = \sqrt{-1}$ (real overload)
- cplx omega (idx D)

  D-th root of unity.
- template<typename Derived >
  dyn_col_vect< double > schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

Schmidt coefficients of the bi-partite pure state A.

- template<typename Derived >
  dyn_col_vect< double > schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt coefficients of the bi-partite pure state A.
- template<typename Derived >
  cmat schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt basis on Alice side.
- template<typename Derived >
  cmat schmidtA (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt basis on Alice side.
- template<typename Derived >
  cmat schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt basis on Bob side.
- template<typename Derived >
  cmat schmidtB (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt basis on Bob side.
- template<typename Derived >
  std::vector< double > schmidtprobs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt probabilities of the bi-partite pure state A.
- template<typename Derived >
  std::vector< double > schmidtprobs (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt probabilities of the bi-partite pure state A.
- template<typename Derived >
  double entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Entanglement of the bi-partite pure state A.
- template<typename Derived >
  double entanglement (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Entanglement of the bi-partite pure state A.
- template<typename Derived >
  double gconcurrence (const Eigen::MatrixBase< Derived > &A)

  G-concurrence of the bi-partite pure state A.
- template<typename Derived >
  double negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Negativity of the bi-partite mixed state A.
- template<typename Derived >
  double negativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Negativity of the bi-partite mixed state A.
- template<typename Derived >
  double lognegativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Logarithmic negativity of the bi-partite mixed state A.
- template<typename Derived >
  double lognegativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Logarithmic negativity of the bi-partite mixed state A.
- template<typename Derived >
  double concurrence (const Eigen::MatrixBase< Derived > &A)

  Wootters concurrence of the bi-partite qubit mixed state A.
- template<typename Derived >
  double entropy (const Eigen::MatrixBase< Derived > &A)

  von-Neumann entropy of the density matrix A
- double entropy (const std::vector< double > &prob)

  Shannon entropy of the probability distribution prob.

- template<typename Derived >
  double renyi (const Eigen::MatrixBase< Derived > &A, double alpha)

  Renyi- α entropy of the density matrix A, for $\alpha \geq 0$.
- double renyi (const std::vector< double > &prob, double alpha)

  Renyi- α entropy of the probability distribution prob, for $\alpha \geq 0$.
- template<typename Derived >
  double tsallis (const Eigen::MatrixBase< Derived > &A, double q)

  Tsallis- q entropy of the density matrix A, for $q \geq 0$.
- double tsallis (const std::vector< double > &prob, double q)

  Tsallis- q entropy of the probability distribution prob, for $q \geq 0$.
- template<typename Derived >
  double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, const std::vector< idx > &dims)

  Quantum mutual information between 2 subsystems of a composite system.
- template<typename Derived >
  double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, idx d=2)

  Quantum mutual information between 2 subsystems of a composite system.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > transpose (const Eigen::MatrixBase< Derived > &A)

  Transpose.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > conjugate (const Eigen::MatrixBase< Derived > &A)

  Complex conjugate.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > adjoint (const Eigen::MatrixBase< Derived > &A)

  Adjoint.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > inverse (const Eigen::MatrixBase< Derived > &A)

  Inverse.
- template<typename Derived >
  Derived::Scalar trace (const Eigen::MatrixBase< Derived > &A)

  Trace.
- template<typename Derived >
  Derived::Scalar det (const Eigen::MatrixBase< Derived > &A)

  Determinant.
- template<typename Derived >
  Derived::Scalar logdet (const Eigen::MatrixBase< Derived > &A)

  Logarithm of the determinant.
- template<typename Derived >
  Derived::Scalar sum (const Eigen::MatrixBase< Derived > &A)

  Element-wise sum of A.
- template<typename Derived >
  Derived::Scalar prod (const Eigen::MatrixBase< Derived > &A)

  Element-wise product of A.
- template<typename Derived >
  double norm (const Eigen::MatrixBase< Derived > &A)

  Frobenius norm.
- template<typename Derived >
  std::pair< dyn_col_vect< cplx >, cmat > eig (const Eigen::MatrixBase< Derived > &A)

  Full eigen decomposition.
- template<typename Derived >
  dyn_col_vect< cplx > evals (const Eigen::MatrixBase< Derived > &A)

Eigenvalues.

- template<typename Derived >
  cmat evects (const Eigen::MatrixBase< Derived > &A)

  Eigenvectors.
- template<typename Derived >
  std::pair< dyn_col_vect< double >, cmat > heig (const Eigen::MatrixBase< Derived > &A)

  Full eigen decomposition of Hermitian expression.
- template<typename Derived >
  dyn_col_vect< double > hevals (const Eigen::MatrixBase< Derived > &A)

  Hermitian eigenvalues.
- template<typename Derived >
  cmat hevects (const Eigen::MatrixBase< Derived > &A)

  Hermitian eigenvectors.
- template<typename Derived >
  std::tuple< cmat, dyn_col_vect< double >, cmat > svd (const Eigen::MatrixBase< Derived > &A)

  Full singular value decomposition.
- template<typename Derived >
  dyn_col_vect< double > svals (const Eigen::MatrixBase< Derived > &A)

  Singular values.
- template<typename Derived >
  cmat svdU (const Eigen::MatrixBase< Derived > &A)

  Left singular vectors.
- template<typename Derived >
  cmat svdV (const Eigen::MatrixBase< Derived > &A)

  Right singular vectors.
- template<typename Derived >
  cmat funm (const Eigen::MatrixBase< Derived > &A, cplx(∗f)(const cplx &))

  Functional calculus f(A)
- template<typename Derived >
  cmat sqrtm (const Eigen::MatrixBase< Derived > &A)

  Matrix square root.
- template<typename Derived >
  cmat absm (const Eigen::MatrixBase< Derived > &A)

  Matrix absolute value.
- template<typename Derived >
  cmat expm (const Eigen::MatrixBase< Derived > &A)

  Matrix exponential.
- template<typename Derived >
  cmat logm (const Eigen::MatrixBase< Derived > &A)

  Matrix logarithm.
- template<typename Derived >
  cmat sinm (const Eigen::MatrixBase< Derived > &A)

  Matrix sin.
- template<typename Derived >
  cmat cosm (const Eigen::MatrixBase< Derived > &A)

  Matrix cos.
- template<typename Derived >
  cmat spectralpowm (const Eigen::MatrixBase< Derived > &A, const cplx z)

  Matrix power.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > powm (const Eigen::MatrixBase< Derived > &A, idx n)

  Fast matrix power based on the SQUARE-AND-MULTIPLY algorithm.

- template<typename Derived >
  double schatten (const Eigen::MatrixBase< Derived > &A, double p)

  Schatten matrix norm.
- template<typename OutputScalar , typename Derived >
  dyn_mat< OutputScalar > cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(∗f)(const typename Derived::Scalar &))

  Functor.
- template<typename T >
  dyn_mat< typename T::Scalar > kron (const T &head)

  Kronecker product.
- template<typename T , typename ... Args>
  dyn_mat< typename T::Scalar > kron (const T &head, const Args &... tail)

  Kronecker product.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > kron (const std::vector< Derived > &As)

  Kronecker product.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > kron (const std::initializer_list< Derived > &As)

  Kronecker product.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > kronpow (const Eigen::MatrixBase< Derived > &A, idx n)

  Kronecker power.
- template<typename T >
  dyn_mat< typename T::Scalar > dirsum (const T &head)

  Direct sum.
- template<typename T , typename ... Args>
  dyn_mat< typename T::Scalar > dirsum (const T &head, const Args &... tail)

  Direct sum.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > dirsum (const std::vector< Derived > &As)

  Direct sum.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > dirsum (const std::initializer_list< Derived > &As)

  Direct sum.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > dirsumpow (const Eigen::MatrixBase< Derived > &A, idx n)

  Direct sum power.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > reshape (const Eigen::MatrixBase< Derived > &A, idx rows, idx cols)

  Reshape.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::↩
  MatrixBase< Derived2 > &B)

  Commutator.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)

  Anti-commutator.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > prj (const Eigen::MatrixBase< Derived > &A)

  Projector.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > grams (const std::vector< Derived > &As)

Gram-Schmidt orthogonalization.

- template<typename Derived >
  dyn_mat< typename Derived::Scalar > grams (const std::initializer_list< Derived > &As)

  Gram-Schmidt orthogonalization.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > grams (const Eigen::MatrixBase< Derived > &A)

  Gram-Schmidt orthogonalization.
- std::vector< idx > n2multiidx (idx n, const std::vector< idx > &dims)

  Non-negative integer index to multi-index.
- idx multiidx2n (const std::vector< idx > &midx, const std::vector< idx > &dims)

  Multi-index to non-negative integer index.
- ket mket (const std::vector< idx > &mask, const std::vector< idx > &dims)

  Multi-partite qudit ket.
- ket mket (const std::vector< idx > &mask, idx d=2)

  Multi-partite qudit ket.
- cmat mprj (const std::vector< idx > &mask, const std::vector< idx > &dims)

  Projector onto multi-partite qudit ket.
- cmat mprj (const std::vector< idx > &mask, idx d=2)

  Projector onto multi-partite qudit ket.
- template<typename InputIterator >
  std::vector< double > abssq (InputIterator first, InputIterator last)

  Computes the absolute values squared of an STL-like range of complex numbers.
- template<typename Container >
  std::vector< double > abssq (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type ∗=nullptr)

  Computes the absolute values squared of an STL-like container.
- template<typename Derived >
  std::vector< double > abssq (const Eigen::MatrixBase< Derived > &A)

  Computes the absolute values squared of an Eigen expression.
- template<typename InputIterator >
  std::iterator_traits< InputIterator >::value_type sum (InputIterator first, InputIterator last)

  Element-wise sum of an STL-like range.
- template<typename Container >
  Container::value_type sum (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type ∗=nullptr)

  Element-wise sum of the elements of an STL-like container.
- template<typename InputIterator >
  std::iterator_traits< InputIterator >::value_type prod (InputIterator first, InputIterator last)

  Element-wise product of an STL-like range.
- template<typename Container >
  Container::value_type prod (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type ∗=nullptr)

  Element-wise product of the elements of an STL-like container.
- template<typename Derived >
  dyn_col_vect< typename Derived::Scalar > rho2pure (const Eigen::MatrixBase< Derived > &A)

  Finds the pure state representation of a matrix proportional to a projector onto a pure state.
- template<typename T >
  std::vector< T > complement (std::vector< T > subsys, idx N)

  Constructs the complement of a subsystem vector.
- template<typename Derived >
  std::vector< double > rho2bloch (const Eigen::MatrixBase< Derived > &A)

  Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix A.
- cmat bloch2rho (const std::vector< double > &r)

Computes the density matrix corresponding to the 3-dimensional real Bloch vector r.

- template< typename Derived >
  internal::IOManipEigen disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)

  Eigen expression ostream manipulator.
- internal::IOManipEigen disp (cplx z, double chop=qpp::chop)

  Complex number ostream manipulator.
- template< typename InputIterator >
  internal::IOManipRange< InputIterator > disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")

  Range ostream manipulator.
- template< typename Container >
  internal::IOManipRange< typename Container::const_iterator > disp (const Container &c, const std::string &separator, const std::string &start="[", const std::string &end="]", typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.
- template< typename PointerType >
  internal::IOManipPointer< PointerType > disp (const PointerType *p, idx N, const std::string &separator, const std::string &start="[", const std::string &end="]")

  C-style pointer ostream manipulator.
- template< typename Derived >
  void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

  Saves Eigen expression to a binary file (internal format) in double precision.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > load (const std::string &fname)

  Loads Eigen matrix from a binary file (internal format) in double precision.
- template< typename Derived >
  dyn_col_vect< typename Derived::Scalar > ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::↩
  MatrixBase< Derived > &psi, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Generalized inner product.
- template< typename Derived >
  dyn_col_vect< typename Derived::Scalar > ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::↩
  MatrixBase< Derived > &psi, const std::vector< idx > &subsys, idx d=2)

  Generalized inner product.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

  Measures the state A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)

  Measures the state A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &U)

  Measures the state A in the orthonormal basis specified by the unitary matrix U.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- template<typename Derived >
  std::tuple< std::vector< idx >, double, cmat > measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, std::vector< idx > dims)

  Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.
- template<typename Derived >
  std::tuple< std::vector< idx >, double, cmat > measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, idx d=2)

  Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.
- template<typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< cplx > >::type loadM←
  ATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< typename Derived::←
  Scalar > >::type loadMATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value >::type saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std←
  ::string &mode)

  Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value >::type saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std←
  ::string &mode)

  Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.
- std::vector< int > x2contfrac (double x, idx N, idx cut=1e5)

  Simple continued fraction expansion.
- double contfrac2x (const std::vector< int > &cf, idx N=idx(-1))

  Real representation of a simple continued fraction.
- bigint gcd (bigint a, bigint b)

  Greatest common divisor of two integers.
- bigint gcd (const std::vector< bigint > &as)

  Greatest common divisor of a list of integers.
- bigint lcm (bigint a, bigint b)

  Least common multiple of two integers.

- bigint lcm (const std::vector< bigint > &as)

  Least common multiple of a list of integers.
- std::vector< idx > invperm (const std::vector< idx > &perm)

  Inverse permutation.
- std::vector< idx > compperm (const std::vector< idx > &perm, const std::vector< idx > &sigma)

  Compose permutations.
- std::vector< bigint > factors (bigint a)

  Prime factor decomposition.
- bigint modmul (bigint a, bigint b, bigint p)

  Modular multiplication without overflow.
- bigint modpow (bigint a, bigint n, bigint p)

  Fast integer power modulo p based on the SQUARE-AND-MULTIPLY algorithm.
- std::tuple< bigint, bigint, bigint > egcd (bigint a, bigint b)

  Extended greatest common divisor of two integers.
- bigint modinv (bigint a, bigint p)

  Modular inverse of a mod p.
- bool isprime (bigint p, idx k=80)

  Primality test based on the Miller-Rabin's algorithm.
- bigint randprime (bigint a, bigint b, idx N=1000)

  Generates a random big prime uniformly distributed in the interval [a, b].
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx d=2)

  Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen↩
  ::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen↩
  ::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, idx d=2)

  Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- template<typename Derived >
  cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

  Applies the channel specified by the set of Kraus operators Ks to the density matrix A.
- template<typename Derived >
  cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.
- template<typename Derived >
  cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)

  Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.
- cmat kraus2super (const std::vector< cmat > &Ks)

  Superoperator matrix.
- cmat kraus2choi (const std::vector< cmat > &Ks)

  Choi matrix.

- std::vector< cmat > choi2kraus (const cmat &A)

    Orthogonal Kraus operators from Choi matrix.
- cmat choi2super (const cmat &A)

    Converts Choi matrix to superoperator matrix.
- cmat super2choi (const cmat &A)

    Converts superoperator matrix to Choi matrix.
- template<typename Derived >
dyn_mat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, const std↩
::vector< idx > &dims)

    Partial trace.
- template<typename Derived >
dyn_mat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, idx d=2)

    Partial trace.
- template<typename Derived >
dyn_mat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, const std↩
::vector< idx > &dims)

    Partial trace.
- template<typename Derived >
dyn_mat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, idx d=2)

    Partial trace.
- template<typename Derived >
dyn_mat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector<
idx > &subsys, const std::vector< idx > &dims)

    Partial trace.
- template<typename Derived >
dyn_mat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector<
idx > &subsys, idx d=2)

    Partial trace.
- template<typename Derived >
dyn_mat< typename Derived::Scalar > ptranspose (const Eigen::MatrixBase< Derived > &A, const std↩
::vector< idx > &subsys, const std::vector< idx > &dims)

    Partial transpose.
- template<typename Derived >
dyn_mat< typename Derived::Scalar > ptranspose (const Eigen::MatrixBase< Derived > &A, const std↩
::vector< idx > &subsys, idx d=2)

    Partial transpose.
- template<typename Derived >
dyn_mat< typename Derived::Scalar > syspermute (const Eigen::MatrixBase< Derived > &A, const std↩
::vector< idx > &perm, const std::vector< idx > &dims)

    Subsystem permutation.
- template<typename Derived >
dyn_mat< typename Derived::Scalar > syspermute (const Eigen::MatrixBase< Derived > &A, const std↩
::vector< idx > &perm, idx d=2)

    Subsystem permutation.
- double rand (double a, double b)

    Generates a random real number uniformly distributed in the interval [a, b)
- bigint rand (bigint a, bigint b)

    Generates a random big integer uniformly distributed in the interval [a, b].
- idx randidx (idx a=std::numeric_limits< idx >::min(), idx b=std::numeric_limits< idx >::max())

    Generates a random index (idx) uniformly distributed in the interval [a, b].
- template<typename Derived >
Derived rand (idx rows, idx cols, double a=0, double b=1)

    Generates a random matrix with entries uniformly distributed in the interval [a, b)

- template<>
  dmat rand (idx rows, idx cols, double a, double b)

  Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)
- template<>
  cmat rand (idx rows, idx cols, double a, double b)

  Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)
- template<typename Derived >
  Derived randn (idx rows, idx cols, double mean=0, double sigma=1)

  Generates a random matrix with entries normally distributed in N(mean, sigma)
- template<>
  dmat randn (idx rows, idx cols, double mean, double sigma)

  Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)
- template<>
  cmat randn (idx rows, idx cols, double mean, double sigma)

  Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)
- double randn (double mean=0, double sigma=1)

  Generates a random real number (double) normally distributed in N(mean, sigma)
- cmat randU (idx D=2)

  Generates a random unitary matrix.
- cmat randV (idx Din, idx Dout)

  Generates a random isometry matrix.
- std::vector< cmat > randkraus (idx N, idx D=2)

  Generates a set of random Kraus operators.
- cmat randH (idx D=2)

  Generates a random Hermitian matrix.
- ket randket (idx D=2)

  Generates a random normalized ket (pure state vector)
- cmat randrho (idx D=2)

  Generates a random density matrix.
- std::vector< idx > randperm (idx N)

  Generates a random uniformly distributed permutation.
- std::vector< double > randprob (idx N)

  Generates a random probability vector uniformly distributed over the probability simplex.
- std::vector< double > uniform (idx N)

  Uniform probability distribution vector.
- std::vector< double > marginalX (const dmat &probXY)

  Marginal distribution.
- std::vector< double > marginalY (const dmat &probXY)

  Marginal distribution.
- template<typename Container >
  double avg (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Average.
- template<typename Container >
  double cov (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if< is_↩ iterable< Container >::value >::type *=nullptr)

  Covariance.

- template< typename Container >
  double var (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_iterable< Container >::value >::type ∗=nullptr)

  Variance.
- template< typename Container >
  double sigma (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↩ iterable< Container >::value >::type ∗=nullptr)

  Standard deviation.
- template< typename Container >
  double cor (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if< is_↩ iterable< Container >::value >::type ∗=nullptr)

  Correlation.

Variables

- constexpr double chop = 1e-10

  Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.
- constexpr double eps = 1e-12

  Used to decide whether a number or expression in double precision is zero or not.
- constexpr idx maxn = 64

  Maximum number of allowed qubits/qudits (subsystems)
- constexpr double pi = 3.141592653589793238462643383279502884

  π
- constexpr double ee = 2.718281828459045235360287471352662497

  Base of natural logarithm, e.
- constexpr double infty = std::numeric_limits<double>::max()

  Used to denote infinity in double precision.

6.1.1 Detailed Description

Quantum++ main namespace.

6.1.2 Typedef Documentation

6.1.2.1 bigint

```
using qpp::bigint = typedef long long int
```

Big integer.

6.1.2.2 bra

```
using qpp::bra = typedef Eigen::RowVectorXcd
```

Complex (double precision) dynamic Eigen row vector.

6.1.2.3 cmat

```
using qpp::cmat = typedef Eigen::MatrixXcd
```

Complex (double precision) dynamic Eigen matrix.

6.1.2.4 cplx

```
using qpp::cplx = typedef std::complex<double>
```

Complex number in double precision.

6.1.2.5 dmat

```
using qpp::dmat = typedef Eigen::MatrixXd
```

Real (double precision) dynamic Eigen matrix.

6.1.2.6 dyn_col_vect

```
template<typename Scalar >
using qpp::dyn_col_vect = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, 1>
```

Dynamic Eigen column vector over the field specified by *Scalar*.

Example:

```
// type of colvect is Eigen::Matrix<float, Eigen::Dynamic, 1>
dyn_col_vect<float> colvect(2);
```

6.1.2.7 dyn_mat

```
template<typename Scalar >
using qpp::dyn_mat = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>
```

Dynamic Eigen matrix over the field specified by *Scalar*.

Example:

```
// type of mat is Eigen::Matrix<float, Eigen::Dynamic, Eigen::Dynamic>
dyn_mat<float> mat(2, 3);
```

6.1.2.8 dyn_row_vect

```
template<typename Scalar >
using qpp::dyn_row_vect = typedef Eigen::Matrix<Scalar, 1, Eigen::Dynamic>
```

Dynamic Eigen row vector over the field specified by *Scalar*.

Example:

```
// type of rowvect is Eigen::Matrix<float, 1, Eigen::Dynamic>
dyn_row_vect<float> rowvect(3);
```

6.1.2.9 idx

```
using qpp::idx = typedef std::size_t
```

Non-negative integer index.

6.1.2.10 ket

```
using qpp::ket = typedef Eigen::VectorXcd
```

Complex (double precision) dynamic Eigen column vector.

6.1.2.11 to_void

```
template<typename... Ts>
using qpp::to_void = typedef typename make_void<Ts...>::type
```

Alias template that implements the proposal for void_t.

See also

http://www.open-std.org/jtc1/sc22/wg21/docs/papers/2014/n3911

6.1.3 Function Documentation

6.1.3.1 absm()

```
template<typename Derived >
cmat qpp::absm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix absolute value.

Parameters

A	Eigen expression

Returns

Matrix absolute value of *A*

6.1.3.2 abssq() [1/3]

```
template<typename InputIterator >
std::vector<double> qpp::abssq (
            InputIterator first,
            InputIterator last )
```

Computes the absolute values squared of an STL-like range of complex numbers.

Parameters

first	Iterator to the first element of the range
last	Iterator to the last element of the range

Returns

Real vector consisting of the range absolute values squared

6.1.3.3 abssq() [2/3]

```
template<typename Container >
std::vector<double> qpp::abssq (
            const Container & c,
            typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Computes the absolute values squared of an STL-like container.

Parameters

c	STL-like container

Returns

Real vector consisting of the container's absolute values squared

6.1.3.4 abssq() [3/3]

```
template<typename Derived >
std::vector<double> qpp::abssq (
            const Eigen::MatrixBase< Derived > & A )
```

Computes the absolute values squared of an Eigen expression.

Parameters

A	Eigen expression

Returns

Real vector consisting of the absolute values squared

6.1.3.5 adjoint()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::adjoint (
            const Eigen::MatrixBase< Derived > & A )
```

Adjoint.

Parameters

A	Eigen expression

Returns

Adjoint (Hermitian conjugate) of *A*, as a dynamic matrix over the same scalar field as *A*

6.1.3.6 anticomm()

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::anticomm (
            const Eigen::MatrixBase< Derived1 > & A,
            const Eigen::MatrixBase< Derived2 > & B )
```

Anti-commutator.

See also

qpp::comm()

Anti-commutator $\{A, B\} = AB + BA$. Both *A* and *B* must be Eigen expressions over the same scalar field.

Parameters

A	Eigen expression
B	Eigen expression

Returns

Anti-commutator $AB + BA$, as a dynamic matrix over the same scalar field as *A*

6.1.3.7 apply() [1/5]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::apply (
            const Eigen::MatrixBase< Derived1 > & state,
            const Eigen::MatrixBase< Derived2 > & A,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Applies the gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

state	Eigen expression
A	Eigen expression
subsys	Subsystem indexes where the gate *A* is applied
dims	Dimensions of the multi-partite system

Returns

Gate *A* applied to the part *subsys* of *state*

6.1.3.8 apply() [2/5]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::apply (
            const Eigen::MatrixBase< Derived1 > & state,
            const Eigen::MatrixBase< Derived2 > & A,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Applies the gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

state	Eigen expression
A	Eigen expression
subsys	Subsystem indexes where the gate *A* is applied
d	Subsystem dimensions

Returns

Gate *A* applied to the part *subsys* of *state*

6.1.3.9 apply() [3/5]

```
template<typename Derived >
cmat qpp::apply (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks )
```

Applies the channel specified by the set of Kraus operators *Ks* to the density matrix *A*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators

Returns

Output density matrix after the action of the channel

6.1.3.10 apply() [4/5]

```
template<typename Derived >
cmat qpp::apply (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< cmat > & Ks,
             const std::vector< idx > & subsys,
             const std::vector< idx > & dims )
```

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *A*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes where the Kraus operators *Ks* are applied
dims	Dimensions of the multi-partite system

Returns

Output density matrix after the action of the channel

6.1.3.11 apply() [5/5]

```
template<typename Derived >
cmat qpp::apply (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< cmat > & Ks,
             const std::vector< idx > & subsys,
             idx d = 2 )
```

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *A*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes where the Kraus operators *Ks* are applied
d	Subsystem dimensions

Returns

Output density matrix after the action of the channel

6.1.3.12 applyCTRL() [1/2]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (
            const Eigen::MatrixBase< Derived1 > & state,
            const Eigen::MatrixBase< Derived2 > & A,
            const std::vector< idx > & ctrl,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Applies the controlled-gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

See also

qpp::Gates::CTRL()

Note

The dimension of the gate *A* must match the dimension of *subsys*. Also, all control subsystems in *ctrl* must have the same dimension.

Parameters

state	Eigen expression
A	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate *A* is applied
dims	Dimensions of the multi-partite system

Returns

CTRL-A gate applied to the part *subsys* of *state*

6.1.3.13 applyCTRL() [2/2]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (
             const Eigen::MatrixBase< Derived1 > & state,
             const Eigen::MatrixBase< Derived2 > & A,
             const std::vector< idx > & ctrl,
             const std::vector< idx > & subsys,
             idx d = 2 )
```

Applies the controlled-gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

See also

qpp::Gates::CTRL()

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

state	Eigen expression
A	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate *A* is applied
d	Subsystem dimensions

Returns

CTRL-A gate applied to the part *subsys* of *state*

6.1.3.14 avg()

```
template<typename Container >
double qpp::avg (
             const std::vector< double > & prob,
             const Container & X,
             typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Average.

Parameters

prob	Real probability vector representing the probability distribution of *X*
X	Real random variable values represented by an STL-like container

Returns

Average of *X*

6.1.3.15 bloch2rho()

```
cmat qpp::bloch2rho (
            const std::vector< double > & r )  [inline]
```

Computes the density matrix corresponding to the 3-dimensional real Bloch vector *r*.

See also

qpp::rho2bloch()

Parameters

r	3-dimensional real vector

Returns

Qubit density matrix

6.1.3.16 choi2kraus()

```
std::vector<cmat> qpp::choi2kraus (
            const cmat & A )  [inline]
```

Orthogonal Kraus operators from Choi matrix.

See also

qpp::kraus2choi()

Extracts a set of orthogonal (under Hilbert-Schmidt operator norm) Kraus operators from the Choi matrix *A*

Note

The Kraus operators satisfy $Tr(K_i^\dagger K_j) = \delta_{ij}$ for all $i \neq j$

Parameters

A	Choi matrix

Returns

Set of orthogonal Kraus operators

6.1.3.17 choi2super()

```
cmat qpp::choi2super (
             const cmat & A )  [inline]
```

Converts Choi matrix to superoperator matrix.

See also

qpp::super2choi()

Parameters

A	Choi matrix

Returns

Superoperator matrix

6.1.3.18 comm()

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::comm (
             const Eigen::MatrixBase< Derived1 > & A,
             const Eigen::MatrixBase< Derived2 > & B )
```

Commutator.

See also

qpp::anticomm()

Commutator $[A, B] = AB - BA$. Both *A* and *B* must be Eigen expressions over the same scalar field.

Parameters

A	Eigen expression
B	Eigen expression

Returns

Commutator $AB - BA$, as a dynamic matrix over the same scalar field as *A*

6.1.3.19 complement()

```
template<typename T >
std::vector<T> qpp::complement (
            std::vector< T > subsys,
            idx N )
```

Constructs the complement of a subsystem vector.

Parameters

subsys	Subsystem vector
N	Total number of systems

Returns

Complement of *subsys* with respect to the set $\{0, 1, \ldots, N-1\}$

6.1.3.20 compperm()

```
std::vector<idx> qpp::compperm (
            const std::vector< idx > & perm,
            const std::vector< idx > & sigma )  [inline]
```

Compose permutations.

Parameters

perm	Permutation
sigma	Permutation

Returns

Composition of the permutations *perm* ∘ *sigma* = perm(sigma)

6.1.3.21 concurrence()

```
template<typename Derived >
double qpp::concurrence (
            const Eigen::MatrixBase< Derived > & A )
```

Wootters concurrence of the bi-partite qubit mixed state *A*.

Parameters

A	Eigen expression

Returns

Wootters concurrence

6.1.3.22 conjugate()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::conjugate (
            const Eigen::MatrixBase< Derived > & A )
```

Complex conjugate.

Parameters

A	Eigen expression

Returns

Complex conjugate of *A*, as a dynamic matrix over the same scalar field as *A*

6.1.3.23 contfrac2x()

```
double qpp::contfrac2x (
            const std::vector< int > & cf,
            idx N = idx(-1) )  [inline]
```

Real representation of a simple continued fraction.

See also

qpp::x2contfrac()

Note

If *N* is greater than the size of *cf* (by default it is), then all terms in *cf* are considered.

Parameters

cf	Integer vector containing the simple continued fraction expansion
N	Number of terms considered in the continued fraction expansion.

Returns

Real representation of the simple continued fraction

6.1.3.24 cor()

```
template<typename Container >
double qpp::cor (
            const dmat & probXY,
            const Container & X,
            const Container & Y,
            typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Correlation.

Parameters

probXY	Real matrix representing the joint probability distribution of *X* and *Y* in lexicographical order (*X* labels the rows, *Y* labels the columns)
X	Real random variable values represented by an STL-like container
Y	Real random variable values represented by an STL-like container

Returns

Correlation of *X* and *Y*

6.1.3.25 cosm()

```
template<typename Derived >
cmat qpp::cosm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix cos.

Parameters

A	Eigen expression

Returns

Matrix cosine of *A*

6.1.3.26 cov()

```
template<typename Container >
double qpp::cov (
            const dmat & probXY,
            const Container & X,
            const Container & Y,
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Covariance.

Parameters

probXY	Real matrix representing the joint probability distribution of *X* and *Y* in lexicographical order (*X* labels the rows, *Y* labels the columns)
X	Real random variable values represented by an STL-like container
Y	Real random variable values represented by an STL-like container

Returns

Covariance of *X* and *Y*

6.1.3.27 cwise()

```
template<typename OutputScalar , typename Derived >
dyn_mat<OutputScalar> qpp::cwise (
            const Eigen::MatrixBase< Derived > & A,
            OutputScalar(*)(const typename Derived::Scalar &) f )
```

Functor.

Parameters

A	Eigen expression
f	Pointer-to-function from scalars of *A* to *OutputScalar*

Returns

Component-wise $f(A)$, as a dynamic matrix over the *OutputScalar* scalar field

6.1.3.28 det()

```
template<typename Derived >
Derived::Scalar qpp::det (
            const Eigen::MatrixBase< Derived > & A )
```

Determinant.

Parameters

A	Eigen expression

Returns

Determinant of *A*, as a scalar over the same scalar field as *A*. Returns $\pm\infty$ when the determinant overflows/underflows.

6.1.3.29 dirsum() [1/4]

```
template<typename T >
dyn_mat<typename T::Scalar> qpp::dirsum (
             const T & head )
```

Direct sum.

See also

qpp::dirsumpow()

Used to stop the recursion for the variadic template version of qpp::dirsum()

Parameters

head	Eigen expression

Returns

Its argument *head*

6.1.3.30 dirsum() [2/4]

```
template<typename T , typename ...  Args>
dyn_mat<typename T::Scalar> qpp::dirsum (
             const T & head,
             const Args &...  tail )
```

Direct sum.

See also

qpp::dirsumpow()

Parameters

head	Eigen expression
tail	Variadic Eigen expression (zero or more parameters)

Returns

Direct sum of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.31 dirsum() [3/4]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::dirsum (
             const std::vector< Derived > & As )
```

Direct sum.

See also

qpp::dirsumpow()

Parameters

As	std::vector of Eigen expressions

Returns

Direct sum of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.32 dirsum() [4/4]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::dirsum (
             const std::initializer_list< Derived > & As )
```

Direct sum.

See also

qpp::dirsumpow()

Parameters

As	std::initializer_list of Eigen expressions, such as *{A1*, A2, ... ,Ak}

Returns

Direct sum of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.33 dirsumpow()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::dirsumpow (
            const Eigen::MatrixBase< Derived > & A,
            idx n )
```

Direct sum power.

See also

qpp::dirsum()

Parameters

A	Eigen expression
n	Non-negative integer

Returns

Direct sum of *A* with itself *n* times $A^{\oplus n}$, as a dynamic matrix over the same scalar field as *A*

6.1.3.34 disp() [1/5]

```
template<typename Derived >
internal::IOManipEigen qpp::disp (
            const Eigen::MatrixBase< Derived > & A,
            double chop = qpp::chop )
```

Eigen expression ostream manipulator.

Parameters

A	Eigen expression
chop	Set to zero the elements smaller in absolute value than *chop*

Returns

Instance of qpp::internal::IOManipEigen

6.1.3.35 disp() [2/5]

```
internal::IOManipEigen qpp::disp (
            cplx z,
            double chop = qpp::chop )  [inline]
```

Complex number ostream manipulator.

Parameters

z	Complex number (or any other type implicitly cast-able to std::complex<double>)
chop	Set to zero the elements smaller in absolute value than *chop*

Returns

Instance of qpp::internal::IOManipEigen

6.1.3.36 disp() [3/5]

```
template<typename InputIterator >
internal::IOManipRange<InputIterator> qpp::disp (
            InputIterator first,
            InputIterator last,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]" )
```

Range ostream manipulator.

Parameters

first	Iterator to the first element of the range
last	Iterator to the last element of the range
separator	Separator
start	Left marking
end	Right marking

Returns

Instance of qpp::internal::IOManipRange

6.1.3.37 disp() [4/5]

```
template<typename Container >
internal::IOManipRange<typename Container::const_iterator> qpp::disp (
             const Container & c,
             const std::string & separator,
             const std::string & start = "[",
             const std::string & end = "]",
             typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.

Parameters

c	Container
separator	Separator
start	Left marking
end	Right marking

Returns

Instance of qpp::internal::IOManipRange

6.1.3.38 disp() [5/5]

```
template<typename PointerType >
internal::IOManipPointer<PointerType> qpp::disp (
             const PointerType * p,
             idx N,
             const std::string & separator,
             const std::string & start = "[",
             const std::string & end = "]" )
```

C-style pointer ostream manipulator.

Parameters

p	Pointer to the first element
N	Number of elements to be displayed
separator	Separator
start	Left marking
end	Right marking

Returns

Instance of qpp::internal::IOManipPointer

6.1.3.39 egcd()

```
std::tuple<bigint, bigint, bigint> qpp::egcd (
            bigint a,
            bigint b )  [inline]
```

Extended greatest common divisor of two integers.

See also

qpp::gcd()

Parameters

a	Integer
b	Integer

Returns

Tuple of: 1. Integer m, 2. Integer n, and 3. Non-negative integer $gcd(a,b)$ such that $ma + nb = gcd(a,b)$

6.1.3.40 eig()

```
template<typename Derived >
std::pair<dyn_col_vect < cplx>, cmat> qpp::eig (
            const Eigen::MatrixBase< Derived > & A )
```

Full eigen decomposition.

See also

qpp::heig()

Parameters

A	Eigen expression

Returns

Pair of: 1. Eigenvalues of *A*, as a complex dynamic column vector, and 2. Eigenvectors of *A*, as columns of a complex dynamic matrix

6.1.3.41 entanglement() [1/2]

```
template<typename Derived >
double qpp::entanglement (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< idx > & dims )
```

Entanglement of the bi-partite pure state *A*.

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

See also

qpp::entropy()

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Entanglement, with the logarithm in base 2

6.1.3.42 entanglement() [2/2]

```
template<typename Derived >
double qpp::entanglement (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Entanglement of the bi-partite pure state *A*.

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

See also

qpp::entropy()

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Entanglement, with the logarithm in base 2

6.1.3.43 entropy() [1/2]

```
template<typename Derived >
double qpp::entropy (
            const Eigen::MatrixBase< Derived > & A )
```

von-Neumann entropy of the density matrix *A*

Parameters

A	Eigen expression

Returns

von-Neumann entropy, with the logarithm in base 2

6.1.3.44 entropy() [2/2]

```
double qpp::entropy (
            const std::vector< double > & prob )  [inline]
```

Shannon entropy of the probability distribution *prob*.

Parameters

prob	Real probability vector

Returns

Shannon entropy, with the logarithm in base 2

6.1.3.45 evals()

```
template<typename Derived >
dyn_col_vect<cplx> qpp::evals (
            const Eigen::MatrixBase< Derived > & A )
```

Eigenvalues.

See also

qpp::hevals()

Parameters

A	Eigen expression

Returns

Eigenvalues of *A*, as a complex dynamic column vector

6.1.3.46 evects()

```
template<typename Derived >
cmat qpp::evects (
            const Eigen::MatrixBase< Derived > & A )
```

Eigenvectors.

See also

qpp::hevects()

Parameters

A	Eigen expression

Returns

Eigenvectors of *A*, as columns of a complex dynamic matrix

6.1.3.47 expm()

```
template<typename Derived >
cmat qpp::expm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix exponential.

Parameters

A	Eigen expression

Returns

Matrix exponential of *A*

6.1.3.48 factors()

```
std::vector<bigint> qpp::factors (
            bigint a )  [inline]
```

Prime factor decomposition.

Note

Runs in $\mathcal{O}(\sqrt{n})$ time complexity

Parameters

a	Integer different from 0, 1 or -1

Returns

Integer vector containing the factors

6.1.3.49 funm()

```
template<typename Derived >
cmat qpp::funm (
            const Eigen::MatrixBase< Derived > & A,
            cplx(*)(const cplx &) f )
```

Functional calculus f(A)

Parameters

A	Eigen expression
f	Pointer-to-function from complex to complex

Returns

$f(A)$

6.1.3.50 gcd() [1/2]

```
bigint qpp::gcd (
            bigint a,
            bigint b )  [inline]
```

Greatest common divisor of two integers.

See also

qpp::lcm()

Parameters

a	Integer
b	Integer

Returns

Greatest common divisor of *a* and *b*

6.1.3.51 gcd() [2/2]

```
bigint qpp::gcd (
            const std::vector< bigint > & as )  [inline]
```

Greatest common divisor of a list of integers.

See also

qpp::lcm()

Parameters

as	List of integers

Returns

Greatest common divisor of all numbers in *as*

6.1.3.52 gconcurrence()

```
template<typename Derived >
double qpp::gconcurrence (
            const Eigen::MatrixBase< Derived > & A )
```

G-concurrence of the bi-partite pure state *A*.

Note

Both local dimensions must be equal

Uses qpp::logdet() to avoid overflows

See also

qpp::logdet()

Parameters

A	Eigen expression

Returns

G-concurrence

6.1.3.53 grams() [1/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::grams (
            const std::vector< Derived > & As )
```

Gram-Schmidt orthogonalization.

Parameters

As	std::vector of Eigen expressions as column vectors

Returns

Gram-Schmidt vectors of *As* as columns of a dynamic matrix over the same scalar field as its arguments

6.1.3.54 grams() [2/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::grams (
            const std::initializer_list< Derived > & As )
```

Gram-Schmidt orthogonalization.

Parameters

As	std::initializer_list of Eigen expressions as column vectors

Returns

Gram-Schmidt vectors of *As* as columns of a dynamic matrix over the same scalar field as its arguments

6.1.3.55 grams() [3/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::grams (
            const Eigen::MatrixBase< Derived > & A )
```

Gram-Schmidt orthogonalization.

Parameters

A	Eigen expression, the input vectors are the columns of *A*

Returns

Gram-Schmidt vectors of the columns of *A*, as columns of a dynamic matrix over the same scalar field as *A*

6.1.3.56 heig()

```
template<typename Derived >
std::pair<dyn_col_vect < double>, cmat> qpp::heig (
            const Eigen::MatrixBase< Derived > & A )
```

Full eigen decomposition of Hermitian expression.

See also

qpp::eig()

Parameters

A	Eigen expression

Returns

Pair of: 1. Eigenvalues of *A*, as a real dynamic column vector, and 2. Eigenvectors of *A*, as columns of a complex dynamic matrix

6.1.3.57 hevals()

```
template<typename Derived >
dyn_col_vect<double> qpp::hevals (
            const Eigen::MatrixBase< Derived > & A )
```

Hermitian eigenvalues.

See also

qpp::evals()

Parameters

A	Eigen expression

Returns

Eigenvalues of Hermitian *A*, as a real dynamic column vector

6.1.3.58 hevects()

```
template<typename Derived >
cmat qpp::hevects (
             const Eigen::MatrixBase< Derived > & A )
```

Hermitian eigenvectors.

See also

qpp::evects()

Parameters

A	Eigen expression

Returns

Eigenvectors of Hermitian *A*, as columns of a complex matrix

6.1.3.59 inverse()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::inverse (
             const Eigen::MatrixBase< Derived > & A )
```

Inverse.

Parameters

A	Eigen expression

Returns

Inverse of *A*, as a dynamic matrix over the same scalar field as *A*

6.1.3.60 invperm()

```
std::vector<idx> qpp::invperm (
            const std::vector< idx > & perm )  [inline]
```

Inverse permutation.

Parameters

perm	Permutation

Returns

Inverse of the permutation *perm*

6.1.3.61 ip() [1/2]

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::ip (
            const Eigen::MatrixBase< Derived > & phi,
            const Eigen::MatrixBase< Derived > & psi,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Generalized inner product.

Parameters

phi	Column vector Eigen expression
psi	Column vector Eigen expression
subsys	Subsystem indexes over which *phi* is defined
dims	Dimensions of the multi-partite system

Returns

Inner product $\langle \phi_{subsys} | \psi \rangle$, as a scalar or column vector over the remaining Hilbert space

6.1.3.62 ip() [2/2]

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::ip (
            const Eigen::MatrixBase< Derived > & phi,
            const Eigen::MatrixBase< Derived > & psi,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Generalized inner product.

Parameters

phi	Column vector Eigen expression
psi	Column vector Eigen expression
subsys	Subsystem indexes over which *phi* is defined
d	Subsystem dimensions

Returns

Inner product $\langle \phi_{subsys} | \psi \rangle$, as a scalar or column vector over the remaining Hilbert space

6.1.3.63 isprime()

```
bool qpp::isprime (
            bigint p,
            idx k = 80 )  [inline]
```

Primality test based on the Miller-Rabin's algorithm.

Parameters

p	Integer different from 0, 1 or -1
k	Number of iterations. The probability of a false positive is 2^{-k}.

Returns

True if the number is (most-likely) prime, false otherwise

6.1.3.64 kraus2choi()

```
cmat qpp::kraus2choi (
            const std::vector< cmat > & Ks )  [inline]
```

Choi matrix.

See also

qpp::choi2kraus()

Constructs the Choi matrix of the channel specified by the set of Kraus operators *Ks* in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

Note

The superoperator matrix S and the Choi matrix C are related by $S_{ab,mn} = C_{ma,nb}$

Parameters

Ks	Set of Kraus operators

Returns

Choi matrix

6.1.3.65 kraus2super()

```
cmat qpp::kraus2super (
             const std::vector< cmat > & Ks )  [inline]
```

Superoperator matrix.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators *Ks* in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

Parameters

Ks	Set of Kraus operators

Returns

Superoperator matrix

6.1.3.66 kron() [1/4]

```
template<typename T >
dyn_mat<typename T::Scalar> qpp::kron (
             const T & head )
```

Kronecker product.

See also

qpp::kronpow()

Used to stop the recursion for the variadic template version of qpp::kron()

Parameters

head	Eigen expression

Returns

Its argument *head*

6.1.3.67 kron() [2/4]

```
template<typename T , typename ...  Args>
dyn_mat<typename T::Scalar> qpp::kron (
             const T & head,
             const Args &...  tail )
```

Kronecker product.

See also

qpp::kronpow()

Parameters

head	Eigen expression
tail	Variadic Eigen expression (zero or more parameters)

Returns

Kronecker product of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.68 kron() [3/4]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::kron (
             const std::vector< Derived > & As )
```

Kronecker product.

See also

qpp::kronpow()

Parameters

As	std::vector of Eigen expressions

Returns

Kronecker product of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.69 kron() [4/4]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::kron (
             const std::initializer_list< Derived > & As )
```

Kronecker product.

See also

qpp::kronpow()

Parameters

As	std::initializer_list of Eigen expressions, such as *{A1*, A2, ... ,Ak}

Returns

Kronecker product of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.70 kronpow()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::kronpow (
             const Eigen::MatrixBase< Derived > & A,
             idx n )
```

Kronecker power.

See also

qpp::kron()

Parameters

A	Eigen expression
n	Non-negative integer

Returns

Kronecker product of *A* with itself *n* times $A^{\otimes n}$, as a dynamic matrix over the same scalar field as *A*

6.1.3.71 lcm() [1/2]

```
bigint qpp::lcm (
            bigint a,
            bigint b )  [inline]
```

Least common multiple of two integers.

See also

qpp::gcd()

Parameters

a	Integer
b	Integer

Returns

Least common multiple of *a* and *b*

6.1.3.72 lcm() [2/2]

```
bigint qpp::lcm (
            const std::vector< bigint > & as )  [inline]
```

Least common multiple of a list of integers.

See also

qpp::gcd()

Parameters

as	List of integers

Returns

Least common multiple of all numbers in *as*

6.1.3.73 load()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::load (
             const std::string & fname )
```

Loads Eigen matrix from a binary file (internal format) in double precision.

See also

qpp::save()

The template parameter cannot be automatically deduced and must be explicitly provided, depending on the scalar field of the matrix that is being loaded.

Example:

```
// loads a previously saved Eigen dynamic complex matrix from "input.bin"
cmat mat = load<cmat>("input.bin");
```

Parameters

fname	Output file name

6.1.3.74 loadMATLAB() [1/2]

```
template<typename Derived >
std::enable_if<std::is_same<typename Derived::Scalar, cplx>::value, dyn_mat < cplx> >::type
qpp::loadMATLAB (
             const std::string & mat_file,
             const std::string & var_name )
```

Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.

See also

qpp::saveMATLAB()

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen ket
// from the MATLAB file "input.mat"
ket psi = loadMATLAB<ket>("input.mat");
```

Template Parameters

Derived	Complex Eigen type

Parameters

mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be loaded

Returns

Eigen dynamic matrix

6.1.3.75 loadMATLAB() [2/2]

```
template<typename Derived >
std::enable_if<!std::is_same<typename Derived::Scalar, cplx>::value, dyn_mat < typename Derived↩
::Scalar> >::type qpp::loadMATLAB (
             const std::string & mat_file,
             const std::string & var_name )
```

Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.

See also

qpp::saveMATLAB()

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen dynamic double matrix
// from the MATLAB file "input.mat"
dmat mat = loadMATLAB<dmat>("input.mat");
```

Template Parameters

Derived	Non-complex Eigen type

Parameters

mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be loaded

Returns

Eigen dynamic matrix

6.1.3.76 logdet()

```
template<typename Derived >
Derived::Scalar qpp::logdet (
            const Eigen::MatrixBase< Derived > & A )
```

Logarithm of the determinant.

Useful when the determinant overflows/underflows

Parameters

A	Eigen expression

Returns

Logarithm of the determinant of *A*, as a scalar over the same scalar field as *A*

6.1.3.77 logm()

```
template<typename Derived >
cmat qpp::logm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix logarithm.

Parameters

A	Eigen expression

Returns

Matrix logarithm of *A*

6.1.3.78 lognegativity() [1/2]

```
template<typename Derived >
double qpp::lognegativity (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Logarithmic negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Logarithmic negativity, with the logarithm in base 2

6.1.3.79 lognegativity() [2/2]

```
template<typename Derived >
double qpp::lognegativity (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Logarithmic negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Logarithmic negativity, with the logarithm in base 2

6.1.3.80 marginalX()

```
std::vector<double> qpp::marginalX (
            const dmat & probXY )  [inline]
```

Marginal distribution.

Parameters

probXY	Real matrix representing the joint probability distribution of *X* and *Y* in lexicographical order (*X* labels the rows, *Y* labels the columns)

Returns

Real vector consisting of the marginal distribution of *X*

6.1.3.81 marginalY()

```
std::vector<double> qpp::marginalY (
            const dmat & probXY )  [inline]
```

Marginal distribution.

Parameters

probXY	Real matrix representing the joint probability distribution of *X* and *Y* in lexicographical order (*X* labels the rows, *Y* labels the columns)

Returns

Real vector consisting of the marginal distribution of *Y*

6.1.3.82 measure() [1/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks )
```

Measures the state *A* using the set of Kraus operators *Ks*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.83 measure() [2/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::initializer_list< cmat > & Ks )
```

Measures the state *A* using the set of Kraus operators *Ks*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.84 measure() [3/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const cmat & U )
```

Measures the state *A* in the orthonormal basis specified by the unitary matrix *U*.

Parameters

A	Eigen expression
U	Unitary matrix whose columns represent the measurement basis vectors

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.85 measure() [4/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.86 measure() [5/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::initializer_list< cmat > & Ks,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.87 measure() [6/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< cmat > & Ks,
             const std::vector< idx > & subsys,
             idx d = 2 )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.88 measure() [7/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
             const Eigen::MatrixBase< Derived > & A,
             const std::initializer_list< cmat > & Ks,
             const std::vector< idx > & subsys,
             idx d = 2 )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.89 measure() [8/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const cmat & V,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 POVM specified by the matrix *V*.

See also

qpp::measure_seq()

Note

The dimension of *V* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
V	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 POVM
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.90 measure() [9/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const cmat & V,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 POVM specified by the matrix *V*.

See also

qpp::measure_seq()

Note

The dimension of *V* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
V	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 POVM
subsys	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.91 measure_seq() [1/2]

```
template<typename Derived >
std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (
            const Eigen::MatrixBase< Derived > & A,
            std::vector< idx > subsys,
            std::vector< idx > dims )
```

Sequentially measures the part *subsys* of the multi-partite state vector or density matrix *A* in the computational basis.

See also

qpp::measure()

Parameters

A	Eigen expression
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *subsys*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.92 measure_seq() [2/2]

```
template<typename Derived >
std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (
            const Eigen::MatrixBase< Derived > & A,
            std::vector< idx > subsys,
            idx d = 2 )
```

Sequentially measures the part *subsys* of the multi-partite state vector or density matrix *A* in the computational basis.

See also

qpp::measure()

Parameters

A	Eigen expression
subsys	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *subsys*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.93 mket() [1/2]

```
ket qpp::mket (
            const std::vector< idx > & mask,
            const std::vector< idx > & dims ) [inline]
```

Multi-partite qudit ket.

Constructs the multi-partite qudit ket $|\mathrm{mask}\rangle$, where *mask* is a std::vector of non-negative integers. Each element in *mask* has to be smaller than the corresponding element in *dims*.

Parameters

mask	std::vector of non-negative integers
dims	Dimensions of the multi-partite system

Returns

Multi-partite qudit state vector, as a complex dynamic column vector

6.1.3.94 mket() [2/2]

```
ket qpp::mket (
            const std::vector< idx > & mask,
            idx d = 2 )  [inline]
```

Multi-partite qudit ket.

Constructs the multi-partite qudit ket $|\mathrm{mask}\rangle$, all subsystem having equal dimension *d*. *mask* is a std::vector of non-negative integers, and each element in *mask* has to be strictly smaller than *d*.

Parameters

mask	std::vector of non-negative integers
d	Subsystem dimensions

Returns

Multi-partite qudit state vector, as a complex dynamic column vector

6.1.3.95 modinv()

```
bigint qpp::modinv (
            bigint a,
            bigint p )  [inline]
```

Modular inverse of *a* mod *p*.

See also

qpp::egcd()

Note

a and *p* must be co-prime

Parameters

a	Non-negative integer
p	Non-negative integer

Returns

Modular inverse $a^{-1} \mod p$

6.1.3.96 modmul()

```
bigint qpp::modmul (
            bigint a,
            bigint b,
            bigint p )  [inline]
```

Modular multiplication without overflow.

Computes $ab \bmod p$ without overflow

Parameters

a	Integer
b	Integer
p	Positive integer

Returns

$ab \bmod p$ avoiding overflow

6.1.3.97 modpow()

```
bigint qpp::modpow (
            bigint a,
            bigint n,
            bigint p )  [inline]
```

Fast integer power modulo *p* based on the SQUARE-AND-MULTIPLY algorithm.

Note

Uses qpp::modmul() that avoids overflows

Computes $a^n \bmod p$

Parameters

a	Non-negative integer
n	Non-negative integer
p	Strictly positive integer

Returns

$a^n \bmod p$

6.1.3.98 mprj() [1/2]

```
cmat qpp::mprj (
            const std::vector< idx > & mask,
            const std::vector< idx > & dims )  [inline]
```

Projector onto multi-partite qudit ket.

Constructs the projector onto the multi-partite qudit ket $|\mathrm{mask}\rangle$, where *mask* is a std::vector of non-negative integers. Each element in *mask* has to be smaller than the corresponding element in *dims*.

Parameters

mask	std::vector of non-negative integers
dims	Dimensions of the multi-partite system

Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

6.1.3.99 mprj() [2/2]

```
cmat qpp::mprj (
            const std::vector< idx > & mask,
            idx d = 2 )  [inline]
```

Projector onto multi-partite qudit ket.

Constructs the projector onto the multi-partite qudit ket $|\mathrm{mask}\rangle$, all subsystem having equal dimension *d*. *mask* is a std::vector of non-negative integers, and each element in *mask* has to be strictly smaller than *d*.

Parameters

mask	std::vector of non-negative integers
d	Subsystem dimensions

Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

6.1.3.100 multiidx2n()

```
idx qpp::multiidx2n (
            const std::vector< idx > & midx,
            const std::vector< idx > & dims )  [inline]
```

Multi-index to non-negative integer index.

See also

qpp::n2multiidx()

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

Parameters

midx	Multi-index
dims	Dimensions of the multi-partite system

Returns

Non-negative integer index

6.1.3.101 n2multiidx()

```
std::vector<idx> qpp::n2multiidx (
            idx n,
            const std::vector< idx > & dims )  [inline]
```

Non-negative integer index to multi-index.

See also

qpp::multiidx2n()

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

Parameters

n	Non-negative integer index
dims	Dimensions of the multi-partite system

Returns

Multi-index of the same size as *dims*

6.1.3.102 negativity() [1/2]

```
template<typename Derived >
double qpp::negativity (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Negativity

6.1.3.103 negativity() [2/2]

```
template<typename Derived >
double qpp::negativity (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Negativity

6.1.3.104 norm()

```
template<typename Derived >
double qpp::norm (
            const Eigen::MatrixBase< Derived > & A )
```

Frobenius norm.

Parameters

A	Eigen expression

Returns

Frobenius norm of *A*

6.1.3.105 omega()

```
cplx qpp::omega (
             idx D )  [inline]
```

D-th root of unity.

Parameters

D	Non-negative integer

Returns

D-th root of unity $\exp(2\pi i/D)$

6.1.3.106 operator"""" _i() [1/2]

```
constexpr cplx qpp::operator"" _i (
             unsigned long long int x )  [inline], [noexcept]
```

User-defined literal for complex $i = \sqrt{-1}$ (integer overload)

Example:

```
cplx z = 4_i; // type of z is std::complex<double>
```

6.1.3.107 operator"""" _i() [2/2]

```
constexpr cplx qpp::operator"" _i (
             long double x )  [inline], [noexcept]
```

User-defined literal for complex $i = \sqrt{-1}$ (real overload)

Example:

```
cplx z = 4.5_i; // type of z is std::complex<double>
```

6.1.3.108 powm()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::powm (
            const Eigen::MatrixBase< Derived > & A,
            idx n )
```

Fast matrix power based on the SQUARE-AND-MULTIPLY algorithm.

See also

qpp::spectralpowm()

Explicitly multiplies the matrix *A* with itself *n* times. By convention $A^0 = I$.

Parameters

A	Eigen expression
n	Non-negative integer

Returns

Matrix power A^n, as a dynamic matrix over the same scalar field as *A*

6.1.3.109 prj()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::prj (
            const Eigen::MatrixBase< Derived > & A )
```

Projector.

Normalized projector onto state vector

Parameters

A	Eigen expression

Returns

Projector onto the state vector *A*, or the matrix *Zero* if *A* has norm zero (i.e. smaller than qpp::eps), as a dynamic matrix over the same scalar field as *A*

6.1.3.110 prod() [1/3]

```
template<typename Derived >
Derived::Scalar qpp::prod (
            const Eigen::MatrixBase< Derived > & A )
```

Element-wise product of *A*.

Parameters

A	Eigen expression

Returns

Element-wise product of *A*, as a scalar over the same scalar field as *A*

6.1.3.111 prod() [2/3]

```
template<typename InputIterator >
std::iterator_traits<InputIterator>::value_type qpp::prod (
            InputIterator first,
            InputIterator last )
```

Element-wise product of an STL-like range.

Parameters

first	Iterator to the first element of the range
last	Iterator to the last element of the range

Returns

Element-wise product of the range, as a scalar over the same scalar field as the range

6.1.3.112 prod() [3/3]

```
template<typename Container >
Container::value_type qpp::prod (
            const Container & c,
            typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Element-wise product of the elements of an STL-like container.

Parameters

c	STL-like container

Returns

Element-wise product of the elements of the container, as a scalar over the same scalar field as the container

6.1.3.113 ptrace() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Partial trace.

See also

qpp::ptrace1(), qpp::ptrace2()

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

Parameters

A	Eigen expression
subsys	Subsystem indexes
dims	Dimensions of the multi-partite system

Returns

Partial trace $Tr_{subsys}(\cdot)$ over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.114 ptrace() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Partial trace.

See also

qpp::ptrace1(), qpp::ptrace2()

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

Parameters

A	Eigen expression
subsys	Subsystem indexes
d	Subsystem dimensions

Returns

Partial trace $Tr_{subsys}(\cdot)$ over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.115 ptrace1() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace1 (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< idx > & dims )
```

Partial trace.

See also

qpp::ptrace2()

Partial trace over the first subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Partial trace $Tr_{A}(\cdot)$ over the first subsytem A in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.116 ptrace1() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace1 (
             const Eigen::MatrixBase< Derived > & A,
             idx d = 2 )
```

Partial trace.

See also

qpp::ptrace2()

Partial trace over the first subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Partial trace $Tr_A(\cdot)$ over the first subsytem A in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.117 ptrace2() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace2 (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Partial trace.

See also

qpp::ptrace1()

Partial trace over the second subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Partial trace $Tr_B(\cdot)$ over the second subsytem B in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.118 ptrace2() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace2 (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Partial trace.

See also

qpp::ptrace1()

Partial trace over the second subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Partial trace $Tr_B(\cdot)$ over the second subsytem B in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.119 ptranspose() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptranspose (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

Parameters

A	Eigen expression
subsys	Subsystem indexes
dims	Dimensions of the multi-partite system

Returns

Partial transpose $(\cdot)^{T_{subsys}}$ over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.120 ptranspose() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptranspose (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

Parameters

A	Eigen expression
subsys	Subsystem indexes
d	Subsystem dimensions

Returns

Partial transpose $(\cdot)^{T_{subsys}}$ over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.121 qmutualinfo() [1/2]

```
template<typename Derived >
double qpp::qmutualinfo (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsysA,
            const std::vector< idx > & subsysB,
            const std::vector< idx > & dims )
```

Quantum mutual information between 2 subsystems of a composite system.

Parameters

A	Eigen expression
subsysA	Indexes of the first subsystem
subsysB	Indexes of the second subsystem
dims	Dimensions of the multi-partite system

Returns

Mutual information between the 2 subsystems

6.1.3.122 qmutualinfo() [2/2]

```
template<typename Derived >
double qpp::qmutualinfo (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsysA,
            const std::vector< idx > & subsysB,
            idx d = 2 )
```

Quantum mutual information between 2 subsystems of a composite system.

Parameters

A	Eigen expression
subsysA	Indexes of the first subsystem
subsysB	Indexes of the second subsystem
d	Subsystem dimensions

Returns

Mutual information between the 2 subsystems

6.1.3.123 rand() [1/5]

```
double qpp::rand (
            double a,
            double b )  [inline]
```

Generates a random real number uniformly distributed in the interval [a, b)

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

Returns

Random real number (double) uniformly distributed in the interval [a, b)

6.1.3.124 rand() [2/5]

```
bigint qpp::rand (
            bigint a,
            bigint b )  [inline]
```

Generates a random big integer uniformly distributed in the interval [a, b].

Note

To avoid ambiguity with double qpp::rand(double, double) cast at least one of the arguments to qpp::bigint

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, belongs to it

Returns

Random big integer uniformly distributed in the interval [a, b]

6.1.3.125 rand() [3/5]

```
template<typename Derived >
Derived qpp::rand (
            idx rows,
            idx cols,
            double a = 0,
            double b = 1 )
```

Generates a random matrix with entries uniformly distributed in the interval [a, b)

If complex, then both real and imaginary parts are uniformly distributed in [a, b)

This is the generic version that always throws qpp::Exception::Type::UNDEFINED_TYPE. It is specialized only for qpp::dmat and qpp::cmat

6.1.3.126 rand() [4/5]

```
template<>
dmat qpp::rand (
            idx rows,
            idx cols,
            double a,
            double b )  [inline]
```

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries uniformly distributed in [-1,1)
dmat mat = rand<dmat>(3, 3, -1, 1);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
a	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

Returns

Random real matrix

6.1.3.127 rand() [5/5]

```
template<>
cmat qpp::rand (
             idx rows,
             idx cols,
             double a,
             double b )  [inline]
```

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) uniformly distributed in [-1,1)
cmat mat = rand<cmat>(3, 3, -1, 1);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
a	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

Returns

Random complex matrix

6.1.3.128 randH()

```
cmat qpp::randH (
             idx D = 2 )  [inline]
```

Generates a random Hermitian matrix.

Parameters

D	Dimension of the Hilbert space

Returns

Random Hermitian matrix

6.1.3.129 randidx()

```
idx qpp::randidx (
            idx a = std::numeric_limits<idx>::min(),
            idx b = std::numeric_limits<idx>::max() )  [inline]
```

Generates a random index (idx) uniformly distributed in the interval [a, b].

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, belongs to it

Returns

Random index (idx) uniformly distributed in the interval [a, b]

6.1.3.130 randket()

```
ket qpp::randket (
            idx D = 2 )  [inline]
```

Generates a random normalized ket (pure state vector)

Parameters

D	Dimension of the Hilbert space

Returns

Random normalized ket

6.1.3.131 randkraus()

```
std::vector<cmat> qpp::randkraus (
            idx N,
            idx D = 2 )  [inline]
```

Generates a set of random Kraus operators.

Note

The set of Kraus operators satisfy the closure condition $\sum_i K_i^\dagger K_i = I$

Parameters

N	Number of Kraus operators
D	Dimension of the Hilbert space

Returns

Set of *N* Kraus operators satisfying the closure condition

6.1.3.132 randn() [1/4]

```
template<typename Derived >
Derived qpp::randn (
             idx rows,
             idx cols,
             double mean = 0,
             double sigma = 1 )
```

Generates a random matrix with entries normally distributed in N(mean, sigma)

If complex, then both real and imaginary parts are normally distributed in N(mean, sigma)

This is the generic version that always throws qpp::Exception::Type::UNDEFINED_TYPE. It is specialized only for qpp::dmat and qpp::cmat

6.1.3.133 randn() [2/4]

```
template<>
dmat qpp::randn (
             idx rows,
             idx cols,
             double mean,
             double sigma )  [inline]
```

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries normally distributed in N(0,2)
dmat mat = randn<dmat>(3, 3, 0, 2);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
mean	Mean
sigma	Standard deviation

Returns

Random real matrix

6.1.3.134 randn() [3/4]

```
template<>
cmat qpp::randn (
            idx rows,
            idx cols,
            double mean,
            double sigma )  [inline]
```

Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) normally distributed in N(0,2)
cmat mat = randn<cmat>(3, 3, 0, 2);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
mean	Mean
sigma	Standard deviation

Returns

Random complex matrix

6.1.3.135 randn() [4/4]

```
double qpp::randn (
            double mean = 0,
            double sigma = 1 )  [inline]
```

Generates a random real number (double) normally distributed in N(mean, sigma)

Parameters

mean	Mean
sigma	Standard deviation

Returns

Random real number normally distributed in N(mean, sigma)

6.1.3.136 randperm()

```
std::vector<idx> qpp::randperm (
             idx N )  [inline]
```

Generates a random uniformly distributed permutation.

Uses Knuth shuffle method (as implemented by std::shuffle), so that all permutations are equally probable

Parameters

N	Size of the permutation

Returns

Random permutation of size *N*

6.1.3.137 randprime()

```
bigint qpp::randprime (
             bigint a,
             bigint b,
             idx N = 1000 )  [inline]
```

Generates a random big prime uniformly distributed in the interval [a, b].

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, belongs to it
N	Maximum number of candidates

Returns

Random big integer uniformly distributed in the interval [a, b]

6.1.3.138 randprob()

```
std::vector<double> qpp::randprob (
            idx N )  [inline]
```

Generates a random probability vector uniformly distributed over the probability simplex.

Parameters

N	Size of the probability vector

Returns

Random probability vector

6.1.3.139 randrho()

```
cmat qpp::randrho (
            idx D = 2 )  [inline]
```

Generates a random density matrix.

Parameters

D	Dimension of the Hilbert space

Returns

Random density matrix

6.1.3.140 randU()

```
cmat qpp::randU (
            idx D = 2 )  [inline]
```

Generates a random unitary matrix.

Parameters

D	Dimension of the Hilbert space

Returns

Random unitary

6.1.3.141 randV()

```
cmat qpp::randV (
            idx Din,
            idx Dout )  [inline]
```

Generates a random isometry matrix.

Parameters

Din	Size of the input Hilbert space
Dout	Size of the output Hilbert space

Returns

Random isometry matrix

6.1.3.142 renyi() [1/2]

```
template<typename Derived >
double qpp::renyi (
            const Eigen::MatrixBase< Derived > & A,
            double alpha )
```

Renyi- α entropy of the density matrix *A*, for $\alpha \geq 0$.

Note

When $\alpha \to 1$ the Renyi entropy converges to the von-Neumann entropy, with the logarithm in base 2

Parameters

A	Eigen expression
alpha	Non-negative real number, use qpp::infty for $\alpha = \infty$

Returns

Renyi- α entropy, with the logarithm in base 2

6.1.3.143 renyi() [2/2]

```
double qpp::renyi (
            const std::vector< double > & prob,
            double alpha )  [inline]
```

Renyi- α entropy of the probability distribution *prob*, for $\alpha \geq 0$.

Note

When $\alpha \rightarrow 1$ the Renyi entropy converges to the Shannon entropy, with the logarithm in base 2

Parameters

prob	Real probability vector
alpha	Non-negative real number, use qpp::infty for $\alpha = \infty$

Returns

Renyi- α entropy, with the logarithm in base 2

6.1.3.144 reshape()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::reshape (
            const Eigen::MatrixBase< Derived > & A,
            idx rows,
            idx cols )
```

Reshape.

Uses column-major order when reshaping (same as MATLAB)

Parameters

A	Eigen expression
rows	Number of rows of the reshaped matrix
cols	Number of columns of the reshaped matrix

Returns

Reshaped matrix with *rows* rows and *cols* columns, as a dynamic matrix over the same scalar field as *A*

6.1.3.145 rho2bloch()

```
template<typename Derived >
std::vector<double> qpp::rho2bloch (
            const Eigen::MatrixBase< Derived > & A )
```

Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix *A*.

See also

qpp::bloch2rho()

Note

It is implicitly assumed that the density matrix is Hermitian

Parameters

A	Eigen expression

Returns

3-dimensional Bloch vector

6.1.3.146 rho2pure()

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::rho2pure (
            const Eigen::MatrixBase< Derived > & A )
```

Finds the pure state representation of a matrix proportional to a projector onto a pure state.

Note

No purity check is done, the input state *A* must have rank one, otherwise the function returns the first non-zero eigenvector of *A*

Parameters

A	Eigen expression, assumed to be proportional to a projector onto a pure state, i.e. *A* is assumed to have rank one

Returns

The unique non-zero eigenvector of *A* (up to a phase), as a dynamic column vector over the same scalar field as *A*

6.1.3.147 save()

```
template<typename Derived >
void qpp::save (
             const Eigen::MatrixBase< Derived > & A,
             const std::string & fname )
```

Saves Eigen expression to a binary file (internal format) in double precision.

See also

qpp::load()

Parameters

A	Eigen expression
fname	Output file name

6.1.3.148 saveMATLAB() [1/2]

```
template<typename Derived >
std::enable_if<std::is_same<typename Derived::Scalar, cplx>::value>::type qpp::saveMATLAB (
             const Eigen::MatrixBase< Derived > & A,
             const std::string & mat_file,
             const std::string & var_name,
             const std::string & mode )
```

Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.

See also

qpp::loadMATLAB()

Template Parameters

Complex	Eigen type

Parameters

A	Eigen expression over the complex field

Parameters

mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be saved
mode	Saving mode (append, overwrite etc.), see MATLAB *matOpen()* documentation for details

6.1.3.149 saveMATLAB() [2/2]

```
template<typename Derived >
std::enable_if<!std::is_same<typename Derived::Scalar, cplx>::value>::type qpp::saveMATLAB (
            const Eigen::MatrixBase< Derived > & A,
            const std::string & mat_file,
            const std::string & var_name,
            const std::string & mode )
```

Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.

See also

qpp::loadMATLAB()

Template Parameters

Npn-complex	Eigen type

Parameters

A	Non-complex Eigen expression
mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be saved
mode	Saving mode (append, overwrite etc.), see MATLAB *matOpen()* documentation for details

6.1.3.150 schatten()

```
template<typename Derived >
double qpp::schatten (
            const Eigen::MatrixBase< Derived > & A,
            double p )
```

Schatten matrix norm.

Parameters

A	Eigen expression
p	Real number, greater or equal to 1, use qpp::infty for $p = \infty$

Returns

Schatten-*p* matrix norm of *A*

6.1.3.151 schmidtA() [1/2]

```
template<typename Derived >
cmat qpp::schmidtA (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Schmidt basis on Alice side.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Unitary matrix U whose columns represent the Schmidt basis vectors on Alice side.

6.1.3.152 schmidtA() [2/2]

```
template<typename Derived >
cmat qpp::schmidtA (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Schmidt basis on Alice side.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Unitary matrix U whose columns represent the Schmidt basis vectors on Alice side.

6.1.3.153 schmidtB() [1/2]

```
template<typename Derived >
cmat qpp::schmidtB (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< idx > & dims )
```

Schmidt basis on Bob side.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Unitary matrix V whose columns represent the Schmidt basis vectors on Bob side.

6.1.3.154 schmidtB() [2/2]

```
template<typename Derived >
cmat qpp::schmidtB (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Schmidt basis on Bob side.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Unitary matrix V whose columns represent the Schmidt basis vectors on Bob side.

6.1.3.155 schmidtcoeffs() [1/2]

```
template<typename Derived >
dyn_col_vect<double> qpp::schmidtcoeffs (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Schmidt coefficients of the bi-partite pure state *A*.

Note

The sum of the squares of the Schmidt coefficients equals 1

See also

qpp::schmidtprobs()

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Schmidt coefficients of *A*, ordered in decreasing order, as a real dynamic column vector

6.1.3.156 schmidtcoeffs() [2/2]

```
template<typename Derived >
dyn_col_vect<double> qpp::schmidtcoeffs (
             const Eigen::MatrixBase< Derived > & A,
             idx d = 2 )
```

Schmidt coefficients of the bi-partite pure state *A*.

Note

The sum of the squares of the Schmidt coefficients equals 1

See also

qpp::schmidtprobs()

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Schmidt coefficients of *A*, ordered in decreasing order, as a real dynamic column vector

6.1.3.157 schmidtprobs() [1/2]

```
template<typename Derived >
std::vector<double> qpp::schmidtprobs (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< idx > & dims )
```

Schmidt probabilities of the bi-partite pure state *A*.

Defined as the squares of the Schmidt coefficients. The sum of the Schmidt probabilities equals 1.

See also

qpp::schmidtcoeffs()

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Real vector consisting of the Schmidt probabilites of *A*, ordered in decreasing order

6.1.3.158 schmidtprobs() [2/2]

```
template<typename Derived >
std::vector<double> qpp::schmidtprobs (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Schmidt probabilities of the bi-partite pure state *A*.

Defined as the squares of the Schmidt coefficients. The sum of the Schmidt probabilities equals 1.

See also

qpp::schmidtcoeffs()

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Real vector consisting of the Schmidt probabilites of *A*, ordered in decreasing order

6.1.3.159 sigma()

```
template<typename Container >
double qpp::sigma (
            const std::vector< double > & prob,
            const Container & X,
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Standard deviation.

Parameters

prob	Real probability vector representing the probability distribution of *X*
X	Real random variable values represented by an STL-like container

Returns

Standard deviation of *X*

6.1.3.160 sinm()

```
template<typename Derived >
cmat qpp::sinm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix sin.

Parameters

A	Eigen expression

Returns

Matrix sine of *A*

6.1.3.161 spectralpowm()

```
template<typename Derived >
cmat qpp::spectralpowm (
            const Eigen::MatrixBase< Derived > & A,
            const cplx z )
```

Matrix power.

See also

qpp::powm()

Uses the spectral decomposition of *A* to compute the matrix power. By convention $A^0 = I$.

Parameters

A	Eigen expression
z	Complex number

Returns

Matrix power A^z

6.1.3.162 sqrtm()

```
template<typename Derived >
cmat qpp::sqrtm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix square root.

Parameters

A	Eigen expression

Returns

Matrix square root of *A*

6.1.3.163 sum() [1/3]

```
template<typename Derived >
Derived::Scalar qpp::sum (
            const Eigen::MatrixBase< Derived > & A )
```

Element-wise sum of *A*.

Parameters

A	Eigen expression

Returns

Element-wise sum of *A*, as a scalar over the same scalar field as *A*

6.1.3.164 sum() [2/3]

```
template<typename InputIterator >
std::iterator_traits<InputIterator>::value_type qpp::sum (
            InputIterator first,
            InputIterator last )
```

Element-wise sum of an STL-like range.

Parameters

first	Iterator to the first element of the range
last	Iterator to the last element of the range

Returns

Element-wise sum of the range, as a scalar over the same scalar field as the range

6.1.3.165 sum() [3/3]

```
template<typename Container >
Container::value_type qpp::sum (
            const Container & c,
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Element-wise sum of the elements of an STL-like container.

Parameters

c	STL-like container

Returns

Element-wise sum of the elements of the container, as a scalar over the same scalar field as the container

6.1.3.166 super2choi()

```
cmat qpp::super2choi (
            const cmat & A )  [inline]
```

Converts superoperator matrix to Choi matrix.

See also

qpp::choi2super()

Parameters

A	Superoperator matrix

Returns

Choi matrix

6.1.3.167 svals()

```
template<typename Derived >
dyn_col_vect<double> qpp::svals (
             const Eigen::MatrixBase< Derived > & A )
```

Singular values.

Parameters

A	Eigen expression

Returns

Singular values of *A*, ordered in decreasing order, as a real dynamic column vector

6.1.3.168 svd()

```
template<typename Derived >
std::tuple<cmat, dyn_col_vect < double>, cmat> qpp::svd (
             const Eigen::MatrixBase< Derived > & A )
```

Full singular value decomposition.

Parameters

A	Eigen expression

Returns

Tuple of: 1. Left sigular vectors of *A*, as columns of a complex dynamic matrix, 2. Singular values of *A*, ordered in decreasing order, as a real dynamic column vector, and 3. Right singular vectors of *A*, as columns of a complex dynamic matrix

6.1.3.169 svdU()

```
template<typename Derived >
cmat qpp::svdU (
             const Eigen::MatrixBase< Derived > & A )
```

Left singular vectors.

Parameters

A	Eigen expression

Returns

Complex dynamic matrix, whose columns are the left singular vectors of *A*

6.1.3.170 svdV()

```
template<typename Derived >
cmat qpp::svdV (
             const Eigen::MatrixBase< Derived > & A )
```

Right singular vectors.

Parameters

A	Eigen expression

Returns

Complex dynamic matrix, whose columns are the right singular vectors of *A*

6.1.3.171 syspermute() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::syspermute (
             const Eigen::MatrixBase< Derived > & A,
             const std::vector< idx > & perm,
             const std::vector< idx > & dims )
```

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit *perm*[*i*] is permuted to the location *i*.

Parameters

A	Eigen expression
perm	Permutation
dims	Dimensions of the multi-partite system

Returns

Permuted system, as a dynamic matrix over the same scalar field as *A*

6.1.3.172 syspermute() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::syspermute (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & perm,
            idx d = 2 )
```

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit *perm*[*i*] is permuted to the location *i*.

Parameters

A	Eigen expression
perm	Permutation
d	Subsystem dimensions

Returns

Permuted system, as a dynamic matrix over the same scalar field as *A*

6.1.3.173 trace()

```
template<typename Derived >
Derived::Scalar qpp::trace (
            const Eigen::MatrixBase< Derived > & A )
```

Trace.

Parameters

A	Eigen expression

Returns

Trace of *A*, as a scalar over the same scalar field as *A*

6.1.3.174 transpose()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::transpose (
            const Eigen::MatrixBase< Derived > & A )
```

Transpose.

Parameters

A	Eigen expression

Returns

Transpose of *A*, as a dynamic matrix over the same scalar field as *A*

6.1.3.175 tsallis() [1/2]

```
template<typename Derived >
double qpp::tsallis (
            const Eigen::MatrixBase< Derived > & A,
            double q )
```

Tsallis- q entropy of the density matrix *A*, for $q \geq 0$.

Note

When $q \to 1$ the Tsallis entropy converges to the von-Neumann entropy, with the logarithm in base e

Parameters

A	Eigen expression
q	Non-negative real number

Returns

Tsallis- q entropy

6.1.3.176 tsallis() [2/2]

```
double qpp::tsallis (
            const std::vector< double > & prob,
            double q ) [inline]
```

Tsallis- q entropy of the probability distribution *prob*, for $q \geq 0$.

Note

When $q \to 1$ the Tsallis entropy converges to the Shannon entropy, with the logarithm in base e

Parameters

prob	Real probability vector
q	Non-negative real number

Returns

Tsallis- q entropy

6.1.3.177 uniform()

```
std::vector<double> qpp::uniform (
            idx N )  [inline]
```

Uniform probability distribution vector.

Parameters

N	Size of the alphabet

Returns

Real vector consisting of a uniform distribution of size *N*

6.1.3.178 var()

```
template<typename Container >
double qpp::var (
            const std::vector< double > & prob,
            const Container & X,
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Variance.

Parameters

prob	Real probability vector representing the probability distribution of *X*
X	Real random variable values represented by an STL-like container

Returns

Variance of *X*

6.1.3.179 x2contfrac()

```
std::vector<int> qpp::x2contfrac (
             double x,
             idx N,
             idx cut = 1e5 )  [inline]
```

Simple continued fraction expansion.

See also

qpp::contfrac2x()

Parameters

x	Real number
N	Maximum number of terms in the expansion
cut	Stop the expansion when the next term is greater than *cut*

Returns

Integer vector containing the simple continued fraction expansion of *x*. If there are *M* less than *N* terms in the expansion, a shorter vector with *M* components is returned.

6.1.4 Variable Documentation

6.1.4.1 chop

```
constexpr double qpp::chop = 1e-10
```

Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.

6.1.4.2 ee

```
constexpr double qpp::ee = 2.718281828459045235360287471352662497
```

Base of natural logarithm, e.

6.1.4.3 eps

```
constexpr double qpp::eps = 1e-12
```

Used to decide whether a number or expression in double precision is zero or not.

Example:

```
if(std::abs(x) < qpp::eps) // x is zero
```

6.1.4.4 infty

```
constexpr double qpp::infty = std::numeric_limits<double>::max()
```

Used to denote infinity in double precision.

6.1.4.5 maxn

```
constexpr idx qpp::maxn = 64
```

Maximum number of allowed qubits/qudits (subsystems)

Used internally to allocate arrays on the stack (for performance reasons):

6.1.4.6 pi

```
constexpr double qpp::pi = 3.141592653589793238462643383279502884
```

π

6.2 qpp::exception Namespace Reference

Quantum++ exception hierarchy namespace.

Classes

- class CustomException

  Custom exception.
- class DimsInvalid

  Invalid dimension(s) exception.
- class DimsMismatchCvector

  Dimension(s) mismatch column vector size exception.
- class DimsMismatchMatrix

  Dimension(s) mismatch matrix size exception.
- class DimsMismatchRvector

  Dimension(s) mismatch row vector size exception.
- class DimsMismatchVector

  Dimension(s) mismatch vector size exception.
- class DimsNotEqual

  Dimensions not equal exception.
- class Exception

  Base class for generating Quantum++ custom exceptions.
- class MatrixMismatchSubsys

  Matrix mismatch subsystems exception.
- class MatrixNotCvector

  Matrix is not a column vector exception.
- class MatrixNotRvector

  Matrix is not a row vector exception.
- class MatrixNotSquare

  Matrix is not square exception.
- class MatrixNotSquareNorCvector

  Matrix is not square nor column vector exception.
- class MatrixNotSquareNorRvector

  Matrix is not square nor row vector exception.
- class MatrixNotSquareNorVector

  Matrix is not square nor vector exception.
- class MatrixNotVector

  Matrix is not a vector exception.
- class NoCodeword

  Codeword does not exist exception.
- class NotBipartite

  Not bi-partite exception.
- class NotQubitCvector

  Column vector is not 2 x 1 exception.
- class NotQubitMatrix

  Matrix is not 2 x 2 exception.
- class NotQubitRvector

  Row vector is not 1 x 2 exception.
- class NotQubitSubsys

  Subsystems are not qubits exception.
- class NotQubitVector

  Vector is not 2 x 1 nor 1 x 2 exception.
- class OutOfRange

  Parameter out of range exception.
- class PermInvalid

Invalid permutation exception.

- class PermMismatchDims

  Permutation mismatch dimensions exception.
- class SizeMismatch

  Size mismatch exception.
- class SubsysMismatchDims

  Subsystems mismatch dimensions exception.
- class TypeMismatch

  Type mismatch exception.
- class UndefinedType

  Not defined for this type exception.
- class Unknown

  Unknown exception.
- class ZeroSize

  Object has zero size exception.

6.2.1 Detailed Description

Quantum++ exception hierarchy namespace.

6.3 qpp::experimental Namespace Reference

Experimental/test functions/classes, do not use or modify.

6.3.1 Detailed Description

Experimental/test functions/classes, do not use or modify.

6.4 qpp::internal Namespace Reference

Internal utility functions, do not use them directly or modify them.

Classes

- struct Display_Impl_
- class IOManipEigen
- class IOManipPointer
- class IOManipRange
- class Singleton

  Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

Functions

- void n2multiidx (idx n, idx numdims, const idx ∗const dims, idx ∗result) noexcept
- idx multiidx2n (const idx ∗const midx, idx numdims, const idx ∗const dims) noexcept
- template< typename Derived >
  bool check_square_mat (const Eigen::MatrixBase< Derived > &A)
- template< typename Derived >
  bool check_vector (const Eigen::MatrixBase< Derived > &A)
- template< typename Derived >
  bool check_rvector (const Eigen::MatrixBase< Derived > &A)
- template< typename Derived >
  bool check_cvector (const Eigen::MatrixBase< Derived > &A)
- template< typename T >
  bool check_nonzero_size (const T &x) noexcept
- template< typename T1 , typename T2 >
  bool check_matching_sizes (const T1 &lhs, const T2 &rhs) noexcept
- bool check_dims (const std::vector< idx > &dims)
- template< typename Derived >
  bool check_dims_match_mat (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template< typename Derived >
  bool check_dims_match_cvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template< typename Derived >
  bool check_dims_match_rvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- bool check_eq_dims (const std::vector< idx > &dims, idx dim) noexcept
- bool check_subsys_match_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)
- template< typename Derived >
  bool check_qubit_matrix (const Eigen::MatrixBase< Derived > &A) noexcept
- template< typename Derived >
  bool check_qubit_cvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template< typename Derived >
  bool check_qubit_rvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template< typename Derived >
  bool check_qubit_vector (const Eigen::MatrixBase< Derived > &A) noexcept
- bool check_perm (const std::vector< idx > &perm)
- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::↩
  MatrixBase< Derived2 > &B)
- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > dirsum2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen↩
  ::MatrixBase< Derived2 > &B)
- template< typename T >
  void variadic_vector_emplace (std::vector< T > &)
- template< typename T , typename First , typename ... Args>
  void variadic_vector_emplace (std::vector< T > &v, First &&first, Args &&... args)
- idx get_num_subsys (idx sz, idx d)
- idx get_dim_subsys (idx sz, idx N)

6.4.1 Detailed Description

Internal utility functions, do not use them directly or modify them.

6.4.2 Function Documentation

6.4.2.1 check_cvector()

```
template<typename Derived >
bool qpp::internal::check_cvector (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.2 check_dims()

```
bool qpp::internal::check_dims (
            const std::vector< idx > & dims )  [inline]
```

6.4.2.3 check_dims_match_cvect()

```
template<typename Derived >
bool qpp::internal::check_dims_match_cvect (
            const std::vector< idx > & dims,
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.4 check_dims_match_mat()

```
template<typename Derived >
bool qpp::internal::check_dims_match_mat (
            const std::vector< idx > & dims,
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.5 check_dims_match_rvect()

```
template<typename Derived >
bool qpp::internal::check_dims_match_rvect (
            const std::vector< idx > & dims,
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.6 check_eq_dims()

```
bool qpp::internal::check_eq_dims (
            const std::vector< idx > & dims,
            idx dim )  [inline], [noexcept]
```

6.4.2.7 check_matching_sizes()

```
template<typename T1 , typename T2 >
bool qpp::internal::check_matching_sizes (
             const T1 & lhs,
             const T2 & rhs ) [noexcept]
```

6.4.2.8 check_nonzero_size()

```
template<typename T >
bool qpp::internal::check_nonzero_size (
             const T & x ) [noexcept]
```

6.4.2.9 check_perm()

```
bool qpp::internal::check_perm (
             const std::vector< idx > & perm ) [inline]
```

6.4.2.10 check_qubit_cvector()

```
template<typename Derived >
bool qpp::internal::check_qubit_cvector (
             const Eigen::MatrixBase< Derived > & A ) [noexcept]
```

6.4.2.11 check_qubit_matrix()

```
template<typename Derived >
bool qpp::internal::check_qubit_matrix (
             const Eigen::MatrixBase< Derived > & A ) [noexcept]
```

6.4.2.12 check_qubit_rvector()

```
template<typename Derived >
bool qpp::internal::check_qubit_rvector (
             const Eigen::MatrixBase< Derived > & A ) [noexcept]
```

6.4.2.13 check_qubit_vector()

```
template<typename Derived >
bool qpp::internal::check_qubit_vector (
            const Eigen::MatrixBase< Derived > & A ) [noexcept]
```

6.4.2.14 check_rvector()

```
template<typename Derived >
bool qpp::internal::check_rvector (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.15 check_square_mat()

```
template<typename Derived >
bool qpp::internal::check_square_mat (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.16 check_subsys_match_dims()

```
bool qpp::internal::check_subsys_match_dims (
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims ) [inline]
```

6.4.2.17 check_vector()

```
template<typename Derived >
bool qpp::internal::check_vector (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.18 dirsum2()

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::internal::dirsum2 (
            const Eigen::MatrixBase< Derived1 > & A,
            const Eigen::MatrixBase< Derived2 > & B )
```

6.4.2.19 get_dim_subsys()

```
idx qpp::internal::get_dim_subsys (
            idx sz,
            idx N )  [inline]
```

6.4.2.20 get_num_subsys()

```
idx qpp::internal::get_num_subsys (
            idx sz,
            idx d )  [inline]
```

6.4.2.21 kron2()

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::internal::kron2 (
            const Eigen::MatrixBase< Derived1 > & A,
            const Eigen::MatrixBase< Derived2 > & B )
```

6.4.2.22 multiidx2n()

```
idx qpp::internal::multiidx2n (
            const idx *const midx,
            idx numdims,
            const idx *const dims )  [inline], [noexcept]
```

6.4.2.23 n2multiidx()

```
void qpp::internal::n2multiidx (
            idx n,
            idx numdims,
            const idx *const dims,
            idx * result )  [inline], [noexcept]
```

6.4.2.24 variadic_vector_emplace() [1/2]

```
template<typename T >
void qpp::internal::variadic_vector_emplace (
            std::vector< T > &  )
```

6.4.2.25 variadic_vector_emplace() [2/2]

```
template<typename T , typename First , typename ...  Args>
void qpp::internal::variadic_vector_emplace (
            std::vector< T > & v,
            First && first,
            Args &&...  args )
```

Chapter 7

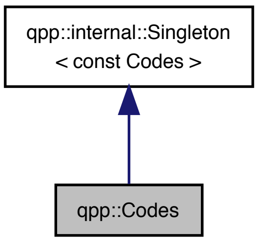
Class Documentation

7.1 qpp::Codes Class Reference

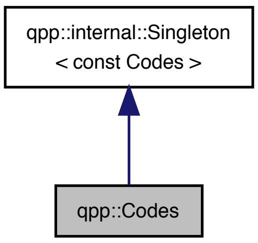
const Singleton class that defines quantum error correcting codes

`#include <classes/codes.h>`

Inheritance diagram for qpp::Codes:



Collaboration diagram for qpp::Codes:



Public Types

- enum Type { Type::FIVE_QUBIT = 1, Type::SEVEN_QUBIT_STEANE, Type::NINE_QUBIT_SHOR }

  Code types, add more codes here if needed.

Public Member Functions

- ket codeword (Type type, idx i) const

  Returns the codeword of the specified code type.

Private Member Functions

- Codes ()

  Default constructor.
- ∼Codes ()=default

  Default destructor.

Friends

- class internal::Singleton< const Codes >

Additional Inherited Members

7.1.1 Detailed Description

const Singleton class that defines quantum error correcting codes

7.1.2 Member Enumeration Documentation

7.1.2.1 Type

```
enum qpp::Codes::Type [strong]
```

Code types, add more codes here if needed.

See also

qpp::Codes::codeword()

Enumerator

FIVE_QUBIT	[[5,1,3]] qubit code
SEVEN_QUBIT_STEANE	[[7,1,3]] Steane qubit code
NINE_QUBIT_SHOR	[[9,1,3]] Shor qubit code

7.1.3 Constructor & Destructor Documentation

7.1.3.1 Codes()

```
qpp::Codes::Codes ( )  [inline], [private]
```

Default constructor.

7.1.3.2 ∼Codes()

```
qpp::Codes::∼Codes ( )  [private], [default]
```

Default destructor.

7.1.4 Member Function Documentation

7.1.4.1 codeword()

```
ket qpp::Codes::codeword (
             Type type,
             idx i ) const  [inline]
```

Returns the codeword of the specified code type.

See also

qpp::Codes::Type

Parameters

type	Code type
i	Codeword index

Returns

i-th codeword of the code *type*

7.1.5 Friends And Related Function Documentation

7.1.5.1 internal::Singleton< const Codes >

```
friend class internal::Singleton< const Codes > [friend]
```

The documentation for this class was generated from the following file:

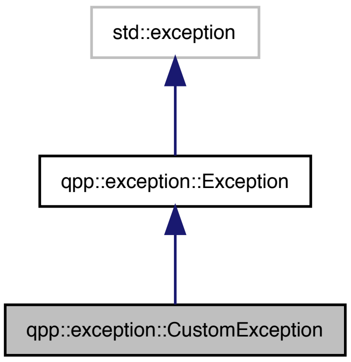
- classes/codes.h

7.2 qpp::exception::CustomException Class Reference

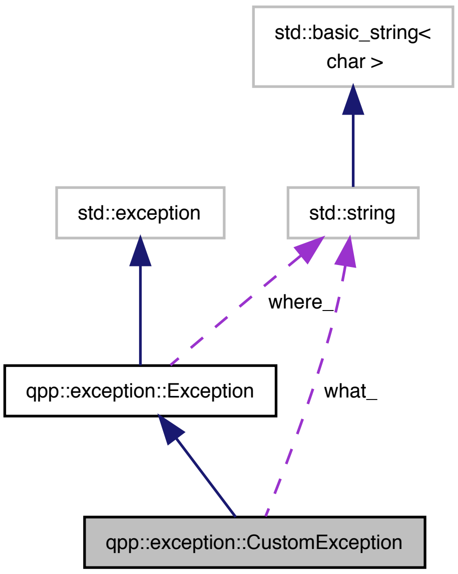
Custom exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::CustomException:



Collaboration diagram for qpp::exception::CustomException:


std::basic_string< char >
std::exception
std::string
where_
what_
qpp::exception::Exception
qpp::exception::CustomException

Public Member Functions

- CustomException (const std::string &where, const std::string &what)

Private Member Functions

- std::string type_description () const override
  Exception type description.

Private Attributes

- std::string what_ {}

7.2.1 Detailed Description

Custom exception.

Custom exception, the user must provide a custom message

7.2.2 Constructor & Destructor Documentation

7.2.2.1 CustomException()

```
qpp::exception::CustomException::CustomException (
            const std::string & where,
            const std::string & what )  [inline]
```

7.2.3 Member Function Documentation

7.2.3.1 type_description()

```
std::string qpp::exception::CustomException::type_description ( ) const  [inline], [override],
[private], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

7.2.4 Member Data Documentation

7.2.4.1 what_

```
std::string qpp::exception::CustomException::what_ {}  [private]
```

The documentation for this class was generated from the following file:

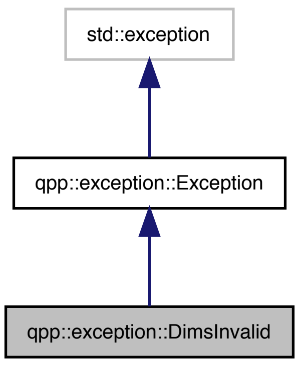
- classes/exception.h

7.3 qpp::exception::DimsInvalid Class Reference

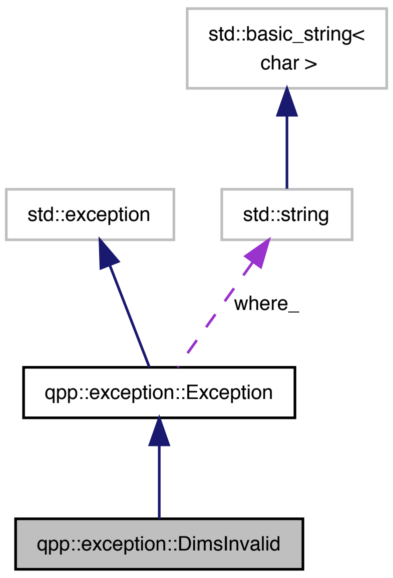
Invalid dimension(s) exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsInvalid:



Collaboration diagram for qpp::exception::DimsInvalid:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.3.1 Detailed Description

Invalid dimension(s) exception.

std::vector<idx> of dimensions has zero size or contains zeros

7.3.2 Member Function Documentation

7.3.2.1 type_description()

```
std::string qpp::exception::DimsInvalid::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

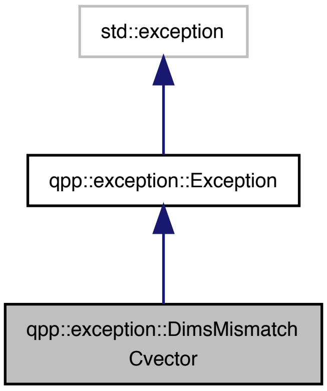
- classes/exception.h

7.4 qpp::exception::DimsMismatchCvector Class Reference

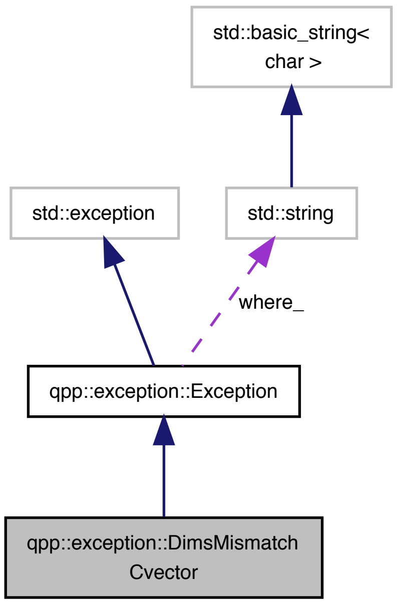
Dimension(s) mismatch column vector size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsMismatchCvector:


std::exception
qpp::exception::Exception
qpp::exception::DimsMismatch Cvector

Collaboration diagram for qpp::exception::DimsMismatchCvector:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::DimsMismatch Cvector

Public Member Functions

- std::string type_description () const override

    Exception type description.

7.4.1 Detailed Description

Dimension(s) mismatch column vector size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of the Eigen::↩
Matrix (assumed to be a column vector)

7.4.2 Member Function Documentation

7.4.2.1 type_description()

```
std::string qpp::exception::DimsMismatchCvector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

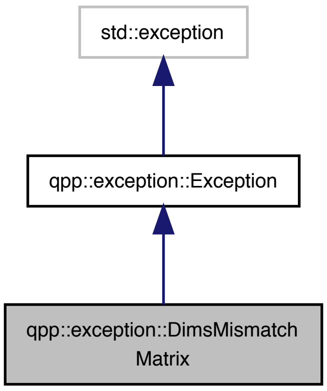
- classes/exception.h

7.5 qpp::exception::DimsMismatchMatrix Class Reference

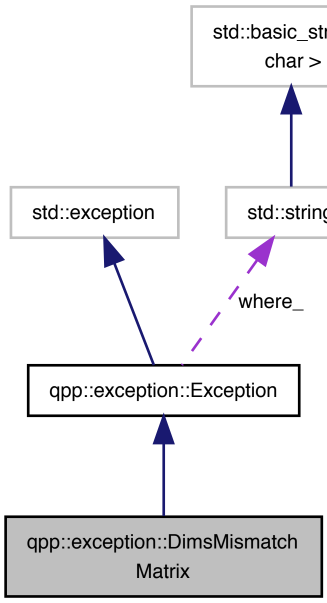
Dimension(s) mismatch matrix size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsMismatchMatrix:


std::exception
qpp::exception::Exception
qpp::exception::DimsMismatch Matrix

Collaboration diagram for qpp::exception::DimsMismatchMatrix:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::DimsMismatch Matrix

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.5.1 Detailed Description

Dimension(s) mismatch matrix size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of rows of the Eigen::Matrix (assumed to be a square matrix)

7.5.2 Member Function Documentation

7.5.2.1 type_description()

```
std::string qpp::exception::DimsMismatchMatrix::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

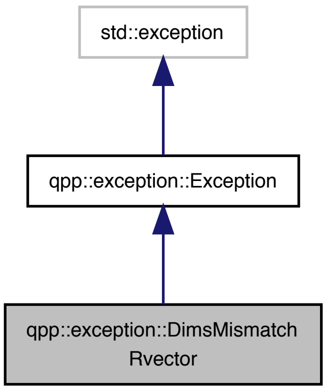
- classes/exception.h

7.6 qpp::exception::DimsMismatchRvector Class Reference

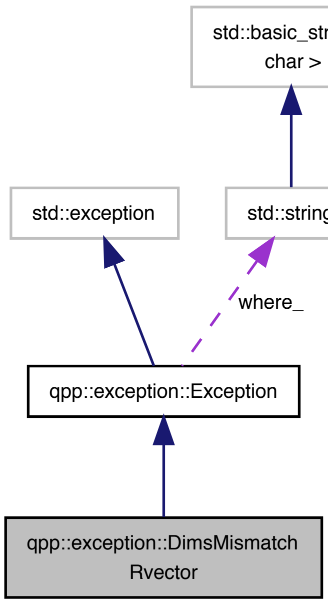
Dimension(s) mismatch row vector size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsMismatchRvector:


std::exception
qpp::exception::Exception
qpp::exception::DimsMismatch Rvector

Collaboration diagram for qpp::exception::DimsMismatchRvector:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::DimsMismatch Rvector

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.6.1 Detailed Description

Dimension(s) mismatch row vector size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of the Eigen::↩ Matrix (assumed to be a row vector)

7.6.2 Member Function Documentation

7.6.2.1 type_description()

```
std::string qpp::exception::DimsMismatchRvector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

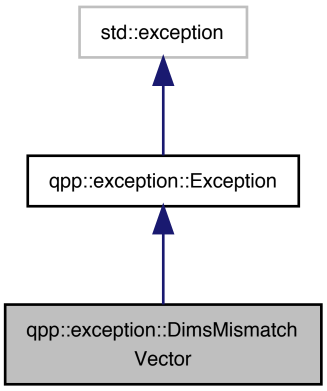
- classes/exception.h

7.7 qpp::exception::DimsMismatchVector Class Reference

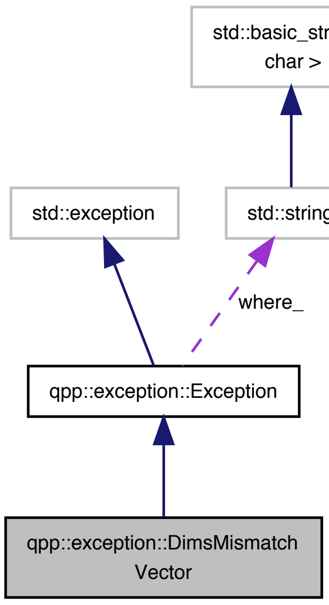
Dimension(s) mismatch vector size exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::DimsMismatchVector:


std::exception
qpp::exception::Exception
qpp::exception::DimsMismatch Vector

Collaboration diagram for qpp::exception::DimsMismatchVector:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::DimsMismatch Vector

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.7.1 Detailed Description

Dimension(s) mismatch vector size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of the Eigen::↩
Matrix (assumed to be a row/column vector)

7.7.2 Member Function Documentation

7.7.2.1 type_description()

```
std::string qpp::exception::DimsMismatchVector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

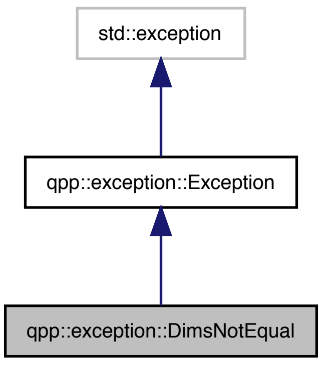
- classes/exception.h

7.8 qpp::exception::DimsNotEqual Class Reference

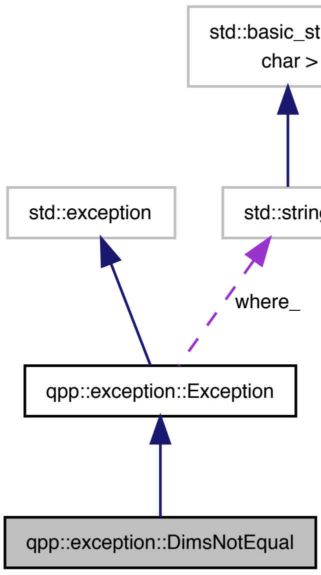
Dimensions not equal exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsNotEqual:



Collaboration diagram for qpp::exception::DimsNotEqual:



Public Member Functions

- std::string type_description () const override
  Exception type description.

7.8.1 Detailed Description

Dimensions not equal exception.

Local/global dimensions are not equal

7.8.2 Member Function Documentation

7.8.2.1 type_description()

```
std::string qpp::exception::DimsNotEqual::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

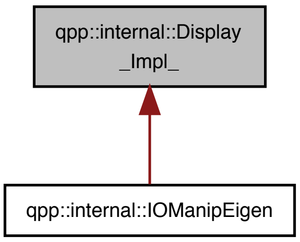
The documentation for this class was generated from the following file:

- classes/exception.h

7.9 qpp::internal::Display_Impl_ Struct Reference

```
#include <internal/util.h>
```

Inheritance diagram for qpp::internal::Display_Impl_:



Public Member Functions

- template<typename T >
  std::ostream & display_impl_ (const T &A, std::ostream &os, double chop=qpp::chop) const

7.9.1 Member Function Documentation

7.9.1.1 display_impl_()

```
template<typename T >
std::ostream& qpp::internal::Display_Impl_::display_impl_ (
             const T & A,
             std::ostream & os,
             double chop = qpp::chop ) const  [inline]
```

The documentation for this struct was generated from the following file:

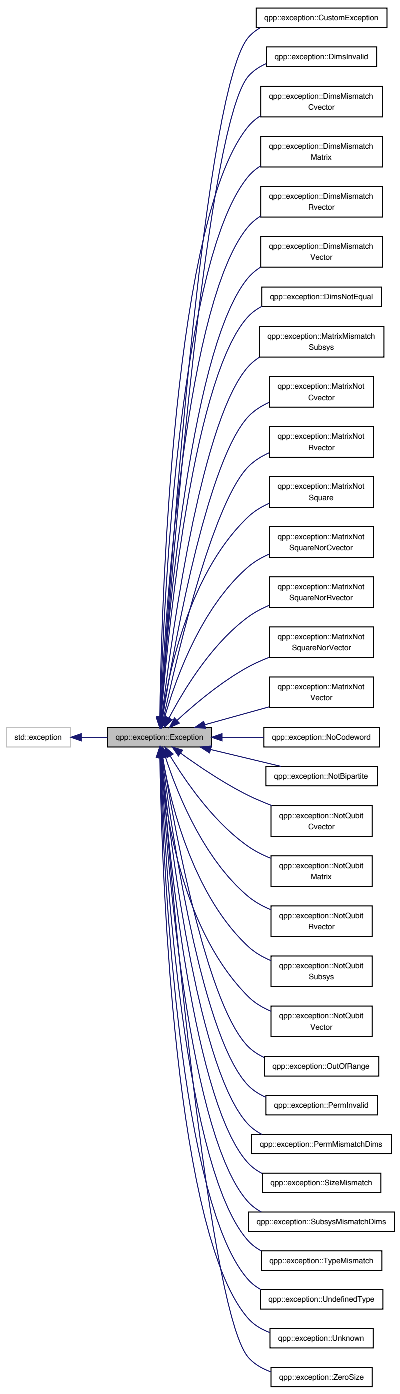
- internal/util.h

7.10 qpp::exception::Exception Class Reference

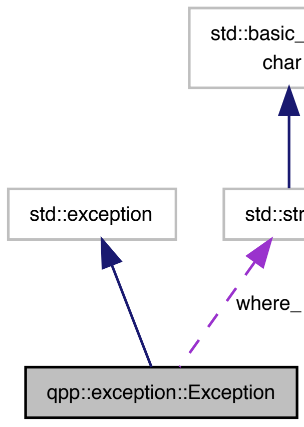
Base class for generating Quantum++ custom exceptions.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::Exception:


std::exception
qpp::exception::Exception
qpp::exception::CustomException
qpp::exception::DimsInvalid
qpp::exception::DimsMismatch Cvector
qpp::exception::DimsMismatch Matrix
qpp::exception::DimsMismatch Rvector
qpp::exception::DimsMismatch Vector
qpp::exception::DimsNotEqual
qpp::exception::MatrixMismatch Subsys
qpp::exception::MatrixNot Cvector
qpp::exception::MatrixNot Rvector
qpp::exception::MatrixNot Square
qpp::exception::MatrixNot SquareNorCvector
qpp::exception::MatrixNot SquareNorRvector
qpp::exception::MatrixNot SquareNorVector
qpp::exception::MatrixNot Vector
qpp::exception::NoCodeword
qpp::exception::NotBipartite
qpp::exception::NotQubit Cvector
qpp::exception::NotQubit Matrix
qpp::exception::NotQubit Rvector
qpp::exception::NotQubit Subsys
qpp::exception::NotQubit Vector
qpp::exception::OutOfRange
qpp::exception::PermInvalid
qpp::exception::PermMismatchDims
qpp::exception::SizeMismatch
qpp::exception::SubsysMismatchDims
qpp::exception::TypeMismatch
qpp::exception::UndefinedType
qpp::exception::Unknown
qpp::exception::ZeroSize

Collaboration diagram for qpp::exception::Exception:



Public Member Functions

- Exception (const std::string &where)

    Constructs an exception.
- virtual const char ∗ what () const noexcept override

    Overrides std::exception::what()
- virtual std::string type_description () const =0

    Exception type description.

Private Attributes

- std::string where_

7.10.1 Detailed Description

Base class for generating Quantum++ custom exceptions.

Derive from this class if more exceptions are needed, making sure to override qpp::exception::Exception::type_↩ description() in the derived class and to inherit the constructor qpp::exception::Exception::Exception(). Preferably keep your newly defined exception classes in the namespace qpp::exception.

Example:

```
namespace qpp
{
namespace exception
{
    class ZeroSize : public Exception
    {
    public:
        std::string type_description() const override
        {
            return "Object has zero size";
        }

        // inherit the base class' qpp::exception::Exception constructor
        using Exception::Exception;
    };
} // namespace exception
} // namespace qpp
```

7.10.2 Constructor & Destructor Documentation

7.10.2.1 Exception()

```
qpp::exception::Exception::Exception (
             const std::string & where )  [inline]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

7.10.3 Member Function Documentation

7.10.3.1 type_description()

```
std::string qpp::exception::Exception::type_description ( ) const  [inline], [pure virtual]
```

Exception type description.

Returns

Exception type description

Implemented in qpp::exception::CustomException, qpp::exception::UndefinedType, qpp::exception::SizeMismatch, qpp::exception::TypeMismatch, qpp::exception::OutOfRange, qpp::exception::NoCodeword, qpp::exception::↩ NotBipartite, qpp::exception::NotQubitSubsys, qpp::exception::NotQubitVector, qpp::exception::NotQubitRvector, qpp::exception::NotQubitCvector, qpp::exception::NotQubitMatrix, qpp::exception::PermMismatchDims, qpp↩ ::exception::PermInvalid, qpp::exception::SubsysMismatchDims, qpp::exception::DimsMismatchVector, qpp↩ ::exception::DimsMismatchRvector, qpp::exception::DimsMismatchCvector, qpp::exception::DimsMismatch↩ Matrix, qpp::exception::DimsNotEqual, qpp::exception::DimsInvalid, qpp::exception::MatrixMismatchSubsys, qpp↩ ::exception::MatrixNotSquareNorVector, qpp::exception::MatrixNotSquareNorRvector, qpp::exception::MatrixNot↩ SquareNorCvector, qpp::exception::MatrixNotVector, qpp::exception::MatrixNotRvector, qpp::exception::Matrix↩ NotCvector, qpp::exception::MatrixNotSquare, qpp::exception::ZeroSize, and qpp::exception::Unknown.

7.10.3.2 what()

```
virtual const char* qpp::exception::Exception::what ( ) const  [inline], [override], [virtual],
[noexcept]
```

Overrides std::exception::what()

Returns

Exception description

7.10.4 Member Data Documentation

7.10.4.1 where_

```
std::string qpp::exception::Exception::where_  [private]
```

The documentation for this class was generated from the following file:

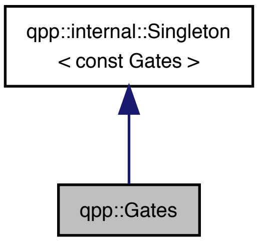
- classes/exception.h

7.11 qpp::Gates Class Reference

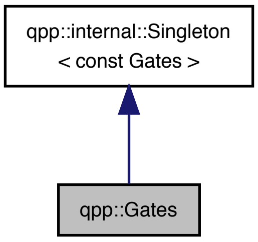
const Singleton class that implements most commonly used gates

```
#include <classes/gates.h>
```

Inheritance diagram for qpp::Gates:



Collaboration diagram for qpp::Gates:



Public Member Functions

- cmat Rn (double theta, const std::vector< double > &n) const

  Qubit rotation of theta about the 3-dimensional real (unit) vector n.
- cmat Zd (idx D=2) const

  Generalized Z gate for qudits.
- cmat Fd (idx D=2) const

  Fourier transform gate for qudits.
- cmat Xd (idx D=2) const

  Generalized X gate for qudits.
- template<typename Derived = Eigen::MatrixXcd>
  Derived Id (idx D=2) const

  Identity gate.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > CTRL (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx N, idx d=2) const

  Generates the multi-partite multiple-controlled-A gate in matrix form.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, idx pos, const std::vector< idx > &dims) const

  Expands out.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, idx pos, const std::initializer_list< idx > &dims) const

  Expands out.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, idx pos, idx N, idx d=2) const

  Expands out.

Public Attributes

- cmat Id2 {cmat::Identity(2, 2)}

  Identity gate.
- cmat H {cmat::Zero(2, 2)}

  Hadamard gate.
- cmat X {cmat::Zero(2, 2)}

  Pauli Sigma-X gate.
- cmat Y {cmat::Zero(2, 2)}

  Pauli Sigma-Y gate.
- cmat Z {cmat::Zero(2, 2)}

  Pauli Sigma-Z gate.
- cmat S {cmat::Zero(2, 2)}

  S gate.
- cmat T {cmat::Zero(2, 2)}

  T gate.
- cmat CNOT {cmat::Identity(4, 4)}

  Controlled-NOT control target gate.
- cmat CZ {cmat::Identity(4, 4)}

  Controlled-Phase gate.
- cmat CNOTba {cmat::Zero(4, 4)}

Controlled-NOT target control gate.
- cmat SWAP {cmat::Identity(4, 4)}

  SWAP gate.
- cmat TOF {cmat::Identity(8, 8)}

  Toffoli gate.
- cmat FRED {cmat::Identity(8, 8)}

  Fredkin gate.

Private Member Functions

- Gates ()

  Initializes the gates.
- ∼Gates ()=default

  Default destructor.

Friends

- class internal::Singleton< const Gates >

Additional Inherited Members

7.11.1 Detailed Description

const Singleton class that implements most commonly used gates

7.11.2 Constructor & Destructor Documentation

7.11.2.1 Gates()

```
qpp::Gates::Gates ( )  [inline], [private]
```

Initializes the gates.

7.11.2.2 ∼Gates()

```
qpp::Gates::∼Gates ( )  [private], [default]
```

Default destructor.

7.11.3 Member Function Documentation

7.11.3.1 CTRL()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::CTRL (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & ctrl,
            const std::vector< idx > & subsys,
            idx N,
            idx d = 2 ) const  [inline]
```

Generates the multi-partite multiple-controlled-*A* gate in matrix form.

See also

qpp::applyCTRL()

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

A	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate *A* is applied
N	Total number of subsystems
d	Subsystem dimensions

Returns

CTRL-A gate, as a matrix over the same scalar field as *A*

7.11.3.2 expandout() [1/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
            const Eigen::MatrixBase< Derived > & A,
            idx pos,
            const std::vector< idx > & dims ) const  [inline]
```

Expands out.

See also

qpp::kron()

Expands out *A* as a matrix in a multi-partite system. Faster than using qpp::kron(I, I, ..., I, A, I, ..., I).

Parameters

A	Eigen expression
pos	Position
dims	Dimensions of the multi-partite system

Returns

Tensor product $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$, with *A* on position *pos*, as a dynamic matrix over the same scalar field as *A*

7.11.3.3 expandout() [2/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
            const Eigen::MatrixBase< Derived > & A,
            idx pos,
            const std::initializer_list< idx > & dims ) const  [inline]
```

Expands out.

See also

qpp::kron()

Expands out *A* as a matrix in a multi-partite system. Faster than using qpp::kron(I, I, ..., I, A, I, ..., I).

Note

The std::initializer_list overload exists because otherwise, in the degenerate case when *dims* has only one element, the one element list is implicitly converted to the element's underlying type, i.e. qpp::idx, which has the net effect of picking the wrong (non-vector) qpp::expandout() overload

Parameters

A	Eigen expression
pos	Position
dims	Dimensions of the multi-partite system

Returns

Tensor product $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$, with *A* on position *pos*, as a dynamic matrix over the same scalar field as *A*

7.11.3.4 expandout() [3/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
             const Eigen::MatrixBase< Derived > & A,
             idx pos,
             idx N,
             idx d = 2 ) const  [inline]
```

Expands out.

See also

qpp::kron()

Expands out *A* as a matrix in a multi-partite system. Faster than using qpp::kron(I, I, ..., I, A, I, ..., I).

Parameters

A	Eigen expression
pos	Position
N	Number of subsystems
d	Subsystem dimension

Returns

Tensor product $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$, with *A* on position *pos*, as a dynamic matrix over the same scalar field as *A*

7.11.3.5 Fd()

```
cmat qpp::Gates::Fd (
             idx D = 2 ) const  [inline]
```

Fourier transform gate for qudits.

Note

Defined as $F = \sum_{j,k=0}^{D-1} \exp(2\pi \mathrm{i} jk/D)|j\rangle\langle k|$

Parameters

D	Dimension of the Hilbert space

Returns

Fourier transform gate for qudits

7.11.3.6 Id()

```
template<typename Derived = Eigen::MatrixXcd>
Derived qpp::Gates::Id (
             idx D = 2 ) const  [inline]
```

Identity gate.

Note

Can change the return type from complex matrix (default) by explicitly specifying the template parameter

Parameters

D	Dimension of the Hilbert space

Returns

Identity gate on a Hilbert space of dimension *D*

7.11.3.7 Rn()

```
cmat qpp::Gates::Rn (
             double theta,
             const std::vector< double > & n ) const  [inline]
```

Qubit rotation of *theta* about the 3-dimensional real (unit) vector *n*.

Parameters

theta	Rotation angle
n	3-dimensional real (unit) vector

Returns

Rotation gate

7.11.3.8 Xd()

```
cmat qpp::Gates::Xd (
             idx D = 2 ) const  [inline]
```

Generalized X gate for qudits.

Note

Defined as $X = \sum_{j=0}^{D-1} |j \oplus 1\rangle\langle j|$, i.e. raising operator $X|j\rangle = |j \oplus 1\rangle$

Parameters

D	Dimension of the Hilbert space

Returns

Generalized X gate for qudits

7.11.3.9 Zd()

```
cmat qpp::Gates::Zd (
            idx D = 2 ) const  [inline]
```

Generalized Z gate for qudits.

Note

Defined as $Z = \sum_{j=0}^{D-1} \exp(2\pi \mathrm{i} j/D)|j\rangle\langle j|$

Parameters

D	Dimension of the Hilbert space

Returns

Generalized Z gate for qudits

7.11.4 Friends And Related Function Documentation

7.11.4.1 internal::Singleton< const Gates >

```
friend class internal::Singleton< const Gates >  [friend]
```

7.11.5 Member Data Documentation

7.11.5.1 CNOT

```
cmat qpp::Gates::CNOT {cmat::Identity(4, 4)}
```

Controlled-NOT control target gate.

7.11.5.2 CNOTba

```
cmat qpp::Gates::CNOTba {cmat::Zero(4, 4)}
```

Controlled-NOT target control gate.

7.11.5.3 CZ

```
cmat qpp::Gates::CZ {cmat::Identity(4, 4)}
```

Controlled-Phase gate.

7.11.5.4 FRED

```
cmat qpp::Gates::FRED {cmat::Identity(8, 8)}
```

Fredkin gate.

7.11.5.5 H

```
cmat qpp::Gates::H {cmat::Zero(2, 2)}
```

Hadamard gate.

7.11.5.6 Id2

```
cmat qpp::Gates::Id2 {cmat::Identity(2, 2)}
```

Identity gate.

7.11.5.7 S

```
cmat qpp::Gates::S {cmat::Zero(2, 2)}
```

S gate.

7.11.5.8 SWAP

```
cmat qpp::Gates::SWAP {cmat::Identity(4, 4)}
```

SWAP gate.

7.11.5.9 T

```
cmat qpp::Gates::T {cmat::Zero(2, 2)}
```

T gate.

7.11.5.10 TOF

```
cmat qpp::Gates::TOF {cmat::Identity(8, 8)}
```

Toffoli gate.

7.11.5.11 X

```
cmat qpp::Gates::X {cmat::Zero(2, 2)}
```

Pauli Sigma-X gate.

7.11.5.12 Y

```
cmat qpp::Gates::Y {cmat::Zero(2, 2)}
```

Pauli Sigma-Y gate.

7.11.5.13 Z

```
cmat qpp::Gates::Z {cmat::Zero(2, 2)}
```

Pauli Sigma-Z gate.

The documentation for this class was generated from the following file:

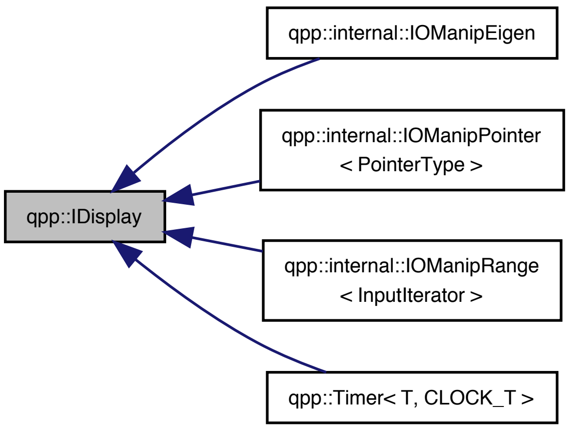
- classes/gates.h

7.12 qpp::IDisplay Class Reference

Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

```
#include <classes/idisplay.h>
```

Inheritance diagram for qpp::IDisplay:


qpp::internal::IOManipEigen
qpp::internal::IOManipPointer < PointerType >
qpp::IDisplay
qpp::internal::IOManipRange < InputIterator >
qpp::Timer< T, CLOCK_T >

Public Member Functions

- IDisplay ()=default
  Default constructor.
- IDisplay (const IDisplay &)=default
  Default copy constructor.
- IDisplay (IDisplay &&)=default
  Default move constructor.
- IDisplay & operator= (const IDisplay &)=default
  Default copy assignment operator.
- IDisplay & operator= (IDisplay &&)=default
  Default move assignment operator.
- virtual ∼IDisplay ()=default
  Default virtual destructor.

Private Member Functions

- virtual std::ostream & display (std::ostream &os) const =0

  Must be overridden by all derived classes.

Friends

- std::ostream & operator<< (std::ostream &os, const IDisplay &rhs)

  Overloads the extraction operator.

7.12.1 Detailed Description

Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

This class defines friend inline std::ostream& operator<< (std::ostream& os, const qpp::IDisplay& rhs). The latter delegates the work to the pure private virtual function qpp::IDisplay::display() which has to be overridden by all derived classes.

7.12.2 Constructor & Destructor Documentation

7.12.2.1 IDisplay() [1/3]

```
qpp::IDisplay::IDisplay ( )  [default]
```

Default constructor.

7.12.2.2 IDisplay() [2/3]

```
qpp::IDisplay::IDisplay (
             const IDisplay &  )  [default]
```

Default copy constructor.

7.12.2.3 IDisplay() [3/3]

```
qpp::IDisplay::IDisplay (
             IDisplay &&  )  [default]
```

Default move constructor.

7.12.2.4 ∼IDisplay()

```
virtual qpp::IDisplay::∼IDisplay ( )  [virtual], [default]
```

Default virtual destructor.

7.12.3 Member Function Documentation

7.12.3.1 display()

```
virtual std::ostream& qpp::IDisplay::display (
            std::ostream & os ) const  [private], [pure virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implemented in qpp::internal::IOManipEigen, qpp::Timer< T, CLOCK_T >, qpp::internal::IOManipPointer< PointerType >, and qpp::internal::IOManipRange< InputIterator >.

7.12.3.2 operator=() [1/2]

```
IDisplay& qpp::IDisplay::operator= (
            const IDisplay &  )  [default]
```

Default copy assignment operator.

7.12.3.3 operator=() [2/2]

```
IDisplay& qpp::IDisplay::operator= (
            IDisplay &&  )  [default]
```

Default move assignment operator.

7.12.4 Friends And Related Function Documentation

7.12.4.1 operator<<

```
std::ostream& operator<< (
            std::ostream & os,
            const IDisplay & rhs )  [friend]
```

Overloads the extraction operator.

Delegates the work to the virtual function qpp::IDisplay::display()

The documentation for this class was generated from the following file:

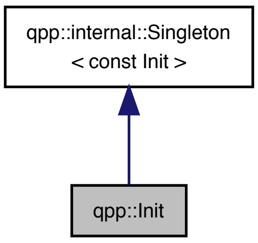
- classes/idisplay.h

7.13 qpp::Init Class Reference

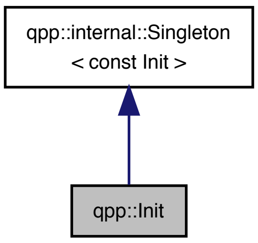
const Singleton class that performs additional initializations/cleanups

```
#include <classes/init.h>
```

Inheritance diagram for qpp::Init:



Collaboration diagram for qpp::Init:



Private Member Functions

- Init ()

    Additional initializations.
- ∼Init ()

    Cleanups.

Friends

- class internal::Singleton< const Init >

Additional Inherited Members

7.13.1 Detailed Description

const Singleton class that performs additional initializations/cleanups

7.13.2 Constructor & Destructor Documentation

7.13.2.1 Init()

```
qpp::Init::Init ( )  [inline], [private]
```

Additional initializations.

7.13.2.2 ∼Init()

```
qpp::Init::~Init ( )  [inline], [private]
```

Cleanups.

7.13.3 Friends And Related Function Documentation

7.13.3.1 internal::Singleton< const Init >

```
friend class internal::Singleton< const Init >  [friend]
```

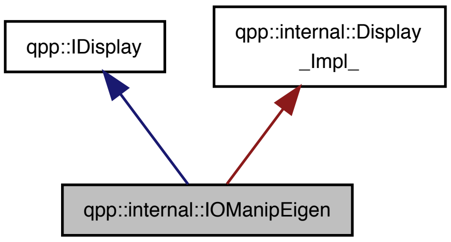
The documentation for this class was generated from the following file:

- classes/init.h

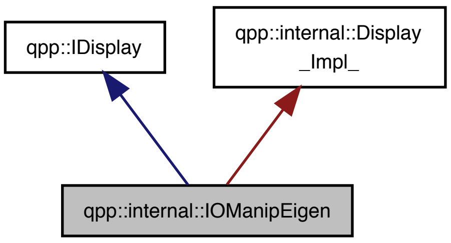
7.14 qpp::internal::IOManipEigen Class Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipEigen:



Collaboration diagram for qpp::internal::IOManipEigen:



Public Member Functions

- template<typename Derived >
  IOManipEigen (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)
- IOManipEigen (const cplx z, double chop=qpp::chop)

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  Must be overridden by all derived classes.

Private Attributes

- cmat A_
- double chop_

7.14.1 Constructor & Destructor Documentation

7.14.1.1 IOManipEigen() [1/2]

```
template<typename Derived >
qpp::internal::IOManipEigen::IOManipEigen (
             const Eigen::MatrixBase< Derived > & A,
             double chop = qpp::chop )  [inline], [explicit]
```

7.14.1.2 IOManipEigen() [2/2]

```
qpp::internal::IOManipEigen::IOManipEigen (
             const cplx z,
             double chop = qpp::chop )  [inline], [explicit]
```

7.14.2 Member Function Documentation

7.14.2.1 display()

```
std::ostream& qpp::internal::IOManipEigen::display (
             std::ostream & os ) const  [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implements qpp::IDisplay.

7.14.3 Member Data Documentation

7.14.3.1 A_

```
cmat qpp::internal::IOManipEigen::A_  [private]
```

7.14.3.2 chop_

```
double qpp::internal::IOManipEigen::chop_  [private]
```

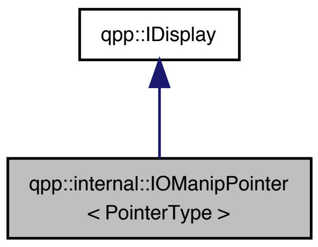
The documentation for this class was generated from the following file:

- internal/classes/iomanip.h

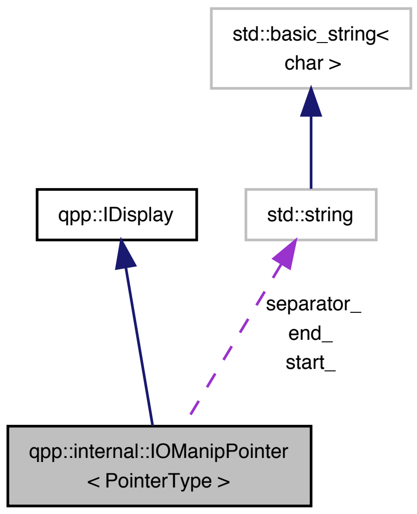
7.15 qpp::internal::IOManipPointer< PointerType > Class Template Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipPointer< PointerType >:



Collaboration diagram for qpp::internal::IOManipPointer< PointerType >:


std::basic_string< char >
qpp::IDisplay
std::string
separator_
end_
start_
qpp::internal::IOManipPointer < PointerType >

Public Member Functions

- IOManipPointer (const PointerType ∗p, idx N, const std::string &separator, const std::string &start="[", const std::string &end="]")
- IOManipPointer (const IOManipPointer &)=default
- IOManipPointer & operator= (const IOManipPointer &)=default

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  Must be overridden by all derived classes.

Private Attributes

- const PointerType ∗ p_
- idx N_
- std::string separator_
- std::string start_
- std::string end_

7.15.1 Constructor & Destructor Documentation

7.15.1.1 IOManipPointer() [1/2]

```
template<typename PointerType>
qpp::internal::IOManipPointer< PointerType >::IOManipPointer (
            const PointerType * p,
            idx N,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]" )  [inline], [explicit]
```

7.15.1.2 IOManipPointer() [2/2]

```
template<typename PointerType>
qpp::internal::IOManipPointer< PointerType >::IOManipPointer (
            const IOManipPointer< PointerType > &  )  [default]
```

7.15.2 Member Function Documentation

7.15.2.1 display()

```
template<typename PointerType>
std::ostream& qpp::internal::IOManipPointer< PointerType >::display (
            std::ostream & os ) const  [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implements qpp::IDisplay.

7.15.2.2 operator=()

```
template<typename PointerType>
IOManipPointer& qpp::internal::IOManipPointer< PointerType >::operator= (
            const IOManipPointer< PointerType > &  )  [default]
```

7.15.3 Member Data Documentation

7.15.3.1 end_

```
template<typename PointerType>
std::string qpp::internal::IOManipPointer< PointerType >::end_  [private]
```

7.15.3.2 N_

```
template<typename PointerType>
idx qpp::internal::IOManipPointer< PointerType >::N_  [private]
```

7.15.3.3 p_

```
template<typename PointerType>
const PointerType* qpp::internal::IOManipPointer< PointerType >::p_  [private]
```

7.15.3.4 separator_

```
template<typename PointerType>
std::string qpp::internal::IOManipPointer< PointerType >::separator_  [private]
```

7.15.3.5 start_

```
template<typename PointerType>
std::string qpp::internal::IOManipPointer< PointerType >::start_  [private]
```

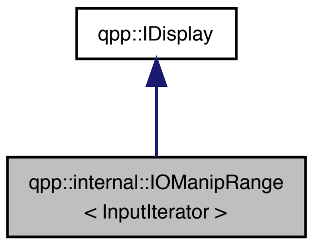
The documentation for this class was generated from the following file:

- internal/classes/iomanip.h

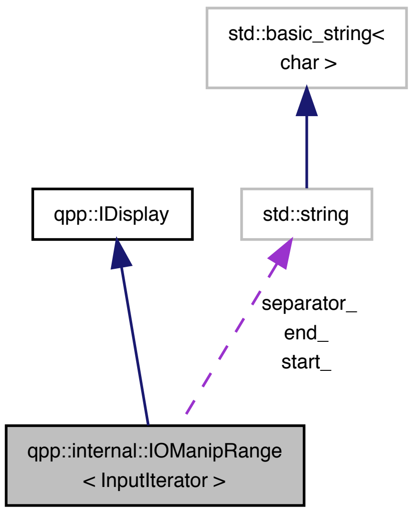
7.16 qpp::internal::IOManipRange< InputIterator > Class Template Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipRange< InputIterator >:



Collaboration diagram for qpp::internal::IOManipRange< InputIterator >:


std::basic_string< char >
qpp::IDisplay
std::string
separator_
end_
start_
qpp::internal::IOManipRange < InputIterator >

Public Member Functions

- IOManipRange (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")
- IOManipRange (const IOManipRange &)=default
- IOManipRange & operator= (const IOManipRange &)=default

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  Must be overridden by all derived classes.

Private Attributes

- InputIterator first_
- InputIterator last_
- std::string separator_
- std::string start_
- std::string end_

7.16.1 Constructor & Destructor Documentation

7.16.1.1 IOManipRange() [1/2]

```
template<typename InputIterator>
qpp::internal::IOManipRange< InputIterator >::IOManipRange (
            InputIterator first,
            InputIterator last,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]" )  [inline], [explicit]
```

7.16.1.2 IOManipRange() [2/2]

```
template<typename InputIterator>
qpp::internal::IOManipRange< InputIterator >::IOManipRange (
            const IOManipRange< InputIterator > &  )  [default]
```

7.16.2 Member Function Documentation

7.16.2.1 display()

```
template<typename InputIterator>
std::ostream& qpp::internal::IOManipRange< InputIterator >::display (
            std::ostream & os ) const  [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implements qpp::IDisplay.

7.16.2.2 operator=()

```
template<typename InputIterator>
IOManipRange& qpp::internal::IOManipRange< InputIterator >::operator= (
            const IOManipRange< InputIterator > &  )  [default]
```

7.16.3 Member Data Documentation

7.16.3.1 end_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::end_  [private]
```

7.16.3.2 first_

```
template<typename InputIterator>
InputIterator qpp::internal::IOManipRange< InputIterator >::first_  [private]
```

7.16.3.3 last_

```
template<typename InputIterator>
InputIterator qpp::internal::IOManipRange< InputIterator >::last_  [private]
```

7.16.3.4 separator_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::separator_  [private]
```

7.16.3.5 start_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::start_  [private]
```

The documentation for this class was generated from the following file:

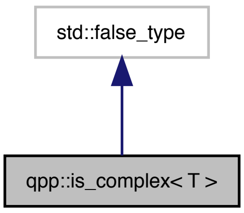
- internal/classes/iomanip.h

7.17 qpp::is_complex< T > Struct Template Reference

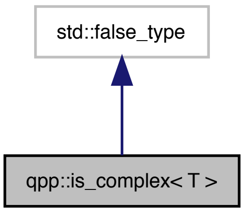
Checks whether the type is a complex type.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_complex< T >:



Collaboration diagram for qpp::is_complex< T >:



7.17.1 Detailed Description

template<typename T>
struct qpp::is_complex< T >

Checks whether the type is a complex type.

Provides the constant member *value* which is equal to *true*, if the type is a complex type, i.e. *std::complex<T>*

The documentation for this struct was generated from the following file:

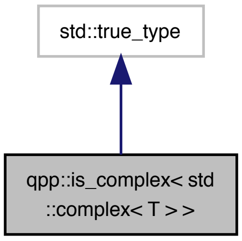
- traits.h

7.18 qpp::is_complex< std::complex< T > > Struct Template Reference

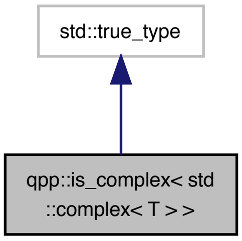
Checks whether the type is a complex number type, specialization for complex types.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_complex< std::complex< T > >:



Collaboration diagram for qpp::is_complex< std::complex< T > >:



7.18.1 Detailed Description

template<typename T>
struct qpp::is_complex< std::complex< T > >

Checks whether the type is a complex number type, specialization for complex types.

The documentation for this struct was generated from the following file:

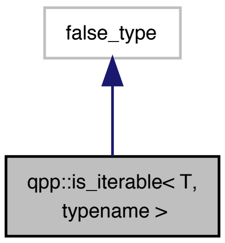
- traits.h

7.19 qpp::is_iterable< T, typename > Struct Template Reference

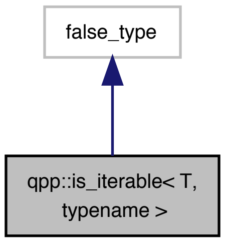
Checks whether *T* is compatible with an STL-like iterable container.

`#include <traits.h>`

Inheritance diagram for qpp::is_iterable< T, typename >:



Collaboration diagram for qpp::is_iterable< T, typename >:



7.19.1 Detailed Description

template<typename T, typename = void>
struct qpp::is_iterable< T, typename >

Checks whether *T* is compatible with an STL-like iterable container.

Provides the constant member *value* which is equal to *true*, if *T* is compatible with an iterable container, i.e. provides at least *begin()* and *end()* member functions. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

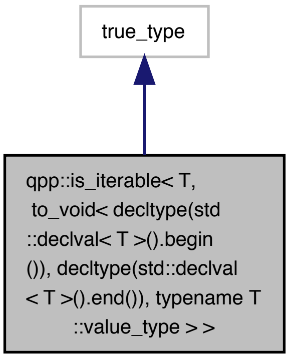
- traits.h

7.20 qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > > Struct Template Reference

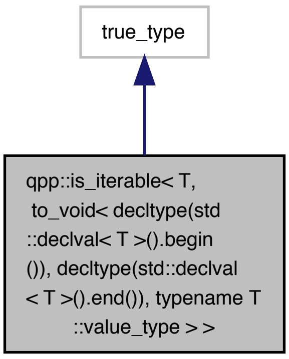
Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >:


true_type
qpp::is_iterable< T, to_void< decltype(std ::declval< T >().begin ()), decltype(std::declval < T >().end()), typename T ::value_type > >

Collaboration diagram for qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >:


true_type
qpp::is_iterable< T, to_void< decltype(std ::declval< T >().begin ()), decltype(std::declval < T >().end()), typename T ::value_type > >

7.20.1 Detailed Description

template<typename T>
struct qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T↩ ::value_type > >

Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

The documentation for this struct was generated from the following file:

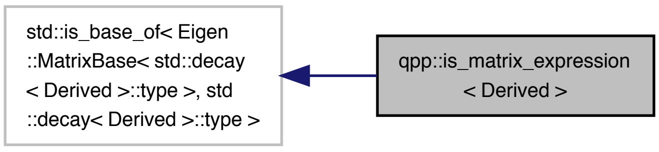
- traits.h

7.21 qpp::is_matrix_expression< Derived > Struct Template Reference

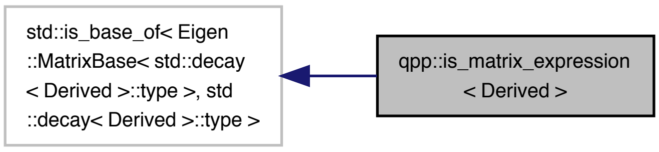
Checks whether the type is an Eigen matrix expression.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_matrix_expression< Derived >:


std::is_base_of< Eigen ::MatrixBase< std::decay < Derived >::type >, std ::decay< Derived >::type >
qpp::is_matrix_expression < Derived >

Collaboration diagram for qpp::is_matrix_expression< Derived >:


std::is_base_of< Eigen ::MatrixBase< std::decay < Derived >::type >, std ::decay< Derived >::type >
qpp::is_matrix_expression < Derived >

7.21.1 Detailed Description

template<typename Derived>
struct qpp::is_matrix_expression< Derived >

Checks whether the type is an Eigen matrix expression.

Provides the constant member *value* which is equal to *true*, if the type is an Eigen matrix expression of type *Eigen↩ ::MatrixBase<Derived>*. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

- traits.h

7.22 qpp::make_void< Ts > Struct Template Reference

Helper for qpp::to_void<> alias template.

```
#include <traits.h>
```

Public Types

- typedef void type

7.22.1 Detailed Description

template<typename... Ts>
struct qpp::make_void< Ts >

Helper for qpp::to_void<> alias template.

See also

qpp::to_void<>

7.22.2 Member Typedef Documentation

7.22.2.1 type

```
template<typename... Ts>
typedef void qpp::make_void< Ts >::type
```

The documentation for this struct was generated from the following file:

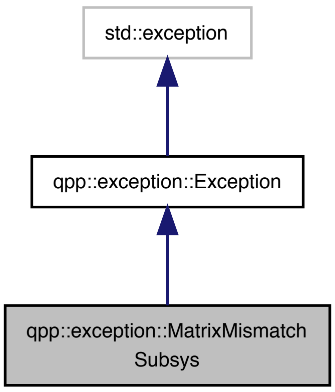
- traits.h

7.23 qpp::exception::MatrixMismatchSubsys Class Reference

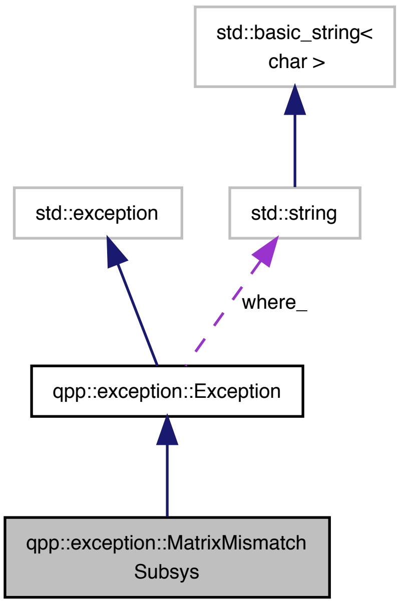
Matrix mismatch subsystems exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixMismatchSubsys:



Collaboration diagram for qpp::exception::MatrixMismatchSubsys:



Public Member Functions

- std::string type_description () const override

    Exception type description.

7.23.1 Detailed Description

Matrix mismatch subsystems exception.

Matrix size mismatch subsystem sizes (e.g. in qpp::apply())

7.23.2 Member Function Documentation

7.23.2.1 type_description()

```
std::string qpp::exception::MatrixMismatchSubsys::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

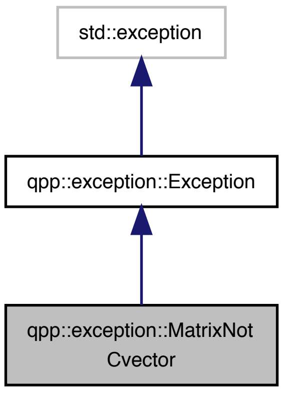
- classes/exception.h

7.24 qpp::exception::MatrixNotCvector Class Reference

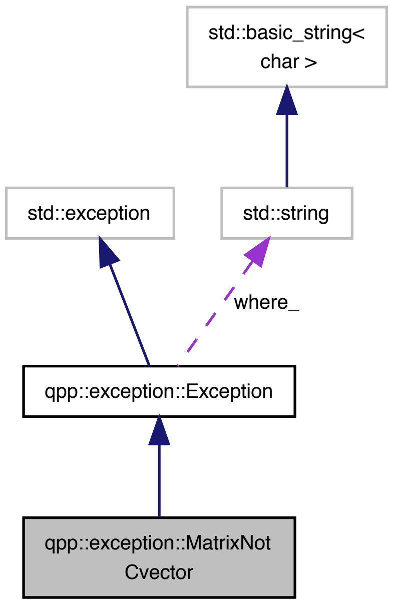
Matrix is not a column vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotCvector:



Collaboration diagram for qpp::exception::MatrixNotCvector:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::MatrixNot Cvector

Public Member Functions

- std::string type_description () const override

    Exception type description.

7.24.1 Detailed Description

Matrix is not a column vector exception.

Eigen::Matrix is not a column vector

7.24.2 Member Function Documentation

7.24.2.1 type_description()

`std::string qpp::exception::MatrixNotCvector::type_description ( ) const [inline], [override], [virtual]`

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

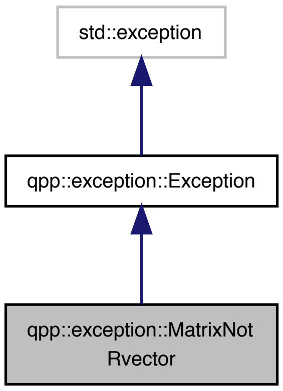
- classes/exception.h

7.25 qpp::exception::MatrixNotRvector Class Reference

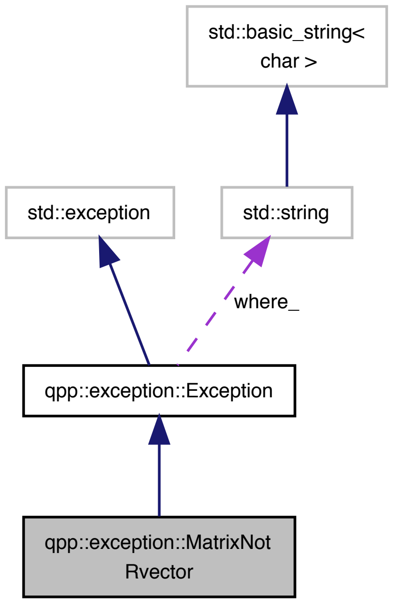
Matrix is not a row vector exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::MatrixNotRvector:



Collaboration diagram for qpp::exception::MatrixNotRvector:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.25.1 Detailed Description

Matrix is not a row vector exception.

Eigen::Matrix is not a row vector

7.25.2 Member Function Documentation

7.25.2.1 type_description()

```
std::string qpp::exception::MatrixNotRvector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

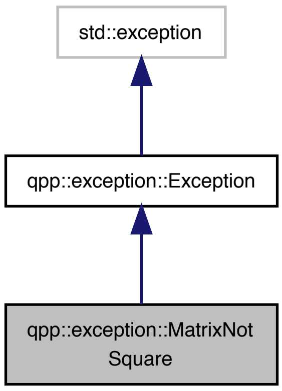
- classes/exception.h

7.26 qpp::exception::MatrixNotSquare Class Reference

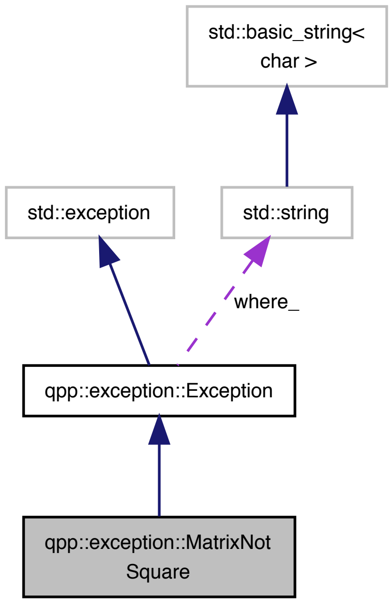
Matrix is not square exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquare:



Collaboration diagram for qpp::exception::MatrixNotSquare:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::MatrixNot Square

Public Member Functions

- std::string type_description () const override
  Exception type description.

7.26.1 Detailed Description

Matrix is not square exception.

Eigen::Matrix is not a square matrix

7.26.2 Member Function Documentation

7.26.2.1 type_description()

```
std::string qpp::exception::MatrixNotSquare::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

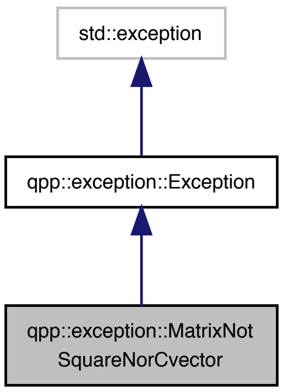
- classes/exception.h

7.27 qpp::exception::MatrixNotSquareNorCvector Class Reference

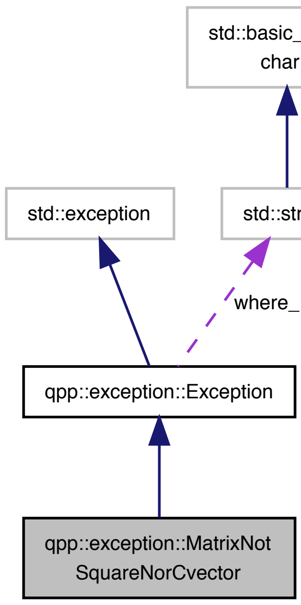
Matrix is not square nor column vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorCvector:


std::exception
qpp::exception::Exception
qpp::exception::MatrixNot SquareNorCvector

Collaboration diagram for qpp::exception::MatrixNotSquareNorCvector:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::MatrixNot SquareNorCvector

Public Member Functions

- std::string type_description () const override

    Exception type description.

7.27.1 Detailed Description

Matrix is not square nor column vector exception.

Eigen::Matrix is not a square matrix nor a column vector

7.27.2 Member Function Documentation

7.27.2.1 type_description()

```
std::string qpp::exception::MatrixNotSquareNorCvector::type_description ( ) const  [inline],
[override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

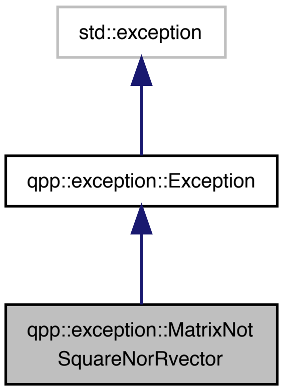
- classes/exception.h

7.28 qpp::exception::MatrixNotSquareNorRvector Class Reference

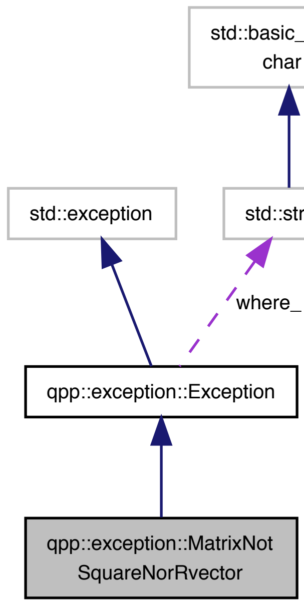
Matrix is not square nor row vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorRvector:


std::exception
qpp::exception::Exception
qpp::exception::MatrixNot SquareNorRvector

Collaboration diagram for qpp::exception::MatrixNotSquareNorRvector:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::MatrixNot SquareNorRvector

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.28.1 Detailed Description

Matrix is not square nor row vector exception.

Eigen::Matrix is not a square matrix nor a row vector

7.28.2 Member Function Documentation

7.28.2.1 type_description()

```
std::string qpp::exception::MatrixNotSquareNorRvector::type_description ( ) const  [inline],
[override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

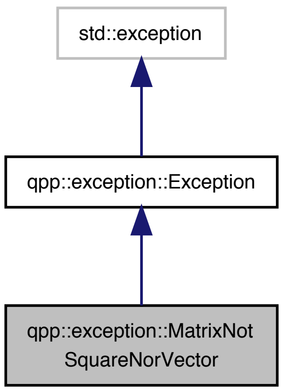
- classes/exception.h

7.29 qpp::exception::MatrixNotSquareNorVector Class Reference

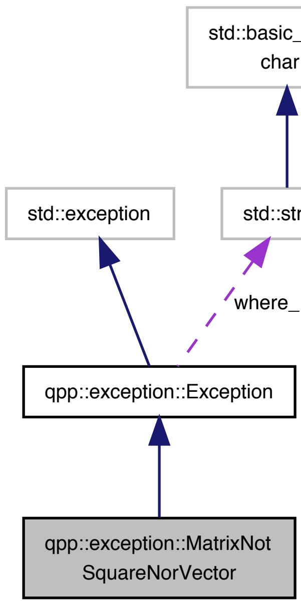
Matrix is not square nor vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorVector:


std::exception
qpp::exception::Exception
qpp::exception::MatrixNot SquareNorVector

Collaboration diagram for qpp::exception::MatrixNotSquareNorVector:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::MatrixNotSquareNorVector

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.29.1 Detailed Description

Matrix is not square nor vector exception.

Eigen::Matrix is not a square matrix nor a row/column vector

7.29.2 Member Function Documentation

7.29.2.1 type_description()

```
std::string qpp::exception::MatrixNotSquareNorVector::type_description ( ) const  [inline],
[override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

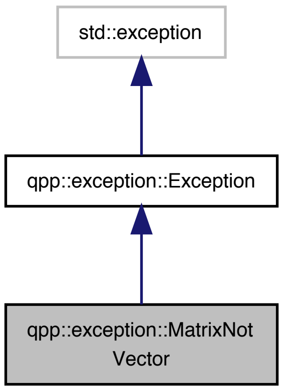
- classes/exception.h

7.30 qpp::exception::MatrixNotVector Class Reference

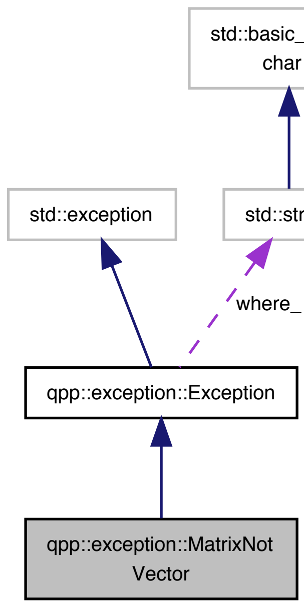
Matrix is not a vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotVector:



Collaboration diagram for qpp::exception::MatrixNotVector:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::MatrixNot Vector

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.30.1 Detailed Description

Matrix is not a vector exception.

Eigen::Matrix is not a row or column vector

7.30.2 Member Function Documentation

7.30.2.1 type_description()

```
std::string qpp::exception::MatrixNotVector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

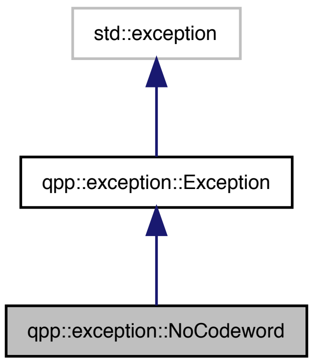
- classes/exception.h

7.31 qpp::exception::NoCodeword Class Reference

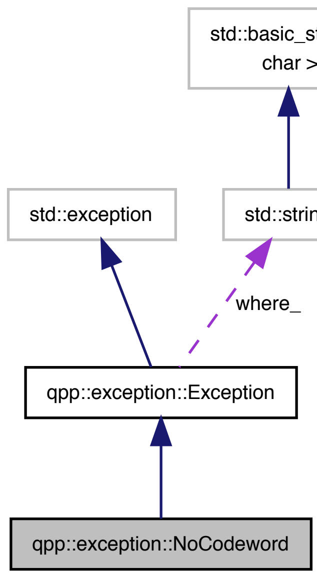
Codeword does not exist exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NoCodeword:



Collaboration diagram for qpp::exception::NoCodeword:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::NoCodeword

Public Member Functions

- std::string type_description () const override

    Exception type description.

7.31.1 Detailed Description

Codeword does not exist exception.

Codeword does not exist, thrown when calling qpp::Codes::codeword() with an invalid index

7.31.2 Member Function Documentation

7.31.2.1 type_description()

```
std::string qpp::exception::NoCodeword::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

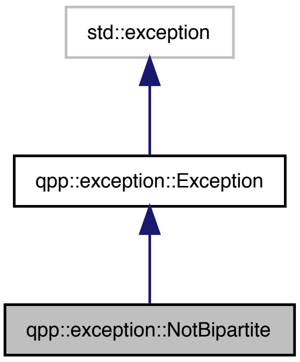
- classes/exception.h

7.32 qpp::exception::NotBipartite Class Reference

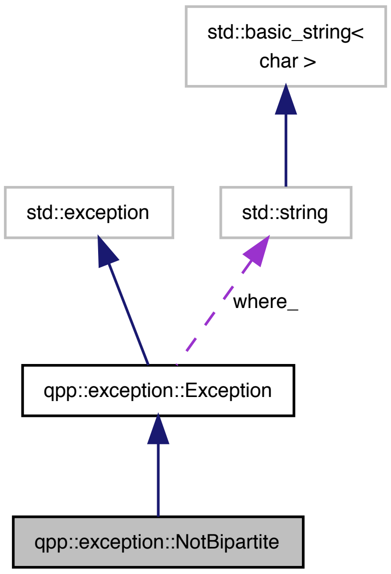
Not bi-partite exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotBipartite:



Collaboration diagram for qpp::exception::NotBipartite:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::NotBipartite

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.32.1 Detailed Description

Not bi-partite exception.

std::vector<idx> of dimensions has size different from 2

7.32.2 Member Function Documentation

7.32.2.1 type_description()

```
std::string qpp::exception::NotBipartite::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

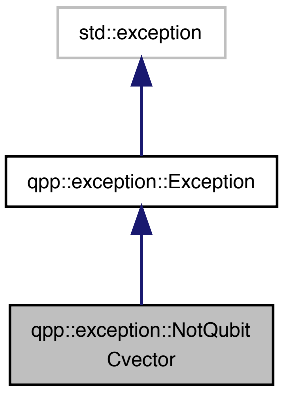
- classes/exception.h

7.33 qpp::exception::NotQubitCvector Class Reference

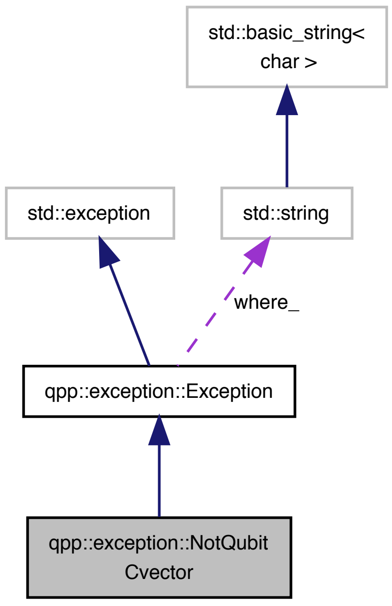
Column vector is not 2 x 1 exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitCvector:



Collaboration diagram for qpp::exception::NotQubitCvector:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::NotQubit Cvector

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.33.1 Detailed Description

Column vector is not 2 x 1 exception.

Eigen::Matrix is not 2 x 1

7.33.2 Member Function Documentation

7.33.2.1 type_description()

```
std::string qpp::exception::NotQubitCvector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

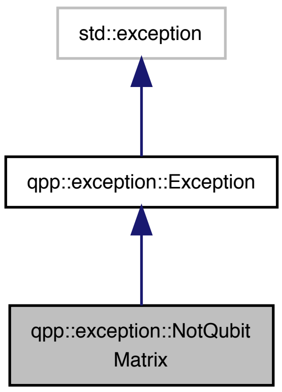
- classes/exception.h

7.34 qpp::exception::NotQubitMatrix Class Reference

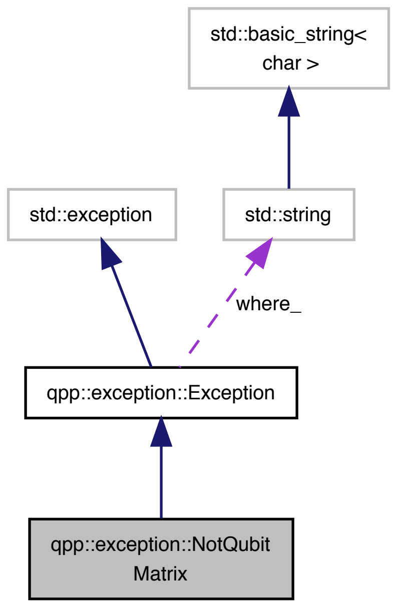
Matrix is not 2 x 2 exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitMatrix:



Collaboration diagram for qpp::exception::NotQubitMatrix:



Public Member Functions

- std::string type_description () const override

    Exception type description.

7.34.1 Detailed Description

Matrix is not 2 x 2 exception.

Eigen::Matrix is not 2 x 2

7.34.2 Member Function Documentation

7.34.2.1 type_description()

```
std::string qpp::exception::NotQubitMatrix::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

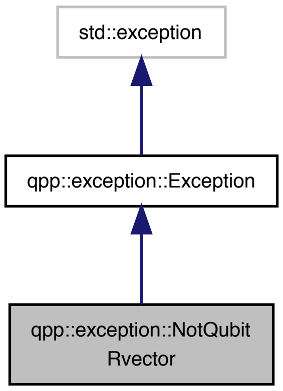
- classes/exception.h

7.35 qpp::exception::NotQubitRvector Class Reference

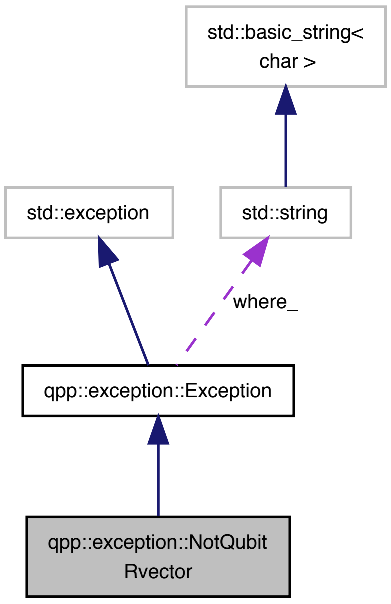
Row vector is not 1 x 2 exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitRvector:



Collaboration diagram for qpp::exception::NotQubitRvector:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::NotQubit Rvector

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.35.1 Detailed Description

Row vector is not 1 x 2 exception.

Eigen::Matrix is not 1 x 2

7.35.2 Member Function Documentation

7.35.2.1 type_description()

```
std::string qpp::exception::NotQubitRvector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

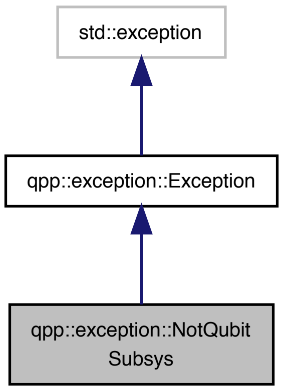
- classes/exception.h

7.36 qpp::exception::NotQubitSubsys Class Reference

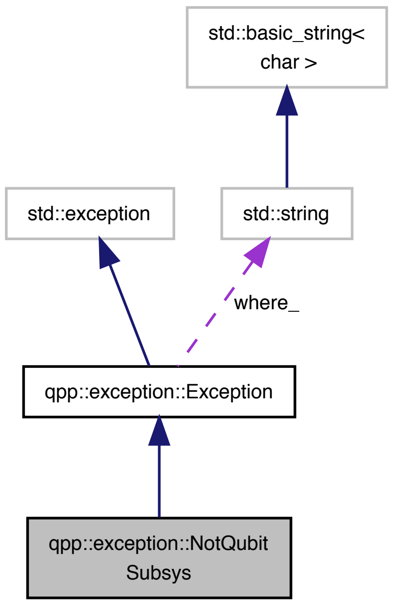
Subsystems are not qubits exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitSubsys:



Collaboration diagram for qpp::exception::NotQubitSubsys:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::NotQubit Subsys

Public Member Functions

- std::string type_description () const override
  Exception type description.

7.36.1 Detailed Description

Subsystems are not qubits exception.

Subsystems are not 2-dimensional (qubits)

7.36.2 Member Function Documentation

7.36.2.1 type_description()

```
std::string qpp::exception::NotQubitSubsys::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

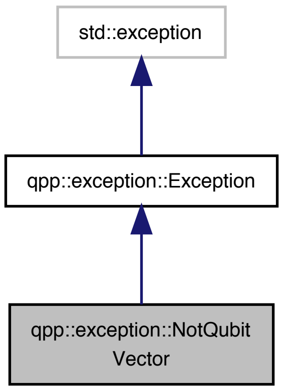
- classes/exception.h

7.37 qpp::exception::NotQubitVector Class Reference

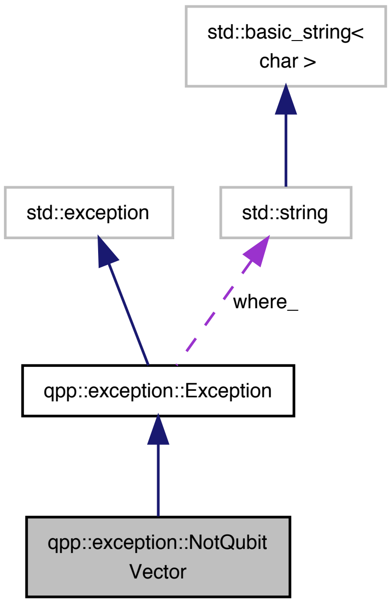
Vector is not 2 x 1 nor 1 x 2 exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitVector:



Collaboration diagram for qpp::exception::NotQubitVector:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::NotQubit Vector

Public Member Functions

- std::string type_description () const override

    Exception type description.

7.37.1 Detailed Description

Vector is not 2 x 1 nor 1 x 2 exception.

Eigen::Matrix is not 2 x 1 nor 1 x 2

7.37.2 Member Function Documentation

7.37.2.1 type_description()

```
std::string qpp::exception::NotQubitVector::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

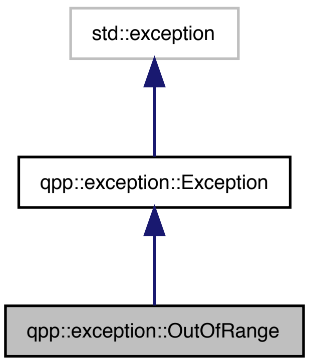
- classes/exception.h

7.38 qpp::exception::OutOfRange Class Reference

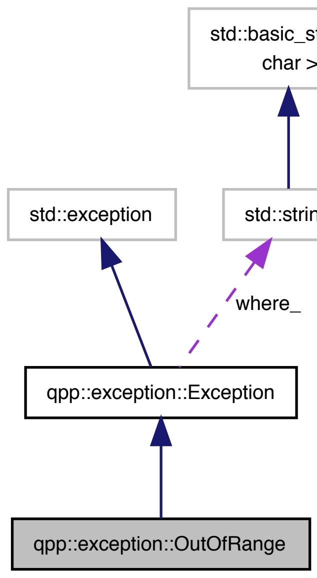
Parameter out of range exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::OutOfRange:



Collaboration diagram for qpp::exception::OutOfRange:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::OutOfRange

Public Member Functions

- std::string type_description () const override
  Exception type description.

7.38.1 Detailed Description

Parameter out of range exception.

Parameter out of range

7.38.2 Member Function Documentation

7.38.2.1 type_description()

```
std::string qpp::exception::OutOfRange::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

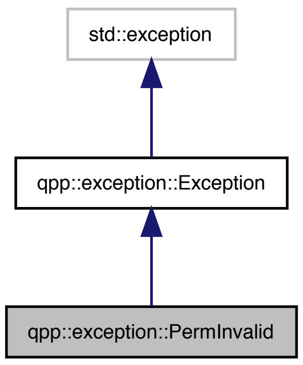
- classes/exception.h

7.39 qpp::exception::PermInvalid Class Reference

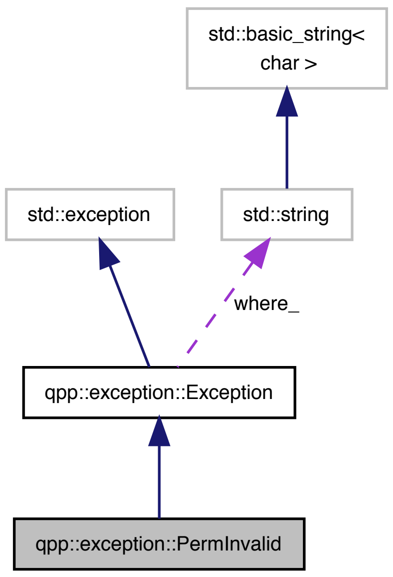
Invalid permutation exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::PermInvalid:



Collaboration diagram for qpp::exception::PermInvalid:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::PermInvalid

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.39.1 Detailed Description

Invalid permutation exception.

std::vector<idx> does note represent a valid permutation

7.39.2 Member Function Documentation

7.39.2.1 type_description()

```
std::string qpp::exception::PermInvalid::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

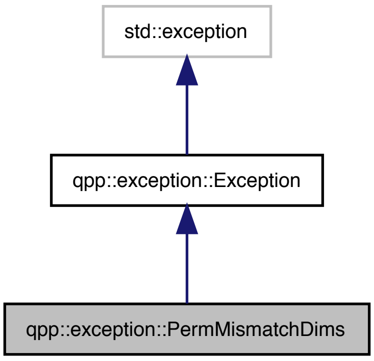
- classes/exception.h

7.40 qpp::exception::PermMismatchDims Class Reference

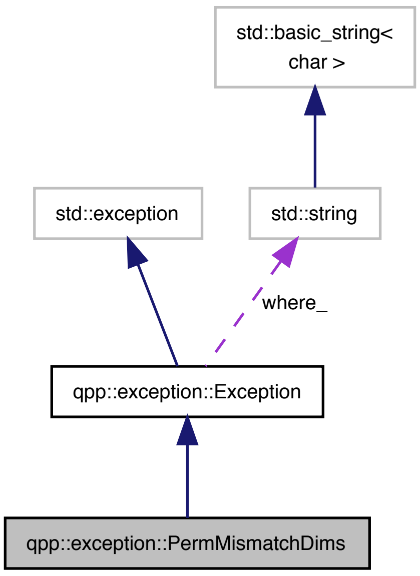
Permutation mismatch dimensions exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::PermMismatchDims:



Collaboration diagram for qpp::exception::PermMismatchDims:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::PermMismatchDims

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.40.1 Detailed Description

Permutation mismatch dimensions exception.

Size of the std::vector<idx> representing the permutation is different from the size of the std::vector<idx> of dimensions

7.40.2 Member Function Documentation

7.40.2.1 type_description()

```
std::string qpp::exception::PermMismatchDims::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

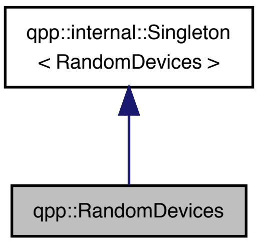
- classes/exception.h

7.41 qpp::RandomDevices Class Reference

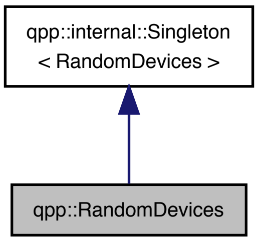
Singeleton class that manages the source of randomness in the library.

`#include <classes/random_devices.h>`

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



Public Member Functions

- std::mt19937 & get_prng ()

  Returns a reference to the internal PRNG object.
- std::istream & load (std::istream &is)

  Loads the state of the PRNG from an input stream.
- std::ostream & save (std::ostream &os) const

  Saves the state of the PRNG to an output stream.

Private Member Functions

- RandomDevices ()

  Initializes and seeds the random number generators.
- ∼RandomDevices ()=default

  Default destructor.

Private Attributes

- std::random_device rd_

  *used to seed std::mt19937 prng_*
- std::mt19937 prng_

  Mersenne twister random number generator.

Friends

- class internal::Singleton< RandomDevices >

Additional Inherited Members

7.41.1 Detailed Description

Singleton class that manages the source of randomness in the library.

Consists of a wrapper around an std::mt19937 Mersenne twister random number generator engine and an std↵ ::random_device engine. The latter is used to seed the Mersenne twister.

Warning

> This class DOES NOT seed the standard C number generator used by Eigen::Matrix::Random(), since it is not thread safe. Do not use Eigen::Matrix::Random() or functions that depend on the C style random number engine, but use qpp::rand() instead!

7.41.2 Constructor & Destructor Documentation

7.41.2.1 RandomDevices()

```
qpp::RandomDevices::RandomDevices ( )  [inline], [private]
```

Initializes and seeds the random number generators.

7.41.2.2 ∼RandomDevices()

```
qpp::RandomDevices::∼RandomDevices ( )  [private], [default]
```

Default destructor.

7.41.3 Member Function Documentation

7.41.3.1 get_prng()

```
std::mt19937& qpp::RandomDevices::get_prng ( )  [inline]
```

Returns a reference to the internal PRNG object.

Returns

> Reference to the internal PRNG object

7.41.3.2 load()

```
std::istream& qpp::RandomDevices::load (
            std::istream & is )  [inline]
```

Loads the state of the PRNG from an input stream.

Parameters

is	Input stream

Returns

The input stream

7.41.3.3 save()

```
std::ostream& qpp::RandomDevices::save (
            std::ostream & os ) const  [inline]
```

Saves the state of the PRNG to an output stream.

Parameters

os	Output stream

Returns

The output stream

7.41.4 Friends And Related Function Documentation

7.41.4.1 internal::Singleton< RandomDevices >

```
friend class internal::Singleton< RandomDevices >  [friend]
```

7.41.5 Member Data Documentation

7.41.5.1 prng_

```
std::mt19937 qpp::RandomDevices::prng_  [private]
```

Mersenne twister random number generator.

7.41.5.2 rd_

```
std::random_device qpp::RandomDevices::rd_  [private]
```

used to seed std::mt19937 prng_

The documentation for this class was generated from the following file:

- classes/random_devices.h

7.42 qpp::internal::Singleton< T > Class Template Reference

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

```
#include <internal/classes/singleton.h>
```

Static Public Member Functions

- static T & get_instance () noexcept(std::is_nothrow_constructible< T >::value)
- static T & get_thread_local_instance () noexcept(std::is_nothrow_constructible< T >::value)

Protected Member Functions

- Singleton () noexcept=default
- Singleton (const Singleton &)=delete
- Singleton & operator= (const Singleton &)=delete
- virtual ~Singleton ()=default

7.42.1 Detailed Description

template<typename T>
class qpp::internal::Singleton< T >

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

To implement a singleton, derive your class from qpp::internal::Singleton, make qpp::internal::Singleton a friend of your class, then declare the constructor and destructor of your class as private. To get an instance, use the static member function qpp::internal::Singleton::get_instance() (qpp::internal::Singleton::get_thread_local_↩instance()), which returns a reference (thread_local reference) to your newly created singleton (thread-safe in C++11).

Example:

```
class MySingleton: public qpp::internal::Singleton<MySingleton>
{
       friend class qpp::internal::Singleton<MySingleton>;
public:
    // Declare all public members here
private:
    MySingleton()
    {
        // Implement the constructor here
    }
    ~MySingleton()
    {
        // Implement the destructor here
    }
};

MySingleton& mySingleton = MySingleton::get_instance(); // Get an instance
thread_local MySingleton& tls = MySingleton::get_thread_local_instance();
// Get a thread_local instance
```

See also

Code of qpp::Codes, qpp::Gates, qpp::Init, qpp::RandomDevices, qpp::States or qpp.h for real world examples of usage.

7.42.2 Constructor & Destructor Documentation

7.42.2.1 Singleton() [1/2]

```
template<typename T>
qpp::internal::Singleton< T >::Singleton ( )  [protected], [default], [noexcept]
```

7.42.2.2 Singleton() [2/2]

```
template<typename T>
qpp::internal::Singleton< T >::Singleton (
             const Singleton< T > &  )  [protected], [delete]
```

7.42.2.3 ∼Singleton()

```
template<typename T>
virtual qpp::internal::Singleton< T >::∼Singleton ( )  [protected], [virtual], [default]
```

7.42.3 Member Function Documentation

7.42.3.1 get_instance()

```
template<typename T>
static T& qpp::internal::Singleton< T >::get_instance ( )  [inline], [static], [noexcept]
```

7.42.3.2 get_thread_local_instance()

```
template<typename T>
static T& qpp::internal::Singleton< T >::get_thread_local_instance ( )  [inline], [static],
[noexcept]
```

7.42.3.3 operator=()

```
template<typename T>
Singleton& qpp::internal::Singleton< T >::operator= (
             const Singleton< T > &  )  [protected], [delete]
```

The documentation for this class was generated from the following file:

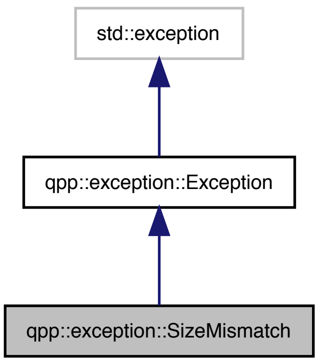
- internal/classes/singleton.h

7.43 qpp::exception::SizeMismatch Class Reference

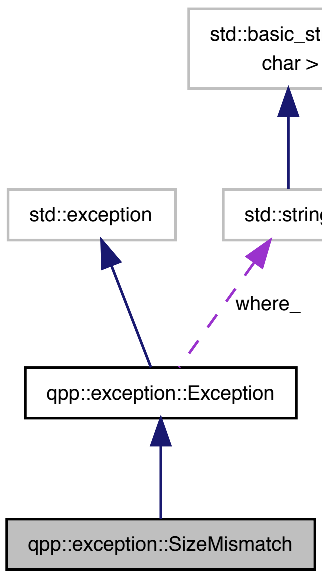
Size mismatch exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::SizeMismatch:



Collaboration diagram for qpp::exception::SizeMismatch:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::SizeMismatch

Public Member Functions

- std::string type_description () const override

    Exception type description.

7.43.1 Detailed Description

Size mismatch exception.

Sizes do not match

7.43.2 Member Function Documentation

7.43.2.1 type_description()

```
std::string qpp::exception::SizeMismatch::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

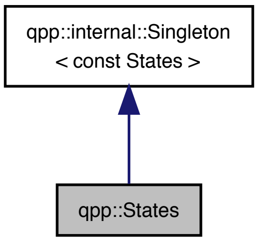
- classes/exception.h

7.44 qpp::States Class Reference

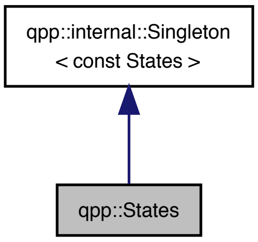
const Singleton class that implements most commonly used states

```
#include <classes/states.h>
```

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



Public Member Functions

- ket mes (idx d=2) const

  Maximally entangled state of 2 qudits.
- ket zero (idx n, idx d=2) const

  Zero state of n qudits.
- ket one (idx n, idx d=2) const

  One state of n qudits.
- ket jn (idx j, idx n, idx d=2) const

  $|j\rangle^{\otimes n}$ *state of n qudits*
- ket plus (idx n) const

  Plus state of n qubits.
- ket minus (idx n) const

  Minus state of n qubits.

Public Attributes

- ket x0 {ket::Zero(2)}

  Pauli Sigma-X 0-eigenstate |+>
- ket x1 {ket::Zero(2)}

  Pauli Sigma-X 1-eigenstate |->
- ket y0 {ket::Zero(2)}

  Pauli Sigma-Y 0-eigenstate |y+>
- ket y1 {ket::Zero(2)}

  Pauli Sigma-Y 1-eigenstate |y->
- ket z0 {ket::Zero(2)}

  Pauli Sigma-Z 0-eigenstate |0>
- ket z1 {ket::Zero(2)}

  Pauli Sigma-Z 1-eigenstate |1>
- cmat px0 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-X 0-eigenstate |+><+|.
- cmat px1 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-X 1-eigenstate |-><-|.
- cmat py0 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-Y 0-eigenstate |y+><y+|.
- cmat py1 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-Y 1-eigenstate |y-><y-|.
- cmat pz0 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-Z 0-eigenstate |0><0|.
- cmat pz1 {cmat::Zero(2, 2)}

  Projector onto the Pauli Sigma-Z 1-eigenstate |1><1|.
- ket b00 {ket::Zero(4)}

  Bell-00 state (following the convention in Nielsen and Chuang)
- ket b01 {ket::Zero(4)}

  Bell-01 state (following the convention in Nielsen and Chuang)
- ket b10 {ket::Zero(4)}

  Bell-10 state (following the convention in Nielsen and Chuang)
- ket b11 {ket::Zero(4)}

  Bell-11 state (following the convention in Nielsen and Chuang)
- cmat pb00 {cmat::Zero(4, 4)}

  Projector onto the Bell-00 state.
- cmat pb01 {cmat::Zero(4, 4)}

  Projector onto the Bell-01 state.
- cmat pb10 {cmat::Zero(4, 4)}

  Projector onto the Bell-10 state.
- cmat pb11 {cmat::Zero(4, 4)}

  Projector onto the Bell-11 state.
- ket GHZ {ket::Zero(8)}

  GHZ state.
- ket W {ket::Zero(8)}

  W state.
- cmat pGHZ {cmat::Zero(8, 8)}

  Projector onto the GHZ state.
- cmat pW {cmat::Zero(8, 8)}

  Projector onto the W state.

Private Member Functions

- States ()
- ∼States ()=default

  Default destructor.

Friends

- class internal::Singleton< const States >

Additional Inherited Members

7.44.1 Detailed Description

const Singleton class that implements most commonly used states

7.44.2 Constructor & Destructor Documentation

7.44.2.1 States()

```
qpp::States::States ( )  [inline], [private]
```

Initialize the states

7.44.2.2 ∼States()

```
qpp::States::∼States ( )  [private], [default]
```

Default destructor.

7.44.3 Member Function Documentation

7.44.3.1 jn()

```
ket qpp::States::jn (
            idx j,
            idx n,
            idx d = 2 ) const  [inline]
```

$|j\rangle^{\otimes n}$ state of *n* qudits

Parameters

j	Non-negative integer
n	Non-negative integer
d	Subsystem dimensions

Returns

$|j\rangle^{\otimes n}$ state of *n* qudits

7.44.3.2 mes()

```
ket qpp::States::mes (
              idx d = 2 ) const  [inline]
```

Maximally entangled state of 2 qudits.

Parameters

d	Subsystem dimensions

Returns

Maximally entangled state $\frac{1}{\sqrt{d}}\sum_{j=0}^{d-1}|jj\rangle$ of 2 qudits

7.44.3.3 minus()

```
ket qpp::States::minus (
              idx n ) const  [inline]
```

Minus state of *n* qubits.

Parameters

n	Non-negative integer

Returns

Minus state $|-\rangle^{\otimes n}$ of *n* qubits

7.44.3.4 one()

```
ket qpp::States::one (
            idx n,
            idx d = 2 ) const  [inline]
```

One state of *n* qudits.

Parameters

n	Non-negative integer
d	Subsystem dimensions

Returns

One state $|1\rangle^{\otimes n}$ of *n* qudits

7.44.3.5 plus()

```
ket qpp::States::plus (
            idx n ) const  [inline]
```

Plus state of *n* qubits.

Parameters

n	Non-negative integer

Returns

Plus state $|+\rangle^{\otimes n}$ of *n* qubits

7.44.3.6 zero()

```
ket qpp::States::zero (
            idx n,
            idx d = 2 ) const  [inline]
```

Zero state of *n* qudits.

Parameters

n	Non-negative integer
d	Subsystem dimensions

Returns

Zero state $|0\rangle^{\otimes n}$ of *n* qudits

7.44.4 Friends And Related Function Documentation

7.44.4.1 internal::Singleton< const States >

```
friend class internal::Singleton< const States >  [friend]
```

7.44.5 Member Data Documentation

7.44.5.1 b00

```
ket qpp::States::b00 {ket::Zero(4)}
```

Bell-00 state (following the convention in Nielsen and Chuang)

7.44.5.2 b01

```
ket qpp::States::b01 {ket::Zero(4)}
```

Bell-01 state (following the convention in Nielsen and Chuang)

7.44.5.3 b10

```
ket qpp::States::b10 {ket::Zero(4)}
```

Bell-10 state (following the convention in Nielsen and Chuang)

7.44.5.4 b11

```
ket qpp::States::b11 {ket::Zero(4)}
```

Bell-11 state (following the convention in Nielsen and Chuang)

7.44.5.5 GHZ

```
ket qpp::States::GHZ {ket::Zero(8)}
```

GHZ state.

7.44.5.6 pb00

```
cmat qpp::States::pb00 {cmat::Zero(4, 4)}
```

Projector onto the Bell-00 state.

7.44.5.7 pb01

```
cmat qpp::States::pb01 {cmat::Zero(4, 4)}
```

Projector onto the Bell-01 state.

7.44.5.8 pb10

```
cmat qpp::States::pb10 {cmat::Zero(4, 4)}
```

Projector onto the Bell-10 state.

7.44.5.9 pb11

```
cmat qpp::States::pb11 {cmat::Zero(4, 4)}
```

Projector onto the Bell-11 state.

7.44.5.10 pGHZ

```
cmat qpp::States::pGHZ {cmat::Zero(8, 8)}
```

Projector onto the GHZ state.

7.44.5.11 pW

```
cmat qpp::States::pW {cmat::Zero(8, 8)}
```

Projector onto the W state.

7.44.5.12 px0

```
cmat qpp::States::px0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-X 0-eigenstate |+><+|.

7.44.5.13 px1

```
cmat qpp::States::px1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-X 1-eigenstate |-><-|.

7.44.5.14 py0

```
cmat qpp::States::py0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Y 0-eigenstate |y+><y+|.

7.44.5.15 py1

```
cmat qpp::States::py1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Y 1-eigenstate |y-><y-|.

7.44.5.16 pz0

```
cmat qpp::States::pz0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Z 0-eigenstate |0><0|.

7.44.5.17 pz1

```
cmat qpp::States::pz1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Z 1-eigenstate |1><1|.

7.44.5.18 W

```
ket qpp::States::W {ket::Zero(8)}
```

W state.

7.44.5.19 x0

```
ket qpp::States::x0 {ket::Zero(2)}
```

Pauli Sigma-X 0-eigenstate |+>

7.44.5.20 x1

```
ket qpp::States::x1 {ket::Zero(2)}
```

Pauli Sigma-X 1-eigenstate |->

7.44.5.21 y0

```
ket qpp::States::y0 {ket::Zero(2)}
```

Pauli Sigma-Y 0-eigenstate |y+>

7.44.5.22 y1

```
ket qpp::States::y1 {ket::Zero(2)}
```

Pauli Sigma-Y 1-eigenstate |y->

7.44.5.23 z0

```
ket qpp::States::z0 {ket::Zero(2)}
```

Pauli Sigma-Z 0-eigenstate |0>

7.44.5.24 z1

```
ket qpp::States::z1 {ket::Zero(2)}
```

Pauli Sigma-Z 1-eigenstate |1>

The documentation for this class was generated from the following file:

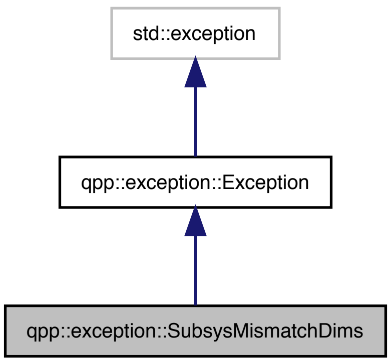
- classes/states.h

7.45 qpp::exception::SubsysMismatchDims Class Reference

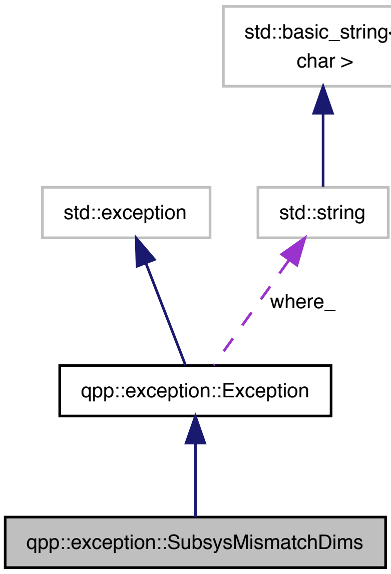
Subsystems mismatch dimensions exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::SubsysMismatchDims:



Collaboration diagram for qpp::exception::SubsysMismatchDims:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::SubsysMismatchDims

Public Member Functions

- std::string type_description () const override

    Exception type description.

7.45.1 Detailed Description

Subsystems mismatch dimensions exception.

std::vector<idx> of subsystem labels has duplicates, or has entries that are larger than the size of the std↩
::vector<idx> of dimensions

7.45.2 Member Function Documentation

7.45.2.1 type_description()

```
std::string qpp::exception::SubsysMismatchDims::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

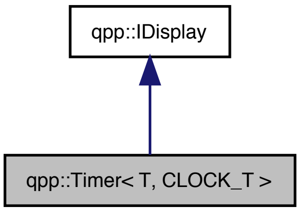
- classes/exception.h

7.46 qpp::Timer< T, CLOCK_T > Class Template Reference

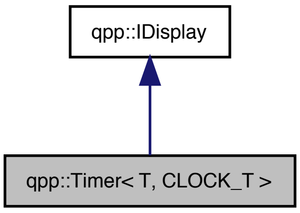
Chronometer.

```
#include <classes/timer.h>
```

Inheritance diagram for qpp::Timer< T, CLOCK_T >:



Collaboration diagram for qpp::Timer< T, CLOCK_T >:



Public Member Functions

- Timer () noexcept

  Constructs an instance with the current time as the starting point.
- void tic () noexcept

  Resets the chronometer.
- const Timer & toc () noexcept

  Stops the chronometer.
- double tics () const noexcept

  Time passed in the duration specified by T.
- template<typename U = T>
  U get_duration () const noexcept

  Duration specified by U.
- Timer (const Timer &)=default

  Default copy constructor.
- Timer (Timer &&)=default

  Default move constructor.
- Timer & operator= (const Timer &)=default

  Default copy assignment operator.
- Timer & operator= (Timer &&)=default

  Default move assignment operator.
- virtual ∼Timer ()=default

  Default virtual destructor.

Protected Attributes

- CLOCK_T::time_point start_
- CLOCK_T::time_point end_

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  qpp::IDisplay::display() override

7.46.1 Detailed Description

**template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock>
class qpp::Timer< T, CLOCK_T >**

Chronometer.

Template Parameters

T	Tics duration, default is std::chrono::duration<double, 1>, i.e. seconds in double precision
CLOCK←_T	Clock's type, default is std::chrono::steady_clock, not affected by wall clock changes during runtime

7.46.2 Constructor & Destructor Documentation

7.46.2.1 Timer() [1/3]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
qpp::Timer< T, CLOCK_T >::Timer ( )  [inline], [noexcept]
```

Constructs an instance with the current time as the starting point.

7.46.2.2 Timer() [2/3]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
qpp::Timer< T, CLOCK_T >::Timer (
             const Timer< T, CLOCK_T > &  )  [default]
```

Default copy constructor.

7.46.2.3 Timer() [3/3]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
qpp::Timer< T, CLOCK_T >::Timer (
             Timer< T, CLOCK_T > &&  )  [default]
```

Default move constructor.

7.46.2.4 ∼Timer()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
virtual qpp::Timer< T, CLOCK_T >::∼Timer ( )  [virtual], [default]
```

Default virtual destructor.

7.46.3 Member Function Documentation

7.46.3.1 display()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
std::ostream& qpp::Timer< T, CLOCK_T >::display (
             std::ostream & os ) const  [inline], [override], [private], [virtual]
```

qpp::IDisplay::display() override

Parameters

os	Output stream

Returns

Writes to the output stream the number of tics (specified by T) that passed between the instantiation/reset and invocation of qpp::Timer::toc().

Implements qpp::IDisplay.

7.46.3.2 get_duration()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
template<typename U = T>
U qpp::Timer< T, CLOCK_T >::get_duration ( ) const  [inline], [noexcept]
```

Duration specified by U.

Template Parameters

U	Duration, default is T, which defaults to std::chrono::duration<double, 1>, i.e. seconds in double precision

Returns

Duration that passed between the instantiation/reset and invocation of qpp::Timer::toc()

7.46.3.3 operator=() [1/2]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
Timer& qpp::Timer< T, CLOCK_T >::operator= (
             const Timer< T, CLOCK_T > &  )  [default]
```

Default copy assignment operator.

7.46.3.4 operator=() [2/2]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
Timer& qpp::Timer< T, CLOCK_T >::operator= (
             Timer< T, CLOCK_T > &&  )  [default]
```

Default move assignment operator.

7.46.3.5 tic()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
void qpp::Timer< T, CLOCK_T >::tic ( )  [inline], [noexcept]
```

Resets the chronometer.

Resets the starting/ending point to the current time

7.46.3.6 tics()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
double qpp::Timer< T, CLOCK_T >::tics ( ) const  [inline], [noexcept]
```

Time passed in the duration specified by T.

Returns

Number of tics (specified by T) that passed between the instantiation/reset and invocation of qpp::Timer::toc()

7.46.3.7 toc()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
const Timer& qpp::Timer< T, CLOCK_T >::toc ( )  [inline], [noexcept]
```

Stops the chronometer.

Set the current time as the ending point

Returns

Current instance

7.46.4 Member Data Documentation

7.46.4.1 end_

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
CLOCK_T::time_point qpp::Timer< T, CLOCK_T >::end_  [protected]
```

7.46.4.2 start_

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
CLOCK_T::time_point qpp::Timer< T, CLOCK_T >::start_  [protected]
```

The documentation for this class was generated from the following file:

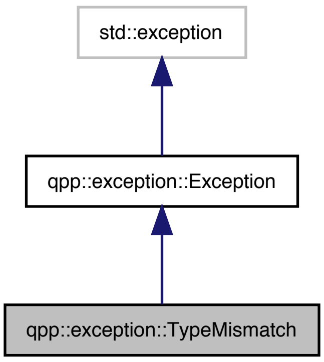
- classes/timer.h

7.47 qpp::exception::TypeMismatch Class Reference

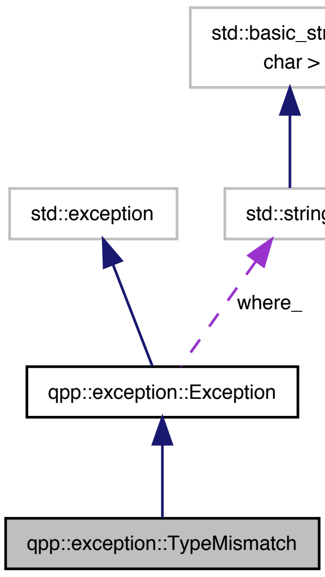
Type mismatch exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::TypeMismatch:



Collaboration diagram for qpp::exception::TypeMismatch:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::TypeMismatch

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.47.1 Detailed Description

Type mismatch exception.

Scalar types do not match

7.47.2 Member Function Documentation

7.47.2.1 type_description()

```
std::string qpp::exception::TypeMismatch::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

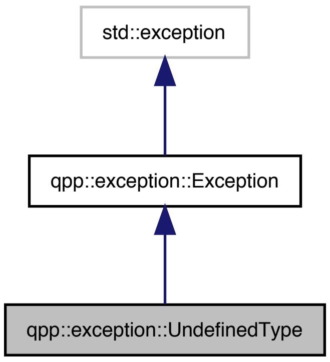
- classes/exception.h

7.48 qpp::exception::UndefinedType Class Reference

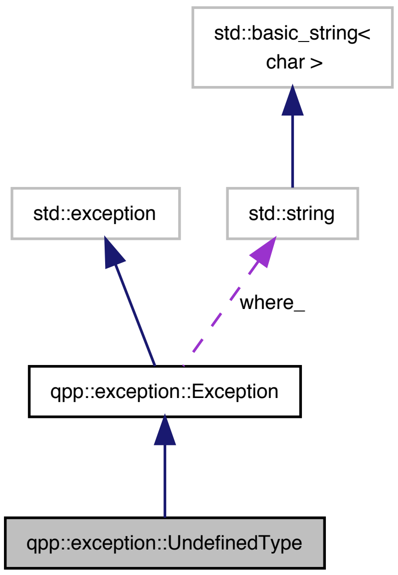
Not defined for this type exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::UndefinedType:



Collaboration diagram for qpp::exception::UndefinedType:


std::basic_string< char >
std::exception
std::string
where_
qpp::exception::Exception
qpp::exception::UndefinedType

Public Member Functions

- std::string type_description () const override

  Exception type description.

7.48.1 Detailed Description

Not defined for this type exception.

Templated specialization is not defined for this type

7.48.2 Member Function Documentation

7.48.2.1 type_description()

```
std::string qpp::exception::UndefinedType::type_description ( ) const  [inline], [override],
[virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

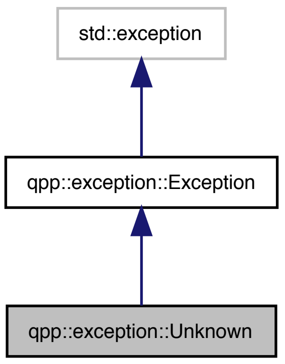
- classes/exception.h

7.49 qpp::exception::Unknown Class Reference

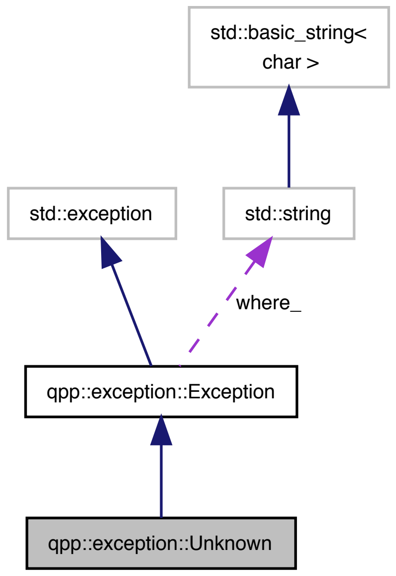
Unknown exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::Unknown:



Collaboration diagram for qpp::exception::Unknown:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.49.1 Detailed Description

Unknown exception.

Thrown when no other exception is suitable (not recommended, it is better to define another suitable exception type)

7.49.2 Member Function Documentation

7.49.2.1 type_description()

```
std::string qpp::exception::Unknown::type_description ( ) const  [inline], [override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

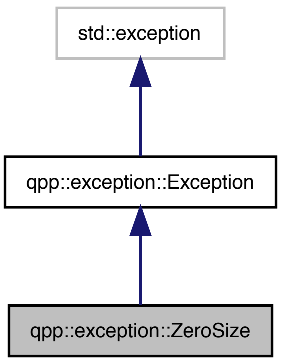
- classes/exception.h

7.50 qpp::exception::ZeroSize Class Reference

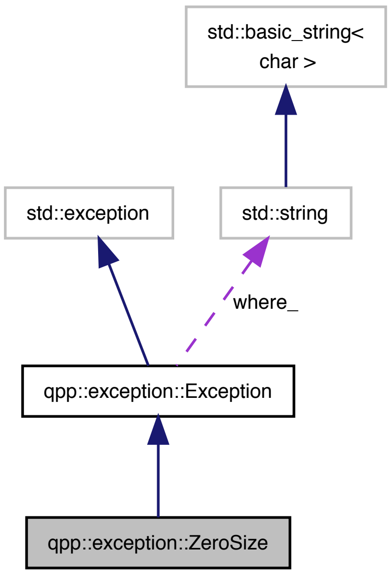
Object has zero size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::ZeroSize:



Collaboration diagram for qpp::exception::ZeroSize:



Public Member Functions

- std::string type_description () const override

  Exception type description.

7.50.1 Detailed Description

Object has zero size exception.

Zero sized object, e.g. empty Eigen::Matrix or std::vector with no elements

7.50.2 Member Function Documentation

7.50.2.1 type_description()

```
std::string qpp::exception::ZeroSize::type_description ( ) const  [inline], [override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements qpp::exception::Exception.

The documentation for this class was generated from the following file:

- classes/exception.h

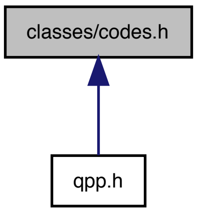
Chapter 8

File Documentation

8.1 classes/codes.h File Reference

Quantum error correcting codes.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::Codes

  const Singleton class that defines quantum error correcting codes

Namespaces

- qpp

  Quantum++ main namespace.

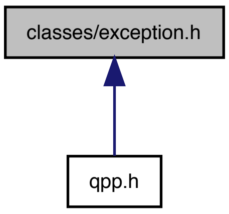
8.1.1 Detailed Description

Quantum error correcting codes.

8.2 classes/exception.h File Reference

Exceptions.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::exception::Exception

    Base class for generating Quantum++ custom exceptions.
- class qpp::exception::Unknown

    Unknown exception.
- class qpp::exception::ZeroSize

    Object has zero size exception.
- class qpp::exception::MatrixNotSquare

    Matrix is not square exception.
- class qpp::exception::MatrixNotCvector

    Matrix is not a column vector exception.
- class qpp::exception::MatrixNotRvector

    Matrix is not a row vector exception.
- class qpp::exception::MatrixNotVector

    Matrix is not a vector exception.
- class qpp::exception::MatrixNotSquareNorCvector

    Matrix is not square nor column vector exception.
- class qpp::exception::MatrixNotSquareNorRvector

    Matrix is not square nor row vector exception.
- class qpp::exception::MatrixNotSquareNorVector

    Matrix is not square nor vector exception.
- class qpp::exception::MatrixMismatchSubsys

    Matrix mismatch subsystems exception.
- class qpp::exception::DimsInvalid

    Invalid dimension(s) exception.
- class qpp::exception::DimsNotEqual

    Dimensions not equal exception.
- class qpp::exception::DimsMismatchMatrix

    Dimension(s) mismatch matrix size exception.
- class qpp::exception::DimsMismatchCvector

Dimension(s) mismatch column vector size exception.
- class qpp::exception::DimsMismatchRvector

  Dimension(s) mismatch row vector size exception.
- class qpp::exception::DimsMismatchVector

  Dimension(s) mismatch vector size exception.
- class qpp::exception::SubsysMismatchDims

  Subsystems mismatch dimensions exception.
- class qpp::exception::PermInvalid

  Invalid permutation exception.
- class qpp::exception::PermMismatchDims

  Permutation mismatch dimensions exception.
- class qpp::exception::NotQubitMatrix

  Matrix is not 2 x 2 exception.
- class qpp::exception::NotQubitCvector

  Column vector is not 2 x 1 exception.
- class qpp::exception::NotQubitRvector

  Row vector is not 1 x 2 exception.
- class qpp::exception::NotQubitVector

  Vector is not 2 x 1 nor 1 x 2 exception.
- class qpp::exception::NotQubitSubsys

  Subsystems are not qubits exception.
- class qpp::exception::NotBipartite

  Not bi-partite exception.
- class qpp::exception::NoCodeword

  Codeword does not exist exception.
- class qpp::exception::OutOfRange

  Parameter out of range exception.
- class qpp::exception::TypeMismatch

  Type mismatch exception.
- class qpp::exception::SizeMismatch

  Size mismatch exception.
- class qpp::exception::UndefinedType

  Not defined for this type exception.
- class qpp::exception::CustomException

  Custom exception.

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::exception

  Quantum++ exception hierarchy namespace.

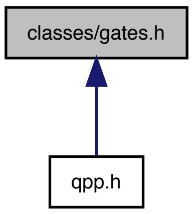
8.2.1 Detailed Description

Exceptions.

8.3 classes/gates.h File Reference

Quantum gates.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::Gates

  const Singleton class that implements most commonly used gates

Namespaces

- qpp

  Quantum++ main namespace.

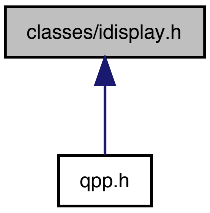
8.3.1 Detailed Description

Quantum gates.

8.4 classes/idisplay.h File Reference

Display interface via the non-virtual interface (NVI)

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::IDisplay

  Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

Namespaces

- qpp

  Quantum++ main namespace.

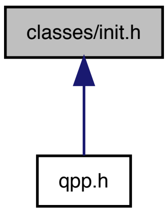
8.4.1 Detailed Description

Display interface via the non-virtual interface (NVI)

8.5 classes/init.h File Reference

Initialization.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::Init

  const Singleton class that performs additional initializations/cleanups

Namespaces

- qpp

  Quantum++ main namespace.

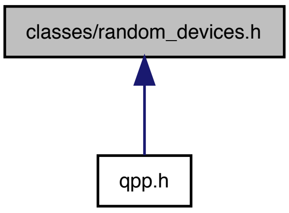
8.5.1 Detailed Description

Initialization.

8.6 classes/random_devices.h File Reference

Random devices.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::RandomDevices

    Singeleton class that manages the source of randomness in the library.

Namespaces

- qpp

    Quantum++ main namespace.

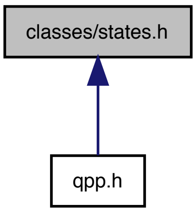
8.6.1 Detailed Description

Random devices.

8.7 classes/states.h File Reference

Quantum states.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::States

  const Singleton class that implements most commonly used states

Namespaces

- qpp

  Quantum++ main namespace.

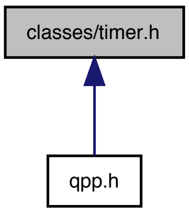
8.7.1 Detailed Description

Quantum states.

8.8 classes/timer.h File Reference

Timing.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::Timer< T, CLOCK_T >

  Chronometer.

Namespaces

- qpp

  Quantum++ main namespace.

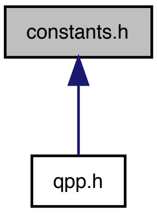
8.8.1 Detailed Description

Timing.

8.9 constants.h File Reference

Constants.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

    Quantum++ main namespace.

Functions

- constexpr cplx qpp::operator"" _i (unsigned long long int x) noexcept

    User-defined literal for complex $i = \sqrt{-1}$ (integer overload)
- constexpr cplx qpp::operator"" _i (long double x) noexcept

    User-defined literal for complex $i = \sqrt{-1}$ (real overload)
- cplx qpp::omega (idx D)

    D-th root of unity.

Variables

- constexpr double qpp::chop = 1e-10

    Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.
- constexpr double qpp::eps = 1e-12

    Used to decide whether a number or expression in double precision is zero or not.
- constexpr idx qpp::maxn = 64

    Maximum number of allowed qubits/qudits (subsystems)
- constexpr double qpp::pi = 3.141592653589793238462643383279502884

    π
- constexpr double qpp::ee = 2.718281828459045235360287471352662497

    Base of natural logarithm, e.
- constexpr double qpp::infty = std::numeric_limits$<$double$>$::max()

    Used to denote infinity in double precision.

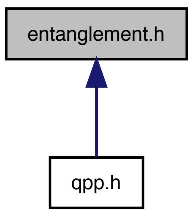
8.9.1 Detailed Description

Constants.

8.10 entanglement.h File Reference

Entanglement functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

    Quantum++ main namespace.

Functions

- template< typename Derived >
  dyn_col_vect< double > qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

    Schmidt coefficients of the bi-partite pure state A.
- template< typename Derived >
  dyn_col_vect< double > qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, idx d=2)

    Schmidt coefficients of the bi-partite pure state A.
- template< typename Derived >
  cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

    Schmidt basis on Alice side.
- template< typename Derived >
  cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > &A, idx d=2)

    Schmidt basis on Alice side.
- template< typename Derived >
  cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

    Schmidt basis on Bob side.
- template< typename Derived >
  cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > &A, idx d=2)

Schmidt basis on Bob side.

- template<typename Derived >
  std::vector< double > qpp::schmidtprobs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt probabilities of the bi-partite pure state A.
- template<typename Derived >
  std::vector< double > qpp::schmidtprobs (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt probabilities of the bi-partite pure state A.
- template<typename Derived >
  double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Entanglement of the bi-partite pure state A.
- template<typename Derived >
  double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Entanglement of the bi-partite pure state A.
- template<typename Derived >
  double qpp::gconcurrence (const Eigen::MatrixBase< Derived > &A)

  G-concurrence of the bi-partite pure state A.
- template<typename Derived >
  double qpp::negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Negativity of the bi-partite mixed state A.
- template<typename Derived >
  double qpp::negativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Negativity of the bi-partite mixed state A.
- template<typename Derived >
  double qpp::lognegativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Logarithmic negativity of the bi-partite mixed state A.
- template<typename Derived >
  double qpp::lognegativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Logarithmic negativity of the bi-partite mixed state A.
- template<typename Derived >
  double qpp::concurrence (const Eigen::MatrixBase< Derived > &A)

  Wootters concurrence of the bi-partite qubit mixed state A.

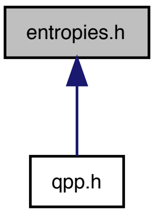
8.10.1 Detailed Description

Entanglement functions.

8.11 entropies.h File Reference

Entropy functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template< typename Derived >
  double qpp::entropy (const Eigen::MatrixBase< Derived > &A)

  von-Neumann entropy of the density matrix A
- double qpp::entropy (const std::vector< double > &prob)

  Shannon entropy of the probability distribution prob.
- template< typename Derived >
  double qpp::renyi (const Eigen::MatrixBase< Derived > &A, double alpha)

  Renyi- α entropy of the density matrix A, for $\alpha \geq 0$.
- double qpp::renyi (const std::vector< double > &prob, double alpha)

  Renyi- α entropy of the probability distribution prob, for $\alpha \geq 0$.
- template< typename Derived >
  double qpp::tsallis (const Eigen::MatrixBase< Derived > &A, double q)

  Tsallis- q entropy of the density matrix A, for $q \geq 0$.
- double qpp::tsallis (const std::vector< double > &prob, double q)

  Tsallis- q entropy of the probability distribution prob, for $q \geq 0$.
- template< typename Derived >
  double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, const std::vector< idx > &dims)

  Quantum mutual information between 2 subsystems of a composite system.
- template< typename Derived >
  double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, idx d=2)

  Quantum mutual information between 2 subsystems of a composite system.

8.11.1 Detailed Description

Entropy functions.

8.12 experimental/experimental.h File Reference

Experimental/test functions/classes.

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::experimental

  Experimental/test functions/classes, do not use or modify.

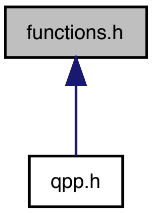
8.12.1 Detailed Description

Experimental/test functions/classes.

8.13 functions.h File Reference

Generic quantum computing functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::transpose (const Eigen::MatrixBase< Derived > &A)

  Transpose.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::conjugate (const Eigen::MatrixBase< Derived > &A)

  Complex conjugate.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::adjoint (const Eigen::MatrixBase< Derived > &A)

  Adjoint.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::inverse (const Eigen::MatrixBase< Derived > &A)

  Inverse.
- template<typename Derived >
  Derived::Scalar qpp::trace (const Eigen::MatrixBase< Derived > &A)

  Trace.
- template<typename Derived >
  Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > &A)

  Determinant.
- template<typename Derived >
  Derived::Scalar qpp::logdet (const Eigen::MatrixBase< Derived > &A)

  Logarithm of the determinant.
- template<typename Derived >
  Derived::Scalar qpp::sum (const Eigen::MatrixBase< Derived > &A)

  Element-wise sum of A.
- template<typename Derived >
  Derived::Scalar qpp::prod (const Eigen::MatrixBase< Derived > &A)

  Element-wise product of A.
- template<typename Derived >
  double qpp::norm (const Eigen::MatrixBase< Derived > &A)

  Frobenius norm.
- template<typename Derived >
  std::pair< dyn_col_vect< cplx >, cmat > qpp::eig (const Eigen::MatrixBase< Derived > &A)

  Full eigen decomposition.
- template<typename Derived >
  dyn_col_vect< cplx > qpp::evals (const Eigen::MatrixBase< Derived > &A)

  Eigenvalues.
- template<typename Derived >
  cmat qpp::evects (const Eigen::MatrixBase< Derived > &A)

  Eigenvectors.
- template<typename Derived >
  std::pair< dyn_col_vect< double >, cmat > qpp::heig (const Eigen::MatrixBase< Derived > &A)

  Full eigen decomposition of Hermitian expression.
- template<typename Derived >
  dyn_col_vect< double > qpp::hevals (const Eigen::MatrixBase< Derived > &A)

  Hermitian eigenvalues.
- template<typename Derived >
  cmat qpp::hevects (const Eigen::MatrixBase< Derived > &A)

  Hermitian eigenvectors.
- template<typename Derived >
  std::tuple< cmat, dyn_col_vect< double >, cmat > qpp::svd (const Eigen::MatrixBase< Derived > &A)

  Full singular value decomposition.

- template<typename Derived >
  dyn_col_vect< double > qpp::svals (const Eigen::MatrixBase< Derived > &A)

  Singular values.
- template<typename Derived >
  cmat qpp::svdU (const Eigen::MatrixBase< Derived > &A)

  Left singular vectors.
- template<typename Derived >
  cmat qpp::svdV (const Eigen::MatrixBase< Derived > &A)

  Right singular vectors.
- template<typename Derived >
  cmat qpp::funm (const Eigen::MatrixBase< Derived > &A, cplx(∗f)(const cplx &))

  Functional calculus f(A)
- template<typename Derived >
  cmat qpp::sqrtm (const Eigen::MatrixBase< Derived > &A)

  Matrix square root.
- template<typename Derived >
  cmat qpp::absm (const Eigen::MatrixBase< Derived > &A)

  Matrix absolute value.
- template<typename Derived >
  cmat qpp::expm (const Eigen::MatrixBase< Derived > &A)

  Matrix exponential.
- template<typename Derived >
  cmat qpp::logm (const Eigen::MatrixBase< Derived > &A)

  Matrix logarithm.
- template<typename Derived >
  cmat qpp::sinm (const Eigen::MatrixBase< Derived > &A)

  Matrix sin.
- template<typename Derived >
  cmat qpp::cosm (const Eigen::MatrixBase< Derived > &A)

  Matrix cos.
- template<typename Derived >
  cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived > &A, const cplx z)

  Matrix power.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::powm (const Eigen::MatrixBase< Derived > &A, idx n)

  Fast matrix power based on the SQUARE-AND-MULTIPLY algorithm.
- template<typename Derived >
  double qpp::schatten (const Eigen::MatrixBase< Derived > &A, double p)

  Schatten matrix norm.
- template<typename OutputScalar , typename Derived >
  dyn_mat< OutputScalar > qpp::cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(∗f)(const typename Derived::Scalar &))

  Functor.
- template<typename T >
  dyn_mat< typename T::Scalar > qpp::kron (const T &head)

  Kronecker product.
- template<typename T , typename ... Args>
  dyn_mat< typename T::Scalar > qpp::kron (const T &head, const Args &... tail)

  Kronecker product.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::kron (const std::vector< Derived > &As)

  Kronecker product.

- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::kron (const std::initializer_list< Derived > &As)

  Kronecker product.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::kronpow (const Eigen::MatrixBase< Derived > &A, idx n)

  Kronecker power.
- template<typename T >
  dyn_mat< typename T::Scalar > qpp::dirsum (const T &head)

  Direct sum.
- template<typename T , typename ... Args>
  dyn_mat< typename T::Scalar > qpp::dirsum (const T &head, const Args &... tail)

  Direct sum.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::dirsum (const std::vector< Derived > &As)

  Direct sum.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::dirsum (const std::initializer_list< Derived > &As)

  Direct sum.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::dirsumpow (const Eigen::MatrixBase< Derived > &A, idx n)

  Direct sum power.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::reshape (const Eigen::MatrixBase< Derived > &A, idx rows, idx cols)

  Reshape.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)

  Commutator.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)

  Anti-commutator.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::prj (const Eigen::MatrixBase< Derived > &A)

  Projector.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::grams (const std::vector< Derived > &As)

  Gram-Schmidt orthogonalization.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::grams (const std::initializer_list< Derived > &As)

  Gram-Schmidt orthogonalization.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::grams (const Eigen::MatrixBase< Derived > &A)

  Gram-Schmidt orthogonalization.
- std::vector< idx > qpp::n2multiidx (idx n, const std::vector< idx > &dims)

  Non-negative integer index to multi-index.
- idx qpp::multiidx2n (const std::vector< idx > &midx, const std::vector< idx > &dims)

  Multi-index to non-negative integer index.
- ket qpp::mket (const std::vector< idx > &mask, const std::vector< idx > &dims)

  Multi-partite qudit ket.
- ket qpp::mket (const std::vector< idx > &mask, idx d=2)

  Multi-partite qudit ket.

- cmat qpp::mprj (const std::vector< idx > &mask, const std::vector< idx > &dims)

    Projector onto multi-partite qudit ket.
- cmat qpp::mprj (const std::vector< idx > &mask, idx d=2)

    Projector onto multi-partite qudit ket.
- template<typename InputIterator >
  std::vector< double > qpp::abssq (InputIterator first, InputIterator last)

    Computes the absolute values squared of an STL-like range of complex numbers.
- template<typename Container >
  std::vector< double > qpp::abssq (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type ∗=nullptr)

    Computes the absolute values squared of an STL-like container.
- template<typename Derived >
  std::vector< double > qpp::abssq (const Eigen::MatrixBase< Derived > &A)

    Computes the absolute values squared of an Eigen expression.
- template<typename InputIterator >
  std::iterator_traits< InputIterator >::value_type qpp::sum (InputIterator first, InputIterator last)

    Element-wise sum of an STL-like range.
- template<typename Container >
  Container::value_type qpp::sum (const Container &c, typename std::enable_if< is_iterable< Container >↩ ::value >::type ∗=nullptr)

    Element-wise sum of the elements of an STL-like container.
- template<typename InputIterator >
  std::iterator_traits< InputIterator >::value_type qpp::prod (InputIterator first, InputIterator last)

    Element-wise product of an STL-like range.
- template<typename Container >
  Container::value_type qpp::prod (const Container &c, typename std::enable_if< is_iterable< Container >↩ ::value >::type ∗=nullptr)

    Element-wise product of the elements of an STL-like container.
- template<typename Derived >
  dyn_col_vect< typename Derived::Scalar > qpp::rho2pure (const Eigen::MatrixBase< Derived > &A)

    Finds the pure state representation of a matrix proportional to a projector onto a pure state.
- template<typename T >
  std::vector< T > qpp::complement (std::vector< T > subsys, idx N)

    Constructs the complement of a subsystem vector.
- template<typename Derived >
  std::vector< double > qpp::rho2bloch (const Eigen::MatrixBase< Derived > &A)

    Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix A.
- cmat qpp::bloch2rho (const std::vector< double > &r)

    Computes the density matrix corresponding to the 3-dimensional real Bloch vector r.

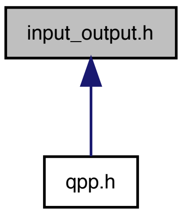
8.13.1 Detailed Description

Generic quantum computing functions.

8.14 input_output.h File Reference

Input/output functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template< typename Derived >
  internal::IOManipEigen qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)

  Eigen expression ostream manipulator.
- internal::IOManipEigen qpp::disp (cplx z, double chop=qpp::chop)

  Complex number ostream manipulator.
- template< typename InputIterator >
  internal::IOManipRange< InputIterator > qpp::disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")

  Range ostream manipulator.
- template< typename Container >
  internal::IOManipRange< typename Container::const_iterator > qpp::disp (const Container &c, const std↩
  ::string &separator, const std::string &start="[", const std::string &end="]", typename std::enable_if< is_↩
  iterable< Container >::value >::type ∗=nullptr)

  Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.
- template< typename PointerType >
  internal::IOManipPointer< PointerType > qpp::disp (const PointerType ∗p, idx N, const std::string &separator, const std::string &start="[", const std::string &end="]")

  C-style pointer ostream manipulator.
- template< typename Derived >
  void qpp::save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

  Saves Eigen expression to a binary file (internal format) in double precision.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::load (const std::string &fname)

  Loads Eigen matrix from a binary file (internal format) in double precision.

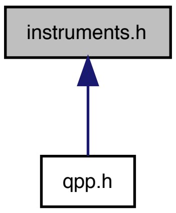
8.14.1 Detailed Description

Input/output functions.

8.15 instruments.h File Reference

Measurement functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

    Quantum++ main namespace.

Functions

- template< typename Derived >
  dyn_col_vect< typename Derived::Scalar > qpp::ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, const std::vector< idx > &dims)

    Generalized inner product.
- template< typename Derived >
  dyn_col_vect< typename Derived::Scalar > qpp::ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, idx d=2)

    Generalized inner product.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

    Measures the state A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)

    Measures the state A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &U)

    Measures the state A in the orthonormal basis specified by the unitary matrix U.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

    Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- template<typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, idx d=2)

  Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- template<typename Derived >
  std::tuple< std::vector< idx >, double, cmat > qpp::measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, std::vector< idx > dims)

  Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.
- template<typename Derived >
  std::tuple< std::vector< idx >, double, cmat > qpp::measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, idx d=2)

  Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.

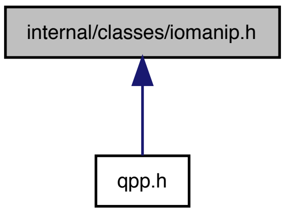
8.15.1 Detailed Description

Measurement functions.

8.16 internal/classes/iomanip.h File Reference

Input/output manipulators.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::internal::IOManipRange< InputIterator >
- class qpp::internal::IOManipPointer< PointerType >
- class qpp::internal::IOManipEigen

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::internal

  Internal utility functions, do not use them directly or modify them.

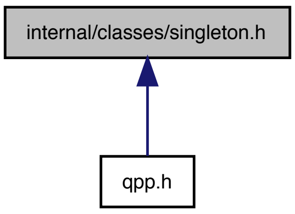
8.16.1 Detailed Description

Input/output manipulators.

8.17 internal/classes/singleton.h File Reference

Singleton pattern via CRTP.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::internal::Singleton< T >

  Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::internal

  Internal utility functions, do not use them directly or modify them.

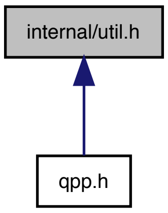
8.17.1 Detailed Description

Singleton pattern via CRTP.

8.18 internal/util.h File Reference

Internal utility functions.

This graph shows which files directly or indirectly include this file:



Classes

- struct qpp::internal::Display_Impl_

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::internal

  Internal utility functions, do not use them directly or modify them.

Functions

- void qpp::internal::n2multiidx (idx n, idx numdims, const idx ∗const dims, idx ∗result) noexcept
- idx qpp::internal::multiidx2n (const idx ∗const midx, idx numdims, const idx ∗const dims) noexcept
- template<typename Derived >

  bool qpp::internal::check_square_mat (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >

  bool qpp::internal::check_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >

  bool qpp::internal::check_rvector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >

  bool qpp::internal::check_cvector (const Eigen::MatrixBase< Derived > &A)
- template<typename T >

  bool qpp::internal::check_nonzero_size (const T &x) noexcept

- template<typename T1 , typename T2 >
  bool qpp::internal::check_matching_sizes (const T1 &lhs, const T2 &rhs) noexcept
- bool qpp::internal::check_dims (const std::vector< idx > &dims)
- template<typename Derived >
  bool qpp::internal::check_dims_match_mat (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool qpp::internal::check_dims_match_cvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool qpp::internal::check_dims_match_rvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- bool qpp::internal::check_eq_dims (const std::vector< idx > &dims, idx dim) noexcept
- bool qpp::internal::check_subsys_match_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)
- template<typename Derived >
  bool qpp::internal::check_qubit_matrix (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool qpp::internal::check_qubit_cvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool qpp::internal::check_qubit_rvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool qpp::internal::check_qubit_vector (const Eigen::MatrixBase< Derived > &A) noexcept
- bool qpp::internal::check_perm (const std::vector< idx > &perm)
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::internal::kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::internal::dirsum2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename T >
  void qpp::internal::variadic_vector_emplace (std::vector< T > &)
- template<typename T , typename First , typename ... Args>
  void qpp::internal::variadic_vector_emplace (std::vector< T > &v, First &&first, Args &&... args)
- idx qpp::internal::get_num_subsys (idx sz, idx d)
- idx qpp::internal::get_dim_subsys (idx sz, idx N)

8.18.1 Detailed Description

Internal utility functions.

8.19 MATLAB/matlab.h File Reference

Input/output interfacing with MATLAB.

```
#include "mat.h"
#include "mex.h"
```

Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template<typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< cplx > >::type qpp↵::loadMATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< typename Derived::↵Scalar > >::type qpp::loadMATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value >::type qpp::saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)

  Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value >::type qpp::saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)

  Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.

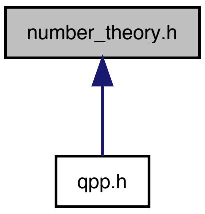
8.19.1 Detailed Description

Input/output interfacing with MATLAB.

8.20 number_theory.h File Reference

Number theory functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- std::vector< int > qpp::x2contfrac (double x, idx N, idx cut=1e5)

  Simple continued fraction expansion.
- double qpp::contfrac2x (const std::vector< int > &cf, idx N=idx(-1))

  Real representation of a simple continued fraction.
- bigint qpp::gcd (bigint a, bigint b)

  Greatest common divisor of two integers.
- bigint qpp::gcd (const std::vector< bigint > &as)

  Greatest common divisor of a list of integers.
- bigint qpp::lcm (bigint a, bigint b)

  Least common multiple of two integers.
- bigint qpp::lcm (const std::vector< bigint > &as)

  Least common multiple of a list of integers.
- std::vector< idx > qpp::invperm (const std::vector< idx > &perm)

  Inverse permutation.
- std::vector< idx > qpp::compperm (const std::vector< idx > &perm, const std::vector< idx > &sigma)

  Compose permutations.
- std::vector< bigint > qpp::factors (bigint a)

  Prime factor decomposition.
- bigint qpp::modmul (bigint a, bigint b, bigint p)

  Modular multiplication without overflow.
- bigint qpp::modpow (bigint a, bigint n, bigint p)

  Fast integer power modulo p based on the SQUARE-AND-MULTIPLY algorithm.
- std::tuple< bigint, bigint, bigint > qpp::egcd (bigint a, bigint b)

  Extended greatest common divisor of two integers.
- bigint qpp::modinv (bigint a, bigint p)

  Modular inverse of a mod p.
- bool qpp::isprime (bigint p, idx k=80)

  Primality test based on the Miller-Rabin's algorithm.
- bigint qpp::randprime (bigint a, bigint b, idx N=1000)

  Generates a random big prime uniformly distributed in the interval [a, b].

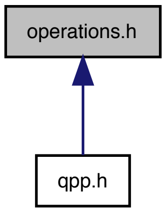
8.20.1 Detailed Description

Number theory functions.

8.21 operations.h File Reference

Quantum operation functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx d=2)

  Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, idx d=2)

  Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- template< typename Derived >
  cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

  Applies the channel specified by the set of Kraus operators Ks to the density matrix A.
- template< typename Derived >
  cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std↩
  ::vector< idx > &subsys, const std::vector< idx > &dims)

  Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.
- template< typename Derived >
  cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std↩
  ::vector< idx > &subsys, idx d=2)

  Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.

- cmat qpp::kraus2super (const std::vector< cmat > &Ks)

  Superoperator matrix.
- cmat qpp::kraus2choi (const std::vector< cmat > &Ks)

  Choi matrix.
- std::vector< cmat > qpp::choi2kraus (const cmat &A)

  Orthogonal Kraus operators from Choi matrix.
- cmat qpp::choi2super (const cmat &A)

  Converts Choi matrix to superoperator matrix.
- cmat qpp::super2choi (const cmat &A)

  Converts superoperator matrix to Choi matrix.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &dims)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &dims)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &subsys, const std::vector< idx > &dims)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &subsys, idx d=2)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Partial transpose.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)

  Partial transpose.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, const std::vector< idx > &dims)

  Subsystem permutation.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, idx d=2)

  Subsystem permutation.

8.21.1 Detailed Description

Quantum operation functions.

8.22 qpp.h File Reference

Quantum++ main header file, includes all other necessary headers.

```
#include <algorithm>
#include <cassert>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <exception>
#include <fstream>
#include <functional>
#include <initializer_list>
#include <iomanip>
#include <iterator>
#include <limits>
#include <memory>
#include <numeric>
#include <ostream>
#include <random>
#include <sstream>
#include <stdexcept>
#include <string>
#include <tuple>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "types.h"
#include "classes/exception.h"
#include "constants.h"
#include "traits.h"
#include "classes/idisplay.h"
#include "internal/util.h"
#include "internal/classes/iomanip.h"
#include "input_output.h"
#include "internal/classes/singleton.h"
#include "classes/init.h"
#include "functions.h"
#include "classes/codes.h"
#include "classes/gates.h"
#include "classes/states.h"
#include "classes/random_devices.h"
#include "statistics.h"
#include "operations.h"
#include "entropies.h"
#include "entanglement.h"
#include "random.h"
#include "classes/timer.h"
#include "instruments.h"
#include "number_theory.h"
```

Namespaces

- qpp

  Quantum++ main namespace.

Macros

- #define QPP_UNUSED_

8.22.1 Detailed Description

Quantum++ main header file, includes all other necessary headers.

8.22.2 Macro Definition Documentation

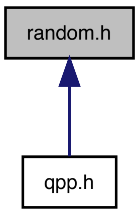
8.22.2.1 QPP_UNUSED_

```
#define QPP_UNUSED_
```

8.23 random.h File Reference

Randomness-related functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- double qpp::rand (double a, double b)

  Generates a random real number uniformly distributed in the interval [a, b)
- bigint qpp::rand (bigint a, bigint b)

  Generates a random big integer uniformly distributed in the interval [a, b].
- idx qpp::randidx (idx a=std::numeric_limits< idx >::min(), idx b=std::numeric_limits< idx >::max())

  Generates a random index (idx) uniformly distributed in the interval [a, b].
- template<typename Derived >
  Derived qpp::rand (idx rows, idx cols, double a=0, double b=1)

  Generates a random matrix with entries uniformly distributed in the interval [a, b)
- template<>
  dmat qpp::rand (idx rows, idx cols, double a, double b)

  Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)
- template<>
  cmat qpp::rand (idx rows, idx cols, double a, double b)

  Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)
- template<typename Derived >
  Derived qpp::randn (idx rows, idx cols, double mean=0, double sigma=1)

  Generates a random matrix with entries normally distributed in N(mean, sigma)
- template<>
  dmat qpp::randn (idx rows, idx cols, double mean, double sigma)

  Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)
- template<>
  cmat qpp::randn (idx rows, idx cols, double mean, double sigma)

  Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)
- double qpp::randn (double mean=0, double sigma=1)

  Generates a random real number (double) normally distributed in N(mean, sigma)
- cmat qpp::randU (idx D=2)

  Generates a random unitary matrix.
- cmat qpp::randV (idx Din, idx Dout)

  Generates a random isometry matrix.
- std::vector< cmat > qpp::randkraus (idx N, idx D=2)

  Generates a set of random Kraus operators.
- cmat qpp::randH (idx D=2)

  Generates a random Hermitian matrix.
- ket qpp::randket (idx D=2)

  Generates a random normalized ket (pure state vector)
- cmat qpp::randrho (idx D=2)

  Generates a random density matrix.
- std::vector< idx > qpp::randperm (idx N)

  Generates a random uniformly distributed permutation.
- std::vector< double > qpp::randprob (idx N)

  Generates a random probability vector uniformly distributed over the probability simplex.

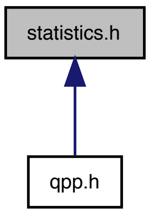
8.23.1 Detailed Description

Randomness-related functions.

8.24 statistics.h File Reference

Statistics functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- std::vector< double > qpp::uniform (idx N)

  Uniform probability distribution vector.
- std::vector< double > qpp::marginalX (const dmat &probXY)

  Marginal distribution.
- std::vector< double > qpp::marginalY (const dmat &probXY)

  Marginal distribution.
- template<typename Container >
  double qpp::avg (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↩
  iterable< Container >::value >::type ∗=nullptr)

  Average.
- template<typename Container >
  double qpp::cov (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if<
  is_iterable< Container >::value >::type ∗=nullptr)

  Covariance.
- template<typename Container >
  double qpp::var (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↩
  iterable< Container >::value >::type ∗=nullptr)

  Variance.
- template<typename Container >
  double qpp::sigma (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↩
  iterable< Container >::value >::type ∗=nullptr)

  Standard deviation.
- template<typename Container >
  double qpp::cor (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if<
  is_iterable< Container >::value >::type ∗=nullptr)

  Correlation.

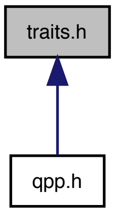
8.24.1 Detailed Description

Statistics functions.

8.25 traits.h File Reference

Type traits.

This graph shows which files directly or indirectly include this file:



Classes

- struct qpp::make_void< Ts >

  Helper for qpp::to_void<> alias template.
- struct qpp::is_iterable< T, typename >

  Checks whether T is compatible with an STL-like iterable container.
- struct qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().↩ end()), typename T::value_type > >

  Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.
- struct qpp::is_matrix_expression< Derived >

  Checks whether the type is an Eigen matrix expression.
- struct qpp::is_complex< T >

  Checks whether the type is a complex type.
- struct qpp::is_complex< std::complex< T > >

  Checks whether the type is a complex number type, specialization for complex types.

Namespaces

- qpp

  Quantum++ main namespace.

Typedefs

- template<typename... Ts>
  using qpp::to_void = typename make_void< Ts... >::type

  Alias template that implements the proposal for void_t.

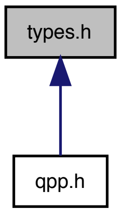
8.25.1 Detailed Description

Type traits.

8.26 types.h File Reference

Type aliases.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

    Quantum++ main namespace.

Typedefs

- using qpp::idx = std::size_t

    Non-negative integer index.
- using qpp::bigint = long long int

    Big integer.
- using qpp::cplx = std::complex< double >

    Complex number in double precision.
- using qpp::ket = Eigen::VectorXcd

    Complex (double precision) dynamic Eigen column vector.
- using qpp::bra = Eigen::RowVectorXcd

    Complex (double precision) dynamic Eigen row vector.
- using qpp::cmat = Eigen::MatrixXcd

    Complex (double precision) dynamic Eigen matrix.
- using qpp::dmat = Eigen::MatrixXd

    Real (double precision) dynamic Eigen matrix.
- template<typename Scalar >
  using qpp::dyn_mat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >

    Dynamic Eigen matrix over the field specified by Scalar.
- template<typename Scalar >
  using qpp::dyn_col_vect = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >

    Dynamic Eigen column vector over the field specified by Scalar.
- template<typename Scalar >
  using qpp::dyn_row_vect = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >

    Dynamic Eigen row vector over the field specified by Scalar.

8.26.1 Detailed Description

Type aliases.

8.27 /Users/vlad/Dropbox/programming/cpp/qpp/README.md File Reference

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