

quantum++

0.1

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# Contents

<b>1</b>	<b>quantum++ - A C++11 quantum computing library</b>	<b>1</b>
<b>2</b>	<b>Namespace Index</b>	<b>3</b>
2.1	Namespace List . . . . .	3
<b>3</b>	<b>Hierarchical Index</b>	<b>5</b>
3.1	Class Hierarchy . . . . .	5
<b>4</b>	<b>Class Index</b>	<b>7</b>
4.1	Class List . . . . .	7
<b>5</b>	<b>File Index</b>	<b>9</b>
5.1	File List . . . . .	9
<b>6</b>	<b>Namespace Documentation</b>	<b>11</b>
6.1	qpp Namespace Reference . . . . .	11
6.1.1	Typedef Documentation . . . . .	18
6.1.1.1	bra . . . . .	18
6.1.1.2	cmat . . . . .	18
6.1.1.3	cplx . . . . .	18
6.1.1.4	dmat . . . . .	19
6.1.1.5	DynMat . . . . .	19
6.1.1.6	ket . . . . .	19
6.1.2	Function Documentation . . . . .	19
6.1.2.1	absm . . . . .	19
6.1.2.2	adjoint . . . . .	19
6.1.2.3	amplitudes . . . . .	20
6.1.2.4	amplitudes . . . . .	20
6.1.2.5	anticomm . . . . .	21
6.1.2.6	apply . . . . .	22
6.1.2.7	applyCTRL . . . . .	23
6.1.2.8	channel . . . . .	24
6.1.2.9	channel . . . . .	25

6.1.2.10	choi	26
6.1.2.11	choi2kraus	27
6.1.2.12	comm	28
6.1.2.13	compperm	29
6.1.2.14	conjugate	30
6.1.2.15	cosm	30
6.1.2.16	cwise	31
6.1.2.17	det	31
6.1.2.18	disp	32
6.1.2.19	disp	32
6.1.2.20	disp	33
6.1.2.21	disp	33
6.1.2.22	displn	33
6.1.2.23	displn	34
6.1.2.24	displn	34
6.1.2.25	displn	35
6.1.2.26	entanglement	35
6.1.2.27	evals	36
6.1.2.28	evects	37
6.1.2.29	expandout	37
6.1.2.30	expm	38
6.1.2.31	funm	39
6.1.2.32	gconcurrence	39
6.1.2.33	grams	40
6.1.2.34	grams	41
6.1.2.35	grams	41
6.1.2.36	hevals	42
6.1.2.37	hevects	42
6.1.2.38	inverse	43
6.1.2.39	invperm	43
6.1.2.40	kron	44
6.1.2.41	kron	44
6.1.2.42	kron	45
6.1.2.43	kron	45
6.1.2.44	kronpow	46
6.1.2.45	load	46
6.1.2.46	loadMATLABmatrix	47
6.1.2.47	loadMATLABmatrix	47
6.1.2.48	loadMATLABmatrix	47
6.1.2.49	logdet	48

6.1.2.50	logm	48
6.1.2.51	mket	49
6.1.2.52	mket	49
6.1.2.53	mket	50
6.1.2.54	mprj	50
6.1.2.55	mprj	51
6.1.2.56	mprj	51
6.1.2.57	multiidx2n	52
6.1.2.58	n2multiidx	52
6.1.2.59	norm	53
6.1.2.60	omega	53
6.1.2.61	operator""_i	54
6.1.2.62	operator""_i	54
6.1.2.63	powm	54
6.1.2.64	prj	55
6.1.2.65	prod	55
6.1.2.66	prod	56
6.1.2.67	ptrace	56
6.1.2.68	ptrace1	57
6.1.2.69	ptrace2	58
6.1.2.70	ptranspose	59
6.1.2.71	qmutualinfo	60
6.1.2.72	rand	61
6.1.2.73	rand	61
6.1.2.74	rand	62
6.1.2.75	rand	62
6.1.2.76	randH	63
6.1.2.77	randint	63
6.1.2.78	randket	64
6.1.2.79	randkraus	64
6.1.2.80	randn	65
6.1.2.81	randn	65
6.1.2.82	randn	66
6.1.2.83	randn	66
6.1.2.84	randperm	67
6.1.2.85	randrho	67
6.1.2.86	randU	68
6.1.2.87	randV	68
6.1.2.88	renyi	68
6.1.2.89	renyi_inf	69

6.1.2.90	reshape	70
6.1.2.91	save	70
6.1.2.92	saveMATLABmatrix	70
6.1.2.93	saveMATLABmatrix	70
6.1.2.94	saveMATLABmatrix	71
6.1.2.95	schmidtcoeff	71
6.1.2.96	schmidtprob	72
6.1.2.97	schmidtU	73
6.1.2.98	schmidtV	74
6.1.2.99	shannon	75
6.1.2.100	sinm	76
6.1.2.101	spectralpowm	77
6.1.2.102	sqrtm	77
6.1.2.103	sum	78
6.1.2.104	sum	78
6.1.2.105	super	79
6.1.2.106	syspermute	79
6.1.2.107	trace	80
6.1.2.108	transpose	81
6.1.2.109	tsallis	81
6.1.3	Variable Documentation	82
6.1.3.1	chop	82
6.1.3.2	ee	82
6.1.3.3	eps	82
6.1.3.4	gt	82
6.1.3.5	init	82
6.1.3.6	maxn	83
6.1.3.7	pi	83
6.1.3.8	rdevs	83
6.1.3.9	st	83
6.2	qpp::internal Namespace Reference	83
6.2.1	Detailed Description	84
6.2.2	Function Documentation	84
6.2.2.1	_check_col_vector	84
6.2.2.2	_check_dims	84
6.2.2.3	_check_dims_match_cvect	84
6.2.2.4	_check_dims_match_mat	84
6.2.2.5	_check_dims_match_rvect	84
6.2.2.6	_check_eq_dims	84
6.2.2.7	_check_nonzero_size	84

6.2.2.8	<a href="#">_check_perm</a>	84
6.2.2.9	<a href="#">_check_row_vector</a>	84
6.2.2.10	<a href="#">_check_square_mat</a>	84
6.2.2.11	<a href="#">_check_subsys_match_dims</a>	84
6.2.2.12	<a href="#">_check_vector</a>	84
6.2.2.13	<a href="#">_kron2</a>	85
6.2.2.14	<a href="#">_multiidx2n</a>	85
6.2.2.15	<a href="#">_n2multiidx</a>	85
6.2.2.16	<a href="#">variadic_vector_emplace</a>	85
6.2.2.17	<a href="#">variadic_vector_emplace</a>	85
6.3	<a href="#">qpp::obsolete Namespace Reference</a>	85
6.3.1	<a href="#">Function Documentation</a>	86
6.3.1.1	<a href="#">apply</a>	86
6.3.1.2	<a href="#">channel</a>	87
6.3.1.3	<a href="#">super</a>	88
<b>7</b>	<b><a href="#">Class Documentation</a></b>	<b>91</b>
7.1	<a href="#">qpp::Exception Class Reference</a>	91
7.1.1	<a href="#">Detailed Description</a>	92
7.1.2	<a href="#">Member Enumeration Documentation</a>	92
7.1.2.1	<a href="#">Type</a>	92
7.1.3	<a href="#">Constructor &amp; Destructor Documentation</a>	93
7.1.3.1	<a href="#">Exception</a>	93
7.1.3.2	<a href="#">Exception</a>	94
7.1.4	<a href="#">Member Function Documentation</a>	94
7.1.4.1	<a href="#">_construct_exception_msg</a>	94
7.1.4.2	<a href="#">what</a>	94
7.1.5	<a href="#">Member Data Documentation</a>	95
7.1.5.1	<a href="#">_custom</a>	95
7.1.5.2	<a href="#">_msg</a>	95
7.1.5.3	<a href="#">_type</a>	95
7.1.5.4	<a href="#">_where</a>	95
7.2	<a href="#">qpp::Gates Class Reference</a>	95
7.2.1	<a href="#">Detailed Description</a>	97
7.2.2	<a href="#">Constructor &amp; Destructor Documentation</a>	97
7.2.2.1	<a href="#">Gates</a>	97
7.2.3	<a href="#">Member Function Documentation</a>	97
7.2.3.1	<a href="#">CTRL</a>	97
7.2.3.2	<a href="#">Fd</a>	98
7.2.3.3	<a href="#">Id</a>	99

7.2.3.4	Rn	99
7.2.3.5	Xd	99
7.2.3.6	Zd	100
7.2.4	Friends And Related Function Documentation	100
7.2.4.1	internal::Singleton< const Gates >	100
7.2.5	Member Data Documentation	100
7.2.5.1	CNOTab	100
7.2.5.2	CNOTba	100
7.2.5.3	CZ	100
7.2.5.4	FRED	100
7.2.5.5	H	100
7.2.5.6	Id2	101
7.2.5.7	S	101
7.2.5.8	SWAP	101
7.2.5.9	T	101
7.2.5.10	TOF	101
7.2.5.11	X	101
7.2.5.12	Y	101
7.2.5.13	Z	101
7.3	qpp::Init Class Reference	101
7.3.1	Detailed Description	102
7.3.2	Constructor & Destructor Documentation	103
7.3.2.1	Init	103
7.3.2.2	~Init	103
7.3.3	Friends And Related Function Documentation	103
7.3.3.1	internal::Singleton< const Init >	103
7.4	qpp::Qudit Class Reference	103
7.4.1	Constructor & Destructor Documentation	103
7.4.1.1	Qudit	104
7.4.2	Member Function Documentation	104
7.4.2.1	getD	104
7.4.2.2	getRho	104
7.4.2.3	measure	104
7.4.2.4	measure	105
7.4.3	Member Data Documentation	105
7.4.3.1	_D	105
7.4.3.2	_rho	105
7.5	qpp::RandomDevices Class Reference	105
7.5.1	Detailed Description	106
7.5.2	Constructor & Destructor Documentation	106



7.5.2.1	RandomDevices	106
7.5.3	Friends And Related Function Documentation	107
7.5.3.1	internal::Singleton< RandomDevices >	107
7.5.4	Member Data Documentation	107
7.5.4.1	_rd	107
7.5.4.2	_rng	107
7.6	qpp::internal::Singleton< T > Class Template Reference	107
7.6.1	Detailed Description	108
7.6.2	Constructor & Destructor Documentation	108
7.6.2.1	Singleton	108
7.6.2.2	~Singleton	108
7.6.2.3	Singleton	108
7.6.3	Member Function Documentation	108
7.6.3.1	get_instance	108
7.6.3.2	operator=	108
7.7	qpp::States Class Reference	108
7.7.1	Detailed Description	110
7.7.2	Constructor & Destructor Documentation	110
7.7.2.1	States	110
7.7.3	Friends And Related Function Documentation	111
7.7.3.1	internal::Singleton< const States >	111
7.7.4	Member Data Documentation	111
7.7.4.1	b00	111
7.7.4.2	b01	111
7.7.4.3	b10	111
7.7.4.4	b11	111
7.7.4.5	GHZ	111
7.7.4.6	pb00	111
7.7.4.7	pb01	111
7.7.4.8	pb10	111
7.7.4.9	pb11	111
7.7.4.10	pGHZ	111
7.7.4.11	pW	111
7.7.4.12	px0	112
7.7.4.13	px1	112
7.7.4.14	py0	112
7.7.4.15	py1	112
7.7.4.16	pz0	112
7.7.4.17	pz1	112
7.7.4.18	W	112

7.7.4.19	x0	112
7.7.4.20	x1	112
7.7.4.21	y0	112
7.7.4.22	y1	112
7.7.4.23	z0	112
7.7.4.24	z1	113
7.8	qpp::Timer Class Reference	113
7.8.1	Detailed Description	113
7.8.2	Constructor & Destructor Documentation	113
7.8.2.1	Timer	113
7.8.3	Member Function Documentation	114
7.8.3.1	seconds	114
7.8.3.2	tic	114
7.8.3.3	toc	114
7.8.4	Friends And Related Function Documentation	114
7.8.4.1	operator<<	114
7.8.5	Member Data Documentation	114
7.8.5.1	_end	114
7.8.5.2	_start	114
<b>8</b>	<b>File Documentation</b>	<b>115</b>
8.1	include/classes/exception.h File Reference	115
8.2	include/classes/gates.h File Reference	116
8.3	include/classes/init.h File Reference	116
8.4	include/classes/qudit.h File Reference	117
8.5	include/classes/randevs.h File Reference	117
8.6	include/classes/singleton.h File Reference	118
8.7	include/classes/states.h File Reference	119
8.8	include/classes/timer.h File Reference	119
8.9	include/constants.h File Reference	120
8.10	include/entanglement.h File Reference	121
8.11	include/entropies.h File Reference	122
8.12	include/functions.h File Reference	123
8.13	include/internal.h File Reference	126
8.14	include/io.h File Reference	128
8.15	include/matlab.h File Reference	129
8.16	include/obsolete.h File Reference	130
8.17	include/operations.h File Reference	131
8.18	include/qpp.h File Reference	133
8.19	include/random.h File Reference	134

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8.20 <a href="#">include/types.h File Reference</a> . . . . .	135
<a href="#">Index</a>	137



## Chapter 1

# quantum++ - A C++11 quantum computing library

Version

0.1

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This is the main page of the documentation. More coming soon.



## Chapter 2

# Namespace Index

### 2.1 Namespace List

Here is a list of all namespaces with brief descriptions:

<a href="#">qpp</a>	11
<a href="#">qpp::internal</a>	83
<a href="#">qpp::obsolete</a>	85





## Chapter 3

# Hierarchical Index

### 3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

exception	
qpp::Exception . . . . .	91
qpp::Qudit . . . . .	103
qpp::internal::Singleton< T > . . . . .	107
qpp::Init . . . . .	101
qpp::States . . . . .	108
qpp::internal::Singleton< const Gates > . . . . .	107
qpp::Gates . . . . .	95
qpp::internal::Singleton< const Init > . . . . .	107
qpp::internal::Singleton< const States > . . . . .	107
qpp::internal::Singleton< RandomDevices > . . . . .	107
qpp::RandomDevices . . . . .	105
qpp::Timer . . . . .	113



## Chapter 4

# Class Index

### 4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

<a href="#">qpp::Exception</a>	Generates custom exceptions, used when validating function parameters . . . . .	91
<a href="#">qpp::Gates</a>	Const Singleton class that implements most commonly used gates . . . . .	95
<a href="#">qpp::Init</a>	Const Singleton class that performs additional initializations/cleanups . . . . .	101
<a href="#">qpp::Qudit</a>	. . . . .	103
<a href="#">qpp::RandomDevices</a>	Singleton class that manages the source of randomness in the library . . . . .	105
<a href="#">qpp::internal::Singleton&lt; T &gt;</a>	<a href="#">Singleton</a> policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern) . . . . .	107
<a href="#">qpp::States</a>	Const Singleton class that implements most commonly used states . . . . .	108
<a href="#">qpp::Timer</a>	Measures time . . . . .	113



## Chapter 5

# File Index

### 5.1 File List

Here is a list of all files with brief descriptions:

include/	constants.h	120
include/	entanglement.h	121
include/	entropies.h	122
include/	functions.h	123
include/	internal.h	126
include/	io.h	128
include/	matlab.h	129
include/	obsolete.h	130
include/	operations.h	131
include/	qpp.h	133
include/	random.h	134
include/	types.h	135
include/classes/	exception.h	115
include/classes/	gates.h	116
include/classes/	init.h	116
include/classes/	qudit.h	117
include/classes/	randevs.h	117
include/classes/	singleton.h	118
include/classes/	states.h	119
include/classes/	timer.h	119



## Chapter 6

# Namespace Documentation

### 6.1 qpp Namespace Reference

#### Namespaces

- [internal](#)
- [obsolete](#)

#### Classes

- class [Exception](#)  
*Generates custom exceptions, used when validating function parameters.*
- class [Gates](#)  
*const Singleton class that implements most commonly used gates*
- class [Init](#)  
*const Singleton class that performs additional initializations/cleanups*
- class [Qudit](#)
- class [RandomDevices](#)  
*Singleton class that manages the source of randomness in the library.*
- class [States](#)  
*const Singleton class that implements most commonly used states*
- class [Timer](#)  
*Measures time.*

#### Typedefs

- using [cplx](#) = std::complex< double >  
*Complex number in double precision.*
- using [cmat](#) = Eigen::MatrixXcd  
*Complex (double precision) dynamic Eigen matrix.*
- using [dmat](#) = Eigen::MatrixXd  
*Real (double precision) dynamic Eigen matrix.*
- using [ket](#) = Eigen::Matrix< [cplx](#), Eigen::Dynamic, 1 >  
*Complex (double precision) dynamic Eigen column matrix.*
- using [bra](#) = Eigen::Matrix< [cplx](#), 1, Eigen::Dynamic >  
*Complex (double precision) dynamic Eigen row matrix.*
- template<typename Scalar >  
using [DynMat](#) = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >  
*Dynamic Eigen matrix over the field specified by Scalar.*

## Functions

- `constexpr std::complex< double > operator""_i` (unsigned long long int x)  
*User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)*
- `constexpr std::complex< double > operator""_i` (long double x)  
*User-defined literal for complex  $i = \sqrt{-1}$  (real overload)*
- `std::complex< double > omega` (std::size\_t D)  
*D-th root of unity.*
- `template<typename Derived >`  
`cmat schmidtcoeff` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)  
*Schmidt coefficients of the bi-partite pure state A.*
- `template<typename Derived >`  
`cmat schmidtU` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)  
*Schmidt basis on Alice's side.*
- `template<typename Derived >`  
`cmat schmidtV` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)  
*Schmidt basis on Bob's side.*
- `template<typename Derived >`  
`cmat schmidtprob` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)  
*Schmidt probabilities of the bi-partite pure state A.*
- `template<typename Derived >`  
`double entanglement` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)  
*Entanglement of the bi-partite pure state A.*
- `template<typename Derived >`  
`double gconcurrence` (const Eigen::MatrixBase< Derived > &A)  
*G-concurrence of the bi-partite pure state A.*
- `template<typename Derived >`  
`double shannon` (const Eigen::MatrixBase< Derived > &A)  
*Shannon/von-Neumann entropy of the probability distribution/density matrix A.*
- `template<typename Derived >`  
`double renyi` (const double alpha, const Eigen::MatrixBase< Derived > &A)  
*Renyi-  $\alpha$  entropy of the probability distribution/density matrix A, for  $\alpha \geq 0$ .*
- `template<typename Derived >`  
`double renyi_inf` (const Eigen::MatrixBase< Derived > &A)  
*Renyi-  $\infty$  entropy (min entropy) of the probability distribution/density matrix A.*
- `template<typename Derived >`  
`double tsallis` (const double alpha, const Eigen::MatrixBase< Derived > &A)  
*Tsallis-  $\alpha$  entropy of the probability distribution/density matrix A, for  $\alpha \geq 0$*
- `template<typename Derived >`  
`double qmutualinfo` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &subsysA, const std::vector< std::size\_t > &subsysB, const std::vector< std::size\_t > &dims)  
*Quantum mutual information between 2 subsystems of a composite system.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > transpose` (const Eigen::MatrixBase< Derived > &A)  
*Transpose.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > conjugate` (const Eigen::MatrixBase< Derived > &A)  
*Complex conjugate.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > adjoint` (const Eigen::MatrixBase< Derived > &A)  
*Adjoint.*



- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > inverse (const Eigen::MatrixBase< Derived > &A)`  
*Inverse.*
- `template<typename Derived >`  
`Derived::Scalar trace (const Eigen::MatrixBase< Derived > &A)`  
*Trace.*
- `template<typename Derived >`  
`Derived::Scalar det (const Eigen::MatrixBase< Derived > &A)`  
*Determinant.*
- `template<typename Derived >`  
`Derived::Scalar logdet (const Eigen::MatrixBase< Derived > &A)`  
*Logarithm of the determinant.*
- `template<typename Derived >`  
`Derived::Scalar sum (const Eigen::MatrixBase< Derived > &A)`  
*Element-wise sum of A.*
- `template<typename Derived >`  
`Derived::Scalar prod (const Eigen::MatrixBase< Derived > &A)`  
*Element-wise product of A.*
- `template<typename Derived >`  
`double norm (const Eigen::MatrixBase< Derived > &A)`  
*Trace norm.*
- `template<typename Derived >`  
`cmat evals (const Eigen::MatrixBase< Derived > &A)`  
*Eigenvalues.*
- `template<typename Derived >`  
`cmat evecs (const Eigen::MatrixBase< Derived > &A)`  
*Eigenvectors.*
- `template<typename Derived >`  
`dmat hevals (const Eigen::MatrixBase< Derived > &A)`  
*Hermitian eigenvalues.*
- `template<typename Derived >`  
`cmat hevecs (const Eigen::MatrixBase< Derived > &A)`  
*Hermitian eigenvectors.*
- `template<typename Derived >`  
`cmat funm (const Eigen::MatrixBase< Derived > &A, cplx(*f)(const cplx &))`  
*Functional calculus  $f(A)$*
- `template<typename Derived >`  
`cmat sqrtm (const Eigen::MatrixBase< Derived > &A)`  
*Matrix square root.*
- `template<typename Derived >`  
`cmat absm (const Eigen::MatrixBase< Derived > &A)`  
*Matrix absolut value.*
- `template<typename Derived >`  
`cmat expm (const Eigen::MatrixBase< Derived > &A)`  
*Matrix exponential.*
- `template<typename Derived >`  
`cmat logm (const Eigen::MatrixBase< Derived > &A)`  
*Matrix logarithm.*
- `template<typename Derived >`  
`cmat sinm (const Eigen::MatrixBase< Derived > &A)`  
*Matrix sin.*
- `template<typename Derived >`  
`cmat cosm (const Eigen::MatrixBase< Derived > &A)`

*Matrix cos.*

- template<typename Derived >  
[cmat spectralpowm](#) (const Eigen::MatrixBase< Derived > &A, const [cplx](#) z)

*Matrix power.*

- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [powm](#) (const Eigen::MatrixBase< Derived > &A, std::size\_t n)

*Matrix power.*

- template<typename OutputScalar , typename Derived >  
[DynMat](#)< OutputScalar > [cwise](#) (const Eigen::MatrixBase< Derived > &A, OutputScalar(\*f)(const typename Derived::Scalar &))

*Functor.*

- template<typename T >  
[DynMat](#)< typename T::Scalar > [kron](#) (const T &head)

*Kronecker product (variadic overload)*

- template<typename T , typename... Args>  
[DynMat](#)< typename T::Scalar > [kron](#) (const T &head, const Args &...tail)

*Kronecker product (variadic overload)*

- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [kron](#) (const std::vector< Derived > &As)

*Kronecker product (std::vector overload)*

- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [kron](#) (const std::initializer\_list< Derived > &As)

*Kronecker product (std::initializer\_list overload)*

- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [kronpow](#) (const Eigen::MatrixBase< Derived > &A, std::size\_t n)

*Kronecker power.*

- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [reshape](#) (const Eigen::MatrixBase< Derived > &A, std::size\_t rows, std::size\_t cols)

*Reshape.*

- template<typename Derived1 , typename Derived2 >  
[DynMat](#)< typename Derived1::Scalar > [comm](#) (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)

*Commutator.*

- template<typename Derived1 , typename Derived2 >  
[DynMat](#)< typename Derived1::Scalar > [anticomm](#) (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)

*Anti-commutator.*

- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [prj](#) (const Eigen::MatrixBase< Derived > &V)

*Projector.*

- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [expandout](#) (const Eigen::MatrixBase< Derived > &A, std::size\_t pos, const std::vector< std::size\_t > &dims)

*Expand out.*

- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [grams](#) (const std::vector< Derived > &Vs)

*Gram-Schmidt orthogonalization (std::vector overload)*

- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [grams](#) (const std::initializer\_list< Derived > &Vs)

*Gram-Schmidt orthogonalization (std::initializer\_list overload)*

- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [grams](#) (const Eigen::MatrixBase< Derived > &A)

- Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)*

  - `std::vector< std::size_t > n2multiidx` (`std::size_t n`, `const std::vector< std::size_t > &dims`)

*Non-negative integer index to multi-index.*
- `std::size_t multiidx2n` (`const std::vector< std::size_t > &midx`, `const std::vector< std::size_t > &dims`)

*Multi-index to non-negative integer index.*
- `ket mket` (`const std::vector< std::size_t > &mask`)

*Multi-partite qubit ket.*
- `ket mket` (`const std::vector< std::size_t > &mask`, `const std::vector< std::size_t > &dims`)

*Multi-partite qudit ket (different dimensions overload)*
- `ket mket` (`const std::vector< std::size_t > &mask`, `std::size_t d`)

*Multi-partite qudit ket (same dimensions overload)*
- `cmat mprj` (`const std::vector< std::size_t > &mask`)

*Projector onto multi-partite qubit ket.*
- `cmat mprj` (`const std::vector< std::size_t > &mask`, `const std::vector< std::size_t > &dims`)

*Projector onto multi-partite qudit ket (different dimensions overload)*
- `cmat mprj` (`const std::vector< std::size_t > &mask`, `std::size_t d`)

*Projector onto multi-partite qudit ket (same dimensions overload)*
- `std::vector< std::size_t > invperm` (`const std::vector< std::size_t > &perm`)

*Inverse permutation.*
- `std::vector< std::size_t > compperm` (`const std::vector< std::size_t > &perm`, `const std::vector< std::size_t > &sigma`)

*Compose permutations.*
- `template<typename InputIterator >`  
`std::vector< double > amplitudes` (`InputIterator first`, `InputIterator last`)

*Computes the absolut values squared of a range of complex numbers.*
- `template<typename Derived >`  
`std::vector< double > amplitudes` (`const Eigen::MatrixBase< Derived > &V`)

*Computes the absolut values squared of a column vector.*
- `template<typename InputIterator >`  
`auto sum` (`InputIterator first`, `InputIterator last`) -> `typename InputIterator::value_type`

*Element-wise sum of a range.*
- `template<typename InputIterator >`  
`auto prod` (`InputIterator first`, `InputIterator last`) -> `typename InputIterator::value_type`

*Element-wise product of a range.*
- `template<typename T >`  
`void disp` (`const T &x`, `const std::string &separator`, `const std::string &start="[`, `const std::string &end="]"`, `std::ostream &os=std::cout`)

*Displays a standard container that supports std::begin, std::end and forward iteration. Does not add a newline.*
- `template<typename T >`  
`void displn` (`const T &x`, `const std::string &separator`, `const std::string &start="[`, `const std::string &end="]"`, `std::ostream &os=std::cout`)

*Displays a standard container that supports std::begin, std::end and forward iteration. Adds a newline.*
- `template<typename T >`  
`void disp` (`const T *x`, `const std::size_t n`, `const std::string &separator`, `const std::string &start="[`, `const std::string &end="]"`, `std::ostream &os=std::cout`)

*Displays a C-style array. Does not add a newline.*
- `template<typename T >`  
`void displn` (`const T *x`, `const std::size_t n`, `const std::string &separator`, `const std::string &start="[`, `const std::string &end="]"`, `std::ostream &os=std::cout`)

*Displays a C-style array. Adds a newline.*
- `template<typename Derived >`  
`void disp` (`const Eigen::MatrixBase< Derived > &A`, `double chop=qpp::chop`, `std::ostream &os=std::cout`)

- Displays an Eigen expression in matrix friendly form. Does not add a new line.*

  - `template<typename Derived >`  
`void displn (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop, std::ostream &os=std::cout)`  
*Displays an Eigen expression in matrix friendly form. Adds a newline.*
  - `void disp (const cplx z, double chop=qpp::chop, std::ostream &os=std::cout)`  
*Displays a number (implicitly converted to `std::complex<double>`) in friendly form. Does not add a new line.*
  - `void displn (const cplx z, double chop=qpp::chop, std::ostream &os=std::cout)`  
*Displays a number (implicitly converted to `std::complex<double>`) in friendly form. Adds a new line.*
  - `template<typename Derived >`  
`void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)`  
*Saves Eigen expression to a binary file (internal format) in double precision.*
  - `template<typename Derived >`  
`DynMat< typename Derived::Scalar > load (const std::string &fname)`  
*Loads Eigen matrix from a binary file (internal format) in double precision.*
  - `template<typename Derived >`  
`Derived loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`  
*Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.*
  - `template<>`  
`dmat loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`  
*Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))*
  - `template<>`  
`cmat loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`  
*Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))*
  - `template<typename Derived >`  
`void saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`  
*Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.*
  - `template<>`  
`void saveMATLABmatrix (const Eigen::MatrixBase< dmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`  
*Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))*
  - `template<>`  
`void saveMATLABmatrix (const Eigen::MatrixBase< cmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`  
*Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))*
  - `template<typename Derived1 , typename Derived2 >`  
`DynMat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size_t > &ctrl, const std::vector< std::size_t > &subsys, std::size_t n, std::size_t d=2)`  
*Applies the controlled-gate A to the part subsys of a multipartite state vector or density matrix.*
  - `template<typename Derived1 , typename Derived2 >`  
`DynMat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size_t > &subsys, std::size_t n, std::size_t d=2)`  
*Applies the gate A to the part subsys of a multipartite state vector or density matrix.*
  - `template<typename Derived >`  
`cmat channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks)`  
*Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.*
  - `template<typename Derived >`  
`cmat channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< std::size_t > &subsys, std::size_t n, std::size_t d=2)`  
*Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.*
  - `cmat super (const std::vector< cmat > &Ks)`

- Superoperator matrix representation.*

  - `cmat choi` (const std::vector< `cmat` > &Ks)
- Choi matrix representation.*

  - std::vector< `cmat` > `choi2kraus` (const `cmat` &A)
- Extracts orthogonal Kraus operators from Choi matrix.*

  - template<typename Derived >  
`DynMat`< typename Derived::Scalar > `ptrace1` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- Partial trace.*

  - template<typename Derived >  
`DynMat`< typename Derived::Scalar > `ptrace2` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- Partial trace.*

  - template<typename Derived >  
`DynMat`< typename Derived::Scalar > `ptrace` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- Partial trace.*

  - template<typename Derived >  
`DynMat`< typename Derived::Scalar > `ptranspose` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- Partial transpose.*

  - template<typename Derived >  
`DynMat`< typename Derived::Scalar > `syspermute` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &perm, const std::vector< std::size\_t > &dims)
- System permutation.*

  - template<typename Derived >  
Derived `rand` (std::size\_t rows, std::size\_t cols, double a=0, double b=1)
- Generates a random matrix with entries uniformly distributed in the interval [a, b)*

  - template<>  
`dmat rand` (std::size\_t rows, std::size\_t cols, double a, double b)
- Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices ([qpp::dmat](#))*

  - template<>  
`cmat rand` (std::size\_t rows, std::size\_t cols, double a, double b)
- Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices ([qpp::cmat](#))*

  - double `rand` (double a=0, double b=1)
- Generates a random real number uniformly distributed in the interval [a, b)*

  - int `randint` (int a=std::numeric\_limits< int >::min(), int b=std::numeric\_limits< int >::max())
- Generates a random integer (int) uniformly distributed in the interval [a, b].*

  - template<typename Derived >  
Derived `randn` (std::size\_t rows, std::size\_t cols, double mean=0, double sigma=1)
- Generates a random matrix with entries normally distributed in N(mean, sigma)*

  - template<>  
`dmat randn` (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices ([qpp::dmat](#))*

  - template<>  
`cmat randn` (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices ([qpp::cmat](#))*

  - double `randn` (double mean=0, double sigma=1)
- Generates a random real number (double) normally distributed in N(mean, sigma)*

  - `cmat randU` (std::size\_t D)

- Generates a random unitary matrix.*

  - `cmat randV` (`std::size_t Din`, `std::size_t Dout`)

*Generates a random isometry matrix.*

  - `std::vector< cmat > randkraus` (`std::size_t n`, `std::size_t D`)

*Generates a set of random Kraus operators.*

  - `cmat randH` (`std::size_t D`)

*Generates a random Hermitian matrix.*

  - `ket randket` (`std::size_t D`)

*Generates a random normalized ket (pure state vector)*

  - `cmat randrho` (`std::size_t D`)

*Generates a random density matrix.*

  - `std::vector< std::size_t > randperm` (`std::size_t n`)

*Generates a random uniformly distributed permutation.*

## Variables

- `constexpr double chop` = 1e-10  
*Used in `qpp::disp()` and `qpp::displn()` for setting to zero numbers that have their absolute value smaller than `qpp::ct←→::chop`.*
- `constexpr double eps` = 1e-12  
*Used to decide whether a number or expression in double precision is zero or not.*
- `constexpr std::size_t maxn` = 64  
*Maximum number of qubits.*
- `constexpr double pi` = 3.141592653589793238462643383279502884  
 $\pi$
- `constexpr double ee` = 2.718281828459045235360287471352662497  
*Base of natural logarithm,  $e$ .*
- `RandomDevices & rdevs` = `RandomDevices::get_instance()`  
*`qpp::RandomDevices` Singleton*
- `const Gates & gt` = `Gates::get_instance()`  
*`qpp::Gates` const Singleton*
- `const States & st` = `States::get_instance()`  
*`qpp::States` const Singleton*
- `const Init & init` = `Init::get_instance()`  
*`qpp::Init` const Singleton*

## 6.1.1 Typedef Documentation

### 6.1.1.1 `using qpp::bra = typedef Eigen::Matrix<cplx, 1, Eigen::Dynamic>`

Complex (double precision) dynamic Eigen row matrix.

### 6.1.1.2 `using qpp::cmat = typedef Eigen::MatrixXcd`

Complex (double precision) dynamic Eigen matrix.

### 6.1.1.3 `using qpp::cplx = typedef std::complex<double>`

Complex number in double precision.

#### 6.1.1.4 using qpp::dmat = typedef Eigen::MatrixXd

Real (double precision) dynamic Eigen matrix.

#### 6.1.1.5 template<typename Scalar > using qpp::DynMat = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>

Dynamic Eigen matrix over the field specified by *Scalar*.

Example:

```
auto mat = DynMat<float>(2,3); // type of mat is Eigen::Matrix<float, Eigen::Dynamic, Eigen::Dynamic>
```

#### 6.1.1.6 using qpp::ket = typedef Eigen::Matrix<cplx, Eigen::Dynamic, 1>

Complex (double precision) dynamic Eigen column matrix.

### 6.1.2 Function Documentation

#### 6.1.2.1 template<typename Derived > cmat qpp::absm ( const Eigen::MatrixBase< Derived > & A )

Matrix absolut value.

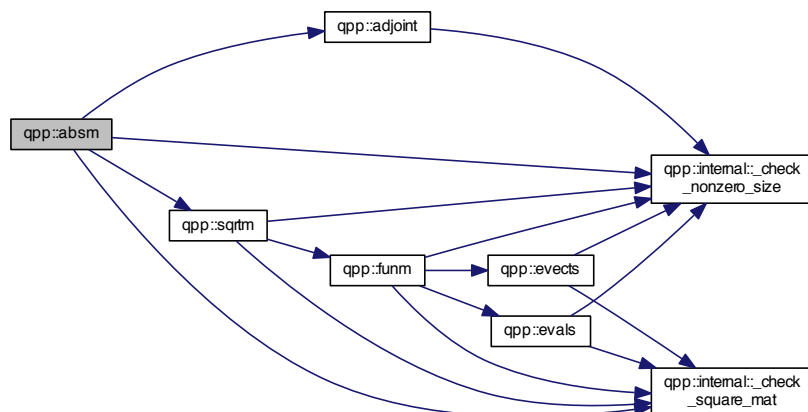
Parameters

A	Eigen expression
---	------------------

Returns

Matrix absolut value of A

Here is the call graph for this function:



#### 6.1.2.2 template<typename Derived > DynMat<typename Derived::Scalar> qpp::adjoint ( const Eigen::MatrixBase< Derived > & A )

Adjoint.

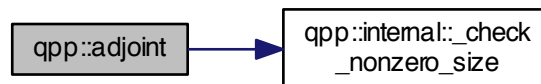
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Adjoint (Hermitian conjugate) of  $A$ , as a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:



6.1.2.3 `template<typename InputIterator > std::vector<double> qpp::amplitudes ( InputIterator first, InputIterator last )`

Computes the absolut values squared of a range of complex numbers.

## Parameters

<i>first</i>	Iterator to the first element of the range
<i>last</i>	Iterator to the last element of the range

## Returns

Real vector consisting of the range's absolut values squared

6.1.2.4 `template<typename Derived > std::vector<double> qpp::amplitudes ( const Eigen::MatrixBase< Derived > &  $V$  )`

Computes the absolut values squared of a column vector.

## Parameters

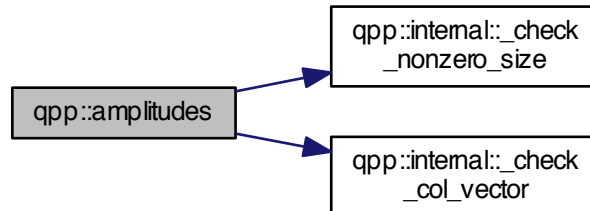
$V$	Eigen expression
-----	------------------



**Returns**

Real vector consisting of the absolut values squared

Here is the call graph for this function:



**6.1.2.5** `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::anticomm ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )`

Anti-commutator.

Anti-commutator  $\{A, B\} = AB + BA$

Both  $A$  and  $B$  must be Eigen expressions over the same scalar field

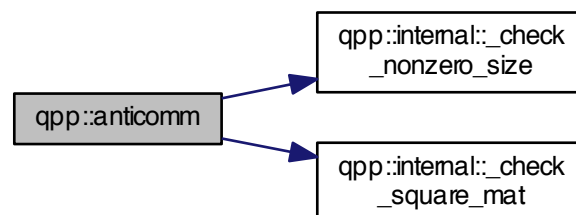
**Parameters**

$A$	Eigen expression
$B$	Eigen expression

**Returns**

Anti-commutator  $AB + BA$ , as a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:



6.1.2.6 `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::apply ( const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector< std::size_t > & subsys, std::size_t n, std::size_t d = 2 )`

Applies the gate *A* to the part *subsys* of a multipartite state vector or density matrix.

#### Note

The dimension of the gate *A* must match the dimension of *subsys*

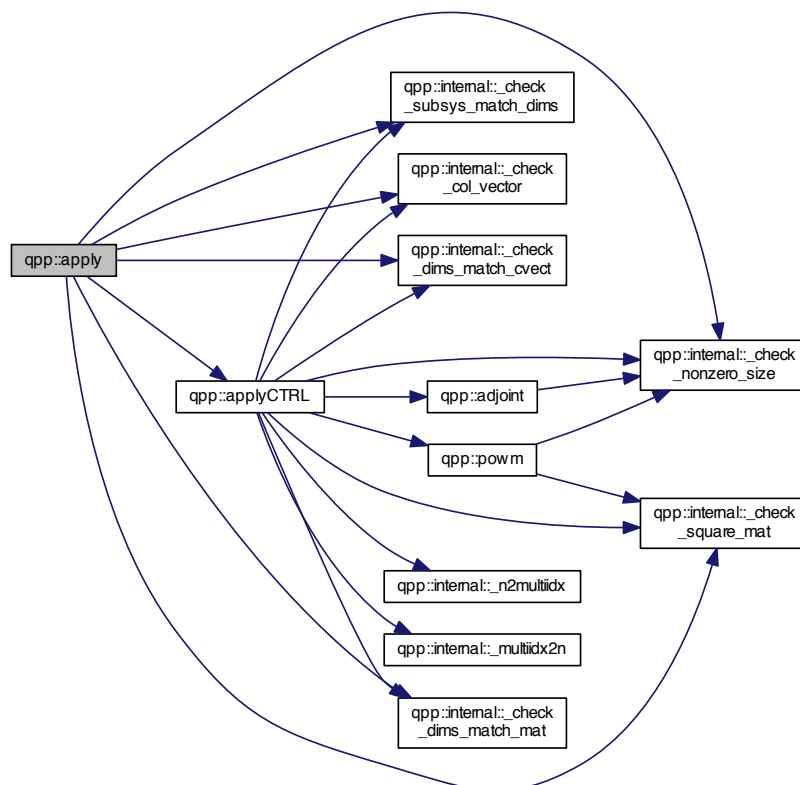
#### Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>n</i>	Total number of subsystems
<i>d</i>	Local dimensions of all local Hilbert spaces (must all be equal)

#### Returns

Gate *A* applied to the part *subsys* of *state*

Here is the call graph for this function:



6.1.2.7 `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::applyCTRL ( const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector< std::size_t > & ctrl, const std::vector< std::size_t > & subsys, std::size_t n, std::size_t d = 2 )`

Applies the controlled-gate  $A$  to the part *subsys* of a multipartite state vector or density matrix.

#### Note

The dimension of the gate  $A$  must match the dimension of *subsys*

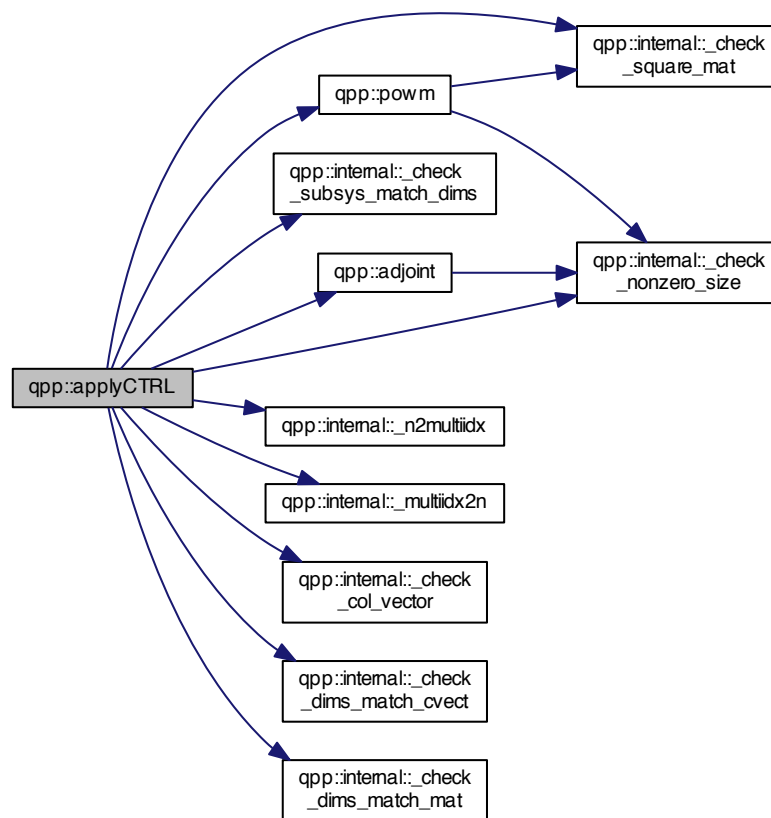
#### Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>ctrl</i>	Control subsystem indexes
<i>subsys</i>	Subsystem indexes where the gate $A$ is applied
<i>n</i>	Total number of subsystems
<i>d</i>	Local dimensions of all local Hilbert spaces (must all be equal)

#### Returns

CTRL- $A$  gate applied to the part *subsys* of *state*

Here is the call graph for this function:



6.1.2.8 `template<typename Derived > cmat qpp::channel ( const Eigen::MatrixBase< Derived > & rho, const std::vector< cmat > & Ks )`

Applies the channel specified by the set of Kraus operators *Ks* to the density matrix *rho*.

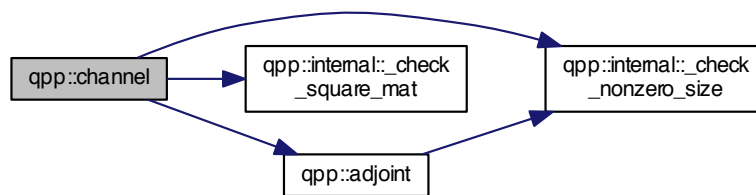
## Parameters

<i>rho</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators

## Returns

Output density matrix after the action of the channel

Here is the call graph for this function:



**6.1.2.9** `template<typename Derived> cmat qpp::channel ( const Eigen::MatrixBase< Derived> & rho, const std::vector< cmat> & Ks, const std::vector< std::size_t> & subsys, std::size_t n, std::size_t d = 2 )`

Applies the channel specified by the set of Kraus operators *Ks* to the part of the density matrix *rho* specified by *subsys*.

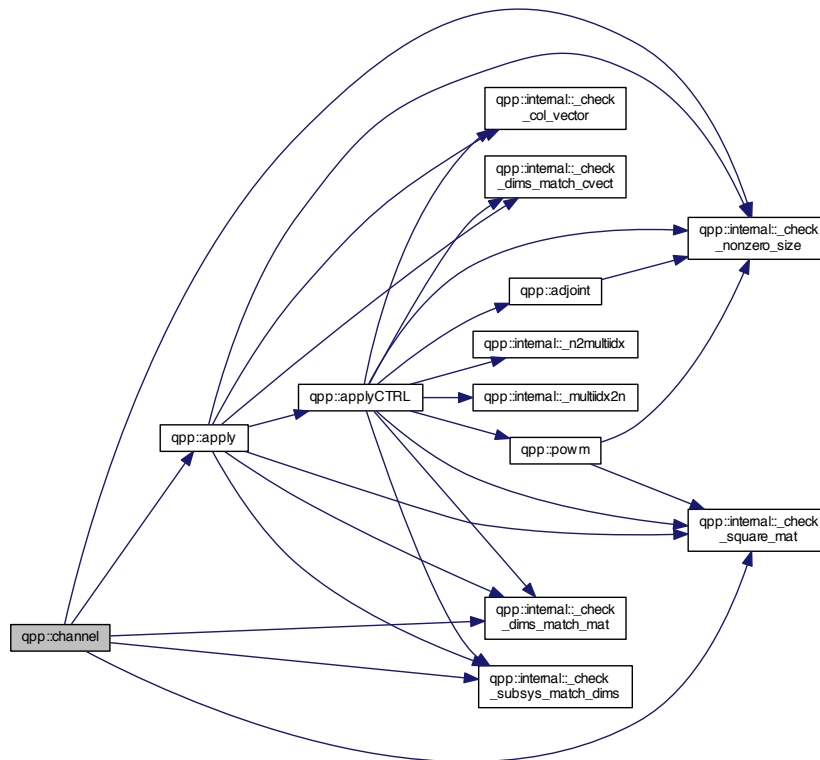
## Parameters

<i>rho</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystems' indexes
<i>n</i>	Total number of subsystems
<i>d</i>	Local dimensions of all local Hilbert spaces (must all be equal)

**Returns**

Output density matrix after the action of the channel

Here is the call graph for this function:



### 6.1.2.10 `cmat qpp::choi ( const std::vector< cmat > & Ks )`

Choi matrix representation.

Constructs the Choi matrix of the channel specified by the set of Kraus operators  $K_s$  in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

**Note**

The superoperator matrix  $S$  and the Choi matrix  $C$  are related by  $S_{ab,mn} = C_{ma,nb}$

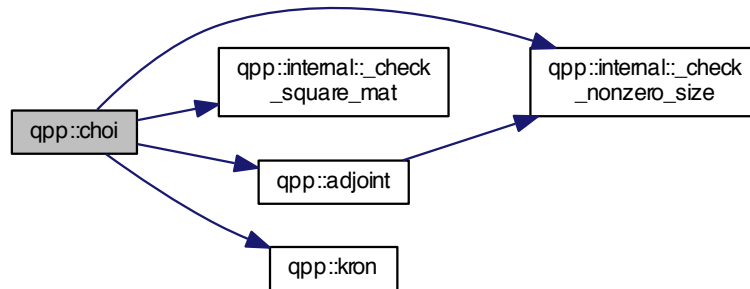
**Parameters**

$K_s$	Set of Kraus operators
-------	------------------------

## Returns

Choi matrix representation

Here is the call graph for this function:



#### 6.1.2.11 `std::vector<cmat> qpp::choi2kraus ( const cmat & A )`

Extracts orthogonal Kraus operators from Choi matrix.

Extracts a set of orthogonal (under Hilbert-Schmidt operator norm) Kraus operators from the Choi representation  $A$  of the channel

## Note

The Kraus operators satisfy  $Tr(K_i^\dagger K_j) = \delta_{ij}$  for all  $i \neq j$

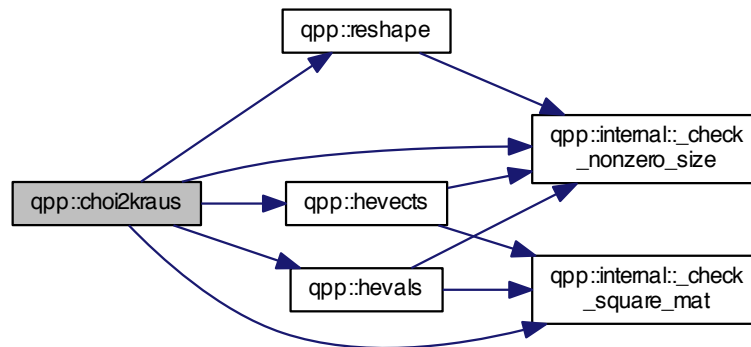
## Parameters

$A$	Choi matrix
-----	-------------

**Returns**

Set of Kraus operators

Here is the call graph for this function:



**6.1.2.12** `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::comm ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )`

Commutator.

Commutator  $[A, B] = AB - BA$

Both  $A$  and  $B$  must be Eigen expressions over the same scalar field

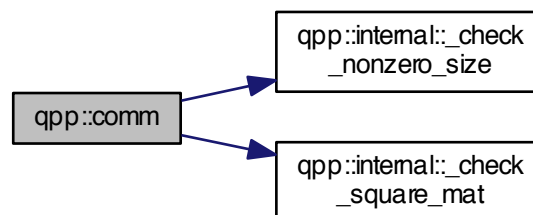
**Parameters**

$A$	Eigen expression
$B$	Eigen expression

**Returns**

Commutator  $AB - BA$ , as a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:





6.1.2.13 `std::vector<std::size_t> qpp::compperm ( const std::vector< std::size_t > & perm, const std::vector< std::size_t > & sigma )`

Compose permutations.

## Parameters

<i>perm</i>	Permutation
<i>sigma</i>	Permutation

## Returns

Composition of the permutations  $perm \circ sigma = perm(sigma)$

Here is the call graph for this function:



6.1.2.14 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::conjugate ( const Eigen::MatrixBase<Derived> & A )`

Complex conjugate.

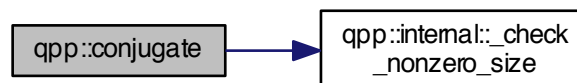
## Parameters

<i>A</i>	Eigen expression
----------	------------------

## Returns

Complex conjugate of *A*, as a dynamic matrix over the same scalar field as *A*

Here is the call graph for this function:



6.1.2.15 `template<typename Derived> cmat qpp::cosm ( const Eigen::MatrixBase<Derived> & A )`

Matrix cos.

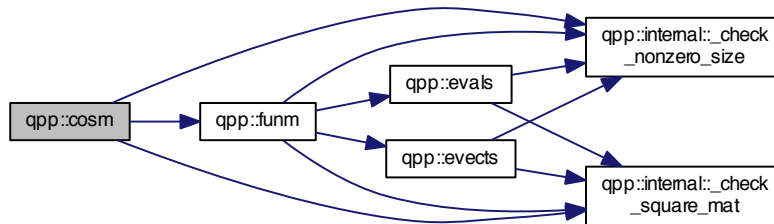
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Matrix cosine of  $A$

Here is the call graph for this function:



**6.1.2.16** `template<typename OutputScalar , typename Derived > DynMat<OutputScalar> qpp::cwise ( const Eigen::MatrixBase< Derived > & A, OutputScalar*)(const typename Derived::Scalar &) f )`

Functor.

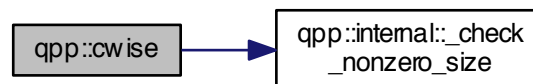
## Parameters

$A$	Eigen expression
$f$	Pointer-to-function from scalars of $A$ to <i>OutputScalar</i>

## Returns

Component-wise  $f(A)$ , as a dynamic matrix over the *OutputScalar* scalar field

Here is the call graph for this function:



**6.1.2.17** `template<typename Derived > Derived::Scalar qpp::det ( const Eigen::MatrixBase< Derived > & A )`

Determinant.

## Parameters

<i>A</i>	Eigen expression
----------	------------------

## Returns

Determinant of *A*, as a scalar in the same scalar field as *A* Returns  $\pm\infty$  when the determinant overflows/underflows

Here is the call graph for this function:



**6.1.2.18** `template<typename T> void qpp::disp ( const T & x, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )`

Displays a standard container that supports `std::begin`, `std::end` and forward iteration. Does not add a newline.

## See also

[`qpp::displn\(\)`](#)

## Parameters

<i>x</i>	Container
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking
<i>os</i>	Output stream

**6.1.2.19** `template<typename T> void qpp::disp ( const T * x, const std::size_t n, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )`

Displays a C-style array. Does not add a newline.

## See also

[`qpp::displn\(\)`](#)

## Parameters

<i>x</i>	Pointer to the first element
----------	------------------------------

<i>n</i>	Number of elements to be displayed
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking
<i>os</i>	Output stream

6.1.2.20 `template<typename Derived > void qpp::disp ( const Eigen::MatrixBase< Derived > & A, double chop = qpp::chop, std::ostream & os = std::cout )`

Displays an Eigen expression in matrix friendly form. Does not add a new line.

See also

[`qpp::displn\(\)`](#)

Parameters

<i>A</i>	Eigen expression
<i>chop</i>	Set to zero the elements smaller in absolute value than <i>chop</i>
<i>os</i>	Output stream

6.1.2.21 `void qpp::disp ( const cplx z, double chop = qpp::chop, std::ostream & os = std::cout )`

Displays a number (implicitly converted to `std::complex<double>`) in friendly form. Does not add a new line.

See also

[`qpp::displn\(\)`](#)

Parameters

<i>z</i>	Real/complex number
<i>chop</i>	Set to zero the elements smaller in absolute value than <i>chop</i>
<i>os</i>	Output stream

Here is the call graph for this function:



6.1.2.22 `template<typename T > void qpp::displn ( const T & x, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )`

Displays a standard container that supports `std::begin`, `std::end` and forward iteration. Adds a newline.

See also

[`qpp::disp\(\)`](#)

## Parameters

<i>x</i>	Container
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking
<i>os</i>	Output stream

Here is the call graph for this function:



**6.1.2.23** `template<typename T> void qpp::displn ( const T * x, const std::size_t n, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )`

Displays a C-style array. Adds a newline.

See also

[qpp::disp\(\)](#)

## Parameters

<i>x</i>	Pointer to the first element
<i>n</i>	Number of elements to be displayed
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking
<i>os</i>	Output stream

Here is the call graph for this function:



**6.1.2.24** `template<typename Derived> void qpp::displn ( const Eigen::MatrixBase< Derived> & A, double chop = qpp::chop, std::ostream & os = std::cout )`

Displays an Eigen expression in matrix friendly form. Adds a newline.

See also

[qpp::disp\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>chop</i>	Set to zero the elements smaller in absolute value than <i>chop</i>
<i>os</i>	Output stream

Here is the call graph for this function:



6.1.2.25 `void qpp::displn ( const cplx z, double chop = qpp::chop, std::ostream & os = std::cout )`

Displays a number (implicitly converted to `std::complex<double>`) in friendly form. Adds a new line.

See also

[qpp::disp\(\)](#)

Parameters

<i>z</i>	Real/complex number
<i>chop</i>	Set to zero the elements smaller in absolute value than <i>chop</i>
<i>os</i>	Output stream

Here is the call graph for this function:



6.1.2.26 `template<typename Derived> double qpp::entanglement ( const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & dims )`

Entanglement of the bi-partite pure state *A*.

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

See also

[qpp::shannon\(\)](#)

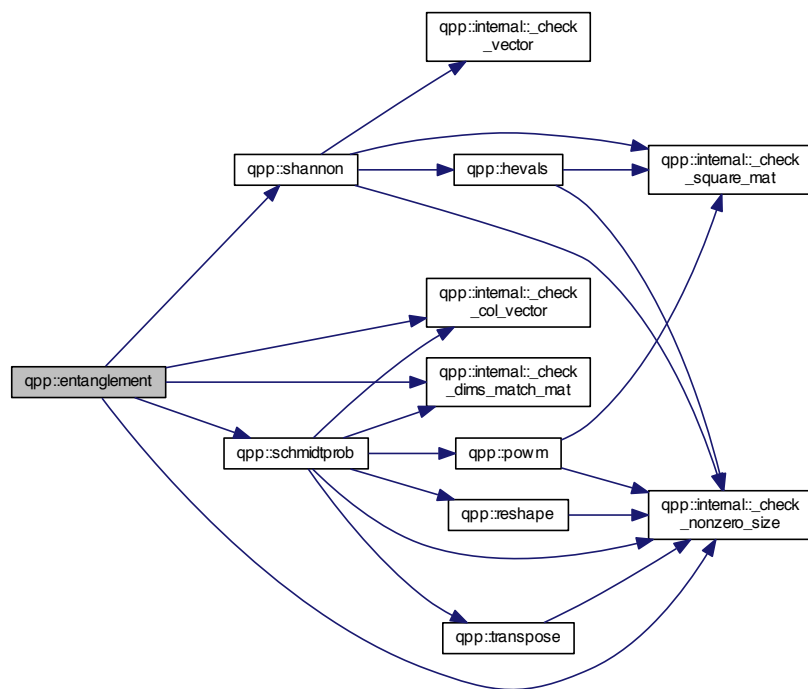
## Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Subsystems' dimensions

## Returns

Entanglement, with the logarithm in base 2

Here is the call graph for this function:



6.1.2.27 `template<typename Derived> cmat qpp::evals ( const Eigen::MatrixBase< Derived> & A )`

Eigenvalues.

## Parameters

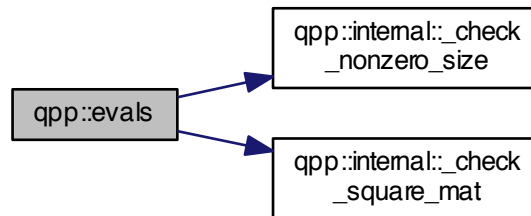
<i>A</i>	Eigen expression
----------	------------------



## Returns

Eigenvalues of  $A$ , as a complex dynamic column vector

Here is the call graph for this function:



6.1.2.28 `template<typename Derived> cmat qpp::evecs ( const Eigen::MatrixBase< Derived > & A )`

Eigenvectors.

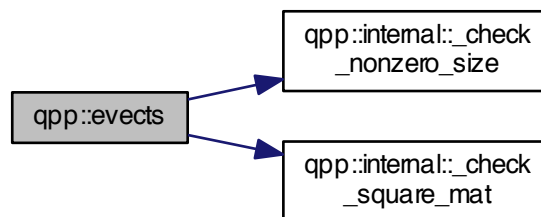
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Eigenvectors of  $A$ , as columns of a complex matrix

Here is the call graph for this function:



6.1.2.29 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::expandout ( const Eigen::MatrixBase< Derived > & A, std::size_t pos, const std::vector< std::size_t > & dims )`

Expand out.

Expand out  $A$  as a matrix in a multi-partite system

Faster than using `qpp::kron(I, I, ..., I, A, I, ..., I)`

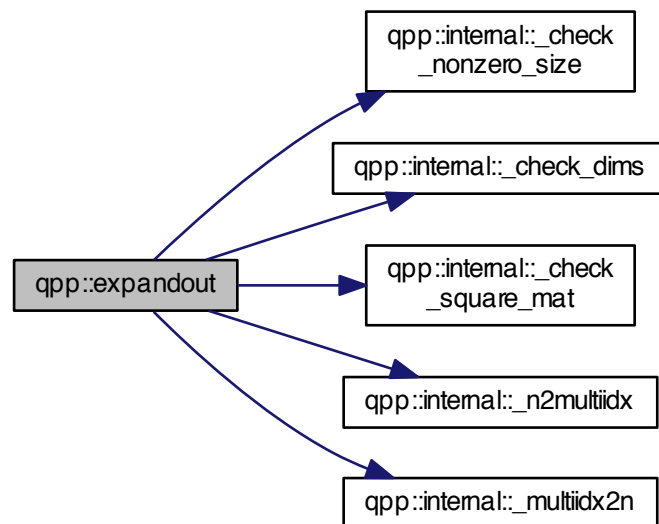
## Parameters

$A$	Eigen expression
$pos$	Position
$dims$	Dimensions of the multi-partite system

## Returns

Tensor product  $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$ , with  $A$  on position  $pos$ , as a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:



6.1.2.30 `template<typename Derived> cmat qpp::expm ( const Eigen::MatrixBase< Derived> & A )`

Matrix exponential.

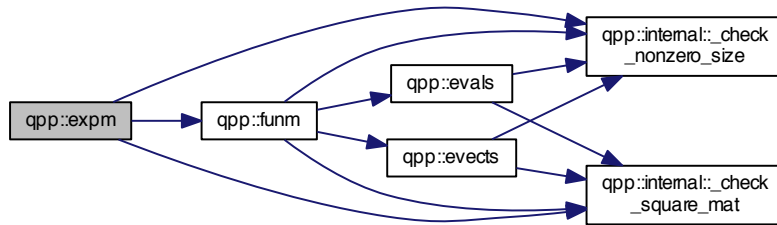
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Matrix exponential of  $A$

Here is the call graph for this function:



6.1.2.31 `template<typename Derived> cmat qpp::funm ( const Eigen::MatrixBase< Derived> & A, cplx(*) (const cplx &) f )`

Functional calculus  $f(A)$

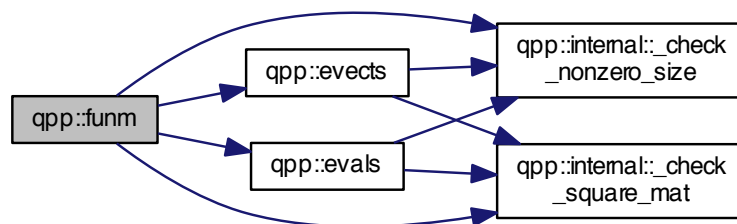
## Parameters

$A$	Eigen expression
$f$	Pointer-to-function from complex to complex

## Returns

$f(A)$

Here is the call graph for this function:



6.1.2.32 `template<typename Derived> double qpp::gconcurrence ( const Eigen::MatrixBase< Derived> & A )`

G-concurrence of the bi-partite pure state  $A$ .

Uses [qpp::logdet\(\)](#) to avoid overflows

See also

[qpp::logdet\(\)](#)

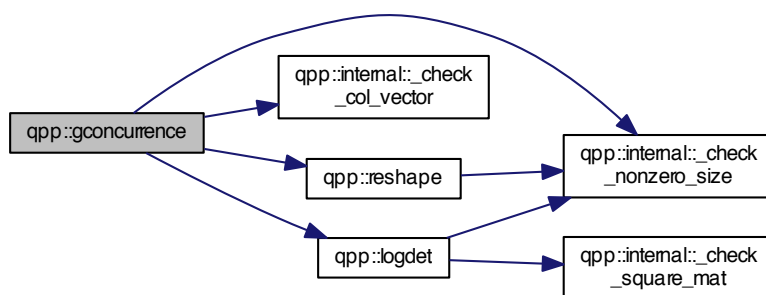
Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Subsystems' dimensions

Returns

G-concurrence

Here is the call graph for this function:



6.1.2.33 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::grams ( const std::vector< Derived > & Vs )`

Gram-Schmidt orthogonalization (std::vector overload)

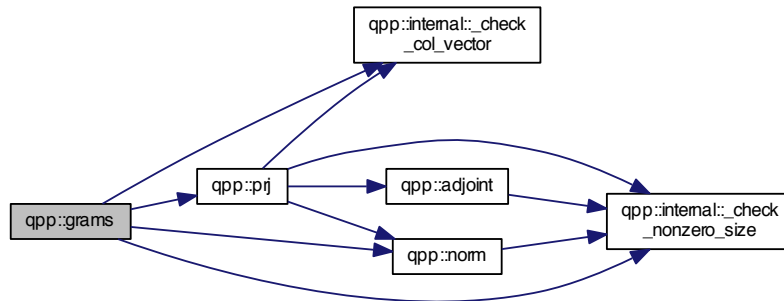
Parameters

<i>Vs</i>	std::vector of Eigen expressions as column vectors
-----------	--

## Returns

Gram-Schmidt vectors of  $V$ s as columns of a dynamic matrix over the same scalar field as its arguments

Here is the call graph for this function:



**6.1.2.34** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::grams ( const std::initializer_list<Derived> & Vs )`

Gram-Schmidt orthogonalization (std::initializer\_list overload)

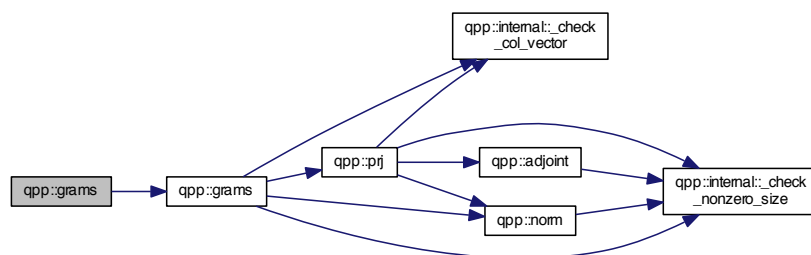
## Parameters

$V$ s	std::initializer_list of Eigen expressions as column vectors
-------	--

## Returns

Gram-Schmidt vectors of  $V$ s as columns of a dynamic matrix over the same scalar field as its arguments

Here is the call graph for this function:



**6.1.2.35** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::grams ( const Eigen::MatrixBase<Derived> & A )`

Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)

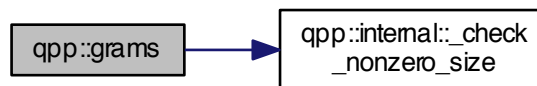
## Parameters

$A$	Eigen expression, the input vectors are the columns of $A$
-----	--

## Returns

Gram-Schmidt vectors of the columns of  $A$ , as columns of a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:



### 6.1.2.36 `template<typename Derived> dmat qpp::hevals ( const Eigen::MatrixBase< Derived> & A )`

Hermitian eigenvalues.

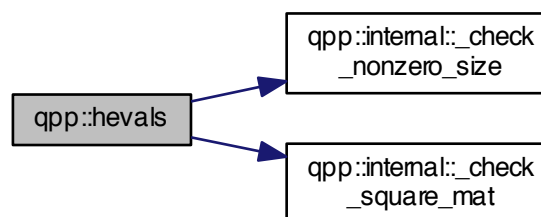
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Eigenvalues of Hermitian  $A$ , as a real dynamic column vector

Here is the call graph for this function:



### 6.1.2.37 `template<typename Derived> cmat qpp::hevects ( const Eigen::MatrixBase< Derived> & A )`

Hermitian eigenvectors.

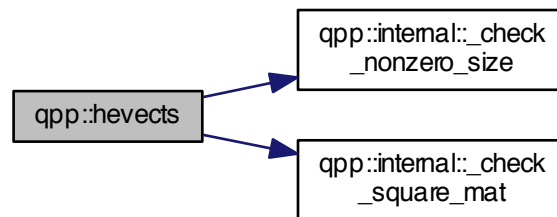
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Eigenvectors of Hermitian  $A$ , as columns of a complex matrix

Here is the call graph for this function:



**6.1.2.38** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::inverse ( const Eigen::MatrixBase<Derived> & A )`

Inverse.

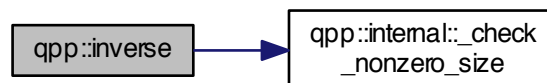
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Inverse of  $A$ , as a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:



**6.1.2.39** `std::vector<std::size_t> qpp::invperm ( const std::vector< std::size_t > & perm )`

Inverse permutation.

## Parameters

<i>perm</i>	Permutation
-------------	-------------

## Returns

Inverse of the permutation *perm*

Here is the call graph for this function:



#### 6.1.2.40 `template<typename T> DynMat<typename T::Scalar> qpp::kron ( const T & head )`

Kronecker product (variadic overload)

Used to stop the recursion for the variadic template version of [qpp::kron\(\)](#)

## Parameters

<i>head</i>	Eigen expression
-------------	------------------

## Returns

Its argument *head*

#### 6.1.2.41 `template<typename T , typename... Args> DynMat<typename T::Scalar> qpp::kron ( const T & head, const Args &... tail )`

Kronecker product (variadic overload)

## Parameters

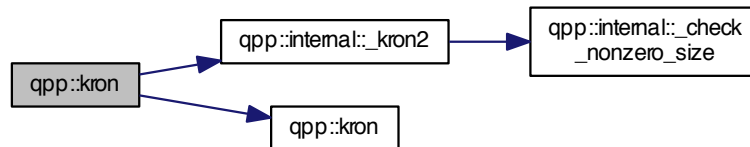
<i>head</i>	Eigen expression
<i>tail</i>	Variadic Eigen expression (zero or more parameters)



**Returns**

Kronecker product of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

Here is the call graph for this function:



**6.1.2.42** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::kron ( const std::vector< Derived> & As )`

Kronecker product (std::vector overload)

**Parameters**

<b>As</b>	std::vector of Eigen expressions
-----------	----------------------------------

**Returns**

Kronecker product of all elements in As, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

Here is the call graph for this function:



**6.1.2.43** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::kron ( const std::initializer_list< Derived> & As )`

Kronecker product (std::initializer\_list overload)

**Parameters**

<i>As</i>	std::initializer_list of Eigen expressions, such as {A1, A2, ... ,Ak}
-----------	---

**Returns**

Kronecker product of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

Here is the call graph for this function:



**6.1.2.44** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::kronpow ( const Eigen::MatrixBase<Derived> & A, std::size_t n )`

Kronecker power.

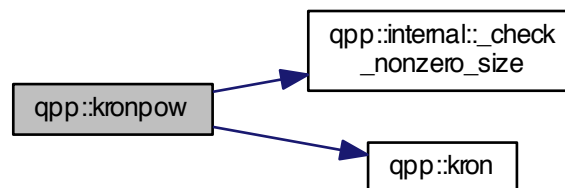
**Parameters**

<i>A</i>	Eigen expression
<i>n</i>	Non-negative integer

**Returns**

Kronecker product of *A* with itself *n* times  $A^{\otimes n}$ , as a dynamic matrix over the same scalar field as *A*

Here is the call graph for this function:



**6.1.2.45** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::load ( const std::string & fname )`

Loads Eigen matrix from a binary file (internal format) in double precision.

The template parameter cannot be automatically deduced and must be explicitly provided, depending on the scalar field of the matrix that is being loaded.

Example:

```
// loads a previously saved Eigen dynamic complex matrix from "input.bin"
auto mat = load<cmat>("input.bin");
```

See also

[qpp::loadMATLABmatrix\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>fname</i>	Output file name

**6.1.2.46** `template<typename Derived > Derived qpp::loadMATLABmatrix ( const std::string & mat_file, const std::string & var_name )`

Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.

This is the generic version that always throws [qpp::Exception::Type::UNDEFINED\\_TYPE](#). It is specialized only for [qpp::dmat](#) and [qpp::cmat](#) (the only matrix types that can be loaded)

**6.1.2.47** `template<> dmat qpp::loadMATLABmatrix ( const std::string & mat_file, const std::string & var_name )`

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen dynamic double matrix from the
MATLAB file "input.mat"
auto mat = loadMATLABmatrix<dmat>("input.mat");
```

Note

If *var\_name* is a complex matrix, only the real part is loaded

Parameters

<i>mat_file</i>	MATALB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be loaded

Returns

Eigen double dynamic matrix ([qpp::dmat](#))

**6.1.2.48** `template<> cmat qpp::loadMATLABmatrix ( const std::string & mat_file, const std::string & var_name )`

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen dynamic complex matrix from the
MATLAB file "input.mat"
auto mat = loadMATLABmatrix<cmat>("input.mat");
```

## Parameters

<i>mat_file</i>	MATALB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be loaded

## Returns

Eigen complex dynamic matrix ([qpp::cmat](#))

6.1.2.49 `template<typename Derived > Derived::Scalar qpp::logdet ( const Eigen::MatrixBase< Derived > & A )`

Logarithm of the determinant.

Especially useful when the determinant overflows/underflows

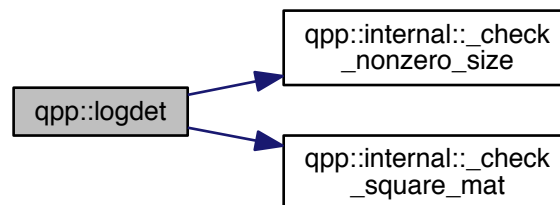
## Parameters

<i>A</i>	Eigen expression
----------	------------------

## Returns

Logarithm of the determinant of *A*, as a scalar in the same scalar field as *A*

Here is the call graph for this function:



6.1.2.50 `template<typename Derived > cmat qpp::logm ( const Eigen::MatrixBase< Derived > & A )`

Matrix logarithm.

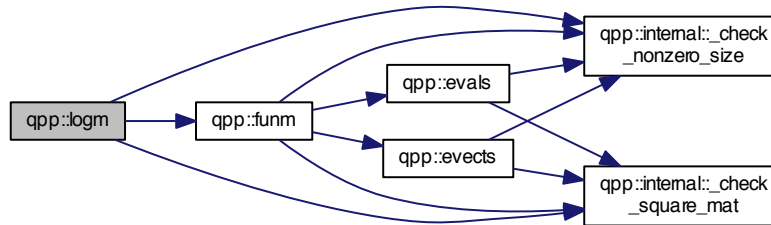
## Parameters

<i>A</i>	Eigen expression
----------	------------------

## Returns

Matrix logarithm of  $A$

Here is the call graph for this function:



#### 6.1.2.51 ket qpp::mket ( const std::vector< std::size\_t > & mask )

Multi-partite qubit ket.

Constructs the multi-partite qubit ket  $|\text{mask}\rangle$ , where *mask* is a std::vector of 0's and 1's

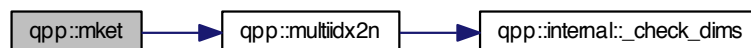
## Parameters

<i>mask</i>	std::vector of 0's and 1's
-------------	----------------------------

## Returns

Multi-partite qubit state vector, as a complex dynamic column vector

Here is the call graph for this function:



#### 6.1.2.52 ket qpp::mket ( const std::vector< std::size\_t > & mask, const std::vector< std::size\_t > & dims )

Multi-partite qudit ket (different dimensions overload)

Constructs the multi-partite qudit ket  $|\text{mask}\rangle$ , where *mask* is a std::vector of non-negative integers  
Each element in *mask* has to be smaller than the corresponding element in *dims*

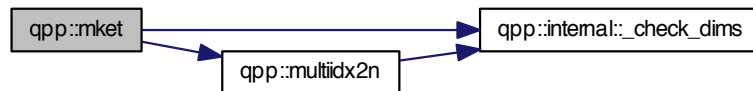
## Parameters

<i>mask</i>	std::vector of non-negative integers
<i>dims</i>	Dimensions of the multi-partite system

**Returns**

Multi-partite qudit state vector, as a complex dynamic column vector

Here is the call graph for this function:



### 6.1.2.53 ket qpp::mket ( const std::vector< std::size\_t > & mask, std::size\_t d )

Multi-partite qudit ket (same dimensions overload)

Constructs the multi-partite qudit ket  $|\text{mask}\rangle$ , all subsystem having equal dimension  $d$   
 $\text{mask}$  is a std::vector of non-negative integers, and each element in  $\text{mask}$  has to be strictly smaller than  $d$

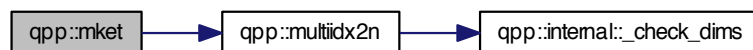
**Parameters**

<i>mask</i>	std::vector of non-negative integers
<i>d</i>	Subsystems' dimension

**Returns**

Multi-partite qudit state vector, as a complex dynamic column vector

Here is the call graph for this function:



### 6.1.2.54 cmat qpp::mprj ( const std::vector< std::size\_t > & mask )

Projector onto multi-partite qubit ket.

Constructs the projector onto the multi-partite qubit ket  $|\text{mask}\rangle$ , where  $\text{mask}$  is a std::vector of 0's and 1's

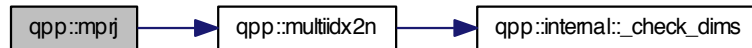
## Parameters

<i>mask</i>	std::vector of 0's and 1's
-------------	----------------------------

## Returns

Projector onto multi-partite qubit state vector, as a complex dynamic matrix

Here is the call graph for this function:



#### 6.1.2.55 cmat qpp::mprj ( const std::vector< std::size\_t > & mask, const std::vector< std::size\_t > & dims )

Projector onto multi-partite qudit ket (different dimensions overload)

Constructs the projector onto the multi-partite qudit ket  $|mask\rangle$ , where *mask* is a std::vector of non-negative integers. Each element in *mask* has to be smaller than the corresponding element in *dims*.

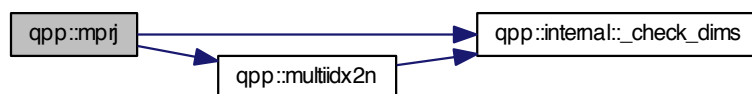
## Parameters

<i>mask</i>	std::vector of non-negative integers
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

Here is the call graph for this function:



#### 6.1.2.56 cmat qpp::mprj ( const std::vector< std::size\_t > & mask, std::size\_t d )

Projector onto multi-partite qudit ket (same dimensions overload)

Constructs the projector onto the multi-partite qudit ket  $|mask\rangle$ , all subsystem having equal dimension *d*. *mask* is a std::vector of non-negative integers, and each element in *mask* has to be strictly smaller than *d*.

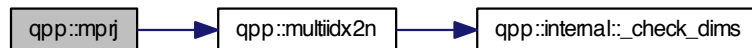
## Parameters

<i>mask</i>	std::vector of non-negative integers
<i>d</i>	Subsystems' dimension

## Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

Here is the call graph for this function:



6.1.2.57 `std::size_t qpp::multiidx2n ( const std::vector< std::size_t > & midx, const std::vector< std::size_t > & dims )`

Multi-index to non-negative integer index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

## Parameters

<i>midx</i>	Multi-index
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Non-negative integer index

Here is the call graph for this function:



6.1.2.58 `std::vector<std::size_t> qpp::n2multiidx ( std::size_t n, const std::vector< std::size_t > & dims )`

Non-negative integer index to multi-index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.



## Parameters

<i>n</i>	Non-negative integer index
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Multi-index of the same size as *dims*

Here is the call graph for this function:



### 6.1.2.59 `template<typename Derived> double qpp::norm ( const Eigen::MatrixBase< Derived> & A )`

Trace norm.

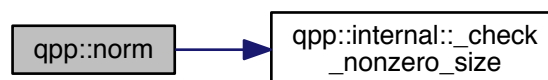
## Parameters

<i>A</i>	Eigen expression
----------	------------------

## Returns

Trace norm (Frobenius norm) of *A*, as a real number

Here is the call graph for this function:



### 6.1.2.60 `std::complex<double> qpp::omega ( std::size_t D )`

D-th root of unity.

## Parameters

$D$	Non-negative integer
-----	----------------------

**Returns**

D-th root of unity  $\exp(2\pi i/D)$

**6.1.2.61** `constexpr std::complex<double> qpp::operator""_i ( unsigned long long int x )`

User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)

Example:

```
auto z = 4_i; // type of z is std::complex<double>
```

**6.1.2.62** `constexpr std::complex<double> qpp::operator""_i ( long double x )`

User-defined literal for complex  $i = \sqrt{-1}$  (real overload)

Example:

```
auto z = 4.5_i; // type of z is std::complex<double>
```

**6.1.2.63** `template<typename Derived > DynMat<typename Derived::Scalar> qpp::powm ( const Eigen::MatrixBase<Derived > &A, std::size_t n )`

Matrix power.

Explicitly multiplies the matrix  $A$  with itself  $n$  times

By convention  $A^0 = I$

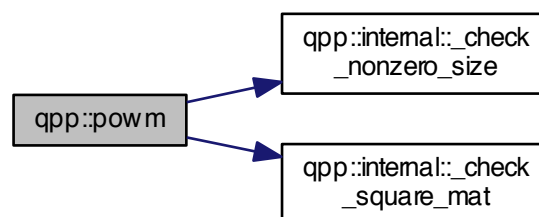
**Parameters**

$A$	Eigen expression
$n$	Non-negative integer

**Returns**

Matrix power  $A^n$ , as a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:



6.1.2.64 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::prj ( const Eigen::MatrixBase< Derived> & V )`

Projector.

Normalized projector onto state vector

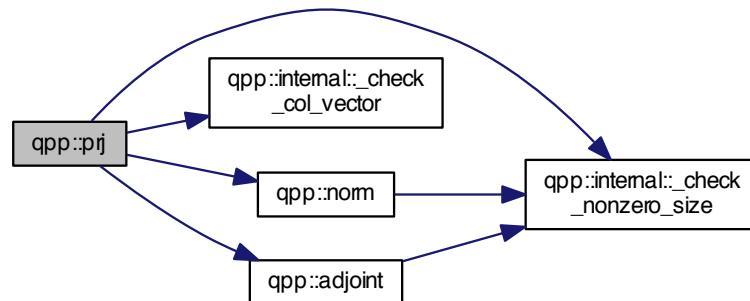
Parameters

<code>V</code>	Eigen expression
----------------	------------------

Returns

Projector onto the state vector  $V$ , or the matrix  $Zero$  if  $V$  has norm zero (i.e. smaller than `qpp::eps`), as a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:



6.1.2.65 `template<typename Derived> Derived::Scalar qpp::prod ( const Eigen::MatrixBase< Derived> & A )`

Element-wise product of  $A$ .

Parameters

<code>A</code>	Eigen expression
----------------	------------------

Returns

Element-wise product of  $A$ , as a scalar in the same scalar field as  $A$

Here is the call graph for this function:



6.1.2.66 `template<typename InputIterator > auto qpp::prod ( InputIterator first, InputIterator last ) -> typename InputIterator::value_type`

Element-wise product of a range.

Parameters

<i>first</i>	Iterator to the first element of the range
<i>last</i>	Iterator to the last element of the range

Returns

Element-wise product of the range, as a scalar in the same scalar field as the range

6.1.2.67 `template<typename Derived > DynMat<typename Derived::Scalar> qpp::ptrace ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size_t > & subsys, const std::vector< std::size_t > & dims )`

Partial trace.

Partial trace of the multi-partite density matrix over a list of subsystems

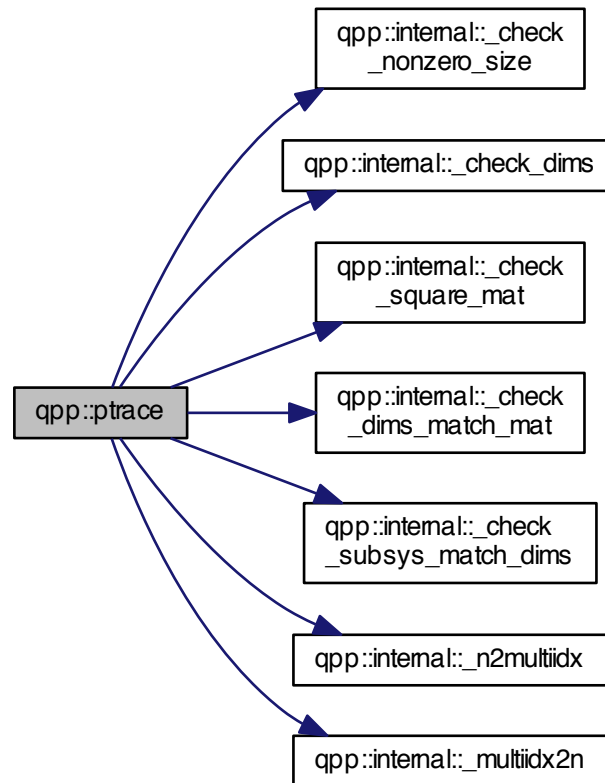
Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes
<i>dims</i>	Dimensions of the multi-partite system

Returns

Partial trace  $Tr_{subsys}(\cdot)$  over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

Here is the call graph for this function:



**6.1.2.68** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::ptrace1 ( const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & dims )`

Partial trace.

Partial trace of density matrix over the first subsystem in a bi-partite system

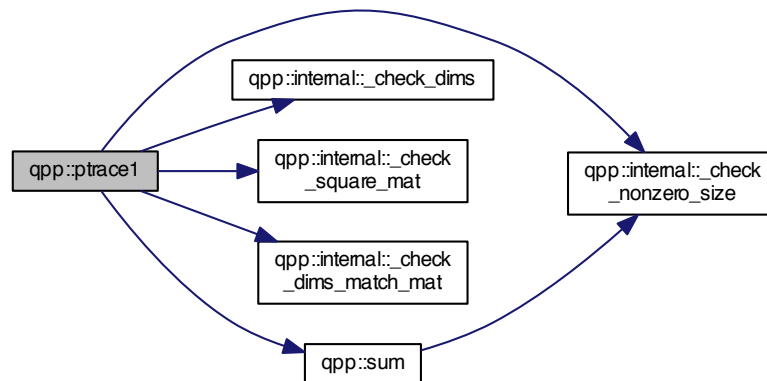
Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of bi-partite system (must be a <code>std::vector</code> with 2 elements)

**Returns**

Partial trace  $Tr_A(\cdot)$  over the first subsystem  $A$  in a bi-partite system  $A \otimes B$ , as a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:



6.1.2.69 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::ptrace2 ( const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & dims )`

Partial trace.

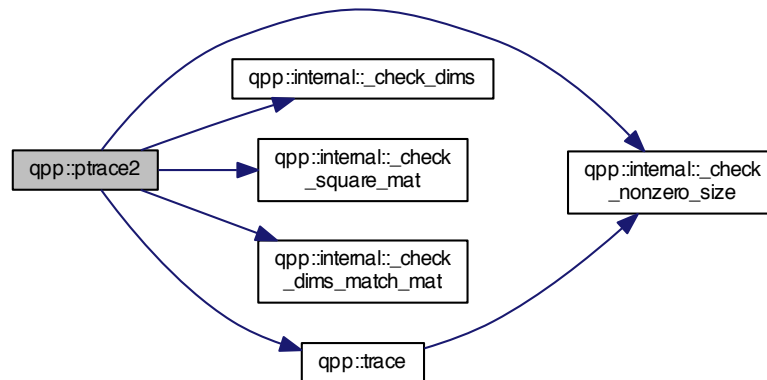
**Parameters**

$A$	Eigen expression
$dims$	Dimensions of bi-partite system (must be a <code>std::vector</code> with 2 elements)

**Returns**

Partial trace  $Tr_B(\cdot)$  over the second subsystem  $B$  in a bi-partite system  $A \otimes B$ , as a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:



**6.1.2.70** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::ptranspose ( const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & subsys, const std::vector< std::size_t > & dims )`

Partial transpose.

Partial transpose of the multi-partite density matrix over a list of subsystems

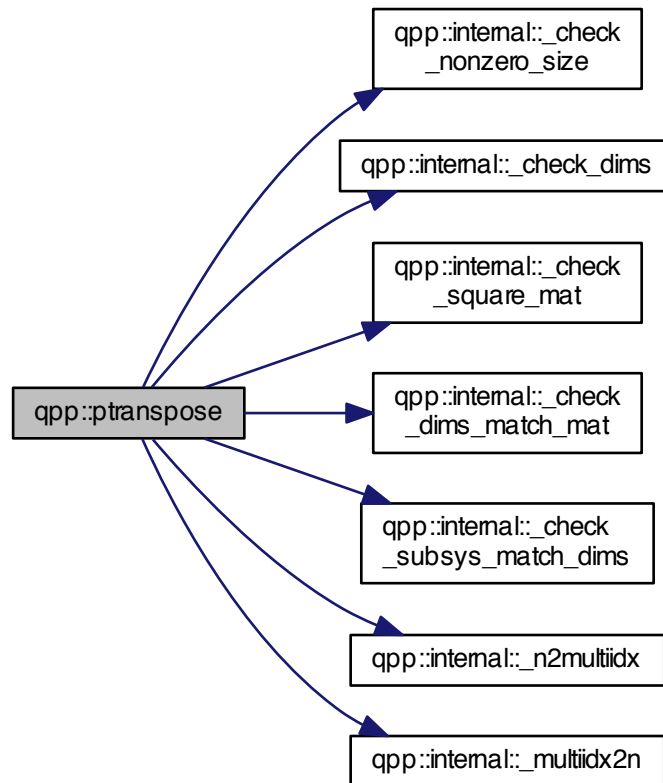
**Parameters**

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes
<i>dims</i>	Dimensions of the multi-partite system

**Returns**

Partial transpose  $(\cdot)^{T_{subsys}}$  over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

Here is the call graph for this function:



6.1.2.71 `template<typename Derived> double qpp::qmutualinfo ( const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & subsysA, const std::vector< std::size_t> & subsysB, const std::vector< std::size_t> & dims )`

Quantum mutual information between 2 subsystems of a composite system.

Parameters

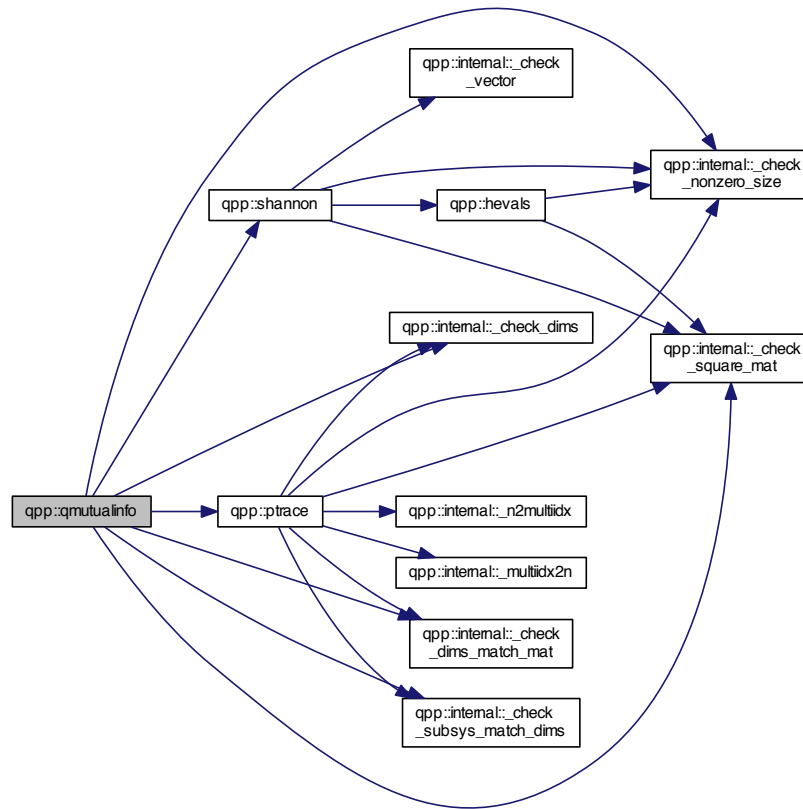
<i>A</i>	Eigen expression
<i>subsysA</i>	Indexes of the first subsystem
<i>subsysB</i>	Indexes of the second subsystem
<i>dims</i>	Subsystems' dimensions



## Returns

Mutual information between the 2 subsystems

Here is the call graph for this function:



#### 6.1.2.72 `template<typename Derived> Derived qpp::rand ( std::size_t rows, std::size_t cols, double a = 0, double b = 1 )`

Generates a random matrix with entries uniformly distributed in the interval [a, b)

If complex, then both real and imaginary parts are uniformly distributed in [a, b)

This is the generic version that always throws `qpp::Exception::Type::UNDEFINED_TYPE`. It is specialized only for `qpp::dmat` and `qpp::cmat`

#### 6.1.2.73 `template<> dmat qpp::rand ( std::size_t rows, std::size_t cols, double a, double b )`

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (`qpp::dmat`)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd, with entries uniformly distributed in [-1,1)
auto mat = rand<dmat>(3, 3, -1, 1);
```

**Parameters**

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

**Returns**

Random real matrix

#### 6.1.2.74 `template<> cmat qpp::rand ( std::size_t rows, std::size_t cols, double a, double b )`

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices ([qpp::cmat](#))

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd, with entries (both real and imaginary) uniformly distributed
// in [-1,1)
auto mat = rand<cmat>(3, 3, -1, 1);
```

**Parameters**

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

**Returns**

Random complex matrix

Here is the call graph for this function:



#### 6.1.2.75 `double qpp::rand ( double a = 0, double b = 1 )`

Generates a random real number uniformly distributed in the interval [a, b)

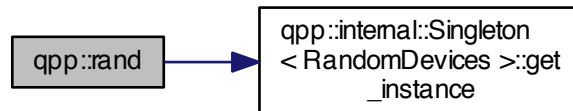
**Parameters**

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

**Returns**

Random real number (double) uniformly distributed in the interval [a, b)

Here is the call graph for this function:

**6.1.2.76 cmat qpp::randH ( std::size\_t *D* )**

Generates a random Hermitian matrix.

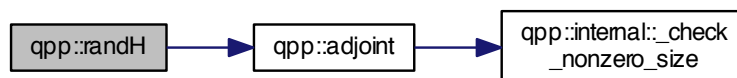
**Parameters**

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

**Returns**

Random Hermitian matrix

Here is the call graph for this function:

**6.1.2.77 int qpp::randint ( int *a* = std::numeric\_limits<int>::min(), int *b* = std::numeric\_limits<int>::max() )**

Generates a random integer (int) uniformly distributed in the interval [a, b].

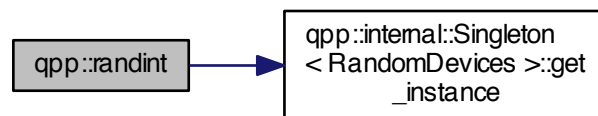
## Parameters

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

## Returns

Random integer (int) uniformly distributed in the interval [a, b]

Here is the call graph for this function:

6.1.2.78 ket `qpp::randket ( std::size_t D )`

Generates a random normalized ket (pure state vector)

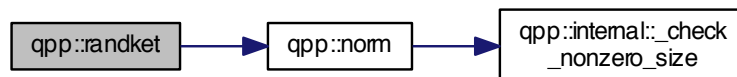
## Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

## Returns

Random normalized ket

Here is the call graph for this function:

6.1.2.79 `std::vector<cmat> qpp::randkraus ( std::size_t n, std::size_t D )`

Generates a set of random Kraus operators.

## Note

The set of Kraus operators satisfy the closure condition  $\sum_i K_i^\dagger K_i = I$

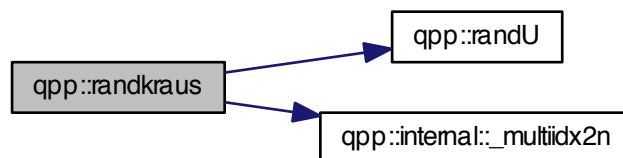
## Parameters

$n$	Number of Kraus operators
$D$	Dimension of the Hilbert space

## Returns

Set of  $n$  Kraus operators satisfying the closure condition

Here is the call graph for this function:



**6.1.2.80** `template<typename Derived > Derived qpp::randn ( std::size_t rows, std::size_t cols, double mean = 0, double sigma = 1 )`

Generates a random matrix with entries normally distributed in  $N(\text{mean}, \text{sigma})$

If complex, then both real and imaginary parts are normally distributed in  $N(\text{mean}, \text{sigma})$

This is the generic version that always throws [`qpp::Exception::Type::UNDEFINED\_TYPE`](#). It is specialized only for [`qpp::dmat`](#) and [`qpp::cmat`](#)

**6.1.2.81** `template<> dmat qpp::randn ( std::size_t rows, std::size_t cols, double mean, double sigma )`

Generates a random real matrix with entries normally distributed in  $N(\text{mean}, \text{sigma})$ , specialization for double matrices ([`qpp::dmat`](#))

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd, with entries normally distributed in N(0,2)
auto mat = randn<dmat>(3, 3, 0, 2);
```

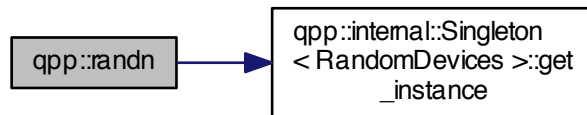
## Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

**Returns**

Random real matrix

Here is the call graph for this function:



#### 6.1.2.82 `template<> cmat qpp::randn ( std::size_t rows, std::size_t cols, double mean, double sigma )`

Generates a random complex matrix with entries (both real and imaginary) normally distributed in  $N(\text{mean}, \text{sigma})$ , specialization for complex matrices ([qpp::cmat](#))

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd, with entries (both real and imaginary) normally distributed
// in N(0,2)
auto mat = randn<cmat>(3, 3, 0, 2);
```

**Parameters**

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

**Returns**

Random complex matrix

Here is the call graph for this function:



#### 6.1.2.83 `double qpp::randn ( double mean = 0, double sigma = 1 )`

Generates a random real number (double) normally distributed in  $N(\text{mean}, \text{sigma})$

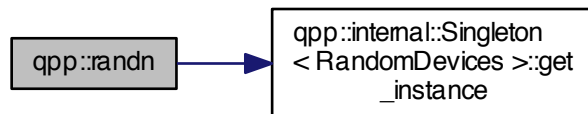
## Parameters

<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

## Returns

Random real number normally distributed in  $N(\text{mean}, \text{sigma})$

Here is the call graph for this function:



#### 6.1.2.84 `std::vector<std::size_t> qpp::randperm ( std::size_t n )`

Generates a random uniformly distributed permutation.

Uses Knuth's shuffle method (as implemented by `std::shuffle`), so that all permutations are equally probable

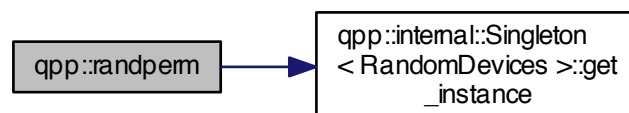
## Parameters

<i>n</i>	Size of the permutation
----------	-------------------------

## Returns

Random permutation of size *n*

Here is the call graph for this function:



#### 6.1.2.85 `cmat qpp::randrho ( std::size_t D )`

Generates a random density matrix.

## Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

## Returns

Random density matrix

6.1.2.86 `cmat qpp::randU ( std::size_t D )`

Generates a random unitary matrix.

## Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

## Returns

Random unitary

6.1.2.87 `cmat qpp::randV ( std::size_t Din, std::size_t Dout )`

Generates a random isometry matrix.

## Parameters

<i>Din</i>	Size of the input Hilbert space
<i>Dout</i>	Size of the output Hilbert space

## Returns

Random isometry matrix

Here is the call graph for this function:

6.1.2.88 `template<typename Derived> double qpp::renyi ( const double alpha, const Eigen::MatrixBase< Derived > & A )`

Renyi-  $\alpha$  entropy of the probability distribution/density matrix  $A$ , for  $\alpha \geq 0$ .

## Parameters

<i>alpha</i>	Non-negative real number
--------------	--------------------------

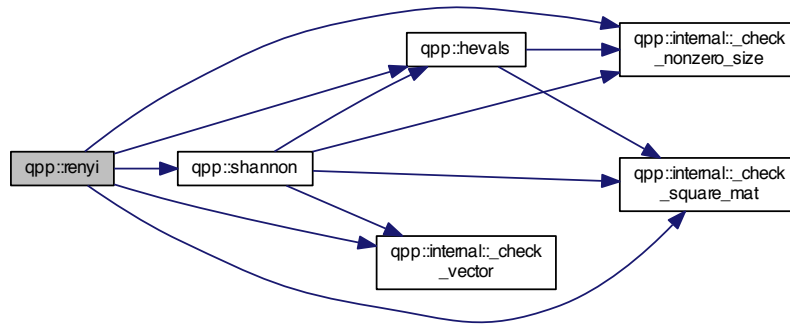


A	Eigen expression, representing a probability distribution (real dynamic column vector) or a density matrix (complex dynamic matrix)
---	---

**Returns**

Renyi-  $\alpha$  entropy, with the logarithm in base 2

Here is the call graph for this function:



6.1.2.89 `template<typename Derived> double qpp::renyi_inf ( const Eigen::MatrixBase< Derived > & A )`

Renyi-  $\infty$  entropy (min entropy) of the probability distribution/density matrix  $A$ .

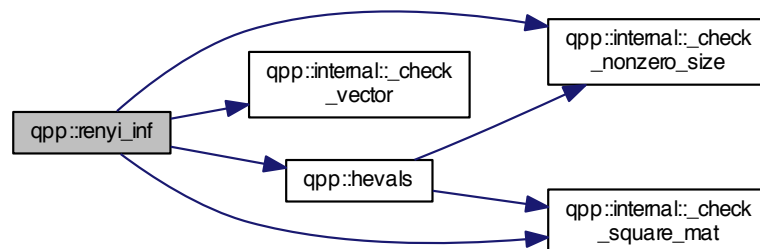
**Parameters**

A	Eigen expression, representing a probability distribution (real dynamic column vector) or a density matrix (complex dynamic matrix)
---	---

**Returns**

Renyi-  $\infty$  entropy (min entropy), with the logarithm in base 2

Here is the call graph for this function:



6.1.2.90 `template<typename Derived > DynMat<typename Derived::Scalar> qpp::reshape ( const Eigen::MatrixBase<Derived > & A, std::size_t rows, std::size_t cols )`

Reshape.

Uses column-major order when reshaping (same as MATLAB)

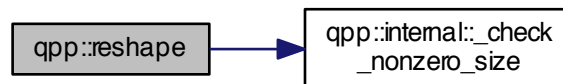
Parameters

<i>A</i>	Eigen expression
<i>rows</i>	Number of rows of the reshaped matrix
<i>cols</i>	Number of columns of the reshaped matrix

Returns

Reshaped matrix with *rows* rows and *cols* columns, as a dynamic matrix over the same scalar field as *A*

Here is the call graph for this function:



6.1.2.91 `template<typename Derived > void qpp::save ( const Eigen::MatrixBase<Derived > & A, const std::string & fname )`

Saves Eigen expression to a binary file (internal format) in double precision.

See also

[qpp::saveMATLABmatrix\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>fname</i>	Output file name

6.1.2.92 `template<typename Derived > void qpp::saveMATLABmatrix ( const Eigen::MatrixBase<Derived > & A, const std::string & mat_file, const std::string & var_name, const std::string & mode )`

Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.

This is the generic version that always throws [qpp::Exception::Type::UNDEFINED\\_TYPE](#). It is specialized only for [qpp::dmat](#) and [qpp::cmat](#) (the only matrix types that can be saved)

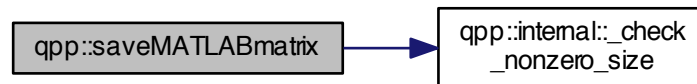
6.1.2.93 `template<> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase<dmat > & A, const std::string & mat_file, const std::string & var_name, const std::string & mode )`

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))

## Parameters

<i>A</i>	Eigen expression over the complex field
<i>mat_file</i>	MATALB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be saved
<i>mode</i>	Saving mode (append, overwrite etc.), see MATLAB's <i>matOpen()</i> documentation for details

Here is the call graph for this function:



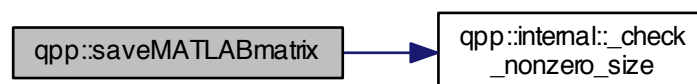
6.1.2.94 `template<> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< cmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode )`

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))

## Parameters

<i>A</i>	Eigen expression over the complex field
<i>mat_file</i>	MATALB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be saved
<i>mode</i>	Saving mode (append, overwrite etc.), see MATLAB's <i>matOpen()</i> documentation for details

Here is the call graph for this function:



6.1.2.95 `template<typename Derived > cmat qpp::schmidtcoeff ( const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims )`

Schmidt coefficients of the bi-partite pure state *A*.

## Note

The sum of the squares of the Schmidt coefficients equals 1

## See also

[qpp::schmidtprob\(\)](#)

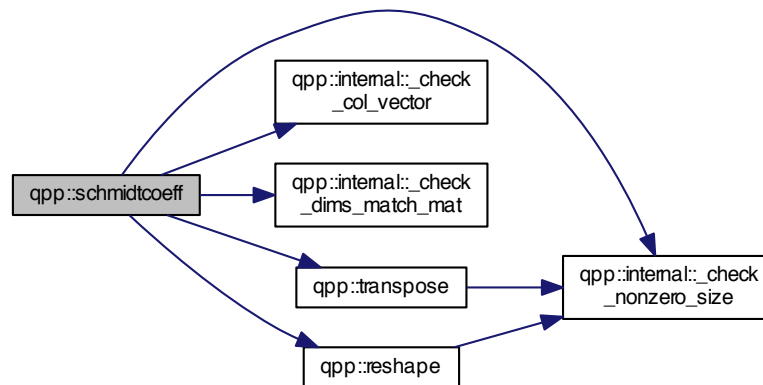
## Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Subsystems' dimensions

## Returns

Schmidt coefficients of *A*, as a complex dynamic matrix, with the Schmidt coefficients on the diagonal

Here is the call graph for this function:



6.1.2.96 `template<typename Derived> cmat qpp::schmidtprob ( const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & dims )`

Schmidt probabilities of the bi-partite pure state *A*.

Defined as the squares of the Schmidt coefficients

The sum of the Schmidt probabilities equals 1

## See also

[`qpp::schmidtcoeff\(\)`](#)

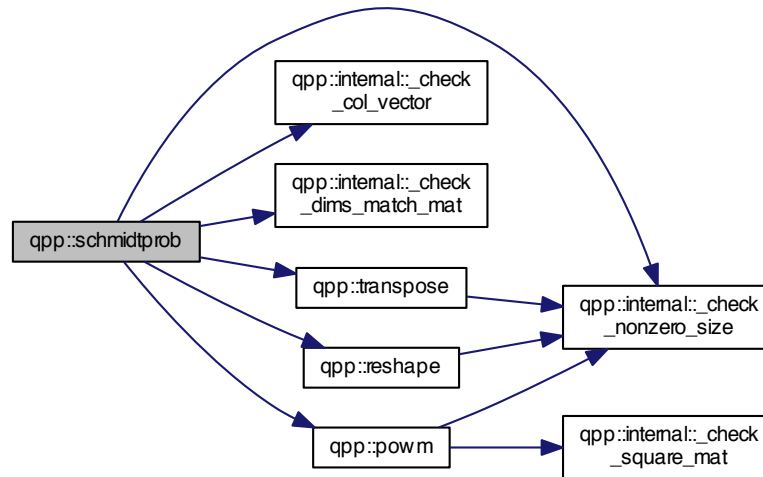
## Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Subsystems' dimensions

## Returns

Schmidt probabilities of  $A$ , as a complex dynamic matrix, with the Schmidt probabilities on the diagonal

Here is the call graph for this function:



```
6.1.2.97 template<typename Derived> cmat qpp::schmidtU ( const Eigen::MatrixBase< Derived > & A, const std::vector<
std::size_t> & dims )
```

Schmidt basis on Alice's side.

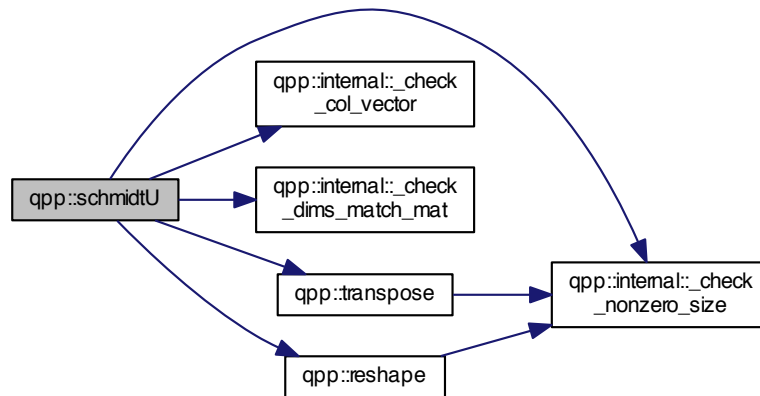
## Parameters

$A$	Eigen expression
$dims$	Subsystems' dimensions

**Returns**

Unitary matrix  $U$  representing the Schmidt basis on Alice's side, as a complex dynamic matrix, acting on the computational basis as  $U|j\rangle = |\bar{j}\rangle$  (Schmidt vector)

Here is the call graph for this function:



**6.1.2.98** `template<typename Derived> cmat qpp::schmidtV ( const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & dims )`

Schmidt basis on Bob's side.

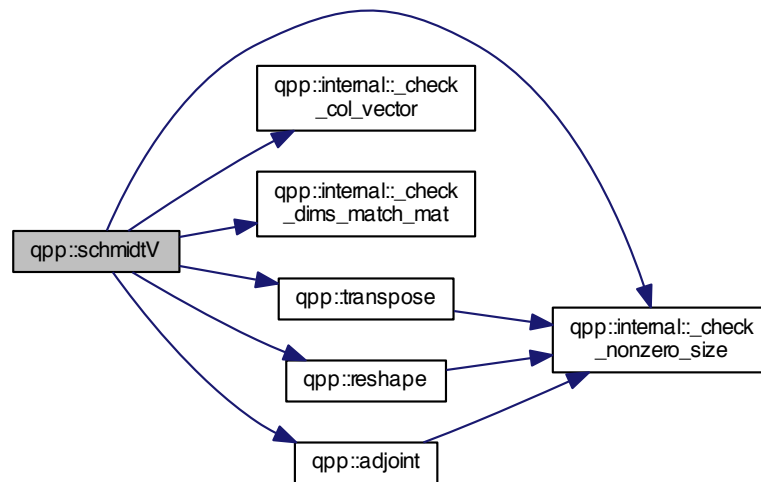
**Parameters**

<i>A</i>	Eigen expression
<i>dims</i>	Subsystems' dimensions

**Returns**

Unitary matrix  $V$  representing the Schmidt basis on Bob's side, as a complex dynamic matrix, acting on the computational basis as  $V|j\rangle = |\bar{j}\rangle$  (Schmidt vector)

Here is the call graph for this function:



#### 6.1.2.99 `template<typename Derived> double qpp::shannon ( const Eigen::MatrixBase< Derived > & A )`

Shannon/von-Neumann entropy of the probability distribution/density matrix *A*.

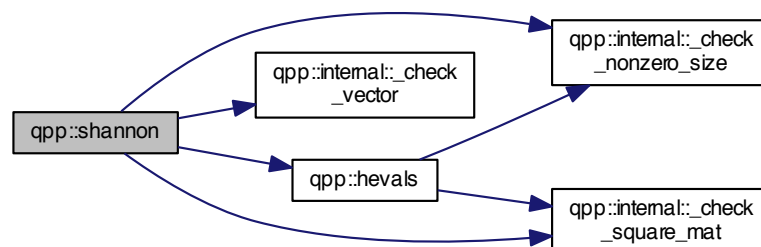
##### Parameters

<i>A</i>	Eigen expression, representing a probability distribution (real dynamic column vector) or a density matrix (complex dynamic matrix)
----------	---

##### Returns

Shannon/von-Neumann entropy, with the logarithm in base 2

Here is the call graph for this function:



6.1.2.100 `template<typename Derived > cmat qpp::sinm ( const Eigen::MatrixBase< Derived > & A )`

Matrix sin.



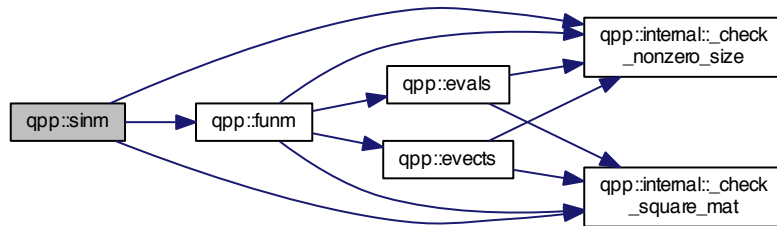
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Matrix sine of  $A$

Here is the call graph for this function:



6.1.2.101 `template<typename Derived> cmat qpp::spectralpowm ( const Eigen::MatrixBase< Derived> & A, const cplx z )`

Matrix power.

Uses the spectral decomposition of  $A$  to compute the matrix power

By convention  $A^0 = I$

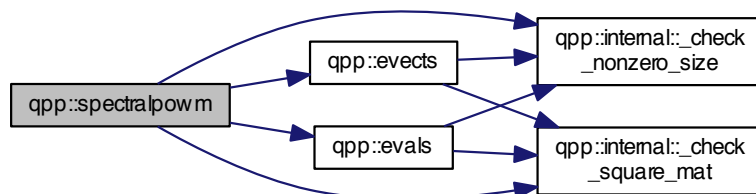
## Parameters

$A$	Eigen expression
$z$	Complex number

## Returns

Matrix power  $A^z$

Here is the call graph for this function:



6.1.2.102 `template<typename Derived> cmat qpp::sqrtm ( const Eigen::MatrixBase< Derived> & A )`

Matrix square root.

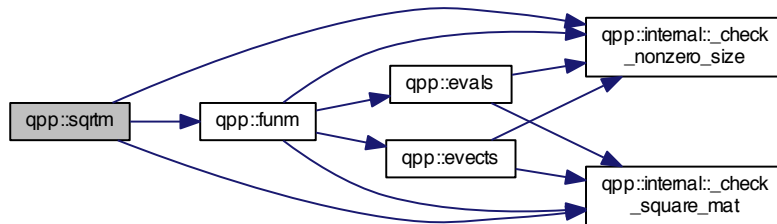
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Matrix square root of  $A$

Here is the call graph for this function:



6.1.2.103 `template<typename Derived > Derived::Scalar qpp::sum ( const Eigen::MatrixBase< Derived > & A )`

Element-wise sum of  $A$ .

## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Element-wise sum of  $A$ , as a scalar in the same scalar field as  $A$

Here is the call graph for this function:



6.1.2.104 `template<typename InputIterator > auto qpp::sum ( InputIterator first, InputIterator last ) -> typename InputIterator::value_type`

Element-wise sum of a range.

## Parameters

<i>first</i>	Iterator to the first element of the range
<i>last</i>	Iterator to the last element of the range

## Returns

Element-wise sum of the range, as a scalar in the same scalar field as the range

6.1.2.105 `cmat qpp::super ( const std::vector< cmat > & Ks )`

Superoperator matrix representation.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators  $K_s$  in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

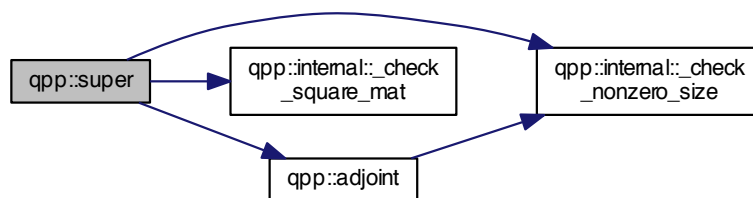
## Parameters

$K_s$	Set of Kraus operators
-------	------------------------

## Returns

Superoperator matrix representation

Here is the call graph for this function:

6.1.2.106 `template<typename Derived > DynMat<typename Derived::Scalar> qpp::syspermute ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size_t > & perm, const std::vector< std::size_t > & dims )`

System permutation.

Permutes the subsystems in a state vector or density matrix

The qubit  $perm[i]$  is permuted to the location  $i$

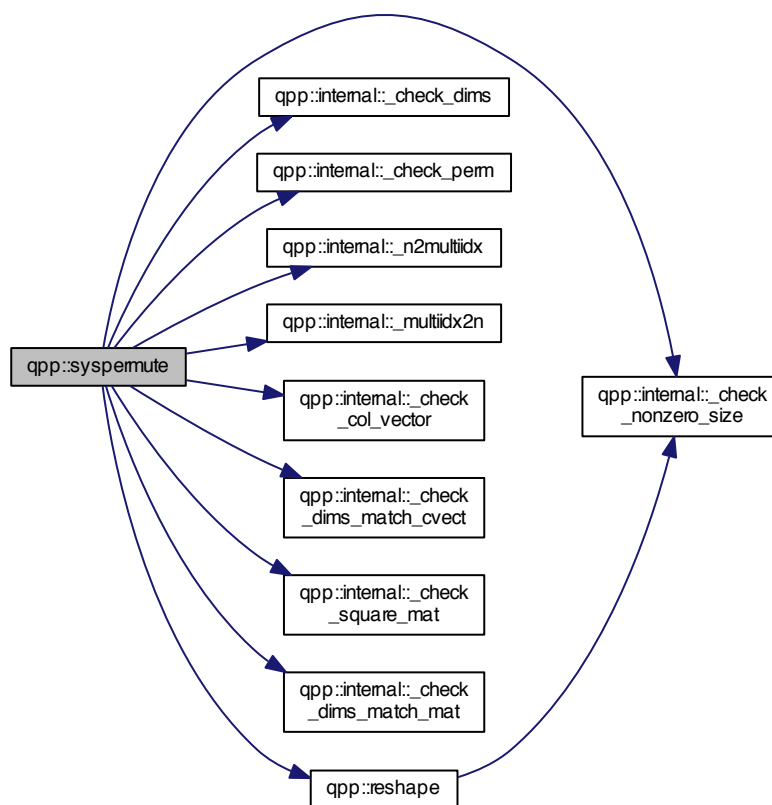
## Parameters

$A$	Eigen expression
$perm$	Permutation
$dims$	Subsystems' dimensions

## Returns

Permuted system, as a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:



6.1.2.107 `template<typename Derived > Derived::Scalar qpp::trace ( const Eigen::MatrixBase< Derived > & A )`

Trace.

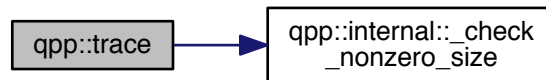
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Trace of  $A$ , as a scalar in the same scalar field as  $A$

Here is the call graph for this function:



6.1.2.108 `template<typename Derived > DynMat<typename Derived::Scalar> qpp::transpose ( const Eigen::MatrixBase<Derived > & A )`

Transpose.

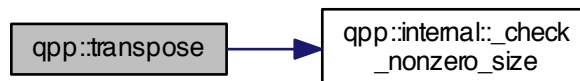
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Transpose of  $A$ , as a dynamic matrix over the same scalar field as  $A$

Here is the call graph for this function:



6.1.2.109 `template<typename Derived > double qpp::tsallis ( const double  $\alpha$ , const Eigen::MatrixBase<Derived > & A )`

Tsallis-  $\alpha$  entropy of the probability distribution/density matrix  $A$ , for  $\alpha \geq 0$

.

When  $\alpha \rightarrow 1$  the Tsallis entropy converges to the Shannon/von-Neumann entropy, with the logarithm in base  $e$

## Parameters

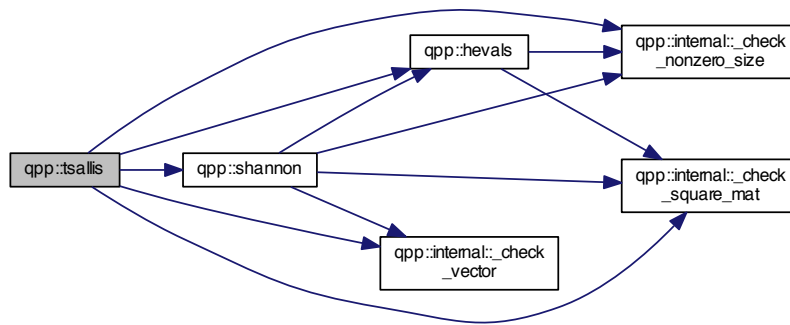
$\alpha$	Non-negative real number
----------	--------------------------

A	Eigen expression, representing a probability distribution (real dynamic column vector) or a density matrix (complex dynamic matrix)
---	---

### Returns

Renyi-  $\alpha$  entropy, with the logarithm in base 2

Here is the call graph for this function:



## 6.1.3 Variable Documentation

### 6.1.3.1 constexpr double qpp::chop = 1e-10

Used in [qpp::disp\(\)](#) and [qpp::displn\(\)](#) for setting to zero numbers that have their absolute value smaller than  $qpp::ct::chop$ .

### 6.1.3.2 constexpr double qpp::ee = 2.718281828459045235360287471352662497

Base of natural logarithm,  $e$ .

### 6.1.3.3 constexpr double qpp::eps = 1e-12

Used to decide whether a number or expression in double precision is zero or not.

Example:

```
if(std::abs(x) < qpp::eps) // x is zero
```

### 6.1.3.4 const Gates& qpp::gt = Gates::get\_instance()

[qpp::Gates](#) const Singleton

Initializes the gates, see the class [qpp::Gates](#)

### 6.1.3.5 const Init& qpp::init = Init::get\_instance()

[qpp::Init](#) const Singleton

Additional initializations/cleanups

## 6.1.3.6 constexpr std::size\_t qpp::maxn = 64

Maximum number of qubits.

Used internally to statically allocate arrays (for speed reasons)

## 6.1.3.7 constexpr double qpp::pi = 3.141592653589793238462643383279502884

$\pi$

## 6.1.3.8 RandomDevices&amp; qpp::rdevs = RandomDevices::get\_instance()

[qpp::RandomDevices](#) Singleton

Initializes the random devices, see the class [qpp::RandomDevices](#)

## 6.1.3.9 const States&amp; qpp::st = States::get\_instance()

[qpp::States](#) const Singleton

Initializes the states, see the class [qpp::States](#)

## 6.2 qpp::internal Namespace Reference

### Classes

- class [Singleton](#)  
*[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)*

### Functions

- void [\\_n2multiidx](#) (std::size\_t n, std::size\_t numdims, const std::size\_t \*dims, std::size\_t \*result)
- std::size\_t [\\_multiidx2n](#) (const std::size\_t \*midx, std::size\_t numdims, const std::size\_t \*dims)
- template<typename Derived >  
 bool [\\_check\\_square\\_mat](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
 bool [\\_check\\_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
 bool [\\_check\\_row\\_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
 bool [\\_check\\_col\\_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename T >  
 bool [\\_check\\_nonzero\\_size](#) (const T &x)
- bool [\\_check\\_dims](#) (const std::vector< std::size\_t > &dims)
- template<typename Derived >  
 bool [\\_check\\_dims\\_match\\_mat](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
 bool [\\_check\\_dims\\_match\\_cvect](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &V)
- template<typename Derived >  
 bool [\\_check\\_dims\\_match\\_rvect](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &V)

- `bool _check_eq_dims` (const std::vector< std::size\_t > &dims, std::size\_t dim)
- `bool _check_subsys_match_dims` (const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- `bool _check_perm` (const std::vector< std::size\_t > &perm)
- `template<typename Derived1 , typename Derived2 >`  
`DynMat< typename Derived1::Scalar > _kron2` (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- `template<typename T >`  
`void variadic_vector_emplace` (std::vector< T > &)
- `template<typename T , typename First , typename... Args>`  
`void variadic_vector_emplace` (std::vector< T > &v, First &&first, Args &&...args)

### 6.2.1 Detailed Description

Internal implementation details, do not modify/use the functions/classes unless you know what you are doing

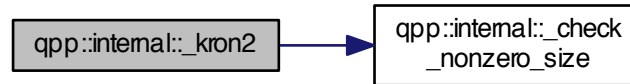
### 6.2.2 Function Documentation

- 6.2.2.1 `template<typename Derived > bool qpp::internal::_check_col_vector ( const Eigen::MatrixBase< Derived > & A )`
- 6.2.2.2 `bool qpp::internal::_check_dims ( const std::vector< std::size_t > & dims )`
- 6.2.2.3 `template<typename Derived > bool qpp::internal::_check_dims_match_cvect ( const std::vector< std::size_t > & dims, const Eigen::MatrixBase< Derived > & V )`
- 6.2.2.4 `template<typename Derived > bool qpp::internal::_check_dims_match_mat ( const std::vector< std::size_t > & dims, const Eigen::MatrixBase< Derived > & A )`
- 6.2.2.5 `template<typename Derived > bool qpp::internal::_check_dims_match_rvect ( const std::vector< std::size_t > & dims, const Eigen::MatrixBase< Derived > & V )`
- 6.2.2.6 `bool qpp::internal::_check_eq_dims ( const std::vector< std::size_t > & dims, std::size_t dim )`
- 6.2.2.7 `template<typename T > bool qpp::internal::_check_nonzero_size ( const T & x )`
- 6.2.2.8 `bool qpp::internal::_check_perm ( const std::vector< std::size_t > & perm )`
- 6.2.2.9 `template<typename Derived > bool qpp::internal::_check_row_vector ( const Eigen::MatrixBase< Derived > & A )`
- 6.2.2.10 `template<typename Derived > bool qpp::internal::_check_square_mat ( const Eigen::MatrixBase< Derived > & A )`
- 6.2.2.11 `bool qpp::internal::_check_subsys_match_dims ( const std::vector< std::size_t > & subsys, const std::vector< std::size_t > & dims )`
- 6.2.2.12 `template<typename Derived > bool qpp::internal::_check_vector ( const Eigen::MatrixBase< Derived > & A )`



6.2.2.13 `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::internal::_kron2 ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )`

Here is the call graph for this function:



6.2.2.14 `std::size_t qpp::internal::_multiidx2n ( const std::size_t * midx, std::size_t numdims, const std::size_t * dims )`  
[inline]

6.2.2.15 `void qpp::internal::_n2multiidx ( std::size_t n, std::size_t numdims, const std::size_t * dims, std::size_t * result )`  
[inline]

6.2.2.16 `template<typename T > void qpp::internal::variadic_vector_emplace ( std::vector< T > & )`

6.2.2.17 `template<typename T , typename First , typename... Args> void qpp::internal::variadic_vector_emplace ( std::vector< T > & v, First && first, Args &&... args )`

Here is the call graph for this function:



## 6.3 qpp::obsolete Namespace Reference

### Functions

- `template<typename Derived1 , typename Derived2 > DynMat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`  
*Applies the gate A to the part subsys of a multipartite state vector or density matrix.*
- `template<typename Derived > cmat channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`  
*Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.*

- `cmat super` (const std::vector< `cmat` > &Ks)

*Superoperator matrix representation.*

### 6.3.1 Function Documentation

6.3.1.1 `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::obsolete::apply`  
`( const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector<`  
`std::size_t > & subsys, const std::vector< std::size_t > & dims )`

Applies the gate *A* to the part *subsys* of a multipartite state vector or density matrix.

#### Note

The dimension of the gate *A* must match the dimension of *subsys*

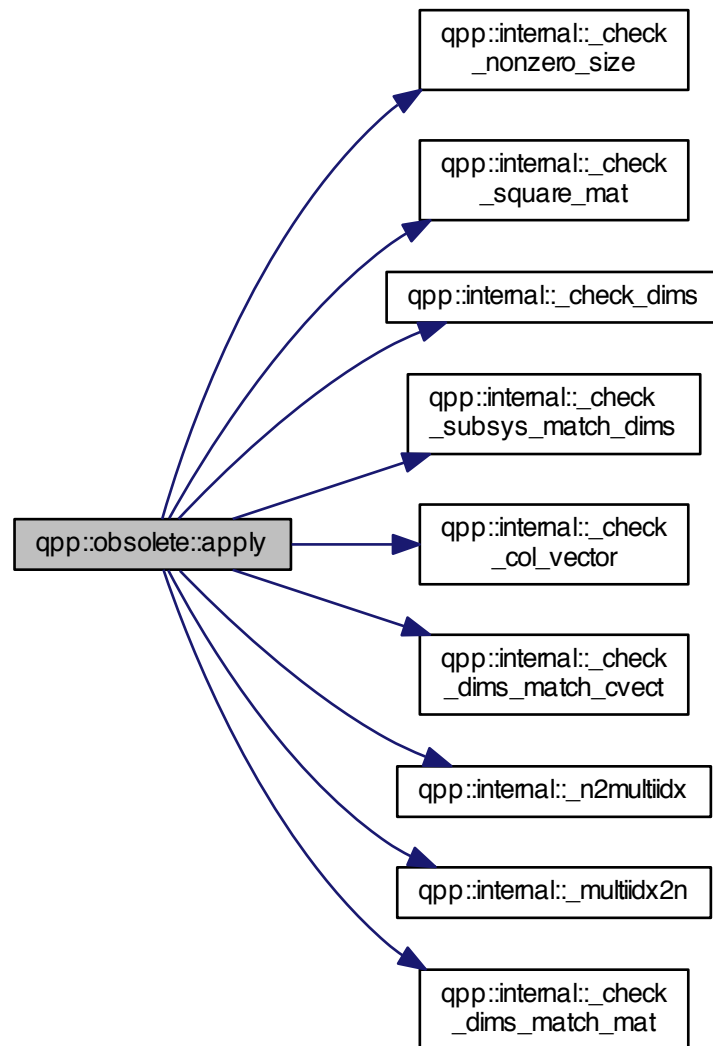
#### Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>dims</i>	Local dimensions of all local Hilbert spaces (can be different)

#### Returns

Gate *A* applied to the part *subsys* of *state*

Here is the call graph for this function:



**6.3.1.2** `template<typename Derived > cmat qpp::obsolete::channel ( const Eigen::MatrixBase< Derived > & rho, const std::vector< cmat > & Ks, const std::vector< std::size_t > & subsys, const std::vector< std::size_t > & dims )`

Applies the channel specified by the set of Kraus operators *Ks* to the part of the density matrix *rho* specified by *subsys*.

Parameters

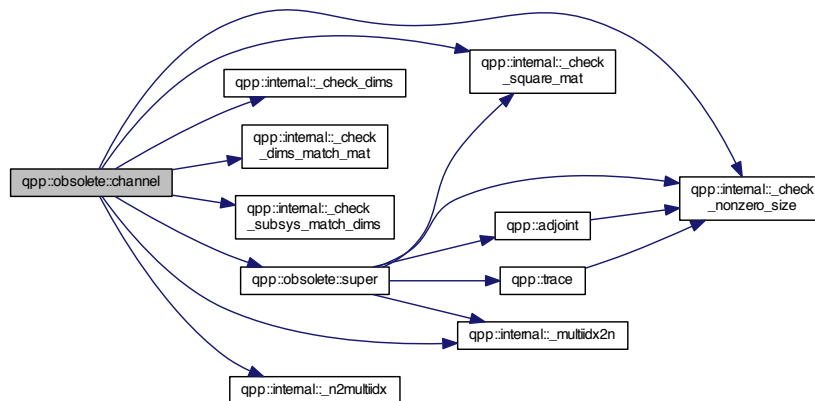
<i>rho</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators

<i>subsys</i>	Subsystems' indexes
<i>dims</i>	Local dimensions of all local Hilbert spaces (can be different)

### Returns

Output density matrix after the action of the channel

Here is the call graph for this function:



### 6.3.1.3 cmat qpp::obsolete::super ( const std::vector< cmat > & Ks )

Superoperator matrix representation.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators  $K_s$  in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

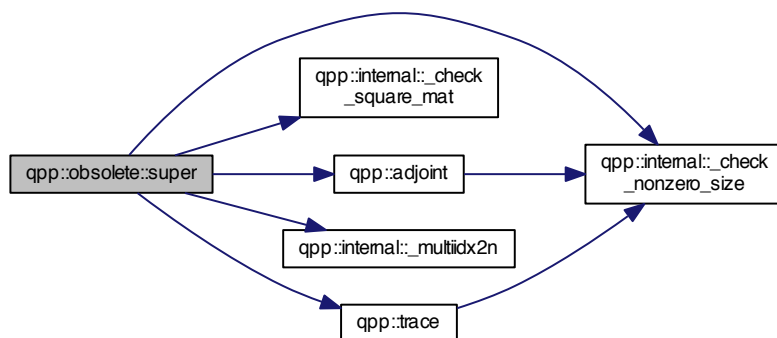
### Parameters

$K_s$	Set of Kraus operators
-------	------------------------

## Returns

Superoperator matrix representation

Here is the call graph for this function:





## Chapter 7

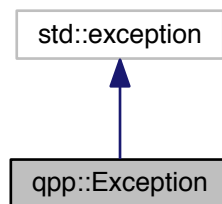
# Class Documentation

### 7.1 qpp::Exception Class Reference

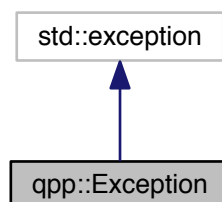
Generates custom exceptions, used when validating function parameters.

```
#include <exception.h>
```

Inheritance diagram for qpp::Exception:



Collaboration diagram for qpp::Exception:



## Public Types

- enum [Type](#) {  
[Type::UNKNOWN\\_EXCEPTION](#) = 1, [Type::ZERO\\_SIZE](#), [Type::MATRIX\\_NOT\\_SQUARE](#), [Type::MATRIX\\_NOT\\_CVECTOR](#),  
[Type::MATRIX\\_NOT\\_RVECTOR](#), [Type::MATRIX\\_NOT\\_VECTOR](#), [Type::MATRIX\\_NOT\\_SQUARE\\_OR\\_CVECTOR](#), [Type::MATRIX\\_NOT\\_SQUARE\\_OR\\_RVECTOR](#),  
[Type::MATRIX\\_NOT\\_SQUARE\\_OR\\_VECTOR](#), [Type::DIMS\\_INVALID](#), [Type::DIMS\\_NOT\\_EQUAL](#), [Type::DIMS\\_MISMATCH\\_MATRIX](#),  
[Type::DIMS\\_MISMATCH\\_CVECTOR](#), [Type::DIMS\\_MISMATCH\\_RVECTOR](#), [Type::DIMS\\_MISMATCH\\_VECTOR](#), [Type::SUBSYS\\_MISMATCH\\_DIMS](#),  
[Type::PERM\\_INVALID](#), [Type::NOT\\_QUBIT\\_GATE](#), [Type::NOT\\_QUBIT\\_SUBSYS](#), [Type::NOT\\_BIPARTITE](#),  
[Type::OUT\\_OF\\_RANGE](#), [Type::TYPE\\_MISMATCH](#), [Type::UNDEFINED\\_TYPE](#), [Type::CUSTOM\\_EXCEPTION](#) }

*Exception types, add more exceptions here if needed.*

## Public Member Functions

- [Exception](#) (const std::string &where, const [Type](#) &type)  
*Constructs an exception.*
- [Exception](#) (const std::string &where, const std::string &custom)  
*Constructs an exception.*
- virtual const char \* [what](#) () const noexcept override  
*Overrides std::exception::what()*

## Private Member Functions

- std::string [\\_construct\\_exception\\_msg](#) ()  
*Constructs the exception's description from its type.*

## Private Attributes

- std::string [\\_where](#)
- std::string [\\_msg](#)
- [Type](#) [\\_type](#)
- std::string [\\_custom](#)

### 7.1.1 Detailed Description

Generates custom exceptions, used when validating function parameters.

Customize this class if more exceptions are needed

### 7.1.2 Member Enumeration Documentation

#### 7.1.2.1 enum `qpp::Exception::Type` `[strong]`

[Exception](#) types, add more exceptions here if needed.



See also

qpp::Exception:: [\\_construct\\_exception\\_msg\(\)](#)

Enumerator

**UNKNOWN\_EXCEPTION** UNKNOWN\_EXCEPTION. Unknown exception

**ZERO\_SIZE** ZERO\_SIZE. Zero sized object, e.g. empty Eigen::Matrix or std::vector with no elements

**MATRIX\_NOT\_SQUARE** MATRIX\_NOT\_SQUARE. Eigen::Matrix is not square

**MATRIX\_NOT\_CVECTOR** MATRIX\_NOT\_CVECTOR. Eigen::Matrix is not a column vector

**MATRIX\_NOT\_RVECTOR** MATRIX\_NOT\_RVECTOR. Eigen::Matrix is not a row vector

**MATRIX\_NOT\_VECTOR** MATRIX\_NOT\_VECTOR. Eigen::Matrix is not a row/column vector

**MATRIX\_NOT\_SQUARE\_OR\_CVECTOR** MATRIX\_NOT\_SQUARE\_OR\_CVECTOR. Eigen::Matrix is not square nor a column vector

**MATRIX\_NOT\_SQUARE\_OR\_RVECTOR** MATRIX\_NOT\_SQUARE\_OR\_RVECTOR. Eigen::Matrix is not square nor a row vector

**MATRIX\_NOT\_SQUARE\_OR\_VECTOR** MATRIX\_NOT\_SQUARE\_OR\_VECTOR. Eigen::Matrix is not square nor a row/column vector

**DIMS\_INVALID** DIMS\_INVALID. std::vector<std::size\_t> representing the dimensions has zero size or contains zeros

**DIMS\_NOT\_EQUAL** DIMS\_NOT\_EQUAL. std::vector<std::size\_t> representing the dimensions contains non-equal elements

**DIMS\_MISMATCH\_MATRIX** DIMS\_MISMATCH\_MATRIX. Product of the dimensions' std::vector<std::size\_t> is not equal to the number of rows of Eigen::Matrix (assumed to be square)

**DIMS\_MISMATCH\_CVECTOR** DIMS\_MISMATCH\_CVECTOR. Product of the dimensions' std::vector<std::size\_t> is not equal to the number of cols of Eigen::Matrix (assumed to be a column vector)

**DIMS\_MISMATCH\_RVECTOR** DIMS\_MISMATCH\_RVECTOR. Product of the dimensions' std::vector<std::size\_t> is not equal to the number of cols of Eigen::Matrix (assumed to be a row vector)

**DIMS\_MISMATCH\_VECTOR** DIMS\_MISMATCH\_VECTOR. Product of the dimensions' std::vector<std::size\_t> is not equal to the number of cols of Eigen::Matrix (assumed to be a row/column vector)

**SUBSYS\_MISMATCH\_DIMS** SUBSYS\_MISMATCH\_DIMS. std::vector<std::size\_t> representing the subsystems' labels has duplicates, or has entries that are larger than the size of the std::vector<std::size\_t> representing the dimensions

**PERM\_INVALID** PERM\_INVALID. Invalid std::vector<std::size\_t> permutation

**NOT\_QUBIT\_GATE** NOT\_QUBIT\_GATE. Eigen::Matrix is not 2 x 2

**NOT\_QUBIT\_SUBSYS** NOT\_QUBIT\_SUBSYS. Subsystems are not 2-dimensional

**NOT\_BIPARTITE** NOT\_BIPARTITE. std::vector<std::size\_t> representing the dimensions has size different from 2

**OUT\_OF\_RANGE** OUT\_OF\_RANGE. Parameter out of range

**TYPE\_MISMATCH** TYPE\_MISMATCH. Types do not match (i.e. Matrix<double> vs Matrix<cp1x>)

**UNDEFINED\_TYPE** UNDEFINED\_TYPE. Templated function not defined for this type

**CUSTOM\_EXCEPTION** CUSTOM\_EXCEPTION. Custom exception, user must provide a custom message

### 7.1.3 Constructor & Destructor Documentation

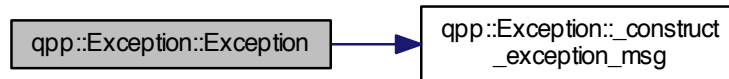
7.1.3.1 qpp::Exception::Exception ( const std::string & *where*, const Type & *type* ) [inline]

Constructs an exception.

## Parameters

<i>where</i>	Text representing where the exception occurred
<i>type</i>	<a href="#">Exception</a> 's type, see the strong enumeration <code>qpp::Exception::TYPE</code>

Here is the call graph for this function:



### 7.1.3.2 `qpp::Exception::Exception ( const std::string & where, const std::string & custom ) [inline]`

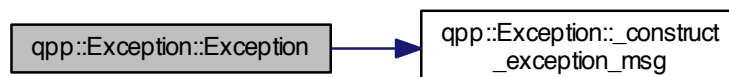
Constructs an exception.

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

## Parameters

<i>where</i>	Text representing where the exception occurred
<i>custom</i>	<a href="#">Exception</a> 's description

Here is the call graph for this function:



## 7.1.4 Member Function Documentation

### 7.1.4.1 `std::string qpp::Exception::_construct_exception_msg ( ) [inline], [private]`

Constructs the exception's description from its type.

Must modify the code of this function if more exceptions are added

## Returns

[Exception](#)'s description

### 7.1.4.2 `virtual const char* qpp::Exception::what ( ) const [inline], [override], [virtual], [noexcept]`

Overrides `std::exception::what()`

Returns

[Exception](#)'s description

### 7.1.5 Member Data Documentation

7.1.5.1 `std::string qpp::Exception::_custom` [private]

7.1.5.2 `std::string qpp::Exception::_msg` [private]

7.1.5.3 `Type qpp::Exception::_type` [private]

7.1.5.4 `std::string qpp::Exception::_where` [private]

The documentation for this class was generated from the following file:

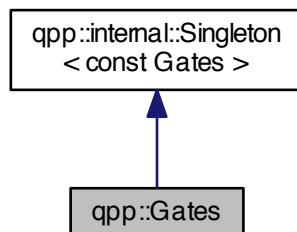
- `include/classes/exception.h`

## 7.2 qpp::Gates Class Reference

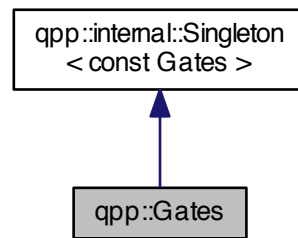
const Singleton class that implements most commonly used gates

```
#include <gates.h>
```

Inheritance diagram for qpp::Gates:



Collaboration diagram for `qpp::Gates`:



## Public Member Functions

- `cmat Rn` (double theta, `std::vector< double > n`) const  
*Rotation of theta about the 3-dimensional real unit vector n.*
- `cmat Zd` (`std::size_t D`) const  
*Generalized Z gate for qudits.*
- `cmat Fd` (`std::size_t D`) const  
*Fourier transform gate for qudits.*
- `cmat Xd` (`std::size_t D`) const  
*Generalized X gate for qudits.*
- `template<typename Derived = Eigen::MatrixXcd>`  
`Derived Id` (`std::size_t D`) const  
*Identity gate.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > CTRL` (const `Eigen::MatrixBase< Derived > &A`, const `std::vector< std::size_t > &ctrl`, const `std::vector< std::size_t > &subsys`, `std::size_t n`, `std::size_t d=2`) const  
*Generates the multipartite multiple-controlled-A gate in matrix form.*

## Public Attributes

- `cmat Id2` { `cmat::Identity(2, 2)` }  
*Identity gate.*
- `cmat H` { `cmat::Zero(2, 2)` }  
*Hadamard gate.*
- `cmat X` { `cmat::Zero(2, 2)` }  
*Pauli Sigma-X gate.*
- `cmat Y` { `cmat::Zero(2, 2)` }  
*Pauli Sigma-Y gate.*
- `cmat Z` { `cmat::Zero(2, 2)` }  
*Pauli Sigma-Z gate.*
- `cmat S` { `cmat::Zero(2, 2)` }  
*S gate.*
- `cmat T` { `cmat::Zero(2, 2)` }  
*T gate.*
- `cmat CNOTab` { `cmat::Identity(4, 4)` }

- Controlled-NOT control target gate.*
- [cmat CZ](#) { cmat::Identity(4, 4) }
- Controlled-Phase gate.*
- [cmat CNOTba](#) { cmat::Zero(4, 4) }
- Controlled-NOT target control gate.*
- [cmat SWAP](#) { cmat::Identity(4, 4) }
- SWAP gate.*
- [cmat TOF](#) { cmat::Identity(8, 8) }
- Toffoli gate.*
- [cmat FRED](#) { cmat::Identity(8, 8) }
- Fredkin gate.*

## Private Member Functions

- [Gates](#) ()  
*Initializes the gates.*

## Friends

- class [internal::Singleton](#)< [const Gates](#) >

## Additional Inherited Members

### 7.2.1 Detailed Description

const Singleton class that implements most commonly used gates

### 7.2.2 Constructor & Destructor Documentation

#### 7.2.2.1 qpp::Gates::Gates ( ) [inline], [private]

Initializes the gates.

### 7.2.3 Member Function Documentation

#### 7.2.3.1 template<typename Derived> DynMat<typename Derived::Scalar> qpp::Gates::CTRL ( const Eigen::MatrixBase<Derived> & A, const std::vector< std::size\_t> & ctrl, const std::vector< std::size\_t> & subsys, std::size\_t n, std::size\_t d = 2 ) const [inline]

Generates the multipartite multiple-controlled-A gate in matrix form.

#### Note

The dimension of the gate *A* must match the dimension of *subsys*

#### Parameters

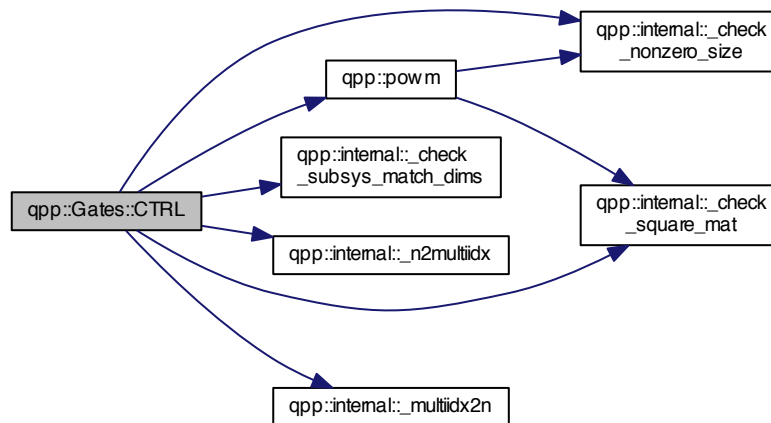
<i>A</i>	Eigen expression
----------	------------------

<i>ctrl</i>	Control subsystem indexes
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>n</i>	Total number of subsystems
<i>d</i>	Local dimensions of all local Hilbert spaces (must all be equal)

**Returns**

CTRL-A gate, as a matrix over the same scalar field as *A*

Here is the call graph for this function:



### 7.2.3.2 `cmat qpp::Gates::Fd ( std::size_t D ) const [inline]`

Fourier transform gate for qudits.

**Note**

Defined as  $F = \sum_{jk} \exp(2\pi i jk/D) |j\rangle\langle k|$

**Parameters**

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

**Returns**

Fourier transform gate for qudits

Here is the call graph for this function:



7.2.3.3 `template<typename Derived = Eigen::MatrixXcd> Derived qpp::Gates::Id ( std::size_t D ) const` `[inline]`

Identity gate.

Note

Can change the return type from complex matrix (default) by explicitly specifying the template parameter

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Identity gate

7.2.3.4 `cmat qpp::Gates::Rn ( double theta, std::vector< double > n ) const` `[inline]`

Rotation of *theta* about the 3-dimensional real unit vector *n*.

Parameters

<i>theta</i>	Rotation angle
<i>n</i>	3-dimensional real unit vector

Returns

Rotation gate

7.2.3.5 `cmat qpp::Gates::Xd ( std::size_t D ) const` `[inline]`

Generalized X gate for qudits.

Note

Defined as  $X = \sum_j |j \oplus 1\rangle \langle j|$

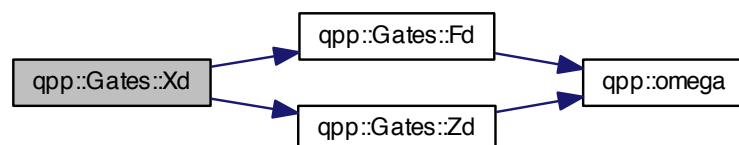
Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Generalized X gate for qudits

Here is the call graph for this function:



### 7.2.3.6 `cmat qpp::Gates::Zd ( std::size_t D ) const [inline]`

Generalized Z gate for qudits.

#### Note

Defined as  $Z = \sum_j \exp(2\pi i j/D) |j\rangle\langle j|$

#### Parameters

$D$	Dimension of the Hilbert space
-----	--------------------------------

#### Returns

Generalized Z gate for qudits

Here is the call graph for this function:



## 7.2.4 Friends And Related Function Documentation

### 7.2.4.1 `friend class internal::Singleton< const Gates > [friend]`

## 7.2.5 Member Data Documentation

### 7.2.5.1 `cmat qpp::Gates::CNOTab { cmat::Identity(4, 4) }`

Controlled-NOT control target gate.

### 7.2.5.2 `cmat qpp::Gates::CNOTba { cmat::Zero(4, 4) }`

Controlled-NOT target control gate.

### 7.2.5.3 `cmat qpp::Gates::CZ { cmat::Identity(4, 4) }`

Controlled-Phase gate.

### 7.2.5.4 `cmat qpp::Gates::FRED { cmat::Identity(8, 8) }`

Fredkin gate.

### 7.2.5.5 `cmat qpp::Gates::H { cmat::Zero(2, 2) }`

Hadamard gate.



7.2.5.6 `cmat qpp::Gates::Id2 { cmat::Identity(2, 2) }`

Identity gate.

7.2.5.7 `cmat qpp::Gates::S { cmat::Zero(2, 2) }`

S gate.

7.2.5.8 `cmat qpp::Gates::SWAP { cmat::Identity(4, 4) }`

SWAP gate.

7.2.5.9 `cmat qpp::Gates::T { cmat::Zero(2, 2) }`

T gate.

7.2.5.10 `cmat qpp::Gates::TOF { cmat::Identity(8, 8) }`

Toffoli gate.

7.2.5.11 `cmat qpp::Gates::X { cmat::Zero(2, 2) }`

Pauli Sigma-X gate.

7.2.5.12 `cmat qpp::Gates::Y { cmat::Zero(2, 2) }`

Pauli Sigma-Y gate.

7.2.5.13 `cmat qpp::Gates::Z { cmat::Zero(2, 2) }`

Pauli Sigma-Z gate.

The documentation for this class was generated from the following file:

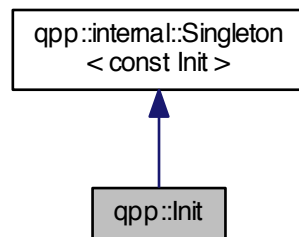
- [include/classes/gates.h](#)

## 7.3 qpp::Init Class Reference

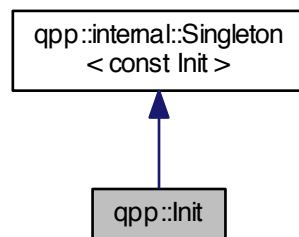
const Singleton class that performs additional initializations/cleanups

```
#include <init.h>
```

Inheritance diagram for `qpp::Init`:



Collaboration diagram for `qpp::Init`:



## Public Member Functions

- [Init \(\)](#)  
*Additional initializations.*

## Private Member Functions

- [~Init \(\)](#)  
*Cleanups.*

## Friends

- class [internal::Singleton<const Init>](#)

## Additional Inherited Members

### 7.3.1 Detailed Description

const Singleton class that performs additional initializations/cleanups

### 7.3.2 Constructor & Destructor Documentation

#### 7.3.2.1 qpp::Init::Init ( ) [inline]

Additional initializations.

#### 7.3.2.2 qpp::Init::~~Init ( ) [inline],[private]

Cleanups.

### 7.3.3 Friends And Related Function Documentation

#### 7.3.3.1 friend class internal::Singleton< const Init > [friend]

The documentation for this class was generated from the following file:

- include/classes/[init.h](#)

## 7.4 qpp::Qudit Class Reference

```
#include <qudit.h>
```

### Public Member Functions

- [Qudit](#) (const [cmat](#) &rho=[States::get\\_instance\(\)](#).pz0)
- std::size\_t [measure](#) (const [cmat](#) &U, bool destructive=false)
- std::size\_t [measure](#) (bool destructive=false)
- [cmat](#) [getRho](#) () const
- std::size\_t [getD](#) () const

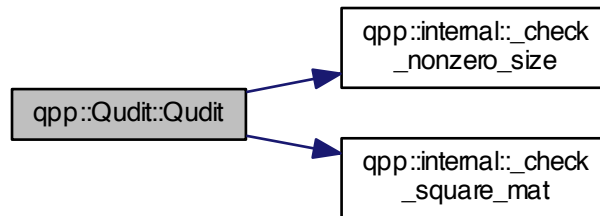
### Private Attributes

- [cmat\\_rho](#)
- std::size\_t [\\_D](#)

### 7.4.1 Constructor & Destructor Documentation

#### 7.4.1.1 `qpp::Qudit::Qudit ( const cmat & rho = States::get_instance() .pz0 ) [inline]`

Here is the call graph for this function:



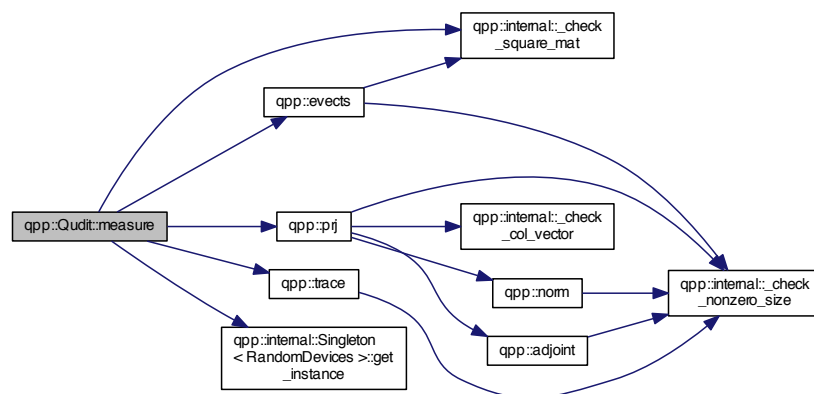
### 7.4.2 Member Function Documentation

#### 7.4.2.1 `std::size_t qpp::Qudit::getD ( ) const [inline]`

#### 7.4.2.2 `cmat qpp::Qudit::getRho ( ) const [inline]`

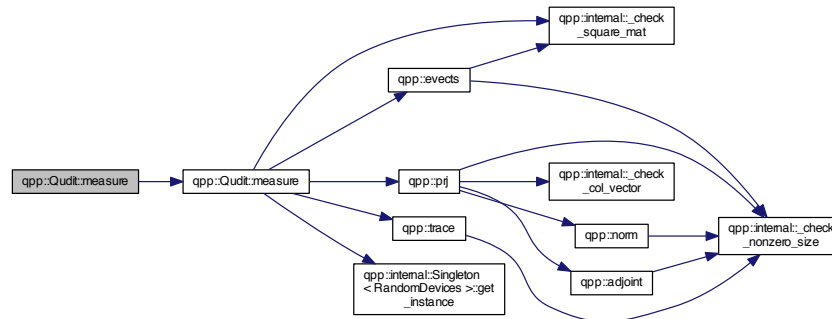
#### 7.4.2.3 `std::size_t qpp::Qudit::measure ( const cmat & U, bool destructive = false ) [inline]`

Here is the call graph for this function:



7.4.2.4 `std::size_t qpp::Qudit::measure ( bool destructive = false ) [inline]`

Here is the call graph for this function:



### 7.4.3 Member Data Documentation

7.4.3.1 `std::size_t qpp::Qudit::_D [private]`

7.4.3.2 `cmat qpp::Qudit::_rho [private]`

The documentation for this class was generated from the following file:

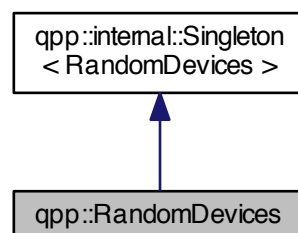
- [include/classes/qudit.h](#)

## 7.5 qpp::RandomDevices Class Reference

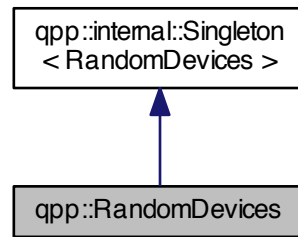
Singleton class that manages the source of randomness in the library.

```
#include <randevs.h>
```

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



## Public Attributes

- `std::mt19937 _rng`  
*Mersenne twister random number generator engine.*

## Private Member Functions

- `RandomDevices ()`  
*Initializes and seeds the random number generators.*

## Private Attributes

- `std::random_device _rd`  
*used to seed std::mt19937 \_rng*

## Friends

- class `internal::Singleton< RandomDevices >`

## Additional Inherited Members

### 7.5.1 Detailed Description

Singleton class that manages the source of randomness in the library.

It consists of a wrapper around an `std::mt19937` Mersenne twister random number generator engine and an `std::random_device` engine. The latter is used to seed the Mersenne twister. The class also seeds the standard `std::srand` C number generator, as it is used by Eigen.

### 7.5.2 Constructor & Destructor Documentation

#### 7.5.2.1 `qpp::RandomDevices::RandomDevices ( )` `[inline]`, `[private]`

Initializes and seeds the random number generators.

### 7.5.3 Friends And Related Function Documentation

7.5.3.1 friend class internal::Singleton< RandomDevices > [friend]

### 7.5.4 Member Data Documentation

7.5.4.1 std::random\_device qpp::RandomDevices::\_rd [private]

used to seed std::mt19937 \_rng

7.5.4.2 std::mt19937 qpp::RandomDevices::\_rng

Mersenne twister random number generator engine.

The documentation for this class was generated from the following file:

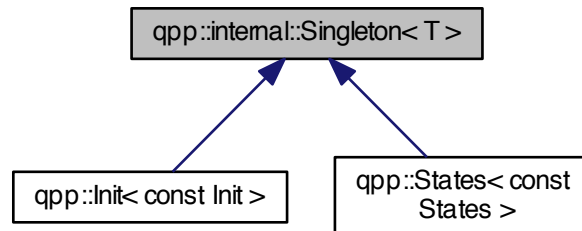
- include/classes/[randevs.h](#)

## 7.6 qpp::internal::Singleton< T > Class Template Reference

[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

```
#include <singleton.h>
```

Inheritance diagram for qpp::internal::Singleton< T >:



### Static Public Member Functions

- static T & [get\\_instance](#) ()

### Protected Member Functions

- [Singleton](#) ()=default
- virtual [~Singleton](#) ()
- [Singleton](#) (const [Singleton](#) &)=delete
- [Singleton](#) & [operator=](#) (const [Singleton](#) &)=delete

### 7.6.1 Detailed Description

`template<typename T>class qpp::internal::Singleton< T >`

[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

To implement a singleton, derive your class from [qpp::internal::Singleton](#), make [qpp::internal::Singleton](#) a friend of your class, then declare the constructor of your class as private. To get an instance, use the static member function [qpp::internal::Singleton::get\\_instance\(\)](#), which returns a reference to your newly created singleton (thread-safe in C++11).

Example:

```
class MySingleton: public qpp::internal::Singleton<MySingleton>
{
    friend class qpp::internal::Singleton<MySingleton>;
public:
    // Declare all public members here
private:
    MySingleton()
    {
        // Implement the constructor here
    }
};

MySingleton& mySingleton = MySingleton::get_instance(); // Get an instance
```

See also

Code of [qpp::Gates](#), [qpp::RandomDevices](#), [qpp::States](#) or [qpp.h](#) for real world examples of usage.

### 7.6.2 Constructor & Destructor Documentation

7.6.2.1 `template<typename T> qpp::internal::Singleton< T >::Singleton ( )` [protected],[default]

7.6.2.2 `template<typename T> virtual qpp::internal::Singleton< T >::~~Singleton ( )` [inline],[protected],[virtual]

7.6.2.3 `template<typename T> qpp::internal::Singleton< T >::Singleton ( const Singleton< T > & )` [protected],[delete]

### 7.6.3 Member Function Documentation

7.6.3.1 `template<typename T> static T& qpp::internal::Singleton< T >::get_instance ( )` [inline],[static]

7.6.3.2 `template<typename T> Singleton& qpp::internal::Singleton< T >::operator= ( const Singleton< T > & )` [protected],[delete]

The documentation for this class was generated from the following file:

- [include/classes/singleton.h](#)

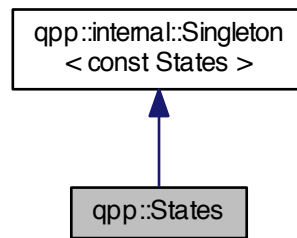
## 7.7 qpp::States Class Reference

const Singleton class that implements most commonly used states

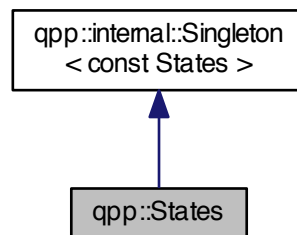
```
#include <states.h>
```



Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



## Public Attributes

- **ket x0** { ket::Zero(2) }  
*Pauli Sigma-X 0-eigenstate  $|+\rangle$*
- **ket x1** { ket::Zero(2) }  
*Pauli Sigma-X 1-eigenstate  $|-\rangle$*
- **ket y0** { ket::Zero(2) }  
*Pauli Sigma-Y 0-eigenstate.*
- **ket y1** { ket::Zero(2) }  
*Pauli Sigma-Y 1-eigenstate.*
- **ket z0** { ket::Zero(2) }  
*Pauli Sigma-Z 0-eigenstate  $|0\rangle$*
- **ket z1** { ket::Zero(2) }  
*Pauli Sigma-Z 1-eigenstate  $|1\rangle$*
- **cmat px0** { cmat::Zero(2, 2) }  
*Projector onto the Pauli Sigma-X 0-eigenstate  $|+\rangle\langle+|$ .*
- **cmat px1** { cmat::Zero(2, 2) }  
*Projector onto the Pauli Sigma-X 1-eigenstate  $|-\rangle\langle-|$ .*
- **cmat py0** { cmat::Zero(2, 2) }

- Projector onto the Pauli Sigma-Y 0-eigenstate.*
- [cmat py1](#) { cmat::Zero(2, 2) }
- Projector onto the Pauli Sigma-Y 1-eigenstate.*
- [cmat pz0](#) { cmat::Zero(2, 2) }
- Projector onto the Pauli Sigma-Z 0-eigenstate  $|0\rangle\langle 0|$ .*
- [cmat pz1](#) { cmat::Zero(2, 2) }
- Projector onto the Pauli Sigma-Z 1-eigenstate  $|1\rangle\langle 1|$ .*
- [ket b00](#) { ket::Zero(4) }
- Bell-00 state (following the convention in Nielsen and Chuang)*
- [ket b01](#) { ket::Zero(4) }
- Bell-01 state (following the convention in Nielsen and Chuang)*
- [ket b10](#) { ket::Zero(4) }
- Bell-10 state (following the convention in Nielsen and Chuang)*
- [ket b11](#) { ket::Zero(4) }
- Bell-11 state (following the convention in Nielsen and Chuang)*
- [cmat pb00](#) { cmat::Zero(4, 4) }
- Projector onto the Bell-00 state.*
- [cmat pb01](#) { cmat::Zero(4, 4) }
- Projector onto the Bell-01 state.*
- [cmat pb10](#) { cmat::Zero(4, 4) }
- Projector onto the Bell-10 state.*
- [cmat pb11](#) { cmat::Zero(4, 4) }
- Projector onto the Bell-11 state.*
- [ket GHZ](#) { ket::Zero(8) }
- GHZ state.*
- [ket W](#) { ket::Zero(8) }
- W state.*
- [cmat pGHZ](#) { cmat::Zero(8, 8) }
- Projector onto the GHZ state.*
- [cmat pW](#) { cmat::Zero(8, 8) }
- Projector onto the W state.*

## Private Member Functions

- [States](#) ()

## Friends

- class [internal::Singleton](#)< const [States](#) >

## Additional Inherited Members

### 7.7.1 Detailed Description

const Singleton class that implements most commonly used states

### 7.7.2 Constructor & Destructor Documentation

#### 7.7.2.1 `qpp::States::States ( ) [inline],[private]`

Initialize the states

### 7.7.3 Friends And Related Function Documentation

7.7.3.1 friend class internal::Singleton< const States > [friend]

### 7.7.4 Member Data Documentation

7.7.4.1 ket qpp::States::b00 { ket::Zero(4) }

Bell-00 state (following the convention in Nielsen and Chuang)

7.7.4.2 ket qpp::States::b01 { ket::Zero(4) }

Bell-01 state (following the convention in Nielsen and Chuang)

7.7.4.3 ket qpp::States::b10 { ket::Zero(4) }

Bell-10 state (following the convention in Nielsen and Chuang)

7.7.4.4 ket qpp::States::b11 { ket::Zero(4) }

Bell-11 state (following the convention in Nielsen and Chuang)

7.7.4.5 ket qpp::States::GHZ { ket::Zero(8) }

GHZ state.

7.7.4.6 cmat qpp::States::pb00 { cmat::Zero(4, 4) }

Projector onto the Bell-00 state.

7.7.4.7 cmat qpp::States::pb01 { cmat::Zero(4, 4) }

Projector onto the Bell-01 state.

7.7.4.8 cmat qpp::States::pb10 { cmat::Zero(4, 4) }

Projector onto the Bell-10 state.

7.7.4.9 cmat qpp::States::pb11 { cmat::Zero(4, 4) }

Projector onto the Bell-11 state.

7.7.4.10 cmat qpp::States::pGHZ { cmat::Zero(8, 8) }

Projector onto the GHZ state.

7.7.4.11 cmat qpp::States::pW { cmat::Zero(8, 8) }

Projector onto the W state.

7.7.4.12 `cmat qpp::States::px0 { cmat::Zero(2, 2) }`

Projector onto the Pauli Sigma-X 0-eigenstate  $|+\rangle\langle+|$ .

7.7.4.13 `cmat qpp::States::px1 { cmat::Zero(2, 2) }`

Projector onto the Pauli Sigma-X 1-eigenstate  $|-\rangle\langle-|$ .

7.7.4.14 `cmat qpp::States::py0 { cmat::Zero(2, 2) }`

Projector onto the Pauli Sigma-Y 0-eigenstate.

7.7.4.15 `cmat qpp::States::py1 { cmat::Zero(2, 2) }`

Projector onto the Pauli Sigma-Y 1-eigenstate.

7.7.4.16 `cmat qpp::States::pz0 { cmat::Zero(2, 2) }`

Projector onto the Pauli Sigma-Z 0-eigenstate  $|0\rangle\langle 0|$ .

7.7.4.17 `cmat qpp::States::pz1 { cmat::Zero(2, 2) }`

Projector onto the Pauli Sigma-Z 1-eigenstate  $|1\rangle\langle 1|$ .

7.7.4.18 `ket qpp::States::W { ket::Zero(8) }`

W state.

7.7.4.19 `ket qpp::States::x0 { ket::Zero(2) }`

Pauli Sigma-X 0-eigenstate  $|+\rangle$

7.7.4.20 `ket qpp::States::x1 { ket::Zero(2) }`

Pauli Sigma-X 1-eigenstate  $|-\rangle$

7.7.4.21 `ket qpp::States::y0 { ket::Zero(2) }`

Pauli Sigma-Y 0-eigenstate.

7.7.4.22 `ket qpp::States::y1 { ket::Zero(2) }`

Pauli Sigma-Y 1-eigenstate.

7.7.4.23 `ket qpp::States::z0 { ket::Zero(2) }`

Pauli Sigma-Z 0-eigenstate  $|0\rangle$

7.7.4.24 ket qpp::States::z1 { ket::Zero(2) }

Pauli Sigma-Z 1-eigenstate  $|1\rangle$

The documentation for this class was generated from the following file:

- include/classes/[states.h](#)

## 7.8 qpp::Timer Class Reference

Measures time.

```
#include <timer.h>
```

### Public Member Functions

- [Timer](#) ()  
*Constructs an instance with the current time as the starting point.*
- void [tic](#) ()  
*Resets the chronometer.*
- void [toc](#) ()  
*Stops the chronometer.*
- double [seconds](#) () const  
*Time passed in seconds.*

### Protected Attributes

- std::chrono::steady\_clock::time\_point [\\_start](#)
- std::chrono::steady\_clock::time\_point [\\_end](#)

### Friends

- std::ostream & [operator<<](#) (std::ostream &os, const [Timer](#) &rhs)  
*Overload for std::ostream operators.*

### 7.8.1 Detailed Description

Measures time.

Uses a std::chrono::steady\_clock. It is not affected by wall clock changes during runtime.

### 7.8.2 Constructor & Destructor Documentation

7.8.2.1 qpp::Timer::Timer ( ) [inline]

Constructs an instance with the current time as the starting point.

### 7.8.3 Member Function Documentation

#### 7.8.3.1 `double qpp::Timer::seconds ( ) const` `[inline]`

Time passed in seconds.

##### Returns

Number of seconds that passed between the instantiation/reset and invocation of [qpp::Timer::toc\(\)](#)

#### 7.8.3.2 `void qpp::Timer::tic ( )` `[inline]`

Resets the chronometer.

Resets the starting/ending point to the current time

#### 7.8.3.3 `void qpp::Timer::toc ( )` `[inline]`

Stops the chronometer.

Set the current time as the ending point

### 7.8.4 Friends And Related Function Documentation

#### 7.8.4.1 `std::ostream& operator<< ( std::ostream & os, const Timer & rhs )` `[friend]`

Overload for std::ostream operators.

##### Parameters

<code>os</code>	Output stream
<code>rhs</code>	<a href="#">Timer</a> instance

##### Returns

Writes to the output stream the number of seconds that passed between the instantiation/reset and invocation of [qpp::Timer::toc\(\)](#).

### 7.8.5 Member Data Documentation

#### 7.8.5.1 `std::chrono::steady_clock::time_point qpp::Timer::_end` `[protected]`

#### 7.8.5.2 `std::chrono::steady_clock::time_point qpp::Timer::_start` `[protected]`

The documentation for this class was generated from the following file:

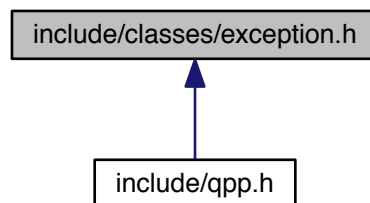
- include/classes/[timer.h](#)

## Chapter 8

# File Documentation

### 8.1 include/classes/exception.h File Reference

This graph shows which files directly or indirectly include this file:



#### Classes

- class [qpp::Exception](#)

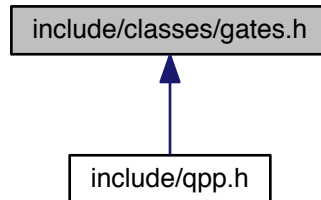
*Generates custom exceptions, used when validating function parameters.*

#### Namespaces

- [qpp](#)

## 8.2 include/classes/gates.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

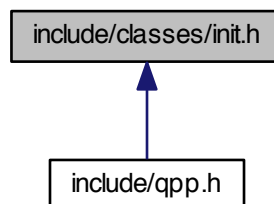
- class [qpp::Gates](#)  
*const Singleton class that implements most commonly used gates*

### Namespaces

- [qpp](#)

## 8.3 include/classes/init.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

- class [qpp::Init](#)  
*const Singleton class that performs additional initializations/cleanups*

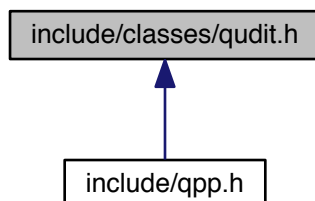


### Namespaces

- [qpp](#)

## 8.4 include/classes/qudit.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

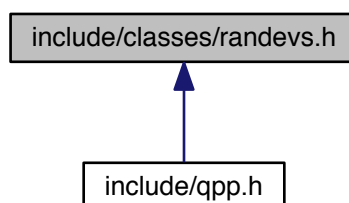
- class [qpp::Qudit](#)

### Namespaces

- [qpp](#)

## 8.5 include/classes/randevs.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

- class [qpp::RandomDevices](#)

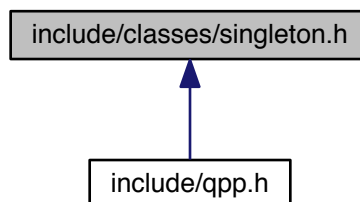
*Singleton class that manages the source of randomness in the library.*

## Namespaces

- [qpp](#)

## 8.6 include/classes/singleton.h File Reference

This graph shows which files directly or indirectly include this file:



## Classes

- class [qpp::internal::Singleton< T >](#)

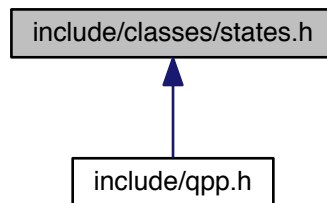
*[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)*

## Namespaces

- [qpp](#)
- [qpp::internal](#)

## 8.7 include/classes/states.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

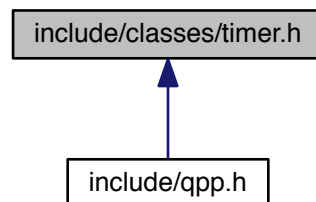
- class [qpp::States](#)  
*const Singleton class that implements most commonly used states*

### Namespaces

- [qpp](#)

## 8.8 include/classes/timer.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

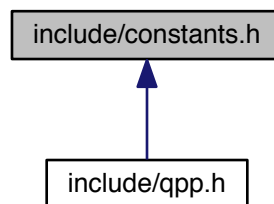
- class [qpp::Timer](#)  
*Measures time.*

## Namespaces

- [qpp](#)

## 8.9 include/constants.h File Reference

This graph shows which files directly or indirectly include this file:



## Namespaces

- [qpp](#)

## Functions

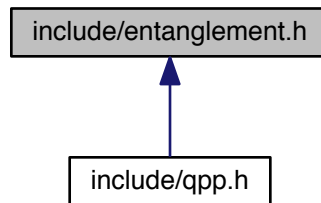
- constexpr std::complex< double > [qpp::operator""\\_i](#) (unsigned long long int x)  
*User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)*
- constexpr std::complex< double > [qpp::operator""\\_i](#) (long double x)  
*User-defined literal for complex  $i = \sqrt{-1}$  (real overload)*
- std::complex< double > [qpp::omega](#) (std::size\_t D)  
*D-th root of unity.*

## Variables

- constexpr double [qpp::chop](#) = 1e-10  
*Used in [qpp::disp\(\)](#) and [qpp::displn\(\)](#) for setting to zero numbers that have their absolute value smaller than [qpp::ct->::chop](#).*
- constexpr double [qpp::eps](#) = 1e-12  
*Used to decide whether a number or expression in double precision is zero or not.*
- constexpr std::size\_t [qpp::maxn](#) = 64  
*Maximum number of qubits.*
- constexpr double [qpp::pi](#) = 3.141592653589793238462643383279502884  
 $\pi$
- constexpr double [qpp::ee](#) = 2.718281828459045235360287471352662497  
*Base of natural logarithm,  $e$ .*

## 8.10 include/entanglement.h File Reference

This graph shows which files directly or indirectly include this file:



### Namespaces

- [qpp](#)

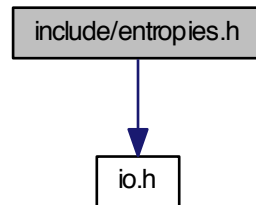
### Functions

- `template<typename Derived >`  
`cmat qpp::schmidtcoeff (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`  
*Schmidt coefficients of the bi-partite pure state A.*
- `template<typename Derived >`  
`cmat qpp::schmidtU (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`  
*Schmidt basis on Alice's side.*
- `template<typename Derived >`  
`cmat qpp::schmidtV (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`  
*Schmidt basis on Bob's side.*
- `template<typename Derived >`  
`cmat qpp::schmidtprob (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`  
*Schmidt probabilities of the bi-partite pure state A.*
- `template<typename Derived >`  
`double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`  
*Entanglement of the bi-partite pure state A.*
- `template<typename Derived >`  
`double qpp::gconcurrence (const Eigen::MatrixBase< Derived > &A)`  
*G-concurrence of the bi-partite pure state A.*

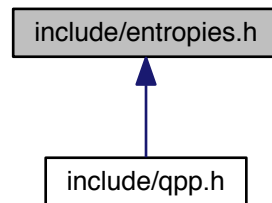
## 8.11 include/entropies.h File Reference

```
#include "io.h"
```

Include dependency graph for entropies.h:



This graph shows which files directly or indirectly include this file:



### Namespaces

- [qpp](#)

### Functions

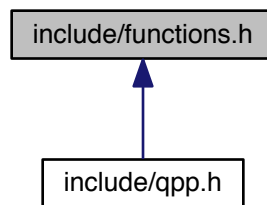
- `template<typename Derived >`  
`double qpp::shannon (const Eigen::MatrixBase< Derived > &A)`  
*Shannon/von-Neumann entropy of the probability distribution/density matrix A.*
- `template<typename Derived >`  
`double qpp::renyi (const double alpha, const Eigen::MatrixBase< Derived > &A)`  
*Renyi-  $\alpha$  entropy of the probability distribution/density matrix A, for  $\alpha \geq 0$ .*
- `template<typename Derived >`  
`double qpp::renyi\_inf (const Eigen::MatrixBase< Derived > &A)`  
*Renyi-  $\infty$  entropy (min entropy) of the probability distribution/density matrix A.*
- `template<typename Derived >`  
`double qpp::tsallis (const double alpha, const Eigen::MatrixBase< Derived > &A)`

*Tsallis-  $\alpha$  entropy of the probability distribution/density matrix  $A$ , for  $\alpha \geq 0$*

- `template<typename Derived >`  
`double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsysA, const std::vector< std::size_t > &subsysB, const std::vector< std::size_t > &dims)`  
*Quantum mutual information between 2 subsystems of a composite system.*

## 8.12 include/functions.h File Reference

This graph shows which files directly or indirectly include this file:



### Namespaces

- [qpp](#)

### Functions

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::transpose (const Eigen::MatrixBase< Derived > &A)`  
*Transpose.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::conjugate (const Eigen::MatrixBase< Derived > &A)`  
*Complex conjugate.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::adjoint (const Eigen::MatrixBase< Derived > &A)`  
*Adjoint.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::inverse (const Eigen::MatrixBase< Derived > &A)`  
*Inverse.*
- `template<typename Derived >`  
`Derived::Scalar qpp::trace (const Eigen::MatrixBase< Derived > &A)`  
*Trace.*
- `template<typename Derived >`  
`Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > &A)`  
*Determinant.*
- `template<typename Derived >`  
`Derived::Scalar qpp::logdet (const Eigen::MatrixBase< Derived > &A)`  
*Logarithm of the determinant.*

- template<typename Derived >  
Derived::Scalar [qpp::sum](#) (const Eigen::MatrixBase< Derived > &A)  
*Element-wise sum of A.*
- template<typename Derived >  
Derived::Scalar [qpp::prod](#) (const Eigen::MatrixBase< Derived > &A)  
*Element-wise product of A.*
- template<typename Derived >  
double [qpp::norm](#) (const Eigen::MatrixBase< Derived > &A)  
*Trace norm.*
- template<typename Derived >  
cmat [qpp::evals](#) (const Eigen::MatrixBase< Derived > &A)  
*Eigenvalues.*
- template<typename Derived >  
cmat [qpp::evecs](#) (const Eigen::MatrixBase< Derived > &A)  
*Eigenvectors.*
- template<typename Derived >  
dmat [qpp::hevals](#) (const Eigen::MatrixBase< Derived > &A)  
*Hermitian eigenvalues.*
- template<typename Derived >  
cmat [qpp::hevecs](#) (const Eigen::MatrixBase< Derived > &A)  
*Hermitian eigenvectors.*
- template<typename Derived >  
cmat [qpp::funm](#) (const Eigen::MatrixBase< Derived > &A, cplx(\*f)(const cplx &))  
*Functional calculus  $f(A)$*
- template<typename Derived >  
cmat [qpp::sqrtm](#) (const Eigen::MatrixBase< Derived > &A)  
*Matrix square root.*
- template<typename Derived >  
cmat [qpp::absm](#) (const Eigen::MatrixBase< Derived > &A)  
*Matrix absolut value.*
- template<typename Derived >  
cmat [qpp::expm](#) (const Eigen::MatrixBase< Derived > &A)  
*Matrix exponential.*
- template<typename Derived >  
cmat [qpp::logm](#) (const Eigen::MatrixBase< Derived > &A)  
*Matrix logarithm.*
- template<typename Derived >  
cmat [qpp::sinm](#) (const Eigen::MatrixBase< Derived > &A)  
*Matrix sin.*
- template<typename Derived >  
cmat [qpp::cosm](#) (const Eigen::MatrixBase< Derived > &A)  
*Matrix cos.*
- template<typename Derived >  
cmat [qpp::spectralpowm](#) (const Eigen::MatrixBase< Derived > &A, const cplx z)  
*Matrix power.*
- template<typename Derived >  
DynMat< typename Derived::Scalar > [qpp::powm](#) (const Eigen::MatrixBase< Derived > &A, std::size\_t n)  
*Matrix power.*
- template<typename OutputScalar , typename Derived >  
DynMat< OutputScalar > [qpp::cwise](#) (const Eigen::MatrixBase< Derived > &A, OutputScalar(\*f)(const type-name Derived::Scalar &))  
*Functor.*



- `template<typename T >`  
`DynMat< typename T::Scalar > qpp::kron (const T &head)`  
*Kronecker product (variadic overload)*
- `template<typename T, typename... Args>`  
`DynMat< typename T::Scalar > qpp::kron (const T &head, const Args &...tail)`  
*Kronecker product (variadic overload)*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::kron (const std::vector< Derived > &As)`  
*Kronecker product (std::vector overload)*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::kron (const std::initializer_list< Derived > &As)`  
*Kronecker product (std::initializer\_list overload)*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::kronpow (const Eigen::MatrixBase< Derived > &A, std::size_t n)`  
*Kronecker power.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::reshape (const Eigen::MatrixBase< Derived > &A, std::size_t rows, std::size_t cols)`  
*Reshape.*
- `template<typename Derived1, typename Derived2 >`  
`DynMat< typename Derived1::Scalar > qpp::comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`  
*Commutator.*
- `template<typename Derived1, typename Derived2 >`  
`DynMat< typename Derived1::Scalar > qpp::anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`  
*Anti-commutator.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::prj (const Eigen::MatrixBase< Derived > &V)`  
*Projector.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::expandout (const Eigen::MatrixBase< Derived > &A, std::size_t pos, const std::vector< std::size_t > &dims)`  
*Expand out.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::grams (const std::vector< Derived > &Vs)`  
*Gram-Schmidt orthogonalization (std::vector overload)*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::grams (const std::initializer_list< Derived > &Vs)`  
*Gram-Schmidt orthogonalization (std::initializer\_list overload)*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::grams (const Eigen::MatrixBase< Derived > &A)`  
*Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)*
- `std::vector< std::size_t > qpp::n2multiidx (std::size_t n, const std::vector< std::size_t > &dims)`  
*Non-negative integer index to multi-index.*
- `std::size_t qpp::multiidx2n (const std::vector< std::size_t > &midx, const std::vector< std::size_t > &dims)`  
*Multi-index to non-negative integer index.*
- `ket qpp::mket (const std::vector< std::size_t > &mask)`  
*Multi-partite qubit ket.*
- `ket qpp::mket (const std::vector< std::size_t > &mask, const std::vector< std::size_t > &dims)`  
*Multi-partite qudit ket (different dimensions overload)*
- `ket qpp::mket (const std::vector< std::size_t > &mask, std::size_t d)`

*Multi-partite qudit ket (same dimensions overload)*

- `cmat qpp::mprj` (const std::vector< std::size\_t > &mask)

*Projector onto multi-partite qubit ket.*

- `cmat qpp::mprj` (const std::vector< std::size\_t > &mask, const std::vector< std::size\_t > &dims)

*Projector onto multi-partite qudit ket (different dimensions overload)*

- `cmat qpp::mprj` (const std::vector< std::size\_t > &mask, std::size\_t d)

*Projector onto multi-partite qudit ket (same dimensions overload)*

- `std::vector< std::size_t > qpp::invperm` (const std::vector< std::size\_t > &perm)

*Inverse permutation.*

- `std::vector< std::size_t > qpp::compperm` (const std::vector< std::size\_t > &perm, const std::vector< std::size\_t > &sigma)

*Compose permutations.*

- `template<typename InputIterator >`  
`std::vector< double > qpp::amplitudes` (InputIterator first, InputIterator last)

*Computes the absolut values squared of a range of complex numbers.*

- `template<typename Derived >`  
`std::vector< double > qpp::amplitudes` (const Eigen::MatrixBase< Derived > &V)

*Computes the absolut values squared of a column vector.*

- `template<typename InputIterator >`  
`auto qpp::sum` (InputIterator first, InputIterator last) -> typename InputIterator::value\_type

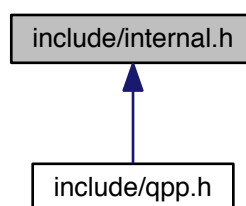
*Element-wise sum of a range.*

- `template<typename InputIterator >`  
`auto qpp::prod` (InputIterator first, InputIterator last) -> typename InputIterator::value\_type

*Element-wise product of a range.*

## 8.13 include/internal.h File Reference

This graph shows which files directly or indirectly include this file:



## Namespaces

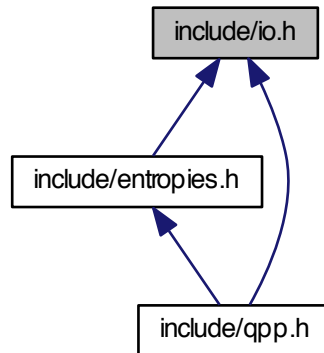
- `qpp::internal`
- `qpp`

## Functions

- void [qpp::internal::\\_n2multiidx](#) (std::size\_t n, std::size\_t numdims, const std::size\_t \*dims, std::size\_t \*result)
- std::size\_t [qpp::internal::\\_multiidx2n](#) (const std::size\_t \*midx, std::size\_t numdims, const std::size\_t \*dims)
- template<typename Derived >  
bool [qpp::internal::\\_check\\_square\\_mat](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [qpp::internal::\\_check\\_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [qpp::internal::\\_check\\_row\\_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [qpp::internal::\\_check\\_col\\_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename T >  
bool [qpp::internal::\\_check\\_nonzero\\_size](#) (const T &x)
- bool [qpp::internal::\\_check\\_dims](#) (const std::vector< std::size\_t > &dims)
- template<typename Derived >  
bool [qpp::internal::\\_check\\_dims\\_match\\_mat](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [qpp::internal::\\_check\\_dims\\_match\\_cvect](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &V)
- template<typename Derived >  
bool [qpp::internal::\\_check\\_dims\\_match\\_rvect](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &V)
- bool [qpp::internal::\\_check\\_eq\\_dims](#) (const std::vector< std::size\_t > &dims, std::size\_t dim)
- bool [qpp::internal::\\_check\\_subsys\\_match\\_dims](#) (const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- bool [qpp::internal::\\_check\\_perm](#) (const std::vector< std::size\_t > &perm)
- template<typename Derived1 , typename Derived2 >  
DynMat< typename Derived1::Scalar > [qpp::internal::\\_kron2](#) (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename T >  
void [qpp::internal::variadic\\_vector\\_emplace](#) (std::vector< T > &)
- template<typename T , typename First , typename... Args>  
void [qpp::internal::variadic\\_vector\\_emplace](#) (std::vector< T > &v, First &&first, Args &&...args)

## 8.14 include/io.h File Reference

This graph shows which files directly or indirectly include this file:



### Namespaces

- [qpp](#)

### Functions

- `template<typename T >`  
`void qpp::disp (const T &x, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)`  
*Displays a standard container that supports std::begin, std::end and forward iteration. Does not add a newline.*
- `template<typename T >`  
`void qpp::displn (const T &x, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)`  
*Displays a standard container that supports std::begin, std::end and forward iteration. Adds a newline.*
- `template<typename T >`  
`void qpp::disp (const T *x, const std::size_t n, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)`  
*Displays a C-style array. Does not add a newline.*
- `template<typename T >`  
`void qpp::displn (const T *x, const std::size_t n, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)`  
*Displays a C-style array. Adds a newline.*
- `template<typename Derived >`  
`void qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop, std::ostream &os=std::cout)`  
*Displays an Eigen expression in matrix friendly form. Does not add a new line.*
- `template<typename Derived >`  
`void qpp::displn (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop, std::ostream &os=std::cout)`  
*Displays an Eigen expression in matrix friendly form. Adds a newline.*
- `void qpp::disp (const cplx z, double chop=qpp::chop, std::ostream &os=std::cout)`

- Displays a number (implicitly converted to `std::complex<double>`) in friendly form. Does not add a new line.*

• void [qpp::displn](#) (const cplx z, double chop=[qpp::chop](#), std::ostream &os=std::cout)

*Displays a number (implicitly converted to `std::complex<double>`) in friendly form. Adds a new line.*
- template<typename Derived >

void [qpp::save](#) (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

*Saves Eigen expression to a binary file (internal format) in double precision.*
- template<typename Derived >

DynMat< typename Derived::Scalar > [qpp::load](#) (const std::string &fname)

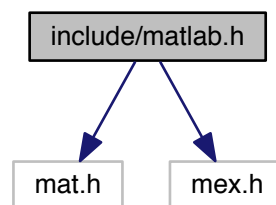
*Loads Eigen matrix from a binary file (internal format) in double precision.*

## 8.15 include/matlab.h File Reference

```
#include "mat.h"
```

```
#include "mex.h"
```

Include dependency graph for matlab.h:



### Namespaces

- [qpp](#)

### Functions

- template<typename Derived >

Derived [qpp::loadMATLABmatrix](#) (const std::string &mat\_file, const std::string &var\_name)

*Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.*
- template<>

dmat [qpp::loadMATLABmatrix](#) (const std::string &mat\_file, const std::string &var\_name)

*Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))*
- template<>

cmat [qpp::loadMATLABmatrix](#) (const std::string &mat\_file, const std::string &var\_name)

*Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))*
- template<typename Derived >

void [qpp::saveMATLABmatrix](#) (const Eigen::MatrixBase< Derived > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)

*Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.*
- template<>

void [qpp::saveMATLABmatrix](#) (const Eigen::MatrixBase< dmat > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)

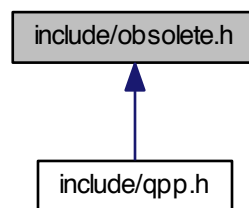
*Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))*

- `template<>`  
`void qpp::saveMATLABmatrix (const Eigen::MatrixBase< cmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`

*Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))*

## 8.16 include/obsolete.h File Reference

This graph shows which files directly or indirectly include this file:



### Namespaces

- [qpp](#)
- [qpp::obsolete](#)

### Functions

- `template<typename Derived1 , typename Derived2 >`  
`DynMat< typename Derived1::Scalar > qpp::obsolete::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`

*Applies the gate A to the part subsys of a multipartite state vector or density matrix.*

- `template<typename Derived >`  
`cmat qpp::obsolete::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`

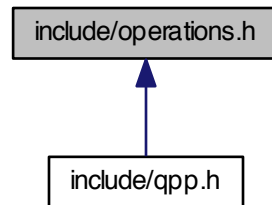
*Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.*

- `cmat qpp::obsolete::super (const std::vector< cmat > &Ks)`

*Superoperator matrix representation.*

## 8.17 include/operations.h File Reference

This graph shows which files directly or indirectly include this file:



### Namespaces

- [qpp](#)

### Functions

- `template<typename Derived1 , typename Derived2 >`  
`DynMat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size_t > &ctrl, const std::vector< std::size_t > &subsys, std::size_t n, std::size_t d=2)`  
*Applies the controlled-gate A to the part subsys of a multipartite state vector or density matrix.*
- `template<typename Derived1 , typename Derived2 >`  
`DynMat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size_t > &subsys, std::size_t n, std::size_t d=2)`  
*Applies the gate A to the part subsys of a multipartite state vector or density matrix.*
- `template<typename Derived >`  
`cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks)`  
*Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.*
- `template<typename Derived >`  
`cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< std::size_t > &subsys, std::size_t n, std::size_t d=2)`  
*Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.*
- `cmat qpp::super (const std::vector< cmat > &Ks)`  
*Superoperator matrix representation.*
- `cmat qpp::choi (const std::vector< cmat > &Ks)`  
*Choi matrix representation.*
- `std::vector< cmat > qpp::choi2kraus (const cmat &A)`  
*Extracts orthogonal Kraus operators from Choi matrix.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`  
*Partial trace.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`

*Partial trace.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`

*Partial trace.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`

*Partial transpose.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &perm, const std::vector< std::size_t > &dims)`

*System permutation.*



## 8.18 include/qpp.h File Reference

```
#include <algorithm>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <exception>
#include <fstream>
#include <functional>
#include <iomanip>
#include <iostream>
#include <iterator>
#include <limits>
#include <numeric>
#include <ostream>
#include <random>
#include <sstream>
#include <stdexcept>
#include <string>
#include <tuple>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "constants.h"
#include "types.h"
#include "classes/exception.h"
#include "classes/singleton.h"
#include "classes/states.h"
#include "classes/randevs.h"
#include "internal.h"
#include "classes/init.h"
#include "functions.h"
#include "classes/gates.h"
#include "entropies.h"
#include "entanglement.h"
#include "operations.h"
#include "io.h"
#include "random.h"
#include "classes/qudit.h"
#include "classes/timer.h"
#include "obsolete.h"
```

Include dependency graph for qpp.h:



## Namespaces

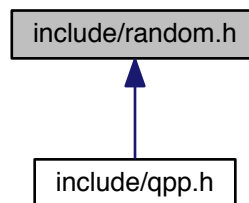
- [qpp](#)

## Variables

- RandomDevices & `qpp::rdevs` = RandomDevices::get\_instance()  
*`qpp::RandomDevices` Singleton*
- const Gates & `qpp::gt` = Gates::get\_instance()  
*`qpp::Gates` const Singleton*
- const States & `qpp::st` = States::get\_instance()  
*`qpp::States` const Singleton*
- const Init & `qpp::init` = Init::get\_instance()  
*`qpp::Init` const Singleton*

## 8.19 include/random.h File Reference

This graph shows which files directly or indirectly include this file:



## Namespaces

- `qpp`

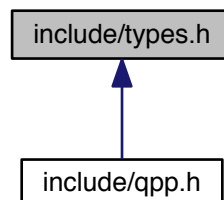
## Functions

- template<typename Derived >  
Derived `qpp::rand` (std::size\_t rows, std::size\_t cols, double a=0, double b=1)  
*Generates a random matrix with entries uniformly distributed in the interval [a, b]*
- template<>  
dmat `qpp::rand` (std::size\_t rows, std::size\_t cols, double a, double b)  
*Generates a random real matrix with entries uniformly distributed in the interval [a, b], specialization for double matrices (`qpp::dmat`)*
- template<>  
cmat `qpp::rand` (std::size\_t rows, std::size\_t cols, double a, double b)  
*Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b], specialization for complex matrices (`qpp::cmat`)*
- double `qpp::rand` (double a=0, double b=1)  
*Generates a random real number uniformly distributed in the interval [a, b]*
- int `qpp::randint` (int a=std::numeric\_limits< int >::min(), int b=std::numeric\_limits< int >::max())  
*Generates a random integer (int) uniformly distributed in the interval [a, b].*
- template<typename Derived >  
Derived `qpp::randn` (std::size\_t rows, std::size\_t cols, double mean=0, double sigma=1)

- Generates a random matrix with entries normally distributed in  $N(\text{mean}, \text{sigma})$*
- `template<>`  
`dmat qpp::randn (std::size_t rows, std::size_t cols, double mean, double sigma)`  
*Generates a random real matrix with entries normally distributed in  $N(\text{mean}, \text{sigma})$ , specialization for double matrices ([qpp::dmat](#))*
  - `template<>`  
`cmat qpp::randn (std::size_t rows, std::size_t cols, double mean, double sigma)`  
*Generates a random complex matrix with entries (both real and imaginary) normally distributed in  $N(\text{mean}, \text{sigma})$ , specialization for complex matrices ([qpp::cmat](#))*
  - `double qpp::randn (double mean=0, double sigma=1)`  
*Generates a random real number (double) normally distributed in  $N(\text{mean}, \text{sigma})$*
  - `cmat qpp::randU (std::size_t D)`  
*Generates a random unitary matrix.*
  - `cmat qpp::randV (std::size_t Din, std::size_t Dout)`  
*Generates a random isometry matrix.*
  - `std::vector< cmat > qpp::randkraus (std::size_t n, std::size_t D)`  
*Generates a set of random Kraus operators.*
  - `cmat qpp::randH (std::size_t D)`  
*Generates a random Hermitian matrix.*
  - `ket qpp::randket (std::size_t D)`  
*Generates a random normalized ket (pure state vector)*
  - `cmat qpp::randrho (std::size_t D)`  
*Generates a random density matrix.*
  - `std::vector< std::size_t > qpp::randperm (std::size_t n)`  
*Generates a random uniformly distributed permutation.*

## 8.20 include/types.h File Reference

This graph shows which files directly or indirectly include this file:



## Namespaces

- [qpp](#)

## Typedefs

- using `qpp::cplx` = `std::complex< double >`  
*Complex number in double precision.*
- using `qpp::cmat` = `Eigen::MatrixXcd`  
*Complex (double precision) dynamic Eigen matrix.*
- using `qpp::dmat` = `Eigen::MatrixXd`  
*Real (double precision) dynamic Eigen matrix.*
- using `qpp::ket` = `Eigen::Matrix< cplx, Eigen::Dynamic, 1 >`  
*Complex (double precision) dynamic Eigen column matrix.*
- using `qpp::bra` = `Eigen::Matrix< cplx, 1, Eigen::Dynamic >`  
*Complex (double precision) dynamic Eigen row matrix.*
- template<typename Scalar >  
using `qpp::DynMat` = `Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >`  
*Dynamic Eigen matrix over the field specified by Scalar.*

# Index

absm  
    qpp, 19  
adjoint  
    qpp, 19  
amplitudes  
    qpp, 20  
anticomm  
    qpp, 21  
apply  
    qpp, 21  
  
bra  
    qpp, 18  
  
CUSTOM\_EXCEPTION  
    qpp::Exception, 93  
channel  
    qpp, 23, 25  
choi  
    qpp, 26  
choi2kraus  
    qpp, 27  
chop  
    qpp, 82  
cmat  
    qpp, 18  
comm  
    qpp, 28  
compperm  
    qpp, 28  
conjugate  
    qpp, 30  
cosm  
    qpp, 30  
cplx  
    qpp, 18  
cwise  
    qpp, 31  
  
DIMS\_INVALID  
    qpp::Exception, 93  
DIMS\_MISMATCH\_CVECTOR  
    qpp::Exception, 93  
DIMS\_MISMATCH\_MATRIX  
    qpp::Exception, 93  
DIMS\_MISMATCH\_RVECTOR  
    qpp::Exception, 93  
DIMS\_MISMATCH\_VECTOR  
    qpp::Exception, 93  
DIMS\_NOT\_EQUAL  
    qpp::Exception, 93  
  
det  
    qpp, 31  
disp  
    qpp, 32, 33  
displn  
    qpp, 33–35  
dmat  
    qpp, 18  
  
ee  
    qpp, 82  
entanglement  
    qpp, 35  
eps  
    qpp, 82  
evals  
    qpp, 36  
evects  
    qpp, 37  
expandout  
    qpp, 37  
expm  
    qpp, 38  
  
funm  
    qpp, 39  
  
gconcurrency  
    qpp, 39  
grams  
    qpp, 40, 41  
gt  
    qpp, 82  
  
hevals  
    qpp, 42  
hevects  
    qpp, 42  
  
init  
    qpp, 82  
inverse  
    qpp, 43  
invperm  
    qpp, 43  
  
ket  
    qpp, 19  
kron  
    qpp, 44, 45

- kronpow
  - qpp, [46](#)
- load
  - qpp, [46](#)
- logdet
  - qpp, [48](#)
- logm
  - qpp, [48](#)
- MATRIX\_NOT\_CVECTOR
  - qpp::Exception, [93](#)
- MATRIX\_NOT\_RVECTOR
  - qpp::Exception, [93](#)
- MATRIX\_NOT\_SQUARE
  - qpp::Exception, [93](#)
- MATRIX\_NOT\_SQUARE\_OR\_CVECTOR
  - qpp::Exception, [93](#)
- MATRIX\_NOT\_SQUARE\_OR\_RVECTOR
  - qpp::Exception, [93](#)
- MATRIX\_NOT\_SQUARE\_OR\_VECTOR
  - qpp::Exception, [93](#)
- MATRIX\_NOT\_VECTOR
  - qpp::Exception, [93](#)
- maxn
  - qpp, [82](#)
- mket
  - qpp, [49](#), [50](#)
- mprj
  - qpp, [50](#), [51](#)
- multiidx2n
  - qpp, [52](#)
- n2multiidx
  - qpp, [52](#)
- NOT\_BIPARTITE
  - qpp::Exception, [93](#)
- NOT\_QUBIT\_GATE
  - qpp::Exception, [93](#)
- NOT\_QUBIT\_SUBSYS
  - qpp::Exception, [93](#)
- norm
  - qpp, [53](#)
- OUT\_OF\_RANGE
  - qpp::Exception, [93](#)
- omega
  - qpp, [53](#)
- PERM\_INVALID
  - qpp::Exception, [93](#)
- pi
  - qpp, [83](#)
- powm
  - qpp, [54](#)
- prj
  - qpp, [54](#)
- prod
  - qpp, [55](#)
- ptrace
  - qpp, [56](#)
- ptrace1
  - qpp, [57](#)
- ptrace2
  - qpp, [58](#)
- ptranspose
  - qpp, [59](#)
- qmutualinfo
  - qpp, [60](#)
- qpp, [11](#)
  - absm, [19](#)
  - adjoint, [19](#)
  - amplitudes, [20](#)
  - anticomm, [21](#)
  - apply, [21](#)
  - bra, [18](#)
  - channel, [23](#), [25](#)
  - choi, [26](#)
  - choi2kraus, [27](#)
  - chop, [82](#)
  - cmat, [18](#)
  - comm, [28](#)
  - compperm, [28](#)
  - conjugate, [30](#)
  - cosm, [30](#)
  - cplx, [18](#)
  - cwise, [31](#)
  - det, [31](#)
  - disp, [32](#), [33](#)
  - displn, [33–35](#)
  - dmat, [18](#)
  - ee, [82](#)
  - entanglement, [35](#)
  - eps, [82](#)
  - evals, [36](#)
  - evects, [37](#)
  - expandout, [37](#)
  - expm, [38](#)
  - funm, [39](#)
  - gconcurrency, [39](#)
  - grams, [40](#), [41](#)
  - gt, [82](#)
  - hevals, [42](#)
  - hevects, [42](#)
  - init, [82](#)
  - inverse, [43](#)
  - invperm, [43](#)
  - ket, [19](#)
  - kron, [44](#), [45](#)
  - kronpow, [46](#)
  - load, [46](#)
  - logdet, [48](#)
  - logm, [48](#)
  - maxn, [82](#)
  - mket, [49](#), [50](#)
  - mprj, [50](#), [51](#)
  - multiidx2n, [52](#)

- n2multiidx, [52](#)
- norm, [53](#)
- omega, [53](#)
- pi, [83](#)
- powm, [54](#)
- prj, [54](#)
- prod, [55](#)
- ptrace, [56](#)
- ptrace1, [57](#)
- ptrace2, [58](#)
- ptranspose, [59](#)
- qmutualinfo, [60](#)
- rand, [61](#), [62](#)
- randint, [63](#)
- randket, [64](#)
- randkraus, [64](#)
- randn, [65](#), [66](#)
- randperm, [67](#)
- randrho, [67](#)
- rdevs, [83](#)
- renyi, [68](#)
- reshape, [69](#)
- save, [70](#)
- schmidtcoeff, [71](#)
- schmidtprob, [72](#)
- shannon, [75](#)
- sinm, [75](#)
- spectralpowm, [77](#)
- sqrtn, [77](#)
- st, [83](#)
- sum, [78](#)
- super, [79](#)
- syspermute, [79](#)
- trace, [80](#)
- transpose, [81](#)
- tsallis, [81](#)
- qpp::Exception
  - CUSTOM\_EXCEPTION, [93](#)
  - DIMS\_INVALID, [93](#)
  - DIMS\_MISMATCH\_CVECTOR, [93](#)
  - DIMS\_MISMATCH\_MATRIX, [93](#)
  - DIMS\_MISMATCH\_RVECTOR, [93](#)
  - DIMS\_MISMATCH\_VECTOR, [93](#)
  - DIMS\_NOT\_EQUAL, [93](#)
  - MATRIX\_NOT\_CVECTOR, [93](#)
  - MATRIX\_NOT\_RVECTOR, [93](#)
  - MATRIX\_NOT\_SQUARE, [93](#)
  - MATRIX\_NOT\_SQUARE\_OR\_CVECTOR, [93](#)
  - MATRIX\_NOT\_SQUARE\_OR\_RVECTOR, [93](#)
  - MATRIX\_NOT\_SQUARE\_OR\_VECTOR, [93](#)
  - MATRIX\_NOT\_VECTOR, [93](#)
  - NOT\_BIPARTITE, [93](#)
  - NOT\_QUBIT\_GATE, [93](#)
  - NOT\_QUBIT\_SUBSYS, [93](#)
  - OUT\_OF\_RANGE, [93](#)
  - PERM\_INVALID, [93](#)
  - SUBSYS\_MISMATCH\_DIMS, [93](#)
  - TYPE\_MISMATCH, [93](#)
  - UNDEFINED\_TYPE, [93](#)
  - UNKNOWN\_EXCEPTION, [93](#)
  - ZERO\_SIZE, [93](#)
- rand
  - qpp, [61](#), [62](#)
- randint
  - qpp, [63](#)
- randket
  - qpp, [64](#)
- randkraus
  - qpp, [64](#)
- randn
  - qpp, [65](#), [66](#)
- randperm
  - qpp, [67](#)
- randrho
  - qpp, [67](#)
- rdevs
  - qpp, [83](#)
- renyi
  - qpp, [68](#)
- reshape
  - qpp, [69](#)
- SUBSYS\_MISMATCH\_DIMS
  - qpp::Exception, [93](#)
- save
  - qpp, [70](#)
- schmidtcoeff
  - qpp, [71](#)
- schmidtprob
  - qpp, [72](#)
- shannon
  - qpp, [75](#)
- sinm
  - qpp, [75](#)
- spectralpowm
  - qpp, [77](#)
- sqrtn
  - qpp, [77](#)
- st
  - qpp, [83](#)
- sum
  - qpp, [78](#)
- super
  - qpp, [79](#)
- syspermute
  - qpp, [79](#)
- TYPE\_MISMATCH
  - qpp::Exception, [93](#)
- trace
  - qpp, [80](#)
- transpose
  - qpp, [81](#)
- tsallis
  - qpp, [81](#)

UNDEFINED\_TYPE

qpp::Exception, [93](#)

UNKNOWN\_EXCEPTION

qpp::Exception, [93](#)

ZERO\_SIZE

qpp::Exception, [93](#)