

quantum++  
0.1

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# Chapter 1

## quantum++ - A C++11 quantum computing library

### Version

0.1

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A simple example:

```
#include "qpp.h"

// #include "matlab.h" // support for MATLAB

using namespace std;
using namespace qpp;

cplx pow3(const cplx& z) // a test function
{
    return std::pow(z, 3);
}

int main()
{
    cout << "Starting qpp..." << endl;
    // output format
    // cout << std::scientific;
    cout << std::fixed; // use fixed format for nice formatting
    cout << std::setprecision(4); // only for fixed or scientific modes

    // TESTING
    // testing channel and Gates::apply
    cout << endl << "Testing channel(...) and Gates::apply(...)." << endl;
    cmat rho = randrho(16);
    cmat K = kron(gt.Id2, gt.X, gt.Y, gt.Z);
    vector<std::size_t> p = randperm(4); // permutation
    cout << "Permutation: ";
    displn(p, " ", " ");
    vector<std::size_t> invp = invperm(p); // inverse permutation
    cout << "Inverse permutation: ";
    displn(invp, " ", " ");
    cmat r1 = channel(rho, { K }, p, { 2, 2, 2, 2 });
    cmat r2 = syspermute(channel(syspermute(rho, p, { 2, 2, 2, 2 }), { K },
        { 0,
            1, 2, 3 }, { 2, 2, 2, 2 }), invp, { 2, 2, 2, 2 });
    cout << norm(r1 - r2) << endl << endl;

    r1 = gt.apply(rho, K, p, { 2, 2, 2, 2 });
    r2 = syspermute(
        gt.apply(syspermute(rho, p, { 2, 2, 2, 2 }), K, { 0, 1, 2, 3 }, { 2,
            2, 2, 2 }), invp, { 2, 2, 2, 2 });
    cout << norm(r1 - r2) << endl << endl;
```

```

displn(channel(prj(mket( { 0, 1 })), { gt.CNOTab, { 1, 0 }, { 2, 2 }));
cout << endl;
displn(gt.apply(mket( { 0, 0 }), gt.CNOTab, { 0, 1 }, { 2, 2 }));

// quantum teleportation
cout << endl << "Qudit teleportation." << endl;
ket psi = randket(2); // a random state;
cout << "|psi><psi|:" << endl;
displn(prj(psi));
cmat telecircuit = expandout(gt.H, { 0 }, { 2, 2, 2 })
    gt.CTRL(gt.X, { 0 }, { 1 }, 3);
ket psiin = kron(psi, st.b00); // input state
ket psiout = telecircuit * psiin; // output state before measurement
// measure Alice's qubits, measurement results are 1 0
psiout = kron(prj(st.z1), prj(st.z0), gt.Id2) * psiout;
// apply correction
psiout = expandout(powm(gt.Z, 1) * powm(gt.X, 0), { 2 }, { 2, 2, 2 })
    psiout;
// not necessary to normalize, prj() takes care of it below
cmat rhoout = ptrace(prj(psiout), { 0, 1 }, { 2, 2, 2 });
cout << endl << "Teleported state:" << endl;
displn(rhoout);
cout << "Difference in norm: " << norm(prj(psi) - rhoout) << endl;

// qudit measurements
cout << endl << "Qudit measurements." << endl;
cout << "Initially in state |0><0|." << endl;
ket zd0(3);
zd0 << 1, 0, 0;
Qudit q(prj(zd0));
cout << "Measuring Z operator non-destructively. Results:" << endl;
cout << q.measure() << endl;
cout << q.measure() << endl;
cout << q.measure() << endl;
cout << "Measuring X operator non-destructively. Results:" << endl;
cout << q.measure(gt.Xd(3)) << endl;
cout << q.measure(gt.Xd(3)) << endl;
cout << q.measure(gt.Xd(3)) << endl;
// von Neumann projective measurement
cout << "Measuring X operator destructively (collapse). Results:" << endl;
cout << q.measure(gt.Xd(3), true) << endl;
cout << q.measure(gt.Xd(3)) << endl;
cout << q.measure(gt.Xd(3)) << endl;
cout << "Finally measuring Z operator destructively. Results:" << endl;
cout << q.measure(true) << endl;
cout << q.measure() << endl;
cout << q.measure() << endl;
cout << "Final state of qudit:" << endl;
displn(q.getRho());

// Bell state generator
cout << endl << "Bell state generator: " << endl;
cmat circuit;
circuit = gt.CTRL(gt.X, { 0 }, { 1 }, 2) * expandout(gt.
    H, 0, { 2, 2 });
cmat input = kron(st.z0, st.z0);
cmat output = circuit * input;
cout << "Circuit matrix representation: " << endl;
displn(circuit);
cout << endl << "Output (|Bell_0> state) of the circuit on |00>: " << endl;
displn(output);

// 3-qubit repition code
cout << endl << "3-qubit repetition code: " << endl;
cmat rep;
rep = gt.CTRL(gt.X, { 0 }, { 2 }, 3) * gt.CTRL(gt.X, { 0 }, { 1 }, 3);
input = kron(st.z1, st.z0, st.z0);
output = rep * input;
cout << "Circuit acting on |000> produces |111>. Check: " << endl;
displn(output);

// functor test
cout << endl << "Functor z^3 acting on:" << endl;
cmat a(2, 2);
a << 1, 2, 3, 4;
displn(a);
cout << "Result (with lambda):" << endl;
// functor z^3 componentwise, specify OutputScalar and Derived for lambdas
displn(cwise<cplx, cmatrix>(a, [](const cplx& z)->cplx
    { return z*z*z; }));
cout << "Result (with proper function):" << endl;
// automatic type deduction for proper functions
displn(cwise(a, &pow3));

// Gram-Schmidt
cout << endl << "Gram-Schmidt on matrix:" << endl;

```

```

cmat A(3, 3);
A << 1, 1, 0, 0, 2, 0, 0, 0, 0;
displn(A);
cmat Ags = grams(A);
cout << endl << "Result:" << endl;
displn(Ags);
cout << endl << "Projector is:" << endl;
displn(Ags * adjoint(Ags));

// spectral decomposition test
cout << endl << "Spectral decomposition tests." << endl;
std::size_t D = 4;
cmat rH = randH(D);
dmat evalsH = hevals(rH);
cmat evecsH = hevecs(rH);
cmat spec = cmat::Zero(D, D);
for (std::size_t i = 0; i < D; i++)
    spec += evalsH(i) * prj((cmat) evecsH.col(i));
cout << "Original matrix: " << endl;
displn(rH);
cout << endl << "Reconstructed from spectral decomposition: " << endl;
displn(spec);
cout << "Difference in norm: " << norm(spec - rH) << endl;

// channel tests
cout << endl << "Channel tests." << endl;
std::size_t nk = 10, d = 2; // nk Kraus on d-dimensional system
cout << "Generating a random channel with " << nk
    << " Kraus operators on a " << d << " dimensional space..." << endl;
std::vector<cmat> Ks = randkraus(nk, d);

cmat rho_in = randrho(d); // input state
cmat rho_out = channel(rho_in, Ks); // output state

cout << "Computing its Choi matrix..." << endl;
cmat choim = choi(Ks);
cout << "Choi matrix:" << endl;
displn(choim);
cout << endl << "The eigenvalues of the Choi matrix are: " << endl;
displn(transpose(hevals(choim)));
cout << endl << "Their sum is: " << sum(hevals(choim)) << endl;
std::vector<cmat> Kperps = choi2kraus(choim);
cout << endl << "The Kraus rank of the channel is: " << Kperps.size()
    << endl;
cmat rho_out1 = channel(rho_in, Kperps);
cout << endl << "Difference in norm on output states: "
    << norm(rho_out1 - rho_out) << endl;
cout << endl << "Superoperator matrix:" << endl;
cmat smat = super(Ks);
displn(smat);
cout << endl << "The eigenvalues of the superoperator matrix are: " << endl;
cmat evalsupop = evals(smat);
displn(transpose(evalsupop));
cout << endl << "Their absolute values are: " << endl;
for (std::size_t i = 0; i < (std::size_t) evalsupop.size(); i++)
    cout << std::abs((cplx) evalsupop(i)) << " ";
cout << endl << endl << "Difference in norm for superoperator action: ";
cmat rho_out2 = transpose(
    (cmat) reshape(smat * reshape(transpose(rho_in), d * d, 1), d, d));
cout << norm(rho_out - rho_out2) << endl;

// statistics tests
cout << endl << "Statistics tests." << endl;
std::vector<cplx> ampl = { 1. + 1_i, 1. - 1_i };
cmat va(1, 4);
va << 0.1, 1, 1. + 1_i, 1. + 2_i;
DiscreteDistributionAbsSquare dc(va);
cout << "The probabilities are: ";
displn(dc.probabilities(), " ", "{", " }");

// // TIMING tests
cout << endl << "Timing tests..." << endl;
std::size_t n = 12; // number of qubits
std::size_t N = std::pow(2, n);
vector<std::size_t> dims(n, 2); // local dimensions
cout << "n = " << n << " qubits, matrix size " << N << " x " << N << "."
    << endl;

// matrix initialization
cout << endl << "Matrix initialization timing." << endl;
// start the timer, automatic tic() in the constructor
Timer t, total;
cmat randcmat = cmat::Random(N, N);
t.toc(); // read the time
cout << "Took " << t << " seconds." << endl;

// lazy matrix product

```

```

cout << endl << "Lazy matrix product timing." << endl;
t.tic();
auto lazyprod = randcmat * randcmat; // lazyprod has type GenMatProduct
t.toc(); // read the time
cout << "Took " << t << " seconds." << endl;

// ptrace1 timing
cout << endl << "ptrace1 timing." << endl;
t.tic(); // reset the chronometer
// trace away half of the qubits
ptrace1(randcmat,
        { (std::size_t) std::sqrt(N), (std::size_t) std::sqrt(N) });
t.toc(); // read the time
cout << "Took " << t << " seconds." << endl;

// ptrace2 timing
cout << endl << "ptrace2 timing." << endl;
t.tic(); // reset the chronometer
// trace away half of the qubits
ptrace2(randcmat,
        { (std::size_t) std::sqrt(N), (std::size_t) std::sqrt(N) });
t.toc(); // read the time
cout << "Took " << t << " seconds." << endl;

// ptrace
cout << endl << "ptrace timing." << endl;
vector<std::size_t> subsys_ptrace = { 0 };
cout << "Subsystem(s): ";
displn(subsys_ptrace, " ", "");
t.tic();
ptrace(randcmat, subsys_ptrace, dims);
t.toc();
cout << "Took " << t << " seconds." << endl;

// ptranspose
cout << endl << "ptranspose timing." << endl;
vector<std::size_t> subsys_ptranspose; // partially transpose n-1 subsystems
for (std::size_t i = 0; i < n - 1; i++)
    subsys_ptranspose.push_back(i);
cout << "Subsystem(s): ";
displn(subsys_ptranspose, " ", "");
t.tic();
ptranspose(randcmat, subsys_ptranspose, dims);
t.toc();
cout << "Took " << t << " seconds." << endl;

// syspermute
cout << endl << "syspermute timing." << endl;
vector<std::size_t> perm; // left-shift all subsystems by 1
for (std::size_t i = 0; i < n; i++)
    perm.push_back((i + 1) % n);
cout << "Subsystem(s): ";
displn(perm, " ", "");
t.tic();
syspermute(randcmat, perm, dims);
t.toc();
cout << "Took " << t << " seconds." << endl;

// // matrix product
// cout << endl << "Matrix product timing." << endl;
// t.tic(); // reset the chronometer
// cmat prodmat = randcmat * randcmat; // explicit cmat now
// t.toc(); // read the time
// cout << "Took " << t << " seconds." << endl;

// END TIMING
total.toc(); // read the total running time
cout << endl << "Total time: " << total.seconds() << " seconds.";
cout << endl << "Exiting qpp..." << endl;
}

```



## Chapter 2

# Namespace Index

### 2.1 Namespace List

Here is a list of all namespaces with brief descriptions:

<a href="#">qpp</a> . . . . .	<a href="#">13</a>
<a href="#">qpp::internal</a> . . . . .	<a href="#">68</a>



## Chapter 3

# Hierarchical Index

### 3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

qpp::DiscreteDistribution . . . . .	71
qpp::DiscreteDistributionAbsSquare . . . . .	72
exception	
qpp::Exception . . . . .	73
qpp::NormalDistribution . . . . .	82
qpp::Qudit . . . . .	83
qpp::Singleton< T > . . . . .	86
qpp::Gates . . . . .	76
qpp::RandomDevices . . . . .	85
qpp::Singleton< const Gates > . . . . .	86
qpp::Singleton< const States > . . . . .	86
qpp::States . . . . .	87
qpp::Singleton< RandomDevices > . . . . .	86
qpp::Timer . . . . .	90
qpp::UniformIntDistribution . . . . .	91
qpp::UniformRealDistribution . . . . .	91



## Chapter 4

# Class Index

### 4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

<a href="#">qpp::DiscreteDistribution</a>	71
<a href="#">qpp::DiscreteDistributionAbsSquare</a>	72
<a href="#">qpp::Exception</a>	73
<a href="#">qpp::Gates</a>	76
<a href="#">qpp::NormalDistribution</a>	82
<a href="#">qpp::Qudit</a>	83
<a href="#">qpp::RandomDevices</a>	85
<a href="#">qpp::Singleton&lt; T &gt;</a>	86
<a href="#">qpp::States</a>	87
<a href="#">qpp::Timer</a>	90
<a href="#">qpp::UniformIntDistribution</a>	91
<a href="#">qpp::UniformRealDistribution</a>	91



## Chapter 5

# File Index

### 5.1 File List

Here is a list of all files with brief descriptions:

include/ <a href="#">channels.h</a>	93
include/ <a href="#">constants.h</a>	98
include/ <a href="#">entanglement.h</a>	99
include/ <a href="#">entropies.h</a>	100
include/ <a href="#">functions.h</a>	101
include/ <a href="#">internal.h</a>	104
include/ <a href="#">io.h</a>	105
include/ <a href="#">matlab.h</a>	106
include/ <a href="#">qpp.h</a>	107
include/ <a href="#">random.h</a>	108
include/ <a href="#">types.h</a>	109
include/classes/ <a href="#">exception.h</a>	94
include/classes/ <a href="#">gates.h</a>	94
include/classes/ <a href="#">qudit.h</a>	95
include/classes/ <a href="#">randevs.h</a>	95
include/classes/ <a href="#">singleton.h</a>	96
include/classes/ <a href="#">stat.h</a>	97
include/classes/ <a href="#">states.h</a>	97
include/classes/ <a href="#">timer.h</a>	98





## Chapter 6

# Namespace Documentation

### 6.1 qpp Namespace Reference

#### Namespaces

- [internal](#)

#### Classes

- class [DiscreteDistribution](#)
- class [DiscreteDistributionAbsSquare](#)
- class [Exception](#)
- class [Gates](#)
- class [NormalDistribution](#)
- class [Qudit](#)
- class [RandomDevices](#)
- class [Singleton](#)
- class [States](#)
- class [Timer](#)
- class [UniformIntDistribution](#)
- class [UniformRealDistribution](#)

#### Typedefs

- using [cplx](#) = std::complex< double >  
*Complex number in double precision.*
- using [cmat](#) = Eigen::MatrixXcd  
*Complex (double precision) dynamic Eigen matrix.*
- using [dmat](#) = Eigen::MatrixXd  
*Real (double precision) dynamic Eigen matrix.*
- using [ket](#) = Eigen::Matrix< [cplx](#), Eigen::Dynamic, 1 >  
*Complex (double precision) dynamic Eigen column matrix.*
- using [bra](#) = Eigen::Matrix< [cplx](#), 1, Eigen::Dynamic >  
*Complex (double precision) dynamic Eigen row matrix.*
- template<typename Scalar >  
using [DynMat](#) = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >  
*Dynamic Eigen matrix over the field specified by Scalar.*

## Functions

- `cmat super` (const std::vector< `cmat` > &Ks)  
*Superoperator matrix representation.*
- `cmat choi` (const std::vector< `cmat` > &Ks)  
*Choi matrix representation.*
- `std::vector< cmat > choi2kraus` (const `cmat` &A)  
*Extracts orthogonal Kraus operators from Choi matrix.*
- template<typename Derived >  
`cmat channel` (const Eigen::MatrixBase< Derived > &rho, const std::vector< `cmat` > &Ks)  
*Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.*
- template<typename Derived >  
`cmat channel` (const Eigen::MatrixBase< Derived > &rho, const std::vector< `cmat` > &Ks, const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)  
*Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.*
- constexpr std::complex< double > `operator""_i` (unsigned long long int x)  
*User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)*
- constexpr std::complex< double > `operator""_i` (long double x)  
*User-defined literal for complex  $i = \sqrt{-1}$  (real overload)*
- std::complex< double > `omega` (std::size\_t D)  
*D-th root of unity.*
- template<typename Derived >  
`cmat schmidtcoeff` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- template<typename Derived >  
`cmat schmidtU` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- template<typename Derived >  
`cmat schmidtV` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- template<typename Derived >  
`cmat schmidtprob` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- template<typename Derived >  
double `entanglement` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- template<typename Derived >  
double `gconcurrence` (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
double `shannon` (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
double `renyi` (const double alpha, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
double `renyi_inf` (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
double `tsallis` (const double alpha, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
double `qmutualinfo` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- template<typename Derived >  
`DynMat`< typename Derived::Scalar > `transpose` (const Eigen::MatrixBase< Derived > &A)  
*Transpose.*
- template<typename Derived >  
`DynMat`< typename Derived::Scalar > `conjugate` (const Eigen::MatrixBase< Derived > &A)  
*Complex conjugate.*
- template<typename Derived >  
`DynMat`< typename Derived::Scalar > `adjoint` (const Eigen::MatrixBase< Derived > &A)  
*Adjoint.*

- template<typename Derived >  
**DynMat**< typename Derived::Scalar > **inverse** (const Eigen::MatrixBase< Derived > &A)  
*Inverse.*
- template<typename Derived >  
 Derived::Scalar **trace** (const Eigen::MatrixBase< Derived > &A)  
*Trace.*
- template<typename Derived >  
 Derived::Scalar **det** (const Eigen::MatrixBase< Derived > &A)  
*Determinant.*
- template<typename Derived >  
 Derived::Scalar **logdet** (const Eigen::MatrixBase< Derived > &A)  
*Logarithm of the determinant.*
- template<typename Derived >  
 Derived::Scalar **sum** (const Eigen::MatrixBase< Derived > &A)  
*Element-wise sum.*
- template<typename Derived >  
 double **norm** (const Eigen::MatrixBase< Derived > &A)  
*Trace norm.*
- template<typename Derived >  
**cmat evals** (const Eigen::MatrixBase< Derived > &A)  
*Eigenvalues.*
- template<typename Derived >  
**cmat evecs** (const Eigen::MatrixBase< Derived > &A)  
*Eigenvectors.*
- template<typename Derived >  
**dmat hevals** (const Eigen::MatrixBase< Derived > &A)  
*Hermitian eigenvalues.*
- template<typename Derived >  
**cmat hevecs** (const Eigen::MatrixBase< Derived > &A)  
*Hermitian eigenvectors.*
- template<typename Derived >  
**cmat funm** (const Eigen::MatrixBase< Derived > &A, **cplx**(\*f)(const **cplx** &))  
*Functional calculus  $f(A)$*
- template<typename Derived >  
**cmat sqrtm** (const Eigen::MatrixBase< Derived > &A)  
*Matrix square root.*
- template<typename Derived >  
**cmat absm** (const Eigen::MatrixBase< Derived > &A)  
*Matrix absolut value.*
- template<typename Derived >  
**cmat expm** (const Eigen::MatrixBase< Derived > &A)  
*Matrix exponential.*
- template<typename Derived >  
**cmat logm** (const Eigen::MatrixBase< Derived > &A)  
*Matrix logarithm.*
- template<typename Derived >  
**cmat sinm** (const Eigen::MatrixBase< Derived > &A)  
*Matrix sin.*
- template<typename Derived >  
**cmat cosm** (const Eigen::MatrixBase< Derived > &A)  
*Matrix cos.*
- template<typename Derived >  
**cmat spectralpwm** (const Eigen::MatrixBase< Derived > &A, const **cplx** z)

*Matrix power.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > powm (const Eigen::MatrixBase< Derived > &A, std::size_t n)`

*Matrix power.*

- `template<typename OutputScalar , typename Derived >`  
`DynMat< OutputScalar > cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const typename Derived::Scalar &))`

*Functor.*

- `template<typename T >`  
`DynMat< typename T::Scalar > kron (const T &head)`

*Kronecker product (variadic overload)*

- `template<typename T , typename... Args>`  
`DynMat< typename T::Scalar > kron (const T &head, const Args &...tail)`

*Kronecker product (variadic overload)*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > kron (const std::vector< Derived > &As)`

*Kronecker product (std::vector overload)*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > kron (const std::initializer_list< Derived > &As)`

*Kronecker product (std::initializer\_list overload)*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > kronpow (const Eigen::MatrixBase< Derived > &A, std::size_t n)`

*Kronecker power.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > reshape (const Eigen::MatrixBase< Derived > &A, std::size_t rows, std::size_t cols)`

*Reshape.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &perm, const std::vector< std::size_t > &dims)`

*System permutation.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`

*Partial trace.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`

*Partial trace.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`

*Partial trace.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`

*Partial transpose.*

- `template<typename Derived1 , typename Derived2 >`  
`DynMat< typename Derived1::Scalar > comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`

*Commutator.*

- `template<typename Derived1 , typename Derived2 >`  
`DynMat< typename Derived1::Scalar > anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`

- Anti-commutator.*
- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [prj](#) (const Eigen::MatrixBase< Derived > &V)
- Projector.*
- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [expandout](#) (const Eigen::MatrixBase< Derived > &A, std::size\_t pos, const std::vector< std::size\_t > &dims)
- Expand out.*
- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [grams](#) (const std::vector< Derived > &Vs)
- Gram-Schmidt orthogonalization (std::vector overload)*
- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [grams](#) (const std::initializer\_list< Derived > &Vs)
- Gram-Schmidt orthogonalization (std::initializer\_list overload)*
- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [grams](#) (const Eigen::MatrixBase< Derived > &A)
- Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)*
- std::vector< std::size\_t > [n2multiidx](#) (std::size\_t n, const std::vector< std::size\_t > &dims)
- Non-negative integer index to multi-index.*
- std::size\_t [multiidx2n](#) (const std::vector< std::size\_t > &midx, const std::vector< std::size\_t > &dims)
- Multi-index to non-negative integer index.*
- [ket mket](#) (const std::vector< std::size\_t > &mask)
- Multi-partite qubit ket.*
- [ket mket](#) (const std::vector< std::size\_t > &mask, const std::vector< std::size\_t > &dims)
- Multi-partite qudit ket (different dimensions overload)*
- [ket mket](#) (const std::vector< std::size\_t > &mask, std::size\_t d)
- Multi-partite qudit ket (same dimensions overload)*
- std::vector< std::size\_t > [invperm](#) (const std::vector< std::size\_t > &perm)
- Inverse permutation.*
- std::vector< std::size\_t > [compperm](#) (const std::vector< std::size\_t > &perm, const std::vector< std::size\_t > &sigma)
- Compose permutations.*
- template<typename T >  
void [disp](#) (const T &x, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)
- template<typename T >  
void [displn](#) (const T &x, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)
- template<typename T >  
void [disp](#) (const T \*x, const std::size\_t n, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)
- template<typename T >  
void [displn](#) (const T \*x, const std::size\_t n, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)
- template<typename Derived >  
void [disp](#) (const Eigen::MatrixBase< Derived > &A, double [chop=chop](#), std::ostream &os=std::cout)
- template<typename Derived >  
void [displn](#) (const Eigen::MatrixBase< Derived > &A, double [chop=chop](#), std::ostream &os=std::cout)
- void [disp](#) (const [cplx](#) c, double [chop=chop](#), std::ostream &os=std::cout)
- void [displn](#) (const [cplx](#) c, double [chop=chop](#), std::ostream &os=std::cout)
- template<typename Derived >  
void [save](#) (const Eigen::MatrixBase< Derived > &A, const std::string &fname)
- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [load](#) (const std::string &fname)

- `template<typename Derived >`  
Derived `loadMATLABmatrix` (const std::string &mat\_file, const std::string &var\_name)
- `template<>`  
`dmat loadMATLABmatrix` (const std::string &mat\_file, const std::string &var\_name)
- `template<>`  
`cmat loadMATLABmatrix` (const std::string &mat\_file, const std::string &var\_name)
- `template<typename Derived >`  
void `saveMATLABmatrix` (const Eigen::MatrixBase< Derived > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)
- `template<>`  
void `saveMATLABmatrix` (const Eigen::MatrixBase< `dmat` > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)
- `template<>`  
void `saveMATLABmatrix` (const Eigen::MatrixBase< `cmat` > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)
- `template<typename Derived >`  
Derived `rand` (std::size\_t rows, std::size\_t cols, double a=0, double b=1)
- `template<>`  
`dmat rand` (std::size\_t rows, std::size\_t cols, double a, double b)
- `template<>`  
`cmat rand` (std::size\_t rows, std::size\_t cols, double a, double b)
- double `rand` (double a=0, double b=1)
- long long `randint` (long long a, long long b)
- `template<typename Derived >`  
Derived `randn` (std::size\_t rows, std::size\_t cols, double mean=0, double sigma=1)
- `template<>`  
`dmat randn` (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- `template<>`  
`cmat randn` (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- double `randn` (double mean=0, double sigma=1)
- `cmat randU` (std::size\_t D)
- `cmat randV` (std::size\_t Din, std::size\_t Dout)
- std::vector< `cmat` > `randkraus` (std::size\_t n, std::size\_t D)
- `cmat randH` (std::size\_t D)
- `ket randket` (std::size\_t D)
- `cmat randrho` (std::size\_t D)
- std::vector< std::size\_t > `randperm` (std::size\_t n)

## Variables

- constexpr double `chop` = 1e-10  
*Used in `qpp::disp()` and `qpp::displn()` for setting to zero numbers that have their absolute value smaller than `qpp::ct::chop`.*
- constexpr double `eps` = 1e-12  
*Used to decide whether a number or expression in double precision is zero or not.*
- constexpr std::size\_t `maxn` = 64  
*Maximum number of qubits.*
- constexpr double `pi` = 3.141592653589793238462643383279502884  
 $\pi$
- constexpr double `ee` = 2.718281828459045235360287471352662497  
*Base of natural logarithm,  $e$ .*
- `RandomDevices` & `rdevs` = `RandomDevices::get_instance()`  
*`qpp::RandomDevices Singleton`*
- const `Gates` & `gt` = `Gates::get_instance()`

- `qpp::Gates` *const Singleton*
- `const States & st = States::get_instance()`
- `qpp::States` *const Singleton*

## 6.1.1 Typedef Documentation

### 6.1.1.1 `using qpp::bra = typedef Eigen::Matrix<cplx, 1, Eigen::Dynamic>`

Complex (double precision) dynamic Eigen row matrix.

### 6.1.1.2 `using qpp::cmat = typedef Eigen::MatrixXcd`

Complex (double precision) dynamic Eigen matrix.

### 6.1.1.3 `using qpp::cplx = typedef std::complex<double>`

Complex number in double precision.

### 6.1.1.4 `using qpp::dmat = typedef Eigen::MatrixXd`

Real (double precision) dynamic Eigen matrix.

### 6.1.1.5 `template<typename Scalar > using qpp::DynMat = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>`

Dynamic Eigen matrix over the field specified by *Scalar*.

Example:

```
auto mat = DynMat<float>(2,3); // type of mat is Eigen::Matrix<float, Eigen::Dynamic, Eigen::Dynamic>
```

### 6.1.1.6 `using qpp::ket = typedef Eigen::Matrix<cplx, Eigen::Dynamic, 1>`

Complex (double precision) dynamic Eigen column matrix.

## 6.1.2 Function Documentation

### 6.1.2.1 `template<typename Derived > cmat qpp::absm ( const Eigen::MatrixBase< Derived > & A )`

Matrix absolut value.

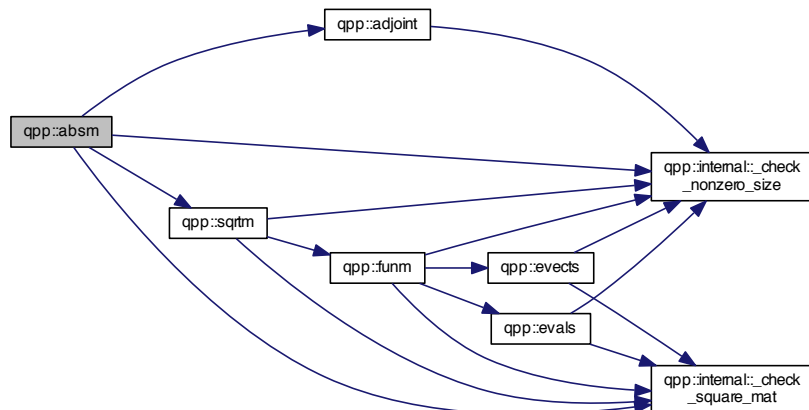
Parameters

<i>A</i>	Eigen expression
----------	------------------

## Returns

Matrix absolut value of  $A$ , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.2 `template<typename Derived > DynMat<typename Derived::Scalar> qpp::adjoint ( const Eigen::MatrixBase< Derived > & A )`

Adjoint.

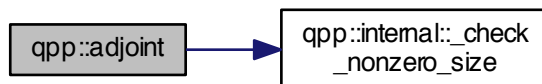
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Adjoint (Hermitian conjugate) of  $A$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.3 `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::anticomm ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )`

Anti-commutator.

Anti-commutator  $\{A, B\} = AB + BA$

Both  $A$  and  $B$  must be Eigen expressions over the same scalar field



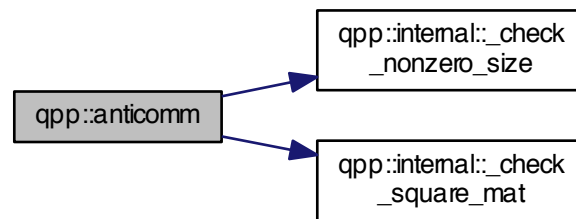
## Parameters

$A$	Eigen expression
$B$	Eigen expression

## Returns

Anti-commutator  $AB + BA$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.4 `template<typename Derived > cmat qpp::channel ( const Eigen::MatrixBase< Derived > & rho, const std::vector< cmat > & Ks )`

Applies the channel specified by the set of Kraus operators  $Ks$  to the density matrix  $\rho$ .

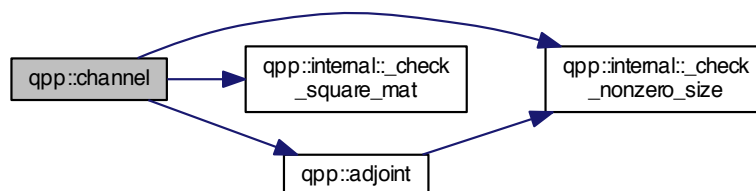
## Parameters

$\rho$	Eigen expression
$Ks$	<code>std::vector</code> of Eigen expressions representing the set of Kraus operators

## Returns

Output density matrix, as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.5 `template<typename Derived > cmat qpp::channel ( const Eigen::MatrixBase< Derived > & rho, const std::vector< cmat > & Ks, const std::vector< std::size_t > & subsys, const std::vector< std::size_t > & dims )`

Applies the channel specified by the set of Kraus operators *Ks* to the part of the density matrix *rho* specified by *subsys*.

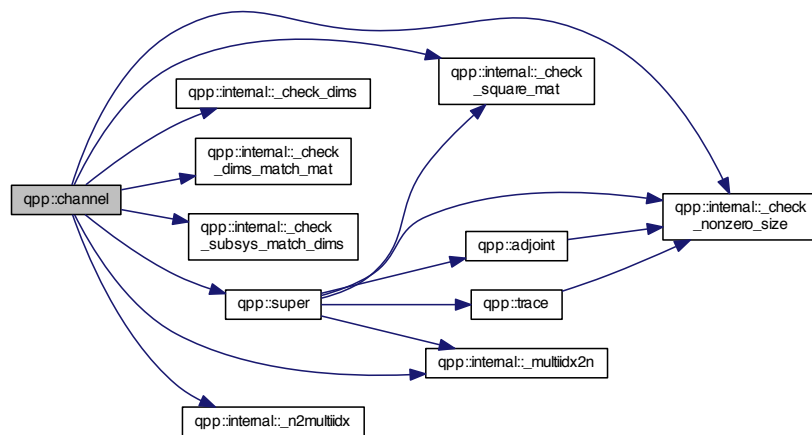
## Parameters

<i>rho</i>	Eigen expression
<i>Ks</i>	std::vector of Eigen expressions representing the set of Kraus operators
<i>subsys</i>	Subsystems' indexes
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Output density matrix, as a dynamic matrix over the complex field

Here is the call graph for this function:



## 6.1.2.6 cmat qpp::choi ( const std::vector&lt; cmat &gt; &amp; Ks )

Choi matrix representation.

Constructs the Choi matrix of the channel specified by the set of Kraus operators  $Ks$  in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

## Note

the superoperator matrix  $S$  and the Choi matrix  $C$  are related by  $S_{ab,mn} = C_{ma,nb}$

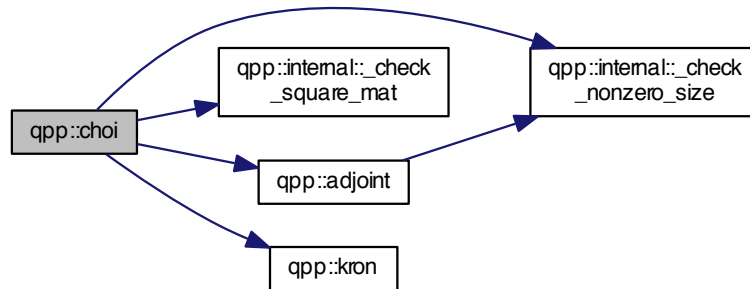
## Parameters

<i>Ks</i>	std::vector of Eigen expressions representing the set of Kraus operators
-----------	--

**Returns**

Choi matrix representation, as a dynamic matrix over the complex field

Here is the call graph for this function:



### 6.1.2.7 `std::vector<cmat> qpp::choi2kraus ( const cmat & A )`

Extracts orthogonal Kraus operators from Choi matrix.

Extracts a set of orthogonal (under Hilbert-Schmidt operator norm) Kraus operators from the Choi representation  $A$  of the channel

**Note**

The Kraus operators satisfy  $Tr(K_i^\dagger K_j) = \delta_{ij}$  for all  $i \neq j$

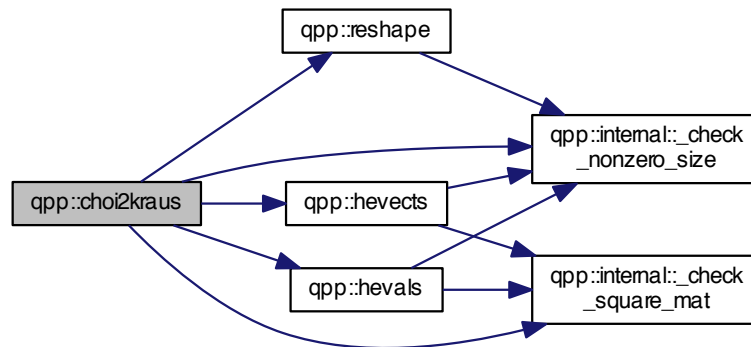
**Parameters**

$A$	Choi matrix
-----	-------------

## Returns

std::vector of dynamic matrices over the complex field representing the set of Kraus operators

Here is the call graph for this function:



**6.1.2.8** `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::comm ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )`

Commutator.

Commutator  $[A, B] = AB - BA$

Both  $A$  and  $B$  must be Eigen expressions over the same scalar field

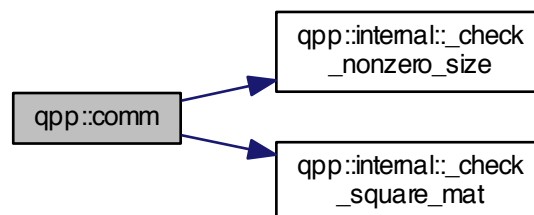
## Parameters

$A$	Eigen expression
$B$	Eigen expression

## Returns

Commutator  $AB - BA$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.9 `std::vector<std::size_t> qpp::compperm ( const std::vector< std::size_t > & perm, const std::vector< std::size_t > & sigma )`

Compose permutations.

## Parameters

<i>perm</i>	Permutation
<i>sigma</i>	Permutation

## Returns

Composition of the permutations  $perm \circ sigma = perm(sigma)$

Here is the call graph for this function:



6.1.2.10 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::conjugate ( const Eigen::MatrixBase<Derived> & A )`

Complex conjugate.

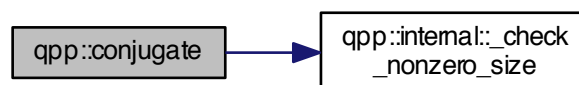
## Parameters

<i>A</i>	Eigen expression
----------	------------------

## Returns

Complex conjugate of *A*, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.11 `template<typename Derived> cmat qpp::cosm ( const Eigen::MatrixBase<Derived> & A )`

Matrix cos.

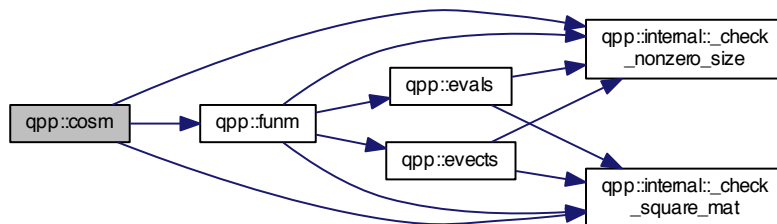
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Matrix cosine of  $A$ , as a dynamic matrix over the complex field

Here is the call graph for this function:



**6.1.2.12** `template<typename OutputScalar , typename Derived > DynMat<OutputScalar> qpp::cwise ( const Eigen::MatrixBase< Derived > & A, OutputScalar*)(const typename Derived::Scalar &) f )`

Functor.

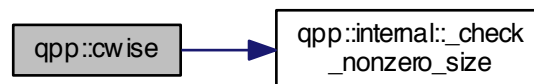
## Parameters

$A$	Eigen expression
$f$	Pointer-to-function from scalars of $A$ to <i>OutputScalar</i>

## Returns

Component-wise  $f(A)$ , as a dynamic matrix over the *OutputScalar* scalar field

Here is the call graph for this function:



**6.1.2.13** `template<typename Derived > Derived::Scalar qpp::det ( const Eigen::MatrixBase< Derived > & A )`

Determinant.



## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Determinant of  $A$ , as a dynamic matrix over the same scalar field  
 Returns  $\pm\infty$  when the determinant overflows/underflows

Here is the call graph for this function:



6.1.2.14 `template<typename T> void qpp::disp ( const T & x, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )`

6.1.2.15 `template<typename T> void qpp::disp ( const T * x, const std::size_t n, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )`

6.1.2.16 `template<typename Derived> void qpp::disp ( const Eigen::MatrixBase< Derived> & A, double chop = chop, std::ostream & os = std::cout )`

6.1.2.17 `void qpp::disp ( const cplx c, double chop = chop, std::ostream & os = std::cout )`

Here is the call graph for this function:



6.1.2.18 `template<typename T> void qpp::displn ( const T & x, const std::string & separator, const std::string & start = " [", const std::string & end = "]" , std::ostream & os = std::cout )`

Here is the call graph for this function:



6.1.2.19 `template<typename T> void qpp::displn ( const T * x, const std::size_t n, const std::string & separator, const std::string & start = " [", const std::string & end = "]" , std::ostream & os = std::cout )`

Here is the call graph for this function:



6.1.2.20 `template<typename Derived> void qpp::displn ( const Eigen::MatrixBase< Derived > & A, double chop = chop, std::ostream & os = std::cout )`

Here is the call graph for this function:



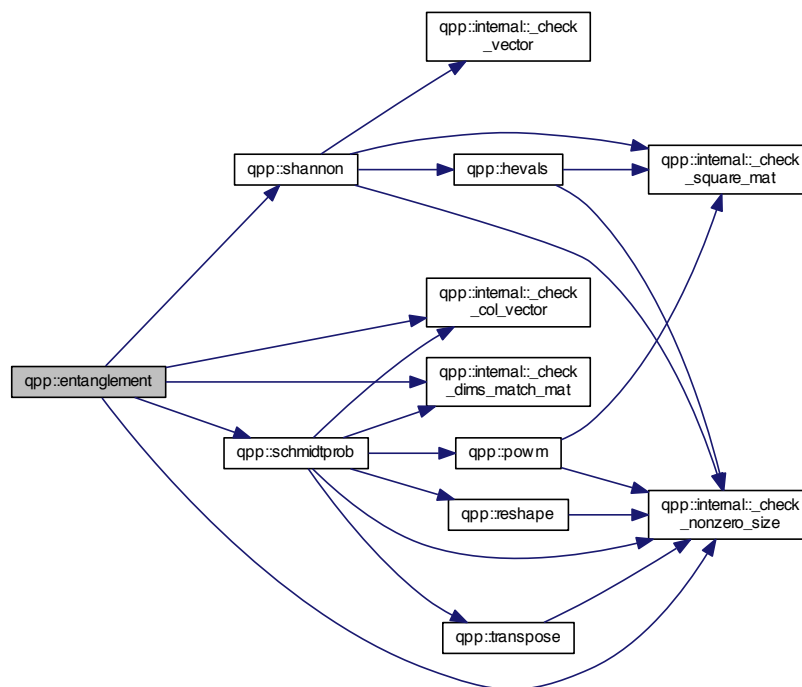
6.1.2.21 `void qpp::displn ( const cplx c, double chop = chop, std::ostream & os = std::cout )`

Here is the call graph for this function:



6.1.2.22 `template<typename Derived> double qpp::entanglement ( const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & dims )`

Here is the call graph for this function:



6.1.2.23 `template<typename Derived> cmat qpp::evals ( const Eigen::MatrixBase< Derived> & A )`

Eigenvalues.

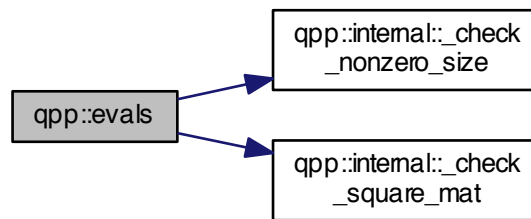
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Eigenvalues of  $A$ , as a diagonal dynamic matrix over the complex field, with eigenvalues on the diagonal

Here is the call graph for this function:



6.1.2.24 `template<typename Derived> cmat qpp::evecs ( const Eigen::MatrixBase< Derived> & A )`

Eigenvectors.

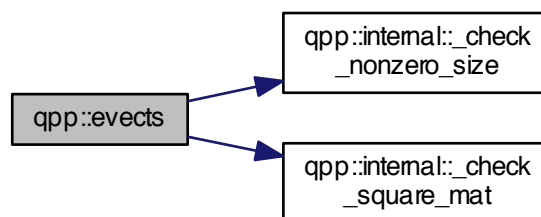
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Eigenvectors of  $A$ , as columns of a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.25 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::expandout ( const Eigen::MatrixBase<Derived> & A, std::size_t pos, const std::vector< std::size_t> & dims )`

Expand out.

Expand out  $A$  as a matrix in a multi-partite system

Faster than using `qpp::kron(I, I, ..., I, A, I, ..., I)`

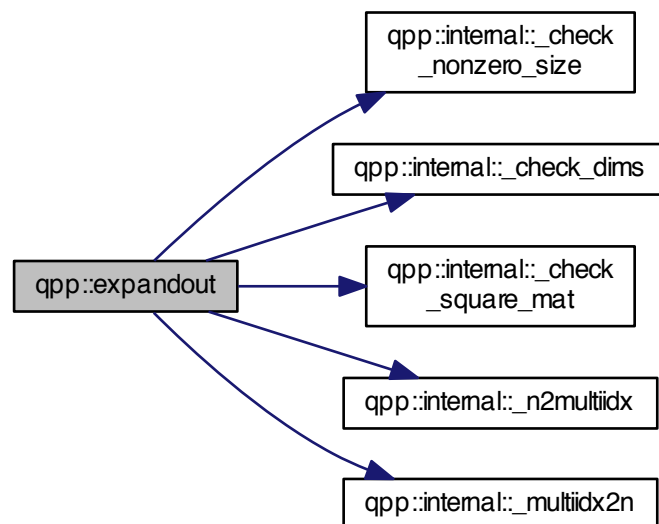
Parameters

$A$	Eigen expression
$pos$	Position
$dims$	Dimensions of the multi-partite system

Returns

Tensor product  $I \otimes \dots \otimes I \otimes A \otimes I \otimes \dots \otimes I$ , with  $A$  on position  $pos$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.26 `template<typename Derived> cmat qpp::expm ( const Eigen::MatrixBase<Derived> & A )`

Matrix exponential.

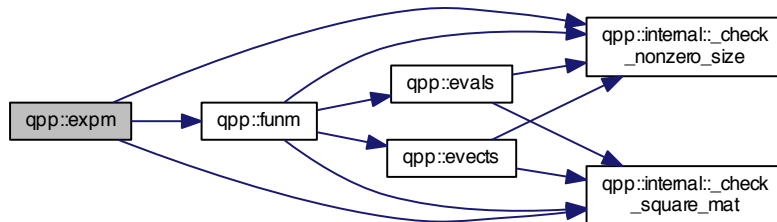
Parameters

$A$	Eigen expression
-----	------------------

**Returns**

Matrix exponential of  $A$ , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.27 `template<typename Derived> cmat qpp::funm ( const Eigen::MatrixBase< Derived> & A, cplx(*) (const cplx &) f )`

Functional calculus  $f(A)$

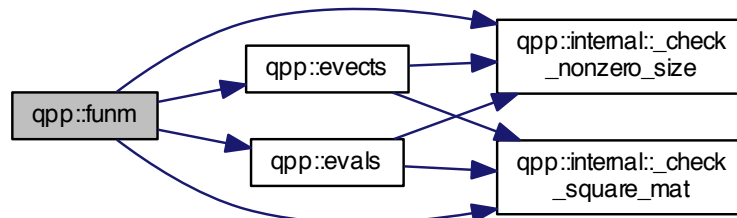
**Parameters**

$A$	Eigen expression
$f$	Pointer-to-function from complex to complex

**Returns**

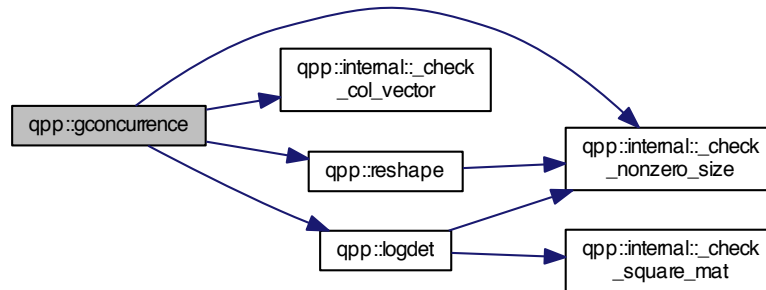
$f(A)$ , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.28 `template<typename Derived> double qpp::gconcurrency ( const Eigen::MatrixBase< Derived> & A )`

Here is the call graph for this function:



6.1.2.29 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::grams ( const std::vector< Derived> & Vs )`

Gram-Schmidt orthogonalization (std::vector overload)

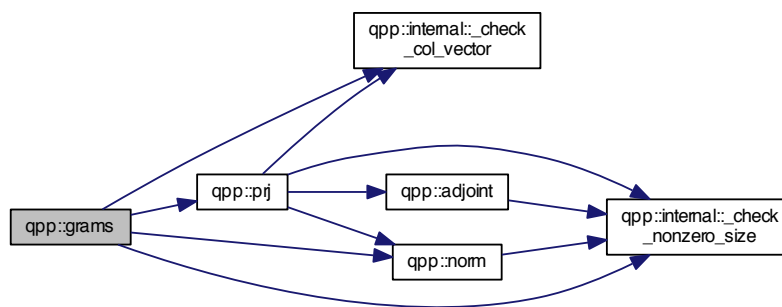
Parameters

<code>Vs</code>	std::vector of Eigen expressions as column vectors
-----------------	--

Returns

Gram-Schmidt vectors of `Vs` as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.30 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::grams ( const std::initializer_list< Derived> & Vs )`

Gram-Schmidt orthogonalization (std::initializer\_list overload)

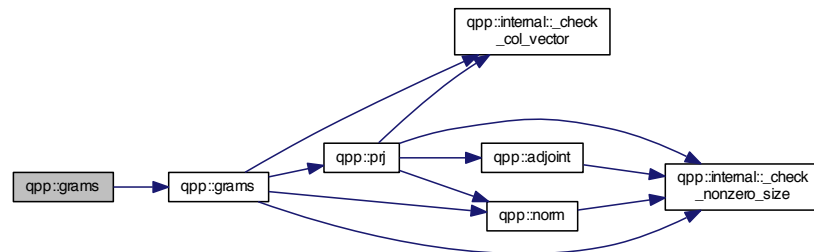
## Parameters

$V$ s	std::initializer_list of Eigen expressions as column vectors
-------	--

## Returns

Gram-Schmidt vectors of  $V$ s as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.31 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::grams ( const Eigen::MatrixBase<Derived> & A )`

Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)

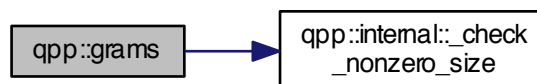
## Parameters

$A$	Eigen expression, the input vectors are the columns of $A$
-----	--

## Returns

Gram-Schmidt vectors of the columns of  $A$ , as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.32 `template<typename Derived> dmat qpp::hevals ( const Eigen::MatrixBase<Derived> & A )`

Hermitian eigenvalues.



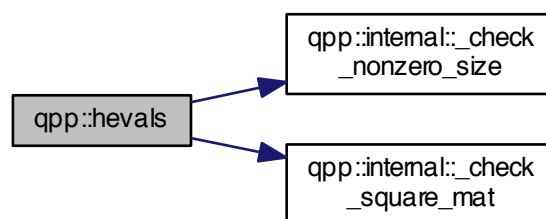
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Eigenvalues of Hermitian  $A$ , as a diagonal dynamic matrix over the real field, with eigenvalues on the diagonal

Here is the call graph for this function:



6.1.2.33 `template<typename Derived> cmat qpp::hevects ( const Eigen::MatrixBase< Derived > & A )`

Hermitian eigenvectors.

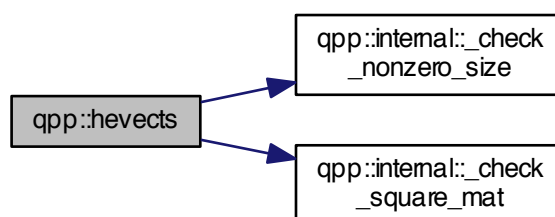
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Eigenvectors of Hermitian  $A$ , as columns of a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.34 `template<typename Derived > DynMat<typename Derived::Scalar> qpp::inverse ( const Eigen::MatrixBase<Derived > & A )`

Inverse.

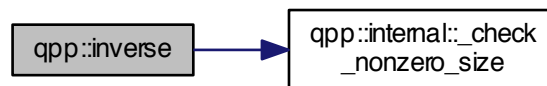
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Inverse of  $A$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.35 `std::vector<std::size_t> qpp::invperm ( const std::vector< std::size_t > & perm )`

Inverse permutation.

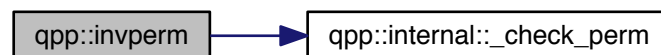
## Parameters

<i>perm</i>	Permutation
-------------	-------------

## Returns

Inverse of the permutation *perm*

Here is the call graph for this function:



6.1.2.36 `template<typename T> DynMat<typename T::Scalar> qpp::kron ( const T & head )`

Kronecker product (variadic overload)

Used to stop the recursion for the variadic template version of [qpp::kron\(\)](#)

## Parameters

<i>head</i>	Eigen expression
-------------	------------------

**Returns**

Its argument *head*

**6.1.2.37** `template<typename T, typename... Args> DynMat<typename T::Scalar> qpp::kron ( const T & head, const Args &... tail )`

Kronecker product (variadic overload)

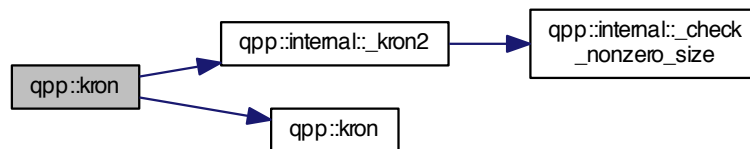
**Parameters**

<i>head</i>	Eigen expression
<i>tail</i>	Variadic Eigen expression (zero or more parameters)

**Returns**

Kronecker product of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



**6.1.2.38** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::kron ( const std::vector< Derived > & As )`

Kronecker product (std::vector overload)

**Parameters**

<i>As</i>	std::vector of Eigen expressions
-----------	----------------------------------

**Returns**

Kronecker product of all elements in  $As$ , evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



**6.1.2.39** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::kron ( const std::initializer_list< Derived > & As )`

Kronecker product (std::initializer\_list overload)

**Parameters**

$As$	std::initializer_list of Eigen expressions, such as $\{A1, A2, \dots, Ak\}$
------	---

**Returns**

Kronecker product of all elements in  $As$ , evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



**6.1.2.40** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::kronpow ( const Eigen::MatrixBase< Derived > & A, std::size_t n )`

Kronecker power.

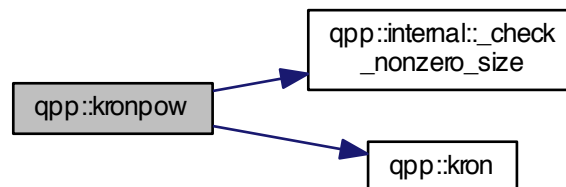
**Parameters**

$A$	Eigen expression
$n$	Non-negative integer

**Returns**

Kronecker product of  $A$  with itself  $n$  times  $A^{\otimes n}$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.41 `template<typename Derived > DynMat<typename Derived::Scalar> qpp::load ( const std::string & fname )`

6.1.2.42 `template<typename Derived > Derived qpp::loadMATLABmatrix ( const std::string & mat_file, const std::string & var_name )`

6.1.2.43 `template<> dmat qpp::loadMATLABmatrix ( const std::string & mat_file, const std::string & var_name )`

6.1.2.44 `template<> cmat qpp::loadMATLABmatrix ( const std::string & mat_file, const std::string & var_name )`

6.1.2.45 `template<typename Derived > Derived::Scalar qpp::logdet ( const Eigen::MatrixBase< Derived > & A )`

Logarithm of the determinant.

Especially useful when the determinant overflows/underflows

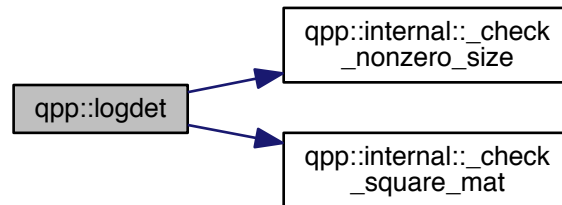
**Parameters**

$A$	Eigen expression
-----	------------------

## Returns

Logarithm of the determinant of  $A$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.46 `template<typename Derived> cmat qpp::logm ( const Eigen::MatrixBase< Derived> & A )`

Matrix logarithm.

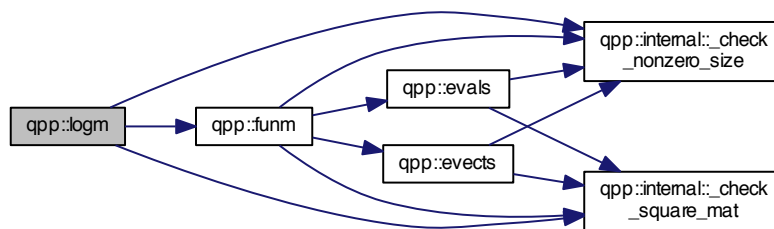
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Matrix logarithm of  $A$ , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.47 `ket qpp::mket ( const std::vector< std::size_t> & mask )`

Multi-partite qubit ket.

Constructs the multi-partite qubit ket  $|\text{mask}\rangle$ , where *mask* is a `std::vector` of 0's and 1's

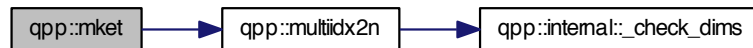
## Parameters

<i>mask</i>	std::vector of 0's and 1's
-------------	----------------------------

## Returns

Multi-partite qubit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



#### 6.1.2.48 ket qpp::mket ( const std::vector< std::size\_t > & mask, const std::vector< std::size\_t > & dims )

Multi-partite qudit ket (different dimensions overload)

Constructs the multi-partite qudit ket  $|\text{mask}\rangle$ , where *mask* is a std::vector of non-negative integers  
Each element in *mask* has to be smaller than the corresponding element in *dims*

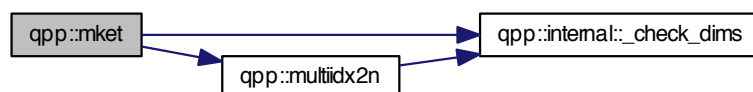
## Parameters

<i>mask</i>	std::vector of non-negative integers
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Multi-partite qudit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



#### 6.1.2.49 ket qpp::mket ( const std::vector< std::size\_t > & mask, std::size\_t d )

Multi-partite qudit ket (same dimensions overload)

Constructs the multi-partite qudit ket  $|\text{mask}\rangle$  in a multi-partite system, all subsystem having equal dimension *d*  
*mask* is a std::vector of non-negative integers, and each element in *mask* has to be strictly smaller than *d*



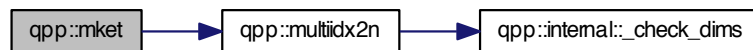
## Parameters

<i>mask</i>	std::vector of non-negative integers
<i>d</i>	Subsystems' dimension

## Returns

Multi-partite qudit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



6.1.2.50 `std::size_t qpp::multidx2n ( const std::vector< std::size_t > & midx, const std::vector< std::size_t > & dims )`

Multi-index to non-negative integer index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

## Parameters

<i>midx</i>	Multi-index
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Non-negative integer index

Here is the call graph for this function:



6.1.2.51 `std::vector<std::size_t> qpp::n2multidx ( std::size_t n, const std::vector< std::size_t > & dims )`

Non-negative integer index to multi-index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

## Parameters

<i>n</i>	Non-negative integer index
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Multi-index of the same size as *dims*

Here is the call graph for this function:



#### 6.1.2.52 `template<typename Derived > double qpp::norm ( const Eigen::MatrixBase< Derived > & A )`

Trace norm.

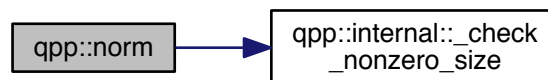
## Parameters

<i>A</i>	Eigen expression
----------	------------------

## Returns

Trace norm (Frobenius norm) of *A*, as a real number

Here is the call graph for this function:



#### 6.1.2.53 `std::complex<double> qpp::omega ( std::size_t D )`

D-th root of unity.

## Parameters

$D$	Non-negative integer
-----	----------------------

**Returns**

$D$ -th root of unity  $\exp(2\pi i/D)$

**6.1.2.54** `constexpr std::complex<double> qpp::operator""_i ( unsigned long long int x )`

User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)

Example:

```
auto z = 4_i; // type of z is std::complex<double>
```

**6.1.2.55** `constexpr std::complex<double> qpp::operator""_i ( long double x )`

User-defined literal for complex  $i = \sqrt{-1}$  (real overload)

Example:

```
auto z = 4.5_i; // type of z is std::complex<double>
```

**6.1.2.56** `template<typename Derived > DynMat<typename Derived::Scalar> qpp::powm ( const Eigen::MatrixBase<Derived > &A, std::size_t n )`

Matrix power.

Explicitly multiplies the matrix  $A$  with itself  $n$  times

By convention  $A^0 = I$

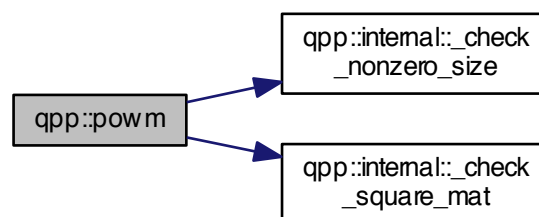
**Parameters**

$A$	Eigen expression
$n$	Non-negative integer

**Returns**

Matrix power  $A^n$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.57 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::prj ( const Eigen::MatrixBase< Derived> & V )`

Projector.

Normalized projector onto state vector

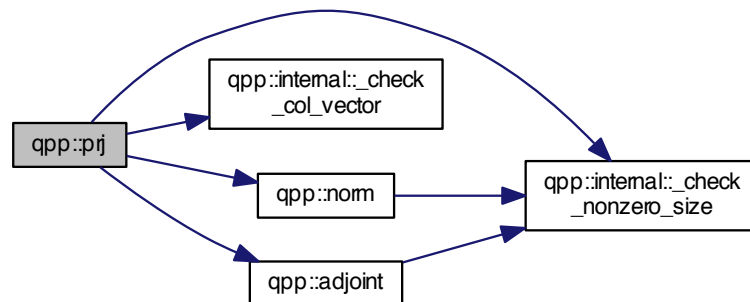
Parameters

<i>V</i>	Eigen expression
----------	------------------

Returns

Projector onto the state vector *V*, or the matrix *Zero* if *V* has norm zero (i.e. smaller than [qpp::eps](#)), as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.58 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::ptrace ( const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & subsys, const std::vector< std::size_t> & dims )`

Partial trace.

Partial trace of the multi-partite density matrix over a list of subsystems

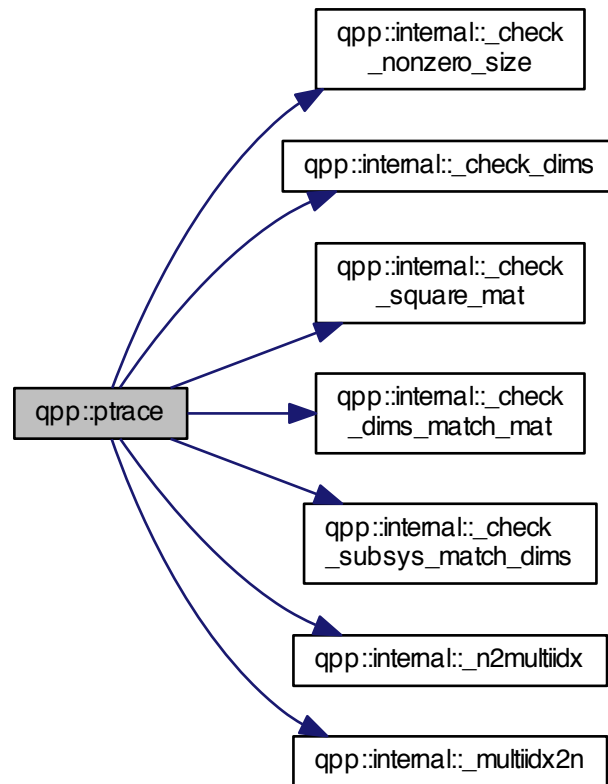
Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystems' indexes
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Partial trace  $Tr_{subsys}(\cdot)$  over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.59 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::ptrace1 ( const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & dims )`

Partial trace.

Partial trace of density matrix over the first subsystem in a bi-partite system

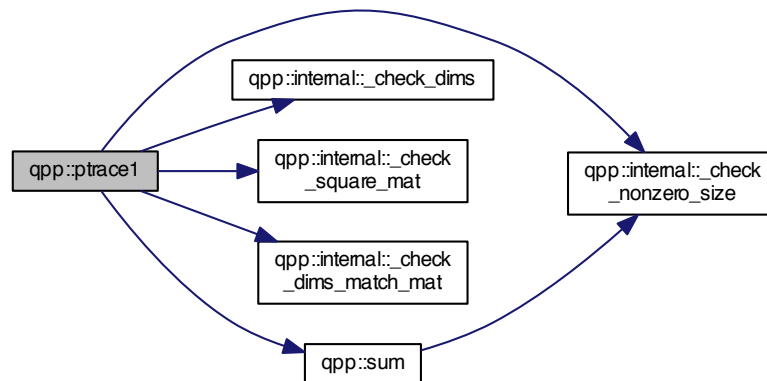
## Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of bi-partite system (must be a <code>std::vector</code> with 2 elements)

**Returns**

Partial trace  $Tr_A(\cdot)$  over the first subsystem  $A$  in a bi-partite system  $A \otimes B$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.60 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::ptrace2 ( const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & dims )`

Partial trace.

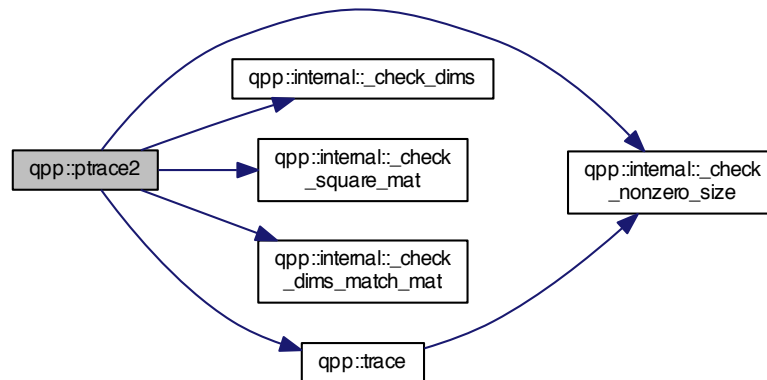
**Parameters**

$A$	Eigen expression
$dims$	Dimensions of bi-partite system (must be a <code>std::vector</code> with 2 elements)

**Returns**

Partial trace  $Tr_B(\cdot)$  over the second subsystem  $B$  in a bi-partite system  $A \otimes B$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



**6.1.2.61** `template<typename Derived> DynMat<typename Derived::Scalar> qpp::ptranspose ( const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & subsys, const std::vector< std::size_t > & dims )`

Partial transpose.

Partial transpose of the multi-partite density matrix over a list of subsystems

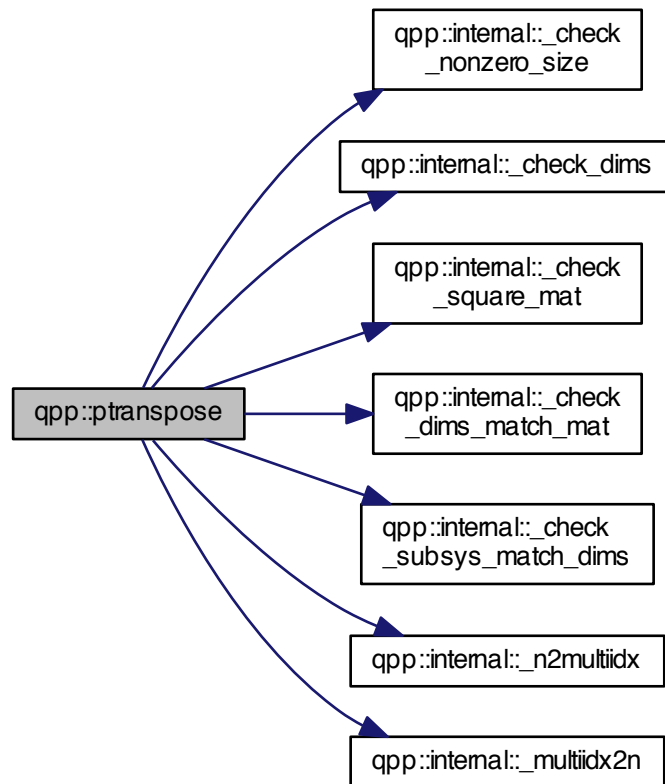
**Parameters**

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystems' indexes
<i>dims</i>	Dimensions of the multi-partite system

**Returns**

Partial transpose  $(\cdot)^{T_{subsys}}$  over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field

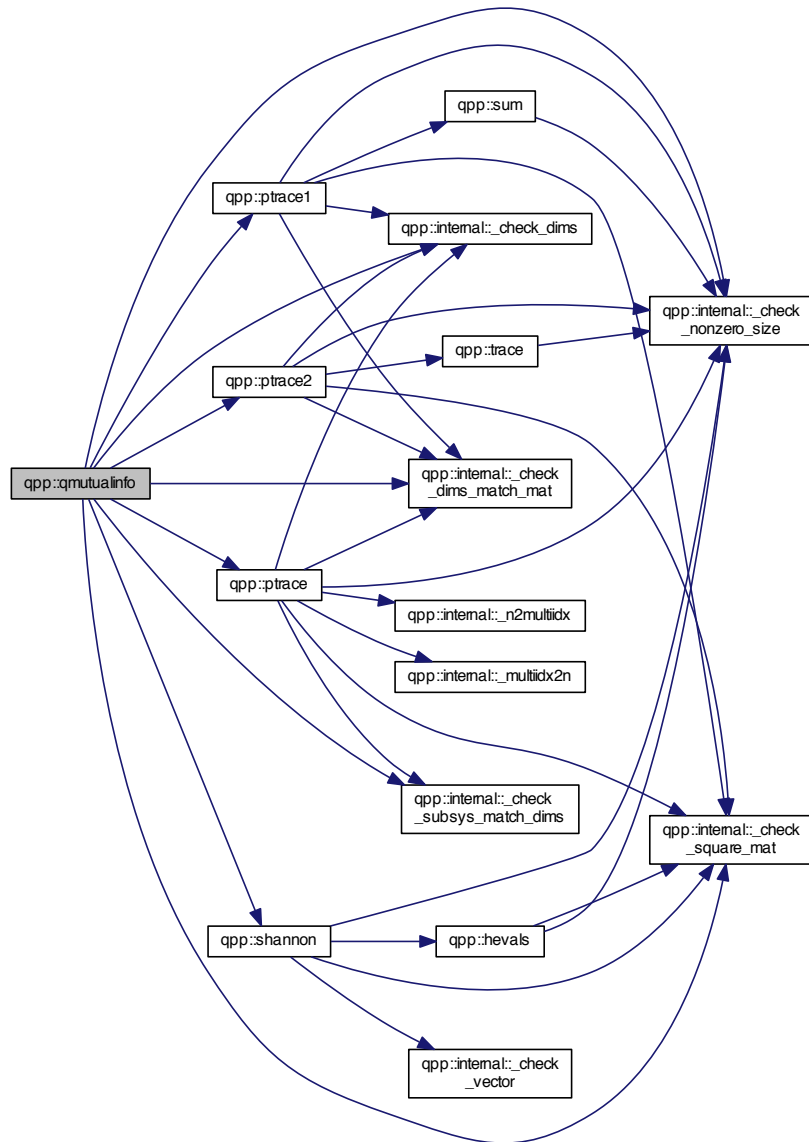
Here is the call graph for this function:





6.1.2.62 `template<typename Derived> double qpp::qmutualinfo ( const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & subsys, const std::vector< std::size_t> & dims )`

Here is the call graph for this function:



6.1.2.63 `template<typename Derived> Derived qpp::rand ( std::size_t rows, std::size_t cols, double a = 0, double b = 1 )`

6.1.2.64 `template<> dmat qpp::rand ( std::size_t rows, std::size_t cols, double a, double b )`

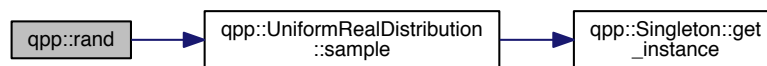
6.1.2.65 `template<> cmat qpp::rand ( std::size_t rows, std::size_t cols, double a, double b )`

Here is the call graph for this function:



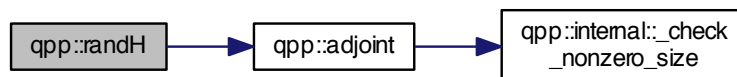
6.1.2.66 `double qpp::rand ( double a = 0, double b = 1 )`

Here is the call graph for this function:



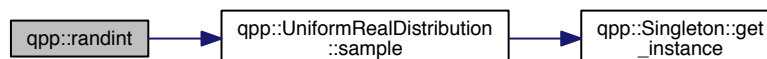
6.1.2.67 `cmat qpp::randH ( std::size_t D )`

Here is the call graph for this function:



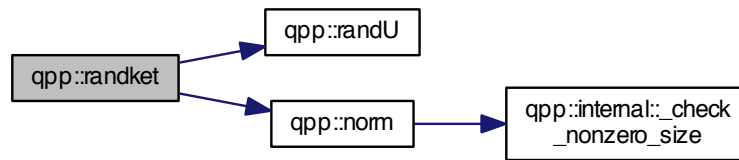
6.1.2.68 `long long qpp::randint ( long long a, long long b )`

Here is the call graph for this function:

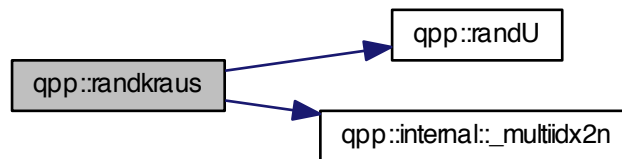


6.1.2.69 `ket qpp::randket ( std::size_t D )`

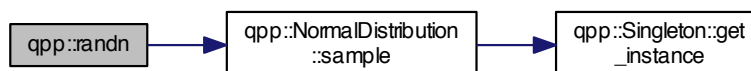
Here is the call graph for this function:

6.1.2.70 `std::vector<cmat> qpp::randkraus ( std::size_t n, std::size_t D )`

Here is the call graph for this function:

6.1.2.71 `template<typename Derived > Derived qpp::randn ( std::size_t rows, std::size_t cols, double mean = 0, double sigma = 1 )`6.1.2.72 `template<> dmat qpp::randn ( std::size_t rows, std::size_t cols, double mean, double sigma )`

Here is the call graph for this function:



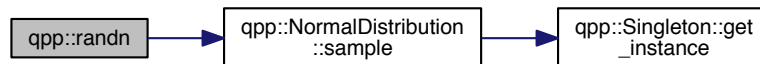
6.1.2.73 `template<> cmat qpp::randn ( std::size_t rows, std::size_t cols, double mean, double sigma )`

Here is the call graph for this function:



6.1.2.74 `double qpp::randn ( double mean = 0, double sigma = 1 )`

Here is the call graph for this function:



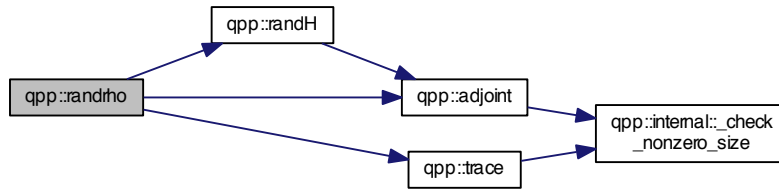
6.1.2.75 `std::vector<std::size_t> qpp::randperm ( std::size_t n )`

Here is the call graph for this function:



6.1.2.76 `cmat qpp::randrho ( std::size_t D )`

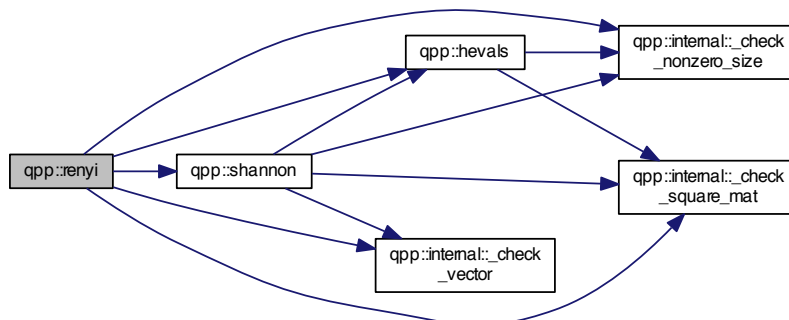
Here is the call graph for this function:

6.1.2.77 `cmat qpp::randU ( std::size_t D )`6.1.2.78 `cmat qpp::randV ( std::size_t Din, std::size_t Dout )`

Here is the call graph for this function:

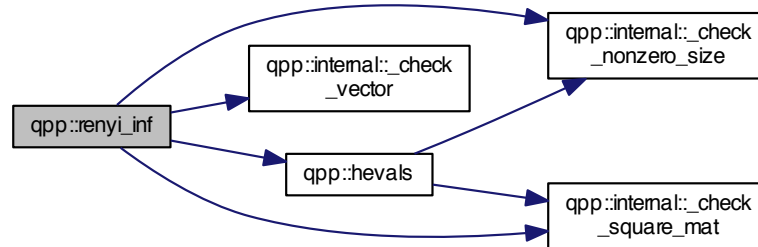
6.1.2.79 `template<typename Derived> double qpp::renyi ( const double alpha, const Eigen::MatrixBase< Derived > & A )`

Here is the call graph for this function:



6.1.2.80 `template<typename Derived> double qpp::renyi_inf ( const Eigen::MatrixBase< Derived> & A )`

Here is the call graph for this function:



6.1.2.81 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::reshape ( const Eigen::MatrixBase< Derived> & A, std::size_t rows, std::size_t cols )`

Reshape.

Uses column-major order when reshaping (same as MATLAB)

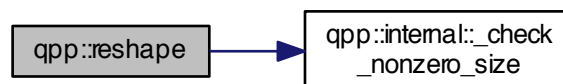
Parameters

<i>A</i>	Eigen expression
<i>rows</i>	Number of rows of the reshaped matrix
<i>cols</i>	Number of columns of the reshaped matrix

Returns

Reshaped matrix with *rows* rows and *cols* columns, as a dynamic matrix over the same scalar field

Here is the call graph for this function:

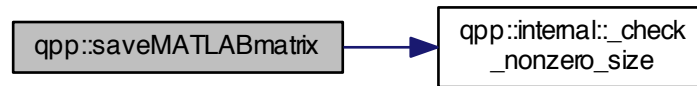


6.1.2.82 `template<typename Derived> void qpp::save ( const Eigen::MatrixBase< Derived> & A, const std::string & fname )`

6.1.2.83 `template<typename Derived> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< Derived> & A, const std::string & mat_file, const std::string & var_name, const std::string & mode )`

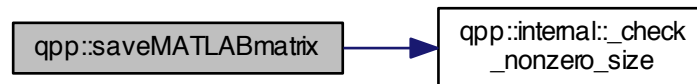
6.1.2.84 `template<> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< dmat > & A, const std::string & mat_file, const std::string & var_name, const std::string & mode )`

Here is the call graph for this function:



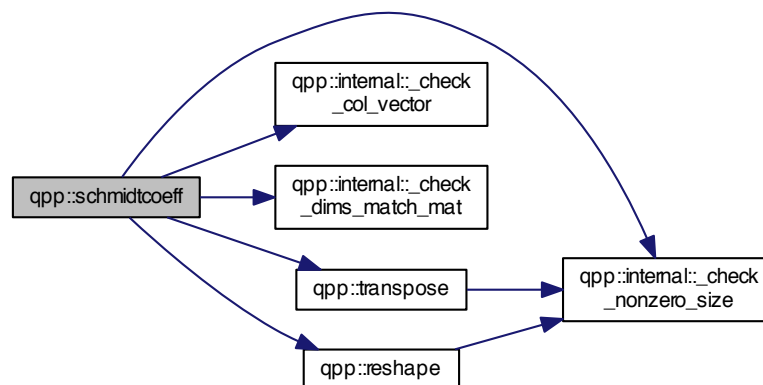
6.1.2.85 `template<> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< cmat > & A, const std::string & mat_file, const std::string & var_name, const std::string & mode )`

Here is the call graph for this function:



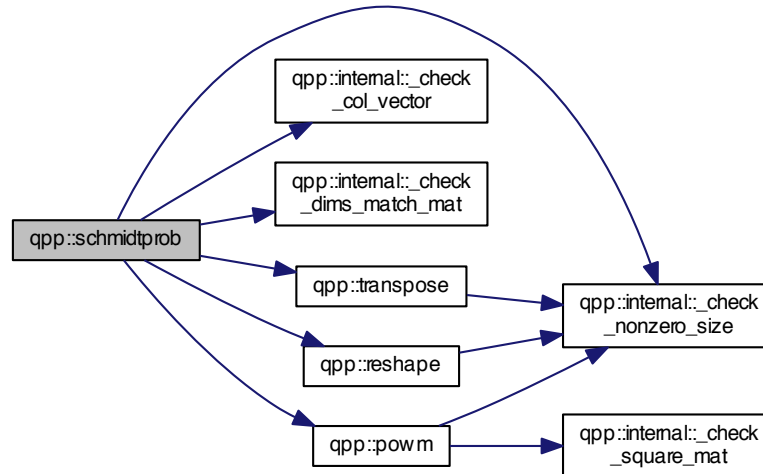
6.1.2.86 `template<typename Derived > cmat qpp::schmidtcoeff ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size_t > & dims )`

Here is the call graph for this function:



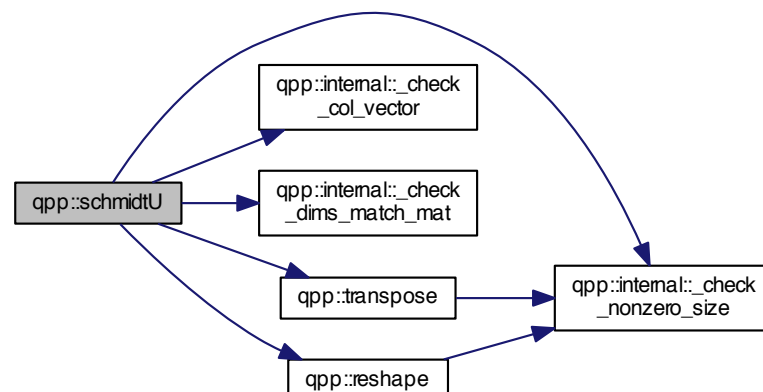
6.1.2.87 `template<typename Derived> cmat qpp::schmidtprob ( const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & dims )`

Here is the call graph for this function:



6.1.2.88 `template<typename Derived> cmat qpp::schmidtU ( const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & dims )`

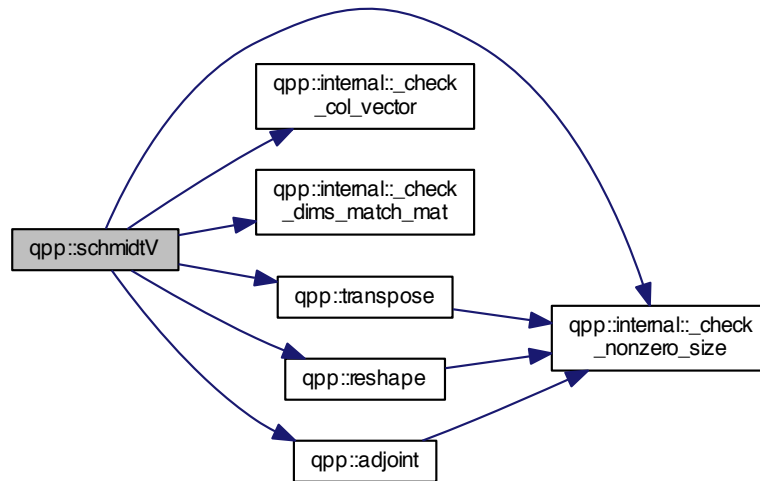
Here is the call graph for this function:





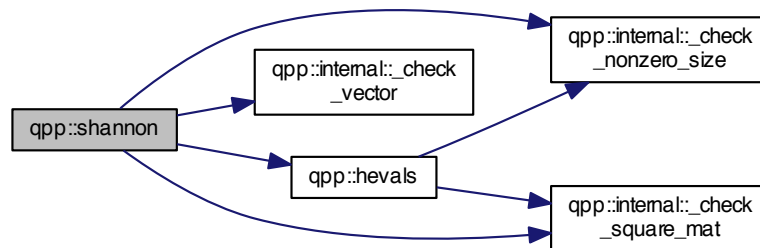
6.1.2.89 `template<typename Derived> cmat qpp::schmidtV ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size_t> & dims )`

Here is the call graph for this function:



6.1.2.90 `template<typename Derived> double qpp::shannon ( const Eigen::MatrixBase< Derived > & A )`

Here is the call graph for this function:



6.1.2.91 `template<typename Derived> cmat qpp::sinm ( const Eigen::MatrixBase< Derived > & A )`

Matrix sin.

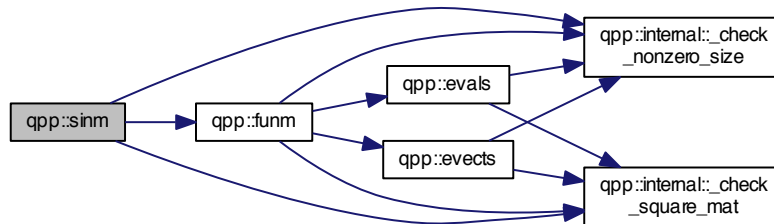
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Matrix sine of  $A$ , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.92 `template<typename Derived> cmat qpp::spectralpowm ( const Eigen::MatrixBase< Derived> & A, const cplx z )`

Matrix power.

Uses the spectral decomposition of  $A$  to compute the matrix power

By convention  $A^0 = I$

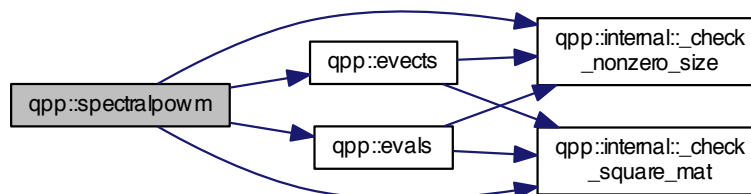
## Parameters

$A$	Eigen expression
$z$	Complex number

## Returns

Matrix power  $A^z$ , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.93 `template<typename Derived> cmat qpp::sqrtm ( const Eigen::MatrixBase< Derived> & A )`

Matrix square root.

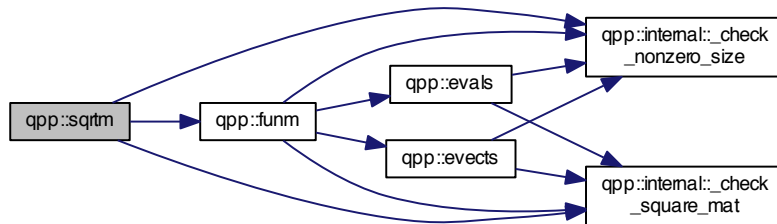
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Matrix square root of  $A$ , as a dynamic matrix over the complex field

Here is the call graph for this function:



#### 6.1.2.94 `template<typename Derived> Derived::Scalar qpp::sum ( const Eigen::MatrixBase< Derived> & A )`

Element-wise sum.

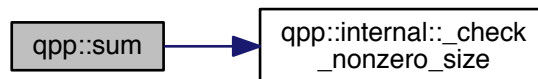
## Parameters

$A$	Eigen expression
-----	------------------

## Returns

Element-wise sum of  $A$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



#### 6.1.2.95 `cmat qpp::super ( const std::vector< cmat> & Ks )`

Superoperator matrix representation.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators  $K_s$  in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

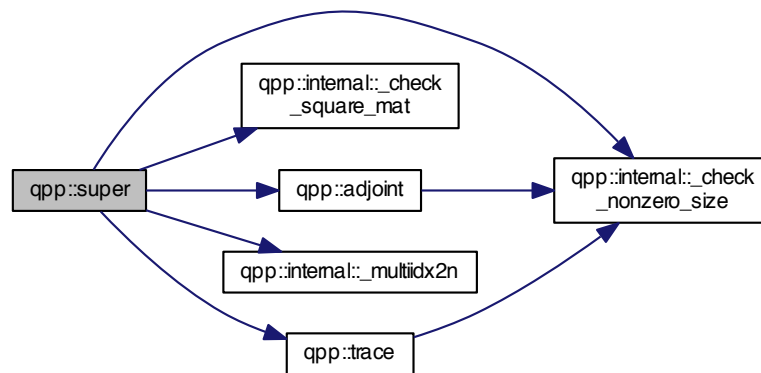
## Parameters

<i>Ks</i>	std::vector of Eigen expressions representing the set of Kraus operators
-----------	--

## Returns

Superoperator matrix representation, as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.96 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::syspermute ( const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & perm, const std::vector< std::size_t > & dims )`

System permutation.

Permutes the subsystems in a state vector or density matrix

The qubit *perm*[*i*] is permuted to the location *i*

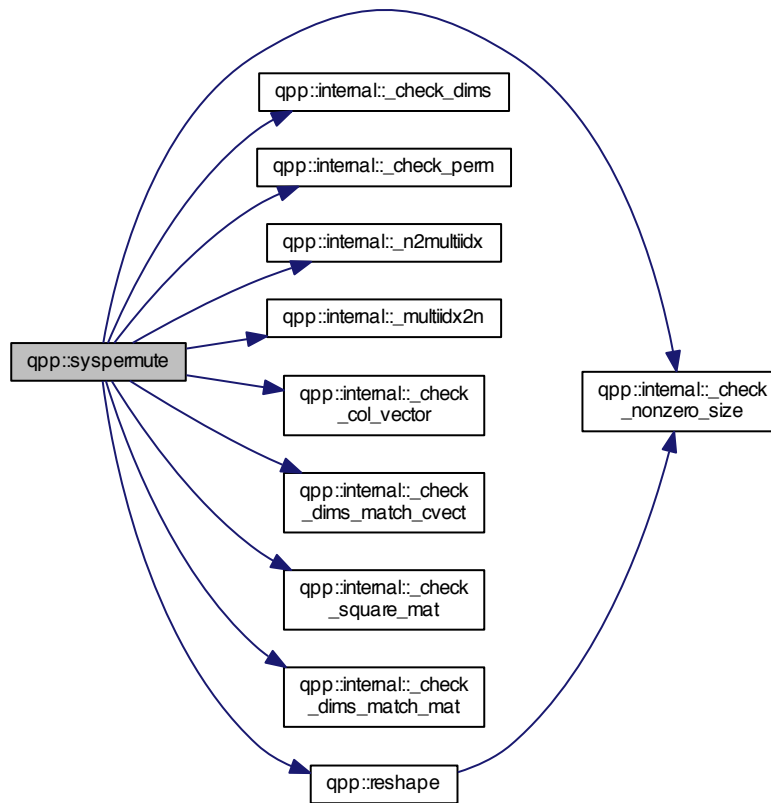
## Parameters

<i>A</i>	Eigen expression
<i>perm</i>	Permutation
<i>dims</i>	Subsystems' dimensions

## Returns

Permuted system, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.97 `template<typename Derived> Derived::Scalar qpp::trace ( const Eigen::MatrixBase< Derived> & A )`

Trace.

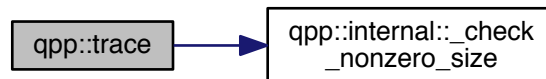
## Parameters

A	Eigen expression
---	------------------

**Returns**

Trace of  $A$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



**6.1.2.98** `template<typename Derived > DynMat<typename Derived::Scalar> qpp::transpose ( const Eigen::MatrixBase<Derived > & A )`

Transpose.

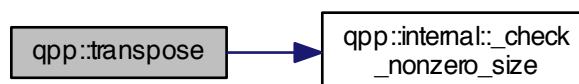
**Parameters**

$A$	Eigen expression
-----	------------------

**Returns**

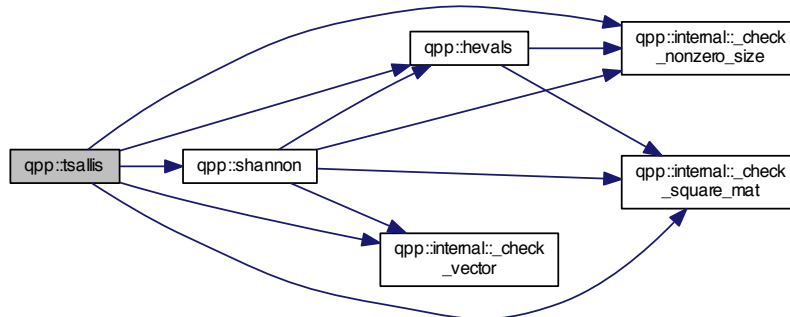
Transpose of  $A$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.99 `template<typename Derived> double qpp::tsallis ( const double alpha, const Eigen::MatrixBase< Derived > & A )`

Here is the call graph for this function:



### 6.1.3 Variable Documentation

6.1.3.1 `constexpr double qpp::chop = 1e-10`

Used in [qpp::disp\(\)](#) and [qpp::displn\(\)](#) for setting to zero numbers that have their absolute value smaller than `qpp::ct::chop`.

6.1.3.2 `constexpr double qpp::ee = 2.718281828459045235360287471352662497`

Base of natural logarithm,  $e$ .

6.1.3.3 `constexpr double qpp::eps = 1e-12`

Used to decide whether a number or expression in double precision is zero or not.

Example:

```
if(std::abs(x) < qpp::ct::eps) // x is zero
```

6.1.3.4 `const Gates& qpp::gt = Gates::get_instance()`

[qpp::Gates](#) const [Singleton](#)

Initializes the gates, see the class [qpp::Gates](#)

6.1.3.5 `constexpr std::size_t qpp::maxn = 64`

Maximum number of qubits.

Used internally to statically allocate arrays (for speed reasons)

6.1.3.6 `constexpr double qpp::pi = 3.141592653589793238462643383279502884`

$\pi$

### 6.1.3.7 RandomDevices& qpp::rdevs = RandomDevices::get\_instance()

[qpp::RandomDevices](#) Singleton

Initializes the random devices, see the class [qpp::RandomDevices](#)

### 6.1.3.8 const States& qpp::st = States::get\_instance()

[qpp::States](#) const Singleton

Initializes the states, see the class [qpp::States](#)

## 6.2 qpp::internal Namespace Reference

### Functions

- void [\\_n2multiidx](#) (std::size\_t n, std::size\_t numdims, const std::size\_t \*dims, std::size\_t \*result)
- std::size\_t [\\_multiidx2n](#) (const std::size\_t \*midx, std::size\_t numdims, const std::size\_t \*dims)
- template<typename Derived >  
bool [\\_check\\_square\\_mat](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [\\_check\\_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [\\_check\\_row\\_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [\\_check\\_col\\_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename T >  
bool [\\_check\\_nonzero\\_size](#) (const T &x)
- bool [\\_check\\_dims](#) (const std::vector< std::size\_t > &dims)
- template<typename Derived >  
bool [\\_check\\_dims\\_match\\_mat](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [\\_check\\_dims\\_match\\_cvect](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &V)
- template<typename Derived >  
bool [\\_check\\_dims\\_match\\_rvect](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &V)
- bool [\\_check\\_eq\\_dims](#) (const std::vector< std::size\_t > &dims, std::size\_t dim)
- bool [\\_check\\_subsys\\_match\\_dims](#) (const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- bool [\\_check\\_perm](#) (const std::vector< std::size\_t > &perm)
- template<typename Derived1 , typename Derived2 >  
[DynMat](#)< typename Derived1::Scalar > [\\_kron2](#) (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename T >  
void [variadic\\_vector\\_emplace](#) (std::vector< T > &)
- template<typename T , typename First , typename... Args>  
void [variadic\\_vector\\_emplace](#) (std::vector< T > &v, First &&first, Args &&...args)

### 6.2.1 Detailed Description

Internal functions, do not modify or use directly



## 6.2.2 Function Documentation

6.2.2.1 `template<typename Derived > bool qpp::internal::_check_col_vector ( const Eigen::MatrixBase< Derived > & A )`

6.2.2.2 `bool qpp::internal::_check_dims ( const std::vector< std::size_t > & dims )`

6.2.2.3 `template<typename Derived > bool qpp::internal::_check_dims_match_cvect ( const std::vector< std::size_t > & dims, const Eigen::MatrixBase< Derived > & V )`

6.2.2.4 `template<typename Derived > bool qpp::internal::_check_dims_match_mat ( const std::vector< std::size_t > & dims, const Eigen::MatrixBase< Derived > & A )`

6.2.2.5 `template<typename Derived > bool qpp::internal::_check_dims_match_rvect ( const std::vector< std::size_t > & dims, const Eigen::MatrixBase< Derived > & V )`

6.2.2.6 `bool qpp::internal::_check_eq_dims ( const std::vector< std::size_t > & dims, std::size_t dim )`

6.2.2.7 `template<typename T > bool qpp::internal::_check_nonzero_size ( const T & x )`

6.2.2.8 `bool qpp::internal::_check_perm ( const std::vector< std::size_t > & perm )`

6.2.2.9 `template<typename Derived > bool qpp::internal::_check_row_vector ( const Eigen::MatrixBase< Derived > & A )`

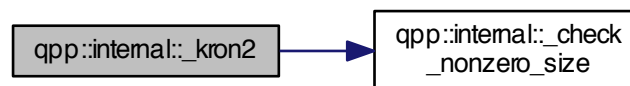
6.2.2.10 `template<typename Derived > bool qpp::internal::_check_square_mat ( const Eigen::MatrixBase< Derived > & A )`

6.2.2.11 `bool qpp::internal::_check_subsys_match_dims ( const std::vector< std::size_t > & subsys, const std::vector< std::size_t > & dims )`

6.2.2.12 `template<typename Derived > bool qpp::internal::_check_vector ( const Eigen::MatrixBase< Derived > & A )`

6.2.2.13 `template<typename Derived1, typename Derived2 > DynMat<typename Derived1::Scalar> qpp::internal::_kron2 ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )`

Here is the call graph for this function:



6.2.2.14 `std::size_t qpp::internal::_multiidx2n ( const std::size_t * midx, std::size_t numdims, const std::size_t * dims )`

6.2.2.15 `void qpp::internal::_n2multiidx ( std::size_t n, std::size_t numdims, const std::size_t * dims, std::size_t * result )`

6.2.2.16 `template<typename T > void qpp::internal::variadic_vector_emplace ( std::vector< T > & )`

6.2.2.17 `template<typename T , typename First , typename... Args> void qpp::internal::variadic_vector_emplace (`  
`std::vector< T > & v, First && first, Args &&... args )`

Here is the call graph for this function:



# Chapter 7

## Class Documentation

### 7.1 qpp::DiscreteDistribution Class Reference

```
#include <stat.h>
```

#### Public Member Functions

- `template<typename InputIterator >`  
`DiscreteDistribution` (InputIterator first, InputIterator last)
- `DiscreteDistribution` (std::initializer\_list< double > weights)
- `DiscreteDistribution` (std::vector< double > weights)
- `std::size_t sample` ()
- `std::vector< double > probabilities` () const

#### Protected Attributes

- `std::discrete_distribution`  
< std::size\_t > `_d`

#### 7.1.1 Constructor & Destructor Documentation

7.1.1.1 `template<typename InputIterator > qpp::DiscreteDistribution::DiscreteDistribution ( InputIterator first, InputIterator last )` [inline]

7.1.1.2 `qpp::DiscreteDistribution::DiscreteDistribution ( std::initializer_list< double > weights )` [inline]

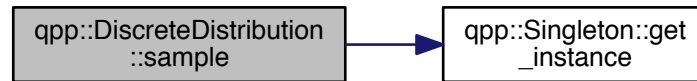
7.1.1.3 `qpp::DiscreteDistribution::DiscreteDistribution ( std::vector< double > weights )` [inline]

#### 7.1.2 Member Function Documentation

7.1.2.1 `std::vector<double> qpp::DiscreteDistribution::probabilities ( ) const` [inline]

### 7.1.2.2 `std::size_t qpp::DiscreteDistribution::sample ( )` `[inline]`

Here is the call graph for this function:



## 7.1.3 Member Data Documentation

### 7.1.3.1 `std::discrete_distribution<std::size_t> qpp::DiscreteDistribution::_d` `[protected]`

The documentation for this class was generated from the following file:

- `include/classes/stat.h`

## 7.2 `qpp::DiscreteDistributionAbsSquare` Class Reference

```
#include <stat.h>
```

### Public Member Functions

- `template<typename InputIterator >`  
`DiscreteDistributionAbsSquare` (`InputIterator first`, `InputIterator last`)
- `DiscreteDistributionAbsSquare` (`std::initializer_list< cplx > amplitudes`)
- `DiscreteDistributionAbsSquare` (`std::vector< cplx > amplitudes`)
- `template<typename Derived >`  
`DiscreteDistributionAbsSquare` (`const Eigen::MatrixBase< Derived > &V`)
- `std::size_t sample ( )`
- `std::vector< double > probabilities ( ) const`

### Protected Member Functions

- `template<typename InputIterator >`  
`std::vector< double > cplx2weights` (`InputIterator first`, `InputIterator last`) `const`

### Protected Attributes

- `std::discrete_distribution`  
`< std::size_t > _d`

### 7.2.1 Constructor & Destructor Documentation

7.2.1.1 `template<typename InputIterator > qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare ( InputIterator first, InputIterator last ) [inline]`

7.2.1.2 `qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare ( std::initializer_list< cplx > amplitudes ) [inline]`

7.2.1.3 `qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare ( std::vector< cplx > amplitudes ) [inline]`

7.2.1.4 `template<typename Derived > qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare ( const Eigen::MatrixBase< Derived > & V ) [inline]`

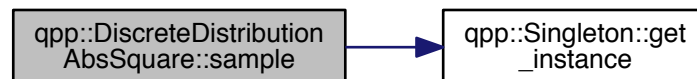
### 7.2.2 Member Function Documentation

7.2.2.1 `template<typename InputIterator > std::vector<double> qpp::DiscreteDistributionAbsSquare::cplx2weights ( InputIterator first, InputIterator last ) const [inline], [protected]`

7.2.2.2 `std::vector<double> qpp::DiscreteDistributionAbsSquare::probabilities ( ) const [inline]`

7.2.2.3 `std::size_t qpp::DiscreteDistributionAbsSquare::sample ( ) [inline]`

Here is the call graph for this function:



### 7.2.3 Member Data Documentation

7.2.3.1 `std::discrete_distribution<std::size_t> qpp::DiscreteDistributionAbsSquare::_d [protected]`

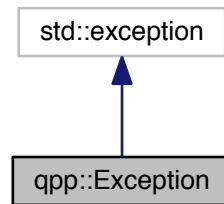
The documentation for this class was generated from the following file:

- [include/classes/stat.h](#)

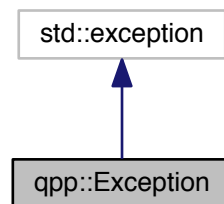
## 7.3 qpp::Exception Class Reference

```
#include <exception.h>
```

Inheritance diagram for qpp::Exception:



Collaboration diagram for qpp::Exception:



## Public Types

- enum `Type` {  
`Type::UNKNOWN_EXCEPTION = 1`, `Type::ZERO_SIZE`, `Type::MATRIX_NOT_SQUARE`, `Type::MATRIX_NOT_CVECTOR`,  
`Type::MATRIX_NOT_RVECTOR`, `Type::MATRIX_NOT_VECTOR`, `Type::MATRIX_NOT_SQUARE_OR_CVECTOR`,  
`Type::MATRIX_NOT_SQUARE_OR_RVECTOR`, `Type::MATRIX_NOT_SQUARE_OR_VECTOR`, `Type::DIMS_INVALID`, `Type::DIMS_NOT_EQUAL`, `Type::DIMS_MISMATCH_MATRIX`,  
`Type::DIMS_MISMATCH_CVECTOR`, `Type::DIMS_MISMATCH_RVECTOR`, `Type::DIMS_MISMATCH_VECTOR`,  
`Type::SUBSYS_MISMATCH_DIMS`, `Type::PERM_INVALID`, `Type::NOT_QUBIT_GATE`, `Type::NOT_QUBIT_SUBSYS`, `Type::NOT_BIPARTITE`,  
`Type::OUT_OF_RANGE`, `Type::TYPE_MISMATCH`, `Type::UNDEFINED_TYPE`, `Type::CUSTOM_EXCEPTION` }

## Public Member Functions

- `Exception` (const std::string &where, const `Type` &type)
- `Exception` (const std::string &where, const std::string &custom)
- virtual const char \* `what` () const noexcept override

## Private Member Functions

- `std::string _construct_exception_msg ()`

## Private Attributes

- `std::string _where`
- `std::string _msg`
- `Type _type`
- `std::string _custom`

### 7.3.1 Member Enumeration Documentation

#### 7.3.1.1 enum `qpp::Exception::Type` [strong]

Enumerator

- UNKNOWN\_EXCEPTION** Unknown exception
- ZERO\_SIZE** Zero sized object, e.g. empty `Eigen::Matrix` or `std::vector` with no elements
- MATRIX\_NOT\_SQUARE** `Eigen::Matrix` is not square
- MATRIX\_NOT\_CVECTOR** `Eigen::Matrix` is not a column vector
- MATRIX\_NOT\_RVECTOR** `Eigen::Matrix` is not a row vector
- MATRIX\_NOT\_VECTOR** `Eigen::Matrix` is not a row/column vector
- MATRIX\_NOT\_SQUARE\_OR\_CVECTOR** `Eigen::Matrix` is not square nor a column vector
- MATRIX\_NOT\_SQUARE\_OR\_RVECTOR** `Eigen::Matrix` is not square nor a row vector
- MATRIX\_NOT\_SQUARE\_OR\_VECTOR** `Eigen::Matrix` is not square nor a row/column vector
- DIMS\_INVALID** `std::vector<std::size_t>` representing the dimensions has zero size or contains zeros
- DIMS\_NOT\_EQUAL** `std::vector<std::size_t>` representing the dimensions contains non-equal elements
- DIMS\_MISMATCH\_MATRIX** Product of the dimensions' `std::vector<std::size_t>` is not equal to the number of rows of `Eigen::Matrix` (assumed to be square)
- DIMS\_MISMATCH\_CVECTOR** Product of the dimensions' `std::vector<std::size_t>` is not equal to the number of cols of `Eigen::Matrix` (assumed to be a column vector)
- DIMS\_MISMATCH\_RVECTOR** Product of the dimensions' `std::vector<std::size_t>` is not equal to the number of cols of `Eigen::Matrix` (assumed to be a row vector)
- DIMS\_MISMATCH\_VECTOR** Product of the dimensions' `std::vector<std::size_t>` is not equal to the number of cols of `Eigen::Matrix` (assumed to be a row/column vector)
- SUBSYS\_MISMATCH\_DIMS** `std::vector<std::size_t>` representing the subsystems' labels has duplicates, or has entries that are larger than the size of the `std::vector<std::size_t>` representing the dimensions
- PERM\_INVALID** Invalid `std::vector<std::size_t>` permutation
- NOT\_QUBIT\_GATE** `Eigen::Matrix` is not 2 x 2
- NOT\_QUBIT\_SUBSYS** Subsystems are not 2-dimensional
- NOT\_BIPARTITE** `std::vector<std::size_t>` representing the dimensions has size different from 2
- OUT\_OF\_RANGE** Parameter out of range
- TYPE\_MISMATCH** Types do not match (i.e. `Matrix<double>` vs `Matrix<cplx>`)
- UNDEFINED\_TYPE** Templated function not defined for this type
- CUSTOM\_EXCEPTION** Custom exception, user must provide a custom message

### 7.3.2 Constructor & Destructor Documentation

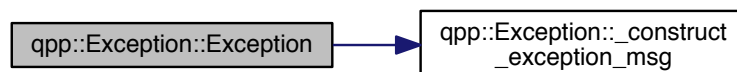
7.3.2.1 `qpp::Exception::Exception ( const std::string & where, const Type & type )` `[inline]`

Here is the call graph for this function:



7.3.2.2 `qpp::Exception::Exception ( const std::string & where, const std::string & custom )` `[inline]`

Here is the call graph for this function:



### 7.3.3 Member Function Documentation

7.3.3.1 `std::string qpp::Exception::_construct_exception_msg ( )` `[inline]`, `[private]`

7.3.3.2 `virtual const char* qpp::Exception::what ( ) const` `[inline]`, `[override]`, `[virtual]`, `[noexcept]`

### 7.3.4 Member Data Documentation

7.3.4.1 `std::string qpp::Exception::_custom` `[private]`

7.3.4.2 `std::string qpp::Exception::_msg` `[private]`

7.3.4.3 `Type qpp::Exception::_type` `[private]`

7.3.4.4 `std::string qpp::Exception::_where` `[private]`

The documentation for this class was generated from the following file:

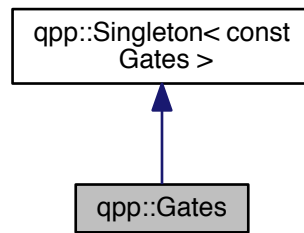
- [include/classes/exception.h](#)

## 7.4 qpp::Gates Class Reference

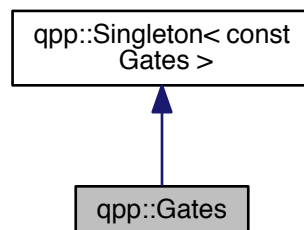
```
#include <gates.h>
```



Inheritance diagram for qpp::Gates:



Collaboration diagram for qpp::Gates:



## Public Member Functions

- [cmat Rn](#) (double theta, std::vector< double > n) const
- [cmat Zd](#) (std::size\_t D) const
- [cmat Fd](#) (std::size\_t D) const
- [cmat Xd](#) (std::size\_t D) const
- template<typename Derived = Eigen::MatrixXcd>  
Derived [ld](#) (std::size\_t D) const
- template<typename Derived1 , typename Derived2 >  
[DynMat](#)< typename Derived1::Scalar > [applyCTRL](#) (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size\_t > &ctrl, const std::vector< std::size\_t > &subsys, std::size\_t n, std::size\_t d=2) const
- template<typename Derived1 , typename Derived2 >  
[DynMat](#)< typename Derived1::Scalar > [apply](#) (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims) const
- template<typename Derived >  
[DynMat](#)< typename Derived::Scalar > [CTRL](#) (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &ctrl, const std::vector< std::size\_t > &subsys, std::size\_t n, std::size\_t d=2) const

## Public Attributes

- [cmat Id2](#) { cmat::Identity(2, 2) }
- [cmat H](#) { cmat::Zero(2, 2) }
- [cmat X](#) { cmat::Zero(2, 2) }
- [cmat Y](#) { cmat::Zero(2, 2) }
- [cmat Z](#) { cmat::Zero(2, 2) }
- [cmat S](#) { cmat::Zero(2, 2) }
- [cmat T](#) { cmat::Zero(2, 2) }
- [cmat CNOTab](#) { cmat::Identity(4, 4) }
- [cmat CZ](#) { cmat::Identity(4, 4) }
- [cmat CNOTba](#) { cmat::Zero(4, 4) }
- [cmat SWAP](#) { cmat::Identity(4, 4) }
- [cmat TOF](#) { cmat::Identity(8, 8) }
- [cmat FRED](#) { cmat::Identity(8, 8) }

## Private Member Functions

- [Gates](#) ()

## Friends

- class [Singleton](#)< const [Gates](#) >

## Additional Inherited Members

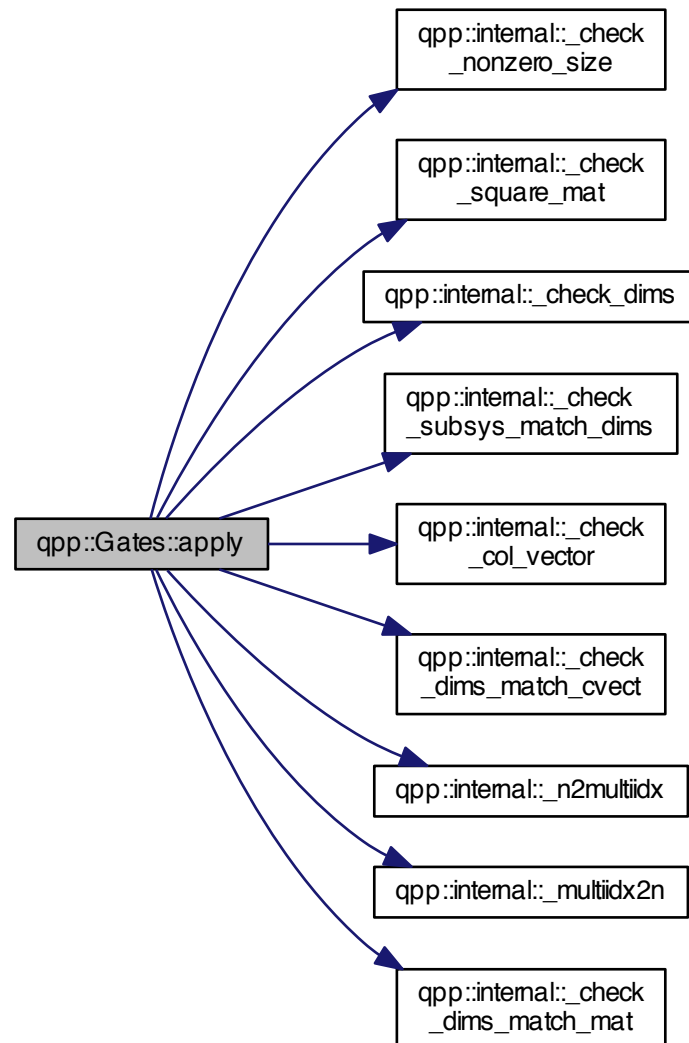
### 7.4.1 Constructor & Destructor Documentation

7.4.1.1 `qpp::Gates::Gates ( )` [inline], [private]

### 7.4.2 Member Function Documentation

7.4.2.1 `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::Gates::apply  
( const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector<  
std::size_t > & subsys, const std::vector< std::size_t > & dims ) const [inline]`

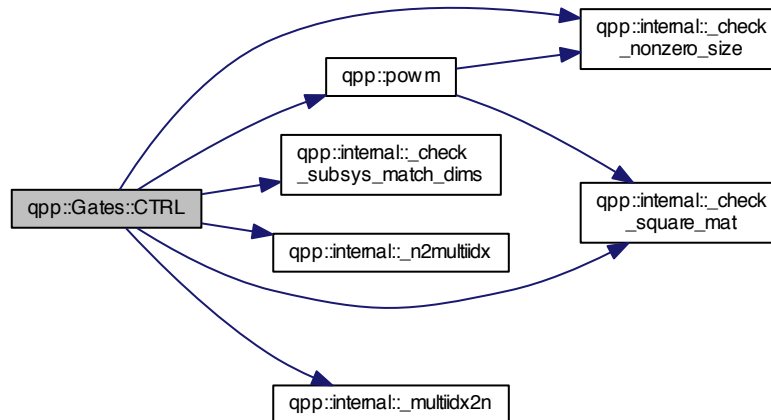
Here is the call graph for this function:



7.4.2.2 `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::Gates::applyCTRL  
( const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector<  
std::size_t > & ctrl, const std::vector< std::size_t > & subsys, std::size_t n, std::size_t d=2 ) const [inline]`

7.4.2.3 `template<typename Derived > DynMat<typename Derived::Scalar> qpp::Gates::CTRL ( const Eigen::MatrixBase<Derived > & A, const std::vector< std::size_t > & ctrl, const std::vector< std::size_t > & subsys, std::size_t n, std::size_t d = 2 ) const [inline]`

Here is the call graph for this function:



7.4.2.4 `cmat qpp::Gates::Fd ( std::size_t D ) const [inline]`

Here is the call graph for this function:



7.4.2.5 `template<typename Derived = Eigen::MatrixXcd> Derived qpp::Gates::Id ( std::size_t D ) const [inline]`

7.4.2.6 `cmat qpp::Gates::Rn ( double theta, std::vector< double > n ) const [inline]`

7.4.2.7 `cmat qpp::Gates::Xd ( std::size_t D ) const [inline]`

Here is the call graph for this function:



7.4.2.8 `cmat qpp::Gates::Zd ( std::size_t D ) const [inline]`

Here is the call graph for this function:



### 7.4.3 Friends And Related Function Documentation

7.4.3.1 `friend class Singleton< const Gates > [friend]`

### 7.4.4 Member Data Documentation

7.4.4.1 `cmat qpp::Gates::CNOTab { cmat::Identity(4, 4) }`

7.4.4.2 `cmat qpp::Gates::CNOTba { cmat::Zero(4, 4) }`

7.4.4.3 `cmat qpp::Gates::CZ { cmat::Identity(4, 4) }`

7.4.4.4 `cmat qpp::Gates::FRED { cmat::Identity(8, 8) }`

7.4.4.5 `cmat qpp::Gates::H { cmat::Zero(2, 2) }`

7.4.4.6 `cmat qpp::Gates::Id2 { cmat::Identity(2, 2) }`

7.4.4.7 `cmat qpp::Gates::S { cmat::Zero(2, 2) }`

7.4.4.8 `cmat qpp::Gates::SWAP { cmat::Identity(4, 4) }`

7.4.4.9 `cmat qpp::Gates::T { cmat::Zero(2, 2) }`

7.4.4.10 `cmat qpp::Gates::TOF { cmat::Identity(8, 8) }`

7.4.4.11 `cmat qpp::Gates::X { cmat::Zero(2, 2) }`

7.4.4.12 `cmat qpp::Gates::Y { cmat::Zero(2, 2) }`

7.4.4.13 `cmat qpp::Gates::Z { cmat::Zero(2, 2) }`

The documentation for this class was generated from the following file:

- [include/classes/gates.h](#)

## 7.5 qpp::NormalDistribution Class Reference

```
#include <stat.h>
```

### Public Member Functions

- [NormalDistribution](#) (double mean=0, double sigma=1)
- double [sample](#) ()

### Protected Attributes

- `std::normal_distribution _d`

#### 7.5.1 Constructor & Destructor Documentation

7.5.1.1 `qpp::NormalDistribution::NormalDistribution ( double mean = 0, double sigma = 1 )` `[inline]`

#### 7.5.2 Member Function Documentation

7.5.2.1 `double qpp::NormalDistribution::sample ( )` `[inline]`

Here is the call graph for this function:



#### 7.5.3 Member Data Documentation

7.5.3.1 `std::normal_distribution qpp::NormalDistribution::_d` `[protected]`

The documentation for this class was generated from the following file:

- [include/classes/stat.h](#)

## 7.6 qpp::Qudit Class Reference

```
#include <qudit.h>
```

### Public Member Functions

- [Qudit](#) (const [cmat](#) &rho=[States::get\\_instance\(\)](#).pz0)
- std::size\_t [measure](#) (const [cmat](#) &U, bool destructive=false)
- std::size\_t [measure](#) (bool destructive=false)
- [cmat](#) [getRho](#) () const
- std::size\_t [getD](#) () const

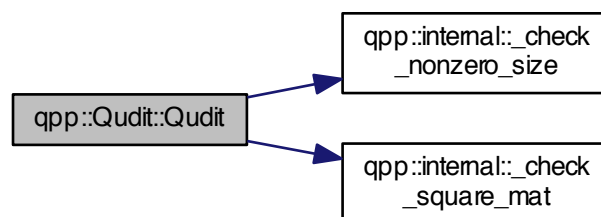
### Private Attributes

- [cmat\\_rho](#)
- std::size\_t [\\_D](#)

### 7.6.1 Constructor & Destructor Documentation

7.6.1.1 `qpp::Qudit::Qudit ( const cmat & rho = States::get_instance() .pz0 ) [inline]`

Here is the call graph for this function:



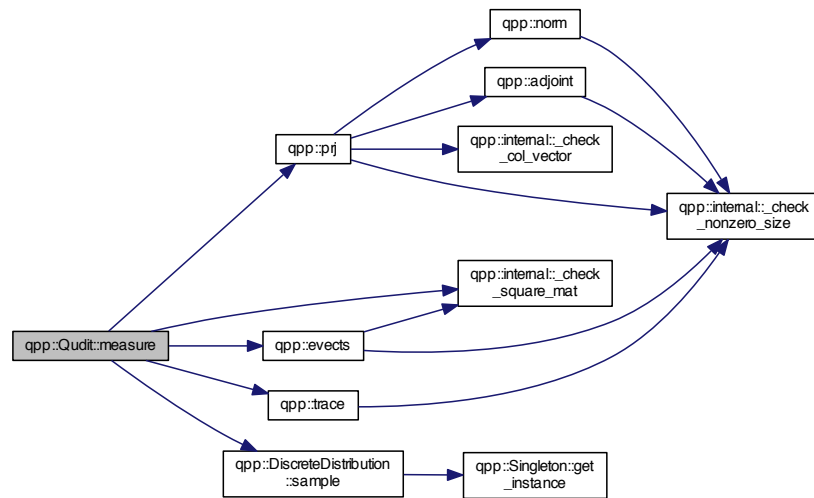
### 7.6.2 Member Function Documentation

7.6.2.1 `std::size_t qpp::Qudit::getD ( ) const [inline]`

7.6.2.2 `cmat qpp::Qudit::getRho ( ) const [inline]`

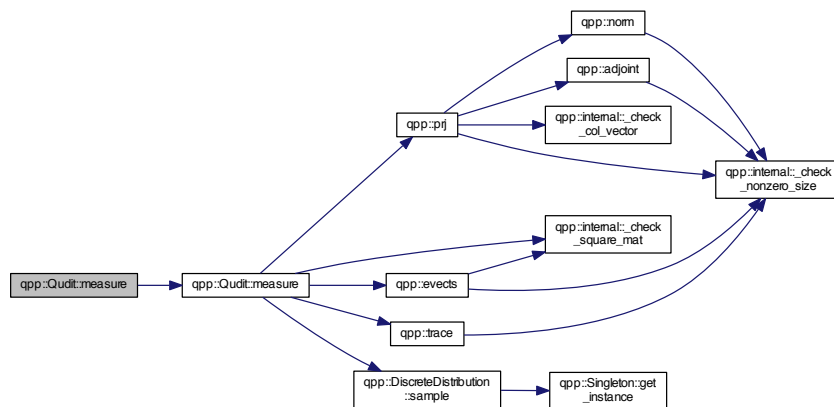
### 7.6.2.3 `std::size_t qpp::Qudit::measure ( const cmat & U, bool destructive = false ) [inline]`

Here is the call graph for this function:



### 7.6.2.4 `std::size_t qpp::Qudit::measure ( bool destructive = false ) [inline]`

Here is the call graph for this function:



## 7.6.3 Member Data Documentation

### 7.6.3.1 `std::size_t qpp::Qudit::_D [private]`

### 7.6.3.2 `cmat qpp::Qudit::_rho [private]`

The documentation for this class was generated from the following file:

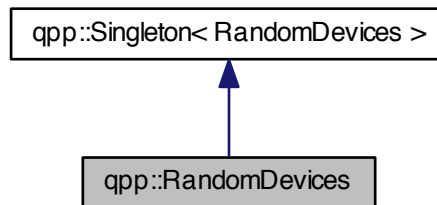
- [include/classes/qudit.h](#)



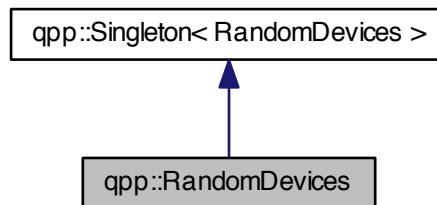
## 7.7 qpp::RandomDevices Class Reference

```
#include <randevs.h>
```

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



### Public Attributes

- [std::mt19937 \\_rng](#)

### Private Member Functions

- [RandomDevices \(\)](#)

### Private Attributes

- [std::random\\_device \\_rd](#)

### Friends

- class [Singleton< RandomDevices >](#)

## Additional Inherited Members

### 7.7.1 Constructor & Destructor Documentation

7.7.1.1 `qpp::RandomDevices::RandomDevices ( )` `[inline],[private]`

### 7.7.2 Friends And Related Function Documentation

7.7.2.1 `friend class Singleton< RandomDevices >` `[friend]`

### 7.7.3 Member Data Documentation

7.7.3.1 `std::random_device qpp::RandomDevices::_rd` `[private]`

7.7.3.2 `std::mt19937 qpp::RandomDevices::_rng`

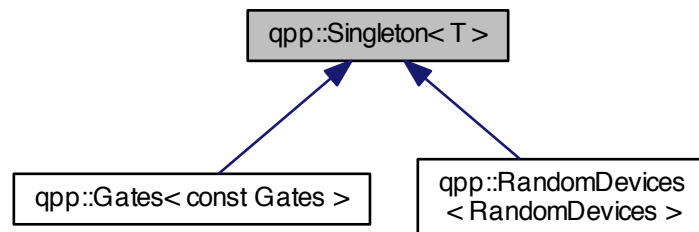
The documentation for this class was generated from the following file:

- `include/classes/randevs.h`

## 7.8 `qpp::Singleton< T >` Class Template Reference

```
#include <singleton.h>
```

Inheritance diagram for `qpp::Singleton< T >`:



## Static Public Member Functions

- static `T & get_instance ()`

## Protected Member Functions

- `Singleton ()=default`
- virtual `~Singleton ()`
- `Singleton (const Singleton &)=delete`
- `Singleton & operator= (const Singleton &)=delete`

### 7.8.1 Constructor & Destructor Documentation

7.8.1.1 `template<typename T> qpp::Singleton< T >::Singleton ( )` `[protected]`, `[default]`

7.8.1.2 `template<typename T> virtual qpp::Singleton< T >::~~Singleton ( )` `[inline]`, `[protected]`, `[virtual]`

7.8.1.3 `template<typename T> qpp::Singleton< T >::Singleton ( const Singleton< T > & )` `[protected]`, `[delete]`

### 7.8.2 Member Function Documentation

7.8.2.1 `template<typename T> static T& qpp::Singleton< T >::get_instance ( )` `[inline]`, `[static]`

7.8.2.2 `template<typename T> Singleton& qpp::Singleton< T >::operator= ( const Singleton< T > & )` `[protected]`, `[delete]`

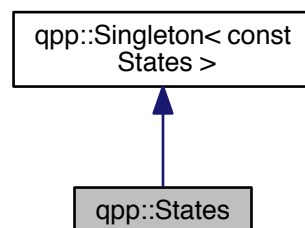
The documentation for this class was generated from the following file:

- `include/classes/singleton.h`

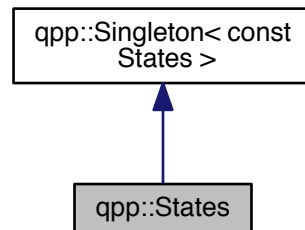
## 7.9 qpp::States Class Reference

```
#include <states.h>
```

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



## Public Attributes

- [ket x0](#) { ket::Zero(2) }
- [ket x1](#) { ket::Zero(2) }
- [ket y0](#) { ket::Zero(2) }
- [ket y1](#) { ket::Zero(2) }
- [ket z0](#) { ket::Zero(2) }
- [ket z1](#) { ket::Zero(2) }
- [cmat px0](#) { cmat::Zero(2, 2) }
- [cmat px1](#) { cmat::Zero(2, 2) }
- [cmat py0](#) { cmat::Zero(2, 2) }
- [cmat py1](#) { cmat::Zero(2, 2) }
- [cmat pz0](#) { cmat::Zero(2, 2) }
- [cmat pz1](#) { cmat::Zero(2, 2) }
- [ket b00](#) { ket::Zero(4) }
- [ket b01](#) { ket::Zero(4) }
- [ket b10](#) { ket::Zero(4) }
- [ket b11](#) { ket::Zero(4) }
- [cmat pb00](#) { cmat::Zero(4, 4) }
- [cmat pb01](#) { cmat::Zero(4, 4) }
- [cmat pb10](#) { cmat::Zero(4, 4) }
- [cmat pb11](#) { cmat::Zero(4, 4) }
- [ket GHZ](#) { ket::Zero(8) }
- [ket W](#) { ket::Zero(8) }
- [cmat pGHZ](#) { cmat::Zero(8, 8) }
- [cmat pW](#) { cmat::Zero(8, 8) }

## Private Member Functions

- [States](#) ()

## Friends

- class [Singleton< const States >](#)

## Additional Inherited Members

### 7.9.1 Constructor & Destructor Documentation

7.9.1.1 `qpp::States::States ( ) [inline], [private]`

### 7.9.2 Friends And Related Function Documentation

7.9.2.1 `friend class Singleton< const States > [friend]`

### 7.9.3 Member Data Documentation

7.9.3.1 `ket qpp::States::b00 { ket::Zero(4) }`

7.9.3.2 `ket qpp::States::b01 { ket::Zero(4) }`

7.9.3.3 `ket qpp::States::b10 { ket::Zero(4) }`

7.9.3.4 `ket qpp::States::b11 { ket::Zero(4) }`

7.9.3.5 `ket qpp::States::GHZ { ket::Zero(8) }`

7.9.3.6 `cmat qpp::States::pb00 { cmat::Zero(4, 4) }`

7.9.3.7 `cmat qpp::States::pb01 { cmat::Zero(4, 4) }`

7.9.3.8 `cmat qpp::States::pb10 { cmat::Zero(4, 4) }`

7.9.3.9 `cmat qpp::States::pb11 { cmat::Zero(4, 4) }`

7.9.3.10 `cmat qpp::States::pGHZ { cmat::Zero(8, 8) }`

7.9.3.11 `cmat qpp::States::pW { cmat::Zero(8, 8) }`

7.9.3.12 `cmat qpp::States::px0 { cmat::Zero(2, 2) }`

7.9.3.13 `cmat qpp::States::px1 { cmat::Zero(2, 2) }`

7.9.3.14 `cmat qpp::States::py0 { cmat::Zero(2, 2) }`

7.9.3.15 `cmat qpp::States::py1 { cmat::Zero(2, 2) }`

7.9.3.16 `cmat qpp::States::pz0 { cmat::Zero(2, 2) }`

7.9.3.17 `cmat qpp::States::pz1 { cmat::Zero(2, 2) }`

7.9.3.18 `ket qpp::States::W { ket::Zero(8) }`

7.9.3.19 `ket qpp::States::x0 { ket::Zero(2) }`

7.9.3.20 `ket qpp::States::x1 { ket::Zero(2) }`

7.9.3.21 `ket qpp::States::y0 { ket::Zero(2) }`

7.9.3.22 `ket qpp::States::y1 { ket::Zero(2) }`

7.9.3.23 `ket qpp::States::z0 { ket::Zero(2) }`

7.9.3.24 `ket qpp::States::z1 { ket::Zero(2) }`

The documentation for this class was generated from the following file:

- [include/classes/states.h](#)

## 7.10 qpp::Timer Class Reference

```
#include <timer.h>
```

### Public Member Functions

- [Timer](#) ()
- void [tic](#) ()
- void [toc](#) ()
- double [seconds](#) () const

### Protected Attributes

- `std::chrono::steady_clock::time_point` [\\_start](#)
- `std::chrono::steady_clock::time_point` [\\_end](#)

### Friends

- `std::ostream & operator<< (std::ostream &os, const Timer &rhs)`

### 7.10.1 Constructor & Destructor Documentation

7.10.1.1 `qpp::Timer::Timer ( )` [[inline](#)]

### 7.10.2 Member Function Documentation

7.10.2.1 `double qpp::Timer::seconds ( )` const [[inline](#)]

7.10.2.2 `void qpp::Timer::tic ( )` [[inline](#)]

7.10.2.3 `void qpp::Timer::toc ( )` [[inline](#)]

### 7.10.3 Friends And Related Function Documentation

7.10.3.1 `std::ostream& operator<< ( std::ostream & os, const Timer & rhs )` [[friend](#)]

### 7.10.4 Member Data Documentation

7.10.4.1 `std::chrono::steady_clock::time_point` `qpp::Timer::_end` [[protected](#)]

7.10.4.2 `std::chrono::steady_clock::time_point` `qpp::Timer::_start` [[protected](#)]

The documentation for this class was generated from the following file:

- [include/classes/timer.h](#)

## 7.11 qpp::UniformIntDistribution Class Reference

```
#include <stat.h>
```

### Public Member Functions

- [UniformIntDistribution](#) (int a=0, int b=1)
- int [sample](#) ()

### Protected Attributes

- std::uniform\_int\_distribution [\\_d](#)

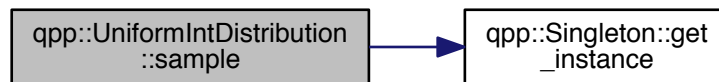
#### 7.11.1 Constructor & Destructor Documentation

7.11.1.1 `qpp::UniformIntDistribution::UniformIntDistribution ( int a = 0, int b = 1 )` `[inline]`

#### 7.11.2 Member Function Documentation

7.11.2.1 `int qpp::UniformIntDistribution::sample ( )` `[inline]`

Here is the call graph for this function:



#### 7.11.3 Member Data Documentation

7.11.3.1 `std::uniform_int_distribution qpp::UniformIntDistribution::_d` `[protected]`

The documentation for this class was generated from the following file:

- include/classes/[stat.h](#)

## 7.12 qpp::UniformRealDistribution Class Reference

```
#include <stat.h>
```

### Public Member Functions

- [UniformRealDistribution](#) (double a=0, double b=1)
- double [sample](#) ()

## Protected Attributes

- `std::uniform_real_distribution _d`

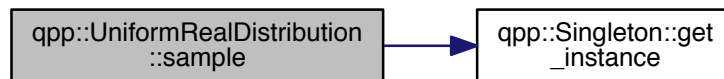
## 7.12.1 Constructor & Destructor Documentation

7.12.1.1 `qpp::UniformRealDistribution::UniformRealDistribution ( double a = 0, double b = 1 )` `[inline]`

## 7.12.2 Member Function Documentation

7.12.2.1 `double qpp::UniformRealDistribution::sample ( )` `[inline]`

Here is the call graph for this function:



## 7.12.3 Member Data Documentation

7.12.3.1 `std::uniform_real_distribution qpp::UniformRealDistribution::_d` `[protected]`

The documentation for this class was generated from the following file:

- `include/classes/stat.h`

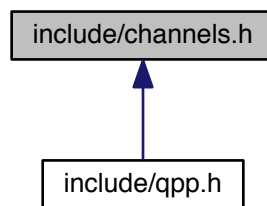


## Chapter 8

# File Documentation

### 8.1 include/channels.h File Reference

This graph shows which files directly or indirectly include this file:



### Namespaces

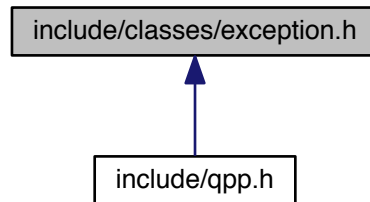
- [qpp](#)

### Functions

- `cmat qpp::super (const std::vector< cmat > &Ks)`  
*Superoperator matrix representation.*
- `cmat qpp::choi (const std::vector< cmat > &Ks)`  
*Choi matrix representation.*
- `std::vector< cmat > qpp::choi2kraus (const cmat &A)`  
*Extracts orthogonal Kraus operators from Choi matrix.*
- `template<typename Derived >`  
`cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks)`  
*Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.*
- `template<typename Derived >`  
`cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`  
*Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.*

## 8.2 include/classes/exception.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

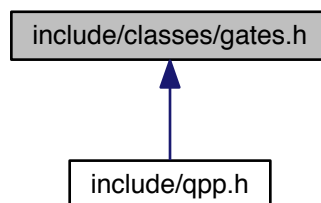
- class [qpp::Exception](#)

### Namespaces

- [qpp](#)

## 8.3 include/classes/gates.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

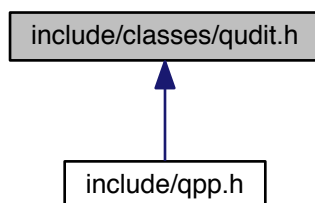
- class [qpp::Gates](#)

### Namespaces

- [qpp](#)

## 8.4 include/classes/qudit.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

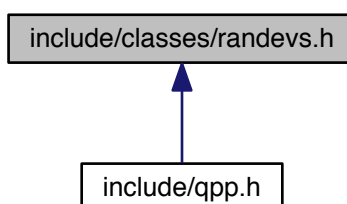
- class [qpp::Qudit](#)

### Namespaces

- [qpp](#)

## 8.5 include/classes/randevs.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

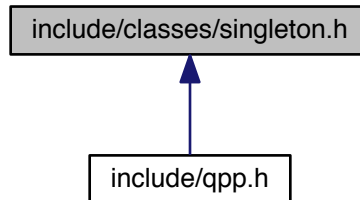
- class [qpp::RandomDevices](#)

### Namespaces

- [qpp](#)

## 8.6 include/classes/singleton.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

- class [qpp::Singleton< T >](#)

### Namespaces

- [qpp](#)

### Macros

- [#define CLASS\\_SINGLETON\(Foo\)](#)
- [#define CLASS\\_CONST\\_SINGLETON\(Foo\)](#)

#### 8.6.1 Macro Definition Documentation

##### 8.6.1.1 [#define CLASS\\_CONST\\_SINGLETON\( Foo \)](#)

###### Value:

```

class Foo: public Singleton<const Foo>\
{
    friend class Singleton<const Foo>;
}
  
```

##### 8.6.1.2 [#define CLASS\\_SINGLETON\( Foo \)](#)

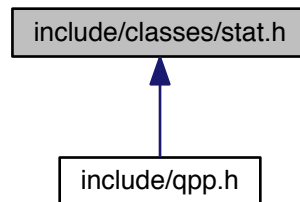
###### Value:

```

class Foo: public Singleton<Foo>\
{
    friend class Singleton<Foo>;
}
  
```

## 8.7 include/classes/stat.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

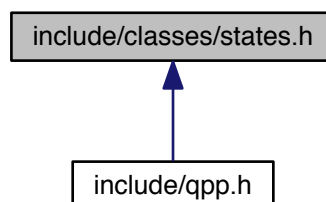
- class [qpp::NormalDistribution](#)
- class [qpp::UniformRealDistribution](#)
- class [qpp::UniformIntDistribution](#)
- class [qpp::DiscreteDistribution](#)
- class [qpp::DiscreteDistributionAbsSquare](#)

### Namespaces

- [qpp](#)

## 8.8 include/classes/states.h File Reference

This graph shows which files directly or indirectly include this file:



### Classes

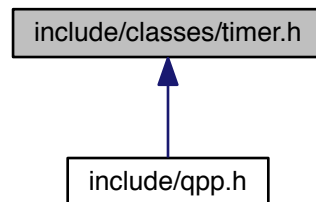
- class [qpp::States](#)

## Namespaces

- [qpp](#)

## 8.9 include/classes/timer.h File Reference

This graph shows which files directly or indirectly include this file:



## Classes

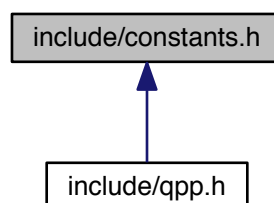
- class [qpp::Timer](#)

## Namespaces

- [qpp](#)

## 8.10 include/constants.h File Reference

This graph shows which files directly or indirectly include this file:



## Namespaces

- [qpp](#)

## Functions

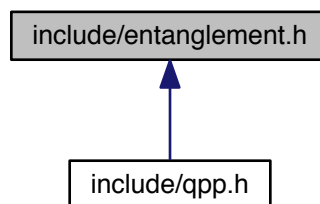
- constexpr std::complex< double > [qpp::operator""\\_i](#) (unsigned long long int x)  
*User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)*
- constexpr std::complex< double > [qpp::operator""\\_i](#) (long double x)  
*User-defined literal for complex  $i = \sqrt{-1}$  (real overload)*
- std::complex< double > [qpp::omega](#) (std::size\_t D)  
*D-th root of unity.*

## Variables

- constexpr double [qpp::chop](#) = 1e-10  
*Used in [qpp::disp\(\)](#) and [qpp::displn\(\)](#) for setting to zero numbers that have their absolute value smaller than [qpp::ct->::chop](#).*
- constexpr double [qpp::eps](#) = 1e-12  
*Used to decide whether a number or expression in double precision is zero or not.*
- constexpr std::size\_t [qpp::maxn](#) = 64  
*Maximum number of qubits.*
- constexpr double [qpp::pi](#) = 3.141592653589793238462643383279502884  
 $\pi$
- constexpr double [qpp::ee](#) = 2.718281828459045235360287471352662497  
*Base of natural logarithm,  $e$ .*

## 8.11 include/entanglement.h File Reference

This graph shows which files directly or indirectly include this file:



## Namespaces

- [qpp](#)

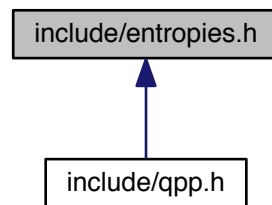
## Functions

- template<typename Derived >  
cmat [qpp::schmidtcoeff](#) (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- template<typename Derived >  
cmat [qpp::schmidtU](#) (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)

- `template<typename Derived >`  
`cmat qpp::schmidtV (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`
- `template<typename Derived >`  
`cmat qpp::schmidtprob (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`
- `template<typename Derived >`  
`double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`
- `template<typename Derived >`  
`double qpp::gconcurrence (const Eigen::MatrixBase< Derived > &A)`

## 8.12 include/entropies.h File Reference

This graph shows which files directly or indirectly include this file:



## Namespaces

- [qpp](#)

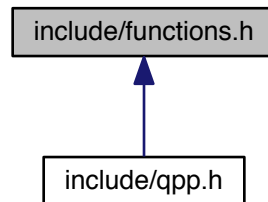
## Functions

- `template<typename Derived >`  
`double qpp::shannon (const Eigen::MatrixBase< Derived > &A)`
- `template<typename Derived >`  
`double qpp::renyi (const double alpha, const Eigen::MatrixBase< Derived > &A)`
- `template<typename Derived >`  
`double qpp::renyi\_inf (const Eigen::MatrixBase< Derived > &A)`
- `template<typename Derived >`  
`double qpp::tsallis (const double alpha, const Eigen::MatrixBase< Derived > &A)`
- `template<typename Derived >`  
`double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`



## 8.13 include/functions.h File Reference

This graph shows which files directly or indirectly include this file:



### Namespaces

- [qpp](#)

### Functions

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::transpose (const Eigen::MatrixBase< Derived > &A)`  
*Transpose.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::conjugate (const Eigen::MatrixBase< Derived > &A)`  
*Complex conjugate.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::adjoint (const Eigen::MatrixBase< Derived > &A)`  
*Adjoint.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::inverse (const Eigen::MatrixBase< Derived > &A)`  
*Inverse.*
- `template<typename Derived >`  
`Derived::Scalar qpp::trace (const Eigen::MatrixBase< Derived > &A)`  
*Trace.*
- `template<typename Derived >`  
`Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > &A)`  
*Determinant.*
- `template<typename Derived >`  
`Derived::Scalar qpp::logdet (const Eigen::MatrixBase< Derived > &A)`  
*Logarithm of the determinant.*
- `template<typename Derived >`  
`Derived::Scalar qpp::sum (const Eigen::MatrixBase< Derived > &A)`  
*Element-wise sum.*
- `template<typename Derived >`  
`double qpp::norm (const Eigen::MatrixBase< Derived > &A)`  
*Trace norm.*
- `template<typename Derived >`  
`cmat qpp::evals (const Eigen::MatrixBase< Derived > &A)`

*Eigenvalues.*

- `template<typename Derived >`  
`cmat qpp::evects (const Eigen::MatrixBase< Derived > &A)`

*Eigenvectors.*

- `template<typename Derived >`  
`dmat qpp::hevals (const Eigen::MatrixBase< Derived > &A)`

*Hermitian eigenvalues.*

- `template<typename Derived >`  
`cmat qpp::hevects (const Eigen::MatrixBase< Derived > &A)`

*Hermitian eigenvectors.*

- `template<typename Derived >`  
`cmat qpp::funm (const Eigen::MatrixBase< Derived > &A, cplx(*f)(const cplx &))`

*Functional calculus  $f(A)$* 

- `template<typename Derived >`  
`cmat qpp::sqrtm (const Eigen::MatrixBase< Derived > &A)`

*Matrix square root.*

- `template<typename Derived >`  
`cmat qpp::absm (const Eigen::MatrixBase< Derived > &A)`

*Matrix absolut value.*

- `template<typename Derived >`  
`cmat qpp::expm (const Eigen::MatrixBase< Derived > &A)`

*Matrix exponential.*

- `template<typename Derived >`  
`cmat qpp::logm (const Eigen::MatrixBase< Derived > &A)`

*Matrix logarithm.*

- `template<typename Derived >`  
`cmat qpp::sinm (const Eigen::MatrixBase< Derived > &A)`

*Matrix sin.*

- `template<typename Derived >`  
`cmat qpp::cosm (const Eigen::MatrixBase< Derived > &A)`

*Matrix cos.*

- `template<typename Derived >`  
`cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived > &A, const cplx z)`

*Matrix power.*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::powm (const Eigen::MatrixBase< Derived > &A, std::size_t n)`

*Matrix power.*

- `template<typename OutputScalar , typename Derived >`  
`DynMat< OutputScalar > qpp::cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const type-  
name Derived::Scalar &))`

*Functor.*

- `template<typename T >`  
`DynMat< typename T::Scalar > qpp::kron (const T &head)`

*Kronecker product (variadic overload)*

- `template<typename T , typename... Args>`  
`DynMat< typename T::Scalar > qpp::kron (const T &head, const Args &...tail)`

*Kronecker product (variadic overload)*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::kron (const std::vector< Derived > &As)`

*Kronecker product (std::vector overload)*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::kron (const std::initializer_list< Derived > &As)`

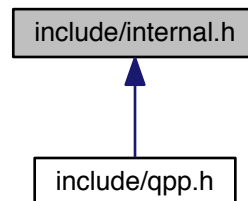
*Kronecker product (std::initializer\_list overload)*

- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::kronpow (const Eigen::MatrixBase< Derived > &A, std::size_t n)`  
*Kronecker power.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::reshape (const Eigen::MatrixBase< Derived > &A, std::size_t rows, std::size_t cols)`  
*Reshape.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &perm, const std::vector< std::size_t > &dims)`  
*System permutation.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`  
*Partial trace.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`  
*Partial trace.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`  
*Partial trace.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`  
*Partial transpose.*
- `template<typename Derived1, typename Derived2 >`  
`DynMat< typename Derived1::Scalar > qpp::comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`  
*Commutator.*
- `template<typename Derived1, typename Derived2 >`  
`DynMat< typename Derived1::Scalar > qpp::anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`  
*Anti-commutator.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::prj (const Eigen::MatrixBase< Derived > &V)`  
*Projector.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::expandout (const Eigen::MatrixBase< Derived > &A, std::size_t pos, const std::vector< std::size_t > &dims)`  
*Expand out.*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::grams (const std::vector< Derived > &Vs)`  
*Gram-Schmidt orthogonalization (std::vector overload)*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::grams (const std::initializer_list< Derived > &Vs)`  
*Gram-Schmidt orthogonalization (std::initializer\_list overload)*
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::grams (const Eigen::MatrixBase< Derived > &A)`  
*Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)*
- `std::vector< std::size_t > qpp::n2multiidx (std::size_t n, const std::vector< std::size_t > &dims)`  
*Non-negative integer index to multi-index.*

- `std::size_t qpp::multiidx2n` (const std::vector< std::size\_t > &midx, const std::vector< std::size\_t > &dims)  
*Multi-index to non-negative integer index.*
- `ket qpp::mket` (const std::vector< std::size\_t > &mask)  
*Multi-partite qubit ket.*
- `ket qpp::mket` (const std::vector< std::size\_t > &mask, const std::vector< std::size\_t > &dims)  
*Multi-partite qudit ket (different dimensions overload)*
- `ket qpp::mket` (const std::vector< std::size\_t > &mask, std::size\_t d)  
*Multi-partite qudit ket (same dimensions overload)*
- `std::vector< std::size_t > qpp::invperm` (const std::vector< std::size\_t > &perm)  
*Inverse permutation.*
- `std::vector< std::size_t > qpp::compperm` (const std::vector< std::size\_t > &perm, const std::vector< std::size\_t > &sigma)  
*Compose permutations.*

## 8.14 include/internal.h File Reference

This graph shows which files directly or indirectly include this file:



## Namespaces

- `qpp::internal`
- `qpp`

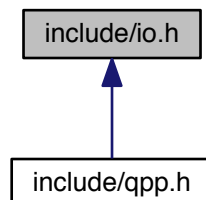
## Functions

- `void qpp::internal::_n2multiidx` (std::size\_t n, std::size\_t numdims, const std::size\_t \*dims, std::size\_t \*result)
- `std::size_t qpp::internal::_multiidx2n` (const std::size\_t \*midx, std::size\_t numdims, const std::size\_t \*dims)
- `template<typename Derived >`  
`bool qpp::internal::_check_square_mat` (const Eigen::MatrixBase< Derived > &A)
- `template<typename Derived >`  
`bool qpp::internal::_check_vector` (const Eigen::MatrixBase< Derived > &A)
- `template<typename Derived >`  
`bool qpp::internal::_check_row_vector` (const Eigen::MatrixBase< Derived > &A)
- `template<typename Derived >`  
`bool qpp::internal::_check_col_vector` (const Eigen::MatrixBase< Derived > &A)
- `template<typename T >`  
`bool qpp::internal::_check_nonzero_size` (const T &x)
- `bool qpp::internal::_check_dims` (const std::vector< std::size\_t > &dims)

- template<typename Derived >  
bool [qpp::internal::\\_check\\_dims\\_match\\_mat](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [qpp::internal::\\_check\\_dims\\_match\\_cvect](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &V)
- template<typename Derived >  
bool [qpp::internal::\\_check\\_dims\\_match\\_rvect](#) (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &V)
- bool [qpp::internal::\\_check\\_eq\\_dims](#) (const std::vector< std::size\_t > &dims, std::size\_t dim)
- bool [qpp::internal::\\_check\\_subsys\\_match\\_dims](#) (const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- bool [qpp::internal::\\_check\\_perm](#) (const std::vector< std::size\_t > &perm)
- template<typename Derived1 , typename Derived2 >  
DynMat< typename Derived1::Scalar > [qpp::internal::\\_kron2](#) (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename T >  
void [qpp::internal::variadic\\_vector\\_emplace](#) (std::vector< T > &)
- template<typename T , typename First , typename... Args>  
void [qpp::internal::variadic\\_vector\\_emplace](#) (std::vector< T > &v, First &&first, Args &&...args)

## 8.15 include/io.h File Reference

This graph shows which files directly or indirectly include this file:



### Namespaces

- [qpp](#)

### Functions

- template<typename T >  
void [qpp::disp](#) (const T &x, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)
- template<typename T >  
void [qpp::displin](#) (const T &x, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)
- template<typename T >  
void [qpp::disp](#) (const T \*x, const std::size\_t n, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)

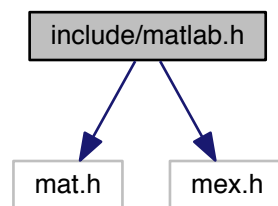
- `template<typename T >`  
`void qpp::displn (const T *x, const std::size_t n, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)`
- `template<typename Derived >`  
`void qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=chop, std::ostream &os=std::cout)`
- `template<typename Derived >`  
`void qpp::displn (const Eigen::MatrixBase< Derived > &A, double chop=chop, std::ostream &os=std::cout)`
- `void qpp::disp (const cplx c, double chop=chop, std::ostream &os=std::cout)`
- `void qpp::displn (const cplx c, double chop=chop, std::ostream &os=std::cout)`
- `template<typename Derived >`  
`void qpp::save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)`
- `template<typename Derived >`  
`DynMat< typename Derived::Scalar > qpp::load (const std::string &fname)`

## 8.16 include/matlab.h File Reference

```
#include "mat.h"
```

```
#include "mex.h"
```

Include dependency graph for matlab.h:



## Namespaces

- [qpp](#)

## Functions

- `template<typename Derived >`  
`Derived qpp::loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`
- `template<>`  
`dmat qpp::loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`
- `template<>`  
`cmat qpp::loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`
- `template<typename Derived >`  
`void qpp::saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`
- `template<>`  
`void qpp::saveMATLABmatrix (const Eigen::MatrixBase< dmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`

- `template<>`  
void [qpp::saveMATLABmatrix](#) (const Eigen::MatrixBase< cmat > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)

## 8.17 include/qpp.h File Reference

```
#include <algorithm>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <exception>
#include <fstream>
#include <functional>
#include <iomanip>
#include <iostream>
#include <iterator>
#include <numeric>
#include <ostream>
#include <random>
#include <stdexcept>
#include <string>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "constants.h"
#include "types.h"
#include "classes/exception.h"
#include "classes/singleton.h"
#include "classes/states.h"
#include "classes/randevs.h"
#include "internal.h"
#include "functions.h"
#include "classes/gates.h"
#include "classes/stat.h"
#include "entropies.h"
#include "entanglement.h"
#include "channels.h"
#include "io.h"
#include "random.h"
#include "classes/qudit.h"
#include "classes/timer.h"
```

Include dependency graph for qpp.h:



### Namespaces

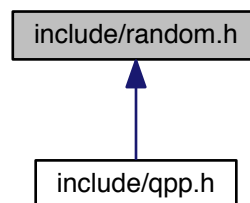
- [qpp](#)

## Variables

- RandomDevices & `qpp::rdevs` = RandomDevices::get\_instance()  
*qpp::RandomDevices Singleton*
- const Gates & `qpp::gt` = Gates::get\_instance()  
*qpp::Gates const Singleton*
- const States & `qpp::st` = States::get\_instance()  
*qpp::States const Singleton*

## 8.18 include/random.h File Reference

This graph shows which files directly or indirectly include this file:



## Namespaces

- `qpp`

## Functions

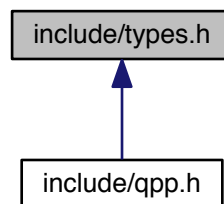
- template<typename Derived >  
Derived `qpp::rand` (std::size\_t rows, std::size\_t cols, double a=0, double b=1)
- template<>  
dmat `qpp::rand` (std::size\_t rows, std::size\_t cols, double a, double b)
- template<>  
cmat `qpp::rand` (std::size\_t rows, std::size\_t cols, double a, double b)
- double `qpp::rand` (double a=0, double b=1)
- long long `qpp::randint` (long long a, long long b)
- template<typename Derived >  
Derived `qpp::randn` (std::size\_t rows, std::size\_t cols, double mean=0, double sigma=1)
- template<>  
dmat `qpp::randn` (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- template<>  
cmat `qpp::randn` (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- double `qpp::randn` (double mean=0, double sigma=1)
- cmatrix `qpp::randU` (std::size\_t D)
- cmatrix `qpp::randV` (std::size\_t Din, std::size\_t Dout)
- std::vector< cmatrix > `qpp::randkraus` (std::size\_t n, std::size\_t D)
- cmatrix `qpp::randH` (std::size\_t D)



- ket [qpp::randket](#) (std::size\_t D)
- cmat [qpp::randrho](#) (std::size\_t D)
- std::vector< std::size\_t > [qpp::randperm](#) (std::size\_t n)

## 8.19 include/types.h File Reference

This graph shows which files directly or indirectly include this file:



### Namespaces

- [qpp](#)

### Typedefs

- using [qpp::cplx](#) = std::complex< double >  
*Complex number in double precision.*
- using [qpp::cmat](#) = Eigen::MatrixXcd  
*Complex (double precision) dynamic Eigen matrix.*
- using [qpp::dmat](#) = Eigen::MatrixXd  
*Real (double precision) dynamic Eigen matrix.*
- using [qpp::ket](#) = Eigen::Matrix< cplx, Eigen::Dynamic, 1 >  
*Complex (double precision) dynamic Eigen column matrix.*
- using [qpp::bra](#) = Eigen::Matrix< cplx, 1, Eigen::Dynamic >  
*Complex (double precision) dynamic Eigen row matrix.*
- template<typename Scalar >  
using [qpp::DynMat](#) = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >  
*Dynamic Eigen matrix over the field specified by Scalar.*

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