Quantum++ A C++11 quantum computing library

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Abstract: Quantum++ is a modern general-purpose multi-threaded quantum computing library written in C++11 and composed solely of header files. The library is not restricted to qubit systems or specific quantum information processing tasks, being capable of simulating arbitrary quantum processes. The main design factors taken in consideration were the ease of use, portability, and performance. The library's simulation capabilities are only restricted by the amount of available physical memory. On a typical machine (Intel i5 8Gb RAM) Quantum++ can successfully simulate the evolution of 25 qubits in a pure state or of 12 qubits in a mixed state reasonably fast.

Contents

1	Introduction	2
2	Installation	3
3	Data types, constants and global objects	3
	3.1 Data types	4
	3.2 Constants	4
	3.3 Singleton classes and their global instances	4
4	Simple examples	4
	4.1 Gates and states	5
	4.2 Measurements	
	4.3 Quantum operations	8
	4.4 Timing	10
	4.5 Input/output	
	4.6 Exceptions	
5	Brief description of Quantum++ file structure	13
6	Advanced topics	13
	6.1 Aliasing	13
	6.2 Type deduction via auto	
	6.3 Optimizations	
	6.4 Extending Quantum++	

Listings

1	Minimal example
2	Gates and states
3	Measurements
4	Quantum operations
5	Timing
6	Input/output
7	Exceptions 15

1 Introduction

Quantum++, available online at http://vsoftco.github.io/qpp, is a C++11 general purpose quantum computing library, composed solely of header files. It uses the Eigen 3 linear algebra library and, if available, the OpenMP multi-processing library. For additional Eigen 3 documentation see http://eigen.tuxfamily.org/dox/. For a simple Eigen 3 quick ASCII reference see http://eigen.tuxfamily.org/dox/AsciiQuickReference.txt.

The simulator defines a large collection of (template) quantum computing related functions and a few useful classes. The main data types are complex vectors and complex matrices, which I will describe below. Most functions operate on such vectors/matrices and *always* return the result by value. Collection of objects are implemented via the standard library container std::vector<>, instantiated accordingly.

Although there are many available quantum computing libraries/simulators written in various programming languages, see [1] for a comprehensive list, I hope what makes Quantum++ different is the ease of use, portability and high performance. The library is not restricted to specific quantum information tasks, but it is intended to be multi-purpose and capable of simulating arbitrary quantum processes. I have chosen the C++ programming language (standard C++11) in implementing the library as it is by now a mature standard, fully (or almost fully) implemented by most important compilers, and highly portable.

In the reminder of this manuscript I describe the main features of the library, "in a nutshell" fashion, via a series of simple examples. I assume that the reader is familiar with the basic concepts of quantum mechanics/quantum information, as I do not provide any introduction to this field. For a comprehensive introduction to the latter see e.g. [2]. This document is not intended to be a comprehensive documentation, but only a brief introduction to the library and its main features. For a detailed reference see the official manual available as a .pdf file in ./doc/refman.pdf. For detailed installation instructions as well as for additional information regarding the library see the main repository page at http://vsoftco.github.io/qpp. If you are interesting in contributing, or for any comments or suggestions, please email me at vgheorgh@gmail.com.

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2 Installation

To get started with Quantum++, first install the Eigen 3 library from http://eigen.tuxfamily.org into your home directory¹, as \$HOME/eigen. You can change the name of the directory, but in the current document I will use \$HOME/eigen as the location of the Eigen 3 library. Next, download the Quantum++ library from http://vsoftco.github.io/qpp/ and unzip it into the home directory as \$HOME/qpp. Finally, make sure that your compiler supports C++11 and preferably OpenMP. For a compiler I recommend g++ version 4.8.2 or later or clang version 3.7 or later (previous versions of clang do not support OpenMP). You are now ready to go!

We next build a simple minimal example to test that the installation was successful. Create a directory called \$HOME/testing, and inside it create the file minimal.cpp, with the content listed in Listing 1. A verbatim copy of the above program is also available at \$HOME/qpp/examples/minimal.cpp.

```
// Minimal example
// Source: ./examples/minimal.cpp
#include <iostream>
#include "qpp.h"

using namespace qpp;

int main()
{
    std::cout << "Hello Quantum++!\nThis is the |0> state:\n";
    std::cout << disp(st.z0) << '\n';
}</pre>
```

Listing 1: Minimal example

Next, compile the file using a C++11 compliant compiler. In the following I assume you use g++, but the building instructions are similar for other compilers. From the directory \$HOME/testing type

```
g++ -std=c++11 -isystem $HOME/eigen -I $HOME/qpp/include minimal.cpp -o minimal
```

Your compile command may differ from the above, depending on the C++ compiler and operating system. If everything went fine, the above command should build an executable minimal in \$HOME/testing, which can be run by typing ./minimal. The output should be similar to the following:

```
Hello Quantum++!
This is the |0> state:

1
0
```

Listing 1 output

In line 4 of Listing 1 we include the main header file of the library qpp.h This header file includes all other necessary internal Quantum++ header files. In line 11 we display the state $|0\rangle$ represented by the singleton st.z0 in a nice format using the display manipulator disp().

3 Data types, constants and global objects

All header files of Quantum++ are located inside the ./include directory. All functions, classes and global objects defined by the library belong to the namespace qpp. To avoid additional typing, I will omit the prefix qpp:: in the rest of this document. I recommend to use using namespace qpp; in your main .cpp file

 $^{^{1}}$ I implicitly assume that you use a UNIX-like system, although everything should translate into Windows as well, with slight modifications

3.1 Data types

The most important data types are defined in the header file types.h. We list them in Table 1.

idx	Index (non-negative integer), alias for std::size_t		
bigint	Big integer, alias for long long int		
cplx	Complex number, alias for std::complex <double></double>		
cmat	Complex dynamic matrix, alias for Eigen::MatrixXcd		
dmat	Double dynamic matrix, alias for Eigen::MatrixXd		
ket	Complex dynamic column vector, alias for Eigen::VectorXcd		
bra	Complex dynamic row vector, alias for Eigen::RowVectorXcd		
dyn_mat <scalar></scalar>	Dynamic matrix template alias over the field Scalar, alias for		
	Eigen::Matrix <scalar, eigen::dynamic="" eigen::dynamic,=""></scalar,>		
dyn_col_vect <scalar></scalar>	Dynamic column vector template alias over the field Scalar, alias for		
	Eigen::Matrix <scalar, 1="" eigen::dynamic,=""></scalar,>		
dyn_row_vect <scalar></scalar>	Dynamic row vector template alias over the field Scalar, alias for		
	Eigen::Matrix <scalar, 1,="" eigen::dynamic=""></scalar,>		

Table 1: User-defined data types

3.2 Constants

The important constants are defined in the header file constants.h and are listed in Table 2.

<pre>constexpr idx maxn = 64;</pre>	Maximum number of allowed qu(d)its (subsystems)
<pre>constexpr double pi = 3.1415;</pre>	π
<pre>constexpr double ee = 2.7182;</pre>	e, base of natural logarithms
constexpr double eps = 1e-12;	Used in comparing floating point values to zero
<pre>constexpr double chop = 1e-10;</pre>	Used in display manipulators to set numbers to zero
<pre>constexpr double infty =;</pre>	Used to denote infinity in double precision
constexpr cplx operator""_i	User-defined literal for the imaginary number $i := \sqrt{-1}$
(unsigned long long int x)	
constexpr cplx operator""_i	User-defined literal for the imaginary number $i := \sqrt{-1}$
(unsigned long double int x)	
cplx omega(idx D)	D-th root of unity $e^{2\pi i/D}$

Table 2: User-defined constants

3.3 Singleton classes and their global instances

Some useful classes are defined as singletons and their instances are globally available, being initialized at runtime in the header file qpp.h, before main(). They are listed in Table 3.

4 Simple examples

All of the examples of this section are copied verbatim from the directory ./examples and are fully compilable. For convenience, the location of the source file is displayed in the first line of each example as a C++ comment. The examples are simple and demonstrate the main features of Quantum++. They cover

<pre>const Init& init = Init::get_instance();</pre>	Library initialization
<pre>const Codes& codes = Codes::get_instance();</pre>	Quantum error correcting codes
<pre>const Gates& gt = Gates::get_instance();</pre>	Quantum gates
<pre>const States& st = States::get_instance();</pre>	Quantum states
RandomDevices& rdevs =	Random devices/generators/engines
<pre>RandomDevices::get_thread_local_instance();</pre>	

Table 3: Global singleton classes and instances

only a small part of library functions, but enough to get the interested user started. For an extensive reference of all library functions, including various overloads, the user should consult the complete reference ./doc/refman.pdf. See the rest of the examples (not discussed in this document) in ./examples/. for more comprehensive code snippets.

4.1 Gates and states

Let us introduce the main objects used by Quantum++: gates, states and basic operations. Consider the code in Listing 2.

```
// Gates and states
   // Source: ./examples/gates_states.cpp
   #include <iostream>
   #include "qpp.h"
   using namespace qpp;
   int main()
       ket psi = st.z0; // |0> state
10
       cmat U = gt.X;
11
       ket result = U * psi;
12
13
       std::cout << ">> The result of applying the bit-flip gate X on |0> is:\n";
14
       std::cout << disp(result) << '\n';</pre>
15
16
       psi = mket({1, 0}); // |10> state
17
       U = gt.CNOT; // Controlled-NOT
18
       result = U * psi;
19
       std::cout << ">> The result of applying the gate CNOT on |10> is:\n";
21
       std::cout << disp(result) << '\n';</pre>
22
23
       U = randU();
       std::cout << ">> Generating a random one-qubit gate U:\n";
25
       std::cout << disp(U) << '\n';</pre>
27
       result = applyCTRL(psi, U, {0}, {1}); // Controlled-U
       std::cout << ">> The result of applying the CTRL-U gate on |10> is:\n";
29
       std::cout << disp(result) << '\n';</pre>
```

A possible output is:

```
>> The result of applying the bit-flip gate X on |0> is:
0
1
>> The result of applying the gate CNOT on |10> is:
0
0
0
1
>> Generating a random one-qubit gate U:
-0.791458 + 0.232875i -0.168866 - 0.539303i
-0.458344 - 0.330583i -0.470968 + 0.677366i
>> The result of applying the CTRL-U gate on |10> is:
                   0
                   0
-0.791458 + 0.232875i
-0.458344 - 0.330583i
```

Listing 2 output

In line 4 of Listing 2 we bring the namespace qpp into the global namespace.

In line 10 we use the States singleton st to declare psi as the zero eigenvector $|0\rangle$ of the Z Pauli operator. In line 11 we use the Gates singleton gt and assign to U the bit flip gate gt.X. In line 12 we compute the result of the operation $X|0\rangle$, and display the result $|1\rangle$ in lines 14 and 15. In line 15 we use the display manipulator disp(), which is especially useful when displaying complex matrices, as it displays the entries of the latter in the form a+bi, in contrast to the form (a,b) used by the C++ standard library. The manipulator also accepts additional parameters that allows e.g. setting to zero numbers smaller than some given value (useful to chop small values), and it is in addition overloaded for standard containers, iterators and C-style arrays.

In line 17 we reassign to psi the state $|10\rangle$ via the function mket(). We could have also used the Eigen 3 insertion operator

```
ket psi(4); // must specify the dimension before insertion of elements via <<
psi << 0, 0, 1, 0;</pre>
```

however the mket() function is more concise. In line 18 we declare a gate U as the Controlled-NOT with control as the first subsystem, and target as the last, using the global singleton gt. In line 19 we declare the ket result as the result of applying the Controlled-NOT gate to the state $|10\rangle$, i.e. $|11\rangle$. We then display the result of the computation in lines 21 and 22.

Next, in line 24 we generate a random unitary gate via the function randU(), then in line 28 apply the Controlled-U, with control as the first qubit and target as the second qubit, to the state psi. Finally, we display the result in lines 29 and 30.

4.2 Measurements

Let us now complicate things a bit and introduce measurements. Consider the example in Listing 3.

```
// Measurements
// Source: ./examples/measurements.cpp
// #include <iostream>
// #include <tuple>
```

```
#include "qpp.h"
  using namespace qpp;
  int main()
       ket psi = mket({0, 0});
11
       cmat U = gt.CNOT * kron(gt.H, gt.Id2);
12
       ket result = U * psi; // we have the Bell state (|00> + |11>) / sqrt(2)
13
14
       std::cout << ">>> We just produced the Bell state:\n";
15
       std::cout << disp(result) << '\n';</pre>
16
17
       // apply a bit flip on the second qubit
18
       result = apply(result, gt.X, {1}); // we produced (|01> + |10>) / sqrt(2)
       std::cout << ">> We produced the Bell state:\n";
20
       std::cout << disp(result) << '\n';</pre>
21
22
       // measure the first qubit in the X basis
       auto measured = measure(result, gt.H, {0});
24
       std::cout << ">> Measurement result: " << std::get<0>(measured) << '\n';
       std::cout << ">> Probabilities: ";
       std::cout << disp(std::get<1>(measured), ", ") << '\n';
       std::cout << ">> Resulting states:\n";
28
       for (auto&& it : std::get<2>(measured))
           std::cout << disp(it) << "\n\n";
30
  }
```

Listing 3: Measurements

A possible output is:

```
>> We just produced the Bell state:

0.707107

0
0
0.707107

>> We produced the Bell state:

0
0.707107

0.707107

0
>> Measurement result: 0
>> Probabilities: [0.5, 0.5]
>> Resulting states:
0.707107

-0.707107

-0.707107
```

Listing 3 output

In line 12 of Listing 3 we use the function kron() to create the tensor product (Kronecker product) of the Hadamard gate on the first qubit and identity on the second qubit, then we left-multiply it by the Controlled-NOT gate. In line 13 we compute the result of the operation $CNOT_{ab}(H \otimes I)|00\rangle$, which is the Bell state $(|00\rangle + |11\rangle)/\sqrt{2}$. We display it in lines 15 and 16.

In line 19 we use the function apply() to apply the gate X on the second qubit² of the previously produced Bell state. The function apply() takes as its third parameter a list of subsystems, and in our case {1} denotes the *second* subsystem, not the first. The function apply(), as well as many other functions that we will encounter, have a variety of useful overloads, see doc/refman.pdf for a detailed library reference. In lines 20 and 21 we display the newly created Bell state.

In line 24 we use the function measure() to perform a measurement of the first qubit (subsystem {0}) in the X basis. You may be confused by the apparition of gt.H, however this overload of the function measure() takes as its second parameter the measurement basis, specified as the columns of a complex matrix. In our case, the eigenvectors of the X operator are just the columns of the Hadamard matrix. As mentioned before, as all other library functions, measure() returns by value, hence it does not modify its argument. The return of measure is a tuple consisting of the measurement result, the outcome probabilities, and the possible output states. Technically measure() returns a tuple of 3 elements

```
std::tuple<qpp::idx, std::vector<double>, std::vector<qpp::cmat>>
```

The first element represents the measurement result, the second the possible output probabilities and the third the output output states. Instead of using this long type definition, we use the new C++11 auto keyword to define the type of the result measured of measure(). In lines 25-30 we use the standard std::get<>() function to retrieve each element of the tuple, then display the measurement result, the probabilities and the resulting output states.

4.3 Quantum operations

In Listing 4 we introduce quantum operations: quantum channels, as well as the partial trace and partial transpose operations.

```
// Quantum operations
   // Source: ./examples/quantum_operations.cpp
   #include <iostream>
   #include <vector>
   #include "qpp.h"
   using namespace qpp;
   int main()
   {
10
       cmat rho = st.pb00; // projector onto the Bell state (|00> + |11>) / sqrt(2)
11
       std::cout << ">> Initial state:\n";
12
       std::cout << disp(rho) << '\n';
13
14
       // partial transpose of first subsystem
15
       cmat rhoTA = ptranspose(rho, {0});
16
       std::cout << ">> Eigenvalues of the partial transpose "
17
                  << "of Bell-0 state are:\n";
18
       std::cout << disp(transpose(hevals(rhoTA))) << '\n';</pre>
19
20
       std::cout << ">> Measurement channel with 2 Kraus operators:\n";
       std::vector<cmat> Ks{st.pz0, st.pz1}; // 2 Kraus operators
22
```

²Quantum++ uses the C/C++ numbering convention, with indexes starting from zero.

```
std::cout << disp(Ks[0]) << "\nand\n" << disp(Ks[1]) << '\n';
23
24
       std::cout << ">> Superoperator matrix of the channel:\n";
25
       std::cout << disp(kraus2super(Ks)) << '\n';</pre>
27
       std::cout << ">> Choi matrix of the channel:\n";
       std::cout << disp(kraus2choi(Ks)) << '\n';</pre>
29
       // apply the channel onto the first subsystem
31
       cmat rhoOut = apply(rho, Ks, {0});
32
       std::cout << ">> After applying the measurement channel "
33
                  << "on the first qubit:\n";
34
       std::cout << disp(rhoOut) << '\n';</pre>
35
       // take the partial trace over the second subsystem
37
       cmat rhoA = ptrace(rhoOut, {1});
38
       std::cout << ">> After partially tracing down the second subsystem:\n";
       std::cout << disp(rhoA) << '\n';</pre>
40
41
       // compute the von-Neumann entropy
42
       double ent = entropy(rhoA);
       std::cout << ">> Entropy: " << ent << '\n';
44
  }
```

Listing 4: Quantum operations

The output of this program is:

```
>> Initial state:
0.5
    0
              0.5
        0
 0
      0
          0
                0
     0
                0
 0
          0
              0.5
          0
>> Eigenvalues of the partial transpose of Bell-O state are:
       0.5
             0.5
                   0.5
>> Measurement channel with 2 Kraus operators:
1
0
    0
and
0
    0
0
    1
>> Superoperator matrix of the channel:
    0
        0
            0
1
0
    0
        0
            0
0
    0
        0
            0
0
    0
        0
            1
>> Choi matrix of the channel:
    0
        0
            0
1
        0
0
    0
            0
0
    0
        0
            0
    0
>> After applying the measurement channel on the first qubit:
```

Listing 4 output

The example should by now be self-explanatory. In line 11 of Listing 4 we define the input state **rho** as the projector onto the Bell state $(|00\rangle + |11\rangle)/\sqrt{2}$, then display it in lines 12 and 13.

In lines 16–19 we partially transpose the first qubit, then display the eigenvalues of the resulting matrix rhoTA.

In lines 21–23 we define a quantum channel Ks consisting of two Kraus operators: $|0\rangle\langle 0|$ and $|1\rangle\langle 1|$, then display the latter. Note that Quantum++ uses the std::vector<cmat> container to store the Kraus operators and define a quantum channel.

In lines 25–29 we display the superoperator matrix as well as the Choi matrix of the channel Ks.

Next, in lines 32–35 we apply the channel Ks to the first qubit of the input state rho, then display the output state rhoOut.

In lines 38–40 we take the partial trace of the output state rhoOut, then display the resulting state rhoA. Finally, in lines 43 and 44 we compute the von-Neumann entropy of the resulting state and display it.

4.4 Timing

To facilitate simple timing tasks, Quantum++ provides a Timer class that uses internally a std::steady_clock. The program in Listing 5 demonstrate its usage.

```
// Timing
  // Source: ./examples/timing.cpp
  #include <iomanip>
  #include <iostream>
  #include <vector>
   #include "qpp.h"
  using namespace qpp;
   int main()
10
11
       std::cout << std::setprecision(8); // increase the default output precision</pre>
12
13
       // get the first codeword from Shor's [[9,1,3]] code
14
       ket c0 = codes.codeword(Codes::Type::NINE_QUBIT_SHOR, 0);
15
16
       Timer<> t; // declare and start a timer
17
       std::vector<idx> perm = randperm(9); // declare a random permutation
18
       ket cOperm = syspermute(cO, perm); // permute the system
19
       t.toc(); // stops the timer
20
       std::cout << ">> Permuting subsystems according to " << disp(perm, ", ");
21
       std::cout << "\n>> It took " << t << " seconds to permute the subsytems.\n";
22
23
       t.tic(); // restart the timer
24
       std::cout << ">> Inverse permutation: ";
```

```
std::cout << disp(invperm(perm), ", ") << '\n';
ket c0invperm = syspermute(c0perm, invperm(perm)); // permute again
std::cout << ">> It took " << t.toc();
std::cout << " seconds to un-permute the subsystems.\n";

std::cout << ">> Norm difference: " << norm(c0invperm - c0) << '\n';
}</pre>
```

Listing 5: Timing

A possible output of this program is:

```
>> Permuting subsystems according to [6, 4, 7, 0, 3, 1, 8, 5, 2]
>> It took 0.000685 seconds to permute the subsystems.
>> Inverse permutation: [3, 5, 8, 4, 1, 7, 0, 2, 6]
>> It took 0.000415 seconds to un-permute the subsystems.
>> Norm difference: 0
```

Listing 5 output

In line 12 of Listing 5 we change the default output precision from 4 to 8 decimals after the delimiter. In line 15 we use the Codes singleton codes to retrieve in c0 the first codeword of the Shor's [[9,1,3]] quantum error correcting code.

In line 17 we declare an instance timer of the class Timer. In line 18 we declare a random permutation perm via the function randperm(). In line 19 we permute the codeword according to the permutation perm using the function syspermute() and store the result. In line 20 we stop the timer. In line 21 we display the permutation, using an overloaded form of the disp() manipulator for C++ standard library containers. The latter takes a std::string as its second parameter to specify the delimiter between the elements of the container. In line 22 we display the elapsed time using the ostream operator<<() operator overload for Timer objects.

Next, in line 24 we reset the timer, then display the inverse permutation of perm in lines 25 and 26. In line 27 we permute the already permuted state coperm according to the inverse permutation of perm, and store the result in coinvperm. In lines 28 and 29 we display the elapsed time. Note that in line 28 we used directly t.toc() in the stream insertion operator, since, for convenience, the member function Timer::toc() returns a const Timer&.

Finally, in line 31, we verify that by permuting and permuting again using the inverse permutation we recover the initial codeword, i.e. the norm difference has to be zero.

4.5 Input/output

We now introduce the input/output functions of Quantum++, as well as the input/output interfacing with MATLAB. The program in Listing 6 saves a matrix in both Quantum++ internal format as well as in MATLAB format, then loads it back and tests that the norm difference between the saved/loaded matrix is zero.

```
1  // Input/output
2  // Source: ./examples/input_output.cpp
3  #include <iostream>
4  #include "qpp.h"
5  #include "MATLAB/matlab.h" // must be explicitly included
6
7  using namespace qpp;
8
9  int main()
```

```
{
10
       // Quantum++ native input/output
11
       cmat rho = randrho(256); // an 8 qubit density operator
12
       save(rho, "rho.dat"); // save it
       cmat loaded_rho = load<cmat>("rho.dat"); // load it back
14
       // display the difference in norm, should be 0
       std::cout << ">> Norm difference load/save: ";
16
       std::cout << norm(loaded_rho - rho) << '\n';</pre>
17
18
       // interfacing with MATLAB
19
       saveMATLAB(rho, "rho.mat", "rho", "w");
20
       loaded_rho = loadMATLAB<cmat>("rho.mat", "rho");
21
       // display the difference in norm, should be 0
22
       std::cout << ">> Norm difference MATLAB load/save: ";
23
       std::cout << norm(loaded_rho - rho) << '\n';</pre>
24
   }
25
```

Listing 6: Input/output

The output of this program is:

```
>> Norm difference load/save: 0
>> Norm difference MATLAB load/save: 0
```

Listing 6 output

Note that in order to use the MATLAB input/output interface support, you need to explicitly include the header file MATLAB/matlab.h, and you also need to have MATLAB or MATLAB compiler installed, otherwise the program fails to compile. See the file ./README.md for extensive details about compiling with MATLAB support.

4.6 Exceptions

Most Quantum++ functions throw exceptions in the case of unrecoverable errors, such as out-of-range input parameters, input/output errors etc. The exceptions are handled via the class Exception, derived from std::exception. The exception types are hard-coded inside the strongly-typed enumeration (enum class) Exception::Type. If you want to add more exceptions, augment the enumeration Exception::Type and also modify accordingly the member function Exception::construct_exception_msg_(), which constructs the exception message displayed via the overridden virtual function Exception::what(). Listing 7 illustrates the basics of exception handling in Quantum++.

```
// Exceptions
  // Source: ./examples/exceptions.cpp
   #include <exception>
  #include <iostream>
   #include "qpp.h"
   using namespace qpp;
   int main()
   {
10
       cmat rho = randrho(16); // 4 qubits (subsystems)
11
       try
12
       {
13
           // the line below throws qpp::exception::SubsysMismatchDims
14
```

```
double mInfo = qmutualinfo(rho, {0}, {4});
std::cout << ">> Mutual information between first and last subsystem: ";
std::cout << mInfo << '\n';

std::cout << mInfo </ mInfo
```

Listing 7: Exceptions

The output of this program is:

```
>> Exception caught: IN qpp::qmutualinfo(): Subsystems mismatch dimensions!
```

Listing 7 output

In line 11 of Listing 7 we define a random density matrix on four qubits (dimension 16). In line 15, we compute the mutual information between the first and the 5-th subsystem. Line 15 throws an exception of type qpp::exception::SubsysMismatchDim exception, as there are only four systems. We next catch the exception in line 19 via the std::exception standard exception base class. We could have also used the Quantum++ exception base class qpp::exception::Exception, however using the std::exception allows the catching of other exceptions, not just of the type Exception. Finally, in line 21 we display the corresponding exception message.

5 Brief description of Quantum++ file structure

A brief description of the Quantum++ file structure is presented in Figure 1. The directories and their brief descriptions are emphasized using **bold fonts**. The main header file qpp.h is emphasized in red fonts.

6 Advanced topics

6.1 Aliasing

Aliasing occurs whenever the same Eigen 3 matrix/vector appears on both sides of the assignment operator, and happens because of Eigen 3's lazy evaluation system. Examples that exhibit aliasing:

```
mat = 2 * mat;
or
mat = mat.transpose();
Aliasing does not occur in statements like
mat = f(mat);
```

where f() returns by value. Aliasing produces in general unexpected results, and should be avoided at all costs.

Whereas the first line produces aliasing, it is not dangerous, since the assignment is done in a one-to-one manner, i.e. each element (i,j) on the left hand side of the assignment operator is solely a function of the the same (i,j) element on the right hand side, i.e. mat(i,j) = f(mat(i,j)), $\forall i,j$. The problem appears whenever coefficients are being combined and overlap, such as in the second example, where mat(i,j) = mat(j,i), $\forall i,j$. To avoid aliasing, use the member function eval() to transform the right hand side object into a temporary, such as

$_\operatorname{doc}/$ Documentation
igsquare html/
index.html
quick.pdf
refman.pdf
$_$ examples $/$
ex*.cppExample source file
$_$ include $/$ \cdots Header file
LMATLAB/MATLAB suppor
matlab.h
classes/ Class definition
codes.hQuantum error correcting code
exception.h Exception
gates.h Quantum gate
idisplay.hInterface for stream extraction
init.hInitialization
random_devices.h
states.hQuantum state
timer.h
experimental/ Experimental/test functions/classes, do not use or modify
experimental.h Experimental/test functions/classe
internal implementation details, do not use/modify
classes/Internal class definition
iomanip.h
singleton.h
util.hInternal utility function
constants.h
entanglement.h
entropies.h Entropy function
functions.h
input_output.h
input_output.h
input_output.h
input_output.h
input_output.hinput/output functioninstruments.h Measurement function Number_theory.h Number theory function Quantum operation function qpp.h Quantum++ main header file, includes all other necessary header
input_output.h
input_output.h Input/output function instruments.h Measurement function number_theory.h Number theory function operations.h Quantum operation function qpp.h Quantum++ main header file, includes all other necessary header random.h Randomness function statistics.h Statistics function traits.h Type trait types.h Type aliase unit_tests/ Unit testing with Google Mock/Test (included in lib CHANGES Modifications added by each version CMakeLists.txt cmake configuration file, builds ./examples/minimal.cpp and the unit test
input_output.h
input_output.h
input_output.h
input_output.h

Figure 1: Quantum++ file structure

```
mat = 2 * mat.eval();
```

In general, aliasing can not be detected at compile time, but can be detected at runtime whenever the compile flag EIGEN_NO_DEBUG is not set. Quantum++ does not set this flag in debug mode. I highly recommend to first compile your program in debug mode to detect aliasing run-time assertions, as well as other possible issues that may have escaped you, such as assigning to a matrix another matrix of different dimension etc.

For more details about aliasing, see the official Eigen 3 documentation at http://eigen.tuxfamily.org/dox/group__TopicAliasing.html.

6.2 Type deduction via auto

Avoid the usage of auto when working with Eigen 3 expressions, e.g. avoid writing code like

```
auto mat = A * B + C;
but write instead
cmat mat = A * B + C;
or
auto mat = (A * B + C).eval();
```

to force evaluation, as otherwise you may get unexpected results. The "problem" lies in the Eigen 3 lazy evaluation system and reference binding, see e.g. http://stackoverflow.com/q/26705446/3093378 for more details. In short, the reference to the internal data represented by the expression A * B + C is dangling at the end of the auto mat = A * B + C; statement.

6.3 Optimizations

Whenever testing your application, I recommend compiling in debug mode, as Eigen 3 run-time assertions can provide extremely helpful feedback on potential issues. Whenever the code is production-ready, you should always compile with optimization flags turned on, such as -03 (for g++) and -DEIGEN_NO_DEBUG. You should also turn on the OpenMP (if available) multi-processing flag (-fopenmp for g++), as it enables multi-core/multi-processing with shared memory. Eigen 3 uses multi-processing when available, e.g. in matrix multiplication. Quantum++ also uses multi-processing in computationally-intensive functions.

Since most Quantum++ functions return by value, in assignments of the form

```
mat = f(another_mat);
```

there is an additional copy assignment operator when assigning the temporary returned by f() back to mat. As far as I know, this extra copy operation is not elided. Unfortunately, Eigen 3 does not yet support move semantics, which would have got rid of this additional assignment via the corresponding move assignment operator. If in the future Eigen 3 will support move semantics, the additional assignment operator will be "free", and you won't have to modify any existing code to enable the optimization; the Eigen 3 move assignment operator should take care of it for you.

Note that in a line of the form

```
cmat mat = f(another_mat);
```

most compilers perform return value optimization (RVO), i.e. the temporary on the right hand side is constructed directly inside the object mat, the copy constructor being elided.

6.4 Extending Quantum++

Most Quantum++ operate on Eigen 3 matrices/vectors, and return either a matrix or a scalar. In principle, you may be tempted to write a new function such as

```
cmat f(const cmat& A){...}
```

The problem with the approach above is that Eigen 3 uses expression templates as the type of each expression, i.e. different expressions have in general different types, see the official Eigen 3 documentation at http://eigen.tuxfamily.org/dox/TopicFunctionTakingEigenTypes.html for more details. The correct way to write a generic function that is guaranteed to work with any matrix expression is to make your function template and declare the input parameter as Eigen::MatrixBase<Derived>, where Derived is the template parameter. For example, the Quantum++ transpose() function is defined as

```
template<typename Derived>
dyn_mat<typename Derived::Scalar>
transpose(const Eigen::MatrixBase<Derived>& A)

{
    const dyn_mat<typename Derived::Scalar>& rA = A.derived();

// check zero-size
    if (!internal::check_nonzero_size(rA))
        throw Exception("qpp::transpose()", Exception::Type::ZERO_SIZE);

return rA.transpose();
}
```

It takes an Eigen 3 matrix expression, line 3, and returns a dynamic matrix over the scalar field of the expression, line 2. In line 5 we implicitly convert the input expression A to a dynamic matrix rA over the same scalar field as the expression, via binding to a const reference, therefore paying no copying cost. We then use rA instead of the original expression A in the rest of the function. Note that most of the time it is OK to use the original expression, however there are some cases where you may get a compile time error if the expression is not explicitly casted to a matrix. For consistency, I use this reference binding trick in the code of all Quantum++ functions.

As you may have already seen, Quantum++ consists mainly of a collection of functions and few classes. There is no complicated class hierarchy, and you can regard the Quantum++ API as a medium-level API. You may extend it to incorporate graphical input, e.g. use a graphical library such as Qt, or build a more sophisticated library on top of it. I recommend to read the source code and make yourself familiar with the library before deciding to extend it. You should also check the complete reference manual ./doc/refman.pdf for an extensive documentation of all functions and classes. I hope you find Quantum++ useful and wish you a happy usage!

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