

Quantum++

v1.0-rc2

Generated by Doxygen 1.8.13



# Contents

<b>1</b>	<b>Quantum++</b>	<b>1</b>
<b>2</b>	<b>Namespace Index</b>	<b>7</b>
2.1	Namespace List . . . . .	7
<b>3</b>	<b>Hierarchical Index</b>	<b>9</b>
3.1	Class Hierarchy . . . . .	9
<b>4</b>	<b>Class Index</b>	<b>11</b>
4.1	Class List . . . . .	11
<b>5</b>	<b>File Index</b>	<b>15</b>
5.1	File List . . . . .	15
<b>6</b>	<b>Namespace Documentation</b>	<b>17</b>
6.1	qpp Namespace Reference . . . . .	17
6.1.1	Detailed Description . . . . .	26
6.1.2	Typedef Documentation . . . . .	26
6.1.2.1	bigint . . . . .	26
6.1.2.2	bra . . . . .	26
6.1.2.3	cmat . . . . .	26
6.1.2.4	cplx . . . . .	26
6.1.2.5	dmat . . . . .	26
6.1.2.6	dyn_col_vect . . . . .	27
6.1.2.7	dyn_mat . . . . .	27
6.1.2.8	dyn_row_vect . . . . .	27

6.1.2.9	idx	27
6.1.2.10	ket	28
6.1.2.11	to_void	28
6.1.3	Function Documentation	28
6.1.3.1	apply() [1/5]	28
6.1.3.2	apply() [2/5]	29
6.1.3.3	apply() [3/5]	29
6.1.3.4	apply() [4/5]	30
6.1.3.5	apply() [5/5]	30
6.1.3.6	applyCTRL() [1/2]	31
6.1.3.7	applyCTRL() [2/2]	31
6.1.3.8	avg()	32
6.1.3.9	choi2kraus()	32
6.1.3.10	choi2super()	33
6.1.3.11	compperm()	33
6.1.3.12	concurrence()	34
6.1.3.13	contfrac2x()	34
6.1.3.14	cor()	34
6.1.3.15	cov()	35
6.1.3.16	disp() [1/5]	35
6.1.3.17	disp() [2/5]	36
6.1.3.18	disp() [3/5]	36
6.1.3.19	disp() [4/5]	37
6.1.3.20	disp() [5/5]	37
6.1.3.21	egcd()	38
6.1.3.22	entanglement() [1/2]	38
6.1.3.23	entanglement() [2/2]	39
6.1.3.24	entropy() [1/2]	39
6.1.3.25	entropy() [2/2]	40
6.1.3.26	factors()	40

6.1.3.27	<a href="#">gcd()</a> <a href="#">[1/2]</a>	40
6.1.3.28	<a href="#">gcd()</a> <a href="#">[2/2]</a>	41
6.1.3.29	<a href="#">gconcurrency()</a>	41
6.1.3.30	<a href="#">invperm()</a>	42
6.1.3.31	<a href="#">ip()</a> <a href="#">[1/2]</a>	42
6.1.3.32	<a href="#">ip()</a> <a href="#">[2/2]</a>	43
6.1.3.33	<a href="#">isprime()</a>	43
6.1.3.34	<a href="#">kraus2choi()</a>	43
6.1.3.35	<a href="#">kraus2super()</a>	44
6.1.3.36	<a href="#">lcm()</a> <a href="#">[1/2]</a>	44
6.1.3.37	<a href="#">lcm()</a> <a href="#">[2/2]</a>	45
6.1.3.38	<a href="#">load()</a>	45
6.1.3.39	<a href="#">loadMATLAB()</a> <a href="#">[1/2]</a>	46
6.1.3.40	<a href="#">loadMATLAB()</a> <a href="#">[2/2]</a>	46
6.1.3.41	<a href="#">lognegativity()</a> <a href="#">[1/2]</a>	47
6.1.3.42	<a href="#">lognegativity()</a> <a href="#">[2/2]</a>	48
6.1.3.43	<a href="#">marginalX()</a>	48
6.1.3.44	<a href="#">marginalY()</a>	48
6.1.3.45	<a href="#">measure()</a> <a href="#">[1/9]</a>	49
6.1.3.46	<a href="#">measure()</a> <a href="#">[2/9]</a>	49
6.1.3.47	<a href="#">measure()</a> <a href="#">[3/9]</a>	50
6.1.3.48	<a href="#">measure()</a> <a href="#">[4/9]</a>	50
6.1.3.49	<a href="#">measure()</a> <a href="#">[5/9]</a>	51
6.1.3.50	<a href="#">measure()</a> <a href="#">[6/9]</a>	51
6.1.3.51	<a href="#">measure()</a> <a href="#">[7/9]</a>	52
6.1.3.52	<a href="#">measure()</a> <a href="#">[8/9]</a>	53
6.1.3.53	<a href="#">measure()</a> <a href="#">[9/9]</a>	53
6.1.3.54	<a href="#">measure_seq()</a> <a href="#">[1/2]</a>	54
6.1.3.55	<a href="#">measure_seq()</a> <a href="#">[2/2]</a>	55
6.1.3.56	<a href="#">modinv()</a>	55

6.1.3.57	<code>modmul()</code>	56
6.1.3.58	<code>modpow()</code>	56
6.1.3.59	<code>negativity()</code> [1/2]	57
6.1.3.60	<code>negativity()</code> [2/2]	57
6.1.3.61	<code>omega()</code>	57
6.1.3.62	<code>operator""_i()</code> [1/2]	59
6.1.3.63	<code>operator""_i()</code> [2/2]	59
6.1.3.64	<code>ptrace()</code> [1/2]	59
6.1.3.65	<code>ptrace()</code> [2/2]	60
6.1.3.66	<code>ptrace1()</code> [1/2]	60
6.1.3.67	<code>ptrace1()</code> [2/2]	61
6.1.3.68	<code>ptrace2()</code> [1/2]	61
6.1.3.69	<code>ptrace2()</code> [2/2]	62
6.1.3.70	<code>ptranspose()</code> [1/2]	62
6.1.3.71	<code>ptranspose()</code> [2/2]	63
6.1.3.72	<code>qmutualinfo()</code> [1/2]	63
6.1.3.73	<code>qmutualinfo()</code> [2/2]	64
6.1.3.74	<code>rand()</code> [1/5]	64
6.1.3.75	<code>rand()</code> [2/5]	65
6.1.3.76	<code>rand()</code> [3/5]	65
6.1.3.77	<code>rand()</code> [4/5]	66
6.1.3.78	<code>rand()</code> [5/5]	66
6.1.3.79	<code>randH()</code>	67
6.1.3.80	<code>randidx()</code>	67
6.1.3.81	<code>randket()</code>	68
6.1.3.82	<code>randkraus()</code>	68
6.1.3.83	<code>randn()</code> [1/4]	68
6.1.3.84	<code>randn()</code> [2/4]	69
6.1.3.85	<code>randn()</code> [3/4]	69
6.1.3.86	<code>randn()</code> [4/4]	70

6.1.3.87	<code>randperm()</code>	70
6.1.3.88	<code>randprime()</code>	71
6.1.3.89	<code>randprob()</code>	71
6.1.3.90	<code>randrho()</code>	71
6.1.3.91	<code>randU()</code>	72
6.1.3.92	<code>randV()</code>	72
6.1.3.93	<code>renyi()</code> [1/2]	73
6.1.3.94	<code>renyi()</code> [2/2]	73
6.1.3.95	<code>save()</code>	74
6.1.3.96	<code>saveMATLAB()</code> [1/2]	74
6.1.3.97	<code>saveMATLAB()</code> [2/2]	75
6.1.3.98	<code>schmidtA()</code> [1/2]	75
6.1.3.99	<code>schmidtA()</code> [2/2]	76
6.1.3.100	<code>schmidtB()</code> [1/2]	76
6.1.3.101	<code>schmidtB()</code> [2/2]	76
6.1.3.102	<code>schmidtcoeffs()</code> [1/2]	77
6.1.3.103	<code>schmidtcoeffs()</code> [2/2]	77
6.1.3.104	<code>schmidtprobs()</code> [1/2]	78
6.1.3.105	<code>schmidtprobs()</code> [2/2]	78
6.1.3.106	<code>sigma()</code>	79
6.1.3.107	<code>super2choi()</code>	79
6.1.3.108	<code>syspermute()</code> [1/2]	81
6.1.3.109	<code>syspermute()</code> [2/2]	81
6.1.3.110	<code>tsallis()</code> [1/2]	82
6.1.3.111	<code>tsallis()</code> [2/2]	82
6.1.3.112	<code>uniform()</code>	83
6.1.3.113	<code>var()</code>	83
6.1.3.114	<code>x2contfrac()</code>	83
6.1.4	Variable Documentation	84
6.1.4.1	<code>chop</code>	84

6.1.4.2	<a href="#">ee</a>	84
6.1.4.3	<a href="#">eps</a>	84
6.1.4.4	<a href="#">infty</a>	85
6.1.4.5	<a href="#">maxn</a>	85
6.1.4.6	<a href="#">pi</a>	85
6.2	<a href="#">qpp::exception Namespace Reference</a>	85
6.2.1	<a href="#">Detailed Description</a>	86
6.3	<a href="#">qpp::experimental Namespace Reference</a>	87
6.3.1	<a href="#">Detailed Description</a>	87
6.4	<a href="#">qpp::internal Namespace Reference</a>	87
6.4.1	<a href="#">Detailed Description</a>	88
6.4.2	<a href="#">Function Documentation</a>	88
6.4.2.1	<a href="#">check_cvector()</a>	88
6.4.2.2	<a href="#">check_dims()</a>	88
6.4.2.3	<a href="#">check_dims_match_cvect()</a>	89
6.4.2.4	<a href="#">check_dims_match_mat()</a>	89
6.4.2.5	<a href="#">check_dims_match_rvect()</a>	89
6.4.2.6	<a href="#">check_eq_dims()</a>	89
6.4.2.7	<a href="#">check_matching_sizes()</a>	89
6.4.2.8	<a href="#">check_nonzero_size()</a>	89
6.4.2.9	<a href="#">check_perm()</a>	90
6.4.2.10	<a href="#">check_qubit_cvector()</a>	90
6.4.2.11	<a href="#">check_qubit_matrix()</a>	90
6.4.2.12	<a href="#">check_qubit_rvector()</a>	90
6.4.2.13	<a href="#">check_qubit_vector()</a>	90
6.4.2.14	<a href="#">check_rvector()</a>	90
6.4.2.15	<a href="#">check_square_mat()</a>	91
6.4.2.16	<a href="#">check_subsys_match_dims()</a>	91
6.4.2.17	<a href="#">check_vector()</a>	91
6.4.2.18	<a href="#">dirsum2()</a>	91
6.4.2.19	<a href="#">get_dim_subsys()</a>	91
6.4.2.20	<a href="#">get_num_subsys()</a>	91
6.4.2.21	<a href="#">kron2()</a>	92
6.4.2.22	<a href="#">multiidx2n()</a>	92
6.4.2.23	<a href="#">n2multiidx()</a>	92
6.4.2.24	<a href="#">variadic_vector_emplace()</a> <sup>[1/2]</sup>	92
6.4.2.25	<a href="#">variadic_vector_emplace()</a> <sup>[2/2]</sup>	92



<b>7</b>	<b>Class Documentation</b>	<b>93</b>
7.1	qpp::experimental::Bit_circuit Class Reference	93
7.1.1	Member Function Documentation	94
7.1.1.1	CNOT()	95
7.1.1.2	FRED()	95
7.1.1.3	NOT()	95
7.1.1.4	reset()	95
7.1.1.5	SWAP()	95
7.1.1.6	TOF()	95
7.1.1.7	X()	95
7.1.2	Member Data Documentation	96
7.1.2.1	gate_count	96
7.2	qpp::Bit_circuit Class Reference	96
7.2.1	Detailed Description	96
7.3	qpp::Codes Class Reference	96
7.3.1	Detailed Description	97
7.3.2	Member Enumeration Documentation	97
7.3.2.1	Type	98
7.3.3	Constructor & Destructor Documentation	98
7.3.3.1	Codes()	98
7.3.3.2	~Codes()	98
7.3.4	Member Function Documentation	98
7.3.4.1	codeword()	98
7.3.5	Friends And Related Function Documentation	99
7.3.5.1	internal::Singleton< const Codes >	99
7.4	qpp::exception::CustomException Class Reference	99
7.4.1	Detailed Description	100
7.4.2	Constructor & Destructor Documentation	100
7.4.2.1	CustomException()	101
7.4.3	Member Function Documentation	101

7.4.3.1	<a href="#">type_description()</a>	101
7.4.4	<a href="#">Member Data Documentation</a>	101
7.4.4.1	<a href="#">what_</a>	101
7.5	<a href="#">qpp::exception::DimsInvalid Class Reference</a>	102
7.5.1	<a href="#">Detailed Description</a>	103
7.5.2	<a href="#">Member Function Documentation</a>	103
7.5.2.1	<a href="#">type_description()</a>	103
7.6	<a href="#">qpp::exception::DimsMismatchCvector Class Reference</a>	103
7.6.1	<a href="#">Detailed Description</a>	105
7.6.2	<a href="#">Member Function Documentation</a>	105
7.6.2.1	<a href="#">type_description()</a>	105
7.7	<a href="#">qpp::exception::DimsMismatchMatrix Class Reference</a>	105
7.7.1	<a href="#">Detailed Description</a>	106
7.7.2	<a href="#">Member Function Documentation</a>	106
7.7.2.1	<a href="#">type_description()</a>	107
7.8	<a href="#">qpp::exception::DimsMismatchRvector Class Reference</a>	107
7.8.1	<a href="#">Detailed Description</a>	108
7.8.2	<a href="#">Member Function Documentation</a>	108
7.8.2.1	<a href="#">type_description()</a>	109
7.9	<a href="#">qpp::exception::DimsMismatchVector Class Reference</a>	109
7.9.1	<a href="#">Detailed Description</a>	110
7.9.2	<a href="#">Member Function Documentation</a>	110
7.9.2.1	<a href="#">type_description()</a>	111
7.10	<a href="#">qpp::exception::DimsNotEqual Class Reference</a>	111
7.10.1	<a href="#">Detailed Description</a>	112
7.10.2	<a href="#">Member Function Documentation</a>	112
7.10.2.1	<a href="#">type_description()</a>	112
7.11	<a href="#">qpp::internal::Display_Impl_ Struct Reference</a>	113
7.11.1	<a href="#">Member Function Documentation</a>	113
7.11.1.1	<a href="#">display_impl_()</a>	113

7.12	<a href="#">qpp::experimental::Dynamic_bitset Class Reference</a>	114
7.12.1	<a href="#">Member Typedef Documentation</a>	116
7.12.1.1	<a href="#">storage_type</a>	116
7.12.1.2	<a href="#">value_type</a>	116
7.12.2	<a href="#">Constructor &amp; Destructor Documentation</a>	116
7.12.2.1	<a href="#">Dynamic_bitset()</a>	116
7.12.3	<a href="#">Member Function Documentation</a>	116
7.12.3.1	<a href="#">all()</a>	116
7.12.3.2	<a href="#">any()</a>	117
7.12.3.3	<a href="#">count()</a>	117
7.12.3.4	<a href="#">data()</a>	117
7.12.3.5	<a href="#">flip() [1/2]</a>	117
7.12.3.6	<a href="#">flip() [2/2]</a>	118
7.12.3.7	<a href="#">get()</a>	118
7.12.3.8	<a href="#">index_()</a>	118
7.12.3.9	<a href="#">none()</a>	118
7.12.3.10	<a href="#">offset_()</a>	119
7.12.3.11	<a href="#">operator!=()</a>	119
7.12.3.12	<a href="#">operator==()</a>	119
7.12.3.13	<a href="#">rand() [1/2]</a>	120
7.12.3.14	<a href="#">rand() [2/2]</a>	120
7.12.3.15	<a href="#">reset() [1/2]</a>	120
7.12.3.16	<a href="#">reset() [2/2]</a>	121
7.12.3.17	<a href="#">set() [1/2]</a>	121
7.12.3.18	<a href="#">set() [2/2]</a>	121
7.12.3.19	<a href="#">size()</a>	121
7.12.3.20	<a href="#">storage_size()</a>	122
7.12.3.21	<a href="#">to_string()</a>	122
7.12.4	<a href="#">Friends And Related Function Documentation</a>	122
7.12.4.1	<a href="#">operator&lt;&lt;</a>	122

7.12.5	Member Data Documentation . . . . .	123
7.12.5.1	N_ . . . . .	123
7.12.5.2	storage_size_ . . . . .	123
7.12.5.3	v_ . . . . .	123
7.13	qpp::Dynamic_bitset Class Reference . . . . .	123
7.13.1	Detailed Description . . . . .	123
7.14	qpp::exception::Exception Class Reference . . . . .	124
7.14.1	Detailed Description . . . . .	125
7.14.2	Constructor & Destructor Documentation . . . . .	126
7.14.2.1	Exception() . . . . .	126
7.14.3	Member Function Documentation . . . . .	126
7.14.3.1	type_description() . . . . .	126
7.14.3.2	what() . . . . .	126
7.14.4	Member Data Documentation . . . . .	127
7.14.4.1	where_ . . . . .	127
7.15	qpp::experimental::Bit_circuit::Gate_count Struct Reference . . . . .	127
7.15.1	Member Data Documentation . . . . .	127
7.15.1.1	CNOT . . . . .	127
7.15.1.2	FRED . . . . .	127
7.15.1.3	NOT . . . . .	128
7.15.1.4	SWAP . . . . .	128
7.15.1.5	TOF . . . . .	128
7.15.1.6	X . . . . .	128
7.16	qpp::Gates Class Reference . . . . .	128
7.16.1	Detailed Description . . . . .	130
7.16.2	Constructor & Destructor Documentation . . . . .	130
7.16.2.1	Gates() . . . . .	131
7.16.2.2	~Gates() . . . . .	131
7.16.3	Member Function Documentation . . . . .	131
7.16.3.1	CTRL() . . . . .	131

7.16.3.2	<a href="#">expandout()</a> [1/3]	132
7.16.3.3	<a href="#">expandout()</a> [2/3]	132
7.16.3.4	<a href="#">expandout()</a> [3/3]	133
7.16.3.5	<a href="#">Fd()</a>	133
7.16.3.6	<a href="#">Id()</a>	134
7.16.3.7	<a href="#">Rn()</a>	134
7.16.3.8	<a href="#">Xd()</a>	135
7.16.3.9	<a href="#">Zd()</a>	135
7.16.4	<a href="#">Friends And Related Function Documentation</a>	135
7.16.4.1	<a href="#">internal::Singleton&lt; const Gates &gt;</a>	136
7.16.5	<a href="#">Member Data Documentation</a>	136
7.16.5.1	<a href="#">CNOT</a>	136
7.16.5.2	<a href="#">CNOTba</a>	136
7.16.5.3	<a href="#">CZ</a>	136
7.16.5.4	<a href="#">FRED</a>	136
7.16.5.5	<a href="#">H</a>	136
7.16.5.6	<a href="#">Id2</a>	137
7.16.5.7	<a href="#">S</a>	137
7.16.5.8	<a href="#">SWAP</a>	137
7.16.5.9	<a href="#">T</a>	137
7.16.5.10	<a href="#">TOF</a>	137
7.16.5.11	<a href="#">X</a>	137
7.16.5.12	<a href="#">Y</a>	138
7.16.5.13	<a href="#">Z</a>	138
7.17	<a href="#">qpp::IDisplay Class Reference</a>	138
7.17.1	<a href="#">Detailed Description</a>	139
7.17.2	<a href="#">Constructor &amp; Destructor Documentation</a>	139
7.17.2.1	<a href="#">IDisplay()</a> [1/3]	139
7.17.2.2	<a href="#">IDisplay()</a> [2/3]	140
7.17.2.3	<a href="#">IDisplay()</a> [3/3]	140

7.17.2.4	<a href="#">~IDisplay()</a>	140
7.17.3	<a href="#">Member Function Documentation</a>	140
7.17.3.1	<a href="#">display()</a>	140
7.17.3.2	<a href="#">operator=()</a> [1/2]	140
7.17.3.3	<a href="#">operator=()</a> [2/2]	141
7.17.4	<a href="#">Friends And Related Function Documentation</a>	141
7.17.4.1	<a href="#">operator&lt;&lt;</a>	141
7.18	<a href="#">qpp::Init Class Reference</a>	141
7.18.1	<a href="#">Detailed Description</a>	142
7.18.2	<a href="#">Constructor &amp; Destructor Documentation</a>	142
7.18.2.1	<a href="#">Init()</a>	142
7.18.2.2	<a href="#">~Init()</a>	143
7.18.3	<a href="#">Friends And Related Function Documentation</a>	143
7.18.3.1	<a href="#">internal::Singleton&lt; const Init &gt;</a>	143
7.19	<a href="#">qpp::internal::IOManipEigen Class Reference</a>	143
7.19.1	<a href="#">Constructor &amp; Destructor Documentation</a>	144
7.19.1.1	<a href="#">IOManipEigen()</a> [1/2]	144
7.19.1.2	<a href="#">IOManipEigen()</a> [2/2]	144
7.19.2	<a href="#">Member Function Documentation</a>	144
7.19.2.1	<a href="#">display()</a>	144
7.19.3	<a href="#">Member Data Documentation</a>	145
7.19.3.1	<a href="#">A_</a>	145
7.19.3.2	<a href="#">chop_</a>	145
7.20	<a href="#">qpp::internal::IOManipPointer&lt; PointerType &gt; Class Template Reference</a>	145
7.20.1	<a href="#">Constructor &amp; Destructor Documentation</a>	146
7.20.1.1	<a href="#">IOManipPointer()</a> [1/2]	147
7.20.1.2	<a href="#">IOManipPointer()</a> [2/2]	147
7.20.2	<a href="#">Member Function Documentation</a>	147
7.20.2.1	<a href="#">display()</a>	147
7.20.2.2	<a href="#">operator=()</a>	147

7.20.3	Member Data Documentation . . . . .	147
7.20.3.1	end_ . . . . .	148
7.20.3.2	N_ . . . . .	148
7.20.3.3	p_ . . . . .	148
7.20.3.4	separator_ . . . . .	148
7.20.3.5	start_ . . . . .	148
7.21	qpp::internal::IOManipRange< InputIterator > Class Template Reference . . . . .	149
7.21.1	Constructor & Destructor Documentation . . . . .	150
7.21.1.1	IOManipRange() [1/2] . . . . .	150
7.21.1.2	IOManipRange() [2/2] . . . . .	150
7.21.2	Member Function Documentation . . . . .	150
7.21.2.1	display() . . . . .	150
7.21.2.2	operator=() . . . . .	151
7.21.3	Member Data Documentation . . . . .	151
7.21.3.1	end_ . . . . .	151
7.21.3.2	first_ . . . . .	151
7.21.3.3	last_ . . . . .	151
7.21.3.4	separator_ . . . . .	151
7.21.3.5	start_ . . . . .	151
7.22	qpp::is_complex< T > Struct Template Reference . . . . .	152
7.22.1	Detailed Description . . . . .	152
7.23	qpp::is_complex< std::complex< T > > Struct Template Reference . . . . .	153
7.23.1	Detailed Description . . . . .	153
7.24	qpp::is_iterable< T, typename > Struct Template Reference . . . . .	154
7.24.1	Detailed Description . . . . .	154
7.25	qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > > Struct Template Reference . . . . .	155
7.25.1	Detailed Description . . . . .	156
7.26	qpp::is_matrix_expression< Derived > Struct Template Reference . . . . .	156
7.26.1	Detailed Description . . . . .	157
7.27	qpp::make_void< Ts > Struct Template Reference . . . . .	157

7.27.1 Detailed Description . . . . .	157
7.27.2 Member Typedef Documentation . . . . .	157
7.27.2.1 type . . . . .	157
7.28 qpp::exception::MatrixMismatchSubsys Class Reference . . . . .	158
7.28.1 Detailed Description . . . . .	159
7.28.2 Member Function Documentation . . . . .	159
7.28.2.1 type_description() . . . . .	159
7.29 qpp::exception::MatrixNotCvector Class Reference . . . . .	159
7.29.1 Detailed Description . . . . .	161
7.29.2 Member Function Documentation . . . . .	161
7.29.2.1 type_description() . . . . .	161
7.30 qpp::exception::MatrixNotRvector Class Reference . . . . .	161
7.30.1 Detailed Description . . . . .	162
7.30.2 Member Function Documentation . . . . .	162
7.30.2.1 type_description() . . . . .	162
7.31 qpp::exception::MatrixNotSquare Class Reference . . . . .	163
7.31.1 Detailed Description . . . . .	164
7.31.2 Member Function Documentation . . . . .	164
7.31.2.1 type_description() . . . . .	164
7.32 qpp::exception::MatrixNotSquareNorCvector Class Reference . . . . .	165
7.32.1 Detailed Description . . . . .	166
7.32.2 Member Function Documentation . . . . .	166
7.32.2.1 type_description() . . . . .	166
7.33 qpp::exception::MatrixNotSquareNorRvector Class Reference . . . . .	167
7.33.1 Detailed Description . . . . .	168
7.33.2 Member Function Documentation . . . . .	168
7.33.2.1 type_description() . . . . .	168
7.34 qpp::exception::MatrixNotSquareNorVector Class Reference . . . . .	169
7.34.1 Detailed Description . . . . .	170
7.34.2 Member Function Documentation . . . . .	170



7.34.2.1	<a href="#">type_description()</a>	170
7.35	<a href="#">qpp::exception::MatrixNotVector Class Reference</a>	171
7.35.1	<a href="#">Detailed Description</a>	172
7.35.2	<a href="#">Member Function Documentation</a>	172
7.35.2.1	<a href="#">type_description()</a>	172
7.36	<a href="#">qpp::exception::NoCodeword Class Reference</a>	173
7.36.1	<a href="#">Detailed Description</a>	174
7.36.2	<a href="#">Member Function Documentation</a>	174
7.36.2.1	<a href="#">type_description()</a>	174
7.37	<a href="#">qpp::exception::NotBipartite Class Reference</a>	175
7.37.1	<a href="#">Detailed Description</a>	176
7.37.2	<a href="#">Member Function Documentation</a>	176
7.37.2.1	<a href="#">type_description()</a>	176
7.38	<a href="#">qpp::exception::NotQubitCvector Class Reference</a>	176
7.38.1	<a href="#">Detailed Description</a>	178
7.38.2	<a href="#">Member Function Documentation</a>	178
7.38.2.1	<a href="#">type_description()</a>	178
7.39	<a href="#">qpp::exception::NotQubitMatrix Class Reference</a>	178
7.39.1	<a href="#">Detailed Description</a>	179
7.39.2	<a href="#">Member Function Documentation</a>	179
7.39.2.1	<a href="#">type_description()</a>	179
7.40	<a href="#">qpp::exception::NotQubitRvector Class Reference</a>	180
7.40.1	<a href="#">Detailed Description</a>	181
7.40.2	<a href="#">Member Function Documentation</a>	181
7.40.2.1	<a href="#">type_description()</a>	181
7.41	<a href="#">qpp::exception::NotQubitSubsys Class Reference</a>	182
7.41.1	<a href="#">Detailed Description</a>	183
7.41.2	<a href="#">Member Function Documentation</a>	183
7.41.2.1	<a href="#">type_description()</a>	183
7.42	<a href="#">qpp::exception::NotQubitVector Class Reference</a>	184

7.42.1 Detailed Description . . . . .	185
7.42.2 Member Function Documentation . . . . .	185
7.42.2.1 type_description() . . . . .	185
7.43 qpp::exception::OutOfRange Class Reference . . . . .	186
7.43.1 Detailed Description . . . . .	187
7.43.2 Member Function Documentation . . . . .	187
7.43.2.1 type_description() . . . . .	187
7.44 qpp::exception::PermInvalid Class Reference . . . . .	188
7.44.1 Detailed Description . . . . .	189
7.44.2 Member Function Documentation . . . . .	189
7.44.2.1 type_description() . . . . .	189
7.45 qpp::exception::PermMismatchDims Class Reference . . . . .	189
7.45.1 Detailed Description . . . . .	191
7.45.2 Member Function Documentation . . . . .	191
7.45.2.1 type_description() . . . . .	191
7.46 qpp::RandomDevices Class Reference . . . . .	191
7.46.1 Detailed Description . . . . .	193
7.46.2 Constructor & Destructor Documentation . . . . .	193
7.46.2.1 RandomDevices() . . . . .	193
7.46.2.2 ~RandomDevices() . . . . .	193
7.46.3 Member Function Documentation . . . . .	193
7.46.3.1 get_prng() . . . . .	193
7.46.3.2 load() . . . . .	193
7.46.3.3 save() . . . . .	194
7.46.4 Friends And Related Function Documentation . . . . .	194
7.46.4.1 internal::Singleton< RandomDevices > . . . . .	194
7.46.5 Member Data Documentation . . . . .	194
7.46.5.1 prng_ . . . . .	194
7.46.5.2 rd_ . . . . .	195
7.47 qpp::internal::Singleton< T > Class Template Reference . . . . .	195

7.47.1 Detailed Description . . . . .	195
7.47.2 Constructor & Destructor Documentation . . . . .	196
7.47.2.1 Singleton() [1/2] . . . . .	196
7.47.2.2 Singleton() [2/2] . . . . .	196
7.47.2.3 ~Singleton() . . . . .	196
7.47.3 Member Function Documentation . . . . .	196
7.47.3.1 get_instance() . . . . .	197
7.47.3.2 get_thread_local_instance() . . . . .	197
7.47.3.3 operator=() . . . . .	197
7.48 qpp::exception::SizeMismatch Class Reference . . . . .	197
7.48.1 Detailed Description . . . . .	198
7.48.2 Member Function Documentation . . . . .	198
7.48.2.1 type_description() . . . . .	198
7.49 qpp::States Class Reference . . . . .	199
7.49.1 Detailed Description . . . . .	201
7.49.2 Constructor & Destructor Documentation . . . . .	201
7.49.2.1 States() . . . . .	201
7.49.2.2 ~States() . . . . .	201
7.49.3 Member Function Documentation . . . . .	201
7.49.3.1 jn() . . . . .	201
7.49.3.2 mes() . . . . .	202
7.49.3.3 minus() . . . . .	202
7.49.3.4 one() . . . . .	203
7.49.3.5 plus() . . . . .	203
7.49.3.6 zero() . . . . .	203
7.49.4 Friends And Related Function Documentation . . . . .	204
7.49.4.1 internal::Singleton< const States > . . . . .	204
7.49.5 Member Data Documentation . . . . .	204
7.49.5.1 b00 . . . . .	204
7.49.5.2 b01 . . . . .	204

7.49.5.3	b10	204
7.49.5.4	b11	204
7.49.5.5	GHZ	205
7.49.5.6	pb00	205
7.49.5.7	pb01	205
7.49.5.8	pb10	205
7.49.5.9	pb11	205
7.49.5.10	pGHZ	205
7.49.5.11	pW	206
7.49.5.12	px0	206
7.49.5.13	px1	206
7.49.5.14	py0	206
7.49.5.15	py1	206
7.49.5.16	pz0	206
7.49.5.17	pz1	207
7.49.5.18	W	207
7.49.5.19	x0	207
7.49.5.20	x1	207
7.49.5.21	y0	207
7.49.5.22	y1	207
7.49.5.23	z0	208
7.49.5.24	z1	208
7.50	qpp::exception::SubsysMismatchDims Class Reference	208
7.50.1	Detailed Description	209
7.50.2	Member Function Documentation	209
7.50.2.1	type_description()	209
7.51	qpp::Timer< T, CLOCK_T > Class Template Reference	210
7.51.1	Detailed Description	211
7.51.2	Constructor & Destructor Documentation	212
7.51.2.1	Timer() [1/3]	212

7.51.2.2	<a href="#">Timer() [2/3]</a>	212
7.51.2.3	<a href="#">Timer() [3/3]</a>	212
7.51.2.4	<a href="#">~Timer()</a>	212
7.51.3	<a href="#">Member Function Documentation</a>	212
7.51.3.1	<a href="#">display()</a>	212
7.51.3.2	<a href="#">get_duration()</a>	213
7.51.3.3	<a href="#">operator=() [1/2]</a>	213
7.51.3.4	<a href="#">operator=() [2/2]</a>	213
7.51.3.5	<a href="#">tic()</a>	214
7.51.3.6	<a href="#">tics()</a>	214
7.51.3.7	<a href="#">toc()</a>	214
7.51.4	<a href="#">Member Data Documentation</a>	214
7.51.4.1	<a href="#">end_</a>	214
7.51.4.2	<a href="#">start_</a>	215
7.52	<a href="#">qpp::exception::TypeMismatch Class Reference</a>	215
7.52.1	<a href="#">Detailed Description</a>	216
7.52.2	<a href="#">Member Function Documentation</a>	216
7.52.2.1	<a href="#">type_description()</a>	216
7.53	<a href="#">qpp::exception::UndefinedType Class Reference</a>	217
7.53.1	<a href="#">Detailed Description</a>	218
7.53.2	<a href="#">Member Function Documentation</a>	218
7.53.2.1	<a href="#">type_description()</a>	218
7.54	<a href="#">qpp::exception::Unknown Class Reference</a>	218
7.54.1	<a href="#">Detailed Description</a>	220
7.54.2	<a href="#">Member Function Documentation</a>	220
7.54.2.1	<a href="#">type_description()</a>	220
7.55	<a href="#">qpp::exception::ZeroSize Class Reference</a>	220
7.55.1	<a href="#">Detailed Description</a>	221
7.55.2	<a href="#">Member Function Documentation</a>	221
7.55.2.1	<a href="#">type_description()</a>	221

<b>8</b>	<b>File Documentation</b>	<b>223</b>
8.1	classes/codes.h File Reference . . . . .	223
8.1.1	Detailed Description . . . . .	223
8.2	classes/exception.h File Reference . . . . .	223
8.2.1	Detailed Description . . . . .	225
8.3	classes/gates.h File Reference . . . . .	225
8.3.1	Detailed Description . . . . .	225
8.4	classes/ideplay.h File Reference . . . . .	226
8.4.1	Detailed Description . . . . .	226
8.5	classes/init.h File Reference . . . . .	226
8.5.1	Detailed Description . . . . .	227
8.6	classes/random_devices.h File Reference . . . . .	227
8.6.1	Detailed Description . . . . .	227
8.7	classes/states.h File Reference . . . . .	227
8.7.1	Detailed Description . . . . .	228
8.8	classes/timer.h File Reference . . . . .	228
8.8.1	Detailed Description . . . . .	228
8.9	constants.h File Reference . . . . .	228
8.9.1	Detailed Description . . . . .	229
8.10	entanglement.h File Reference . . . . .	229
8.10.1	Detailed Description . . . . .	231
8.11	entropies.h File Reference . . . . .	231
8.11.1	Detailed Description . . . . .	231
8.12	experimental/experimental.h File Reference . . . . .	232
8.12.1	Detailed Description . . . . .	232
8.12.2	Typedef Documentation . . . . .	232
8.12.2.1	idx . . . . .	232
8.13	functions.h File Reference . . . . .	233
8.13.1	Detailed Description . . . . .	233
8.14	input_output.h File Reference . . . . .	233

8.14.1 Detailed Description . . . . .	234
8.15 instruments.h File Reference . . . . .	234
8.15.1 Detailed Description . . . . .	236
8.16 internal/classes/iomanip.h File Reference . . . . .	236
8.16.1 Detailed Description . . . . .	236
8.17 internal/classes/singleton.h File Reference . . . . .	237
8.17.1 Detailed Description . . . . .	237
8.18 internal/util.h File Reference . . . . .	237
8.18.1 Detailed Description . . . . .	239
8.19 MATLAB/matlab.h File Reference . . . . .	239
8.19.1 Detailed Description . . . . .	240
8.20 number_theory.h File Reference . . . . .	240
8.20.1 Detailed Description . . . . .	241
8.21 operations.h File Reference . . . . .	241
8.21.1 Detailed Description . . . . .	243
8.22 qpp.h File Reference . . . . .	243
8.22.1 Detailed Description . . . . .	244
8.22.2 Macro Definition Documentation . . . . .	244
8.22.2.1 QPP_UNUSED_ . . . . .	244
8.23 random.h File Reference . . . . .	244
8.23.1 Detailed Description . . . . .	245
8.24 statistics.h File Reference . . . . .	246
8.24.1 Detailed Description . . . . .	246
8.25 traits.h File Reference . . . . .	247
8.25.1 Detailed Description . . . . .	247
8.26 types.h File Reference . . . . .	248
8.26.1 Detailed Description . . . . .	249
8.27 /Users/vlad/Dropbox/programming/cpp/qpp/README.md File Reference . . . . .	249





# Chapter 1

## Quantum++

Version 1.0-rc2 - 6 September 2017

**Build status:**

**Chat (questions/issues)**

Quantum++ is a modern C++11 general purpose quantum computing library, composed solely of template header files. Quantum++ is written in standard C++11 and has very low external dependencies, using only the [Eigen 3](#) linear algebra header-only template library and, if available, the [OpenMP](#) multi-processing library.

Quantum++ is not restricted to qubit systems or specific quantum information processing tasks, being capable of simulating arbitrary quantum processes. The main design factors taken in consideration were the ease of use, high portability, and high performance. The library's simulation capabilities are only restricted by the amount of available physical memory. On a typical machine (Intel i5 8Gb RAM) Quantum++ can successfully simulate the evolution of 25 qubits in a pure state or of 12 qubits in a mixed state reasonably fast.

To report any bugs or ask for additional features/enhancements, please [submit an issue](#) with an appropriate label.

If you are interesting in contributing to this project, feel free to contact me. Alternatively, create a custom branch, add your contribution, then finally create a pull request. If I accept the pull request, I will merge your custom branch with the latest development branch. The latter will eventually be merged into a future release version. To contribute, you need to have a solid knowledge of C++ (preferably C++11), including templates and the standard library, a basic knowledge of quantum computing and linear algebra, and working experience with [Eigen 3](#).

For additional [Eigen 3](#) documentation see <http://eigen.tuxfamily.org/dox/>. For a simple [Eigen 3](#) quick ASCII reference see <http://eigen.tuxfamily.org/dox/AsciiQuickReference.txt>.

Copyright (c) 2013 - 2017 Vlad Gheorghiu, vgheorgh AT gmail DOT com.

Quantum++ is licensed under the MIT license, see COPYING for the full terms and conditions of the license.

## Building instructions for POSIX-compliant platforms

### Configuration

- Compiler: `g++` version 5.0 or later (for good C++11 support)
- `Eigen 3` linear algebra library. I assume here that the library is installed in `$HOME/eigen`, although the location may vary, e.g. if the library was installed using a package manager.
- Quantum++ library located in `$HOME/qpp`

### Optional

- `CMake` version 3.0 or later, highly recommended
- `MATLAB` compiler include header files: `/Applications/MATLAB_R2016a.app/extern/include`
- `MATLAB` compiler shared library files: `/Applications/MATLAB_R2016a.app/bin/maci64`

### Building using `CMake` (version 3.0 or later)

The current version of the repository has a `./CMakeLists.txt` configuration file for building examples using `CMake`. To build an example using `CMake`, I recommend an out-of-source build, i.e., from the root of the project (where `./include` is located), type

```
mkdir ./build
cd ./build
cmake ..
make
```

The commands above build the release version (default) executable `qpp`, from the source file `./examples/minimal.cpp`, without `MATLAB` support (default), inside the directory `./build`.

If the location of `Eigen 3` is not detected automatically by the `CMake` build script, then the build script will fail (with an error message). In this case the location of `Eigen 3` needs to be specified manually in the `CMake` build command line by passing the `-DEIGEN3_INCLUDE_DIR=path_to_eigen3` flag, e.g.

```
cmake .. -DEIGEN3_INCLUDE_DIR=/usr/local/eigen3
```

To build a different configuration, e.g. the debug version with `MATLAB` support, type from the root of the project

```
cd ./build
rm -rf *
cmake -DCMAKE_BUILD_TYPE=Debug -DWITH_MATLAB=ON ..
make
```

Or, to disable `OpenMP` support (enabled by default), type

```
cd ./build
rm -rf *
cmake -DWITH_OPENMP=OFF ..
make
```

To change the name of the example file or the location of `MATLAB` installation, edit the `./CMakeLists.txt` file. Inspect also `./CMakeLists.txt` for additional fine-tuning options. Do not forget to clean the `./build` directory before a fresh build!

## Building without an automatic build system

- Example file: `$HOME/qpp/examples/minimal.cpp`
- Output executable: `$HOME/qpp/examples/minimal`
- You must run the commands below from inside the directory `$HOME/qpp/examples`

### Release version (without MATLAB support)

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -O3 -DNDEBUG -DEIGEN_NO_DEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    minimal.cpp -o minimal
```

### Debug version (without MATLAB support)

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -g3 -DDEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    minimal.cpp -o minimal
```

### Release version (with MATLAB support)

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -O3 -DNDEBUG -DEIGEN_NO_DEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    -I/Applications/MATLAB_R2016a.app/extern/include \
    -L/Applications/MATLAB_R2016a.app/bin/maci64 \
    -lmx -lmat minimal.cpp -o minimal
```

### Debug version (with MATLAB support)

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -g3 -DDEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    -I /Applications/MATLAB_R2016a.app/extern/include \
    -L /Applications/MATLAB_R2016a.app/bin/maci64 \
    -lmx -lmat minimal.cpp -o minimal
```

## Additional building instructions for particular platforms

### Windows via Visual Studio

- Quantum++ contains a full **Visual Studio 2017** solution under the folder `./VisualStudio`. The solution expects **Eigen 3** to be installed under `C:\eigen`. Use this solution at first to get you started. A unit testing project (`qpp_testing`) with **Google Test 1.8.0** is also included in the solution.
- **Visual Studio** versions preceding version 2015 do not have full C++11 support. If you decide to use **Visual Studio** make sure you install version 2015 or later. I recommend using **Visual Studio 2017**.
- **Visual Studio 2015/2017** only supports **OpenMP 2.0**. Quantum++ uses features from **OpenMP 3.0**, hence Quantum++ will not compile on **Visual Studio 2015/2017** if you `#define WITH_↵ OPENMP_` in your source file and enable **OpenMP** (disabled by default) in

\*Project/Properties/Configuration Properties/C\_C++/Language/Open MP Support\*

## Windows via Cygwin

- Some earlier versions of **Cygwin** had a bug related to lack of support for some C++11 math functions, see <http://stackoverflow.com/questions/28997206/cygwin-support-for-c11-in-g4-9-2> for more details. Quick fix: patch the standard library header file `<cmath>` using the provided patch `./cmath_cygwin.patch`. Later **Cygwin** versions seem to have fixed the issue (as of Nov. 2016).

## OS X/macOS

- If you want to compile with **clang++** version 3.7 or later, I highly recommend to install it via **macports**. See **Additional remarks** for more details.
- If you run the program with **MATLAB** support, make sure that the environment variable `DYLD_LIBRARY_PATH` is set to point to the **MATLAB** compiler library location, see the `run_mac_MATLAB` script. Otherwise, you get a runtime error similar to

```
> dyld: Library not loaded: @rpath/libmat.dylib.
```

- I recommend running via a script, as otherwise setting the `DYLD_LIBRARY_PATH` globally may interfere with **macports**' **CMake** installation (in case you use **CMake** from **macports**). If you use a script, then the environment variable is local to the script and does not interfere with the rest of the system.
- Example of script, assumed to be located in the root directory of Quantum++

```
#!/bin/sh

MATLAB=/Applications/MATLAB_R2016a.app
export DYLD_LIBRARY_PATH=$DYLD_LIBRARY_PATH:$MATLAB/bin/maci64

./build/qpp
```

- If you build a debug version with **g++** and use **gdb** to step inside template functions you may want to add `-fno-weak` compiler flag. See <http://stackoverflow.com/questions/23330641/gnu-gdb-can-not-st> for more details about this problem.

## Unit testing

Quantum++ was extensively tested under multiple flavours of Linux, **OS X/macOS**, **Windows XP/7/10**, **Solaris 11.x** via a suite of unit tests constructed with **Google Test 1.8.0** (included with the project in `./unit_tests/lib/gtest-1.8.0`). The source code of the unit tests is provided under `./unit_tests/tests`.

To build and run the unit tests under any POSIX-compliant platform, I strongly recommend to use **CMake** version 3.0 or later. Assuming you do use **CMake**, switch to the `./unit_tests` directory, create a build directory inside it, then from the newly created `./unit_tests/build` type

```
cmake ..
make
```

The commands above build `./unit_tests/build/tests/qpp_testing`, which you then may run. Note that `qpp::Timer` tests or tests related to random functions such as `qpp::rand()` may sometime (very rarely) fail, due to timing imprecision or statistical errors. Such behaviour is perfectly normal.

To run the unit tests in **Windows** under **Visual Studio**, use the provided solution and run the `qpp_testing` project from the Solution Explorer.

## Note

The **CMake** configuration file `./unit_tests/CMakeLists.txt` defines the same building options and default choices as the main `./CMakeLists.txt` of Quantum++. Therefore you can use the same flags as the ones mentioned at the beginning of this document when customizing the build. You should modify `./unit_tests/CMakeLists.txt` accordingly in case your **Eigen 3** library or **MATLAB** include/library files are in a different location than the one assumed in this document.

## Additional remarks

- If you use **clang++** version 3.7 or later and want to use **OpenMP** (enabled by default), make sure to modify `CLANG_LIBOMP` and `CLANG_LIBOMP_INCLUDE` in `CMakeLists.txt` so they point to the correct location of the **OpenMP** library, as otherwise **clang++** will not find `<omp.h>` and the `libomp` shared library. Under Linux, you may need to modify also `-fopenmp=...` flag as well. As such, I do not recommend using **clang++** with **OpenMP** due to various platform-dependent issues.



## Chapter 2

# Namespace Index

### 2.1 Namespace List

Here is a list of all namespaces with brief descriptions:

<a href="#">qpp</a>	Quantum++ main namespace . . . . .	17
<a href="#">qpp::exception</a>	Quantum++ exception hierarchy namespace . . . . .	85
<a href="#">qpp::experimental</a>	Experimental/test functions/classes, do not use or modify . . . . .	87
<a href="#">qpp::internal</a>	Internal utility functions, do not use them directly or modify them . . . . .	87





## Chapter 3

# Hierarchical Index

### 3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

qpp::Bit_circuit . . . . .	96
qpp::internal::Display_Impl_ . . . . .	113
qpp::internal::IOManipEigen . . . . .	143
qpp::experimental::Dynamic_bitset . . . . .	114
qpp::experimental::Bit_circuit . . . . .	93
qpp::Dynamic_bitset . . . . .	123
std::exception	
qpp::exception::Exception . . . . .	124
qpp::exception::CustomException . . . . .	99
qpp::exception::DimsInvalid . . . . .	102
qpp::exception::DimsMismatchCvector . . . . .	103
qpp::exception::DimsMismatchMatrix . . . . .	105
qpp::exception::DimsMismatchRvector . . . . .	107
qpp::exception::DimsMismatchVector . . . . .	109
qpp::exception::DimsNotEqual . . . . .	111
qpp::exception::MatrixMismatchSubsys . . . . .	158
qpp::exception::MatrixNotCvector . . . . .	159
qpp::exception::MatrixNotRvector . . . . .	161
qpp::exception::MatrixNotSquare . . . . .	163
qpp::exception::MatrixNotSquareNorCvector . . . . .	165
qpp::exception::MatrixNotSquareNorRvector . . . . .	167
qpp::exception::MatrixNotSquareNorVector . . . . .	169
qpp::exception::MatrixNotVector . . . . .	171
qpp::exception::NoCodeword . . . . .	173
qpp::exception::NotBipartite . . . . .	175
qpp::exception::NotQubitCvector . . . . .	176
qpp::exception::NotQubitMatrix . . . . .	178
qpp::exception::NotQubitRvector . . . . .	180
qpp::exception::NotQubitSubsys . . . . .	182
qpp::exception::NotQubitVector . . . . .	184
qpp::exception::OutOfRange . . . . .	186
qpp::exception::PermInvalid . . . . .	188
qpp::exception::PermMismatchDims . . . . .	189
qpp::exception::SizeMismatch . . . . .	197
qpp::exception::SubsysMismatchDims . . . . .	208

qpp::exception::TypeMismatch	215
qpp::exception::UndefinedType	217
qpp::exception::Unknown	218
qpp::exception::ZeroSize	220
false_type	
qpp::is_complex< T >	152
qpp::is_iterable< T, typename >	154
qpp::experimental::Bit_circuit::Gate_count	127
qpp::IDisplay	138
qpp::internal::IOManipEigen	143
qpp::internal::IOManipPointer< PointerType >	145
qpp::internal::IOManipRange< InputIterator >	149
qpp::Timer< T, CLOCK_T >	210
is_base_of	
qpp::is_matrix_expression< Derived >	156
qpp::make_void< Ts >	157
qpp::internal::Singleton< T >	195
qpp::internal::Singleton< const Codes >	195
qpp::Codes	96
qpp::internal::Singleton< const Gates >	195
qpp::Gates	128
qpp::internal::Singleton< const Init >	195
qpp::Init	141
qpp::internal::Singleton< const States >	195
qpp::States	199
qpp::internal::Singleton< RandomDevices >	195
qpp::RandomDevices	191
true_type	
qpp::is_complex< std::complex< T > >	153
qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >	155

## Chapter 4

# Class Index

### 4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

<a href="#">qpp::experimental::Bit_circuit</a>	93
<a href="#">qpp::Bit_circuit</a>	
Classical reversible circuit simulator	96
<a href="#">qpp::Codes</a>	
Const Singleton class that defines quantum error correcting codes	96
<a href="#">qpp::exception::CustomException</a>	
Custom exception	99
<a href="#">qpp::exception::DimsInvalid</a>	
Invalid dimension(s) exception	102
<a href="#">qpp::exception::DimsMismatchCvector</a>	
Dimension(s) mismatch column vector size exception	103
<a href="#">qpp::exception::DimsMismatchMatrix</a>	
Dimension(s) mismatch matrix size exception	105
<a href="#">qpp::exception::DimsMismatchRvector</a>	
Dimension(s) mismatch row vector size exception	107
<a href="#">qpp::exception::DimsMismatchVector</a>	
Dimension(s) mismatch vector size exception	109
<a href="#">qpp::exception::DimsNotEqual</a>	
Dimensions not equal exception	111
<a href="#">qpp::internal::Display_Impl_</a>	113
<a href="#">qpp::experimental::Dynamic_bitset</a>	114
<a href="#">qpp::Dynamic_bitset</a>	
Dynamic bitset class, allows the specification of the number of bits at runtime (unlike <code>std::bitset&lt;N&gt;</code> )	123
<a href="#">qpp::exception::Exception</a>	
Base class for generating Quantum++ custom exceptions	124
<a href="#">qpp::experimental::Bit_circuit::Gate_count</a>	127
<a href="#">qpp::Gates</a>	
Const Singleton class that implements most commonly used gates	128
<a href="#">qpp::IDisplay</a>	
Abstract class (interface) that mandates the definition of virtual <code>std::ostream&amp; display(std::ostream&amp; os) const</code>	138
<a href="#">qpp::Init</a>	
Const Singleton class that performs additional initializations/cleanups	141
<a href="#">qpp::internal::LOManipEigen</a>	143

<a href="#">qpp::internal::IOManipPointer&lt; PointerType &gt;</a>	145
<a href="#">qpp::internal::IOManipRange&lt; InputIterator &gt;</a>	149
<a href="#">qpp::is_complex&lt; T &gt;</a>	
Checks whether the type is a complex type	152
<a href="#">qpp::is_complex&lt; std::complex&lt; T &gt; &gt;</a>	
Checks whether the type is a complex number type, specialization for complex types	153
<a href="#">qpp::is_iterable&lt; T, typename &gt;</a>	
Checks whether <i>T</i> is compatible with an STL-like iterable container	154
<a href="#">qpp::is_iterable&lt; T, to_void&lt; decltype(std::declval&lt; T &gt;().begin()), decltype(std::declval&lt; T &gt;().end()),     typename T::value_type &gt; &gt;</a>	
Checks whether <i>T</i> is compatible with an STL-like iterable container, specialization for STL-like iterable containers	155
<a href="#">qpp::is_matrix_expression&lt; Derived &gt;</a>	
Checks whether the type is an Eigen matrix expression	156
<a href="#">qpp::make_void&lt; Ts &gt;</a>	
Helper for <a href="#">qpp::to_void&lt;&gt;</a> alias template	157
<a href="#">qpp::exception::MatrixMismatchSubsys</a>	
Matrix mismatch subsystems exception	158
<a href="#">qpp::exception::MatrixNotCvector</a>	
Matrix is not a column vector exception	159
<a href="#">qpp::exception::MatrixNotRvector</a>	
Matrix is not a row vector exception	161
<a href="#">qpp::exception::MatrixNotSquare</a>	
Matrix is not square exception	163
<a href="#">qpp::exception::MatrixNotSquareNorCvector</a>	
Matrix is not square nor column vector exception	165
<a href="#">qpp::exception::MatrixNotSquareNorRvector</a>	
Matrix is not square nor row vector exception	167
<a href="#">qpp::exception::MatrixNotSquareNorVector</a>	
Matrix is not square nor vector exception	169
<a href="#">qpp::exception::MatrixNotVector</a>	
Matrix is not a vector exception	171
<a href="#">qpp::exception::NoCodeword</a>	
Codeword does not exist exception	173
<a href="#">qpp::exception::NotBipartite</a>	
Not bi-partite exception	175
<a href="#">qpp::exception::NotQubitCvector</a>	
Column vector is not 2 x 1 exception	176
<a href="#">qpp::exception::NotQubitMatrix</a>	
Matrix is not 2 x 2 exception	178
<a href="#">qpp::exception::NotQubitRvector</a>	
Row vector is not 1 x 2 exception	180
<a href="#">qpp::exception::NotQubitSubsys</a>	
Subsystems are not qubits exception	182
<a href="#">qpp::exception::NotQubitVector</a>	
Vector is not 2 x 1 nor 1 x 2 exception	184
<a href="#">qpp::exception::OutOfRange</a>	
Parameter out of range exception	186
<a href="#">qpp::exception::PermInvalid</a>	
Invalid permutation exception	188
<a href="#">qpp::exception::PermMismatchDims</a>	
Permutation mismatch dimensions exception	189
<a href="#">qpp::RandomDevices</a>	
Singleton class that manages the source of randomness in the library	191
<a href="#">qpp::internal::Singleton&lt; T &gt;</a>	
Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)	195

<a href="#">qpp::exception::SizeMismatch</a>	
Size mismatch exception . . . . .	197
<a href="#">qpp::States</a>	
Const Singleton class that implements most commonly used states . . . . .	199
<a href="#">qpp::exception::SubsysMismatchDims</a>	
Subsystems mismatch dimensions exception . . . . .	208
<a href="#">qpp::Timer&lt; T, CLOCK_T &gt;</a>	
Chronometer . . . . .	210
<a href="#">qpp::exception::TypeMismatch</a>	
Type mismatch exception . . . . .	215
<a href="#">qpp::exception::UndefinedType</a>	
Not defined for this type exception . . . . .	217
<a href="#">qpp::exception::Unknown</a>	
Unknown exception . . . . .	218
<a href="#">qpp::exception::ZeroSize</a>	
Object has zero size exception . . . . .	220



## Chapter 5

# File Index

### 5.1 File List

Here is a list of all files with brief descriptions:

<a href="#">constants.h</a>	
Constants . . . . .	228
<a href="#">entanglement.h</a>	
Entanglement functions . . . . .	229
<a href="#">entropies.h</a>	
Entropy functions . . . . .	231
<a href="#">functions.h</a>	
Generic quantum computing functions . . . . .	233
<a href="#">input_output.h</a>	
Input/output functions . . . . .	233
<a href="#">instruments.h</a>	
Measurement functions . . . . .	234
<a href="#">number_theory.h</a>	
Number theory functions . . . . .	240
<a href="#">operations.h</a>	
Quantum operation functions . . . . .	241
<a href="#">qpp.h</a>	
Quantum++ main header file, includes all other necessary headers . . . . .	243
<a href="#">random.h</a>	
Randomness-related functions . . . . .	244
<a href="#">statistics.h</a>	
Statistics functions . . . . .	246
<a href="#">traits.h</a>	
Type traits . . . . .	247
<a href="#">types.h</a>	
Type aliases . . . . .	248
classes/ <a href="#">codes.h</a>	
Quantum error correcting codes . . . . .	223
classes/ <a href="#">exception.h</a>	
Exceptions . . . . .	223
classes/ <a href="#">gates.h</a>	
Quantum gates . . . . .	225
classes/ <a href="#">display.h</a>	
Display interface via the non-virtual interface (NVI) . . . . .	226
classes/ <a href="#">init.h</a>	
Initialization . . . . .	226

classes/ <a href="#">random_devices.h</a>	
Random devices . . . . .	227
classes/ <a href="#">states.h</a>	
Quantum states . . . . .	227
classes/ <a href="#">timer.h</a>	
Timing . . . . .	228
experimental/ <a href="#">experimental.h</a>	
Experimental/test functions/classes . . . . .	232
internal/ <a href="#">util.h</a>	
Internal utility functions . . . . .	237
internal/classes/ <a href="#">iomanip.h</a>	
Input/output manipulators . . . . .	236
internal/classes/ <a href="#">singleton.h</a>	
Singleton pattern via CRTP . . . . .	237
MATLAB/ <a href="#">matlab.h</a>	
Input/output interfacing with MATLAB . . . . .	239



## Chapter 6

# Namespace Documentation

### 6.1 qpp Namespace Reference

Quantum++ main namespace.

#### Namespaces

- [exception](#)  
*Quantum++ exception hierarchy namespace.*
- [experimental](#)  
*Experimental/test functions/classes, do not use or modify.*
- [internal](#)  
*Internal utility functions, do not use them directly or modify them.*

#### Classes

- class [Bit\\_circuit](#)  
*Classical reversible circuit simulator.*
- class [Codes](#)  
*const Singleton class that defines quantum error correcting codes*
- class [Dynamic\\_bitset](#)  
*Dynamic bitset class, allows the specification of the number of bits at runtime (unlike `std::bitset<N>`)*
- class [Gates](#)  
*const Singleton class that implements most commonly used gates*
- class [IDisplay](#)  
*Abstract class (interface) that mandates the definition of virtual `std::ostream& display(std::ostream& os) const`.*
- class [Init](#)  
*const Singleton class that performs additional initializations/cleanups*
- struct [is\\_complex](#)  
*Checks whether the type is a complex type.*
- struct [is\\_complex< std::complex< T > >](#)  
*Checks whether the type is a complex number type, specialization for complex types.*
- struct [is\\_iterable](#)  
*Checks whether T is compatible with an STL-like iterable container.*

- struct `is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >`  
*Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.*
- struct `is_matrix_expression`  
*Checks whether the type is an Eigen matrix expression.*
- struct `make_void`  
*Helper for `qpp::to_void<>` alias template.*
- class `RandomDevices`  
*Singleton class that manages the source of randomness in the library.*
- class `States`  
*const Singleton class that implements most commonly used states*
- class `Timer`  
*Chronometer.*

## Typedefs

- template<typename... Ts>  
using `to_void` = typename `make_void< Ts... >::type`  
*Alias template that implements the proposal for `void_t`.*
- using `idx` = `std::size_t`  
*Non-negative integer index.*
- using `bigint` = `long long int`  
*Big integer.*
- using `cplx` = `std::complex< double >`  
*Complex number in double precision.*
- using `ket` = `Eigen::VectorXcd`  
*Complex (double precision) dynamic Eigen column vector.*
- using `bra` = `Eigen::RowVectorXcd`  
*Complex (double precision) dynamic Eigen row vector.*
- using `cmat` = `Eigen::MatrixXcd`  
*Complex (double precision) dynamic Eigen matrix.*
- using `dmat` = `Eigen::MatrixXd`  
*Real (double precision) dynamic Eigen matrix.*
- template<typename Scalar >  
using `dyn_mat` = `Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >`  
*Dynamic Eigen matrix over the field specified by Scalar.*
- template<typename Scalar >  
using `dyn_col_vect` = `Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >`  
*Dynamic Eigen column vector over the field specified by Scalar.*
- template<typename Scalar >  
using `dyn_row_vect` = `Eigen::Matrix< Scalar, 1, Eigen::Dynamic >`  
*Dynamic Eigen row vector over the field specified by Scalar.*

## Functions

- constexpr `cplx operator"" _i` (unsigned long long int x) noexcept  
*User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)*
- constexpr `cplx operator"" _i` (long double x) noexcept  
*User-defined literal for complex  $i = \sqrt{-1}$  (real overload)*
- `cplx omega` (idx D)  
*D-th root of unity.*
- template<typename Derived >  
`dyn_col_vect< double > schmidtcoeffs` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)  
*Schmidt coefficients of the bi-partite pure state A.*
- template<typename Derived >  
`dyn_col_vect< double > schmidtcoeffs` (const Eigen::MatrixBase< Derived > &A, idx d=2)  
*Schmidt coefficients of the bi-partite pure state A.*
- template<typename Derived >  
`cmat schmidtA` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)  
*Schmidt basis on Alice side.*
- template<typename Derived >  
`cmat schmidtA` (const Eigen::MatrixBase< Derived > &A, idx d=2)  
*Schmidt basis on Alice side.*
- template<typename Derived >  
`cmat schmidtB` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)  
*Schmidt basis on Bob side.*
- template<typename Derived >  
`cmat schmidtB` (const Eigen::MatrixBase< Derived > &A, idx d=2)  
*Schmidt basis on Bob side.*
- template<typename Derived >  
`std::vector< double > schmidtprobs` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)  
*Schmidt probabilities of the bi-partite pure state A.*
- template<typename Derived >  
`std::vector< double > schmidtprobs` (const Eigen::MatrixBase< Derived > &A, idx d=2)  
*Schmidt probabilities of the bi-partite pure state A.*
- template<typename Derived >  
`double entanglement` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)  
*Entanglement of the bi-partite pure state A.*
- template<typename Derived >  
`double entanglement` (const Eigen::MatrixBase< Derived > &A, idx d=2)  
*Entanglement of the bi-partite pure state A.*
- template<typename Derived >  
`double gconcurrence` (const Eigen::MatrixBase< Derived > &A)  
*G-concurrence of the bi-partite pure state A.*
- template<typename Derived >  
`double negativity` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)  
*Negativity of the bi-partite mixed state A.*
- template<typename Derived >  
`double negativity` (const Eigen::MatrixBase< Derived > &A, idx d=2)  
*Negativity of the bi-partite mixed state A.*
- template<typename Derived >  
`double lognegativity` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)  
*Logarithmic negativity of the bi-partite mixed state A.*

- `template<typename Derived >`  
`double lognegativity (const Eigen::MatrixBase< Derived > &A, idx d=2)`  
*Logarithmic negativity of the bi-partite mixed state A.*
- `template<typename Derived >`  
`double concurrence (const Eigen::MatrixBase< Derived > &A)`  
*Wootters concurrence of the bi-partite qubit mixed state A.*
- `template<typename Derived >`  
`double entropy (const Eigen::MatrixBase< Derived > &A)`  
*von-Neumann entropy of the density matrix A*
- `double entropy (const std::vector< double > &prob)`  
*Shannon entropy of the probability distribution prob.*
- `template<typename Derived >`  
`double renyi (const Eigen::MatrixBase< Derived > &A, double alpha)`  
*Renyi-  $\alpha$  entropy of the density matrix A, for  $\alpha \geq 0$ .*
- `double renyi (const std::vector< double > &prob, double alpha)`  
*Renyi-  $\alpha$  entropy of the probability distribution prob, for  $\alpha \geq 0$ .*
- `template<typename Derived >`  
`double tsallis (const Eigen::MatrixBase< Derived > &A, double q)`  
*Tsallis-  $q$  entropy of the density matrix A, for  $q \geq 0$ .*
- `double tsallis (const std::vector< double > &prob, double q)`  
*Tsallis-  $q$  entropy of the probability distribution prob, for  $q \geq 0$ .*
- `template<typename Derived >`  
`double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsA, const std::vector< idx > &subsB, const std::vector< idx > &dims)`  
*Quantum mutual information between 2 subsystems of a composite system.*
- `template<typename Derived >`  
`double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsA, const std::vector< idx > &subsB, idx d=2)`  
*Quantum mutual information between 2 subsystems of a composite system.*
- `template<typename Derived >`  
`internal::IOManipEigen disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)`  
*Eigen expression ostream manipulator.*
- `internal::IOManipEigen disp (cplx z, double chop=qpp::chop)`  
*Complex number ostream manipulator.*
- `template<typename InputIterator >`  
`internal::IOManipRange< InputIterator > disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[" , const std::string &end="]")`  
*Range ostream manipulator.*
- `template<typename Container >`  
`internal::IOManipRange< typename Container::const_iterator > disp (const Container &c, const std::string &separator, const std::string &start="[" , const std::string &end="]", typename std::enable_if< is\_iterable< Container >::value >::type !=nullptr)`  
*Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.*
- `template<typename PointerType >`  
`internal::IOManipPointer< PointerType > disp (const PointerType *p, idx N, const std::string &separator, const std::string &start="[" , const std::string &end="]")`  
*C-style pointer ostream manipulator.*
- `template<typename Derived >`  
`void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)`  
*Saves Eigen expression to a binary file (internal format) in double precision.*
- `template<typename Derived >`  
`dyn\_mat< typename Derived::Scalar > load (const std::string &fname)`  
*Loads Eigen matrix from a binary file (internal format) in double precision.*

- `template<typename Derived >`  
`dyn_col_vect< typename Derived::Scalar > ip` (const Eigen::MatrixBase< Derived > &phi, const Eigen::↵  
MatrixBase< Derived > &psi, const std::vector< idx > &subs, const std::vector< idx > &dims)  
*Generalized inner product.*
- `template<typename Derived >`  
`dyn_col_vect< typename Derived::Scalar > ip` (const Eigen::MatrixBase< Derived > &phi, const Eigen::↵  
MatrixBase< Derived > &psi, const std::vector< idx > &subs, idx d=2)  
*Generalized inner product.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure` (const Eigen::MatrixBase< Derived  
> &A, const std::vector< cmat > &Ks)  
*Measures the state A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure` (const Eigen::MatrixBase< Derived  
> &A, const std::initializer\_list< cmat > &Ks)  
*Measures the state A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure` (const Eigen::MatrixBase< Derived  
> &A, const cmat &U)  
*Measures the state A in the orthonormal basis specified by the unitary matrix U.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure` (const Eigen::MatrixBase< Derived  
> &A, const std::vector< cmat > &Ks, const std::vector< idx > &subs, const std::vector< idx > &dims)  
*Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure` (const Eigen::MatrixBase< Derived  
> &A, const std::initializer\_list< cmat > &Ks, const std::vector< idx > &subs, const std::vector< idx >  
&dims)  
*Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure` (const Eigen::MatrixBase< Derived  
> &A, const std::vector< cmat > &Ks, const std::vector< idx > &subs, idx d=2)  
*Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure` (const Eigen::MatrixBase< Derived  
> &A, const std::initializer\_list< cmat > &Ks, const std::vector< idx > &subs, idx d=2)  
*Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure` (const Eigen::MatrixBase< Derived  
> &A, const cmat &V, const std::vector< idx > &subs, const std::vector< idx > &dims)  
*Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM  
specified by the matrix V.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure` (const Eigen::MatrixBase< Derived  
> &A, const cmat &V, const std::vector< idx > &subs, idx d=2)  
*Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM  
specified by the matrix V.*
- `template<typename Derived >`  
`std::tuple< std::vector< idx >, double, cmat > measure_seq` (const Eigen::MatrixBase< Derived > &A,  
std::vector< idx > subs, std::vector< idx > dims)  
*Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.*
- `template<typename Derived >`  
`std::tuple< std::vector< idx >, double, cmat > measure_seq` (const Eigen::MatrixBase< Derived > &A,  
std::vector< idx > subs, idx d=2)  
*Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.*

- `template<typename Derived >`  
`std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value, dyn\_mat< cplx > >::type loadMATLAB (const std::string &mat_file, const std::string &var_name)`  
*Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.*
- `template<typename Derived >`  
`std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value, dyn\_mat< typename Derived::Scalar > >::type loadMATLAB (const std::string &mat_file, const std::string &var_name)`  
*Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.*
- `template<typename Derived >`  
`std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value >::type saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`  
*Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.*
- `template<typename Derived >`  
`std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value >::type saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`  
*Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.*
- `std::vector< int > x2contfrac (double x, idx N, idx cut=1e5)`  
*Simple continued fraction expansion.*
- `double contfrac2x (const std::vector< int > &cf, idx N=idx(-1))`  
*Real representation of a simple continued fraction.*
- `bigint gcd (bigint a, bigint b)`  
*Greatest common divisor of two integers.*
- `bigint gcd (const std::vector< bigint > &as)`  
*Greatest common divisor of a list of integers.*
- `bigint lcm (bigint a, bigint b)`  
*Least common multiple of two integers.*
- `bigint lcm (const std::vector< bigint > &as)`  
*Least common multiple of a list of integers.*
- `std::vector< idx > invperm (const std::vector< idx > &perm)`  
*Inverse permutation.*
- `std::vector< idx > compperm (const std::vector< idx > &perm, const std::vector< idx > &sigma)`  
*Compose permutations.*
- `std::vector< bigint > factors (bigint a)`  
*Prime factor decomposition.*
- `bigint modmul (bigint a, bigint b, bigint p)`  
*Modular multiplication without overflow.*
- `bigint modpow (bigint a, bigint n, bigint p)`  
*Fast integer power modulo p based on the SQUARE-AND-MULTIPLY algorithm.*
- `std::tuple< bigint, bigint, bigint > egcd (bigint a, bigint b)`  
*Extended greatest common divisor of two integers.*
- `bigint modinv (bigint a, bigint p)`  
*Modular inverse of a mod p.*
- `bool isprime (bigint p, idx k=80)`  
*Primality test based on the Miller-Rabin's algorithm.*
- `bigint randprime (bigint a, bigint b, idx N=1000)`  
*Generates a random big prime uniformly distributed in the interval [a, b].*
- `template<typename Derived1 , typename Derived2 >`  
`dyn\_mat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

*Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.*

- `template<typename Derived1 , typename Derived2 >`  
`dyn_mat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx d=2)`

*Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.*

- `template<typename Derived1 , typename Derived2 >`  
`dyn_mat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

*Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.*

- `template<typename Derived1 , typename Derived2 >`  
`dyn_mat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, idx d=2)`

*Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.*

- `template<typename Derived >`  
`cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)`

*Applies the channel specified by the set of Kraus operators Ks to the density matrix A.*

- `template<typename Derived >`  
`cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

*Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.*

- `template<typename Derived >`  
`cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)`

*Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.*

- `cmat kraus2super (const std::vector< cmat > &Ks)`

*Superoperator matrix.*

- `cmat kraus2choi (const std::vector< cmat > &Ks)`

*Choi matrix.*

- `std::vector< cmat > choi2kraus (const cmat &A)`

*Orthogonal Kraus operators from Choi matrix.*

- `cmat choi2super (const cmat &A)`

*Converts Choi matrix to superoperator matrix.*

- `cmat super2choi (const cmat &A)`

*Converts superoperator matrix to Choi matrix.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`

*Partial trace.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, idx d=2)`

*Partial trace.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`

*Partial trace.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, idx d=2)`

*Partial trace.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

*Partial trace.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > ptrace` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &subsys, `idx` d=2)  
*Partial trace.*
- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > ptrtranspose` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &subsys, const std::vector< `idx` > &dims)  
*Partial transpose.*
- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > ptrtranspose` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &subsys, `idx` d=2)  
*Partial transpose.*
- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > syspermute` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &perm, const std::vector< `idx` > &dims)  
*Subsystem permutation.*
- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > syspermute` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &perm, `idx` d=2)  
*Subsystem permutation.*
- `double rand` (double a, double b)  
*Generates a random real number uniformly distributed in the interval [a, b)*
- `bigint rand` (bigint a, bigint b)  
*Generates a random big integer uniformly distributed in the interval [a, b].*
- `idx randidx` (`idx` a=std::numeric\_limits< `idx` >::min(), `idx` b=std::numeric\_limits< `idx` >::max())  
*Generates a random index (idx) uniformly distributed in the interval [a, b].*
- `template<typename Derived >`  
`Derived rand` (`idx` rows, `idx` cols, double a=0, double b=1)  
*Generates a random matrix with entries uniformly distributed in the interval [a, b)*
- `template<>`  
`dmat rand` (`idx` rows, `idx` cols, double a, double b)  
*Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (`qpp::dmat`)*
- `template<>`  
`cmat rand` (`idx` rows, `idx` cols, double a, double b)  
*Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (`qpp::cmat`)*
- `template<typename Derived >`  
`Derived randn` (`idx` rows, `idx` cols, double mean=0, double `sigma`=1)  
*Generates a random matrix with entries normally distributed in N(mean, sigma)*
- `template<>`  
`dmat randn` (`idx` rows, `idx` cols, double mean, double `sigma`)  
*Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (`qpp::dmat`)*
- `template<>`  
`cmat randn` (`idx` rows, `idx` cols, double mean, double `sigma`)  
*Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (`qpp::cmat`)*
- `double randn` (double mean=0, double `sigma`=1)  
*Generates a random real number (double) normally distributed in N(mean, sigma)*
- `cmat randU` (`idx` D=2)  
*Generates a random unitary matrix.*
- `cmat randV` (`idx` Din, `idx` Dout)



- Generates a random isometry matrix.*

  - `std::vector< cmat > randkraus (idx N, idx D=2)`

*Generates a set of random Kraus operators.*
- `cmat randH (idx D=2)`

*Generates a random Hermitian matrix.*
- `ket randket (idx D=2)`

*Generates a random normalized ket (pure state vector)*
- `cmat randrho (idx D=2)`

*Generates a random density matrix.*
- `std::vector< idx > randperm (idx N)`

*Generates a random uniformly distributed permutation.*
- `std::vector< double > randprob (idx N)`

*Generates a random probability vector uniformly distributed over the probability simplex.*
- `std::vector< double > uniform (idx N)`

*Uniform probability distribution vector.*
- `std::vector< double > marginalX (const dmat &probXY)`

*Marginal distribution.*
- `std::vector< double > marginalY (const dmat &probXY)`

*Marginal distribution.*
- `template<typename Container >  
double avg (const std::vector< double > &prob, const Container &X, typename std::enable_if< is\_iterable< Container >::value >::type != nullptr)`

*Average.*
- `template<typename Container >  
double cov (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if< is\_iterable< Container >::value >::type != nullptr)`

*Covariance.*
- `template<typename Container >  
double var (const std::vector< double > &prob, const Container &X, typename std::enable_if< is\_iterable< Container >::value >::type != nullptr)`

*Variance.*
- `template<typename Container >  
double sigma (const std::vector< double > &prob, const Container &X, typename std::enable_if< is\_iterable< Container >::value >::type != nullptr)`

*Standard deviation.*
- `template<typename Container >  
double cor (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if< is\_iterable< Container >::value >::type != nullptr)`

*Correlation.*

## Variables

- `constexpr double chop = 1e-10`

*Used in [qpp::disp\(\)](#) for setting to zero numbers that have their absolute value smaller than [qpp::chop](#).*
- `constexpr double eps = 1e-12`

*Used to decide whether a number or expression in double precision is zero or not.*
- `constexpr idx maxn = 64`

*Maximum number of allowed qubits/qudits (subsystems)*
- `constexpr double pi = 3.141592653589793238462643383279502884`

$\pi$
- `constexpr double ee = 2.718281828459045235360287471352662497`

*Base of natural logarithm, e.*
- `constexpr double infy = std::numeric_limits<double>::max()`

*Used to denote infinity in double precision.*

### 6.1.1 Detailed Description

Quantum++ main namespace.

### 6.1.2 Typedef Documentation

#### 6.1.2.1 bigint

```
using qpp::bigint = typedef long long int
```

Big integer.

#### 6.1.2.2 bra

```
using qpp::bra = typedef Eigen::RowVectorXcd
```

Complex (double precision) dynamic Eigen row vector.

#### 6.1.2.3 cmat

```
using qpp::cmat = typedef Eigen::MatrixXcd
```

Complex (double precision) dynamic Eigen matrix.

#### 6.1.2.4 cplx

```
using qpp::cplx = typedef std::complex<double>
```

Complex number in double precision.

#### 6.1.2.5 dmat

```
using qpp::dmat = typedef Eigen::MatrixXd
```

Real (double precision) dynamic Eigen matrix.

### 6.1.2.6 dyn\_col\_vect

```
template<typename Scalar >
using qpp::dyn_col_vect = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, 1>
```

Dynamic Eigen column vector over the field specified by *Scalar*.

Example:

```
// type of colvect is Eigen::Matrix<float, Eigen::Dynamic, 1>
dyn_col_vect<float> colvect(2);
```

### 6.1.2.7 dyn\_mat

```
template<typename Scalar >
using qpp::dyn_mat = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>
```

Dynamic Eigen matrix over the field specified by *Scalar*.

Example:

```
// type of mat is Eigen::Matrix<float, Eigen::Dynamic, Eigen::Dynamic>
dyn_mat<float> mat(2, 3);
```

### 6.1.2.8 dyn\_row\_vect

```
template<typename Scalar >
using qpp::dyn_row_vect = typedef Eigen::Matrix<Scalar, 1, Eigen::Dynamic>
```

Dynamic Eigen row vector over the field specified by *Scalar*.

Example:

```
// type of rowvect is Eigen::Matrix<float, 1, Eigen::Dynamic>
dyn_row_vect<float> rowvect(3);
```

### 6.1.2.9 idx

```
using qpp::idx = typedef std::size_t
```

Non-negative integer index.

#### 6.1.2.10 ket

```
using qpp::ket = typedef Eigen::VectorXcd
```

Complex (double precision) dynamic Eigen column vector.

#### 6.1.2.11 to\_void

```
template<typename... Ts>
using qpp::to_void = typedef typename make_void<Ts...>::type
```

Alias template that implements the proposal for void\_t.

See also

<http://www.open-std.org/jtc1/sc22/wg21/docs/papers/2014/n3911>

### 6.1.3 Function Documentation

#### 6.1.3.1 apply() [1/5]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::apply (
    const Eigen::MatrixBase< Derived1 > & state,
    const Eigen::MatrixBase< Derived2 > & A,
    const std::vector< idx > & subsys,
    const std::vector< idx > & dims )
```

Applies the gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>dims</i>	Dimensions of the multi-partite system

Returns

Gate *A* applied to the part *subsys* of *state*

6.1.3.2 `apply()` [2/5]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::apply (
    const Eigen::MatrixBase< Derived1 > & state,
    const Eigen::MatrixBase< Derived2 > & A,
    const std::vector< idx > & subsys,
    idx d = 2 )
```

Applies the gate  $A$  to the part *subsys* of the multi-partite state vector or density matrix *state*.

**Note**

The dimension of the gate  $A$  must match the dimension of *subsys*

**Parameters**

<i>state</i>	Eigen expression
$A$	Eigen expression
<i>subsys</i>	Subsystem indexes where the gate $A$ is applied
$d$	Subsystem dimensions

**Returns**

Gate  $A$  applied to the part *subsys* of *state*

6.1.3.3 `apply()` [3/5]

```
template<typename Derived >
cmat qpp::apply (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< cmat > & Ks )
```

Applies the channel specified by the set of Kraus operators  $Ks$  to the density matrix  $A$ .

**Parameters**

$A$	Eigen expression
$Ks$	Set of Kraus operators

**Returns**

Output density matrix after the action of the channel

#### 6.1.3.4 `apply()` [4/5]

```
template<typename Derived >
cmat qpp::apply (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< cmat > & Ks,
    const std::vector< idx > & subsys,
    const std::vector< idx > & dims )
```

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *A*.

##### Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes where the Kraus operators <i>Ks</i> are applied
<i>dims</i>	Dimensions of the multi-partite system

##### Returns

Output density matrix after the action of the channel

#### 6.1.3.5 `apply()` [5/5]

```
template<typename Derived >
cmat qpp::apply (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< cmat > & Ks,
    const std::vector< idx > & subsys,
    idx d = 2 )
```

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *A*.

##### Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes where the Kraus operators <i>Ks</i> are applied
<i>d</i>	Subsystem dimensions

##### Returns

Output density matrix after the action of the channel

6.1.3.6 `applyCTRL()` [1/2]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (
    const Eigen::MatrixBase< Derived1 > & state,
    const Eigen::MatrixBase< Derived2 > & A,
    const std::vector< idx > & ctrl,
    const std::vector< idx > & subsys,
    const std::vector< idx > & dims )
```

Applies the controlled-gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

See also

[qpp::Gates::CTRL\(\)](#)

Note

The dimension of the gate *A* must match the dimension of *subsys*. Also, all control subsystems in *ctrl* must have the same dimension.

Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>ctrl</i>	Control subsystem indexes
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>dims</i>	Dimensions of the multi-partite system

Returns

CTRL-A gate applied to the part *subsys* of *state*

6.1.3.7 `applyCTRL()` [2/2]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (
    const Eigen::MatrixBase< Derived1 > & state,
    const Eigen::MatrixBase< Derived2 > & A,
    const std::vector< idx > & ctrl,
    const std::vector< idx > & subsys,
    idx d = 2 )
```

Applies the controlled-gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

See also

[qpp::Gates::CTRL\(\)](#)

Note

The dimension of the gate *A* must match the dimension of *subsys*

**Parameters**

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>ctrl</i>	Control subsystem indexes
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>d</i>	Subsystem dimensions

**Returns**

CTRL-A gate applied to the part *subsys* of *state*

**6.1.3.8 avg()**

```
template<typename Container >
double qpp::avg (
    const std::vector< double > & prob,
    const Container & X,
    typename std::enable_if< is\_iterable< Container >::value >::type * = nullptr )
```

Average.

**Parameters**

<i>prob</i>	Real probability vector representing the probability distribution of <i>X</i>
<i>X</i>	Real random variable values represented by an STL-like container

**Returns**

Average of *X*

**6.1.3.9 choi2kraus()**

```
std::vector<cmat> qpp::choi2kraus (
    const cmat & A ) [inline]
```

Orthogonal Kraus operators from Choi matrix.

**See also**

[qpp::kraus2choi\(\)](#)

Extracts a set of orthogonal (under Hilbert-Schmidt operator norm) Kraus operators from the Choi matrix *A*

**Note**

The Kraus operators satisfy  $Tr(K_i^\dagger K_j) = \delta_{ij}$  for all  $i \neq j$



## Parameters

<i>A</i>	Choi matrix
----------	-------------

## Returns

Set of orthogonal Kraus operators

6.1.3.10 `choi2super()`

```
cmat qpp::choi2super (
    const cmat & A ) [inline]
```

Converts Choi matrix to superoperator matrix.

## See also

[qpp::super2choi\(\)](#)

## Parameters

<i>A</i>	Choi matrix
----------	-------------

## Returns

Superoperator matrix

6.1.3.11 `compperm()`

```
std::vector<idx> qpp::compperm (
    const std::vector< idx > & perm,
    const std::vector< idx > & sigma ) [inline]
```

Compose permutations.

## Parameters

<i>perm</i>	Permutation
<i>sigma</i>	Permutation

## Returns

Composition of the permutations  $perm \circ sigma = perm(sigma)$

#### 6.1.3.12 concurrence()

```
template<typename Derived >
double qpp::concurrence (
    const Eigen::MatrixBase< Derived > & A )
```

Wootters concurrence of the bi-partite qubit mixed state  $A$ .

##### Parameters

$A$	Eigen expression
-----	------------------

##### Returns

Wootters concurrence

#### 6.1.3.13 contfrac2x()

```
double qpp::contfrac2x (
    const std::vector< int > & cf,
    idx N = idx(-1) ) [inline]
```

Real representation of a simple continued fraction.

##### See also

[qpp::x2contfrac\(\)](#)

##### Note

If  $N$  is greater than the size of  $cf$  (by default it is), then all terms in  $cf$  are considered.

##### Parameters

$cf$	Integer vector containing the simple continued fraction expansion
$N$	Number of terms considered in the continued fraction expansion.

##### Returns

Real representation of the simple continued fraction

#### 6.1.3.14 cor()

```
template<typename Container >
double qpp::cor (
```

```

const dmat & probXY,
const Container & X,
const Container & Y,
typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )

```

Correlation.

#### Parameters

<i>probXY</i>	Real matrix representing the joint probability distribution of <i>X</i> and <i>Y</i> in lexicographical order ( <i>X</i> labels the rows, <i>Y</i> labels the columns)
<i>X</i>	Real random variable values represented by an STL-like container
<i>Y</i>	Real random variable values represented by an STL-like container

#### Returns

Correlation of *X* and *Y*

#### 6.1.3.15 cov()

```

template<typename Container >
double qpp::cov (
    const dmat & probXY,
    const Container & X,
    const Container & Y,
    typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )

```

Covariance.

#### Parameters

<i>probXY</i>	Real matrix representing the joint probability distribution of <i>X</i> and <i>Y</i> in lexicographical order ( <i>X</i> labels the rows, <i>Y</i> labels the columns)
<i>X</i>	Real random variable values represented by an STL-like container
<i>Y</i>	Real random variable values represented by an STL-like container

#### Returns

Covariance of *X* and *Y*

#### 6.1.3.16 disp() [1/5]

```

template<typename Derived >
internal::IOManipEigen qpp::disp (
    const Eigen::MatrixBase< Derived > & A,
    double chop = qpp::chop )

```

Eigen expression ostream manipulator.

## Parameters

<i>A</i>	Eigen expression
<i>chop</i>	Set to zero the elements smaller in absolute value than <i>chop</i>

## Returns

Instance of [qpp::internal::IOManipEigen](#)

6.1.3.17 `disp()` [2/5]

```
internal::IOManipEigen qpp::disp (
    cplx z,
    double chop = qpp::chop ) [inline]
```

Complex number ostream manipulator.

## Parameters

<i>z</i>	Complex number (or any other type implicitly cast-able to <code>std::complex&lt;double&gt;</code> )
<i>chop</i>	Set to zero the elements smaller in absolute value than <i>chop</i>

## Returns

Instance of [qpp::internal::IOManipEigen](#)

6.1.3.18 `disp()` [3/5]

```
template<typename InputIterator >
internal::IOManipRange<InputIterator> qpp::disp (
    InputIterator first,
    InputIterator last,
    const std::string & separator,
    const std::string & start = "[",
    const std::string & end = "]" )
```

Range ostream manipulator.

## Parameters

<i>first</i>	Iterator to the first element of the range
<i>last</i>	Iterator to the last element of the range
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking

## Returns

Instance of [qpp::internal::IOManipRange](#)

6.1.3.19 `disp()` [4/5]

```
template<typename Container >
internal::IOManipRange<typename Container::const_iterator> qpp::disp (
    const Container & c,
    const std::string & separator,
    const std::string & start = "[",
    const std::string & end = "]",
    typename std::enable_if< is\_iterable< Container >::value >::type * = nullptr )
```

Standard container ostream manipulator. The container must support `std::begin()`, `std::end()` and forward iteration.

## Parameters

<i>c</i>	Container
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking

## Returns

Instance of [qpp::internal::IOManipRange](#)

6.1.3.20 `disp()` [5/5]

```
template<typename PointerType >
internal::IOManipPointer<PointerType> qpp::disp (
    const PointerType * p,
    idx N,
    const std::string & separator,
    const std::string & start = "[",
    const std::string & end = "]" )
```

C-style pointer ostream manipulator.

## Parameters

<i>p</i>	Pointer to the first element
<i>N</i>	Number of elements to be displayed
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking

**Returns**

Instance of [qpp::internal::IOManipPointer](#)

**6.1.3.21 egcd()**

```
std::tuple<bigint, bigint, bigint> qpp::egcd (
    bigint a,
    bigint b ) [inline]
```

Extended greatest common divisor of two integers.

**See also**

[qpp::gcd\(\)](#)

**Parameters**

<i>a</i>	Integer
<i>b</i>	Integer

**Returns**

Tuple of: 1. Integer  $m$ , 2. Integer  $n$ , and 3. Non-negative integer  $gcd(a, b)$  such that  $ma + nb = gcd(a, b)$

**6.1.3.22 entanglement()** [1/2]

```
template<typename Derived >
double qpp::entanglement (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & dims )
```

Entanglement of the bi-partite pure state  $A$ .

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

**See also**

[qpp::entropy\(\)](#)

**Parameters**

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

**Returns**

Entanglement, with the logarithm in base 2

**6.1.3.23 entanglement()** [2/2]

```
template<typename Derived >
double qpp::entanglement (
    const Eigen::MatrixBase< Derived > & A,
    idx d = 2 )
```

Entanglement of the bi-partite pure state  $A$ .

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

**See also**

[qpp::entropy\(\)](#)

**Parameters**

$A$	Eigen expression
$d$	Subsystem dimensions

**Returns**

Entanglement, with the logarithm in base 2

**6.1.3.24 entropy()** [1/2]

```
template<typename Derived >
double qpp::entropy (
    const Eigen::MatrixBase< Derived > & A )
```

von-Neumann entropy of the density matrix  $A$

**Parameters**

$A$	Eigen expression
-----	------------------

**Returns**

von-Neumann entropy, with the logarithm in base 2

**6.1.3.25 entropy()** [2/2]

```
double qpp::entropy (
    const std::vector< double > & prob ) [inline]
```

Shannon entropy of the probability distribution *prob*.

**Parameters**

<i>prob</i>	Real probability vector
-------------	-------------------------

**Returns**

Shannon entropy, with the logarithm in base 2

**6.1.3.26 factors()**

```
std::vector<bigint> qpp::factors (
    bigint a ) [inline]
```

Prime factor decomposition.

**Note**

Runs in  $\mathcal{O}(\sqrt{n})$  time complexity

**Parameters**

<i>a</i>	Integer different from 0, 1 or -1
----------	-----------------------------------

**Returns**

Integer vector containing the factors

**6.1.3.27 gcd()** [1/2]

```
bigint qpp::gcd (
    bigint a,
    bigint b ) [inline]
```

Greatest common divisor of two integers.

**See also**

[qpp::lcm\(\)](#)



## Parameters

<i>a</i>	Integer
<i>b</i>	Integer

## Returns

Greatest common divisor of *a* and *b*

## 6.1.3.28 gcd() [2/2]

```
bigint qpp::gcd (
    const std::vector< bigint > & as ) [inline]
```

Greatest common divisor of a list of integers.

## See also

[qpp::lcm\(\)](#)

## Parameters

<i>as</i>	List of integers
-----------	------------------

## Returns

Greatest common divisor of all numbers in *as*

## 6.1.3.29 gconcurrency()

```
template<typename Derived >
double qpp::gconcurrency (
    const Eigen::MatrixBase< Derived > & A )
```

G-concurrency of the bi-partite pure state *A*.

## Note

Both local dimensions must be equal

Uses [qpp::logdet\(\)](#) to avoid overflows

## See also

[qpp::logdet\(\)](#)

## Parameters

<i>A</i>	Eigen expression
----------	------------------

## Returns

G-concurrence

6.1.3.30 `invperm()`

```
std::vector<idx> qpp::invperm (
    const std::vector< idx > & perm ) [inline]
```

Inverse permutation.

## Parameters

<i>perm</i>	Permutation
-------------	-------------

## Returns

Inverse of the permutation *perm*

6.1.3.31 `ip()` [1/2]

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::ip (
    const Eigen::MatrixBase< Derived > & phi,
    const Eigen::MatrixBase< Derived > & psi,
    const std::vector< idx > & subsys,
    const std::vector< idx > & dims )
```

Generalized inner product.

## Parameters

<i>phi</i>	Column vector Eigen expression
<i>psi</i>	Column vector Eigen expression
<i>subsys</i>	Subsystem indexes over which <i>phi</i> is defined
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Inner product  $\langle \phi_{subsys} | \psi \rangle$ , as a scalar or column vector over the remaining Hilbert space

## 6.1.3.32 ip() [2/2]

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::ip (
    const Eigen::MatrixBase< Derived > & phi,
    const Eigen::MatrixBase< Derived > & psi,
    const std::vector< idx > & subsys,
    idx d = 2 )
```

Generalized inner product.

## Parameters

<i>phi</i>	Column vector Eigen expression
<i>psi</i>	Column vector Eigen expression
<i>subsys</i>	Subsystem indexes over which <i>phi</i> is defined
<i>d</i>	Subsystem dimensions

## Returns

Inner product  $\langle \phi_{subsys} | \psi \rangle$ , as a scalar or column vector over the remaining Hilbert space

## 6.1.3.33 isprime()

```
bool qpp::isprime (
    bigint p,
    idx k = 80 ) [inline]
```

Primality test based on the Miller-Rabin's algorithm.

## Parameters

<i>p</i>	Integer different from 0, 1 or -1
<i>k</i>	Number of iterations. The probability of a false positive is $2^{-k}$ .

## Returns

True if the number is (most-likely) prime, false otherwise

## 6.1.3.34 kraus2choi()

```
cmat qpp::kraus2choi (
    const std::vector< cmat > & Ks ) [inline]
```

Choi matrix.

See also

[qpp::choi2kraus\(\)](#)

Constructs the Choi matrix of the channel specified by the set of Kraus operators  $Ks$  in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

Note

The superoperator matrix  $S$  and the Choi matrix  $C$  are related by  $S_{ab,mn} = C_{ma,nb}$

Parameters

$Ks$	Set of Kraus operators
------	------------------------

Returns

Choi matrix

#### 6.1.3.35 kraus2super()

```
cmat qpp::kraus2super (
    const std::vector< cmat > & Ks ) [inline]
```

Superoperator matrix.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators  $Ks$  in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

Parameters

$Ks$	Set of Kraus operators
------	------------------------

Returns

Superoperator matrix

#### 6.1.3.36 lcm() [1/2]

```
bigint qpp::lcm (
    bigint a,
    bigint b ) [inline]
```

Least common multiple of two integers.

See also

[qpp::gcd\(\)](#)

## Parameters

<i>a</i>	Integer
<i>b</i>	Integer

## Returns

Least common multiple of *a* and *b*

## 6.1.3.37 lcm() [2/2]

```
bigint qpp::lcm (
    const std::vector< bigint > & as ) [inline]
```

Least common multiple of a list of integers.

## See also

[qpp::gcd\(\)](#)

## Parameters

<i>as</i>	List of integers
-----------	------------------

## Returns

Least common multiple of all numbers in *as*

## 6.1.3.38 load()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::load (
    const std::string & fname )
```

Loads Eigen matrix from a binary file (internal format) in double precision.

## See also

[qpp::save\(\)](#)

The template parameter cannot be automatically deduced and must be explicitly provided, depending on the scalar field of the matrix that is being loaded.

## Example:

```
// loads a previously saved Eigen dynamic complex matrix from "input.bin"
cmat mat = load<cmat>("input.bin");
```

## Parameters

<i>fname</i>	Output file name
--------------	------------------

## 6.1.3.39 loadMATLAB() [1/2]

```
template<typename Derived >
std::enable_if<std::is_same<typename Derived::Scalar, cplx>::value, dyn_mat < cplx> >::type
qpp::loadMATLAB (
    const std::string & mat_file,
    const std::string & var_name )
```

Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.

## See also

[qpp::saveMATLAB\(\)](#)

The template parameter cannot be automatically deduced and must be explicitly provided

## Example:

```
// loads a previously saved Eigen ket
// from the MATLAB file "input.mat"
ket psi = loadMATLAB<ket>("input.mat");
```

## Template Parameters

<i>Derived</i>	Complex Eigen type
----------------	--------------------

## Parameters

<i>mat_file</i>	MATALB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be loaded

## Returns

Eigen dynamic matrix

## 6.1.3.40 loadMATLAB() [2/2]

```
template<typename Derived >
std::enable_if<!  
std::is_same<typename Derived::Scalar, cplx>::value, dyn_mat < typename Derived  
::Scalar> >::type qpp::loadMATLAB (
    const std::string & mat_file,
    const std::string & var_name )
```

Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.

See also

[qpp::saveMATLAB\(\)](#)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen dynamic double matrix
// from the MATLAB file "input.mat"
dmat mat = loadMATLAB<dmat>("input.mat");
```

#### Template Parameters

<i>Derived</i>	Non-complex Eigen type
----------------	------------------------

#### Parameters

<i>mat_file</i>	MATALB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be loaded

#### Returns

Eigen dynamic matrix

#### 6.1.3.41 lognegativity() [1/2]

```
template<typename Derived >
double qpp::lognegativity (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & dims )
```

Logarithmic negativity of the bi-partite mixed state A.

#### Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

#### Returns

Logarithmic negativity, with the logarithm in base 2

#### 6.1.3.42 lognegativity() [2/2]

```
template<typename Derived >
double qpp::lognegativity (
    const Eigen::MatrixBase< Derived > & A,
    idx d = 2 )
```

Logarithmic negativity of the bi-partite mixed state  $A$ .

##### Parameters

$A$	Eigen expression
$d$	Subsystem dimensions

##### Returns

Logarithmic negativity, with the logarithm in base 2

#### 6.1.3.43 marginalX()

```
std::vector<double> qpp::marginalX (
    const dmat & probXY ) [inline]
```

Marginal distribution.

##### Parameters

$probXY$	Real matrix representing the joint probability distribution of $X$ and $Y$ in lexicographical order ( $X$ labels the rows, $Y$ labels the columns)
----------	--

##### Returns

Real vector consisting of the marginal distribution of  $X$

#### 6.1.3.44 marginalY()

```
std::vector<double> qpp::marginalY (
    const dmat & probXY ) [inline]
```

Marginal distribution.

##### Parameters

$probXY$	Real matrix representing the joint probability distribution of $X$ and $Y$ in lexicographical order ( $X$ labels the rows, $Y$ labels the columns)
----------	--



**Returns**

Real vector consisting of the marginal distribution of  $Y$

**6.1.3.45 measure()** [1/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< cmat > & Ks )
```

Measures the state  $A$  using the set of Kraus operators  $Ks$ .

**Parameters**

$A$	Eigen expression
$Ks$	Set of Kraus operators

**Returns**

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

**6.1.3.46 measure()** [2/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
    const Eigen::MatrixBase< Derived > & A,
    const std::initializer_list< cmat > & Ks )
```

Measures the state  $A$  using the set of Kraus operators  $Ks$ .

**Parameters**

$A$	Eigen expression
$Ks$	Set of Kraus operators

**Returns**

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

**6.1.3.47** `measure()` [3/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
    const Eigen::MatrixBase< Derived > & A,
    const cmat & U )
```

Measures the state  $A$  in the orthonormal basis specified by the unitary matrix  $U$ .

**Parameters**

$A$	Eigen expression
$U$	Unitary matrix whose columns represent the measurement basis vectors

**Returns**

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

**6.1.3.48** `measure()` [4/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< cmat > & Ks,
    const std::vector< idx > & subsys,
    const std::vector< idx > & dims )
```

Measures the part *subsys* of the multi-partite state vector or density matrix  $A$  using the set of Kraus operators  $Ks$ .

**See also**

[qpp::measure\\_seq\(\)](#)

**Note**

The dimension of all  $Ks$  must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

**Parameters**

$A$	Eigen expression
$Ks$	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
<i>dims</i>	Dimensions of the multi-partite system

**Returns**

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

**6.1.3.49 measure()** [5/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
    const Eigen::MatrixBase< Derived > & A,
    const std::initializer_list< cmat > & Ks,
    const std::vector< idx > & subsys,
    const std::vector< idx > & dims )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

**See also**

[qpp::measure\\_seq\(\)](#)

**Note**

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

**Parameters**

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
<i>dims</i>	Dimensions of the multi-partite system

**Returns**

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

**6.1.3.50 measure()** [6/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< cmat > & Ks,
    const std::vector< idx > & subsys,
    idx d = 2 )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

[qpp::measure\\_seq\(\)](#)

Note

The dimension of all  $K$ s must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

$A$	Eigen expression
$K$ s	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
$d$	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

#### 6.1.3.51 `measure()` [7/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
    const Eigen::MatrixBase< Derived > & A,
    const std::initializer_list< cmat > & Ks,
    const std::vector< idx > & subsys,
    idx d = 2 )
```

Measures the part *subsys* of the multi-partite state vector or density matrix  $A$  using the set of Kraus operators  $K$ s.

See also

[qpp::measure\\_seq\(\)](#)

Note

The dimension of all  $K$ s must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

$A$	Eigen expression
$K$ s	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
$d$	Subsystem dimensions

## Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.52 `measure()` [8/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
    const Eigen::MatrixBase< Derived > & A,
    const cmat & V,
    const std::vector< idx > & subsys,
    const std::vector< idx > & dims )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 POVM specified by the matrix *V*.

## See also

[qpp::measure\\_seq\(\)](#)

## Note

The dimension of *V* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

## Parameters

<i>A</i>	Eigen expression
<i>V</i>	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 POVM
<i>subsys</i>	Subsystem indexes that are measured
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.53 `measure()` [9/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
    const Eigen::MatrixBase< Derived > & A,
    const cmat & V,
    const std::vector< idx > & subsys,
    idx d = 2 )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 POVM specified by the matrix *V*.

## See also

[qpp::measure\\_seq\(\)](#)

## Note

The dimension of  $V$  must match the dimension of  $subsys$ . The measurement is destructive, i.e. the measured subsystems are traced away.

## Parameters

$A$	Eigen expression
$V$	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 POVM
$subsys$	Subsystem indexes that are measured
$d$	Subsystem dimensions

## Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.54 `measure_seq()` [1/2]

```
template<typename Derived >
std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (
    const Eigen::MatrixBase< Derived > & A,
    std::vector< idx > subsys,
    std::vector< idx > dims )
```

Sequentially measures the part  $subsys$  of the multi-partite state vector or density matrix  $A$  in the computational basis.

## See also

[qpp::measure\(\)](#)

## Parameters

$A$	Eigen expression
$subsys$	Subsystem indexes that are measured
$dims$	Dimensions of the multi-partite system

## Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to  $subsys$ , i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.55 `measure_seq()` [2/2]

```
template<typename Derived >
std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (
    const Eigen::MatrixBase< Derived > & A,
    std::vector< idx > subsys,
    idx d = 2 )
```

Sequentially measures the part *subsys* of the multi-partite state vector or density matrix *A* in the computational basis.

See also

[qpp::measure\(\)](#)

## Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes that are measured
<i>d</i>	Subsystem dimensions

## Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *subsys*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.56 `modinv()`

```
bigint qpp::modinv (
    bigint a,
    bigint p ) [inline]
```

Modular inverse of *a* mod *p*.

See also

[qpp::egcd\(\)](#)

## Note

*a* and *p* must be co-prime

## Parameters

<i>a</i>	Non-negative integer
<i>p</i>	Non-negative integer

**Returns**

Modular inverse  $a^{-1} \bmod p$

**6.1.3.57 modmul()**

```
bigint qpp::modmul (
    bigint a,
    bigint b,
    bigint p ) [inline]
```

Modular multiplication without overflow.

Computes  $ab \bmod p$  without overflow

**Parameters**

$a$	Integer
$b$	Integer
$p$	Positive integer

**Returns**

$ab \bmod p$  avoiding overflow

**6.1.3.58 modpow()**

```
bigint qpp::modpow (
    bigint a,
    bigint n,
    bigint p ) [inline]
```

Fast integer power modulo  $p$  based on the SQUARE-AND-MULTIPLY algorithm.

**Note**

Uses [qpp::modmul\(\)](#) that avoids overflows

Computes  $a^n \bmod p$

**Parameters**

$a$	Non-negative integer
$n$	Non-negative integer
$p$	Strictly positive integer



## Returns

$$a^n \bmod p$$

## 6.1.3.59 negativity() [1/2]

```
template<typename Derived >
double qpp::negativity (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & dims )
```

Negativity of the bi-partite mixed state  $A$ .

## Parameters

$A$	Eigen expression
$dims$	Dimensions of the bi-partite system

## Returns

Negativity

## 6.1.3.60 negativity() [2/2]

```
template<typename Derived >
double qpp::negativity (
    const Eigen::MatrixBase< Derived > & A,
    idx d = 2 )
```

Negativity of the bi-partite mixed state  $A$ .

## Parameters

$A$	Eigen expression
$d$	Subsystem dimensions

## Returns

Negativity

## 6.1.3.61 omega()

```
cplx qpp::omega (
    idx D ) [inline]
```

D-th root of unity.

## Parameters

<i>D</i>	Non-negative integer
----------	----------------------

## Returns

D-th root of unity  $\exp(2\pi i/D)$

6.1.3.62 `operator""_i()` [1/2]

```
constexpr cpplx qpp::operator"" _i (
    unsigned long long int x ) [inline], [noexcept]
```

User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)

Example:

```
cpplx z = 4_i; // type of z is std::complex<double>
```

6.1.3.63 `operator""_i()` [2/2]

```
constexpr cpplx qpp::operator"" _i (
    long double x ) [inline], [noexcept]
```

User-defined literal for complex  $i = \sqrt{-1}$  (real overload)

Example:

```
cpplx z = 4.5_i; // type of z is std::complex<double>
```

6.1.3.64 `ptrace()` [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & subsys,
    const std::vector< idx > & dims )
```

Partial trace.

See also

[`qpp::ptrace1\(\)`](#), [`qpp::ptrace2\(\)`](#)

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

## Parameters

$A$	Eigen expression
$subsys$	Subsystem indexes
$dims$	Dimensions of the multi-partite system

## Returns

Partial trace  $Tr_{subsys}(\cdot)$  over the subsystems  $subsys$  in a multi-partite system, as a dynamic matrix over the same scalar field as  $A$

6.1.3.65 `ptrace()` [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & subsys,
    idx d = 2 )
```

Partial trace.

## See also

[qpp::ptrace1\(\)](#), [qpp::ptrace2\(\)](#)

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

## Parameters

$A$	Eigen expression
$subsys$	Subsystem indexes
$d$	Subsystem dimensions

## Returns

Partial trace  $Tr_{subsys}(\cdot)$  over the subsystems  $subsys$  in a multi-partite system, as a dynamic matrix over the same scalar field as  $A$

6.1.3.66 `ptrace1()` [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace1 (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & dims )
```

Partial trace.

See also

[qpp::ptrace2\(\)](#)

Partial trace over the first subsystem of bi-partite state vector or density matrix

Parameters

$A$	Eigen expression
$dims$	Dimensions of the bi-partite system

Returns

Partial trace  $Tr_A(\cdot)$  over the first subsystem  $A$  in a bi-partite system  $A \otimes B$ , as a dynamic matrix over the same scalar field as  $A$

#### 6.1.3.67 ptrace1() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace1 (
    const Eigen::MatrixBase< Derived > & A,
    idx d = 2 )
```

Partial trace.

See also

[qpp::ptrace2\(\)](#)

Partial trace over the first subsystem of bi-partite state vector or density matrix

Parameters

$A$	Eigen expression
$d$	Subsystem dimensions

Returns

Partial trace  $Tr_A(\cdot)$  over the first subsystem  $A$  in a bi-partite system  $A \otimes B$ , as a dynamic matrix over the same scalar field as  $A$

#### 6.1.3.68 ptrace2() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace2 (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & dims )
```

Partial trace.

See also

[qpp::ptrace1\(\)](#)

Partial trace over the second subsystem of bi-partite state vector or density matrix

Parameters

$A$	Eigen expression
$dims$	Dimensions of the bi-partite system

Returns

Partial trace  $Tr_B(\cdot)$  over the second subsystem  $B$  in a bi-partite system  $A \otimes B$ , as a dynamic matrix over the same scalar field as  $A$

#### 6.1.3.69 ptrace2() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace2 (
    const Eigen::MatrixBase< Derived > & A,
    idx d = 2 )
```

Partial trace.

See also

[qpp::ptrace1\(\)](#)

Partial trace over the second subsystem of bi-partite state vector or density matrix

Parameters

$A$	Eigen expression
$d$	Subsystem dimensions

Returns

Partial trace  $Tr_B(\cdot)$  over the second subsystem  $B$  in a bi-partite system  $A \otimes B$ , as a dynamic matrix over the same scalar field as  $A$

#### 6.1.3.70 ptranspose() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptranspose (
```

```
const Eigen::MatrixBase< Derived > & A,
const std::vector< idx > & subsys,
const std::vector< idx > & dims )
```

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

#### Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes
<i>dims</i>	Dimensions of the multi-partite system

#### Returns

Partial transpose  $(\cdot)^{T_{subsys}}$  over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

#### 6.1.3.71 ptranspose() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptranspose (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & subsys,
    idx d = 2 )
```

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

#### Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes
<i>d</i>	Subsystem dimensions

#### Returns

Partial transpose  $(\cdot)^{T_{subsys}}$  over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

#### 6.1.3.72 qmutualinfo() [1/2]

```
template<typename Derived >
double qpp::qmutualinfo (
```

```
const Eigen::MatrixBase< Derived > & A,
const std::vector< idx > & subsysA,
const std::vector< idx > & subsysB,
const std::vector< idx > & dims )
```

Quantum mutual information between 2 subsystems of a composite system.

#### Parameters

<i>A</i>	Eigen expression
<i>subsysA</i>	Indexes of the first subsystem
<i>subsysB</i>	Indexes of the second subsystem
<i>dims</i>	Dimensions of the multi-partite system

#### Returns

Mutual information between the 2 subsystems

#### 6.1.3.73 qmutualinfo() [2/2]

```
template<typename Derived >
double qpp::qmutualinfo (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & subsysA,
    const std::vector< idx > & subsysB,
    idx d = 2 )
```

Quantum mutual information between 2 subsystems of a composite system.

#### Parameters

<i>A</i>	Eigen expression
<i>subsysA</i>	Indexes of the first subsystem
<i>subsysB</i>	Indexes of the second subsystem
<i>d</i>	Subsystem dimensions

#### Returns

Mutual information between the 2 subsystems

#### 6.1.3.74 rand() [1/5]

```
double qpp::rand (
    double a,
    double b ) [inline]
```

Generates a random real number uniformly distributed in the interval [a, b)



## Parameters

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

## Returns

Random real number (double) uniformly distributed in the interval [a, b)

6.1.3.75 `rand()` [2/5]

```
bigint qpp::rand (
    bigint a,
    bigint b ) [inline]
```

Generates a random big integer uniformly distributed in the interval [a, b].

## Note

To avoid ambiguity with double `qpp::rand(double, double)` cast at least one of the arguments to `qpp::bigint`

## Parameters

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, belongs to it

## Returns

Random big integer uniformly distributed in the interval [a, b]

6.1.3.76 `rand()` [3/5]

```
template<typename Derived >
Derived qpp::rand (
    idx rows,
    idx cols,
    double a = 0,
    double b = 1 )
```

Generates a random matrix with entries uniformly distributed in the interval [a, b)

If complex, then both real and imaginary parts are uniformly distributed in [a, b)

This is the generic version that always throws `qpp::Exception::Type::UNDEFINED_TYPE`. It is specialized only for `qpp::dmat` and `qpp::cmat`

**6.1.3.77 rand()** [4/5]

```
template<>
dmat qpp::rand (
    idx rows,
    idx cols,
    double a,
    double b ) [inline]
```

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (**qpp::dmat**)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries uniformly distributed in [-1,1)
dmat mat = rand<dmat>(3, 3, -1, 1);
```

**Parameters**

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

**Returns**

Random real matrix

**6.1.3.78 rand()** [5/5]

```
template<>
cmat qpp::rand (
    idx rows,
    idx cols,
    double a,
    double b ) [inline]
```

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (**qpp::cmat**)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) uniformly distributed in [-1,1)
cmat mat = rand<cmat>(3, 3, -1, 1);
```

## Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

## Returns

Random complex matrix

## 6.1.3.79 randH()

```
cmat qpp::randH (
    idx D = 2 ) [inline]
```

Generates a random Hermitian matrix.

## Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

## Returns

Random Hermitian matrix

## 6.1.3.80 randidx()

```
idx qpp::randidx (
    idx a = std::numeric_limits<idx>::min(),
    idx b = std::numeric_limits<idx>::max() ) [inline]
```

Generates a random index (idx) uniformly distributed in the interval [a, b].

## Parameters

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, belongs to it

## Returns

Random index (idx) uniformly distributed in the interval [a, b]

## 6.1.3.81 randket()

```
ket qpp::randket (
    idx D = 2 ) [inline]
```

Generates a random normalized ket (pure state vector)

## Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

## Returns

Random normalized ket

## 6.1.3.82 randkraus()

```
std::vector<cmat> qpp::randkraus (
    idx N,
    idx D = 2 ) [inline]
```

Generates a set of random Kraus operators.

## Note

The set of Kraus operators satisfy the closure condition  $\sum_i K_i^\dagger K_i = I$

## Parameters

<i>N</i>	Number of Kraus operators
<i>D</i>	Dimension of the Hilbert space

## Returns

Set of *N* Kraus operators satisfying the closure condition

## 6.1.3.83 randn() [1/4]

```
template<typename Derived >
Derived qpp::randn (
    idx rows,
    idx cols,
    double mean = 0,
    double sigma = 1 )
```

Generates a random matrix with entries normally distributed in  $N(\text{mean}, \text{sigma})$

If complex, then both real and imaginary parts are normally distributed in  $N(\text{mean}, \text{sigma})$

This is the generic version that always throws `qpp::Exception::Type::UNDEFINED_TYPE`. It is specialized only for `qpp::dmat` and `qpp::cmat`

#### 6.1.3.84 randn() [2/4]

```
template<>
dmat qpp::randn (
    idx rows,
    idx cols,
    double mean,
    double sigma ) [inline]
```

Generates a random real matrix with entries normally distributed in  $N(\text{mean}, \text{sigma})$ , specialization for double matrices (`qpp::dmat`)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries normally distributed in N(0,2)
dmat mat = randn<dmat>(3, 3, 0, 2);
```

#### Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

#### Returns

Random real matrix

#### 6.1.3.85 randn() [3/4]

```
template<>
cmat qpp::randn (
    idx rows,
    idx cols,
    double mean,
    double sigma ) [inline]
```

Generates a random complex matrix with entries (both real and imaginary) normally distributed in  $N(\text{mean}, \text{sigma})$ , specialization for complex matrices (`qpp::cmat`)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) normally distributed in N(0,2)
cmat mat = randn<cmat>(3, 3, 0, 2);
```

#### Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

#### Returns

Random complex matrix

#### 6.1.3.86 randn() [4/4]

```
double qpp::randn (
    double mean = 0,
    double sigma = 1 ) [inline]
```

Generates a random real number (double) normally distributed in N(mean, sigma)

#### Parameters

<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

#### Returns

Random real number normally distributed in N(mean, sigma)

#### 6.1.3.87 randperm()

```
std::vector<idx> qpp::randperm (
    idx N ) [inline]
```

Generates a random uniformly distributed permutation.

Uses Knuth shuffle method (as implemented by std::shuffle), so that all permutations are equally probable

#### Parameters

<i>N</i>	Size of the permutation
----------	-------------------------

**Returns**

Random permutation of size  $N$

**6.1.3.88 randprime()**

```
bigint qpp::randprime (
    bigint a,
    bigint b,
    idx N = 1000 ) [inline]
```

Generates a random big prime uniformly distributed in the interval  $[a, b]$ .

**Parameters**

$a$	Beginning of the interval, belongs to it
$b$	End of the interval, belongs to it
$N$	Maximum number of candidates

**Returns**

Random big integer uniformly distributed in the interval  $[a, b]$

**6.1.3.89 randprob()**

```
std::vector<double> qpp::randprob (
    idx N ) [inline]
```

Generates a random probability vector uniformly distributed over the probability simplex.

**Parameters**

$N$	Size of the probability vector
-----	--------------------------------

**Returns**

Random probability vector

**6.1.3.90 randrho()**

```
cmat qpp::randrho (
    idx D = 2 ) [inline]
```

Generates a random density matrix.

**Parameters**

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

**Returns**

Random density matrix

**6.1.3.91 randU()**

```
cmat qpp::randU (
    idx D = 2 ) [inline]
```

Generates a random unitary matrix.

**Parameters**

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

**Returns**

Random unitary

**6.1.3.92 randV()**

```
cmat qpp::randV (
    idx Din,
    idx Dout ) [inline]
```

Generates a random isometry matrix.

**Parameters**

<i>Din</i>	Size of the input Hilbert space
<i>Dout</i>	Size of the output Hilbert space

**Returns**

Random isometry matrix



**6.1.3.93** `renyi()` [1/2]

```
template<typename Derived >
double qpp::renyi (
    const Eigen::MatrixBase< Derived > & A,
    double alpha )
```

Renyi-  $\alpha$  entropy of the density matrix  $A$ , for  $\alpha \geq 0$ .

**Note**

When  $\alpha \rightarrow 1$  the Renyi entropy converges to the von-Neumann entropy, with the logarithm in base 2

**Parameters**

<i>A</i>	Eigen expression
<i>alpha</i>	Non-negative real number, use <code>qpp::infy</code> for $\alpha = \infty$

**Returns**

Renyi-  $\alpha$  entropy, with the logarithm in base 2

**6.1.3.94** `renyi()` [2/2]

```
double qpp::renyi (
    const std::vector< double > & prob,
    double alpha ) [inline]
```

Renyi-  $\alpha$  entropy of the probability distribution  $prob$ , for  $\alpha \geq 0$ .

**Note**

When  $\alpha \rightarrow 1$  the Renyi entropy converges to the Shannon entropy, with the logarithm in base 2

**Parameters**

<i>prob</i>	Real probability vector
<i>alpha</i>	Non-negative real number, use <code>qpp::infy</code> for $\alpha = \infty$

**Returns**

Renyi-  $\alpha$  entropy, with the logarithm in base 2

**6.1.3.95 save()**

```
template<typename Derived >
void qpp::save (
    const Eigen::MatrixBase< Derived > & A,
    const std::string & fname )
```

Saves Eigen expression to a binary file (internal format) in double precision.

See also

[qpp::load\(\)](#)

**Parameters**

<i>A</i>	Eigen expression
<i>fname</i>	Output file name

**6.1.3.96 saveMATLAB()** [1/2]

```
template<typename Derived >
std::enable_if<std::is_same<typename Derived::Scalar, cplx>::value>::type qpp::saveMATLAB (
    const Eigen::MatrixBase< Derived > & A,
    const std::string & mat_file,
    const std::string & var_name,
    const std::string & mode )
```

Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.

See also

[qpp::loadMATLAB\(\)](#)

**Template Parameters**

<i>Complex</i>	Eigen type
----------------	------------

**Parameters**

<i>A</i>	Eigen expression over the complex field
<i>mat_file</i>	MATALB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be saved
<i>mode</i>	Saving mode (append, overwrite etc.), see MATLAB <i>matOpen()</i> documentation for details

**6.1.3.97 saveMATLAB()** [2/2]

```
template<typename Derived >
std::enable_if<!std::is_same<typename Derived::Scalar, cplx>::value>::type qpp::saveMATLAB (
    const Eigen::MatrixBase< Derived > & A,
    const std::string & mat_file,
    const std::string & var_name,
    const std::string & mode )
```

Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.

See also

[qpp::loadMATLAB\(\)](#)

**Template Parameters**

<i>Npn-complex</i>	Eigen type
--------------------	------------

**Parameters**

<i>A</i>	Non-complex Eigen expression
<i>mat_file</i>	MATALB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be saved
<i>mode</i>	Saving mode (append, overwrite etc.), see MATLAB <i>matOpen()</i> documentation for details

**6.1.3.98 schmidtA()** [1/2]

```
template<typename Derived >
cmat qpp::schmidtA (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & dims )
```

Schmidt basis on Alice side.

**Parameters**

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

**Returns**

Unitary matrix  $U$  whose columns represent the Schmidt basis vectors on Alice side.

**6.1.3.99 schmidtA()** [2/2]

```
template<typename Derived >
cmat qpp::schmidtA (
    const Eigen::MatrixBase< Derived > & A,
    idx d = 2 )
```

Schmidt basis on Alice side.

**Parameters**

<i>A</i>	Eigen expression
<i>d</i>	Subsystem dimensions

**Returns**

Unitary matrix  $U$  whose columns represent the Schmidt basis vectors on Alice side.

**6.1.3.100 schmidtB()** [1/2]

```
template<typename Derived >
cmat qpp::schmidtB (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & dims )
```

Schmidt basis on Bob side.

**Parameters**

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

**Returns**

Unitary matrix  $V$  whose columns represent the Schmidt basis vectors on Bob side.

**6.1.3.101 schmidtB()** [2/2]

```
template<typename Derived >
cmat qpp::schmidtB (
    const Eigen::MatrixBase< Derived > & A,
    idx d = 2 )
```

Schmidt basis on Bob side.

## Parameters

$A$	Eigen expression
$d$	Subsystem dimensions

## Returns

Unitary matrix  $V$  whose columns represent the Schmidt basis vectors on Bob side.

6.1.3.102 `schmidtcoeffs()` [1/2]

```
template<typename Derived >
dyn_col_vect<double> qpp::schmidtcoeffs (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & dims )
```

Schmidt coefficients of the bi-partite pure state  $A$ .

## Note

The sum of the squares of the Schmidt coefficients equals 1

## See also

[qpp::schmidtprobs\(\)](#)

## Parameters

$A$	Eigen expression
$dims$	Dimensions of the bi-partite system

## Returns

Schmidt coefficients of  $A$ , ordered in decreasing order, as a real dynamic column vector

6.1.3.103 `schmidtcoeffs()` [2/2]

```
template<typename Derived >
dyn_col_vect<double> qpp::schmidtcoeffs (
    const Eigen::MatrixBase< Derived > & A,
    idx d = 2 )
```

Schmidt coefficients of the bi-partite pure state  $A$ .

**Note**

The sum of the squares of the Schmidt coefficients equals 1

**See also**

[qpp::schmidtprobs\(\)](#)

**Parameters**

$A$	Eigen expression
$d$	Subsystem dimensions

**Returns**

Schmidt coefficients of  $A$ , ordered in decreasing order, as a real dynamic column vector

**6.1.3.104 schmidtprobs()** [1/2]

```
template<typename Derived >
std::vector<double> qpp::schmidtprobs (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & dims )
```

Schmidt probabilities of the bi-partite pure state  $A$ .

Defined as the squares of the Schmidt coefficients. The sum of the Schmidt probabilities equals 1.

**See also**

[qpp::schmidtcoeffs\(\)](#)

**Parameters**

$A$	Eigen expression
$dims$	Dimensions of the bi-partite system

**Returns**

Real vector consisting of the Schmidt probabilities of  $A$ , ordered in decreasing order

**6.1.3.105 schmidtprobs()** [2/2]

```
template<typename Derived >
std::vector<double> qpp::schmidtprobs (
```

```
const Eigen::MatrixBase< Derived > & A,
idx d = 2 )
```

Schmidt probabilities of the bi-partite pure state  $A$ .

Defined as the squares of the Schmidt coefficients. The sum of the Schmidt probabilities equals 1.

See also

[qpp::schmidtcoeffs\(\)](#)

#### Parameters

$A$	Eigen expression
$d$	Subsystem dimensions

#### Returns

Real vector consisting of the Schmidt probabilities of  $A$ , ordered in decreasing order

#### 6.1.3.106 sigma()

```
template<typename Container >
double qpp::sigma (
    const std::vector< double > & prob,
    const Container & X,
    typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Standard deviation.

#### Parameters

$prob$	Real probability vector representing the probability distribution of $X$
$X$	Real random variable values represented by an STL-like container

#### Returns

Standard deviation of  $X$

#### 6.1.3.107 super2choi()

```
cmat qpp::super2choi (
    const cmat & A ) [inline]
```

Converts superoperator matrix to Choi matrix.

See also

[qpp::choi2super\(\)](#)



## Parameters

<i>A</i>	Superoperator matrix
----------	----------------------

## Returns

Choi matrix

## 6.1.3.108 syspermute() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::syspermute (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & perm,
    const std::vector< idx > & dims )
```

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit *perm*[*i*] is permuted to the location *i*.

## Parameters

<i>A</i>	Eigen expression
<i>perm</i>	Permutation
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Permuted system, as a dynamic matrix over the same scalar field as *A*

## 6.1.3.109 syspermute() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::syspermute (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & perm,
    idx d = 2 )
```

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit *perm*[*i*] is permuted to the location *i*.

## Parameters

<i>A</i>	Eigen expression
<i>perm</i>	Permutation
<i>d</i>	Subsystem dimensions

**Returns**

Permuted system, as a dynamic matrix over the same scalar field as  $A$

**6.1.3.110 tsallis()** [1/2]

```
template<typename Derived >
double qpp::tsallis (
    const Eigen::MatrixBase< Derived > & A,
    double q )
```

Tsallis-  $q$  entropy of the density matrix  $A$ , for  $q \geq 0$ .

**Note**

When  $q \rightarrow 1$  the Tsallis entropy converges to the von-Neumann entropy, with the logarithm in base  $e$

**Parameters**

$A$	Eigen expression
$q$	Non-negative real number

**Returns**

Tsallis-  $q$  entropy

**6.1.3.111 tsallis()** [2/2]

```
double qpp::tsallis (
    const std::vector< double > & prob,
    double q ) [inline]
```

Tsallis-  $q$  entropy of the probability distribution  $prob$ , for  $q \geq 0$ .

**Note**

When  $q \rightarrow 1$  the Tsallis entropy converges to the Shannon entropy, with the logarithm in base  $e$

**Parameters**

$prob$	Real probability vector
$q$	Non-negative real number

**Returns**

Tsallis-  $q$  entropy

**6.1.3.112 uniform()**

```
std::vector<double> qpp::uniform (
    idx N ) [inline]
```

Uniform probability distribution vector.

**Parameters**

$N$	Size of the alphabet
-----	----------------------

**Returns**

Real vector consisting of a uniform distribution of size  $N$

**6.1.3.113 var()**

```
template<typename Container >
double qpp::var (
    const std::vector< double > & prob,
    const Container & X,
    typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Variance.

**Parameters**

$prob$	Real probability vector representing the probability distribution of $X$
$X$	Real random variable values represented by an STL-like container

**Returns**

Variance of  $X$

**6.1.3.114 x2contfrac()**

```
std::vector<int> qpp::x2contfrac (
    double x,
    idx N,
    idx cut = 1e5 ) [inline]
```

Simple continued fraction expansion.

See also

[qpp::contfrac2x\(\)](#)

#### Parameters

$x$	Real number
$N$	Maximum number of terms in the expansion
$cut$	Stop the expansion when the next term is greater than $cut$

#### Returns

Integer vector containing the simple continued fraction expansion of  $x$ . If there are  $M$  less than  $N$  terms in the expansion, a shorter vector with  $M$  components is returned.

### 6.1.4 Variable Documentation

#### 6.1.4.1 chop

```
constexpr double qpp::chop = 1e-10
```

Used in [qpp::disp\(\)](#) for setting to zero numbers that have their absolute value smaller than [qpp::chop](#).

#### 6.1.4.2 ee

```
constexpr double qpp::ee = 2.718281828459045235360287471352662497
```

Base of natural logarithm,  $e$ .

#### 6.1.4.3 eps

```
constexpr double qpp::eps = 1e-12
```

Used to decide whether a number or expression in double precision is zero or not.

Example:

```
if (std::abs(x) < qpp::eps) // x is zero
```

## 6.1.4.4 infty

```
constexpr double qpp::infty = std::numeric_limits<double>::max()
```

Used to denote infinity in double precision.

## 6.1.4.5 maxn

```
constexpr idx qpp::maxn = 64
```

Maximum number of allowed qubits/qudits (subsystems)

Used internally to allocate arrays on the stack (for performance reasons):

## 6.1.4.6 pi

```
constexpr double qpp::pi = 3.141592653589793238462643383279502884
```

$\pi$

## 6.2 qpp::exception Namespace Reference

Quantum++ exception hierarchy namespace.

### Classes

- class [CustomException](#)  
*Custom exception.*
- class [DimsInvalid](#)  
*Invalid dimension(s) exception.*
- class [DimsMismatchCvector](#)  
*Dimension(s) mismatch column vector size exception.*
- class [DimsMismatchMatrix](#)  
*Dimension(s) mismatch matrix size exception.*
- class [DimsMismatchRvector](#)  
*Dimension(s) mismatch row vector size exception.*
- class [DimsMismatchVector](#)  
*Dimension(s) mismatch vector size exception.*
- class [DimsNotEqual](#)  
*Dimensions not equal exception.*
- class [Exception](#)  
*Base class for generating Quantum++ custom exceptions.*
- class [MatrixMismatchSubsys](#)  
*Matrix mismatch subsystems exception.*
- class [MatrixNotCvector](#)

- Matrix is not a column vector exception.*

  - class [MatrixNotRvector](#)
- Matrix is not a row vector exception.*

  - class [MatrixNotSquare](#)
- Matrix is not square exception.*

  - class [MatrixNotSquareNorCvector](#)
- Matrix is not square nor column vector exception.*

  - class [MatrixNotSquareNorRvector](#)
- Matrix is not square nor row vector exception.*

  - class [MatrixNotSquareNorVector](#)
- Matrix is not square nor vector exception.*

  - class [MatrixNotVector](#)
- Matrix is not a vector exception.*

  - class [NoCodeword](#)
- Codeword does not exist exception.*

  - class [NotBipartite](#)
- Not bi-partite exception.*

  - class [NotQubitCvector](#)
- Column vector is not 2 x 1 exception.*

  - class [NotQubitMatrix](#)
- Matrix is not 2 x 2 exception.*

  - class [NotQubitRvector](#)
- Row vector is not 1 x 2 exception.*

  - class [NotQubitSubsys](#)
- Subsystems are not qubits exception.*

  - class [NotQubitVector](#)
- Vector is not 2 x 1 nor 1 x 2 exception.*

  - class [OutOfRange](#)
- Parameter out of range exception.*

  - class [PermInvalid](#)
- Invalid permutation exception.*

  - class [PermMismatchDims](#)
- Permutation mismatch dimensions exception.*

  - class [SizeMismatch](#)
- Size mismatch exception.*

  - class [SubsysMismatchDims](#)
- Subsystems mismatch dimensions exception.*

  - class [TypeMismatch](#)
- Type mismatch exception.*

  - class [UndefinedType](#)
- Not defined for this type exception.*

  - class [Unknown](#)
- Unknown exception.*

  - class [ZeroSize](#)
- Object has zero size exception.*

### 6.2.1 Detailed Description

Quantum++ exception hierarchy namespace.

## 6.3 qpp::experimental Namespace Reference

Experimental/test functions/classes, do not use or modify.

### Classes

- class [Bit\\_circuit](#)
- class [Dynamic\\_bitset](#)

### 6.3.1 Detailed Description

Experimental/test functions/classes, do not use or modify.

## 6.4 qpp::internal Namespace Reference

Internal utility functions, do not use them directly or modify them.

### Classes

- struct [Display\\_Impl\\_](#)
- class [IOManipEigen](#)
- class [IOManipPointer](#)
- class [IOManipRange](#)
- class [Singleton](#)

*Singleton* policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

### Functions

- void [n2multiidx](#) ([idx](#) n, [idx](#) numdims, const [idx](#) \*const dims, [idx](#) \*result) noexcept
- [idx](#) [multiidx2n](#) (const [idx](#) \*const midx, [idx](#) numdims, const [idx](#) \*const dims) noexcept
- template<typename Derived >  
bool [check\\_square\\_mat](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [check\\_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [check\\_rvector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [check\\_cvector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename T >  
bool [check\\_nonzero\\_size](#) (const T &x) noexcept
- template<typename T1 , typename T2 >  
bool [check\\_matching\\_sizes](#) (const T1 &lhs, const T2 &rhs) noexcept
- bool [check\\_dims](#) (const std::vector< [idx](#) > &dims)
- template<typename Derived >  
bool [check\\_dims\\_match\\_mat](#) (const std::vector< [idx](#) > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [check\\_dims\\_match\\_cvect](#) (const std::vector< [idx](#) > &dims, const Eigen::MatrixBase< Derived > &A)

- `template<typename Derived >`  
`bool check_dims_match_rvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)`
- `bool check_eq_dims (const std::vector< idx > &dims, idx dim) noexcept`
- `bool check_subsys_match_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)`
- `template<typename Derived >`  
`bool check_qubit_matrix (const Eigen::MatrixBase< Derived > &A) noexcept`
- `template<typename Derived >`  
`bool check_qubit_cvector (const Eigen::MatrixBase< Derived > &A) noexcept`
- `template<typename Derived >`  
`bool check_qubit_rvector (const Eigen::MatrixBase< Derived > &A) noexcept`
- `template<typename Derived >`  
`bool check_qubit_vector (const Eigen::MatrixBase< Derived > &A) noexcept`
- `bool check_perm (const std::vector< idx > &perm)`
- `template<typename Derived1 , typename Derived2 >`  
`dyn\_mat< typename Derived1::Scalar > kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
- `template<typename Derived1 , typename Derived2 >`  
`dyn\_mat< typename Derived1::Scalar > dirsum2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
- `template<typename T >`  
`void variadic\_vector\_emplace (std::vector< T > &)`
- `template<typename T , typename First , typename ... Args>`  
`void variadic\_vector\_emplace (std::vector< T > &v, First &&first, Args &&... args)`
- `idx\_get\_num\_subsys (idx sz, idx d)`
- `idx\_get\_dim\_subsys (idx sz, idx N)`

### 6.4.1 Detailed Description

Internal utility functions, do not use them directly or modify them.

### 6.4.2 Function Documentation

#### 6.4.2.1 `check_cvector()`

```
template<typename Derived >
bool qpp::internal::check_cvector (
    const Eigen::MatrixBase< Derived > & A )
```

#### 6.4.2.2 `check_dims()`

```
bool qpp::internal::check_dims (
    const std::vector< idx > & dims ) [inline]
```



#### 6.4.2.3 check\_dims\_match\_cvect()

```
template<typename Derived >
bool qpp::internal::check_dims_match_cvect (
    const std::vector< idx > & dims,
    const Eigen::MatrixBase< Derived > & A )
```

#### 6.4.2.4 check\_dims\_match\_mat()

```
template<typename Derived >
bool qpp::internal::check_dims_match_mat (
    const std::vector< idx > & dims,
    const Eigen::MatrixBase< Derived > & A )
```

#### 6.4.2.5 check\_dims\_match\_rvect()

```
template<typename Derived >
bool qpp::internal::check_dims_match_rvect (
    const std::vector< idx > & dims,
    const Eigen::MatrixBase< Derived > & A )
```

#### 6.4.2.6 check\_eq\_dims()

```
bool qpp::internal::check_eq_dims (
    const std::vector< idx > & dims,
    idx dim ) [inline], [noexcept]
```

#### 6.4.2.7 check\_matching\_sizes()

```
template<typename T1 , typename T2 >
bool qpp::internal::check_matching_sizes (
    const T1 & lhs,
    const T2 & rhs ) [noexcept]
```

#### 6.4.2.8 check\_nonzero\_size()

```
template<typename T >
bool qpp::internal::check_nonzero_size (
    const T & x ) [noexcept]
```

#### 6.4.2.9 check\_perm()

```
bool qpp::internal::check_perm (
    const std::vector< idx > & perm ) [inline]
```

#### 6.4.2.10 check\_qubit\_cvector()

```
template<typename Derived >
bool qpp::internal::check_qubit_cvector (
    const Eigen::MatrixBase< Derived > & A ) [noexcept]
```

#### 6.4.2.11 check\_qubit\_matrix()

```
template<typename Derived >
bool qpp::internal::check_qubit_matrix (
    const Eigen::MatrixBase< Derived > & A ) [noexcept]
```

#### 6.4.2.12 check\_qubit\_rvector()

```
template<typename Derived >
bool qpp::internal::check_qubit_rvector (
    const Eigen::MatrixBase< Derived > & A ) [noexcept]
```

#### 6.4.2.13 check\_qubit\_vector()

```
template<typename Derived >
bool qpp::internal::check_qubit_vector (
    const Eigen::MatrixBase< Derived > & A ) [noexcept]
```

#### 6.4.2.14 check\_rvector()

```
template<typename Derived >
bool qpp::internal::check_rvector (
    const Eigen::MatrixBase< Derived > & A )
```

#### 6.4.2.15 check\_square\_mat()

```
template<typename Derived >
bool qpp::internal::check_square_mat (
    const Eigen::MatrixBase< Derived > & A )
```

#### 6.4.2.16 check\_subsys\_match\_dims()

```
bool qpp::internal::check_subsys_match_dims (
    const std::vector< idx > & subsys,
    const std::vector< idx > & dims ) [inline]
```

#### 6.4.2.17 check\_vector()

```
template<typename Derived >
bool qpp::internal::check_vector (
    const Eigen::MatrixBase< Derived > & A )
```

#### 6.4.2.18 dirsum2()

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::internal::dirsum2 (
    const Eigen::MatrixBase< Derived1 > & A,
    const Eigen::MatrixBase< Derived2 > & B )
```

#### 6.4.2.19 get\_dim\_subsys()

```
idx qpp::internal::get_dim_subsys (
    idx sz,
    idx N ) [inline]
```

#### 6.4.2.20 get\_num\_subsys()

```
idx qpp::internal::get_num_subsys (
    idx sz,
    idx d ) [inline]
```

**6.4.2.21 kron2()**

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::internal::kron2 (
    const Eigen::MatrixBase< Derived1 > & A,
    const Eigen::MatrixBase< Derived2 > & B )
```

**6.4.2.22 multiidx2n()**

```
idx qpp::internal::multiidx2n (
    const idx *const midx,
    idx numdims,
    const idx *const dims ) [inline], [noexcept]
```

**6.4.2.23 n2multiidx()**

```
void qpp::internal::n2multiidx (
    idx n,
    idx numdims,
    const idx *const dims,
    idx * result ) [inline], [noexcept]
```

**6.4.2.24 variadic\_vector\_emplace()** [1/2]

```
template<typename T >
void qpp::internal::variadic_vector_emplace (
    std::vector< T > & )
```

**6.4.2.25 variadic\_vector\_emplace()** [2/2]

```
template<typename T , typename First , typename ... Args>
void qpp::internal::variadic_vector_emplace (
    std::vector< T > & v,
    First && first,
    Args &&... args )
```

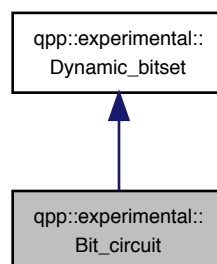
## Chapter 7

# Class Documentation

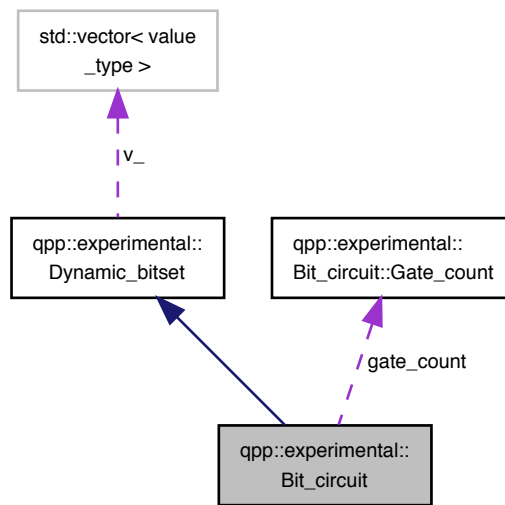
### 7.1 qpp::experimental::Bit\_circuit Class Reference

```
#include <experimental/experimental.h>
```

Inheritance diagram for qpp::experimental::Bit\_circuit:



Collaboration diagram for `qpp::experimental::Bit_circuit`:



## Classes

- struct [Gate\\_count](#)

## Public Member Functions

- [Bit\\_circuit](#) & [X](#) ([idx](#) pos)
- [Bit\\_circuit](#) & [NOT](#) ([idx](#) pos)
- [Bit\\_circuit](#) & [CNOT](#) (const std::vector< [idx](#) > &pos)
- [Bit\\_circuit](#) & [TOF](#) (const std::vector< [idx](#) > &pos)
- [Bit\\_circuit](#) & [SWAP](#) (const std::vector< [idx](#) > &pos)
- [Bit\\_circuit](#) & [FRED](#) (const std::vector< [idx](#) > &pos)
- [Bit\\_circuit](#) & [reset](#) () noexcept

## Public Attributes

- struct [qpp::experimental::Bit\\_circuit::Gate\\_count](#) [gate\\_count](#)

## Additional Inherited Members

### 7.1.1 Member Function Documentation

#### 7.1.1.1 CNOT()

```
Bit_circuit& qpp::experimental::Bit_circuit::CNOT (
    const std::vector< idx > & pos ) [inline]
```

#### 7.1.1.2 FRED()

```
Bit_circuit& qpp::experimental::Bit_circuit::FRED (
    const std::vector< idx > & pos ) [inline]
```

#### 7.1.1.3 NOT()

```
Bit_circuit& qpp::experimental::Bit_circuit::NOT (
    idx pos ) [inline]
```

#### 7.1.1.4 reset()

```
Bit_circuit& qpp::experimental::Bit_circuit::reset ( ) [inline], [noexcept]
```

#### 7.1.1.5 SWAP()

```
Bit_circuit& qpp::experimental::Bit_circuit::SWAP (
    const std::vector< idx > & pos ) [inline]
```

#### 7.1.1.6 TOF()

```
Bit_circuit& qpp::experimental::Bit_circuit::TOF (
    const std::vector< idx > & pos ) [inline]
```

#### 7.1.1.7 X()

```
Bit_circuit& qpp::experimental::Bit_circuit::X (
    idx pos ) [inline]
```

## 7.1.2 Member Data Documentation

### 7.1.2.1 gate\_count

```
struct qpp::experimental::Bit_circuit::Gate_count qpp::experimental::Bit_circuit::gate_count
```

The documentation for this class was generated from the following file:

- experimental/[experimental.h](#)

## 7.2 qpp::Bit\_circuit Class Reference

Classical reversible circuit simulator.

```
#include <experimental/experimental.h>
```

### 7.2.1 Detailed Description

Classical reversible circuit simulator.

The documentation for this class was generated from the following file:

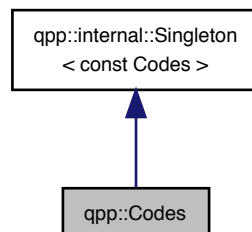
- experimental/[experimental.h](#)

## 7.3 qpp::Codes Class Reference

const Singleton class that defines quantum error correcting codes

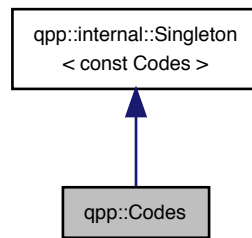
```
#include <classes/codes.h>
```

Inheritance diagram for qpp::Codes:





Collaboration diagram for qpp::Codes:



## Public Types

- enum `Type` { `Type::FIVE_QUBIT` = 1, `Type::SEVEN_QUBIT_STEANE`, `Type::NINE_QUBIT_SHOR` }  
Code types, add more codes here if needed.

## Public Member Functions

- `ket codeword` (`Type` type, `idx` i) const  
Returns the codeword of the specified code type.

## Private Member Functions

- `Codes` ()  
Default constructor.
- `~Codes` ()=default  
Default destructor.

## Friends

- class `internal::Singleton< const Codes >`

## Additional Inherited Members

### 7.3.1 Detailed Description

const Singleton class that defines quantum error correcting codes

### 7.3.2 Member Enumeration Documentation

### 7.3.2.1 Type

```
enum qpp::Codes::Type [strong]
```

Code types, add more codes here if needed.

See also

[qpp::Codes::codeword\(\)](#)

#### Enumerator

FIVE_QUBIT	[[5,1,3]] qubit code
SEVEN_QUBIT_STEANE	[[7,1,3]] Steane qubit code
NINE_QUBIT_SHOR	[[9,1,3]] Shor qubit code

## 7.3.3 Constructor & Destructor Documentation

### 7.3.3.1 Codes()

```
qpp::Codes::Codes ( ) [inline], [private]
```

Default constructor.

### 7.3.3.2 ~Codes()

```
qpp::Codes::~~Codes ( ) [private], [default]
```

Default destructor.

## 7.3.4 Member Function Documentation

### 7.3.4.1 codeword()

```
ket qpp::Codes::codeword (
    Type type,
    idx i ) const [inline]
```

Returns the codeword of the specified code type.

See also

[qpp::Codes::Type](#)

## Parameters

<i>type</i>	Code type
<i>i</i>	Codeword index

## Returns

*i*-th codeword of the code *type*

## 7.3.5 Friends And Related Function Documentation

## 7.3.5.1 internal::Singleton&lt; const Codes &gt;

```
friend class internal::Singleton< const Codes > [friend]
```

The documentation for this class was generated from the following file:

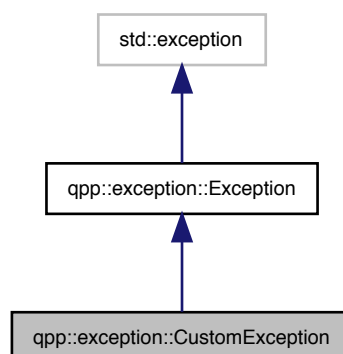
- [classes/codes.h](#)

## 7.4 qpp::exception::CustomException Class Reference

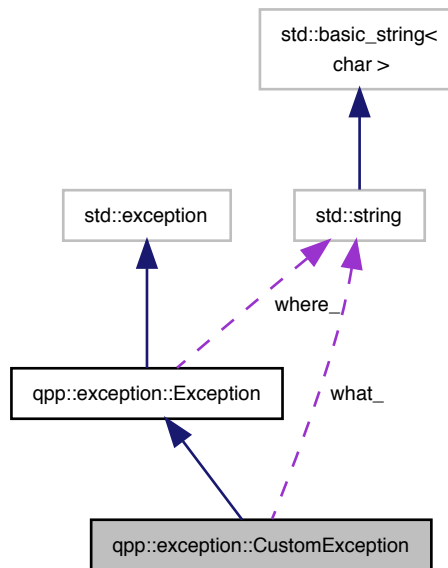
Custom exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::CustomException:



Collaboration diagram for `qpp::exception::CustomException`:



## Public Member Functions

- [CustomException](#) (const std::string &where, const std::string &[what](#))

## Private Member Functions

- std::string [type\\_description](#) () const override  
*[Exception](#) type description.*

## Private Attributes

- std::string [what\\_](#) {}

### 7.4.1 Detailed Description

Custom exception.

Custom exception, the user must provide a custom message

### 7.4.2 Constructor & Destructor Documentation

#### 7.4.2.1 CustomException()

```
qpp::exception::CustomException::CustomException (
    const std::string & where,
    const std::string & what ) [inline]
```

### 7.4.3 Member Function Documentation

#### 7.4.3.1 type\_description()

```
std::string qpp::exception::CustomException::type_description( ) const [inline], [override],
[private], [virtual]
```

[Exception](#) type description.

#### Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

### 7.4.4 Member Data Documentation

#### 7.4.4.1 what\_

```
std::string qpp::exception::CustomException::what_ {} [private]
```

The documentation for this class was generated from the following file:

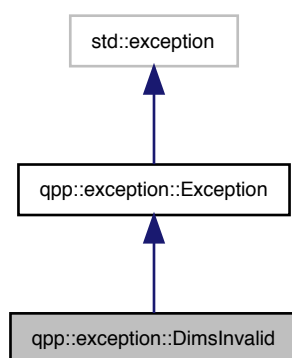
- [classes/exception.h](#)

## 7.5 qpp::exception::DimsInvalid Class Reference

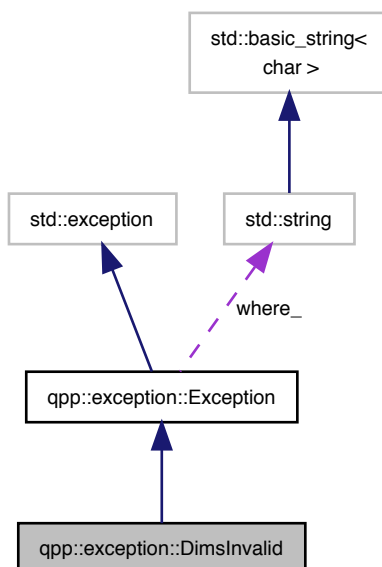
Invalid dimension(s) exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsInvalid:



Collaboration diagram for qpp::exception::DimsInvalid:



## Public Member Functions

- `std::string type_description ()` const override  
*Exception type description.*

### 7.5.1 Detailed Description

Invalid dimension(s) exception.

`std::vector<idx>` of dimensions has zero size or contains zeros

### 7.5.2 Member Function Documentation

#### 7.5.2.1 type\_description()

```
std::string qpp::exception::DimsInvalid::type_description ( ) const [inline], [override],  
[virtual]
```

*Exception* type description.

#### Returns

*Exception* type description

Implements `qpp::exception::Exception`.

The documentation for this class was generated from the following file:

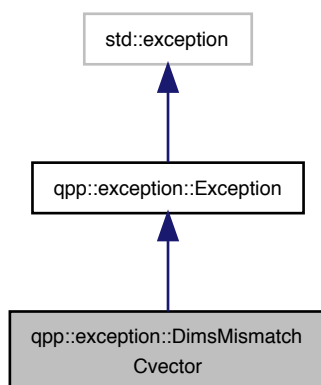
- `classes/exception.h`

## 7.6 qpp::exception::DimsMismatchCvector Class Reference

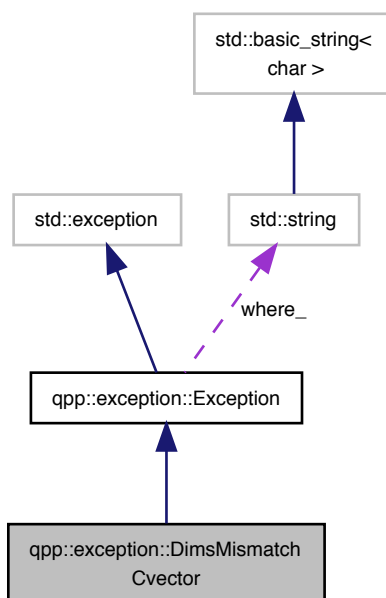
Dimension(s) mismatch column vector size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsMismatchCvector:



Collaboration diagram for qpp::exception::DimsMismatchCvector:



## Public Member Functions

- `std::string type\_description () const` override  
*[Exception](#) type description.*



### 7.6.1 Detailed Description

Dimension(s) mismatch column vector size exception.

Product of the elements of `std::vector<idx>` of dimensions is not equal to the number of elements of the `Eigen::Matrix` (assumed to be a column vector)

### 7.6.2 Member Function Documentation

#### 7.6.2.1 type\_description()

```
std::string qpp::exception::DimsMismatchCvector::type_description ( ) const [inline], [override], [virtual]
```

[Exception](#) type description.

#### Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

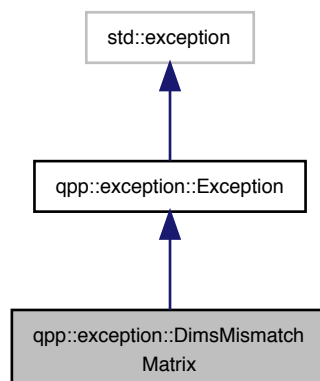
- [classes/exception.h](#)

## 7.7 qpp::exception::DimsMismatchMatrix Class Reference

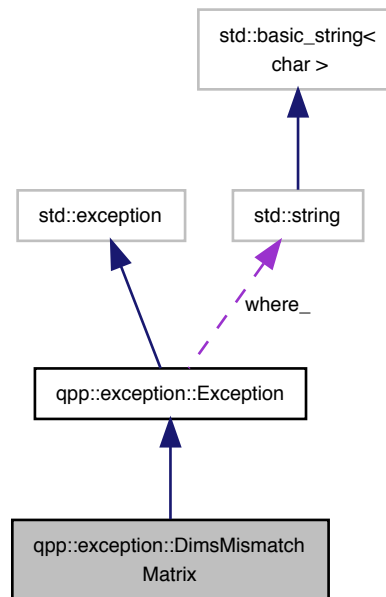
Dimension(s) mismatch matrix size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for `qpp::exception::DimsMismatchMatrix`:



Collaboration diagram for `qpp::exception::DimsMismatchMatrix`:



## Public Member Functions

- `std::string type_description ()` const override  
*Exception type description.*

### 7.7.1 Detailed Description

Dimension(s) mismatch matrix size exception.

Product of the elements of `std::vector<idx>` of dimensions is not equal to the number of rows of the `Eigen::Matrix` (assumed to be a square matrix)

### 7.7.2 Member Function Documentation

## 7.7.2.1 type\_description()

```
std::string qpp::exception::DimsMismatchMatrix::type_description ( ) const [inline], [override],  
[virtual]
```

Exception type description.

## Returns

Exception type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

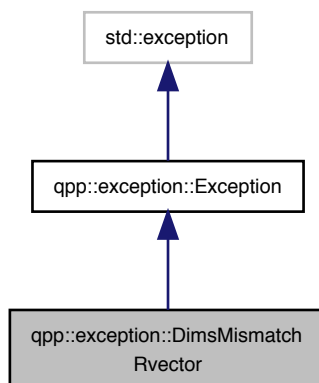
- [classes/exception.h](#)

## 7.8 qpp::exception::DimsMismatchRvector Class Reference

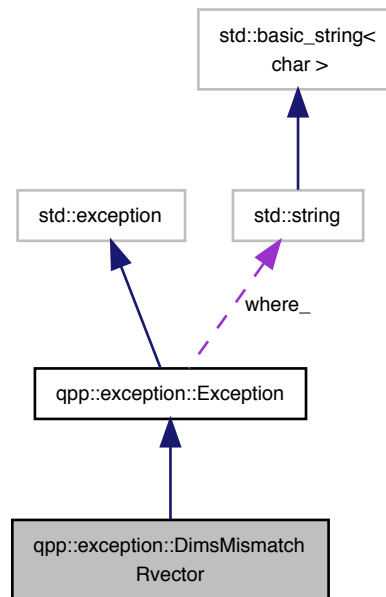
Dimension(s) mismatch row vector size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsMismatchRvector:



Collaboration diagram for `qpp::exception::DimsMismatchRvector`:



## Public Member Functions

- `std::string type_description ()` const override  
*Exception type description.*

### 7.8.1 Detailed Description

Dimension(s) mismatch row vector size exception.

Product of the elements of `std::vector<idx>` of dimensions is not equal to the number of elements of the Eigen::↵ Matrix (assumed to be a row vector)

### 7.8.2 Member Function Documentation

### 7.8.2.1 type\_description()

```
std::string qpp::exception::DimsMismatchRvector::type_description ( ) const [inline], [override],  
[virtual]
```

[Exception](#) type description.

#### Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

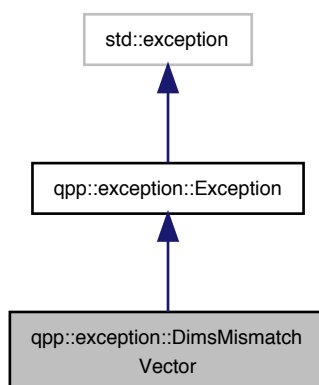
- [classes/exception.h](#)

## 7.9 qpp::exception::DimsMismatchVector Class Reference

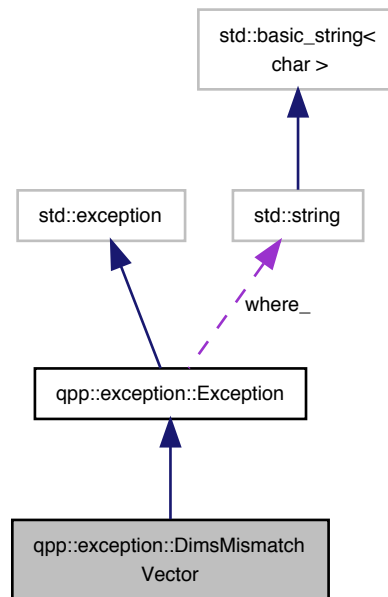
Dimension(s) mismatch vector size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsMismatchVector:



Collaboration diagram for `qpp::exception::DimsMismatchVector`:



## Public Member Functions

- `std::string type_description ()` const override  
*Exception type description.*

### 7.9.1 Detailed Description

Dimension(s) mismatch vector size exception.

Product of the elements of `std::vector<idx>` of dimensions is not equal to the number of elements of the Eigen::↵ Matrix (assumed to be a row/column vector)

### 7.9.2 Member Function Documentation

## 7.9.2.1 type\_description()

```
std::string qpp::exception::DimsMismatchVector::type_description ( ) const [inline], [override],  
[virtual]
```

Exception type description.

## Returns

Exception type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

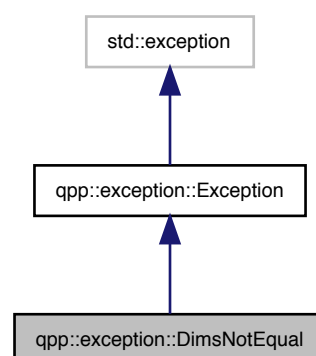
- [classes/exception.h](#)

## 7.10 qpp::exception::DimsNotEqual Class Reference

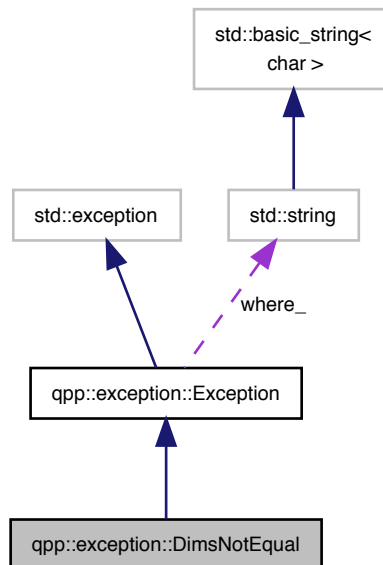
Dimensions not equal exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::DimsNotEqual:



Collaboration diagram for `qpp::exception::DimsNotEqual`:



## Public Member Functions

- `std::string type_description ()` const override  
*Exception type description.*

### 7.10.1 Detailed Description

Dimensions not equal exception.

Local/global dimensions are not equal

### 7.10.2 Member Function Documentation

#### 7.10.2.1 type\_description()

```
std::string qpp::exception::DimsNotEqual::type_description ( ) const [inline], [override],
[virtual]
```

*Exception type description.*

#### Returns

*Exception type description*

Implements `qpp::exception::Exception`.

The documentation for this class was generated from the following file:

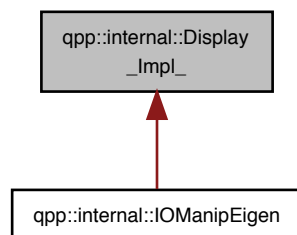
- `classes/exception.h`



## 7.11 qpp::internal::Display\_Impl\_ Struct Reference

```
#include <internal/util.h>
```

Inheritance diagram for qpp::internal::Display\_Impl\_:



### Public Member Functions

- `template<typename T >`  
`std::ostream & display\_impl\_ (const T &A, std::ostream &os, double chop=qpp::chop) const`

### 7.11.1 Member Function Documentation

#### 7.11.1.1 `display_impl_()`

```
template<typename T >
std::ostream& qpp::internal::Display_Impl_::display_impl_ (
    const T & A,
    std::ostream & os,
    double chop = qpp::chop ) const [inline]
```

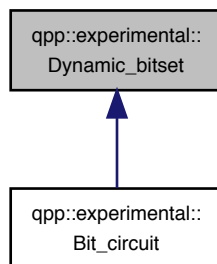
The documentation for this struct was generated from the following file:

- [internal/util.h](#)

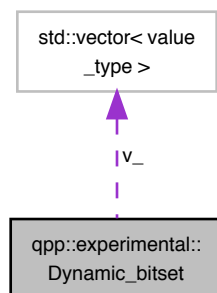
## 7.12 qpp::experimental::Dynamic\_bitset Class Reference

```
#include <experimental/experimental.h>
```

Inheritance diagram for qpp::experimental::Dynamic\_bitset:



Collaboration diagram for qpp::experimental::Dynamic\_bitset:



### Public Types

- using `value_type` = unsigned int  
*Type of the storage elements.*
- using `storage_type` = std::vector< `value_type` >  
*Type of the storage.*

## Public Member Functions

- [Dynamic\\_bitset](#) (idx N)  
*Constructor, initializes all bits to false (zero)*
- const [storage\\_type](#) & [data](#) () const  
*Raw storage space of the bitset.*
- [idx size](#) () const  
*Number of bits stored in the bitset.*
- [idx storage\\_size](#) () const  
*Size of the underlying storage space (in units of value\_type, unsigned int by default)*
- [idx count](#) () const noexcept
- bool [get](#) (idx pos) const
- bool [none](#) () const noexcept
- bool [all](#) () const noexcept
- bool [any](#) () const noexcept
- [Dynamic\\_bitset](#) & [set](#) (idx pos, bool value=true)
- [Dynamic\\_bitset](#) & [set](#) () noexcept
- [Dynamic\\_bitset](#) & [rand](#) (idx pos, double p=0.5)
- [Dynamic\\_bitset](#) & [rand](#) (double p=0.5)
- [Dynamic\\_bitset](#) & [reset](#) (idx pos)
- [Dynamic\\_bitset](#) & [reset](#) () noexcept
- [Dynamic\\_bitset](#) & [flip](#) (idx pos)
- [Dynamic\\_bitset](#) & [flip](#) () noexcept
- bool [operator==](#) (const [Dynamic\\_bitset](#) &rhs) const noexcept
- bool [operator!=](#) (const [Dynamic\\_bitset](#) &rhs) const noexcept
- template<class CharT = char, class Traits = std::char\_traits<CharT>, class Allocator = std::allocator<CharT>>  
std::basic\_string< CharT, Traits, Allocator > [to\\_string](#) (CharT zero=CharT('0'), CharT one=CharT('1')) const

## Protected Member Functions

- [idx index\\_](#) (idx pos) const  
*Index of the pos bit in the storage space.*
- [idx offset\\_](#) (idx pos) const  
*Offset of the pos bit in the storage space relative to its index.*

## Protected Attributes

- [idx storage\\_size\\_](#)  
*Storage size.*
- [idx N\\_](#)  
*Number of bits.*
- std::vector< [value\\_type](#) > [v\\_](#)  
*Storage space.*

## Friends

- std::ostream & [operator<<](#) (std::ostream &os, const [Dynamic\\_bitset](#) &rhs)

## 7.12.1 Member Typedef Documentation

### 7.12.1.1 storage\_type

```
using qpp::experimental::Dynamic_bitset::storage_type = std::vector<value_type>
```

Type of the storage.

### 7.12.1.2 value\_type

```
using qpp::experimental::Dynamic_bitset::value_type = unsigned int
```

Type of the storage elements.

## 7.12.2 Constructor & Destructor Documentation

### 7.12.2.1 Dynamic\_bitset()

```
qpp::experimental::Dynamic_bitset::Dynamic_bitset (  
    idx N ) [inline]
```

Constructor, initializes all bits to false (zero)

#### Parameters

$N$	Number of bits in the bitset
-----	------------------------------

## 7.12.3 Member Function Documentation

### 7.12.3.1 all()

```
bool qpp::experimental::Dynamic_bitset::all ( ) const [inline], [noexcept]
```

#### Returns

### 7.12.3.2 any()

```
bool qpp::experimental::Dynamic_bitset::any ( ) const [inline], [noexcept]
```

Returns

### 7.12.3.3 count()

```
idx qpp::experimental::Dynamic_bitset::count ( ) const [inline], [noexcept]
```

Returns

### 7.12.3.4 data()

```
const storage_type& qpp::experimental::Dynamic_bitset::data ( ) const [inline]
```

Raw storage space of the bitset.

Returns

Const reference to the underlying storage space

### 7.12.3.5 flip() [1/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::flip (
    idx pos ) [inline]
```

Parameters

<i>pos</i>	
------------	--

Returns

### 7.12.3.6 flip() [2/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::flip ( ) [inline], [noexcept]
```

#### Returns

### 7.12.3.7 get()

```
bool qpp::experimental::Dynamic_bitset::get (
    idx pos ) const [inline]
```

#### Parameters

<i>pos</i>	
------------	--

#### Returns

### 7.12.3.8 index\_()

```
idx qpp::experimental::Dynamic_bitset::index_ (
    idx pos ) const [inline], [protected]
```

Index of the *pos* bit in the storage space.

#### Parameters

<i>pos</i>	Bit location
------------	--------------

#### Returns

Index of the *pos* bit in the storage space

### 7.12.3.9 none()

```
bool qpp::experimental::Dynamic_bitset::none ( ) const [inline], [noexcept]
```

#### Returns

### 7.12.3.10 offset\_()

```
idx qpp::experimental::Dynamic_bitset::offset_ (
    idx pos ) const [inline], [protected]
```

Offset of the *pos* bit in the storage space relative to its index.

#### Parameters

<i>pos</i>	Bit location
------------	--------------

#### Returns

Offset of the *pos* bit in the storage space relative to its index

### 7.12.3.11 operator!=(())

```
bool qpp::experimental::Dynamic_bitset::operator!= (
    const Dynamic_bitset & rhs ) const [inline], [noexcept]
```

#### Parameters

<i>rhs</i>	
------------	--

#### Returns

### 7.12.3.12 operator==(())

```
bool qpp::experimental::Dynamic_bitset::operator== (
    const Dynamic_bitset & rhs ) const [inline], [noexcept]
```

#### Parameters

<i>rhs</i>	
------------	--

#### Returns

#### 7.12.3.13 rand() [1/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::rand (
    idx pos,
    double p = 0.5 ) [inline]
```

##### Parameters

<i>pos</i>	
<i>p</i>	

##### Returns

#### 7.12.3.14 rand() [2/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::rand (
    double p = 0.5 ) [inline]
```

##### Parameters

<i>p</i>	
----------	--

##### Returns

#### 7.12.3.15 reset() [1/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::reset (
    idx pos ) [inline]
```

##### Parameters

<i>pos</i>	
------------	--

##### Returns



### 7.12.3.16 reset() [2/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::reset ( ) [inline], [noexcept]
```

Returns

### 7.12.3.17 set() [1/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::set (
    idx pos,
    bool value = true ) [inline]
```

Parameters

<i>pos</i>	
<i>value</i>	

Returns

### 7.12.3.18 set() [2/2]

```
Dynamic_bitset& qpp::experimental::Dynamic_bitset::set ( ) [inline], [noexcept]
```

Returns

### 7.12.3.19 size()

```
idx qpp::experimental::Dynamic_bitset::size ( ) const [inline]
```

Number of bits stored in the bitset.

Returns

Number of bits

### 7.12.3.20 storage\_size()

```
idx qpp::experimental::Dynamic_bitset::storage_size ( ) const [inline]
```

Size of the underlying storage space (in units of value\_type, unsigned int by default)

#### Returns

Size of the underlying storage space

### 7.12.3.21 to\_string()

```
template<class CharT = char, class Traits = std::char_traits<CharT>, class Allocator = std::
::allocator<CharT>>
std::basic_string<CharT, Traits, Allocator> qpp::experimental::Dynamic_bitset::to_string (
    CharT zero = CharT('0'),
    CharT one = CharT('1') ) const [inline]
```

#### Template Parameters

<i>CharT</i>	
<i>Traits</i>	
<i>Allocator</i>	

#### Parameters

<i>zero</i>	
<i>one</i>	

#### Returns

## 7.12.4 Friends And Related Function Documentation

### 7.12.4.1 operator<<

```
std::ostream& operator<< (
    std::ostream & os,
    const Dynamic_bitset & rhs ) [friend]
```

#### Parameters

<i>os</i>	
<i>rhs</i>	

Returns

## 7.12.5 Member Data Documentation

### 7.12.5.1 N\_

`idx` qpp::experimental::Dynamic\_bitset::N\_ [protected]

Number of bits.

### 7.12.5.2 storage\_size\_

`idx` qpp::experimental::Dynamic\_bitset::storage\_size\_ [protected]

Storage size.

### 7.12.5.3 v\_

`std::vector<value_type>` qpp::experimental::Dynamic\_bitset::v\_ [protected]

Storage space.

The documentation for this class was generated from the following file:

- experimental/[experimental.h](#)

## 7.13 qpp::Dynamic\_bitset Class Reference

Dynamic bitset class, allows the specification of the number of bits at runtime (unlike `std::bitset<N>`)

```
#include <experimental/experimental.h>
```

### 7.13.1 Detailed Description

Dynamic bitset class, allows the specification of the number of bits at runtime (unlike `std::bitset<N>`)

The documentation for this class was generated from the following file:

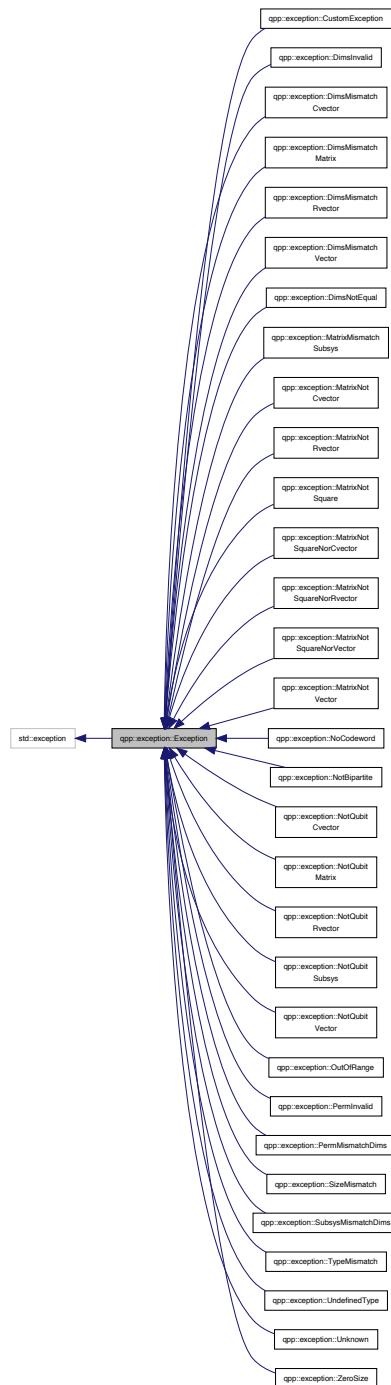
- experimental/[experimental.h](#)

## 7.14 qpp::exception::Exception Class Reference

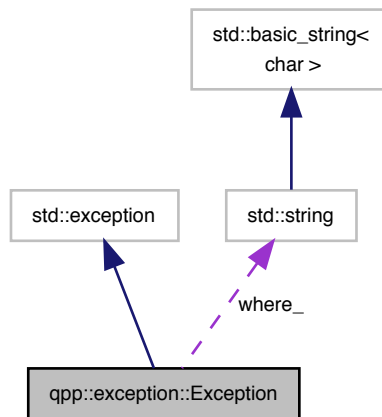
Base class for generating Quantum++ custom exceptions.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::Exception:



Collaboration diagram for qpp::exception::Exception:



## Public Member Functions

- [Exception](#) (const std::string &where)  
*Constructs an exception.*
- virtual const char \* [what](#) () const noexcept override  
*Overrides std::exception::what()*
- virtual std::string [type\\_description](#) () const =0  
*Exception type description.*

## Private Attributes

- std::string [where\\_](#)

### 7.14.1 Detailed Description

Base class for generating Quantum++ custom exceptions.

Derive from this class if more exceptions are needed, making sure to override [qpp::exception::Exception::type\\_description\(\)](#) in the derived class and to inherit the constructor [qpp::exception::Exception::Exception\(\)](#). Preferably keep your newly defined exception classes in the namespace [qpp::exception](#).

Example:

```

namespace qpp
{
namespace exception
{
    class ZeroSize : public Exception
    {
    public:
        std::string type_description() const override
        {
            return "Object has zero size";
        }

        // inherit the base class' qpp::exception::Exception constructor
        using Exception::Exception;
    };
} // namespace exception
} // namespace qpp
  
```

## 7.14.2 Constructor & Destructor Documentation

### 7.14.2.1 Exception()

```
qpp::exception::Exception::Exception (
    const std::string & where ) [inline]
```

Constructs an exception.

#### Parameters

<i>where</i>	Text representing where the exception occurred
--------------	--

## 7.14.3 Member Function Documentation

### 7.14.3.1 type\_description()

```
std::string qpp::exception::Exception::type_description ( ) const [inline], [pure virtual]
```

[Exception](#) type description.

#### Returns

[Exception](#) type description

Implemented in [qpp::exception::CustomException](#), [qpp::exception::UndefinedType](#), [qpp::exception::SizeMismatch](#), [qpp::exception::TypeMismatch](#), [qpp::exception::OutOfRange](#), [qpp::exception::NoCodeword](#), [qpp::exception::NotBipartite](#), [qpp::exception::NotQubitSubsys](#), [qpp::exception::NotQubitVector](#), [qpp::exception::NotQubitRvector](#), [qpp::exception::NotQubitCvector](#), [qpp::exception::NotQubitMatrix](#), [qpp::exception::PermMismatchDims](#), [qpp::exception::PermInvalid](#), [qpp::exception::SubsysMismatchDims](#), [qpp::exception::DimsMismatchVector](#), [qpp::exception::DimsMismatchRvector](#), [qpp::exception::DimsMismatchCvector](#), [qpp::exception::DimsMismatchMatrix](#), [qpp::exception::DimsNotEqual](#), [qpp::exception::DimsInvalid](#), [qpp::exception::MatrixMismatchSubsys](#), [qpp::exception::MatrixNotSquareNorVector](#), [qpp::exception::MatrixNotSquareNorRvector](#), [qpp::exception::MatrixNotSquareNorCvector](#), [qpp::exception::MatrixNotVector](#), [qpp::exception::MatrixNotRvector](#), [qpp::exception::MatrixNotCvector](#), [qpp::exception::MatrixNotSquare](#), [qpp::exception::ZeroSize](#), and [qpp::exception::Unknown](#).

### 7.14.3.2 what()

```
virtual const char* qpp::exception::Exception::what ( ) const [inline], [override], [virtual],
[noexcept]
```

Overrides `std::exception::what()`

#### Returns

[Exception](#) description

### 7.14.4 Member Data Documentation

#### 7.14.4.1 where\_

```
std::string qpp::exception::Exception::where_ [private]
```

The documentation for this class was generated from the following file:

- classes/[exception.h](#)

## 7.15 qpp::experimental::Bit\_circuit::Gate\_count Struct Reference

```
#include <experimental/experimental.h>
```

### Public Attributes

- [idx NOT](#) = 0
- [idx & X](#) = [NOT](#)
- [idx CNOT](#) = 0
- [idx SWAP](#) = 0
- [idx FRED](#) = 0
- [idx TOF](#) = 0

### 7.15.1 Member Data Documentation

#### 7.15.1.1 CNOT

```
idx qpp::experimental::Bit_circuit::Gate_count::CNOT = 0
```

#### 7.15.1.2 FRED

```
idx qpp::experimental::Bit_circuit::Gate_count::FRED = 0
```

### 7.15.1.3 NOT

```
idx qpp::experimental::Bit_circuit::Gate_count::NOT = 0
```

### 7.15.1.4 SWAP

```
idx qpp::experimental::Bit_circuit::Gate_count::SWAP = 0
```

### 7.15.1.5 TOF

```
idx qpp::experimental::Bit_circuit::Gate_count::TOF = 0
```

### 7.15.1.6 X

```
idx& qpp::experimental::Bit_circuit::Gate_count::X = NOT
```

The documentation for this struct was generated from the following file:

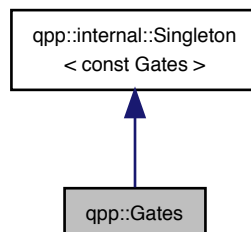
- experimental/[experimental.h](#)

## 7.16 qpp::Gates Class Reference

const Singleton class that implements most commonly used gates

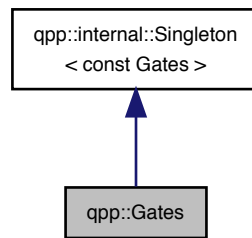
```
#include <classes/gates.h>
```

Inheritance diagram for qpp::Gates:





Collaboration diagram for qpp::Gates:



## Public Member Functions

- **cmat Rn** (double theta, const std::vector< double > &n) const  
*Qubit rotation of theta about the 3-dimensional real (unit) vector n.*
- **cmat Zd** (idx D=2) const  
*Generalized Z gate for qudits.*
- **cmat Fd** (idx D=2) const  
*Fourier transform gate for qudits.*
- **cmat Xd** (idx D=2) const  
*Generalized X gate for qudits.*
- template<typename Derived = Eigen::MatrixXcd>  
Derived **Id** (idx D=2) const  
*Identity gate.*
- template<typename Derived >  
**dyn\_mat**< typename Derived::Scalar > **CTRL** (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx N, idx d=2) const  
*Generates the multi-partite multiple-controlled-A gate in matrix form.*
- template<typename Derived >  
**dyn\_mat**< typename Derived::Scalar > **expandout** (const Eigen::MatrixBase< Derived > &A, idx pos, const std::vector< idx > &dims) const  
*Expands out.*
- template<typename Derived >  
**dyn\_mat**< typename Derived::Scalar > **expandout** (const Eigen::MatrixBase< Derived > &A, idx pos, const std::initializer\_list< idx > &dims) const  
*Expands out.*
- template<typename Derived >  
**dyn\_mat**< typename Derived::Scalar > **expandout** (const Eigen::MatrixBase< Derived > &A, idx pos, idx N, idx d=2) const  
*Expands out.*

## Public Attributes

- **cmat Id2** {cmat::Identity(2, 2)}  
*Identity gate.*
- **cmat H** {cmat::Zero(2, 2)}

- Hadamard gate.*
- [cmat X](#) {cmat::Zero(2, 2)}
- Pauli Sigma-X gate.*
- [cmat Y](#) {cmat::Zero(2, 2)}
- Pauli Sigma-Y gate.*
- [cmat Z](#) {cmat::Zero(2, 2)}
- Pauli Sigma-Z gate.*
- [cmat S](#) {cmat::Zero(2, 2)}
- S gate.*
- [cmat T](#) {cmat::Zero(2, 2)}
- T gate.*
- [cmat CNOT](#) {cmat::Identity(4, 4)}
- Controlled-NOT control target gate.*
- [cmat CZ](#) {cmat::Identity(4, 4)}
- Controlled-Phase gate.*
- [cmat CNOTba](#) {cmat::Zero(4, 4)}
- Controlled-NOT target control gate.*
- [cmat SWAP](#) {cmat::Identity(4, 4)}
- SWAP gate.*
- [cmat TOF](#) {cmat::Identity(8, 8)}
- Toffoli gate.*
- [cmat FRED](#) {cmat::Identity(8, 8)}
- Fredkin gate.*

## Private Member Functions

- [Gates](#) ()
- Initializes the gates.*
- [~Gates](#) ()=default
- Default destructor.*

## Friends

- class [internal::Singleton](#)< const [Gates](#) >

## Additional Inherited Members

### 7.16.1 Detailed Description

const Singleton class that implements most commonly used gates

### 7.16.2 Constructor & Destructor Documentation

## 7.16.2.1 Gates()

```
qpp::Gates::Gates ( ) [inline], [private]
```

Initializes the gates.

## 7.16.2.2 ~Gates()

```
qpp::Gates::~~Gates ( ) [private], [default]
```

Default destructor.

## 7.16.3 Member Function Documentation

## 7.16.3.1 CTRL()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::CTRL (
    const Eigen::MatrixBase< Derived > & A,
    const std::vector< idx > & ctrl,
    const std::vector< idx > & subsys,
    idx N,
    idx d = 2 ) const [inline]
```

Generates the multi-partite multiple-controlled- $A$  gate in matrix form.

See also

[qpp::applyCTRL\(\)](#)

Note

The dimension of the gate  $A$  must match the dimension of *subsys*

## Parameters

$A$	Eigen expression
<i>ctrl</i>	Control subsystem indexes
<i>subsys</i>	Subsystem indexes where the gate $A$ is applied
$N$	Total number of subsystems
$d$	Subsystem dimensions

**Returns**

CTRL-A gate, as a matrix over the same scalar field as  $A$

**7.16.3.2 expandout()** [1/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
    const Eigen::MatrixBase< Derived > & A,
    idx pos,
    const std::vector< idx > & dims ) const [inline]
```

Expands out.

**See also**

qpp::kron()

Expands out  $A$  as a matrix in a multi-partite system. Faster than using `qpp::kron(I, I, ..., I, A, I, ..., I)`.

**Parameters**

$A$	Eigen expression
$pos$	Position
$dims$	Dimensions of the multi-partite system

**Returns**

Tensor product  $I \otimes \dots \otimes I \otimes A \otimes I \otimes \dots \otimes I$ , with  $A$  on position  $pos$ , as a dynamic matrix over the same scalar field as  $A$

**7.16.3.3 expandout()** [2/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
    const Eigen::MatrixBase< Derived > & A,
    idx pos,
    const std::initializer_list< idx > & dims ) const [inline]
```

Expands out.

**See also**

qpp::kron()

Expands out  $A$  as a matrix in a multi-partite system. Faster than using `qpp::kron(I, I, ..., I, A, I, ..., I)`.

**Note**

The `std::initializer_list` overload exists because otherwise, in the degenerate case when  $dims$  has only one element, the one element list is implicitly converted to the element's underlying type, i.e. `qpp::idx`, which has the net effect of picking the wrong (non-vector) `qpp::expandout()` overload

## Parameters

<i>A</i>	Eigen expression
<i>pos</i>	Position
<i>dims</i>	Dimensions of the multi-partite system

## Returns

Tensor product  $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$ , with  $A$  on position  $pos$ , as a dynamic matrix over the same scalar field as  $A$

## 7.16.3.4 expandout() [3/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
    const Eigen::MatrixBase< Derived > & A,
    idx pos,
    idx N,
    idx d = 2 ) const [inline]
```

Expands out.

## See also

qpp::kron()

Expands out  $A$  as a matrix in a multi-partite system. Faster than using `qpp::kron(I, I, ..., I, A, I, ..., I)`.

## Parameters

<i>A</i>	Eigen expression
<i>pos</i>	Position
<i>N</i>	Number of subsystems
<i>d</i>	Subsystem dimension

## Returns

Tensor product  $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$ , with  $A$  on position  $pos$ , as a dynamic matrix over the same scalar field as  $A$

## 7.16.3.5 Fd()

```
cmat qpp::Gates::Fd (
    idx D = 2 ) const [inline]
```

Fourier transform gate for qudits.

**Note**

Defined as  $F = \sum_{j,k=0}^{D-1} \exp(2\pi i j k / D) |j\rangle \langle k|$

**Parameters**

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

**Returns**

Fourier transform gate for qudits

**7.16.3.6 Id()**

```
template<typename Derived = Eigen::MatrixXcd>
Derived qpp::Gates::Id (
    idx D = 2 ) const [inline]
```

Identity gate.

**Note**

Can change the return type from complex matrix (default) by explicitly specifying the template parameter

**Parameters**

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

**Returns**

Identity gate on a Hilbert space of dimension *D*

**7.16.3.7 Rn()**

```
cmat qpp::Gates::Rn (
    double theta,
    const std::vector< double > & n ) const [inline]
```

Qubit rotation of *theta* about the 3-dimensional real (unit) vector *n*.

**Parameters**

<i>theta</i>	Rotation angle
<i>n</i>	3-dimensional real (unit) vector

## Returns

Rotation gate

## 7.16.3.8 Xd()

```
cmat qpp::Gates::Xd (
    idx D = 2 ) const [inline]
```

Generalized X gate for qudits.

## Note

Defined as  $X = \sum_{j=0}^{D-1} |j \oplus 1\rangle\langle j|$ , i.e. raising operator  $X|j\rangle = |j \oplus 1\rangle$

## Parameters

$D$	Dimension of the Hilbert space
-----	--------------------------------

## Returns

Generalized X gate for qudits

## 7.16.3.9 Zd()

```
cmat qpp::Gates::Zd (
    idx D = 2 ) const [inline]
```

Generalized Z gate for qudits.

## Note

Defined as  $Z = \sum_{j=0}^{D-1} \exp(2\pi i j/D) |j\rangle\langle j|$

## Parameters

$D$	Dimension of the Hilbert space
-----	--------------------------------

## Returns

Generalized Z gate for qudits

## 7.16.4 Friends And Related Function Documentation

#### 7.16.4.1 internal::Singleton< const Gates >

```
friend class internal::Singleton< const Gates > [friend]
```

### 7.16.5 Member Data Documentation

#### 7.16.5.1 CNOT

```
cmat qpp::Gates::CNOT {cmat::Identity(4, 4)}
```

Controlled-NOT control target gate.

#### 7.16.5.2 CNOTba

```
cmat qpp::Gates::CNOTba {cmat::Zero(4, 4)}
```

Controlled-NOT target control gate.

#### 7.16.5.3 CZ

```
cmat qpp::Gates::CZ {cmat::Identity(4, 4)}
```

Controlled-Phase gate.

#### 7.16.5.4 FRED

```
cmat qpp::Gates::FRED {cmat::Identity(8, 8)}
```

Fredkin gate.

#### 7.16.5.5 H

```
cmat qpp::Gates::H {cmat::Zero(2, 2)}
```

Hadamard gate.



#### 7.16.5.6 Id2

```
cmat qpp::Gates::Id2 {cmat::Identity(2, 2)}
```

Identity gate.

#### 7.16.5.7 S

```
cmat qpp::Gates::S {cmat::Zero(2, 2)}
```

S gate.

#### 7.16.5.8 SWAP

```
cmat qpp::Gates::SWAP {cmat::Identity(4, 4)}
```

SWAP gate.

#### 7.16.5.9 T

```
cmat qpp::Gates::T {cmat::Zero(2, 2)}
```

T gate.

#### 7.16.5.10 TOF

```
cmat qpp::Gates::TOF {cmat::Identity(8, 8)}
```

Toffoli gate.

#### 7.16.5.11 X

```
cmat qpp::Gates::X {cmat::Zero(2, 2)}
```

Pauli Sigma-X gate.

#### 7.16.5.12 Y

```
cmat qpp::Gates::Y {cmat::Zero(2, 2)}
```

Pauli Sigma-Y gate.

#### 7.16.5.13 Z

```
cmat qpp::Gates::Z {cmat::Zero(2, 2)}
```

Pauli Sigma-Z gate.

The documentation for this class was generated from the following file:

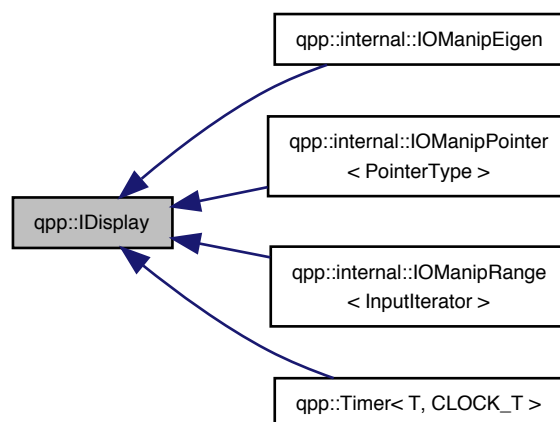
- [classes/gates.h](#)

## 7.17 qpp::IDisplay Class Reference

Abstract class (interface) that mandates the definition of virtual `std::ostream& display(std::ostream& os) const`.

```
#include <classes/ideisplay.h>
```

Inheritance diagram for qpp::IDisplay:



## Public Member Functions

- [IDisplay](#) ()=default  
*Default constructor.*
- [IDisplay](#) (const [IDisplay](#) &)=default  
*Default copy constructor.*
- [IDisplay](#) ([IDisplay](#) &&)=default  
*Default move constructor.*
- [IDisplay](#) & [operator=](#) (const [IDisplay](#) &)=default  
*Default copy assignment operator.*
- [IDisplay](#) & [operator=](#) ([IDisplay](#) &&)=default  
*Default move assignment operator.*
- virtual [~IDisplay](#) ()=default  
*Default virtual destructor.*

## Private Member Functions

- virtual std::ostream & [display](#) (std::ostream &os) const =0  
*Must be overridden by all derived classes.*

## Friends

- std::ostream & [operator<<](#) (std::ostream &os, const [IDisplay](#) &rhs)  
*Overloads the extraction operator.*

### 7.17.1 Detailed Description

Abstract class (interface) that mandates the definition of virtual std::ostream& [display](#)(std::ostream& os) const.

This class defines friend inline std::ostream& [operator<<](#) (std::ostream& os, const [qpp::IDisplay](#)& rhs). The latter delegates the work to the pure private virtual function [qpp::IDisplay::display\(\)](#) which has to be overridden by all derived classes.

### 7.17.2 Constructor & Destructor Documentation

#### 7.17.2.1 IDisplay() [1/3]

```
qpp::IDisplay::IDisplay ( ) [default]
```

Default constructor.

#### 7.17.2.2 IDisplay() [2/3]

```
qpp::IDisplay::IDisplay (
    const IDisplay & ) [default]
```

Default copy constructor.

#### 7.17.2.3 IDisplay() [3/3]

```
qpp::IDisplay::IDisplay (
    IDisplay && ) [default]
```

Default move constructor.

#### 7.17.2.4 ~IDisplay()

```
virtual qpp::IDisplay::~~IDisplay ( ) [virtual], [default]
```

Default virtual destructor.

### 7.17.3 Member Function Documentation

#### 7.17.3.1 display()

```
virtual std::ostream& qpp::IDisplay::display (
    std::ostream & os ) const [private], [pure virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overridden member function in the derived class. This function is automatically invoked by friend inline `std::ostream& operator<<(std::ostream& os, const IDisplay& rhs)`.

Implemented in `qpp::internal::IOManipEigen`, `qpp::Timer< T, CLOCK_T >`, `qpp::internal::IOManipPointer< PointerType >`, and `qpp::internal::IOManipRange< InputIterator >`.

#### 7.17.3.2 operator=() [1/2]

```
IDisplay& qpp::IDisplay::operator= (
    const IDisplay & ) [default]
```

Default copy assignment operator.

## 7.17.3.3 operator=() [2/2]

```
IDisplay& qpp::IDisplay::operator= (
    IDisplay && ) [default]
```

Default move assignment operator.

## 7.17.4 Friends And Related Function Documentation

## 7.17.4.1 operator&lt;&lt;

```
std::ostream& operator<< (
    std::ostream & os,
    const IDisplay & rhs ) [friend]
```

Overloads the extraction operator.

Delegates the work to the virtual function [qpp::IDisplay::display\(\)](#)

The documentation for this class was generated from the following file:

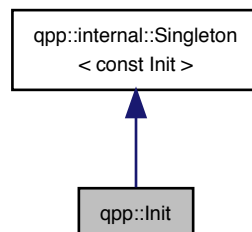
- [classes/ideplay.h](#)

## 7.18 qpp::Init Class Reference

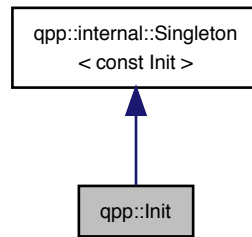
const Singleton class that performs additional initializations/cleanups

```
#include <classes/init.h>
```

Inheritance diagram for qpp::Init:



Collaboration diagram for qpp::Init:



### Private Member Functions

- [Init \(\)](#)  
*Additional initializations.*
- [~Init \(\)](#)  
*Cleanups.*

### Friends

- class [internal::Singleton< const Init >](#)

### Additional Inherited Members

#### 7.18.1 Detailed Description

const Singleton class that performs additional initializations/cleanups

#### 7.18.2 Constructor & Destructor Documentation

##### 7.18.2.1 Init()

```
qpp::Init::Init ( ) [inline], [private]
```

Additional initializations.

## 7.18.2.2 ~Init()

```
qpp::Init::~~Init ( ) [inline], [private]
```

Cleanups.

## 7.18.3 Friends And Related Function Documentation

## 7.18.3.1 internal::Singleton&lt; const Init &gt;

```
friend class internal::Singleton< const Init > [friend]
```

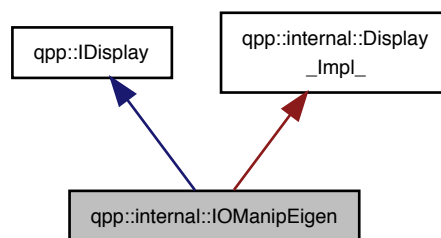
The documentation for this class was generated from the following file:

- [classes/init.h](#)

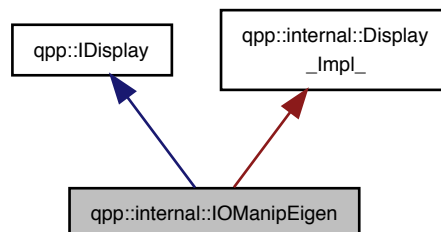
## 7.19 qpp::internal::IOManipEigen Class Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipEigen:



Collaboration diagram for qpp::internal::IOManipEigen:



## Public Member Functions

- `template<typename Derived >`  
`IManipEigen` (const `Eigen::MatrixBase< Derived >` &A, double `chop=qpp::chop`)
- `IManipEigen` (const `cplx` z, double `chop=qpp::chop`)

## Private Member Functions

- `std::ostream & display` (`std::ostream &os`) const override  
*Must be overridden by all derived classes.*

## Private Attributes

- `cmat A_`
- double `chop_`

## 7.19.1 Constructor & Destructor Documentation

### 7.19.1.1 IManipEigen() [1/2]

```
template<typename Derived >
qpp::internal::IManipEigen::IManipEigen (
    const Eigen::MatrixBase< Derived > & A,
    double chop = qpp::chop ) [inline], [explicit]
```

### 7.19.1.2 IManipEigen() [2/2]

```
qpp::internal::IManipEigen::IManipEigen (
    const cplx z,
    double chop = qpp::chop ) [inline], [explicit]
```

## 7.19.2 Member Function Documentation

### 7.19.2.1 display()

```
std::ostream& qpp::internal::IManipEigen::display (
    std::ostream & os ) const [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overridden member function in the derived class. This function is automatically invoked by friend inline `std::ostream& operator<<(std::ostream& os, const IDisplay& rhs)`.

Implements `qpp::IDisplay`.



### 7.19.3 Member Data Documentation

#### 7.19.3.1 A\_

```
cmat qpp::internal::IOManipEigen::A_ [private]
```

#### 7.19.3.2 chop\_

```
double qpp::internal::IOManipEigen::chop_ [private]
```

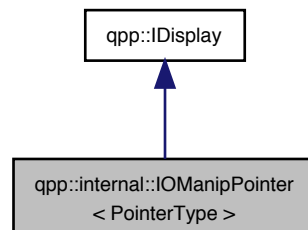
The documentation for this class was generated from the following file:

- [internal/classes/iomanip.h](#)

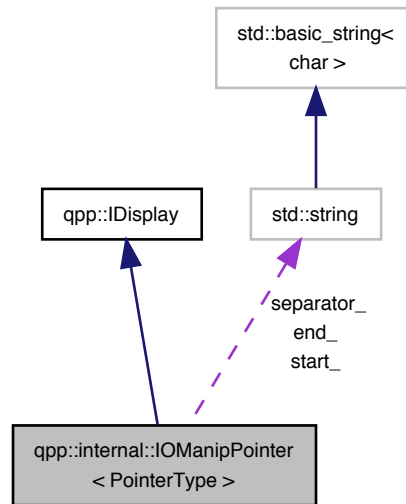
## 7.20 qpp::internal::IOManipPointer< PointerType > Class Template Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipPointer< PointerType >:



Collaboration diagram for `qpp::internal::IOManipPointer< PointerType >`:



## Public Member Functions

- `IOManipPointer` (const PointerType \*p, idx N, const std::string &separator, const std::string &start="[" , const std::string &end="]")
- `IOManipPointer` (const IOManipPointer &)=default
- `IOManipPointer & operator=` (const IOManipPointer &)=default

## Private Member Functions

- `std::ostream & display` (std::ostream &os) const override  
*Must be overridden by all derived classes.*

## Private Attributes

- const PointerType \* `p_`
- idx `N_`
- std::string `separator_`
- std::string `start_`
- std::string `end_`

### 7.20.1 Constructor & Destructor Documentation

## 7.20.1.1 IManipPointer() [1/2]

```
template<typename PointerType>
qpp::internal::IManipPointer< PointerType >::IManipPointer (
    const PointerType * p,
    idx N,
    const std::string & separator,
    const std::string & start = "[",
    const std::string & end = "]" ) [inline], [explicit]
```

## 7.20.1.2 IManipPointer() [2/2]

```
template<typename PointerType>
qpp::internal::IManipPointer< PointerType >::IManipPointer (
    const IManipPointer< PointerType > & ) [default]
```

## 7.20.2 Member Function Documentation

## 7.20.2.1 display()

```
template<typename PointerType>
std::ostream& qpp::internal::IManipPointer< PointerType >::display (
    std::ostream & os ) const [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overridden member function in the derived class. This function is automatically invoked by friend inline `std::ostream& operator<<(std::ostream& os, const IDisplay& rhs)`.

Implements [qpp::IDisplay](#).

## 7.20.2.2 operator=()

```
template<typename PointerType>
IManipPointer& qpp::internal::IManipPointer< PointerType >::operator= (
    const IManipPointer< PointerType > & ) [default]
```

## 7.20.3 Member Data Documentation

#### 7.20.3.1 end\_

```
template<typename PointerType>
std::string qpp::internal::IManipPointer< PointerType >::end_ [private]
```

#### 7.20.3.2 N\_

```
template<typename PointerType>
idx qpp::internal::IManipPointer< PointerType >::N_ [private]
```

#### 7.20.3.3 p\_

```
template<typename PointerType>
const PointerType* qpp::internal::IManipPointer< PointerType >::p_ [private]
```

#### 7.20.3.4 separator\_

```
template<typename PointerType>
std::string qpp::internal::IManipPointer< PointerType >::separator_ [private]
```

#### 7.20.3.5 start\_

```
template<typename PointerType>
std::string qpp::internal::IManipPointer< PointerType >::start_ [private]
```

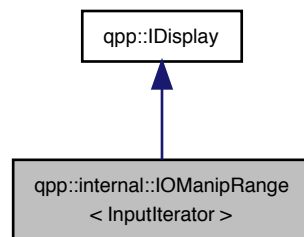
The documentation for this class was generated from the following file:

- [internal/classes/iomanip.h](#)

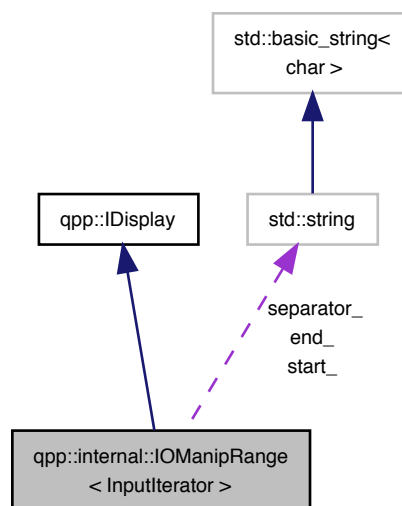
## 7.21 qpp::internal::IOManipRange< InputIterator > Class Template Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipRange< InputIterator >:



Collaboration diagram for qpp::internal::IOManipRange< InputIterator >:



### Public Member Functions

- [IOManipRange](#) (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[, const std::string &end="]")
- [IOManipRange](#) (const [IOManipRange](#) &)=default
- [IOManipRange](#) & [operator=](#) (const [IOManipRange](#) &)=default

## Private Member Functions

- `std::ostream & display (std::ostream &os)` const override

*Must be overridden by all derived classes.*

## Private Attributes

- InputIterator `first_`
- InputIterator `last_`
- `std::string` `separator_`
- `std::string` `start_`
- `std::string` `end_`

## 7.21.1 Constructor & Destructor Documentation

### 7.21.1.1 IOManipRange() [1/2]

```
template<typename InputIterator>
qpp::internal::IOManipRange< InputIterator >::IOManipRange (
    InputIterator first,
    InputIterator last,
    const std::string & separator,
    const std::string & start = "[",
    const std::string & end = "]" ) [inline], [explicit]
```

### 7.21.1.2 IOManipRange() [2/2]

```
template<typename InputIterator>
qpp::internal::IOManipRange< InputIterator >::IOManipRange (
    const IOManipRange< InputIterator > & ) [default]
```

## 7.21.2 Member Function Documentation

### 7.21.2.1 display()

```
template<typename InputIterator>
std::ostream& qpp::internal::IOManipRange< InputIterator >::display (
    std::ostream & os ) const [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overridden member function in the derived class. This function is automatically invoked by friend inline `std::ostream& operator<<(std::ostream& os, const IDisplay& rhs)`.

Implements `qpp::IDisplay`.

### 7.21.2.2 operator=()

```
template<typename InputIterator>
IOManipRange& qpp::internal::IOManipRange< InputIterator >::operator= (
    const IOManipRange< InputIterator > & ) [default]
```

## 7.21.3 Member Data Documentation

### 7.21.3.1 end\_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::end_ [private]
```

### 7.21.3.2 first\_

```
template<typename InputIterator>
InputIterator qpp::internal::IOManipRange< InputIterator >::first_ [private]
```

### 7.21.3.3 last\_

```
template<typename InputIterator>
InputIterator qpp::internal::IOManipRange< InputIterator >::last_ [private]
```

### 7.21.3.4 separator\_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::separator_ [private]
```

### 7.21.3.5 start\_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::start_ [private]
```

The documentation for this class was generated from the following file:

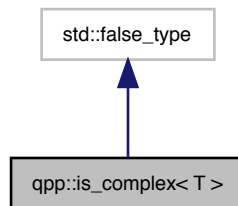
- [internal/classes/iomanip.h](#)

## 7.22 qpp::is\_complex< T > Struct Template Reference

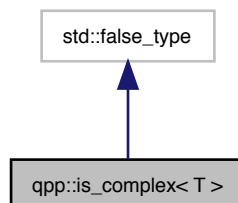
Checks whether the type is a complex type.

```
#include <traits.h>
```

Inheritance diagram for qpp::is\_complex< T >:



Collaboration diagram for qpp::is\_complex< T >:



### 7.22.1 Detailed Description

```
template<typename T>  
struct qpp::is_complex< T >
```

Checks whether the type is a complex type.

Provides the constant member *value* which is equal to *true*, if the type is a complex type, i.e. *std::complex< T >*

The documentation for this struct was generated from the following file:

- [traits.h](#)

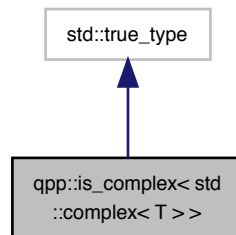


## 7.23 qpp::is\_complex< std::complex< T > > Struct Template Reference

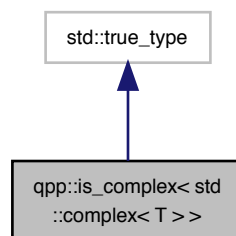
Checks whether the type is a complex number type, specialization for complex types.

```
#include <traits.h>
```

Inheritance diagram for qpp::is\_complex< std::complex< T > >:



Collaboration diagram for qpp::is\_complex< std::complex< T > >:



### 7.23.1 Detailed Description

```
template<typename T>  
struct qpp::is_complex< std::complex< T > >
```

Checks whether the type is a complex number type, specialization for complex types.

The documentation for this struct was generated from the following file:

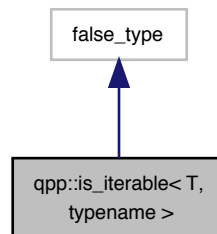
- [traits.h](#)

## 7.24 qpp::is\_iterable< T, typename > Struct Template Reference

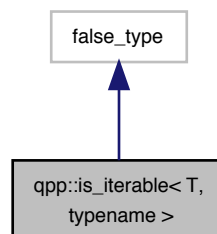
Checks whether *T* is compatible with an STL-like iterable container.

```
#include <traits.h>
```

Inheritance diagram for `qpp::is_iterable< T, typename >`:



Collaboration diagram for `qpp::is_iterable< T, typename >`:



### 7.24.1 Detailed Description

```
template<typename T, typename = void>  
struct qpp::is_iterable< T, typename >
```

Checks whether *T* is compatible with an STL-like iterable container.

Provides the constant member *value* which is equal to *true*, if *T* is compatible with an iterable container, i.e. provides at least *begin()* and *end()* member functions. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

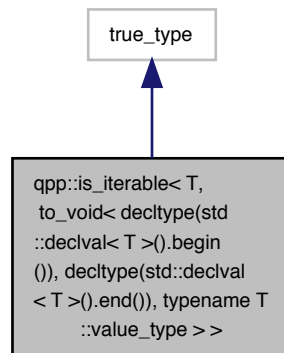
- [traits.h](#)

## 7.25 `qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >` Struct Template Reference

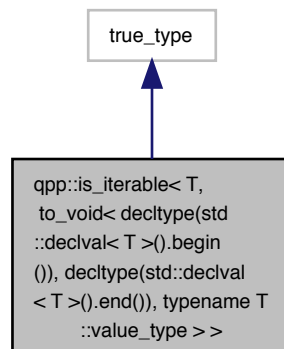
Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

```
#include <traits.h>
```

Inheritance diagram for `qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >`:



Collaboration diagram for `qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >`:



### 7.25.1 Detailed Description

```
template<typename T>
struct qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >
```

Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

The documentation for this struct was generated from the following file:

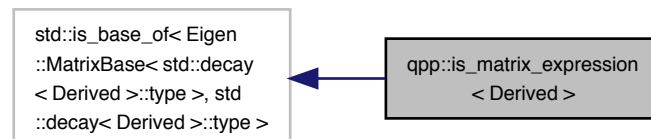
- [traits.h](#)

## 7.26 qpp::is\_matrix\_expression< Derived > Struct Template Reference

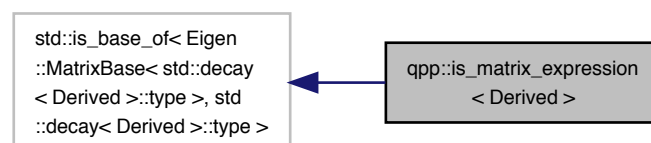
Checks whether the type is an Eigen matrix expression.

```
#include <traits.h>
```

Inheritance diagram for qpp::is\_matrix\_expression< Derived >:



Collaboration diagram for qpp::is\_matrix\_expression< Derived >:



### 7.26.1 Detailed Description

```
template<typename Derived>
struct qpp::is_matrix_expression< Derived >
```

Checks whether the type is an Eigen matrix expression.

Provides the constant member *value* which is equal to *true*, if the type is an Eigen matrix expression of type *EigenMatrixBase<Derived>*. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

- [traits.h](#)

## 7.27 `qpp::make_void< Ts >` Struct Template Reference

Helper for [qpp::to\\_void<>](#) alias template.

```
#include <traits.h>
```

### Public Types

- typedef void [type](#)

### 7.27.1 Detailed Description

```
template<typename... Ts>
struct qpp::make_void< Ts >
```

Helper for [qpp::to\\_void<>](#) alias template.

See also

[qpp::to\\_void<>](#)

### 7.27.2 Member Typedef Documentation

#### 7.27.2.1 `type`

```
template<typename... Ts>
typedef void qpp::make\_void< Ts >::type
```

The documentation for this struct was generated from the following file:

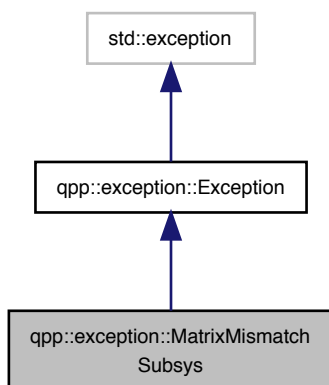
- [traits.h](#)

## 7.28 qpp::exception::MatrixMismatchSubsys Class Reference

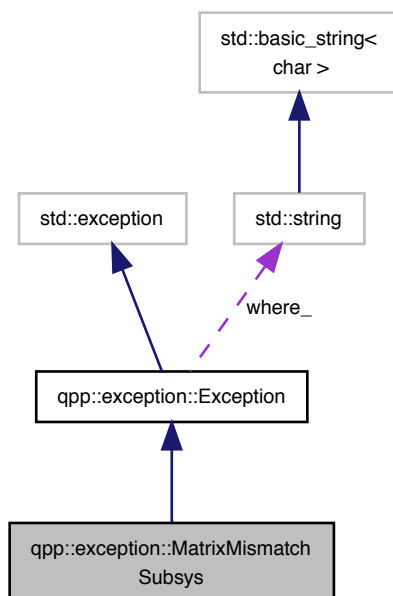
Matrix mismatch subsystems exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixMismatchSubsys:



Collaboration diagram for qpp::exception::MatrixMismatchSubsys:



## Public Member Functions

- `std::string type_description ()` const override  
*Exception type description.*

### 7.28.1 Detailed Description

Matrix mismatch subsystems exception.

Matrix size mismatch subsystem sizes (e.g. in `qpp::apply()`)

### 7.28.2 Member Function Documentation

#### 7.28.2.1 type\_description()

```
std::string qpp::exception::MatrixMismatchSubsys::type_description ( ) const [inline], [override],  
[virtual]
```

*Exception type description.*

#### Returns

*Exception type description*

Implements `qpp::exception::Exception`.

The documentation for this class was generated from the following file:

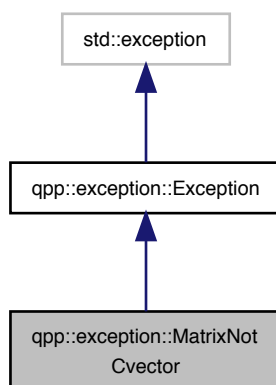
- `classes/exception.h`

## 7.29 qpp::exception::MatrixNotCvector Class Reference

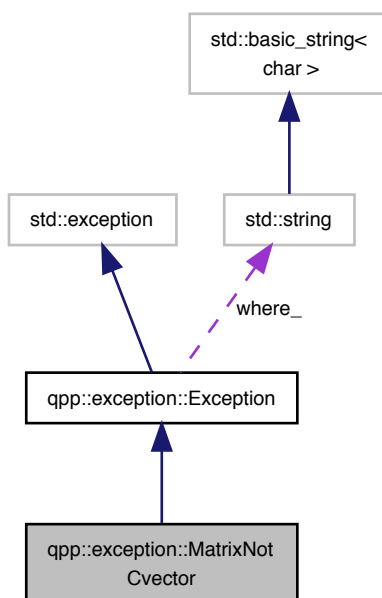
Matrix is not a column vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotCvector:



Collaboration diagram for qpp::exception::MatrixNotCvector:



## Public Member Functions

- `std::string type\_description () const` override  
*[Exception](#) type description.*



### 7.29.1 Detailed Description

Matrix is not a column vector exception.

Eigen::Matrix is not a column vector

### 7.29.2 Member Function Documentation

#### 7.29.2.1 type\_description()

```
std::string qpp::exception::MatrixNotCvector::type_description ( ) const [inline], [override],  
[virtual]
```

Exception type description.

#### Returns

Exception type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

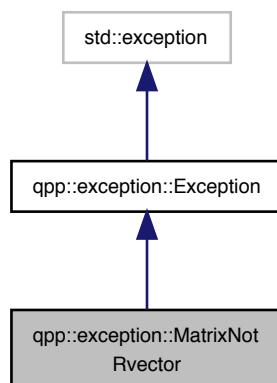
- [classes/exception.h](#)

## 7.30 qpp::exception::MatrixNotRvector Class Reference

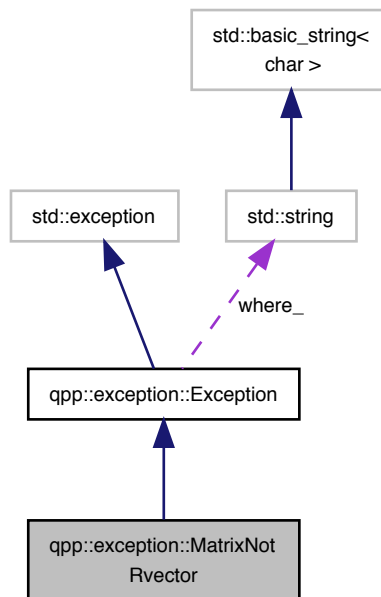
Matrix is not a row vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotRvector:



Collaboration diagram for `qpp::exception::MatrixNotRvector`:



## Public Member Functions

- `std::string type_description () const` override  
*Exception type description.*

### 7.30.1 Detailed Description

Matrix is not a row vector exception.

Eigen::Matrix is not a row vector

### 7.30.2 Member Function Documentation

#### 7.30.2.1 type\_description()

```
std::string qpp::exception::MatrixNotRvector::type_description ( ) const [inline], [override], [virtual]
```

*Exception type description.*

## Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

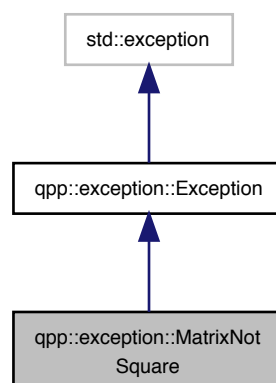
- [classes/exception.h](#)

## 7.31 qpp::exception::MatrixNotSquare Class Reference

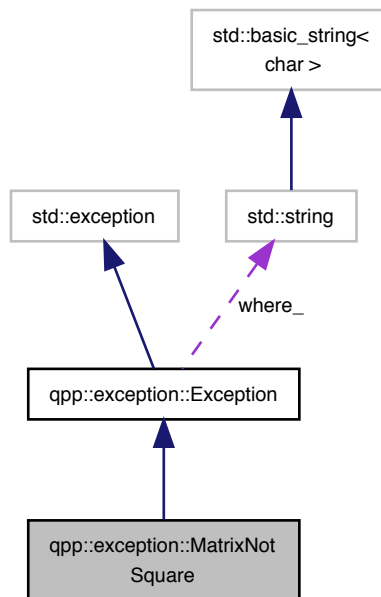
Matrix is not square exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquare:



Collaboration diagram for `qpp::exception::MatrixNotSquare`:



## Public Member Functions

- `std::string type_description () const` override  
*Exception type description.*

### 7.31.1 Detailed Description

Matrix is not square exception.

Eigen::Matrix is not a square matrix

### 7.31.2 Member Function Documentation

#### 7.31.2.1 type\_description()

```
std::string qpp::exception::MatrixNotSquare::type_description ( ) const [inline], [override], [virtual]
```

*Exception type description.*

## Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

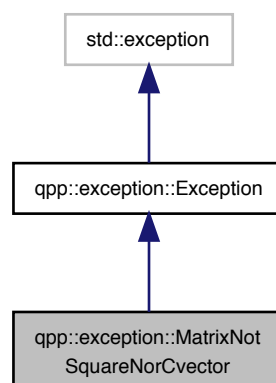
- [classes/exception.h](#)

## 7.32 qpp::exception::MatrixNotSquareNorCvector Class Reference

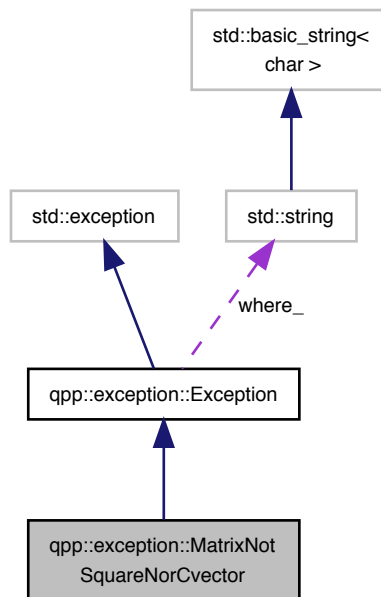
Matrix is not square nor column vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorCvector:



Collaboration diagram for `qpp::exception::MatrixNotSquareNorCvector`:



## Public Member Functions

- `std::string type_description () const` override  
*Exception type description.*

### 7.32.1 Detailed Description

Matrix is not square nor column vector exception.

Eigen::Matrix is not a square matrix nor a column vector

### 7.32.2 Member Function Documentation

#### 7.32.2.1 type\_description()

```
std::string qpp::exception::MatrixNotSquareNorCvector::type_description ( ) const [inline],
[override], [virtual]
```

*Exception type description.*

## Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

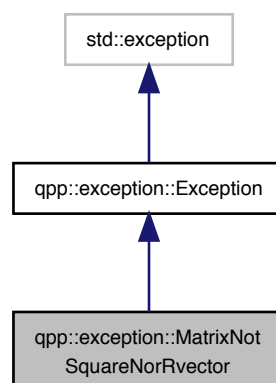
- [classes/exception.h](#)

## 7.33 qpp::exception::MatrixNotSquareNorRvector Class Reference

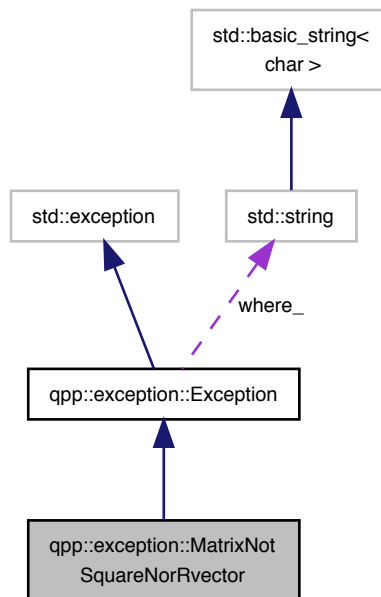
Matrix is not square nor row vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorRvector:



Collaboration diagram for `qpp::exception::MatrixNotSquareNorRvector`:



## Public Member Functions

- `std::string type_description () const` override  
*Exception type description.*

### 7.33.1 Detailed Description

Matrix is not square nor row vector exception.

Eigen::Matrix is not a square matrix nor a row vector

### 7.33.2 Member Function Documentation

#### 7.33.2.1 type\_description()

```
std::string qpp::exception::MatrixNotSquareNorRvector::type_description ( ) const [inline],
[override], [virtual]
```

*Exception type description.*



## Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

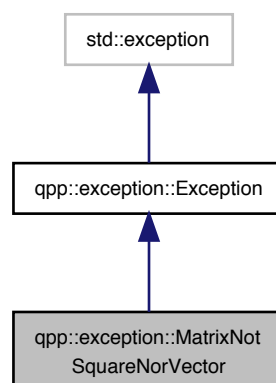
- [classes/exception.h](#)

## 7.34 qpp::exception::MatrixNotSquareNorVector Class Reference

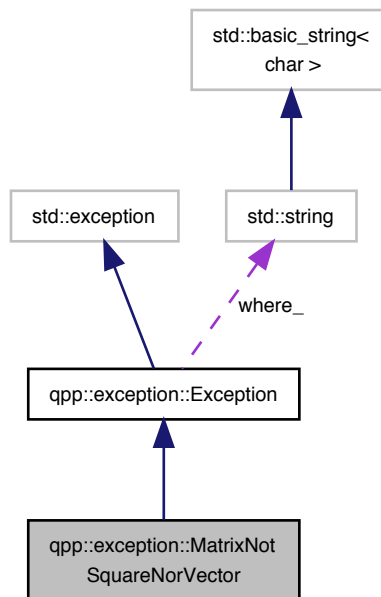
Matrix is not square nor vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorVector:



Collaboration diagram for `qpp::exception::MatrixNotSquareNorVector`:



## Public Member Functions

- `std::string type_description () const` override  
*Exception type description.*

### 7.34.1 Detailed Description

Matrix is not square nor vector exception.

Eigen::Matrix is not a square matrix nor a row/column vector

### 7.34.2 Member Function Documentation

#### 7.34.2.1 type\_description()

```
std::string qpp::exception::MatrixNotSquareNorVector::type_description ( ) const [inline],
[override], [virtual]
```

*Exception type description.*

## Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

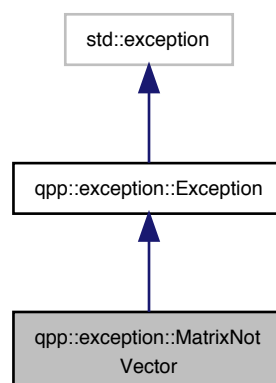
- [classes/exception.h](#)

## 7.35 qpp::exception::MatrixNotVector Class Reference

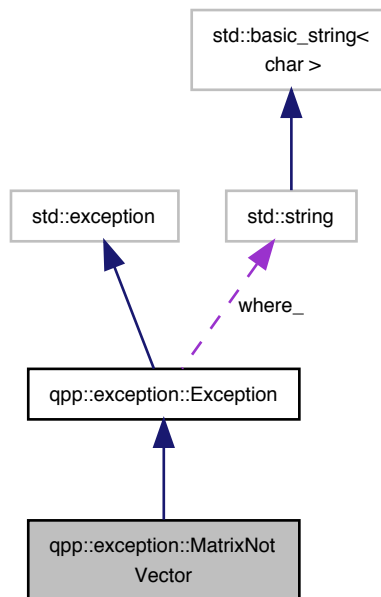
Matrix is not a vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotVector:



Collaboration diagram for qpp::exception::MatrixNotVector:



## Public Member Functions

- `std::string type_description () const` override  
*Exception type description.*

### 7.35.1 Detailed Description

Matrix is not a vector exception.

Eigen::Matrix is not a row or column vector

### 7.35.2 Member Function Documentation

#### 7.35.2.1 type\_description()

```
std::string qpp::exception::MatrixNotVector::type_description ( ) const [inline], [override], [virtual]
```

*Exception type description.*

## Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

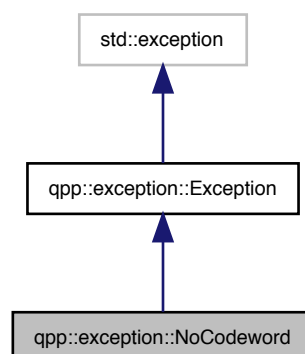
- [classes/exception.h](#)

## 7.36 qpp::exception::NoCodeword Class Reference

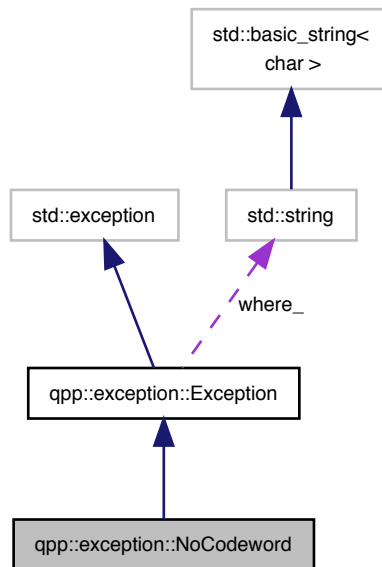
Codeword does not exist exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NoCodeword:



Collaboration diagram for `qpp::exception::NoCodeword`:



## Public Member Functions

- `std::string type_description ()` const override  
*Exception type description.*

### 7.36.1 Detailed Description

Codeword does not exist exception.

Codeword does not exist, thrown when calling `qpp::Codes::codeword()` with an invalid index

### 7.36.2 Member Function Documentation

#### 7.36.2.1 type\_description()

```
std::string qpp::exception::NoCodeword::type_description ( ) const [inline], [override],
[virtual]
```

*Exception type description.*

#### Returns

*Exception type description*

Implements `qpp::exception::Exception`.

The documentation for this class was generated from the following file:

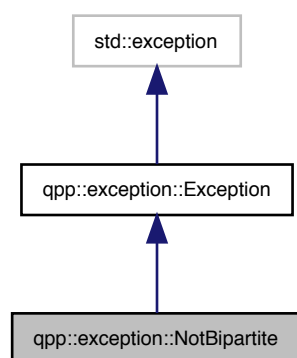
- `classes/exception.h`

## 7.37 qpp::exception::NotBipartite Class Reference

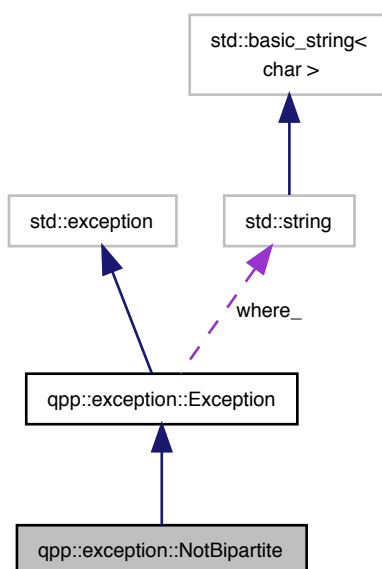
Not bi-partite exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotBipartite:



Collaboration diagram for qpp::exception::NotBipartite:



## Public Member Functions

- `std::string type\_description () const` override  
*[Exception](#) type description.*

### 7.37.1 Detailed Description

Not bi-partite exception.

`std::vector<idx>` of dimensions has size different from 2

### 7.37.2 Member Function Documentation

#### 7.37.2.1 `type_description()`

```
std::string qpp::exception::NotBipartite::type_description ( ) const [inline], [override],  
[virtual]
```

[Exception](#) type description.

#### Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

- `classes/exception.h`

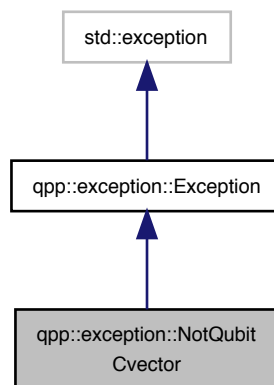
## 7.38 `qpp::exception::NotQubitCvector` Class Reference

Column vector is not 2 x 1 exception.

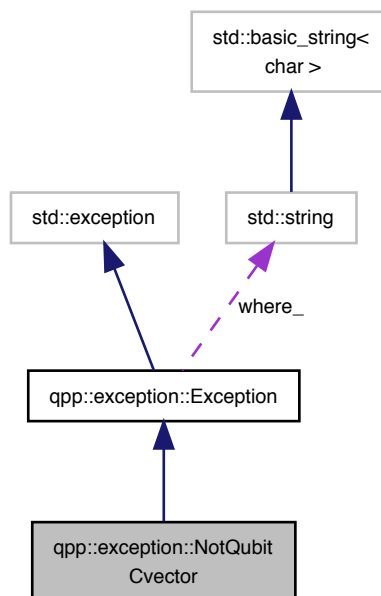
```
#include <classes/exception.h>
```



Inheritance diagram for qpp::exception::NotQubitCvector:



Collaboration diagram for qpp::exception::NotQubitCvector:



## Public Member Functions

- `std::string` [type\\_description](#) () const override  
*[Exception](#) type description.*

### 7.38.1 Detailed Description

Column vector is not 2 x 1 exception.

Eigen::Matrix is not 2 x 1

### 7.38.2 Member Function Documentation

#### 7.38.2.1 type\_description()

```
std::string qpp::exception::NotQubitCvector::type_description ( ) const [inline], [override],  
[virtual]
```

Exception type description.

#### Returns

Exception type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

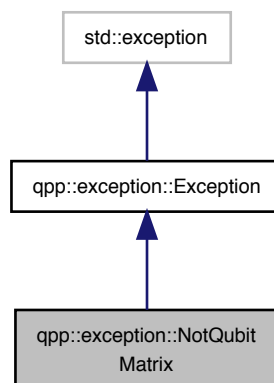
- [classes/exception.h](#)

## 7.39 qpp::exception::NotQubitMatrix Class Reference

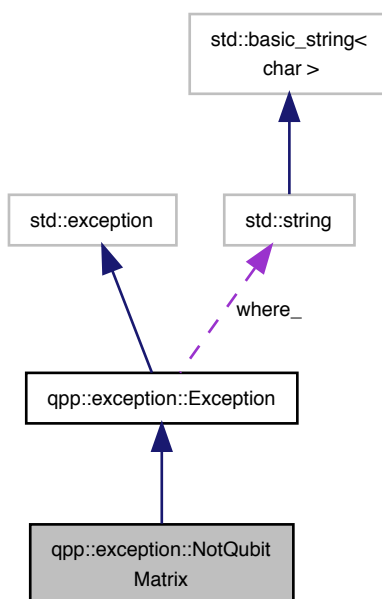
Matrix is not 2 x 2 exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitMatrix:



Collaboration diagram for qpp::exception::NotQubitMatrix:



## Public Member Functions

- `std::string type_description () const` override  
*Exception type description.*

### 7.39.1 Detailed Description

Matrix is not 2 x 2 exception.

Eigen::Matrix is not 2 x 2

### 7.39.2 Member Function Documentation

#### 7.39.2.1 type\_description()

```
std::string qpp::exception::NotQubitMatrix::type_description ( ) const [inline], [override], [virtual]
```

*Exception type description.*

**Returns**

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

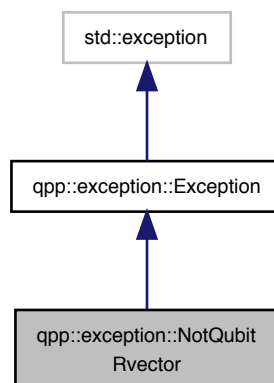
- [classes/exception.h](#)

## 7.40 qpp::exception::NotQubitRvector Class Reference

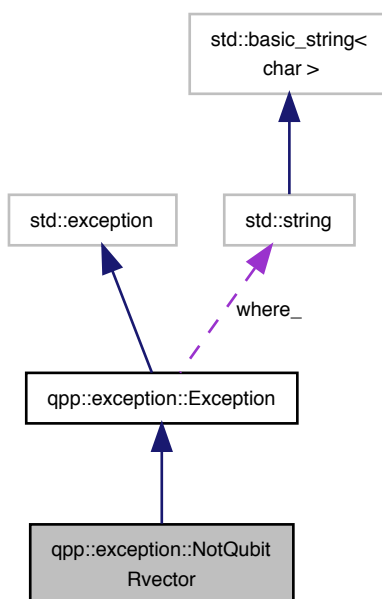
Row vector is not 1 x 2 exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitRvector:



Collaboration diagram for qpp::exception::NotQubitRvector:



## Public Member Functions

- `std::string type_description () const` override  
*Exception type description.*

### 7.40.1 Detailed Description

Row vector is not 1 x 2 exception.

Eigen::Matrix is not 1 x 2

### 7.40.2 Member Function Documentation

#### 7.40.2.1 type\_description()

```
std::string qpp::exception::NotQubitRvector::type_description ( ) const [inline], [override], [virtual]
```

*Exception type description.*

**Returns**

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

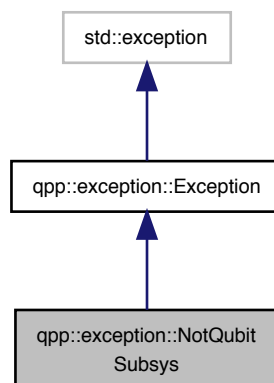
- [classes/exception.h](#)

## 7.41 qpp::exception::NotQubitSubsys Class Reference

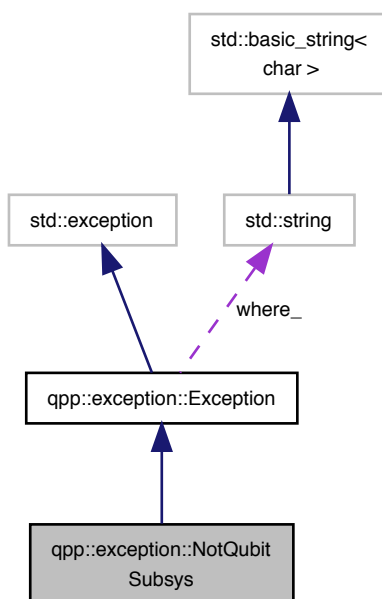
Subsystems are not qubits exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitSubsys:



Collaboration diagram for qpp::exception::NotQubitSubsys:



## Public Member Functions

- `std::string type\_description () const` override  
*[Exception](#) type description.*

### 7.41.1 Detailed Description

Subsystems are not qubits exception.

Subsystems are not 2-dimensional (qubits)

### 7.41.2 Member Function Documentation

#### 7.41.2.1 `type_description()`

```
std::string qpp::exception::NotQubitSubsys::type_description ( ) const [inline], [override], [virtual]
```

[Exception](#) type description.

**Returns**

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

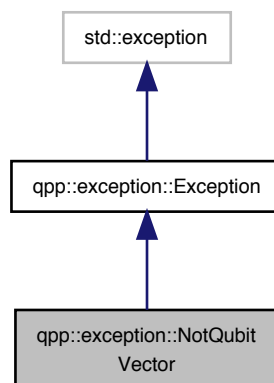
- [classes/exception.h](#)

## 7.42 qpp::exception::NotQubitVector Class Reference

Vector is not 2 x 1 nor 1 x 2 exception.

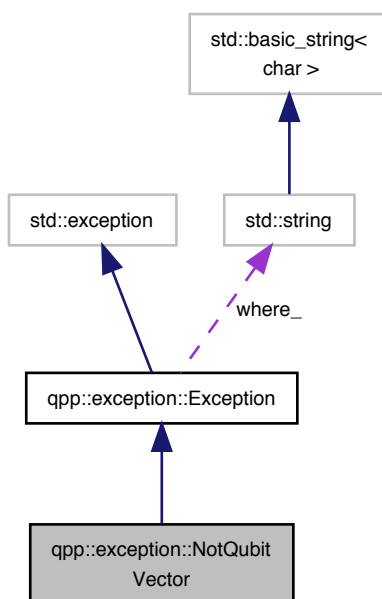
```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitVector:





Collaboration diagram for qpp::exception::NotQubitVector:



## Public Member Functions

- `std::string type_description () const` override  
*Exception type description.*

### 7.42.1 Detailed Description

Vector is not 2 x 1 nor 1 x 2 exception.

Eigen::Matrix is not 2 x 1 nor 1 x 2

### 7.42.2 Member Function Documentation

#### 7.42.2.1 type\_description()

```
std::string qpp::exception::NotQubitVector::type_description ( ) const [inline], [override], [virtual]
```

*Exception type description.*

## Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

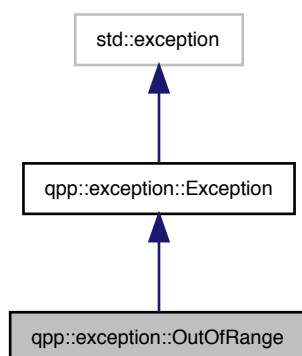
- [classes/exception.h](#)

## 7.43 qpp::exception::OutOfRange Class Reference

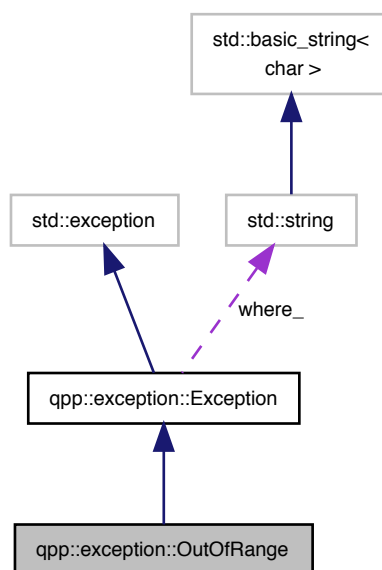
Parameter out of range exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::OutOfRange:



Collaboration diagram for qpp::exception::OutOfRange:



## Public Member Functions

- `std::string type_description () const` override  
*Exception type description.*

### 7.43.1 Detailed Description

Parameter out of range exception.

Parameter out of range

### 7.43.2 Member Function Documentation

#### 7.43.2.1 type\_description()

```
std::string qpp::exception::OutOfRange::type_description ( ) const [inline], [override],
[virtual]
```

*Exception type description.*

#### Returns

*Exception type description*

Implements `qpp::exception::Exception`.

The documentation for this class was generated from the following file:

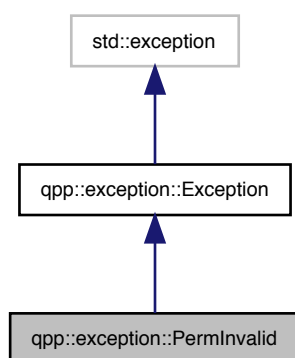
- `classes/exception.h`

## 7.44 qpp::exception::PermlInvalid Class Reference

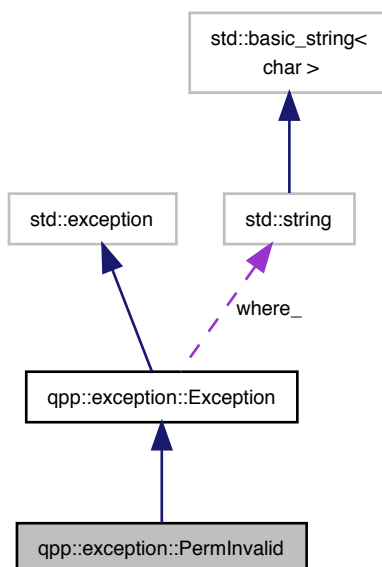
Invalid permutation exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::PermlInvalid:



Collaboration diagram for qpp::exception::PermlInvalid:



## Public Member Functions

- `std::string type_description ()` const override  
*Exception type description.*

### 7.44.1 Detailed Description

Invalid permutation exception.

`std::vector<idx>` does not represent a valid permutation

### 7.44.2 Member Function Documentation

#### 7.44.2.1 type\_description()

```
std::string qpp::exception::PermInvalid::type_description ( ) const [inline], [override],  
[virtual]
```

*Exception type description.*

#### Returns

*Exception type description*

Implements `qpp::exception::Exception`.

The documentation for this class was generated from the following file:

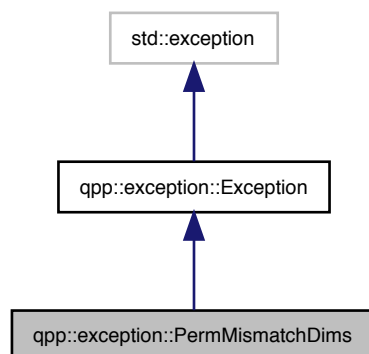
- `classes/exception.h`

## 7.45 qpp::exception::PermMismatchDims Class Reference

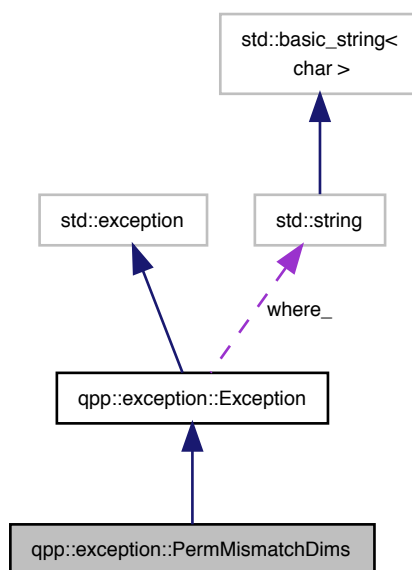
Permutation mismatch dimensions exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::PermMismatchDims:



Collaboration diagram for qpp::exception::PermMismatchDims:



## Public Member Functions

- `std::string` [type\\_description](#) () const override  
*[Exception](#) type description.*

### 7.45.1 Detailed Description

Permutation mismatch dimensions exception.

Size of the `std::vector<idx>` representing the permutation is different from the size of the `std::vector<idx>` of dimensions

### 7.45.2 Member Function Documentation

#### 7.45.2.1 type\_description()

```
std::string qpp::exception::PermMismatchDims::type_description ( ) const [inline], [override], [virtual]
```

Exception type description.

Returns

Exception type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

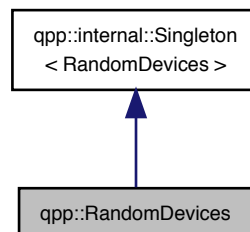
- [classes/exception.h](#)

## 7.46 qpp::RandomDevices Class Reference

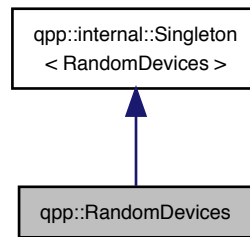
Singleton class that manages the source of randomness in the library.

```
#include <classes/random_devices.h>
```

Inheritance diagram for `qpp::RandomDevices`:



Collaboration diagram for `qpp::RandomDevices`:



## Public Member Functions

- `std::mt19937 & get\_prng ()`  
*Returns a reference to the internal PRNG object.*
- `std::istream & load (std::istream &is)`  
*Loads the state of the PRNG from an input stream.*
- `std::ostream & save (std::ostream &os) const`  
*Saves the state of the PRNG to an output stream.*

## Private Member Functions

- `RandomDevices ()`  
*Initializes and seeds the random number generators.*
- `~RandomDevices ()=default`  
*Default destructor.*

## Private Attributes

- `std::random_device rd\_`  
*used to seed `std::mt19937 prng_`*
- `std::mt19937 prng\_`  
*Mersenne twister random number generator.*

## Friends

- class `internal::Singleton< RandomDevices >`



## Additional Inherited Members

### 7.46.1 Detailed Description

Singleton class that manages the source of randomness in the library.

Consists of a wrapper around an `std::mt19937` Mersenne twister random number generator engine and an `std::random_device` engine. The latter is used to seed the Mersenne twister.

#### Warning

This class DOES NOT seed the standard C number generator used by `Eigen::Matrix::Random()`, since it is not thread safe. Do not use `Eigen::Matrix::Random()` or functions that depend on the C style random number engine, but use `qpp::rand()` instead!

### 7.46.2 Constructor & Destructor Documentation

#### 7.46.2.1 RandomDevices()

```
qpp::RandomDevices::RandomDevices ( ) [inline], [private]
```

Initializes and seeds the random number generators.

#### 7.46.2.2 ~RandomDevices()

```
qpp::RandomDevices::~~RandomDevices ( ) [private], [default]
```

Default destructor.

### 7.46.3 Member Function Documentation

#### 7.46.3.1 get\_prng()

```
std::mt19937& qpp::RandomDevices::get_prng ( ) [inline]
```

Returns a reference to the internal PRNG object.

#### Returns

Reference to the internal PRNG object

#### 7.46.3.2 load()

```
std::istream& qpp::RandomDevices::load (
    std::istream & is ) [inline]
```

Loads the state of the PRNG from an input stream.

**Parameters**

<i>is</i>	Input stream
-----------	--------------

**Returns**

The input stream

**7.46.3.3 save()**

```
std::ostream& qpp::RandomDevices::save (
    std::ostream & os ) const [inline]
```

Saves the state of the PRNG to an output stream.

**Parameters**

<i>os</i>	Output stream
-----------	---------------

**Returns**

The output stream

**7.46.4 Friends And Related Function Documentation****7.46.4.1 internal::Singleton< RandomDevices >**

```
friend class internal::Singleton< RandomDevices > [friend]
```

**7.46.5 Member Data Documentation****7.46.5.1 prng\_**

```
std::mt19937 qpp::RandomDevices::prng_ [private]
```

Mersenne twister random number generator.

## 7.46.5.2 rd\_

```
std::random_device qpp::RandomDevices::rd_ [private]
```

used to seed std::mt19937 prng\_

The documentation for this class was generated from the following file:

- [classes/random\\_devices.h](#)

## 7.47 qpp::internal::Singleton&lt; T &gt; Class Template Reference

[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

```
#include <internal/classes/singleton.h>
```

## Static Public Member Functions

- static T & [get\\_instance](#) () noexcept(std::is\_nothrow\_constructible< T >::value)
- static T & [get\\_thread\\_local\\_instance](#) () noexcept(std::is\_nothrow\_constructible< T >::value)

## Protected Member Functions

- [Singleton](#) () noexcept=default
- [Singleton](#) (const [Singleton](#) &)=delete
- [Singleton](#) & [operator=](#) (const [Singleton](#) &)=delete
- virtual [~Singleton](#) ()=default

## 7.47.1 Detailed Description

```
template<typename T>
class qpp::internal::Singleton< T >
```

[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

To implement a singleton, derive your class from [qpp::internal::Singleton](#), make [qpp::internal::Singleton](#) a friend of your class, then declare the constructor and destructor of your class as private. To get an instance, use the static member function [qpp::internal::Singleton::get\\_instance\(\)](#) ([qpp::internal::Singleton::get\\_thread\\_local\\_instance\(\)](#)), which returns a reference (thread\_local reference) to your newly created singleton (thread-safe in C++11).

Example:

```

class MySingleton: public qpp::internal::Singleton<MySingleton>
{
    friend class qpp::internal::Singleton<MySingleton>;
public:
    // Declare all public members here
private:
    MySingleton()
    {
        // Implement the constructor here
    }
    ~MySingleton()
    {
        // Implement the destructor here
    }
};

MySingleton& mySingleton = MySingleton::get_instance(); // Get an instance
thread_local MySingleton& tls = MySingleton::get_thread_local_instance();
// Get a thread_local instance

```

#### See also

Code of [qpp::Codes](#), [qpp::Gates](#), [qpp::Init](#), [qpp::RandomDevices](#), [qpp::States](#) or [qpp.h](#) for real world examples of usage.

## 7.47.2 Constructor & Destructor Documentation

### 7.47.2.1 Singleton() [1/2]

```

template<typename T>
qpp::internal::Singleton< T >::Singleton ( ) [protected], [default], [noexcept]

```

### 7.47.2.2 Singleton() [2/2]

```

template<typename T>
qpp::internal::Singleton< T >::Singleton (
    const Singleton< T > & ) [protected], [delete]

```

### 7.47.2.3 ~Singleton()

```

template<typename T>
virtual qpp::internal::Singleton< T >::~~Singleton ( ) [protected], [virtual], [default]

```

## 7.47.3 Member Function Documentation

## 7.47.3.1 get\_instance()

```
template<typename T>
static T& qpp::internal::Singleton< T >::get_instance ( ) [inline], [static], [noexcept]
```

## 7.47.3.2 get\_thread\_local\_instance()

```
template<typename T>
static T& qpp::internal::Singleton< T >::get_thread_local_instance ( ) [inline], [static],
[noexcept]
```

## 7.47.3.3 operator=()

```
template<typename T>
Singleton& qpp::internal::Singleton< T >::operator= (
    const Singleton< T > & ) [protected], [delete]
```

The documentation for this class was generated from the following file:

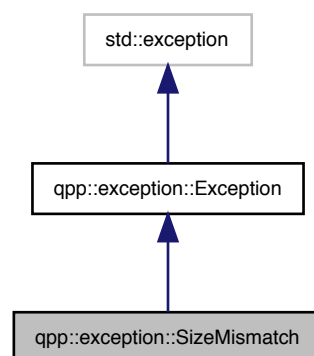
- [internal/classes/singleton.h](#)

## 7.48 qpp::exception::SizeMismatch Class Reference

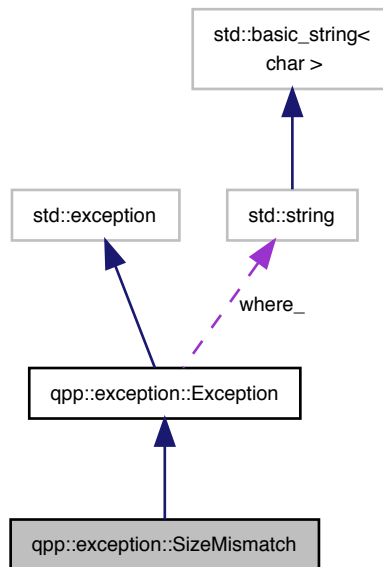
Size mismatch exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::SizeMismatch:



Collaboration diagram for `qpp::exception::SizeMismatch`:



## Public Member Functions

- `std::string type_description ()` const override  
*Exception type description.*

### 7.48.1 Detailed Description

Size mismatch exception.

Sizes do not match

### 7.48.2 Member Function Documentation

#### 7.48.2.1 type\_description()

```
std::string qpp::exception::SizeMismatch::type_description ( ) const [inline], [override],
[virtual]
```

*Exception type description.*

**Returns**

*Exception type description*

Implements `qpp::exception::Exception`.

The documentation for this class was generated from the following file:

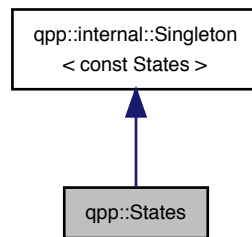
- `classes/exception.h`

## 7.49 qpp::States Class Reference

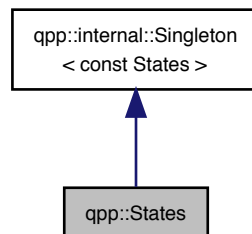
const Singleton class that implements most commonly used states

```
#include <classes/states.h>
```

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



### Public Member Functions

- `ket mes (idx d=2) const`  
*Maximally entangled state of 2 qudits.*
- `ket zero (idx n, idx d=2) const`  
*Zero state of n qudits.*
- `ket one (idx n, idx d=2) const`  
*One state of n qudits.*
- `ket jn (idx j, idx n, idx d=2) const`  
 $|j\rangle^{\otimes n}$  *state of n qudits*
- `ket plus (idx n) const`  
*Plus state of n qubits.*
- `ket minus (idx n) const`  
*Minus state of n qubits.*

## Public Attributes

- `ket x0 {ket::Zero(2)}`  
*Pauli Sigma-X 0-eigenstate  $|+\rangle$*
- `ket x1 {ket::Zero(2)}`  
*Pauli Sigma-X 1-eigenstate  $|-\rangle$*
- `ket y0 {ket::Zero(2)}`  
*Pauli Sigma-Y 0-eigenstate  $|y+\rangle$*
- `ket y1 {ket::Zero(2)}`  
*Pauli Sigma-Y 1-eigenstate  $|y-\rangle$*
- `ket z0 {ket::Zero(2)}`  
*Pauli Sigma-Z 0-eigenstate  $|0\rangle$*
- `ket z1 {ket::Zero(2)}`  
*Pauli Sigma-Z 1-eigenstate  $|1\rangle$*
- `cmat px0 {cmat::Zero(2, 2)}`  
*Projector onto the Pauli Sigma-X 0-eigenstate  $|+\rangle\langle+|$ .*
- `cmat px1 {cmat::Zero(2, 2)}`  
*Projector onto the Pauli Sigma-X 1-eigenstate  $|-\rangle\langle-|$ .*
- `cmat py0 {cmat::Zero(2, 2)}`  
*Projector onto the Pauli Sigma-Y 0-eigenstate  $|y+\rangle\langle y+|$ .*
- `cmat py1 {cmat::Zero(2, 2)}`  
*Projector onto the Pauli Sigma-Y 1-eigenstate  $|y-\rangle\langle y-|$ .*
- `cmat pz0 {cmat::Zero(2, 2)}`  
*Projector onto the Pauli Sigma-Z 0-eigenstate  $|0\rangle\langle 0|$ .*
- `cmat pz1 {cmat::Zero(2, 2)}`  
*Projector onto the Pauli Sigma-Z 1-eigenstate  $|1\rangle\langle 1|$ .*
- `ket b00 {ket::Zero(4)}`  
*Bell-00 state (following the convention in Nielsen and Chuang)*
- `ket b01 {ket::Zero(4)}`  
*Bell-01 state (following the convention in Nielsen and Chuang)*
- `ket b10 {ket::Zero(4)}`  
*Bell-10 state (following the convention in Nielsen and Chuang)*
- `ket b11 {ket::Zero(4)}`  
*Bell-11 state (following the convention in Nielsen and Chuang)*
- `cmat pb00 {cmat::Zero(4, 4)}`  
*Projector onto the Bell-00 state.*
- `cmat pb01 {cmat::Zero(4, 4)}`  
*Projector onto the Bell-01 state.*
- `cmat pb10 {cmat::Zero(4, 4)}`  
*Projector onto the Bell-10 state.*
- `cmat pb11 {cmat::Zero(4, 4)}`  
*Projector onto the Bell-11 state.*
- `ket GHZ {ket::Zero(8)}`  
*GHZ state.*
- `ket W {ket::Zero(8)}`  
*W state.*
- `cmat pGHZ {cmat::Zero(8, 8)}`  
*Projector onto the GHZ state.*
- `cmat pW {cmat::Zero(8, 8)}`  
*Projector onto the W state.*



## Private Member Functions

- [States](#) ()
- [~States](#) ()=default  
*Default destructor.*

## Friends

- class [internal::Singleton< const States >](#)

## Additional Inherited Members

### 7.49.1 Detailed Description

const Singleton class that implements most commonly used states

### 7.49.2 Constructor & Destructor Documentation

#### 7.49.2.1 States()

```
qpp::States::States ( ) [inline], [private]
```

Initialize the states

#### 7.49.2.2 ~States()

```
qpp::States::~~States ( ) [private], [default]
```

Default destructor.

### 7.49.3 Member Function Documentation

#### 7.49.3.1 jn()

```
ket qpp::States::jn (
    idx j,
    idx n,
    idx d = 2 ) const [inline]
```

$|j\rangle^{\otimes n}$  state of  $n$  qudits

**Parameters**

$j$	Non-negative integer
$n$	Non-negative integer
$d$	Subsystem dimensions

**Returns**

$|j\rangle^{\otimes n}$  state of  $n$  qudits

**7.49.3.2 mes()**

```
ket qpp::States::mes (
    idx d = 2 ) const [inline]
```

Maximally entangled state of 2 qudits.

**Parameters**

$d$	Subsystem dimensions
-----	----------------------

**Returns**

Maximally entangled state  $\frac{1}{\sqrt{d}} \sum_{j=0}^{d-1} |jj\rangle$  of 2 qudits

**7.49.3.3 minus()**

```
ket qpp::States::minus (
    idx n ) const [inline]
```

Minus state of  $n$  qubits.

**Parameters**

$n$	Non-negative integer
-----	----------------------

**Returns**

Minus state  $|-\rangle^{\otimes n}$  of  $n$  qubits

## 7.49.3.4 one()

```
ket qpp::States::one (
    idx n,
    idx d = 2 ) const [inline]
```

One state of  $n$  qudits.

## Parameters

$n$	Non-negative integer
$d$	Subsystem dimensions

## Returns

One state  $|1\rangle^{\otimes n}$  of  $n$  qudits

## 7.49.3.5 plus()

```
ket qpp::States::plus (
    idx n ) const [inline]
```

Plus state of  $n$  qubits.

## Parameters

$n$	Non-negative integer
-----	----------------------

## Returns

Plus state  $|+\rangle^{\otimes n}$  of  $n$  qubits

## 7.49.3.6 zero()

```
ket qpp::States::zero (
    idx n,
    idx d = 2 ) const [inline]
```

Zero state of  $n$  qudits.

## Parameters

$n$	Non-negative integer
$d$	Subsystem dimensions

**Returns**

Zero state  $|0\rangle^{\otimes n}$  of  $n$  qudits

**7.49.4 Friends And Related Function Documentation****7.49.4.1 internal::Singleton< const States >**

```
friend class internal::Singleton< const States > [friend]
```

**7.49.5 Member Data Documentation****7.49.5.1 b00**

```
ket qpp::States::b00 {ket::Zero(4)}
```

Bell-00 state (following the convention in Nielsen and Chuang)

**7.49.5.2 b01**

```
ket qpp::States::b01 {ket::Zero(4)}
```

Bell-01 state (following the convention in Nielsen and Chuang)

**7.49.5.3 b10**

```
ket qpp::States::b10 {ket::Zero(4)}
```

Bell-10 state (following the convention in Nielsen and Chuang)

**7.49.5.4 b11**

```
ket qpp::States::b11 {ket::Zero(4)}
```

Bell-11 state (following the convention in Nielsen and Chuang)

#### 7.49.5.5 GHZ

```
ket qpp::States::GHZ {ket::Zero(8)}
```

GHZ state.

#### 7.49.5.6 pb00

```
cmat qpp::States::pb00 {cmat::Zero(4, 4)}
```

Projector onto the Bell-00 state.

#### 7.49.5.7 pb01

```
cmat qpp::States::pb01 {cmat::Zero(4, 4)}
```

Projector onto the Bell-01 state.

#### 7.49.5.8 pb10

```
cmat qpp::States::pb10 {cmat::Zero(4, 4)}
```

Projector onto the Bell-10 state.

#### 7.49.5.9 pb11

```
cmat qpp::States::pb11 {cmat::Zero(4, 4)}
```

Projector onto the Bell-11 state.

#### 7.49.5.10 pGHZ

```
cmat qpp::States::pGHZ {cmat::Zero(8, 8)}
```

Projector onto the GHZ state.

#### 7.49.5.11 pW

```
cmat qpp::States::pW {cmat::Zero(8, 8)}
```

Projector onto the W state.

#### 7.49.5.12 px0

```
cmat qpp::States::px0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-X 0-eigenstate  $|+\rangle\langle+|$ .

#### 7.49.5.13 px1

```
cmat qpp::States::px1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-X 1-eigenstate  $|-\rangle\langle-|$ .

#### 7.49.5.14 py0

```
cmat qpp::States::py0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Y 0-eigenstate  $|y+\rangle\langle y+|$ .

#### 7.49.5.15 py1

```
cmat qpp::States::py1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Y 1-eigenstate  $|y-\rangle\langle y-|$ .

#### 7.49.5.16 pz0

```
cmat qpp::States::pz0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Z 0-eigenstate  $|0\rangle\langle 0|$ .

#### 7.49.5.17 pz1

```
cmat qpp::States::pz1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Z 1-eigenstate  $|1\rangle\langle 1|$ .

#### 7.49.5.18 W

```
ket qpp::States::W {ket::Zero(8)}
```

W state.

#### 7.49.5.19 x0

```
ket qpp::States::x0 {ket::Zero(2)}
```

Pauli Sigma-X 0-eigenstate  $|+\rangle$

#### 7.49.5.20 x1

```
ket qpp::States::x1 {ket::Zero(2)}
```

Pauli Sigma-X 1-eigenstate  $|-\rangle$

#### 7.49.5.21 y0

```
ket qpp::States::y0 {ket::Zero(2)}
```

Pauli Sigma-Y 0-eigenstate  $|y+\rangle$

#### 7.49.5.22 y1

```
ket qpp::States::y1 {ket::Zero(2)}
```

Pauli Sigma-Y 1-eigenstate  $|y-\rangle$

### 7.49.5.23 z0

```
ket qpp::States::z0 {ket::Zero(2)}
```

Pauli Sigma-Z 0-eigenstate  $|0\rangle$

### 7.49.5.24 z1

```
ket qpp::States::z1 {ket::Zero(2)}
```

Pauli Sigma-Z 1-eigenstate  $|1\rangle$

The documentation for this class was generated from the following file:

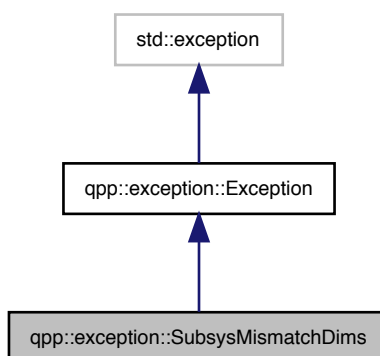
- [classes/states.h](#)

## 7.50 qpp::exception::SubsysMismatchDims Class Reference

Subsystems mismatch dimensions exception.

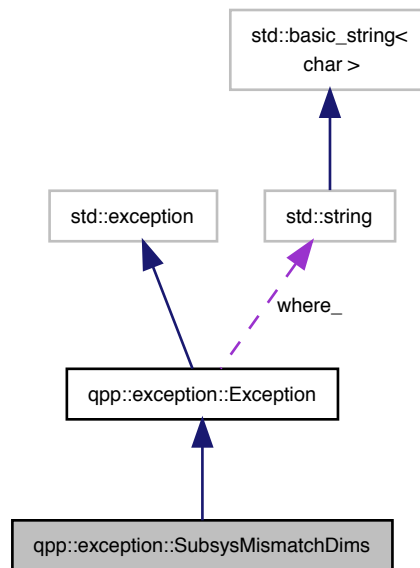
```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::SubsysMismatchDims:





Collaboration diagram for qpp::exception::SubsysMismatchDims:



## Public Member Functions

- `std::string type_description ()` const override  
*Exception type description.*

### 7.50.1 Detailed Description

Subsystems mismatch dimensions exception.

`std::vector<idx>` of subsystem labels has duplicates, or has entries that are larger than the size of the `std::vector<idx>` of dimensions

### 7.50.2 Member Function Documentation

#### 7.50.2.1 type\_description()

```
std::string qpp::exception::SubsysMismatchDims::type_description ( ) const [inline], [override], [virtual]
```

*Exception type description.*

## Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

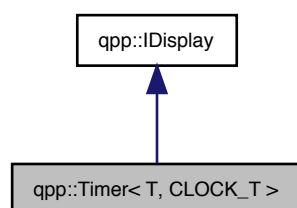
- [classes/exception.h](#)

## 7.51 qpp::Timer< T, CLOCK\_T > Class Template Reference

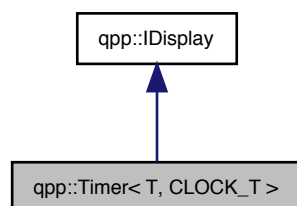
Chronometer.

```
#include <classes/timer.h>
```

Inheritance diagram for qpp::Timer< T, CLOCK\_T >:



Collaboration diagram for qpp::Timer< T, CLOCK\_T >:



## Public Member Functions

- [Timer](#) () noexcept  
*Constructs an instance with the current time as the starting point.*
- void [tic](#) () noexcept  
*Resets the chronometer.*
- const [Timer](#) & [toc](#) () noexcept  
*Stops the chronometer.*
- double [tics](#) () const noexcept  
*Time passed in the duration specified by T.*
- template<typename U = T>  
U [get\\_duration](#) () const noexcept  
*Duration specified by U.*
- [Timer](#) (const [Timer](#) &)=default  
*Default copy constructor.*
- [Timer](#) ([Timer](#) &&)=default  
*Default move constructor.*
- [Timer](#) & [operator=](#) (const [Timer](#) &)=default  
*Default copy assignment operator.*
- [Timer](#) & [operator=](#) ([Timer](#) &&)=default  
*Default move assignment operator.*
- virtual [~Timer](#) ()=default  
*Default virtual destructor.*

## Protected Attributes

- CLOCK\_T::time\_point [start\\_](#)
- CLOCK\_T::time\_point [end\\_](#)

## Private Member Functions

- std::ostream & [display](#) (std::ostream &os) const override  
*qpp::!Display::display() override*

### 7.51.1 Detailed Description

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock>
class qpp::Timer< T, CLOCK_T >
```

Chronometer.

#### Template Parameters

<i>T</i>	Tics duration, default is std::chrono::duration<double, 1>, i.e. seconds in double precision
<i>CLOCK_T</i>	Clock's type, default is std::chrono::steady_clock, not affected by wall clock changes during runtime

## 7.51.2 Constructor & Destructor Documentation

### 7.51.2.1 `Timer()` [1/3]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↵
_clock>
qpp::Timer< T, CLOCK_T >::Timer ( ) [inline], [noexcept]
```

Constructs an instance with the current time as the starting point.

### 7.51.2.2 `Timer()` [2/3]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↵
_clock>
qpp::Timer< T, CLOCK_T >::Timer (
    const Timer< T, CLOCK_T > & ) [default]
```

Default copy constructor.

### 7.51.2.3 `Timer()` [3/3]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↵
_clock>
qpp::Timer< T, CLOCK_T >::Timer (
    Timer< T, CLOCK_T > && ) [default]
```

Default move constructor.

### 7.51.2.4 `~Timer()`

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↵
_clock>
virtual qpp::Timer< T, CLOCK_T >::~~Timer ( ) [virtual], [default]
```

Default virtual destructor.

## 7.51.3 Member Function Documentation

### 7.51.3.1 `display()`

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↵
_clock>
std::ostream& qpp::Timer< T, CLOCK_T >::display (
    std::ostream & os ) const [inline], [override], [private], [virtual]
```

`qpp::IDisplay::display()` override

## Parameters

<code>os</code>	Output stream
-----------------	---------------

## Returns

Writes to the output stream the number of tics (specified by `T`) that passed between the instantiation/reset and invocation of `qpp::Timer::toc()`.

Implements `qpp::IDisplay`.

7.51.3.2 `get_duration()`

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_
_clock>
template<typename U = T>
U qpp::Timer< T, CLOCK_T >::get_duration ( ) const [inline], [noexcept]
```

Duration specified by `U`.

## Template Parameters

<code>U</code>	Duration, default is <code>T</code> , which defaults to <code>std::chrono::duration&lt;double, 1&gt;</code> , i.e. seconds in double precision
----------------	--

## Returns

Duration that passed between the instantiation/reset and invocation of `qpp::Timer::toc()`

7.51.3.3 `operator=()` [1/2]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_
_clock>
Timer& qpp::Timer< T, CLOCK_T >::operator= (
    const Timer< T, CLOCK_T > & ) [default]
```

Default copy assignment operator.

7.51.3.4 `operator=()` [2/2]

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_
_clock>
Timer& qpp::Timer< T, CLOCK_T >::operator= (
    Timer< T, CLOCK_T > && ) [default]
```

Default move assignment operator.

### 7.51.3.5 tic()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↵
_clock>
void qpp::Timer< T, CLOCK_T >::tic ( ) [inline], [noexcept]
```

Resets the chronometer.

Resets the starting/ending point to the current time

### 7.51.3.6 tics()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↵
_clock>
double qpp::Timer< T, CLOCK_T >::tics ( ) const [inline], [noexcept]
```

Time passed in the duration specified by T.

#### Returns

Number of tics (specified by T) that passed between the instantiation/reset and invocation of `qpp::Timer::toc()`

### 7.51.3.7 toc()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↵
_clock>
const Timer& qpp::Timer< T, CLOCK_T >::toc ( ) [inline], [noexcept]
```

Stops the chronometer.

Set the current time as the ending point

#### Returns

Current instance

## 7.51.4 Member Data Documentation

### 7.51.4.1 end\_

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↵
_clock>
CLOCK_T::time_point qpp::Timer< T, CLOCK_T >::end_ [protected]
```

## 7.51.4.2 start\_

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↵_clock>
CLOCK_T::time_point qpp::Timer< T, CLOCK_T >::start_ [protected]
```

The documentation for this class was generated from the following file:

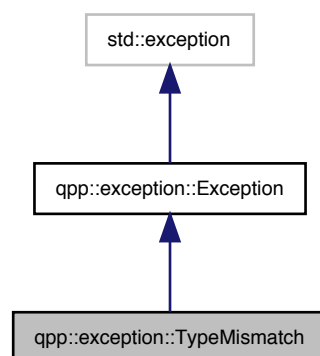
- [classes/timer.h](#)

## 7.52 qpp::exception::TypeMismatch Class Reference

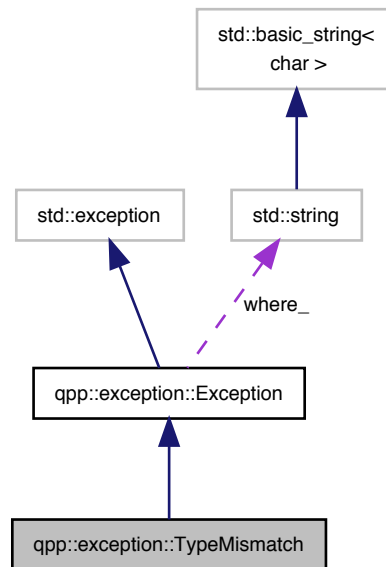
Type mismatch exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::TypeMismatch:



Collaboration diagram for `qpp::exception::TypeMismatch`:



## Public Member Functions

- `std::string type_description ()` const override  
*Exception type description.*

### 7.52.1 Detailed Description

Type mismatch exception.

Scalar types do not match

### 7.52.2 Member Function Documentation

#### 7.52.2.1 type\_description()

```
std::string qpp::exception::TypeMismatch::type_description ( ) const [inline], [override], [virtual]
```

*Exception type description.*

#### Returns

*Exception type description*

Implements `qpp::exception::Exception`.

The documentation for this class was generated from the following file:

- `classes/exception.h`

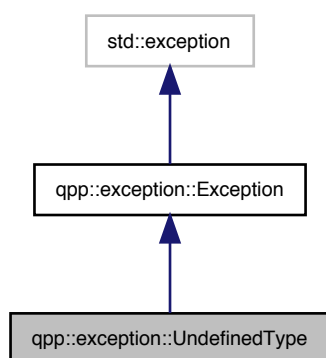


## 7.53 qpp::exception::UndefinedType Class Reference

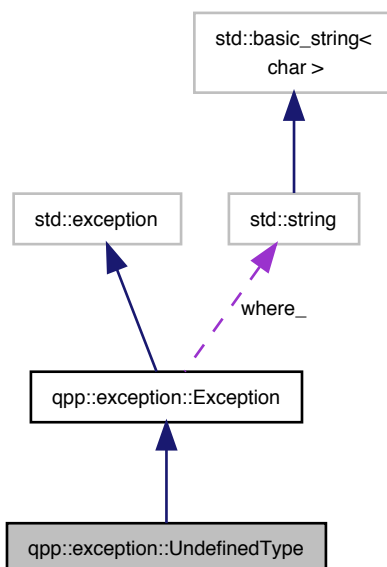
Not defined for this type exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::UndefinedType:



Collaboration diagram for qpp::exception::UndefinedType:



## Public Member Functions

- `std::string type\_description () const` override  
*[Exception](#) type description.*

### 7.53.1 Detailed Description

Not defined for this type exception.

Templated specialization is not defined for this type

### 7.53.2 Member Function Documentation

#### 7.53.2.1 `type_description()`

```
std::string qpp::exception::UndefinedType::type_description ( ) const [inline], [override],  
[virtual]
```

[Exception](#) type description.

#### Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

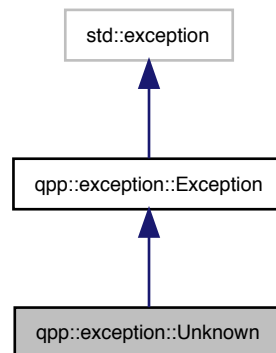
- `classes/exception.h`

## 7.54 `qpp::exception::Unknown` Class Reference

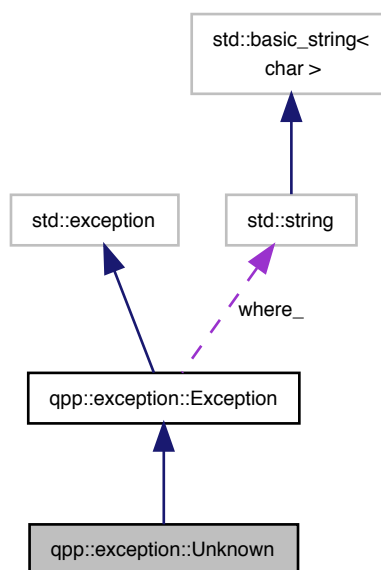
[Unknown](#) exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::Unknown:



Collaboration diagram for qpp::exception::Unknown:



## Public Member Functions

- `std::string type\_description () const` override  
*[Exception](#) type description.*

### 7.54.1 Detailed Description

[Unknown](#) exception.

Thrown when no other exception is suitable (not recommended, it is better to define another suitable exception type)

### 7.54.2 Member Function Documentation

#### 7.54.2.1 `type_description()`

```
std::string qpp::exception::Unknown::type_description ( ) const [inline], [override], [virtual]
```

[Exception](#) type description.

#### Returns

[Exception](#) type description

Implements [qpp::exception::Exception](#).

The documentation for this class was generated from the following file:

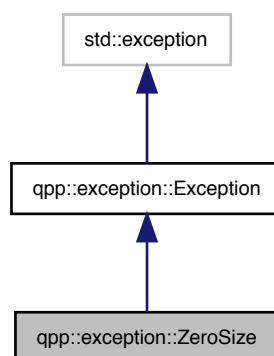
- [classes/exception.h](#)

## 7.55 `qpp::exception::ZeroSize` Class Reference

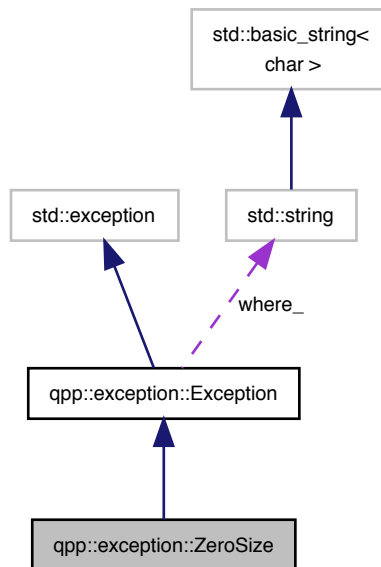
Object has zero size exception.

```
#include <classes/exception.h>
```

Inheritance diagram for `qpp::exception::ZeroSize`:



Collaboration diagram for qpp::exception::ZeroSize:



## Public Member Functions

- `std::string type_description () const` override  
*Exception type description.*

### 7.55.1 Detailed Description

Object has zero size exception.

Zero sized object, e.g. empty Eigen::Matrix or std::vector with no elements

### 7.55.2 Member Function Documentation

#### 7.55.2.1 type\_description()

```
std::string qpp::exception::ZeroSize::type_description ( ) const [inline], [override], [virtual]
```

*Exception type description.*

Returns

*Exception type description*

Implements `qpp::exception::Exception`.

The documentation for this class was generated from the following file:

- `classes/exception.h`



## Chapter 8

# File Documentation

### 8.1 classes/codes.h File Reference

Quantum error correcting codes.

#### Classes

- class [qpp::Codes](#)  
*const Singleton class that defines quantum error correcting codes*

#### Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

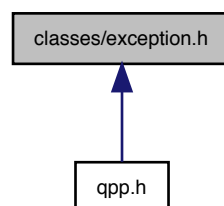
#### 8.1.1 Detailed Description

Quantum error correcting codes.

### 8.2 classes/exception.h File Reference

Exceptions.

This graph shows which files directly or indirectly include this file:



## Classes

- class [qpp::exception::Exception](#)  
*Base class for generating Quantum++ custom exceptions.*
- class [qpp::exception::Unknown](#)  
*Unknown exception.*
- class [qpp::exception::ZeroSize](#)  
*Object has zero size exception.*
- class [qpp::exception::MatrixNotSquare](#)  
*Matrix is not square exception.*
- class [qpp::exception::MatrixNotCvector](#)  
*Matrix is not a column vector exception.*
- class [qpp::exception::MatrixNotRvector](#)  
*Matrix is not a row vector exception.*
- class [qpp::exception::MatrixNotVector](#)  
*Matrix is not a vector exception.*
- class [qpp::exception::MatrixNotSquareNorCvector](#)  
*Matrix is not square nor column vector exception.*
- class [qpp::exception::MatrixNotSquareNorRvector](#)  
*Matrix is not square nor row vector exception.*
- class [qpp::exception::MatrixNotSquareNorVector](#)  
*Matrix is not square nor vector exception.*
- class [qpp::exception::MatrixMismatchSubsys](#)  
*Matrix mismatch subsystems exception.*
- class [qpp::exception::DimsInvalid](#)  
*Invalid dimension(s) exception.*
- class [qpp::exception::DimsNotEqual](#)  
*Dimensions not equal exception.*
- class [qpp::exception::DimsMismatchMatrix](#)  
*Dimension(s) mismatch matrix size exception.*
- class [qpp::exception::DimsMismatchCvector](#)  
*Dimension(s) mismatch column vector size exception.*
- class [qpp::exception::DimsMismatchRvector](#)  
*Dimension(s) mismatch row vector size exception.*
- class [qpp::exception::DimsMismatchVector](#)  
*Dimension(s) mismatch vector size exception.*
- class [qpp::exception::SubsysMismatchDims](#)  
*Subsystems mismatch dimensions exception.*
- class [qpp::exception::PermInvalid](#)  
*Invalid permutation exception.*
- class [qpp::exception::PermMismatchDims](#)  
*Permutation mismatch dimensions exception.*
- class [qpp::exception::NotQubitMatrix](#)  
*Matrix is not 2 x 2 exception.*
- class [qpp::exception::NotQubitCvector](#)  
*Column vector is not 2 x 1 exception.*
- class [qpp::exception::NotQubitRvector](#)  
*Row vector is not 1 x 2 exception.*
- class [qpp::exception::NotQubitVector](#)  
*Vector is not 2 x 1 nor 1 x 2 exception.*
- class [qpp::exception::NotQubitSubsys](#)



- Subsystems are not qubits exception.*
- class [qpp::exception::NotBipartite](#)  
*Not bi-partite exception.*
- class [qpp::exception::NoCodeword](#)  
*Codeword does not exist exception.*
- class [qpp::exception::OutOfRange](#)  
*Parameter out of range exception.*
- class [qpp::exception::TypeMismatch](#)  
*Type mismatch exception.*
- class [qpp::exception::SizeMismatch](#)  
*Size mismatch exception.*
- class [qpp::exception::UndefinedType](#)  
*Not defined for this type exception.*
- class [qpp::exception::CustomException](#)  
*Custom exception.*

## Namespaces

- [qpp](#)  
*Quantum++ main namespace.*
- [qpp::exception](#)  
*Quantum++ exception hierarchy namespace.*

### 8.2.1 Detailed Description

Exceptions.

## 8.3 classes/gates.h File Reference

Quantum gates.

## Classes

- class [qpp::Gates](#)  
*const Singleton class that implements most commonly used gates*

## Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

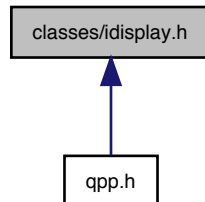
### 8.3.1 Detailed Description

Quantum gates.

## 8.4 classes/ideisplay.h File Reference

Display interface via the non-virtual interface (NVI)

This graph shows which files directly or indirectly include this file:



### Classes

- class [qpp::IDisplay](#)  
*Abstract class (interface) that mandates the definition of virtual `std::ostream& display(std::ostream& os) const`.*

### Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

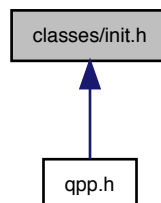
#### 8.4.1 Detailed Description

Display interface via the non-virtual interface (NVI)

## 8.5 classes/init.h File Reference

Initialization.

This graph shows which files directly or indirectly include this file:



## Classes

- class [qpp::Init](#)  
*const Singleton class that performs additional initializations/cleanups*

## Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

### 8.5.1 Detailed Description

Initialization.

## 8.6 classes/random\_devices.h File Reference

Random devices.

## Classes

- class [qpp::RandomDevices](#)  
*Singleton class that manages the source of randomness in the library.*

## Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

### 8.6.1 Detailed Description

Random devices.

## 8.7 classes/states.h File Reference

Quantum states.

## Classes

- class [qpp::States](#)  
*const Singleton class that implements most commonly used states*

## Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

### 8.7.1 Detailed Description

Quantum states.

## 8.8 classes/timer.h File Reference

Timing.

### Classes

- class [qpp::Timer< T, CLOCK\\_T >](#)  
*Chronometer.*

## Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

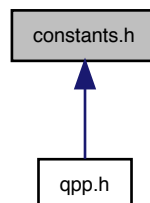
### 8.8.1 Detailed Description

Timing.

## 8.9 constants.h File Reference

Constants.

This graph shows which files directly or indirectly include this file:



## Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

## Functions

- constexpr cplx [qpp::operator"" \\_i](#) (unsigned long long int x) noexcept  
*User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)*
- constexpr cplx [qpp::operator"" \\_i](#) (long double x) noexcept  
*User-defined literal for complex  $i = \sqrt{-1}$  (real overload)*
- cplx [qpp::omega](#) (idx D)  
*D-th root of unity.*

## Variables

- constexpr double [qpp::chop](#) = 1e-10  
*Used in [qpp::disp\(\)](#) for setting to zero numbers that have their absolute value smaller than [qpp::chop](#).*
- constexpr double [qpp::eps](#) = 1e-12  
*Used to decide whether a number or expression in double precision is zero or not.*
- constexpr idx [qpp::maxn](#) = 64  
*Maximum number of allowed qubits/qudits (subsystems)*
- constexpr double [qpp::pi](#) = 3.141592653589793238462643383279502884  
 $\pi$
- constexpr double [qpp::ee](#) = 2.718281828459045235360287471352662497  
*Base of natural logarithm,  $e$ .*
- constexpr double [qpp::infty](#) = std::numeric\_limits<double>::max()  
*Used to denote infinity in double precision.*

## 8.9.1 Detailed Description

Constants.

## 8.10 entanglement.h File Reference

Entanglement functions.

## Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

## Functions

- `template<typename Derived >  
dyn_col_vect< double > qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`  
*Schmidt coefficients of the bi-partite pure state A.*
- `template<typename Derived >  
dyn_col_vect< double > qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, idx d=2)`  
*Schmidt coefficients of the bi-partite pure state A.*
- `template<typename Derived >  
cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`  
*Schmidt basis on Alice side.*
- `template<typename Derived >  
cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > &A, idx d=2)`  
*Schmidt basis on Alice side.*
- `template<typename Derived >  
cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`  
*Schmidt basis on Bob side.*
- `template<typename Derived >  
cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > &A, idx d=2)`  
*Schmidt basis on Bob side.*
- `template<typename Derived >  
std::vector< double > qpp::schmidtprobs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`  
*Schmidt probabilities of the bi-partite pure state A.*
- `template<typename Derived >  
std::vector< double > qpp::schmidtprobs (const Eigen::MatrixBase< Derived > &A, idx d=2)`  
*Schmidt probabilities of the bi-partite pure state A.*
- `template<typename Derived >  
double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`  
*Entanglement of the bi-partite pure state A.*
- `template<typename Derived >  
double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, idx d=2)`  
*Entanglement of the bi-partite pure state A.*
- `template<typename Derived >  
double qpp::gconcurrence (const Eigen::MatrixBase< Derived > &A)`  
*G-concurrence of the bi-partite pure state A.*
- `template<typename Derived >  
double qpp::negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`  
*Negativity of the bi-partite mixed state A.*
- `template<typename Derived >  
double qpp::negativity (const Eigen::MatrixBase< Derived > &A, idx d=2)`  
*Negativity of the bi-partite mixed state A.*
- `template<typename Derived >  
double qpp::lognegativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`  
*Logarithmic negativity of the bi-partite mixed state A.*
- `template<typename Derived >  
double qpp::lognegativity (const Eigen::MatrixBase< Derived > &A, idx d=2)`  
*Logarithmic negativity of the bi-partite mixed state A.*
- `template<typename Derived >  
double qpp::concurrence (const Eigen::MatrixBase< Derived > &A)`  
*Wootters concurrence of the bi-partite qubit mixed state A.*

### 8.10.1 Detailed Description

Entanglement functions.

## 8.11 entropies.h File Reference

Entropy functions.

### Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

### Functions

- `template<typename Derived >`  
`double qpp::entropy (const Eigen::MatrixBase< Derived > &A)`  
*von-Neumann entropy of the density matrix A*
- `double qpp::entropy (const std::vector< double > &prob)`  
*Shannon entropy of the probability distribution prob.*
- `template<typename Derived >`  
`double qpp::renyi (const Eigen::MatrixBase< Derived > &A, double alpha)`  
*Renyi-  $\alpha$  entropy of the density matrix A, for  $\alpha \geq 0$ .*
- `double qpp::renyi (const std::vector< double > &prob, double alpha)`  
*Renyi-  $\alpha$  entropy of the probability distribution prob, for  $\alpha \geq 0$ .*
- `template<typename Derived >`  
`double qpp::tsallis (const Eigen::MatrixBase< Derived > &A, double q)`  
*Tsallis-  $q$  entropy of the density matrix A, for  $q \geq 0$ .*
- `double qpp::tsallis (const std::vector< double > &prob, double q)`  
*Tsallis-  $q$  entropy of the probability distribution prob, for  $q \geq 0$ .*
- `template<typename Derived >`  
`double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, const std::vector< idx > &dims)`  
*Quantum mutual information between 2 subsystems of a composite system.*
- `template<typename Derived >`  
`double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, idx d=2)`  
*Quantum mutual information between 2 subsystems of a composite system.*

### 8.11.1 Detailed Description

Entropy functions.

## 8.12 experimental/experimental.h File Reference

Experimental/test functions/classes.

```
#include <algorithm>
#include <cassert>
#include <climits>
#include <cstdint>
#include <random>
#include <utility>
#include <vector>
```

### Classes

- class [qpp::experimental::Dynamic\\_bitset](#)
- class [qpp::experimental::Bit\\_circuit](#)
- struct [qpp::experimental::Bit\\_circuit::Gate\\_count](#)

### Namespaces

- [qpp](#)  
*Quantum++ main namespace.*
- [qpp::experimental](#)  
*Experimental/test functions/classes, do not use or modify.*

### Typedefs

- using [idx](#) = `std::size_t`

#### 8.12.1 Detailed Description

Experimental/test functions/classes.

#### 8.12.2 Typedef Documentation

##### 8.12.2.1 idx

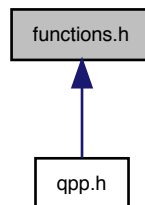
```
using idx = std::size_t
```



## 8.13 functions.h File Reference

Generic quantum computing functions.

This graph shows which files directly or indirectly include this file:



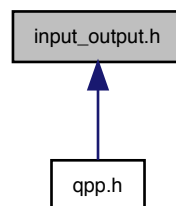
### 8.13.1 Detailed Description

Generic quantum computing functions.

## 8.14 input\_output.h File Reference

Input/output functions.

This graph shows which files directly or indirectly include this file:



## Namespaces

- [qpp](#)

*Quantum++ main namespace.*

## Functions

- `template<typename Derived >`  
`internal::IOManipEigen qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)`  
*Eigen expression ostream manipulator.*
- `internal::IOManipEigen qpp::disp (cplx z, double chop=qpp::chop)`  
*Complex number ostream manipulator.*
- `template<typename InputIterator >`  
`internal::IOManipRange< InputIterator > qpp::disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[" , const std::string &end="]")`  
*Range ostream manipulator.*
- `template<typename Container >`  
`internal::IOManipRange< typename Container::const_iterator > qpp::disp (const Container &c, const std::string &separator, const std::string &start="[" , const std::string &end="]", typename std::enable_if< is_iterable< Container >::value >::type !=nullptr)`  
*Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.*
- `template<typename PointerType >`  
`internal::IOManipPointer< PointerType > qpp::disp (const PointerType *p, idx N, const std::string &separator, const std::string &start="[" , const std::string &end="]")`  
*C-style pointer ostream manipulator.*
- `template<typename Derived >`  
`void qpp::save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)`  
*Saves Eigen expression to a binary file (internal format) in double precision.*
- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > qpp::load (const std::string &fname)`  
*Loads Eigen matrix from a binary file (internal format) in double precision.*

### 8.14.1 Detailed Description

Input/output functions.

## 8.15 instruments.h File Reference

Measurement functions.

## Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

## Functions

- `template<typename Derived >`  
`dyn_col_vect< typename Derived::Scalar > qpp::ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, const std::vector< idx > &dims)`  
*Generalized inner product.*
- `template<typename Derived >`  
`dyn_col_vect< typename Derived::Scalar > qpp::ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, idx d=2)`  
*Generalized inner product.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)`  
*Measures the state A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)`  
*Measures the state A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &U)`  
*Measures the state A in the orthonormal basis specified by the unitary matrix U.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)`  
*Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)`  
*Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)`  
*Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)`  
*Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, const std::vector< idx > &dims)`  
*Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.*
- `template<typename Derived >`  
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, idx d=2)`  
*Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.*
- `template<typename Derived >`  
`std::tuple< std::vector< idx >, double, cmat > qpp::measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, std::vector< idx > dims)`  
*Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.*

- `template<typename Derived >`  
`std::tuple< std::vector< idx >, double, cmat > qpp::measure\_seq (const Eigen::MatrixBase< Derived > &A,`  
`std::vector< idx > subsys, idx d=2)`

*Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.*

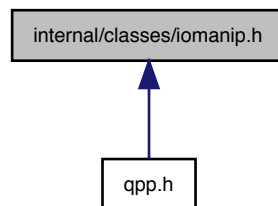
### 8.15.1 Detailed Description

Measurement functions.

## 8.16 internal/classes/iomanip.h File Reference

Input/output manipulators.

This graph shows which files directly or indirectly include this file:



### Classes

- class [qpp::internal::IOManipRange< InputIterator >](#)
- class [qpp::internal::IOManipPointer< PointerType >](#)
- class [qpp::internal::IOManipEigen](#)

### Namespaces

- [qpp](#)  
*Quantum++ main namespace.*
- [qpp::internal](#)  
*Internal utility functions, do not use them directly or modify them.*

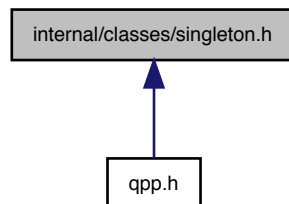
### 8.16.1 Detailed Description

Input/output manipulators.

## 8.17 internal/classes/singleton.h File Reference

Singleton pattern via CRTP.

This graph shows which files directly or indirectly include this file:



### Classes

- class [qpp::internal::Singleton< T >](#)  
*[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)*

### Namespaces

- [qpp](#)  
*Quantum++ main namespace.*
- [qpp::internal](#)  
*Internal utility functions, do not use them directly or modify them.*

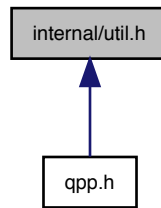
#### 8.17.1 Detailed Description

Singleton pattern via CRTP.

## 8.18 internal/util.h File Reference

Internal utility functions.

This graph shows which files directly or indirectly include this file:



## Classes

- struct [qpp::internal::Display\\_Impl\\_](#)

## Namespaces

- [qpp](#)  
*Quantum++ main namespace.*
- [qpp::internal](#)  
*Internal utility functions, do not use them directly or modify them.*

## Functions

- void [qpp::internal::n2multiidx](#) ([idx](#) n, [idx](#) numdims, const [idx](#) \*const dims, [idx](#) \*result) noexcept
- [idx](#) [qpp::internal::multiidx2n](#) (const [idx](#) \*const midx, [idx](#) numdims, const [idx](#) \*const dims) noexcept
- template<typename Derived >  
bool [qpp::internal::check\\_square\\_mat](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [qpp::internal::check\\_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [qpp::internal::check\\_rvector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [qpp::internal::check\\_cvector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename T >  
bool [qpp::internal::check\\_nonzero\\_size](#) (const T &x) noexcept
- template<typename T1 , typename T2 >  
bool [qpp::internal::check\\_matching\\_sizes](#) (const T1 &lhs, const T2 &rhs) noexcept
- bool [qpp::internal::check\\_dims](#) (const std::vector< [idx](#) > &dims)
- template<typename Derived >  
bool [qpp::internal::check\\_dims\\_match\\_mat](#) (const std::vector< [idx](#) > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >  
bool [qpp::internal::check\\_dims\\_match\\_cvect](#) (const std::vector< [idx](#) > &dims, const Eigen::MatrixBase< Derived > &A)

- `template<typename Derived >`  
`bool qpp::internal::check_dims_match_rvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)`
- `bool qpp::internal::check_eq_dims (const std::vector< idx > &dims, idx dim) noexcept`
- `bool qpp::internal::check_subsys_match_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)`
- `template<typename Derived >`  
`bool qpp::internal::check_qubit_matrix (const Eigen::MatrixBase< Derived > &A) noexcept`
- `template<typename Derived >`  
`bool qpp::internal::check_qubit_cvector (const Eigen::MatrixBase< Derived > &A) noexcept`
- `template<typename Derived >`  
`bool qpp::internal::check_qubit_rvector (const Eigen::MatrixBase< Derived > &A) noexcept`
- `template<typename Derived >`  
`bool qpp::internal::check_qubit_vector (const Eigen::MatrixBase< Derived > &A) noexcept`
- `bool qpp::internal::check_perm (const std::vector< idx > &perm)`
- `template<typename Derived1 , typename Derived2 >`  
`dyn_mat< typename Derived1::Scalar > qpp::internal::kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
- `template<typename Derived1 , typename Derived2 >`  
`dyn_mat< typename Derived1::Scalar > qpp::internal::dirsum2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
- `template<typename T >`  
`void qpp::internal::variadic_vector_emplace (std::vector< T > &)`
- `template<typename T , typename First , typename ... Args>`  
`void qpp::internal::variadic_vector_emplace (std::vector< T > &v, First &&first, Args &&... args)`
- `idx qpp::internal::get_num_subsys (idx sz, idx d)`
- `idx qpp::internal::get_dim_subsys (idx sz, idx N)`

### 8.18.1 Detailed Description

Internal utility functions.

## 8.19 MATLAB/matlab.h File Reference

Input/output interfacing with MATLAB.

```
#include "mat.h"
#include "mex.h"
```

### Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

## Functions

- `template<typename Derived >`  
`std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< cplx > >::type qpp::loadMATLAB (const std::string &mat_file, const std::string &var_name)`  
*Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.*
- `template<typename Derived >`  
`std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< typename Derived::Scalar > >::type qpp::loadMATLAB (const std::string &mat_file, const std::string &var_name)`  
*Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.*
- `template<typename Derived >`  
`std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value >::type qpp::saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`  
*Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.*
- `template<typename Derived >`  
`std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value >::type qpp::saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`  
*Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.*

### 8.19.1 Detailed Description

Input/output interfacing with MATLAB.

## 8.20 number\_theory.h File Reference

Number theory functions.

## Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

## Functions

- `std::vector< int > qpp::x2contfrac (double x, idx N, idx cut=1e5)`  
*Simple continued fraction expansion.*
- `double qpp::contfrac2x (const std::vector< int > &cf, idx N=idx(-1))`  
*Real representation of a simple continued fraction.*
- `bigint qpp::gcd (bigint a, bigint b)`  
*Greatest common divisor of two integers.*
- `bigint qpp::gcd (const std::vector< bigint > &as)`  
*Greatest common divisor of a list of integers.*
- `bigint qpp::lcm (bigint a, bigint b)`  
*Least common multiple of two integers.*
- `bigint qpp::lcm (const std::vector< bigint > &as)`  
*Least common multiple of a list of integers.*



- `std::vector< idx > qpp::invperm` (const `std::vector< idx > &perm`)  
*Inverse permutation.*
- `std::vector< idx > qpp::compperm` (const `std::vector< idx > &perm`, const `std::vector< idx > &sigma`)  
*Compose permutations.*
- `std::vector< bigint > qpp::factors` (bigint a)  
*Prime factor decomposition.*
- `bigint qpp::modmul` (bigint a, bigint b, bigint p)  
*Modular multiplication without overflow.*
- `bigint qpp::modpow` (bigint a, bigint n, bigint p)  
*Fast integer power modulo p based on the SQUARE-AND-MULTIPLY algorithm.*
- `std::tuple< bigint, bigint, bigint > qpp::egcd` (bigint a, bigint b)  
*Extended greatest common divisor of two integers.*
- `bigint qpp::modinv` (bigint a, bigint p)  
*Modular inverse of a mod p.*
- `bool qpp::isprime` (bigint p, `idx` k=80)  
*Primality test based on the Miller-Rabin's algorithm.*
- `bigint qpp::randprime` (bigint a, bigint b, `idx` N=1000)  
*Generates a random big prime uniformly distributed in the interval [a, b].*

### 8.20.1 Detailed Description

Number theory functions.

## 8.21 operations.h File Reference

Quantum operation functions.

### Namespaces

- `qpp`  
*Quantum++ main namespace.*

### Functions

- `template<typename Derived1 , typename Derived2 >`  
`dyn_mat< typename Derived1::Scalar > qpp::applyCTRL` (const `Eigen::MatrixBase< Derived1 > &state`, const `Eigen::MatrixBase< Derived2 > &A`, const `std::vector< idx > &ctrl`, const `std::vector< idx > &subsys`, const `std::vector< idx > &dims`)  
*Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.*
- `template<typename Derived1 , typename Derived2 >`  
`dyn_mat< typename Derived1::Scalar > qpp::applyCTRL` (const `Eigen::MatrixBase< Derived1 > &state`, const `Eigen::MatrixBase< Derived2 > &A`, const `std::vector< idx > &ctrl`, const `std::vector< idx > &subsys`, `idx` d=2)  
*Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.*
- `template<typename Derived1 , typename Derived2 >`  
`dyn_mat< typename Derived1::Scalar > qpp::apply` (const `Eigen::MatrixBase< Derived1 > &state`, const `Eigen::MatrixBase< Derived2 > &A`, const `std::vector< idx > &subsys`, const `std::vector< idx > &dims`)

*Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.*

- `template<typename Derived1 , typename Derived2 >`  
`dyn_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, idx d=2)`

*Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.*

- `template<typename Derived >`  
`cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)`

*Applies the channel specified by the set of Kraus operators Ks to the density matrix A.*

- `template<typename Derived >`  
`cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

*Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.*

- `template<typename Derived >`  
`cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)`

*Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix A.*

- `cmat qpp::kraus2super (const std::vector< cmat > &Ks)`

*Superoperator matrix.*

- `cmat qpp::kraus2choi (const std::vector< cmat > &Ks)`

*Choi matrix.*

- `std::vector< cmat > qpp::choi2kraus (const cmat &A)`

*Orthogonal Kraus operators from Choi matrix.*

- `cmat qpp::choi2super (const cmat &A)`

*Converts Choi matrix to superoperator matrix.*

- `cmat qpp::super2choi (const cmat &A)`

*Converts superoperator matrix to Choi matrix.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`

*Partial trace.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, idx d=2)`

*Partial trace.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`

*Partial trace.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, idx d=2)`

*Partial trace.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

*Partial trace.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)`

*Partial trace.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

*Partial transpose.*

- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const`  
`std::vector< idx > &subsys, idx d=2)`  
*Partial transpose.*
- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const`  
`std::vector< idx > &perm, const std::vector< idx > &dims)`  
*Subsystem permutation.*
- `template<typename Derived >`  
`dyn_mat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const`  
`std::vector< idx > &perm, idx d=2)`  
*Subsystem permutation.*

### 8.21.1 Detailed Description

Quantum operation functions.

## 8.22 qpp.h File Reference

Quantum++ main header file, includes all other necessary headers.

```
#include <algorithm>
#include <cassert>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <exception>
#include <fstream>
#include <functional>
#include <initializer_list>
#include <iomanip>
#include <iterator>
#include <limits>
#include <memory>
#include <numeric>
#include <ostream>
#include <random>
#include <sstream>
#include <stdexcept>
#include <string>
#include <tuple>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "types.h"
#include "classes/exception.h"
#include "constants.h"
#include "traits.h"
#include "classes/ideplay.h"
```

```
#include "internal/util.h"
#include "internal/classes/iomanip.h"
#include "input_output.h"
#include "internal/classes/singleton.h"
#include "classes/init.h"
#include "functions.h"
```

## Namespaces

- [qpp](#)

*Quantum++ main namespace.*

## Macros

- `#define` [QPP\\_UNUSED\\_](#)

### 8.22.1 Detailed Description

Quantum++ main header file, includes all other necessary headers.

### 8.22.2 Macro Definition Documentation

#### 8.22.2.1 QPP\_UNUSED\_

```
#define QPP_UNUSED_
```

## 8.23 random.h File Reference

Randomness-related functions.

## Namespaces

- [qpp](#)

*Quantum++ main namespace.*

## Functions

- double `qpp::rand` (double a, double b)  
*Generates a random real number uniformly distributed in the interval [a, b]*
- bigint `qpp::rand` (bigint a, bigint b)  
*Generates a random big integer uniformly distributed in the interval [a, b].*
- `idx qpp::randidx` (`idx` a=`std::numeric_limits< idx >::min()`, `idx` b=`std::numeric_limits< idx >::max()`)  
*Generates a random index (idx) uniformly distributed in the interval [a, b].*
- `template<typename Derived >`  
`Derived qpp::rand` (`idx` rows, `idx` cols, double a=0, double b=1)  
*Generates a random matrix with entries uniformly distributed in the interval [a, b]*
- `template<>`  
`dmat qpp::rand` (`idx` rows, `idx` cols, double a, double b)  
*Generates a random real matrix with entries uniformly distributed in the interval [a, b], specialization for double matrices (`qpp::dmat`)*
- `template<>`  
`cmat qpp::rand` (`idx` rows, `idx` cols, double a, double b)  
*Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b], specialization for complex matrices (`qpp::cmat`)*
- `template<typename Derived >`  
`Derived qpp::randn` (`idx` rows, `idx` cols, double mean=0, double sigma=1)  
*Generates a random matrix with entries normally distributed in  $N(\text{mean}, \text{sigma})$*
- `template<>`  
`dmat qpp::randn` (`idx` rows, `idx` cols, double mean, double sigma)  
*Generates a random real matrix with entries normally distributed in  $N(\text{mean}, \text{sigma})$ , specialization for double matrices (`qpp::dmat`)*
- `template<>`  
`cmat qpp::randn` (`idx` rows, `idx` cols, double mean, double sigma)  
*Generates a random complex matrix with entries (both real and imaginary) normally distributed in  $N(\text{mean}, \text{sigma})$ , specialization for complex matrices (`qpp::cmat`)*
- double `qpp::randn` (double mean=0, double sigma=1)  
*Generates a random real number (double) normally distributed in  $N(\text{mean}, \text{sigma})$*
- `cmat qpp::randU` (`idx` D=2)  
*Generates a random unitary matrix.*
- `cmat qpp::randV` (`idx` Din, `idx` Dout)  
*Generates a random isometry matrix.*
- `std::vector< cmat > qpp::randkraus` (`idx` N, `idx` D=2)  
*Generates a set of random Kraus operators.*
- `cmat qpp::randH` (`idx` D=2)  
*Generates a random Hermitian matrix.*
- `ket qpp::randket` (`idx` D=2)  
*Generates a random normalized ket (pure state vector)*
- `cmat qpp::randrho` (`idx` D=2)  
*Generates a random density matrix.*
- `std::vector< idx > qpp::randperm` (`idx` N)  
*Generates a random uniformly distributed permutation.*
- `std::vector< double > qpp::randprob` (`idx` N)  
*Generates a random probability vector uniformly distributed over the probability simplex.*

### 8.23.1 Detailed Description

Randomness-related functions.

## 8.24 statistics.h File Reference

Statistics functions.

### Namespaces

- [qpp](#)

*Quantum++ main namespace.*

### Functions

- `std::vector< double > qpp::uniform (idx N)`  
*Uniform probability distribution vector.*
- `std::vector< double > qpp::marginalX (const dmat &probXY)`  
*Marginal distribution.*
- `std::vector< double > qpp::marginalY (const dmat &probXY)`  
*Marginal distribution.*
- `template<typename Container >`  
`double qpp::avg (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↔`  
`iterable< Container >::value >::type !=nullptr)`  
*Average.*
- `template<typename Container >`  
`double qpp::cov (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if<`  
`is_iterable< Container >::value >::type !=nullptr)`  
*Covariance.*
- `template<typename Container >`  
`double qpp::var (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↔`  
`iterable< Container >::value >::type !=nullptr)`  
*Variance.*
- `template<typename Container >`  
`double qpp::sigma (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↔`  
`iterable< Container >::value >::type !=nullptr)`  
*Standard deviation.*
- `template<typename Container >`  
`double qpp::cor (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if<`  
`is_iterable< Container >::value >::type !=nullptr)`  
*Correlation.*

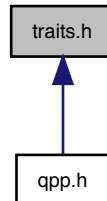
### 8.24.1 Detailed Description

Statistics functions.

## 8.25 traits.h File Reference

Type traits.

This graph shows which files directly or indirectly include this file:



### Classes

- struct [qpp::make\\_void< Ts >](#)  
*Helper for [qpp::to\\_void<>](#) alias template.*
- struct [qpp::is\\_iterable< T, typename >](#)  
*Checks whether T is compatible with an STL-like iterable container.*
- struct [qpp::is\\_iterable< T, to\\_void< decltype\(std::declval< T >\(\).begin\(\)\), decltype\(std::declval< T >\(\).↵end\(\)\), typename T::value\\_type >>](#)  
*Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.*
- struct [qpp::is\\_matrix\\_expression< Derived >](#)  
*Checks whether the type is an Eigen matrix expression.*
- struct [qpp::is\\_complex< T >](#)  
*Checks whether the type is a complex type.*
- struct [qpp::is\\_complex< std::complex< T > >](#)  
*Checks whether the type is a complex number type, specialization for complex types.*

### Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

### Typedefs

- `template<typename... Ts>`  
`using qpp::to\_void = typename make_void< Ts... >::type`  
*Alias template that implements the proposal for void\_t.*

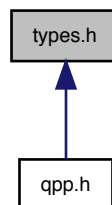
#### 8.25.1 Detailed Description

Type traits.

## 8.26 types.h File Reference

Type aliases.

This graph shows which files directly or indirectly include this file:



### Namespaces

- [qpp](#)  
*Quantum++ main namespace.*

### Typedefs

- using [qpp::idx](#) = std::size\_t  
*Non-negative integer index.*
- using [qpp::bigint](#) = long long int  
*Big integer.*
- using [qpp::cplx](#) = std::complex< double >  
*Complex number in double precision.*
- using [qpp::ket](#) = Eigen::VectorXcd  
*Complex (double precision) dynamic Eigen column vector.*
- using [qpp::bra](#) = Eigen::RowVectorXcd  
*Complex (double precision) dynamic Eigen row vector.*
- using [qpp::cmat](#) = Eigen::MatrixXcd  
*Complex (double precision) dynamic Eigen matrix.*
- using [qpp::dmat](#) = Eigen::MatrixXd  
*Real (double precision) dynamic Eigen matrix.*
- template<typename Scalar >  
using [qpp::dyn\\_mat](#) = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >  
*Dynamic Eigen matrix over the field specified by Scalar.*
- template<typename Scalar >  
using [qpp::dyn\\_col\\_vect](#) = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >  
*Dynamic Eigen column vector over the field specified by Scalar.*
- template<typename Scalar >  
using [qpp::dyn\\_row\\_vect](#) = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >  
*Dynamic Eigen row vector over the field specified by Scalar.*



### 8.26.1 Detailed Description

Type aliases.

## 8.27 /Users/vlad/Dropbox/programming/cpp/qpp/README.md File Reference



# Index

/Users/vlad/Dropbox/programming/cpp/qpp/README↵  
E.md, [249](#)

~Codes

qpp::Codes, [98](#)

~Gates

qpp::Gates, [131](#)

~IDisplay

qpp::IDisplay, [140](#)

~Init

qpp::Init, [142](#)

~RandomDevices

qpp::RandomDevices, [193](#)

~Singleton

qpp::internal::Singleton, [196](#)

~States

qpp::States, [201](#)

~Timer

qpp::Timer, [212](#)

A\_

qpp::internal::IOManipEigen, [145](#)

all

qpp::experimental::Dynamic\_bitset, [116](#)

any

qpp::experimental::Dynamic\_bitset, [116](#)

apply

qpp, [28–30](#)

applyCTRL

qpp, [30, 31](#)

avg

qpp, [32](#)

b00

qpp::States, [204](#)

b01

qpp::States, [204](#)

b10

qpp::States, [204](#)

b11

qpp::States, [204](#)

bigint

qpp, [26](#)

bra

qpp, [26](#)

CNOTba

qpp::Gates, [136](#)

CNOT

qpp::Gates, [136](#)

qpp::experimental::Bit\_circuit, [94](#)

qpp::experimental::Bit\_circuit::Gate\_count, [127](#)

CTRL

qpp::Gates, [131](#)

check\_cvector

qpp::internal, [88](#)

check\_dims

qpp::internal, [88](#)

check\_dims\_match\_cvect

qpp::internal, [88](#)

check\_dims\_match\_mat

qpp::internal, [89](#)

check\_dims\_match\_rvect

qpp::internal, [89](#)

check\_eq\_dims

qpp::internal, [89](#)

check\_matching\_sizes

qpp::internal, [89](#)

check\_nonzero\_size

qpp::internal, [89](#)

check\_perm

qpp::internal, [89](#)

check\_qubit\_cvector

qpp::internal, [90](#)

check\_qubit\_matrix

qpp::internal, [90](#)

check\_qubit\_rvector

qpp::internal, [90](#)

check\_qubit\_vector

qpp::internal, [90](#)

check\_rvector

qpp::internal, [90](#)

check\_square\_mat

qpp::internal, [90](#)

check\_subsys\_match\_dims

qpp::internal, [91](#)

check\_vector

qpp::internal, [91](#)

choi2kraus

qpp, [32](#)

choi2super

qpp, [33](#)

chop

qpp, [84](#)

chop\_

qpp::internal::IOManipEigen, [145](#)

classes/codes.h, [223](#)

classes/exception.h, [223](#)

classes/gates.h, [225](#)

classes/ideisplay.h, [226](#)

- classes/init.h, 226
- classes/random\_devices.h, 227
- classes/states.h, 227
- classes/timer.h, 228
- cmat
  - qpp, 26
- Codes
  - qpp::Codes, 98
- codeword
  - qpp::Codes, 98
- compperm
  - qpp, 33
- concurrence
  - qpp, 33
- constants.h, 228
- contrac2x
  - qpp, 34
- cor
  - qpp, 34
- count
  - qpp::experimental::Dynamic\_bitset, 117
- cov
  - qpp, 35
- cplx
  - qpp, 26
- CustomException
  - qpp::exception::CustomException, 100
- CZ
  - qpp::Gates, 136
- data
  - qpp::experimental::Dynamic\_bitset, 117
- dirsum2
  - qpp::internal, 91
- disp
  - qpp, 35–37
- display
  - qpp::IDisplay, 140
  - qpp::Timer, 212
  - qpp::internal::LOManipEigen, 144
  - qpp::internal::LOManipPointer, 147
  - qpp::internal::LOManipRange, 150
- display\_impl\_
  - qpp::internal::Display\_Impl\_, 113
- dmat
  - qpp, 26
- dyn\_col\_vect
  - qpp, 26
- dyn\_mat
  - qpp, 27
- dyn\_row\_vect
  - qpp, 27
- Dynamic\_bitset
  - qpp::experimental::Dynamic\_bitset, 116
- ee
  - qpp, 84
- egcd
  - qpp, 38
- end\_
  - qpp::Timer, 214
  - qpp::internal::LOManipPointer, 147
  - qpp::internal::LOManipRange, 151
- entanglement
  - qpp, 38, 39
- entanglement.h, 229
- entropies.h, 231
- entropy
  - qpp, 39
- eps
  - qpp, 84
- Exception
  - qpp::exception::Exception, 126
- expandout
  - qpp::Gates, 132, 133
- experimental.h
  - idx, 232
- experimental/experimental.h, 232
- FRED
  - qpp::Gates, 136
  - qpp::experimental::Bit\_circuit, 95
  - qpp::experimental::Bit\_circuit::Gate\_count, 127
- factors
  - qpp, 40
- Fd
  - qpp::Gates, 133
- first\_
  - qpp::internal::LOManipRange, 151
- flip
  - qpp::experimental::Dynamic\_bitset, 117
- functions.h, 233
- GHZ
  - qpp::States, 204
- gate\_count
  - qpp::experimental::Bit\_circuit, 96
- Gates
  - qpp::Gates, 130
- gcd
  - qpp, 40, 41
- gconcurrency
  - qpp, 41
- get
  - qpp::experimental::Dynamic\_bitset, 118
- get\_dim\_subsys
  - qpp::internal, 91
- get\_duration
  - qpp::Timer, 213
- get\_instance
  - qpp::internal::Singleton, 196
- get\_num\_subsys
  - qpp::internal, 91
- get\_prng
  - qpp::RandomDevices, 193
- get\_thread\_local\_instance
  - qpp::internal::Singleton, 197

- H
  - qpp::Gates, 136
- IDisplay
  - qpp::IDisplay, 139, 140
- IOManipEigen
  - qpp::internal::IOManipEigen, 144
- IOManipPointer
  - qpp::internal::IOManipPointer, 146, 147
- IOManipRange
  - qpp::internal::IOManipRange, 150
- Id
  - qpp::Gates, 134
- Id2
  - qpp::Gates, 136
- idx
  - experimental.h, 232
  - qpp, 27
- index\_
  - qpp::experimental::Dynamic\_bitset, 118
- infty
  - qpp, 84
- Init
  - qpp::Init, 142
- input\_output.h, 233
- instruments.h, 234
- internal/classes/iomanip.h, 236
- internal/classes/singleton.h, 237
- internal/util.h, 237
- internal::Singleton< const Codes >
  - qpp::Codes, 99
- internal::Singleton< const Gates >
  - qpp::Gates, 135
- internal::Singleton< const Init >
  - qpp::Init, 143
- internal::Singleton< const States >
  - qpp::States, 204
- internal::Singleton< RandomDevices >
  - qpp::RandomDevices, 194
- invperm
  - qpp, 42
- ip
  - qpp, 42, 43
- isprime
  - qpp, 43
- jn
  - qpp::States, 201
- ket
  - qpp, 27
- kraus2choi
  - qpp, 43
- kraus2super
  - qpp, 44
- kron2
  - qpp::internal, 91
- last\_
  - qpp::internal::IOManipRange, 151
- lcm
  - qpp, 44, 45
- load
  - qpp, 45
  - qpp::RandomDevices, 193
- loadMATLAB
  - qpp, 46
- lognegativity
  - qpp, 47
- MATLAB/matlab.h, 239
- marginalX
  - qpp, 48
- marginalY
  - qpp, 48
- maxn
  - qpp, 85
- measure
  - qpp, 49–53
- measure\_seq
  - qpp, 54
- mes
  - qpp::States, 202
- minus
  - qpp::States, 202
- modinv
  - qpp, 55
- modmul
  - qpp, 56
- modpow
  - qpp, 56
- multiidx2n
  - qpp::internal, 92
- n2multiidx
  - qpp::internal, 92
- N\_
  - qpp::experimental::Dynamic\_bitset, 123
  - qpp::internal::IOManipPointer, 148
- NOT
  - qpp::experimental::Bit\_circuit, 95
  - qpp::experimental::Bit\_circuit::Gate\_count, 127
- negativity
  - qpp, 57
- none
  - qpp::experimental::Dynamic\_bitset, 118
- number\_theory.h, 240
- offset\_
  - qpp::experimental::Dynamic\_bitset, 118
- omega
  - qpp, 57
- one
  - qpp::States, 202
- operations.h, 241
- operator!=
  - qpp::experimental::Dynamic\_bitset, 119
- operator<<

- qpp::IDisplay, 141
- qpp::experimental::Dynamic\_bitset, 122
- operator=
  - qpp::IDisplay, 140
  - qpp::Timer, 213
  - qpp::internal::IOManipPointer, 147
  - qpp::internal::IOManipRange, 150
  - qpp::internal::Singleton, 197
- operator==
  - qpp::experimental::Dynamic\_bitset, 119
- operator""\_i
  - qpp, 59
- p\_
  - qpp::internal::IOManipPointer, 148
- pGHZ
  - qpp::States, 205
- pb00
  - qpp::States, 205
- pb01
  - qpp::States, 205
- pb10
  - qpp::States, 205
- pb11
  - qpp::States, 205
- pi
  - qpp, 85
- plus
  - qpp::States, 203
- prng\_
  - qpp::RandomDevices, 194
- ptrace
  - qpp, 59, 60
- ptrace1
  - qpp, 60, 61
- ptrace2
  - qpp, 61, 62
- ptranspose
  - qpp, 62, 63
- pW
  - qpp::States, 205
- px0
  - qpp::States, 206
- px1
  - qpp::States, 206
- py0
  - qpp::States, 206
- py1
  - qpp::States, 206
- pz0
  - qpp::States, 206
- pz1
  - qpp::States, 206
- QPP\_UNUSED\_
  - qpp.h, 244
- qmutualinfo
  - qpp, 63, 64
- qpp, 17
  - apply, 28–30
  - applyCTRL, 30, 31
  - avg, 32
  - bigint, 26
  - bra, 26
  - choi2kraus, 32
  - choi2super, 33
  - chop, 84
  - cmat, 26
  - compperm, 33
  - concurrency, 33
  - contfrac2x, 34
  - cor, 34
  - cov, 35
  - cplx, 26
  - disp, 35–37
  - dmat, 26
  - dyn\_col\_vect, 26
  - dyn\_mat, 27
  - dyn\_row\_vect, 27
  - ee, 84
  - egcd, 38
  - entanglement, 38, 39
  - entropy, 39
  - eps, 84
  - factors, 40
  - gcd, 40, 41
  - gconcurrency, 41
  - idx, 27
  - infty, 84
  - invperm, 42
  - ip, 42, 43
  - isprime, 43
  - ket, 27
  - kraus2choi, 43
  - kraus2super, 44
  - lcm, 44, 45
  - load, 45
  - loadMATLAB, 46
  - lognegativity, 47
  - marginalX, 48
  - marginalY, 48
  - maxn, 85
  - measure, 49–53
  - measure\_seq, 54
  - modinv, 55
  - modmul, 56
  - modpow, 56
  - negativity, 57
  - omega, 57
  - operator""\_i, 59
  - pi, 85
  - ptrace, 59, 60
  - ptrace1, 60, 61
  - ptrace2, 61, 62
  - ptranspose, 62, 63
  - qmutualinfo, 63, 64
  - rand, 64–66

- randH, 67
- randidx, 67
- randket, 67
- randkraus, 68
- randn, 68–70
- randperm, 70
- randprime, 71
- randprob, 71
- randrho, 71
- randU, 72
- randV, 72
- renyi, 72, 73
- save, 73
- saveMATLAB, 74
- schmidtA, 75
- schmidtB, 76
- schmidtcoeffs, 77
- schmidtprobs, 78
- sigma, 79
- super2choi, 79
- syspermute, 81
- to\_void, 28
- tsallis, 82
- uniform, 83
- var, 83
- x2contfrac, 83
- qpp.h, 243
  - QPP\_UNUSED\_, 244
- qpp::Bit\_circuit, 96
- qpp::Codes, 96
  - ~Codes, 98
  - Codes, 98
  - codeword, 98
  - internal::Singleton< const Codes >, 99
  - Type, 97
- qpp::Dynamic\_bitset, 123
- qpp::Gates, 128
  - ~Gates, 131
  - CNOTba, 136
  - CNOT, 136
  - CTRL, 131
  - CZ, 136
  - expandout, 132, 133
  - FRED, 136
  - Fd, 133
  - Gates, 130
  - H, 136
  - Id, 134
  - Id2, 136
  - internal::Singleton< const Gates >, 135
  - Rn, 134
  - S, 137
  - SWAP, 137
  - T, 137
  - TOF, 137
  - X, 137
  - Xd, 135
  - Y, 137
  - Z, 138
  - Zd, 135
- qpp::IDisplay, 138
  - ~IDisplay, 140
  - display, 140
  - IDisplay, 139, 140
  - operator<<, 141
  - operator=, 140
- qpp::Init, 141
  - ~Init, 142
  - Init, 142
  - internal::Singleton< const Init >, 143
- qpp::RandomDevices, 191
  - ~RandomDevices, 193
  - get\_prng, 193
  - internal::Singleton< RandomDevices >, 194
  - load, 193
  - prng\_, 194
  - RandomDevices, 193
  - rd\_, 194
  - save, 194
- qpp::States, 199
  - ~States, 201
  - b00, 204
  - b01, 204
  - b10, 204
  - b11, 204
  - GHZ, 204
  - internal::Singleton< const States >, 204
  - jn, 201
  - mes, 202
  - minus, 202
  - one, 202
  - pGHZ, 205
  - pb00, 205
  - pb01, 205
  - pb10, 205
  - pb11, 205
  - plus, 203
  - pW, 205
  - px0, 206
  - px1, 206
  - py0, 206
  - py1, 206
  - pz0, 206
  - pz1, 206
  - States, 201
  - W, 207
  - x0, 207
  - x1, 207
  - y0, 207
  - y1, 207
  - z0, 207
  - z1, 208
  - zero, 203
- qpp::Timer
  - ~Timer, 212
  - display, 212

- end\_, 214
- get\_duration, 213
- operator=, 213
- start\_, 214
- tic, 213
- tics, 214
- Timer, 212
- toc, 214
- qpp::Timer< T, CLOCK\_T >, 210
- qpp::exception, 85
- qpp::exception::CustomException, 99
  - CustomException, 100
  - type\_description, 101
  - what\_, 101
- qpp::exception::DimsInvalid, 102
  - type\_description, 103
- qpp::exception::DimsMismatchCvector, 103
  - type\_description, 105
- qpp::exception::DimsMismatchMatrix, 105
  - type\_description, 106
- qpp::exception::DimsMismatchRvector, 107
  - type\_description, 108
- qpp::exception::DimsMismatchVector, 109
  - type\_description, 110
- qpp::exception::DimsNotEqual, 111
  - type\_description, 112
- qpp::exception::Exception, 124
  - Exception, 126
  - type\_description, 126
  - what, 126
  - where\_, 127
- qpp::exception::MatrixMismatchSubsys, 158
  - type\_description, 159
- qpp::exception::MatrixNotCvector, 159
  - type\_description, 161
- qpp::exception::MatrixNotRvector, 161
  - type\_description, 162
- qpp::exception::MatrixNotSquare, 163
  - type\_description, 164
- qpp::exception::MatrixNotSquareNorCvector, 165
  - type\_description, 166
- qpp::exception::MatrixNotSquareNorRvector, 167
  - type\_description, 168
- qpp::exception::MatrixNotSquareNorVector, 169
  - type\_description, 170
- qpp::exception::MatrixNotVector, 171
  - type\_description, 172
- qpp::exception::NoCodeword, 173
  - type\_description, 174
- qpp::exception::NotBipartite, 175
  - type\_description, 176
- qpp::exception::NotQubitCvector, 176
  - type\_description, 178
- qpp::exception::NotQubitMatrix, 178
  - type\_description, 179
- qpp::exception::NotQubitRvector, 180
  - type\_description, 181
- qpp::exception::NotQubitSubsys, 182
  - type\_description, 183
- qpp::exception::NotQubitVector, 184
  - type\_description, 185
- qpp::exception::OutOfRange, 186
  - type\_description, 187
- qpp::exception::PermInvalid, 188
  - type\_description, 189
- qpp::exception::PermMismatchDims, 189
  - type\_description, 191
- qpp::exception::SizeMismatch, 197
  - type\_description, 198
- qpp::exception::SubsysMismatchDims, 208
  - type\_description, 209
- qpp::exception::TypeMismatch, 215
  - type\_description, 216
- qpp::exception::UndefinedType, 217
  - type\_description, 218
- qpp::exception::Unknown, 218
  - type\_description, 220
- qpp::exception::ZeroSize, 220
  - type\_description, 221
- qpp::experimental, 87
- qpp::experimental::Bit\_circuit, 93
  - CNOT, 94
  - FRED, 95
  - gate\_count, 96
  - NOT, 95
  - reset, 95
  - SWAP, 95
  - TOF, 95
  - X, 95
- qpp::experimental::Bit\_circuit::Gate\_count, 127
  - CNOT, 127
  - FRED, 127
  - NOT, 127
  - SWAP, 128
  - TOF, 128
  - X, 128
- qpp::experimental::Dynamic\_bitset, 114
  - all, 116
  - any, 116
  - count, 117
  - data, 117
  - Dynamic\_bitset, 116
  - flip, 117
  - get, 118
  - index\_, 118
  - N\_, 123
  - none, 118
  - offset\_, 118
  - operator!=, 119
  - operator<<, 122
  - operator==, 119
  - rand, 119, 120
  - reset, 120
  - set, 121
  - size, 121
  - storage\_size, 121



- storage\_size\_, 123
- storage\_type, 116
- to\_string, 122
- v\_, 123
- value\_type, 116
- qpp::internal, 87
  - check\_cvector, 88
  - check\_dims, 88
  - check\_dims\_match\_cvect, 88
  - check\_dims\_match\_mat, 89
  - check\_dims\_match\_rvect, 89
  - check\_eq\_dims, 89
  - check\_matching\_sizes, 89
  - check\_nonzero\_size, 89
  - check\_perm, 89
  - check\_qubit\_cvector, 90
  - check\_qubit\_matrix, 90
  - check\_qubit\_rvector, 90
  - check\_qubit\_vector, 90
  - check\_rvector, 90
  - check\_square\_mat, 90
  - check\_subsys\_match\_dims, 91
  - check\_vector, 91
  - dirsum2, 91
  - get\_dim\_subsys, 91
  - get\_num\_subsys, 91
  - kron2, 91
  - multiidx2n, 92
  - n2multiidx, 92
  - variadic\_vector\_emplace, 92
- qpp::internal::Display\_Impl\_, 113
  - display\_impl\_, 113
- qpp::internal::IOManipEigen, 143
  - A\_, 145
  - chop\_, 145
  - display, 144
  - IOManipEigen, 144
- qpp::internal::IOManipPointer
  - display, 147
  - end\_, 147
  - IOManipPointer, 146, 147
  - N\_, 148
  - operator=, 147
  - p\_, 148
  - separator\_, 148
  - start\_, 148
- qpp::internal::IOManipPointer< PointerType >, 145
- qpp::internal::IOManipRange
  - display, 150
  - end\_, 151
  - first\_, 151
  - IOManipRange, 150
  - last\_, 151
  - operator=, 150
  - separator\_, 151
  - start\_, 151
- qpp::internal::IOManipRange< InputIterator >, 149
- qpp::internal::Singleton
  - ~Singleton, 196
  - get\_instance, 196
  - get\_thread\_local\_instance, 197
  - operator=, 197
  - Singleton, 196
- qpp::internal::Singleton< T >, 195
- qpp::is\_complex< std::complex< T > >, 153
- qpp::is\_complex< T >, 152
- qpp::is\_iterable< T, to\_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().begin()), typename T::value\_type > >, 155
- qpp::is\_iterable< T, typename >, 154
- qpp::is\_matrix\_expression< Derived >, 156
- qpp::make\_void
  - type, 157
- qpp::make\_void< Ts >, 157
- rand
  - qpp, 64–66
  - qpp::experimental::Dynamic\_bitset, 119, 120
- randH
  - qpp, 67
- randidx
  - qpp, 67
- randket
  - qpp, 67
- randkraus
  - qpp, 68
- randn
  - qpp, 68–70
- random.h, 244
- RandomDevices
  - qpp::RandomDevices, 193
- randperm
  - qpp, 70
- randprime
  - qpp, 71
- randprob
  - qpp, 71
- randrho
  - qpp, 71
- randU
  - qpp, 72
- randV
  - qpp, 72
- rd\_
  - qpp::RandomDevices, 194
- renyi
  - qpp, 72, 73
- reset
  - qpp::experimental::Bit\_circuit, 95
  - qpp::experimental::Dynamic\_bitset, 120
- Rn
  - qpp::Gates, 134
- S
  - qpp::Gates, 137
- SWAP
  - qpp::Gates, 137

- qpp::experimental::Bit\_circuit, 95
  - qpp::experimental::Bit\_circuit::Gate\_count, 128
- save
  - qpp, 73
  - qpp::RandomDevices, 194
- saveMATLAB
  - qpp, 74
- schmidtA
  - qpp, 75
- schmidtB
  - qpp, 76
- schmidtcoeffs
  - qpp, 77
- schmidtprobs
  - qpp, 78
- separator\_
  - qpp::internal::IOManipPointer, 148
  - qpp::internal::IOManipRange, 151
- set
  - qpp::experimental::Dynamic\_bitset, 121
- sigma
  - qpp, 79
- Singleton
  - qpp::internal::Singleton, 196
- size
  - qpp::experimental::Dynamic\_bitset, 121
- start\_
  - qpp::Timer, 214
  - qpp::internal::IOManipPointer, 148
  - qpp::internal::IOManipRange, 151
- States
  - qpp::States, 201
- statistics.h, 246
- storage\_size
  - qpp::experimental::Dynamic\_bitset, 121
- storage\_size\_
  - qpp::experimental::Dynamic\_bitset, 123
- storage\_type
  - qpp::experimental::Dynamic\_bitset, 116
- super2choi
  - qpp, 79
- syspermute
  - qpp, 81
- T
  - qpp::Gates, 137
- TOF
  - qpp::Gates, 137
  - qpp::experimental::Bit\_circuit, 95
  - qpp::experimental::Bit\_circuit::Gate\_count, 128
- tic
  - qpp::Timer, 213
- tics
  - qpp::Timer, 214
- Timer
  - qpp::Timer, 212
- to\_string
  - qpp::experimental::Dynamic\_bitset, 122
- to\_void
  - qpp, 28
- toc
  - qpp::Timer, 214
- traits.h, 247
- tsallis
  - qpp, 82
- Type
  - qpp::Codes, 97
- type
  - qpp::make\_void, 157
- type\_description
  - qpp::exception::CustomException, 101
  - qpp::exception::DimsInvalid, 103
  - qpp::exception::DimsMismatchCvector, 105
  - qpp::exception::DimsMismatchMatrix, 106
  - qpp::exception::DimsMismatchRvector, 108
  - qpp::exception::DimsMismatchVector, 110
  - qpp::exception::DimsNotEqual, 112
  - qpp::exception::Exception, 126
  - qpp::exception::MatrixMismatchSubsys, 159
  - qpp::exception::MatrixNotCvector, 161
  - qpp::exception::MatrixNotRvector, 162
  - qpp::exception::MatrixNotSquare, 164
  - qpp::exception::MatrixNotSquareNorCvector, 166
  - qpp::exception::MatrixNotSquareNorRvector, 168
  - qpp::exception::MatrixNotSquareNorVector, 170
  - qpp::exception::MatrixNotVector, 172
  - qpp::exception::NoCodeword, 174
  - qpp::exception::NotBipartite, 176
  - qpp::exception::NotQubitCvector, 178
  - qpp::exception::NotQubitMatrix, 179
  - qpp::exception::NotQubitRvector, 181
  - qpp::exception::NotQubitSubsys, 183
  - qpp::exception::NotQubitVector, 185
  - qpp::exception::OutOfRange, 187
  - qpp::exception::PermInvalid, 189
  - qpp::exception::PermMismatchDims, 191
  - qpp::exception::SizeMismatch, 198
  - qpp::exception::SubsysMismatchDims, 209
  - qpp::exception::TypeMismatch, 216
  - qpp::exception::UndefinedType, 218
  - qpp::exception::Unknown, 220
  - qpp::exception::ZeroSize, 221
- types.h, 248
- uniform
  - qpp, 83
- v\_
  - qpp::experimental::Dynamic\_bitset, 123
- value\_type
  - qpp::experimental::Dynamic\_bitset, 116
- var
  - qpp, 83
- variadic\_vector\_emplace
  - qpp::internal, 92
- W
  - qpp::States, 207

what  
    qpp::exception::Exception, [126](#)  
what\_  
    qpp::exception::CustomException, [101](#)  
where\_  
    qpp::exception::Exception, [127](#)  
  
X  
    qpp::Gates, [137](#)  
    qpp::experimental::Bit\_circuit, [95](#)  
    qpp::experimental::Bit\_circuit::Gate\_count, [128](#)  
x0  
    qpp::States, [207](#)  
x1  
    qpp::States, [207](#)  
x2contfrac  
    qpp, [83](#)  
Xd  
    qpp::Gates, [135](#)  
  
Y  
    qpp::Gates, [137](#)  
y0  
    qpp::States, [207](#)  
y1  
    qpp::States, [207](#)  
  
Z  
    qpp::Gates, [138](#)  
z0  
    qpp::States, [207](#)  
z1  
    qpp::States, [208](#)  
Zd  
    qpp::Gates, [135](#)  
zero  
    qpp::States, [203](#)