quantum++ 0.1

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### **Contents**

1	quantum++ - A C++11 quantum computing library			1		
2	Nam	nespace	Index			5
	2.1	Names	space List			5
3	Hier	archica	l Index			7
	3.1	Class	Hierarchy			7
4	Clas	ss Index				9
	4.1	Class	List			9
5	File	Index				11
	5.1	File Lis	st			11
6	Nam	nespace	Docume	ition		13
	6.1	qpp Na	amespace	eference		13
		6.1.1	Typedef	cumentation		21
			6.1.1.1	ra		21
			6.1.1.2	mat		21
			6.1.1.3	plx		21
			6.1.1.4	mat		21
			6.1.1.5	)ynColVect		22
			6.1.1.6	OynMat		22
			6.1.1.7	)ynRowVect		22
			6.1.1.8	et		22
		6.1.2	Function	ocumentation		22
			6.1.2.1	bsm		22
			6.1.2.2	bssq		23
			6.1.2.3	bssq		23
			6.1.2.4	djoint		24
			6.1.2.5	nticomm		24
			6.1.2.6	pply		25
			6107	pplyCTPI		26

iv CONTENTS

6.1.2.8	channel	27
6.1.2.9	channel	28
6.1.2.10	choi	29
6.1.2.11	choi2kraus	30
6.1.2.12	comm	31
6.1.2.13	compperm	32
6.1.2.14	concurrence	33
6.1.2.15	conjugate	34
6.1.2.16	cosm	35
6.1.2.17	cwise	35
6.1.2.18	det	36
6.1.2.19	disp	36
6.1.2.20	disp	37
6.1.2.21	disp	37
6.1.2.22	disp	38
6.1.2.23	disp	38
6.1.2.24	displn	39
6.1.2.25	displn	39
6.1.2.26	displn	40
6.1.2.27	displn	41
6.1.2.28	displn	41
6.1.2.29	entanglement	42
6.1.2.30	evals	43
6.1.2.31	evects	44
6.1.2.32	expm	44
6.1.2.33	funm	45
6.1.2.34	gconcurrence	45
6.1.2.35	grams	46
6.1.2.36	grams	47
6.1.2.37	grams	47
6.1.2.38	hevals	48
6.1.2.39	hevects	48
6.1.2.40	inverse	49
6.1.2.41	invperm	49
6.1.2.42	kron	50
6.1.2.43	kron	50
6.1.2.44	kron	51
6.1.2.45	kron	51
6.1.2.46	kronpow	52
6.1.2.47	load	52

CONTENTS

6.1.2.48	loadMATLABmatrix	53
6.1.2.49	loadMATLABmatrix	53
6.1.2.50	loadMATLABmatrix	53
6.1.2.51	logdet	54
6.1.2.52	logm	54
6.1.2.53	lognegativity	55
6.1.2.54	measure	56
6.1.2.55	measure	56
6.1.2.56	measure	57
6.1.2.57	mket	58
6.1.2.58	mket	58
6.1.2.59	mprj	59
6.1.2.60	mprj	59
6.1.2.61	multiidx2n	60
6.1.2.62	n2multiidx	60
6.1.2.63	negativity	61
6.1.2.64	norm	62
6.1.2.65	omega	62
6.1.2.66	operator""""_i	63
6.1.2.67	operator"""_i	63
6.1.2.68	powm	63
6.1.2.69	prj	64
6.1.2.70	prod	64
6.1.2.71	prod	65
6.1.2.72	ptrace	65
6.1.2.73	ptrace1	66
6.1.2.74	ptrace2	67
6.1.2.75	ptranspose	68
6.1.2.76	qmutualinfo	69
6.1.2.77	rand	70
6.1.2.78	rand	70
6.1.2.79	rand	71
6.1.2.80	rand	71
6.1.2.81	randH	72
6.1.2.82	randint	72
6.1.2.83	randket	73
6.1.2.84	randkraus	73
6.1.2.85	randn	74
6.1.2.86		74
6.1.2.87	randn	75

vi CONTENTS

	6.1.2.88	randn	٠.	•	/5
	6.1.2.89	randperm			76
	6.1.2.90	randrho			76
	6.1.2.91	randU			77
	6.1.2.92	randV			77
	6.1.2.93	renyi			77
	6.1.2.94	reshape			78
	6.1.2.95	save			79
	6.1.2.96	saveMATLABmatrix			79
	6.1.2.97	saveMATLABmatrix			79
	6.1.2.98	saveMATLABmatrix			79
	6.1.2.99	schatten			80
	6.1.2.100	O schmidtcoeff			81
	6.1.2.101	1 schmidtprob			81
	6.1.2.102	2 schmidtU			82
	6.1.2.103	3 schmidtV			83
	6.1.2.104	4 shannon			84
	6.1.2.105	5 sinm			85
	6.1.2.106	6 spectralpowm			85
	6.1.2.107	7 sqrtm			86
	6.1.2.108	8 sum			86
	6.1.2.109	9 sum			87
	6.1.2.110	O super			87
	6.1.2.111	1 svals			88
	6.1.2.112	2 svdU			88
	6.1.2.113	3 svdV			89
	6.1.2.114	4 syspermute			89
	6.1.2.115	5 trace			90
	6.1.2.116	6 transpose			91
	6.1.2.117	7 tsallis			91
6.1.3	Variable [	Documentation			92
	6.1.3.1	chop			92
	6.1.3.2	ee			92
	6.1.3.3	eps			92
	6.1.3.4	gt			92
	6.1.3.5	infty			92
	6.1.3.6	init			93
	6.1.3.7	maxn			93
	6.1.3.8	pi			93
	6.1.3.9	rdevs			93

CONTENTS vii

			6.1.3.10 st
	6.2	qpp::ex	perimental Namespace Reference
		6.2.1	Detailed Description
		6.2.2	Function Documentation
			6.2.2.1 apply
			6.2.2.2 channel
			6.2.2.3 choi
			6.2.2.4 CTRL
			6.2.2.5 randkraus
			6.2.2.6 renyi_inf
			6.2.2.7 super
	6.3	qpp::in	ernal Namespace Reference
		6.3.1	Detailed Description
		6.3.2	Function Documentation
			6.3.2.1 _check_col_vector
			6.3.2.2 _check_dims
			6.3.2.3 _check_dims_match_cvect
			6.3.2.4checkdimsmatchmat
			6.3.2.5 _check_dims_match_rvect
			6.3.2.6 _check_eq_dims
			6.3.2.7 _check_nonzero_size
			6.3.2.8 _check_perm
			6.3.2.9 _check_row_vector
			6.3.2.10 _check_square_mat
			6.3.2.11 _check_subsys_match_dims
			6.3.2.12 _check_vector
			6.3.2.13 _kron2
			6.3.2.14 _multiidx2n
			6.3.2.15 _n2multiidx
			6.3.2.16 variadic_vector_emplace
			6.3.2.17 variadic_vector_emplace
_	Olas	- D	- Andrews
7	7.1		nentation 105 ception Class Reference
	7.1	7.1.1	Detailed Description
		7.1.2	Member Enumeration Documentation
		7.1.2	7.1.2.1 Type
		7.1.3	Constructor & Destructor Documentation
		1.1.3	7.1.3.1 Exception
			·
			7.1.3.2 Exception

viii CONTENTS

	7.1.4	Member Function Documentation
		7.1.4.1 _construct_exception_msg
		7.1.4.2 what
	7.1.5	Member Data Documentation
		7.1.5.1 _custom
		7.1.5.2 _msg
		7.1.5.3 _type
		7.1.5.4 _where
7.2	qpp::G	ates Class Reference
	7.2.1	Detailed Description
	7.2.2	Constructor & Destructor Documentation
		7.2.2.1 Gates
	7.2.3	Member Function Documentation
		7.2.3.1 CTRL
		7.2.3.2 expandout
		7.2.3.3 Fd
		7.2.3.4 ld
		7.2.3.5 Rn
		7.2.3.6 Xd
		7.2.3.7 Zd
	7.2.4	Friends And Related Function Documentation
		7.2.4.1 internal::Singleton < const Gates >
	7.2.5	Member Data Documentation
		7.2.5.1 CNOTab
		7.2.5.2 CNOTba
		7.2.5.3 CZ
		7.2.5.4 FRED
		7.2.5.5 H
		7.2.5.6 ld2
		7.2.5.7 S
		7.2.5.8 SWAP
		7.2.5.9 T
		7.2.5.10 TOF
		7.2.5.11 X
		7.2.5.12 Y
		7.2.5.13 Z
7.3		it Class Reference
	7.3.1	Detailed Description
	7.3.2	Constructor & Destructor Documentation
		7.3.2.1 Init

CONTENTS

		7.3.2.2 ~Init
	7.3.3	Friends And Related Function Documentation
		7.3.3.1 internal::Singleton < const Init >
7.4	qpp::ex	xperimental::Qudit Class Reference
	7.4.1	Constructor & Destructor Documentation
		7.4.1.1 Qudit
	7.4.2	Member Function Documentation
		7.4.2.1 getD
		7.4.2.2 getRho
		7.4.2.3 measure
		7.4.2.4 measure
	7.4.3	Member Data Documentation
		7.4.3.1 _D
		7.4.3.2 _rho
7.5	qpp::R	andomDevices Class Reference
	7.5.1	Detailed Description
	7.5.2	Constructor & Destructor Documentation
		7.5.2.1 RandomDevices
	7.5.3	Friends And Related Function Documentation
		7.5.3.1 internal::Singleton < RandomDevices >
	7.5.4	Member Data Documentation
		7.5.4.1 _rd
		7.5.4.2 _rng
7.6		ternal::Singleton < T > Class Template Reference
	7.6.1	Detailed Description
	7.6.2	Constructor & Destructor Documentation
		7.6.2.1 Singleton
		7.6.2.2 ~Singleton
		7.6.2.3 Singleton
	7.6.3	Member Function Documentation
		7.6.3.1 get_instance
		7.6.3.2 operator=
7.7	qpp::S	tates Class Reference
	7.7.1	Detailed Description
	7.7.2	Constructor & Destructor Documentation
		7.7.2.1 States
	7.7.3	Friends And Related Function Documentation
		7.7.3.1 internal::Singleton < const States >
	7.7.4	Member Data Documentation
		7.7.4.1 b00

X CONTENTS

			7.7.4.2 b01		
			7.7.4.3 b10		
			7.7.4.4 b11		
			7.7.4.5 GHZ		
			7.7.4.6 pb00		
			7.7.4.7 pb01		
			7.7.4.8 pb10		
			7.7.4.9 pb11		
			7.7.4.10 pGHZ		
			7.7.4.11 pW		
			7.7.4.12 px0		
			7.7.4.13 px1		
			7.7.4.14 py0		
			7.7.4.15 py1		
			7.7.4.16 pz0		
			7.7.4.17 pz1		
			7.7.4.18 W		
			7.7.4.19 x0		
			7.7.4.20 x1		
			7.7.4.21 y0		
			7.7.4.22 y1		
			7.7.4.23 z0		
			7.7.4.24 z1		
	7.8	qpp::Ti	mer Class Reference		
		7.8.1	Detailed Description		
		7.8.2	Constructor & Destructor Documentation		
			7.8.2.1 Timer		
		7.8.3	Member Function Documentation		
			7.8.3.1 seconds		
			7.8.3.2 tic		
			7.8.3.3 toc		
		7.8.4	Friends And Related Function Documentation		
			7.8.4.1 operator<<		
		7.8.5	Member Data Documentation		
			7.8.5.1 _end		
			7.8.5.2 _start		
8	File	Docume	entation 13		
•	8.1		/classes/exception.h File Reference		
	8.2		/classes/gates.h File Reference		
	0.2	. Include, siacocorgation in the relevance of the relationship in			

CONTENTS xi

8.3	3 include/classes/init.h File Reference	132
8.4	include/classes/randevs.h File Reference	133
8.5	include/classes/singleton.h File Reference	133
8.6	include/classes/states.h File Reference	134
8.7	7 include/classes/timer.h File Reference	135
8.8	3 include/constants.h File Reference	135
8.9	9 include/entanglement.h File Reference	136
8.1	10 include/entropies.h File Reference	137
8.1	11 include/experimental/classes/qudit.h File Reference	138
8.1	12 include/experimental/test.h File Reference	139
8.1	13 include/functions.h File Reference	140
8.1	4 include/internal/functions.h File Reference	143
8.1	15 include/instruments.h File Reference	144
8.1	16 include/io.h File Reference	145
8.1	17 include/MATLAB/matlab.h File Reference	146
8.1	18 include/operations.h File Reference	147
8.1		
8.2		
8.2		
	22 mainpage.dox File Reference	
0.2	.c. mainpago.dox i no rioletende	102
Index		153

### **Chapter 1**

### quantum++ - A C++11 quantum computing library

```
Version
     0.1
Author
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     (c) 2013 - 2014 Vlad Gheorghiu (vgheorgh@gmail.com)
An example is worth more than one thousand words:)
#include "gpp.h"
// #include "MATLAB/matlab.h" // support for MATLAB
using namespace qpp;
int main()
    // Qudit Teleportation
       ket mes_AB = ket::Zero(D * D); // maximally entangled state resource
for (std::size_t i = 0; i < D; i++)
   mes_AB += mket( { i, i }, D);</pre>
       mes_AB /= std::sqrt((double) D);
       cmat Bell_aA = adjoint( // circuit that measures in the qudit Bell basis
       std::cout << ">> Initial state: " << std::endl;
       displn(psi_a);
ket input_aAB = kron(psi_a, mes_AB); // joint input state aAB
        // output before measurement
       std::discrete_distribution<std::size_t> dd(measured_aA.first.begin(),
       measured_aA.first.end());
std::cout << ">> Measurement probabilities: ";
       displn(measured_aA.first, ", ");
       std::size_t m = dd(rdevs._rng); // sample
auto midx = n2multiidx(m, { D, D });
       std::cout << ">> Measurement result: ";
       displn(midx, " ");
        // conditional result on B before correction
       ket output_m_aAB = apply(output_aAB, prj(mket(midx, D)), { 0, 1 }, 3, D)
               / std::sqrt(measured_aA.first[m]);
       cmat correction_B = powm(gt.Zd(D), midx[0])
                 powm(adjoint(gt.Xd(D)), midx[1]); // correction operator
```

```
// apply correction on B
    output_aAB = apply(output_m_aAB, correction_B, { 2 }, 3, D);
    cmat rho_B = ptracel(prj(output_aAB), { D * D, D });
std::cout << ">> Bob's density operator: " << std::endl;</pre>
    displn(rho_B);
                    ">> Norm difference: " << norm(rho_B - prj(psi_a))
    std::cout <<
              << std::endl; // verification
// Oudit Dense Coding
    ket mes_AB = ket::Zero(D * D); // maximally entangled state resource
    for (std::size_t i = 0; i < D; i++)
  mes_AB += mket( { i, i }, D);</pre>
    mes_AB /= std::sqrt((double) D);
    cmat Bell_AB = adjoint( // circuit that measures in the qudit Bell basis
             gt.CTRL(gt.Xd(D), { 0 }, { 1 }, 2, D)
                         kron(gt.Fd(D), gt.Id(D)));
    // equal probabilities of choosing a message
    std::uniform_int_distribution<std::size_t> uid(0, D * D - 1);
std::size_t m_A = uid(rdevs._rng); // sample, obtain the message index
auto midx = n2multiidx(m_A, { D, D });
std::cout << ">> Alice sent: ";
displn(midx, " ");
    // Alice's operation
    cmat U_A = powm(gt.Zd(D), midx[0]) * powm(adjoint(
  gt.Xd(D)), midx[1]);
// Alice encodes the message
    ket psi_AB = apply(mes_AB, U_A, { 0 }, 2, D);
    // Bob measures the joint system in the qudit Bell basis
    psi\_AB = apply(psi\_AB, Bell\_AB, { 0, 1 }, 2, D);
    auto measured = measure(psi_AB, gt.Id(D * D));
std::cout << ">> Bob measurement probabilities: ";
displn(measured.first, ", ");
    // Bob samples according to the measurement probabilities
    std::discrete_distribution<std::size_t> dd(measured.first.begin(),
             measured.first.end());
    std::size_t m_B = dd(rdevs._rng);
std::cout << ">> Bob received: ";
    displn(n2multiidx(m_B, { D, D }), " ");
// Grover's search algorithm, we time it
    Timer t; // set a timer
std::size_t n = 4; // number of qubits
    std::cout << std::endl << "**** Grover on n = " << n << " qubits ****"
              << std::endl;
    // mark an element randomly
    std::uniform_int_distribution<std::size_t> uid(0, N - 1);
    std::size_t marked = uid(rdevs._rng);
std::cout << ">> Marked state: " << marked << " -> ";
displn(n2multiidx(marked, dims), " ");
     \texttt{ket psi} = \texttt{mket(n2multiidx(0, dims));} \ // \ \texttt{computational |0>^\wedge times n} 
    psi = (kronpow(gt.H, n) * psi).eval(); // apply H^\otimes n, no aliasing
    cmat G = 2 * prj(psi) - gt.Id(N); // Diffusion operator
    // number of queries
    std::size_t nqueries = std::ceil(pi * std::sqrt(N) / 4.);
    std::cout << ">> We run " << nqueries << " queries" << std::endl;
for (std::size_t i = 0; i < nqueries; i++)</pre>
        psi(marked) = -psi(marked); // apply the oracle first, no aliasing psi = (G \star psi).eval(); // then the diffusion operator, no aliasing
    // we now measure the state in the computational basis
    std::cout << ">> Probability of all results: ";
displn(measured.first, ", ");
    std::cout << ">> Let's sample..." << std::endl;
    std::discrete_distribution<std::size_t> dd(measured.first.begin(),
             measured.first.end());
    std::size_t result = dd(rdevs._rng);
if (result == marked)
         std::cout << ">> Hooray, we obtained the correct result: ";
         std::cout << ">> Not there yet... we obtained: ";
    std::cout << result << " -> ";
    displn(n2multiidx(result, dims), " ");
    // stop the timer and display it
```

```
std::cout << ">> It took " << t.toc()
              << " seconds to simulate Grover on " << n << " qubits."
               << std::endl;
}
// Entanglement
     std::cout << std::endl << "**** Entanglement ****" << std::endl;</pre>
    cmat rho = 0.2 * st.pb00 + 0.8 * st.pb11;
std::cout << ">> rho: " << std::endl;</pre>
    displn(rho);
    std::cout << ">> Concurrence of rho: " << concurrence(rho) << std::endl;
std::cout << ">> Negativity of rho: " << negativity(rho, { 2, 2 })</pre>
               << std::end1;
     std::cout << ">>> Logarithimc negativity of rho: "
    << lognegativity(rho, { 2, 2 }) << std::endl;
ket psi = 0.8 * mket( { 0, 0 }) + 0.6 * mket( { 1, 1 });</pre>
    // apply some local random unitaries
psi = kron(randU(2), randU(2)) * psi;
     std::cout << ">> psi: " << std::endl;
    displn(psi);
std::cout << ">> Entanglement of psi: " << entanglement(psi, { 2, 2 })</pre>
              << std::endl;
     std::cout << ">> Concurrence of psi: " << concurrence(prj(psi))
              << std::endl;
     std::cout << ">> G-Concurrence of psi: " << gconcurrence(psi)
               << std::endl;
     std::cout << ">> Schmidt coefficients of psi: " << std::endl;</pre>
    displn(schmidtcoeff(psi, { 2, 2 }));
std::cout << ">>> Schmidt probabilities of psi: " << std::endl;</pre>
    displn(schmidtprob(psi, { 2, 2 }));
cmat U = schmidtU(psi, { 2, 2 });
cmat V = schmidtV(psi, { 2, 2 });
     std::cout << ">> Schmidt vectors on Alice's side: " << std::endl;</pre>
     displn(U);
     std::cout << ">> Schmidt vectors on Bob's side: " << std::endl;
    displn(V);
    std::cout << ">> State psi in the Schmidt basis: " << std::endl;
    displn(adjoint(kron(U, V)) * psi);
     // reconstructed state
     ket psi_from_schmidt = schmidtcoeff(psi, { 2, 2 })(0)
                kron(U.col(0), V.col(0))
               + schmidtcoeff(psi, { 2, 2 })(1) * kron(U.col(1), V.col(1));
    std::cout
               << ">> State psi reconstructed from the Schmidt decomposition: " \,
               << std::endl;
    displn(psi_from_schmidt);
std::cout << ">>> Norm difference: " << norm(psi - psi_from_schmidt)</pre>
               << std::endl;
}
```

4	quantum++ - A C++11 quantum computing library

# Chapter 2

# Namespace Index

Z. I Mailles Dace Lis	2.1	Nam	espace	List
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пеге	15	a iisi	OI 8	all	namespaces	WILLI	briei	descrip	แบบเร.

qpp	
qpp::experimental	
qpp::internal	

6 Namespace Index

# **Chapter 3**

## **Hierarchical Index**

### 3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

d::exception	
qpp::Exception	105
pp::experimental::Qudit	118
pp::internal::Singleton < T >	122
pp::internal::Singleton $<$ const Gates $>$	122
qpp::Gates	109
pp::internal::Singleton < const Init >	122
qpp::Init	116
pp::internal::Singleton < const States >	122
qpp::States	123
pp::internal::Singleton < RandomDevices >	122
qpp::RandomDevices	120
pp::Timer	127

8 **Hierarchical Index** 

## **Chapter 4**

## **Class Index**

### 4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

qpp::Exception	
Generates custom exceptions, used when validating function parameters	105
qpp::Gates	
Const Singleton class that implements most commonly used gates	109
qpp::Init	
Const Singleton class that performs additional initializations/cleanups	116
qpp::experimental::Qudit	118
qpp::RandomDevices	
Singeleton class that manages the source of randomness in the library	120
qpp::internal::Singleton< T >	
Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously	
recurring template pattern)	122
qpp::States	
Const Singleton class that implements most commonly used states	123
qpp::Timer	
Measures time	127

10 Class Index

## **Chapter 5**

## File Index

### 5.1 File List

Here is a list of all files with brief descriptions:

include/constants.n
include/entanglement.h
include/entropies.h
include/functions.h
include/instruments.h
include/io.h
include/operations.h
include/qpp.h
include/random.h
include/types.h
include/classes/exception.h
include/classes/gates.h
include/classes/init.h
include/classes/randevs.h
include/classes/singleton.h
include/classes/states.h
include/classes/timer.h
include/experimental/test.h
include/experimental/classes/qudit.h
include/internal/functions.h
include/MATLAB/matlab.h

12 File Index

### **Chapter 6**

### **Namespace Documentation**

#### 6.1 qpp Namespace Reference

#### **Namespaces**

- · experimental
- internal

#### Classes

class Exception

Generates custom exceptions, used when validating function parameters.

class Gates

const Singleton class that implements most commonly used gates

class Init

const Singleton class that performs additional initializations/cleanups

· class RandomDevices

Singeleton class that manages the source of randomness in the library.

· class States

const Singleton class that implements most commonly used states

class Timer

Measures time.

#### **Typedefs**

```
    using cplx = std::complex < double >
        Complex number in double precision.
```

 $\bullet \ \ \text{template}{<} \text{typename Scalar} >$ 

```
using DynMat = Eigen::Matrix < Scalar, Eigen::Dynamic, Eigen::Dynamic >
```

Dynamic Eigen matrix over the field specified by Scalar.

```
    template<typename Scalar >
        using DynColVect = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >
```

Dynamic Eigen column vector over the field specified by Scalar.

```
    template<typename Scalar >
        using DynRowVect = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >
        Dynamic Eigen row vector over the field specified by Scalar.
```

using ket = DynColVect< cplx >

Complex (double precision) dynamic Eigen column vector.

using bra = DynRowVect< cplx >

Complex (double precision) dynamic Eigen row vector.

using cmat = DynMat< cplx >

Complex (double precision) dynamic Eigen matrix.

using dmat = DynMat< double >

Real (double precision) dynamic Eigen matrix.

#### **Functions**

```
    constexpr std::complex< double > operator""_i (unsigned long long int x)
```

User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)

constexpr std::complex< double > operator""\_i (long double x)

User-defined literal for complex  $i = \sqrt{-1}$  (real overload)

std::complex< double > omega (std::size t D)

D-th root of unity.

template<typename Derived >

DynColVect< cplx > schmidtcoeff (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t
> &dims)

Schmidt coefficients of the bi-partite pure state A.

template<typename Derived >

cmat schmidtU (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &dims)

Schmidt basis on Alice's side.

template<typename Derived >

cmat schmidtV (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)

Schmidt basis on Bob's side.

template<typename Derived >

Schmidt probabilities of the bi-partite pure state A.

 $\bullet \ \ \text{template}{<} \text{typename Derived} >$ 

double entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)

Entanglement of the bi-partite pure state A.

template<typename Derived >

double gconcurrence (const Eigen::MatrixBase< Derived > &A)

G-concurrence of the bi-partite pure state A.

template<typename Derived >

double negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)

Negativity of the bi-partite mixed state A.

template<typename Derived >

Logarithmic negativity of the bi-partite mixed state A.

• template<typename Derived >

double concurrence (const Eigen::MatrixBase< Derived > &A)

Wootters concurrence of the bi-partite qubit mixed state A.

• template<typename Derived >

double shannon (const Eigen::MatrixBase< Derived > &A)

Shannon/von-Neumann entropy of the probability distribution/density matrix A.

template<typename Derived >

 $\mbox{double renyi (const Eigen::MatrixBase} < \mbox{Derived} > \&\mbox{A, double alpha)}$ 

Renyi-  $\alpha$  entropy of the probability distribution/density matrix A, for  $\alpha \geq 0$ .

```
• template<typename Derived >
  double tsallis (const Eigen::MatrixBase< Derived > &A, double alpha)
      Tsallis- \alpha entropy of the probability distribution/density matrix A, for \alpha \geq 0

    template<typename Derived >

  double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &subsysA,
  const std::vector< std::size_t > &subsysB, const std::vector< std::size_t > &dims)
      Quantum mutual information between 2 subsystems of a composite system.
• template<typename Derived >
  DynMat< typename Derived::Scalar > transpose (const Eigen::MatrixBase< Derived > &A)
      Transpose.

    template<typename Derived >

  DynMat< typename Derived::Scalar > conjugate (const Eigen::MatrixBase< Derived > &A)
      Complex conjugate.

    template<typename Derived >

  DynMat< typename Derived::Scalar > adjoint (const Eigen::MatrixBase< Derived > &A)
     Adjoint.

    template<typename Derived >

  DynMat< typename Derived::Scalar > inverse (const Eigen::MatrixBase< Derived > &A)
• template<typename Derived >
  Derived::Scalar trace (const Eigen::MatrixBase< Derived > &A)
      Trace.
• template<typename Derived >
  Derived::Scalar det (const Eigen::MatrixBase < Derived > &A)
     Determinant.
template<typename Derived >
  Derived::Scalar logdet (const Eigen::MatrixBase< Derived > &A)
     Logarithm of the determinant.

    template<typename Derived >

  Derived::Scalar sum (const Eigen::MatrixBase< Derived > &A)
     Element-wise sum of A.

    template<typename Derived >

  {\tt Derived::Scalar\ prod\ (const\ Eigen::MatrixBase<\ Derived>\&A)}
      Element-wise product of A.
• template<typename Derived >
  double norm (const Eigen::MatrixBase< Derived > &A)
     Frobenius norm.

    template<typename Derived >

  DynColVect< cplx > evals (const Eigen::MatrixBase< Derived > &A)
     Eigenvalues.

    template<typename Derived >

  cmat evects (const Eigen::MatrixBase< Derived > &A)
     Eigenvectors.

    template<typename Derived >

  DynColVect< double > hevals (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvalues.

    template<typename Derived >

  cmat hevects (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvectors.

    template<typename Derived >

  DynColVect< double > svals (const Eigen::MatrixBase< Derived > &A)
```

Singular values.

```
• template<typename Derived >
  cmat svdU (const Eigen::MatrixBase< Derived > &A)
     Left singular vectors.
• template<typename Derived >
  cmat svdV (const Eigen::MatrixBase< Derived > &A)
     Right singular vectors.
• template<typename Derived >
  cmat funm (const Eigen::MatrixBase< Derived > &A, cplx(*f)(const cplx &))
     Functional calculus f(A)

    template<typename Derived >

  cmat sqrtm (const Eigen::MatrixBase< Derived > &A)
     Matrix square root.

    template<typename Derived >

  cmat absm (const Eigen::MatrixBase< Derived > &A)
     Matrix absolut value.

    template<typename Derived >

  cmat expm (const Eigen::MatrixBase< Derived > &A)
     Matrix exponential.
• template<typename Derived >
  cmat logm (const Eigen::MatrixBase< Derived > &A)
     Matrix logarithm.

    template<typename Derived >

  cmat sinm (const Eigen::MatrixBase< Derived > &A)
     Matrix sin.
• template<typename Derived >
  cmat cosm (const Eigen::MatrixBase< Derived > &A)
     Matrix cos.
• template<typename Derived >
  cmat spectralpowm (const Eigen::MatrixBase< Derived > &A, const cplx z)
     Matrix power.
 \bullet \ \ \mathsf{template} \mathord{<} \mathsf{typename} \ \mathsf{Derived} >
  DynMat< typename Derived::Scalar > powm (const Eigen::MatrixBase< Derived > &A, std::size_t n)
     Matrix power.
• template<typename Derived >
  double schatten (const Eigen::MatrixBase< Derived > &A, std::size_t p)
     Schatten norm.
• template<typename OutputScalar , typename Derived >
  DynMat< OutputScalar > cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const typename
  Derived::Scalar &))
     Functor.
template<typename T >
  DynMat< typename T::Scalar > kron (const T &head)
     Kronecker product (variadic overload)
• template<typename T , typename... Args>
  DynMat< typename T::Scalar > kron (const T &head, const Args &...tail)
     Kronecker product (variadic overload)

    template<typename Derived >

  DynMat< typename Derived::Scalar > kron (const std::vector< Derived > &As)
     Kronecker product (std::vector overload)

    template<typename Derived >

  DynMat< typename Derived::Scalar > kron (const std::initializer_list< Derived > &As)
```

Kronecker product (std::initializer list overload)

```
    template<typename Derived >

  DynMat< typename Derived::Scalar > kronpow (const Eigen::MatrixBase< Derived > &A, std::size t n)
      Kronecker power.

    template<typename Derived >

  DynMat< typename Derived::Scalar > reshape (const Eigen::MatrixBase< Derived > &A, std::size t rows,
  std::size t cols)
      Reshape.
• template<typename Derived1 , typename Derived2 >
  DynMat< typename Derived1::Scalar > comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::←
  MatrixBase< Derived2 > &B)
      Commutator.

    template<typename Derived1 , typename Derived2 >

  DynMat< typename Derived1::Scalar > anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen←
  ::MatrixBase< Derived2 > &B)
      Anti-commutator.
template<typename Derived >
  DynMat< typename Derived::Scalar > prj (const Eigen::MatrixBase< Derived > &V)
      Projector.

    template<typename Derived >

  DynMat< typename Derived::Scalar > grams (const std::vector< Derived > &Vs)
      Gram-Schmidt orthogonalization (std::vector overload)

    template<typename Derived >

  DynMat< typename Derived::Scalar > grams (const std::initializer_list< Derived > &Vs)
      Gram-Schmidt orthogonalization (std::initializer_list overload)

    template<typename Derived >

  DynMat< typename Derived::Scalar > grams (const Eigen::MatrixBase< Derived > &A)
      Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)

    std::vector< std::size_t > n2multiidx (std::size_t n, const std::vector< std::size_t > &dims)

      Non-negative integer index to multi-index.

    std::size t multiidx2n (const std::vector < std::size t > &midx, const std::vector < std::size t > &dims)

      Multi-index to non-negative integer index.

    ket mket (const std::vector< std::size_t > &mask, const std::vector< std::size_t > &dims)

      Multi-partite qudit ket (different dimensions overload)

    ket mket (const std::vector< std::size t > &mask, std::size t d=2)

      Multi-partite qudit ket (same dimensions overload)

    cmat mprj (const std::vector< std::size_t > &mask, const std::vector< std::size_t > &dims)

      Projector onto multi-partite qudit ket (different dimensions overload)

    cmat mprj (const std::vector < std::size_t > &mask, std::size_t d=2)

      Projector onto multi-partite qudit ket (same dimensions overload)

    std::vector< std::size_t > invperm (const std::vector< std::size_t > &perm)

      Inverse permutation.
• std::vector< std::size t > compperm (const std::vector< std::size t > &perm, const std::vector< std::size t
  > &sigma)
      Compose permutations.

    template<typename InputIterator >

  {\tt std::vector} < {\tt double} > {\tt abssq} \ ({\tt InputIterator} \ {\sf first}, \ {\tt InputIterator} \ {\sf last})
      Computes the absolut values squared of a range of complex numbers.

    template<typename Derived >

  {\it std::} {\it vector} < {\it double} > {\it abssq} \; ({\it const} \; {\it Eigen::} {\it MatrixBase} < {\it Derived} > \& {\it V})
      Computes the absolut values squared of a column vector.

    template<typename InputIterator >

  auto sum (InputIterator first, InputIterator last) -> typename InputIterator::value_type
```

Element-wise sum of a range.

template<typename InputIterator >
 auto prod (InputIterator first, InputIterator last) -> typename InputIterator::value\_type

Element-wise product of a range.

template<typename Derived >

```
std::pair< std::vector< double >
```

, std::vector < cmat > > measure (const Eigen::MatrixBase < Derived > &A, const std::vector < cmat > &Ks)

Measures the state A using the set of Kraus operators Ks.

• template<typename Derived >

```
std::pair < std::vector < double >
```

, std::vector < cmat >> measure (const Eigen::MatrixBase < Derived > &A, const std::initializer\_list < cmat > &Ks)

Measures the state A using the set of Kraus operators Ks (std::initializer\_list overload)

template<typename Derived >

```
std::pair < std::vector < double >
```

, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &M)

Measures the state A in the orthonormal basis specified by the eigenvectors of M.

template<typename InputIterator >

void disp (const InputIterator &first, const InputIterator &last, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a range. Does not add a newline.

template<typename InputIterator >

std::ostream & displn (const InputIterator &first, const InputIterator &last, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a range. Adds a newline.

• template<typename T >

std::ostream & disp (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a standard container that supports std::begin, std::end and forward iteration. Does not add a newline.

• template<typename T >

std::ostream & displn (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a standard container that supports std::begin, std::end and forward iteration. Adds a newline.

• template<typename T >

std::ostream & disp (const T \*x, const std::size\_t n, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a C-style array. Does not add a newline.

 $\bullet \ \ template {<} typename \ T >$ 

std::ostream & displn (const T \*x, const std::size\_t n, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a C-style array. Adds a newline.

• template<typename Derived >

std::ostream & disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop, std::ostream &os=std::cout)

Displays an Eigen expression in matrix friendly form. Does not add a new line.

template<typename Derived >

std::ostream & displn (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop, std::ostream &os=std::cout)

Displays an Eigen expression in matrix friendly form. Adds a newline.

std::ostream & disp (const cplx z, double chop=qpp::chop, std::ostream &os=std::cout)

Displays a number (implicitly converted to std::complex<double>) in friendly form. Does not add a new line.

• std::ostream & displn (const cplx z, double chop=qpp::chop, std::ostream &os=std::cout)

Displays a number (implicitly converted to std::complex<double>) in friendly form. Adds a new line.

• template<typename Derived >

void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

Saves Eigen expression to a binary file (internal format) in double precision.

• template<typename Derived >

DynMat< typename Derived::Scalar > load (const std::string &fname)

Loads Eigen matrix from a binary file (internal format) in double precision.

• template<typename Derived >

Derived loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.

template<>

dmat loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices (qpp::dmat)

template<>

cmat loadMATLABmatrix (const std::string &mat file, const std::string &var name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

• template<typename Derived >

void saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat\_file, const std
::string &var\_name, const std::string &mode)

Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.

template<>

void saveMATLABmatrix (const Eigen::MatrixBase< dmat > &A, const std::string &mat\_file, const std::string &var name, const std::string &mode)

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices (qpp::dmat)

• template<>

void saveMATLABmatrix (const Eigen::MatrixBase< cmat > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

• template<typename Derived1 , typename Derived2 >

DynMat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size\_t > &ctrl, const std::vector< std::size\_t > &subsys, std::size\_t n, std::size\_t d=2)

Applies the controlled-gate A to the part subsys of a multipartite state vector or density matrix.

- template<typename Derived1 , typename Derived2 >

DynMat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen 
 ::MatrixBase< Derived2 > &A, const std::vector< std::size\_t > &subsys, std::size\_t n, std::size\_t d=2)

Applies the gate A to the part subsys of a multipartite state vector or density matrix.

 $\bullet \ \ \text{template}{<} \text{typename Derived} >$ 

```
cmat channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks)
```

Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.

template<typename Derived >

cmat channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector<
std::size\_t > &subsys, std::size\_t n, std::size\_t d=2)

Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.

cmat super (const std::vector < cmat > &Ks)

Superoperator matrix representation.

cmat choi (const std::vector< cmat > &Ks)

Choi matrix representation.

std::vector< cmat > choi2kraus (const cmat &A)

Extracts orthogonal Kraus operators from Choi matrix.

template<typename Derived >

DynMat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &dims)

Partial trace.

template<typename Derived >

DynMat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector<
std::size\_t > &dims)

Partial trace.

template<typename Derived >

DynMat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector<
std::size\_t > &subsys, const std::vector< std::size\_t > &dims)

Partial trace.

template<typename Derived >

DynMat< typename Derived::Scalar > ptranspose (const Eigen::MatrixBase< Derived > &A, const std
::vector< std::size t > &subsys, const std::vector< std::size t > &dims)

Partial transpose.

• template<typename Derived >

DynMat< typename Derived::Scalar > syspermute (const Eigen::MatrixBase< Derived > &A, const std⇔ ::vector< std::size\_t > &perm, const std::vector< std::size\_t > &dims)

System permutation.

template<typename Derived >

Derived rand (std::size t rows, std::size t cols, double a=0, double b=1)

Generates a random matrix with entries uniformly distributed in the interval [a, b)

template<>

dmat rand (std::size\_t rows, std::size\_t cols, double a, double b)

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)

template<>

cmat rand (std::size\_t rows, std::size\_t cols, double a, double b)

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)

• double rand (double a=0, double b=1)

Generates a random real number uniformly distributed in the interval [a, b)

int randint (int a=std::numeric\_limits< int >::min(), int b=std::numeric\_limits< int >::max())

Generates a random integer (int) uniformly distributed in the interval [a, b].

• template<typename Derived >

Derived randn (std::size\_t rows, std::size\_t cols, double mean=0, double sigma=1)

Generates a random matrix with entries normally distributed in N(mean, sigma)

template<>

dmat randn (std::size\_t rows, std::size\_t cols, double mean, double sigma)

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)

template<>

cmat randn (std::size\_t rows, std::size\_t cols, double mean, double sigma)

Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)

double randn (double mean=0, double sigma=1)

Generates a random real number (double) normally distributed in N(mean, sigma)

• cmat randU (std::size\_t D)

Generates a random unitary matrix.

cmat randV (std::size\_t Din, std::size\_t Dout)

Generates a random isometry matrix.

• std::vector< cmat > randkraus (std::size\_t N, std::size\_t D)

Generates a set of random Kraus operators.

cmat randH (std::size\_t D)

Generates a random Hermitian matrix.

ket randket (std::size\_t D)

Generates a random normalized ket (pure state vector)

• cmat randrho (std::size\_t D)

Generates a random density matrix.

std::vector< std::size\_t > randperm (std::size\_t n)

Generates a random uniformly distributed permutation.

#### **Variables**

• constexpr double chop = 1e-10

Used in qpp::disp() and qpp::displn() for setting to zero numbers that have their absolute value smaller than qpp::ct← ::chop.

• constexpr double eps = 1e-12

Used to decide whether a number or expression in double precision is zero or not.

• constexpr std::size\_t maxn = 64

Maximum number of qubits.

• constexpr double pi = 3.141592653589793238462643383279502884

π

• constexpr double ee = 2.718281828459045235360287471352662497

Base of natural logarithm, e.

constexpr std::size\_t infty = -1

Used to denote infinity.

• RandomDevices & rdevs = RandomDevices::get\_instance()

qpp::RandomDevices Singleton

• const Gates & gt = Gates::get\_instance()

qpp::Gates const Singleton

• const States & st = States::get\_instance()

qpp::States const Singleton

const Init & init = Init::get\_instance()

qpp::Init const Singleton

#### 6.1.1 Typedef Documentation

6.1.1.1 using qpp::bra = typedef DynRowVect<cplx>

Complex (double precision) dynamic Eigen row vector.

6.1.1.2 using qpp::cmat = typedef DynMat<cplx>

Complex (double precision) dynamic Eigen matrix.

6.1.1.3 using qpp::cplx = typedef std::complex<double>

Complex number in double precision.

6.1.1.4 using qpp::dmat = typedef DynMat<double>

Real (double precision) dynamic Eigen matrix.

6.1.1.5 template < typename Scalar > using qpp::DynColVect = typedef Eigen::Matrix < Scalar, Eigen::Dynamic, 1>

Dynamic Eigen column vector over the field specified by Scalar.

Example:

```
auto colvect = DynColVect<float>(2); // type of colvect is Eigen::Matrix<float, Eigen::Dynamic, 1>
```

6.1.1.6 template<typename Scalar > using qpp::DynMat = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>

Dynamic Eigen matrix over the field specified by Scalar.

Example:

```
auto mat = DynMat<float>(2,3); // type of mat is Eigen::Matrix<float, Eigen::Dynamic>
```

6.1.1.7 template < typename Scalar > using qpp::DynRowVect = typedef Eigen::Matrix < Scalar, 1, Eigen::Dynamic >

Dynamic Eigen row vector over the field specified by Scalar.

Example:

```
auto rowvect = DynRowVect<float>(3); // type of rowvect is Eigen::Matrix<float, 1, Eigen::Dynamic>
```

6.1.1.8 using qpp::ket = typedef DynColVect<cplx>

Complex (double precision) dynamic Eigen column vector.

- 6.1.2 Function Documentation
- 6.1.2.1 template < typename Derived > cmat qpp::absm ( const Eigen::MatrixBase < Derived > & A )

Matrix absolut value.

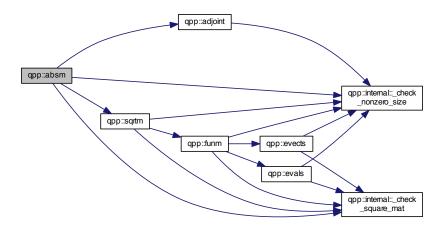
**Parameters** 

A Eigen expression

#### Returns

Matrix absolut value of A

Here is the call graph for this function:



6.1.2.2 template<typename InputIterator > std::vector<double> qpp::abssq ( InputIterator first, InputIterator last )

Computes the absolut values squared of a range of complex numbers.

#### **Parameters**

first	Iterator to the first element of the range
last	Iterator to the last element of the range

#### Returns

Real vector consisting of the range's absolut values squared

 $6.1.2.3 \quad template < typename \ Derived > std::vector < double > qpp::abssq \ ( \ const \ Eigen::MatrixBase < Derived > \& \ V \ )$ 

Computes the absolut values squared of a column vector.

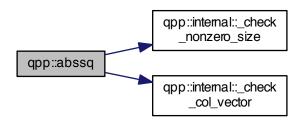
#### **Parameters**

V	Eigen expression

#### Returns

Real vector consisting of the absolut values squared

Here is the call graph for this function:



6.1.2.4 template<typename Derived > DynMat<typename Derived::Scalar> qpp::adjoint ( const Eigen::MatrixBase< Derived > & A )

#### Adjoint.

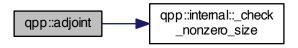
#### **Parameters**

Α	Eigen expression

#### Returns

Adjoint (Hermitian conjugate) of A, as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.5 template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::anticomm ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B)

#### Anti-commutator.

Anti-commutator  $\{A,B\} = AB + BA$ 

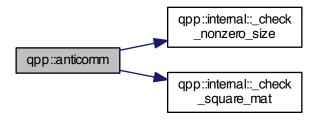
Both A and B must be Eigen expressions over the same scalar field

A	Eigen expression
В	Eigen expression

#### Returns

Anti-commutator AB + BA, as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.6 template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::apply ( const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector< std::size\_t > & subsys, std::size\_t n, std::size\_t d = 2)

Applies the gate A to the part subsys of a multipartite state vector or density matrix.

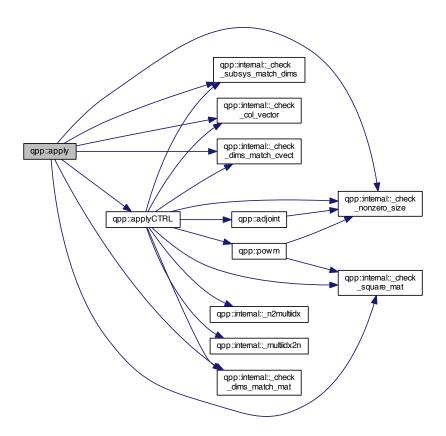
## Note

The dimension of the gate A must match the dimension of subsys

state	Eigen expression
Α	Eigen expression
subsys	Subsystem indexes where the gate A is applied
n	Total number of subsystems
d	Local dimensions of all local Hilbert spaces (must all be equal)

Gate A applied to the part subsys of state

Here is the call graph for this function:



6.1.2.7 template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::applyCTRL ( const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector< std::size\_t > & ctrl, const std::vector< std::size\_t > & subsys, std::size\_t d = 2)

Applies the controlled-gate A to the part subsys of a multipartite state vector or density matrix.

## Note

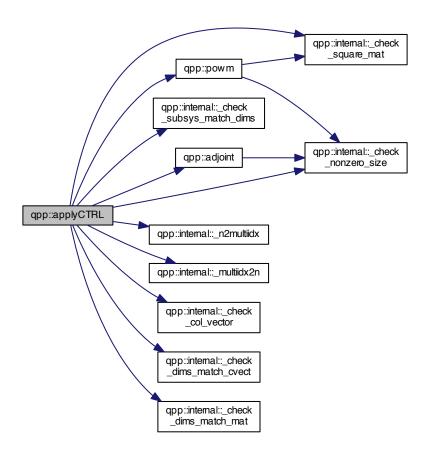
The dimension of the gate A must match the dimension of subsys

state	Eigen expression
Α	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate A is applied

n	Total number of subsystems
d	Local dimensions of all local Hilbert spaces (must all be equal)

CTRL-A gate applied to the part subsys of state

Here is the call graph for this function:



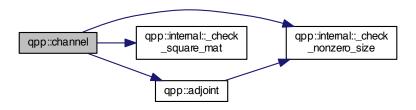
6.1.2.8 template<typename Derived > cmat qpp::channel ( const Eigen::MatrixBase< Derived > & rho, const std::vector< cmat > & Ks )

Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.

rho	Eigen expression
Ks	Set of Kraus operators

Output density matrix after the action of the channel

Here is the call graph for this function:



6.1.2.9 template<typename Derived > cmat qpp::channel ( const Eigen::MatrixBase< Derived > & rho, const std::vector< cmat > & Ks, const std::vector< std::size\_t > & subsys, std::size\_t n, std::size\_t d = 2 )

Applies the channel specified by the set of Kraus operators *Ks* to the part of the density matrix *rho* specified by *subsys*.

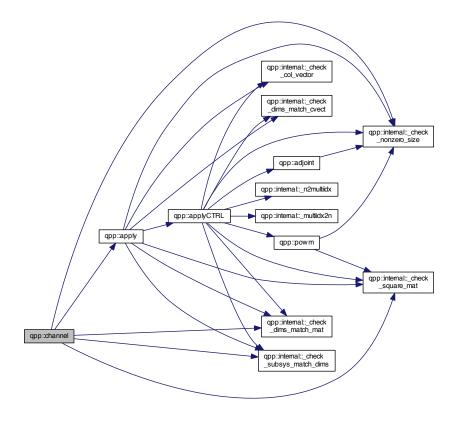
### **Parameters**

rho	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystems' indexes
n	Total number of subsystems
d	Local dimensions of all local Hilbert spaces (must all be equal)

## Returns

Output density matrix after the action of the channel

Here is the call graph for this function:



# 6.1.2.10 cmat qpp::choi ( const std::vector < cmat > & Ks )

Choi matrix representation.

Constructs the Choi matrix of the channel specified by the set of Kraus operators  $\mathit{Ks}$  in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|,\,|0\rangle\langle 1|$  etc.

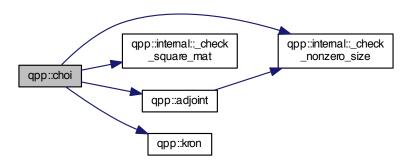
## Note

The superoperator matrix S and the Choi matrix C are related by  $S_{ab,mn} = C_{ma,nb}$ 

Ks	Set of Kraus operators

Choi matrix representation

Here is the call graph for this function:



6.1.2.11 std::vector<cmat> qpp::choi2kraus ( const cmat & A )

Extracts orthogonal Kraus operators from Choi matrix.

Extracts a set of orthogonal (under Hilbert-Schmidt operator norm) Kraus operators from the Choi representation *A* of the channel

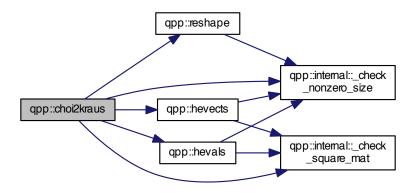
Note

The Kraus operators satisfy  $Tr(K_i^\dagger K_j) = \delta_{ij}$  for all i 
eq j

A   Choi	i matrix
----------	----------

Set of Kraus operators

Here is the call graph for this function:



6.1.2.12 template < typename Derived1 , typename Derived2 > DynMat < typename Derived1::Scalar > qpp::comm ( const Eigen::MatrixBase < Derived1 > & A, const Eigen::MatrixBase < Derived2 > & B)

Commutator.

Commutator [A,B] = AB - BA

Both A and B must be Eigen expressions over the same scalar field

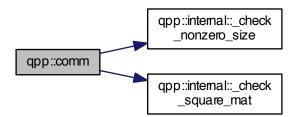
Parameters

Α	Eigen expression
В	Eigen expression

# Returns

Commutator AB - BA, as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.13 std::vector < std::size\_t > & perm, const std::vector < std::size\_t > & perm, const std::vector < std::size\_t > & sigma )

Compose permutations.

perm	Permutation
sigma	Permutation

### Returns

Composition of the permutations *perm* o *sigma* = perm(sigma)

Here is the call graph for this function:



6.1.2.14 template < typename Derived > double qpp::concurrence ( const Eigen::MatrixBase < Derived > & A )

Wootters concurrence of the bi-partite qubit mixed state A.

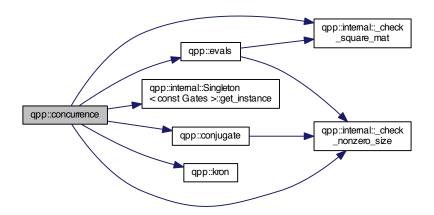
## **Parameters**

Α	Eigen expression
---	------------------

# Returns

Wootters concurrence

Here is the call graph for this function:



6.1.2.15 template < typename Derived > DynMat < typename Derived::Scalar > qpp::conjugate ( const Eigen::MatrixBase < Derived > & A )

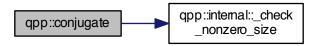
Complex conjugate.

Α	Eigen expression

### Returns

Complex conjugate of A, as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.16 template < typename Derived > cmat qpp::cosm ( const Eigen::MatrixBase < Derived > & A )

## Matrix cos.

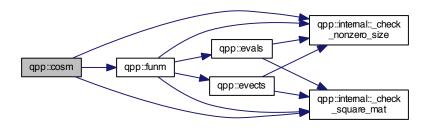
### **Parameters**

A Eigen expression	
--------------------	--

# Returns

Matrix cosine of A

Here is the call graph for this function:



6.1.2.17 template<typename OutputScalar , typename Derived > DynMat<OutputScalar> qpp::cwise ( const Eigen::MatrixBase< Derived > & A, OutputScalar(\*)(const typename Derived::Scalar &) f )

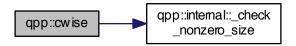
Functor.

Α	Eigen expression
f	Pointer-to-function from scalars of A to OutputScalar

### Returns

Component-wise f(A), as a dynamic matrix over the *OutputScalar* scalar field

Here is the call graph for this function:



6.1.2.18 template < typename Derived > Derived::Scalar qpp::det ( const Eigen::MatrixBase < Derived > & A )

#### Determinant.

### **Parameters**

Α	Eigen expression
---	------------------

## Returns

Determinant of A, as a scalar in the same scalar field as A Returns  $\pm \infty$  when the determinant overflows/underflows

Here is the call graph for this function:



6.1.2.19 template < typename InputIterator > void qpp::disp ( const InputIterator & first, const InputIterator & last, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )

Displays a range. Does not add a newline.

#### See also

qpp::displn()

first	Iterator to the first element of the range
last	Iterator to the last element of the range
separator	Separator
start	Left marking
end	Right marking
os	Output stream

### Returns

Output stream

6.1.2.20 template<typename T > std::ostream& qpp::disp ( const T & x, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )

Displays a standard container that supports std::begin, std::end and forward iteration. Does not add a newline.

## See also

qpp::displn()

### **Parameters**

X	Container
separator	Separator
start	Left marking
end	Right marking
os	Output stream

### Returns

Output stream

Here is the call graph for this function:



6.1.2.21 template<typename T > std::ostream& qpp::disp ( const T \* x, const std::size\_t n, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )

Displays a C-style array. Does not add a newline.

## See also

qpp::displn()

X	Pointer to the first element
n	Number of elements to be displayed
separator	Separator
start	Left marking
end	Right marking
os	Output stream

## Returns

Output stream

6.1.2.22 template < typename Derived > std::ostream& qpp::disp ( const Eigen::MatrixBase < Derived > & A, double chop = qpp::chop, std::ostream & os = std::cout )

Displays an Eigen expression in matrix friendly form. Does not add a new line.

# See also

qpp::displn()

## **Parameters**

Α	Eigen expression
chop	Set to zero the elements smaller in absolute value than <i>chop</i>
os	Output stream

### Returns

Output stream

6.1.2.23 std::ostream& qpp::disp ( const cplx z, double chop = qpp::chop, std::ostream & os = std::cout )

Displays a number (implicitly converted to std::complex<double>) in friendly form. Does not add a new line.

### See also

qpp::displn()

Z	Real/complex number
chop	Set to zero the elements smaller in absolute value than <i>chop</i>
os	Output stream

Output stream

Here is the call graph for this function:



6.1.2.24 template < typename InputIterator > std::ostream & qpp::displn ( const InputIterator & first, const InputIterator & last, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )

Displays a range. Adds a newline.

See also

qpp::disp()

#### **Parameters**

first	Iterator to the first element of the range
last	Iterator to the last element of the range
separator	Separator
start	Left marking
end	Right marking
os	Output stream

#### Returns

Output stream

Here is the call graph for this function:



6.1.2.25 template<typename T > std::ostream& qpp::displn ( const T & x, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )

Displays a standard container that supports std::begin, std::end and forward iteration. Adds a newline.

# See also

qpp::disp()

### **Parameters**

X	Container
separator	Separator
start	Left marking
end	Right marking
os	Output stream

# Returns

Output stream

Here is the call graph for this function:



6.1.2.26 template < typename T > std::ostream& qpp::displn ( const T \* x, const std::size\_t n, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )

Displays a C-style array. Adds a newline.

### See also

qpp::disp()

X	Pointer to the first element
n	Number of elements to be displayed
separator	Separator
start	Left marking
end	Right marking
os	Output stream

Output stream

Here is the call graph for this function:



6.1.2.27 template<typename Derived > std::ostream& qpp::displn ( const Eigen::MatrixBase< Derived > & A, double chop = qpp::chop, std::ostream & os = std::cout )

Displays an Eigen expression in matrix friendly form. Adds a newline.

See also

qpp::disp()

#### **Parameters**

Α	Eigen expression
chop	Set to zero the elements smaller in absolute value than <i>chop</i>
os	Output stream

#### Returns

Output stream

Here is the call graph for this function:



6.1.2.28 std::ostream& qpp::displn ( const cplx z, double chop = qpp::chop, std::ostream & os = std::cout )

Displays a number (implicitly converted to std::complex<double>) in friendly form. Adds a new line.

See also

qpp::disp()

Z	Real/complex number
chop	Set to zero the elements smaller in absolute value than <i>chop</i>
os	Output stream

## Returns

Output stream

Here is the call graph for this function:



6.1.2.29 template < typename Derived > double qpp::entanglement ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

Entanglement of the bi-partite pure state A.

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

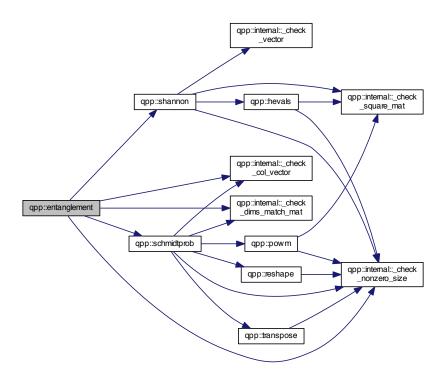
# See also

qpp::shannon()

Α	Eigen expression
dims	Subsystems' dimensions

Entanglement, with the logarithm in base 2

Here is the call graph for this function:



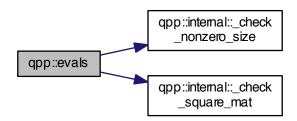
6.1.2.30 template<typename Derived > DynColVect<cplx> qpp::evals ( const Eigen::MatrixBase< Derived > & A )

Eigenvalues.

Α	Eigen expression

Eigenvalues of A, as a complex dynamic column vector

Here is the call graph for this function:



6.1.2.31 template<typename Derived > cmat qpp::evects ( const Eigen::MatrixBase< Derived > & A )

## Eigenvectors.

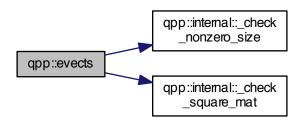
#### **Parameters**

Λ	Figure assessing
A	Eigen expression

### Returns

Eigenvectors of A, as columns of a complex matrix

Here is the call graph for this function:



6.1.2.32 template < typename Derived > cmat qpp::expm ( const Eigen::MatrixBase < Derived > & A )

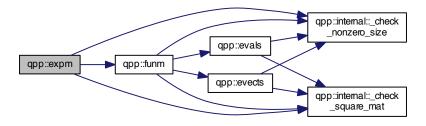
Matrix exponential.

Α	Eigen expression
---	------------------

### Returns

Matrix exponential of A

Here is the call graph for this function:



6.1.2.33 template < typename Derived > cmat qpp::funm ( const Eigen::MatrixBase < Derived > & A, cplx(\*)(const cplx &) f)

# Functional calculus f(A)

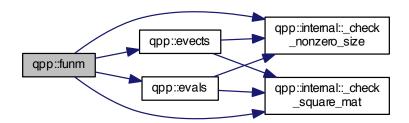
### **Parameters**

Α	Eigen expression
f	Pointer-to-function from complex to complex

## Returns

f(A)

Here is the call graph for this function:



6.1.2.34 template < typename Derived > double qpp::gconcurrence ( const Eigen::MatrixBase < Derived > & A )

G-concurrence of the bi-partite pure state A.

Note

Both local dimensions must be equal

Uses qpp::logdet() to avoid overflows

See also

qpp::logdet()

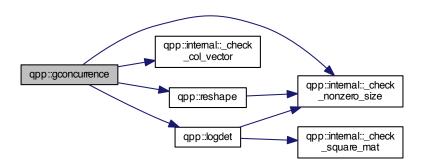
**Parameters** 

A Eigen expression	Α
--------------------	---

Returns

G-concurrence

Here is the call graph for this function:



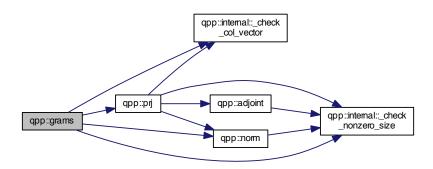
6.1.2.35 template<typename Derived > DynMat<typename Derived::Scalar> qpp::grams ( const std::vector< Derived > & Vs )

Gram-Schmidt orthogonalization (std::vector overload)

Vs
----

Gram-Schmidt vectors of *Vs* as columns of a dynamic matrix over the same scalar field as its arguments

Here is the call graph for this function:



6.1.2.36 template<typename Derived > DynMat<typename Derived::Scalar> qpp::grams ( const std::initializer\_list< Derived > & Vs )

Gram-Schmidt orthogonalization (std::initializer\_list overload)

## **Parameters**

Vs std::initializer_list of Eigen expressions as column vectors
---

## Returns

Gram-Schmidt vectors of  $\mathit{Vs}$  as columns of a dynamic matrix over the same scalar field as its arguments

Here is the call graph for this function:



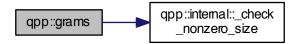
6.1.2.37 template<typename Derived > DynMat<typename Derived::Scalar> qpp::grams ( const Eigen::MatrixBase< Derived > & A )

Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)

A Eigen expression, the input vectors are the columns of A

### Returns

Gram-Schmidt vectors of the columns of *A*, as columns of a dynamic matrix over the same scalar field as *A*Here is the call graph for this function:



6.1.2.38 template<typename Derived > DynColVect<double> qpp::hevals ( const Eigen::MatrixBase< Derived > & A )

Hermitian eigenvalues.

#### **Parameters**

Α	Eigen expression

## Returns

Eigenvalues of Hermitian A, as a real dynamic column vector

Here is the call graph for this function:



6.1.2.39 template < typename Derived > cmat qpp::hevects ( const Eigen::MatrixBase < Derived > & A )

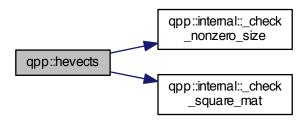
Hermitian eigenvectors.

Α	Eigen expression
---	------------------

### Returns

Eigenvectors of Hermitian A, as columns of a complex matrix

Here is the call graph for this function:



6.1.2.40 template < typename Derived > DynMat < typename Derived::Scalar > qpp::inverse ( const Eigen::MatrixBase < Derived > & A )

Inverse.

# **Parameters**

A	Ligen expression

## Returns

Inverse of A, as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.41 std::vector<std::size\_t> qpp::invperm ( const std::vector< std::size\_t > & perm )

Inverse permutation.

perm	Permutation
------	-------------

## Returns

Inverse of the permutation perm

Here is the call graph for this function:



6.1.2.42 template<typename T > DynMat<typename T::Scalar> qpp::kron ( const T & head )

Kronecker product (variadic overload)

Used to stop the recursion for the variadic template version of qpp::kron()

## **Parameters**

head Eigen expression	
-----------------------	--

# Returns

Its argument head

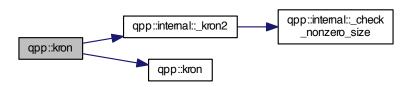
6.1.2.43 template<typename T , typename... Args> DynMat<typename T::Scalar> qpp::kron ( const T & head, const Args &... tail )

Kronecker product (variadic overload)

head	Eigen expression
tail	Variadic Eigen expression (zero or more parameters)

Kronecker product of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

Here is the call graph for this function:



6.1.2.44 template < typename Derived > DynMat < typename Derived::Scalar > qpp::kron ( const std::vector < Derived > & As )

Kronecker product (std::vector overload)

### **Parameters**

As	std::vector of Eigen expressions

### Returns

Kronecker product of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

Here is the call graph for this function:



6.1.2.45 template < typename Derived > DynMat < typename Derived::Scalar > qpp::kron ( const std::initializer\_list < Derived > & As )

Kronecker product (std::initializer\_list overload)

ſ	As	std::initializer_list of Eigen expressions, such as {A1, A2,, Ak}
	710	otalimitalizar_list or Eigen expressions, saon as [717, 712,, 718]

Kronecker product of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

Here is the call graph for this function:



6.1.2.46 template<typename Derived > DynMat<typename Derived::Scalar> qpp::kronpow ( const Eigen::MatrixBase< Derived > & A, std::size\_t n )

Kronecker power.

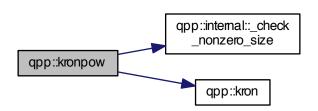
#### **Parameters**

Α	Eigen expression
n	Non-negative integer

#### Returns

Kronecker product of A with itself n times  $A^{\otimes n}$ , as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.47 template<typename Derived > DynMat<typename Derived::Scalar> qpp::load ( const std::string & fname )

Loads Eigen matrix from a binary file (internal format) in double precision.

The template parameter cannot be automatically deduced and must be explicitly provided, depending on the scalar field of the matrix that is being loaded.

Example:

```
// loads a previously saved Eigen dynamic complex matrix from "input.bin"
auto mat = load<cmat>("input.bin");
```

#### See also

gpp::loadMATLABmatrix()

#### **Parameters**

Α	Eigen expression
fname	Output file name

6.1.2.48 template < typename Derived > Derived qpp::loadMATLABmatrix ( const std::string & mat\_file, const std::string & var\_name )

Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.

This is the generic version that always throws *qpp::Exception::Type::UNDEFINED\_TYPE*. It is specialized only for *qpp::dmat* and *qpp::cmat* (the only matrix types that can be loaded)

6.1.2.49 template <> dmat qpp::loadMATLABmatrix ( const std::string & mat\_file, const std::string & var\_name )

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices (qpp::dmat)

The template parameter cannot be automatically deduced and must be explicitly provided

#### Example:

```
// loads a previously saved Eigen dynamic double matrix from the
MATLAB file "input.mat"
auto mat = loadMATLABmatrix<dmat>("input.mat");
```

#### Note

If var\_name is a complex matrix, only the real part is loaded

#### **Parameters**

mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be loaded

## Returns

Eigen double dynamic matrix (qpp::dmat)

6.1.2.50 template <> cmat qpp::loadMATLABmatrix ( const std::string & mat\_file, const std::string & var\_name )

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

The template parameter cannot be automatically deduced and must be explicitly provided

# Example:

```
// loads a previously saved Eigen dynamic complex matrix from the
MATLAB file "input.mat"
auto mat = loadMATLABmatrix<cmat>("input.mat");
```

mat_file	MATALB .mat file
var name	Variable name in the .mat file representing the matrix to be loaded

### Returns

Eigen complex dynamic matrix (qpp::cmat)

6.1.2.51 template<typename Derived > Derived::Scalar qpp::logdet ( const Eigen::MatrixBase< Derived > & A )

Logarithm of the determinant.

Especially useful when the determinant overflows/underflows

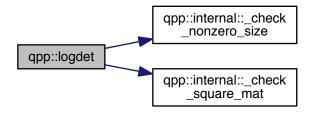
#### **Parameters**

Α	Eigen expression

## Returns

Logarithm of the determinant of A, as a scalar in the same scalar field as A

Here is the call graph for this function:



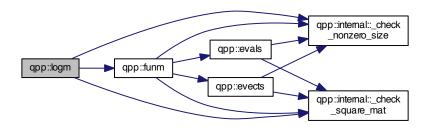
6.1.2.52 template < typename Derived > cmat qpp::logm ( const Eigen::MatrixBase < Derived > & A )

Matrix logarithm.

Α	Eigen expression

Matrix logarithm of A

Here is the call graph for this function:



6.1.2.53 template < typename Derived > double qpp::lognegativity ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

Logarithmic negativity of the bi-partite mixed state A.

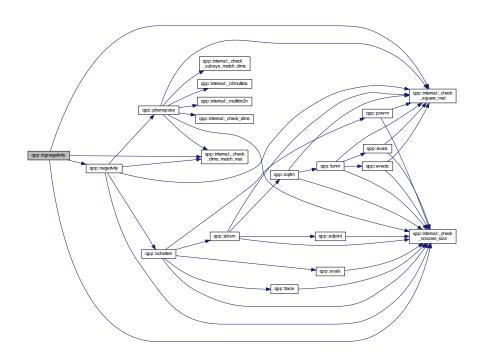
## **Parameters**

Α	Eigen expression
dims	Subsystems' dimensions

### Returns

Logarithmic negativity, with the logarithm in base 2

Here is the call graph for this function:



6.1.2.54 template < typename Derived > std::pair < std::vector < double > , std::vector < cmat > > qpp::measure ( const Eigen::MatrixBase < Derived > & A, const std::vector < cmat > & Ks )

Measures the state A using the set of Kraus operators Ks.

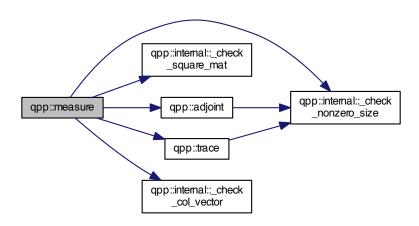
## **Parameters**

Α	Eigen expression
Ks	Set of Kraus operators

## Returns

Pair of vector of probabilities and vector of post-measurement normalized states

Here is the call graph for this function:

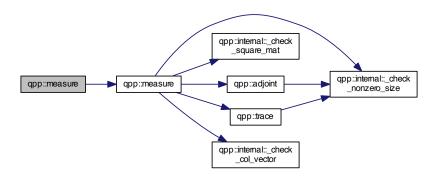


Measures the state A using the set of Kraus operators Ks (std::initializer\_list overload)

Δ.	Fire our contraction
A	Eigen expression
Ks	Set of Kraus operators

Pair of vector of probabilities and vector of post-measurement normalized states

Here is the call graph for this function:



6.1.2.56 template < typename Derived > std::pair < std::vector < double > , std::vector < cmat > > qpp::measure ( const Eigen::MatrixBase < Derived > & A, const cmat & M)

Measures the state A in the orthonormal basis specified by the eigenvectors of M.

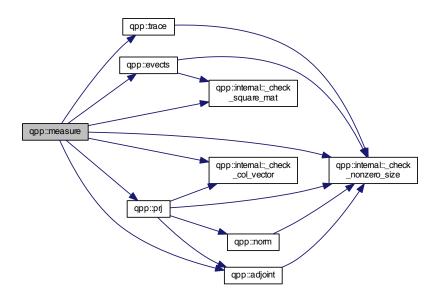
# **Parameters**

Α	Eigen expression
М	Normal matrix whose eigenvectors define the measurement basis

## Returns

Pair of vector of probabilities and vector of post-measurement normalized states

Here is the call graph for this function:



6.1.2.57 ket qpp::mket ( const std::vector < std::size\_t > & mask, const std::vector < std::size\_t > & dims )

Multi-partite qudit ket (different dimensions overload)

Constructs the multi-partite qudit ket  $|mask\rangle$ , where mask is a std::vector of non-negative integers Each element in mask has to be smaller than the corresponding element in dims

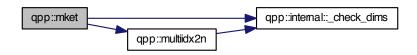
## Parameters

mask	std::vector of non-negative integers
dims	Dimensions of the multi-partite system

### Returns

Multi-partite qudit state vector, as a complex dynamic column vector

Here is the call graph for this function:



6.1.2.58 ket qpp::mket ( const std::vector < std::size\_t > & mask, std::size\_t d = 2 )

Multi-partite qudit ket (same dimensions overload)

Constructs the multi-partite qudit ket  $|mask\rangle$ , all subsystem having equal dimension d mask is a std::vector of non-negative integers, and each element in mask has to be strictly smaller than d

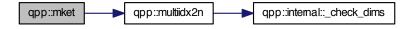
#### **Parameters**

mask	std::vector of non-negative integers
d	Subsystems' dimension

### Returns

Multi-partite qudit state vector, as a complex dynamic column vector

Here is the call graph for this function:



6.1.2.59 cmat qpp::mprj ( const std::vector< std::size\_t > & mask, const std::vector< std::size\_t > & dims )

Projector onto multi-partite qudit ket (different dimensions overload)

Constructs the projector onto the multi-partite qudit ket  $|mask\rangle$ , where mask is a std::vector of non-negative integers Each element in mask has to be smaller than the corresponding element in dims

### **Parameters**

mask	std::vector of non-negative integers
dims	Dimensions of the multi-partite system

### Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

Here is the call graph for this function:



6.1.2.60 cmat qpp::mprj ( const std::vector < std::size\_t > & mask, std::size\_t d = 2 )

Projector onto multi-partite qudit ket (same dimensions overload)

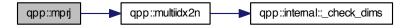
Constructs the projector onto the multi-partite qudit ket  $|mask\rangle$ , all subsystem having equal dimension d mask is a std::vector of non-negative integers, and each element in mask has to be strictly smaller than d

mask	std::vector of non-negative integers
d	Subsystems' dimension

## Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

Here is the call graph for this function:



6.1.2.61 std::size\_t qpp::multiidx2n ( const std::vector < std::size\_t > & midx, const std::vector < std::size\_t > & dims )

Multi-index to non-negative integer index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

#### **Parameters**

midx	Multi-index
dims	Dimensions of the multi-partite system

### Returns

Non-negative integer index

Here is the call graph for this function:



6.1.2.62 std::vector<std::size\_t> qpp::n2multiidx ( std::size\_t n, const std::vector< std::size\_t > & dims )

Non-negative integer index to multi-index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

n	Non-negative integer index
dims	Dimensions of the multi-partite system

# Returns

Multi-index of the same size as dims

Here is the call graph for this function:



6.1.2.63 template < typename Derived > double qpp::negativity ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

Negativity of the bi-partite mixed state A.

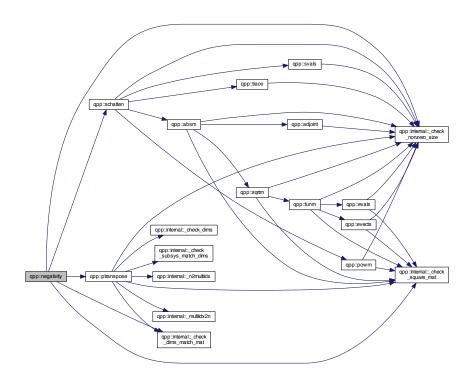
## **Parameters**

Α	Eigen expression
dims	Subsystems' dimensions

## Returns

Negativity

Here is the call graph for this function:



6.1.2.64 template<typename Derived > double qpp::norm ( const Eigen::MatrixBase< Derived > & A )

Frobenius norm.

#### **Parameters**

Α	Eigen expression

## Returns

Frobenius norm of A, as a real number

Here is the call graph for this function:



6.1.2.65 std::complex<double> qpp::omega ( std::size\_t D )

D-th root of unity.

D	Non-negative integer
---	----------------------

#### Returns

D-th root of unity  $\exp(2\pi i/D)$ 

6.1.2.66 constexpr std::complex<double> qpp::operator""\_i ( unsigned long long int x )

User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)

# Example:

```
auto z = 4_i; // type of z is std::complex<double>
```

6.1.2.67 constexpr std::complex<double> qpp::operator""\_i ( long double x )

User-defined literal for complex  $i = \sqrt{-1}$  (real overload)

## Example:

```
auto z = 4.5_i; // type of z is std::complex<double>
```

6.1.2.68 template<typename Derived > DynMat<typename Derived::Scalar> qpp::powm ( const Eigen::MatrixBase< Derived > & A, std::size\_t n )

Matrix power.

Explicitly multiplies the matrix A with itself n times

By convention  $A^0 = I$ 

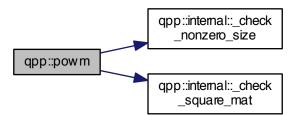
### **Parameters**

Α	Eigen expression
n	Non-negative integer

### Returns

Matrix power  $A^n$ , as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.69 template < typename Derived > DynMat < typename Derived::Scalar > qpp::prj ( const Eigen::MatrixBase < Derived > & V )

Projector.

Normalized projector onto state vector

**Parameters** 

V	Eigen expression

## Returns

Projector onto the state vector V, or the matrix Zero if V has norm zero (i.e. smaller than qpp::eps), as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



 $6.1.2.70 \quad template < type name \ Derived > Derived:: Scalar \ qpp::prod \ ( \ const \ Eigen:: Matrix Base < Derived > \& \ \textit{A} \ )$ 

Element-wise product of A.

### **Parameters**

Α	Eigen expression

### Returns

Element-wise product of A, as a scalar in the same scalar field as A

Here is the call graph for this function:



6.1.2.71 template<typename InputIterator > auto qpp::prod ( InputIterator first, InputIterator last ) -> typename InputIterator::value\_type

Element-wise product of a range.

#### **Parameters**

first	Iterator to the first element of the range
last	Iterator to the last element of the range

## Returns

Element-wise product of the range, as a scalar in the same scalar field as the range

6.1.2.72 template < typename Derived > DynMat < typename Derived::Scalar > qpp::ptrace ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & subsys, const std::vector < std::size\_t > & dims )

## Partial trace.

Partial trace of the multi-partite density matrix over a list of subsystems

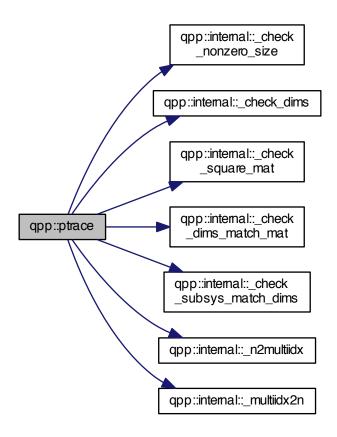
## **Parameters**

Α	Eigen expression
subsys	Subsystem indexes
dims	Dimensions of the multi-partite system

### Returns

Partial trace  $Tr_{subsys}(\cdot)$  over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.73 template < typename Derived > DynMat < typename Derived::Scalar > qpp::ptrace1 ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

## Partial trace.

Partial trace of density matrix over the first subsystem in a bi-partite system

Α	Eigen expression
dims	Dimensions of bi-partite system (must be a std::vector with 2 elements)

Partial trace  $Tr_A(\cdot)$  over the first subsytem A in a bi-partite system  $A\otimes B$ , as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.74 template < typename Derived > DynMat < typename Derived::Scalar > qpp::ptrace2 ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims)

# Partial trace.

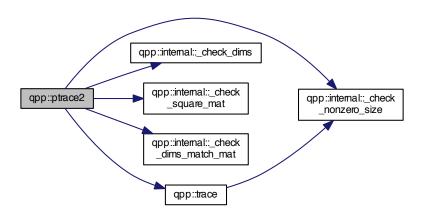
## **Parameters**

Α	Eigen expression
dims	Dimensions of bi-partite system (must be a std::vector with 2 elements)

### Returns

Partial trace  $Tr_B(\cdot)$  over the second subsystem B in a bi-partite system  $A\otimes B$ , as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



# Partial transpose.

Partial transpose of the multi-partite density matrix over a list of subsystems

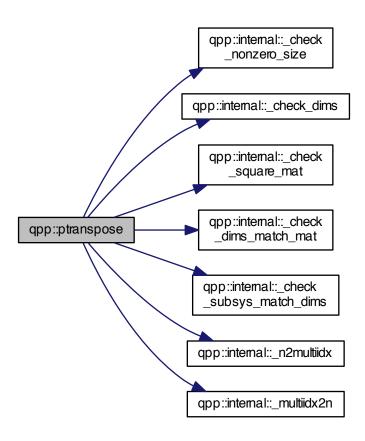
### **Parameters**

Α	Eigen expression
subsys	Subsystem indexes
dims	Dimensions of the multi-partite system

### Returns

Partial transpose  $(\cdot)^{T_{subsys}}$  over the subsytems subsys in a multi-partite system, as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.76 template < typename Derived > double qpp::qmutualinfo ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & subsysB, const std::vector < std::size\_t > & subsysB, const std::vector < std::size\_t > & dims )

Quantum mutual information between 2 subsystems of a composite system.

Α	Eigen expression
subsysA	Indexes of the first subsystem
subsysB	Indexes of the second subsystem
dims	Subsystems' dimensions

Mutual information between the 2 subsystems

Here is the call graph for this function:



6.1.2.77 template < typename Derived > Derived qpp::rand ( std::size\_t rows, std::size\_t cols, double a = 0, double b = 1 )

Generates a random matrix with entries uniformly distributed in the interval [a, b)

If complex, then both real and imaginary parts are uniformly distributed in [a, b)

This is the generic version that always throws *qpp::Exception::Type::UNDEFINED\_TYPE*. It is specialized only for *qpp::dmat* and *qpp::cmat* 

6.1.2.78 template <> dmat qpp::rand ( std::size\_t rows, std::size\_t cols, double a, double b )

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (*qpp::dmat*)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd, with entries uniformly distributed in [-1,1) auto mat = rand<dmat>(3, 3, -1, 1);
```

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
а	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

### Returns

Random real matrix

6.1.2.79 template<> cmat qpp::rand ( std::size\_t rows, std::size\_t cols, double a, double b )

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (*qpp::cmat*)

The template parameter cannot be automatically deduced and must be explicitly provided

## Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd, with entries (both real and imaginary) uniformly distributed
    in [-1,1)
auto mat = rand<cmat>(3, 3, -1, 1);
```

#### **Parameters**

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
а	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

### Returns

Random complex matrix

Here is the call graph for this function:



6.1.2.80 double qpp::rand ( double a = 0, double b = 1 )

Generates a random real number uniformly distributed in the interval [a, b)

а	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

Random real number (double) uniformly distributed in the interval [a, b)

Here is the call graph for this function:



## 6.1.2.81 cmat qpp::randH ( std::size\_t D )

Generates a random Hermitian matrix.

### **Parameters**

D	Dimension of the Hilbert space

## Returns

Random Hermitian matrix

Here is the call graph for this function:



Generates a random integer (int) uniformly distributed in the interval [a, b].

а	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

## Returns

Random integer (int) uniformly distributed in the interval [a, b]

Here is the call graph for this function:



## 6.1.2.83 ket qpp::randket ( std::size\_t D )

Generates a random normalized ket (pure state vector)

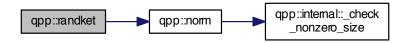
#### **Parameters**

D	Dimension of the Hilbert space

### Returns

Random normalized ket

Here is the call graph for this function:



6.1.2.84 std::vector<cmat> qpp::randkraus ( std::size\_t N, std::size\_t D )

Generates a set of random Kraus operators.

Note

The set of Kraus operators satisfy the closure condition  $\sum_i K_i^\dagger K_i = I$ 

N	Number of Kraus operators
D	Dimension of the Hilbert space

#### Returns

Set of N Kraus operators satisfying the closure condition

Here is the call graph for this function:



6.1.2.85 template<typename Derived > Derived qpp::randn ( std::size\_t rows, std::size\_t cols, double mean = 0, double sigma = 1 )

Generates a random matrix with entries normally distributed in N(mean, sigma)

If complex, then both real and imaginary parts are normally distributed in N(mean, sigma)

This is the generic version that always throws *qpp::Exception::Type::UNDEFINED\_TYPE*. It is specialized only for *qpp::dmat* and *qpp::cmat* 

6.1.2.86 template<> dmat qpp::randn ( std::size\_t rows, std::size\_t cols, double mean, double sigma )

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (*qpp::dmat*)

The template parameter cannot be automatically deduced and must be explicitly provided

#### Example:

```
// generates a 3 x 3 random Eigen::MatrixXd, with entries normally distributed in N(0,2) auto mat = randn<dmat>(3, 3, 0, 2);
```

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
mean	Mean
sigma	Standard deviation

Random real matrix

Here is the call graph for this function:



6.1.2.87 template <> cmat qpp::randn ( std::size\_t rows, std::size\_t cols, double mean, double sigma )

Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (*qpp::cmat*)

The template parameter cannot be automatically deduced and must be explicitly provided

### Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd, with entries (both real and imaginary) normally distributed in N(0,2) auto mat = randn<cmat>(3, 3, 0, 2);
```

## **Parameters**

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
mean	Mean
sigma	Standard deviation

## Returns

Random complex matrix

Here is the call graph for this function:



6.1.2.88 double qpp::randn ( double mean = 0, double sigma = 1 )

Generates a random real number (double) normally distributed in N(mean, sigma)

mean	Mean
sigma	Standard deviation

## Returns

Random real number normally distributed in N(mean, sigma)

Here is the call graph for this function:



6.1.2.89 std::vector<std::size\_t> qpp::randperm ( std::size\_t n )

Generates a random uniformly distributed permutation.

Uses Knuth's shuffle method (as implemented by std::shuffle), so that all permutations are equally probable Parameters

n

## Returns

Random permutation of size n

Here is the call graph for this function:



6.1.2.90 cmat qpp::randrho ( std::size\_t D )

Generates a random density matrix.

D	Dimension of the Hilbert space
---	--------------------------------

### Returns

Random density matrix

6.1.2.91 cmat qpp::randU ( std::size\_t D )

Generates a random unitary matrix.

**Parameters** 

D	Dimension of the Hilbert space

# Returns

Random unitary

6.1.2.92 cmat qpp::randV ( std::size\_t Din, std::size\_t Dout )

Generates a random isometry matrix.

#### **Parameters**

Din	Size of the input Hilbert space
Dout	Size of the output Hilbert space

## Returns

Random isometry matrix

Here is the call graph for this function:



 $\textbf{6.1.2.93} \quad \textbf{template} < \textbf{typename Derived} > \textbf{double qpp::renyi} \, ( \, \, \textbf{const Eigen::MatrixBase} < \, \textbf{Derived} > \textbf{\&} \, \textbf{\textit{A}}, \, \, \textbf{double alpha} \, \, )$ 

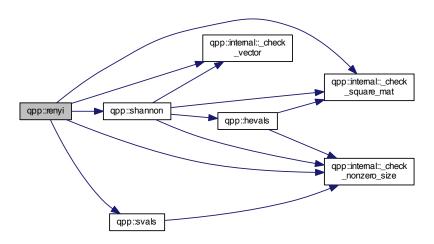
Renyi-  $\alpha$  entropy of the probability distribution/density matrix A, for  $\alpha \geq 0$ .

A	Eigen expression, representing a probability distribution (real dynamic column vector) or a
	density matrix (complex dynamic matrix)

- 1:- 1	Management to a second and the secon
ainna	Non-negative real number, use <i>qpp::infty</i> for $\alpha = \infty$
۵.۱۵.۱۵	rion negative real names, and apprintly to se

Renyi-  $\alpha$  entropy, with the logarithm in base 2

Here is the call graph for this function:



## Reshape.

Uses column-major order when reshaping (same as MATLAB)

#### **Parameters**

Α	Eigen expression
rows	Number of rows of the reshaped matrix
cols	Number of columns of the reshaped matrix

## Returns

Reshaped matrix with rows rows and cols columns, as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.95 template<typename Derived > void qpp::save ( const Eigen::MatrixBase< Derived > & A, const std::string & fname )

Saves Eigen expression to a binary file (internal format) in double precision.

See also

qpp::saveMATLABmatrix()

#### **Parameters**

Α	Eigen expression
fname	Output file name

6.1.2.96 template<typename Derived > void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< Derived > & A, const std::string & mat\_file, const std::string & mode )

Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.

This is the generic version that always throws *qpp::Exception::Type::UNDEFINED\_TYPE*. It is specialized only for *qpp::dmat* and *qpp::cmat* (the only matrix types that can be saved)

6.1.2.97 template<> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< dmat > & A, const std::string & mat\_file, const std::string & var\_name, const std::string & mode )

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices (qpp::dmat)

#### **Parameters**

Α	Eigen expression over the complex field
mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be saved
mode	Saving mode (append, overwrite etc.), see MATLAB's matOpen() documentation for details

Here is the call graph for this function:

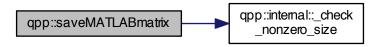


6.1.2.98 template<> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< cmat > & A, const std::string & mat\_file, const std::string & var\_name, const std::string & mode )

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

Α	Eigen expression over the complex field
mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be saved
mode	Saving mode (append, overwrite etc.), see MATLAB's matOpen() documentation for details

Here is the call graph for this function:



6.1.2.99 template < typename Derived > double qpp::schatten ( const Eigen::MatrixBase < Derived > & A, std::size\_t p )

## Schatten norm.

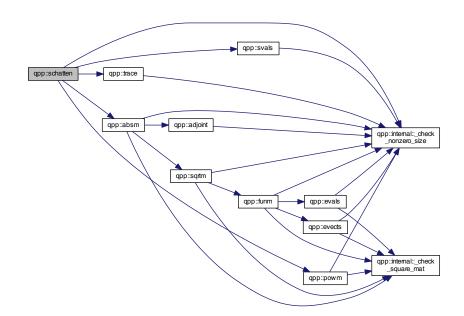
### **Parameters**

Α	Eigen expression
р	Integer, greater or equal to 1

### Returns

Schatten-p norm of A, as a real number

Here is the call graph for this function:



6.1.2.100 template<typename Derived > DynColVect<cplx> qpp::schmidtcoeff ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & dims )

Schmidt coefficients of the bi-partite pure state A.

Note

The sum of the squares of the Schmidt coefficients equals 1

## See also

qpp::schmidtprob()

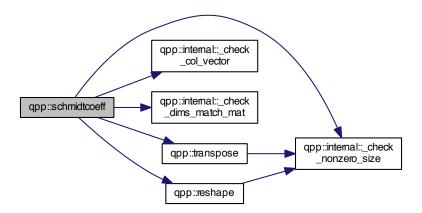
#### **Parameters**

Α	Eigen expression
dims	Subsystems' dimensions

### Returns

Schmidt coefficients of A, as a complex dynamic column vector

Here is the call graph for this function:



6.1.2.101 template<typename Derived > DynColVect<double> qpp::schmidtprob ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size t > & dims )

Schmidt probabilities of the bi-partite pure state A.

Defined as the squares of the Schmidt coefficients The sum of the Schmidt probabilities equals 1

See also

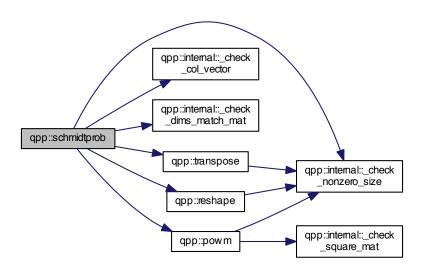
qpp::schmidtcoeff()

Α	Eigen expression
dims	Subsystems' dimensions

# Returns

Schmidt probabilites of A, as a real dynamic column vector

Here is the call graph for this function:



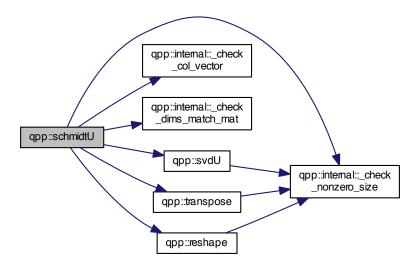
6.1.2.102 template < typename Derived > cmat qpp::schmidtU ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

Schmidt basis on Alice's side.

Α	Eigen expression
dims	Subsystems' dimensions

Unitary matrix  $\boldsymbol{U}$  whose columns represent the Schmidt basis vectors on Alice's side.

Here is the call graph for this function:



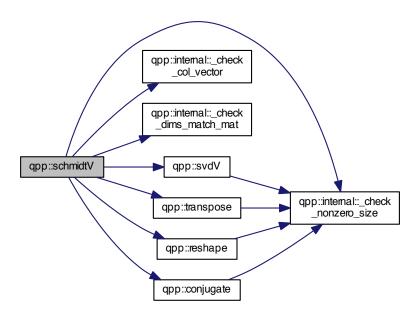
6.1.2.103 template < typename Derived > cmat qpp::schmidtV ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

Schmidt basis on Bob's side.

Λ	Figen expression
Λ	Ligen expression
dims	Subsystems' dimensions

Unitary matrix  ${\it V}$  whose columns represent the Schmidt basis vectors on Bob's side.

Here is the call graph for this function:



6.1.2.104 template < typename Derived > double qpp::shannon ( const Eigen::MatrixBase < Derived > & A )

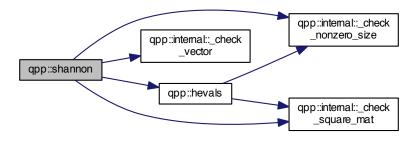
Shannon/von-Neumann entropy of the probability distribution/density matrix  $\boldsymbol{A}$ .

# **Parameters**

A Eigen expression, representing a probability distribution (real dynamic column vector) or a density matrix (complex dynamic matrix)

Shannon/von-Neumann entropy, with the logarithm in base 2

Here is the call graph for this function:



6.1.2.105 template < typename Derived > cmat qpp::sinm ( const Eigen::MatrixBase < Derived > & A )

Matrix sin.

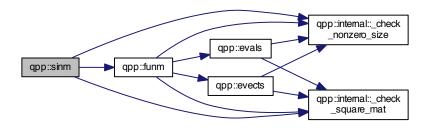
**Parameters** 

Α	Eigen expression

Returns

Matrix sine of A

Here is the call graph for this function:



 $6.1.2.106 \quad template < typename \ Derived > cmat \ qpp::spectralpowm \ ( \ const \ Eigen::MatrixBase < Derived > \& \ \textit{A}, \ const \ cplx \ \textit{z} \ )$ 

Matrix power.

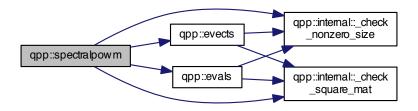
Uses the spectral decomposition of  $\emph{A}$  to compute the matrix power By convention  $\emph{A}^0 = \emph{I}$ 

Α	Eigen expression
Z	Complex number

## Returns

Matrix power  $A^z$ 

Here is the call graph for this function:



6.1.2.107 template < typename Derived > cmat qpp::sqrtm ( const Eigen::MatrixBase < Derived > & A )

Matrix square root.

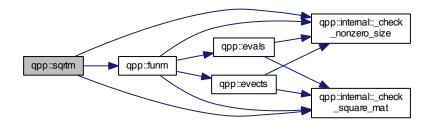
## **Parameters**

Α	Eigen expression

## Returns

Matrix square root of A

Here is the call graph for this function:



6.1.2.108 template < typename Derived > Derived::Scalar qpp::sum ( const Eigen::MatrixBase < Derived > & A )

Element-wise sum of A.

Α	Eigen expression
---	------------------

#### Returns

Element-wise sum of A, as a scalar in the same scalar field as A

Here is the call graph for this function:



6.1.2.109 template<typename InputIterator > auto qpp::sum ( InputIterator first, InputIterator last ) -> typename InputIterator::value\_type

Element-wise sum of a range.

### **Parameters**

first	Iterator to the first element of the range
last	Iterator to the last element of the range

### Returns

Element-wise sum of the range, as a scalar in the same scalar field as the range

6.1.2.110 cmat qpp::super ( const std::vector < cmat > & Ks )

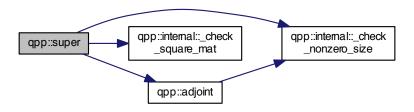
Superoperator matrix representation.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators Ks in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

	Set of Kraus operators
--	------------------------

Superoperator matrix representation

Here is the call graph for this function:



6.1.2.111 template<typename Derived > DynColVect<double> qpp::svals ( const Eigen::MatrixBase< Derived > & A )

Singular values.

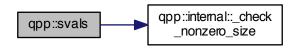
## **Parameters**

Α	Eigen expression

# Returns

Singular values of A, as a real dynamic column vector

Here is the call graph for this function:



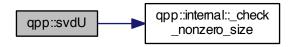
6.1.2.112 template<typename Derived > cmat qpp::svdU ( const Eigen::MatrixBase< Derived > & A )

Left singular vectors.

Α	Eigen expression

Complex dynamic matrix, whose columns are the left singular vectors of A

Here is the call graph for this function:



6.1.2.113 template<typename Derived > cmat qpp::svdV ( const Eigen::MatrixBase< Derived > & A )

Right singular vectors.

**Parameters** 

Α	Eigen expression

## Returns

Complex dynamic matrix, whose columns are the right singular vectors of A

Here is the call graph for this function:



6.1.2.114 template < typename Derived > DynMat < typename Derived::Scalar > qpp::syspermute ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & perm, const std::vector < std::size\_t > & dims )

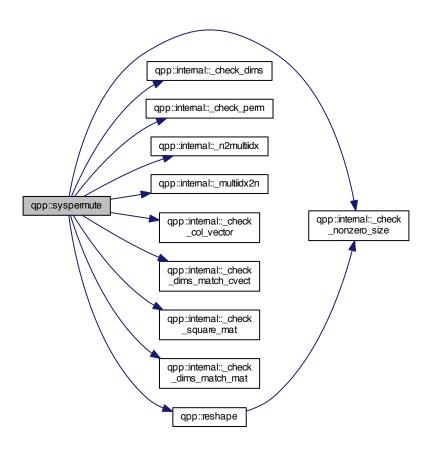
System permutation.

Permutes the subsystems in a state vector or density matrix The qubit perm[i] is permuted to the location i

Α	Eigen expression
perm	Permutation
dims	Subsystems' dimensions

Permuted system, as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.115 template<typename Derived > Derived::Scalar qpp::trace ( const Eigen::MatrixBase< Derived > & A )

## Trace.

Α	Eigen expression

Trace of A, as a scalar in the same scalar field as A

Here is the call graph for this function:



6.1.2.116 template < typename Derived > DynMat < typename Derived::Scalar > qpp::transpose ( const Eigen::MatrixBase < Derived > &  $\bf A$  )

Transpose.

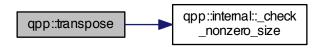
#### **Parameters**

Α	Eigen expression
---	------------------

### Returns

Transpose of A, as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



6.1.2.117 template < typename Derived > double qpp::tsallis ( const Eigen::MatrixBase < Derived > & A, double alpha )

Tsallis-  $\alpha$  entropy of the probability distribution/density matrix A, for  $\alpha \geq 0$ 

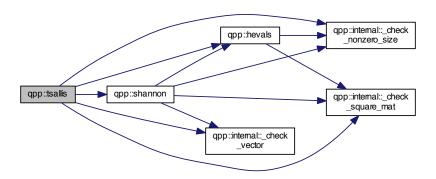
When  $\alpha \to 1$  the Tsallis entropy converges to the Shannon/von-Neumann entropy, with the logarithm in base e

A Eigen expression, representing a probability distribution (real dynamic column vector) or a density matrix (complex dynamic matrix)

alpha	Non-negative real number

Renyi-  $\alpha$  entropy, with the logarithm in base 2

Here is the call graph for this function:



# 6.1.3 Variable Documentation

### 6.1.3.1 constexpr double qpp::chop = 1e-10

Used in *qpp::disp()* and *qpp::displn()* for setting to zero numbers that have their absolute value smaller than *qpp*::ct::chop.

6.1.3.2 constexpr double qpp::ee = 2.718281828459045235360287471352662497

Base of natural logarithm, e.

6.1.3.3 constexpr double qpp::eps = 1e-12

Used to decide whether a number or expression in double precision is zero or not.

Example:

```
if(std::abs(x) < qpp::eps) // x is zero</pre>
```

## 6.1.3.4 const Gates& qpp::gt = Gates::get\_instance()

qpp::Gates const Singleton

Initializes the gates, see the class qpp::Gates

6.1.3.5 constexpr std::size\_t qpp::infty = -1

Used to denote infinity.

```
6.1.3.6 const Init& qpp::init = Init::get_instance()
```

qpp::Init const Singleton

Additional initializations/cleanups

6.1.3.7 constexpr std::size\_t qpp::maxn = 64

Maximum number of qubits.

Used internally to allocate arrays on the stack (for speed reasons)

6.1.3.8 constexpr double qpp::pi = 3.141592653589793238462643383279502884

 $\pi$ 

#### 6.1.3.9 RandomDevices& qpp::rdevs = RandomDevices::get\_instance()

qpp::RandomDevices Singleton

Initializes the random devices, see the class qpp::RandomDevices

6.1.3.10 const States& qpp::st = States::get\_instance()

qpp::States const Singleton

Initializes the states, see the class *qpp::States* 

# 6.2 gpp::experimental Namespace Reference

### **Classes**

class Qudit

# **Functions**

Applies the gate A to the part subsys of a multipartite state vector or density matrix.

template<typename Derived >
 cmat channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector<
 std::size\_t > &subsys, const std::vector< std::size\_t > &dims)

Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.

cmat super (const std::vector < cmat > &Ks)

Superoperator matrix representation.

• template<typename Derived >

DynMat< typename Derived::Scalar > CTRL (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &ctrl, const std::vector< std::size t > &subsys, std::size t n, std::size t d=2)

Generates the multipartite multiple-controlled-A gate in matrix form.

cmat choi (const std::vector< cmat > &Ks)

Choi matrix representation.

• std::vector< cmat > randkraus (std::size\_t n, std::size\_t D)

Generates a set of random Kraus operators.

 template<typename Derived > double renyi\_inf (const Eigen::MatrixBase< Derived > &A)

Renyi- ∞ entropy (min entropy) of the probability distribution/density matrix A.

# 6.2.1 Detailed Description

Experimental/test functions, do not use/modify these functions/classes

## 6.2.2 Function Documentation

6.2.2.1 template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::experimental::apply ( const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector< std::size\_t > & subsys, const std::vector< std::size\_t > & dims )

Applies the gate A to the part subsys of a multipartite state vector or density matrix.

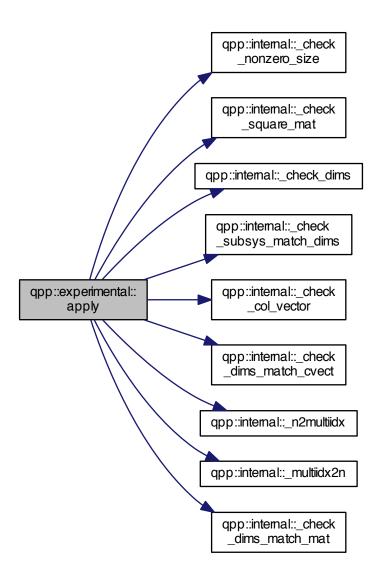
Note

The dimension of the gate A must match the dimension of subsys

state	Eigen expression
Α	Eigen expression
subsys	Subsystem indexes where the gate A is applied
dims	Local dimensions of all local Hilbert spaces (can be different)

Gate A applied to the part subsys of state

Here is the call graph for this function:



6.2.2.2 template<typename Derived > cmat qpp::experimental::channel ( const Eigen::MatrixBase< Derived > & rho, const std::vector< cmat > & Ks, const std::vector< std::size\_t > & subsys, const std::vector< std::size\_t > & dims )

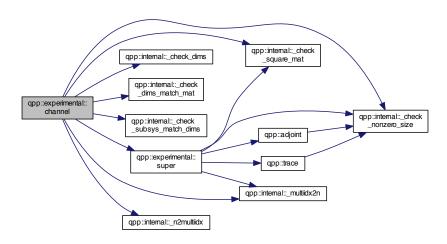
Applies the channel specified by the set of Kraus operators *Ks* to the part of the density matrix *rho* specified by *subsys*.

rho	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystems' indexes
dims	Local dimensions of all local Hilbert spaces (can be different)

## Returns

Output density matrix after the action of the channel

Here is the call graph for this function:



6.2.2.3 cmat qpp::experimental::choi ( const std::vector< cmat > & Ks )

Choi matrix representation.

Constructs the Choi matrix of the channel specified by the set of Kraus operators Ks in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

Note

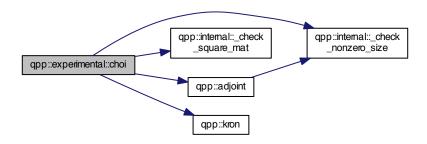
The superoperator matrix S and the Choi matrix C are related by  $S_{ab,mn} = C_{ma,nb}$ 

Ks	Set of Kraus operators

#### Returns

Choi matrix representation

Here is the call graph for this function:



6.2.2.4 template<typename Derived > DynMat<typename Derived::Scalar> qpp::experimental::CTRL ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & ctrl, const std::vector< std::size\_t > & subsys, std::size\_t n, std::size\_t d = 2 )

Generates the multipartite multiple-controlled-A gate in matrix form.

# Note

The dimension of the gate A must match the dimension of subsys

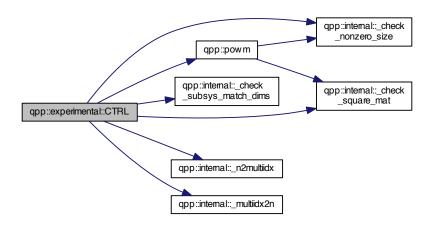
#### **Parameters**

Α	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate A is applied
n	Total number of subsystes
d	Local dimensions of all local Hilbert spaces (must all be equal)

#### Returns

CTRL-A gate, as a matrix over the same scalar field as A

Here is the call graph for this function:



6.2.2.5 std::vector<cmat> qpp::experimental::randkraus ( std::size\_t n, std::size\_t D )

Generates a set of random Kraus operators.

# Note

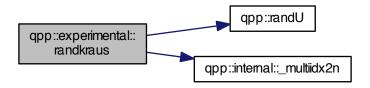
The set of Kraus operators satisfy the closure condition  $\sum_i K_i^\dagger K_i = I$ 

# **Parameters**

n	Number of Kraus operators
D	Dimension of the Hilbert space

#### Returns

Set of *n* Kraus operators satisfying the closure condition



 $\textbf{6.2.2.6} \quad \textbf{template} \\ < \textbf{typename Derived} \\ > \textbf{double qpp::experimental::renyi\_inf ( const Eigen::MatrixBase} \\ < \textbf{Derived} \\ > \textbf{\& A )} \\$ 

Renyi-  $\infty$  entropy (min entropy) of the probability distribution/density matrix A.

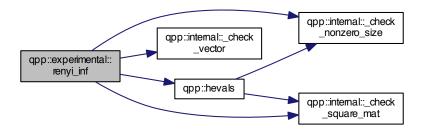
#### **Parameters**

A Eigen expression, representing a probability distribution (real dynamic column vector) or a density matrix (complex dynamic matrix)

# Returns

Renyi- ∞ entropy (min entropy), with the logarithm in base 2

Here is the call graph for this function:



# 6.2.2.7 cmat qpp::experimental::super ( const std::vector < cmat > & Ks )

Superoperator matrix representation.

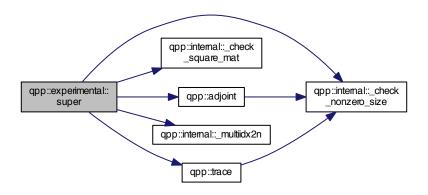
Constructs the superoperator matrix of the channel specified by the set of Kraus operators Ks in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

# **Parameters**

Ks	Set of Kraus operators

# Returns

Superoperator matrix representation



# 6.3 qpp::internal Namespace Reference

#### Classes

· class Singleton

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

#### **Functions**

- void n2multiidx (std::size t n, std::size t numdims, const std::size t \*dims, std::size t \*result)
- std::size\_t \_multiidx2n (const std::size\_t \*midx, std::size\_t numdims, const std::size\_t \*dims)
- template<typename Derived >

bool <u>\_check\_square\_mat</u> (const Eigen::MatrixBase< Derived > &A)

template<typename Derived >

bool <u>\_check\_vector</u> (const Eigen::MatrixBase< Derived > &A)

template<typename Derived >

bool check row vector (const Eigen::MatrixBase< Derived > &A)

template<typename Derived >

bool <u>\_check\_col\_vector</u> (const Eigen::MatrixBase< Derived > &A)

• template<typename T >

bool check nonzero size (const T &x)

- bool <u>\_check\_dims</u> (const std::vector< std::size\_t > &dims)
- template<typename Derived >

bool \_check\_dims\_match\_mat (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &A)

• template<typename Derived >

bool \_check\_dims\_match\_cvect (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &V)

template<typename Derived >

bool \_check\_dims\_match\_rvect (const std::vector< std::size\_t > &dims, const Eigen::MatrixBase< Derived > &V)

- bool <u>\_check\_eq\_dims</u> (const std::vector< std::size\_t > &dims, std::size\_t dim)
- bool \_check\_subsys\_match\_dims (const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- bool \_check\_perm (const std::vector< std::size\_t > &perm)
- template<typename Derived1 , typename Derived2 >

DynMat< typename Derived1::Scalar > \_kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::← MatrixBase< Derived2 > &B)

• template<typename T >

void variadic\_vector\_emplace (std::vector< T > &)

template<typename T, typename First, typename... Args>
 void variadic\_vector\_emplace (std::vector< T > &v, First &&first, Args &&...args)

# 6.3.1 Detailed Description

Internal implementation details, do not use/modify these functions/classes

# 6.3.2 Function Documentation

- 6.3.2.1 template < typename Derived > bool qpp::internal::\_check\_col\_vector ( const Eigen::MatrixBase < Derived > & A )
- 6.3.2.2 bool qpp::internal::\_check\_dims ( const std::vector < std::size\_t > & dims )

- 6.3.2.3 template<typename Derived > bool qpp::internal::\_check\_dims\_match\_cvect ( const std::vector< std::size\_t > & dims, const Eigen::MatrixBase< Derived > & V )
- 6.3.2.4 template<typename Derived > bool qpp::internal::\_check\_dims\_match\_mat ( const std::vector< std::size\_t > & dims, const Eigen::MatrixBase< Derived > & A )
- 6.3.2.5 template<typename Derived > bool qpp::internal::\_check\_dims\_match\_rvect ( const std::vector< std::size\_t > & dims, const Eigen::MatrixBase< Derived > & V )
- 6.3.2.6 bool qpp::internal::\_check\_eq\_dims ( const std::vector < std::size\_t > & dims, std::size\_t dim )
- 6.3.2.7 template<typename T > bool qpp::internal::\_check\_nonzero\_size ( const T & x )
- 6.3.2.8 bool qpp::internal::\_check\_perm ( const std::vector < std::size\_t > & perm )
- 6.3.2.9 template < typename Derived > bool qpp::internal::\_check\_row\_vector ( const Eigen::MatrixBase < Derived > & A )
- 6.3.2.10 template < typename Derived > bool qpp::internal::\_check\_square\_mat ( const Eigen::MatrixBase < Derived > & A )
- 6.3.2.11 bool qpp::internal::\_check\_subsys\_match\_dims ( const std::vector< std::size\_t > & subsys, const std::vector< std::size\_t > & dims )
- 6.3.2.12 template < typename Derived > bool qpp::internal::\_check\_vector ( const Eigen::MatrixBase < Derived > & A )

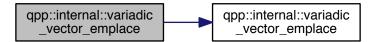


- 6.3.2.14 std::size\_t qpp::internal::\_multiidx2n ( const std::size\_t \* midx, std::size\_t numdims, const std::size\_t \* dims )

  [inline]
- 6.3.2.15 void qpp::internal::\_n2multiidx ( std::size\_t *n*, std::size\_t *numdims*, const std::size\_t \* *dims*, std::size\_t \* *result* )

  [inline]
- 6.3.2.16 template < typename T > void qpp::internal::variadic\_vector\_emplace(\_std::vector < T > & \_)

6.3.2.17 template < typename T , typename First , typename... Args > void qpp::internal::variadic\_vector\_emplace ( std::vector < T > & v, First && first, Args &&... args )



# **Chapter 7**

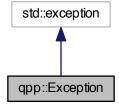
# **Class Documentation**

7.1 qpp::Exception Class Reference

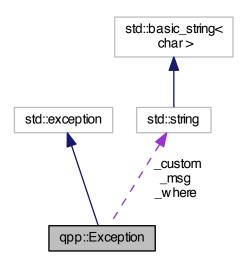
Generates custom exceptions, used when validating function parameters.

#include <exception.h>

Inheritance diagram for qpp::Exception:



Collaboration diagram for qpp::Exception:



# **Public Types**

• enum Type {

Type::UNKNOWN\_EXCEPTION = 1, Type::ZERO\_SIZE, Type::MATRIX\_NOT\_SQUARE, Type::MATRIX\_← NOT\_CVECTOR,

Type::MATRIX\_NOT\_RVECTOR, Type::MATRIX\_NOT\_VECTOR, Type::MATRIX\_NOT\_SQUARE\_OR\_C↔ VECTOR, Type::MATRIX\_NOT\_SQUARE\_OR\_RVECTOR,

Type::MATRIX\_NOT\_SQUARE\_OR\_VECTOR, Type::MATRIX\_MISMATCH\_SUBSYS, Type::DIMS\_INVA← LID, Type::DIMS\_NOT\_EQUAL,

Type::DIMS\_MISMATCH\_MATRIX, Type::DIMS\_MISMATCH\_CVECTOR, Type::DIMS\_MISMATCH\_RVE← CTOR, Type::DIMS MISMATCH VECTOR,

Type::SUBSYS\_MISMATCH\_DIMS, Type::PERM\_INVALID, Type::NOT\_QUBIT\_GATE, Type::NOT\_QUBI

T SUBSYS,

Type::NOT\_BIPARTITE, Type::OUT\_OF\_RANGE, Type::TYPE\_MISMATCH, Type::UNDEFINED\_TYPE, Type::CUSTOM\_EXCEPTION }

Exception types, add more exceptions here if needed.

#### **Public Member Functions**

• Exception (const std::string &where, const Type &type)

Constructs an exception.

• Exception (const std::string &where, const std::string &custom)

Constructs an exception.

• virtual const char \* what () const noexceptoverride

Overrides std::exception::what()

#### **Private Member Functions**

• std::string \_construct\_exception\_msg ()

Constructs the exception's description from its type.

#### **Private Attributes**

- · std::string \_where
- std::string \_msg
- Type \_type
- std::string custom

#### 7.1.1 Detailed Description

Generates custom exceptions, used when validating function parameters.

Customize this class if more exceptions are needed

#### 7.1.2 Member Enumeration Documentation

**7.1.2.1 enum qpp::Exception::Type** [strong]

Exception types, add more exceptions here if needed.

See also

qpp:Exception::\_construct\_exception\_msg()

#### **Enumerator**

UNKNOWN EXCEPTION UNKNOWN EXCEPTION. Unknown exception

ZERO\_SIZE ZERO SIZE. Zero sized object, e.g. empty Eigen::Matrix or std::vector with no elements

MATRIX\_NOT\_SQUARE MATRIX\_NOT\_SQUARE. Eigen::Matrix is not square

MATRIX\_NOT\_CVECTOR MATRIX\_NOT\_CVECTOR. Eigen::Matrix is not a column vector

MATRIX\_NOT\_RVECTOR MATRIX NOT RVECTOR. Eigen::Matrix is not a row vector

MATRIX\_NOT\_VECTOR MATRIX\_NOT\_VECTOR. Eigen::Matrix is not a row/column vector

**MATRIX\_NOT\_SQUARE\_OR\_CVECTOR** MATRIX\_NOT\_SQUARE\_OR\_CVECTOR. Eigen::Matrix is not square nor a column vector

**MATRIX\_NOT\_SQUARE\_OR\_RVECTOR** MATRIX\_NOT\_SQUARE\_OR\_RVECTOR. Eigen::Matrix is not square nor a row vector

**MATRIX\_NOT\_SQUARE\_OR\_VECTOR** MATRIX\_NOT\_SQUARE\_OR\_VECTOR. Eigen::Matrix is not square nor a row/column vector

**MATRIX\_MISMATCH\_SUBSYS** SUBSYS\_MISMATCH\_MATRIX.

**DIMS\_INVALID** DIMS\_INVALID. Matrix size mismatch subsystems' size (e.g. in apply(), or channel() std← ::vector<std::size\_t> representing the dimensions has zero size or contains zeros

**DIMS\_NOT\_EQUAL** DIMS\_NOT\_EQUAL. std::vector<std::size\_t> representing the dimensions contains non-equal elements

**DIMS\_MISMATCH\_MATRIX** DIMS\_MISMATCH\_MATRIX. Product of the dimenisons' std::vector<std

∷size t> is not equal to the number of rows of Eigen::Matrix (assumed to be square)

**DIMS\_MISMATCH\_CVECTOR** DIMS\_MISMATCH\_CVECTOR. Product of the dimenisons' std::vector<std↔ ::size\_t> is not equal to the number of cols of Eigen::Matrix (assumed to be a column vector)

**DIMS\_MISMATCH\_RVECTOR** DIMS\_MISMATCH\_RVECTOR. Product of the dimenisons' std::vector<std↔ ::size\_t> is not equal to the number of cols of Eigen::Matrix (assumed to be a row vector)

**DIMS\_MISMATCH\_VECTOR** DIMS\_MISMATCH\_VECTOR. Product of the dimenisons' std::vector<std↔ ::size\_t> is not equal to the number of cols of Eigen::Matrix (assumed to be a row/column vector)

**SUBSYS\_MISMATCH\_DIMS** SUBSYS\_MISMATCH\_DIMS. std::vector<std::size\_t> representing the subsystems' labels has duplicatates, or has entries that are larger than the size of the std::vector<std::size -\_t> representing the dimensions

**PERM\_INVALID** PERM\_INVALID. Invalid std::vector<std::size\_t> permutation

NOT\_QUBIT\_GATE NOT\_QUBIT\_GATE. Eigen::Matrix is not 2 x 2

NOT\_QUBIT\_SUBSYS NOT QUBIT SUBSYS. Subsystems are not 2-dimensional

**NOT\_BIPARTITE** NOT\_BIPARTITE. std::vector<std::size\_t> representing the dimensions has size different from 2

OUT\_OF\_RANGE OUT\_OF\_RANGE. Parameter out of range

TYPE\_MISMATCH TYPE MISMATCH. Types do not match (i.e. Matrix<double> vs Matrix<cplx>)

UNDEFINED\_TYPE UNDEFINED\_TYPE. Templated function not defined for this type

CUSTOM\_EXCEPTION CUSTOM\_EXCEPTION. Custom exception, user must provide a custom message

## 7.1.3 Constructor & Destructor Documentation

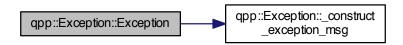
7.1.3.1 qpp::Exception::Exception ( const std::string & where, const Type & type ) [inline]

Constructs an exception.

#### **Parameters**

where	Text representing where the exception occured
type	Exception's type, see the strong enumeration qpp::Exception::TYPE

Here is the call graph for this function:



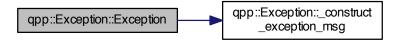
7.1.3.2 qpp::Exception::Exception ( const std::string & where, const std::string & custom ) [inline]

Constructs an exception.

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

#### **Parameters**

where	Text representing where the exception occured
custom	Exception's description



#### 7.1.4 Member Function Documentation

7.1.4.1 std::string qpp::Exception::\_construct\_exception\_msg( ) [inline], [private]

Constructs the exception's description from its type.

Must modify the code of this function if more exceptions are added

Returns

Exception's description

7.1.4.2 virtual const char\* qpp::Exception::what( ) const [inline], [override], [virtual], [noexcept]

Overrides std::exception::what()

Returns

**Exception**'s description

#### 7.1.5 Member Data Documentation

**7.1.5.1** std::string qpp::Exception::\_custom [private]

**7.1.5.2** std::string qpp::Exception::\_msg [private]

7.1.5.3 Type qpp::Exception::\_type [private]

**7.1.5.4 std::string qpp::Exception::\_where** [private]

The documentation for this class was generated from the following file:

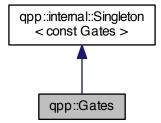
• include/classes/exception.h

# 7.2 qpp::Gates Class Reference

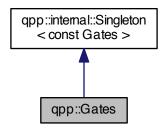
const Singleton class that implements most commonly used gates

```
#include <gates.h>
```

Inheritance diagram for qpp::Gates:



Collaboration diagram for qpp::Gates:



#### **Public Member Functions**

cmat Rn (double theta, std::vector< double > n) const

Rotation of theta about the 3-dimensional real unit vector n.

cmat Zd (std::size\_t D) const

Generalized Z gate for qudits.

cmat Fd (std::size\_t D) const

Fourier transform gate for qudits.

• cmat Xd (std::size t D) const

Generalized X gate for qudits.

• template<typename Derived = Eigen::MatrixXcd>

Derived Id (std::size\_t D) const

Identity gate.

• template<typename Derived >

DynMat< typename Derived::Scalar > CTRL (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &ctrl, const std::vector< std::size\_t > &subsys, std::size\_t n, std::size\_t d=2) const

Generates the multipartite multiple-controlled-A gate in matrix form.

• template<typename Derived >

DynMat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, std::size\_t pos, const std::vector< std::size\_t > &dims) const

Expands out.

# **Public Attributes**

```
• cmat Id2 { cmat::Identity(2, 2) }
```

Identity gate.

cmat H { cmat::Zero(2, 2) }

Hadamard gate.

cmat X { cmat::Zero(2, 2) }

Pauli Sigma-X gate.

cmat Y { cmat::Zero(2, 2) }

Pauli Sigma-Y gate.

cmat Z { cmat::Zero(2, 2) }

Pauli Sigma-Z gate.

cmat S { cmat::Zero(2, 2) }

```
S gate.

cmat T { cmat::Zero(2, 2) }
T gate.

cmat CNOTab { cmat::Identity(4, 4) }
Controlled-NOT control target gate.

cmat CZ { cmat::Identity(4, 4) }
Controlled-Phase gate.

cmat CNOTba { cmat::Zero(4, 4) }
Controlled-NOT target control gate.

cmat SWAP { cmat::Identity(4, 4) }
SWAP gate.

cmat TOF { cmat::Identity(8, 8) }
Toffoli gate.

cmat FRED { cmat::Identity(8, 8) }
Fredkin gate.
```

# **Private Member Functions**

• Gates ()
Initializes the gates.

#### **Friends**

class internal::Singleton < const Gates >

#### **Additional Inherited Members**

# 7.2.1 Detailed Description

const Singleton class that implements most commonly used gates

#### 7.2.2 Constructor & Destructor Documentation

```
7.2.2.1 qpp::Gates::Gates( ) [inline], [private]
```

Initializes the gates.

# 7.2.3 Member Function Documentation

```
7.2.3.1 template<typename Derived > DynMat<typename Derived::Scalar> qpp::Gates::CTRL ( const Eigen::MatrixBase < Derived > & A, const std::vector< std::size_t > & ctrl, const std::vector< std::size_t > & subsys, std::size_t n, std::size_t d = 2 ) const [inline]
```

Generates the multipartite multiple-controlled-A gate in matrix form.

Note

The dimension of the gate A must match the dimension of subsys

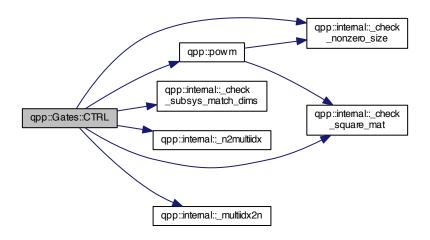
#### **Parameters**

Α	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate A is applied
n	Total number of subsystes
d	Local dimensions of all local Hilbert spaces (must all be equal)

#### Returns

CTRL-A gate, as a matrix over the same scalar field as A

Here is the call graph for this function:



# Expands out.

Expands out *A* as a matrix in a multi-partite system Faster than using *qpp::kron*(I, I, ..., I, A, I, ..., I)

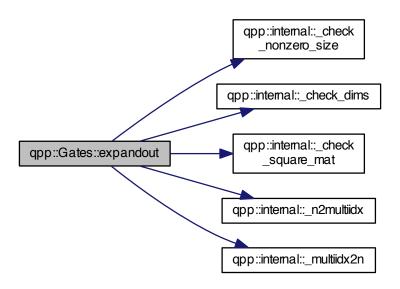
# **Parameters**

Α	Eigen expression
pos	Position
dims	Dimensions of the multi-partite system

#### Returns

Tensor product  $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$ , with A on position pos, as a dynamic matrix over the same scalar field as A

Here is the call graph for this function:



# 7.2.3.3 cmat qpp::Gates::Fd ( std::size\_t D ) const [inline]

Fourier transform gate for qudits.

Note

Defined as 
$$F = \sum_{jk} \exp(2\pi i j k/D) |j\rangle\langle k|$$

# **Parameters**

D Dimension of the Hilbert space	
----------------------------------	--

# Returns

Fourier transform gate for qudits



7.2.3.4 template < typename Derived = Eigen::MatrixXcd > Derived qpp::Gates::Id( std::size\_t D ) const [inline]

Identity gate.

Note

Can change the return type from complex matrix (default) by explicitly specifying the template parameter

#### **Parameters**

D	Dimension of the Hilbert space

#### Returns

Identity gate

7.2.3.5 cmat qpp::Gates::Rn ( double theta, std::vector< double > n ) const [inline]

Rotation of theta about the 3-dimensional real unit vector n.

#### **Parameters**

theta	Rotation angle
n	3-dimensional real unit vector

#### Returns

Rotation gate

7.2.3.6 cmat qpp::Gates::Xd ( std::size\_t D ) const [inline]

Generalized X gate for qudits.

Note

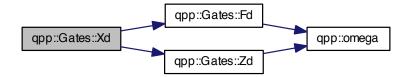
Defined as  $X = \sum_j |j \oplus 1\rangle\langle j|$ 

#### **Parameters**

D   Dimension of the Hilbert space
------------------------------------

# Returns

Generalized X gate for qudits



7.2.3.7 cmat qpp::Gates::Zd ( std::size\_t D ) const [inline]

Generalized Z gate for qudits.

Note

Defined as  $Z = \sum_{j} \exp(2\pi i j/D) |j\rangle\langle j|$ 

#### **Parameters**

D Dimension of the Hilbert space

#### Returns

Generalized Z gate for qudits

Here is the call graph for this function:



# 7.2.4 Friends And Related Function Documentation

**7.2.4.1** friend class internal::Singleton < const Gates > [friend]

# 7.2.5 Member Data Documentation

7.2.5.1 cmat qpp::Gates::CNOTab { cmat::Identity(4, 4) }

Controlled-NOT control target gate.

7.2.5.2 cmat qpp::Gates::CNOTba { cmat::Zero(4, 4) }

Controlled-NOT target control gate.

7.2.5.3 cmat qpp::Gates::CZ { cmat::Identity(4, 4) }

Controlled-Phase gate.

7.2.5.4 cmat qpp::Gates::FRED { cmat::Identity(8, 8) }

Fredkin gate.

7.2.5.5 cmat qpp::Gates::H { cmat::Zero(2, 2) }

Hadamard gate.

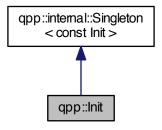
```
7.2.5.6 cmat qpp::Gates::Id2 { cmat::Identity(2, 2) }
Identity gate.
7.2.5.7 cmat qpp::Gates::S { cmat::Zero(2, 2) }
S gate.
7.2.5.8 cmat qpp::Gates::SWAP { cmat::Identity(4, 4) }
SWAP gate.
7.2.5.9 cmat qpp::Gates::T { cmat::Zero(2, 2) }
T gate.
7.2.5.10 cmat qpp::Gates::TOF { cmat::Identity(8, 8) }
Toffoli gate.
7.2.5.11 cmat qpp::Gates::X { cmat::Zero(2, 2) }
Pauli Sigma-X gate.
7.2.5.12 cmat qpp::Gates::Y { cmat::Zero(2, 2) }
Pauli Sigma-Y gate.
7.2.5.13 cmat qpp::Gates::Z { cmat::Zero(2, 2) }
Pauli Sigma-Z gate.
The documentation for this class was generated from the following file:
    • include/classes/gates.h
```

# 7.3 qpp::Init Class Reference

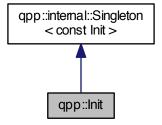
const Singleton class that performs additional initializations/cleanups

#include <init.h>

Inheritance diagram for qpp::Init:



Collaboration diagram for qpp::Init:



# **Public Member Functions**

• Init ()

Additional initializations.

# **Private Member Functions**

• ∼Init ()

Cleanups.

# **Friends**

- class internal::Singleton < const Init >

# **Additional Inherited Members**

# 7.3.1 Detailed Description

const Singleton class that performs additional initializations/cleanups

# 7.3.2 Constructor & Destructor Documentation

```
7.3.2.1 qpp::Init::Init( ) [inline]
```

Additional initializations.

```
7.3.2.2 qpp::Init::~Init() [inline], [private]
```

Cleanups.

#### 7.3.3 Friends And Related Function Documentation

```
7.3.3.1 friend class internal::Singleton < const lnit > [friend]
```

The documentation for this class was generated from the following file:

· include/classes/init.h

# 7.4 qpp::experimental::Qudit Class Reference

```
#include <qudit.h>
```

#### **Public Member Functions**

- Qudit (const cmat &rho=States::get\_instance().pz0)
- std::size\_t measure (const cmat &U, bool destructive=false)
- std::size\_t measure (bool destructive=false)
- cmat getRho () const
- std::size\_t getD () const

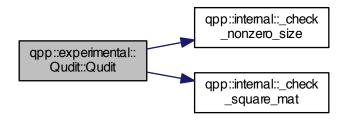
# **Private Attributes**

- cmat \_rho
- std::size\_t \_D

# 7.4.1 Constructor & Destructor Documentation

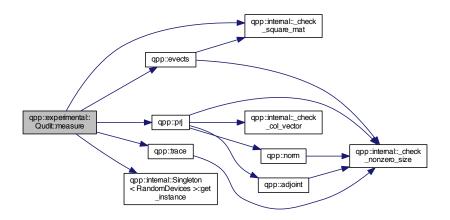
7.4.1.1 qpp::experimental::Qudit::Qudit ( const cmat & rho = States::get\_instance().pz0 ) [inline]

Here is the call graph for this function:



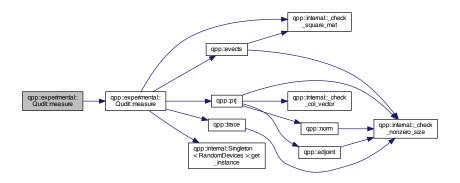
# 7.4.2 Member Function Documentation

- 7.4.2.1 std::size\_t qpp::experimental::Qudit::getD() const [inline]
- **7.4.2.2 cmat qpp::experimental::Qudit::getRho( ) const** [inline]
- 7.4.2.3 std::size\_t qpp::experimental::Qudit::measure ( const cmat & U, bool destructive = false ) [inline]



7.4.2.4 std::size\_t qpp::experimental::Qudit::measure ( bool destructive = false ) [inline]

Here is the call graph for this function:



#### 7.4.3 Member Data Documentation

**7.4.3.1** std::size\_t qpp::experimental::Qudit::\_D [private]

**7.4.3.2 cmat qpp::experimental::Qudit::\_rho** [private]

The documentation for this class was generated from the following file:

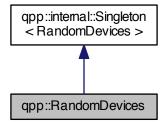
• include/experimental/classes/qudit.h

# 7.5 qpp::RandomDevices Class Reference

Singeleton class that manages the source of randomness in the library.

#include <randevs.h>

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



# **Public Attributes**

std::mt19937 \_rng

Mersenne twister random number generator engine.

#### **Private Member Functions**

• RandomDevices ()

Initializes and seeds the random number generators.

# **Private Attributes**

std::random\_device \_rd
 used to seed std::mt19937 \_rng

# **Friends**

class internal::Singleton < RandomDevices >

# **Additional Inherited Members**

# 7.5.1 Detailed Description

Singeleton class that manages the source of randomness in the library.

It consists of a wrapper around an std::mt19937 Mersenne twister random number generator engine and an std⇔ ::random\_device engine. The latter is used to seed the Mersenne twister. The class also seeds the standard std::srand C number generator, as it is used by Eigen.

#### 7.5.2 Constructor & Destructor Documentation

7.5.2.1 qpp::RandomDevices::RandomDevices() [inline], [private]

Initializes and seeds the random number generators.

#### 7.5.3 Friends And Related Function Documentation

```
7.5.3.1 friend class internal::Singleton < RandomDevices > [friend]
```

#### 7.5.4 Member Data Documentation

```
7.5.4.1 std::random_device qpp::RandomDevices::_rd [private]
used to seed std::mt19937 _rng
```

```
7.5.4.2 std::mt19937 qpp::RandomDevices::_rng
```

Mersenne twister random number generator engine.

The documentation for this class was generated from the following file:

· include/classes/randevs.h

# 7.6 qpp::internal::Singleton < T > Class Template Reference

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

```
#include <singleton.h>
```

#### **Static Public Member Functions**

• static T & get\_instance ()

#### **Protected Member Functions**

- Singleton ()=default
- virtual ∼Singleton ()
- Singleton (const Singleton &)=delete
- Singleton & operator= (const Singleton &)=delete

# 7.6.1 Detailed Description

```
template<typename T>class qpp::internal::Singleton< T>
```

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

To implement a singleton, derive your class from *qpp::internal::Singleton*, make *qpp::internal::Singleton* a friend of your class, then declare the constructor of your class as private. To get an instance, use the static member function *qpp::internal::Singleton::get\_instance()*, which returns a reference to your newly created singleton (thread-safe in C++11).

#### Example:

```
class MySingleton: public qpp::internal::Singleton<MySingleton>{
         friend class qpp::internal::Singleton<MySingleton>;
public:
         // Declare all public members here
private:
         MySingleton()
```

```
{
      // Implement the constructor here
  }
};

MySingleton& mySingleton = MySingleton::get_instance(); // Get an instance
```

See also

Code of *qpp::Gates*, *qpp::RandomDevices*, *qpp::States* or *qpp.h* for real world examples of usage.

- 7.6.2 Constructor & Destructor Documentation
- $\textbf{7.6.2.1} \quad template < typename \ \textbf{T} > \textbf{qpp::internal::Singleton} < \textbf{T} > :: \textbf{Singleton} ( \ ) \quad \texttt{[protected], [default]}$
- 7.6.2.2 template<typename T> virtual qpp::internal::Singleton< T>::~Singleton( ) [inline], [protected], [virtual]
- 7.6.2.3 template<typename T> qpp::internal::Singleton < T >::Singleton ( const Singleton < T > & ) [protected], [delete]
- 7.6.3 Member Function Documentation
- 7.6.3.1 template < typename T > static T& qpp::internal::Singleton < T >::get\_instance( ) [inline], [static]
- 7.6.3.2 template<typename T> Singleton& qpp::internal::Singleton< T>::operator=( const Singleton< T>& ) [protected], [delete]

The documentation for this class was generated from the following file:

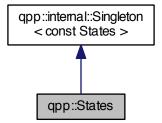
• include/classes/singleton.h

# 7.7 qpp::States Class Reference

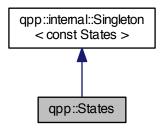
const Singleton class that implements most commonly used states

```
#include <states.h>
```

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



#### **Public Attributes**

```
    ket x0 { ket::Zero(2) }

      Pauli Sigma-X 0-eigenstate |+>

    ket x1 { ket::Zero(2) }

      Pauli Sigma-X 1-eigenstate |->
ket y0 { ket::Zero(2) }
      Pauli Sigma-Y 0-eigenstate.
ket y1 { ket::Zero(2) }
      Pauli Sigma-Y 1-eigenstate.

    ket z0 { ket::Zero(2) }

      Pauli Sigma-Z 0-eigenstate | 0>

    ket z1 { ket::Zero(2) }

      Pauli Sigma-Z 1-eigenstate | 1>

    cmat px0 { cmat::Zero(2, 2) }

      Projector onto the Pauli Sigma-X 0-eigenstate |+><+|.

    cmat px1 { cmat::Zero(2, 2) }

      Projector onto the Pauli Sigma-X 1-eigenstate |-><-|.
cmat py0 { cmat::Zero(2, 2) }
      Projector onto the Pauli Sigma-Y 0-eigenstate.

    cmat py1 { cmat::Zero(2, 2) }

      Projector onto the Pauli Sigma-Y 1-eigenstate.

    cmat pz0 { cmat::Zero(2, 2) }

      Projector onto the Pauli Sigma-Z 0-eigenstate |0><0|.
cmat pz1 { cmat::Zero(2, 2) }
      Projector onto the Pauli Sigma-Z 1-eigenstate | 1><1|.
ket b00 { ket::Zero(4) }
      Bell-00 state (following the convention in Nielsen and Chuang)
ket b01 { ket::Zero(4) }
      Bell-01 state (following the convention in Nielsen and Chuang)

    ket b10 { ket::Zero(4) }

      Bell-10 state (following the convention in Nielsen and Chuang)
ket b11 { ket::Zero(4) }
      Bell-11 state (following the convention in Nielsen and Chuang)
```

cmat pb00 { cmat::Zero(4, 4) }

```
Projector onto the Bell-00 state.

cmat pb01 { cmat::Zero(4, 4) }

Projector onto the Bell-01 state.

cmat pb10 { cmat::Zero(4, 4) }

Projector onto the Bell-10 state.

cmat pb11 { cmat::Zero(4, 4) }

Projector onto the Bell-11 state.

ket GHZ { ket::Zero(8) }

GHZ state.

ket W { ket::Zero(8) }

W state.

cmat pGHZ { cmat::Zero(8, 8) }

Projector onto the GHZ state.

cmat pW { cmat::Zero(8, 8) }

Projector onto the W state.
```

#### **Private Member Functions**

• States ()

#### **Friends**

class internal::Singleton < const States >

# **Additional Inherited Members**

# 7.7.1 Detailed Description

Initialize the states

const Singleton class that implements most commonly used states

# 7.7.2 Constructor & Destructor Documentation

```
7.7.2.1 qpp::States::States() [inline], [private]
```

# 7.7.3 Friends And Related Function Documentation

**7.7.3.1 friend class internal::Singleton** < **const States** > [friend]

# 7.7.4 Member Data Documentation

7.7.4.1 ket qpp::States::b00 { ket::Zero(4) }

Bell-00 state (following the convention in Nielsen and Chuang)

7.7.4.2 ket qpp::States::b01 { ket::Zero(4) }

Bell-01 state (following the convention in Nielsen and Chuang)

```
7.7.4.3 ket qpp::States::b10 { ket::Zero(4) }
Bell-10 state (following the convention in Nielsen and Chuang)
7.7.4.4 ket qpp::States::b11 { ket::Zero(4) }
Bell-11 state (following the convention in Nielsen and Chuang)
7.7.4.5 ket qpp::States::GHZ { ket::Zero(8) }
GHZ state.
7.7.4.6 cmat qpp::States::pb00 { cmat::Zero(4, 4) }
Projector onto the Bell-00 state.
7.7.4.7 cmat qpp::States::pb01 { cmat::Zero(4, 4) }
Projector onto the Bell-01 state.
7.7.4.8 cmat qpp::States::pb10 { cmat::Zero(4, 4) }
Projector onto the Bell-10 state.
7.7.4.9 cmat qpp::States::pb11 { cmat::Zero(4, 4) }
Projector onto the Bell-11 state.
7.7.4.10 cmat qpp::States::pGHZ { cmat::Zero(8, 8) }
Projector onto the GHZ state.
7.7.4.11 cmat qpp::States::pW { cmat::Zero(8, 8) }
Projector onto the W state.
7.7.4.12 cmat qpp::States::px0 { cmat::Zero(2, 2) }
Projector onto the Pauli Sigma-X 0-eigenstate |+><+|.
7.7.4.13 cmat qpp::States::px1 { cmat::Zero(2, 2) }
Projector onto the Pauli Sigma-X 1-eigenstate |-><-|.
7.7.4.14 cmat qpp::States::py0 { cmat::Zero(2, 2) }
```

Projector onto the Pauli Sigma-Y 0-eigenstate.

```
7.7.4.15 cmat qpp::States::py1 { cmat::Zero(2, 2) }
Projector onto the Pauli Sigma-Y 1-eigenstate.
7.7.4.16 cmat qpp::States::pz0 { cmat::Zero(2, 2) }
Projector onto the Pauli Sigma-Z 0-eigenstate |0><0|.
7.7.4.17 cmat qpp::States::pz1 { cmat::Zero(2, 2) }
Projector onto the Pauli Sigma-Z 1-eigenstate |1><1|.
7.7.4.18 ket qpp::States::W { ket::Zero(8) }
W state.
7.7.4.19 ket qpp::States::x0 { ket::Zero(2) }
Pauli Sigma-X 0-eigenstate |+>
7.7.4.20 ket qpp::States::x1 { ket::Zero(2) }
Pauli Sigma-X 1-eigenstate |->
7.7.4.21 ket qpp::States::y0 { ket::Zero(2) }
Pauli Sigma-Y 0-eigenstate.
7.7.4.22 ket qpp::States::y1 { ket::Zero(2) }
Pauli Sigma-Y 1-eigenstate.
7.7.4.23 ket qpp::States::z0 { ket::Zero(2) }
Pauli Sigma-Z 0-eigenstate |0>
7.7.4.24 ket qpp::States::z1 { ket::Zero(2) }
Pauli Sigma-Z 1-eigenstate |1>
The documentation for this class was generated from the following file:
```

# 7.8 qpp::Timer Class Reference

• include/classes/states.h

#### Measures time.

```
#include <timer.h>
```

#### **Public Member Functions**

• Timer ()

Constructs an instance with the current time as the starting point.

void tic ()

Resets the chronometer.

• const Timer & toc ()

Stops the chronometer.

· double seconds () const

Time passed in seconds.

#### **Protected Attributes**

```
• std::chrono::steady_clock::time_point _start
```

```
• std::chrono::steady_clock::time_point _end
```

#### **Friends**

std::ostream & operator<< (std::ostream &os, const Timer &rhs)</li>
 Overload for std::ostream operators.

# 7.8.1 Detailed Description

Measures time.

Uses a std::chrono::steady\_clock. It is not affected by wall clock changes during runtime.

#### 7.8.2 Constructor & Destructor Documentation

```
7.8.2.1 qpp::Timer::Timer() [inline]
```

Constructs an instance with the current time as the starting point.

#### 7.8.3 Member Function Documentation

```
7.8.3.1 double qpp::Timer::seconds ( ) const [inline]
```

Time passed in seconds.

#### Returns

Number of seconds that passed between the instantiation/reset and invocation of qpp::Timer::toc()

```
7.8.3.2 void qpp::Timer::tic() [inline]
```

Resets the chronometer.

Resets the starting/ending point to the current time

7.8.3.3 const Timer& qpp::Timer::toc( ) [inline]

Stops the chronometer.

Set the current time as the ending point

Returns

Current instance

#### 7.8.4 Friends And Related Function Documentation

7.8.4.1 std::ostream & operator << ( std::ostream & os, const Timer & rhs ) [friend]

Overload for std::ostream operators.

#### **Parameters**

os	Output stream
rhs	Timer instance

#### Returns

Writes to the output stream the number of seconds that passed between the instantiation/reset and invocation of qpp::Timer::toc().

# 7.8.5 Member Data Documentation

```
7.8.5.1 std::chrono::steady_clock::time_point qpp::Timer::_end [protected]
```

**7.8.5.2 std::chrono::steady\_clock::time\_point qpp::Timer::\_start** [protected]

The documentation for this class was generated from the following file:

· include/classes/timer.h

# **Chapter 8**

# **File Documentation**

# 8.1 include/classes/exception.h File Reference

This graph shows which files directly or indirectly include this file:



# **Classes**

class qpp::Exception

Generates custom exceptions, used when validating function parameters.

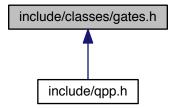
# **Namespaces**

• qpp

132 File Documentation

# 8.2 include/classes/gates.h File Reference

This graph shows which files directly or indirectly include this file:



# Classes

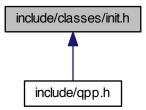
class qpp::Gates
 const Singleton class that implements most commonly used gates

# **Namespaces**

qpp

# 8.3 include/classes/init.h File Reference

This graph shows which files directly or indirectly include this file:



# **Classes**

class qpp::Init

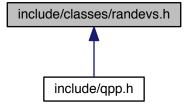
const Singleton class that performs additional initializations/cleanups

# **Namespaces**

• qpp

# 8.4 include/classes/randevs.h File Reference

This graph shows which files directly or indirectly include this file:



# Classes

• class qpp::RandomDevices

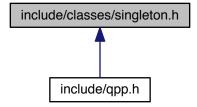
Singeleton class that manages the source of randomness in the library.

# **Namespaces**

• qpp

# 8.5 include/classes/singleton.h File Reference

This graph shows which files directly or indirectly include this file:



# Classes

class qpp::internal::Singleton< T >

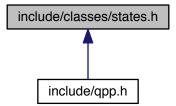
Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

# **Namespaces**

- qpp
- · qpp::internal

# 8.6 include/classes/states.h File Reference

This graph shows which files directly or indirectly include this file:



# Classes

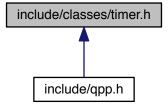
class qpp::States

const Singleton class that implements most commonly used states

# **Namespaces**

# 8.7 include/classes/timer.h File Reference

This graph shows which files directly or indirectly include this file:



# Classes

• class qpp::Timer

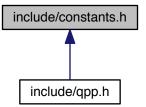
Measures time.

# **Namespaces**

• qpp

# 8.8 include/constants.h File Reference

This graph shows which files directly or indirectly include this file:



# **Namespaces**

## **Functions**

```
 \bullet \ \ constexpr \ std::complex < double > qpp::operator""\_i \ (unsigned \ long \ long \ int \ x) \\
```

User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)

constexpr std::complex< double > qpp::operator""\_i (long double x)

User-defined literal for complex  $i = \sqrt{-1}$  (real overload)

• std::complex< double > qpp::omega (std::size\_t D)

D-th root of unity.

#### **Variables**

• constexpr double <a href="mailto:qpp::chop">qpp::chop</a> = 1e-10

Used in qpp::disp() and qpp::displn() for setting to zero numbers that have their absolute value smaller than qpp::ct← ::chop.

constexpr double qpp::eps = 1e-12

Used to decide whether a number or expression in double precision is zero or not.

• constexpr std::size\_t qpp::maxn = 64

Maximum number of qubits.

• constexpr double qpp::pi = 3.141592653589793238462643383279502884

 $\pi$ 

• constexpr double qpp::ee = 2.718281828459045235360287471352662497

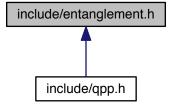
Base of natural logarithm, e.

• constexpr std::size\_t qpp::infty = -1

Used to denote infinity.

# 8.9 include/entanglement.h File Reference

This graph shows which files directly or indirectly include this file:



## **Namespaces**

#### **Functions**

template<typename Derived >
 DynColVect< cplx > qpp::schmidtcoeff (const Eigen::MatrixBase< Derived > &A, const std::vector< std
 ::size\_t > &dims)

Schmidt coefficients of the bi-partite pure state A.

template<typename Derived >

 $\verb|cmat|| \textit{qpp::schmidtU}| (const| Eigen::MatrixBase < Derived > \&A, const| std::vector < std::size\_t > \&dims)|$ 

Schmidt basis on Alice's side.

template<typename Derived >

 $\verb|cmat|| \verb|qpp::schmidtV| (const| Eigen::MatrixBase < Derived > \&A, const| std::vector < std::size\_t > \&dims)|$ 

Schmidt basis on Bob's side.

• template<typename Derived >

 $\label{lem:def:def:def:def:DynColVect} \mbox{DynColVect} < \mbox{double} > \mbox{qpp::schmidtprob} \mbox{ (const Eigen::MatrixBase} < \mbox{Derived} > \&\mbox{A, const std::vector} < \mbox{std} :: \mbox{size\_t} > \&\mbox{dims})$ 

Schmidt probabilities of the bi-partite pure state A.

template<typename Derived >

 $\label{lem:double qpp::entanglement} double \ qpp::entanglement \ (const \ Eigen::MatrixBase < Derived > \&A, \ const \ std::vector < std::size\_t > \&dims) \\ Entanglement \ of \ the \ bi-partite \ pure \ state \ A.$ 

template<typename Derived >

double <a href="mailto:qpp::gconcurrence">qpp::gconcurrence</a> (const Eigen::MatrixBase</a> Derived > &A)

G-concurrence of the bi-partite pure state A.

template<typename Derived >

double qpp::negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)

Negativity of the bi-partite mixed state A.

 $\bullet \ \ \text{template}{<} \text{typename Derived} >$ 

 $\label{lognegativity} \textit{double qpp::lognegativity} \; (\textit{const Eigen::MatrixBase} < \textit{Derived} > \&A, \; \textit{const std::vector} < \textit{std::size\_t} > \& \textit{dims})$ 

Logarithmic negativity of the bi-partite mixed state A.

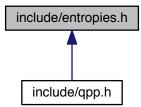
• template<typename Derived >

double <a href="mailto:qpp::concurrence">qpp::concurrence</a> (const Eigen::MatrixBase</a> Derived > &A)

Wootters concurrence of the bi-partite qubit mixed state A.

# 8.10 include/entropies.h File Reference

This graph shows which files directly or indirectly include this file:



## **Namespaces**

#### **Functions**

```
    template<typename Derived >
        double qpp::shannon (const Eigen::MatrixBase< Derived > &A)
```

Shannon/von-Neumann entropy of the probability distribution/density matrix A.

template<typename Derived >
 double qpp::renyi (const Eigen::MatrixBase< Derived > &A, double alpha)

Renyi-  $\alpha$  entropy of the probability distribution/density matrix A, for  $\alpha \geq 0$ .

template<typename Derived >
 double qpp::tsallis (const Eigen::MatrixBase< Derived > &A, double alpha)

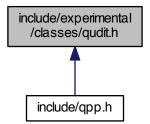
Tsallis-  $\alpha$  entropy of the probability distribution/density matrix A, for  $\alpha \geq 0$ 

template<typename Derived >
 double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t >
 &subsysA, const std::vector< std::size\_t > &subsysB, const std::vector< std::size\_t > &dims)

Quantum mutual information between 2 subsystems of a composite system.

# 8.11 include/experimental/classes/qudit.h File Reference

This graph shows which files directly or indirectly include this file:



## Classes

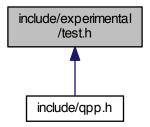
· class qpp::experimental::Qudit

# **Namespaces**

- qpp
- qpp::experimental

# 8.12 include/experimental/test.h File Reference

This graph shows which files directly or indirectly include this file:



## **Namespaces**

- qpp::experimental
- qpp

#### **Functions**

template<typename Derived1, typename Derived2 >
 DynMat< typename Derived1::Scalar > qpp::experimental::apply (const Eigen::MatrixBase< Derived1 >
 &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size\_t > &subsys, const std
 ::vector< std::size\_t > &dims)

Applies the gate A to the part subsys of a multipartite state vector or density matrix.

template<typename Derived >
 cmat qpp::experimental::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat >
 &Ks, const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)

Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.

cmat qpp::experimental::super (const std::vector< cmat > &Ks)

Superoperator matrix representation.

template<typename Derived >
 DynMat< typename Derived::Scalar > qpp::experimental::CTRL (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &crl, const std::vector< std::size\_t > &subsys, std::size\_t n, std::size\_t d=2)

Generates the multipartite multiple-controlled-A gate in matrix form.

cmat qpp::experimental::choi (const std::vector< cmat > &Ks)

Choi matrix representation.

std::vector< cmat > qpp::experimental::randkraus (std::size\_t n, std::size\_t D)

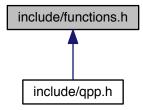
Generates a set of random Kraus operators.

template<typename Derived >
 double qpp::experimental::renyi\_inf (const Eigen::MatrixBase< Derived > &A)

Renyi- $\infty$  entropy (min entropy) of the probability distribution/density matrix A.

#### 8.13 include/functions.h File Reference

This graph shows which files directly or indirectly include this file:



## **Namespaces**

qpp

Element-wise product of A.

double <a href="mailto:qpp::norm">qpp::norm</a> (const Eigen::MatrixBase< Derived > &A)

template<typename Derived >

## **Functions**

```
    template<typename Derived >

  DynMat< typename Derived::Scalar > qpp::transpose (const Eigen::MatrixBase< Derived > &A)
      Transpose.

    template<typename Derived >

  DynMat< typename Derived::Scalar > qpp::conjugate (const Eigen::MatrixBase< Derived > &A)
      Complex conjugate.

    template<typename Derived >

  DynMat< typename Derived::Scalar > qpp::adjoint (const Eigen::MatrixBase< Derived > &A)
• template<typename Derived >
  DynMat< typename Derived::Scalar > qpp::inverse (const Eigen::MatrixBase< Derived > &A)
      Inverse.

    template<typename Derived >

  Derived::Scalar qpp::trace (const Eigen::MatrixBase< Derived > &A)
      Trace.

    template<typename Derived >

  Derived::Scalar <a href="mailto:qpp::det">qpp::det</a> (const Eigen::MatrixBase</a> Derived > &A)
      Determinant.

    template<typename Derived >

  Derived::Scalar qpp::logdet (const Eigen::MatrixBase< Derived > &A)
      Logarithm of the determinant.
template<typename Derived >
  Derived::Scalar qpp::sum (const Eigen::MatrixBase< Derived > &A)
      Element-wise sum of A.
• template<typename Derived >
  Derived::Scalar <a href="mailto:open:prod">open:prod</a> (const Eigen::MatrixBase</a> Derived > &A)
```

```
Frobenius norm.
• template<typename Derived >
  DynColVect< cplx > qpp::evals (const Eigen::MatrixBase< Derived > &A)
     Eigenvalues.

    template<typename Derived >

  cmat qpp::evects (const Eigen::MatrixBase< Derived > &A)
     Eigenvectors.
• template<typename Derived >
  DynColVect< double > qpp::hevals (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvalues.

    template<typename Derived >

  cmat qpp::hevects (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvectors.
• template<typename Derived >
  DynColVect< double > qpp::svals (const Eigen::MatrixBase< Derived > &A)
     Singular values.

    template<typename Derived >

  cmat qpp::svdU (const Eigen::MatrixBase< Derived > &A)
     Left singular vectors.

    template<typename Derived >

  cmat qpp::svdV (const Eigen::MatrixBase< Derived > &A)
     Right singular vectors.
• template<typename Derived >
  cmat qpp::funm (const Eigen::MatrixBase< Derived > &A, cplx(*f)(const cplx &))
     Functional calculus f(A)

    template<typename Derived >

  cmat qpp::sqrtm (const Eigen::MatrixBase< Derived > &A)
     Matrix square root.
• template<typename Derived >
  cmat <a href="mailto:qpp::absm">qpp::absm</a> (const Eigen::MatrixBase</a> Derived > &A)
     Matrix absolut value.

    template<typename Derived >

  cmat qpp::expm (const Eigen::MatrixBase< Derived > &A)
     Matrix exponential.
• template<typename Derived >
  cmat qpp::logm (const Eigen::MatrixBase< Derived > &A)
     Matrix logarithm.
• template<typename Derived >
  cmat qpp::sinm (const Eigen::MatrixBase< Derived > &A)
     Matrix sin.

    template<typename Derived >

  cmat qpp::cosm (const Eigen::MatrixBase< Derived > &A)
     Matrix cos.

    template<typename Derived >

  cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived > &A, const cplx z)
     Matrix power.

    template<typename Derived >

  DynMat< typename Derived::Scalar > qpp::powm (const Eigen::MatrixBase< Derived > &A, std::size_t n)
     Matrix power.

    template<typename Derived >

  double qpp::schatten (const Eigen::MatrixBase< Derived > &A, std::size_t p)
      Schatten norm.
```

• template<typename OutputScalar , typename Derived > DynMat< OutputScalar > qpp::cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(\*f)(const typename Derived::Scalar &)) Functor. template<typename T > DynMat< typename T::Scalar > qpp::kron (const T &head) Kronecker product (variadic overload) • template<typename T , typename... Args> DynMat< typename T::Scalar > qpp::kron (const T &head, const Args &...tail) Kronecker product (variadic overload) template<typename Derived > DynMat< typename Derived::Scalar > qpp::kron (const std::vector< Derived > &As) Kronecker product (std::vector overload) template<typename Derived > DynMat< typename Derived::Scalar > qpp::kron (const std::initializer list< Derived > &As) Kronecker product (std::initializer\_list overload) template<typename Derived > DynMat< typename Derived::Scalar > qpp::kronpow (const Eigen::MatrixBase< Derived > &A, std::size\_t n) Kronecker power. template<typename Derived > DynMat< typename Derived::Scalar > qpp::reshape (const Eigen::MatrixBase< Derived > &A, std::size\_t rows, std::size\_t cols) Reshape. template<typename Derived1 , typename Derived2 > DynMat< typename Derived1::Scalar > qpp::comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B) Commutator. template<typename Derived1 , typename Derived2 > DynMat< typename Derived1::Scalar > qpp::anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B) Anti-commutator. template<typename Derived > DynMat< typename Derived::Scalar > qpp::prj (const Eigen::MatrixBase< Derived > &V) Projector. template < typename Derived > DynMat< typename Derived::Scalar > qpp::grams (const std::vector< Derived > &Vs) Gram-Schmidt orthogonalization (std::vector overload) template<typename Derived > DynMat< typename Derived::Scalar > qpp::grams (const std::initializer\_list< Derived > &Vs) Gram-Schmidt orthogonalization (std::initializer list overload) • template<typename Derived > DynMat< typename Derived::Scalar > qpp::grams (const Eigen::MatrixBase< Derived > &A) Gram-Schmidt orthogonalization (Eigen expression (matrix) overload) std::vector < std::size t > qpp::n2multiidx (std::size t n, const std::vector < std::size t > &dims) Non-negative integer index to multi-index. std::size t qpp::multiidx2n (const std::vector< std::size t > &midx, const std::vector< std::size t > &dims) Multi-index to non-negative integer index. ket qpp::mket (const std::vector< std::size\_t > &mask, const std::vector< std::size\_t > &dims) Multi-partite qudit ket (different dimensions overload) ket qpp::mket (const std::vector< std::size t > &mask, std::size t d=2) Multi-partite qudit ket (same dimensions overload) cmat qpp::mprj (const std::vector< std::size\_t > &mask, const std::vector< std::size\_t > &dims)

Projector onto multi-partite qudit ket (different dimensions overload)

cmat qpp::mprj (const std::vector< std::size\_t > &mask, std::size\_t d=2)

Projector onto multi-partite qudit ket (same dimensions overload)

- std::vector< std::size\_t > qpp::invperm (const std::vector< std::size\_t > &perm)
  - Inverse permutation.

Compose permutations.

template<typename InputIterator >

std::vector< double > qpp::abssq (InputIterator first, InputIterator last)

Computes the absolut values squared of a range of complex numbers.

• template<typename Derived >

std::vector< double > qpp::abssq (const Eigen::MatrixBase< Derived > &V)

Computes the absolut values squared of a column vector.

template<typename InputIterator >

auto qpp::sum (InputIterator first, InputIterator last) -> typename InputIterator::value\_type

Element-wise sum of a range.

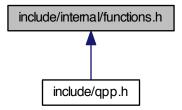
template<typename InputIterator >

auto qpp::prod (InputIterator first, InputIterator last) -> typename InputIterator::value\_type

Element-wise product of a range.

## 8.14 include/internal/functions.h File Reference

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

- · qpp::internal
- qpp

#### **Functions**

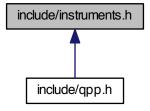
- void qpp::internal:: n2multiidx (std::size t n, std::size t numdims, const std::size t \*dims, std::size t \*result)
- std::size\_t qpp::internal::\_multiidx2n (const std::size\_t \*midx, std::size\_t numdims, const std::size\_t \*dims)
- template<typename Derived >
   bool qpp::internal::\_check\_square\_mat (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_vector (const Eigen::MatrixBase< Derived > &A)

```
    template<typename Derived >
        bool qpp::internal::_check_row_vector (const Eigen::MatrixBase< Derived > &A)
```

- template<typename Derived >
   bool qpp::internal::\_check\_col\_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename T >
   bool qpp::internal:: check nonzero size (const T &x)
- bool qpp::internal::\_check\_dims (const std::vector< std::size\_t > &dims)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_mat (const std::vector< std::size\_t > &dims, const Eigen::Matrix
   Base< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_cvect (const std::vector< std::size\_t > &dims, const Eigen::Matrix
   Base< Derived > &V)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_rvect (const std::vector< std::size\_t > &dims, const Eigen::Matrix
   Base< Derived > &V)
- bool qpp::internal::\_check\_eq\_dims (const std::vector < std::size\_t > &dims, std::size\_t dim)
- bool qpp::internal::\_check\_subsys\_match\_dims (const std::vector< std::size\_t > &subsys, const std
   ::vector< std::size\_t > &dims)
- bool qpp::internal::\_check\_perm (const std::vector< std::size\_t > &perm)
- template<typename Derived1, typename Derived2 >
   DynMat< typename Derived1::Scalar > qpp::internal::\_kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename T >
   void qpp::internal::variadic\_vector\_emplace (std::vector< T > &)
- template<typename T, typename First, typename... Args>
   void qpp::internal::variadic\_vector\_emplace (std::vector< T > &v, First &&first, Args &&...args)

## 8.15 include/instruments.h File Reference

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

#### **Functions**

```
    template<typename Derived >
        std::pair< std::vector< double >
        , std::vector< cmat >> qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat >
        &Ks)
```

Measures the state A using the set of Kraus operators Ks.

```
    template<typename Derived >
        std::pair< std::vector< double >
        , std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)
```

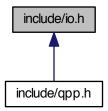
Measures the state A using the set of Kraus operators Ks (std::initializer\_list overload)

```
    template<typename Derived >
        std::pair< std::vector< double >
        , std::vector< cmat >> qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &M)
```

Measures the state A in the orthonormal basis specified by the eigenvectors of M.

#### 8.16 include/io.h File Reference

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

• qpp

#### **Functions**

template<typename InputIterator >
 void qpp::disp (const InputIterator &first, const InputIterator &last, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a range. Does not add a newline.

template<typename InputIterator >
 std::ostream & qpp::displn (const InputIterator &first, const InputIterator &last, const std::string &separator,
 const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a range. Adds a newline.

template<typename T >
 std::ostream & qpp::disp (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a standard container that supports std::begin, std::end and forward iteration. Does not add a newline.

• template<typename T >

std::ostream & qpp::displn (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a standard container that supports std::begin, std::end and forward iteration. Adds a newline.

• template<typename T >

std::ostream & qpp::disp (const T \*x, const std::size\_t n, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a C-style array. Does not add a newline.

• template<typename T >

std::ostream & qpp::displn (const T \*x, const std::size\_t n, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)

Displays a C-style array. Adds a newline.

• template<typename Derived >

std::ostream & qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop, std::ostream &os=std::cout)

Displays an Eigen expression in matrix friendly form. Does not add a new line.

• template<typename Derived >

std::ostream & qpp::displn (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop, std::ostream &os=std::cout)

Displays an Eigen expression in matrix friendly form. Adds a newline.

std::ostream & qpp::disp (const cplx z, double chop=qpp::chop, std::ostream &os=std::cout)

Displays a number (implicitly converted to std::complex<double>) in friendly form. Does not add a new line.

std::ostream & qpp::displn (const cplx z, double chop=qpp::chop, std::ostream &os=std::cout)

Displays a number (implicitly converted to std::complex<double>) in friendly form. Adds a new line.

template<typename Derived >

void qpp::save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

Saves Eigen expression to a binary file (internal format) in double precision.

• template<typename Derived >

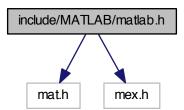
 $\label{eq:const_std::string} \ \, \text{DynMat} < \text{typename Derived::Scalar} > \ \, \text{qpp::load (const std::string \&fname)}$ 

Loads Eigen matrix from a binary file (internal format) in double precision.

## 8.17 include/MATLAB/matlab.h File Reference

#include "mat.h"
#include "mex.h"

Include dependency graph for matlab.h:



#### **Namespaces**

• qpp

#### **Functions**

template < typename Derived >
 Derived qpp::loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.

template<>
 dmat qpp::loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices (qpp::dmat)

template<>

cmat qpp::loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

template<typename Derived >
 void qpp::saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)

Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.

template<>
 void qpp::saveMATLABmatrix (const Eigen::MatrixBase< dmat > &A, const std::string &mat\_file, const std
 ::string &var\_name, const std::string &mode)

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices (qpp::dmat)

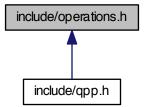
template<>

void qpp::saveMATLABmatrix (const Eigen::MatrixBase< cmat > &A, const std::string &mat\_file, const std
::string &var\_name, const std::string &mode)

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

# 8.18 include/operations.h File Reference

This graph shows which files directly or indirectly include this file:



# **Namespaces**

#### **Functions**

template<typename Derived1 , typename Derived2 >
 DynMat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state,
 const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size\_t > &ctrl, const std::vector< std
 ::size\_t > &subsys, std::size\_t n, std::size\_t d=2)

Applies the controlled-gate A to the part subsys of a multipartite state vector or density matrix.

• template<typename Derived1 , typename Derived2 >

DynMat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size\_t > &subsys, std::size\_t n, std::size\_t d=2)

Applies the gate A to the part subsys of a multipartite state vector or density matrix.

template<typename Derived >

```
cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks)
```

Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.

• template<typename Derived >

```
cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std
::vector< std::size_t > &subsys, std::size_t n, std::size_t d=2)
```

Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.

cmat qpp::super (const std::vector< cmat > &Ks)

Superoperator matrix representation.

cmat qpp::choi (const std::vector< cmat > &Ks)

Choi matrix representation.

std::vector< cmat > qpp::choi2kraus (const cmat &A)

Extracts orthogonal Kraus operators from Choi matrix.

 $\bullet \ \ \mathsf{template} \mathord{<} \mathsf{typename} \ \mathsf{Derived} >$ 

Partial trace.

• template<typename Derived >

```
\label{lem:def:def:DynMat} DynMat < typename \ Derived::Scalar > qpp::ptrace2 \ (const \ Eigen::MatrixBase < Derived > &A, \ const \ std \\ ::vector < std::size_t > &dims)
```

Partial trace.

template<typename Derived >

```
\label{lem:def:def:DynMat} \mbox{DynMat} < \mbox{typename Derived::Scalar} > \mbox{qpp::ptrace (const Eigen::MatrixBase} < \mbox{Derived} > \mbox{\&A, const std} :: \mbox{vector} < \mbox{std::size\_t} > \mbox{\&subsys, const std::vector} < \mbox{std::size\_t} > \mbox{\&dims})
```

Partial trace.

• template<typename Derived >

Partial transpose.

template<typename Derived >

```
DynMat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &perm, const std::vector< std::size_t > &dims)
```

System permutation.

# 8.19 include/qpp.h File Reference

```
#include <algorithm>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <ctime>
#include <exception>
#include <fstream>
#include <functional>
#include <initializer list>
#include <iomanip>
#include <iostream>
#include <iterator>
#include <limits>
#include <numeric>
#include <ostream>
#include <random>
#include <sstream>
#include <stdexcept>
#include <string>
#include <tuple>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "constants.h"
#include "types.h"
#include "classes/exception.h"
#include "classes/singleton.h"
#include "classes/states.h"
#include "classes/randevs.h"
#include "internal/functions.h"
#include "classes/init.h"
#include "functions.h"
#include "classes/gates.h"
#include "operations.h"
#include "entropies.h"
#include "io.h"
#include "entanglement.h"
#include "instruments.h"
#include "random.h"
#include "classes/timer.h"
#include "experimental/test.h"
#include "experimental/classes/qudit.h"
Include dependency graph for qpp.h:
```

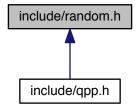
#### **Namespaces**

#### **Variables**

```
    RandomDevices & qpp::rdevs = RandomDevices::get_instance()
        qpp::RandomDevices Singleton
    const Gates & qpp::gt = Gates::get_instance()
        qpp::Gates const Singleton
    const States & qpp::st = States::get_instance()
        qpp::States const Singleton
    const Init & qpp::init = Init::get_instance()
        qpp::Init const Singleton
```

## 8.20 include/random.h File Reference

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

qpp

#### **Functions**

```
    template<typename Derived >
        Derived qpp::rand (std::size_t rows, std::size_t cols, double a=0, double b=1)
        Generates a random matrix with entries uniformly distributed in the interval [a, b)
    template<>
        dmat qpp::rand (std::size_t rows, std::size_t cols, double a, double b)
        Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)
    template<>
        cmat qpp::rand (std::size_t rows, std::size_t cols, double a, double b)
        Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)
```

• double qpp::rand (double a=0, double b=1)

Generates a random real number uniformly distributed in the interval [a, b)

- int qpp::randint (int a=std::numeric\_limits< int >::min(), int b=std::numeric\_limits< int >::max())
  - Generates a random integer (int) uniformly distributed in the interval [a, b].
- template<typename Derived >

Derived qpp::randn (std::size\_t rows, std::size\_t cols, double mean=0, double sigma=1)

Generates a random matrix with entries normally distributed in N(mean, sigma)

template<>

dmat qpp::randn (std::size\_t rows, std::size\_t cols, double mean, double sigma)

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)

template<>

cmat qpp::randn (std::size t rows, std::size t cols, double mean, double sigma)

Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)

• double <a href="mailto:qpp::randn">qpp::randn</a> (double mean=0, double sigma=1)

Generates a random real number (double) normally distributed in N(mean, sigma)

cmat qpp::randU (std::size\_t D)

Generates a random unitary matrix.

cmat qpp::randV (std::size\_t Din, std::size\_t Dout)

Generates a random isometry matrix.

std::vector< cmat > qpp::randkraus (std::size\_t N, std::size\_t D)

Generates a set of random Kraus operators.

cmat qpp::randH (std::size\_t D)

Generates a random Hermitian matrix.

ket qpp::randket (std::size\_t D)

Generates a random normalized ket (pure state vector)

cmat qpp::randrho (std::size\_t D)

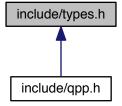
Generates a random density matrix.

std::vector< std::size\_t > qpp::randperm (std::size\_t n)

Generates a random uniformly distributed permutation.

# 8.21 include/types.h File Reference

This graph shows which files directly or indirectly include this file:



## **Namespaces**

# **Typedefs**

```
• using qpp::cplx = std::complex < double >
     Complex number in double precision.
template<typename Scalar >
  using qpp::DynMat = Eigen::Matrix < Scalar, Eigen::Dynamic, Eigen::Dynamic >
     Dynamic Eigen matrix over the field specified by Scalar.
• template<typename Scalar >
 using qpp::DynColVect = Eigen::Matrix < Scalar, Eigen::Dynamic, 1 >
     Dynamic Eigen column vector over the field specified by Scalar.
• template<typename Scalar >
  using qpp::DynRowVect = Eigen::Matrix < Scalar, 1, Eigen::Dynamic >
     Dynamic Eigen row vector over the field specified by Scalar.
using qpp::ket = DynColVect< cplx >
     Complex (double precision) dynamic Eigen column vector.
using qpp::bra = DynRowVect< cplx >
     Complex (double precision) dynamic Eigen row vector.
using qpp::cmat = DynMat< cplx >
     Complex (double precision) dynamic Eigen matrix.
using qpp::dmat = DynMat< double >
     Real (double precision) dynamic Eigen matrix.
```

# 8.22 mainpage.dox File Reference

# Index

aham	ann::Evanntion 107
absm	qpp::Exception, 107 DIMS NOT EQUAL
qpp, 22	
abssq	qpp::Exception, 107 det
qpp, 23	
adjoint	qpp, 36
qpp, 24	disp
anticomm	qpp, 36–38
qpp, 24	displn
apply	qpp, 39–41
qpp, 25	dmat
hus	qpp, 21
bra	00
qpp, 21	66 gpp 92
CUSTOM EXCEPTION	qpp, 92
CUSTOM_EXCEPTION	entanglement
app::Exception, 108	qpp, 42
channel	eps
qpp, 27, 28	qpp, 92
choi	evals
qpp, 29	qpp, 43
choi2kraus	evects
qpp, 30	qpp, 44
chop	expm
qpp, 92	qpp, 44
cmat	funm
qpp, 21	qpp, 45
comm	dbb,
qpp, 31	gconcurrence
compperm	qpp, 45
qpp, 31	grams
concurrence	qpp, 46, 47
qpp, 33	gt
conjugate	qpp, 92
qpp, 33	
cosm	hevals
qpp, 35	hevals qpp, 48
qpp, 35 cplx	
qpp, 35 cplx qpp, 21	qpp, 48
qpp, 35 cplx qpp, 21 cwise	qpp, 48 hevects qpp, 48
qpp, 35 cplx qpp, 21	qpp, 48 hevects qpp, 48 infty
qpp, 35 cplx qpp, 21 cwise qpp, 35	qpp, 48 hevects qpp, 48 infty qpp, 92
qpp, 35 cplx qpp, 21 cwise qpp, 35 DIMS_INVALID	qpp, 48 hevects qpp, 48 infty qpp, 92 init
qpp, 35 cplx qpp, 21 cwise qpp, 35  DIMS_INVALID qpp::Exception, 107	qpp, 48 hevects qpp, 48 infty qpp, 92 init qpp, 92
qpp, 35 cplx qpp, 21 cwise qpp, 35  DIMS_INVALID qpp::Exception, 107 DIMS_MISMATCH_CVECTOR	qpp, 48 hevects qpp, 48 infty qpp, 92 init qpp, 92 inverse
qpp, 35 cplx qpp, 21 cwise qpp, 35  DIMS_INVALID qpp::Exception, 107  DIMS_MISMATCH_CVECTOR qpp::Exception, 107	qpp, 48 hevects qpp, 48 infty qpp, 92 init qpp, 92 inverse qpp, 49
qpp, 35 cplx qpp, 21 cwise qpp, 35  DIMS_INVALID qpp::Exception, 107 DIMS_MISMATCH_CVECTOR qpp::Exception, 107 DIMS_MISMATCH_MATRIX	qpp, 48 hevects qpp, 48 infty qpp, 92 init qpp, 92 inverse qpp, 49 invperm
qpp, 35 cplx qpp, 21 cwise qpp, 35  DIMS_INVALID qpp::Exception, 107  DIMS_MISMATCH_CVECTOR qpp::Exception, 107  DIMS_MISMATCH_MATRIX qpp::Exception, 107	qpp, 48 hevects qpp, 48 infty qpp, 92 init qpp, 92 inverse qpp, 49
qpp, 35 cplx qpp, 21 cwise qpp, 35  DIMS_INVALID qpp::Exception, 107  DIMS_MISMATCH_CVECTOR qpp::Exception, 107  DIMS_MISMATCH_MATRIX qpp::Exception, 107  DIMS_MISMATCH_RVECTOR	qpp, 48 hevects
qpp, 35 cplx qpp, 21 cwise qpp, 35  DIMS_INVALID qpp::Exception, 107  DIMS_MISMATCH_CVECTOR qpp::Exception, 107  DIMS_MISMATCH_MATRIX qpp::Exception, 107	qpp, 48 hevects qpp, 48 infty qpp, 92 init qpp, 92 inverse qpp, 49 invperm

154 INDEX

kron		qpp::Exception, 107
qpp, 50, 51	pi	
kronpow		qpp, 93
qpp, 52	pow	m
load		qpp, 63
load	prj	
qpp, 52		qpp, 63
logdet qpp, 54	prod	
logm		qpp, 64
qpp, 54	ptrac	
lognegativity		qpp, 65
qpp, 55	ptrac	
<b>ЧРР</b> , <b>ОО</b>	ntro	qpp, 66
MATRIX_MISMATCH_SUBSYS	ptrac	
qpp::Exception, 107	ntro	qpp, 67
MATRIX_NOT_CVECTOR	pıraı	nspose
qpp::Exception, 107		qpp, 68
MATRIX_NOT_RVECTOR	qmu	tualinfo
qpp::Exception, 107	•	qpp, 69
MATRIX_NOT_SQUARE	qpp,	
qpp::Exception, 107		absm, 22
MATRIX_NOT_SQUARE_OR_CVECTOR		abssq, 23
qpp::Exception, 107		adjoint, 24
MATRIX_NOT_SQUARE_OR_RVECTOR		anticomm, 24
qpp::Exception, 107		apply, 25
MATRIX_NOT_SQUARE_OR_VECTOR		bra, 21
qpp::Exception, 107		channel, 27, 28
MATRIX_NOT_VECTOR		choi, 29
qpp::Exception, 107		choi2kraus, 30
maxn		chop, 92
qpp, 93		cmat, 21
measure		comm, 31
qpp, 56, 57		compperm, 31
mket		concurrence, 33
qpp, 58		conjugate, 33
mprj		cosm, 35
qpp, 59		cplx, 21
multiidx2n		cwise, 35
qpp, 60		det, 36
n2multiidx		disp, 36–38
qpp, 60		displn, 39-41
NOT BIPARTITE		dmat, 21
qpp::Exception, 108		ee, 92
NOT_QUBIT_GATE		entanglement, 42
qpp::Exception, 108		eps, 92
NOT QUBIT SUBSYS		evals, 43
qpp::Exception, 108		evects, 44
negativity		expm, 44
qpp, 61		funm, 45
norm		gconcurrence, 45
qpp, 62		grams, 46, 47
		gt, 92
OUT_OF_RANGE		hevals, 48
qpp::Exception, 108		hevects, 48
omega		infty, 92
qpp, 62		init, 92
DEDM INIVALID		inverse, 49
PERM_INVALID		invperm, 49

INDEX 155

ket, 22	DIMS_NOT_EQUAL, 107
kron, 50, 51	MATRIX_MISMATCH_SUBSYS, 107
kronpow, 52	MATRIX_NOT_CVECTOR, 107
load, 52	MATRIX_NOT_RVECTOR, 107
logdet, 54	MATRIX_NOT_SQUARE, 107
logm, 54	MATRIX_NOT_SQUARE_OR_CVECTOR, 107
lognegativity, 55	MATRIX_NOT_SQUARE_OR_RVECTOR, 107
maxn, 93	MATRIX_NOT_SQUARE_OR_VECTOR, 107
measure, 56, 57	MATRIX_NOT_VECTOR, 107
mket, 58	NOT BIPARTITE, 108
	NOT QUBIT GATE, 108
mprj, 59	NOT_QUBIT_SUBSYS, 108
multiidx2n, 60	OUT_OF_RANGE, 108
n2multiidx, 60	
negativity, 61	PERM_INVALID, 107
norm, 62	SUBSYS_MISMATCH_DIMS, 107
omega, <mark>62</mark>	TYPE_MISMATCH, 108
pi, 93	UNDEFINED_TYPE, 108
powm, 63	UNKNOWN_EXCEPTION, 107
prj, 63	ZERO_SIZE, 107
prod, 64	
ptrace, 65	rand
ptrace1, 66	qpp, 70, 71
ptrace2, 67	randint
ptranspose, 68	qpp, 72
·	randket
qmutualinfo, 69	qpp, 73
rand, 70, 71	randkraus
randint, 72	qpp, 73
randket, 73	randn
randkraus, 73	qpp, 74, 75
randn, 74, 75	randperm
randperm, 76	•
randrho, 76	qpp, 76
rdevs, 93	randrho
renyi, 77	qpp, 76
reshape, 78	rdevs
save, 78	qpp, 93
schatten, 80	renyi
	qpp, 77
schmidtcoeff, 80	reshape
schmidtprob, 81	qpp, 78
shannon, 84	
sinm, 85	SUBSYS_MISMATCH_DIMS
spectralpowm, 85	qpp::Exception, 107
sqrtm, 86	save
st, 93	qpp, 78
sum, 86, 87	schatten
super, 87	gpp, 80
svals, 88	schmidtcoeff
syspermute, 89	
trace, 90	qpp, 80
	schmidtprob
transpose, 91	qpp, 81
tsallis, 91	shannon
qpp::Exception	qpp, 84
CUSTOM_EXCEPTION, 108	sinm
DIMS_INVALID, 107	qpp, 85
DIMS_MISMATCH_CVECTOR, 107	spectralpowm
DIMS_MISMATCH_MATRIX, 107	qpp, 85
DIMS_MISMATCH_RVECTOR, 107	sqrtm
DIMS_MISMATCH_VECTOR, 107	qpp, 86
/	

156 INDEX

```
st
    qpp, 93
sum
    qpp, 86, 87
super
    qpp, 87
svals
     qpp, <mark>88</mark>
syspermute
    qpp, 89
TYPE_MISMATCH
    qpp::Exception, 108
trace
    qpp, <mark>90</mark>
transpose
    qpp, 91
tsallis
    qpp, 91
UNDEFINED_TYPE
     qpp::Exception, 108
UNKNOWN_EXCEPTION
    qpp::Exception, 107
ZERO_SIZE
    qpp::Exception, 107
```