qpp

0.1

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# Chapter 1

# Namespace Index

### 1.1 Namespace List

Here is a list of all namespaces with brief descriptions:

qpp	
qpp::ct	
qpp::internal	60
<pre>qpp::types</pre>	62

2 Namespace Index

## **Chapter 2**

## **Hierarchical Index**

### 2.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

qpp::DiscreteDistribution	63
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exception	
qpp::Exception	65
qpp::NormalDistribution	74
qpp::Qudit	75
qpp::Singleton< T >	78
qpp::Gates	68
qpp::RandomDevices	77
qpp::Singleton < const Gates >	78
qpp::Singleton < const RandomDevices >	78
qpp::Singleton < const States >	78
qpp::States	79
qpp::Timer	81
qpp::UniformIntDistribution	82
gpp::UniformRealDistribution	83

**Hierarchical Index** 

# **Chapter 3**

## **Class Index**

### 3.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

o::DiscreteDistribution	63
p::DiscreteDistributionAbsSquare	64
p::Exception	65
o::Gates	68
p::NormalDistribution	74
p::Qudit	75
p::RandomDevices	77
o::Singleton $<$ T $>$ $\dots$	78
o::States	79
o::Timer	81
p::UniformIntDistribution	82
p::UniformRealDistribution	83

6 Class Index

# Chapter 4

## File Index

### 4.1 File List

Here is a list of all files with brief descriptions:

include/channels.h
include/constants.h
include/entanglement.h
include/entropies.h
include/functions.h
include/internal.h
include/io.h
include/matlab.h
include/qpp.h
include/random.h
include/types.h
include/classes/exception.h
include/classes/gates.h
include/classes/qudit.h
include/classes/randevs.h
include/classes/singleton.h
include/classes/stat.h
include/classes/states.h
include/classes/timer.h

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### **Chapter 5**

## **Namespace Documentation**

#### 5.1 qpp Namespace Reference

#### **Namespaces**

- ct
- internal
- types

#### Classes

- · class Discrete Distribution
- · class DiscreteDistributionAbsSquare
- class Exception
- · class Gates
- · class NormalDistribution
- class Qudit
- class RandomDevices
- class Singleton
- · class States
- class Timer
- · class UniformIntDistribution
- · class UniformRealDistribution

#### **Functions**

- types::cmat super (const std::vector< types::cmat > &Ks)
- types::cmat choi (const std::vector< types::cmat > &Ks)
- std::vector< types::cmat > choi2kraus (const types::cmat &A)
- template<typename Derived >
   types::cmat channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< types::cmat > &Ks)
- template<typename Derived >
   types::cmat channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< types::cmat > &Ks,
   const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- constexpr std::complex< double > operator""\_i (unsigned long long int x)
- constexpr std::complex< double > operator""\_i (long double x)
- template<typename Derived >
   types::cmat schmidtcoeff (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)

Eigenvalues.

```
• template<typename Derived >
  types::cmat schmidtU (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &dims)
• template<typename Derived >
  types::cmat schmidtV (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)

    template<typename Derived >

  types::cmat schmidtprob (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)
• template<typename Derived >
  double entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)

    template<typename Derived >

  double gconcurrence (const Eigen::MatrixBase< Derived > &A)

    template<typename Derived >

  double shannon (const Eigen::MatrixBase< Derived > &A)

    template<typename Derived >

  double renyi (const double alpha, const Eigen::MatrixBase< Derived > &A)
• template<typename Derived >
  double renyi_inf (const Eigen::MatrixBase< Derived > &A)
• template<typename Derived >
  double tsallis (const double alpha, const Eigen::MatrixBase< Derived > &A)

    template<typename Derived >

  double gmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &subsys,
  const std::vector< std::size t > &dims)

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > transpose (const Eigen::MatrixBase < Derived > &A)
     Transpose.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > conjugate (const Eigen::MatrixBase < Derived > &A)
     Complex conjugate.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > adjoint (const Eigen::MatrixBase < Derived > &A)
     Adjoint.
template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > inverse (const Eigen::MatrixBase < Derived > &A)

    template<typename Derived >

  Derived::Scalar trace (const Eigen::MatrixBase< Derived > &A)

    template<typename Derived >

  Derived::Scalar det (const Eigen::MatrixBase < Derived > &A)
     Determinant

    template<typename Derived >

  Derived::Scalar logdet (const Eigen::MatrixBase< Derived > &A)
     Logarithm of the determinant.

    template<typename Derived >

  Derived::Scalar sum (const Eigen::MatrixBase< Derived > &A)
     Element-wise sum.

    template<typename Derived >

  double norm (const Eigen::MatrixBase< Derived > &A)
     Trace norm.

    template<typename Derived >

  types::cmat evals (const Eigen::MatrixBase< Derived > &A)
```

```
• template<typename Derived >
  types::cmat evects (const Eigen::MatrixBase< Derived > &A)
     Eigenvectors.

    template<typename Derived >

  types::dmat hevals (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvalues.

    template<typename Derived >

  types::cmat hevects (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvectors.

    template<typename Derived >

  types::cmat funm (const Eigen::MatrixBase< Derived > &A, types::cplx(*f)(const types::cplx &))
     Functional calculus f(A)

    template<typename Derived >

  types::cmat sqrtm (const Eigen::MatrixBase< Derived > &A)
     Matrix square root.

    template<typename Derived >

  types::cmat absm (const Eigen::MatrixBase< Derived > &A)
     Matrix absolut value.

    template<typename Derived >

  types::cmat expm (const Eigen::MatrixBase< Derived > &A)
     Matrix exponential.
template<typename Derived >
  types::cmat logm (const Eigen::MatrixBase< Derived > &A)
     Matrix logarithm.

    template<typename Derived >

  types::cmat sinm (const Eigen::MatrixBase< Derived > &A)
• template<typename Derived >
  types::cmat cosm (const Eigen::MatrixBase< Derived > &A)
     Matrix cos.

    template<typename Derived >

  types::cmat spectralpowm (const Eigen::MatrixBase< Derived > &A, const types::cplx z)
     Matrix power.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > powm (const Eigen::MatrixBase< Derived > &A, std::size_t n)
     Matrix power.
• template<typename OutputScalar , typename Derived >
  types::DynMat< OutputScalar > cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const
  typename Derived::Scalar &))
     Functor.
• template<typename T >
  types::DynMat< typename T::Scalar > kron (const T &head)
     Kronecker product (variadic overload)
• template<typename T , typename... Args>
  types::DynMat< typename T::Scalar > kron (const T &head, const Args &...tail)
     Kronecker product (variadic overload)
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > kron (const std::vector < Derived > &As)
     Kronecker product (std::vector overload)

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > kron (const std::initializer_list< Derived > &As)
```

```
Kronecker product (std::initializer_list overload)
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > kronpow (const Eigen::MatrixBase< Derived > &A, std::size_t n)
     Kronecker power.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > reshape (const Eigen::MatrixBase< Derived > &A, std::size t rows, std::size t cols)
     Reshape.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t >
  &perm, const std::vector< std::size t > &dims)
     System permutation.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &dims)
     Partial trace.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)
     Partial trace.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t > &sub-
  sys, const std::vector< std::size_t > &dims)
     Partial trace.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t >
  &subsys, const std::vector< std::size_t > &dims)
     Partial transpose.

    template<typename Derived1 , typename Derived2 >

  types::DynMat< typename
  Derived1::Scalar > comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2
  > &B)
     Commutator.

    template<typename Derived1 , typename Derived2 >

  types::DynMat< typename
  Derived1::Scalar > anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< De-
  rived2 > &B)
     Anti-commutator.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > prj (const Eigen::MatrixBase < Derived > &V)
     Projector.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, std::size_t pos, const std::vector<
  std::size_t > &dims)
     Expand out.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > grams (const std::vector < Derived > &Vs)
```

Gram-Schmidt orthogonalization (std::vector overload)

```
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > grams (const std::initializer_list< Derived > &Vs)
     Gram-Schmidt orthogonalization (std::initializer_list overload)

    template<typename Derived >

  types::DynMat< typename
  {\tt Derived::Scalar} > {\tt grams} \; ({\tt const} \; {\tt Eigen::MatrixBase} < {\tt Derived} > \& {\tt A})
      Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)

    std::vector< std::size t > n2multiidx (std::size t n, const std::vector< std::size t > &dims)

     Non-negative integer index to multi-index.

    std::size_t multiidx2n (const std::vector< std::size_t > &midx, const std::vector< std::size_t > &dims)

     Multi-index to non-negative integer index.

    types::ket mket (const std::vector< std::size t > &mask)

     Multi-partite qubit ket.

    types::ket mket (const std::vector< std::size_t > &mask, const std::vector< std::size_t > &dims)

     Multi-partite qudit ket (different dimensions overload)

    types::ket mket (const std::vector< std::size t > &mask, std::size t d)

     Multi-partite qudit ket (same dimensions overload)

    std::vector< std::size_t > invperm (const std::vector< std::size_t > &perm)

     Inverse permutation.
• std::vector< std::size t > compperm (const std::vector< std::size t > &perm, const std::vector< std::size t
  > &sigma)
     Compose permutations.
• template<typename T >
  void disp (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]",
  std::ostream &os=std::cout)
template<typename T >
  void displn (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]",
  std::ostream &os=std::cout)

    template<typename T >

  void disp (const T *x, const std::size t n, const std::string &separator, const std::string &start="[", const std
  ::string &end="]", std::ostream &os=std::cout)
• template<typename T >
  void displn (const T *x, const std::size_t n, const std::string &separator, const std::string &start="[", const
  std::string &end="]", std::ostream &os=std::cout)

    template<typename Derived >

  void disp (const Eigen::MatrixBase < Derived > &A, double chop=ct::chop, std::ostream &os=std::cout)

    template<typename Derived >

  void displn (const Eigen::MatrixBase < Derived > &A, double chop=ct::chop, std::ostream &os=std::cout)

    void disp (const types::cplx c, double chop=ct::chop, std::ostream &os=std::cout)

• void displn (const types::cplx c, double chop=ct::chop, std::ostream &os=std::cout)

    template<typename Derived >

  void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > load (const std::string &fname)

    template<typename Derived >

  Derived loadMATLABmatrix (const std::string &mat file, const std::string &var name)
template<>
  types::dmat loadMATLABmatrix (const std::string &mat file, const std::string &var name)
• template<>
  types::cmat loadMATLABmatrix (const std::string &mat file, const std::string &var name)

    template<typename Derived >

  void saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std↔
```

::string &var\_name, const std::string &mode)

- template<>
   void saveMATLABmatrix (const Eigen::MatrixBase< types::dmat > &A, const std::string &mat\_file, const std::string &var name, const std::string &mode)
- template<>
   void saveMATLABmatrix (const Eigen::MatrixBase< typename types::cmat > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)
- template<typename Derived >
   Derived rand (std::size\_t rows, std::size\_t cols, double a=0, double b=1)
- template<>
   types::dmat rand (std::size t rows, std::size t cols, double a, double b)
- template<>
   types::cmat rand (std::size\_t rows, std::size\_t cols, double a, double b)
- double rand (double a=0, double b=1)
- long long randint (long long a, long long b)
- template<typename Derived >
   Derived randn (std::size\_t rows, std::size\_t cols, double mean=0, double sigma=1)
- template<>
   types::dmat randn (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- template<>
   types::cmat randn (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- double randn (double mean=0, double sigma=1)
- types::cmat randU (std::size\_t D)
- types::cmat randV (std::size\_t Din, std::size\_t Dout)
- std::vector< types::cmat > randkraus (std::size\_t n, std::size\_t D)
- types::cmat randH (std::size t D)
- types::ket randket (std::size\_t D)
- types::cmat randrho (std::size\_t D)
- std::vector< std::size\_t > randperm (std::size\_t n)

#### **Variables**

- const RandomDevices & rdevs = RandomDevices::get\_instance()
- const Gates & gt = Gates::get\_instance()
- const States & st = States::get\_instance()

#### 5.1.1 Function Documentation

5.1.1.1 template<typename Derived > types::cmat qpp::absm ( const Eigen::MatrixBase< Derived > & A )

Matrix absolut value.

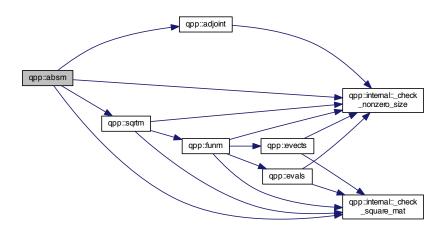
Parameters

A Eigen expression

Returns

Matrix absolut value of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.2 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::adjoint ( const Eigen::MatrixBase< Derived > & A )

Adjoint.

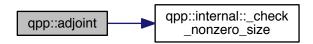
**Parameters** 

A E	Eigen expression

Returns

Adjoint (Hermitian conjugate) of A, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.3 template<typename Derived1 , typename Derived2 > types::DynMat<typename Derived1::Scalar> qpp::anticomm ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )

Anti-commutator.

Anti-commutator  $\{A, B\} = AB + BA$ 

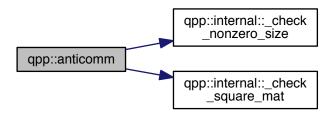
Both A and B must be Eigen expressions over the same scalar field

Α	Eigen expression
В	Eigen expression

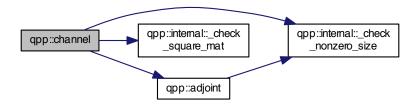
#### Returns

Anti-commutator AB + BA, as a dynamic matrix over the same scalar field

Here is the call graph for this function:

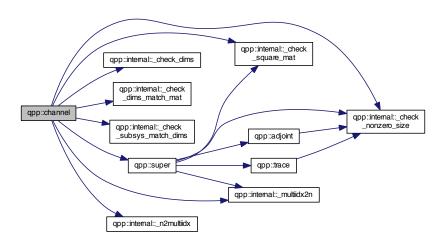


5.1.1.4 template<typename Derived > types::cmat qpp::channel ( const Eigen::MatrixBase< Derived > & rho, const std::vector< types::cmat > & Ks )

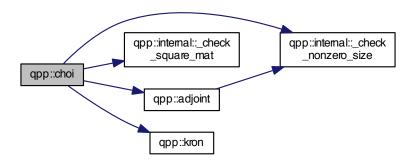


5.1.1.5 template < typename Derived > types::cmat qpp::channel ( const Eigen::MatrixBase < Derived > & rho, const std::vector < types::cmat > & Ks, const std::vector < std::size\_t > & subsys, const std::vector < std::size\_t > & dims 
)

Here is the call graph for this function:

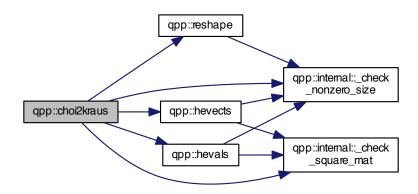


5.1.1.6 types::cmat qpp::choi ( const std::vector< types::cmat > &  $\mathit{Ks}$  )



5.1.1.7 std::vector<types::cmat> qpp::choi2kraus ( const types::cmat & A )

Here is the call graph for this function:



5.1.1.8 template<typename Derived1 , typename Derived2 > types::DynMat<typename Derived1::Scalar> qpp::comm ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )

#### Commutator.

Commutator [A,B] = AB - BA

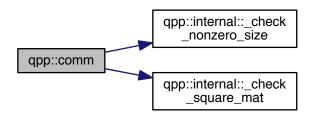
Both A and B must be Eigen expressions over the same scalar field

#### **Parameters**

A	Eigen expression
В	Eigen expression

#### Returns

Commutator AB - BA, as a dynamic matrix over the same scalar field



5.1.1.9 std::vector < std::size\_t > & perm, const std::vector < std::size\_t > & perm, const std::vector < std::size\_t > & sigma )

Compose permutations.

perm	Permutation
sigma	Permutation

#### Returns

Composition of the permutations *perm* o *sigma* = perm(sigma)

Here is the call graph for this function:



5.1.1.10 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::conjugate ( const Eigen::MatrixBase< Derived > & A )

Complex conjugate.

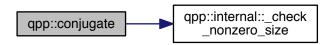
#### **Parameters**

	Α	Eigen expression
--	---	------------------

#### Returns

Complex conjugate of A, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.11 template<typename Derived > types::cmat qpp::cosm ( const Eigen::MatrixBase< Derived > & A )

Matrix cos.

Α	Eigen expression
---	------------------

#### Returns

Matrix cosine of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.12 template < typename OutputScalar , typename Derived > types::DynMat < OutputScalar > qpp::cwise ( const Eigen::MatrixBase < Derived > & A, OutputScalar(\*)(const typename Derived::Scalar &) f )

#### Functor.

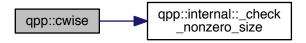
#### **Parameters**

Α	Eigen expression
f	Pointer-to-function from scalars of A to OutputScalar

#### Returns

Component-wise f(A), as a dynamic matrix over the *OutputScalar* scalar field

Here is the call graph for this function:



5.1.1.13 template<typename Derived > Derived::Scalar qpp::det ( const Eigen::MatrixBase< Derived > & A )

Determinant.

Α	Eigen expression

#### Returns

Determinant of A, as a dynamic matrix over the same scalar field Returns  $\pm\infty$  when the determinant overflows/underflows

Here is the call graph for this function:



- 5.1.1.14 template<typename T > void qpp::disp ( const T & x, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )
- 5.1.1.15 template < typename T > void qpp::disp ( const T \* x, const std::size\_t n, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )
- 5.1.1.16 template < typename Derived > void qpp::disp ( const Eigen::MatrixBase < Derived > & A, double chop = ct::chop, std::ostream & os = std::cout )
- 5.1.1.17 void qpp::disp ( const types::cplx c, double chop = ct : :chop, std::ostream & os = std::cout )



5.1.1.18 template<typename T > void qpp::displn ( const T & x, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] ", std::ostream & os = std::cout )

Here is the call graph for this function:



5.1.1.19 template<typename T > void qpp::displn ( const T \* x, const std::size\_t n, const std::string & separator, const std::string & std::string & end = "]", std::ostream & os = std::cout)

Here is the call graph for this function:



5.1.1.20 template < typename Derived > void qpp::displn ( const Eigen::MatrixBase < Derived > & A, double chop = ct::chop, std::ostream & os = std::cout )



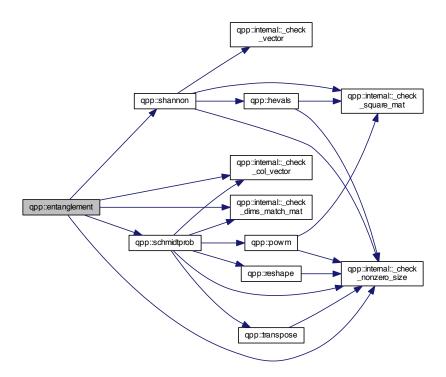
5.1.1.21 void qpp::displn ( const types::cplx c, double chop = ct : :chop, std::ostream & os = std::cout )

Here is the call graph for this function:



5.1.1.22 template < typename Derived > double qpp::entanglement ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

Here is the call graph for this function:



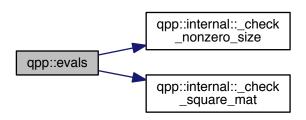
5.1.1.23 template<typename Derived > types::cmat qpp::evals ( const Eigen::MatrixBase< Derived > & A )

Eigenvalues.

Α	Eigen expression
---	------------------

## Returns

Eigenvalues of *A*, as a diagonal dynamic matrix over the complex field, with eigenvalues on the diagonal Here is the call graph for this function:



5.1.1.24 template < typename Derived > types::cmat qpp::evects ( const Eigen::MatrixBase < Derived > & A )

## Eigenvectors.

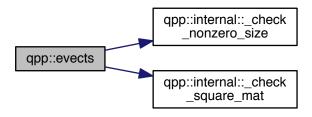
#### **Parameters**

```
A Eigen expression
```

## Returns

Eigenvectors of A, as columns of a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.25 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::expandout ( const Eigen::MatrixBase< Derived > & A, std::size\_t pos, const std::vector< std::size\_t > & dims )

# Expand out.

Expand out A as a matrix in a multi-partite system Faster than using *qpp::kron*(I, I, ..., I, A, I, ..., I)

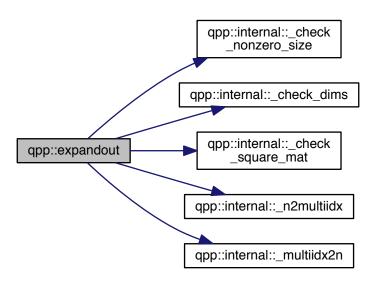
## **Parameters**

Α	Eigen expression
pos	Position
dims	Dimensions of the multi-partite system

## Returns

Tensor product  $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$ , with A on position pos, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



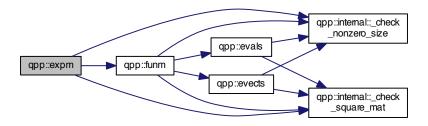
5.1.1.26 template<typename Derived > types::cmat qpp::expm ( const Eigen::MatrixBase< Derived > & A )

Matrix exponential.

A Eigen expression
--------------------

Matrix exponential of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.27 template < typename Derived > types::cmat qpp::funm ( const Eigen::MatrixBase < Derived > & A, types::cplx(\*)(const types::cplx &) f )

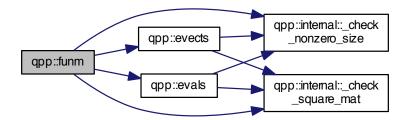
# Functional calculus f(A)

## **Parameters**

Α	Eigen expression
f	Pointer-to-function from complex to complex

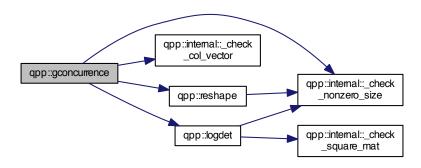
# Returns

f(A), as a dynamic matrix over the complex field



5.1.1.28 template < typename Derived > double qpp::gconcurrence ( const Eigen::MatrixBase < Derived > & A )

Here is the call graph for this function:



5.1.1.29 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::grams ( const std::vector< Derived > & Vs )

Gram-Schmidt orthogonalization (std::vector overload)

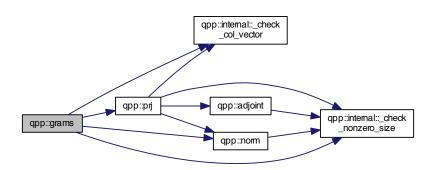
**Parameters** 

Vs	std::vector of Eigen expressions as column vectors
----	--

## Returns

Gram-Schmidt vectors of Vs as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.30 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::grams ( const std::initializer\_list < Derived > & Vs )

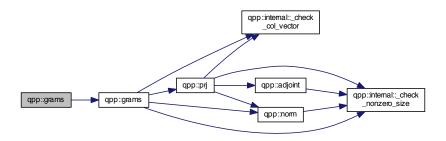
Gram-Schmidt orthogonalization (std::initializer list overload)

Vs std::initializer_list of Eigen expressions as column vectors	3
---	---

## Returns

Gram-Schmidt vectors of Vs as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.31 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::grams ( const Eigen::MatrixBase< Derived > & A )

Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)

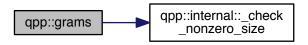
## **Parameters**

Α	Eigen expression, the input vectors are the columns of A

## Returns

Gram-Schmidt vectors of the columns of A, as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



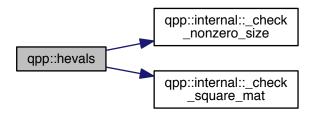
5.1.1.32 template < typename Derived > types::dmat qpp::hevals ( const Eigen::MatrixBase < Derived > & A )

Hermitian eigenvalues.

Α	Eigen expression
---	------------------

## Returns

Eigenvalues of Hermitian *A*, as a diagonal dynamic matrix over the real field, with eigenvalues on the diagonal Here is the call graph for this function:



5.1.1.33 template < typename Derived > types::cmat qpp::hevects ( const Eigen::MatrixBase < Derived > & A )

Hermitian eigenvectors.

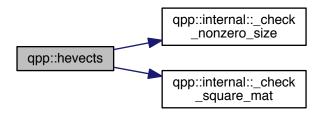
## **Parameters**

Α	Eigen expression

#### Returns

Eigenvectors of Hermitian A, as columns of a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.34 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::inverse ( const Eigen::MatrixBase < Derived > & A )

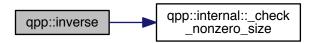
Inverse.

Α	Eigen expression

## Returns

Inverse of A, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.35 std::vector<std::size\_t> qpp::invperm ( const std::vector< std::size\_t> & perm )

Inverse permutation.

#### **Parameters**

ſ	perm	Permutation
	,	

## Returns

Inverse of the permutation perm

Here is the call graph for this function:



5.1.1.36 template < typename T > types::DynMat< typename T::Scalar> qpp::kron ( const T & head )

Kronecker product (variadic overload)

Used to stop the recursion for the variadic template version of *qpp::kron*(...)

head	Eigen expression

Its argument head

5.1.1.37 template < typename T , typename... Args > types::DynMat < typename T::Scalar > qpp::kron ( const T & head, const Args &... tail )

Kronecker product (variadic overload)

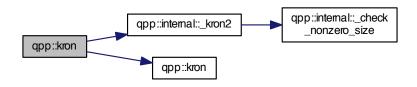
## **Parameters**

head	Eigen expression
tail	Variadic Eigen expression (zero or more parameters)

#### Returns

Kronecker product of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.38 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::kron ( const std::vector< Derived > & As )

Kronecker product (std::vector overload)

	As	std::vector of Eigen expressions
--	----	----------------------------------

Kronecker product of all elements in As, evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.39 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::kron ( const std::initializer\_list < Derived > & As)

Kronecker product (std::initializer\_list overload)

#### **Parameters**

As	std::initializer list of Eigen expressions, such as {A1, A2,, Ak}
AS	stdinitializer_list of Ligeri expressions, such as {A1, A2, ,Ak}

## Returns

Kronecker product of all elements in As, evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



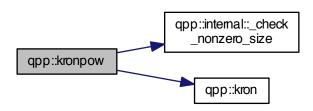
5.1.1.40 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::kronpow ( const Eigen::MatrixBase< Derived > &  $A_r$ , std::size\_t n)

## Kronecker power.

Α	Eigen expression
n	Non-negative integer

Kronecker product of A with itself n times  $A^{\otimes n}$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



- $5.1.1.41 \quad template < typename \ Derived > types:: DynMat < typename \ Derived:: Scalar > qpp:: load ( \ const \ std:: string \ \& \ \textit{fname}$  )
- 5.1.1.42 template < typename Derived > Derived qpp::loadMATLABmatrix ( const std::string &  $mat\_file$ , const std::string &  $var\_name$  )
- 5.1.1.43 template <> types::dmat qpp::loadMATLABmatrix ( const std::string & mat\_file, const std::string & var\_name )
- 5.1.1.44 template<> types::cmat qpp::loadMATLABmatrix ( const std::string & mat\_file, const std::string & var\_name )
- 5.1.1.45 template<typename Derived > Derived::Scalar qpp::logdet ( const Eigen::MatrixBase< Derived > & A )

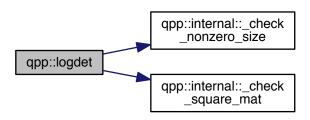
Logarithm of the determinant.

Especially useful when the determinant overflows/underflows

Α	Eigen expression
---	------------------

Logarithm of the determinant of A, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.46 template < typename Derived > types::cmat qpp::logm ( const Eigen::MatrixBase < Derived > & A )

Matrix logarithm.

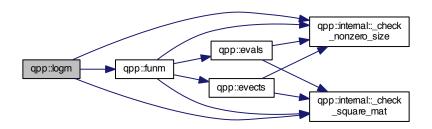
#### **Parameters**

Α	Eigen expression

## Returns

Matrix logarithm of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



# 5.1.1.47 types::ket qpp::mket ( const std::vector< std::size\_t > & mask )

Multi-partite qubit ket.

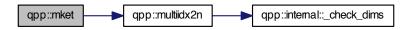
Constructs the multi-partite qubit ket  $|mask\rangle$ , where mask is a std::vector of 0's and 1's

mask	std::vector of 0's and 1's

## Returns

Multi-partite qubit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



5.1.1.48 types::ket qpp::mket ( const std::vector < std::size\_t > & mask, const std::vector < std::size\_t > & dims )

Multi-partite qudit ket (different dimensions overload)

Constructs the multi-partite qudit ket  $|mask\rangle$ , where mask is a std::vector of non-negative integers Each element in mask has to be smaller than the corresponding element in dims

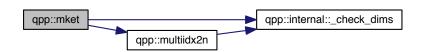
#### **Parameters**

mask	std::vector of non-negative integers

## Returns

Multi-partite qudit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



5.1.1.49 types::ket qpp::mket ( const std::vector < std::size\_t > & mask, std::size\_t d )

Multi-partite qudit ket (same dimensions overload)

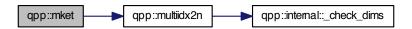
Constructs the multi-partite qudit ket  $|mask\rangle$  in a multi-partite system, all subsystem having equal dimension d mask is a std::vector of non-negative integers, and each element in mask has to be strictly smaller than d

mask	std::vector of non-negative integers
d	Subsystems' dimension

## Returns

Multi-partite qudit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



5.1.1.50 std::size\_t qpp::multiidx2n ( const std::vector < std::size\_t > & midx, const std::vector < std::size\_t > & dims )

Multi-index to non-negative integer index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

#### **Parameters**

midx	Multi-index
dims	Dimensions of the multi-partite system

## Returns

Non-negative integer index

Here is the call graph for this function:



5.1.1.51 std::vector<std::size\_t> qpp::n2multiidx ( std::size\_t n, const std::vector< std::size\_t> & dims )

Non-negative integer index to multi-index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

n	Non-negative integer index
dims	Dimensions of the multi-partite system

## Returns

Multi-index of the same size as dims

Here is the call graph for this function:



5.1.1.52 template<typename Derived > double qpp::norm ( const Eigen::MatrixBase< Derived > & A )

Trace norm.

**Parameters** 

Α	Eigen expression

## Returns

Trace norm (Frobenius norm) of A, as a real number

Here is the call graph for this function:



- 5.1.1.53 constexpr std::complex<double> qpp::operator""\_i ( unsigned long long int x )
- 5.1.1.54 constexpr std::complex < double > qpp::operator""\_i ( long double x )
- 5.1.1.55 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::powm ( const Eigen::MatrixBase < Derived > & A, std::size\_t n)

Matrix power.

By convention  $A^0 = I$ 

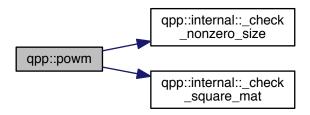
Explicitly multiplies the matrix A with itself n times

Α	Eigen expression
n	Non-negative integer

## Returns

Matrix power  $A^n$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.56 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::prj ( const Eigen::MatrixBase< Derived > & V )

# Projector.

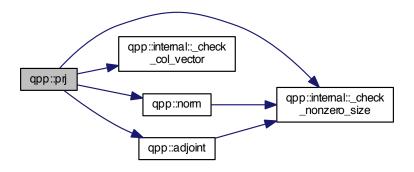
Normalized projector onto state vector

## Parameters

V Eigen expression
--------------------

## Returns

Projector onto the state vector V, or the matrix Zero if V has norm zero (i.e. smaller than qpp::ct::eps), as a dynamic matrix over the same scalar field



5.1.1.57 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::ptrace ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & subsys, const std::vector < std::size\_t > & dims )

Partial trace.

Partial trace of the multi-partite density matrix over a list of subsystems

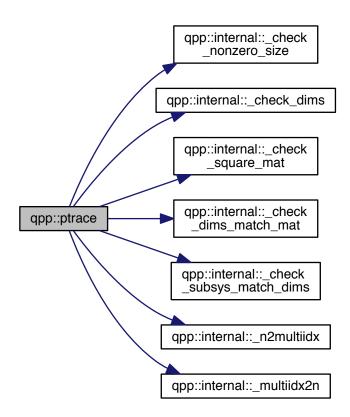
#### **Parameters**

Α	Eigen expression
subsys	Subsystems' indexes
dims	Dimensions of the multi-partite system

#### Returns

Partial trace  $Tr_{subsys}(\cdot)$  over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.58 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::ptrace1 ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & dims )

Partial trace.

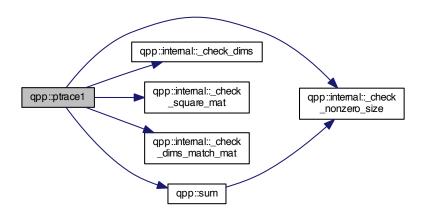
Partial trace of density matrix over the first subsystem in a bi-partite system

Α	Eigen expression
dims	Dimensions of bi-partite system (must be a std::vector with 2 elements)

# Returns

Partial trace  $Tr_A(\cdot)$  over the first subsytem A in a bi-partite system  $A\otimes B$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.59 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::ptrace2 ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & dims )

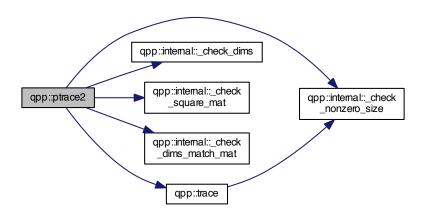
# Partial trace.

Partial trace of density matrix over the second subsystem in a bi-partite system

Α	Eigen expression
dims	Dimensions of bi-partite system (must be a std::vector with 2 elements)

Partial trace  $Tr_B(\cdot)$  over the second subsystem B in a bi-partite system  $A \otimes B$ , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



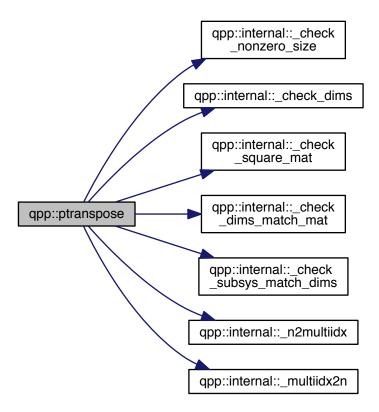
5.1.1.60 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::ptranspose ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & subsys, const std::vector< std::size\_t > & dims )

# Partial transpose.

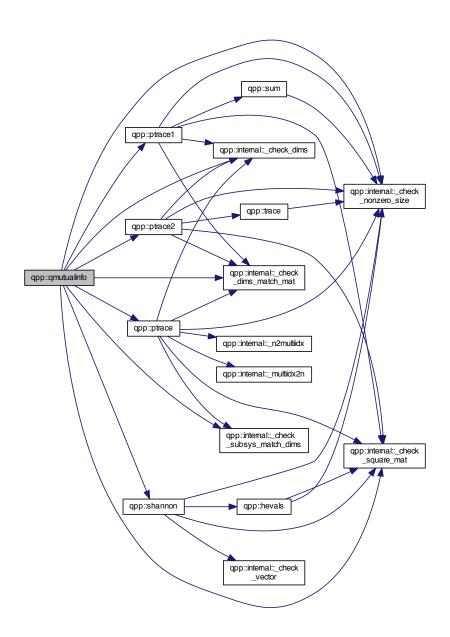
Partial transpose of the multi-partite density matrix over a list of subsystems

Α	Eigen expression
subsys	Subsystems' indexes
dims	Dimensions of the multi-partite system

Partial transpose  $(\cdot)^{T_{subsys}}$  over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field



5.1.1.61 template<typename Derived > double qpp::qmutualinfo ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & subsys, const std::vector< std::size\_t > & dims )



- 5.1.1.62 template < typename Derived > Derived qpp::rand ( std::size\_t rows, std::size\_t cols, double a = 0, double b = 1 )
- 5.1.1.63 template <> types::dmat qpp::rand ( std::size\_t rows, std::size\_t cols, double a, double b )

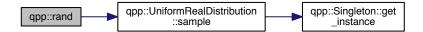
5.1.1.64 template<> types::cmat qpp::rand ( std::size\_t rows, std::size\_t cols, double a, double b )

Here is the call graph for this function:



5.1.1.65 double qpp::rand ( double a = 0, double b = 1 )

Here is the call graph for this function:



5.1.1.66 types::cmat qpp::randH ( std::size\_t D )

Here is the call graph for this function:

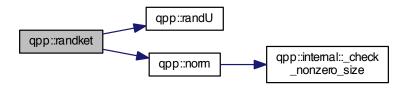


5.1.1.67 long long qpp::randint ( long long a, long long b )



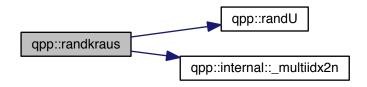
## 5.1.1.68 types::ket qpp::randket ( std::size\_t D )

Here is the call graph for this function:



## 5.1.1.69 std::vector<types::cmat> qpp::randkraus ( std::size\_t n, std::size\_t D )

Here is the call graph for this function:



- 5.1.1.70 template<typename Derived > Derived qpp::randn ( std::size\_t rows, std::size\_t cols, double mean = 0, double sigma = 1)
- 5.1.1.71 template<> types::dmat qpp::randn ( std::size\_t rows, std::size\_t cols, double mean, double sigma )



5.1.1.72 template<> types::cmat qpp::randn ( std::size\_t rows, std::size\_t cols, double mean, double sigma )

Here is the call graph for this function:



5.1.1.73 double qpp::randn ( double mean = 0, double sigma = 1 )

Here is the call graph for this function:

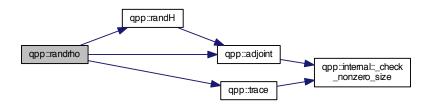


5.1.1.74 std::vector<std::size\_t> qpp::randperm ( std::size\_t n )



## 5.1.1.75 types::cmat qpp::randrho ( std::size\_t D )

Here is the call graph for this function:



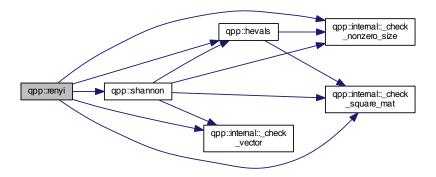
## 5.1.1.76 types::cmat qpp::randU ( std::size\_t D )

# 5.1.1.77 types::cmat qpp::randV ( std::size\_t Din, std::size\_t Dout )

Here is the call graph for this function:

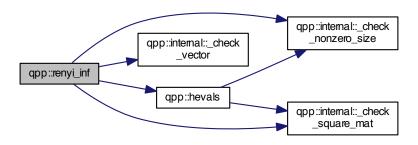


# 5.1.1.78 template < typename Derived > double qpp::renyi ( const double alpha, const Eigen::MatrixBase < Derived > & A )



5.1.1.79 template<typename Derived > double qpp::renyi\_inf ( const Eigen::MatrixBase< Derived > & A )

Here is the call graph for this function:



5.1.1.80 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::reshape ( const Eigen::MatrixBase< Derived > & A, std::size t rows, std::size t cols )

## Reshape.

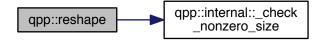
Uses column-major order when reshaping (same as MATLAB)

#### **Parameters**

Α	Eigen expression
rows	Number of rows of the reshaped matrix
cols	Number of columns of the reshaped matrix

## Returns

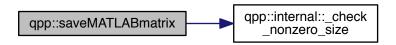
Reshaped matrix with rows rows and cols columns, as a dynamic matrix over the same scalar field



- 5.1.1.81 template < typename Derived > void qpp::save ( const Eigen::MatrixBase < Derived > & A, const std::string & fname )
- 5.1.1.82 template < typename Derived > void qpp::saveMATLABmatrix ( const Eigen::MatrixBase < Derived > & A, const std::string & mat\_file, const std::string & mode )

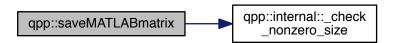
5.1.1.83 template<> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< types::dmat > & A, const std::string & mat\_file, const std::string & var\_name, const std::string & mode )

Here is the call graph for this function:

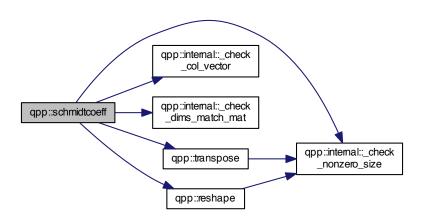


5.1.1.84 template<> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< typename types::cmat > & A, const std::string & mat\_file, const std::string & var\_name, const std::string & mode )

Here is the call graph for this function:

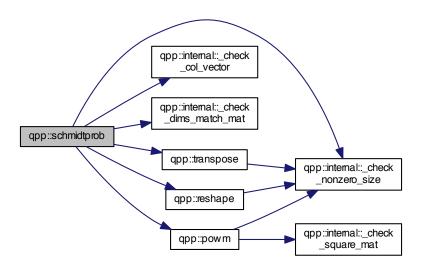


5.1.1.85 template < typename Derived > types::cmat qpp::schmidtcoeff ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

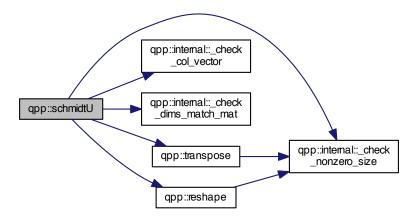


5.1.1.86 template < typename Derived > types::cmat qpp::schmidtprob ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

Here is the call graph for this function:

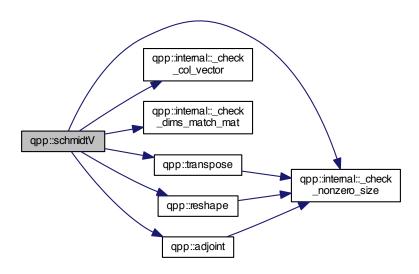


5.1.1.87 template < typename Derived > types::cmat qpp::schmidtU ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )



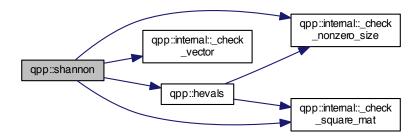
5.1.1.88 template < typename Derived > types::cmat qpp::schmidtV ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & dims )

Here is the call graph for this function:



5.1.1.89 template<typename Derived > double qpp::shannon ( const Eigen::MatrixBase< Derived > & A )

Here is the call graph for this function:



5.1.1.90 template < typename Derived > types::cmat qpp::sinm ( const Eigen::MatrixBase < Derived > & A )

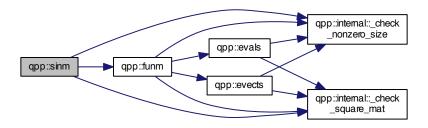
Matrix sin.

Α	Eigen expression
---	------------------

## Returns

Matrix sine of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



5.1.1.91 template<typename Derived > types::cmat qpp::spectralpowm ( const Eigen::MatrixBase< Derived > & A, const types::cplx z )

Matrix power.

By convention  $A^0 = I$ 

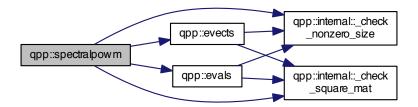
Uses the spectral decomposition of A to compute the matrix power

## **Parameters**

Α	Eigen expression
Z	Complex number

# Returns

Matrix power  $A^z$ , as a dynamic matrix over the complex field



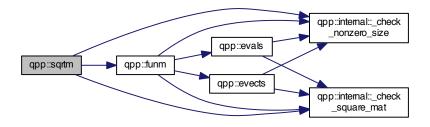
 $\label{topological constraints} \textbf{5.1.1.92} \quad \textbf{template} < \textbf{typename Derived} > \textbf{types::cmat qpp::sqrtm ( const Eigen::MatrixBase} < \textbf{Derived} > \textbf{\& A ) }$  Matrix square root.

Α	Eigen expression

## Returns

Matrix square root of A, as a dynamic matrix over the complex field

Here is the call graph for this function:



 $5.1.1.93 \quad template < typename \ Derived > Derived :: Scalar \ qpp::sum \ ( \ const \ Eigen:: Matrix Base < Derived > \& \ A \ )$ 

Element-wise sum.

**Parameters** 

A Eigen expre	ssion
---------------	-------

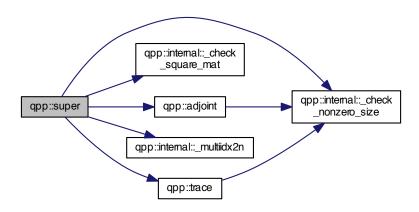
# Returns

Element-wise sum of A, as a dynamic matrix over the same scalar field



5.1.1.94 types::cmat qpp::super ( const std::vector< types::cmat > & Ks )

Here is the call graph for this function:



5.1.1.95 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::syspermute ( const Eigen::MatrixBase < Derived > & A, const std::vector < std::size\_t > & perm, const std::vector < std::size\_t > & dims )

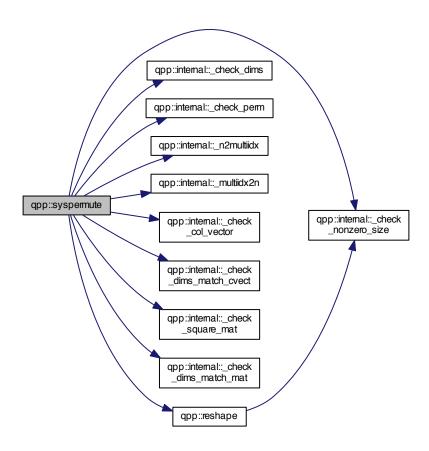
System permutation.

Permutes the subsystems in a state vector or density matrix The qubit perm[i] is permuted to the location i

Α	Eigen expression
perm	Permutation
dims	Subsystems' dimensions

Permuted system, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



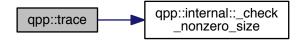
5.1.1.96 template<typename Derived > Derived::Scalar qpp::trace ( const Eigen::MatrixBase< Derived > & A )

Trace.

Α	Eigen expression

Trace of A, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



5.1.1.97 template < typename Derived > types::DynMat < typename Derived::Scalar > qpp::transpose ( const Eigen::MatrixBase < Derived > & A )

# Transpose.

## **Parameters**

```
A | Eigen expression
```

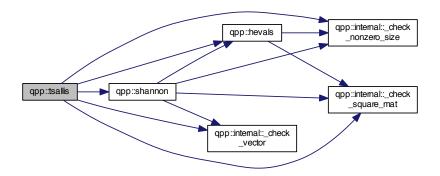
## Returns

Transpose of A, as a dynamic matrix over the same scalar field



5.1.1.98 template < typename Derived > double qpp::tsallis ( const double alpha, const Eigen::MatrixBase < Derived > & A )

Here is the call graph for this function:



#### 5.1.2 Variable Documentation

- 5.1.2.1 const Gates& gpp::gt = Gates::get instance()
- 5.1.2.2 const RandomDevices& gpp::rdevs = RandomDevices::get\_instance()
- 5.1.2.3 const States& qpp::st = States::get\_instance()

# 5.2 qpp::ct Namespace Reference

## **Functions**

std::complex< double > omega (std::size\_t D)

## Variables

- constexpr double chop = 1e-10
- constexpr double eps = 1e-12
- constexpr std::size\_t maxn = 64
- constexpr double pi = 3.141592653589793238462643383279502884
- constexpr double ee = 2.718281828459045235360287471352662497

## 5.2.1 Function Documentation

- 5.2.1.1 std::complex < double > qpp::ct::omega ( std::size\_t D )
- 5.2.2 Variable Documentation
- 5.2.2.1 constexpr double qpp::ct::chop = 1e-10
- 5.2.2.2 constexpr double qpp::ct::ee = 2.718281828459045235360287471352662497
- 5.2.2.3 constexpr double qpp::ct::eps = 1e-12

- 5.2.2.4 constexpr std::size\_t qpp::ct::maxn = 64
- 5.2.2.5 constexpr double qpp::ct::pi = 3.141592653589793238462643383279502884

# 5.3 qpp::internal Namespace Reference

### **Functions**

- void n2multiidx (std::size t n, std::size t numdims, const std::size t \*dims, std::size t \*result)
- std::size\_t \_multiidx2n (const std::size\_t \*midx, std::size\_t numdims, const std::size\_t \*dims)
- template<typename Derived >

```
bool\_check\_square\_mat~(const~Eigen::MatrixBase < Derived > \&A)
```

• template<typename Derived >

bool <u>\_check\_vector</u> (const Eigen::MatrixBase< Derived > &A)

template<typename Derived >

```
bool <u>_check_row_vector</u> (const Eigen::MatrixBase< Derived > &A)
```

template<typename Derived >

```
bool <u>_check_col_vector</u> (const Eigen::MatrixBase< Derived > &A)
```

• template<typename T >

bool check nonzero size (const T &x)

- bool <u>\_check\_dims</u> (const std::vector < std::size\_t > &dims)
- template<typename Derived >

```
bool _check_dims_match_mat (const std::vector< std::size_t > &dims, const Eigen::MatrixBase< Derived > &A)
```

template<typename Derived >

```
bool <u>_check_dims_match_cvect</u> (const std::vector< std::size_t > &dims, const Eigen::MatrixBase< Derived > &V)
```

template<typename Derived >

 $\label{local_bool_check_dims_match_rvect} \mbox{ (const std::vector} < \mbox{ std::size\_t} > \& \mbox{dims, const Eigen::MatrixBase} < \mbox{ Derived} > \& \mbox{V})$ 

- bool <u>\_check\_eq\_dims</u> (const std::vector< std::size\_t > &dims, std::size\_t dim)
- bool \_check\_subsys\_match\_dims (const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)
- bool \_check\_perm (const std::vector< std::size\_t > &perm)
- template<typename Derived1 , typename Derived2 >

```
types::DynMat< typename
```

 $\label{lem:base} Derived1::Scalar > \_kron2 \ (const \ Eigen::MatrixBase < Derived1 > \&A, \ const \ Eigen::MatrixBase < Derived2 > \&B)$ 

template<typename T >

```
void variadic vector emplace (std::vector< T > &)
```

template<typename T, typename First, typename... Args>
 void variadic\_vector\_emplace (std::vector< T > &v, First &&first, Args &&...args)

## 5.3.1 Function Documentation

- 5.3.1.1 template < typename Derived > bool qpp::internal::\_check\_col\_vector ( const Eigen::MatrixBase < Derived > & A )
- 5.3.1.2 bool qpp::internal::\_check\_dims ( const std::vector< std::size\_t > & dims )
- 5.3.1.3 template<typename Derived > bool qpp::internal::\_check\_dims\_match\_cvect ( const std::vector< std::size\_t > & dims, const Eigen::MatrixBase< Derived > & V)
- 5.3.1.4 template<typename Derived > bool qpp::internal::\_check\_dims\_match\_mat ( const std::vector< std::size\_t > & dims, const Eigen::MatrixBase< Derived > & A )

- 5.3.1.5 template<typename Derived > bool qpp::internal::\_check\_dims\_match\_rvect ( const std::vector< std::size\_t > & dims, const Eigen::MatrixBase< Derived > & V )
- 5.3.1.6 bool qpp::internal::\_check\_eq\_dims ( const std::vector < std::size\_t > & dims, std::size\_t dim )
- 5.3.1.7 template < typename T > bool qpp::internal::\_check\_nonzero\_size ( const T & x )
- 5.3.1.8 bool qpp::internal::\_check\_perm ( const std::vector< std::size\_t > & perm )
- 5.3.1.9 template < typename Derived > bool qpp::internal::\_check\_row\_vector ( const Eigen::MatrixBase < Derived > & A )
- 5.3.1.10 template < typename Derived > bool qpp::internal::\_check\_square\_mat ( const Eigen::MatrixBase < Derived > & A )
- 5.3.1.11 bool qpp::internal::\_check\_subsys\_match\_dims ( const std::vector< std::size\_t > & subsys, const std::vector< std::size\_t > & dims )
- 5.3.1.12 template < typename Derived > bool qpp::internal::\_check\_vector ( const Eigen::MatrixBase < Derived > & A )
- 5.3.1.13 template<typename Derived1 , typename Derived2 > types::DynMat<typename Derived1::Scalar> qpp::internal::\_kron2 ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )

Here is the call graph for this function:



- 5.3.1.14 std::size\_t qpp::internal::\_multiidx2n ( const std::size\_t \* midx, std::size\_t numdims, const std::size\_t \* dims )
- 5.3.1.15 void qpp::internal::\_n2multiidx ( std::size\_t n, std::size\_t numdims, const std::size\_t \* dims, std::size\_t \* result )
- 5.3.1.16 template < typename T > void qpp::internal::variadic\_vector\_emplace ( std::vector < T > & )
- 5.3.1.17 template < typename T , typename First , typename... Args > void qpp::internal::variadic\_vector\_emplace ( std::vector < T > & v, First && first, Args &&... args )

Here is the call graph for this function:



# 5.4 qpp::types Namespace Reference

# **Typedefs**

```
using cplx = std::complex< double >
using cmat = Eigen::MatrixXcd
using dmat = Eigen::MatrixXd
using ket = Eigen::Matrix< cplx, Eigen::Dynamic, 1 >
using bra = Eigen::Matrix< cplx, 1, Eigen::Dynamic >
template<typename Scalar >
using DynMat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >
```

# 5.4.1 Typedef Documentation

```
5.4.1.1 using qpp::types::bra = typedef Eigen::Matrix<cplx, 1, Eigen::Dynamic>
```

- 5.4.1.2 using qpp::types::cmat = typedef Eigen::MatrixXcd
- 5.4.1.3 using qpp::types::cplx = typedef std::complex < double >
- 5.4.1.4 using qpp::types::dmat = typedef Eigen::MatrixXd
- 5.4.1.5 template<typename Scalar > using qpp::types::DynMat = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>
- 5.4.1.6 using qpp::types::ket = typedef Eigen::Matrix<cplx, Eigen::Dynamic, 1>

# **Chapter 6**

# **Class Documentation**

# 6.1 qpp::DiscreteDistribution Class Reference

```
#include <stat.h>
```

#### **Public Member Functions**

- template<typename InputIterator >
   DiscreteDistribution (InputIterator first, InputIterator last)
- DiscreteDistribution (std::initializer\_list< double > weights)
- Discrete Distribution (std::vector< double > weights)
- std::size\_t sample ()
- std::vector< double > probabilities () const

#### **Protected Attributes**

```
std::discrete_distributionstd::size_t > _d
```

#### 6.1.1 Constructor & Destructor Documentation

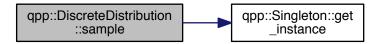
- 6.1.1.1 template<typename InputIterator > qpp::DiscreteDistribution::DiscreteDistribution ( InputIterator first, InputIterator last ) [inline]
- **6.1.1.2** qpp::DiscreteDistribution::DiscreteDistribution ( std::initializer\_list< double > weights ) [inline]
- 6.1.1.3 qpp::DiscreteDistribution::DiscreteDistribution ( std::vector< double > weights ) [inline]

#### 6.1.2 Member Function Documentation

**6.1.2.1** std::vector<double> qpp::DiscreteDistribution::probabilities ( ) const [inline]

6.1.2.2 std::size\_t qpp::DiscreteDistribution::sample() [inline]

Here is the call graph for this function:



# 6.1.3 Member Data Documentation

**6.1.3.1 std::discrete\_distribution<std::size\_t> qpp::DiscreteDistribution::\_d** [protected]

The documentation for this class was generated from the following file:

· include/classes/stat.h

# 6.2 qpp::DiscreteDistributionAbsSquare Class Reference

#include <stat.h>

#### **Public Member Functions**

- template<typename InputIterator >
   DiscreteDistributionAbsSquare (InputIterator first, InputIterator last)
- DiscreteDistributionAbsSquare (std::initializer\_list< types::cplx > amplitudes)
- DiscreteDistributionAbsSquare (std::vector< types::cplx > amplitudes)
- template<typename Derived >
   DiscreteDistributionAbsSquare (const Eigen::MatrixBase< Derived > &V)
- std::size\_t sample ()
- std::vector< double > probabilities () const

#### **Protected Member Functions**

template<typename InputIterator >
 std::vector< double > cplx2weights (InputIterator first, InputIterator last) const

#### **Protected Attributes**

std::discrete\_distributionstd::size\_t > \_d

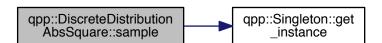
#### 6.2.1 Constructor & Destructor Documentation

- 6.2.1.1 template<typename InputIterator > qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare (InputIterator *first*, InputIterator *last* ) [inline]
- 6.2.1.2 qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare ( std::initializer\_list< types::cplx > amplitudes ) [inline]
- 6.2.1.3 qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare ( std::vector< types::cplx > amplitudes ) [inline]
- 6.2.1.4 template<typename Derived > qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare ( const Eigen::MatrixBase< Derived > & V ) [inline]

#### 6.2.2 Member Function Documentation

- 6.2.2.1 template<typename InputIterator > std::vector<double> qpp::DiscreteDistributionAbsSquare::cplx2weights ( InputIterator first, InputIterator last ) const [inline], [protected]
- **6.2.2.2** std::vector<double> qpp::DiscreteDistributionAbsSquare::probabilities ( ) const [inline]
- **6.2.2.3** std::size\_t qpp::DiscreteDistributionAbsSquare::sample() [inline]

Here is the call graph for this function:



#### 6.2.3 Member Data Documentation

**6.2.3.1** std::discrete\_distribution<std::size\_t> qpp::DiscreteDistributionAbsSquare::\_d [protected]

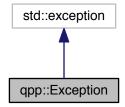
The documentation for this class was generated from the following file:

• include/classes/stat.h

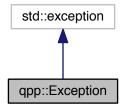
# 6.3 qpp::Exception Class Reference

#include <exception.h>

Inheritance diagram for qpp::Exception:



Collaboration diagram for qpp::Exception:



#### **Public Types**

• enum Type {

Type::UNKNOWN\_EXCEPTION = 1, Type::ZERO\_SIZE, Type::MATRIX\_NOT\_SQUARE, Type::MATRIX\_← NOT\_CVECTOR,

Type::MATRIX\_NOT\_RVECTOR, Type::MATRIX\_NOT\_VECTOR, Type::MATRIX\_NOT\_SQUARE\_OR\_C↔ VECTOR, Type::MATRIX\_NOT\_SQUARE\_OR\_RVECTOR,

Type::MATRIX\_NOT\_SQUARE\_OR\_VECTOR, Type::DIMS\_INVALID, Type::DIMS\_NOT\_EQUAL, Type::D↔ IMS\_MISMATCH\_MATRIX,

 $\label{type::DIMS_MISMATCH_CVECTOR} Type::DIMS\_MISMATCH\_RVECTOR, Type::DIMS\_MISMATCH\_VE \leftarrow CTOR, Type::SUBSYS\_MISMATCH\_DIMS,$ 

Type::PERM\_INVALID, Type::NOT\_QUBIT\_GATE, Type::NOT\_QUBIT\_SUBSYS, Type::NOT\_BIPARTITE, Type::OUT\_OF\_RANGE, Type::TYPE\_MISMATCH, Type::UNDEFINED\_TYPE, Type::CUSTOM\_EXCEPT → ION }

#### **Public Member Functions**

- Exception (const std::string &where, const Type &type)
- Exception (const std::string &where, const std::string &custom)
- virtual const char \* what () const noexceptoverride

#### **Private Member Functions**

• std::string \_construct\_exception\_msg ()

#### **Private Attributes**

- std::string \_where
- std::string \_msg
- Type \_type
- std::string \_custom

#### 6.3.1 Member Enumeration Documentation

**6.3.1.1 enum qpp::Exception::Type** [strong]

#### **Enumerator**

UNKNOWN\_EXCEPTION

ZERO\_SIZE

MATRIX\_NOT\_SQUARE

MATRIX\_NOT\_CVECTOR

MATRIX\_NOT\_RVECTOR

MATRIX\_NOT\_VECTOR

MATRIX\_NOT\_SQUARE\_OR\_CVECTOR

MATRIX\_NOT\_SQUARE\_OR\_RVECTOR

MATRIX\_NOT\_SQUARE\_OR\_VECTOR

DIMS\_INVALID

DIMS\_NOT\_EQUAL

DIMS\_MISMATCH\_MATRIX

DIMS\_MISMATCH\_CVECTOR

DIMS\_MISMATCH\_RVECTOR

DIMS\_MISMATCH\_VECTOR

 $SUBSYS\_MISMATCH\_DIMS$ 

PERM\_INVALID

NOT\_QUBIT\_GATE

NOT\_QUBIT\_SUBSYS

NOT\_BIPARTITE

OUT\_OF\_RANGE

TYPE\_MISMATCH

UNDEFINED\_TYPE

CUSTOM\_EXCEPTION

#### 6.3.2 Constructor & Destructor Documentation

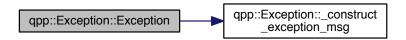
6.3.2.1 qpp::Exception::Exception ( const std::string & where, const Type & type ) [inline]

Here is the call graph for this function:



6.3.2.2 qpp::Exception::Exception ( const std::string & where, const std::string & custom ) [inline]

Here is the call graph for this function:



#### 6.3.3 Member Function Documentation

- **6.3.3.1** std::string qpp::Exception::\_construct\_exception\_msg( ) [inline], [private]
- **6.3.3.2 virtual const char\* qpp::Exception::what ( ) const** [inline], [override], [virtual], [noexcept]
- 6.3.4 Member Data Documentation
- **6.3.4.1 std::string qpp::Exception::\_custom** [private]
- **6.3.4.2 std::string qpp::Exception::\_msg** [private]
- **6.3.4.3 Type qpp::Exception::\_type** [private]
- **6.3.4.4 std::string qpp::Exception::\_where** [private]

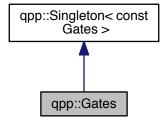
The documentation for this class was generated from the following file:

• include/classes/exception.h

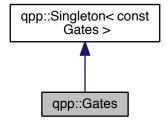
# 6.4 qpp::Gates Class Reference

#include <gates.h>

Inheritance diagram for qpp::Gates:



Collaboration diagram for qpp::Gates:



#### **Public Member Functions**

- types::cmat Rn (double theta, std::vector< double > n) const
- types::cmat Zd (std::size\_t D) const
- types::cmat Fd (std::size\_t D) const
- types::cmat Xd (std::size\_t D) const
- template<typename Derived = Eigen::MatrixXcd>
   Derived Id (std::Size\_t D) const
- template<typename Derived1 , typename Derived2 >

types::DynMat< typename

• template<typename Derived1 , typename Derived2 >

types::DynMat< typename

Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims) const

template<typename Derived >

types::DynMat< typename

 $\label{lem:decomposition} Derived::Scalar > CTRL \ (const \ Eigen::MatrixBase < Derived > \&A, \ const \ std::vector < std::size_t > \&ctrl, \ const \ std::vector < std::size_t > \&subsys, \ std::size_t \ n, \ std::size_t \ d=2) \ const$ 

#### **Public Attributes**

```
types::cmat Id2 { types::cmat::Identity(2, 2) }
types::cmat H { types::cmat::Zero(2, 2) }
types::cmat X { types::cmat::Zero(2, 2) }
types::cmat Y { types::cmat::Zero(2, 2) }
types::cmat Z { types::cmat::Zero(2, 2) }
types::cmat S { types::cmat::Zero(2, 2) }
types::cmat T { types::cmat::Zero(2, 2) }
types::cmat CNOTab { types::cmat::Identity(4, 4) }
types::cmat CNOTba { types::cmat::Zero(4, 4) }
types::cmat SWAP { types::cmat::Identity(4, 4) }
types::cmat TOF { types::cmat::Identity(8, 8) }
types::cmat FRED { types::cmat::Identity(8, 8) }
```

# **Private Member Functions**

• Gates ()

#### **Friends**

class Singleton < const Gates >

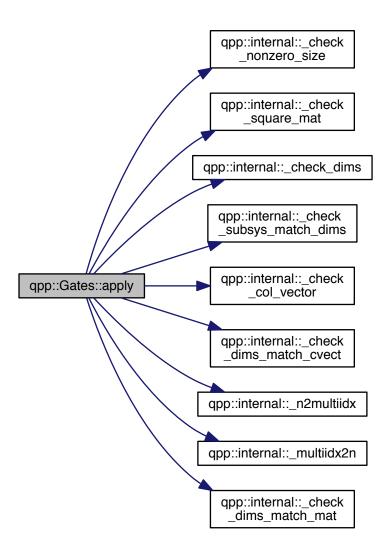
# **Additional Inherited Members**

#### 6.4.1 Constructor & Destructor Documentation

```
6.4.1.1 qpp::Gates::Gates() [inline], [private]
```

#### 6.4.2 Member Function Documentation

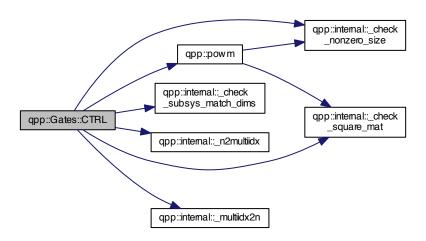
Here is the call graph for this function:



6.4.2.2 template < typename Derived1 , typename Derived2 > types::DynMat < typename Derived1::Scalar > qpp::Gates::applyCTRL ( const Eigen::MatrixBase < Derived1 > & state, const Eigen::MatrixBase < Derived2 > & A, const std::vector < std::size\_t > & subsys, std::size\_t n, std::size\_t d = 2 ) const [inline]

6.4.2.3 template<typename Derived > types::DynMat<typename Derived::Scalar> qpp::Gates::CTRL ( const Eigen::MatrixBase< Derived > & A, const std::vector< std::size\_t > & ctrl, const std::vector< std::size\_t > & subsys, std::size\_t n, std::size\_t d = 2 ) const [inline]

Here is the call graph for this function:



6.4.2.4 types::cmat qpp::Gates::Fd ( std::size\_t D ) const [inline]

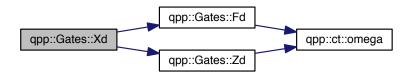
Here is the call graph for this function:



- 6.4.2.5 template<typename Derived = Eigen::MatrixXcd> Derived qpp::Gates::Id ( std::size\_t D ) const [inline]
- 6.4.2.6 types::cmat qpp::Gates::Rn ( double theta, std::vector < double > n ) const [inline]

6.4.2.7 types::cmat qpp::Gates::Xd ( std::size\_t D ) const [inline]

Here is the call graph for this function:



6.4.2.8 types::cmat qpp::Gates::Zd ( std::size\_t D ) const [inline]

Here is the call graph for this function:



- 6.4.3 Friends And Related Function Documentation
- **6.4.3.1 friend class Singleton**< const Gates > [friend]
- 6.4.4 Member Data Documentation
- 6.4.4.1 types::cmat qpp::Gates::CNOTab { types::cmat::Identity(4, 4) }
- 6.4.4.2 types::cmat qpp::Gates::CNOTba { types::cmat::Zero(4, 4) }
- 6.4.4.3 types::cmat qpp::Gates::CZ { types::cmat::Identity(4, 4) }
- 6.4.4.4 types::cmat qpp::Gates::FRED { types::cmat::Identity(8, 8) }
- 6.4.4.5 types::cmat qpp::Gates::H { types::cmat::Zero(2, 2) }
- 6.4.4.6 types::cmat qpp::Gates::ld2 { types::cmat::ldentity(2, 2) }
- 6.4.4.7 types::cmat qpp::Gates::S { types::cmat::Zero(2, 2) }
- 6.4.4.8 types::cmat qpp::Gates::SWAP { types::cmat::Identity(4, 4) }
- 6.4.4.9 types::cmat qpp::Gates::T { types::cmat::Zero(2, 2) }

```
6.4.4.10 types::cmat qpp::Gates::TOF { types::cmat::Identity(8, 8) }
6.4.4.11 types::cmat qpp::Gates::X { types::cmat::Zero(2, 2) }
6.4.4.12 types::cmat qpp::Gates::Y { types::cmat::Zero(2, 2) }
6.4.4.13 types::cmat qpp::Gates::Z { types::cmat::Zero(2, 2) }
```

The documentation for this class was generated from the following file:

• include/classes/gates.h

# 6.5 qpp::NormalDistribution Class Reference

```
#include <stat.h>
```

#### **Public Member Functions**

- NormalDistribution (double mean=0, double sigma=1)
- double sample ()

#### **Protected Attributes**

· std::normal\_distribution\_d

#### 6.5.1 Constructor & Destructor Documentation

6.5.1.1 qpp::NormalDistribution::NormalDistribution ( double mean = 0, double sigma = 1 ) [inline]

# 6.5.2 Member Function Documentation

**6.5.2.1** double qpp::NormalDistribution::sample() [inline]

Here is the call graph for this function:



#### 6.5.3 Member Data Documentation

**6.5.3.1** std::normal\_distribution qpp::NormalDistribution::\_d [protected]

The documentation for this class was generated from the following file:

• include/classes/stat.h

# 6.6 qpp::Qudit Class Reference

```
#include <qudit.h>
```

#### **Public Member Functions**

- Qudit (const types::cmat &rho=States::get\_instance().pz0)
- std::size\_t measure (const types::cmat &U, bool destructive=false)
- std::size\_t measure (bool destructive=false)
- types::cmat getRho () const
- std::size\_t getD () const

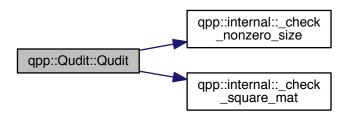
#### **Private Attributes**

- · types::cmat \_rho
- std::size\_t \_D

#### 6.6.1 Constructor & Destructor Documentation

6.6.1.1 qpp::Qudit::Qudit ( const types::cmat & rho = States::get\_instance() .pz0 ) [inline]

Here is the call graph for this function:

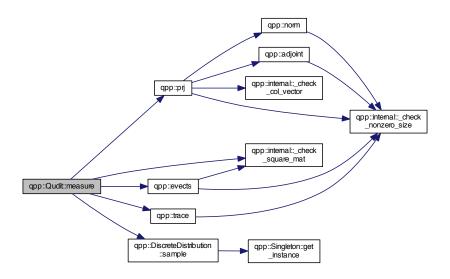


#### 6.6.2 Member Function Documentation

- 6.6.2.1 std::size\_t qpp::Qudit::getD( ) const [inline]
- 6.6.2.2 types::cmat qpp::Qudit::getRho() const [inline]

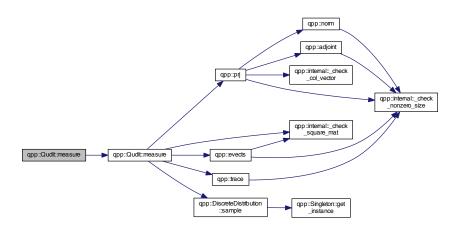
6.6.2.3 std::size\_t qpp::Qudit::measure ( const types::cmat & U, bool destructive = false ) [inline]

Here is the call graph for this function:



6.6.2.4 std::size\_t qpp::Qudit::measure ( bool destructive = false ) [inline]

Here is the call graph for this function:



#### 6.6.3 Member Data Documentation

6.6.3.1 std::size\_t qpp::Qudit::\_D [private]

**6.6.3.2 types::cmat qpp::Qudit::\_rho** [private]

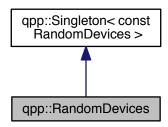
The documentation for this class was generated from the following file:

• include/classes/qudit.h

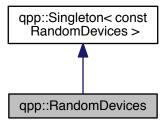
# 6.7 qpp::RandomDevices Class Reference

#include <randevs.h>

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



#### **Public Attributes**

- std::random\_device \_rd
- std::mt19937 \_rng

#### **Private Member Functions**

• RandomDevices ()

# **Friends**

class Singleton < const RandomDevices >

# **Additional Inherited Members**

#### 6.7.1 Constructor & Destructor Documentation

- **6.7.1.1 qpp::RandomDevices::RandomDevices()** [inline], [private]
- 6.7.2 Friends And Related Function Documentation
- **6.7.2.1 friend class Singleton**< **const RandomDevices** > [friend]
- 6.7.3 Member Data Documentation
- 6.7.3.1 std::random\_device qpp::RandomDevices::\_rd
- **6.7.3.2** std::mt19937 qpp::RandomDevices::\_rng [mutable]

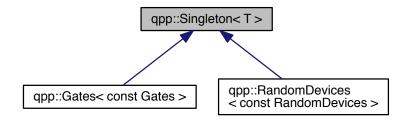
The documentation for this class was generated from the following file:

• include/classes/randevs.h

# 6.8 qpp::Singleton < T > Class Template Reference

#include <singleton.h>

Inheritance diagram for qpp::Singleton < T >:



# **Static Public Member Functions**

static T & get\_instance ()

#### **Protected Member Functions**

- Singleton ()=default
- virtual ∼Singleton ()
- Singleton (const Singleton &)=delete
- Singleton & operator= (const Singleton &)=delete

#### 6.8.1 Constructor & Destructor Documentation

**6.8.1.1** template<typename T> qpp::Singleton<T>::Singleton( ) [protected], [default]

- 6.8.1.2 template<typename T> virtual qpp::Singleton< T>:: $\sim$ Singleton( ) [inline], [protected], [virtual]
- 6.8.2 Member Function Documentation
- 6.8.2.1 template < typename T > static T& qpp::Singleton < T >::get\_instance( ) [inline], [static]
- 6.8.2.2 template<typename T> Singleton& qpp::Singleton< T>::operator= ( const Singleton< T> & ) [protected], [delete]

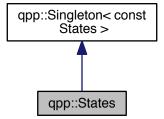
The documentation for this class was generated from the following file:

• include/classes/singleton.h

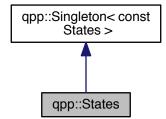
# 6.9 qpp::States Class Reference

#include <states.h>

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



#### **Public Attributes**

```
types::ket x0 { types::ket::Zero(2) }
types::ket x1 { types::ket::Zero(2) }
types::ket y0 { types::ket::Zero(2) }
types::ket y1 { types::ket::Zero(2) }
types::ket z0 { types::ket::Zero(2) }
types::ket z1 { types::ket::Zero(2) }
types::cmat px0 { types::cmat::Zero(2, 2) }
types::cmat px1 { types::cmat::Zero(2, 2) }
types::cmat py0 { types::cmat::Zero(2, 2) }
types::cmat py1 { types::cmat::Zero(2, 2) }
types::cmat pz0 { types::cmat::Zero(2, 2) }
types::cmat pz1 { types::cmat::Zero(2, 2) }
types::ket b00 { types::ket::Zero(4) }
types::ket b01 { types::ket::Zero(4) }
types::ket b10 { types::ket::Zero(4) }
types::ket b11 { types::ket::Zero(4) }
types::cmat pb00 { types::cmat::Zero(4, 4) }
types::cmat pb01 { types::cmat::Zero(4, 4) }
types::cmat pb10 { types::cmat::Zero(4, 4) }
types::cmat pb11 { types::cmat::Zero(4, 4) }
types::ket GHZ { types::ket::Zero(8) }
types::ket W { types::ket::Zero(8) }
types::cmat pGHZ { types::cmat::Zero(8, 8) }
types::cmat pW { types::cmat::Zero(8, 8) }
```

#### **Private Member Functions**

• States ()

#### **Friends**

class Singleton < const States >

# **Additional Inherited Members**

```
6.9.1 Constructor & Destructor Documentation
6.9.1.1 qpp::States::States() [inline], [private]
6.9.2 Friends And Related Function Documentation
6.9.2.1 friend class Singleton < const States > [friend]
6.9.3 Member Data Documentation
6.9.3.1 types::ket qpp::States::b00 { types::ket::Zero(4) }
6.9.3.2 types::ket qpp::States::b01 { types::ket::Zero(4) }
6.9.3.3 types::ket qpp::States::b10 { types::ket::Zero(4) }
```

```
6.9.3.4 types::ket qpp::States::b11 { types::ket::Zero(4) }
6.9.3.5 types::ket qpp::States::GHZ { types::ket::Zero(8) }
6.9.3.6 types::cmat qpp::States::pb00 { types::cmat::Zero(4, 4) }
6.9.3.7 types::cmat qpp::States::pb01 { types::cmat::Zero(4, 4) }
6.9.3.8
        types::cmat qpp::States::pb10 { types::cmat::Zero(4, 4) }
6.9.3.9 types::cmat qpp::States::pb11 { types::cmat::Zero(4, 4) }
6.9.3.10 types::cmat qpp::States::pGHZ { types::cmat::Zero(8, 8) }
6.9.3.11 types::cmat qpp::States::pW { types::cmat::Zero(8, 8) }
6.9.3.12 types::cmat qpp::States::px0 { types::cmat::Zero(2, 2) }
6.9.3.13 types::cmat qpp::States::px1 { types::cmat::Zero(2, 2) }
6.9.3.14 types::cmat qpp::States::py0 { types::cmat::Zero(2, 2) }
6.9.3.15 types::cmat qpp::States::py1 { types::cmat::Zero(2, 2) }
6.9.3.16 types::cmat qpp::States::pz0 { types::cmat::Zero(2, 2) }
6.9.3.17 types::cmat qpp::States::pz1 { types::cmat::Zero(2, 2) }
6.9.3.18 types::ket qpp::States::W { types::ket::Zero(8) }
6.9.3.19 types::ket qpp::States::x0 { types::ket::Zero(2) }
6.9.3.20 types::ket qpp::States::x1 { types::ket::Zero(2) }
6.9.3.21 types::ket qpp::States::y0 { types::ket::Zero(2) }
6.9.3.22 types::ket qpp::States::y1 { types::ket::Zero(2) }
6.9.3.23 types::ket qpp::States::z0 { types::ket::Zero(2) }
6.9.3.24 types::ket qpp::States::z1 { types::ket::Zero(2) }
```

The documentation for this class was generated from the following file:

• include/classes/states.h

# 6.10 qpp::Timer Class Reference

```
#include <timer.h>
```

#### **Public Member Functions**

- Timer ()
- void tic ()

- void toc ()
- double seconds () const

#### **Protected Attributes**

- std::chrono::steady clock::time point start
- std::chrono::steady\_clock::time\_point \_end

#### **Friends**

• std::ostream & operator<< (std::ostream &os, const Timer &rhs)

#### 6.10.1 Constructor & Destructor Documentation

```
6.10.1.1 qpp::Timer::Timer( ) [inline]
```

#### 6.10.2 Member Function Documentation

```
6.10.2.1 double qpp::Timer::seconds ( ) const [inline]
```

```
6.10.2.2 void qpp::Timer::tic( ) [inline]
```

6.10.2.3 void qpp::Timer::toc( ) [inline]

#### 6.10.3 Friends And Related Function Documentation

```
6.10.3.1 std::ostream & os, const Timer & rhs ) [friend]
```

#### 6.10.4 Member Data Documentation

```
6.10.4.1 std::chrono::steady_clock::time_point qpp::Timer::_end [protected]
```

```
6.10.4.2 std::chrono::steady_clock::time_point qpp::Timer::_start [protected]
```

The documentation for this class was generated from the following file:

• include/classes/timer.h

# 6.11 qpp::UniformIntDistribution Class Reference

```
#include <stat.h>
```

#### **Public Member Functions**

- UniformIntDistribution (int a=0, int b=1)
- int sample ()

#### **Protected Attributes**

std::uniform\_int\_distribution \_d

#### 6.11.1 Constructor & Destructor Documentation

**6.11.1.1** qpp::UniformIntDistribution::UniformIntDistribution (int a = 0, int b = 1) [inline]

#### 6.11.2 Member Function Documentation

**6.11.2.1** int qpp::UniformIntDistribution::sample() [inline]

Here is the call graph for this function:



#### 6.11.3 Member Data Documentation

**6.11.3.1 std::uniform\_int\_distribution qpp::UniformIntDistribution::\_d** [protected]

The documentation for this class was generated from the following file:

• include/classes/stat.h

# 6.12 qpp::UniformRealDistribution Class Reference

```
#include <stat.h>
```

#### **Public Member Functions**

- UniformRealDistribution (double a=0, double b=1)
- double sample ()

#### **Protected Attributes**

· std::uniform\_real\_distribution\_d

# 6.12.1 Constructor & Destructor Documentation

**6.12.1.1** qpp::UniformRealDistribution::UniformRealDistribution ( double a = 0, double b = 1 ) [inline]

#### 6.12.2 Member Function Documentation

**6.12.2.1** double qpp::UniformRealDistribution::sample ( ) [inline]

Here is the call graph for this function:



#### 6.12.3 Member Data Documentation

**6.12.3.1 std::uniform\_real\_distribution qpp::UniformRealDistribution::\_d** [protected]

The documentation for this class was generated from the following file:

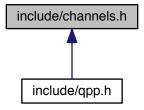
• include/classes/stat.h

# **Chapter 7**

# **File Documentation**

# 7.1 include/channels.h File Reference

This graph shows which files directly or indirectly include this file:



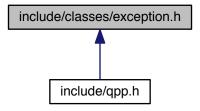
# **Namespaces**

qpp

- types::cmat qpp::super (const std::vector< types::cmat > &Ks)
- types::cmat qpp::choi (const std::vector< types::cmat > &Ks)
- std::vector< types::cmat > qpp::choi2kraus (const types::cmat &A)
- template<typename Derived >
   types::cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< types::cmat > &Ks)
- template<typename Derived >
   types::cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< types::cmat > &Ks,
   const std::vector< std::size\_t > &subsys, const std::vector< std::size\_t > &dims)

# 7.2 include/classes/exception.h File Reference

This graph shows which files directly or indirectly include this file:



#### Classes

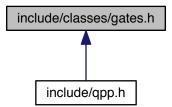
· class qpp::Exception

# **Namespaces**

• qpp

# 7.3 include/classes/gates.h File Reference

This graph shows which files directly or indirectly include this file:



# Classes

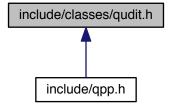
class qpp::Gates

# **Namespaces**

qpp

# 7.4 include/classes/qudit.h File Reference

This graph shows which files directly or indirectly include this file:



#### Classes

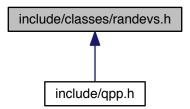
· class qpp::Qudit

# **Namespaces**

• qpp

# 7.5 include/classes/randevs.h File Reference

This graph shows which files directly or indirectly include this file:



# Classes

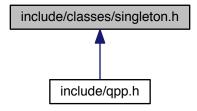
• class qpp::RandomDevices

# **Namespaces**

qpp

# 7.6 include/classes/singleton.h File Reference

This graph shows which files directly or indirectly include this file:



#### **Classes**

class qpp::Singleton< T >

# **Namespaces**

qpp

#### Macros

- #define CLASS\_SINGLETON(Foo)
- #define CLASS\_CONST\_SINGLETON(Foo)

#### 7.6.1 Macro Definition Documentation

# 7.6.1.1 #define CLASS\_CONST\_SINGLETON( Foo )

# Value:

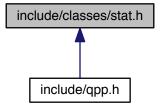
```
class Foo: public Singleton<const Foo>\
{\
          friend class Singleton<const Foo>;
```

#### 7.6.1.2 #define CLASS\_SINGLETON( Foo )

#### Value:

# 7.7 include/classes/stat.h File Reference

This graph shows which files directly or indirectly include this file:



# **Classes**

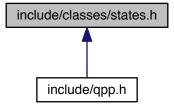
- class qpp::NormalDistribution
- class qpp::UniformRealDistribution
- class qpp::UniformIntDistribution
- class qpp::DiscreteDistribution
- class qpp::DiscreteDistributionAbsSquare

# **Namespaces**

• qpp

# 7.8 include/classes/states.h File Reference

This graph shows which files directly or indirectly include this file:



#### Classes

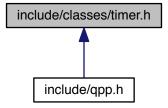
class qpp::States

# **Namespaces**

• qpp

# 7.9 include/classes/timer.h File Reference

This graph shows which files directly or indirectly include this file:



#### Classes

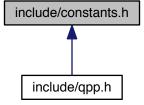
• class qpp::Timer

# **Namespaces**

qpp

# 7.10 include/constants.h File Reference

This graph shows which files directly or indirectly include this file:



# **Namespaces**

qpp

· qpp::ct

#### **Functions**

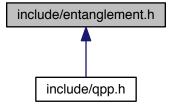
- constexpr std::complex< double > qpp::operator""\_i (unsigned long long int x)
- constexpr std::complex< double > qpp::operator""\_i (long double x)
- std::complex < double > qpp::ct::omega (std::size\_t D)

#### **Variables**

- constexpr double qpp::ct::chop = 1e-10
- constexpr double <a href="mailto:qpp::ct::eps">qpp::ct::eps</a> = 1e-12
- constexpr std::size t qpp::ct::maxn = 64
- constexpr double qpp::ct::pi = 3.141592653589793238462643383279502884
- constexpr double qpp::ct::ee = 2.718281828459045235360287471352662497

# 7.11 include/entanglement.h File Reference

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

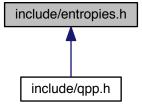
• qpp

- template<typename Derived >
   types::cmat qpp::schmidtcoeff (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t >
   &dims)
- template<typename Derived >
   types::cmat qpp::schmidtU (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- template<typename Derived >
   types::cmat qpp::schmidtV (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)
- template<typename Derived >
   types::cmat qpp::schmidtprob (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t >
   &dims)
- template<typename Derived >
   double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &dims)

 template<typename Derived > double qpp::gconcurrence (const Eigen::MatrixBase< Derived > &A)

# 7.12 include/entropies.h File Reference

This graph shows which files directly or indirectly include this file:



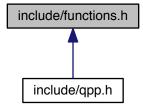
#### **Namespaces**

qpp

- template<typename Derived >
   double qpp::shannon (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   double qpp::renyi (const double alpha, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   double qpp::renyi\_inf (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   double qpp::tsallis (const double alpha, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size\_t > &subsys,
   const std::vector< std::size\_t > &dims)

#### 7.13 include/functions.h File Reference

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

• qpp

```
    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > qpp::transpose (const Eigen::MatrixBase < Derived > &A)
      Transpose.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::conjugate (const Eigen::MatrixBase < Derived > &A)
      Complex conjugate.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::adjoint (const Eigen::MatrixBase < Derived > &A)
      Adjoint.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::inverse (const Eigen::MatrixBase < Derived > &A)
      Inverse.
• template<typename Derived >
  Derived::Scalar <a href="mailto:qpp::trace">qpp::trace</a> (const Eigen::MatrixBase</a> Derived > &A)
• template<typename Derived >
  Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > &A)
      Determinant.
• template<typename Derived >
  Derived::Scalar <a href="mailto:qpp::logdet">qpp::logdet</a> (const Eigen::MatrixBase</a> Derived > &A)
      Logarithm of the determinant.

    template<typename Derived >

  Derived::Scalar <a href="mailto:qpp::sum">qpp::sum</a> (const Eigen::MatrixBase</a> Derived > &A)
      Element-wise sum.
```

```
• template<typename Derived >
  double qpp::norm (const Eigen::MatrixBase< Derived > &A)
      Trace norm.

    template<typename Derived >

  types::cmat qpp::evals (const Eigen::MatrixBase< Derived > &A)
     Eigenvalues.

    template<typename Derived >

  types::cmat qpp::evects (const Eigen::MatrixBase< Derived > &A)
      Eigenvectors.

    template<typename Derived >

  types::dmat qpp::hevals (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvalues.

    template<typename Derived >

  types::cmat qpp::hevects (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvectors.
• template<typename Derived >
  types::cmat qpp::funm (const Eigen::MatrixBase< Derived > &A, types::cplx(*f)(const types::cplx &))
     Functional calculus f(A)

    template<typename Derived >

  types::cmat qpp::sqrtm (const Eigen::MatrixBase< Derived > &A)
     Matrix square root.

    template<typename Derived >

  types::cmat qpp::absm (const Eigen::MatrixBase< Derived > &A)
     Matrix absolut value.

    template<typename Derived >

  types::cmat qpp::expm (const Eigen::MatrixBase< Derived > &A)
     Matrix exponential.

    template<typename Derived >

  types::cmat <a href="mailto:qpp::logm">qpp::logm</a> (const Eigen::MatrixBase</a> Derived > &A)
     Matrix logarithm.

    template<typename Derived >

  types::cmat qpp::sinm (const Eigen::MatrixBase< Derived > &A)
     Matrix sin.

    template<typename Derived >

  types::cmat qpp::cosm (const Eigen::MatrixBase< Derived > &A)
     Matrix cos.

    template<typename Derived >

  types::cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived > &A, const types::cplx z)
     Matrix power.
\bullet \ \ \text{template}{<} \text{typename Derived} >
  types::DynMat< typename
  Derived::Scalar > qpp::powm (const Eigen::MatrixBase< Derived > &A, std::size t n)
     Matrix power.

    template<typename OutputScalar , typename Derived >

  types::DynMat< OutputScalar > qpp::cwise (const Eigen::MatrixBase< Derived > &A, Output↔
  Scalar(*f)(const typename Derived::Scalar &))
     Functor.
template<typename T >
  types::DynMat< typename T::Scalar > qpp::kron (const T &head)
     Kronecker product (variadic overload)
template<typename T, typename... Args>
  types::DynMat< typename T::Scalar > qpp::kron (const T &head, const Args &...tail)
     Kronecker product (variadic overload)
```

```
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::kron (const std::vector< Derived > &As)
     Kronecker product (std::vector overload)

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > qpp::kron (const std::initializer_list< Derived > &As)
     Kronecker product (std::initializer_list overload)
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::kronpow (const Eigen::MatrixBase< Derived > &A, std::size t n)
     Kronecker power.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::reshape (const Eigen::MatrixBase < Derived > &A, std::size_t rows, std::size_t cols)
     Reshape.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t
  > &perm, const std::vector< std::size t > &dims)
     System permutation.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t >
  &dims)
     Partial trace.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t >
  &dims)
     Partial trace.
• template<typename Derived >
  types::DynMat< typename
  Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t >
  &subsys, const std::vector< std::size_t > &dims)
     Partial trace.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size t
  > &subsys, const std::vector< std::size_t > &dims)
     Partial transpose.
• template<typename Derived1 , typename Derived2 >
  types::DynMat< typename
  Derived1::Scalar > qpp::comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< De-
  rived2 > &B)
     Commutator.
• template<typename Derived1 , typename Derived2 >
  types::DynMat< typename
  Derived1::Scalar > qpp::anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase<
  Derived 2 > B
     Anti-commutator.

    template<typename Derived >

  types::DynMat< typename
  Derived::Scalar > qpp::prj (const Eigen::MatrixBase< Derived > &V)
     Projector.
```

• template<typename Derived > types::DynMat< typename Derived::Scalar > qpp::expandout (const Eigen::MatrixBase< Derived > &A, std::size\_t pos, const std↔ ::vector< std::size\_t > &dims) Expand out. • template<typename Derived > types::DynMat< typename Derived::Scalar > qpp::grams (const std::vector< Derived > &Vs) Gram-Schmidt orthogonalization (std::vector overload) • template<typename Derived > types::DynMat< typename Derived::Scalar > qpp::grams (const std::initializer\_list< Derived > &Vs) Gram-Schmidt orthogonalization (std::initializer\_list overload) • template<typename Derived > types::DynMat< typename Derived::Scalar > qpp::grams (const Eigen::MatrixBase < Derived > &A) Gram-Schmidt orthogonalization (Eigen expression (matrix) overload) std::vector< std::size\_t > qpp::n2multiidx (std::size\_t n, const std::vector< std::size\_t > &dims) Non-negative integer index to multi-index. std::size t qpp::multiidx2n (const std::vector< std::size t > &midx, const std::vector< std::size t > &dims) Multi-index to non-negative integer index. types::ket qpp::mket (const std::vector< std::size\_t > &mask) Multi-partite qubit ket. types::ket qpp::mket (const std::vector < std::size\_t > &mask, const std::vector < std::size\_t > &dims) Multi-partite qudit ket (different dimensions overload) types::ket qpp::mket (const std::vector< std::size\_t > &mask, std::size\_t d)

Multi-partite qudit ket (same dimensions overload)

std::vector< std::size\_t > qpp::invperm (const std::vector< std::size\_t > &perm)

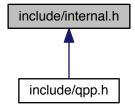
Inverse permutation.

std::vector< std::size\_t > qpp::compperm (const std::vector< std::size\_t > &perm, const std::vector< std
 ::size\_t > &sigma)

Compose permutations.

#### 7.14 include/internal.h File Reference

This graph shows which files directly or indirectly include this file:



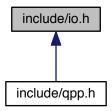
#### **Namespaces**

- qpp
- · qpp::internal

- void qpp::internal:: n2multiidx (std::size t n, std::size t numdims, const std::size t \*dims, std::size t \*result)
- std::size\_t app::internal::\_multiidx2n (const std::size\_t \*midx, std::size\_t numdims, const std::size\_t \*dims)
- template<typename Derived >
   bool qpp::internal::\_check\_square\_mat (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_row\_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_col\_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename T >
   bool qpp::internal::\_check\_nonzero\_size (const T &x)
- bool qpp::internal::\_check\_dims (const std::vector< std::size\_t > &dims)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_mat (const std::vector< std::size\_t > &dims, const Eigen::Matrix
   Base< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_cvect (const std::vector< std::size\_t > &dims, const Eigen::Matrix
   Base< Derived > &V)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_rvect (const std::vector< std::size\_t > &dims, const Eigen::Matrix
   Base< Derived > &V)
- bool qpp::internal::\_check\_eq\_dims (const std::vector < std::size\_t > &dims, std::size\_t dim)
- bool qpp::internal::\_check\_subsys\_match\_dims (const std::vector< std::size\_t > &subsys, const std
   ::vector< std::size\_t > &dims)
- bool qpp::internal::\_check\_perm (const std::vector< std::size\_t > &perm)
- template<typename Derived1, typename Derived2 > types::DynMat< typename</li>
   Derived1::Scalar > qpp::internal::\_kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::Matrix←
   Base< Derived2 > &B)
- template<typename T >
   void qpp::internal::variadic\_vector\_emplace (std::vector< T > &)
- template<typename T, typename First, typename... Args>
   void qpp::internal::variadic\_vector\_emplace (std::vector< T > &v, First &&first, Args &&...args)

#### 7.15 include/io.h File Reference

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

• qpp

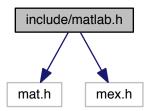
#### **Functions**

- template<typename T >
   void qpp::disp (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]",
   std::ostream &os=std::cout)
- template<typename T >
   void qpp::displn (const T &x, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)
- template<typename T >
   void qpp::disp (const T \*x, const std::size\_t n, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)
- template<typename T >
   void qpp::displn (const T \*x, const std::size\_t n, const std::string &separator, const std::string &start="[", const std::string &end="]", std::ostream &os=std::cout)
- template<typename Derived >
   void qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=ct::chop, std::ostream &os=std::cout)
- template<typename Derived >
   void qpp::displn (const Eigen::MatrixBase< Derived > &A, double chop=ct::chop, std::ostream &os=std
   ::cout)
- void qpp::disp (const types::cplx c, double chop=ct::chop, std::ostream &os=std::cout)
- void qpp::displn (const types::cplx c, double chop=ct::chop, std::ostream &os=std::cout)
- template<typename Derived > void qpp::save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)
   template
- template<typename Derived >
   types::DynMat< typename
   Derived::Scalar > qpp::load (const std::string &fname)

#### 7.16 include/matlab.h File Reference

```
#include "mat.h"
#include "mex.h"
```

Include dependency graph for matlab.h:



#### **Namespaces**

qpp

- template<typename Derived >
   Derived qpp::loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)
- template<>
   types::dmat qpp::loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)
- template<>
  types::cmat qpp::loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)
- template<typename Derived >
   void qpp::saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat\_file, const std::string &var name, const std::string &mode)
- template<>
   void qpp::saveMATLABmatrix (const Eigen::MatrixBase< types::dmat > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)
- template<>
   void qpp::saveMATLABmatrix (const Eigen::MatrixBase< typename types::cmat > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)

# 7.17 include/qpp.h File Reference

```
#include <algorithm>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <exception>
#include <fstream>
#include <functional>
#include <iomanip>
#include <iostream>
#include <iterator>
#include <numeric>
#include <ostream>
#include <random>
#include <stdexcept>
#include <string>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "constants.h"
#include "types.h"
#include "classes/exception.h"
#include "classes/singleton.h"
#include "classes/states.h"
#include "classes/randevs.h"
#include "internal.h"
#include "functions.h"
#include "classes/gates.h"
#include "classes/stat.h"
#include "entropies.h"
#include "entanglement.h"
#include "channels.h"
#include "io.h"
#include "random.h"
#include "classes/qudit.h"
#include "classes/timer.h"
Include dependency graph for qpp.h:
```

# **Namespaces**

• qpp

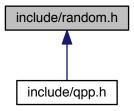
#### **Variables**

const RandomDevices & qpp::rdevs = RandomDevices::get\_instance()

- const Gates & qpp::gt = Gates::get\_instance()
- const States & qpp::st = States::get\_instance()

#### 7.18 include/random.h File Reference

This graph shows which files directly or indirectly include this file:



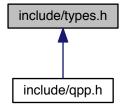
# **Namespaces**

qpp

- template<typename Derived >
   Derived qpp::rand (std::size\_t rows, std::size\_t cols, double a=0, double b=1)
- template<>
   types::dmat qpp::rand (std::size\_t rows, std::size\_t cols, double a, double b)
- template<>
  types::cmat qpp::rand (std::size\_t rows, std::size\_t cols, double a, double b)
- double qpp::rand (double a=0, double b=1)
- long long qpp::randint (long long a, long long b)
- template<typename Derived >
   Derived qpp::randn (std::size\_t rows, std::size\_t cols, double mean=0, double sigma=1)
- template<>
   types::dmat qpp::randn (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- template<>
   types::cmat qpp::randn (std::size\_t rows, std::size\_t cols, double mean, double sigma)
- double <a href="mailto:qpp::randn">qpp::randn</a> (double mean=0, double sigma=1)
- types::cmat qpp::randU (std::size\_t D)
- types::cmat qpp::randV (std::size\_t Din, std::size\_t Dout)
- std::vector< types::cmat > qpp::randkraus (std::size\_t n, std::size\_t D)
- types::cmat qpp::randH (std::size\_t D)
- types::ket qpp::randket (std::size\_t D)
- types::cmat qpp::randrho (std::size\_t D)
- std::vector< std::size\_t > qpp::randperm (std::size\_t n)

# 7.19 include/types.h File Reference

This graph shows which files directly or indirectly include this file:



# **Namespaces**

- qpp
- qpp::types

# **Typedefs**

- using qpp::types::cplx = std::complex< double >
- using qpp::types::cmat = Eigen::MatrixXcd
- using qpp::types::dmat = Eigen::MatrixXd
- using qpp::types::ket = Eigen::Matrix< cplx, Eigen::Dynamic, 1 >
- using qpp::types::bra = Eigen::Matrix< cplx, 1, Eigen::Dynamic >
- template<typename Scalar >
   using qpp::types::DynMat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >

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