Quantum++

v1.2

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Contents

Chapter 1

Quantum++

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Chat (questions/issues)

About

Quantum++ is a modern C++11 general purpose quantum computing library, composed solely of template header files. Quantum++ is written in standard C++11 and has very low external dependencies, using only the `Eigen 3` linear algebra header-only template library and, if available, the `OpenMP` multi-processing library.

Quantum++ is not restricted to qubit systems or specific quantum information processing tasks, being capable of simulating arbitrary quantum processes. The main design factors taken in consideration were the ease of use, high portability, and high performance. The library's simulation capabilities are only restricted by the amount of available physical memory. On a typical machine (Intel i5 8Gb RAM) Quantum++ can successfully simulate the evolution of 25 qubits in a pure state or of 12 qubits in a mixed state reasonably fast.

To report any bugs or ask for additional features/enhancements, please `submit an issue` with an appropriate label.

If you are interesting in contributing to this project, feel free to contact me. Alternatively, create a custom branch, add your contribution, then finally create a pull request. If I accept the pull request, I will merge your custom branch with the latest development branch. The latter will eventually be merged into a future release version. To contribute, you need to have a solid knowledge of C++ (preferably C++11), including templates and the standard library, a basic knowledge of quantum computing and linear algebra, and working experience with `Eigen 3`.

For additional `Eigen 3` documentation see `http://eigen.tuxfamily.org/dox/`. For a simple `Eigen 3` quick ASCII reference see `http://eigen.tuxfamily.org/dox/AsciiQuickReference.txt`.

License

Installation instructions and further documentation

Please see the installation guide https://github.com/vsoftco/qpp/blob/master/INSTALL.md "`INSTALL.md`" and the comprehensive `Wiki` for further documentation and detailed examples.

The official API documentation is available in PDF and HTML formats in the `doc` folder.

Chapter 2

Namespace Index

2.1 Namespace List

Here is a list of all namespaces with brief descriptions:

Chapter 3

Hierarchical Index

3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

Chapter 4

Class Index

4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

Chapter 5

File Index

5.1 File List

Here is a list of all files with brief descriptions:

Chapter 6

Namespace Documentation

6.1 qpp Namespace Reference

Quantum++ main namespace.

Namespaces

- exception

    Quantum++ exception hierarchy namespace.
- experimental

    Experimental/test functions/classes, do not use or modify.
- internal

    Internal utility functions, do not use them directly or modify them.
- literals

Classes

- class Bit_circuit

    Classical reversible circuit simulator.
- class Codes

    const Singleton class that defines quantum error correcting codes
- class Dynamic_bitset

    Dynamic bitset class, allows the specification of the number of bits at runtime.
- class Gates

    const Singleton class that implements most commonly used gates
- class IDisplay

    Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.
- class IJSON

    Abstract class (interface) that mandates the definition of very basic JSON serialization support.
- class Init

    const Singleton class that performs additional initializations/cleanups
- struct is_complex

    Checks whether the type is a complex type.
- struct is_complex< std::complex< T > >

Checks whether the type is a complex number type, specialization for complex types.

- struct is_iterable

  Checks whether T is compatible with an STL-like iterable container.
- struct is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), decltype(∗(std::declv

  Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.
- struct is_matrix_expression

  Checks whether the type is an Eigen matrix expression.
- struct make_void

  Helper for qpp::to_void<> alias template.
- class NoiseBase

  Base class for all noise models, derive your particular noise model.
- class NoiseType

  Contains template tags used to specify the noise type.
- class QCircuit

  Quantum circuit class.
- class QEngine

  Quantum circuit engine, executes qpp::QCircuit.
- class QNoisyEngine

  Noisy quantum circuit engine, executes qpp::QCircuit.
- class QubitAmplitudeDampingNoise

  Qubit amplitude damping noise, as described in Nielsen and Chuang.
- class QubitBitFlipNoise

  Qubit bit flip noise.
- class QubitBitPhaseFlipNoise

  Qubit bit-phase flip (dephasing) noise.
- class QubitDepolarizingNoise

  Qubit depolarizing noise.
- class QubitPhaseDampingNoise

  Qubit phase damping noise, as described in Nielsen and Chuang.
- class QubitPhaseFlipNoise

  Qubit phase flip (dephasing) noise.
- class QuditDepolarizingNoise

  Qudit depolarizing noise.
- class RandomDevices

  Singleton class that manages the source of randomness in the library.
- class States

  const Singleton class that implements most commonly used states
- class Timer

  Chronometer.

Typedefs

- template<typename... Ts>
  using to_void = typename make_void< Ts... >::type

  Alias template that implements the proposal for void_t.
- using idx = std::size_t

  Non-negative integer index, make sure you use an unsigned type.
- using bigint = long long int

  Big integer.
- using cplx = std::complex< double >

Complex number in double precision.

- using ket = Eigen::VectorXcd

  Complex (double precision) dynamic Eigen column vector.
- using bra = Eigen::RowVectorXcd

  Complex (double precision) dynamic Eigen row vector.
- using cmat = Eigen::MatrixXcd

  Complex (double precision) dynamic Eigen matrix.
- using dmat = Eigen::MatrixXd

  Real (double precision) dynamic Eigen matrix.
- template< typename Scalar >
  using dyn_mat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >

  Dynamic Eigen matrix over the field specified by Scalar.
- template< typename Scalar >
  using dyn_col_vect = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >

  Dynamic Eigen column vector over the field specified by Scalar.
- template< typename Scalar >
  using dyn_row_vect = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >

  Dynamic Eigen row vector over the field specified by Scalar.

Functions

- constexpr cplx operator"" _i (long double x) noexcept

  User-defined literal for complex $i = \sqrt{-1}$ *(real overload)*
- cplx omega (idx D)

  D-th root of unity.
- template< typename Derived >
  dyn_col_vect< double > schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt coefficients of the bi-partite pure state A.
- template< typename Derived >
  dyn_col_vect< double > schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt coefficients of the bi-partite pure state A.
- template< typename Derived >
  cmat schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt basis on Alice side.
- template< typename Derived >
  cmat schmidtA (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt basis on Alice side.
- template< typename Derived >
  cmat schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt basis on Bob side.
- template< typename Derived >
  cmat schmidtB (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt basis on Bob side.
- template< typename Derived >
  std::vector< double > schmidtprobs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt probabilities of the bi-partite pure state A.
- template< typename Derived >
  std::vector< double > schmidtprobs (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt probabilities of the bi-partite pure state A.

- template< typename Derived >
double entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

    Entanglement of the bi-partite pure state A.
- template< typename Derived >
double entanglement (const Eigen::MatrixBase< Derived > &A, idx d=2)

    Entanglement of the bi-partite pure state A.
- template< typename Derived >
double gconcurrence (const Eigen::MatrixBase< Derived > &A)

    G-concurrence of the bi-partite pure state A.
- template< typename Derived >
double negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

    Negativity of the bi-partite mixed state A.
- template< typename Derived >
double negativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

    Negativity of the bi-partite mixed state A.
- template< typename Derived >
double lognegativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

    Logarithmic negativity of the bi-partite mixed state A.
- template< typename Derived >
double lognegativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

    Logarithmic negativity of the bi-partite mixed state A.
- template< typename Derived >
double concurrence (const Eigen::MatrixBase< Derived > &A)

    Wootters concurrence of the bi-partite qubit mixed state A.
- template< typename Derived >
double entropy (const Eigen::MatrixBase< Derived > &A)

    von-Neumann entropy of the density matrix A
- double entropy (const std::vector< double > &prob)

    Shannon entropy of the probability distribution prob.
- template< typename Derived >
double renyi (const Eigen::MatrixBase< Derived > &A, double alpha)

    Renyi- α entropy of the density matrix A, for $\alpha \geq 0$.
- double renyi (const std::vector< double > &prob, double alpha)

    Renyi- α entropy of the probability distribution prob, for $\alpha \geq 0$.
- template< typename Derived >
double tsallis (const Eigen::MatrixBase< Derived > &A, double q)

    Tsallis- q entropy of the density matrix A, for $q \geq 0$.
- double tsallis (const std::vector< double > &prob, double q)

    Tsallis- q entropy of the probability distribution prob, for $q \geq 0$.
- template< typename Derived >
double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, const std::vector< idx > &dims)

    Quantum mutual information between 2 subsystems of a composite system.
- template< typename Derived >
double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, idx d=2)

    Quantum mutual information between 2 subsystems of a composite system.
- template< typename Derived >
dyn_mat< typename Derived::Scalar > transpose (const Eigen::MatrixBase< Derived > &A)

    Transpose.
- template< typename Derived >
dyn_mat< typename Derived::Scalar > conjugate (const Eigen::MatrixBase< Derived > &A)

    Complex conjugate.

- template< typename Derived >
dyn_mat< typename Derived::Scalar > adjoint (const Eigen::MatrixBase< Derived > &A)

    Adjoint.
- template< typename Derived >
dyn_mat< typename Derived::Scalar > inverse (const Eigen::MatrixBase< Derived > &A)

    Inverse.
- template< typename Derived >
Derived::Scalar trace (const Eigen::MatrixBase< Derived > &A)

    Trace.
- template< typename Derived >
Derived::Scalar det (const Eigen::MatrixBase< Derived > &A)

    Determinant.
- template< typename Derived >
Derived::Scalar logdet (const Eigen::MatrixBase< Derived > &A)

    Logarithm of the determinant.
- template< typename Derived >
Derived::Scalar sum (const Eigen::MatrixBase< Derived > &A)

    Element-wise sum of A.
- template< typename Derived >
Derived::Scalar prod (const Eigen::MatrixBase< Derived > &A)

    Element-wise product of A.
- template< typename Derived >
double norm (const Eigen::MatrixBase< Derived > &A)

    Frobenius norm.
- template< typename Derived >
dyn_mat< typename Derived::Scalar > normalize (const Eigen::MatrixBase< Derived > &A)

    Normalizes state vector (column or row vector) or density matrix.
- template< typename Derived >
std::pair< dyn_col_vect< cplx >, cmat > eig (const Eigen::MatrixBase< Derived > &A)

    Full eigen decomposition.
- template< typename Derived >
dyn_col_vect< cplx > evals (const Eigen::MatrixBase< Derived > &A)

    Eigenvalues.
- template< typename Derived >
cmat evects (const Eigen::MatrixBase< Derived > &A)

    Eigenvectors.
- template< typename Derived >
std::pair< dyn_col_vect< double >, cmat > heig (const Eigen::MatrixBase< Derived > &A)

    Full eigen decomposition of Hermitian expression.
- template< typename Derived >
dyn_col_vect< double > hevals (const Eigen::MatrixBase< Derived > &A)

    Hermitian eigenvalues.
- template< typename Derived >
cmat hevects (const Eigen::MatrixBase< Derived > &A)

    Eigenvectors of Hermitian matrix.
- template< typename Derived >
std::tuple< cmat, dyn_col_vect< double >, cmat > svd (const Eigen::MatrixBase< Derived > &A)

    Full singular value decomposition.
- template< typename Derived >
dyn_col_vect< double > svals (const Eigen::MatrixBase< Derived > &A)

    Singular values.
- template< typename Derived >
cmat svdU (const Eigen::MatrixBase< Derived > &A)

Left singular vectors.

- template<typename Derived >
  cmat svdV (const Eigen::MatrixBase< Derived > &A)

  Right singular vectors.
- template<typename Derived >
  cmat funm (const Eigen::MatrixBase< Derived > &A, cplx(∗f)(const cplx &))

  Functional calculus f(A)
- template<typename Derived >
  cmat sqrtm (const Eigen::MatrixBase< Derived > &A)

  Matrix square root.
- template<typename Derived >
  cmat absm (const Eigen::MatrixBase< Derived > &A)

  Matrix absolute value.
- template<typename Derived >
  cmat expm (const Eigen::MatrixBase< Derived > &A)

  Matrix exponential.
- template<typename Derived >
  cmat logm (const Eigen::MatrixBase< Derived > &A)

  Matrix logarithm.
- template<typename Derived >
  cmat sinm (const Eigen::MatrixBase< Derived > &A)

  Matrix sin.
- template<typename Derived >
  cmat cosm (const Eigen::MatrixBase< Derived > &A)

  Matrix cos.
- template<typename Derived >
  cmat spectralpowm (const Eigen::MatrixBase< Derived > &A, const cplx z)

  Matrix power.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > powm (const Eigen::MatrixBase< Derived > &A, idx n)

  Fast matrix power based on the SQUARE-AND-MULTIPLY algorithm.
- template<typename Derived >
  double schatten (const Eigen::MatrixBase< Derived > &A, double p)

  Schatten matrix norm.
- template<typename OutputScalar , typename Derived >
  dyn_mat< OutputScalar > cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(∗f)(const typename Derived::Scalar &))

  Functor.
- template<typename T >
  dyn_mat< typename T::Scalar > kron (const T &head)

  Kronecker product.
- template<typename T , typename... Args>
  dyn_mat< typename T::Scalar > kron (const T &head, const Args &... tail)

  Kronecker product.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > kron (const std::vector< Derived > &As)

  Kronecker product.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > kron (const std::initializer_list< Derived > &As)

  Kronecker product.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > kronpow (const Eigen::MatrixBase< Derived > &A, idx n)

  Kronecker power.

- template< typename T >
  dyn_mat< typename T::Scalar > dirsum (const T &head)

  Direct sum.
- template< typename T , typename... Args>
  dyn_mat< typename T::Scalar > dirsum (const T &head, const Args &... tail)

  Direct sum.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > dirsum (const std::vector< Derived > &As)

  Direct sum.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > dirsum (const std::initializer_list< Derived > &As)

  Direct sum.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > dirsumpow (const Eigen::MatrixBase< Derived > &A, idx n)

  Direct sum power.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > reshape (const Eigen::MatrixBase< Derived > &A, idx rows, idx cols)

  Reshape.
- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)

  Commutator.
- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)

  Anti-commutator.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > prj (const Eigen::MatrixBase< Derived > &A)

  Projector.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > grams (const std::vector< Derived > &As)

  Gram-Schmidt orthogonalization.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > grams (const std::initializer_list< Derived > &As)

  Gram-Schmidt orthogonalization.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > grams (const Eigen::MatrixBase< Derived > &A)

  Gram-Schmidt orthogonalization.
- std::vector< idx > n2multiidx (idx n, const std::vector< idx > &dims)

  Non-negative integer index to multi-index.
- idx multiidx2n (const std::vector< idx > &midx, const std::vector< idx > &dims)

  Multi-index to non-negative integer index.
- ket mket (const std::vector< idx > &mask, const std::vector< idx > &dims)

  Multi-partite qudit ket.
- ket mket (const std::vector< idx > &mask, idx d=2)

  Multi-partite qudit ket.
- cmat mprj (const std::vector< idx > &mask, const std::vector< idx > &dims)

  Projector onto multi-partite qudit ket.
- cmat mprj (const std::vector< idx > &mask, idx d=2)

  Projector onto multi-partite qudit ket.
- template< typename InputIterator >
  std::vector< double > abssq (InputIterator first, InputIterator last)

Computes the absolute values squared of an STL-like range of complex numbers.

- template< typename Container >
std::vector< double > abssq (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Computes the absolute values squared of an STL-like container.
- template< typename Derived >
std::vector< double > abssq (const Eigen::MatrixBase< Derived > &A)

  Computes the absolute values squared of an Eigen expression.
- template< typename InputIterator >
std::iterator_traits< InputIterator >::value_type sum (InputIterator first, InputIterator last)

  Element-wise sum of an STL-like range.
- template< typename Container >
Container::value_type sum (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Element-wise sum of the elements of an STL-like container.
- template< typename InputIterator >
std::iterator_traits< InputIterator >::value_type prod (InputIterator first, InputIterator last)

  Element-wise product of an STL-like range.
- template< typename Container >
Container::value_type prod (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Element-wise product of the elements of an STL-like container.
- template< typename Derived >
dyn_col_vect< typename Derived::Scalar > rho2pure (const Eigen::MatrixBase< Derived > &A)

  Finds the pure state representation of a matrix proportional to a projector onto a pure state.
- std::vector< idx > complement (std::vector< idx > subsys, idx n)

  Constructs the complement of a subsystem vector.
- template< typename Derived >
std::vector< double > rho2bloch (const Eigen::MatrixBase< Derived > &A)

  Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix A.
- cmat bloch2rho (const std::vector< double > &r)

  Computes the density matrix corresponding to the 3-dimensional real Bloch vector r.
- template< typename Derived >
std::size_t hash_eigen (const Eigen::MatrixBase< Derived > &A, std::size_t seed=0)

  Computes the hash of en Eigen matrix/vector/expression.
- template< typename Derived >
internal::IOManipEigen disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)

  Eigen expression ostream manipulator.
- internal::IOManipEigen disp (cplx z, double chop=qpp::chop)

  Complex number ostream manipulator.
- template< typename InputIterator >
internal::IOManipRange< InputIterator > disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")

  Range ostream manipulator.
- template< typename Container >
internal::IOManipRange< typename Container::const_iterator > disp (const Container &c, const std::string &separator, const std::string &start="[", const std::string &end="]", typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.
- template< typename PointerType >
internal::IOManipPointer< PointerType > disp (const PointerType *p, idx N, const std::string &separator, const std::string &start="[", const std::string &end="]")

  C-style pointer ostream manipulator.

- template< typename Derived >
  void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

  Saves Eigen expression to a binary file (internal format) in double precision.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > load (const std::string &fname)

  Loads Eigen matrix from a binary file (internal format) in double precision.
- template< typename Derived >
  dyn_col_vect< typename Derived::Scalar > ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, const std::vector< idx > &dims)

  Generalized inner product.
- template< typename Derived >
  dyn_col_vect< typename Derived::Scalar > ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, idx d=2)

  Generalized inner product.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

  Measures the state vector or density operator A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)

  Measures the state vector or density matrix A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &U)

  Measures the state vector or density matrix A in the orthonormal basis specified by the unitary matrix U.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &target, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &target, const std::vector< idx > &dims)

  Measures the part target of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &target, idx d=2)

  Measures the part target of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &target, idx d=2)

  Measures the part target of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &target, const std::vector< idx > &dims)

  Measures the part target of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 projectors specified by the columns of the matrix V.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &target, idx d=2)

  Measures the part target of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 projectors specified by the columns of the matrix V.

- template< typename Derived >
  std::tuple< std::vector< idx >, double, cmat > measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > target, std::vector< idx > dims)

  Sequentially measures the part target of the multi-partite state vector or density matrix A in the computational basis.
- template< typename Derived >
  std::tuple< std::vector< idx >, double, cmat > measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > target, idx d=2)

  Sequentially measures the part target of the multi-partite state vector or density matrix A in the computational basis.
- template< typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< cplx > >::type loadMATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.
- template< typename Derived >
  std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< typename Derived::←Scalar > >::type loadMATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.
- template< typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value >::type saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std←::string &mode)

  Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.
- template< typename Derived >
  std::enable_if< !std::is_same< typename Derived::Scalar, cplx >::value >::type saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)

  Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.
- std::vector< int > x2contfrac (double x, idx N, idx cut=1e5)

  Simple continued fraction expansion.
- double contfrac2x (const std::vector< int > &cf, idx N=idx(-1))

  Real representation of a simple continued fraction.
- bigint gcd (bigint a, bigint b)

  Greatest common divisor of two integers.
- bigint gcd (const std::vector< bigint > &as)

  Greatest common divisor of a list of integers.
- bigint lcm (bigint a, bigint b)

  Least common multiple of two integers.
- bigint lcm (const std::vector< bigint > &as)

  Least common multiple of a list of integers.
- std::vector< idx > invperm (const std::vector< idx > &perm)

  Inverse permutation.
- std::vector< idx > compperm (const std::vector< idx > &perm, const std::vector< idx > &sigma)

  Compose permutations.
- std::vector< bigint > factors (bigint a)

  Prime factor decomposition.
- bigint modmul (bigint a, bigint b, bigint p)

  Modular multiplication without overflow.
- bigint modpow (bigint a, bigint n, bigint p)

  Fast integer power modulo p based on the SQUARE-AND-MULTIPLY algorithm.
- std::tuple< bigint, bigint, bigint > egcd (bigint a, bigint b)

  Extended greatest common divisor of two integers.
- bigint modinv (bigint a, bigint p)

  Modular inverse of a mod p.

- bool isprime (bigint p, idx k=80)

  Primality test based on the Miller-Rabin's algorithm.
- bigint randprime (bigint a, bigint b, idx N=1000)

  Generates a random big prime uniformly distributed in the interval [a, b].
- std::vector< std::pair< int, int > > convergents (const std::vector< int > &cf)

  Convergents.
- std::vector< std::pair< int, int > > convergents (double x, idx N)

  Convergents.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &target, const std::vector< idx > &dims)

  Applies the controlled-gate A to the part target of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &target, idx d=2)

  Applies the controlled-gate A to the part target of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &target, const std::vector< idx > &dims)

  Applies the gate A to the part target of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &target, idx d=2)

  Applies the gate A to the part target of the multi-partite state vector or density matrix state.
- template<typename Derived >
  cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

  Applies the channel specified by the set of Kraus operators Ks to the density matrix A.
- template<typename Derived >
  cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &target, const std::vector< idx > &dims)

  Applies the channel specified by the set of Kraus operators Ks to the part target of the multi-partite density matrix A.
- template<typename Derived >
  cmat apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &target, idx d=2)

  Applies the channel specified by the set of Kraus operators Ks to the part target of the multi-partite density matrix A.
- cmat kraus2super (const std::vector< cmat > &Ks)

  Superoperator matrix.
- cmat kraus2choi (const std::vector< cmat > &Ks)

  Choi matrix.
- std::vector< cmat > choi2kraus (const cmat &A)

  Orthogonal Kraus operators from Choi matrix.
- cmat choi2super (const cmat &A)

  Converts Choi matrix to superoperator matrix.
- cmat super2choi (const cmat &A)

  Converts superoperator matrix to Choi matrix.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, idx d=2)

Partial trace.

- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &target, const std::vector< idx > &dims)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &target, idx d=2)

  Partial trace.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &target, const std::vector< idx > &dims)

  Partial transpose.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &target, idx d=2)

  Partial transpose.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, const std::vector< idx > &dims)

  Subsystem permutation.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, idx d=2)

  Subsystem permutation.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > applyQFT (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &target, idx d=2, bool swap=true)

  Applies the qudit quantum Fourier transform to the part target of the multi-partite state vector or density matrix A.
- template<typename Derived >
  dyn_mat< typename Derived::Scalar > applyTFQ (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &target, idx d=2, bool swap=true)

  Applies the inverse (adjoint) qudit quantum Fourier transform to the part target of the multi-partite state vector or density matrix A.
- template<typename Derived >
  dyn_col_vect< typename Derived::Scalar > TFQ (const Eigen::MatrixBase< Derived > &A, idx d=2, bool swap=true)

  Inverse (adjoint) qudit quantum Fourier transform.
- template<typename Derived >
  dyn_col_vect< typename Derived::Scalar > QFT (const Eigen::MatrixBase< Derived > &A, idx d=2, bool swap=true)

  Qudit quantum Fourier transform.
- double rand (double a, double b)

  Generates a random real number uniformly distributed in the interval [a, b)
- bigint rand (bigint a, bigint b)

  Generates a random big integer uniformly distributed in the interval [a, b].
- idx randidx (idx a=std::numeric_limits< idx >::min(), idx b=std::numeric_limits< idx >::max())

Generates a random index (idx) uniformly distributed in the interval [a, b].

- template< typename Derived >
  Derived rand (idx rows QPP_UNUSED_, idx cols QPP_UNUSED_, double a QPP_UNUSED_=0, double b QPP_UNUSED_=1)

  Generates a random matrix with entries uniformly distributed in the interval [a, b)
- template<>
  dmat rand (idx rows, idx cols, double a, double b)

  Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)
- template<>
  cmat rand (idx rows, idx cols, double a, double b)

  Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)
- template< typename Derived >
  Derived randn (idx rows QPP_UNUSED_, idx cols QPP_UNUSED_, double mean QPP_UNUSED_=0, double sigma QPP_UNUSED_=1)

  Generates a random matrix with entries normally distributed in N(mean, sigma)
- template<>
  dmat randn (idx rows, idx cols, double mean, double sigma)

  Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)
- template<>
  cmat randn (idx rows, idx cols, double mean, double sigma)

  Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)
- double randn (double mean=0, double sigma=1)

  Generates a random real number (double) normally distributed in N(mean, sigma)
- cmat randU (idx D=2)

  Generates a random unitary matrix.
- cmat randV (idx Din, idx Dout)

  Generates a random isometry matrix.
- std::vector< cmat > randkraus (idx N, idx D=2)

  Generates a set of random Kraus operators.
- cmat randH (idx D=2)

  Generates a random Hermitian matrix.
- ket randket (idx D=2)

  Generates a random normalized ket (pure state vector)
- cmat randrho (idx D=2)

  Generates a random density matrix.
- std::vector< idx > randperm (idx N)

  Generates a random uniformly distributed permutation.
- std::vector< double > randprob (idx N)

  Generates a random probability vector uniformly distributed over the probability simplex.
- std::vector< double > uniform (idx N)

  Uniform probability distribution vector.
- std::vector< double > marginalX (const dmat &probXY)

  Marginal distribution.
- std::vector< double > marginalY (const dmat &probXY)

  Marginal distribution.
- template< typename Container >
  double avg (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Average.

- template<typename Container >
  double cov (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Covariance.
- template<typename Container >
  double var (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Variance.
- template<typename Container >
  double sigma (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Standard deviation.
- template<typename Container >
  double cor (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Correlation.

Variables

- constexpr double chop = 1e-10

  Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.
- constexpr idx maxn = 64

  Maximum number of allowed qubits/qudits (subsystems)
- constexpr double pi = 3.141592653589793238462643383279502884

  π
- constexpr double ee = 2.718281828459045235360287471352662497

  Base of natural logarithm, e.
- constexpr double infty = std::numeric_limits<double>::max()

  Used to denote infinity in double precision.

6.1.1 Detailed Description

Quantum++ main namespace.

6.1.2 Typedef Documentation

6.1.2.1 bigint

```
using qpp::bigint = typedef long long int
```

Big integer.

6.1.2.2 bra

```
using qpp::bra = typedef Eigen::RowVectorXcd
```

Complex (double precision) dynamic Eigen row vector.

6.1.2.3 cmat

```
using qpp::cmat = typedef Eigen::MatrixXcd
```

Complex (double precision) dynamic Eigen matrix.

6.1.2.4 cplx

```
using qpp::cplx = typedef std::complex<double>
```

Complex number in double precision.

6.1.2.5 dmat

```
using qpp::dmat = typedef Eigen::MatrixXd
```

Real (double precision) dynamic Eigen matrix.

6.1.2.6 dyn_col_vect

```
template<typename Scalar >
using qpp::dyn_col_vect = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, 1>
```

Dynamic Eigen column vector over the field specified by *Scalar*.

Example:

```
// type of colvect is Eigen::Matrix<float, Eigen::Dynamic, 1>
dyn_col_vect<float> colvect(2);
```

6.1.2.7 dyn_mat

```
template<typename Scalar >
using qpp::dyn_mat = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>
```

Dynamic Eigen matrix over the field specified by *Scalar*.

Example:

```
// type of mat is Eigen::Matrix<float, Eigen::Dynamic, Eigen::Dynamic>
dyn_mat<float> mat(2, 3);
```

6.1.2.8 dyn_row_vect

```
template<typename Scalar >
using qpp::dyn_row_vect = typedef Eigen::Matrix<Scalar, 1, Eigen::Dynamic>
```

Dynamic Eigen row vector over the field specified by *Scalar*.

Example:

```
// type of rowvect is Eigen::Matrix<float, 1, Eigen::Dynamic>
dyn_row_vect<float> rowvect(3);
```

6.1.2.9 idx

```
using qpp::idx = typedef std::size_t
```

Non-negative integer index, make sure you use an unsigned type.

6.1.2.10 ket

```
using qpp::ket = typedef Eigen::VectorXcd
```

Complex (double precision) dynamic Eigen column vector.

6.1.2.11 to_void

```
template<typename... Ts>
using qpp::to_void = typedef typename make_void<Ts...>::type
```

Alias template that implements the proposal for void_t.

See also

http://www.open-std.org/jtc1/sc22/wg21/docs/papers/2014/n3911

6.1.3 Function Documentation

6.1.3.1 absm()

```
template<typename Derived >
cmat qpp::absm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix absolute value.

Parameters

A	Eigen expression

Returns

Matrix absolute value of *A*

6.1.3.2 abssq() [1/3]

```
template<typename InputIterator >
std::vector<double> qpp::abssq (
            InputIterator first,
            InputIterator last )
```

Computes the absolute values squared of an STL-like range of complex numbers.

Parameters

first	Iterator to the first element of the range
last	Iterator to the last element of the range

Returns

Real vector consisting of the range absolute values squared

6.1.3.3 abssq() [2/3]

```
template<typename Container >
std::vector<double> qpp::abssq (
            const Container & c,
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Computes the absolute values squared of an STL-like container.

Parameters

c	STL-like container

Returns

Real vector consisting of the container's absolute values squared

6.1.3.4 abssq() [3/3]

```
template<typename Derived >
std::vector<double> qpp::abssq (
            const Eigen::MatrixBase< Derived > & A )
```

Computes the absolute values squared of an Eigen expression.

Parameters

A	Eigen expression

Returns

Real vector consisting of the absolute values squared

6.1.3.5 adjoint()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::adjoint (
            const Eigen::MatrixBase< Derived > & A )
```

Adjoint.

Parameters

A	Eigen expression

Returns

Adjoint (Hermitian conjugate) of *A*, as a dynamic matrix over the same scalar field as *A*

6.1.3.6 anticomm()

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::anticomm (
            const Eigen::MatrixBase< Derived1 > & A,
            const Eigen::MatrixBase< Derived2 > & B )
```

Anti-commutator.

See also

qpp::comm()

Anti-commutator $\{A,B\} = AB + BA$. Both *A* and *B* must be Eigen expressions over the same scalar field.

Parameters

A	Eigen expression
B	Eigen expression

Returns

Anti-commutator $AB + BA$, as a dynamic matrix over the same scalar field as *A*

6.1.3.7 apply() [1/5]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::apply (
            const Eigen::MatrixBase< Derived1 > & state,
            const Eigen::MatrixBase< Derived2 > & A,
            const std::vector< idx > & target,
            const std::vector< idx > & dims )
```

Applies the gate *A* to the part *target* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate *A* must match the dimension of *target*

Parameters

state	Eigen expression
A	Eigen expression
target	Subsystem indexes where the gate *A* is applied
dims	Dimensions of the multi-partite system

Returns

Gate *A* applied to the part *target* of *state*

6.1.3.8 apply() [2/5]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::apply (
            const Eigen::MatrixBase< Derived1 > & state,
            const Eigen::MatrixBase< Derived2 > & A,
            const std::vector< idx > & target,
            idx d = 2 )
```

Applies the gate *A* to the part *target* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate *A* must match the dimension of *target*

Parameters

state	Eigen expression
A	Eigen expression
target	Subsystem indexes where the gate *A* is applied
d	Subsystem dimensions

Returns

Gate *A* applied to the part *target* of *state*

6.1.3.9 apply() [3/5]

```
template<typename Derived >
cmat qpp::apply (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks )
```

Applies the channel specified by the set of Kraus operators *Ks* to the density matrix *A*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators

Returns

Output density matrix after the action of the channel

6.1.3.10 apply() [4/5]

```
template<typename Derived >
cmat qpp::apply (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks,
            const std::vector< idx > & target,
            const std::vector< idx > & dims )
```

Applies the channel specified by the set of Kraus operators *Ks* to the part *target* of the multi-partite density matrix *A*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
target	Subsystem indexes where the Kraus operators *Ks* are applied
dims	Dimensions of the multi-partite system

Returns

Output density matrix after the action of the channel

6.1.3.11 apply() [5/5]

```
template<typename Derived >
cmat qpp::apply (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks,
            const std::vector< idx > & target,
            idx d = 2 )
```

Applies the channel specified by the set of Kraus operators *Ks* to the part *target* of the multi-partite density matrix *A*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
target	Subsystem indexes where the Kraus operators *Ks* are applied
d	Subsystem dimensions

Returns

Output density matrix after the action of the channel

6.1.3.12 applyCTRL() [1/2]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (
            const Eigen::MatrixBase< Derived1 > & state,
            const Eigen::MatrixBase< Derived2 > & A,
            const std::vector< idx > & ctrl,
            const std::vector< idx > & target,
            const std::vector< idx > & dims )
```

Applies the controlled-gate *A* to the part *target* of the multi-partite state vector or density matrix *state*.

See also

qpp::Gates::CTRL()

Note

The dimension of the gate *A* must match the dimension of *target*. Also, all control subsystems in *ctrl* must have the same dimension.

Parameters

state	Eigen expression
A	Eigen expression
ctrl	Control subsystem indexes
target	Subsystem indexes where the gate *A* is applied
dims	Dimensions of the multi-partite system

Returns

CTRL-A gate applied to the part *target* of *state*

6.1.3.13 applyCTRL() [2/2]

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (
            const Eigen::MatrixBase< Derived1 > & state,
            const Eigen::MatrixBase< Derived2 > & A,
            const std::vector< idx > & ctrl,
            const std::vector< idx > & target,
            idx d = 2 )
```

Applies the controlled-gate *A* to the part *target* of the multi-partite state vector or density matrix *state*.

See also

qpp::Gates::CTRL()

Note

The dimension of the gate *A* must match the dimension of *target*

Parameters

state	Eigen expression
A	Eigen expression
ctrl	Control subsystem indexes
target	Subsystem indexes where the gate *A* is applied
d	Subsystem dimensions

Returns

CTRL-A gate applied to the part *target* of *state*

6.1.3.14 applyQFT()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::applyQFT (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & target,
            idx d = 2,
            bool swap = true )
```

Applies the qudit quantum Fourier transform to the part *target* of the multi-partite state vector or density matrix *A*.

Parameters

A	Eigen expression
target	Subsystem indexes where the QFT is applied
d	Subsystem dimensions
swap	Swaps the qubits/qudits at the end (true by default)

Returns

Qudit Quantum Fourier transform applied to the part *target* of *A*

6.1.3.15 applyTFQ()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::applyTFQ (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & target,
            idx d = 2,
            bool swap = true )
```

Applies the inverse (adjoint) qudit quantum Fourier transform to the part *target* of the multi-partite state vector or density matrix *A*.

Parameters

A	Eigen expression
target	Subsystem indexes where the TFQ is applied
d	Subsystem dimensions
swap	Swaps the qubits/qudits at the end (true by default)

Returns

Inverse (adjoint) qudit Quantum Fourier transform applied to the part *target* of *A*

6.1.3.16 avg()

```
template<typename Container >
double qpp::avg (
            const std::vector< double > & prob,
            const Container & X,
            typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Average.

Parameters

prob	Real probability vector representing the probability distribution of *X*
X	Real random variable values represented by an STL-like container

Returns

Average of *X*

6.1.3.17 bloch2rho()

```
cmat qpp::bloch2rho (
            const std::vector< double > & r ) [inline]
```

Computes the density matrix corresponding to the 3-dimensional real Bloch vector *r*.

See also

qpp::rho2bloch()

Parameters

r	3-dimensional real vector

Returns

Qubit density matrix

6.1.3.18 choi2kraus()

```
std::vector<cmat> qpp::choi2kraus (
            const cmat & A ) [inline]
```

Orthogonal Kraus operators from Choi matrix.

See also

qpp::kraus2choi()

Extracts a set of orthogonal (under Hilbert-Schmidt operator norm) Kraus operators from the Choi matrix *A*

Note

The Kraus operators satisfy $Tr(K_i^\dagger K_j) = \delta_{ij}$ for all $i \neq j$

Parameters

A	Choi matrix

Returns

Set of orthogonal Kraus operators

6.1.3.19 choi2super()

```
cmat qpp::choi2super (
            const cmat & A ) [inline]
```

Converts Choi matrix to superoperator matrix.

See also

qpp::super2choi()

Parameters

A	Choi matrix

Returns

Superoperator matrix

6.1.3.20 comm()

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::comm (
            const Eigen::MatrixBase< Derived1 > & A,
            const Eigen::MatrixBase< Derived2 > & B )
```

Commutator.

See also

qpp::anticomm()

Commutator $[A,B] = AB - BA$. Both *A* and *B* must be Eigen expressions over the same scalar field.

Parameters

A	Eigen expression
B	Eigen expression

Returns

Commutator $AB - BA$, as a dynamic matrix over the same scalar field as *A*

6.1.3.21 complement()

```
std::vector<idx> qpp::complement (
            std::vector< idx > subsys,
            idx n ) [inline]
```

Constructs the complement of a subsystem vector.

Parameters

subsys	Subsystem vector
n	Total number of systems

Returns

Complement of *subsys* with respect to the set $\{0, 1, \ldots, n-1\}$

6.1.3.22 compperm()

```
std::vector<idx> qpp::compperm (
            const std::vector< idx > & perm,
            const std::vector< idx > & sigma ) [inline]
```

Compose permutations.

Parameters

perm	Permutation
sigma	Permutation

Returns

Composition of the permutations *perm* $\circ$ *sigma* = perm(sigma)

6.1.3.23 concurrence()

```
template<typename Derived >
double qpp::concurrence (
            const Eigen::MatrixBase< Derived > & A )
```

Wootters concurrence of the bi-partite qubit mixed state *A*.

Parameters

A	Eigen expression

Returns

Wootters concurrence

6.1.3.24 conjugate()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::conjugate (
            const Eigen::MatrixBase< Derived > & A )
```

Complex conjugate.

Parameters

A	Eigen expression

Returns

Complex conjugate of *A*, as a dynamic matrix over the same scalar field as *A*

6.1.3.25 contfrac2x()

```
double qpp::contfrac2x (
            const std::vector< int > & cf,
            idx N = idx(-1) )  [inline]
```

Real representation of a simple continued fraction.

See also

qpp::x2contfrac()

Note

If *N* is greater than the size of *cf* (by default it is), then all terms in *cf* are considered.

Parameters

cf	Integer vector containing the simple continued fraction expansion
N	Number of terms considered in the continued fraction expansion.

Returns

Real representation of the simple continued fraction

6.1.3.26 convergents() [1/2]

```
std::vector<std::pair<int, int> > qpp::convergents (
            const std::vector< int > & cf ) [inline]
```

Convergents.

See also

qpp::contfrac2x() and qpp::x2contfrac()

Parameters

cf	Continued fraction

Returns

Vector of convergents pairs (a_k, b_k) that approximate the number represented by the continued fraction

6.1.3.27 convergents() [2/2]

```
std::vector<std::pair<int, int> > qpp::convergents (
            double x,
            idx N ) [inline]
```

Convergents.

See also

qpp::contfrac2x() and qpp::x2contfrac()

Note

In the continued fraction expansion of *x* has less terms than *N*, then the series of convergents is truncated to the number of terms in the continued fraction expansion of *x*.

Parameters

x	Real number
N	Number of convergents.

Returns

Vector of convergents pairs (a_k, b_k) that approximate the number *x*

6.1.3.28 cor()

```
template<typename Container >
double qpp::cor (
            const dmat & probXY,
            const Container & X,
            const Container & Y,
            typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Correlation.

Parameters

probXY	Real matrix representing the joint probability distribution of *X* and *Y* in lexicographical order (*X* labels the rows, *Y* labels the columns)
X	Real random variable values represented by an STL-like container
Y	Real random variable values represented by an STL-like container

Returns

Correlation of *X* and *Y*

6.1.3.29 cosm()

```
template<typename Derived >
cmat qpp::cosm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix cos.

Parameters

A	Eigen expression

Returns

Matrix cosine of *A*

6.1.3.30 cov()

```
template<typename Container >
double qpp::cov (
            const dmat & probXY,
            const Container & X,
            const Container & Y,
            typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Covariance.

Parameters

probXY	Real matrix representing the joint probability distribution of *X* and *Y* in lexicographical order (*X* labels the rows, *Y* labels the columns)
X	Real random variable values represented by an STL-like container
Y	Real random variable values represented by an STL-like container

Returns

Covariance of *X* and *Y*

6.1.3.31 cwise()

```
template<typename OutputScalar , typename Derived >
dyn_mat<OutputScalar> qpp::cwise (
            const Eigen::MatrixBase< Derived > & A,
            OutputScalar(*)(const typename Derived::Scalar &) f )
```

Functor.

Parameters

A	Eigen expression
f	Pointer-to-function from scalars of *A* to *OutputScalar*

Returns

Component-wise $f(A)$, as a dynamic matrix over the *OutputScalar* scalar field

6.1.3.32 det()

```
template<typename Derived >
Derived::Scalar qpp::det (
            const Eigen::MatrixBase< Derived > & A )
```

Determinant.

Parameters

A	Eigen expression

Returns

Determinant of *A*, as a scalar over the same scalar field as *A*. Returns $\pm\infty$ when the determinant overflows/underflows.

6.1.3.33 dirsum() [1/4]

```
template<typename T >
dyn_mat<typename T::Scalar> qpp::dirsum (
            const T & head )
```

Direct sum.

See also

qpp::dirsumpow()

Used to stop the recursion for the variadic template version of qpp::dirsum()

Parameters

head	Eigen expression

Returns

Its argument *head*

6.1.3.34 dirsum() [2/4]

```
template<typename T , typename... Args>
dyn_mat<typename T::Scalar> qpp::dirsum (
            const T & head,
            const Args &... tail )
```

Direct sum.

See also

qpp::dirsumpow()

Parameters

head	Eigen expression
tail	Variadic Eigen expression (zero or more parameters)

Returns

Direct sum of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.35 dirsum() [3/4]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::dirsum (
            const std::vector< Derived > & As )
```

Direct sum.

See also

qpp::dirsumpow()

Parameters

As	std::vector of Eigen expressions

Returns

Direct sum of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.36 dirsum() [4/4]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::dirsum (
            const std::initializer_list< Derived > & As )
```

Direct sum.

See also

qpp::dirsumpow()

Parameters

As	std::initializer_list of Eigen expressions, such as *{A1*, A2, ... ,Ak}

Returns

Direct sum of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.37 dirsumpow()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::dirsumpow (
```

```
            const Eigen::MatrixBase< Derived > & A,
            idx n )
```

Direct sum power.

See also

qpp::dirsum()

Parameters

A	Eigen expression
n	Non-negative integer

Returns

Direct sum of *A* with itself *n* times $A^{\oplus n}$, as a dynamic matrix over the same scalar field as *A*

6.1.3.38 disp() [1/5]

```
template<typename Derived >
internal::IOManipEigen qpp::disp (
            const Eigen::MatrixBase< Derived > & A,
            double chop = qpp::chop )
```

Eigen expression ostream manipulator.

Parameters

A	Eigen expression
chop	Set to zero the elements smaller in absolute value than *chop*

Returns

Instance of qpp::internal::IOManipEigen

6.1.3.39 disp() [2/5]

```
internal::IOManipEigen qpp::disp (
            cplx z,
            double chop = qpp::chop )   [inline]
```

Complex number ostream manipulator.

Parameters

z	Complex number (or any other type implicitly cast-able to std::complex<double>)
chop	Set to zero the elements smaller in absolute value than *chop*

Returns

Instance of qpp::internal::IOManipEigen

6.1.3.40 disp() [3/5]

```
template<typename InputIterator >
internal::IOManipRange<InputIterator> qpp::disp (
            InputIterator first,
            InputIterator last,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]" )
```

Range ostream manipulator.

Parameters

first	Iterator to the first element of the range
last	Iterator to the last element of the range
separator	Separator
start	Left marking
end	Right marking

Returns

Instance of qpp::internal::IOManipRange

6.1.3.41 disp() [4/5]

```
template<typename Container >
internal::IOManipRange<typename Container::const_iterator> qpp::disp (
            const Container & c,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]",
            typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.

Parameters

c	Container
separator	Separator
start	Left marking
end	Right marking

Returns

Instance of qpp::internal::IOManipRange

6.1.3.42 disp() [5/5]

```
template<typename PointerType >
internal::IOManipPointer<PointerType> qpp::disp (
            const PointerType * p,
            idx N,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]" )
```

C-style pointer ostream manipulator.

Parameters

p	Pointer to the first element
N	Number of elements to be displayed
separator	Separator
start	Left marking
end	Right marking

Returns

Instance of qpp::internal::IOManipPointer

6.1.3.43 egcd()

```
std::tuple<bigint, bigint, bigint> qpp::egcd (
            bigint a,
            bigint b ) [inline]
```

Extended greatest common divisor of two integers.

See also

qpp::gcd()

Parameters

a	Integer
b	Integer

Returns

Tuple of: 1. Integer m, 2. Integer n, and 3. Non-negative integer $gcd(a, b)$ such that $ma + nb = gcd(a, b)$

6.1.3.44 eig()

```
template<typename Derived >
std::pair<dyn_col_vect<cplx>, cmat> qpp::eig (
            const Eigen::MatrixBase< Derived > & A )
```

Full eigen decomposition.

See also

qpp::heig()

Parameters

A	Eigen expression

Returns

Pair of: 1. Eigenvalues of *A*, as a complex dynamic column vector, and 2. Eigenvectors of *A*, as columns of a complex dynamic matrix

6.1.3.45 entanglement() [1/2]

```
template<typename Derived >
double qpp::entanglement (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Entanglement of the bi-partite pure state *A*.

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

See also

qpp::entropy()

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Entanglement, with the logarithm in base 2

6.1.3.46 entanglement() [2/2]

```
template<typename Derived >
double qpp::entanglement (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Entanglement of the bi-partite pure state *A*.

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

See also

qpp::entropy()

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Entanglement, with the logarithm in base 2

6.1.3.47 entropy() [1/2]

```
template<typename Derived >
double qpp::entropy (
            const Eigen::MatrixBase< Derived > & A )
```

von-Neumann entropy of the density matrix *A*

Parameters

A	Eigen expression

Returns

von-Neumann entropy, with the logarithm in base 2

6.1.3.48 entropy() [2/2]

```
double qpp::entropy (
            const std::vector< double > & prob )  [inline]
```

Shannon entropy of the probability distribution *prob*.

Parameters

prob	Real probability vector

Returns

Shannon entropy, with the logarithm in base 2

6.1.3.49 evals()

```
template<typename Derived >
dyn_col_vect<cplx> qpp::evals (
            const Eigen::MatrixBase< Derived > & A )
```

Eigenvalues.

See also

qpp::hevals()

Parameters

A	Eigen expression

Returns

Eigenvalues of *A*, as a complex dynamic column vector

6.1.3.50 evects()

```
template<typename Derived >
cmat qpp::evects (
            const Eigen::MatrixBase< Derived > & A )
```

Eigenvectors.

See also

qpp::hevects()

Parameters

A	Eigen expression

Returns

Eigenvectors of *A*, as columns of a complex dynamic matrix

6.1.3.51 expm()

```
template<typename Derived >
cmat qpp::expm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix exponential.

Parameters

A	Eigen expression

Returns

Matrix exponential of *A*

6.1.3.52 factors()

```
std::vector<bigint> qpp::factors (
            bigint a )  [inline]
```

Prime factor decomposition.

Note

Runs in $\mathcal{O}(\sqrt{n})$ time complexity

Parameters

a	Integer different from 0, 1 or -1

Returns

Integer vector containing the factors

6.1.3.53 funm()

```
template<typename Derived >
cmat qpp::funm (
            const Eigen::MatrixBase< Derived > & A,
            cplx(*)(const cplx &) f )
```

Functional calculus f(A)

Parameters

A	Eigen expression
f	Pointer-to-function from complex to complex

Returns

$f(A)$

6.1.3.54 gcd() [1/2]

```
bigint qpp::gcd (
            bigint a,
            bigint b ) [inline]
```

Greatest common divisor of two integers.

See also

qpp::lcm()

Parameters

a	Integer
b	Integer

Returns

Greatest common divisor of *a* and *b*

6.1.3.55 gcd() [2/2]

```
bigint qpp::gcd (
            const std::vector< bigint > & as ) [inline]
```

Greatest common divisor of a list of integers.

See also

qpp::lcm()

Parameters

as	List of integers

Returns

Greatest common divisor of all numbers in *as*

6.1.3.56 gconcurrence()

```
template<typename Derived >
double qpp::gconcurrence (
            const Eigen::MatrixBase< Derived > & A )
```

G-concurrence of the bi-partite pure state *A*.

Note

Both local dimensions must be equal

Uses qpp::logdet() to avoid overflows

See also

qpp::logdet()

Parameters

A	Eigen expression

Returns

G-concurrence

6.1.3.57 grams() [1/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::grams (
            const std::vector< Derived > & As )
```

Gram-Schmidt orthogonalization.

Parameters

As	std::vector of Eigen expressions as column vectors

Returns

Gram-Schmidt vectors of *As* as columns of a dynamic matrix over the same scalar field as its arguments

6.1.3.58 grams() [2/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::grams (
            const std::initializer_list< Derived > & As )
```

Gram-Schmidt orthogonalization.

Parameters

As	std::initializer_list of Eigen expressions as column vectors

Returns

Gram-Schmidt vectors of *As* as columns of a dynamic matrix over the same scalar field as its arguments

6.1.3.59 grams() [3/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::grams (
            const Eigen::MatrixBase< Derived > & A )
```

Gram-Schmidt orthogonalization.

Parameters

A	Eigen expression, the input vectors are the columns of *A*

Returns

Gram-Schmidt vectors of the columns of *A*, as columns of a dynamic matrix over the same scalar field as *A*

6.1.3.60 hash_eigen()

```
template<typename Derived >
std::size_t qpp::hash_eigen (
            const Eigen::MatrixBase< Derived > & A,
            std::size_t seed = 0 )
```

Computes the hash of en Eigen matrix/vector/expression.

Note

Code taken from boost::hash_combine(), see https://www.boost.org/doc/libs/1_69_0/doc/html/hash/reference.html#boost.hash_combine

Parameters

A	Eigen expression
seed	Seed, 0 by default

Returns

Hash of its argument

6.1.3.61 heig()

```
template<typename Derived >
std::pair<dyn_col_vect<double>, cmat> qpp::heig (
            const Eigen::MatrixBase< Derived > & A )
```

Full eigen decomposition of Hermitian expression.

See also

qpp::eig()

Parameters

A	Eigen expression

Returns

Pair of: 1. Eigenvalues of *A*, as a real dynamic column vector, and 2. Eigenvectors of *A*, as columns of a complex dynamic matrix

6.1.3.62 hevals()

```
template<typename Derived >
dyn_col_vect<double> qpp::hevals (
            const Eigen::MatrixBase< Derived > & A )
```

Hermitian eigenvalues.

See also

qpp::evals()

Parameters

A	Eigen expression

Returns

Eigenvalues of Hermitian *A*, as a real dynamic column vector

6.1.3.63 hevects()

```
template<typename Derived >
cmat qpp::hevects (
            const Eigen::MatrixBase< Derived > & A )
```

Eigenvectors of Hermitian matrix.

See also

qpp::evects()

Parameters

A	Eigen expression

Returns

Eigenvectors of Hermitian matrix *A*, as columns of a complex matrix

6.1.3.64 inverse()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::inverse (
            const Eigen::MatrixBase< Derived > & A )
```

Inverse.

Parameters

A	Eigen expression

Returns

Inverse of *A*, as a dynamic matrix over the same scalar field as *A*

6.1.3.65 invperm()

```
std::vector<idx> qpp::invperm (
            const std::vector< idx > & perm )  [inline]
```

Inverse permutation.

Parameters

perm	Permutation

Returns

Inverse of the permutation *perm*

6.1.3.66 ip() [1/2]

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::ip (
            const Eigen::MatrixBase< Derived > & phi,
            const Eigen::MatrixBase< Derived > & psi,
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )
```

Generalized inner product.

Parameters

phi	Column vector Eigen expression
psi	Column vector Eigen expression
subsys	Subsystem indexes over which *phi* is defined
dims	Dimensions of the multi-partite system

Returns

Inner product $\langle \phi_{subsys} | \psi \rangle$, as a scalar or column vector over the remaining Hilbert space

6.1.3.67 ip() [2/2]

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::ip (
            const Eigen::MatrixBase< Derived > & phi,
            const Eigen::MatrixBase< Derived > & psi,
            const std::vector< idx > & subsys,
            idx d = 2 )
```

Generalized inner product.

Parameters

phi	Column vector Eigen expression
psi	Column vector Eigen expression
subsys	Subsystem indexes over which *phi* is defined
d	Subsystem dimensions

Returns

Inner product $\langle \phi_{subsys} | \psi \rangle$, as a scalar or column vector over the remaining Hilbert space

6.1.3.68 isprime()

```
bool qpp::isprime (
            bigint p,
            idx k = 80 )  [inline]
```

Primality test based on the Miller-Rabin's algorithm.

Parameters

p	Integer different from 0, 1 or -1
k	Number of iterations. The probability of a false positive is 2^{-k}.

Returns

True if the number is (most-likely) prime, false otherwise

6.1.3.69 kraus2choi()

```
cmat qpp::kraus2choi (
            const std::vector< cmat > & Ks )  [inline]
```

Choi matrix.

See also

qpp::choi2kraus()

Constructs the Choi matrix of the channel specified by the set of Kraus operators *Ks* in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

Note

The superoperator matrix S and the Choi matrix C are related by $S_{ab,mn} = C_{ma,nb}$

Parameters

Ks	Set of Kraus operators

Returns

Choi matrix

6.1.3.70 kraus2super()

```
cmat qpp::kraus2super (
            const std::vector< cmat > & Ks )  [inline]
```

Superoperator matrix.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators *Ks* in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

Parameters

Ks	Set of Kraus operators

Returns

Superoperator matrix

6.1.3.71 kron() [1/4]

```
template<typename T >
dyn_mat<typename T::Scalar> qpp::kron (
            const T & head )
```

Kronecker product.

See also

qpp::kronpow()

Used to stop the recursion for the variadic template version of qpp::kron()

Parameters

head	Eigen expression

Returns

Its argument *head*

6.1.3.72 kron() [2/4]

```
template<typename T , typename... Args>
dyn_mat<typename T::Scalar> qpp::kron (
            const T & head,
            const Args &... tail )
```

Kronecker product.

See also

qpp::kronpow()

Parameters

head	Eigen expression
tail	Variadic Eigen expression (zero or more parameters)

Returns

Kronecker product of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.73 kron() [3/4]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::kron (
            const std::vector< Derived > & As )
```

Kronecker product.

See also

qpp::kronpow()

Parameters

As	std::vector of Eigen expressions

Returns

Kronecker product of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.74 kron() [4/4]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::kron (
            const std::initializer_list< Derived > & As )
```

Kronecker product.

See also

qpp::kronpow()

Parameters

As	std::initializer_list of Eigen expressions, such as *{A1*, A2, ... ,Ak}

Returns

Kronecker product of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.75 kronpow()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::kronpow (
```

```
const Eigen::MatrixBase< Derived > & A,
idx n )
```

Kronecker power.

See also

qpp::kron()

Parameters

A	Eigen expression
n	Non-negative integer

Returns

Kronecker product of *A* with itself *n* times $A^{\otimes n}$, as a dynamic matrix over the same scalar field as *A*

6.1.3.76 lcm() [1/2]

```
bigint qpp::lcm (
            bigint a,
            bigint b ) [inline]
```

Least common multiple of two integers.

See also

qpp::gcd()

Parameters

a	Integer
b	Integer

Returns

Least common multiple of *a* and *b*

6.1.3.77 lcm() [2/2]

```
bigint qpp::lcm (
            const std::vector< bigint > & as ) [inline]
```

Least common multiple of a list of integers.

See also

qpp::gcd()

Parameters

as	List of integers

Returns

Least common multiple of all numbers in *as*

6.1.3.78 load()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::load (
            const std::string & fname )
```

Loads Eigen matrix from a binary file (internal format) in double precision.

See also

qpp::save()

The template parameter cannot be automatically deduced and must be explicitly provided, depending on the scalar field of the matrix that is being loaded.

Example:

```
// loads a previously saved Eigen dynamic complex matrix from "input.bin"
cmat mat = load<cmat>("input.bin");
```

Parameters

fname	Output file name

6.1.3.79 loadMATLAB() [1/2]

```
template<typename Derived >
std::enable_if<std::is_same<typename Derived::Scalar, cplx>::value, dyn_mat<cplx> >::type
qpp::loadMATLAB (
            const std::string & mat_file,
            const std::string & var_name )
```

Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.

See also

qpp::saveMATLAB()

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen ket
// from the MATLAB file "input.mat"
ket psi = loadMATLAB<ket>("input.mat");
```

Template Parameters

Derived	Complex Eigen type

Parameters

mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be loaded

Returns

Eigen dynamic matrix

6.1.3.80 loadMATLAB() [2/2]

```
template<typename Derived >
std::enable_if<!std::is_same<typename Derived::Scalar, cplx>::value, dyn_mat<typename Derived↩
::Scalar> >::type qpp::loadMATLAB (
            const std::string & mat_file,
            const std::string & var_name )
```

Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.

See also

qpp::saveMATLAB()

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen dynamic double matrix
// from the MATLAB file "input.mat"
dmat mat = loadMATLAB<dmat>("input.mat");
```

Template Parameters

Derived	Non-complex Eigen type

Parameters

mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be loaded

Returns

Eigen dynamic matrix

6.1.3.81 logdet()

```
template<typename Derived >
Derived::Scalar qpp::logdet (
            const Eigen::MatrixBase< Derived > & A )
```

Logarithm of the determinant.

Useful when the determinant overflows/underflows

Parameters

A	Eigen expression

Returns

Logarithm of the determinant of *A*, as a scalar over the same scalar field as *A*

6.1.3.82 logm()

```
template<typename Derived >
cmat qpp::logm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix logarithm.

Parameters

A	Eigen expression

Returns

Matrix logarithm of *A*

6.1.3.83 lognegativity() [1/2]

```
template<typename Derived >
double qpp::lognegativity (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Logarithmic negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Logarithmic negativity, with the logarithm in base 2

6.1.3.84 lognegativity() [2/2]

```
template<typename Derived >
double qpp::lognegativity (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Logarithmic negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Logarithmic negativity, with the logarithm in base 2

6.1.3.85 marginalX()

```
std::vector<double> qpp::marginalX (
            const dmat & probXY )  [inline]
```

Marginal distribution.

Parameters

probXY	Real matrix representing the joint probability distribution of *X* and *Y* in lexicographical order (*X* labels the rows, *Y* labels the columns)

Returns

Real vector consisting of the marginal distribution of *X*

6.1.3.86 marginalY()

```
std::vector<double> qpp::marginalY (
            const dmat & probXY ) [inline]
```

Marginal distribution.

Parameters

probXY	Real matrix representing the joint probability distribution of *X* and *Y* in lexicographical order (*X* labels the rows, *Y* labels the columns)

Returns

Real vector consisting of the marginal distribution of *Y*

6.1.3.87 measure() [1/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks )
```

Measures the state vector or density operator *A* using the set of Kraus operators *Ks*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.88 measure() [2/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::initializer_list< cmat > & Ks )
```

Measures the state vector or density matrix *A* using the set of Kraus operators *Ks*.

Parameters

A	Eigen expression
Ks	Set of Kraus operators

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.89 measure() [3/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const cmat & U )
```

Measures the state vector or density matrix *A* in the orthonormal basis specified by the unitary matrix *U*.

Parameters

A	Eigen expression
U	Unitary matrix whose columns represent the measurement basis vectors

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.90 measure() [4/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks,
            const std::vector< idx > & target,
            const std::vector< idx > & dims )
```

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *target*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
target	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.91 measure() [5/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::initializer_list< cmat > & Ks,
            const std::vector< idx > & target,
            const std::vector< idx > & dims )
```

Measures the part *target* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *target*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
target	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.92 measure() [6/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< cmat > & Ks,
            const std::vector< idx > & target,
            idx d = 2 )
```

Measures the part *target* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *target*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
target	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.93 measure() [7/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const std::initializer_list< cmat > & Ks,
            const std::vector< idx > & target,
            idx d = 2 )
```

Measures the part *target* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

qpp::measure_seq()

Note

The dimension of all *Ks* must match the dimension of *target*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
Ks	Set of Kraus operators
target	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.94 measure() [8/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const cmat & V,
            const std::vector< idx > & target,
            const std::vector< idx > & dims )
```

Measures the part *target* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 projectors specified by the columns of the matrix *V*.

See also

qpp::measure_seq()

Note

The dimension of *V* must match the dimension of *target*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
V	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 projectors
target	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.95 measure() [9/9]

```
template<typename Derived >
std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (
            const Eigen::MatrixBase< Derived > & A,
            const cmat & V,
            const std::vector< idx > & target,
            idx d = 2 )
```

Measures the part *target* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 projectors specified by the columns of the matrix *V*.

See also

qpp::measure_seq()

Note

The dimension of *V* must match the dimension of *target*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

A	Eigen expression
V	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 projectors
target	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.96 measure_seq() [1/2]

```
template<typename Derived >
std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (
            const Eigen::MatrixBase< Derived > & A,
            std::vector< idx > target,
            std::vector< idx > dims )
```

Sequentially measures the part *target* of the multi-partite state vector or density matrix *A* in the computational basis.

See also

qpp::measure()

Parameters

A	Eigen expression
target	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *target*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.97 measure_seq() [2/2]

```
template<typename Derived >
std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (
            const Eigen::MatrixBase< Derived > & A,
            std::vector< idx > target,
            idx d = 2 )
```

Sequentially measures the part *target* of the multi-partite state vector or density matrix *A* in the computational basis.

See also

qpp::measure()

Parameters

A	Eigen expression
target	Subsystem indexes that are measured
d	Subsystem dimensions

Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *target*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.98 mket() [1/2]

```
ket qpp::mket (
            const std::vector< idx > & mask,
            const std::vector< idx > & dims )   [inline]
```

Multi-partite qudit ket.

See also

qpp::operator "" _ket()

Constructs the multi-partite qudit ket $|\mathrm{mask}\rangle$, where *mask* is a std::vector of non-negative integers. Each element in *mask* has to be smaller than the corresponding element in *dims*.

Parameters

mask	std::vector of non-negative integers
dims	Dimensions of the multi-partite system

Returns

Multi-partite qudit state vector, as a complex dynamic column vector

6.1.3.99 mket() [2/2]

```
ket qpp::mket (
            const std::vector< idx > & mask,
            idx d = 2 )  [inline]
```

Multi-partite qudit ket.

See also

qpp::operator "" _ket()

Constructs the multi-partite qudit ket $|\mathrm{mask}\rangle$, all subsystem having equal dimension *d*. *mask* is a std::vector of non-negative integers, and each element in *mask* has to be strictly smaller than *d*.

Parameters

mask	std::vector of non-negative integers
d	Subsystem dimensions

Returns

Multi-partite qudit state vector, as a complex dynamic column vector

6.1.3.100 modinv()

```
bigint qpp::modinv (
            bigint a,
            bigint p )  [inline]
```

Modular inverse of *a* mod *p*.

See also

qpp::egcd()

Note

a and *p* must be co-prime

Parameters

a	Non-negative integer
p	Non-negative integer

Returns

Modular inverse $a^{-1} \mod p$

6.1.3.101 modmul()

```
bigint qpp::modmul (
            bigint a,
            bigint b,
            bigint p ) [inline]
```

Modular multiplication without overflow.

Computes $ab \bmod p$ without overflow

Parameters

a	Integer
b	Integer
p	Positive integer

Returns

$ab \bmod p$ avoiding overflow

6.1.3.102 modpow()

```
bigint qpp::modpow (
            bigint a,
```

```
bigint n,
bigint p )   [inline]
```

Fast integer power modulo *p* based on the SQUARE-AND-MULTIPLY algorithm.

Note

Uses qpp::modmul() that avoids overflows

Computes $a^n \bmod p$

Parameters

a	Non-negative integer
n	Non-negative integer
p	Strictly positive integer

Returns

$a^n \bmod p$

6.1.3.103 mprj() [1/2]

```
cmat qpp::mprj (
        const std::vector< idx > & mask,
        const std::vector< idx > & dims )   [inline]
```

Projector onto multi-partite qudit ket.

See also

qpp::operator "" _prj()

Constructs the projector onto the multi-partite qudit ket $|\mathrm{mask}\rangle$, where *mask* is a std::vector of non-negative integers. Each element in *mask* has to be smaller than the corresponding element in *dims*.

Parameters

mask	std::vector of non-negative integers
dims	Dimensions of the multi-partite system

Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

6.1.3.104 mprj() [2/2]

```
cmat qpp::mprj (
            const std::vector< idx > & mask,
            idx d = 2 )  [inline]
```

Projector onto multi-partite qudit ket.

See also

qpp::operator "" _prj()

Constructs the projector onto the multi-partite qudit ket $|\mathrm{mask}\rangle$, all subsystem having equal dimension *d*. *mask* is a std::vector of non-negative integers, and each element in *mask* has to be strictly smaller than *d*.

Parameters

mask	std::vector of non-negative integers
d	Subsystem dimensions

Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

6.1.3.105 multiidx2n()

```
idx qpp::multiidx2n (
            const std::vector< idx > & midx,
            const std::vector< idx > & dims )  [inline]
```

Multi-index to non-negative integer index.

See also

qpp::n2multiidx()

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

Parameters

midx	Multi-index
dims	Dimensions of the multi-partite system

Returns

Non-negative integer index

6.1.3.106 n2multiidx()

```
std::vector<idx> qpp::n2multiidx (
            idx n,
            const std::vector< idx > & dims ) [inline]
```

Non-negative integer index to multi-index.

See also

qpp::multiidx2n()

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

Parameters

n	Non-negative integer index
dims	Dimensions of the multi-partite system

Returns

Multi-index of the same size as *dims*

6.1.3.107 negativity() [1/2]

```
template<typename Derived >
double qpp::negativity (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Negativity

6.1.3.108 negativity() [2/2]

```
template<typename Derived >
double qpp::negativity (
```

```
const Eigen::MatrixBase< Derived > & A,
idx d = 2 )
```

Negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Negativity

6.1.3.109 norm()

```
template<typename Derived >
double qpp::norm (
            const Eigen::MatrixBase< Derived > & A )
```

Frobenius norm.

Parameters

A	Eigen expression

Returns

Frobenius norm of *A*

6.1.3.110 normalize()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::normalize (
            const Eigen::MatrixBase< Derived > & A )
```

Normalizes state vector (column or row vector) or density matrix.

Parameters

A	Eigen expression

Returns

Normalized state vector or density matrix

6.1.3.111 omega()

```
cplx qpp::omega (
            idx D ) [inline]
```

D-th root of unity.

Parameters

D	Non-negative integer

Returns

D-th root of unity $\exp(2\pi i/D)$

6.1.3.112 operator"""" _i()

```
constexpr cplx qpp::operator"" _i (
            long double x ) [inline], [noexcept]
```

User-defined literal for complex $i = \sqrt{-1}$ (real overload)

Example:

```
cplx z = 4.5_i; // type of z is std::complex<double>
```

6.1.3.113 powm()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::powm (
            const Eigen::MatrixBase< Derived > & A,
            idx n )
```

Fast matrix power based on the SQUARE-AND-MULTIPLY algorithm.

See also

qpp::spectralpowm()

Explicitly multiplies the matrix *A* with itself *n* times. By convention $A^0 = I$.

Parameters

A	Eigen expression
n	Non-negative integer

Returns

Matrix power A^n, as a dynamic matrix over the same scalar field as *A*

6.1.3.114 prj()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::prj (
            const Eigen::MatrixBase< Derived > & A )
```

Projector.

Normalized projector onto state vector

Parameters

A	Eigen expression

Returns

Projector onto the state vector *A*, or the matrix *Zero* if *A* has norm zero, as a dynamic matrix over the same scalar field as *A*

6.1.3.115 prod() [1/3]

```
template<typename Derived >
Derived::Scalar qpp::prod (
            const Eigen::MatrixBase< Derived > & A )
```

Element-wise product of *A*.

Parameters

A	Eigen expression

Returns

Element-wise product of *A*, as a scalar over the same scalar field as *A*

6.1.3.116 prod() [2/3]

```
template<typename InputIterator >
std::iterator_traits<InputIterator>::value_type qpp::prod (
            InputIterator first,
            InputIterator last )
```

Element-wise product of an STL-like range.

Parameters

first	Iterator to the first element of the range
last	Iterator to the last element of the range

Returns

Element-wise product of the range, as a scalar over the same scalar field as the range

6.1.3.117 prod() [3/3]

```
template<typename Container >
Container::value_type qpp::prod (
            const Container & c,
            typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Element-wise product of the elements of an STL-like container.

Parameters

c	STL-like container

Returns

Element-wise product of the elements of the container, as a scalar over the same scalar field as the container

6.1.3.118 ptrace() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & target,
            const std::vector< idx > & dims )
```

Partial trace.

See also

qpp::ptrace1(), qpp::ptrace2()

Partial trace of the multi-partite state vector or density matrix over the list *target* of subsystems

Parameters

A	Eigen expression
target	Subsystem indexes
dims	Dimensions of the multi-partite system

Returns

Partial trace $Tr_{subsys}(\cdot)$ over the subsytems *target* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.119 ptrace() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & target,
            idx d = 2 )
```

Partial trace.

See also

qpp::ptrace1(), qpp::ptrace2()

Partial trace of the multi-partite state vector or density matrix over the list *target* of subsystems

Parameters

A	Eigen expression
target	Subsystem indexes
d	Subsystem dimensions

Returns

Partial trace $Tr_{subsys}(\cdot)$ over the subsytems *target* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.120 ptrace1() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace1 (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Partial trace.

See also

qpp::ptrace2()

Partial trace over the first subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Partial trace $Tr_A(\cdot)$ over the first subsytem A in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.121 ptrace1() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace1 (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Partial trace.

See also

qpp::ptrace2()

Partial trace over the first subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Partial trace $Tr_A(\cdot)$ over the first subsytem A in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.122 ptrace2() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace2 (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Partial trace.

See also

qpp::ptrace1()

Partial trace over the second subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Partial trace $Tr_B(\cdot)$ over the second subsytem B in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.123 ptrace2() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptrace2 (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Partial trace.

See also

qpp::ptrace1()

Partial trace over the second subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Partial trace $Tr_B(\cdot)$ over the second subsytem B in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as *A*

6.1.3.124 ptranspose() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptranspose (
```

```
const Eigen::MatrixBase< Derived > & A,
const std::vector< idx > & target,
const std::vector< idx > & dims )
```

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over the list *target* of subsystems

Parameters

A	Eigen expression
target	Subsystem indexes
dims	Dimensions of the multi-partite system

Returns

Partial transpose $(\cdot)^{T_{subsys}}$ over the subsytems *target* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.125 ptranspose() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::ptranspose (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & target,
            idx d = 2 )
```

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over the list *target* of subsystems

Parameters

A	Eigen expression
target	Subsystem indexes
d	Subsystem dimensions

Returns

Partial transpose $(\cdot)^{T_{subsys}}$ over the subsytems *target* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.126 QFT()

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::QFT (
```

```
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2,
            bool swap = true )
```

Qudit quantum Fourier transform.

Parameters

A	Eigen expression
d	Subsystem dimensions
swap	Swaps the qubits/qudits at the end (true by default)

Returns

Qudit quantum Fourier transform applied on *A*

6.1.3.127 qmutualinfo() [1/2]

```
template<typename Derived >
double qpp::qmutualinfo (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsysA,
            const std::vector< idx > & subsysB,
            const std::vector< idx > & dims )
```

Quantum mutual information between 2 subsystems of a composite system.

Parameters

A	Eigen expression
subsysA	Indexes of the first subsystem
subsysB	Indexes of the second subsystem
dims	Dimensions of the multi-partite system

Returns

Mutual information between the 2 subsystems

6.1.3.128 qmutualinfo() [2/2]

```
template<typename Derived >
double qpp::qmutualinfo (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & subsysA,
            const std::vector< idx > & subsysB,
            idx d = 2 )
```

Quantum mutual information between 2 subsystems of a composite system.

Parameters

A	Eigen expression
subsysA	Indexes of the first subsystem
subsysB	Indexes of the second subsystem
d	Subsystem dimensions

Returns

Mutual information between the 2 subsystems

6.1.3.129 rand() [1/5]

```
double qpp::rand (
            double a,
            double b )  [inline]
```

Generates a random real number uniformly distributed in the interval [a, b)

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

Returns

Random real number (double) uniformly distributed in the interval [a, b)

6.1.3.130 rand() [2/5]

```
bigint qpp::rand (
            bigint a,
            bigint b )  [inline]
```

Generates a random big integer uniformly distributed in the interval [a, b].

Note

To avoid ambiguity with double qpp::rand(double, double) cast at least one of the arguments to qpp::bigint

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, belongs to it

Returns

Random big integer uniformly distributed in the interval [a, b]

6.1.3.131 rand() [3/5]

```
template<typename Derived >
Derived qpp::rand (
            idx rows QPP_UNUSED_,
            idx cols QPP_UNUSED_,
            double a QPP_UNUSED_ = 0,
            double b QPP_UNUSED_ = 1 )
```

Generates a random matrix with entries uniformly distributed in the interval [a, b)

If complex, then both real and imaginary parts are uniformly distributed in [a, b)

This is the generic version that always throws qpp::Exception::Type::UNDEFINED_TYPE. It is specialized only for qpp::dmat and qpp::cmat

6.1.3.132 rand() [4/5]

```
template<>
dmat qpp::rand (
            idx rows ,
            idx cols ,
            double a ,
            double b ) [inline]
```

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries uniformly distributed in [-1,1)
dmat mat = rand<dmat>(3, 3, -1, 1);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
a	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

Returns

Random real matrix

6.1.3.133 rand() [5/5]

```
template<>
cmat qpp::rand (
            idx rows ,
            idx cols ,
            double a ,
            double b )  [inline]
```

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) uniformly distributed in [-1,1)
cmat mat = rand<cmat>(3, 3, -1, 1);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
a	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

Returns

Random complex matrix

6.1.3.134 randH()

```
cmat qpp::randH (
            idx D = 2 )  [inline]
```

Generates a random Hermitian matrix.

Parameters

D	Dimension of the Hilbert space

Returns

Random Hermitian matrix

6.1.3.135 randidx()

```
idx qpp::randidx (
            idx a = std::numeric_limits<idx>::min(),
            idx b = std::numeric_limits<idx>::max() )  [inline]
```

Generates a random index (idx) uniformly distributed in the interval [a, b].

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, belongs to it

Returns

Random index (idx) uniformly distributed in the interval [a, b]

6.1.3.136 randket()

```
ket qpp::randket (
            idx D = 2 )  [inline]
```

Generates a random normalized ket (pure state vector)

Parameters

D	Dimension of the Hilbert space

Returns

Random normalized ket

6.1.3.137 randkraus()

```
std::vector<cmat> qpp::randkraus (
            idx N,
            idx D = 2 )  [inline]
```

Generates a set of random Kraus operators.

Note

The set of Kraus operators satisfy the closure condition $\sum_i K_i^\dagger K_i = I$

Parameters

N	Number of Kraus operators
D	Dimension of the Hilbert space

Returns

Set of *N* Kraus operators satisfying the closure condition

6.1.3.138 randn() [1/4]

```
template<typename Derived >
Derived qpp::randn (
            idx rows QPP_UNUSED_,
            idx cols QPP_UNUSED_,
            double mean QPP_UNUSED_ = 0,
            double sigma QPP_UNUSED_ = 1 )
```

Generates a random matrix with entries normally distributed in N(mean, sigma)

If complex, then both real and imaginary parts are normally distributed in N(mean, sigma)

This is the generic version that always throws qpp::Exception::Type::UNDEFINED_TYPE. It is specialized only for qpp::dmat and qpp::cmat

6.1.3.139 randn() [2/4]

```
template<>
dmat qpp::randn (
            idx rows ,
            idx cols ,
            double mean ,
            double sigma ) [inline]
```

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries normally distributed in N(0,2)
dmat mat = randn<dmat>(3, 3, 0, 2);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
mean	Mean
sigma	Standard deviation

Returns

Random real matrix

6.1.3.140 randn() [3/4]

```
template<>
cmat qpp::randn (
            idx rows ,
            idx cols ,
            double mean ,
            double sigma  )  [inline]
```

Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) normally distributed in N(0,2)
cmat mat = randn<cmat>(3, 3, 0, 2);
```

Parameters

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
mean	Mean
sigma	Standard deviation

Returns

Random complex matrix

6.1.3.141 randn() [4/4]

```
double qpp::randn (
            double mean = 0,
            double sigma = 1 )  [inline]
```

Generates a random real number (double) normally distributed in N(mean, sigma)

Parameters

mean	Mean
sigma	Standard deviation

Returns

Random real number normally distributed in N(mean, sigma)

6.1.3.142 randperm()

```
std::vector<idx> qpp::randperm (
            idx N )  [inline]
```

Generates a random uniformly distributed permutation.

Uses Knuth shuffle method (as implemented by std::shuffle), so that all permutations are equally probable

Parameters

N	Size of the permutation

Returns

Random permutation of size *N*

6.1.3.143 randprime()

```
bigint qpp::randprime (
            bigint a,
            bigint b,
            idx N = 1000 )  [inline]
```

Generates a random big prime uniformly distributed in the interval [a, b].

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, belongs to it
N	Maximum number of candidates

Returns

Random big integer uniformly distributed in the interval [a, b]

6.1.3.144 randprob()

```
std::vector<double> qpp::randprob (
            idx N )  [inline]
```

Generates a random probability vector uniformly distributed over the probability simplex.

Parameters

N	Size of the probability vector

Returns

Random probability vector

6.1.3.145 randrho()

```
cmat qpp::randrho (
            idx D = 2 )  [inline]
```

Generates a random density matrix.

Parameters

D	Dimension of the Hilbert space

Returns

Random density matrix

6.1.3.146 randU()

```
cmat qpp::randU (
            idx D = 2 )  [inline]
```

Generates a random unitary matrix.

Parameters

D	Dimension of the Hilbert space

Returns

Random unitary

6.1.3.147 randV()

```
cmat qpp::randV (
            idx Din,
            idx Dout ) [inline]
```

Generates a random isometry matrix.

Parameters

Din	Size of the input Hilbert space
Dout	Size of the output Hilbert space

Returns

Random isometry matrix

6.1.3.148 renyi() [1/2]

```
template<typename Derived >
double qpp::renyi (
            const Eigen::MatrixBase< Derived > & A,
            double alpha )
```

Renyi- α entropy of the density matrix *A*, for $\alpha \geq 0$.

Note

When $\alpha \rightarrow 1$ the Renyi entropy converges to the von-Neumann entropy, with the logarithm in base 2

Parameters

A	Eigen expression
alpha	Non-negative real number, use qpp::infty for $\alpha = \infty$

Returns

Renyi- α entropy, with the logarithm in base 2

6.1.3.149 renyi() [2/2]

```
double qpp::renyi (
            const std::vector< double > & prob,
            double alpha ) [inline]
```

Renyi- α entropy of the probability distribution *prob*, for $\alpha \geq 0$.

Note

When $\alpha \to 1$ the Renyi entropy converges to the Shannon entropy, with the logarithm in base 2

Parameters

prob	Real probability vector
alpha	Non-negative real number, use qpp::infty for $\alpha = \infty$

Returns

Renyi- α entropy, with the logarithm in base 2

6.1.3.150 reshape()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::reshape (
            const Eigen::MatrixBase< Derived > & A,
            idx rows,
            idx cols )
```

Reshape.

Uses column-major order when reshaping (same as MATLAB)

Parameters

A	Eigen expression
rows	Number of rows of the reshaped matrix
cols	Number of columns of the reshaped matrix

Returns

Reshaped matrix with *rows* rows and *cols* columns, as a dynamic matrix over the same scalar field as *A*

6.1.3.151 rho2bloch()

```
template<typename Derived >
std::vector<double> qpp::rho2bloch (
            const Eigen::MatrixBase< Derived > & A )
```

Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix *A*.

See also

qpp::bloch2rho()

Note

It is implicitly assumed that the density matrix is Hermitian

Parameters

A	Eigen expression

Returns

3-dimensional Bloch vector

6.1.3.152 rho2pure()

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::rho2pure (
            const Eigen::MatrixBase< Derived > & A )
```

Finds the pure state representation of a matrix proportional to a projector onto a pure state.

Note

No purity check is done, the input state *A* must have rank one, otherwise the function returns the first non-zero eigenvector of *A*

Parameters

A	Eigen expression, assumed to be proportional to a projector onto a pure state, i.e. *A* is assumed to have rank one

Returns

The unique non-zero eigenvector of *A* (up to a phase), as a dynamic column vector over the same scalar field as *A*

6.1.3.153 save()

```
template<typename Derived >
void qpp::save (
            const Eigen::MatrixBase< Derived > & A,
            const std::string & fname )
```

Saves Eigen expression to a binary file (internal format) in double precision.

See also

qpp::load()

Parameters

A	Eigen expression
fname	Output file name

6.1.3.154 saveMATLAB() [1/2]

```
template<typename Derived >
std::enable_if< std::is_same<typename Derived::Scalar, cplx>::value>::type qpp::saveMATLAB (
            const Eigen::MatrixBase< Derived > & A,
            const std::string & mat_file,
            const std::string & var_name,
            const std::string & mode )
```

Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.

See also

qpp::loadMATLAB()

Template Parameters

Complex	Eigen type

Parameters

A	Eigen expression over the complex field

Parameters

mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be saved
mode	Saving mode (append, overwrite etc.), see MATLAB *matOpen()* documentation for details

6.1.3.155 saveMATLAB() [2/2]

```
template<typename Derived >
std::enable_if< !std::is_same<typename Derived::Scalar, cplx>::value>::type qpp::saveMATLAB (
            const Eigen::MatrixBase< Derived > & A,
            const std::string & mat_file,
            const std::string & var_name,
            const std::string & mode )
```

Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.

See also

qpp::loadMATLAB()

Template Parameters

Npn-complex	Eigen type

Parameters

A	Non-complex Eigen expression
mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be saved
mode	Saving mode (append, overwrite etc.), see MATLAB *matOpen()* documentation for details

6.1.3.156 schatten()

```
template<typename Derived >
double qpp::schatten (
            const Eigen::MatrixBase< Derived > & A,
            double p )
```

Schatten matrix norm.

Parameters

A	Eigen expression
p	Real number, greater or equal to 1, use qpp::infty for $p = \infty$

Returns

Schatten-*p* matrix norm of *A*

6.1.3.157 schmidtA() [1/2]

```
template<typename Derived >
cmat qpp::schmidtA (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Schmidt basis on Alice side.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Unitary matrix U whose columns represent the Schmidt basis vectors on Alice side.

6.1.3.158 schmidtA() [2/2]

```
template<typename Derived >
cmat qpp::schmidtA (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Schmidt basis on Alice side.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Unitary matrix U whose columns represent the Schmidt basis vectors on Alice side.

6.1.3.159 schmidtB() [1/2]

```
template<typename Derived >
cmat qpp::schmidtB (
```

```
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Schmidt basis on Bob side.

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Unitary matrix V whose columns represent the Schmidt basis vectors on Bob side.

6.1.3.160 schmidtB() [2/2]

```
template<typename Derived >
cmat qpp::schmidtB (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Schmidt basis on Bob side.

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Unitary matrix V whose columns represent the Schmidt basis vectors on Bob side.

6.1.3.161 schmidtcoeffs() [1/2]

```
template<typename Derived >
dyn_col_vect<double> qpp::schmidtcoeffs (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Schmidt coefficients of the bi-partite pure state *A*.

Note

The sum of the squares of the Schmidt coefficients equals 1

See also

qpp::schmidtprobs()

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Schmidt coefficients of *A*, ordered in decreasing order, as a real dynamic column vector

6.1.3.162 schmidtcoeffs() [2/2]

```
template<typename Derived >
dyn_col_vect<double> qpp::schmidtcoeffs (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Schmidt coefficients of the bi-partite pure state *A*.

Note

The sum of the squares of the Schmidt coefficients equals 1

See also

qpp::schmidtprobs()

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Schmidt coefficients of *A*, ordered in decreasing order, as a real dynamic column vector

6.1.3.163 schmidtprobs() [1/2]

```
template<typename Derived >
std::vector<double> qpp::schmidtprobs (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & dims )
```

Schmidt probabilities of the bi-partite pure state *A*.

Defined as the squares of the Schmidt coefficients. The sum of the Schmidt probabilities equals 1.

See also

qpp::schmidtcoeffs()

Parameters

A	Eigen expression
dims	Dimensions of the bi-partite system

Returns

Real vector consisting of the Schmidt probabilites of *A*, ordered in decreasing order

6.1.3.164 schmidtprobs() [2/2]

```
template<typename Derived >
std::vector<double> qpp::schmidtprobs (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2 )
```

Schmidt probabilities of the bi-partite pure state *A*.

Defined as the squares of the Schmidt coefficients. The sum of the Schmidt probabilities equals 1.

See also

qpp::schmidtcoeffs()

Parameters

A	Eigen expression
d	Subsystem dimensions

Returns

Real vector consisting of the Schmidt probabilites of *A*, ordered in decreasing order

6.1.3.165 sigma()

```
template<typename Container >
double qpp::sigma (
            const std::vector< double > & prob,
            const Container & X,
            typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Standard deviation.

Parameters

prob	Real probability vector representing the probability distribution of *X*
X	Real random variable values represented by an STL-like container

Returns

Standard deviation of *X*

6.1.3.166 sinm()

```
template<typename Derived >
cmat qpp::sinm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix sin.

Parameters

A	Eigen expression

Returns

Matrix sine of *A*

6.1.3.167 spectralpowm()

```
template<typename Derived >
cmat qpp::spectralpowm (
            const Eigen::MatrixBase< Derived > & A,
            const cplx z )
```

Matrix power.

See also

qpp::powm()

Uses the spectral decomposition of *A* to compute the matrix power. By convention $A^0 = I$.

Parameters

A	Eigen expression
z	Complex number

Returns

Matrix power A^z

6.1.3.168 sqrtm()

```
template<typename Derived >
cmat qpp::sqrtm (
            const Eigen::MatrixBase< Derived > & A )
```

Matrix square root.

Parameters

A	Eigen expression

Returns

Matrix square root of *A*

6.1.3.169 sum() [1/3]

```
template<typename Derived >
Derived::Scalar qpp::sum (
            const Eigen::MatrixBase< Derived > & A )
```

Element-wise sum of *A*.

Parameters

A	Eigen expression

Returns

Element-wise sum of *A*, as a scalar over the same scalar field as *A*

6.1.3.170 sum() [2/3]

```
template<typename InputIterator >
std::iterator_traits<InputIterator>::value_type qpp::sum (
            InputIterator first,
            InputIterator last )
```

Element-wise sum of an STL-like range.

Parameters

first	Iterator to the first element of the range
last	Iterator to the last element of the range

Returns

Element-wise sum of the range, as a scalar over the same scalar field as the range

6.1.3.171 sum() [3/3]

```
template<typename Container >
Container::value_type qpp::sum (
            const Container & c,
            typename std::enable_if< is_iterable< Container >::value >::type *  = nullptr )
```

Element-wise sum of the elements of an STL-like container.

Parameters

c	STL-like container

Returns

Element-wise sum of the elements of the container, as a scalar over the same scalar field as the container

6.1.3.172 super2choi()

```
cmat qpp::super2choi (
            const cmat & A )  [inline]
```

Converts superoperator matrix to Choi matrix.

See also

qpp::choi2super()

Parameters

A	Superoperator matrix

Returns

Choi matrix

6.1.3.173 svals()

```
template<typename Derived >
dyn_col_vect<double> qpp::svals (
            const Eigen::MatrixBase< Derived > & A )
```

Singular values.

Parameters

A	Eigen expression

Returns

Singular values of *A*, ordered in decreasing order, as a real dynamic column vector

6.1.3.174 svd()

```
template<typename Derived >
std::tuple<cmat, dyn_col_vect<double>, cmat> qpp::svd (
            const Eigen::MatrixBase< Derived > & A )
```

Full singular value decomposition.

Parameters

A	Eigen expression

Returns

Tuple of: 1. Left sigular vectors of *A*, as columns of a complex dynamic matrix, 2. Singular values of *A*, ordered in decreasing order, as a real dynamic column vector, and 3. Right singular vectors of *A*, as columns of a complex dynamic matrix

6.1.3.175 svdU()

```
template<typename Derived >
cmat qpp::svdU (
            const Eigen::MatrixBase< Derived > & A )
```

Left singular vectors.

Parameters

A	Eigen expression

Returns

Complex dynamic matrix, whose columns are the left singular vectors of *A*

6.1.3.176 svdV()

```
template<typename Derived >
cmat qpp::svdV (
            const Eigen::MatrixBase< Derived > & A )
```

Right singular vectors.

Parameters

A	Eigen expression

Returns

Complex dynamic matrix, whose columns are the right singular vectors of *A*

6.1.3.177 syspermute() [1/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::syspermute (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & perm,
            const std::vector< idx > & dims )
```

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit *perm*[*i*] is permuted to the location *i*.

Parameters

A	Eigen expression
perm	Permutation
dims	Dimensions of the multi-partite system

Returns

Permuted system, as a dynamic matrix over the same scalar field as *A*

6.1.3.178 syspermute() [2/2]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::syspermute (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & perm,
            idx d = 2 )
```

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit *perm*[*i*] is permuted to the location *i*.

Parameters

A	Eigen expression
perm	Permutation
d	Subsystem dimensions

Returns

Permuted system, as a dynamic matrix over the same scalar field as *A*

6.1.3.179 TFQ()

```
template<typename Derived >
dyn_col_vect<typename Derived::Scalar> qpp::TFQ (
            const Eigen::MatrixBase< Derived > & A,
            idx d = 2,
            bool swap = true )
```

Inverse (adjoint) qudit quantum Fourier transform.

Parameters

A	Eigen expression
d	Subsystem dimensions
swap	Swaps the qubits/qudits at the end (true by default)

Returns

Inverse (adjoint) qudit quantum Fourier transform applied on *A*

6.1.3.180 trace()

```
template<typename Derived >
Derived::Scalar qpp::trace (
            const Eigen::MatrixBase< Derived > & A )
```

Trace.

Parameters

A	Eigen expression

Returns

Trace of *A*, as a scalar over the same scalar field as *A*

6.1.3.181 transpose()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::transpose (
            const Eigen::MatrixBase< Derived > & A )
```

Transpose.

Parameters

A	Eigen expression

Returns

Transpose of *A*, as a dynamic matrix over the same scalar field as *A*

6.1.3.182 tsallis() [1/2]

```
template<typename Derived >
double qpp::tsallis (
            const Eigen::MatrixBase< Derived > & A,
            double q )
```

Tsallis- q entropy of the density matrix *A*, for $q \geq 0$.

Note

When $q \to 1$ the Tsallis entropy converges to the von-Neumann entropy, with the logarithm in base e

Parameters

A	Eigen expression
q	Non-negative real number

Returns

Tsallis- q entropy

6.1.3.183 tsallis() [2/2]

```
double qpp::tsallis (
            const std::vector< double > & prob,
            double q ) [inline]
```

Tsallis- q entropy of the probability distribution *prob*, for $q \geq 0$.

Note

When $q \to 1$ the Tsallis entropy converges to the Shannon entropy, with the logarithm in base e

Parameters

prob	Real probability vector
q	Non-negative real number

Returns

Tsallis- q entropy

6.1.3.184 uniform()

```
std::vector<double> qpp::uniform (
            idx N ) [inline]
```

Uniform probability distribution vector.

Parameters

N	Size of the alphabet

Returns

Real vector consisting of a uniform distribution of size *N*

6.1.3.185 var()

```
template<typename Container >
double qpp::var (
            const std::vector< double > & prob,
            const Container & X,
            typename std::enable_if< is_iterable< Container >::value >::type * = nullptr )
```

Variance.

Parameters

prob	Real probability vector representing the probability distribution of *X*
X	Real random variable values represented by an STL-like container

Returns

Variance of *X*

6.1.3.186 x2contfrac()

```
std::vector<int> qpp::x2contfrac (
            double x,
            idx N,
            idx cut = 1e5 ) [inline]
```

Simple continued fraction expansion.

See also

qpp::contfrac2x()

Parameters

x	Real number
N	Maximum number of terms in the expansion
cut	Stop the expansion when the next term is greater than *cut*

Returns

Integer vector containing the simple continued fraction expansion of *x*. If there are *M* less than *N* terms in the expansion, a shorter vector with *M* components is returned.

6.1.4 Variable Documentation

6.1.4.1 chop

```
constexpr double qpp::chop = 1e-10
```

Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.

6.1.4.2 ee

```
constexpr double qpp::ee = 2.718281828459045235360287471352662497
```

Base of natural logarithm, e.

6.1.4.3 infty

```
constexpr double qpp::infty = std::numeric_limits<double>::max()
```

Used to denote infinity in double precision.

6.1.4.4 maxn

```
constexpr idx qpp::maxn = 64
```

Maximum number of allowed qubits/qudits (subsystems)

Used internally to allocate arrays on the stack (for performance reasons):

6.1.4.5 pi

```
constexpr double qpp::pi = 3.141592653589793238462643383279502884
```

π

6.2 qpp::exception Namespace Reference

Quantum++ exception hierarchy namespace.

Classes

- class CustomException

  Custom exception.
- class DimsInvalid

  Invalid dimension(s) exception.
- class DimsMismatchCvector

  Dimension(s) mismatch column vector size exception.
- class DimsMismatchMatrix

  Dimension(s) mismatch matrix size exception.
- class DimsMismatchRvector

  Dimension(s) mismatch row vector size exception.
- class DimsMismatchVector

  Dimension(s) mismatch vector size exception.
- class DimsNotEqual

  Dimensions not equal exception.
- class Duplicates

  System (e.g. std::vector) has duplicates exception.
- class Exception

  Base class for generating Quantum++ custom exceptions.
- class InvalidIterator

  Invalid iterator.
- class MatrixMismatchSubsys

  Matrix mismatch subsystems exception.
- class MatrixNotCvector

  Matrix is not a column vector exception.
- class MatrixNotRvector

  Matrix is not a row vector exception.
- class MatrixNotSquare

  Matrix is not square exception.
- class MatrixNotSquareNorCvector

  Matrix is not square nor column vector exception.
- class MatrixNotSquareNorRvector

  Matrix is not square nor row vector exception.
- class MatrixNotSquareNorVector

  Matrix is not square nor vector exception.
- class MatrixNotVector

  Matrix is not a vector exception.
- class NoCodeword

  Codeword does not exist exception.
- class NotBipartite

  Not bi-partite exception.
- class NotImplemented

  Code not yet implemented.
- class NotQubitCvector

  Column vector is not 2 x 1 exception.
- class NotQubitMatrix

  Matrix is not 2 x 2 exception.
- class NotQubitRvector

  Row vector is not 1 x 2 exception.
- class NotQubitSubsys

Subsystems are not qubits exception.
- class NotQubitVector

  Vector is not 2 x 1 nor 1 x 2 exception.
- class OutOfRange

  Argument out of range exception.
- class PermInvalid

  Invalid permutation exception.
- class PermMismatchDims

  Permutation mismatch dimensions exception.
- class QuditAlreadyMeasured

  Qudit was already measured exception.
- class SizeMismatch

  Size mismatch exception.
- class SubsysMismatchDims

  Subsystems mismatch dimensions exception.
- class TypeMismatch

  Type mismatch exception.
- class UndefinedType

  Not defined for this type exception.
- class Unknown

  Unknown exception.
- class ZeroSize

  Object has zero size exception.

6.2.1 Detailed Description

Quantum++ exception hierarchy namespace.

6.3 qpp::experimental Namespace Reference

Experimental/test functions/classes, do not use or modify.

6.3.1 Detailed Description

Experimental/test functions/classes, do not use or modify.

6.4 qpp::internal Namespace Reference

Internal utility functions, do not use them directly or modify them.

Classes

- struct Display_Impl_
- class EqualEigen

  Functor for comparing Eigen expressions for equality.
- class HashEigen

  Functor for hashing Eigen expressions.
- class IOManipEigen
- class IOManipPointer
- class IOManipRange
- class Singleton

  Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

Functions

- template< class T >
  void hash_combine (std::size_t &seed, const T &v)
- void n2multiidx (idx n, idx numdims, const idx ∗const dims, idx ∗result) noexcept
- idx multiidx2n (const idx ∗const midx, idx numdims, const idx ∗const dims) noexcept
- template< typename Derived >
  bool check_square_mat (const Eigen::MatrixBase< Derived > &A)
- template< typename Derived >
  bool check_vector (const Eigen::MatrixBase< Derived > &A)
- template< typename Derived >
  bool check_rvector (const Eigen::MatrixBase< Derived > &A)
- template< typename Derived >
  bool check_cvector (const Eigen::MatrixBase< Derived > &A)
- template< typename T >
  bool check_nonzero_size (const T &x) noexcept
- template< typename T1 , typename T2 >
  bool check_matching_sizes (const T1 &lhs, const T2 &rhs) noexcept
- bool check_dims (const std::vector< idx > &dims)
- template< typename Derived >
  bool check_dims_match_mat (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template< typename Derived >
  bool check_dims_match_cvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template< typename Derived >
  bool check_dims_match_rvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- bool check_eq_dims (const std::vector< idx > &dims, idx dim) noexcept
- bool check_no_duplicates (std::vector< idx > v)
- bool check_subsys_match_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)
- template< typename Derived >
  bool check_qubit_matrix (const Eigen::MatrixBase< Derived > &A) noexcept
- template< typename Derived >
  bool check_qubit_cvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template< typename Derived >
  bool check_qubit_rvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template< typename Derived >
  bool check_qubit_vector (const Eigen::MatrixBase< Derived > &A) noexcept
- bool check_perm (const std::vector< idx > &perm)
- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::↩
  MatrixBase< Derived2 > &B)

- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > dirsum2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename T >
  void variadic_vector_emplace (std::vector< T > &)
- template<typename T , typename First , typename... Args>
  void variadic_vector_emplace (std::vector< T > &v, First &&first, Args &&... args)
- idx get_num_subsys (idx D, idx d)
- idx get_dim_subsys (idx sz, idx N)

6.4.1 Detailed Description

Internal utility functions, do not use them directly or modify them.

6.4.2 Function Documentation

6.4.2.1 check_cvector()

```
template<typename Derived >
bool qpp::internal::check_cvector (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.2 check_dims()

```
bool qpp::internal::check_dims (
            const std::vector< idx > & dims )  [inline]
```

6.4.2.3 check_dims_match_cvect()

```
template<typename Derived >
bool qpp::internal::check_dims_match_cvect (
            const std::vector< idx > & dims,
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.4 check_dims_match_mat()

```
template<typename Derived >
bool qpp::internal::check_dims_match_mat (
            const std::vector< idx > & dims,
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.5 check_dims_match_rvect()

```
template<typename Derived >
bool qpp::internal::check_dims_match_rvect (
            const std::vector< idx > & dims,
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.6 check_eq_dims()

```
bool qpp::internal::check_eq_dims (
            const std::vector< idx > & dims,
            idx dim )  [inline], [noexcept]
```

6.4.2.7 check_matching_sizes()

```
template<typename T1 , typename T2 >
bool qpp::internal::check_matching_sizes (
            const T1 & lhs,
            const T2 & rhs )  [noexcept]
```

6.4.2.8 check_no_duplicates()

```
bool qpp::internal::check_no_duplicates (
            std::vector< idx > v )  [inline]
```

6.4.2.9 check_nonzero_size()

```
template<typename T >
bool qpp::internal::check_nonzero_size (
            const T & x )  [noexcept]
```

6.4.2.10 check_perm()

```
bool qpp::internal::check_perm (
            const std::vector< idx > & perm )  [inline]
```

6.4.2.11 check_qubit_cvector()

```
template<typename Derived >
bool qpp::internal::check_qubit_cvector (
            const Eigen::MatrixBase< Derived > & A )  [noexcept]
```

6.4.2.12 check_qubit_matrix()

```
template<typename Derived >
bool qpp::internal::check_qubit_matrix (
            const Eigen::MatrixBase< Derived > & A )  [noexcept]
```

6.4.2.13 check_qubit_rvector()

```
template<typename Derived >
bool qpp::internal::check_qubit_rvector (
            const Eigen::MatrixBase< Derived > & A )  [noexcept]
```

6.4.2.14 check_qubit_vector()

```
template<typename Derived >
bool qpp::internal::check_qubit_vector (
            const Eigen::MatrixBase< Derived > & A )  [noexcept]
```

6.4.2.15 check_rvector()

```
template<typename Derived >
bool qpp::internal::check_rvector (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.16 check_square_mat()

```
template<typename Derived >
bool qpp::internal::check_square_mat (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.17 check_subsys_match_dims()

```
bool qpp::internal::check_subsys_match_dims (
            const std::vector< idx > & subsys,
            const std::vector< idx > & dims )  [inline]
```

6.4.2.18 check_vector()

```
template<typename Derived >
bool qpp::internal::check_vector (
            const Eigen::MatrixBase< Derived > & A )
```

6.4.2.19 dirsum2()

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::internal::dirsum2 (
            const Eigen::MatrixBase< Derived1 > & A,
            const Eigen::MatrixBase< Derived2 > & B )
```

6.4.2.20 get_dim_subsys()

```
idx qpp::internal::get_dim_subsys (
            idx sz,
            idx N )  [inline]
```

6.4.2.21 get_num_subsys()

```
idx qpp::internal::get_num_subsys (
            idx D,
            idx d )  [inline]
```

6.4.2.22 hash_combine()

```
template<class T >
void qpp::internal::hash_combine (
            std::size_t & seed,
            const T & v )
```

6.4.2.23 kron2()

```
template<typename Derived1 , typename Derived2 >
dyn_mat<typename Derived1::Scalar> qpp::internal::kron2 (
            const Eigen::MatrixBase< Derived1 > & A,
            const Eigen::MatrixBase< Derived2 > & B )
```

6.4.2.24 multiidx2n()

```
idx qpp::internal::multiidx2n (
            const idx *const midx,
            idx numdims,
            const idx *const dims ) [inline], [noexcept]
```

6.4.2.25 n2multiidx()

```
void qpp::internal::n2multiidx (
            idx n,
            idx numdims,
            const idx *const dims,
            idx * result ) [inline], [noexcept]
```

6.4.2.26 variadic_vector_emplace() [1/2]

```
template<typename T >
void qpp::internal::variadic_vector_emplace (
            std::vector< T > & )
```

6.4.2.27 variadic_vector_emplace() [2/2]

```
template<typename T , typename First , typename... Args>
void qpp::internal::variadic_vector_emplace (
            std::vector< T > & v,
            First && first,
            Args &&... args )
```

6.5 qpp::literals Namespace Reference

Functions

- constexpr cplx operator"" _i (unsigned long long int x) noexcept

  User-defined literal for complex $i = \sqrt{-1}$ (integer overload)
- template<char... Bits>
  ket operator"" _ket ()

  Multi-partite qubit ket user-defined literal.
- template<char... Bits>
  bra operator"" _bra ()

  Multi-partite qubit bra user-defined literal.
- template<char... Bits>
  cmat operator"" _prj ()

  Multi-partite qubit projector user-defined literal.

6.5.1 Function Documentation

6.5.1.1 operator"""" _bra()

```
template<char... Bits>
bra qpp::literals::operator"" _bra ( )
```

Multi-partite qubit bra user-defined literal.

See also

qpp::mket() and qpp::adjoint()

Constructs the multi-partite qubit bra $\langle \mathrm{Bits} |$

Template Parameters

Bits	String of binary numbers representing the qubit bra

Returns

Multi-partite qubit bra, as a complex dynamic row vector

6.5.1.2 operator"""" _i()

```
constexpr cplx qpp::literals::operator"" _i (
            unsigned long long int x )  [inline], [noexcept]
```

User-defined literal for complex $i = \sqrt{-1}$ (integer overload)

Example:

```
cplx z = 4_i; // type of z is std::complex<double>
```

6.5.1.3 operator"""" _ket()

```
template<char... Bits>
ket qpp::literals::operator"" _ket ( )
```

Multi-partite qubit ket user-defined literal.

See also

qpp::mket()

Constructs the multi-partite qubit ket $|\mathrm{Bits}\rangle$

Template Parameters

Bits	String of binary numbers representing the qubit ket

Returns

Multi-partite qubit ket, as a complex dynamic column vector

6.5.1.4 operator"""" _prj()

```
template<char... Bits>
cmat qpp::literals::operator"" _prj ( )
```

Multi-partite qubit projector user-defined literal.

See also

qpp::mprj()

Constructs the multi-partite qubit projector $|\mathrm{Bits}\rangle\langle\mathrm{Bits}|$ (in the computational basis)

Template Parameters

Bits	String of binary numbers representing the qubit state to project on

Returns

Multi-partite qubit projector, as a complex dynamic matrix

Chapter 7

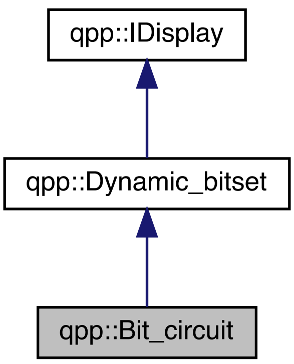
Class Documentation

7.1 qpp::Bit_circuit Class Reference

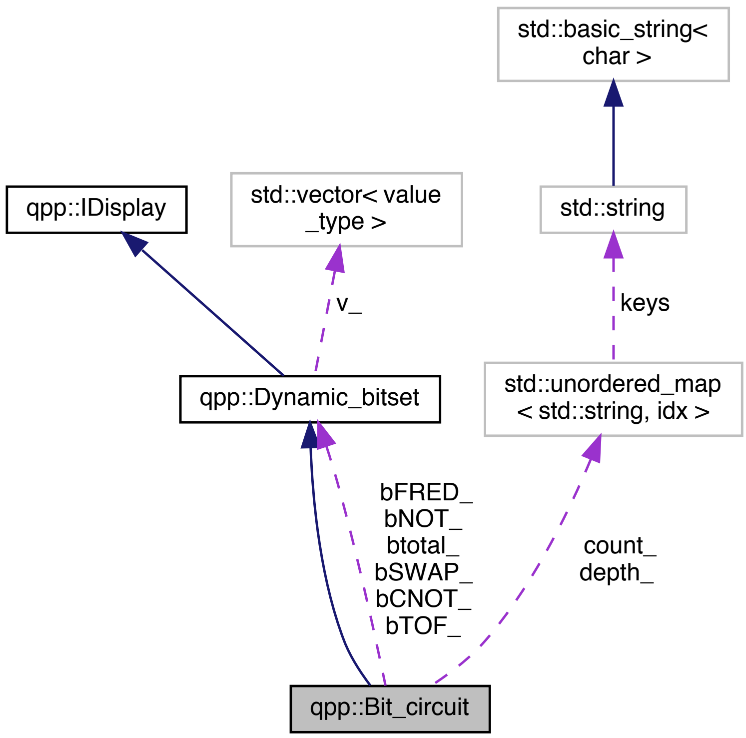
Classical reversible circuit simulator.

```
#include <classes/reversible.h>
```

Inheritance diagram for qpp::Bit_circuit:



Collaboration diagram for qpp::Bit_circuit:



Public Member Functions

- Bit_circuit (idx n)

    Constructs a bit circuit instance.
- Bit_circuit (const Dynamic_bitset &dynamic_bitset)

    Conversion constructor, used to initialize a qpp::Bit_circuit with a qpp::Dynamic_bitset.
- Bit_circuit & X (idx i)

    Bit flip.
- virtual ∼Bit_circuit ()=default

    Default virtual destructor.
- Bit_circuit & NOT (idx i)

    Bit flip.
- Bit_circuit & CNOT (idx ctrl, idx target)

    Controlled-NOT.
- Bit_circuit & TOF (idx i, idx j, idx k)

    Toffoli gate.
- Bit_circuit & SWAP (idx i, idx j)

    Swap bits.
- Bit_circuit & FRED (idx i, idx j, idx k)

    Fredkin gate (Controlled-SWAP)
- Bit_circuit & reset () noexcept

Reset the circuit all zero, clear all gates.
- idx get_gate_count (const std::string &name={}) const

    Bit circuit gate count.
- idx get_gate_depth (const std::string &name={}) const

    Bit circuit gate depth.

Private Attributes

- std::unordered_map< std::string, idx > count_ {}

    gate counts
- std::unordered_map< std::string, idx > depth_ {}

    gate depths
- Dynamic_bitset bNOT_
- Dynamic_bitset bCNOT_
- Dynamic_bitset bSWAP_
- Dynamic_bitset bTOF_
- Dynamic_bitset bFRED_
- Dynamic_bitset btotal_

    used for depth calculations

Additional Inherited Members

7.1.1 Detailed Description

Classical reversible circuit simulator.

7.1.2 Constructor & Destructor Documentation

7.1.2.1 Bit_circuit() [1/2]

```
qpp::Bit_circuit::Bit_circuit (
            idx n )  [inline], [explicit]
```

Constructs a bit circuit instance.

Parameters

n	Number of classical bits

7.1.2.2 Bit_circuit() [2/2]

```
qpp::Bit_circuit::Bit_circuit (
            const Dynamic_bitset & dynamic_bitset )  [inline], [explicit]
```

Conversion constructor, used to initialize a qpp::Bit_circuit with a qpp::Dynamic_bitset.

Parameters

dynamic_bitset	Dynamic bitset

7.1.2.3 ∼Bit_circuit()

```
virtual qpp::Bit_circuit::∼Bit_circuit ( ) [virtual], [default]
```

Default virtual destructor.

7.1.3 Member Function Documentation

7.1.3.1 CNOT()

```
Bit_circuit& qpp::Bit_circuit::CNOT (
            idx ctrl,
            idx target ) [inline]
```

Controlled-NOT.

Parameters

ctrl	Control bit index
target	Target bit index

Returns

Reference to the current instance

7.1.3.2 FRED()

```
Bit_circuit& qpp::Bit_circuit::FRED (
            idx i,
            idx j,
            idx k ) [inline]
```

Fredkin gate (Controlled-SWAP)

Parameters

i	Control bit index
j	Target first bit index
k	Target second bit index

Returns

Reference to the current instance

7.1.3.3 get_gate_count()

```
idx qpp::Bit_circuit::get_gate_count (
            const std::string & name = {} ) const  [inline]
```

Bit circuit gate count.

Note

If *name* is empty (default), returns the total gate count of the circuit

Parameters

name	Gate name (optional). Possible names are NOT (X), CNOT, SWAP, TOF, FRED.

Returns

Gate count

7.1.3.4 get_gate_depth()

```
idx qpp::Bit_circuit::get_gate_depth (
            const std::string & name = {} ) const  [inline]
```

Bit circuit gate depth.

Note

If *name* is empty (default), returns the total gate depth of the circuit

Parameters

name	Gate name (optional). Possible names are NOT (X), CNOT, SWAP, TOF, FRED.

Returns

Gate depth

7.1.3.5 NOT()

```
Bit_circuit& qpp::Bit_circuit::NOT (
             idx i )  [inline]
```

Bit flip.

See also

qpp::Bit_circuit::X()

Parameters

i	Bit position in the circuit

Returns

Reference to the current instance

7.1.3.6 reset()

```
Bit_circuit& qpp::Bit_circuit::reset ( )  [inline], [noexcept]
```

Reset the circuit all zero, clear all gates.

Returns

Reference to the current instance

7.1.3.7 SWAP()

```
Bit_circuit& qpp::Bit_circuit::SWAP (
             idx i,
             idx j )  [inline]
```

Swap bits.

Parameters

i	Bit index
j	Bit index

Returns

Reference to the current instance

7.1.3.8 TOF()

```
Bit_circuit& qpp::Bit_circuit::TOF (
            idx i,
            idx j,
            idx k )  [inline]
```

Toffoli gate.

Parameters

i	Control first bit index
j	Control second bit index
k	Target bit index

Returns

Reference to the current instance

7.1.3.9 X()

```
Bit_circuit& qpp::Bit_circuit::X (
            idx i )  [inline]
```

Bit flip.

See also

qpp::Bit_circuit::NOT()

Parameters

i	Bit position in the circuit

Returns

Reference to the current instance

7.1.4 Member Data Documentation

7.1.4.1 bCNOT_

`Dynamic_bitset qpp::Bit_circuit::bCNOT_ [private]`

7.1.4.2 bFRED_

`Dynamic_bitset qpp::Bit_circuit::bFRED_ [private]`

7.1.4.3 bNOT_

`Dynamic_bitset qpp::Bit_circuit::bNOT_ [private]`

7.1.4.4 bSWAP_

`Dynamic_bitset qpp::Bit_circuit::bSWAP_ [private]`

7.1.4.5 bTOF_

`Dynamic_bitset qpp::Bit_circuit::bTOF_ [private]`

7.1.4.6 btotal_

`Dynamic_bitset qpp::Bit_circuit::btotal_ [private]`

used for depth calculations

7.1.4.7 count_

```
std::unordered_map<std::string, idx> qpp::Bit_circuit::count_ {}  [private]
```

gate counts

7.1.4.8 depth_

```
std::unordered_map<std::string, idx> qpp::Bit_circuit::depth_ {}  [private]
```

gate depths

The documentation for this class was generated from the following file:

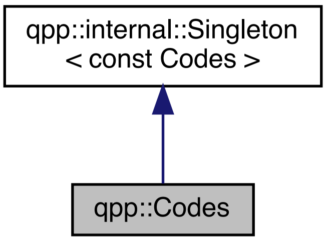
- classes/reversible.h

7.2 qpp::Codes Class Reference

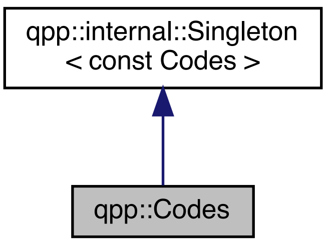
const Singleton class that defines quantum error correcting codes

```
#include <classes/codes.h>
```

Inheritance diagram for qpp::Codes:



Collaboration diagram for qpp::Codes:



Public Types

- enum Type { Type::FIVE_QUBIT, Type::SEVEN_QUBIT_STEANE, Type::NINE_QUBIT_SHOR }
  Code types, add more codes here if needed.

Public Member Functions

- ket codeword (Type type, idx i) const
  Returns the codeword of the specified code type.

Private Member Functions

- Codes ()
  Default constructor.
- ∼Codes ()=default
  Default destructor.

Friends

- class internal::Singleton< const Codes >

Additional Inherited Members

7.2.1 Detailed Description

const Singleton class that defines quantum error correcting codes

7.2.2 Member Enumeration Documentation

7.2.2.1 Type

`enum qpp::Codes::Type [strong]`

Code types, add more codes here if needed.

See also

qpp::Codes::codeword()

Enumerator

FIVE_QUBIT	[[5,1,3]] qubit code
SEVEN_QUBIT_STEANE	[[7,1,3]] Steane qubit code
NINE_QUBIT_SHOR	[[9,1,3]] Shor qubit code

7.2.3 Constructor & Destructor Documentation

7.2.3.1 Codes()

```
qpp::Codes::Codes ( )  [inline], [private]
```

Default constructor.

7.2.3.2 ∼Codes()

```
qpp::Codes::∼Codes ( )  [private], [default]
```

Default destructor.

7.2.4 Member Function Documentation

7.2.4.1 codeword()

```
ket qpp::Codes::codeword (
            Type type,
            idx i ) const  [inline]
```

Returns the codeword of the specified code type.

See also

qpp::Codes::Type

Parameters

type	Code type
i	Codeword index

Returns

i-th codeword of the code *type*

7.2.5 Friends And Related Function Documentation

7.2.5.1 internal::Singleton< const Codes >

```
friend class internal::Singleton< const Codes > [friend]
```

The documentation for this class was generated from the following file:

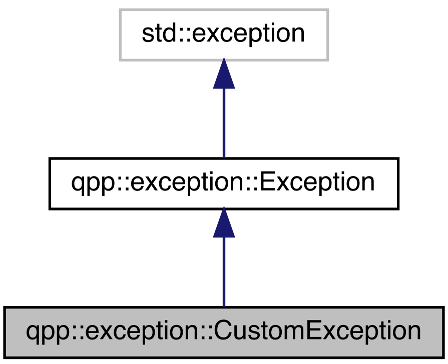
- classes/codes.h

7.3 qpp::exception::CustomException Class Reference

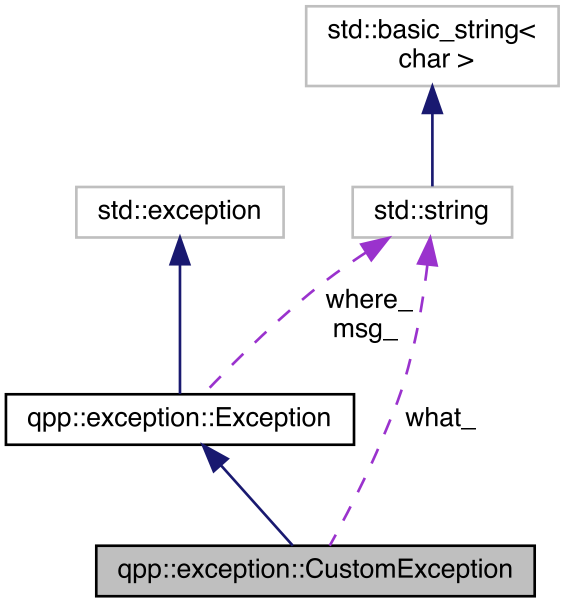
Custom exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::CustomException:



Collaboration diagram for qpp::exception::CustomException:



Public Member Functions

- CustomException (const std::string &where, const std::string &what)

Private Member Functions

- std::string description () const override
  Exception description.

Private Attributes

- std::string what_ {}

7.3.1 Detailed Description

Custom exception.

Custom exception, the user must provide a custom message

7.3.2 Constructor & Destructor Documentation

7.3.2.1 CustomException()

```
qpp::exception::CustomException::CustomException (
            const std::string & where,
            const std::string & what )  [inline]
```

7.3.3 Member Function Documentation

7.3.3.1 description()

```
std::string qpp::exception::CustomException::description ( ) const  [inline], [override],
[private], [virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.3.4 Member Data Documentation

7.3.4.1 what_

```
std::string qpp::exception::CustomException::what_ {}  [private]
```

The documentation for this class was generated from the following file:

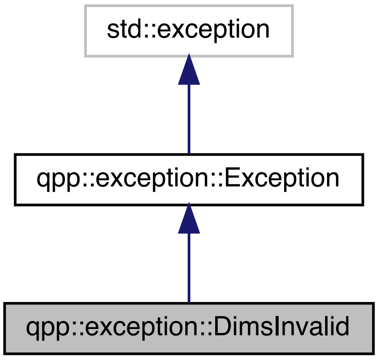
- classes/exception.h

7.4 qpp::exception::DimsInvalid Class Reference

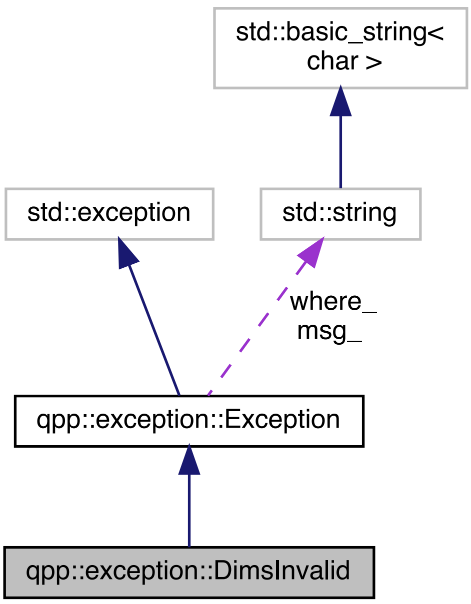
Invalid dimension(s) exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::DimsInvalid:



Collaboration diagram for qpp::exception::DimsInvalid:



Public Member Functions

- std::string description () const override

  Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.4.1 Detailed Description

Invalid dimension(s) exception.

std::vector<idx> of dimensions has zero size or contains zeros

7.4.2 Member Function Documentation

7.4.2.1 description()

```
std::string qpp::exception::DimsInvalid::description ( ) const  [inline], [override], [virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.4.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

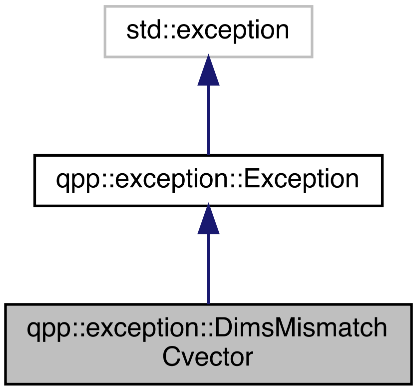
- classes/exception.h

7.5 qpp::exception::DimsMismatchCvector Class Reference

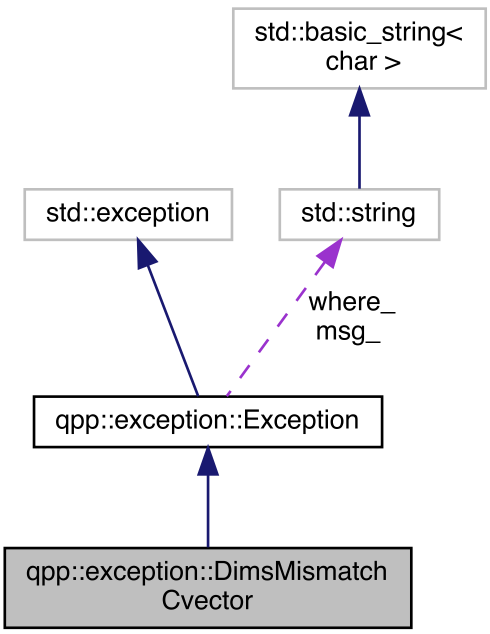
Dimension(s) mismatch column vector size exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::DimsMismatchCvector:



Collaboration diagram for qpp::exception::DimsMismatchCvector:



Public Member Functions

- std::string description () const override
  Exception description.
- Exception (const std::string &where)
  Constructs an exception.

7.5.1 Detailed Description

Dimension(s) mismatch column vector size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of the Eigen::↩ Matrix (assumed to be a column vector)

7.5.2 Member Function Documentation

7.5.2.1 description()

```
std::string qpp::exception::DimsMismatchCvector::description ( ) const  [inline], [override], [virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.5.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

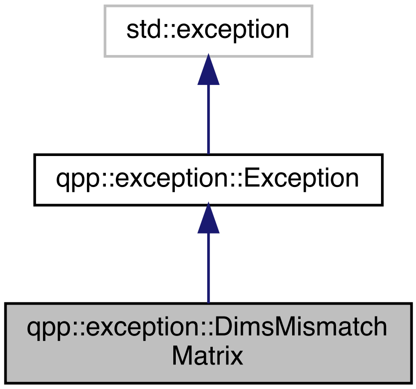
- classes/exception.h

7.6 qpp::exception::DimsMismatchMatrix Class Reference

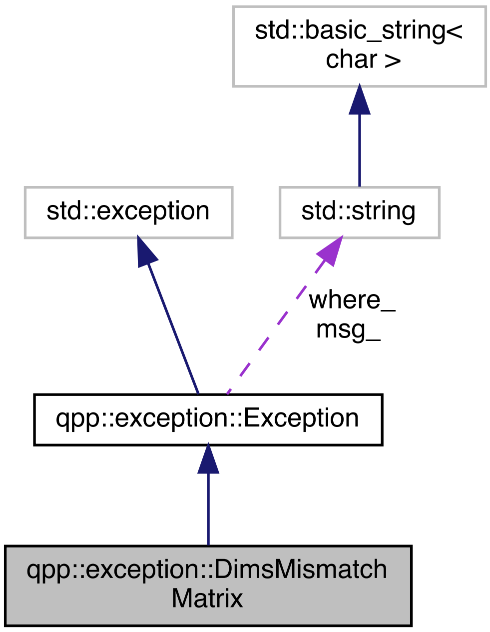
Dimension(s) mismatch matrix size exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::DimsMismatchMatrix:



Collaboration diagram for qpp::exception::DimsMismatchMatrix:



Public Member Functions

- std::string description () const override
  Exception description.
- Exception (const std::string &where)
  Constructs an exception.

7.6.1 Detailed Description

Dimension(s) mismatch matrix size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of rows of the Eigen::Matrix (assumed to be a square matrix)

7.6.2 Member Function Documentation

7.6.2.1 description()

```
std::string qpp::exception::DimsMismatchMatrix::description ( ) const  [inline], [override], [virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.6.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

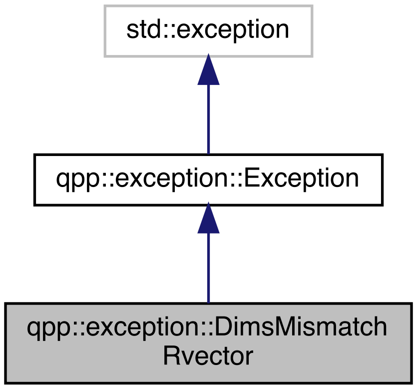
- classes/exception.h

7.7 qpp::exception::DimsMismatchRvector Class Reference

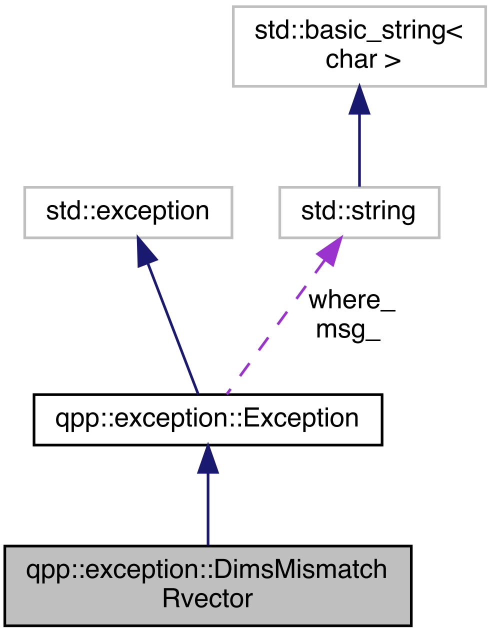
Dimension(s) mismatch row vector size exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::DimsMismatchRvector:



Collaboration diagram for qpp::exception::DimsMismatchRvector:



Public Member Functions

- std::string description () const override

    Exception description.
- Exception (const std::string &where)

    Constructs an exception.

7.7.1 Detailed Description

Dimension(s) mismatch row vector size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of the Eigen::↩
Matrix (assumed to be a row vector)

7.7.2 Member Function Documentation

7.7.2.1 description()

```
std::string qpp::exception::DimsMismatchRvector::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.7.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

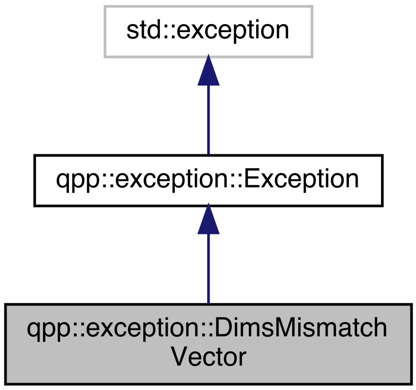
- classes/exception.h

7.8 qpp::exception::DimsMismatchVector Class Reference

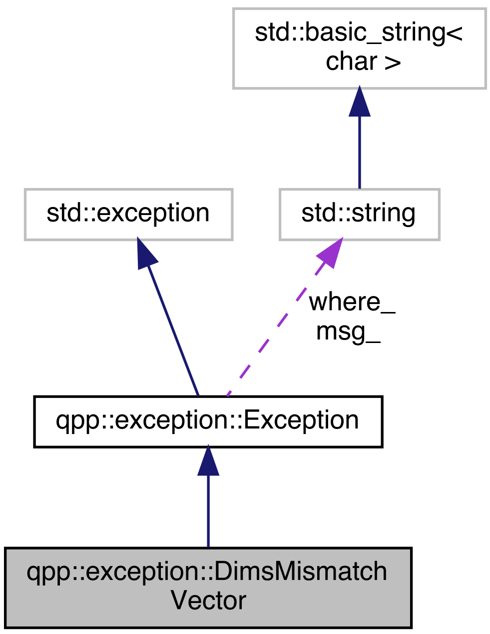
Dimension(s) mismatch vector size exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::DimsMismatchVector:



Collaboration diagram for qpp::exception::DimsMismatchVector:



Public Member Functions

- std::string description () const override

  Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.8.1 Detailed Description

Dimension(s) mismatch vector size exception.

Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of the Eigen::↩
Matrix (assumed to be a row/column vector)

7.8.2 Member Function Documentation

7.8.2.1 description()

`std::string qpp::exception::DimsMismatchVector::description ( ) const [inline], [override], [virtual]`

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.8.2.2 Exception()

`qpp::exception::Exception::Exception [inline], [explicit]`

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

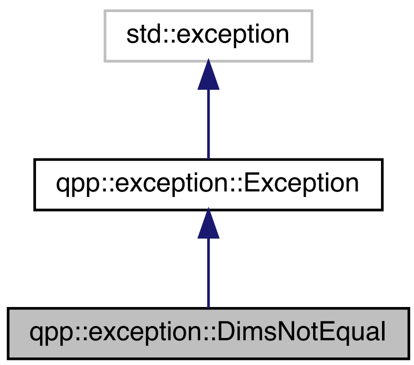
- classes/exception.h

7.9 qpp::exception::DimsNotEqual Class Reference

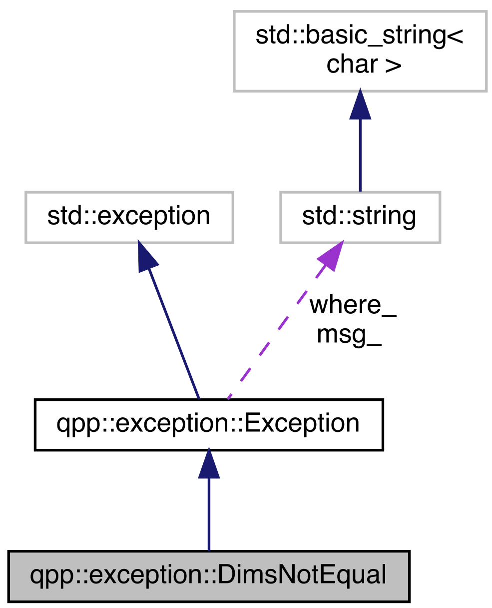
Dimensions not equal exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::DimsNotEqual:



Collaboration diagram for qpp::exception::DimsNotEqual:



Public Member Functions

- std::string description () const override
  Exception description.
- Exception (const std::string &where)
  Constructs an exception.

7.9.1 Detailed Description

Dimensions not equal exception.

Local/global dimensions are not equal

7.9.2 Member Function Documentation

7.9.2.1 description()

```
std::string qpp::exception::DimsNotEqual::description ( ) const  [inline], [override], [virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.9.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

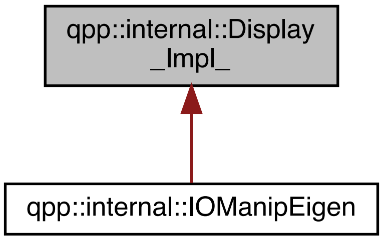
The documentation for this class was generated from the following file:

- classes/exception.h

7.10 qpp::internal::Display_Impl_ Struct Reference

`#include <internal/util.h>`

Inheritance diagram for qpp::internal::Display_Impl_:



Public Member Functions

- template<typename T >
  std::ostream & display_impl_ (const T &A, std::ostream &os, double chop=qpp::chop) const

7.10.1 Member Function Documentation

7.10.1.1 display_impl_()

```
template<typename T >
std::ostream& qpp::internal::Display_Impl_::display_impl_ (
            const T & A,
            std::ostream & os,
            double chop = qpp::chop ) const  [inline]
```

The documentation for this struct was generated from the following file:

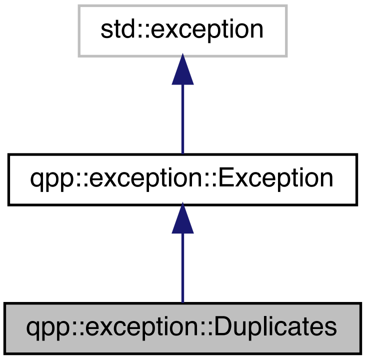
- internal/util.h

7.11 qpp::exception::Duplicates Class Reference

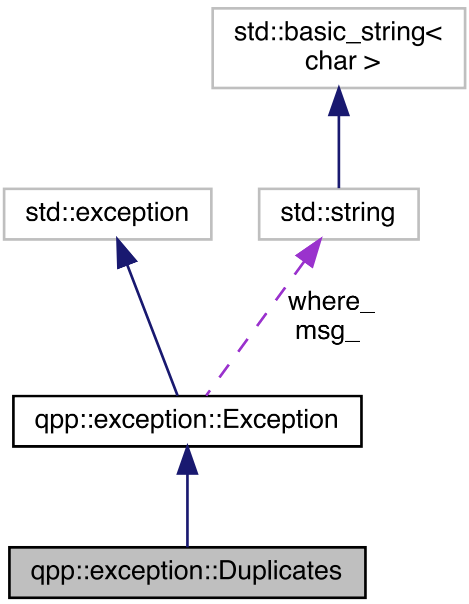
System (e.g. std::vector) has duplicates exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::Duplicates:



Collaboration diagram for qpp::exception::Duplicates:



Public Member Functions

- std::string description () const override

  Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.11.1 Detailed Description

System (e.g. std::vector) has duplicates exception.

7.11.2 Member Function Documentation

7.11.2.1 description()

```
std::string qpp::exception::Duplicates::description ( ) const  [inline], [override], [virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.11.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

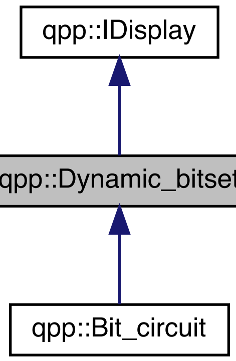
- classes/exception.h

7.12 qpp::Dynamic_bitset Class Reference

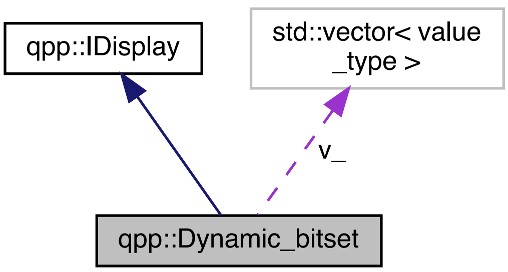
Dynamic bitset class, allows the specification of the number of bits at runtime.

`#include <classes/reversible.h>`

Inheritance diagram for qpp::Dynamic_bitset:



Collaboration diagram for qpp::Dynamic_bitset:



Public Types

- using value_type = unsigned int

    type of the storage elements
- using storage_type = std::vector< value_type >

    type of the storage

Public Member Functions

- Dynamic_bitset (idx n)

    Constructor, initializes all bits to false (zero)

- virtual ∼Dynamic_bitset ()=default

  Default virtual destructor.
- const storage_type & data () const

  Raw storage space of the bitset.
- idx size () const noexcept

  Number of bits stored in the bitset.
- idx storage_size () const noexcept

  Size of the underlying storage space (in units of value_type, unsigned int by default)
- idx count () const noexcept

  Number of bits set to one in the bitset (Hamming weight)
- bool get (idx pos) const noexcept

  The value of the bit at position pos.
- bool none () const noexcept

  Checks whether none of the bits are set.
- bool all () const noexcept

  Checks whether all bits are set.
- bool any () const noexcept

  Checks whether any bit is set.
- Dynamic_bitset & set (idx pos, bool value=true)

  Sets the bit at position pos.
- Dynamic_bitset & set () noexcept

  Set all bits to true.
- Dynamic_bitset & rand (idx pos, double p=0.5)

  Sets the bit at position pos according to a Bernoulli(p) distribution.
- Dynamic_bitset & rand (double p=0.5)

  Sets all bits according to a Bernoulli(p) distribution.
- Dynamic_bitset & reset (idx pos)

  Sets the bit at position pos to false.
- Dynamic_bitset & reset () noexcept

  Sets all bits to false.
- Dynamic_bitset & flip (idx pos)

  Flips the bit at position pos.
- Dynamic_bitset & flip () noexcept

  Flips all bits.
- bool operator== (const Dynamic_bitset &rhs) const noexcept

  Equality operator.
- bool operator!= (const Dynamic_bitset &rhs) const noexcept

  Inequality operator.
- idx operator- (const Dynamic_bitset &rhs) const noexcept

  Number of places the two bitsets differ (Hamming distance)
- template<class CharT = char, class Traits = std::char_traits<CharT>, class Allocator = std::allocator<CharT>>
  std::basic_string< CharT, Traits, Allocator > to_string (CharT zero=CharT('0'), CharT one=CharT('1')) const

  String representation.

Protected Member Functions

- idx index_ (idx pos) const

  Index of the pos bit in the storage space.
- idx offset_ (idx pos) const

  Offset of the pos bit in the storage space relative to its index.

Protected Attributes

- idx storage_size_
  storage size
- idx n_
  number of bits
- std::vector< value_type > v_
  storage space

Private Member Functions

- std::ostream & display (std::ostream &os) const override
  qpp::IDisplay::display() override, displays the bitset bit by bit

7.12.1 Detailed Description

Dynamic bitset class, allows the specification of the number of bits at runtime.

Note

The interface mimics std::bitset<>

7.12.2 Member Typedef Documentation

7.12.2.1 storage_type

```
using qpp::Dynamic_bitset::storage_type = std::vector<value_type>
```

type of the storage

7.12.2.2 value_type

```
using qpp::Dynamic_bitset::value_type = unsigned int
```

type of the storage elements

7.12.3 Constructor & Destructor Documentation

7.12.3.1 Dynamic_bitset()

```
qpp::Dynamic_bitset::Dynamic_bitset (
            idx n ) [inline], [explicit]
```

Constructor, initializes all bits to false (zero)

Parameters

n	Number of bits in the bitset

7.12.3.2 ∼Dynamic_bitset()

```
virtual qpp::Dynamic_bitset::~Dynamic_bitset ( )  [virtual], [default]
```

Default virtual destructor.

7.12.4 Member Function Documentation

7.12.4.1 all()

```
bool qpp::Dynamic_bitset::all ( ) const  [inline], [noexcept]
```

Checks whether all bits are set.

Returns

True if all of the bits are set

7.12.4.2 any()

```
bool qpp::Dynamic_bitset::any ( ) const  [inline], [noexcept]
```

Checks whether any bit is set.

Returns

True if any of the bits is set

7.12.4.3 count()

```
idx qpp::Dynamic_bitset::count ( ) const  [inline], [noexcept]
```

Number of bits set to one in the bitset (Hamming weight)

Returns

Hamming weight

7.12.4.4 data()

```
const storage_type& qpp::Dynamic_bitset::data ( ) const  [inline]
```

Raw storage space of the bitset.

Returns

Const reference to the underlying storage space

7.12.4.5 display()

```
std::ostream& qpp::Dynamic_bitset::display (
             std::ostream & os ) const  [inline], [override], [private], [virtual]
```

qpp::IDisplay::display() override, displays the bitset bit by bit

Parameters

os	Output stream passed by reference

Returns

Reference to the output stream

Implements qpp::IDisplay.

7.12.4.6 flip() [1/2]

```
Dynamic_bitset& qpp::Dynamic_bitset::flip (
             idx pos )  [inline]
```

Flips the bit at position *pos*.

Parameters

pos	Position in the bitset

Returns

Reference to the current instance

7.12.4.7 flip() [2/2]

```
Dynamic_bitset& qpp::Dynamic_bitset::flip ( )  [inline], [noexcept]
```

Flips all bits.

Returns

Reference to the current instance

7.12.4.8 get()

```
bool qpp::Dynamic_bitset::get (
             idx pos ) const  [inline], [noexcept]
```

The value of the bit at position *pos*.

Parameters

pos	Position in the bitset

Returns

The value of the bit at position *pos*

7.12.4.9 index_()

```
idx qpp::Dynamic_bitset::index_ (
             idx pos ) const  [inline], [protected]
```

Index of the *pos* bit in the storage space.

Parameters

pos	Bit location

Returns

Index of the *pos* bit in the storage space

7.12.4.10 none()

```
bool qpp::Dynamic_bitset::none ( ) const [inline], [noexcept]
```

Checks whether none of the bits are set.

Returns

True if none of the bits are set

7.12.4.11 offset_()

```
idx qpp::Dynamic_bitset::offset_ (
            idx pos ) const [inline], [protected]
```

Offset of the *pos* bit in the storage space relative to its index.

Parameters

pos	Bit location

Returns

Offset of the *pos* bit in the storage space relative to its index

7.12.4.12 operator"!=()

```
bool qpp::Dynamic_bitset::operator!= (
            const Dynamic_bitset & rhs ) const [inline], [noexcept]
```

Inequality operator.

Parameters

rhs	Dynamic_bitset against which the inequality is being tested

Returns

True if the bitsets are not equal (bit by bit), false otherwise

7.12.4.13 operator-()

```
idx qpp::Dynamic_bitset::operator- (
            const Dynamic_bitset & rhs ) const  [inline], [noexcept]
```

Number of places the two bitsets differ (Hamming distance)

Parameters

rhs	Dynamic_bitset against which the the Hamming distance is computed

Returns

Hamming distance

7.12.4.14 operator==()

```
bool qpp::Dynamic_bitset::operator== (
            const Dynamic_bitset & rhs ) const  [inline], [noexcept]
```

Equality operator.

Parameters

rhs	Dynamic_bitset against which the equality is being tested

Returns

True if the bitsets are equal (bit by bit), false otherwise

7.12.4.15 rand() [1/2]

```
Dynamic_bitset& qpp::Dynamic_bitset::rand (
            idx pos,
            double p = 0.5 )  [inline]
```

Sets the bit at position *pos* according to a Bernoulli(p) distribution.

Parameters

pos	Position in the bitset
p	Probability

Returns

Reference to the current instance

7.12.4.16 rand() [2/2]

```
Dynamic_bitset& qpp::Dynamic_bitset::rand (
            double p = 0.5 )  [inline]
```

Sets all bits according to a Bernoulli(p) distribution.

Parameters

p	Probability

Returns

Reference to the current instance

7.12.4.17 reset() [1/2]

```
Dynamic_bitset& qpp::Dynamic_bitset::reset (
            idx pos )  [inline]
```

Sets the bit at position *pos* to false.

Parameters

pos	Position in the bitset

Returns

Reference to the current instance

7.12.4.18 reset() [2/2]

```
Dynamic_bitset& qpp::Dynamic_bitset::reset ( )  [inline], [noexcept]
```

Sets all bits to false.

Returns

Reference to the current instance

7.12.4.19 set() [1/2]

```
Dynamic_bitset& qpp::Dynamic_bitset::set (
            idx pos,
            bool value = true )  [inline]
```

Sets the bit at position *pos*.

Parameters

pos	Position in the bitset
value	Bit value

Returns

Reference to the current instance

7.12.4.20 set() [2/2]

```
Dynamic_bitset& qpp::Dynamic_bitset::set ( )  [inline], [noexcept]
```

Set all bits to true.

Returns

Reference to the current instance

7.12.4.21 size()

```
idx qpp::Dynamic_bitset::size ( ) const  [inline], [noexcept]
```

Number of bits stored in the bitset.

Returns

Number of bits stored in the bitset

7.12.4.22 storage_size()

```
idx qpp::Dynamic_bitset::storage_size ( ) const  [inline], [noexcept]
```

Size of the underlying storage space (in units of value_type, unsigned int by default)

Returns

Size of the underlying storage space

7.12.4.23 to_string()

```
template<class CharT = char, class Traits = std::char_traits<CharT>, class Allocator = std↩
::allocator<CharT>>
std::basic_string<CharT, Traits, Allocator> qpp::Dynamic_bitset::to_string (
            CharT zero = CharT('0'),
            CharT one = CharT('1') ) const [inline]
```

String representation.

Template Parameters

CharT	String character type
Traits	String traits
Allocator	String Allocator

Parameters

zero	Character representing the zero
one	Character representing the one

Returns

The bitset as a string

7.12.5 Member Data Documentation

7.12.5.1 n_

```
idx qpp::Dynamic_bitset::n_ [protected]
```

number of bits

7.12.5.2 storage_size_

```
idx qpp::Dynamic_bitset::storage_size_ [protected]
```

storage size

7.12.5.3 v_

```
std::vector<value_type> qpp::Dynamic_bitset::v_ [protected]
```

storage space

The documentation for this class was generated from the following file:

- classes/reversible.h

7.13 qpp::internal::EqualEigen Class Reference

Functor for comparing Eigen expressions for equality.

```
#include <functions.h>
```

Public Member Functions

- template< typename Derived >
  bool operator() (const Eigen::MatrixBase< Derived > &A, const Eigen::MatrixBase< Derived > &B) const

7.13.1 Detailed Description

Functor for comparing Eigen expressions for equality.

Note

Works without assertion fails even if the dimensions of the arguments are different (in which case simply returns false

7.13.2 Member Function Documentation

7.13.2.1 operator()()

```
template<typename Derived >
bool qpp::internal::EqualEigen::operator() (
            const Eigen::MatrixBase< Derived > & A,
            const Eigen::MatrixBase< Derived > & B ) const [inline]
```

The documentation for this class was generated from the following file:

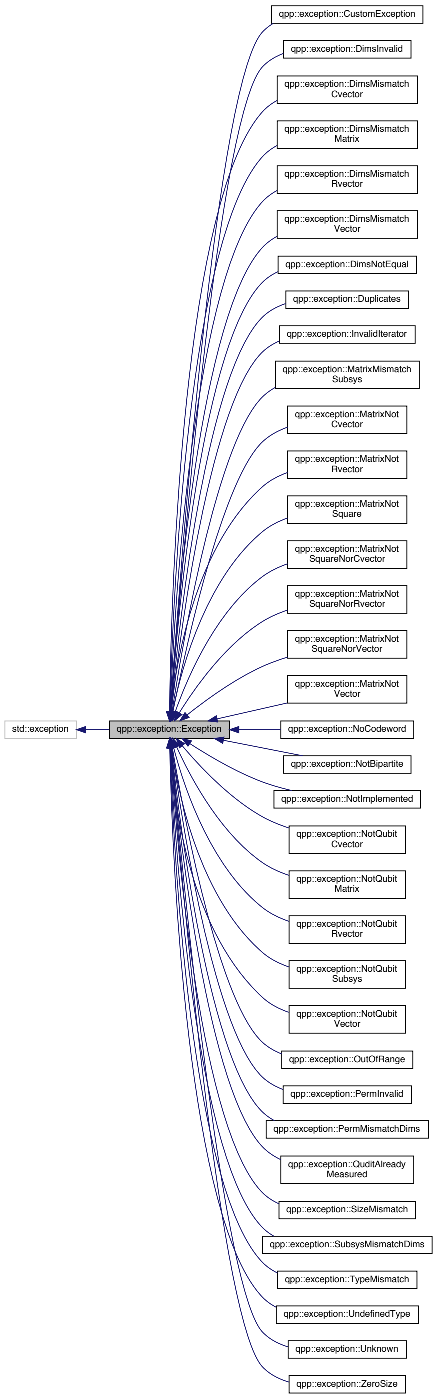
- functions.h

7.14 qpp::exception::Exception Class Reference

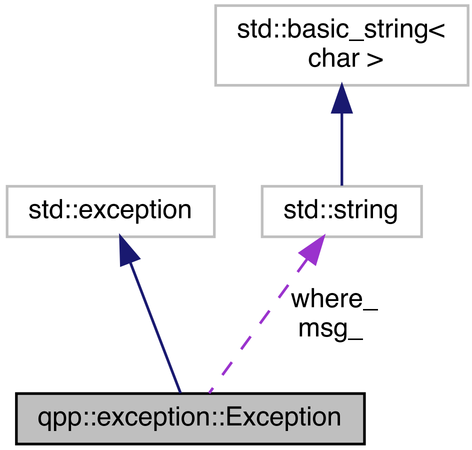
Base class for generating Quantum++ custom exceptions.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::Exception:



Collaboration diagram for qpp::exception::Exception:



Public Member Functions

- Exception (const std::string &where)

    Constructs an exception.
- const char ∗ what () const noexcept override

    Overrides std::exception::what()
- virtual std::string description () const =0

    Exception description.

Private Attributes

- std::string where_
- std::string msg_

7.14.1 Detailed Description

Base class for generating Quantum++ custom exceptions.

Derive from this class if more exceptions are needed, making sure to override qpp::exception::Exception::description() in the derived class and to inherit the constructor qpp::exception::Exception::Exception(). Preferably keep your newly defined exception classes in the namespace qpp::exception.

Example:

```
namespace qpp
{
namespace exception
{
    class ZeroSize : public Exception
    {
    public:
        std::string description() const override
        {
            return "Object has zero size";
        }

        // inherit the base class' qpp::exception::Exception constructor
        using Exception::Exception;
    };
} // namespace exception
} // namespace qpp
```

7.14.2 Constructor & Destructor Documentation

7.14.2.1 Exception()

```
qpp::exception::Exception::Exception (
            const std::string & where )  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

7.14.3 Member Function Documentation

7.14.3.1 description()

```
std::string qpp::exception::Exception::description ( ) const  [inline], [pure virtual]
```

Exception description.

Returns

Exception description

Implemented in qpp::exception::InvalidIterator, qpp::exception::NotImplemented, qpp::exception::CustomException, qpp::exception::Duplicates, qpp::exception::QuditAlreadyMeasured, qpp::exception::UndefinedType, qpp::exception::SizeMismatch, qpp::exception::TypeMismatch, qpp::exception::OutOfRange, qpp::exception::NoCodeword, qpp::exception::NotBipartite, qpp::exception::NotQubitSubsys, qpp::exception::NotQubitVector, qpp::exception::NotQubitRvector, qpp::exception::NotQubitCvector, qpp::exception::NotQubitMatrix, qpp::exception::PermMismatchDims, qpp::exception::PermInvalid, qpp::exception::SubsysMismatchD qpp::exception::DimsMismatchVector, qpp::exception::DimsMismatchRvector, qpp::exception::DimsMismatchCvector, qpp::exception::DimsMismatchMatrix, qpp::exception::DimsNotEqual, qpp::exception::DimsInvalid, qpp::exception::MatrixMismatchSu qpp::exception::MatrixNotSquareNorVector, qpp::exception::MatrixNotSquareNorRvector, qpp::exception::MatrixNotSquareNorCvecto qpp::exception::MatrixNotVector, qpp::exception::MatrixNotRvector, qpp::exception::MatrixNotCvector, qpp::exception::MatrixNotSqua qpp::exception::ZeroSize, and qpp::exception::Unknown.

7.14.3.2 what()

`const char* qpp::exception::Exception::what ( ) const [inline], [override], [noexcept]`

Overrides std::exception::what()

Returns

Exception description

7.14.4 Member Data Documentation

7.14.4.1 msg_

`std::string qpp::exception::Exception::msg_ [mutable], [private]`

7.14.4.2 where_

`std::string qpp::exception::Exception::where_ [private]`

The documentation for this class was generated from the following file:

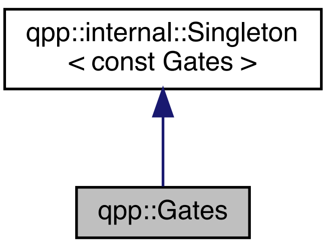
- classes/exception.h

7.15 qpp::Gates Class Reference

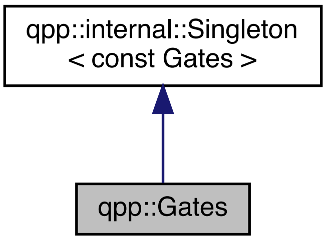
const Singleton class that implements most commonly used gates

`#include <classes/gates.h>`

Inheritance diagram for qpp::Gates:



Collaboration diagram for qpp::Gates:



Public Member Functions

- cmat Rn (double theta, const std::vector< double > &n) const

    Qubit rotation of theta about the 3-dimensional real (unit) vector n.
- cmat RX (double theta) const

    Qubit rotation of theta about the X axis.
- cmat RY (double theta) const

    Qubit rotation of theta about the Y axis.
- cmat RZ (double theta) const

    Qubit rotation of theta about the Z axis.
- cmat Zd (idx D=2) const

    Generalized Z gate for qudits.
- cmat SWAPd (idx D=2) const

    SWAP gate for qudits.
- cmat Fd (idx D=2) const

    Quantum Fourier transform gate for qudits.
- cmat MODMUL (idx a, idx N, idx n) const

    Modular multiplication gate for qubits Implements $|x\rangle \longrightarrow |ax \mathrm{mod} N\rangle$.
- cmat Xd (idx D=2) const

    Generalized X gate for qudits.
- template< typename Derived = Eigen::MatrixXcd>
  Derived Id (idx D=2) const

    Identity gate.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > CTRL (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &ctrl, const std::vector< idx > &target, idx n, idx d=2) const

    Generates the multi-partite multiple-controlled-A gate in matrix form.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, idx pos, const std::vector< idx > &dims) const

    Expands out.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, idx pos, const std::initializer_list< idx > &dims) const

    Expands out.

- template<typename Derived >
  dyn_mat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, idx pos, idx n, idx d=2) const

  Expands out.
- std::string get_name (const cmat &U) const

  Get the name of the most common qubit gates.

Public Attributes

- cmat Id2 {cmat::Identity(2, 2)}

  Identity gate.
- cmat H {cmat::Zero(2, 2)}

  Hadamard gate.
- cmat X {cmat::Zero(2, 2)}

  Pauli Sigma-X gate.
- cmat Y {cmat::Zero(2, 2)}

  Pauli Sigma-Y gate.
- cmat Z {cmat::Zero(2, 2)}

  Pauli Sigma-Z gate.
- cmat S {cmat::Zero(2, 2)}

  S gate.
- cmat T {cmat::Zero(2, 2)}

  T gate.
- cmat CNOT {cmat::Identity(4, 4)}

  Controlled-NOT control target gate.
- cmat CZ {cmat::Identity(4, 4)}

  Controlled-Phase gate.
- cmat CNOTba {cmat::Zero(4, 4)}

  Controlled-NOT target->control gate.
- cmat SWAP {cmat::Identity(4, 4)}

  SWAP gate.
- cmat TOF {cmat::Identity(8, 8)}

  Toffoli gate.
- cmat FRED {cmat::Identity(8, 8)}

  Fredkin gate.

Private Member Functions

- Gates ()

  Initializes the gates.
- ∼Gates ()=default

  Default destructor.

Friends

- class internal::Singleton< const Gates >

Additional Inherited Members

7.15.1 Detailed Description

const Singleton class that implements most commonly used gates

7.15.2 Constructor & Destructor Documentation

7.15.2.1 Gates()

```
qpp::Gates::Gates ( )  [inline], [private]
```

Initializes the gates.

7.15.2.2 ∼Gates()

```
qpp::Gates::~Gates ( )  [private], [default]
```

Default destructor.

7.15.3 Member Function Documentation

7.15.3.1 CTRL()

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::CTRL (
            const Eigen::MatrixBase< Derived > & A,
            const std::vector< idx > & ctrl,
            const std::vector< idx > & target,
            idx n,
            idx d = 2 ) const  [inline]
```

Generates the multi-partite multiple-controlled-*A* gate in matrix form.

See also

qpp::applyCTRL()

Note

The dimension of the gate *A* must match the dimension of *target*

Parameters

A	Eigen expression
ctrl	Control subsystem indexes
target	Subsystem indexes where the gate *A* is applied
n	Total number of subsystems
d	Subsystem dimensions

Returns

CTRL-A gate, as a matrix over the same scalar field as *A*

7.15.3.2 expandout() [1/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
            const Eigen::MatrixBase< Derived > & A,
            idx pos,
            const std::vector< idx > & dims ) const  [inline]
```

Expands out.

See also

qpp::kron()

Expands out *A* as a matrix in a multi-partite system. Faster than using qpp::kron(I, I, ..., I, A, I, ..., I).

Parameters

A	Eigen expression
pos	Position
dims	Dimensions of the multi-partite system

Returns

Tensor product $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$, with *A* on position *pos*, as a dynamic matrix over the same scalar field as *A*

7.15.3.3 expandout() [2/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
            const Eigen::MatrixBase< Derived > & A,
            idx pos,
            const std::initializer_list< idx > & dims ) const  [inline]
```

Expands out.

See also

qpp::kron()

Expands out *A* as a matrix in a multi-partite system. Faster than using qpp::kron(I, I, ..., I, A, I, ..., I).

Note

The std::initializer_list overload exists because otherwise, in the degenerate case when *dims* has only one element, the one element list is implicitly converted to the element's underlying type, i.e. qpp::idx, which has the net effect of picking the wrong (non-vector) qpp::expandout() overload

Parameters

A	Eigen expression
pos	Position
dims	Dimensions of the multi-partite system

Returns

Tensor product $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$, with *A* on position *pos*, as a dynamic matrix over the same scalar field as *A*

7.15.3.4 expandout() [3/3]

```
template<typename Derived >
dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (
            const Eigen::MatrixBase< Derived > & A,
            idx pos,
            idx n,
            idx d = 2 ) const [inline]
```

Expands out.

See also

qpp::kron()

Expands out *A* as a matrix in a multi-partite system. Faster than using qpp::kron(I, I, ..., I, A, I, ..., I).

Parameters

A	Eigen expression
pos	Position
n	Number of subsystems
d	Subsystem dimensions

Returns

Tensor product $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$, with *A* on position *pos*, as a dynamic matrix over the same scalar field as *A*

7.15.3.5 Fd()

```
cmat qpp::Gates::Fd (
            idx D = 2 ) const  [inline]
```

Quantum Fourier transform gate for qudits.

Note

Defined as $F = \sum_{j,k=0}^{D-1} \exp(2\pi \mathrm{i} jk/D)|j\rangle\langle k|$

Parameters

D	Dimension of the Hilbert space

Returns

Fourier transform gate for qudits

7.15.3.6 get_name()

```
std::string qpp::Gates::get_name (
            const cmat & U ) const  [inline]
```

Get the name of the most common qubit gates.

Note

Assumes that the gate *U* is represented by a square matrix. If not, returns the empty string

Parameters

U	Complex matrix representing the quantum gate

Returns

The name of the gate (if any), otherwise the empty string

7.15.3.7 Id()

```
template<typename Derived = Eigen::MatrixXcd>
Derived qpp::Gates::Id (
            idx D = 2 ) const [inline]
```

Identity gate.

Note

Can change the return type from complex matrix (default) by explicitly specifying the template parameter

Parameters

D	Dimension of the Hilbert space

Returns

Identity gate on a Hilbert space of dimension *D*

7.15.3.8 MODMUL()

```
cmat qpp::Gates::MODMUL (
            idx a,
            idx N,
            idx n ) const [inline]
```

Modular multiplication gate for qubits Implements $|x\rangle \longrightarrow |ax \mathrm{mod} N\rangle$.

Note

For the gate to be unitary, *a* and *N* should be co-prime. The function does not check co-primality in release versions!
The number of qubits required to implement the gate should satisfy $n \geq \lceil \log_2(N) \rceil$

Parameters

a	Positive integer less than *N*
N	Positive integer
n	Number of qubits required for implementing the gate

Returns

Modular multiplication gate

7.15.3.9 Rn()

```
cmat qpp::Gates::Rn (
            double theta,
            const std::vector< double > & n ) const  [inline]
```

Qubit rotation of *theta* about the 3-dimensional real (unit) vector *n*.

Parameters

theta	Rotation angle
n	3-dimensional real (unit) vector

Returns

Rotation gate

7.15.3.10 RX()

```
cmat qpp::Gates::RX (
            double theta ) const  [inline]
```

Qubit rotation of *theta* about the X axis.

Parameters

theta	Rotation angle

Returns

Rotation gate

7.15.3.11 RY()

```
cmat qpp::Gates::RY (
            double theta ) const  [inline]
```

Qubit rotation of *theta* about the Y axis.

Parameters

theta	Rotation angle

Returns

Rotation gate

7.15.3.12 RZ()

```
cmat qpp::Gates::RZ (
            double theta ) const  [inline]
```

Qubit rotation of *theta* about the Z axis.

Parameters

theta	Rotation angle

Returns

Rotation gate

7.15.3.13 SWAPd()

```
cmat qpp::Gates::SWAPd (
            idx D = 2 ) const  [inline]
```

SWAP gate for qudits.

Parameters

D	Dimension of the Hilbert space

Returns

SWAP gate for qudits

7.15.3.14 Xd()

```
cmat qpp::Gates::Xd (
            idx D = 2 ) const  [inline]
```

Generalized X gate for qudits.

Note

Defined as $X = \sum_{j=0}^{D-1} |j \oplus 1\rangle\langle j|$, i.e. raising operator $X|j\rangle = |j \oplus 1\rangle$

Parameters

D	Dimension of the Hilbert space

Returns

Generalized X gate for qudits

7.15.3.15 Zd()

```
cmat qpp::Gates::Zd (
            idx D = 2 ) const  [inline]
```

Generalized Z gate for qudits.

Note

Defined as $Z = \sum_{j=0}^{D-1} \exp(2\pi \mathrm{i} j/D)|j\rangle\langle j|$

Parameters

D	Dimension of the Hilbert space

Returns

Generalized Z gate for qudits

7.15.4 Friends And Related Function Documentation

7.15.4.1 internal::Singleton< const Gates >

```
friend class internal::Singleton< const Gates >  [friend]
```

7.15.5 Member Data Documentation

7.15.5.1 CNOT

```
cmat qpp::Gates::CNOT {cmat::Identity(4, 4)}
```

Controlled-NOT control target gate.

7.15.5.2 CNOTba

```
cmat qpp::Gates::CNOTba {cmat::Zero(4, 4)}
```

Controlled-NOT target->control gate.

7.15.5.3 CZ

```
cmat qpp::Gates::CZ {cmat::Identity(4, 4)}
```

Controlled-Phase gate.

7.15.5.4 FRED

```
cmat qpp::Gates::FRED {cmat::Identity(8, 8)}
```

Fredkin gate.

7.15.5.5 H

```
cmat qpp::Gates::H {cmat::Zero(2, 2)}
```

Hadamard gate.

7.15.5.6 Id2

```
cmat qpp::Gates::Id2 {cmat::Identity(2, 2)}
```

Identity gate.

7.15.5.7 S

```
cmat qpp::Gates::S {cmat::Zero(2, 2)}
```

S gate.

7.15.5.8 SWAP

```
cmat qpp::Gates::SWAP {cmat::Identity(4, 4)}
```

SWAP gate.

7.15.5.9 T

```
cmat qpp::Gates::T {cmat::Zero(2, 2)}
```

T gate.

7.15.5.10 TOF

```
cmat qpp::Gates::TOF {cmat::Identity(8, 8)}
```

Toffoli gate.

7.15.5.11 X

```
cmat qpp::Gates::X {cmat::Zero(2, 2)}
```

Pauli Sigma-X gate.

7.15.5.12 Y

```
cmat qpp::Gates::Y {cmat::Zero(2, 2)}
```

Pauli Sigma-Y gate.

7.15.5.13 Z

```
cmat qpp::Gates::Z {cmat::Zero(2, 2)}
```

Pauli Sigma-Z gate.

The documentation for this class was generated from the following file:

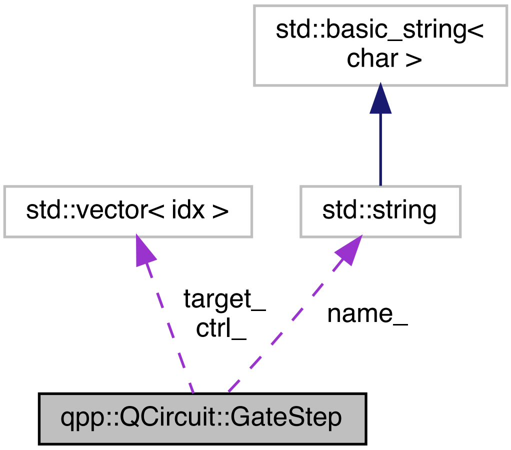
- classes/gates.h

7.16 qpp::QCircuit::GateStep Struct Reference

One step consisting only of gates/operators in the circuit.

`#include <classes/circuits/circuits.h>`

Collaboration diagram for qpp::QCircuit::GateStep:



Public Member Functions

- GateStep ()=default

  Default constructor.
- GateStep (GateType gate_type, std::size_t gate_hash, const std::vector< idx > &ctrl, const std::vector< idx > &target, std::string name={})

  Constructs a gate step instance.

Public Attributes

- GateType gate_type_ = GateType::NONE

  gate type
- std::size_t gate_hash_

  gate hash
- std::vector< idx > ctrl_

  control
- std::vector< idx > target_

  target where the gate is applied
- std::string name_

  custom name of the step

7.16.1 Detailed Description

One step consisting only of gates/operators in the circuit.

7.16.2 Constructor & Destructor Documentation

7.16.2.1 GateStep() [1/2]

```
qpp::QCircuit::GateStep::GateStep ( )  [default]
```

Default constructor.

7.16.2.2 GateStep() [2/2]

```
qpp::QCircuit::GateStep::GateStep (
            GateType gate_type,
            std::size_t gate_hash,
            const std::vector< idx > & ctrl,
            const std::vector< idx > & target,
            std::string name = {} )  [inline], [explicit]
```

Constructs a gate step instance.

Parameters

gate_type	Gate type
gate_hash	Hash of the quantum gate
ctrl	Control qudit indexes
target	Target qudit indexes
name	Optional gate name

7.16.3 Member Data Documentation

7.16.3.1 ctrl_

```
std::vector<idx> qpp::QCircuit::GateStep::ctrl_
```

control

7.16.3.2 gate_hash_

```
std::size_t qpp::QCircuit::GateStep::gate_hash_
```

gate hash

7.16.3.3 gate_type_

```
GateType qpp::QCircuit::GateStep::gate_type_ = GateType::NONE
```

gate type

7.16.3.4 name_

```
std::string qpp::QCircuit::GateStep::name_
```

custom name of the step

7.16.3.5 target_

```
std::vector<idx> qpp::QCircuit::GateStep::target_
```

target where the gate is applied

The documentation for this struct was generated from the following file:

- classes/circuits/circuits.h

7.17 qpp::internal::HashEigen Class Reference

Functor for hashing Eigen expressions.

```
#include <functions.h>
```

Public Member Functions

- template< typename Derived >
  std::size_t operator() (const Eigen::MatrixBase< Derived > &A) const

7.17.1 Detailed Description

Functor for hashing Eigen expressions.

7.17.2 Member Function Documentation

7.17.2.1 operator()()

```
template<typename Derived >
std::size_t qpp::internal::HashEigen::operator() (
            const Eigen::MatrixBase< Derived > & A ) const  [inline]
```

The documentation for this class was generated from the following file:

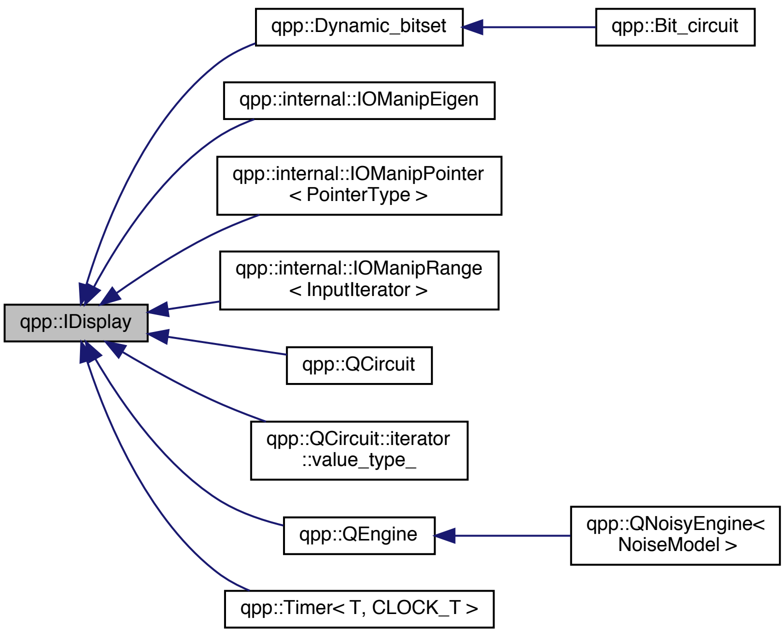
- functions.h

7.18 qpp::IDisplay Class Reference

Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

```
#include <classes/idisplay.h>
```

Inheritance diagram for qpp::IDisplay:



Public Member Functions

- virtual ∼IDisplay ()=default
  Default virtual destructor.

Private Member Functions

- virtual std::ostream & display (std::ostream &os) const =0
  Must be overridden by all derived classes.

Friends

- std::ostream & operator<< (std::ostream &os, const IDisplay &rhs)
  Overloads the extraction operator.

7.18.1 Detailed Description

Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

This class defines friend std::ostream& operator<<(std::ostream& os, const qpp::IDisplay& rhs). The latter delegates the work to the pure private virtual function qpp::IDisplay::display() which has to be overridden by all derived classes.

7.18.2 Constructor & Destructor Documentation

7.18.2.1 ∼IDisplay()

```
virtual qpp::IDisplay::~IDisplay ( )  [virtual], [default]
```

Default virtual destructor.

7.18.3 Member Function Documentation

7.18.3.1 display()

```
virtual std::ostream& qpp::IDisplay::display (
            std::ostream & os ) const  [private], [pure virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implemented in qpp::QCircuit, qpp::QEngine, qpp::QCircuit::iterator::value_type_, qpp::Dynamic_bitset, qpp::internal::IOManipEigen, qpp::Timer< T, CLOCK_T >, qpp::internal::IOManipPointer< PointerType >, and qpp::internal::IOManipRange< InputIterator >.

7.18.4 Friends And Related Function Documentation

7.18.4.1 operator<<

```
std::ostream& operator<< (
            std::ostream & os,
            const IDisplay & rhs )  [friend]
```

Overloads the extraction operator.

Delegates the work to the virtual function qpp::IDisplay::display()

The documentation for this class was generated from the following file:

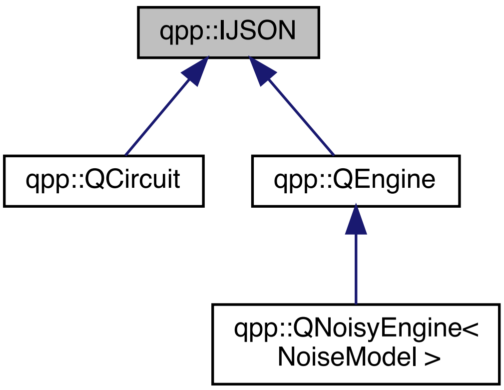
- classes/idisplay.h

7.19 qpp::IJSON Class Reference

Abstract class (interface) that mandates the definition of very basic JSON serialization support.

```
#include <classes/idisplay.h>
```

Inheritance diagram for qpp::IJSON:



Public Member Functions

- virtual ~IJSON ()=default
  Default virtual destructor.
- virtual std::string to_JSON (bool enclosed_in_curly_brackets=true) const =0
  JSON representation of the derived instance, must be overridden by all derived classes.

7.19.1 Detailed Description

Abstract class (interface) that mandates the definition of very basic JSON serialization support.

7.19.2 Constructor & Destructor Documentation

7.19.2.1 ∼IJSON()

```
virtual qpp::IJSON::~IJSON ( )  [virtual], [default]
```

Default virtual destructor.

7.19.3 Member Function Documentation

7.19.3.1 to_JSON()

```
virtual std::string qpp::IJSON::to_JSON (
            bool enclosed_in_curly_brackets = true ) const  [pure virtual]
```

JSON representation of the derived instance, must be overridden by all derived classes.

Parameters

enclosed_in_curly_brackets	If true, encloses the result in curly brackets

Implemented in qpp::QCircuit, and qpp::QEngine.

The documentation for this class was generated from the following file:

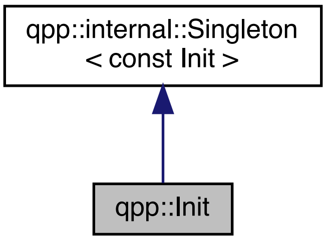
- classes/idisplay.h

7.20 qpp::Init Class Reference

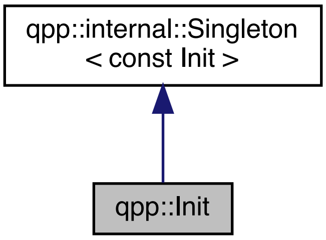
const Singleton class that performs additional initializations/cleanups

```
#include <classes/init.h>
```

Inheritance diagram for qpp::Init:



Collaboration diagram for qpp::Init:



Private Member Functions

- Init ()

  Additional initializations.
- ∼Init ()

  Cleanups.

Friends

- class internal::Singleton< const Init >

Additional Inherited Members

7.20.1 Detailed Description

const Singleton class that performs additional initializations/cleanups

7.20.2 Constructor & Destructor Documentation

7.20.2.1 Init()

`qpp::Init::Init ( ) [inline], [private]`

Additional initializations.

7.20.2.2 ∼Init()

`qpp::Init::∼Init ( ) [inline], [private]`

Cleanups.

7.20.3 Friends And Related Function Documentation

7.20.3.1 internal::Singleton< const Init >

`friend class internal::Singleton< const Init > [friend]`

The documentation for this class was generated from the following file:

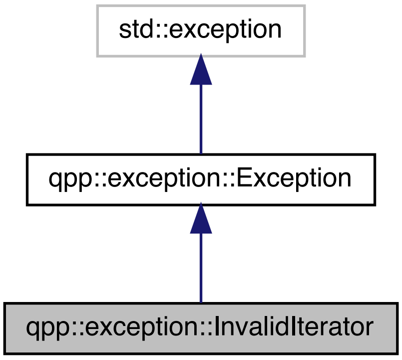
- classes/init.h

7.21 qpp::exception::InvalidIterator Class Reference

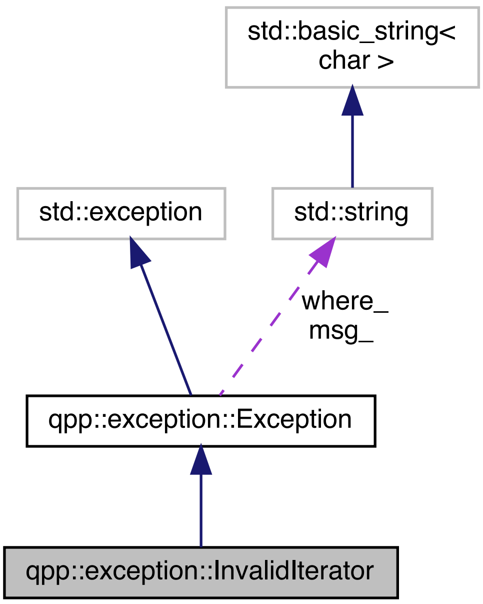
Invalid iterator.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::InvalidIterator:



Collaboration diagram for qpp::exception::InvalidIterator:



Public Member Functions

- std::string description () const override

  Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.21.1 Detailed Description

Invalid iterator.

7.21.2 Member Function Documentation

7.21.2.1 description()

```
std::string qpp::exception::InvalidIterator::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.21.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

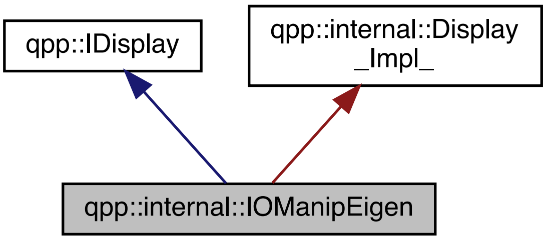
The documentation for this class was generated from the following file:

- classes/exception.h

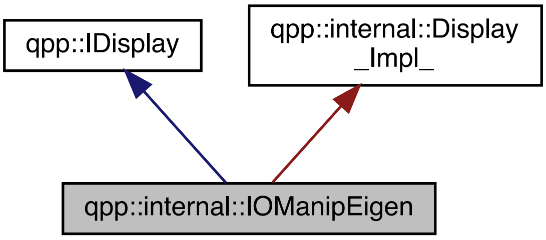
7.22 qpp::internal::IOManipEigen Class Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipEigen:



Collaboration diagram for qpp::internal::IOManipEigen:



Public Member Functions

- template< typename Derived >
  IOManipEigen (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)
- IOManipEigen (const cplx z, double chop=qpp::chop)

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  Must be overridden by all derived classes.

Private Attributes

- cmat A_
- double chop_

7.22.1 Constructor & Destructor Documentation

7.22.1.1 IOManipEigen() [1/2]

```
template<typename Derived >
qpp::internal::IOManipEigen::IOManipEigen (
            const Eigen::MatrixBase< Derived > & A,
            double chop = qpp::chop )  [inline], [explicit]
```

7.22.1.2 IOManipEigen() [2/2]

```
qpp::internal::IOManipEigen::IOManipEigen (
            const cplx z,
            double chop = qpp::chop )  [inline], [explicit]
```

7.22.2 Member Function Documentation

7.22.2.1 display()

```
std::ostream& qpp::internal::IOManipEigen::display (
            std::ostream & os ) const  [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implements qpp::IDisplay.

7.22.3 Member Data Documentation

7.22.3.1 A_

```
cmat qpp::internal::IOManipEigen::A_  [private]
```

7.22.3.2 chop_

```
double qpp::internal::IOManipEigen::chop_  [private]
```

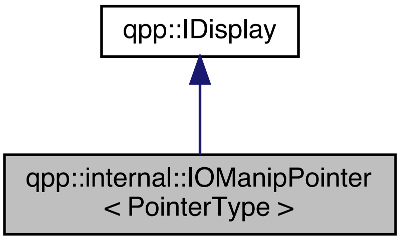
The documentation for this class was generated from the following file:

- internal/classes/iomanip.h

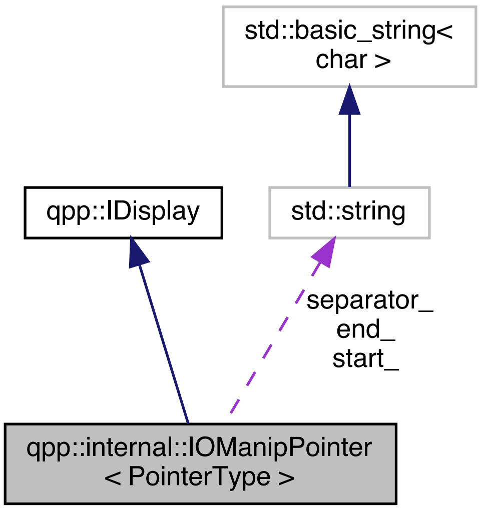
7.23 qpp::internal::IOManipPointer< PointerType > Class Template Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipPointer< PointerType >:



Collaboration diagram for qpp::internal::IOManipPointer< PointerType >:



Public Member Functions

- IOManipPointer (const PointerType ∗p, idx N, const std::string &separator, const std::string &start="[", const std::string &end="]")
- IOManipPointer (const IOManipPointer &)=default
- IOManipPointer & operator= (const IOManipPointer &)=default

Private Member Functions

- std::ostream & display (std::ostream &os) const override

    Must be overridden by all derived classes.

Private Attributes

- const PointerType ∗ p_
- idx N_
- std::string separator_
- std::string start_
- std::string end_

7.23.1 Constructor & Destructor Documentation

7.23.1.1 IOManipPointer() [1/2]

```
template<typename PointerType>
qpp::internal::IOManipPointer< PointerType >::IOManipPointer (
            const PointerType * p,
            idx N,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]" )  [inline], [explicit]
```

7.23.1.2 IOManipPointer() [2/2]

```
template<typename PointerType>
qpp::internal::IOManipPointer< PointerType >::IOManipPointer (
            const IOManipPointer< PointerType > & )  [default]
```

7.23.2 Member Function Documentation

7.23.2.1 display()

```
template<typename PointerType>
std::ostream& qpp::internal::IOManipPointer< PointerType >::display (
            std::ostream & os ) const  [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implements qpp::IDisplay.

7.23.2.2 operator=()

```
template<typename PointerType>
IOManipPointer& qpp::internal::IOManipPointer< PointerType >::operator= (
            const IOManipPointer< PointerType > &  )  [default]
```

7.23.3 Member Data Documentation

7.23.3.1 end_

```
template<typename PointerType>
std::string qpp::internal::IOManipPointer< PointerType >::end_  [private]
```

7.23.3.2 N_

```
template<typename PointerType>
idx qpp::internal::IOManipPointer< PointerType >::N_  [private]
```

7.23.3.3 p_

```
template<typename PointerType>
const PointerType* qpp::internal::IOManipPointer< PointerType >::p_  [private]
```

7.23.3.4 separator_

```
template<typename PointerType>
std::string qpp::internal::IOManipPointer< PointerType >::separator_ [private]
```

7.23.3.5 start_

```
template<typename PointerType>
std::string qpp::internal::IOManipPointer< PointerType >::start_ [private]
```

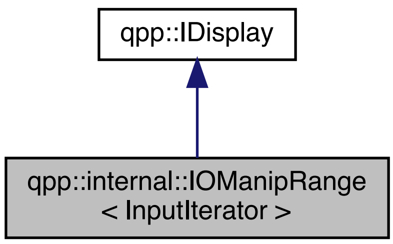
The documentation for this class was generated from the following file:

- internal/classes/iomanip.h

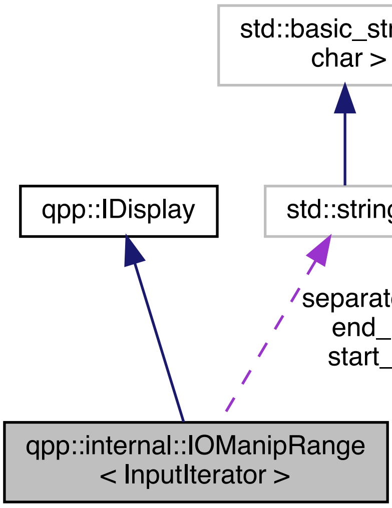
7.24 qpp::internal::IOManipRange< InputIterator > Class Template Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipRange< InputIterator >:



Collaboration diagram for qpp::internal::IOManipRange< InputIterator >:



Public Member Functions

- IOManipRange (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")
- IOManipRange (const IOManipRange &)=default
- IOManipRange & operator= (const IOManipRange &)=default

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  Must be overridden by all derived classes.

Private Attributes

- InputIterator first_
- InputIterator last_
- std::string separator_
- std::string start_
- std::string end_

7.24.1 Constructor & Destructor Documentation

7.24.1.1 IOManipRange() [1/2]

```
template<typename InputIterator>
qpp::internal::IOManipRange< InputIterator >::IOManipRange (
            InputIterator first,
            InputIterator last,
            const std::string & separator,
            const std::string & start = "[",
            const std::string & end = "]" ) [inline], [explicit]
```

7.24.1.2 IOManipRange() [2/2]

```
template<typename InputIterator>
qpp::internal::IOManipRange< InputIterator >::IOManipRange (
            const IOManipRange< InputIterator > & ) [default]
```

7.24.2 Member Function Documentation

7.24.2.1 display()

```
template<typename InputIterator>
std::ostream& qpp::internal::IOManipRange< InputIterator >::display (
            std::ostream & os ) const [inline], [override], [private], [virtual]
```

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implements qpp::IDisplay.

7.24.2.2 operator=()

```
template<typename InputIterator>
IOManipRange& qpp::internal::IOManipRange< InputIterator >::operator= (
            const IOManipRange< InputIterator > & ) [default]
```

7.24.3 Member Data Documentation

7.24.3.1 end_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::end_ [private]
```

7.24.3.2 first_

```
template<typename InputIterator>
InputIterator qpp::internal::IOManipRange< InputIterator >::first_ [private]
```

7.24.3.3 last_

```
template<typename InputIterator>
InputIterator qpp::internal::IOManipRange< InputIterator >::last_ [private]
```

7.24.3.4 separator_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::separator_ [private]
```

7.24.3.5 start_

```
template<typename InputIterator>
std::string qpp::internal::IOManipRange< InputIterator >::start_ [private]
```

The documentation for this class was generated from the following file:

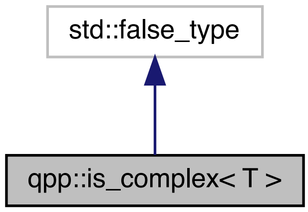
- internal/classes/iomanip.h

7.25 qpp::is_complex< T > Struct Template Reference

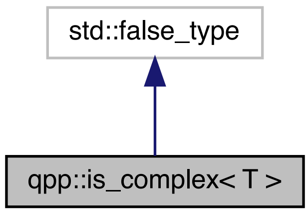
Checks whether the type is a complex type.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_complex< T >:



Collaboration diagram for qpp::is_complex< T >:



7.25.1 Detailed Description

template<typename T>
struct qpp::is_complex< T >

Checks whether the type is a complex type.

Provides the constant member *value* which is equal to *true*, if the type is a complex type, i.e. *std::complex<T>*

The documentation for this struct was generated from the following file:

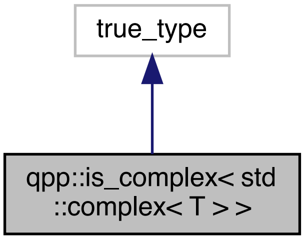
- traits.h

7.26 qpp::is_complex< std::complex< T > > Struct Template Reference

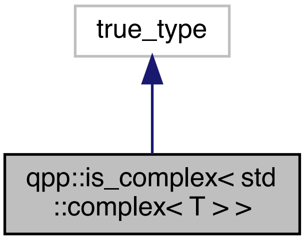
Checks whether the type is a complex number type, specialization for complex types.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_complex< std::complex< T > >:



Collaboration diagram for qpp::is_complex< std::complex< T > >:



7.26.1 Detailed Description

template<typename T>
struct qpp::is_complex< std::complex< T > >

Checks whether the type is a complex number type, specialization for complex types.

The documentation for this struct was generated from the following file:

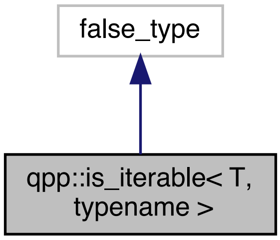
- traits.h

7.27 qpp::is_iterable< T, typename > Struct Template Reference

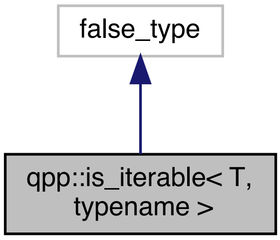
Checks whether *T* is compatible with an STL-like iterable container.

`#include <traits.h>`

Inheritance diagram for qpp::is_iterable< T, typename >:



Collaboration diagram for qpp::is_iterable< T, typename >:



7.27.1 Detailed Description

template<typename T, typename = void>
struct qpp::is_iterable< T, typename >

Checks whether *T* is compatible with an STL-like iterable container.

Provides the constant member *value* which is equal to *true*, if *T* is compatible with an iterable container, i.e. provides at least *begin()* and *end()* member functions and allows de-referencing. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

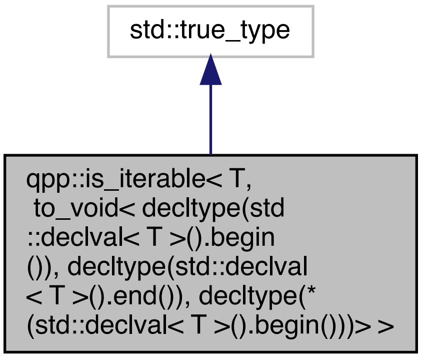
- traits.h

7.28 qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), decltype(∗(std::declval< T >().begin()))> > Struct Template Reference

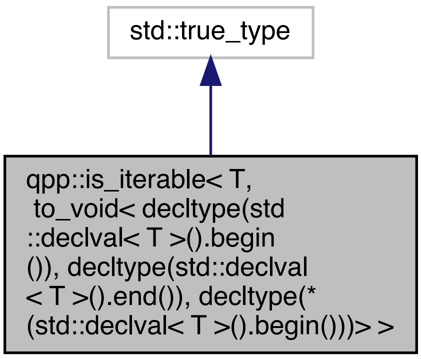
Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), decltype(∗(std::declval< T >().begin()))> >:



Collaboration diagram for qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), decltype(∗(std::declval< T >().begin()))> >:



7.28.1 Detailed Description

template<typename T>
struct qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), decltype(*(std::declval< T >().begin()))> >

Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

The documentation for this struct was generated from the following file:

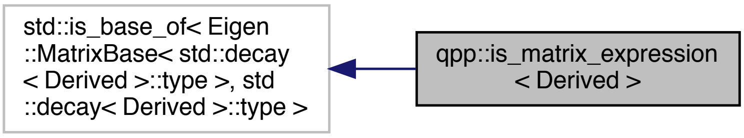
- traits.h

7.29 qpp::is_matrix_expression< Derived > Struct Template Reference

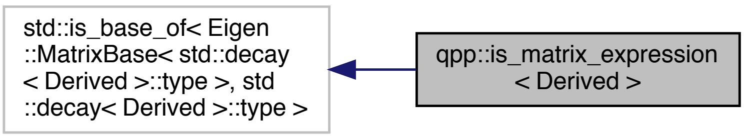
Checks whether the type is an Eigen matrix expression.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_matrix_expression< Derived >:



Collaboration diagram for qpp::is_matrix_expression< Derived >:



7.29.1 Detailed Description

template<typename Derived>
struct qpp::is_matrix_expression< Derived >

Checks whether the type is an Eigen matrix expression.

Provides the constant member *value* which is equal to *true*, if the type is an Eigen matrix expression of type *Eigen::MatrixBase<Derived>*. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

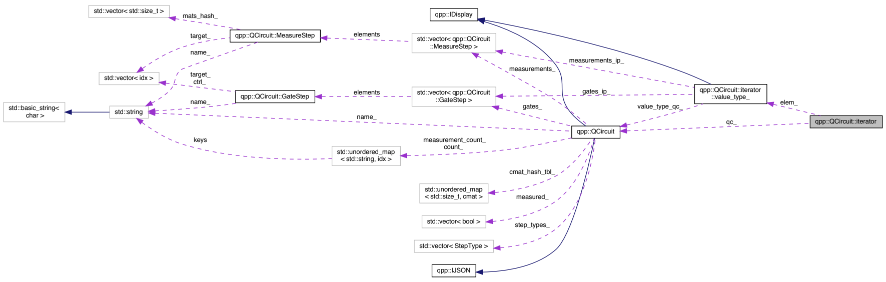
- traits.h

7.30 qpp::QCircuit::iterator Class Reference

Quantum circuit bound-checking (safe) iterator.

```
#include <classes/circuits/circuits.h>
```

Collaboration diagram for qpp::QCircuit::iterator:



Classes

- class value_type_

    Value type class for qpp::QCircuit::iterator.

Public Types

- using difference_type = long long

    iterator trait
- using value_type = value_type_

    iterator trait
- using pointer = const value_type ∗

    iterator trait
- using reference = const value_type &

    iterator trait
- using iterator_category = std::forward_iterator_tag

    iterator trait

Public Member Functions

- iterator ()=default

    Default constructor.
- iterator (const iterator &)=default

    Default copy constructor.
- iterator & operator= (const iterator &)=default

    Default copy assignment operator.
- iterator & operator++ ()

    Prefix increment operator.
- iterator operator++ (int)

    Postfix increment operator.

- bool operator== (const iterator &rhs) const

  Equality operator.
- bool operator!= (iterator rhs) const

  Inequality operator.
- const value_type_ & operator∗ () const

  Safe de-referencing operator.
- void set_begin_ (const QCircuit ∗qc)

  Sets the iterator to std::begin(this)
- void set_end_ (const QCircuit ∗qc)

  Sets the iterator to std::begin(this)

Private Attributes

- const QCircuit ∗ qc_ {nullptr}

  < non-owning pointer to the parent const quantum circuit
- value_type_ elem_ {nullptr}

7.30.1 Detailed Description

Quantum circuit bound-checking (safe) iterator.

Note

The iterator is a const_iterator by default

7.30.2 Member Typedef Documentation

7.30.2.1 difference_type

```
using qpp::QCircuit::iterator::difference_type = long long
```

iterator trait

7.30.2.2 iterator_category

```
using qpp::QCircuit::iterator::iterator_category = std::forward_iterator_tag
```

iterator trait

7.30.2.3 pointer

```
using qpp::QCircuit::iterator::pointer = const value_type*
```

iterator trait

7.30.2.4 reference

```
using qpp::QCircuit::iterator::reference = const value_type&
```

iterator trait

7.30.2.5 value_type

```
using qpp::QCircuit::iterator::value_type = value_type_
```

iterator trait

7.30.3 Constructor & Destructor Documentation

7.30.3.1 iterator() [1/2]

```
qpp::QCircuit::iterator::iterator ( )  [default]
```

Default constructor.

7.30.3.2 iterator() [2/2]

```
qpp::QCircuit::iterator::iterator (
            const iterator & )  [default]
```

Default copy constructor.

7.30.4 Member Function Documentation

7.30.4.1 operator"!=()

```
bool qpp::QCircuit::iterator::operator!= (
            iterator rhs ) const  [inline]
```

Inequality operator.

Parameters

rhs	Iterator against which the inequality is being tested

Returns

True if the iterators are not equal (bit by bit), false otherwise

7.30.4.2 operator*()

```
const value_type_& qpp::QCircuit::iterator::operator* ( ) const  [inline]
```

Safe de-referencing operator.

Returns

Constant reference to the iterator element

7.30.4.3 operator++() [1/2]

```
iterator& qpp::QCircuit::iterator::operator++ ( )  [inline]
```

Prefix increment operator.

Returns

Reference to the current instance

7.30.4.4 operator++() [2/2]

```
iterator qpp::QCircuit::iterator::operator++ (
            int  )  [inline]
```

Postfix increment operator.

Returns

Copy of the current instance before the increment

7.30.4.5 operator=()

```
iterator& qpp::QCircuit::iterator::operator= (
            const iterator & )  [default]
```

Default copy assignment operator.

Returns

Reference to the current instance

7.30.4.6 operator==()

```
bool qpp::QCircuit::iterator::operator== (
            const iterator & rhs ) const  [inline]
```

Equality operator.

Parameters

rhs	Iterator against which the equality is being tested

Returns

True if the iterators are equal, false otherwise

7.30.4.7 set_begin_()

```
void qpp::QCircuit::iterator::set_begin_ (
            const QCircuit * qc )  [inline]
```

Sets the iterator to std::begin(this)

Parameters

qc	Pointer to constant quantum circuit

7.30.4.8 set_end_()

```
void qpp::QCircuit::iterator::set_end_ (
            const QCircuit * qc )  [inline]
```

Sets the iterator to std::begin(this)

Parameters

qc	Pointer to constant quantum circuit

7.30.5 Member Data Documentation

7.30.5.1 elem_

```
value_type_ qpp::QCircuit::iterator::elem_ {nullptr}  [private]
```

7.30.5.2 qc_

```
const QCircuit* qpp::QCircuit::iterator::qc_ {nullptr}  [private]
```

< non-owning pointer to the parent const quantum circuit

The documentation for this class was generated from the following file:

- classes/circuits/circuits.h

7.31 qpp::make_void< Ts > Struct Template Reference

Helper for qpp::to_void<> alias template.

```
#include <traits.h>
```

Public Types

- typedef void type

7.31.1 Detailed Description

template<typename... Ts>
struct qpp::make_void< Ts >

Helper for qpp::to_void<> alias template.

See also

qpp::to_void<>

7.31.2 Member Typedef Documentation

7.31.2.1 type

```
template<typename... Ts>
typedef void qpp::make_void< Ts >::type
```

The documentation for this struct was generated from the following file:

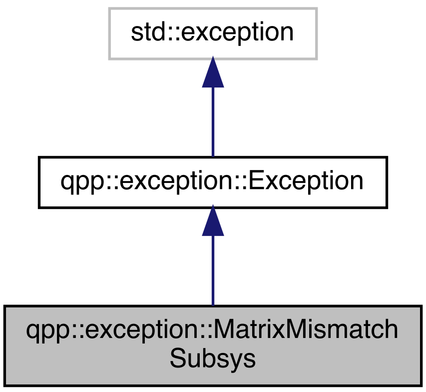
- traits.h

7.32 qpp::exception::MatrixMismatchSubsys Class Reference

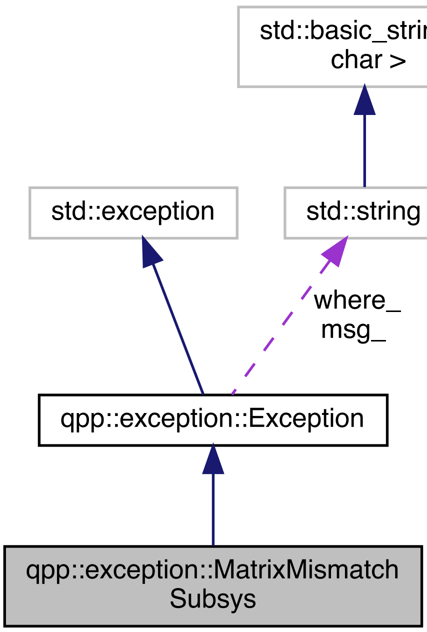
Matrix mismatch subsystems exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixMismatchSubsys:



Collaboration diagram for qpp::exception::MatrixMismatchSubsys:



Public Member Functions

- std::string description () const override

  Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.32.1 Detailed Description

Matrix mismatch subsystems exception.

Matrix size mismatch subsystem sizes (e.g. in qpp::apply())

7.32.2 Member Function Documentation

7.32.2.1 description()

```
std::string qpp::exception::MatrixMismatchSubsys::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.32.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

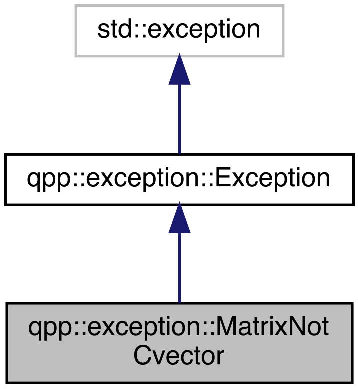
- classes/exception.h

7.33 qpp::exception::MatrixNotCvector Class Reference

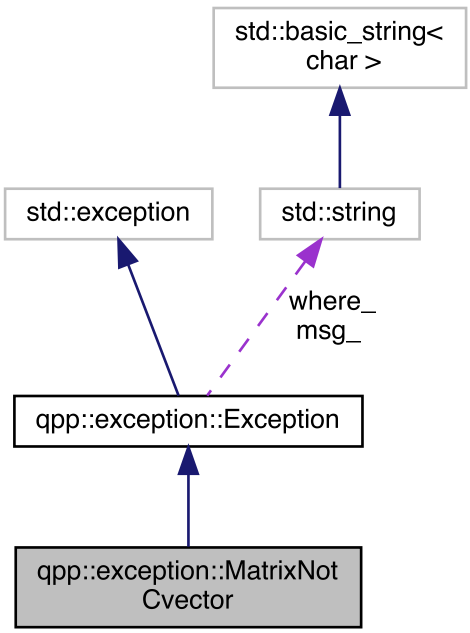
Matrix is not a column vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotCvector:



Collaboration diagram for qpp::exception::MatrixNotCvector:



Public Member Functions

- std::string description () const override

Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.33.1 Detailed Description

Matrix is not a column vector exception.

Eigen::Matrix is not a column vector

7.33.2 Member Function Documentation

7.33.2.1 description()

```
std::string qpp::exception::MatrixNotCvector::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.33.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

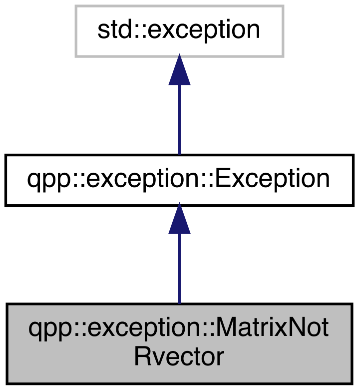
- classes/exception.h

7.34 qpp::exception::MatrixNotRvector Class Reference

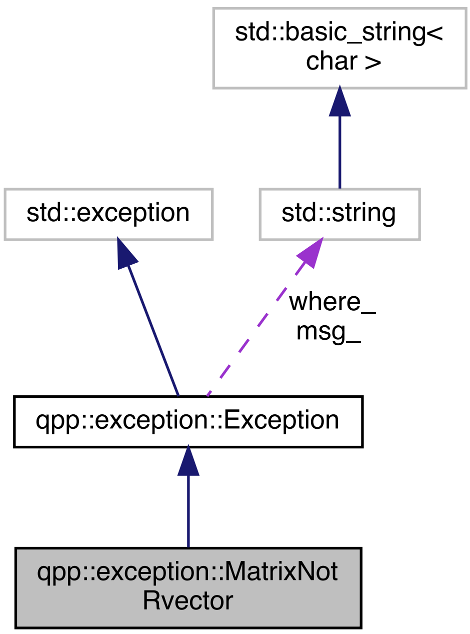
Matrix is not a row vector exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::MatrixNotRvector:



Collaboration diagram for qpp::exception::MatrixNotRvector:



Public Member Functions

- std::string description () const override

Exception description.

- Exception (const std::string &where)

  Constructs an exception.

7.34.1 Detailed Description

Matrix is not a row vector exception.

Eigen::Matrix is not a row vector

7.34.2 Member Function Documentation

7.34.2.1 description()

```
std::string qpp::exception::MatrixNotRvector::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.34.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

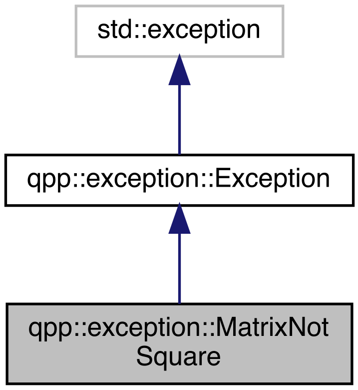
- classes/exception.h

7.35 qpp::exception::MatrixNotSquare Class Reference

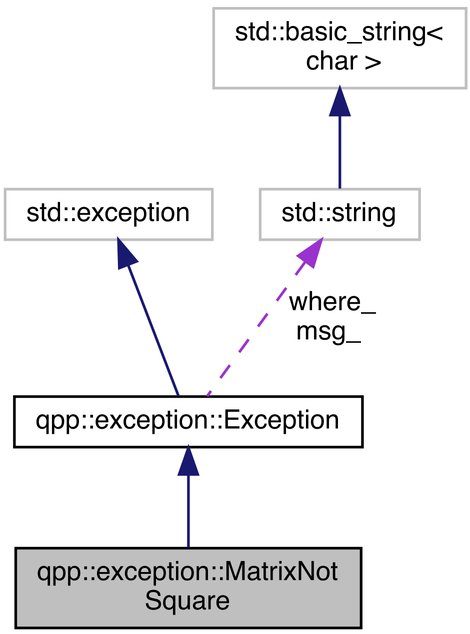
Matrix is not square exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquare:



Collaboration diagram for qpp::exception::MatrixNotSquare:



Public Member Functions

- std::string description () const override

Exception description.

- Exception (const std::string &where)

  Constructs an exception.

7.35.1 Detailed Description

Matrix is not square exception.

Eigen::Matrix is not a square matrix

7.35.2 Member Function Documentation

7.35.2.1 description()

```
std::string qpp::exception::MatrixNotSquare::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.35.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

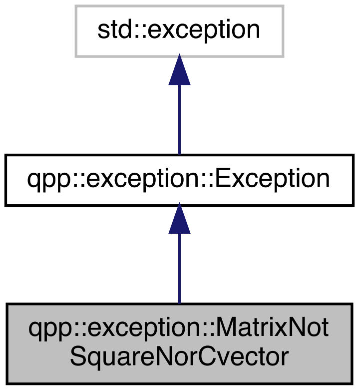
- classes/exception.h

7.36 qpp::exception::MatrixNotSquareNorCvector Class Reference

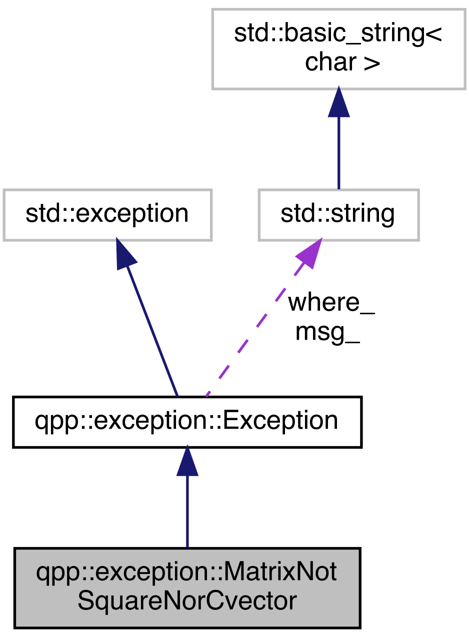
Matrix is not square nor column vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorCvector:



Collaboration diagram for qpp::exception::MatrixNotSquareNorCvector:



Public Member Functions

- std::string description () const override

Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.36.1 Detailed Description

Matrix is not square nor column vector exception.

Eigen::Matrix is not a square matrix nor a column vector

7.36.2 Member Function Documentation

7.36.2.1 description()

`std::string qpp::exception::MatrixNotSquareNorCvector::description ( ) const [inline], [override], [virtual]`

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.36.2.2 Exception()

`qpp::exception::Exception::Exception [inline], [explicit]`

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

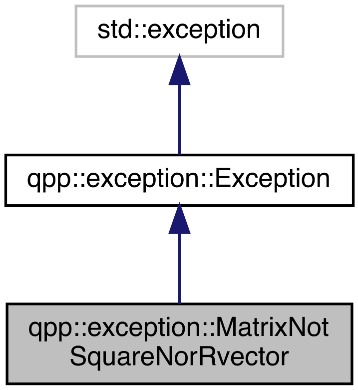
- classes/exception.h

7.37 qpp::exception::MatrixNotSquareNorRvector Class Reference

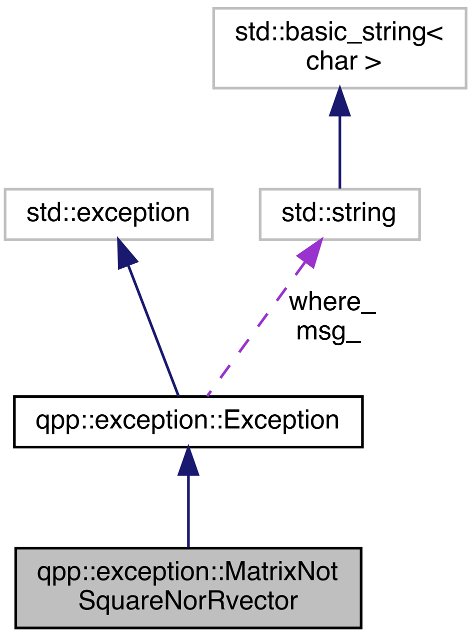
Matrix is not square nor row vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorRvector:



Collaboration diagram for qpp::exception::MatrixNotSquareNorRvector:



Public Member Functions

- std::string description () const override

Exception description.

- Exception (const std::string &where)

  Constructs an exception.

7.37.1 Detailed Description

Matrix is not square nor row vector exception.

Eigen::Matrix is not a square matrix nor a row vector

7.37.2 Member Function Documentation

7.37.2.1 description()

```
std::string qpp::exception::MatrixNotSquareNorRvector::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.37.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

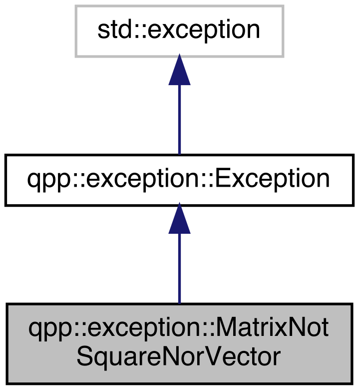
- classes/exception.h

7.38 qpp::exception::MatrixNotSquareNorVector Class Reference

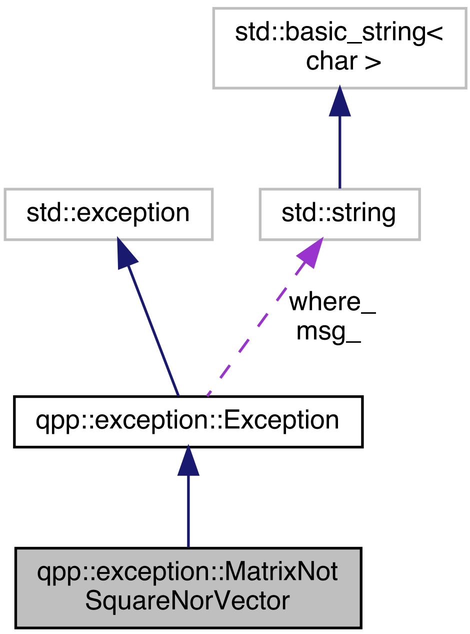
Matrix is not square nor vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotSquareNorVector:



Collaboration diagram for qpp::exception::MatrixNotSquareNorVector:



Public Member Functions

- std::string description () const override

Exception description.

- Exception (const std::string &where)

  Constructs an exception.

7.38.1 Detailed Description

Matrix is not square nor vector exception.

Eigen::Matrix is not a square matrix nor a row/column vector

7.38.2 Member Function Documentation

7.38.2.1 description()

```
std::string qpp::exception::MatrixNotSquareNorVector::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.38.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

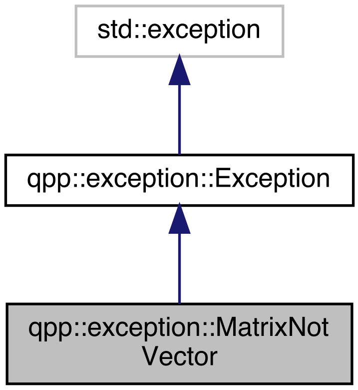
- classes/exception.h

7.39 qpp::exception::MatrixNotVector Class Reference

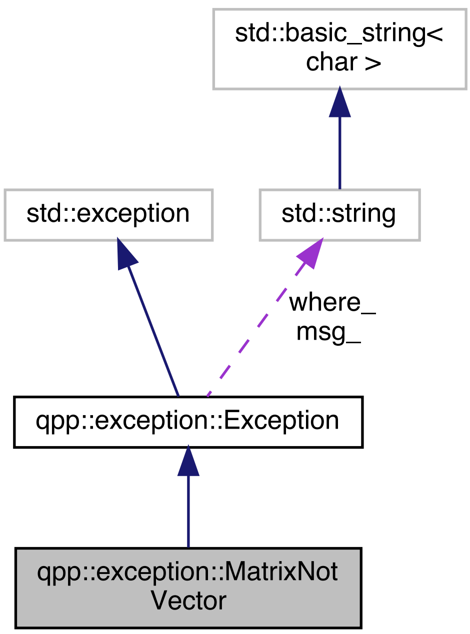
Matrix is not a vector exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::MatrixNotVector:



Collaboration diagram for qpp::exception::MatrixNotVector:



Public Member Functions

- std::string description () const override

Exception description.

- Exception (const std::string &where)

  Constructs an exception.

7.39.1 Detailed Description

Matrix is not a vector exception.

Eigen::Matrix is not a row or column vector

7.39.2 Member Function Documentation

7.39.2.1 description()

```
std::string qpp::exception::MatrixNotVector::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.39.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

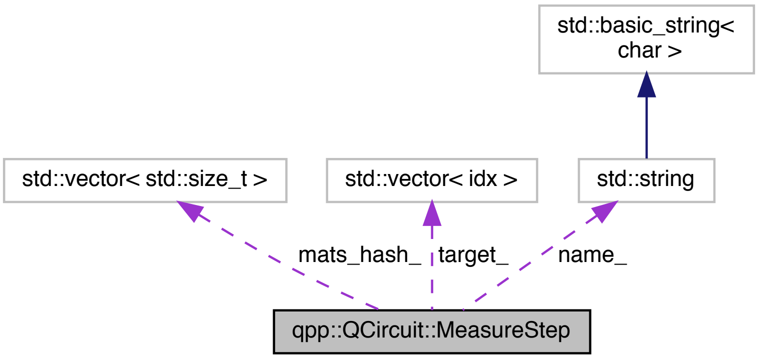
- classes/exception.h

7.40 qpp::QCircuit::MeasureStep Struct Reference

One step consisting only of measurements in the circuit.

`#include <classes/circuits/circuits.h>`

Collaboration diagram for qpp::QCircuit::MeasureStep:



Public Member Functions

- MeasureStep ()=default

    Default constructor.
- MeasureStep (MeasureType measurement_type, const std::vector< std::size_t > &mats_hash, const std↩ ::vector< idx > &target, idx c_reg, std::string name={})

    Constructs a measurement step instance.

Public Attributes

- MeasureType measurement_type_ = MeasureType::NONE

    measurement type
- std::vector< std::size_t > mats_hash_
- std::vector< idx > target_

    target where the measurement is applied
- idx c_reg_ {}
- std::string name_

    custom name of the step

7.40.1 Detailed Description

One step consisting only of measurements in the circuit.

7.40.2 Constructor & Destructor Documentation

7.40.2.1 MeasureStep() [1/2]

```
qpp::QCircuit::MeasureStep::MeasureStep ( )  [default]
```

Default constructor.

7.40.2.2 MeasureStep() [2/2]

```
qpp::QCircuit::MeasureStep::MeasureStep (
            MeasureType measurement_type,
            const std::vector< std::size_t > & mats_hash,
            const std::vector< idx > & target,
            idx c_reg,
            std::string name = {} )  [inline], [explicit]
```

Constructs a measurement step instance.

Parameters

measurement_type	Measurement type
mats_hash	Vector of hashes of the measurement matrix/matrices
target	Target qudit indexes
c_reg	Classical register where the value of the measurement is stored
name	Optional gate name

7.40.3 Member Data Documentation

7.40.3.1 c_reg_

```
idx qpp::QCircuit::MeasureStep::c_reg_ {}
```

index of the classical register where the measurement result is being stored

7.40.3.2 mats_hash_

```
std::vector<std::size_t> qpp::QCircuit::MeasureStep::mats_hash_
```

hashes of measurement matrix/matrices

7.40.3.3 measurement_type_

```
MeasureType qpp::QCircuit::MeasureStep::measurement_type_ = MeasureType::NONE
```

measurement type

7.40.3.4 name_

```
std::string qpp::QCircuit::MeasureStep::name_
```

custom name of the step

7.40.3.5 target_

```
std::vector<idx> qpp::QCircuit::MeasureStep::target_
```

target where the measurement is applied

The documentation for this struct was generated from the following file:

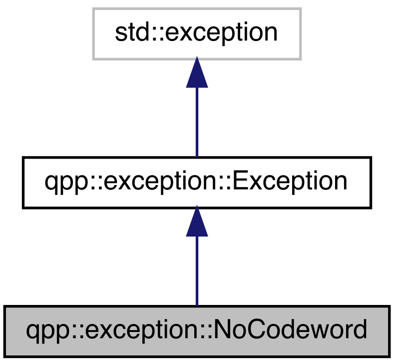
- classes/circuits/circuits.h

7.41 qpp::exception::NoCodeword Class Reference

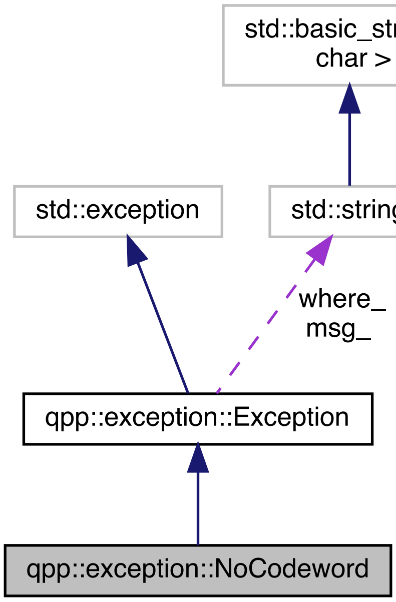
Codeword does not exist exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NoCodeword:



Collaboration diagram for qpp::exception::NoCodeword:



Public Member Functions

- std::string description () const override
    Exception description.
- Exception (const std::string &where)
    Constructs an exception.

7.41.1 Detailed Description

Codeword does not exist exception.

Codeword does not exist, thrown when calling qpp::Codes::codeword() with an invalid index

7.41.2 Member Function Documentation

7.41.2.1 description()

`std::string qpp::exception::NoCodeword::description ( ) const [inline], [override], [virtual]`

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.41.2.2 Exception()

```
qpp::exception::Exception::Exception [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

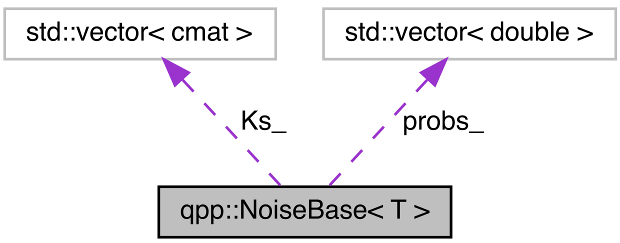
- classes/exception.h

7.42 qpp::NoiseBase< T > Class Template Reference

Base class for all noise models, derive your particular noise model.

```
#include <classes/noise.h>
```

Collaboration diagram for qpp::NoiseBase< T >:



Public Types

- using noise_type = T

Public Member Functions

- template<typename U = noise_type>
  NoiseBase (const std::vector< cmat > &Ks, typename std::enable_if< std::is_same< NoiseType::StateDependent, U >::value >::type ∗=nullptr)

  Constructs a noise instance for StateDependent noise type.

- template<typename U = noise_type>
  NoiseBase (const std::vector< cmat > &Ks, const std::vector< double > &probs, typename std::enable_if< std::is_same< NoiseType::StateIndependent, U >::value >::type *=nullptr)

  Constructs a noise instance for StateIndependent noise type.
- virtual ~NoiseBase ()=default

  Default virtual destructor.
- idx get_d () const noexcept

  Qudit dimension.
- std::vector< cmat > get_Ks () const

  Vector of noise operators.
- std::vector< double > get_probs () const

  Vector of probabilities corresponding to each noise operator.
- idx get_last_idx () const

  Index of the last occurring noise element.
- double get_last_p () const

  Probability of the last occurring noise element.
- cmat get_last_K () const

  Last occurring noise element.
- virtual cmat operator() (const cmat &state) const

  Function invocation operator, applies the underlying noise model on the state vector or density matrix state.
- virtual cmat operator() (const cmat &state, idx target) const

  Function invocation operator, applies the underlying noise model on qudit target of the multi-partite state vector or density matrix state.
- virtual cmat operator() (const cmat &state, const std::vector< idx > &target) const

  Function invocation operator, applies the underlying correlated noise model on qudits specified by target of the multi-partite state vector or density matrix state.

Protected Member Functions

- void compute_probs_ (const cmat &state, const std::vector< idx > &target) const

  Compute probability outcomes for StateDependent noise type, otherwise returns without performing any operation (no-op)
- cmat compute_state_ (const cmat &state, const std::vector< idx > &target) const

  Compute the resulting state after the noise was applied.

Protected Attributes

- const std::vector< cmat > Ks_

  Kraus operators.
- std::vector< double > probs_

  probabilities
- idx d_ {}

  qudit dimension
- idx i_ {}

  index of the last occurring noise element
- bool generated_ {false}

  invoked, or if the noise is state-independent

7.42.1 Detailed Description

template<class T>
class qpp::NoiseBase< T >

Base class for all noise models, derive your particular noise model.

7.42.2 Member Typedef Documentation

7.42.2.1 noise_type

```
template<class T>
using qpp::NoiseBase< T >::noise_type = T
```

7.42.3 Constructor & Destructor Documentation

7.42.3.1 NoiseBase() [1/2]

```
template<class T>
template<typename U = noise_type>
qpp::NoiseBase< T >::NoiseBase (
            const std::vector< cmat > & Ks,
            typename std::enable_if< std::is_same< NoiseType::StateDependent, U >::value >↩
::type * = nullptr ) [inline], [explicit]
```

Constructs a noise instance for StateDependent noise type.

Note

SFINAEd-out for StateIndependent noise

Parameters

Ks	Vector of noise (Kraus) operators that specify the noise

7.42.3.2 NoiseBase() [2/2]

```
template<class T>
template<typename U = noise_type>
```

```
qpp::NoiseBase< T >::NoiseBase (
            const std::vector< cmat > & Ks,
            const std::vector< double > & probs,
            typename std::enable_if< std::is_same< NoiseType::StateIndependent, U >::value
>::type * = nullptr ) [inline], [explicit]
```

Constructs a noise instance for StateIndependent noise type.

Note

SFINAEd-out for StateDependent noise

Parameters

Ks	Vector of noise (Kraus) operators that specify the noise
probs	Vector of probabilities corresponding to each Kraus operator

7.42.3.3 ~NoiseBase()

```
template<class T>
virtual qpp::NoiseBase< T >::~NoiseBase ( ) [virtual], [default]
```

Default virtual destructor.

7.42.4 Member Function Documentation

7.42.4.1 compute_probs_()

```
template<class T>
void qpp::NoiseBase< T >::compute_probs_ (
            const cmat & state,
            const std::vector< idx > & target ) const [inline], [protected]
```

Compute probability outcomes for StateDependent noise type, otherwise returns without performing any operation (no-op)

Parameters

state	State vector or density matrix
target	Qudit indexes where the noise is applied

7.42.4.2 compute_state_()

```
template<class T>
cmat qpp::NoiseBase< T >::compute_state_ (
            const cmat & state,
            const std::vector< idx > & target ) const [inline], [protected]
```

Compute the resulting state after the noise was applied.

Parameters

state	State vector or density matrix
target	Qudit indexes where the noise is applied

Returns

Resulting state after the noise was applied

7.42.4.3 get_d()

```
template<class T>
idx qpp::NoiseBase< T >::get_d ( ) const [inline], [noexcept]
```

Qudit dimension.

Returns

Qudit dimension

7.42.4.4 get_Ks()

```
template<class T>
std::vector<cmat> qpp::NoiseBase< T >::get_Ks ( ) const [inline]
```

Vector of noise operators.

Returns

Vector of noise operators

7.42.4.5 get_last_idx()

```
template<class T>
idx qpp::NoiseBase< T >::get_last_idx ( ) const  [inline]
```

Index of the last occurring noise element.

Returns

Index of the last occurring noise element

7.42.4.6 get_last_K()

```
template<class T>
cmat qpp::NoiseBase< T >::get_last_K ( ) const  [inline]
```

Last occurring noise element.

Returns

Last occurring noise element

7.42.4.7 get_last_p()

```
template<class T>
double qpp::NoiseBase< T >::get_last_p ( ) const  [inline]
```

Probability of the last occurring noise element.

Returns

Probability of the last occurring noise element

7.42.4.8 get_probs()

```
template<class T>
std::vector<double> qpp::NoiseBase< T >::get_probs ( ) const  [inline]
```

Vector of probabilities corresponding to each noise operator.

Returns

Probability vector

7.42.4.9 operator()() [1/3]

```
template<class T>
virtual cmat qpp::NoiseBase< T >::operator() (
             const cmat & state ) const  [inline], [virtual]
```

Function invocation operator, applies the underlying noise model on the state vector or density matrix *state*.

Parameters

state	State vector or density matrix

Returns

Resulting state vector or density matrix

7.42.4.10 operator()() [2/3]

```
template<class T>
virtual cmat qpp::NoiseBase< T >::operator() (
            const cmat & state,
            idx target ) const  [inline], [virtual]
```

Function invocation operator, applies the underlying noise model on qudit *target* of the multi-partite state vector or density matrix *state*.

Parameters

state	Multi-partite state vector or density matrix
target	Qudit index where the noise is applied

Returns

Resulting state vector or density matrix

7.42.4.11 operator()() [3/3]

```
template<class T>
virtual cmat qpp::NoiseBase< T >::operator() (
            const cmat & state,
            const std::vector< idx > & target ) const  [inline], [virtual]
```

Function invocation operator, applies the underlying correlated noise model on qudits specified by *target* of the multi-partite state vector or density matrix *state*.

Parameters

state	Multi-partite state vector or density matrix
target	Qudit indexes where the correlated noise is applied

Returns

Resulting state vector or density matrix

7.42.5 Member Data Documentation

7.42.5.1 d_

```
template<class T>
idx qpp::NoiseBase< T >::d_ {}  [mutable], [protected]
```

qudit dimension

7.42.5.2 generated_

```
template<class T>
bool qpp::NoiseBase< T >::generated_ {false}  [mutable], [protected]
```

invoked, or if the noise is state-independent

set to true after compute_state_() is

7.42.5.3 i_

```
template<class T>
idx qpp::NoiseBase< T >::i_ {}  [mutable], [protected]
```

index of the last occurring noise element

7.42.5.4 Ks_

```
template<class T>
const std::vector<cmat> qpp::NoiseBase< T >::Ks_  [protected]
```

Kraus operators.

7.42.5.5 probs_

```
template<class T>
std::vector<double> qpp::NoiseBase< T >::probs_ [mutable], [protected]
```

probabilities

The documentation for this class was generated from the following file:

- classes/noise.h

7.43 qpp::NoiseType Class Reference

Contains template tags used to specify the noise type.

```
#include <classes/noise.h>
```

Classes

- class StateDependent

  Template tag, used whenever the noise is state-dependent.
- class StateIndependent

  Template tag, used whenever the noise is state-independent.

7.43.1 Detailed Description

Contains template tags used to specify the noise type.

The documentation for this class was generated from the following file:

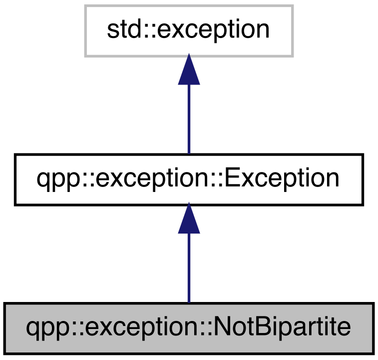
- classes/noise.h

7.44 qpp::exception::NotBipartite Class Reference

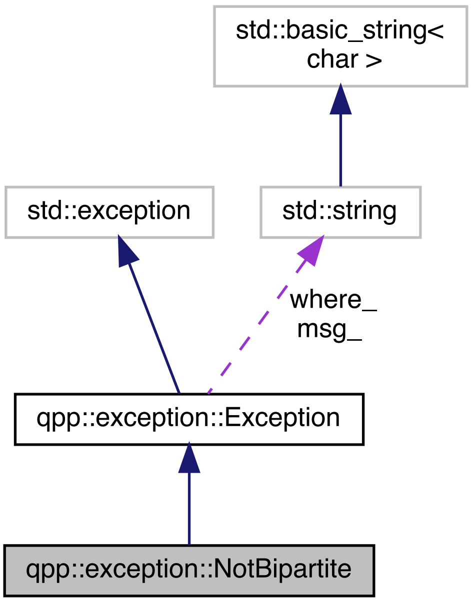
Not bi-partite exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotBipartite:



Collaboration diagram for qpp::exception::NotBipartite:



Public Member Functions

- std::string description () const override

    Exception description.
- Exception (const std::string &where)

    Constructs an exception.

7.44.1 Detailed Description

Not bi-partite exception.

std::vector<idx> of dimensions has size different from 2

7.44.2 Member Function Documentation

7.44.2.1 description()

`std::string qpp::exception::NotBipartite::description ( ) const [inline], [override], [virtual]`

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.44.2.2 Exception()

`qpp::exception::Exception::Exception [inline], [explicit]`

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

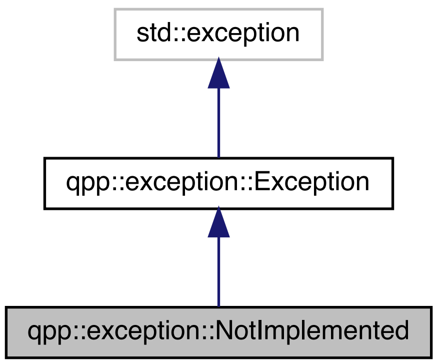
- classes/exception.h

7.45 qpp::exception::NotImplemented Class Reference

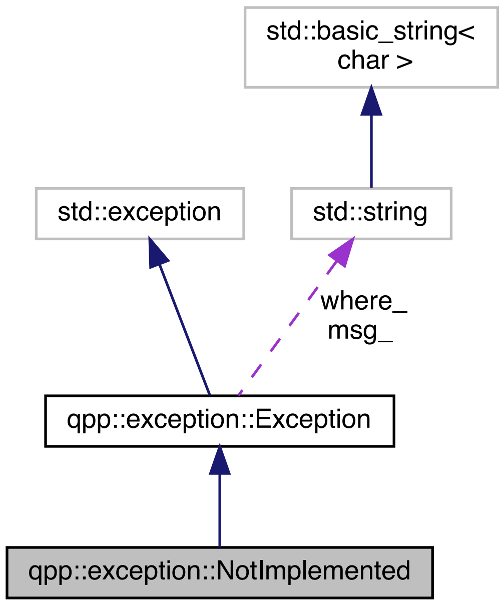
Code not yet implemented.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::NotImplemented:



Collaboration diagram for qpp::exception::NotImplemented:



Public Member Functions

- std::string description () const override

  Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.45.1 Detailed Description

Code not yet implemented.

7.45.2 Member Function Documentation

7.45.2.1 description()

```
std::string qpp::exception::NotImplemented::description ( ) const [inline], [override], [virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.45.2.2 Exception()

```
qpp::exception::Exception::Exception [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

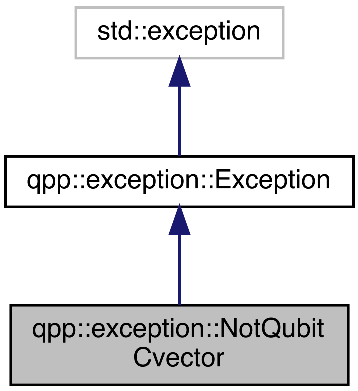
- classes/exception.h

7.46 qpp::exception::NotQubitCvector Class Reference

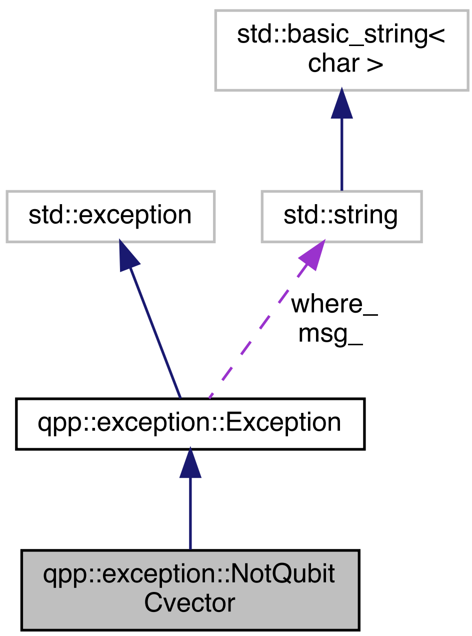
Column vector is not 2 x 1 exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::NotQubitCvector:



Collaboration diagram for qpp::exception::NotQubitCvector:



Public Member Functions

- std::string description () const override

Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.46.1 Detailed Description

Column vector is not 2 x 1 exception.

Eigen::Matrix is not 2 x 1

7.46.2 Member Function Documentation

7.46.2.1 description()

```
std::string qpp::exception::NotQubitCvector::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.46.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

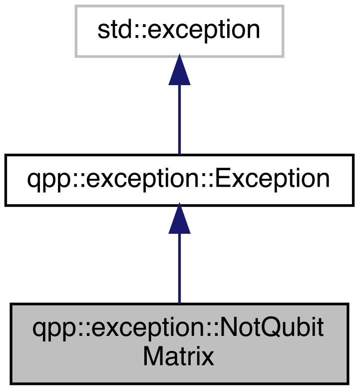
- classes/exception.h

7.47 qpp::exception::NotQubitMatrix Class Reference

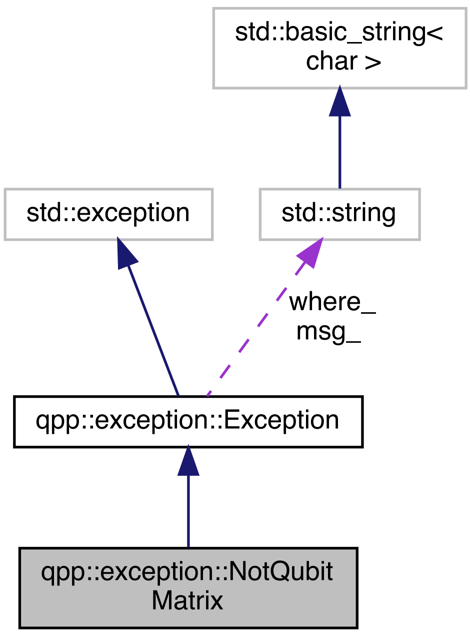
Matrix is not 2 x 2 exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::NotQubitMatrix:



Collaboration diagram for qpp::exception::NotQubitMatrix:



Public Member Functions

- std::string description () const override

Exception description.

- Exception (const std::string &where)

  Constructs an exception.

7.47.1 Detailed Description

Matrix is not 2 x 2 exception.

Eigen::Matrix is not 2 x 2

7.47.2 Member Function Documentation

7.47.2.1 description()

`std::string qpp::exception::NotQubitMatrix::description ( ) const [inline], [override], [virtual]`

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.47.2.2 Exception()

`qpp::exception::Exception::Exception [inline], [explicit]`

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

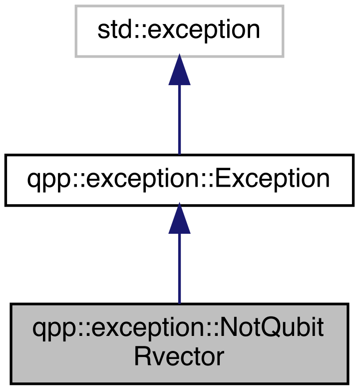
- classes/exception.h

7.48 qpp::exception::NotQubitRvector Class Reference

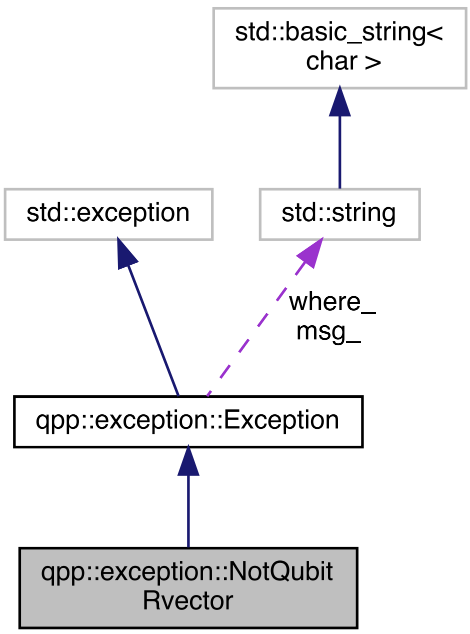
Row vector is not 1 x 2 exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::NotQubitRvector:



Collaboration diagram for qpp::exception::NotQubitRvector:



Public Member Functions

- std::string description () const override

Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.48.1 Detailed Description

Row vector is not 1 x 2 exception.

Eigen::Matrix is not 1 x 2

7.48.2 Member Function Documentation

7.48.2.1 description()

```
std::string qpp::exception::NotQubitRvector::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.48.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

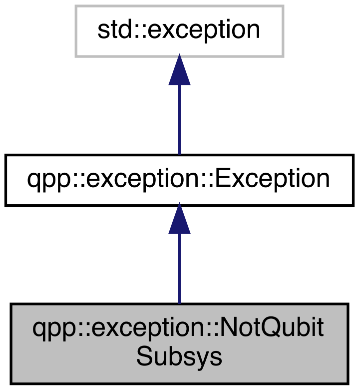
- classes/exception.h

7.49 qpp::exception::NotQubitSubsys Class Reference

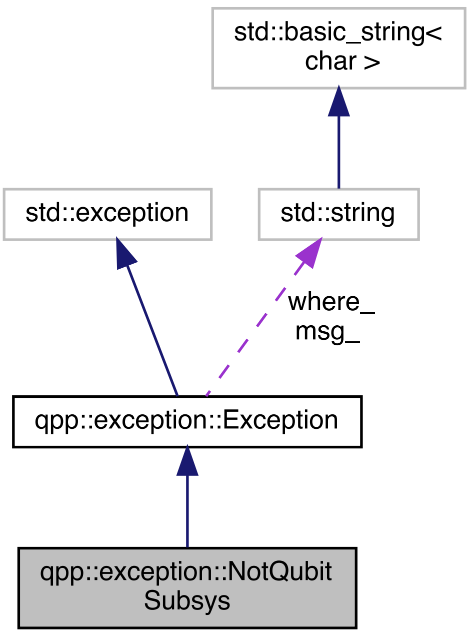
Subsystems are not qubits exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::NotQubitSubsys:



Collaboration diagram for qpp::exception::NotQubitSubsys:



Public Member Functions

- std::string description () const override

Exception description.

- Exception (const std::string &where)

    Constructs an exception.

7.49.1 Detailed Description

Subsystems are not qubits exception.

Subsystems are not 2-dimensional (qubits)

7.49.2 Member Function Documentation

7.49.2.1 description()

```
std::string qpp::exception::NotQubitSubsys::description ( ) const  [inline], [override], [virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.49.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

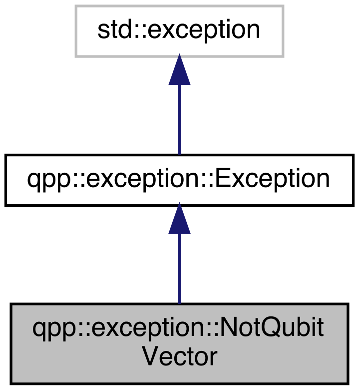
- classes/exception.h

7.50 qpp::exception::NotQubitVector Class Reference

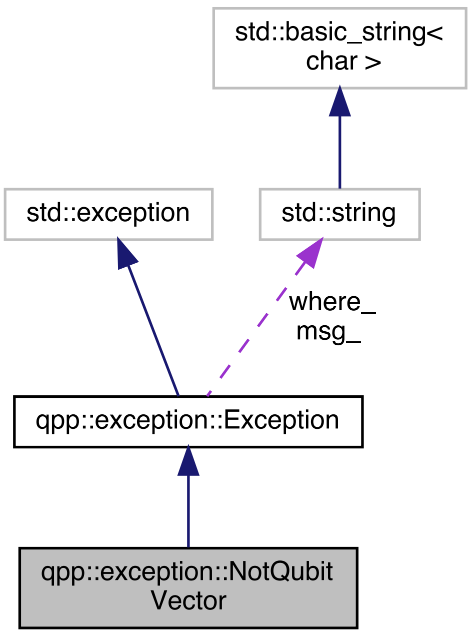
Vector is not 2 x 1 nor 1 x 2 exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::NotQubitVector:



Collaboration diagram for qpp::exception::NotQubitVector:



Public Member Functions

- std::string description () const override

Exception description.

- Exception (const std::string &where)

  Constructs an exception.

7.50.1 Detailed Description

Vector is not 2 x 1 nor 1 x 2 exception.

Eigen::Matrix is not 2 x 1 nor 1 x 2

7.50.2 Member Function Documentation

7.50.2.1 description()

`std::string qpp::exception::NotQubitVector::description ( ) const [inline], [override], [virtual]`

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.50.2.2 Exception()

`qpp::exception::Exception::Exception [inline], [explicit]`

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

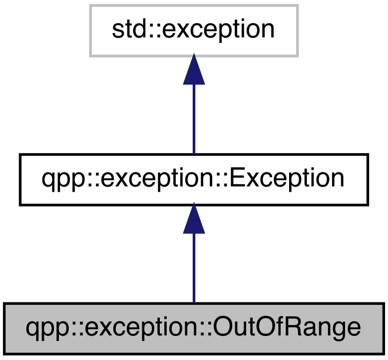
- classes/exception.h

7.51 qpp::exception::OutOfRange Class Reference

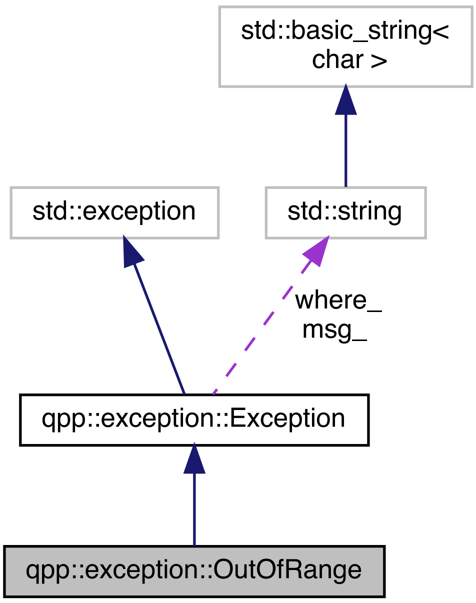
Argument out of range exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::OutOfRange:



Collaboration diagram for qpp::exception::OutOfRange:



Public Member Functions

- std::string description () const override

Exception description.

- Exception (const std::string &where)

Constructs an exception.

7.51.1 Detailed Description

Argument out of range exception.

Argument out of range

7.51.2 Member Function Documentation

7.51.2.1 description()

`std::string qpp::exception::OutOfRange::description ( ) const [inline], [override], [virtual]`

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.51.2.2 Exception()

`qpp::exception::Exception::Exception [inline], [explicit]`

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

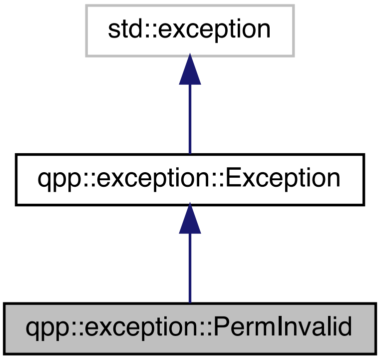
- classes/exception.h

7.52 qpp::exception::PermInvalid Class Reference

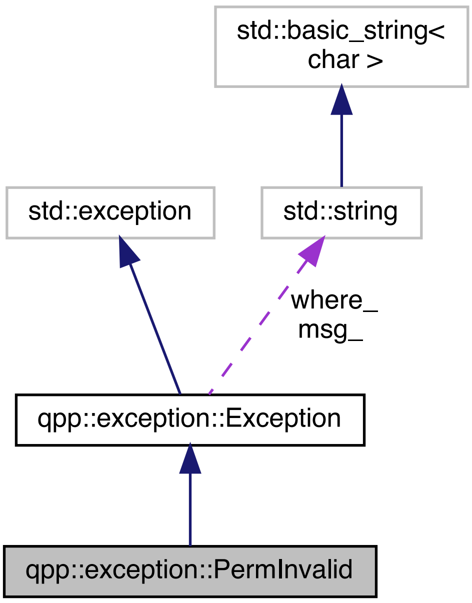
Invalid permutation exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::PermInvalid:



Collaboration diagram for qpp::exception::PermInvalid:



Public Member Functions

- std::string description () const override

Exception description.

- Exception (const std::string &where)

  Constructs an exception.

7.52.1 Detailed Description

Invalid permutation exception.

std::vector<idx> does note represent a valid permutation

7.52.2 Member Function Documentation

7.52.2.1 description()

`std::string qpp::exception::PermInvalid::description ( ) const [inline], [override], [virtual]`

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.52.2.2 Exception()

`qpp::exception::Exception::Exception [inline], [explicit]`

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

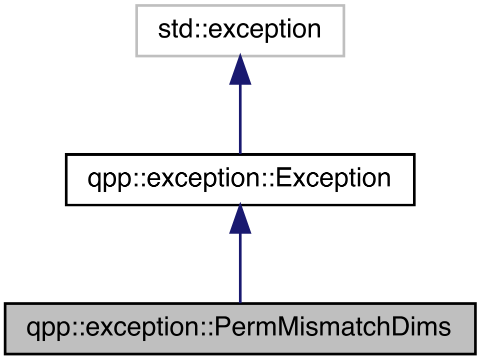
- classes/exception.h

7.53 qpp::exception::PermMismatchDims Class Reference

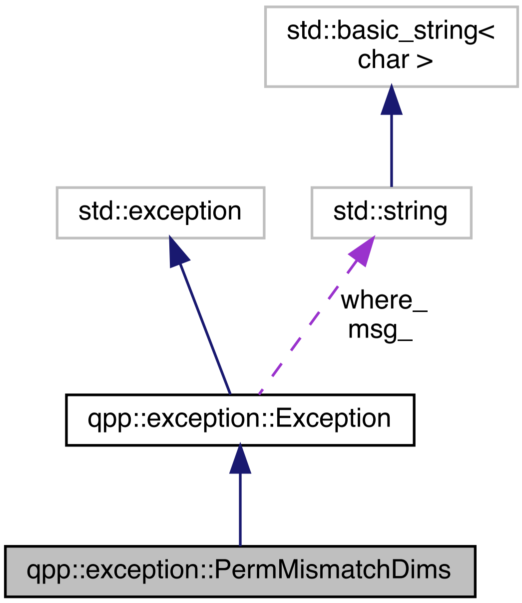
Permutation mismatch dimensions exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::PermMismatchDims:



Collaboration diagram for qpp::exception::PermMismatchDims:



Public Member Functions

- std::string description () const override

Exception description.

- Exception (const std::string &where)

Constructs an exception.

7.53.1 Detailed Description

Permutation mismatch dimensions exception.

Size of the std::vector<idx> representing the permutation is different from the size of the std::vector<idx> of dimensions

7.53.2 Member Function Documentation

7.53.2.1 description()

```
std::string qpp::exception::PermMismatchDims::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.53.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

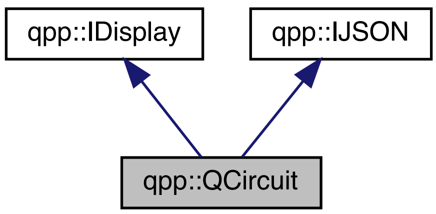
- classes/exception.h

7.54 qpp::QCircuit Class Reference

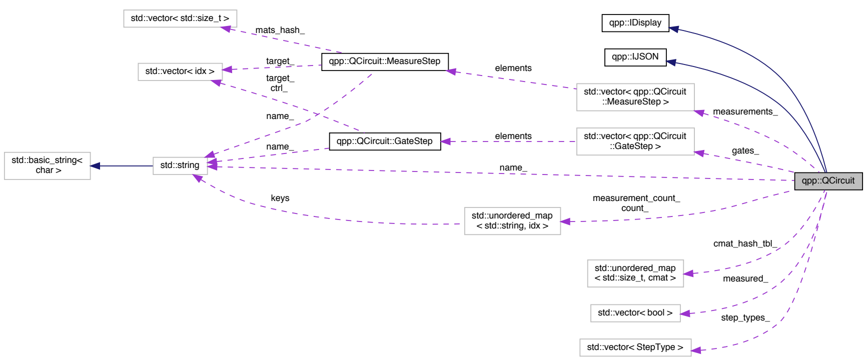
Quantum circuit class.

```
#include <classes/circuits/circuits.h>
```

Inheritance diagram for qpp::QCircuit:



Collaboration diagram for qpp::QCircuit:



Classes

- struct GateStep

    One step consisting only of gates/operators in the circuit.
- class iterator

    Quantum circuit bound-checking (safe) iterator.
- struct MeasureStep

    One step consisting only of measurements in the circuit.

Public Types

- enum GateType {
  GateType::NONE, GateType::SINGLE, GateType::TWO, GateType::THREE,
  GateType::CUSTOM, GateType::FAN, GateType::SINGLE_CTRL_SINGLE_TARGET, GateType::SINGLE_CTRL_MULTIPLE_
  GateType::MULTIPLE_CTRL_SINGLE_TARGET, GateType::MULTIPLE_CTRL_MULTIPLE_TARGET,
  GateType::CUSTOM_CTRL, GateType::SINGLE_cCTRL_SINGLE_TARGET,
  GateType::SINGLE_cCTRL_MULTIPLE_TARGET, GateType::MULTIPLE_cCTRL_SINGLE_TARGET,
  GateType::MULTIPLE_cCTRL_MULTIPLE_TARGET, GateType::CUSTOM_cCTRL }

  Type of gate being executed in a gate step.
- enum MeasureType { MeasureType::NONE, MeasureType::MEASURE_Z, MeasureType::MEASURE_V, MeasureType::MEASURE_V_MANY }

  Type of measurement being executed in a measurement step.
- enum StepType { StepType::NONE, StepType::GATE, StepType::MEASUREMENT, StepType::NOP }

  Types of each step in the quantum circuit.
- using const_iterator = iterator

  both iterators are const_iterators

Public Member Functions

- iterator begin ()

  Iterator to the first element.
- const_iterator begin () const noexcept

  Constant iterator to the first element.
- const_iterator cbegin () const noexcept

  Constant iterator to the first element.
- iterator end ()

  Iterator to the next to the last element.
- const_iterator end () const noexcept

  Constant iterator to the next to the last element.
- const_iterator cend () const noexcept

  Constant iterator to the next to the last element.
- QCircuit (idx nq, idx nc=0, idx d=2, std::string name={})

  Constructs a quantum circuit.
- virtual ~QCircuit ()=default

  Default virtual destructor.
- idx get_nq () const noexcept

  Total number of qudits in the circuit.
- idx get_nc () const noexcept

  Total number of classical dits in the circuit.
- idx get_d () const noexcept

  Dimension of the comprising qudits.
- std::string get_name () const

  Quantum circuit name.
- idx get_measured (idx i) const

  Check whether qudit i was already measured.
- std::vector< idx > get_measured () const

  Vector of already measured qudit indexes.
- std::vector< idx > get_non_measured () const

  Vector of non-measured qudit indexes.
- idx get_gate_count (const std::string &name={}) const

Quantum circuit gate count.
- idx get_gate_depth (const std::string &name={}) const

  Quantum circuit gate depth.
- idx get_measurement_count () const noexcept

  Quantum circuit total measurement count.
- idx get_measurement_count (const std::string &name) const

  Quantum circuit measurement count.
- idx get_step_count () const noexcept

  Quantum circuit total steps count, i.e. the sum of gate count and measurement count.
- idx get_nop_count () const

  No-op count.
- QCircuit & gate (const cmat &U, idx i, std::string name={})

  Applies the single qudit gate U on single qudit i.
- QCircuit & gate (const cmat &U, idx i, idx j, std::string name={})

  Applies the two qudit gate U on qudits i and j.
- QCircuit & gate (const cmat &U, idx i, idx j, idx k, std::string name={})

  Applies the three qudit gate U on qudits i, j and k.
- QCircuit & gate_fan (const cmat &U, const std::vector< idx > &target, std::string name={})

  Applies the single qudit gate U on every qudit listed in target.
- QCircuit & gate_fan (const cmat &U, const std::initializer_list< idx > &target, std::string name={})

  Applies the single qudit gate U on every qudit listed in target.
- QCircuit & gate_fan (const cmat &U, std::string name={})

  Applies the single qudit gate U on every remaining non-measured qudit.
- QCircuit & gate_custom (const cmat &U, const std::vector< idx > &target, std::string name={})

  Jointly applies the custom multiple qudit gate U on the qudit indexes specified by target.
- QCircuit & QFT (const std::vector< idx > &target, bool swap=true)

  Applies the quantum Fourier transform (as a series of gates) on the qudit indexes specified by target.
- QCircuit & QFT (const std::initializer_list< idx > &target, bool swap=true)

  Applies the quantum Fourier transform (as a series of gates) on the qudit indexes specified by target.
- QCircuit & QFT (bool swap=true)

  Applies the quantum Fourier transform (as a series of gates) on all of remaining non-measured qudits.
- QCircuit & TFQ (const std::vector< idx > &target, bool swap QPP_UNUSED_=true)

  Applies the inverse quantum Fourier transform (as a series of gates) on the qudit indexes specified by target.
- QCircuit & TFQ (const std::initializer_list< idx > &target, bool swap=true)

  Applies the inverse quantum Fourier transform (as a series of gates) on the qudit indexes specified by target.
- QCircuit & TFQ (bool swap=true)

  Applies the inverse quantum Fourier transform (as a series of gates) on all of remaining non-measured qudits.
- QCircuit & CTRL (const cmat &U, idx ctrl, idx target, std::string name={})

  Applies the single qudit controlled gate U with control qudit ctrl and target qudit target.
- QCircuit & CTRL (const cmat &U, idx ctrl, const std::vector< idx > &target, std::string name={})

  Applies the single qudit controlled gate U with control qudit ctrl on every qudit listed in target.
- QCircuit & CTRL (const cmat &U, const std::vector< idx > &ctrl, idx target, std::string name={})

  Applies the single qudit controlled gate U with multiple control qudits listed in ctrl on the target qudit target.
- QCircuit & CTRL (const cmat &U, const std::vector< idx > &ctrl, const std::vector< idx > &target, std::string name={})

  Applies the single qudit controlled gate U with multiple control qudits listed in ctrl on every qudit listed in target.
- QCircuit & CTRL_custom (const cmat &U, const std::vector< idx > &ctrl, const std::vector< idx > &target, std::string name={})

  Jointly applies the custom multiple-qudit controlled gate U with multiple control qudits listed in ctrl on the qudit indexes specified by target.
- QCircuit & cCTRL (const cmat &U, idx ctrl_dit, idx target, std::string name={})

Applies the single qubit controlled gate U with classical control dit ctrl and target qudit target.
- QCircuit & cCTRL (const cmat &U, idx ctrl_dit, const std::vector< idx > &target, std::string name={})

  Applies the single qudit controlled gate U with classical control dit ctrl on every qudit listed in target.
- QCircuit & cCTRL (const cmat &U, const std::vector< idx > &ctrl_dits, idx target, std::string name={})

  Applies the single qudit controlled gate U with multiple classical control dits listed in ctrl on the target qudit target.
- QCircuit & cCTRL (const cmat &U, const std::vector< idx > &ctrl_dits, const std::vector< idx > &target, std::string name={})

  Applies the single qudit controlled gate U with multiple classical control dits listed in ctrl on every qudit listed in target.
- QCircuit & cCTRL_custom (const cmat &U, const std::vector< idx > &ctrl_dits, const std::vector< idx > &target, std::string name={})

  Jointly applies the custom multiple-qudit controlled gate U with multiple classical control dits listed in ctrl on the qudit indexes specified by target.
- QCircuit & measureZ (idx target, idx c_reg, std::string name={})

  Measurement of single qudit in the computational basis (Z-basis)
- QCircuit & measureV (const cmat &V, idx target, idx c_reg, std::string name={})

  Measurement of single qudit in the orthonormal basis or rank-1 projectors specified by the columns of matrix V.
- QCircuit & measureV (const cmat &V, const std::vector< idx > &target, idx c_reg, std::string name={})

  Joint measurement of multiple qudits in the orthonormal basis or rank-1 projectors specified by the columns of matrix V.
- QCircuit & nop ()

  No operation (no-op)
- std::string to_JSON (bool enclosed_in_curly_brackets=true) const override

  qpp::IJOSN::to_JSON() override

Private Member Functions

- void add_hash_ (const cmat &U, std::size_t hashU)

  Adds matrix to the hash table.
- const std::vector< MeasureStep > & get_measurements_ () const noexcept

  Vector of qpp::QCircuit::MeasureStep.
- const std::vector< GateStep > & get_gates_ () const noexcept

  Vector of qpp::QCircuit::GateStep.
- const std::unordered_map< std::size_t, cmat > & get_cmat_hash_tbl_ () const noexcept

  Hash table with the matrices used in the circuit.
- std::ostream & display (std::ostream &os) const override

  qpp::IDisplay::display() override

Private Attributes

- const idx nq_

  number of qudits
- const idx nc_

  number of classical "dits"
- const idx d_

  qudit dimension
- std::string name_

  optional circuit name
- std::vector< bool > measured_

  keeps track of the measured qudits
- std::unordered_map< std::size_t, cmat > cmat_hash_tbl_ {}

- std::unordered_map< std::string, idx > count_ {}
  gate counts
- std::unordered_map< std::string, idx > measurement_count_ {}
  measurement counts
- std::vector< GateStep > gates_ {}
  gates
- std::vector< MeasureStep > measurements_ {}
  measurements
- std::vector< StepType > step_types_ {}
  type of each step

Friends

- class QEngine
- std::ostream & operator<< (std::ostream &os, const GateType &gate_type)
  Extraction operator overload for qpp::QCircuit::GateType enum class.
- std::ostream & operator<< (std::ostream &os, const GateStep &gate_step)
  Extraction operator overload for qpp::QCircuit::GateStep class.
- std::ostream & operator<< (std::ostream &os, const MeasureType &measure_type)
  Extraction operator overload for qpp::QCircuit::MeasureType enum class.
- std::ostream & operator<< (std::ostream &os, const MeasureStep &measure_step)
  Extraction operator overload for qpp::QCircuit::MeasureStep class.

7.54.1 Detailed Description

Quantum circuit class.

See also

qpp::QEngine

7.54.2 Member Typedef Documentation

7.54.2.1 const_iterator

```
using qpp::QCircuit::const_iterator = iterator
```

both iterators are const_iterators

7.54.3 Member Enumeration Documentation

7.54.3.1 GateType

```
enum qpp::QCircuit::GateType [strong]
```

Type of gate being executed in a gate step.

Enumerator

NONE	represents no gate
SINGLE	unitary gate on a single qudit
TWO	unitary gate on 2 qudits
THREE	unitary gate on 3 qudits
CUSTOM	custom gate on multiple qudits
FAN	same unitary gate on multiple qudits
SINGLE_CTRL_SINGLE_TARGET	controlled 1 qudit unitary gate with one control and one target
SINGLE_CTRL_MULTIPLE_TARGET	controlled 1 qudit unitary gate with one control and multiple targets
MULTIPLE_CTRL_SINGLE_TARGET	controlled 1 qudit unitary gate with multiple controls and single target
MULTIPLE_CTRL_MULTIPLE_TARGET	controlled 1 qudit unitary gate with multiple controls and multiple targets
CUSTOM_CTRL	custom controlled gate with multiple controls and multiple targets
SINGLE_cCTRL_SINGLE_TARGET	controlled 1 qudit unitary gate with one classical control and one target
SINGLE_cCTRL_MULTIPLE_TARGET	controlled 1 qudit unitary gate with one classical control and multiple targets
MULTIPLE_cCTRL_SINGLE_TARGET	controlled 1 qudit unitary gate with multiple classical controls and single target
MULTIPLE_cCTRL_MULTIPLE_TARGET	controlled 1 qudit unitary gate with multiple classical controls and multiple targets
CUSTOM_cCTRL	custom controlled gate with multiple controls and multiple targets

7.54.3.2 MeasureType

```
enum qpp::QCircuit::MeasureType  [strong]
```

Type of measurement being executed in a measurement step.

Enumerator

NONE	represents no measurement
MEASURE_Z	Z measurement of single qudit.
MEASURE_V	measurement of single qudit in the orthonormal basis or rank-1 projectors specified by the columns of matrix V
MEASURE_V_MANY	measurement of multiple qudits in the orthonormal basis or rank-1 projectors specified by the columns of matrix V

7.54.3.3 StepType

```
enum qpp::QCircuit::StepType  [strong]
```

Types of each step in the quantum circuit.

Enumerator

NONE	represents no step
GATE	quantum gate(s)
MEASUREMENT	measurement
NOP	no-op

7.54.4 Constructor & Destructor Documentation

7.54.4.1 QCircuit()

```
qpp::QCircuit::QCircuit (
            idx nq,
            idx nc = 0,
            idx d = 2,
            std::string name = {} )  [inline], [explicit]
```

Constructs a quantum circuit.

Note

The measurement results can only be stored in the classical dits of which number is specified by *nc*

Parameters

nq	Number of qbits
nc	Number of classical dits (optional)
d	Subsystem dimensions (optional, default is qubit, i.e. $d = 2$)
name	Circuit name (optional)

7.54.4.2 ∼QCircuit()

```
virtual qpp::QCircuit::~QCircuit ( )  [virtual], [default]
```

Default virtual destructor.

7.54.5 Member Function Documentation

7.54.5.1 add_hash_()

```
void qpp::QCircuit::add_hash_ (
            const cmat & U,
            std::size_t hashU )  [inline], [private]
```

Adds matrix to the hash table.

Note

Throws if a hash collision is detected., i.e., if two different matrices have the same hash

Parameters

U	Complex matrix
hashU	Hash value of U

7.54.5.2 begin() [1/2]

```
iterator qpp::QCircuit::begin ( )  [inline]
```

Iterator to the first element.

Returns

Iterator to the first element

7.54.5.3 begin() [2/2]

```
const_iterator qpp::QCircuit::begin ( ) const  [inline], [noexcept]
```

Constant iterator to the first element.

Returns

Constant iterator to the first element

7.54.5.4 cbegin()

```
const_iterator qpp::QCircuit::cbegin ( ) const  [inline], [noexcept]
```

Constant iterator to the first element.

Returns

Constant iterator to the first element

7.54.5.5 cCTRL() [1/4]

```
QCircuit& qpp::QCircuit::cCTRL (
            const cmat & U,
            idx ctrl_dit,
            idx target,
            std::string name = {} )  [inline]
```

Applies the single qubit controlled gate *U* with classical control dit *ctrl* and target qudit *target*.

Parameters

U	Single qudit quantum gate
ctrl_dit	Classical control dit index
target	Target qudit index
name	Optional gate name

Returns

Reference to the current instance

7.54.5.6 cCTRL() [2/4]

```
QCircuit& qpp::QCircuit::cCTRL (
            const cmat & U,
            idx ctrl_dit,
            const std::vector< idx > & target,
            std::string name = {} )  [inline]
```

Applies the single qudit controlled gate *U* with classical control dit *ctrl* on every qudit listed in *target*.

Parameters

U	Single qudit quantum gate
ctrl_dit	Classical control dit index
target	Target qudit indexes; the gate *U* is applied on every one of them depending on the values of the classical control dits
name	Optional gate name

Returns

Reference to the current instance

7.54.5.7 cCTRL() [3/4]

```
QCircuit& qpp::QCircuit::cCTRL (
            const cmat & U,
```

```
const std::vector< idx > & ctrl_dits,
idx target,
std::string name = {} ) [inline]
```

Applies the single qudit controlled gate *U* with multiple classical control dits listed in *ctrl* on the target qudit *target*.

Parameters

U	Single qudit quantum gate
ctrl_dits	Classical control dits indexes
target	Target qudit index
name	Optional gate name

Returns

Reference to the current instance

7.54.5.8 cCTRL() [4/4]

```
QCircuit& qpp::QCircuit::cCTRL (
    const cmat & U,
    const std::vector< idx > & ctrl_dits,
    const std::vector< idx > & target,
    std::string name = {} ) [inline]
```

Applies the single qudit controlled gate *U* with multiple classical control dits listed in *ctrl* on every qudit listed in *target*.

Parameters

U	Single qudit quantum gate
ctrl_dits	Classical control dits indexes
target	Target qudit indexes; the gate *U* is applied on every one of them depending on the values of the classical control dits
name	Optional gate name

Returns

Reference to the current instance

7.54.5.9 cCTRL_custom()

```
QCircuit& qpp::QCircuit::cCTRL_custom (
    const cmat & U,
    const std::vector< idx > & ctrl_dits,
```

```
const std::vector< idx > & target,
std::string name = {} ) [inline]
```

Jointly applies the custom multiple-qudit controlled gate *U* with multiple classical control dits listed in *ctrl* on the qudit indexes specified by *target*.

Parameters

U	Multiple-qudit quantum gate
ctrl_dits	Classical control dits indexes
target	Target qudit indexes where the gate *U* is applied depending on the values of the classical control dits
name	Optional gate name

Returns

Reference to the current instance

7.54.5.10 cend()

```
const_iterator qpp::QCircuit::cend ( ) const [inline], [noexcept]
```

Constant iterator to the next to the last element.

Returns

Constant iterator to the next to the last element

7.54.5.11 CTRL() [1/4]

```
QCircuit& qpp::QCircuit::CTRL (
            const cmat & U,
            idx ctrl,
            idx target,
            std::string name = {} ) [inline]
```

Applies the single qudit controlled gate *U* with control qudit *ctrl* and target qudit *target*.

Parameters

U	Single qudit quantum gate
ctrl	Control qudit index
target	Target qudit index
name	Optional gate name

Returns

Reference to the current instance

7.54.5.12 CTRL() [2/4]

```
QCircuit& qpp::QCircuit::CTRL (
            const cmat & U,
            idx ctrl,
            const std::vector< idx > & target,
            std::string name = {} )  [inline]
```

Applies the single qudit controlled gate *U* with control qudit *ctrl* on every qudit listed in *target*.

Parameters

U	Single qudit quantum gate
ctrl	Control qudit index
target	Target qudit indexes; the gate *U* is applied on every one of them depending on the values of the control qudits
name	Optional gate name

Returns

Reference to the current instance

7.54.5.13 CTRL() [3/4]

```
QCircuit& qpp::QCircuit::CTRL (
            const cmat & U,
            const std::vector< idx > & ctrl,
            idx target,
            std::string name = {} )  [inline]
```

Applies the single qudit controlled gate *U* with multiple control qudits listed in *ctrl* on the target qudit *target*.

Parameters

U	Single qudit quantum gate
ctrl	Control qudit indexes
target	Target qudit index
name	Optional gate name

Returns

Reference to the current instance

7.54.5.14 CTRL() [4/4]

```
QCircuit& qpp::QCircuit::CTRL (
            const cmat & U,
            const std::vector< idx > & ctrl,
            const std::vector< idx > & target,
            std::string name = {} ) [inline]
```

Applies the single qudit controlled gate *U* with multiple control qudits listed in *ctrl* on every qudit listed in *target*.

Parameters

U	Single qudit quantum gate
ctrl	Control qudit indexes
target	Target qudit indexes; the gate *U* is applied on every one of them depending on the values of the control qudits
name	Optional gate name

Returns

Reference to the current instance

7.54.5.15 CTRL_custom()

```
QCircuit& qpp::QCircuit::CTRL_custom (
            const cmat & U,
            const std::vector< idx > & ctrl,
            const std::vector< idx > & target,
            std::string name = {} ) [inline]
```

Jointly applies the custom multiple-qudit controlled gate *U* with multiple control qudits listed in *ctrl* on the qudit indexes specified by *target*.

Parameters

U	Multiple-qudit quantum gate
ctrl	Control qudit indexes
target	Target qudit indexes where the gate *U* is applied depending on the values of the control qudits
name	Optional gate name

Returns

Reference to the current instance

7.54.5.16 display()

```
std::ostream& qpp::QCircuit::display (
            std::ostream & os ) const  [inline], [override], [private], [virtual]
```

qpp::IDisplay::display() override

Writes to the output stream a textual representation of the quantum circuit

Parameters

os	Output stream passed by reference

Returns

Reference to the output stream

Implements qpp::IDisplay.

7.54.5.17 end() [1/2]

```
iterator qpp::QCircuit::end ( )  [inline]
```

Iterator to the next to the last element.

Returns

Iterator to the next to the last element

7.54.5.18 end() [2/2]

```
const_iterator qpp::QCircuit::end ( ) const  [inline], [noexcept]
```

Constant iterator to the next to the last element.

Returns

Constant iterator to the next to the last element

7.54.5.19 gate() [1/3]

```
QCircuit& qpp::QCircuit::gate (
            const cmat & U,
            idx i,
            std::string name = {} )  [inline]
```

Applies the single qudit gate *U* on single qudit *i*.

Parameters

U	Single qudit quantum gate
i	Qudit index
name	Optional gate name

Returns

Reference to the current instance

7.54.5.20 gate() [2/3]

```
QCircuit& qpp::QCircuit::gate (
            const cmat & U,
            idx i,
            idx j,
            std::string name = {} )  [inline]
```

Applies the two qudit gate *U* on qudits *i* and *j*.

Parameters

U	Two qudit quantum gate
i	Qudit index
j	Qudit index
name	Optional gate name

Returns

Reference to the current instance

7.54.5.21 gate() [3/3]

```
QCircuit& qpp::QCircuit::gate (
            const cmat & U,
            idx i,
            idx j,
            idx k,
            std::string name = {} )  [inline]
```

Applies the three qudit gate *U* on qudits *i*, *j* and *k*.

Parameters

U	Three qudit quantum gate
i	Qudit index
j	Qudit index
k	Qudit index
name	Optional gate name

Returns

Reference to the current instance

7.54.5.22 gate_custom()

```
QCircuit& qpp::QCircuit::gate_custom (
            const cmat & U,
            const std::vector< idx > & target,
            std::string name = {} )  [inline]
```

Jointly applies the custom multiple qudit gate *U* on the qudit indexes specified by *target*.

Parameters

U	Multiple qudit quantum gate
target	Subsystem indexes where the gate *U* is applied
name	Optional gate name

Returns

Reference to the current instance

7.54.5.23 gate_fan() [1/3]

```
QCircuit& qpp::QCircuit::gate_fan (
            const cmat & U,
            const std::vector< idx > & target,
            std::string name = {} )  [inline]
```

Applies the single qudit gate *U* on every qudit listed in *target*.

Parameters

U	Single qudit quantum gate
target	Target qudit indexes; the gate *U* is applied on every one of them
name	Optional gate name

Returns

Reference to the current instance

7.54.5.24 gate_fan() [2/3]

```
QCircuit& qpp::QCircuit::gate_fan (
            const cmat & U,
            const std::initializer_list< idx > & target,
            std::string name = {} )  [inline]
```

Applies the single qudit gate *U* on every qudit listed in *target*.

Parameters

U	Single qudit quantum gate
target	Target qudit indexes; the gate *U* is applied on every one of them
name	Optional gate name

Returns

Reference to the current instance

7.54.5.25 gate_fan() [3/3]

```
QCircuit& qpp::QCircuit::gate_fan (
            const cmat & U,
            std::string name = {} )  [inline]
```

Applies the single qudit gate *U* on every remaining non-measured qudit.

Parameters

U	Single qudit quantum gate
name	Optional gate name

Returns

Reference to the current instance

7.54.5.26 get_cmat_hash_tbl_()

```
const std::unordered_map<std::size_t, cmat>& qpp::QCircuit::get_cmat_hash_tbl_ ( ) const
[inline], [private], [noexcept]
```

Hash table with the matrices used in the circuit.

Returns

Hash table with the matrices used in the circuit

7.54.5.27 get_d()

```
idx qpp::QCircuit::get_d ( ) const [inline], [noexcept]
```

Dimension of the comprising qudits.

Returns

Qudit dimension

7.54.5.28 get_gate_count()

```
idx qpp::QCircuit::get_gate_count (
            const std::string & name = {} ) const [inline]
```

Quantum circuit gate count.

Note

If *name* is empty (default), returns the total gate count of the circuit

Parameters

name	Gate name (optional)

Returns

Gate count

7.54.5.29 get_gate_depth()

```
idx qpp::QCircuit::get_gate_depth (
            const std::string & name = {} ) const [inline]
```

Quantum circuit gate depth.

Note

If *name* is empty (default), returns the total gate depth of the circuit

Parameters

name	Gate name (optional)

Returns

Gate depth

7.54.5.30 get_gates_()

```
const std::vector<GateStep>& qpp::QCircuit::get_gates_ ( ) const [inline], [private], [noexcept]
```

Vector of qpp::QCircuit::GateStep.

Returns

Vector of qpp::QCircuit::GateStep

7.54.5.31 get_measured() [1/2]

```
idx qpp::QCircuit::get_measured (
            idx i ) const [inline]
```

Check whether qudit *i* was already measured.

Parameters

i	Qudit index

Returns

True if qudit *i* was already measured, false othwewise

7.54.5.32 get_measured() [2/2]

```
std::vector<idx> qpp::QCircuit::get_measured ( ) const [inline]
```

Vector of already measured qudit indexes.

Returns

Vector of already measured qudit indexes

7.54.5.33 get_measurement_count() [1/2]

```
idx qpp::QCircuit::get_measurement_count ( ) const [inline], [noexcept]
```

Quantum circuit total measurement count.

Returns

Total measurement count

7.54.5.34 get_measurement_count() [2/2]

```
idx qpp::QCircuit::get_measurement_count (
            const std::string & name ) const [inline]
```

Quantum circuit measurement count.

Parameters

name	Measurement name

Returns

Measurement count

7.54.5.35 get_measurements_()

```
const std::vector<MeasureStep>& qpp::QCircuit::get_measurements_ ( ) const [inline], [private],
[noexcept]
```

Vector of qpp::QCircuit::MeasureStep.

Returns

Vector of qpp::QCircuit::MeasureStep

7.54.5.36 get_name()

```
std::string qpp::QCircuit::get_name ( ) const [inline]
```

Quantum circuit name.

Returns

Quantum circuit name

7.54.5.37 get_nc()

```
idx qpp::QCircuit::get_nc ( ) const [inline], [noexcept]
```

Total number of classical dits in the circuit.

Returns

Total number of classical dits

7.54.5.38 get_non_measured()

```
std::vector<idx> qpp::QCircuit::get_non_measured ( ) const [inline]
```

Vector of non-measured qudit indexes.

Returns

Vector of non-measured qudit indexes

7.54.5.39 get_nop_count()

```
idx qpp::QCircuit::get_nop_count ( ) const [inline]
```

No-op count.

Returns

No-op count

7.54.5.40 get_nq()

```
idx qpp::QCircuit::get_nq ( ) const [inline], [noexcept]
```

Total number of qudits in the circuit.

Returns

Total number of qudits

7.54.5.41 get_step_count()

```
idx qpp::QCircuit::get_step_count ( ) const [inline], [noexcept]
```

Quantum circuit total steps count, i.e. the sum of gate count and measurement count.

Returns

Total (gates + measurements) count

7.54.5.42 measureV() [1/2]

```
QCircuit& qpp::QCircuit::measureV (
            const cmat & V,
            idx target,
            idx c_reg,
            std::string name = {} ) [inline]
```

Measurement of single qudit in the orthonormal basis or rank-1 projectors specified by the columns of matrix *V*.

Parameters

V	Orthonormal basis or rank-1 projectors specified by the columns of matrix V
target	Qudit index
c_reg	Classical register where the value of the measurement is stored
name	Optional measurement name

Returns

Reference to the current instance

7.54.5.43 measureV() [2/2]

```
QCircuit& qpp::QCircuit::measureV (
            const cmat & V,
            const std::vector< idx > & target,
            idx c_reg,
            std::string name = {} ) [inline]
```

Joint measurement of multiple qudits in the orthonormal basis or rank-1 projectors specified by the columns of matrix *V*.

Parameters

V	Orthonormal basis or rank-1 projectors specified by the columns of matrix V
target	Target qudit indexes that are jointly measured
c_reg	Classical register where the value of the measurement is stored
name	Optional measurement name

Returns

Reference to the current instance

7.54.5.44 measureZ()

```
QCircuit& qpp::QCircuit::measureZ (
            idx target,
            idx c_reg,
            std::string name = {} ) [inline]
```

Measurement of single qudit in the computational basis (Z-basis)

Parameters

target	Qudit index
c_reg	Classical register where the value of the measurement is being stored
name	Optional measurement name, default is "Measure Z"

Returns

Reference to the current instance

7.54.5.45 nop()

```
QCircuit& qpp::QCircuit::nop ( ) [inline]
```

No operation (no-op)

Note

If the underlying step is executed on a noisy engine, then noise acts before it

Returns

Reference to the current instance

7.54.5.46 QFT() [1/3]

```
QCircuit& qpp::QCircuit::QFT (
            const std::vector< idx > & target,
            bool swap = true ) [inline]
```

Applies the quantum Fourier transform (as a series of gates) on the qudit indexes specified by *target*.

Parameters

target	Subsystem indexes where the quantum Fourier transform is applied
swap	Swaps the qubits at the end (true by default)

Returns

Reference to the current instance

7.54.5.47 QFT() [2/3]

```
QCircuit& qpp::QCircuit::QFT (
            const std::initializer_list< idx > & target,
            bool swap = true ) [inline]
```

Applies the quantum Fourier transform (as a series of gates) on the qudit indexes specified by *target*.

Parameters

target	Subsystem indexes where the quantum Fourier transform is applied
swap	Swaps the qubits at the end (true by default)

Returns

Reference to the current instance

7.54.5.48 QFT() [3/3]

```
QCircuit& qpp::QCircuit::QFT (
            bool swap = true ) [inline]
```

Applies the quantum Fourier transform (as a series of gates) on all of remaining non-measured qudits.

Parameters

swap	Swaps the qubits at the end (true by default)

Returns

Reference to the current instance

7.54.5.49 TFQ() [1/3]

```
QCircuit& qpp::QCircuit::TFQ (
            const std::vector< idx > & target,
            bool swap QPP_UNUSED_ = true ) [inline]
```

Applies the inverse quantum Fourier transform (as a series of gates) on the qudit indexes specified by *target*.

Parameters

target	Subsystem indexes where the inverse quantum Fourier transform is applied
swap	Swaps the qubits at the end (true by default)

Returns

Reference to the current instance

7.54.5.50 TFQ() [2/3]

```
QCircuit& qpp::QCircuit::TFQ (
            const std::initializer_list< idx > & target,
            bool swap = true ) [inline]
```

Applies the inverse quantum Fourier transform (as a series of gates) on the qudit indexes specified by *target*.

Parameters

target	Subsystem indexes where the inverse quantum Fourier transform is applied
swap	Swaps the qubits at the end (true by default)

Returns

Reference to the current instance

7.54.5.51 TFQ() [3/3]

```
QCircuit& qpp::QCircuit::TFQ (
            bool swap = true ) [inline]
```

Applies the inverse quantum Fourier transform (as a series of gates) on all of remaining non-measured qudits.

Parameters

swap	Swaps the qubits at the end (true by default)

Returns

Reference to the current instance

7.54.5.52 to_JSON()

```
std::string qpp::QCircuit::to_JSON (
            bool enclosed_in_curly_brackets = true ) const  [inline], [override], [virtual]
```

qpp::IJOSN::to_JSON() override

Displays the quantum circuit in JSON format

Parameters

enclosed_in_curly_brackets	If true, encloses the result in curly brackets

Returns

String containing the JSON representation of the quantum circuit

Implements qpp::IJSON.

7.54.6 Friends And Related Function Documentation

7.54.6.1 operator<< [1/4]

```
std::ostream& operator<< (
            std::ostream & os,
            const GateType & gate_type )  [friend]
```

Extraction operator overload for qpp::QCircuit::GateType enum class.

Parameters

os	Output stream
gate_type	qpp::QCircuit::GateType enum class

Returns

Output stream

7.54.6.2 operator<< [2/4]

```
std::ostream& operator<< (
            std::ostream & os,
            const GateStep & gate_step )   [friend]
```

Extraction operator overload for qpp::QCircuit::GateStep class.

Parameters

os	Output stream
gate_step	qpp::QCircuit::GateStep class

Returns

Output stream

7.54.6.3 operator<< [3/4]

```
std::ostream& operator<< (
            std::ostream & os,
            const MeasureType & measure_type )   [friend]
```

Extraction operator overload for qpp::QCircuit::MeasureType enum class.

Parameters

os	Output stream
measure_type	qpp::QCircuit::MeasureType enum class

Returns

Output stream

7.54.6.4 operator<< [4/4]

```
std::ostream& operator<< (
            std::ostream & os,
            const MeasureStep & measure_step )   [friend]
```

Extraction operator overload for qpp::QCircuit::MeasureStep class.

Parameters

os	Output stream
measure_step	qpp::QCircuit::MeasureStep enum class

Returns

Output stream

7.54.6.5 QEngine

```
friend class QEngine [friend]
```

7.54.7 Member Data Documentation

7.54.7.1 cmat_hash_tbl_

```
std::unordered_map<std::size_t, cmat> qpp::QCircuit::cmat_hash_tbl_ {} [private]
```

hash table with the matrices used in the circuit, with [Key = idx, Value = cmat]

7.54.7.2 count_

```
std::unordered_map<std::string, idx> qpp::QCircuit::count_ {} [private]
```

gate counts

7.54.7.3 d_

```
const idx qpp::QCircuit::d_ [private]
```

qudit dimension

7.54.7.4 gates_

```
std::vector<GateStep> qpp::QCircuit::gates_ {} [private]
```

gates

7.54.7.5 measured_

```
std::vector<bool> qpp::QCircuit::measured_ [private]
```

keeps track of the measured qudits

7.54.7.6 measurement_count_

```
std::unordered_map<std::string, idx> qpp::QCircuit::measurement_count_ {} [private]
```

measurement counts

7.54.7.7 measurements_

```
std::vector<MeasureStep> qpp::QCircuit::measurements_ {} [private]
```

measurements

7.54.7.8 name_

```
std::string qpp::QCircuit::name_ [private]
```

optional circuit name

7.54.7.9 nc_

```
const idx qpp::QCircuit::nc_ [private]
```

number of classical "dits"

7.54.7.10 nq_

```
const idx qpp::QCircuit::nq_ [private]
```

number of qudits

7.54.7.11 step_types_

```
std::vector<StepType> qpp::QCircuit::step_types_ {}  [private]
```

type of each step

The documentation for this class was generated from the following file:

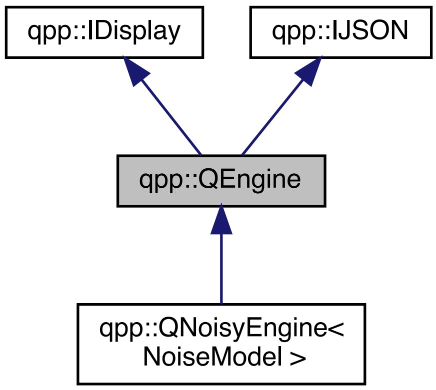
- classes/circuits/circuits.h

7.55 qpp::QEngine Class Reference

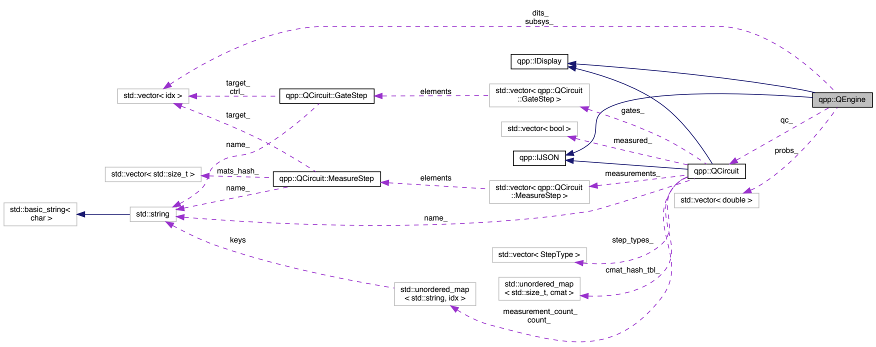
Quantum circuit engine, executes qpp::QCircuit.

```
#include <classes/circuits/engines.h>
```

Inheritance diagram for qpp::QEngine:



Collaboration diagram for qpp::QEngine:



Public Member Functions

- QEngine (const QCircuit &qc)

    Constructs a quantum engine out of a quantum circuit.
- QEngine (const QEngine &)=default

    Default copy constructor.
- QEngine & operator= (const QEngine &)=default

    Default copy assignment operator.
- QEngine (QCircuit &&)=delete

    Disables rvalue QCircuit.
- virtual ∼QEngine ()=default

    Default virtual destructor.
- ket get_psi () const

    Underlying quantum state.
- std::vector< idx > get_dits () const

    Vector with the values of the underlying classical dits.
- idx get_dit (idx i) const

    Value of the classical dit at position i.
- std::vector< double > get_probs () const

    Vector of underlying measurement outcome probabilities.
- bool get_measured (idx i) const

    Check whether qudit i was already measured.
- std::vector< idx > get_measured () const

    Vector of already measured qudit indexes.
- std::vector< idx > get_non_measured () const

    Vector of non-measured qudit indexes.
- const QCircuit & get_circuit () const noexcept

    Quantum circuit.
- QEngine & set_dit (idx i, idx value)

    Sets the classical dit at position i.
- QEngine & set_psi (const ket &psi)

    Sets the underlying quantum state to psi.
- void reset ()

    Resets the engine.
- virtual void execute (const QCircuit::iterator::value_type &elem)

    Executes one step in the quantum circuit.
- void execute (const QCircuit::iterator &it)

    Executes one step in the quantum circuit.
- void execute ()

    Executes the entire quantum circuit.
- std::string to_JSON (bool enclosed_in_curly_brackets=true) const override

    qpp::IJOSN::to_JSON() override

Protected Member Functions

- void set_measured_ (idx i)

    Marks qudit i as measured then re-label accordingly the remaining non-measured qudits.
- std::vector< idx > get_relative_pos_ (std::vector< idx > v)

    Giving a vector V of non-measured qudits, get their relative position with respect to the measured qudits.

Protected Attributes

- const QCircuit $*$ qc_

  pointer to constant quantum circuit
- ket psi_

  state vector
- std::vector$<$ idx $>$ dits_

  classical dits
- std::vector$<$ double $>$ probs_

  measurement probabilities
- std::vector$<$ idx $>$ subsys_

  relabel them after measurements

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  qpp::IDisplay::display() override

7.55.1 Detailed Description

Quantum circuit engine, executes qpp::QCircuit.

See also

qpp::QCircuit

7.55.2 Constructor & Destructor Documentation

7.55.2.1 QEngine() [1/3]

```
qpp::QEngine::QEngine (
            const QCircuit & qc )  [inline], [explicit]
```

Constructs a quantum engine out of a quantum circuit.

Note

The quantum circuit must be an lvalue

See also

qpp::QEngine(QCircuit&&)

Note

The initial underlying quantum state is set to $|0\rangle^{\otimes n}$

Parameters

qc	Quantum circuit

7.55.2.2 QEngine() [2/3]

```
qpp::QEngine::QEngine (
            const QEngine & )  [default]
```

Default copy constructor.

7.55.2.3 QEngine() [3/3]

```
qpp::QEngine::QEngine (
            QCircuit && )  [delete]
```

Disables rvalue QCircuit.

7.55.2.4 ∼QEngine()

```
virtual qpp::QEngine::∼QEngine ( )  [virtual], [default]
```

Default virtual destructor.

7.55.3 Member Function Documentation

7.55.3.1 display()

```
std::ostream& qpp::QEngine::display (
            std::ostream & os ) const  [inline], [override], [private], [virtual]
```

qpp::IDisplay::display() override

Writes to the output stream a textual representation of the state of the engine

Parameters

os	Output stream passed by reference

Returns

Reference to the output stream

Implements qpp::IDisplay.

7.55.3.2 execute() [1/3]

```
virtual void qpp::QEngine::execute (
            const QCircuit::iterator::value_type & elem )  [inline], [virtual]
```

Executes one step in the quantum circuit.

Parameters

elem	Step to be executed

Reimplemented in qpp::QNoisyEngine< NoiseModel >.

7.55.3.3 execute() [2/3]

```
void qpp::QEngine::execute (
            const QCircuit::iterator & it )  [inline]
```

Executes one step in the quantum circuit.

Parameters

it	Iterator to the step to be executed

7.55.3.4 execute() [3/3]

```
void qpp::QEngine::execute ( )  [inline]
```

Executes the entire quantum circuit.

7.55.3.5 get_circuit()

```
const QCircuit& qpp::QEngine::get_circuit ( ) const  [inline], [noexcept]
```

Quantum circuit.

Returns

Underlying quantum circuit

7.55.3.6 get_dit()

```
idx qpp::QEngine::get_dit (
            idx i ) const  [inline]
```

Value of the classical dit at position *i*.

Parameters

i	Classical dit index

Returns

Value of the classical dit at position *i*

7.55.3.7 get_dits()

```
std::vector<idx> qpp::QEngine::get_dits ( ) const  [inline]
```

Vector with the values of the underlying classical dits.

Returns

Vector of underlying classical dits

7.55.3.8 get_measured() [1/2]

```
bool qpp::QEngine::get_measured (
            idx i ) const  [inline]
```

Check whether qudit *i* was already measured.

Parameters

i	Qudit index

Returns

True if qudit *i* was already measured, false othwewise

7.55.3.9 get_measured() [2/2]

```
std::vector< idx > qpp::QEngine::get_measured ( ) const [inline]
```

Vector of already measured qudit indexes.

Returns

Vector of already measured qudit indexes

7.55.3.10 get_non_measured()

```
std::vector< idx > qpp::QEngine::get_non_measured ( ) const [inline]
```

Vector of non-measured qudit indexes.

Returns

Vector of non-measured qudit indexes

7.55.3.11 get_probs()

```
std::vector< double > qpp::QEngine::get_probs ( ) const [inline]
```

Vector of underlying measurement outcome probabilities.

Those should be interpreted as conditional probabilities based on the temporal order of the measurements, i.e. if we measure qubit 0, then measure qubit 1, and finally qubit 2, the resulting vector of outcome probabilities probs[2] should be interpreted as the conditional probability of qubit 2 having the outcome it had given that qubit 1 and qubit 0 had their given outcomes, respectively. As an example, if we measure the qubit 0 followed by the qubit 1 of a maximally entangled state $(|00\rangle + |11\rangle)/\sqrt{2}$, then the vector of outcome probabilities will be [0.5, 1].

Note

The probability vector has the same length as the vector of classical dits. If the measurement result is stored at the index *c_reg*, then the outcome probability is automatically stored at the same index *c_reg* in the probability vector.

Returns

Vector of underlying measurement outcome probabilities

7.55.3.12 get_psi()

```
ket qpp::QEngine::get_psi ( ) const [inline]
```

Underlying quantum state.

Returns

Underlying quantum state

7.55.3.13 get_relative_pos_()

```
std::vector<idx> qpp::QEngine::get_relative_pos_ (
            std::vector< idx > v ) [inline], [protected]
```

Giving a vector *V* of non-measured qudits, get their relative position with respect to the measured qudits.

Parameters

v	

Returns

Vector of qudit indexes

7.55.3.14 operator=()

```
QEngine& qpp::QEngine::operator= (
            const QEngine & ) [default]
```

Default copy assignment operator.

Returns

Reference to the current instance

7.55.3.15 reset()

```
void qpp::QEngine::reset ( ) [inline]
```

Resets the engine.

Re-initializes everything to zero and sets the initial state to $|0\rangle^{\otimes n}$

7.55.3.16 set_dit()

```
QEngine& qpp::QEngine::set_dit (
            idx i,
            idx value ) [inline]
```

Sets the classical dit at position *i*.

Parameters

i	Classical dit index
value	Classical dit value

Returns

Reference to the current instance

7.55.3.17 set_measured_()

```
void qpp::QEngine::set_measured_ (
            idx i )  [inline], [protected]
```

Marks qudit *i* as measured then re-label accordingly the remaining non-measured qudits.

Parameters

i	Qudit index

7.55.3.18 set_psi()

```
QEngine& qpp::QEngine::set_psi (
            const ket & psi )  [inline]
```

Sets the underlying quantum state to *psi*.

Note

The order is lexicographical with respect to the remaining non-measured qudits

Parameters

psi	State vector

Returns

Reference to the current instance

7.55.3.19 to_JSON()

```
std::string qpp::QEngine::to_JSON (
            bool enclosed_in_curly_brackets = true ) const  [inline], [override], [virtual]
```

qpp::IJOSN::to_JSON() override

Displays the state of the engine in JSON format

Parameters

enclosed_in_curly_brackets	If true, encloses the result in curly brackets

Returns

String containing the JSON representation of the state of the engine

Implements qpp::IJSON.

7.55.4 Member Data Documentation

7.55.4.1 dits_

```
std::vector<idx> qpp::QEngine::dits_  [protected]
```

classical dits

7.55.4.2 probs_

```
std::vector<double> qpp::QEngine::probs_  [protected]
```

measurement probabilities

7.55.4.3 psi_

```
ket qpp::QEngine::psi_  [protected]
```

state vector

7.55.4.4 qc_

```
const QCircuit* qpp::QEngine::qc_ [protected]
```

pointer to constant quantum circuit

7.55.4.5 subsys_

```
std::vector<idx> qpp::QEngine::subsys_ [protected]
```

relabel them after measurements

keeps track of the measured subsystems,

The documentation for this class was generated from the following file:

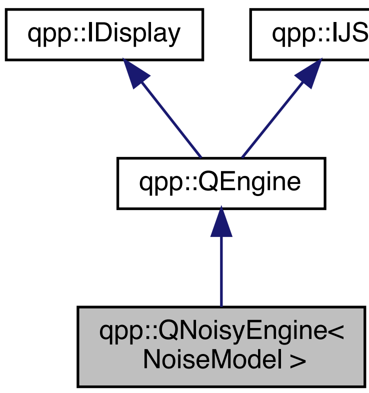
- classes/circuits/engines.h

7.56 qpp::QNoisyEngine< NoiseModel > Class Template Reference

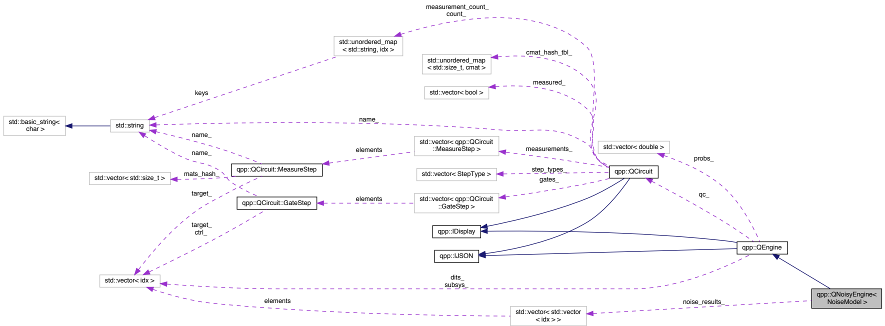
Noisy quantum circuit engine, executes qpp::QCircuit.

```
#include <classes/circuits/engines.h>
```

Inheritance diagram for qpp::QNoisyEngine< NoiseModel >:



Collaboration diagram for qpp::QNoisyEngine< NoiseModel >:



Public Member Functions

- QNoisyEngine (const QCircuit &qc, const NoiseModel &noise)

  Constructs a noisy quantum engine out of a quantum circuit.
- void execute (const QCircuit::iterator::value_type &elem) override

  Executes one step in the quantum circuit.
- std::vector< std::vector< idx > > get_noise_results () const

  Vector of noise results obtained before every step in the circuit.
- virtual void execute (const QCircuit::iterator::value_type &elem)

  Executes one step in the quantum circuit.
- void execute (const QCircuit::iterator &it)

  Executes one step in the quantum circuit.
- void execute ()

  Executes the entire quantum circuit.

Private Attributes

- const NoiseModel noise_

  quantum noise model
- std::vector< std::vector< idx > > noise_results_

  noise results

Additional Inherited Members

7.56.1 Detailed Description

template<typename NoiseModel>
class qpp::QNoisyEngine< NoiseModel >

Noisy quantum circuit engine, executes qpp::QCircuit.

See also

qpp::QCircuit, qpp::NoiseBase

Assumes an uncorrelated noise model that is applied to each non-measured qubit before every step in the logical circuit

Template Parameters

NoiseModel	Quantum noise model, should be derived from qpp::NoiseBase

7.56.2 Constructor & Destructor Documentation

7.56.2.1 QNoisyEngine()

```
template<typename NoiseModel >
qpp::QNoisyEngine< NoiseModel >::QNoisyEngine (
            const QCircuit & qc,
            const NoiseModel & noise )  [inline], [explicit]
```

Constructs a noisy quantum engine out of a quantum circuit.

Parameters

qc	Quantum circuit
noise	Quantum noise model

7.56.3 Member Function Documentation

7.56.3.1 execute() [1/4]

```
template<typename NoiseModel >
virtual void qpp::QEngine::execute  [inline]
```

Executes one step in the quantum circuit.

Parameters

elem	Step to be executed

7.56.3.2 execute() [2/4]

```
template<typename NoiseModel >
void qpp::QEngine::execute  [inline]
```

Executes the entire quantum circuit.

7.56.3.3 execute() [3/4]

```
template<typename NoiseModel >
void qpp::QEngine::execute  [inline]
```

Executes one step in the quantum circuit.

Parameters

it	Iterator to the step to be executed

7.56.3.4 execute() [4/4]

```
template<typename NoiseModel >
void qpp::QNoisyEngine< NoiseModel >::execute (
            const QCircuit::iterator::value_type & elem )  [inline], [override], [virtual]
```

Executes one step in the quantum circuit.

Parameters

elem	Step to be executed

Reimplemented from qpp::QEngine.

7.56.3.5 get_noise_results()

```
template<typename NoiseModel >
std::vector<std::vector<idx> > qpp::QNoisyEngine< NoiseModel >::get_noise_results ( ) const
[inline]
```

Vector of noise results obtained before every step in the circuit.

The first vector contains the noise measurement results obtained before applying the first step in the circuit, and so on, ordered by non-measured qudits. That is, the first element in the vector corresponding to noise obtained before a given step in the circuit represents the noise result obtained on the first non-measured qudit etc.

Returns

Vector of noise results

7.56.4 Member Data Documentation

7.56.4.1 noise_

```
template<typename NoiseModel >
const NoiseModel qpp::QNoisyEngine< NoiseModel >::noise_  [private]
```

quantum noise model

7.56.4.2 noise_results_

```
template<typename NoiseModel >
std::vector<std::vector<idx> > qpp::QNoisyEngine< NoiseModel >::noise_results_  [private]
```

noise results

The documentation for this class was generated from the following file:

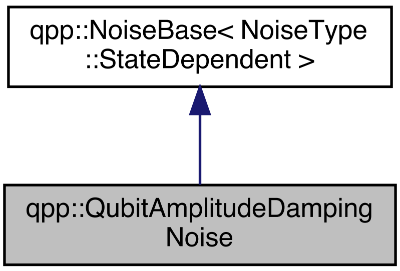
- classes/circuits/engines.h

7.57 qpp::QubitAmplitudeDampingNoise Class Reference

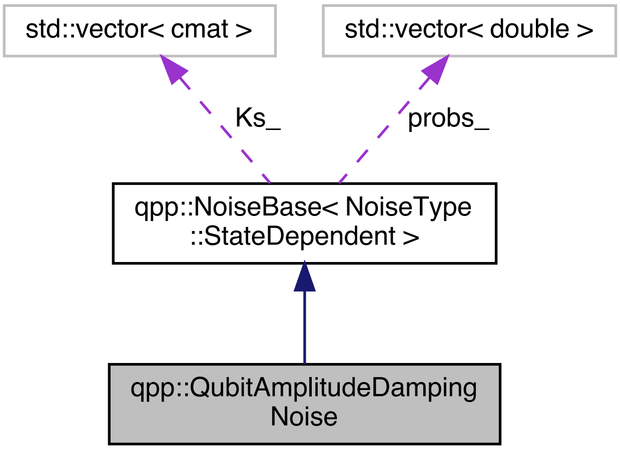
Qubit amplitude damping noise, as described in Nielsen and Chuang.

```
#include <classes/noise.h>
```

Inheritance diagram for qpp::QubitAmplitudeDampingNoise:



Collaboration diagram for qpp::QubitAmplitudeDampingNoise:



Public Member Functions

- QubitAmplitudeDampingNoise (double gamma)

    Qubit amplitude damping noise constructor.

Additional Inherited Members

7.57.1 Detailed Description

Qubit amplitude damping noise, as described in Nielsen and Chuang.

7.57.2 Constructor & Destructor Documentation

7.57.2.1 QubitAmplitudeDampingNoise()

```
qpp::QubitAmplitudeDampingNoise::QubitAmplitudeDampingNoise (
            double gamma )  [inline], [explicit]
```

Qubit amplitude damping noise constructor.

Parameters

gamma	Amplitude damping coefficient

The documentation for this class was generated from the following file:

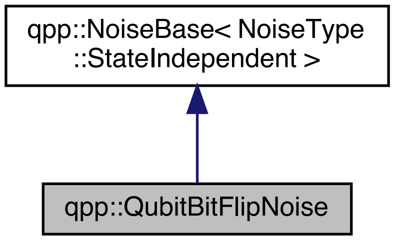
- classes/noise.h

7.58 qpp::QubitBitFlipNoise Class Reference

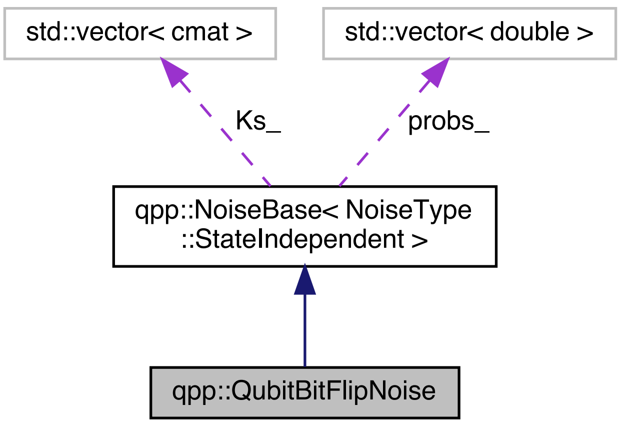
Qubit bit flip noise.

`#include <classes/noise.h>`

Inheritance diagram for qpp::QubitBitFlipNoise:



Collaboration diagram for qpp::QubitBitFlipNoise:



Public Member Functions

- QubitBitFlipNoise (double p)
  Qubit bit flip noise constructor.

Additional Inherited Members

7.58.1 Detailed Description

Qubit bit flip noise.

7.58.2 Constructor & Destructor Documentation

7.58.2.1 QubitBitFlipNoise()

```
qpp::QubitBitFlipNoise::QubitBitFlipNoise (
            double p )  [inline], [explicit]
```

Qubit bit flip noise constructor.

Parameters

p	Noise probability

The documentation for this class was generated from the following file:

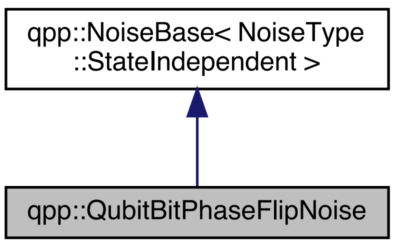
- classes/noise.h

7.59 qpp::QubitBitPhaseFlipNoise Class Reference

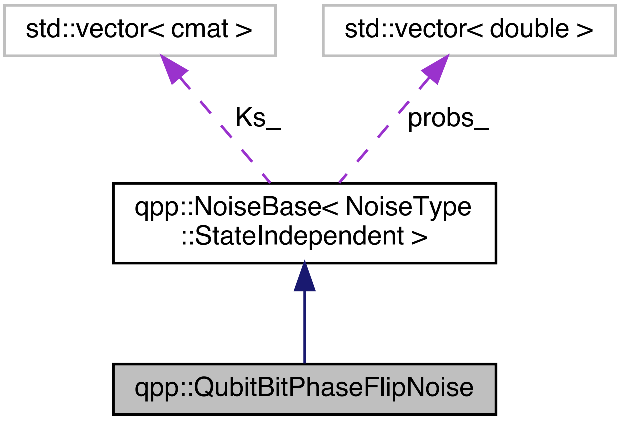
Qubit bit-phase flip (dephasing) noise.

```
#include <classes/noise.h>
```

Inheritance diagram for qpp::QubitBitPhaseFlipNoise:



Collaboration diagram for qpp::QubitBitPhaseFlipNoise:



Public Member Functions

- QubitBitPhaseFlipNoise (double p)
  Qubit bit-phase flip noise constructor.

Additional Inherited Members

7.59.1 Detailed Description

Qubit bit-phase flip (dephasing) noise.

7.59.2 Constructor & Destructor Documentation

7.59.2.1 QubitBitPhaseFlipNoise()

```
qpp::QubitBitPhaseFlipNoise::QubitBitPhaseFlipNoise (
            double p )  [inline], [explicit]
```

Qubit bit-phase flip noise constructor.

Parameters

p	Noise probability

The documentation for this class was generated from the following file:

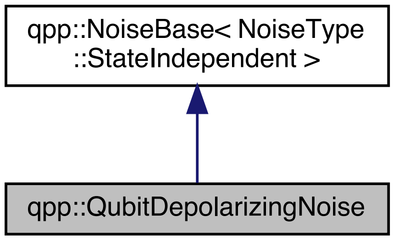
- classes/noise.h

7.60 qpp::QubitDepolarizingNoise Class Reference

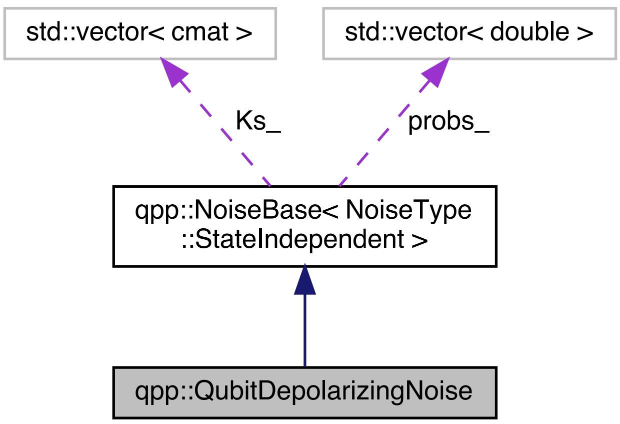
Qubit depolarizing noise.

`#include <classes/noise.h>`

Inheritance diagram for qpp::QubitDepolarizingNoise:



Collaboration diagram for qpp::QubitDepolarizingNoise:



Public Member Functions

- QubitDepolarizingNoise (double p)

  Qubit depolarizing noise constructor.

Additional Inherited Members

7.60.1 Detailed Description

Qubit depolarizing noise.

7.60.2 Constructor & Destructor Documentation

7.60.2.1 QubitDepolarizingNoise()

```
qpp::QubitDepolarizingNoise::QubitDepolarizingNoise (
            double p )  [inline], [explicit]
```

Qubit depolarizing noise constructor.

Parameters

p	Noise probability

The documentation for this class was generated from the following file:

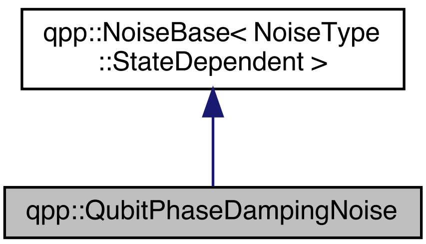
- classes/noise.h

7.61 qpp::QubitPhaseDampingNoise Class Reference

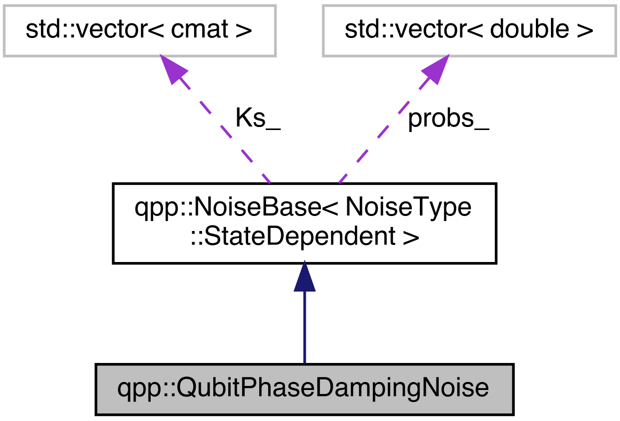
Qubit phase damping noise, as described in Nielsen and Chuang.

```
#include <classes/noise.h>
```

Inheritance diagram for qpp::QubitPhaseDampingNoise:



Collaboration diagram for qpp::QubitPhaseDampingNoise:



Public Member Functions

- QubitPhaseDampingNoise (double lambda)
  Qubit phase damping noise constructor.

Additional Inherited Members

7.61.1 Detailed Description

Qubit phase damping noise, as described in Nielsen and Chuang.

7.61.2 Constructor & Destructor Documentation

7.61.2.1 QubitPhaseDampingNoise()

```
qpp::QubitPhaseDampingNoise::QubitPhaseDampingNoise (
            double lambda )  [inline], [explicit]
```

Qubit phase damping noise constructor.

Parameters

lambda	Phase damping coefficient

The documentation for this class was generated from the following file:

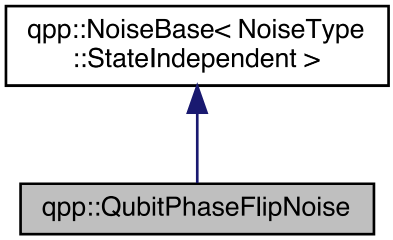
- classes/noise.h

7.62 qpp::QubitPhaseFlipNoise Class Reference

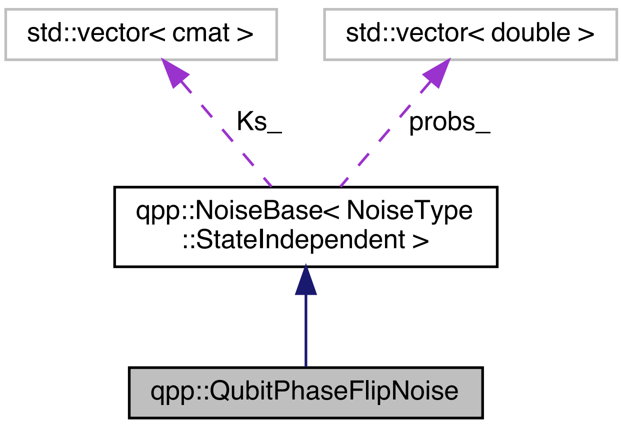
Qubit phase flip (dephasing) noise.

`#include <classes/noise.h>`

Inheritance diagram for qpp::QubitPhaseFlipNoise:



Collaboration diagram for qpp::QubitPhaseFlipNoise:



Public Member Functions

- QubitPhaseFlipNoise (double p)

  Qubit phase flip (dephasing) noise constructor.

Additional Inherited Members

7.62.1 Detailed Description

Qubit phase flip (dephasing) noise.

7.62.2 Constructor & Destructor Documentation

7.62.2.1 QubitPhaseFlipNoise()

```
qpp::QubitPhaseFlipNoise::QubitPhaseFlipNoise (
            double p ) [inline], [explicit]
```

Qubit phase flip (dephasing) noise constructor.

Parameters

p	Noise probability

The documentation for this class was generated from the following file:

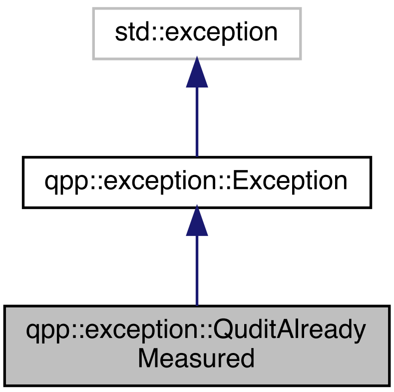
- classes/noise.h

7.63 qpp::exception::QuditAlreadyMeasured Class Reference

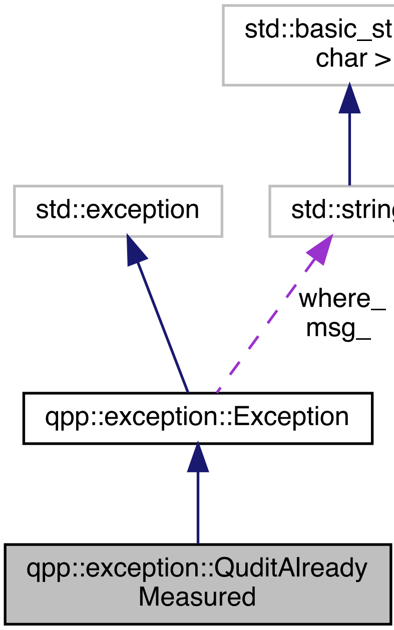
Qudit was already measured exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::QuditAlreadyMeasured:



Collaboration diagram for qpp::exception::QuditAlreadyMeasured:



Public Member Functions

- std::string description () const override

  Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.63.1 Detailed Description

Qudit was already measured exception.

The qudit was already measured and cannot be measured again

7.63.2 Member Function Documentation

7.63.2.1 description()

```
std::string qpp::exception::QuditAlreadyMeasured::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.63.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

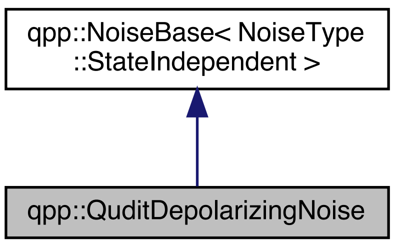
- classes/exception.h

7.64 qpp::QuditDepolarizingNoise Class Reference

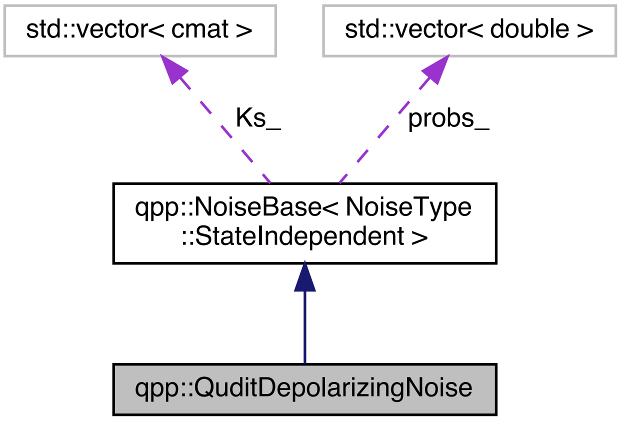
Qudit depolarizing noise.

```
#include <classes/noise.h>
```

Inheritance diagram for qpp::QuditDepolarizingNoise:



Collaboration diagram for qpp::QuditDepolarizingNoise:



Public Member Functions

- QuditDepolarizingNoise (double p, idx d)

  Qudit depolarizing noise constructor.

Private Member Functions

- std::vector< cmat > fill_Ks_ (idx d) const

  Fills the Kraus operator vector.
- std::vector< double > fill_probs_ (double p, idx d) const

  Fills the probability vector.

Additional Inherited Members

7.64.1 Detailed Description

Qudit depolarizing noise.

7.64.2 Constructor & Destructor Documentation

7.64.2.1 QuditDepolarizingNoise()

```
qpp::QuditDepolarizingNoise::QuditDepolarizingNoise (
            double p,
            idx d )  [inline], [explicit]
```

Qudit depolarizing noise constructor.

Parameters

p	Noise probability
d	Qudit dimension

7.64.3 Member Function Documentation

7.64.3.1 fill_Ks_()

```
std::vector<cmat> qpp::QuditDepolarizingNoise::fill_Ks_ (
            idx d ) const  [inline], [private]
```

Fills the Kraus operator vector.

Parameters

d	Qudit dimension

Returns

Vector of Kraus operators representing the depolarizing noise

7.64.3.2 fill_probs_()

```
std::vector<double> qpp::QuditDepolarizingNoise::fill_probs_ (
            double p,
            idx d ) const  [inline], [private]
```

Fills the probability vector.

Parameters

p	Probability
d	Qudit dimension

Returns

Probability vector

The documentation for this class was generated from the following file:

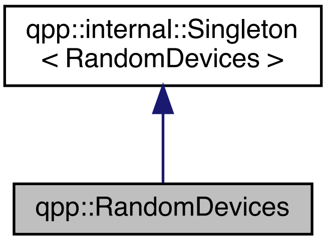
- classes/noise.h

7.65 qpp::RandomDevices Class Reference

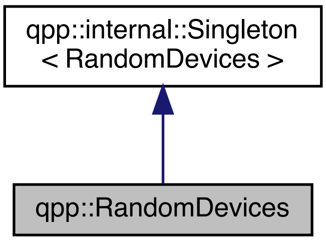
Singleton class that manages the source of randomness in the library.

```
#include <classes/random_devices.h>
```

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



Public Member Functions

- std::mt19937 & get_prng ()

  Returns a reference to the internal PRNG object.
- std::istream & load (std::istream &is)

  Loads the state of the PRNG from an input stream.
- std::ostream & save (std::ostream &os) const

  Saves the state of the PRNG to an output stream.

Private Member Functions

- RandomDevices ()

  Initializes and seeds the random number generators.
- ∼RandomDevices ()=default

  Default destructor.

Private Attributes

- std::random_device rd_

  *used to seed std::mt19937 prng_*
- std::mt19937 prng_

  Mersenne twister random number generator.

Friends

- class internal::Singleton< RandomDevices >

Additional Inherited Members

7.65.1 Detailed Description

Singleton class that manages the source of randomness in the library.

Consists of a wrapper around an std::mt19937 Mersenne twister random number generator engine and an std↩ ::random_device engine. The latter is used to seed the Mersenne twister.

Warning

This class DOES NOT seed the standard C number generator used by Eigen::Matrix::Random(), since it is not thread safe. Do not use Eigen::Matrix::Random() or functions that depend on the C style random number engine, but use qpp::rand() instead!

7.65.2 Constructor & Destructor Documentation

7.65.2.1 RandomDevices()

```
qpp::RandomDevices::RandomDevices ( )  [inline], [private]
```

Initializes and seeds the random number generators.

7.65.2.2 ∼RandomDevices()

```
qpp::RandomDevices::∼RandomDevices ( )  [private], [default]
```

Default destructor.

7.65.3 Member Function Documentation

7.65.3.1 get_prng()

```
std::mt19937& qpp::RandomDevices::get_prng ( )  [inline]
```

Returns a reference to the internal PRNG object.

Returns

Reference to the internal PRNG object

7.65.3.2 load()

```
std::istream& qpp::RandomDevices::load (
            std::istream & is )  [inline]
```

Loads the state of the PRNG from an input stream.

Parameters

is	Input stream

Returns

The input stream

7.65.3.3 save()

```
std::ostream& qpp::RandomDevices::save (
            std::ostream & os ) const  [inline]
```

Saves the state of the PRNG to an output stream.

Parameters

os	Output stream

Returns

The output stream

7.65.4 Friends And Related Function Documentation

7.65.4.1 internal::Singleton< RandomDevices >

```
friend class internal::Singleton< RandomDevices > [friend]
```

7.65.5 Member Data Documentation

7.65.5.1 prng_

```
std::mt19937 qpp::RandomDevices::prng_ [private]
```

Mersenne twister random number generator.

7.65.5.2 rd_

```
std::random_device qpp::RandomDevices::rd_ [private]
```

used to seed std::mt19937 prng_

The documentation for this class was generated from the following file:

- classes/random_devices.h

7.66 qpp::internal::Singleton< T > Class Template Reference

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

```
#include <internal/classes/singleton.h>
```

Static Public Member Functions

- static T & get_instance () noexcept(std::is_nothrow_constructible< T >::value)
- static T & get_thread_local_instance () noexcept(std::is_nothrow_constructible< T >::value)

Protected Member Functions

- Singleton () noexcept=default
- Singleton (const Singleton &)=delete
- Singleton & operator= (const Singleton &)=delete
- virtual ~Singleton ()=default

7.66.1 Detailed Description

template<typename T>
class qpp::internal::Singleton< T >

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

To implement a singleton, derive your class from qpp::internal::Singleton, make qpp::internal::Singleton a friend of your class, then declare the constructor and destructor of your class as private. To get an instance, use the static member function qpp::internal::Singleton::get_instance() (qpp::internal::Singleton::get_thread_local_instance()), which returns a reference (thread_local reference) to your newly created singleton (thread-safe in C++11).

Example:

```
class MySingleton: public qpp::internal::Singleton<MySingleton>
{
       friend class qpp::internal::Singleton<MySingleton>;
public:
    // Declare all public members here
private:
    MySingleton()
    {
        // Implement the constructor here
    }
    ~MySingleton()
    {
        // Implement the destructor here
    }
};

MySingleton& mySingleton = MySingleton::get_instance(); // Get an instance
thread_local MySingleton& tls = MySingleton::get_thread_local_instance();
// Get a thread_local instance
```

See also

Code of qpp::Codes, qpp::Gates, qpp::Init, qpp::RandomDevices, qpp::States or qpp.h for real world examples of usage.

7.66.2 Constructor & Destructor Documentation

7.66.2.1 Singleton() [1/2]

```
template<typename T>
qpp::internal::Singleton< T >::Singleton ( ) [protected], [default], [noexcept]
```

7.66.2.2 Singleton() [2/2]

```
template<typename T>
qpp::internal::Singleton< T >::Singleton (
            const Singleton< T > & ) [protected], [delete]
```

7.66.2.3 ∼Singleton()

```
template<typename T>
virtual qpp::internal::Singleton< T >::∼Singleton ( ) [protected], [virtual], [default]
```

7.66.3 Member Function Documentation

7.66.3.1 get_instance()

```
template<typename T>
static T& qpp::internal::Singleton< T >::get_instance ( ) [inline], [static], [noexcept]
```

7.66.3.2 get_thread_local_instance()

```
template<typename T>
static T& qpp::internal::Singleton< T >::get_thread_local_instance ( ) [inline], [static],
[noexcept]
```

7.66.3.3 operator=()

```
template<typename T>
Singleton& qpp::internal::Singleton< T >::operator= (
            const Singleton< T > & ) [protected], [delete]
```

The documentation for this class was generated from the following file:

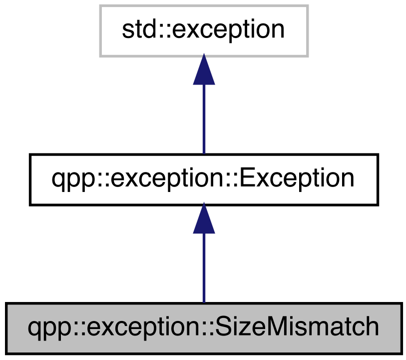
- internal/classes/singleton.h

7.67 qpp::exception::SizeMismatch Class Reference

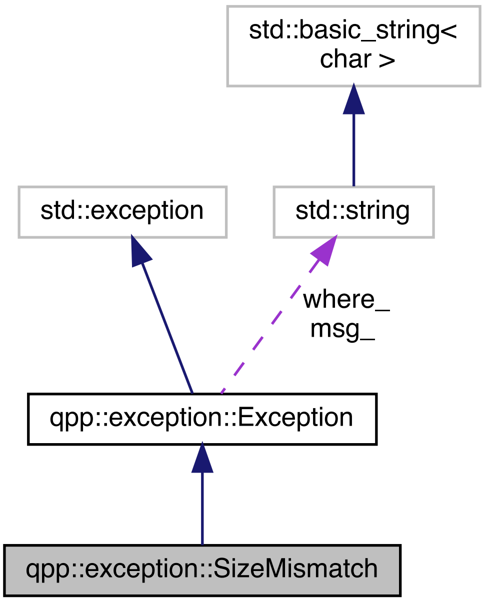
Size mismatch exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::SizeMismatch:



Collaboration diagram for qpp::exception::SizeMismatch:



Public Member Functions

- std::string description () const override
  Exception description.
- Exception (const std::string &where)
  Constructs an exception.

7.67.1 Detailed Description

Size mismatch exception.

Sizes do not match

7.67.2 Member Function Documentation

7.67.2.1 description()

```
std::string qpp::exception::SizeMismatch::description ( ) const  [inline], [override], [virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.67.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

- classes/exception.h

7.68 qpp::NoiseType::StateDependent Class Reference

Template tag, used whenever the noise is state-dependent.

`#include <classes/noise.h>`

7.68.1 Detailed Description

Template tag, used whenever the noise is state-dependent.

The documentation for this class was generated from the following file:

- classes/noise.h

7.69 qpp::NoiseType::StateIndependent Class Reference

Template tag, used whenever the noise is state-independent.

`#include <classes/noise.h>`

7.69.1 Detailed Description

Template tag, used whenever the noise is state-independent.

The documentation for this class was generated from the following file:

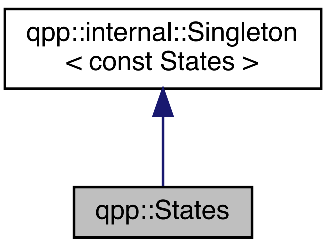
- classes/noise.h

7.70 qpp::States Class Reference

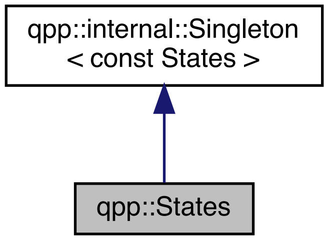
const Singleton class that implements most commonly used states

`#include <classes/states.h>`

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



Public Member Functions

- ket mes (idx d=2) const

    Maximally entangled state of 2 qudits.
- ket zero (idx n, idx d=2) const

    Zero state of n qudits.
- ket one (idx n, idx d=2) const

    One state of n qudits.
- ket jn (idx j, idx n, idx d=2) const

    $|j\rangle^{\otimes n}$ *state of n qudits*
- ket plus (idx n) const

    Plus state of n qubits.
- ket minus (idx n) const

    Minus state of n qubits.

Public Attributes

- ket x0 {ket::Zero(2)}

    Pauli Sigma-X 0-eigenstate |+>
- ket x1 {ket::Zero(2)}

    Pauli Sigma-X 1-eigenstate |->
- ket y0 {ket::Zero(2)}

    Pauli Sigma-Y 0-eigenstate |y+>
- ket y1 {ket::Zero(2)}

    Pauli Sigma-Y 1-eigenstate |y->
- ket z0 {ket::Zero(2)}

    Pauli Sigma-Z 0-eigenstate |0>
- ket z1 {ket::Zero(2)}

    Pauli Sigma-Z 1-eigenstate |1>
- cmat px0 {cmat::Zero(2, 2)}

    Projector onto the Pauli Sigma-X 0-eigenstate |+><+|.
- cmat px1 {cmat::Zero(2, 2)}

    Projector onto the Pauli Sigma-X 1-eigenstate |-><-|.

- cmat py0 {cmat::Zero(2, 2)}

    Projector onto the Pauli Sigma-Y 0-eigenstate |y+><y+|.
- cmat py1 {cmat::Zero(2, 2)}

    Projector onto the Pauli Sigma-Y 1-eigenstate |y-><y-|.
- cmat pz0 {cmat::Zero(2, 2)}

    Projector onto the Pauli Sigma-Z 0-eigenstate |0><0|.
- cmat pz1 {cmat::Zero(2, 2)}

    Projector onto the Pauli Sigma-Z 1-eigenstate |1><1|.
- ket b00 {ket::Zero(4)}

    Bell-00 state, as described in Nielsen and Chuang.
- ket b01 {ket::Zero(4)}

    Bell-01 state, as described in Nielsen and Chuang.
- ket b10 {ket::Zero(4)}

    Bell-10 state, as described in Nielsen and Chuang.
- ket b11 {ket::Zero(4)}

    Bell-11 state, as described in Nielsen and Chuang.
- cmat pb00 {cmat::Zero(4, 4)}

    Projector onto the Bell-00 state.
- cmat pb01 {cmat::Zero(4, 4)}

    Projector onto the Bell-01 state.
- cmat pb10 {cmat::Zero(4, 4)}

    Projector onto the Bell-10 state.
- cmat pb11 {cmat::Zero(4, 4)}

    Projector onto the Bell-11 state.
- ket GHZ {ket::Zero(8)}

    GHZ state.
- ket W {ket::Zero(8)}

    W state.
- cmat pGHZ {cmat::Zero(8, 8)}

    Projector onto the GHZ state.
- cmat pW {cmat::Zero(8, 8)}

    Projector onto the W state.

Private Member Functions

- States ()
- ∼States ()=default

    Default destructor.

Friends

- class internal::Singleton< const States >

Additional Inherited Members

7.70.1 Detailed Description

const Singleton class that implements most commonly used states

7.70.2 Constructor & Destructor Documentation

7.70.2.1 States()

```
qpp::States::States ( )  [inline], [private]
```

Initialize the states

7.70.2.2 ∼States()

```
qpp::States::∼States ( )  [private], [default]
```

Default destructor.

7.70.3 Member Function Documentation

7.70.3.1 jn()

```
ket qpp::States::jn (
            idx j,
            idx n,
            idx d = 2 ) const  [inline]
```

$|j\rangle^{\otimes n}$ state of *n* qudits

Parameters

j	Non-negative integer
n	Non-negative integer
d	Subsystem dimensions

Returns

$|j\rangle^{\otimes n}$ state of *n* qudits

7.70.3.2 mes()

```
ket qpp::States::mes (
            idx d = 2 ) const  [inline]
```

Maximally entangled state of 2 qudits.

Parameters

d	Subsystem dimensions

Returns

Maximally entangled state $\frac{1}{\sqrt{d}} \sum_{j=0}^{d-1} |jj\rangle$ of 2 qudits

7.70.3.3 minus()

```
ket qpp::States::minus (
            idx n ) const  [inline]
```

Minus state of *n* qubits.

Parameters

n	Non-negative integer

Returns

Minus state $|-\rangle^{\otimes n}$ of *n* qubits

7.70.3.4 one()

```
ket qpp::States::one (
            idx n,
            idx d = 2 ) const  [inline]
```

One state of *n* qudits.

Parameters

n	Non-negative integer
d	Subsystem dimensions

Returns

One state $|1\rangle^{\otimes n}$ of *n* qudits

7.70.3.5 plus()

```
ket qpp::States::plus (
            idx n ) const  [inline]
```

Plus state of *n* qubits.

Parameters

n	Non-negative integer

Returns

Plus state $|+\rangle^{\otimes n}$ of *n* qubits

7.70.3.6 zero()

```
ket qpp::States::zero (
            idx n,
            idx d = 2 ) const  [inline]
```

Zero state of *n* qudits.

Parameters

n	Non-negative integer
d	Subsystem dimensions

Returns

Zero state $|0\rangle^{\otimes n}$ of *n* qudits

7.70.4 Friends And Related Function Documentation

7.70.4.1 internal::Singleton< const States >

```
friend class internal::Singleton< const States >  [friend]
```

7.70.5 Member Data Documentation

7.70.5.1 b00

```
ket qpp::States::b00 {ket::Zero(4)}
```

Bell-00 state, as described in Nielsen and Chuang.

7.70.5.2 b01

```
ket qpp::States::b01 {ket::Zero(4)}
```

Bell-01 state, as described in Nielsen and Chuang.

7.70.5.3 b10

```
ket qpp::States::b10 {ket::Zero(4)}
```

Bell-10 state, as described in Nielsen and Chuang.

7.70.5.4 b11

```
ket qpp::States::b11 {ket::Zero(4)}
```

Bell-11 state, as described in Nielsen and Chuang.

7.70.5.5 GHZ

```
ket qpp::States::GHZ {ket::Zero(8)}
```

GHZ state.

7.70.5.6 pb00

```
cmat qpp::States::pb00 {cmat::Zero(4, 4)}
```

Projector onto the Bell-00 state.

7.70.5.7 pb01

```
cmat qpp::States::pb01 {cmat::Zero(4, 4)}
```

Projector onto the Bell-01 state.

7.70.5.8 pb10

```
cmat qpp::States::pb10 {cmat::Zero(4, 4)}
```

Projector onto the Bell-10 state.

7.70.5.9 pb11

```
cmat qpp::States::pb11 {cmat::Zero(4, 4)}
```

Projector onto the Bell-11 state.

7.70.5.10 pGHZ

```
cmat qpp::States::pGHZ {cmat::Zero(8, 8)}
```

Projector onto the GHZ state.

7.70.5.11 pW

```
cmat qpp::States::pW {cmat::Zero(8, 8)}
```

Projector onto the W state.

7.70.5.12 px0

```
cmat qpp::States::px0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-X 0-eigenstate $|+><+|$.

7.70.5.13 px1

```
cmat qpp::States::px1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-X 1-eigenstate |-><-|.

7.70.5.14 py0

```
cmat qpp::States::py0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Y 0-eigenstate |y+><y+|.

7.70.5.15 py1

```
cmat qpp::States::py1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Y 1-eigenstate |y-><y-|.

7.70.5.16 pz0

```
cmat qpp::States::pz0 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Z 0-eigenstate |0><0|.

7.70.5.17 pz1

```
cmat qpp::States::pz1 {cmat::Zero(2, 2)}
```

Projector onto the Pauli Sigma-Z 1-eigenstate |1><1|.

7.70.5.18 W

```
ket qpp::States::W {ket::Zero(8)}
```

W state.

7.70.5.19 x0

```
ket qpp::States::x0 {ket::Zero(2)}
```

Pauli Sigma-X 0-eigenstate |+>

7.70.5.20 x1

```
ket qpp::States::x1 {ket::Zero(2)}
```

Pauli Sigma-X 1-eigenstate |->

7.70.5.21 y0

```
ket qpp::States::y0 {ket::Zero(2)}
```

Pauli Sigma-Y 0-eigenstate |y+>

7.70.5.22 y1

```
ket qpp::States::y1 {ket::Zero(2)}
```

Pauli Sigma-Y 1-eigenstate |y->

7.70.5.23 z0

```
ket qpp::States::z0 {ket::Zero(2)}
```

Pauli Sigma-Z 0-eigenstate |0>

7.70.5.24 z1

```
ket qpp::States::z1 {ket::Zero(2)}
```

Pauli Sigma-Z 1-eigenstate |1>

The documentation for this class was generated from the following file:

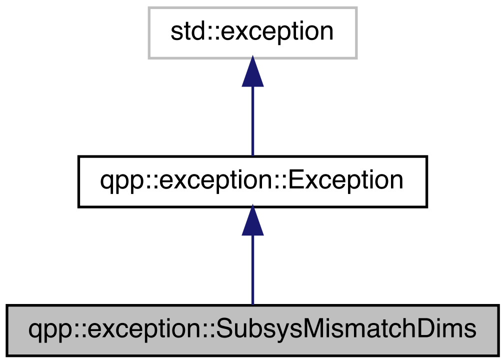
- classes/states.h

7.71 qpp::exception::SubsysMismatchDims Class Reference

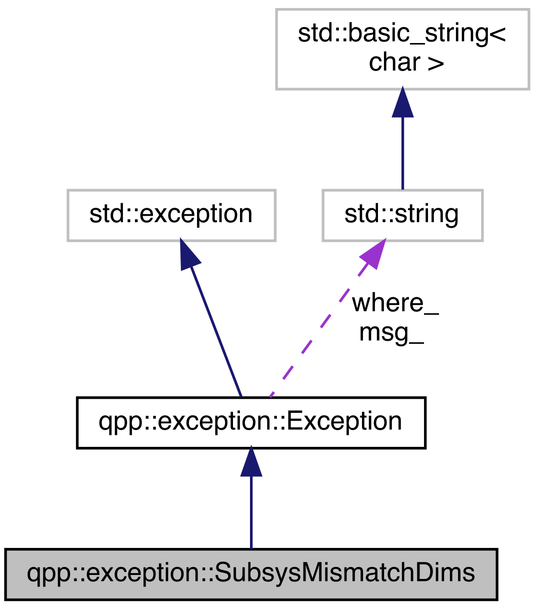
Subsystems mismatch dimensions exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::SubsysMismatchDims:



Collaboration diagram for qpp::exception::SubsysMismatchDims:



Public Member Functions

- std::string description () const override

    Exception description.
- Exception (const std::string &where)

    Constructs an exception.

7.71.1 Detailed Description

Subsystems mismatch dimensions exception.

std::vector<idx> of subsystem labels has duplicates, or has entries that are larger than the size of the std↩ ::vector<idx> of dimensions

7.71.2 Member Function Documentation

7.71.2.1 description()

```
std::string qpp::exception::SubsysMismatchDims::description ( ) const  [inline], [override],
[virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.71.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

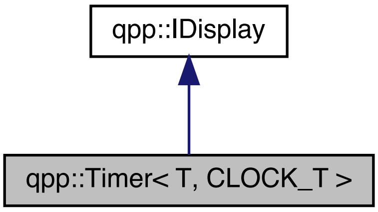
- classes/exception.h

7.72 qpp::Timer< T, CLOCK_T > Class Template Reference

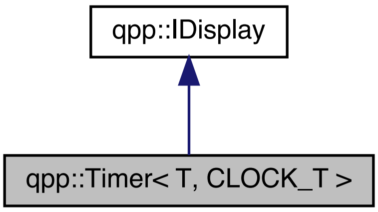
Chronometer.

`#include <classes/timer.h>`

Inheritance diagram for qpp::Timer< T, CLOCK_T >:



Collaboration diagram for qpp::Timer< T, CLOCK_T >:



Public Member Functions

- Timer () noexcept

  Constructs an instance with the current time as the starting point.
- virtual ~Timer ()=default

  Default virtual destructor.
- void tic () noexcept

  Resets the chronometer.
- const Timer & toc () noexcept

  Stops the chronometer.
- double tics () const noexcept

  Time passed in the duration specified by T.
- template<typename U = T>
  U get_duration () const noexcept

  Duration specified by U.

Protected Attributes

- CLOCK_T::time_point start_
- CLOCK_T::time_point end_

Private Member Functions

- std::ostream & display (std::ostream &os) const override

  qpp::IDisplay::display() override

7.72.1 Detailed Description

template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock>
class qpp::Timer< T, CLOCK_T >

Chronometer.

Template Parameters

T	Tics duration, default is std::chrono::duration<double>, i.e. seconds in double precision
CLOCK↩_T	Clock's type, default is std::chrono::steady_clock, not affected by wall clock changes during runtime

7.72.2 Constructor & Destructor Documentation

7.72.2.1 Timer()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
qpp::Timer< T, CLOCK_T >::Timer ( )  [inline], [noexcept]
```

Constructs an instance with the current time as the starting point.

7.72.2.2 ∼Timer()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
virtual qpp::Timer< T, CLOCK_T >::∼Timer ( )  [virtual], [default]
```

Default virtual destructor.

7.72.3 Member Function Documentation

7.72.3.1 display()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
std::ostream& qpp::Timer< T, CLOCK_T >::display (
            std::ostream & os ) const  [inline], [override], [private], [virtual]
```

qpp::IDisplay::display() override

Writes to the output stream the number of tics (specified by T) that passed between the instantiation/reset and invocation of qpp::Timer::toc()

Parameters

os	Output stream passed by reference

Returns

Reference to the output stream

Implements qpp::IDisplay.

7.72.3.2 get_duration()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
template<typename U = T>
U qpp::Timer< T, CLOCK_T >::get_duration ( ) const  [inline], [noexcept]
```

Duration specified by U.

Template Parameters

U	Duration, default is T, which defaults to std::chrono::duration<double>, i.e. seconds in double precision

Returns

Duration that passed between the instantiation/reset and invocation of qpp::Timer::toc()

7.72.3.3 tic()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady←
_clock>
void qpp::Timer< T, CLOCK_T >::tic ( ) [inline], [noexcept]
```

Resets the chronometer.

Resets the starting/ending point to the current time

7.72.3.4 tics()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady←
_clock>
double qpp::Timer< T, CLOCK_T >::tics ( ) const [inline], [noexcept]
```

Time passed in the duration specified by T.

Returns

Number of tics (specified by T) that passed between the instantiation/reset and invocation of qpp::Timer::toc()

7.72.3.5 toc()

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady←
_clock>
const Timer& qpp::Timer< T, CLOCK_T >::toc ( ) [inline], [noexcept]
```

Stops the chronometer.

Set the current time as the ending point

Returns

Reference to the current instance

7.72.4 Member Data Documentation

7.72.4.1 end_

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady←
_clock>
CLOCK_T::time_point qpp::Timer< T, CLOCK_T >::end_ [protected]
```

7.72.4.2 start_

```
template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady↩
_clock>
CLOCK_T::time_point qpp::Timer< T, CLOCK_T >::start_  [protected]
```

The documentation for this class was generated from the following file:

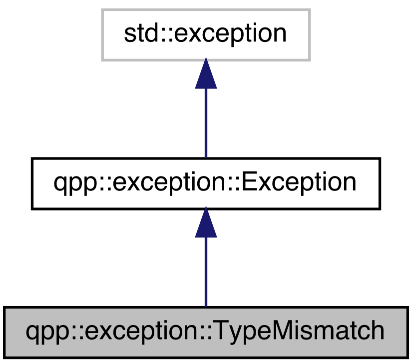
- classes/timer.h

7.73 qpp::exception::TypeMismatch Class Reference

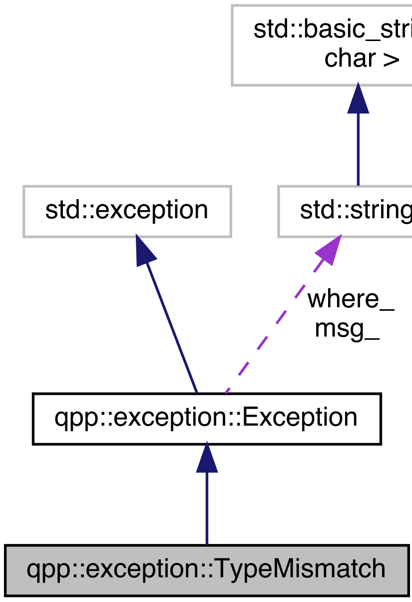
Type mismatch exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::TypeMismatch:



Collaboration diagram for qpp::exception::TypeMismatch:



Public Member Functions

- std::string description () const override
  Exception description.
- Exception (const std::string &where)
  Constructs an exception.

7.73.1 Detailed Description

Type mismatch exception.

Scalar types do not match

7.73.2 Member Function Documentation

7.73.2.1 description()

`std::string qpp::exception::TypeMismatch::description ( ) const [inline], [override], [virtual]`

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.73.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

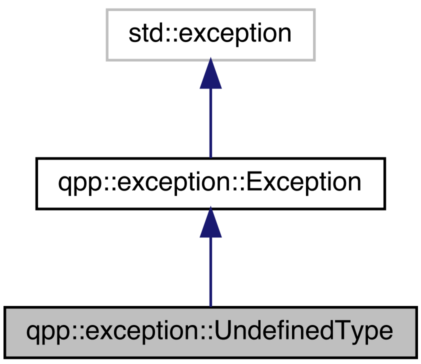
- classes/exception.h

7.74 qpp::exception::UndefinedType Class Reference

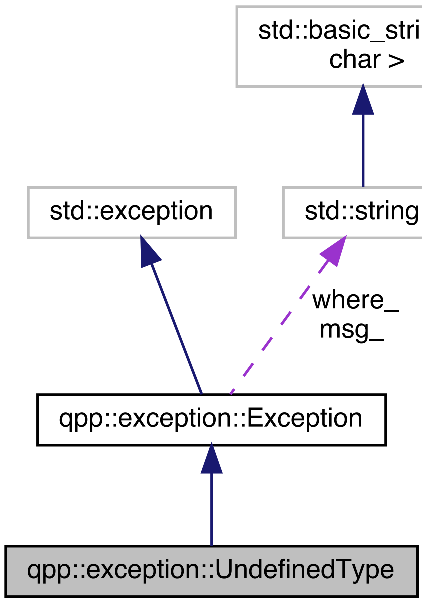
Not defined for this type exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::UndefinedType:



Collaboration diagram for qpp::exception::UndefinedType:



Public Member Functions

- std::string description () const override

  Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.74.1 Detailed Description

Not defined for this type exception.

Templated specialization is not defined for this type

7.74.2 Member Function Documentation

7.74.2.1 description()

`std::string qpp::exception::UndefinedType::description ( ) const [inline], [override], [virtual]`

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.74.2.2 Exception()

qpp::exception::Exception::Exception [inline], [explicit]

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

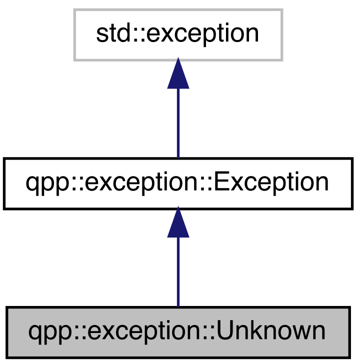
- classes/exception.h

7.75 qpp::exception::Unknown Class Reference

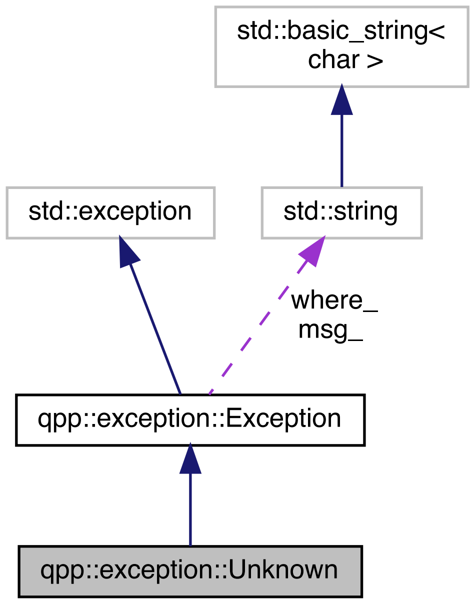
Unknown exception.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::exception::Unknown:



Collaboration diagram for qpp::exception::Unknown:



Public Member Functions

- std::string description () const override

  Exception description.
- Exception (const std::string &where)

  Constructs an exception.

7.75.1 Detailed Description

Unknown exception.

Thrown when no other exception is suitable (not recommended, it is better to define another suitable exception type)

7.75.2 Member Function Documentation

7.75.2.1 description()

```
std::string qpp::exception::Unknown::description ( ) const  [inline], [override], [virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.75.2.2 Exception()

```
qpp::exception::Exception::Exception [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

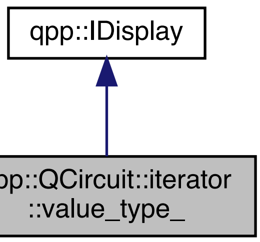
The documentation for this class was generated from the following file:

- classes/exception.h

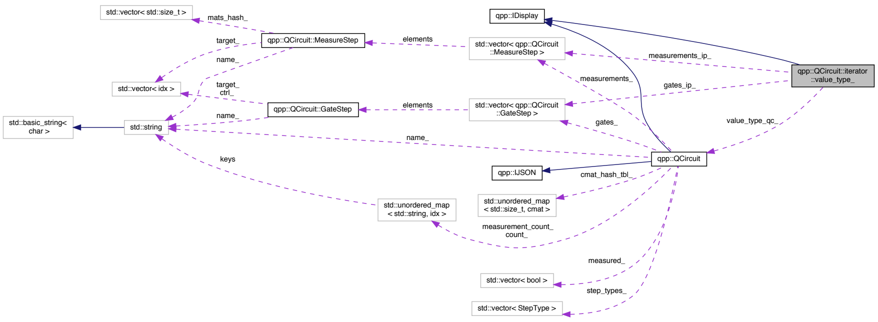
7.76 qpp::QCircuit::iterator::value_type_ Class Reference

Value type class for qpp::QCircuit::iterator.

Inheritance diagram for qpp::QCircuit::iterator::value_type_:



Collaboration diagram for qpp::QCircuit::iterator::value_type_:



Public Member Functions

- value_type_ (const QCircuit ∗value_type_qc)
  Default value_type_ constructor.
- value_type_ (const value_type_ &)=default
  Default copy constructor.
- value_type_ & operator= (const value_type_ &)=default
  Default copy assignment operator.

Public Attributes

- const QCircuit ∗ value_type_qc_
  < non-owning pointer to the grand-parent const quantum circuit
- StepType type_ {StepType::NONE}
  step type
- idx ip_ {static_cast<idx>(-1)}
  instruction pointer
- std::vector< GateStep >::const_iterator gates_ip_ {}
  gates instruction pointer
- std::vector< MeasureStep >::const_iterator measurements_ip_ {}
  measurements instruction pointer

Private Member Functions

- std::ostream & display (std::ostream &os) const override
  qpp::IDisplay::display() override

7.76.1 Detailed Description

Value type class for qpp::QCircuit::iterator.

7.76.2 Constructor & Destructor Documentation

7.76.2.1 value_type_() [1/2]

```
qpp::QCircuit::iterator::value_type_::value_type_ (
            const QCircuit * value_type_qc )  [inline], [explicit]
```

Default value_type_ constructor.

Parameters

value_type_qc	Pointer to constant quantum circuit

7.76.2.2 value_type_() [2/2]

```
qpp::QCircuit::iterator::value_type_::value_type_ (
            const value_type_ & ) [default]
```

Default copy constructor.

7.76.3 Member Function Documentation

7.76.3.1 display()

```
std::ostream& qpp::QCircuit::iterator::value_type_::display (
            std::ostream & os ) const [inline], [override], [private], [virtual]
```

qpp::IDisplay::display() override

Writes to the output stream the textual representation of the iterator de-referenced element

Parameters

os	Output stream passed by reference

Returns

Reference to the output stream

Implements qpp::IDisplay.

7.76.3.2 operator=()

```
value_type_& qpp::QCircuit::iterator::value_type_::operator= (
            const value_type_ & ) [default]
```

Default copy assignment operator.

Returns

Reference to the current instance

7.76.4 Member Data Documentation

7.76.4.1 gates_ip_

```
std::vector<GateStep>::const_iterator qpp::QCircuit::iterator::value_type_::gates_ip_ {}
```

gates instruction pointer

7.76.4.2 ip_

```
idx qpp::QCircuit::iterator::value_type_::ip_ {static_cast<idx>(-1)}
```

instruction pointer

7.76.4.3 measurements_ip_

```
std::vector<MeasureStep>::const_iterator qpp::QCircuit::iterator::value_type_::measurements_←
ip_ {}
```

measurements instruction pointer

7.76.4.4 type_

```
StepType qpp::QCircuit::iterator::value_type_::type_ {StepType::NONE}
```

step type

7.76.4.5 value_type_qc_

```
const QCircuit* qpp::QCircuit::iterator::value_type_::value_type_qc_
```

< non-owning pointer to the grand-parent const quantum circuit

The documentation for this class was generated from the following file:

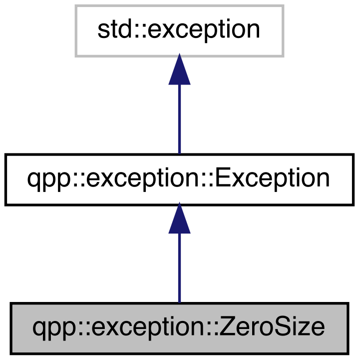
- classes/circuits/circuits.h

7.77 qpp::exception::ZeroSize Class Reference

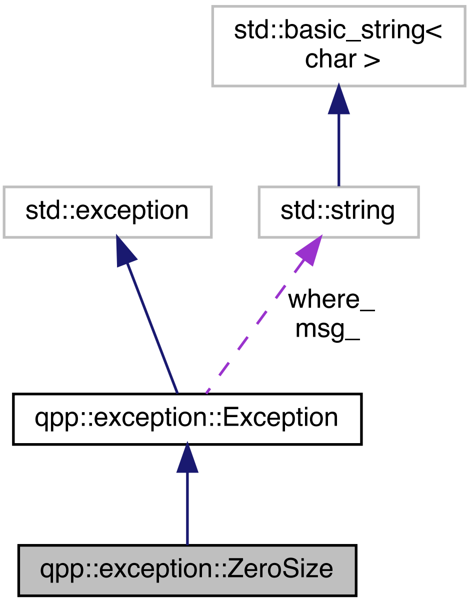
Object has zero size exception.

`#include <classes/exception.h>`

Inheritance diagram for qpp::exception::ZeroSize:



Collaboration diagram for qpp::exception::ZeroSize:



Public Member Functions

- std::string description () const override
  Exception description.
- Exception (const std::string &where)
  Constructs an exception.

7.77.1 Detailed Description

Object has zero size exception.

Zero sized object, e.g. empty Eigen::Matrix or std::vector with no elements

7.77.2 Member Function Documentation

7.77.2.1 description()

```
std::string qpp::exception::ZeroSize::description ( ) const  [inline], [override], [virtual]
```

Exception description.

Returns

Exception description

Implements qpp::exception::Exception.

7.77.2.2 Exception()

```
qpp::exception::Exception::Exception  [inline], [explicit]
```

Constructs an exception.

Parameters

where	Text representing where the exception occurred

The documentation for this class was generated from the following file:

- classes/exception.h

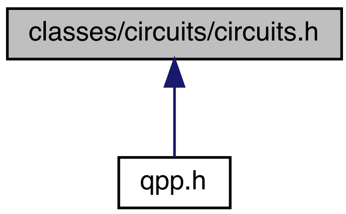
Chapter 8

File Documentation

8.1 classes/circuits/circuits.h File Reference

Qudit quantum circuits.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::QCircuit

    Quantum circuit class.
- struct qpp::QCircuit::GateStep

    One step consisting only of gates/operators in the circuit.
- struct qpp::QCircuit::MeasureStep

    One step consisting only of measurements in the circuit.
- class qpp::QCircuit::iterator

    Quantum circuit bound-checking (safe) iterator.
- class qpp::QCircuit::iterator::value_type_

    Value type class for qpp::QCircuit::iterator.

Namespaces

- qpp

  Quantum++ main namespace.

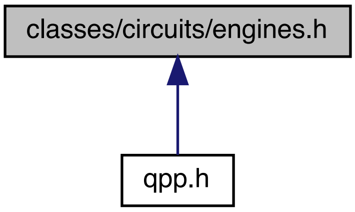
8.1.1 Detailed Description

Qudit quantum circuits.

8.2 classes/circuits/engines.h File Reference

Qudit quantum engines.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::QEngine

  Quantum circuit engine, executes qpp::QCircuit.
- class qpp::QNoisyEngine< NoiseModel >

  Noisy quantum circuit engine, executes qpp::QCircuit.

Namespaces

- qpp

  Quantum++ main namespace.

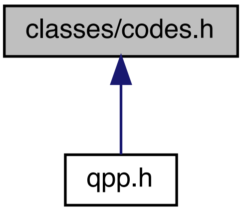
8.2.1 Detailed Description

Qudit quantum engines.

8.3 classes/codes.h File Reference

Quantum error correcting codes.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::Codes

  const Singleton class that defines quantum error correcting codes

Namespaces

- qpp

  Quantum++ main namespace.

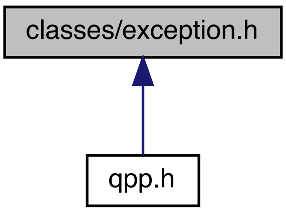
8.3.1 Detailed Description

Quantum error correcting codes.

8.4 classes/exception.h File Reference

Exceptions.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::exception::Exception

  Base class for generating Quantum++ custom exceptions.
- class qpp::exception::Unknown

  Unknown exception.
- class qpp::exception::ZeroSize

  Object has zero size exception.
- class qpp::exception::MatrixNotSquare

  Matrix is not square exception.
- class qpp::exception::MatrixNotCvector

  Matrix is not a column vector exception.
- class qpp::exception::MatrixNotRvector

  Matrix is not a row vector exception.
- class qpp::exception::MatrixNotVector

  Matrix is not a vector exception.
- class qpp::exception::MatrixNotSquareNorCvector

  Matrix is not square nor column vector exception.
- class qpp::exception::MatrixNotSquareNorRvector

  Matrix is not square nor row vector exception.
- class qpp::exception::MatrixNotSquareNorVector

  Matrix is not square nor vector exception.
- class qpp::exception::MatrixMismatchSubsys

  Matrix mismatch subsystems exception.
- class qpp::exception::DimsInvalid

  Invalid dimension(s) exception.
- class qpp::exception::DimsNotEqual

  Dimensions not equal exception.
- class qpp::exception::DimsMismatchMatrix

  Dimension(s) mismatch matrix size exception.
- class qpp::exception::DimsMismatchCvector

  Dimension(s) mismatch column vector size exception.
- class qpp::exception::DimsMismatchRvector

  Dimension(s) mismatch row vector size exception.
- class qpp::exception::DimsMismatchVector

  Dimension(s) mismatch vector size exception.
- class qpp::exception::SubsysMismatchDims

  Subsystems mismatch dimensions exception.
- class qpp::exception::PermInvalid

  Invalid permutation exception.
- class qpp::exception::PermMismatchDims

  Permutation mismatch dimensions exception.
- class qpp::exception::NotQubitMatrix

  Matrix is not 2 x 2 exception.
- class qpp::exception::NotQubitCvector

  Column vector is not 2 x 1 exception.
- class qpp::exception::NotQubitRvector

  Row vector is not 1 x 2 exception.
- class qpp::exception::NotQubitVector

  Vector is not 2 x 1 nor 1 x 2 exception.
- class qpp::exception::NotQubitSubsys

Subsystems are not qubits exception.
- class qpp::exception::NotBipartite

  Not bi-partite exception.
- class qpp::exception::NoCodeword

  Codeword does not exist exception.
- class qpp::exception::OutOfRange

  Argument out of range exception.
- class qpp::exception::TypeMismatch

  Type mismatch exception.
- class qpp::exception::SizeMismatch

  Size mismatch exception.
- class qpp::exception::UndefinedType

  Not defined for this type exception.
- class qpp::exception::QuditAlreadyMeasured

  Qudit was already measured exception.
- class qpp::exception::Duplicates

  System (e.g. std::vector) has duplicates exception.
- class qpp::exception::CustomException

  Custom exception.
- class qpp::exception::NotImplemented

  Code not yet implemented.
- class qpp::exception::InvalidIterator

  Invalid iterator.

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::exception

  Quantum++ exception hierarchy namespace.

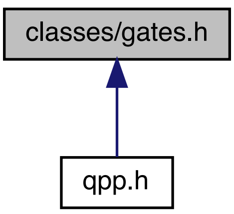
8.4.1 Detailed Description

Exceptions.

8.5 classes/gates.h File Reference

Quantum gates.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::Gates

  const Singleton class that implements most commonly used gates

Namespaces

- qpp

  Quantum++ main namespace.

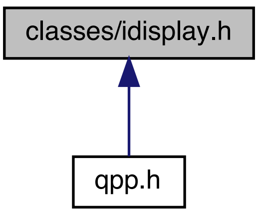
8.5.1 Detailed Description

Quantum gates.

8.6 classes/idisplay.h File Reference

Display interface via the non-virtual interface (NVI) and very basic JSON serialization support interface.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::IDisplay

  Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.
- class qpp::IJSON

  Abstract class (interface) that mandates the definition of very basic JSON serialization support.

Namespaces

- qpp

  Quantum++ main namespace.

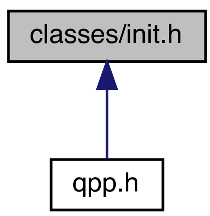
8.6.1 Detailed Description

Display interface via the non-virtual interface (NVI) and very basic JSON serialization support interface.

8.7 classes/init.h File Reference

Initialization.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::Init

  const Singleton class that performs additional initializations/cleanups

Namespaces

- qpp

  Quantum++ main namespace.

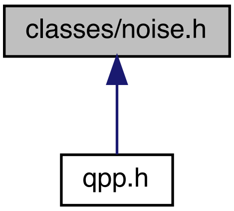
8.7.1 Detailed Description

Initialization.

8.8 classes/noise.h File Reference

Noise models.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::NoiseType

    Contains template tags used to specify the noise type.
- class qpp::NoiseBase$< T >$

    Base class for all noise models, derive your particular noise model.
- class qpp::QubitDepolarizingNoise

    Qubit depolarizing noise.
- class qpp::QubitPhaseFlipNoise

    Qubit phase flip (dephasing) noise.
- class qpp::QubitBitFlipNoise

    Qubit bit flip noise.
- class qpp::QubitBitPhaseFlipNoise

    Qubit bit-phase flip (dephasing) noise.
- class qpp::QubitAmplitudeDampingNoise

    Qubit amplitude damping noise, as described in Nielsen and Chuang.
- class qpp::QubitPhaseDampingNoise

    Qubit phase damping noise, as described in Nielsen and Chuang.
- class qpp::QuditDepolarizingNoise

    Qudit depolarizing noise.

Namespaces

- qpp

    Quantum++ main namespace.

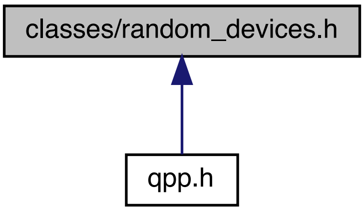
8.8.1 Detailed Description

Noise models.

8.9 classes/random_devices.h File Reference

Random devices.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::RandomDevices

    Singleton class that manages the source of randomness in the library.

Namespaces

- qpp

    Quantum++ main namespace.

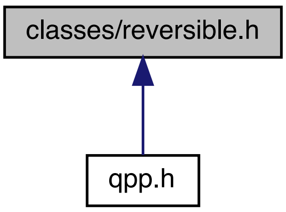
8.9.1 Detailed Description

Random devices.

8.10 classes/reversible.h File Reference

Support for classical reversible circuits.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::Dynamic_bitset

  Dynamic bitset class, allows the specification of the number of bits at runtime.
- class qpp::Bit_circuit

  Classical reversible circuit simulator.

Namespaces

- qpp

  Quantum++ main namespace.

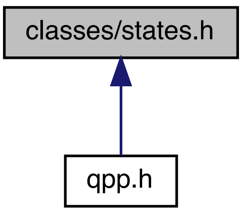
8.10.1 Detailed Description

Support for classical reversible circuits.

8.11 classes/states.h File Reference

Quantum states.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::States

  const Singleton class that implements most commonly used states

Namespaces

- qpp

  Quantum++ main namespace.

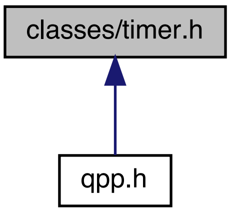
8.11.1 Detailed Description

Quantum states.

8.12 classes/timer.h File Reference

Timing.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::Timer< T, CLOCK_T >

  Chronometer.

Namespaces

- qpp

  Quantum++ main namespace.

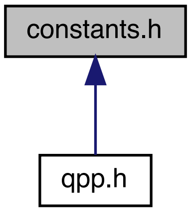
8.12.1 Detailed Description

Timing.

8.13 constants.h File Reference

Constants.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.
- qpp::literals

Functions

- constexpr cplx qpp::literals::operator"" _i (unsigned long long int x) noexcept

  User-defined literal for complex $i = \sqrt{-1}$ *(integer overload)*
- constexpr cplx qpp::operator"" _i (long double x) noexcept

  User-defined literal for complex $i = \sqrt{-1}$ *(real overload)*
- cplx qpp::omega (idx D)

  D-th root of unity.

Variables

- constexpr double qpp::chop = 1e-10

  Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.
- constexpr idx qpp::maxn = 64

  Maximum number of allowed qubits/qudits (subsystems)
- constexpr double qpp::pi = 3.141592653589793238462643383279502884

  π
- constexpr double qpp::ee = 2.718281828459045235360287471352662497

  Base of natural logarithm, e.
- constexpr double qpp::infty = std::numeric_limits<double>::max()

  Used to denote infinity in double precision.

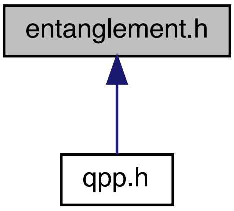
8.13.1 Detailed Description

Constants.

8.14 entanglement.h File Reference

Entanglement functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

    Quantum++ main namespace.

Functions

- template< typename Derived >
  dyn_col_vect< double > qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

    Schmidt coefficients of the bi-partite pure state A.
- template< typename Derived >
  dyn_col_vect< double > qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, idx d=2)

    Schmidt coefficients of the bi-partite pure state A.
- template< typename Derived >
  cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

    Schmidt basis on Alice side.
- template< typename Derived >
  cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > &A, idx d=2)

    Schmidt basis on Alice side.
- template< typename Derived >
  cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

    Schmidt basis on Bob side.
- template< typename Derived >
  cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > &A, idx d=2)

Schmidt basis on Bob side.

- template< typename Derived >
  std::vector< double > qpp::schmidtprobs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Schmidt probabilities of the bi-partite pure state A.
- template< typename Derived >
  std::vector< double > qpp::schmidtprobs (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Schmidt probabilities of the bi-partite pure state A.
- template< typename Derived >
  double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Entanglement of the bi-partite pure state A.
- template< typename Derived >
  double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Entanglement of the bi-partite pure state A.
- template< typename Derived >
  double qpp::gconcurrence (const Eigen::MatrixBase< Derived > &A)

  G-concurrence of the bi-partite pure state A.
- template< typename Derived >
  double qpp::negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Negativity of the bi-partite mixed state A.
- template< typename Derived >
  double qpp::negativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Negativity of the bi-partite mixed state A.
- template< typename Derived >
  double qpp::lognegativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

  Logarithmic negativity of the bi-partite mixed state A.
- template< typename Derived >
  double qpp::lognegativity (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Logarithmic negativity of the bi-partite mixed state A.
- template< typename Derived >
  double qpp::concurrence (const Eigen::MatrixBase< Derived > &A)

  Wootters concurrence of the bi-partite qubit mixed state A.

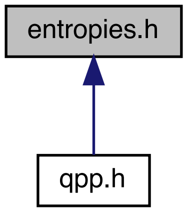
8.14.1 Detailed Description

Entanglement functions.

8.15 entropies.h File Reference

Entropy functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template< typename Derived >
  double qpp::entropy (const Eigen::MatrixBase< Derived > &A)

  von-Neumann entropy of the density matrix A
- double qpp::entropy (const std::vector< double > &prob)

  Shannon entropy of the probability distribution prob.
- template< typename Derived >
  double qpp::renyi (const Eigen::MatrixBase< Derived > &A, double alpha)

  Renyi- α entropy of the density matrix A, for $\alpha \geq 0.$
- double qpp::renyi (const std::vector< double > &prob, double alpha)

  Renyi- α entropy of the probability distribution prob, for $\alpha \geq 0.$
- template< typename Derived >
  double qpp::tsallis (const Eigen::MatrixBase< Derived > &A, double q)

  Tsallis- q entropy of the density matrix A, for $q \geq 0.$
- double qpp::tsallis (const std::vector< double > &prob, double q)

  Tsallis- q entropy of the probability distribution prob, for $q \geq 0.$
- template< typename Derived >
  double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, const std::vector< idx > &dims)

  Quantum mutual information between 2 subsystems of a composite system.
- template< typename Derived >
  double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, idx d=2)

  Quantum mutual information between 2 subsystems of a composite system.

8.15.1 Detailed Description

Entropy functions.

8.16 experimental/experimental.h File Reference

Experimental/test functions/classes.

Namespaces

- qpp
    Quantum++ main namespace.
- qpp::experimental
    Experimental/test functions/classes, do not use or modify.

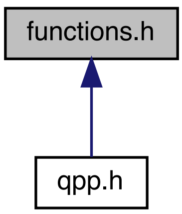
8.16.1 Detailed Description

Experimental/test functions/classes.

8.17 functions.h File Reference

Generic quantum computing functions.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::internal::HashEigen
    Functor for hashing Eigen expressions.
- class qpp::internal::EqualEigen
    Functor for comparing Eigen expressions for equality.

Namespaces

- qpp
    Quantum++ main namespace.
- qpp::literals
- qpp::internal
    Internal utility functions, do not use them directly or modify them.

Functions

- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::transpose (const Eigen::MatrixBase< Derived > &A)

  Transpose.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::conjugate (const Eigen::MatrixBase< Derived > &A)

  Complex conjugate.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::adjoint (const Eigen::MatrixBase< Derived > &A)

  Adjoint.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::inverse (const Eigen::MatrixBase< Derived > &A)

  Inverse.
- template< typename Derived >
  Derived::Scalar qpp::trace (const Eigen::MatrixBase< Derived > &A)

  Trace.
- template< typename Derived >
  Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > &A)

  Determinant.
- template< typename Derived >
  Derived::Scalar qpp::logdet (const Eigen::MatrixBase< Derived > &A)

  Logarithm of the determinant.
- template< typename Derived >
  Derived::Scalar qpp::sum (const Eigen::MatrixBase< Derived > &A)

  Element-wise sum of A.
- template< typename Derived >
  Derived::Scalar qpp::prod (const Eigen::MatrixBase< Derived > &A)

  Element-wise product of A.
- template< typename Derived >
  double qpp::norm (const Eigen::MatrixBase< Derived > &A)

  Frobenius norm.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::normalize (const Eigen::MatrixBase< Derived > &A)

  Normalizes state vector (column or row vector) or density matrix.
- template< typename Derived >
  std::pair< dyn_col_vect< cplx >, cmat > qpp::eig (const Eigen::MatrixBase< Derived > &A)

  Full eigen decomposition.
- template< typename Derived >
  dyn_col_vect< cplx > qpp::evals (const Eigen::MatrixBase< Derived > &A)

  Eigenvalues.
- template< typename Derived >
  cmat qpp::evects (const Eigen::MatrixBase< Derived > &A)

  Eigenvectors.
- template< typename Derived >
  std::pair< dyn_col_vect< double >, cmat > qpp::heig (const Eigen::MatrixBase< Derived > &A)

  Full eigen decomposition of Hermitian expression.
- template< typename Derived >
  dyn_col_vect< double > qpp::hevals (const Eigen::MatrixBase< Derived > &A)

  Hermitian eigenvalues.
- template< typename Derived >
  cmat qpp::hevects (const Eigen::MatrixBase< Derived > &A)

  Eigenvectors of Hermitian matrix.

- template< typename Derived >
  std::tuple< cmat, dyn_col_vect< double >, cmat > qpp::svd (const Eigen::MatrixBase< Derived > &A)

  Full singular value decomposition.
- template< typename Derived >
  dyn_col_vect< double > qpp::svals (const Eigen::MatrixBase< Derived > &A)

  Singular values.
- template< typename Derived >
  cmat qpp::svdU (const Eigen::MatrixBase< Derived > &A)

  Left singular vectors.
- template< typename Derived >
  cmat qpp::svdV (const Eigen::MatrixBase< Derived > &A)

  Right singular vectors.
- template< typename Derived >
  cmat qpp::funm (const Eigen::MatrixBase< Derived > &A, cplx(*f)(const cplx &))

  Functional calculus f(A)
- template< typename Derived >
  cmat qpp::sqrtm (const Eigen::MatrixBase< Derived > &A)

  Matrix square root.
- template< typename Derived >
  cmat qpp::absm (const Eigen::MatrixBase< Derived > &A)

  Matrix absolute value.
- template< typename Derived >
  cmat qpp::expm (const Eigen::MatrixBase< Derived > &A)

  Matrix exponential.
- template< typename Derived >
  cmat qpp::logm (const Eigen::MatrixBase< Derived > &A)

  Matrix logarithm.
- template< typename Derived >
  cmat qpp::sinm (const Eigen::MatrixBase< Derived > &A)

  Matrix sin.
- template< typename Derived >
  cmat qpp::cosm (const Eigen::MatrixBase< Derived > &A)

  Matrix cos.
- template< typename Derived >
  cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived > &A, const cplx z)

  Matrix power.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::powm (const Eigen::MatrixBase< Derived > &A, idx n)

  Fast matrix power based on the SQUARE-AND-MULTIPLY algorithm.
- template< typename Derived >
  double qpp::schatten (const Eigen::MatrixBase< Derived > &A, double p)

  Schatten matrix norm.
- template< typename OutputScalar , typename Derived >
  dyn_mat< OutputScalar > qpp::cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const typename Derived::Scalar &))

  Functor.
- template< typename T >
  dyn_mat< typename T::Scalar > qpp::kron (const T &head)

  Kronecker product.
- template< typename T , typename... Args>
  dyn_mat< typename T::Scalar > qpp::kron (const T &head, const Args &... tail)

  Kronecker product.

- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::kron (const std::vector< Derived > &As)

  Kronecker product.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::kron (const std::initializer_list< Derived > &As)

  Kronecker product.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::kronpow (const Eigen::MatrixBase< Derived > &A, idx n)

  Kronecker power.
- template< typename T >
  dyn_mat< typename T::Scalar > qpp::dirsum (const T &head)

  Direct sum.
- template< typename T , typename... Args>
  dyn_mat< typename T::Scalar > qpp::dirsum (const T &head, const Args &... tail)

  Direct sum.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::dirsum (const std::vector< Derived > &As)

  Direct sum.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::dirsum (const std::initializer_list< Derived > &As)

  Direct sum.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::dirsumpow (const Eigen::MatrixBase< Derived > &A, idx n)

  Direct sum power.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::reshape (const Eigen::MatrixBase< Derived > &A, idx rows, idx cols)

  Reshape.
- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)

  Commutator.
- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)

  Anti-commutator.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::prj (const Eigen::MatrixBase< Derived > &A)

  Projector.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::grams (const std::vector< Derived > &As)

  Gram-Schmidt orthogonalization.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::grams (const std::initializer_list< Derived > &As)

  Gram-Schmidt orthogonalization.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::grams (const Eigen::MatrixBase< Derived > &A)

  Gram-Schmidt orthogonalization.
- std::vector< idx > qpp::n2multiidx (idx n, const std::vector< idx > &dims)

  Non-negative integer index to multi-index.
- idx qpp::multiidx2n (const std::vector< idx > &midx, const std::vector< idx > &dims)

  Multi-index to non-negative integer index.
- ket qpp::mket (const std::vector< idx > &mask, const std::vector< idx > &dims)

Multi-partite qudit ket.
- ket qpp::mket (const std::vector< idx > &mask, idx d=2)

  Multi-partite qudit ket.
- cmat qpp::mprj (const std::vector< idx > &mask, const std::vector< idx > &dims)

  Projector onto multi-partite qudit ket.
- cmat qpp::mprj (const std::vector< idx > &mask, idx d=2)

  Projector onto multi-partite qudit ket.
- template< typename InputIterator >
  std::vector< double > qpp::abssq (InputIterator first, InputIterator last)

  Computes the absolute values squared of an STL-like range of complex numbers.
- template< typename Container >
  std::vector< double > qpp::abssq (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)

  Computes the absolute values squared of an STL-like container.
- template< typename Derived >
  std::vector< double > qpp::abssq (const Eigen::MatrixBase< Derived > &A)

  Computes the absolute values squared of an Eigen expression.
- template< typename InputIterator >
  std::iterator_traits< InputIterator >::value_type qpp::sum (InputIterator first, InputIterator last)

  Element-wise sum of an STL-like range.
- template< typename Container >
  Container::value_type qpp::sum (const Container &c, typename std::enable_if< is_iterable< Container >↩ ::value >::type *=nullptr)

  Element-wise sum of the elements of an STL-like container.
- template< typename InputIterator >
  std::iterator_traits< InputIterator >::value_type qpp::prod (InputIterator first, InputIterator last)

  Element-wise product of an STL-like range.
- template< typename Container >
  Container::value_type qpp::prod (const Container &c, typename std::enable_if< is_iterable< Container >↩ ::value >::type *=nullptr)

  Element-wise product of the elements of an STL-like container.
- template< typename Derived >
  dyn_col_vect< typename Derived::Scalar > qpp::rho2pure (const Eigen::MatrixBase< Derived > &A)

  Finds the pure state representation of a matrix proportional to a projector onto a pure state.
- std::vector< idx > qpp::complement (std::vector< idx > subsys, idx n)

  Constructs the complement of a subsystem vector.
- template< typename Derived >
  std::vector< double > qpp::rho2bloch (const Eigen::MatrixBase< Derived > &A)

  Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix A.
- cmat qpp::bloch2rho (const std::vector< double > &r)

  Computes the density matrix corresponding to the 3-dimensional real Bloch vector r.
- template<char... Bits>
  ket qpp::literals::operator"" _ket ()

  Multi-partite qubit ket user-defined literal.
- template<char... Bits>
  bra qpp::literals::operator"" _bra ()

  Multi-partite qubit bra user-defined literal.
- template<char... Bits>
  cmat qpp::literals::operator"" _prj ()

  Multi-partite qubit projector user-defined literal.
- template< class T >
  void qpp::internal::hash_combine (std::size_t &seed, const T &v)
- template< typename Derived >
  std::size_t qpp::hash_eigen (const Eigen::MatrixBase< Derived > &A, std::size_t seed=0)

  Computes the hash of en Eigen matrix/vector/expression.

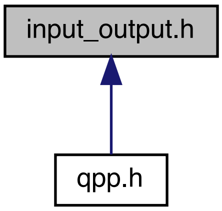
8.17.1 Detailed Description

Generic quantum computing functions.

8.18 input_output.h File Reference

Input/output functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp
  Quantum++ main namespace.

Functions

- template< typename Derived >
  internal::IOManipEigen qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)
  Eigen expression ostream manipulator.
- internal::IOManipEigen qpp::disp (cplx z, double chop=qpp::chop)
  Complex number ostream manipulator.
- template< typename InputIterator >
  internal::IOManipRange< InputIterator > qpp::disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")
  Range ostream manipulator.
- template< typename Container >
  internal::IOManipRange< typename Container::const_iterator > qpp::disp (const Container &c, const std::string &separator, const std::string &start="[", const std::string &end="]", typename std::enable_if< is_iterable< Container >::value >::type *=nullptr)
  Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.
- template< typename PointerType >
  internal::IOManipPointer< PointerType > qpp::disp (const PointerType *p, idx N, const std::string &separator, const std::string &start="[", const std::string &end="]")
  C-style pointer ostream manipulator.
- template< typename Derived >
  void qpp::save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)
  Saves Eigen expression to a binary file (internal format) in double precision.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::load (const std::string &fname)
  Loads Eigen matrix from a binary file (internal format) in double precision.

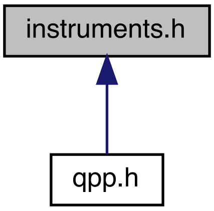
8.18.1 Detailed Description

Input/output functions.

8.19 instruments.h File Reference

Measurement functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

    Quantum++ main namespace.

Functions

- template< typename Derived >
  dyn_col_vect< typename Derived::Scalar > qpp::ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, const std::vector< idx > &dims)

    Generalized inner product.
- template< typename Derived >
  dyn_col_vect< typename Derived::Scalar > qpp::ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, idx d=2)

    Generalized inner product.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

    Measures the state vector or density operator A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)

    Measures the state vector or density matrix A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &U)

Measures the state vector or density matrix A in the orthonormal basis specified by the unitary matrix U.

- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &target, const std::vector< idx > &dims)

  Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &target, const std::vector< idx > &dims)

  Measures the part target of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &target, idx d=2)

  Measures the part target of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &target, idx d=2)

  Measures the part target of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &target, const std::vector< idx > &dims)

  Measures the part target of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 projectors specified by the columns of the matrix V.
- template< typename Derived >
  std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &target, idx d=2)

  Measures the part target of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 projectors specified by the columns of the matrix V.
- template< typename Derived >
  std::tuple< std::vector< idx >, double, cmat > qpp::measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > target, std::vector< idx > dims)

  Sequentially measures the part target of the multi-partite state vector or density matrix A in the computational basis.
- template< typename Derived >
  std::tuple< std::vector< idx >, double, cmat > qpp::measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > target, idx d=2)

  Sequentially measures the part target of the multi-partite state vector or density matrix A in the computational basis.

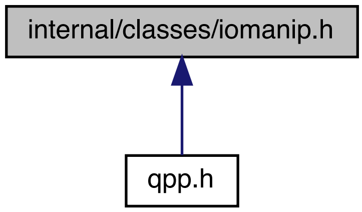
8.19.1 Detailed Description

Measurement functions.

8.20 internal/classes/iomanip.h File Reference

Input/output manipulators.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::internal::IOManipRange< InputIterator >
- class qpp::internal::IOManipPointer< PointerType >
- class qpp::internal::IOManipEigen

Namespaces

- qpp

    Quantum++ main namespace.
- qpp::internal

    Internal utility functions, do not use them directly or modify them.

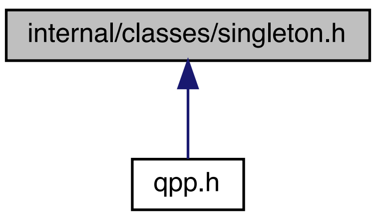
8.20.1 Detailed Description

Input/output manipulators.

8.21 internal/classes/singleton.h File Reference

Singleton pattern via CRTP.

This graph shows which files directly or indirectly include this file:



Classes

- class qpp::internal::Singleton< T >

  Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::internal

  Internal utility functions, do not use them directly or modify them.

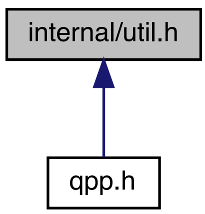
8.21.1 Detailed Description

Singleton pattern via CRTP.

8.22 internal/util.h File Reference

Internal utility functions.

This graph shows which files directly or indirectly include this file:



Classes

- struct qpp::internal::Display_Impl_

Namespaces

- qpp

  Quantum++ main namespace.
- qpp::internal

  Internal utility functions, do not use them directly or modify them.

Functions

- void qpp::internal::n2multiidx (idx n, idx numdims, const idx ∗const dims, idx ∗result) noexcept
- idx qpp::internal::multiidx2n (const idx ∗const midx, idx numdims, const idx ∗const dims) noexcept
- template<typename Derived >
  bool qpp::internal::check_square_mat (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool qpp::internal::check_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool qpp::internal::check_rvector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool qpp::internal::check_cvector (const Eigen::MatrixBase< Derived > &A)
- template<typename T >
  bool qpp::internal::check_nonzero_size (const T &x) noexcept
- template<typename T1 , typename T2 >
  bool qpp::internal::check_matching_sizes (const T1 &lhs, const T2 &rhs) noexcept
- bool qpp::internal::check_dims (const std::vector< idx > &dims)
- template<typename Derived >
  bool qpp::internal::check_dims_match_mat (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool qpp::internal::check_dims_match_cvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
  bool qpp::internal::check_dims_match_rvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- bool qpp::internal::check_eq_dims (const std::vector< idx > &dims, idx dim) noexcept
- bool qpp::internal::check_no_duplicates (std::vector< idx > v)
- bool qpp::internal::check_subsys_match_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)
- template<typename Derived >
  bool qpp::internal::check_qubit_matrix (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool qpp::internal::check_qubit_cvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool qpp::internal::check_qubit_rvector (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
  bool qpp::internal::check_qubit_vector (const Eigen::MatrixBase< Derived > &A) noexcept
- bool qpp::internal::check_perm (const std::vector< idx > &perm)
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::internal::kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::internal::dirsum2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename T >
  void qpp::internal::variadic_vector_emplace (std::vector< T > &)
- template<typename T , typename First , typename... Args>
  void qpp::internal::variadic_vector_emplace (std::vector< T > &v, First &&first, Args &&... args)
- idx qpp::internal::get_num_subsys (idx D, idx d)
- idx qpp::internal::get_dim_subsys (idx sz, idx N)

8.22.1 Detailed Description

Internal utility functions.

8.23 MATLAB/matlab.h File Reference

Input/output interfacing with MATLAB.

```
#include "mat.h"
#include "mex.h"
```

Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template<typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< cplx > >::type qpp::loadMATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a complex Eigen dynamic matrix from a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if<!std::is_same< typename Derived::Scalar, cplx >::value, dyn_mat< typename Derived::↩ Scalar > >::type qpp::loadMATLAB (const std::string &mat_file, const std::string &var_name)

  Loads a non-complex Eigen dynamic matrix from a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if< std::is_same< typename Derived::Scalar, cplx >::value >::type qpp::saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)

  Saves a complex Eigen dynamic matrix to a MATLAB .mat file,.
- template<typename Derived >
  std::enable_if< !std::is_same< typename Derived::Scalar, cplx >::value >::type qpp::saveMATLAB (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)

  Saves a non-complex Eigen dynamic matrix to a MATLAB .mat file,.

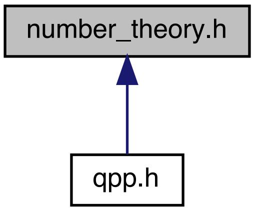
8.23.1 Detailed Description

Input/output interfacing with MATLAB.

8.24 number_theory.h File Reference

Number theory functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

    Quantum++ main namespace.

Functions

- std::vector< int > qpp::x2contfrac (double x, idx N, idx cut=1e5)

    Simple continued fraction expansion.
- double qpp::contfrac2x (const std::vector< int > &cf, idx N=idx(-1))

    Real representation of a simple continued fraction.
- bigint qpp::gcd (bigint a, bigint b)

    Greatest common divisor of two integers.
- bigint qpp::gcd (const std::vector< bigint > &as)

    Greatest common divisor of a list of integers.
- bigint qpp::lcm (bigint a, bigint b)

    Least common multiple of two integers.
- bigint qpp::lcm (const std::vector< bigint > &as)

    Least common multiple of a list of integers.
- std::vector< idx > qpp::invperm (const std::vector< idx > &perm)

    Inverse permutation.
- std::vector< idx > qpp::compperm (const std::vector< idx > &perm, const std::vector< idx > &sigma)

    Compose permutations.
- std::vector< bigint > qpp::factors (bigint a)

    Prime factor decomposition.
- bigint qpp::modmul (bigint a, bigint b, bigint p)

    Modular multiplication without overflow.
- bigint qpp::modpow (bigint a, bigint n, bigint p)

    Fast integer power modulo p based on the SQUARE-AND-MULTIPLY algorithm.
- std::tuple< bigint, bigint, bigint > qpp::egcd (bigint a, bigint b)

    Extended greatest common divisor of two integers.
- bigint qpp::modinv (bigint a, bigint p)

    Modular inverse of a mod p.
- bool qpp::isprime (bigint p, idx k=80)

Primality test based on the Miller-Rabin's algorithm.

- bigint qpp::randprime (bigint a, bigint b, idx N=1000)

  Generates a random big prime uniformly distributed in the interval [a, b].
- std::vector< std::pair< int, int > > qpp::convergents (const std::vector< int > &cf)

  Convergents.
- std::vector< std::pair< int, int > > qpp::convergents (double x, idx N)

  Convergents.

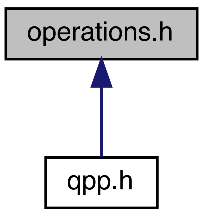
8.24.1 Detailed Description

Number theory functions.

8.25 operations.h File Reference

Quantum operation functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &target, const std::vector< idx > &dims)

  Applies the controlled-gate A to the part target of the multi-partite state vector or density matrix state.
- template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &target, idx d=2)

Applies the controlled-gate A to the part target of the multi-partite state vector or density matrix state.

- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &target, const std::vector< idx > &dims)

  Applies the gate A to the part target of the multi-partite state vector or density matrix state.
- template< typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &target, idx d=2)

  Applies the gate A to the part target of the multi-partite state vector or density matrix state.
- template< typename Derived >
  cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)

  Applies the channel specified by the set of Kraus operators Ks to the density matrix A.
- template< typename Derived >
  cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std↩ ::vector< idx > &target, const std::vector< idx > &dims)

  Applies the channel specified by the set of Kraus operators Ks to the part target of the multi-partite density matrix A.
- template< typename Derived >
  cmat qpp::apply (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std↩ ::vector< idx > &target, idx d=2)

  Applies the channel specified by the set of Kraus operators Ks to the part target of the multi-partite density matrix A.
- cmat qpp::kraus2super (const std::vector< cmat > &Ks)

  Superoperator matrix.
- cmat qpp::kraus2choi (const std::vector< cmat > &Ks)

  Choi matrix.
- std::vector< cmat > qpp::choi2kraus (const cmat &A)

  Orthogonal Kraus operators from Choi matrix.
- cmat qpp::choi2super (const cmat &A)

  Converts Choi matrix to superoperator matrix.
- cmat qpp::super2choi (const cmat &A)

  Converts superoperator matrix to Choi matrix.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &dims)

  Partial trace.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Partial trace.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &dims)

  Partial trace.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, idx d=2)

  Partial trace.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &target, const std::vector< idx > &dims)

  Partial trace.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std↩ ::vector< idx > &target, idx d=2)

  Partial trace.

- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &target, const std::vector< idx > &dims)

  Partial transpose.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &target, idx d=2)

  Partial transpose.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, const std::vector< idx > &dims)

  Subsystem permutation.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, idx d=2)

  Subsystem permutation.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::applyQFT (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &target, idx d=2, bool swap=true)

  Applies the qudit quantum Fourier transform to the part target of the multi-partite state vector or density matrix A.
- template< typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::applyTFQ (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &target, idx d=2, bool swap=true)

  Applies the inverse (adjoint) qudit quantum Fourier transform to the part target of the multi-partite state vector or density matrix A.
- template< typename Derived >
  dyn_col_vect< typename Derived::Scalar > qpp::TFQ (const Eigen::MatrixBase< Derived > &A, idx d=2, bool swap=true)

  Inverse (adjoint) qudit quantum Fourier transform.
- template< typename Derived >
  dyn_col_vect< typename Derived::Scalar > qpp::QFT (const Eigen::MatrixBase< Derived > &A, idx d=2, bool swap=true)

  Qudit quantum Fourier transform.

8.25.1 Detailed Description

Quantum operation functions.

8.26 qpp.h File Reference

Quantum++ main header file, includes all other necessary headers.

```
#include <algorithm>
#include <cassert>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <exception>
#include <fstream>
```

```
#include <functional>
#include <initializer_list>
#include <iomanip>
#include <iterator>
#include <limits>
#include <memory>
#include <numeric>
#include <ostream>
#include <random>
#include <sstream>
#include <stdexcept>
#include <string>
#include <tuple>
#include <type_traits>
#include <unordered_map>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "types.h"
#include "classes/exception.h"
#include "constants.h"
#include "traits.h"
#include "classes/idisplay.h"
#include "internal/util.h"
#include "internal/classes/iomanip.h"
#include "input_output.h"
#include "internal/classes/singleton.h"
#include "classes/random_devices.h"
#include "random.h"
#include "number_theory.h"
#include "functions.h"
#include "classes/init.h"
#include "classes/codes.h"
#include "classes/gates.h"
#include "classes/states.h"
#include "statistics.h"
#include "operations.h"
#include "entropies.h"
#include "entanglement.h"
#include "classes/timer.h"
#include "instruments.h"
#include "classes/reversible.h"
#include "classes/noise.h"
#include "classes/circuits/circuits.h"
#include "classes/circuits/engines.h"
```

Namespaces

- qpp

    Quantum++ main namespace.

Macros

- #define QPP_UNUSED_

8.26.1 Detailed Description

Quantum++ main header file, includes all other necessary headers.

8.26.2 Macro Definition Documentation

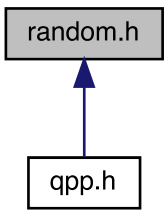
8.26.2.1 QPP_UNUSED_

```
#define QPP_UNUSED_
```

8.27 random.h File Reference

Randomness-related functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- double qpp::rand (double a, double b)

    Generates a random real number uniformly distributed in the interval [a, b)
- bigint qpp::rand (bigint a, bigint b)

    Generates a random big integer uniformly distributed in the interval [a, b].
- idx qpp::randidx (idx a=std::numeric_limits< idx >::min(), idx b=std::numeric_limits< idx >::max())

    Generates a random index (idx) uniformly distributed in the interval [a, b].
- template< typename Derived >
  Derived qpp::rand (idx rows QPP_UNUSED_, idx cols QPP_UNUSED_, double a QPP_UNUSED_=0, double b QPP_UNUSED_=1)

    Generates a random matrix with entries uniformly distributed in the interval [a, b)
- template<>
  dmat qpp::rand (idx rows, idx cols, double a, double b)

    Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)
- template<>
  cmat qpp::rand (idx rows, idx cols, double a, double b)

    Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)
- template< typename Derived >
  Derived qpp::randn (idx rows QPP_UNUSED_, idx cols QPP_UNUSED_, double mean QPP_UNUSED_=0, double sigma QPP_UNUSED_=1)

    Generates a random matrix with entries normally distributed in N(mean, sigma)
- template<>
  dmat qpp::randn (idx rows, idx cols, double mean, double sigma)

    Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)
- template<>
  cmat qpp::randn (idx rows, idx cols, double mean, double sigma)

    Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)
- double qpp::randn (double mean=0, double sigma=1)

    Generates a random real number (double) normally distributed in N(mean, sigma)
- cmat qpp::randU (idx D=2)

    Generates a random unitary matrix.
- cmat qpp::randV (idx Din, idx Dout)

    Generates a random isometry matrix.
- std::vector< cmat > qpp::randkraus (idx N, idx D=2)

    Generates a set of random Kraus operators.
- cmat qpp::randH (idx D=2)

    Generates a random Hermitian matrix.
- ket qpp::randket (idx D=2)

    Generates a random normalized ket (pure state vector)
- cmat qpp::randrho (idx D=2)

    Generates a random density matrix.
- std::vector< idx > qpp::randperm (idx N)

    Generates a random uniformly distributed permutation.
- std::vector< double > qpp::randprob (idx N)

    Generates a random probability vector uniformly distributed over the probability simplex.

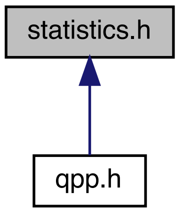
8.27.1 Detailed Description

Randomness-related functions.

8.28 statistics.h File Reference

Statistics functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Functions

- std::vector< double > qpp::uniform (idx N)

  Uniform probability distribution vector.
- std::vector< double > qpp::marginalX (const dmat &probXY)

  Marginal distribution.
- std::vector< double > qpp::marginalY (const dmat &probXY)

  Marginal distribution.
- template<typename Container >
  double qpp::avg (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↩
  iterable< Container >::value >::type ∗=nullptr)

  Average.
- template<typename Container >
  double qpp::cov (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if<
  is_iterable< Container >::value >::type ∗=nullptr)

  Covariance.
- template<typename Container >
  double qpp::var (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↩
  iterable< Container >::value >::type ∗=nullptr)

  Variance.

- template<typename Container >
  double qpp::sigma (const std::vector< double > &prob, const Container &X, typename std::enable_if< is_↩ iterable< Container >::value >::type ∗=nullptr)

  Standard deviation.
- template<typename Container >
  double qpp::cor (const dmat &probXY, const Container &X, const Container &Y, typename std::enable_if< is_iterable< Container >::value >::type ∗=nullptr)

  Correlation.

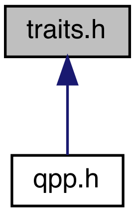
8.28.1 Detailed Description

Statistics functions.

8.29 traits.h File Reference

Type traits.

This graph shows which files directly or indirectly include this file:



Classes

- struct qpp::make_void< Ts >

  Helper for qpp::to_void<> alias template.
- struct qpp::is_iterable< T, typename >

  Checks whether T is compatible with an STL-like iterable container.
- struct qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), decltype(∗(std::

  Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.
- struct qpp::is_matrix_expression< Derived >

  Checks whether the type is an Eigen matrix expression.
- struct qpp::is_complex< T >

  Checks whether the type is a complex type.
- struct qpp::is_complex< std::complex< T > >

  Checks whether the type is a complex number type, specialization for complex types.

Namespaces

- qpp

  Quantum++ main namespace.

Typedefs

- template<typename... Ts>
  using qpp::to_void = typename make_void< Ts... >::type

  Alias template that implements the proposal for void_t.

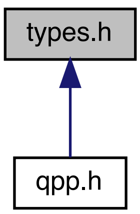
8.29.1 Detailed Description

Type traits.

8.30 types.h File Reference

Type aliases.

This graph shows which files directly or indirectly include this file:



Namespaces

- qpp

  Quantum++ main namespace.

Typedefs

- using qpp::idx = std::size_t

    Non-negative integer index, make sure you use an unsigned type.
- using qpp::bigint = long long int

    Big integer.
- using qpp::cplx = std::complex< double >

    Complex number in double precision.
- using qpp::ket = Eigen::VectorXcd

    Complex (double precision) dynamic Eigen column vector.
- using qpp::bra = Eigen::RowVectorXcd

    Complex (double precision) dynamic Eigen row vector.
- using qpp::cmat = Eigen::MatrixXcd

    Complex (double precision) dynamic Eigen matrix.
- using qpp::dmat = Eigen::MatrixXd

    Real (double precision) dynamic Eigen matrix.
- template<typename Scalar >
  using qpp::dyn_mat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >

    Dynamic Eigen matrix over the field specified by Scalar.
- template<typename Scalar >
  using qpp::dyn_col_vect = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >

    Dynamic Eigen column vector over the field specified by Scalar.
- template<typename Scalar >
  using qpp::dyn_row_vect = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >

    Dynamic Eigen row vector over the field specified by Scalar.

8.30.1 Detailed Description

Type aliases.

Index