

Quantum++
v0.8.3-devel

Generated by Doxygen 1.8.9.1

Tue Oct 13 2015 12:36:21

Contents

1	Quantum++	1
2	Namespace Index	5
2.1	Namespace List	5
3	Hierarchical Index	7
3.1	Class Hierarchy	7
4	Class Index	9
4.1	Class List	9
5	File Index	11
5.1	File List	11
6	Namespace Documentation	13
6.1	qpp Namespace Reference	13
6.1.1	Detailed Description	24
6.1.2	Typedef Documentation	25
6.1.2.1	bigint	25
6.1.2.2	bra	25
6.1.2.3	cmat	25
6.1.2.4	cplx	25
6.1.2.5	dmat	25
6.1.2.6	dyn_col_vect	25
6.1.2.7	dyn_mat	25
6.1.2.8	dyn_row_vect	25
6.1.2.9	idx	25
6.1.2.10	ket	26
6.1.2.11	to_void	26
6.1.2.12	ubigint	26
6.1.3	Function Documentation	26
6.1.3.1	absm	26
6.1.3.2	abssq	26

6.1.3.3	abssq	26
6.1.3.4	abssq	27
6.1.3.5	adjoint	28
6.1.3.6	anticomm	28
6.1.3.7	apply	28
6.1.3.8	apply	29
6.1.3.9	apply	29
6.1.3.10	apply	29
6.1.3.11	apply	30
6.1.3.12	applyCTRL	30
6.1.3.13	applyCTRL	31
6.1.3.14	avg	31
6.1.3.15	bloch2rho	31
6.1.3.16	choi2kraus	32
6.1.3.17	choi2super	32
6.1.3.18	comm	32
6.1.3.19	complement	32
6.1.3.20	compperm	33
6.1.3.21	concurrence	33
6.1.3.22	conjugate	33
6.1.3.23	contfrac2x	33
6.1.3.24	contfrac2x	34
6.1.3.25	cor	34
6.1.3.26	cosm	34
6.1.3.27	cov	34
6.1.3.28	cwise	35
6.1.3.29	det	35
6.1.3.30	dirsum	35
6.1.3.31	dirsum	36
6.1.3.32	dirsum	36
6.1.3.33	dirsum	36
6.1.3.34	dirsumpow	37
6.1.3.35	disp	37
6.1.3.36	disp	37
6.1.3.37	disp	37
6.1.3.38	disp	38
6.1.3.39	disp	38
6.1.3.40	eig	38
6.1.3.41	entanglement	39
6.1.3.42	entropy	39

6.1.3.43	entropy	39
6.1.3.44	evals	40
6.1.3.45	evects	40
6.1.3.46	expm	40
6.1.3.47	factors	40
6.1.3.48	funm	41
6.1.3.49	gcd	41
6.1.3.50	gcd	41
6.1.3.51	gconcurrency	42
6.1.3.52	grams	42
6.1.3.53	grams	42
6.1.3.54	grams	42
6.1.3.55	heig	43
6.1.3.56	hevals	43
6.1.3.57	hevects	43
6.1.3.58	inverse	44
6.1.3.59	invperm	44
6.1.3.60	ip	44
6.1.3.61	ip	44
6.1.3.62	isprime	45
6.1.3.63	kraus2choi	45
6.1.3.64	kraus2super	45
6.1.3.65	kron	46
6.1.3.66	kron	46
6.1.3.67	kron	46
6.1.3.68	kron	47
6.1.3.69	kronpow	47
6.1.3.70	lcm	47
6.1.3.71	lcm	48
6.1.3.72	load	48
6.1.3.73	loadMATLABmatrix	48
6.1.3.74	loadMATLABmatrix	49
6.1.3.75	loadMATLABmatrix	49
6.1.3.76	logdet	49
6.1.3.77	logm	50
6.1.3.78	lognegativity	50
6.1.3.79	marginalX	50
6.1.3.80	marginalY	50
6.1.3.81	measure	51
6.1.3.82	measure	51

6.1.3.83	measure	51
6.1.3.84	measure	52
6.1.3.85	measure	52
6.1.3.86	measure	53
6.1.3.87	measure	53
6.1.3.88	measure	54
6.1.3.89	measure	54
6.1.3.90	measure_seq	55
6.1.3.91	measure_seq	55
6.1.3.92	mket	55
6.1.3.93	mket	56
6.1.3.94	modpow	56
6.1.3.95	mprj	56
6.1.3.96	mprj	57
6.1.3.97	multiidx2n	58
6.1.3.98	n2multiidx	58
6.1.3.99	negativity	58
6.1.3.100	norm	59
6.1.3.101	omega	59
6.1.3.102	operator""_i	59
6.1.3.103	operator""_i	59
6.1.3.104	powm	59
6.1.3.105	prj	60
6.1.3.106	prod	60
6.1.3.107	prod	60
6.1.3.108	prod	60
6.1.3.109	ptrace	61
6.1.3.110	ptrace	61
6.1.3.111	ptrace1	61
6.1.3.112	ptrace2	63
6.1.3.113	ptranspose	63
6.1.3.114	ptranspose	63
6.1.3.115	qmutualinfo	64
6.1.3.116	qmutualinfo	64
6.1.3.117	rand	64
6.1.3.118	rand	65
6.1.3.119	rand	66
6.1.3.120	rand	66
6.1.3.121	rand	66
6.1.3.122	rand	67

6.1.3.123 randH	67
6.1.3.124 randidx	67
6.1.3.125 randket	67
6.1.3.126 randkraus	68
6.1.3.127 randn	68
6.1.3.128 randn	68
6.1.3.129 randn	69
6.1.3.130 randn	69
6.1.3.131 randperm	69
6.1.3.132 randrho	69
6.1.3.133 randU	70
6.1.3.134 randV	70
6.1.3.135 renyi	70
6.1.3.136 renyi	70
6.1.3.137 reshape	71
6.1.3.138 rho2bloch	71
6.1.3.139 rho2pure	71
6.1.3.140 save	72
6.1.3.141 saveMATLABmatrix	72
6.1.3.142 saveMATLABmatrix	72
6.1.3.143 saveMATLABmatrix	72
6.1.3.144 schatten	73
6.1.3.145 schmidtA	73
6.1.3.146 schmidtB	73
6.1.3.147 schmidtcoeffs	73
6.1.3.148 schmidtprobs	74
6.1.3.149 sigma	74
6.1.3.150 sinm	74
6.1.3.151 spectralpowm	75
6.1.3.152 sqrtm	75
6.1.3.153 sum	75
6.1.3.154 sum	75
6.1.3.155 sum	76
6.1.3.156 super2choi	76
6.1.3.157 svals	76
6.1.3.158 svd	76
6.1.3.159 svdU	77
6.1.3.160 svdV	77
6.1.3.161 syspermute	77
6.1.3.162 syspermute	77

6.1.3.163	trace	78
6.1.3.164	transpose	78
6.1.3.165	tsallis	78
6.1.3.166	tsallis	78
6.1.3.167	uniform	79
6.1.3.168	var	79
6.1.3.169	x2contfrac	79
6.1.4	Variable Documentation	79
6.1.4.1	chop	79
6.1.4.2	ee	80
6.1.4.3	eps	80
6.1.4.4	infty	80
6.1.4.5	maxn	80
6.1.4.6	pi	80
6.2	qpp::experimental Namespace Reference	80
6.2.1	Detailed Description	80
6.3	qpp::internal Namespace Reference	80
6.3.1	Detailed Description	81
6.3.2	Function Documentation	81
6.3.2.1	_check_cvector	81
6.3.2.2	_check_dims	81
6.3.2.3	_check_dims_match_cvect	82
6.3.2.4	_check_dims_match_mat	82
6.3.2.5	_check_dims_match_rvect	82
6.3.2.6	_check_eq_dims	82
6.3.2.7	_check_matching_sizes	82
6.3.2.8	_check_nonzero_size	82
6.3.2.9	_check_perm	82
6.3.2.10	_check_qubit_cvector	82
6.3.2.11	_check_qubit_matrix	82
6.3.2.12	_check_qubit_rvector	82
6.3.2.13	_check_qubit_vector	82
6.3.2.14	_check_rvector	82
6.3.2.15	_check_square_mat	82
6.3.2.16	_check_subsys_match_dims	82
6.3.2.17	_check_vector	82
6.3.2.18	_dirsum2	82
6.3.2.19	_kron2	82
6.3.2.20	_multiidx2n	82
6.3.2.21	_n2multiidx	82

6.3.2.22	variadic_vector_emplace	82
6.3.2.23	variadic_vector_emplace	82
7	Class Documentation	83
7.1	qpp::Codes Class Reference	83
7.1.1	Detailed Description	84
7.1.2	Member Enumeration Documentation	84
7.1.2.1	Type	84
7.1.3	Constructor & Destructor Documentation	84
7.1.3.1	Codes	84
7.1.3.2	~Codes	84
7.1.4	Member Function Documentation	85
7.1.4.1	codeword	85
7.1.5	Friends And Related Function Documentation	85
7.1.5.1	internal::Singleton< const Codes >	85
7.2	qpp::Exception Class Reference	85
7.2.1	Detailed Description	87
7.2.2	Member Enumeration Documentation	87
7.2.2.1	Type	87
7.2.3	Constructor & Destructor Documentation	88
7.2.3.1	Exception	88
7.2.3.2	Exception	88
7.2.4	Member Function Documentation	88
7.2.4.1	_construct_exception_msg	88
7.2.4.2	what	89
7.2.5	Member Data Documentation	89
7.2.5.1	_custom	89
7.2.5.2	_msg	89
7.2.5.3	_type	89
7.2.5.4	_where	89
7.3	qpp::Gates Class Reference	89
7.3.1	Detailed Description	91
7.3.2	Constructor & Destructor Documentation	91
7.3.2.1	Gates	91
7.3.2.2	~Gates	91
7.3.3	Member Function Documentation	91
7.3.3.1	CTRL	91
7.3.3.2	expandout	92
7.3.3.3	Fd	92
7.3.3.4	Id	93

7.3.3.5	Rn	93
7.3.3.6	Xd	93
7.3.3.7	Zd	93
7.3.4	Friends And Related Function Documentation	94
7.3.4.1	internal::Singleton< const Gates >	94
7.3.5	Member Data Documentation	94
7.3.5.1	CNOT	94
7.3.5.2	CNOTba	94
7.3.5.3	CZ	94
7.3.5.4	FRED	94
7.3.5.5	H	94
7.3.5.6	Id2	94
7.3.5.7	S	94
7.3.5.8	SWAP	94
7.3.5.9	T	94
7.3.5.10	TOF	95
7.3.5.11	X	95
7.3.5.12	Y	95
7.3.5.13	Z	95
7.4	qpp::IDisplay Class Reference	95
7.4.1	Detailed Description	96
7.4.2	Constructor & Destructor Documentation	96
7.4.2.1	IDisplay	96
7.4.2.2	IDisplay	96
7.4.2.3	IDisplay	96
7.4.2.4	~IDisplay	96
7.4.3	Member Function Documentation	97
7.4.3.1	display	97
7.4.3.2	operator=	97
7.4.3.3	operator=	97
7.4.4	Friends And Related Function Documentation	97
7.4.4.1	operator<<	97
7.5	qpp::Init Class Reference	97
7.5.1	Detailed Description	98
7.5.2	Constructor & Destructor Documentation	98
7.5.2.1	Init	98
7.5.2.2	~Init	98
7.5.3	Friends And Related Function Documentation	98
7.5.3.1	internal::Singleton< const Init >	98
7.6	qpp::internal::IOManipEigen Class Reference	99

7.6.1	Constructor & Destructor Documentation	100
7.6.1.1	IManipEigen	100
7.6.1.2	IManipEigen	100
7.6.2	Member Function Documentation	100
7.6.2.1	display	100
7.6.3	Member Data Documentation	100
7.6.3.1	_A	100
7.6.3.2	_chop	100
7.7	qpp::internal::IManipPointer< PointerType > Class Template Reference	100
7.7.1	Constructor & Destructor Documentation	101
7.7.1.1	IManipPointer	101
7.7.1.2	IManipPointer	101
7.7.2	Member Function Documentation	102
7.7.2.1	display	102
7.7.2.2	operator=	102
7.7.3	Member Data Documentation	102
7.7.3.1	_end	102
7.7.3.2	_n	102
7.7.3.3	_p	102
7.7.3.4	_separator	102
7.7.3.5	_start	102
7.8	qpp::internal::IManipRange< InputIterator > Class Template Reference	102
7.8.1	Constructor & Destructor Documentation	103
7.8.1.1	IManipRange	103
7.8.1.2	IManipRange	103
7.8.2	Member Function Documentation	104
7.8.2.1	display	104
7.8.2.2	operator=	104
7.8.3	Member Data Documentation	104
7.8.3.1	_end	104
7.8.3.2	_first	104
7.8.3.3	_last	104
7.8.3.4	_separator	104
7.8.3.5	_start	104
7.9	qpp::is_complex< T > Struct Template Reference	104
7.9.1	Detailed Description	105
7.10	qpp::is_complex< std::complex< T > > Struct Template Reference	105
7.10.1	Detailed Description	106
7.11	qpp::is_iterable< T, typename > Struct Template Reference	106
7.11.1	Detailed Description	107

7.12	qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type >> Struct Template Reference	107
7.12.1	Detailed Description	108
7.13	qpp::is_matrix_expression< Derived > Struct Template Reference	109
7.13.1	Detailed Description	109
7.14	qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived >> Struct Template Reference	110
7.14.1	Detailed Description	110
7.15	qpp::RandomDevices Class Reference	111
7.15.1	Detailed Description	112
7.15.2	Constructor & Destructor Documentation	112
7.15.2.1	RandomDevices	112
7.15.2.2	~RandomDevices	112
7.15.3	Friends And Related Function Documentation	112
7.15.3.1	internal::Singleton< RandomDevices >	112
7.15.4	Member Data Documentation	112
7.15.4.1	_rd	112
7.15.4.2	_rng	112
7.16	qpp::internal::Singleton< T > Class Template Reference	113
7.16.1	Detailed Description	113
7.16.2	Constructor & Destructor Documentation	114
7.16.2.1	Singleton	114
7.16.2.2	Singleton	114
7.16.2.3	~Singleton	114
7.16.3	Member Function Documentation	114
7.16.3.1	get_instance	114
7.16.3.2	get_thread_local_instance	114
7.16.3.3	operator=	114
7.17	qpp::States Class Reference	114
7.17.1	Detailed Description	116
7.17.2	Constructor & Destructor Documentation	116
7.17.2.1	States	116
7.17.2.2	~States	116
7.17.3	Friends And Related Function Documentation	116
7.17.3.1	internal::Singleton< const States >	116
7.17.4	Member Data Documentation	116
7.17.4.1	b00	116
7.17.4.2	b01	117
7.17.4.3	b10	117
7.17.4.4	b11	117
7.17.4.5	GHZ	117

7.17.4.6	pb00	117
7.17.4.7	pb01	117
7.17.4.8	pb10	117
7.17.4.9	pb11	117
7.17.4.10	pGHZ	117
7.17.4.11	pW	117
7.17.4.12	px0	117
7.17.4.13	px1	117
7.17.4.14	py0	118
7.17.4.15	py1	118
7.17.4.16	pz0	118
7.17.4.17	pz1	118
7.17.4.18	W	118
7.17.4.19	x0	118
7.17.4.20	x1	118
7.17.4.21	y0	118
7.17.4.22	y1	118
7.17.4.23	z0	118
7.17.4.24	z1	118
7.18	qpp::Timer< T, CLOCK_T > Class Template Reference	119
7.18.1	Detailed Description	120
7.18.2	Constructor & Destructor Documentation	120
7.18.2.1	Timer	120
7.18.2.2	Timer	120
7.18.2.3	Timer	120
7.18.2.4	~Timer	120
7.18.3	Member Function Documentation	121
7.18.3.1	display	121
7.18.3.2	get_duration	121
7.18.3.3	operator=	121
7.18.3.4	operator=	121
7.18.3.5	tic	121
7.18.3.6	tics	121
7.18.3.7	toc	122
7.18.4	Member Data Documentation	122
7.18.4.1	_end	122
7.18.4.2	_start	122
8	File Documentation	123
8.1	classes/codes.h File Reference	123

8.1.1	Detailed Description	123
8.2	classes/exception.h File Reference	123
8.2.1	Detailed Description	124
8.3	classes/gates.h File Reference	124
8.3.1	Detailed Description	125
8.4	classes/ideisplay.h File Reference	125
8.4.1	Detailed Description	125
8.5	classes/init.h File Reference	126
8.5.1	Detailed Description	126
8.6	classes/random_devices.h File Reference	126
8.6.1	Detailed Description	127
8.7	classes/states.h File Reference	127
8.7.1	Detailed Description	127
8.8	classes/timer.h File Reference	128
8.8.1	Detailed Description	128
8.9	constants.h File Reference	128
8.9.1	Detailed Description	129
8.10	entanglement.h File Reference	129
8.10.1	Detailed Description	130
8.11	entropies.h File Reference	130
8.11.1	Detailed Description	131
8.12	experimental/experimental.h File Reference	132
8.12.1	Detailed Description	132
8.13	functions.h File Reference	132
8.13.1	Detailed Description	136
8.14	input_output.h File Reference	136
8.14.1	Detailed Description	137
8.15	instruments.h File Reference	137
8.15.1	Detailed Description	139
8.16	internal/classes/iomanip.h File Reference	139
8.16.1	Detailed Description	140
8.17	internal/classes/singleton.h File Reference	140
8.17.1	Detailed Description	141
8.18	internal/util.h File Reference	141
8.18.1	Detailed Description	142
8.19	macros.h File Reference	142
8.19.1	Detailed Description	143
8.19.2	Macro Definition Documentation	143
8.19.2.1	ERROR	143
8.19.2.2	ERRORLN	143

8.19.2.3 PRINT	143
8.19.2.4 PRINTLN	143
8.20 MATLAB/matlab.h File Reference	143
8.20.1 Detailed Description	144
8.21 number_theory.h File Reference	144
8.21.1 Detailed Description	145
8.22 operations.h File Reference	145
8.22.1 Detailed Description	147
8.23 qpp.h File Reference	147
8.23.1 Detailed Description	149
8.24 random.h File Reference	149
8.24.1 Detailed Description	150
8.25 statistics.h File Reference	150
8.25.1 Detailed Description	151
8.26 traits.h File Reference	151
8.26.1 Detailed Description	152
8.27 types.h File Reference	152
8.27.1 Detailed Description	153
Index	155

Chapter 1

Quantum++

Version 0.8.3 - development

Quantum++ is a C++11 general purpose quantum computing library, composed solely of template header files. It uses the [Eigen 3](http://eigen.tuxfamily.org/dox/) linear algebra library and, if available, the [OpenMP](http://openmp.org/) multi-processing library. For additional [Eigen 3](http://eigen.tuxfamily.org/dox/) documentation see <http://eigen.tuxfamily.org/dox/>. For a simple [Eigen 3](http://eigen.tuxfamily.org/dox/AsciiQuickReference.txt) quick AS⇐ CII reference see <http://eigen.tuxfamily.org/dox/AsciiQuickReference.txt>.

Quantum++ is not restricted to qubit systems or specific quantum information processing tasks, being capable of simulating arbitrary quantum processes. The main design factors taken in consideration were the ease of use, high portability, and high performance.

If you are interesting in contributing, please contact me. To contribute, you need to have a decent knowledge of C++ (preferably C++11), including templates and the standard library, a basic knowledge of quantum computing and linear algebra, and some working experience with [Eigen 3](http://eigen.tuxfamily.org/dox/).

Copyright (c) 2013 - 2016 Vlad Gheorghiu, vgheorgh AT gmail DOT com.

Quantum++ is free software: you can redistribute it and/or modify it under the terms of the GNU General Public License as published by the Free Software Foundation, either version 3 of the License, or (at your option) any later version.

Quantum++ is distributed in the hope that it will be useful, but WITHOUT ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU General Public License for more details.

You should have received a copy of the GNU General Public License along with Quantum++. If not, see <http://www.gnu.org/licenses/>.

Building instructions

Configuration:

- Compiler: [g++](http://gcc.gnu.org/) version 4.8 or later (for good C++11 support)
- [Eigen 3](http://eigen.tuxfamily.org/dox/) library located in `$HOME/eigen`
- Quantum++ library located in `$HOME/qpp`
- [MATLAB](http://www.mathworks.com/) compiler include header files: `/Applications/MATLAB_R2014b.app/extern/include`
- [MATLAB](http://www.mathworks.com/) compiler shared library files: `/Applications/MATLAB_R2014b.app/bin/maci64`

Building without a build system

- Example file: `$HOME/qpp/examples/minimal.cpp`

- Output executable: `$HOME/qpp/examples/minimal`
- Must run the commands below from inside the directory `$HOME/qpp/examples`

Release version (without **MATLAB** support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -O3 -DNDEBUG -DEIGEN_NO_DEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    minimal.cpp -o minimal
```

Debug version (without **MATLAB** support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -g3 -DDEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    minimal.cpp -o minimal
```

Release version (with **MATLAB** support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -O3 -DNDEBUG -DEIGEN_NO_DEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    -I/Applications/MATLAB_R2014b.app/extern/include \
    -L/Applications/MATLAB_R2014b.app/bin/maci64 \
    -lmx -lmat minimal.cpp -o minimal
```

Debug version (with **MATLAB** support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -g3 -DDEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    -I /Applications/MATLAB_R2014b.app/extern/include \
    -L /Applications/MATLAB_R2014b.app/bin/maci64 \
    -lmx -lmat minimal.cpp -o minimal
```

Building using **cmake**

The current version of the repository has a `./CMakeLists.txt` configuration file for building examples using **cmake**. To build an example using **cmake**, I recommend an out-of-source build, i.e., from the root of the project (where `./include` is located), type

```
mkdir ./build
cd ./build
cmake ..
make
```

The above commands build the release version (default) executable `qpp`, from the source file `./examples/minimal.cpp`, without **MATLAB** support (default), inside the directory `./build`. To build a different configuration, e.g. debug version with **MATLAB** support, type from the root of the project

```
cd ./build
rm -rf *
cmake -DCMAKE_BUILD_TYPE=Debug -DWITH_MATLAB=ON ..
make
```

Or, to disable **OpenMP** support (enabled by default), type

```
cd ./build
rm -rf *
cmake -DWITH_OPENMP=OFF ..
make
```

To change the name of the example file, the location of the **Eigen 3** library or the location of **MATLAB** installation, edit the `./CMakeLists.txt` file. See also `./CMakeLists.txt` for additional options. Do not forget to remove everything from the `./build` directory before a fresh build!

Additional remarks

- The C++ compiler must be C++11 compliant.
- If using **Windows**, I recommend compiling under **cygwin** via **cmake** and **g++**. See also <http://stackoverflow.com/questions/28997206/cygwin-support-for-c11-in-g4-9-2> for a bug related to lack of support for some C++11 math functions, and how to fix it. Quick fix: patch the standard library header file `<cmath>` using the provided patch `./cmath_cygwin.patch`.
- If your compiler does not support **OpenMP** (as it is the case e.g with **clang++**), disable **OpenMP** in your build, as otherwise the linker may not find the **gomp** library.
- If you run the program on **OS X** with **MATLAB** support, make sure that the environment variable `DYLD_LIBRARY_PATH` is set to point to the **MATLAB** compiler library location, see the `run_OSX_MATLAB` script. Otherwise, you will get a runtime error like `dyld: Library not loaded: @rpath/libmat.dylib`.

* I recommend running via a script, as otherwise setting the `'DYLD_LIBRARY_PATH'` globally may interfere with [macports](https://www.macports.org/) [cmake](http://www.cmake.org/) installation (in case you use [cmake](http://www.cmake.org/) from [macports](https://www.macports.org/)). If you use a script, then the environment variable is local to the script and does not interfere with the rest of the system.

* Example of running script, run from inside the directory where the executable `'qpp'` is located:

```
#!/bin/sh # Run Quantum++ under OS X with MATLAB support

export DYLD_LIBRARY_PATH=$DYLD_LIBRARY_PATH:"/Applications/MATLAB_R2014b.app/bin/maci64"
./qpp
```

- If you build a debug version with **g++** under **OS X** and use **gdb** to step inside template functions you may want to add `-fno-weak` compiler flag. See <http://stackoverflow.com/questions/23330641/gnu-gdb-can-not-step-into-template-functions-os-x-mavericks> for more details about this problem.

Chapter 2

Namespace Index

2.1 Namespace List

Here is a list of all namespaces with brief descriptions:

qpp	Quantum++ main namespace	13
qpp::experimental	Experimental/test functions/classes, do not use or modify	80
qpp::internal	Internal utility functions, do not use/modify	80

Chapter 3

Hierarchical Index

3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

std::exception	
qpp::Exception	85
false_type	
qpp::is_complex< T >	104
qpp::is_iterable< T, typename >	106
qpp::is_matrix_expression< Derived >	109
qpp::IDisplay	95
qpp::internal::IOManipEigen	99
qpp::internal::IOManipPointer< PointerType >	100
qpp::internal::IOManipRange< InputIterator >	102
qpp::Timer< T, CLOCK_T >	119
qpp::internal::Singleton< T >	113
qpp::internal::Singleton< const Codes >	113
qpp::Codes	83
qpp::internal::Singleton< const Gates >	113
qpp::Gates	89
qpp::internal::Singleton< const Init >	113
qpp::Init	97
qpp::internal::Singleton< const States >	113
qpp::States	114
qpp::internal::Singleton< RandomDevices >	113
qpp::RandomDevices	111
true_type	
qpp::is_complex< std::complex< T > >	105
qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >	107
qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >	110

Chapter 4

Class Index

4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

qpp::Codes	Const Singleton class that defines quantum error correcting codes	83
qpp::Exception	Generates custom exceptions, used when validating function parameters	85
qpp::Gates	Const Singleton class that implements most commonly used gates	89
qpp::IDisplay	Abstract class (interface) that mandates the definition of virtual <code>std::ostream& display(std::ostream& os) const</code>	95
qpp::Init	Const Singleton class that performs additional initializations/cleanups	97
qpp::internal::IOManipEigen	99
qpp::internal::IOManipPointer< PointerType >	100
qpp::internal::IOManipRange< InputIterator >	102
qpp::is_complex< T >	Checks whether the type is a complex type	104
qpp::is_complex< std::complex< T > >	Checks whether the type is a complex number type, specialization for complex types	105
qpp::is_iterable< T, typename >	Checks whether <i>T</i> is compatible with an STL-like iterable container	106
qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >	Checks whether <i>T</i> is compatible with an STL-like iterable container, specialization for STL-like iterable containers	107
qpp::is_matrix_expression< Derived >	Checks whether the type is an Eigen matrix expression	109
qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >	Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions	110
qpp::RandomDevices	Singleton class that manages the source of randomness in the library	111
qpp::internal::Singleton< T >	Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)	113
qpp::States	Const Singleton class that implements most commonly used states	114
qpp::Timer< T, CLOCK_T >	Chronometer	119

Chapter 5

File Index

5.1 File List

Here is a list of all files with brief descriptions:

constants.h	
Constants	128
entanglement.h	
Entanglement functions	129
entropies.h	
Entropy functions	130
functions.h	
Generic quantum computing functions	132
input_output.h	
Input/output functions	136
instruments.h	
Measurement functions	137
macros.h	
Preprocessor macros	142
number_theory.h	
Number theory functions	144
operations.h	
Quantum operation functions	145
qpp.h	
Quantum++ main header file, includes all other necessary headers	147
random.h	
Randomness-related functions	149
statistics.h	
Statistics functions	150
traits.h	
Type traits	151
types.h	
Type aliases	152
classes/ codes.h	
Quantum error correcting codes	123
classes/ exception.h	
Exceptions	123
classes/ gates.h	
Quantum gates	124
classes/ display.h	
Display interface via the non-virtual interface (NVI)	125
classes/ init.h	
Initialization	126

classes/ random_devices.h	
Random devices	126
classes/ states.h	
Quantum states	127
classes/ timer.h	
Timing	128
experimental/ experimental.h	
Experimental/test functions/classes	132
internal/ util.h	
Internal utility functions	141
internal/classes/ iomanip.h	
Input/output manipulators	139
internal/classes/ singleton.h	
Singleton pattern via CRTP	140
MATLAB/ matlab.h	
Input/output interfacing with MATLAB	143

Chapter 6

Namespace Documentation

6.1 qpp Namespace Reference

Quantum++ main namespace.

Namespaces

- [experimental](#)
Experimental/test functions/classes, do not use or modify.
- [internal](#)
Internal utility functions, do not use/modify.

Classes

- class [Codes](#)
const Singleton class that defines quantum error correcting codes
- class [Exception](#)
Generates custom exceptions, used when validating function parameters.
- class [Gates](#)
const Singleton class that implements most commonly used gates
- class [IDisplay](#)
Abstract class (interface) that mandates the definition of virtual `std::ostream& display(std::ostream& os) const`.
- class [Init](#)
const Singleton class that performs additional initializations/cleanups
- struct [is_complex](#)
Checks whether the type is a complex type.
- struct [is_complex< std::complex< T > >](#)
Checks whether the type is a complex number type, specialization for complex types.
- struct [is_iterable](#)
Checks whether T is compatible with an STL-like iterable container.
- struct [is_iterable< T, to_void< decltype\(std::declval< T >\(\).begin\(\)\), decltype\(std::declval< T >\(\).end\(\)\), typename T::value_type > >](#)
Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.
- struct [is_matrix_expression](#)
Checks whether the type is an Eigen matrix expression.
- struct [is_matrix_expression< typename Eigen::MatrixBase< Derived > >](#)
Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.

- class [RandomDevices](#)
Singleton class that manages the source of randomness in the library.
- class [States](#)
const Singleton class that implements most commonly used states
- class [Timer](#)
Chronometer.

Typedefs

- `template<typename... >`
`using to_void = void`
Alias template that implements the proposal for void_t.
- `using idx = std::size_t`
Non-negative integer index.
- `using bigint = long long int`
Big integer.
- `using ubigint = unsigned long long int`
Non-negative big integer.
- `using cplx = std::complex< double >`
Complex number in double precision.
- `using ket = Eigen::VectorXcd`
Complex (double precision) dynamic Eigen column vector.
- `using bra = Eigen::RowVectorXcd`
Complex (double precision) dynamic Eigen row vector.
- `using cmat = Eigen::MatrixXcd`
Complex (double precision) dynamic Eigen matrix.
- `using dmat = Eigen::MatrixXd`
Real (double precision) dynamic Eigen matrix.
- `template<typename Scalar >`
`using dyn_mat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >`
Dynamic Eigen matrix over the field specified by Scalar.
- `template<typename Scalar >`
`using dyn_col_vect = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >`
Dynamic Eigen column vector over the field specified by Scalar.
- `template<typename Scalar >`
`using dyn_row_vect = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >`
Dynamic Eigen row vector over the field specified by Scalar.

Functions

- `constexpr cplx operator""_i (unsigned long long int x) noexcept`
User-defined literal for complex $i = \sqrt{-1}$ (integer overload)
- `constexpr cplx operator""_i (long double x) noexcept`
User-defined literal for complex $i = \sqrt{-1}$ (real overload)
- `cplx omega (idx D)`
D-th root of unity.
- `template<typename Derived >`
`dyn_col_vect< double > schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Schmidt coefficients of the bi-partite pure state A.

- `template<typename Derived >`
`cmat schmidtA` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &dims)
Schmidt basis on Alice side.
- `template<typename Derived >`
`cmat schmidtB` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &dims)
Schmidt basis on Bob side.
- `template<typename Derived >`
`std::vector< double > schmidtprobs` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &dims)
Schmidt probabilities of the bi-partite pure state A.
- `template<typename Derived >`
`double entanglement` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &dims)
Entanglement of the bi-partite pure state A.
- `template<typename Derived >`
`double gconcurrence` (const Eigen::MatrixBase< Derived > &A)
G-concurrence of the bi-partite pure state A.
- `template<typename Derived >`
`double negativity` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &dims)
Negativity of the bi-partite mixed state A.
- `template<typename Derived >`
`double lognegativity` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &dims)
Logarithmic negativity of the bi-partite mixed state A.
- `template<typename Derived >`
`double concurrence` (const Eigen::MatrixBase< Derived > &A)
Wootters concurrence of the bi-partite qubit mixed state A.
- `template<typename Derived >`
`double entropy` (const Eigen::MatrixBase< Derived > &A)
von-Neumann entropy of the density matrix A
- `double entropy` (const std::vector< double > &prob)
Shannon entropy of the probability distribution prob.
- `template<typename Derived >`
`double renyi` (const Eigen::MatrixBase< Derived > &A, double alpha)
Renyi- α entropy of the density matrix A, for $\alpha \geq 0$.
- `double renyi` (const std::vector< double > &prob, double alpha)
Renyi- α entropy of the probability distribution prob, for $\alpha \geq 0$.
- `template<typename Derived >`
`double tsallis` (const Eigen::MatrixBase< Derived > &A, double q)
Tsallis- q entropy of the density matrix A, for $q \geq 0$.
- `double tsallis` (const std::vector< double > &prob, double q)
Tsallis- q entropy of the probability distribution prob, for $q \geq 0$.
- `template<typename Derived >`
`double qmutualinfo` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &subsysA, const std::vector< `idx` > &subsysB, const std::vector< `idx` > &dims)
Quantum mutual information between 2 subsystems of a composite system.
- `template<typename Derived >`
`double qmutualinfo` (const Eigen::MatrixBase< Derived > &A, const std::vector< `idx` > &subsysA, const std::vector< `idx` > &subsysB, `idx` d=2)
Quantum mutual information between 2 subsystems of a composite system.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > transpose` (const Eigen::MatrixBase< Derived > &A)
Transpose.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > conjugate` (const Eigen::MatrixBase< Derived > &A)

Complex conjugate.

- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > adjoint (const Eigen::MatrixBase< Derived > &A)`

Adjoint.

- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > inverse (const Eigen::MatrixBase< Derived > &A)`

Inverse.

- `template<typename Derived >`
`Derived::Scalar trace (const Eigen::MatrixBase< Derived > &A)`

Trace.

- `template<typename Derived >`
`Derived::Scalar det (const Eigen::MatrixBase< Derived > &A)`

Determinant.

- `template<typename Derived >`
`Derived::Scalar logdet (const Eigen::MatrixBase< Derived > &A)`

Logarithm of the determinant.

- `template<typename Derived >`
`Derived::Scalar sum (const Eigen::MatrixBase< Derived > &A)`

Element-wise sum of A.

- `template<typename Derived >`
`Derived::Scalar prod (const Eigen::MatrixBase< Derived > &A)`

Element-wise product of A.

- `template<typename Derived >`
`double norm (const Eigen::MatrixBase< Derived > &A)`

Frobenius norm.

- `template<typename Derived >`
`std::pair< dyn_col_vect< cplx >, cmat > eig (const Eigen::MatrixBase< Derived > &A)`

Full eigen decomposition.

- `template<typename Derived >`
`dyn_col_vect< cplx > evals (const Eigen::MatrixBase< Derived > &A)`

Eigenvalues.

- `template<typename Derived >`
`cmat evecs (const Eigen::MatrixBase< Derived > &A)`

Eigenvectors.

- `template<typename Derived >`
`std::pair< dyn_col_vect< double >, cmat > heig (const Eigen::MatrixBase< Derived > &A)`

Full eigen decomposition of Hermitian expression.

- `template<typename Derived >`
`dyn_col_vect< double > hevals (const Eigen::MatrixBase< Derived > &A)`

Hermitian eigenvalues.

- `template<typename Derived >`
`cmat hevecs (const Eigen::MatrixBase< Derived > &A)`

Hermitian eigenvectors.

- `template<typename Derived >`
`std::tuple< cmat, dyn_col_vect< double >, cmat > svd (const Eigen::MatrixBase< Derived > &A)`

Full singular value decomposition.

- `template<typename Derived >`
`dyn_col_vect< double > svals (const Eigen::MatrixBase< Derived > &A)`

Singular values.

- `template<typename Derived >`
`cmat svdU (const Eigen::MatrixBase< Derived > &A)`

Left singular vectors.

- `template<typename Derived >`
`cmat svdV` (const Eigen::MatrixBase< Derived > &A)
Right singular vectors.
- `template<typename Derived >`
`cmat funm` (const Eigen::MatrixBase< Derived > &A, `cplx`(*f)(const `cplx` &))
Functional calculus $f(A)$
- `template<typename Derived >`
`cmat sqrtm` (const Eigen::MatrixBase< Derived > &A)
Matrix square root.
- `template<typename Derived >`
`cmat absm` (const Eigen::MatrixBase< Derived > &A)
Matrix absolut value.
- `template<typename Derived >`
`cmat expm` (const Eigen::MatrixBase< Derived > &A)
Matrix exponential.
- `template<typename Derived >`
`cmat logm` (const Eigen::MatrixBase< Derived > &A)
Matrix logarithm.
- `template<typename Derived >`
`cmat sinm` (const Eigen::MatrixBase< Derived > &A)
Matrix sin.
- `template<typename Derived >`
`cmat cosm` (const Eigen::MatrixBase< Derived > &A)
Matrix cos.
- `template<typename Derived >`
`cmat spectralpowm` (const Eigen::MatrixBase< Derived > &A, const `cplx` z)
Matrix power.
- `template<typename Derived >`
`dyn_mat`< typename Derived::Scalar > `powm` (const Eigen::MatrixBase< Derived > &A, `idx` n)
Matrix power.
- `template<typename Derived >`
`double Schatten` (const Eigen::MatrixBase< Derived > &A, double p)
Schatten matrix norm.
- `template<typename OutputScalar , typename Derived >`
`dyn_mat`< OutputScalar > `cwise` (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const type-
name Derived::Scalar &))
Functor.
- `template<typename T >`
`dyn_mat`< typename T::Scalar > `kron` (const T &head)
Kronecker product.
- `template<typename T , typename... Args>`
`dyn_mat`< typename T::Scalar > `kron` (const T &head, const Args &...tail)
Kronecker product.
- `template<typename Derived >`
`dyn_mat`< typename Derived::Scalar > `kron` (const std::vector< Derived > &As)
Kronecker product.
- `template<typename Derived >`
`dyn_mat`< typename Derived::Scalar > `kron` (const std::initializer_list< Derived > &As)
Kronecker product.
- `template<typename Derived >`
`dyn_mat`< typename Derived::Scalar > `kronpow` (const Eigen::MatrixBase< Derived > &A, `idx` n)
Kronecker power.

- `template<typename T >`
`dyn_mat< typename T::Scalar > dirsum (const T &head)`
Direct sum.
- `template<typename T , typename... Args>`
`dyn_mat< typename T::Scalar > dirsum (const T &head, const Args &...tail)`
Direct sum.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > dirsum (const std::vector< Derived > &As)`
Direct sum.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > dirsum (const std::initializer_list< Derived > &As)`
Direct sum.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > dirsumpow (const Eigen::MatrixBase< Derived > &A, idx n)`
Direct sum power.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > reshape (const Eigen::MatrixBase< Derived > &A, idx rows, idx cols)`
Reshape.
- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
Commutator.
- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
Anti-commutator.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > prj (const Eigen::MatrixBase< Derived > &V)`
Projector.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > grams (const std::vector< Derived > &Vs)`
Gram-Schmidt orthogonalization.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > grams (const std::initializer_list< Derived > &Vs)`
Gram-Schmidt orthogonalization.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > grams (const Eigen::MatrixBase< Derived > &A)`
Gram-Schmidt orthogonalization.
- `std::vector< idx > n2multiidx (idx n, const std::vector< idx > &dims)`
Non-negative integer index to multi-index.
- `idx multiidx2n (const std::vector< idx > &midx, const std::vector< idx > &dims)`
Multi-index to non-negative integer index.
- `ket mket (const std::vector< idx > &mask, const std::vector< idx > &dims)`
Multi-partite qudit ket.
- `ket mket (const std::vector< idx > &mask, idx d=2)`
Multi-partite qudit ket.
- `cmat mprj (const std::vector< idx > &mask, const std::vector< idx > &dims)`
Projector onto multi-partite qudit ket.
- `cmat mprj (const std::vector< idx > &mask, idx d=2)`
Projector onto multi-partite qudit ket.
- `template<typename InputIterator >`
`std::vector< double > abssq (InputIterator first, InputIterator last)`

- Computes the absolute values squared of an STL-like range of complex numbers.*

 - `template<typename Container >`
`std::vector< double > abssq (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type * = nullptr)`

Computes the absolute values squared of an STL-like container.

 - `template<typename Derived >`
`std::vector< double > abssq (const Eigen::MatrixBase< Derived > &A)`

Computes the absolute values squared of an Eigen expression.

 - `template<typename InputIterator >`
`std::iterator_traits< InputIterator >::value_type sum (InputIterator first, InputIterator last)`

Element-wise sum of an STL-like range.

 - `template<typename Container >`
`Container::value_type sum (const Container &c)`

Element-wise sum of the elements of an STL-like container.

 - `template<typename InputIterator >`
`std::iterator_traits< InputIterator >::value_type prod (InputIterator first, InputIterator last)`

Element-wise product of an STL-like range.

 - `template<typename Container >`
`Container::value_type prod (const Container &c)`

Element-wise product of the elements of an STL-like container.

 - `template<typename Derived >`
`dyn_col_vect< typename Derived::Scalar > rho2pure (const Eigen::MatrixBase< Derived > &A)`

Finds the pure state representation of a matrix proportional to a projector onto a pure state.

 - `template<typename T >`
`std::vector< T > complement (std::vector< T > subsys, idx N)`

Constructs the complement of a subsystem vector.

 - `template<typename Derived >`
`std::vector< double > rho2bloch (const Eigen::MatrixBase< Derived > &A)`

Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix A.

 - `cmat bloch2rho (const std::vector< double > &r)`

Computes the density matrix corresponding to the 3-dimensional real Bloch vector r.

 - `template<typename Derived >`
`internal::IOManipEigen disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)`

Eigen expression ostream manipulator.

 - `internal::IOManipEigen disp (cplx z, double chop=qpp::chop)`

Complex number ostream manipulator.

 - `template<typename InputIterator >`
`internal::IOManipRange< InputIterator > disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[" , const std::string &end="]")`

Range ostream manipulator.

 - `template<typename Container >`
`internal::IOManipRange< typename Container::const_iterator > disp (const Container &c, const std::string &separator, const std::string &start="[" , const std::string &end="]")`

Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.

 - `template<typename PointerType >`
`internal::IOManipPointer< PointerType > disp (const PointerType *p, idx n, const std::string &separator, const std::string &start="[" , const std::string &end="]")`

C-style pointer ostream manipulator.

 - `template<typename Derived >`
`void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)`

Saves Eigen expression to a binary file (internal format) in double precision.

 - `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > load (const std::string &fname)`

Loads Eigen matrix from a binary file (internal format) in double precision.

- `template<typename Derived >`
`dyn_col_vect< typename Derived::Scalar > ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::↵`
`MatrixBase< Derived > &psi, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

Generalized inner product.

- `template<typename Derived >`
`dyn_col_vect< typename Derived::Scalar > ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::↵`
`MatrixBase< Derived > &psi, const std::vector< idx > &subsys, idx d=2)`

Generalized inner product.

- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived`
`> &A, const std::vector< cmat > &Ks)`

Measures the state A using the set of Kraus operators Ks.

- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived`
`> &A, const std::initializer_list< cmat > &Ks)`

Measures the state A using the set of Kraus operators Ks.

- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived`
`> &A, const cmat &U)`

Measures the state A in the orthonormal basis specified by the unitary matrix U.

- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived`
`> &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived`
`> &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx >`
`&dims)`

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived`
`> &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)`

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived`
`> &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)`

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived`
`> &A, const cmat &V, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.

- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived`
`> &A, const cmat &V, const std::vector< idx > &subsys, idx d=2)`

Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.

- `template<typename Derived >`
`std::tuple< std::vector< idx >, double, cmat > measure_seq (const Eigen::MatrixBase< Derived > &A,`
`std::vector< idx > subsys, std::vector< idx > dims)`

Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.

- `template<typename Derived >`
`std::tuple< std::vector< idx >, double, cmat > measure_seq (const Eigen::MatrixBase< Derived > &A,`
`std::vector< idx > subsys, idx d=2)`

- Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.*
- template<typename Derived >
Derived [loadMATLABmatrix](#) (const std::string &mat_file, const std::string &var_name)
Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.
 - template<>
[dmat loadMATLABmatrix](#) (const std::string &mat_file, const std::string &var_name)
Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))
 - template<>
[cmat loadMATLABmatrix](#) (const std::string &mat_file, const std::string &var_name)
Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))
 - template<typename Derived >
void [saveMATLABmatrix](#) (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)
Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.
 - template<>
void [saveMATLABmatrix](#) (const Eigen::MatrixBase< [dmat](#) > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)
Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))
 - template<>
void [saveMATLABmatrix](#) (const Eigen::MatrixBase< [cmat](#) > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)
Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))
 - std::vector< int > [x2contfrac](#) (double x, [idx](#) n, [idx](#) cut=1e5)
Simple continued fraction expansion.
 - double [contfrac2x](#) (const std::vector< int > &cf, [idx](#) n)
Real representation of a simple continued fraction.
 - double [contfrac2x](#) (const std::vector< int > &cf)
Real representation of a simple continued fraction.
 - [ubigint gcd](#) ([ubigint](#) m, [ubigint](#) n)
Greatest common divisor of two non-negative integers.
 - [ubigint gcd](#) (const std::vector< [ubigint](#) > &ns)
Greatest common divisor of a list of non-negative integers.
 - [ubigint lcm](#) ([ubigint](#) m, [ubigint](#) n)
Least common multiple of two positive integers.
 - [ubigint lcm](#) (const std::vector< [ubigint](#) > &ns)
Least common multiple of a list of positive integers.
 - std::vector< [idx](#) > [invperm](#) (const std::vector< [idx](#) > &perm)
Inverse permutation.
 - std::vector< [idx](#) > [compperm](#) (const std::vector< [idx](#) > &perm, const std::vector< [idx](#) > &sigma)
Compose permutations.
 - std::vector< [ubigint](#) > [factors](#) ([ubigint](#) n)
Prime factor decomposition.
 - bool [isprime](#) ([ubigint](#) n)
Primality test.
 - [ubigint modpow](#) ([ubigint](#) a, [ubigint](#) n, [ubigint](#) p)
Integer power modulo p.
 - template<typename Derived1 , typename Derived2 >
[dyn_mat](#)< typename Derived1::Scalar > [applyCTRL](#) (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< [idx](#) > &ctrl, const std::vector< [idx](#) > &subsys, const std::vector< [idx](#) > &dims)
Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.

- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx d=2)`
Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)`
Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, idx d=2)`
Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- `template<typename Derived >`
`cmat apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks)`
Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.
- `template<typename Derived >`
`cmat apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)`
Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix rho.
- `template<typename Derived >`
`cmat apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)`
Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix rho.
- `cmat kraus2super (const std::vector< cmat > &Ks)`
Superoperator matrix.
- `cmat kraus2choi (const std::vector< cmat > &Ks)`
Choi matrix.
- `std::vector< cmat > choi2kraus (const cmat &A)`
Orthogonal Kraus operators from Choi matrix.
- `cmat choi2super (const cmat &A)`
Converts Choi matrix to superoperator matrix.
- `cmat super2choi (const cmat &A)`
Converts superoperator matrix to Choi matrix.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Partial trace.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Partial trace.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)`
Partial trace.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)`
Partial trace.

- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > ptranpose` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)
Partial transpose.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > ptranpose` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)
Partial transpose.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > syspermute` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, const std::vector< idx > &dims)
Subsystem permutation.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > syspermute` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, idx d=2)
Subsystem permutation.
- `double rand` (double a=0, double b=1)
Generates a random real number uniformly distributed in the interval [a, b]
- `bigint rand` (bigint a=std::numeric_limits< bigint >::min(), bigint b=std::numeric_limits< bigint >::max())
Generates a random big integer uniformly distributed in the interval [a, b].
- `ubigint rand` (ubigint a=std::numeric_limits< ubigint >::min(), ubigint b=std::numeric_limits< ubigint >::max())
Generates a random non-negative big integer uniformly distributed in the interval [a, b].
- `idx randidx` (idx a=std::numeric_limits< idx >::min(), idx b=std::numeric_limits< idx >::max())
Generates a random index (idx) uniformly distributed in the interval [a, b].
- `template<typename Derived >`
`Derived rand` (idx rows, idx cols, double a=0, double b=1)
Generates a random matrix with entries uniformly distributed in the interval [a, b]
- `template<>`
`dmat rand` (idx rows, idx cols, double a, double b)
Generates a random real matrix with entries uniformly distributed in the interval [a, b], specialization for double matrices (`qpp::dmat`)
- `template<>`
`cmat rand` (idx rows, idx cols, double a, double b)
Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b], specialization for complex matrices (`qpp::cmat`)
- `template<typename Derived >`
`Derived randn` (idx rows, idx cols, double mean=0, double sigma=1)
Generates a random matrix with entries normally distributed in $N(\text{mean}, \text{sigma})$
- `template<>`
`dmat randn` (idx rows, idx cols, double mean, double sigma)
Generates a random real matrix with entries normally distributed in $N(\text{mean}, \text{sigma})$, specialization for double matrices (`qpp::dmat`)
- `template<>`
`cmat randn` (idx rows, idx cols, double mean, double sigma)
Generates a random complex matrix with entries (both real and imaginary) normally distributed in $N(\text{mean}, \text{sigma})$, specialization for complex matrices (`qpp::cmat`)
- `double randn` (double mean=0, double sigma=1)
Generates a random real number (double) normally distributed in $N(\text{mean}, \text{sigma})$
- `cmat randU` (idx D)
Generates a random unitary matrix.
- `cmat randV` (idx Din, idx Dout)
Generates a random isometry matrix.

- `std::vector< cmat > randkraus (idx N, idx D)`
Generates a set of random Kraus operators.
- `cmat randH (idx D)`
Generates a random Hermitian matrix.
- `ket randket (idx D)`
Generates a random normalized ket (pure state vector)
- `cmat randrho (idx D)`
Generates a random density matrix.
- `std::vector< idx > randperm (idx n)`
Generates a random uniformly distributed permutation.
- `std::vector< double > uniform (idx N)`
Uniform probability distribution vector.
- `std::vector< double > marginalX (const dmat &probXY)`
Marginal distribution.
- `std::vector< double > marginalY (const dmat &probXY)`
Marginal distribution.
- `template<typename Container > double avg (const std::vector< double > &prob, const Container &X)`
Average.
- `template<typename Container > double cov (const dmat &probXY, const Container &X, const Container &Y)`
Covariance.
- `template<typename Container > double var (const std::vector< double > &prob, const Container &X)`
Variance.
- `template<typename Container > double sigma (const std::vector< double > &prob, const Container &X)`
Standard deviation.
- `template<typename Container > double cor (const dmat &probXY, const Container &X, const Container &Y)`
Correlation.

Variables

- `constexpr double chop = 1e-10`
Used in `qpp::disp()` for setting to zero numbers that have their absolute value smaller than `qpp::chop`.
- `constexpr double eps = 1e-12`
Used to decide whether a number or expression in double precision is zero or not.
- `constexpr idx maxn = 64`
Maximum number of allowed qu(d)its (subsystems)
- `constexpr double pi = 3.141592653589793238462643383279502884`
 π
- `constexpr double ee = 2.718281828459045235360287471352662497`
Base of natural logarithm, e .
- `constexpr double infity = std::numeric_limits<double>::infinity()`
Used to denote infinity in double precision.

6.1.1 Detailed Description

Quantum++ main namespace.

6.1.2 Typedef Documentation

6.1.2.1 using qpp::bigint = typedef long long int

Big integer.

6.1.2.2 using qpp::bra = typedef Eigen::RowVectorXcd

Complex (double precision) dynamic Eigen row vector.

6.1.2.3 using qpp::cmat = typedef Eigen::MatrixXcd

Complex (double precision) dynamic Eigen matrix.

6.1.2.4 using qpp::cplx = typedef std::complex<double>

Complex number in double precision.

6.1.2.5 using qpp::dmat = typedef Eigen::MatrixXd

Real (double precision) dynamic Eigen matrix.

6.1.2.6 template<typename Scalar > using qpp::dyn_col_vect = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, 1>

Dynamic Eigen column vector over the field specified by *Scalar*.

Example:

```
// type of colvect is Eigen::Matrix<float, Eigen::Dynamic, 1>
auto colvect = dyn_col_vect<float>(2);
```

6.1.2.7 template<typename Scalar > using qpp::dyn_mat = typedef Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>

Dynamic Eigen matrix over the field specified by *Scalar*.

Example:

```
// type of mat is Eigen::Matrix<float, Eigen::Dynamic, Eigen::Dynamic>
auto mat = dyn_mat<float>(2,3);
```

6.1.2.8 template<typename Scalar > using qpp::dyn_row_vect = typedef Eigen::Matrix<Scalar, 1, Eigen::Dynamic>

Dynamic Eigen row vector over the field specified by *Scalar*.

Example:

```
// type of rowvect is Eigen::Matrix<float, 1, Eigen::Dynamic>
auto rowvect = dyn_row_vect<float>(3);
```

6.1.2.9 using qpp::idx = typedef std::size_t

Non-negative integer index.

6.1.2.10 `using qpp::ket = typedef Eigen::VectorXcd`

Complex (double precision) dynamic Eigen column vector.

6.1.2.11 `template<typename... > using qpp::to_void = typedef void`

Alias template that implements the proposal for `void_t`.

See also

<http://www.open-std.org/jtc1/sc22/wg21/docs/papers/2014/n3911>

6.1.2.12 `using qpp::ubigint = typedef unsigned long long int`

Non-negative big integer.

6.1.3 Function Documentation

6.1.3.1 `template<typename Derived > cmat qpp::absm (const Eigen::MatrixBase< Derived > & A)`

Matrix absolut value.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Matrix absolut value of *A*

6.1.3.2 `template<typename InputIterator > std::vector<double> qpp::abssq (InputIterator first, InputIterator last)`

Computes the absolute values squared of an STL-like range of complex numbers.

Parameters

<i>first</i>	Iterator to the first element of the range
<i>last</i>	Iterator to the last element of the range

Returns

Real vector consisting of the range absolut values squared

6.1.3.3 `template<typename Container > std::vector<double> qpp::abssq (const Container & c, typename std::enable_if< is_iterable< Container >::value >::type * = nullptr)`

Computes the absolute values squared of an STL-like container.

Parameters

<i>c</i>	STL-like container
----------	--------------------

Returns

Real vector consisting of the container's absolut values squared

6.1.3.4 `template<typename Derived > std::vector<double> qpp::abssq (const Eigen::MatrixBase< Derived > & A)`

Computes the absolute values squared of an Eigen expression.

Parameters

A	Eigen expression
-----	------------------

Returns

Real vector consisting of the absolut values squared

6.1.3.5 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::adjoint (const Eigen::MatrixBase< Derived > & A)`

Adjoint.

Parameters

A	Eigen expression
-----	------------------

Returns

Adjoint (Hermitian conjugate) of A , as a dynamic matrix over the same scalar field as A

6.1.3.6 `template<typename Derived1 , typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::anticomm (const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B)`

Anti-commutator.

See also

[qpp::comm\(\)](#)

Anti-commutator $\{A, B\} = AB + BA$. Both A and B must be Eigen expressions over the same scalar field.

Parameters

A	Eigen expression
B	Eigen expression

Returns

Anti-commutator $AB + BA$, as a dynamic matrix over the same scalar field as A

6.1.3.7 `template<typename Derived1 , typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::apply (const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector< idx > & subsys, const std::vector< idx > & dims)`

Applies the gate A to the part *subsys* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate A must match the dimension of *subsys*

Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>dims</i>	Dimensions of the multi-partite system

Returns

Gate *A* applied to the part *subsys* of *state*

6.1.3.8 `template<typename Derived1 , typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::apply (const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector< idx > & subsys, idx d = 2)`

Applies the gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>d</i>	Subsystem dimensions

Returns

Gate *A* applied to the part *subsys* of *state*

6.1.3.9 `template<typename Derived > cmat qpp::apply (const Eigen::MatrixBase< Derived > & rho, const std::vector< cmat > & Ks)`

Applies the channel specified by the set of Kraus operators *Ks* to the density matrix *rho*.

Parameters

<i>rho</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators

Returns

Output density matrix after the action of the channel

6.1.3.10 `template<typename Derived > cmat qpp::apply (const Eigen::MatrixBase< Derived > & rho, const std::vector< cmat > & Ks, const std::vector< idx > & subsys, const std::vector< idx > & dims)`

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *rho*.

Parameters

<i>rho</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes where the Kraus operators <i>Ks</i> are applied
<i>dims</i>	Dimensions of the multi-partite system

Returns

Output density matrix after the action of the channel

```
6.1.3.11 template<typename Derived > cmat qpp::apply ( const Eigen::MatrixBase< Derived > & rho, const std::vector<
cmat > & Ks, const std::vector< idx > & subsys, idx d = 2 )
```

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *rho*.

Parameters

<i>rho</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes where the Kraus operators <i>Ks</i> are applied
<i>d</i>	Subsystem dimensions

Returns

Output density matrix after the action of the channel

```
6.1.3.12 template<typename Derived1 , typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (
const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector< idx >
& ctrl, const std::vector< idx > & subsys, const std::vector< idx > & dims )
```

Applies the controlled-gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

See also

[qpp::Gates::CTRL\(\)](#)

Note

The dimension of the gate *A* must match the dimension of *subsys*. Also, all control subsystems in *ctrl* must have the same dimension.

Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>ctrl</i>	Control subsystem indexes
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>dims</i>	Dimensions of the multi-partite system

Returns

CTRL-A gate applied to the part *subsys* of *state*

6.1.3.13 `template<typename Derived1 , typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector< idx > & ctrl, const std::vector< idx > & subsys, idx d = 2)`

Applies the controlled-gate *A* to the part *subsys* of the multi-partite state vector or density matrix *state*.

See also

[qpp::Gates::CTRL\(\)](#)

Note

The dimension of the gate *A* must match the dimension of *subsys*

Parameters

<i>state</i>	Eigen expression
<i>A</i>	Eigen expression
<i>ctrl</i>	Control subsystem indexes
<i>subsys</i>	Subsystem indexes where the gate <i>A</i> is applied
<i>d</i>	Subsystem dimensions

Returns

CTRL-A gate applied to the part *subsys* of *state*

6.1.3.14 `template<typename Container > double qpp::avg (const std::vector< double > & prob, const Container & X)`

Average.

Parameters

<i>prob</i>	Real probability vector representing the probability distribution of <i>X</i>
-------------	---

Returns

Average of *X*

6.1.3.15 `cmat qpp::bloch2rho (const std::vector< double > & r) [inline]`

Computes the density matrix corresponding to the 3-dimensional real Bloch vector *r*.

See also

[qpp::rho2bloch\(\)](#)

Parameters

<i>r</i>	3-dimensional real vector
----------	---------------------------

Returns

Qubit density matrix

6.1.3.16 `std::vector<cmat> qpp::choi2kraus (const cmat & A) [inline]`

Orthogonal Kraus operators from Choi matrix.

See also

[qpp::kraus2choi\(\)](#)

Extracts a set of orthogonal (under Hilbert-Schmidt operator norm) Kraus operators from the Choi matrix A

Note

The Kraus operators satisfy $Tr(K_i^\dagger K_j) = \delta_{ij}$ for all $i \neq j$

Parameters

A	Choi matrix
-----	-------------

Returns

Set of orthogonal Kraus operators

6.1.3.17 `cmat qpp::choi2super (const cmat & A) [inline]`

Converts Choi matrix to superoperator matrix.

See also

[qpp::super2choi\(\)](#)

Parameters

A	Choi matrix
-----	-------------

Returns

Superoperator matrix

6.1.3.18 `template<typename Derived1 , typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::comm (const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B)`

Commutator.

See also

[qpp::anticomm\(\)](#)

Commutator $[A, B] = AB - BA$. Both A and B must be Eigen expressions over the same scalar field.

Parameters

A	Eigen expression
B	Eigen expression

Returns

Commutator $AB - BA$, as a dynamic matrix over the same scalar field as A

6.1.3.19 `template<typename T> std::vector<T> qpp::complement (std::vector< T > subsys, idx N)`

Constructs the complement of a subsystem vector.

Parameters

<i>subsys</i>	Subsystem vector
<i>N</i>	Total number of systems

Returns

The complement of *subsys* with respect to the set $\{0, 1, \dots, N - 1\}$

6.1.3.20 `std::vector<idx> qpp::compperm (const std::vector< idx > & perm, const std::vector< idx > & sigma)`
`[inline]`

Compose permutations.

Parameters

<i>perm</i>	Permutation
<i>sigma</i>	Permutation

Returns

Composition of the permutations $perm \circ sigma = perm(sigma)$

6.1.3.21 `template<typename Derived> double qpp::concurrence (const Eigen::MatrixBase< Derived > & A)`

Wootters concurrence of the bi-partite qubit mixed state *A*.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Wootters concurrence

6.1.3.22 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::conjugate (const Eigen::MatrixBase< Derived > & A)`

Complex conjugate.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Complex conjugate of *A*, as a dynamic matrix over the same scalar field as *A*

6.1.3.23 `double qpp::contfrac2x (const std::vector< int > & cf, idx n)` `[inline]`

Real representation of a simple continued fraction.

See also

[qpp::x2contfrac\(\)](#)

Parameters

<i>cf</i>	Integer vector containing the simple continued fraction expansion
<i>n</i>	Number of terms considered in the continued fraction expansion. If <i>n</i> is greater than the size of <i>cf</i> , then all terms in <i>cf</i> are considered.

Returns

Real representation of the simple continued fraction

6.1.3.24 `double qpp::contfrac2x (const std::vector< int > & cf) [inline]`

Real representation of a simple continued fraction.

See also

[qpp::x2contfrac\(\)](#)

Parameters

<i>cf</i>	Integer vector containing the simple continued fraction expansion
-----------	---

Returns

Real representation of the simple continued fraction

6.1.3.25 `template<typename Container > double qpp::cor (const dmat & probXY, const Container & X, const Container & Y)`

Correlation.

Parameters

<i>probXY</i>	Real matrix representing the joint probability distribution of <i>X</i> and <i>Y</i> in lexicographical order (<i>X</i> labels the rows, <i>Y</i> labels the columns)
<i>X</i>	Random variable values represented by an STL-like container
<i>Y</i>	Random variable values represented by an STL-like container

Returns

Correlation of *X* and *Y*

6.1.3.26 `template<typename Derived > cmat qpp::cosm (const Eigen::MatrixBase< Derived > & A)`

Matrix cos.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Matrix cosine of *A*

6.1.3.27 `template<typename Container > double qpp::cov (const dmat & probXY, const Container & X, const Container & Y)`

Covariance.

Parameters

<i>probXY</i>	Real matrix representing the joint probability distribution of <i>X</i> and <i>Y</i> in lexicographical order (<i>X</i> labels the rows, <i>Y</i> labels the columns)
<i>X</i>	Random variable values represented by an STL-like container
<i>Y</i>	Random variable values represented by an STL-like container

Returns

Covariance of *X* and *Y*

6.1.3.28 `template<typename OutputScalar, typename Derived> dyn_mat<OutputScalar> qpp::cwise (const Eigen::MatrixBase< Derived> & A, OutputScalar (*)(const typename Derived::Scalar &) f)`

Functor.

Parameters

<i>A</i>	Eigen expression
<i>f</i>	Pointer-to-function from scalars of <i>A</i> to <i>OutputScalar</i>

Returns

Component-wise $f(A)$, as a dynamic matrix over the *OutputScalar* scalar field

6.1.3.29 `template<typename Derived> Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived> & A)`

Determinant.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Determinant of *A*, as a scalar over the same scalar field as *A*. Returns $\pm\infty$ when the determinant overflows/underflows.

6.1.3.30 `template<typename T> dyn_mat<typename T::Scalar> qpp::dirsum (const T & head)`

Direct sum.

See also

[qpp::dirsumpow\(\)](#)

Used to stop the recursion for the variadic template version of [qpp::dirsum\(\)](#)

Parameters

<i>head</i>	Eigen expression
-------------	------------------

Returns

Its argument *head*

6.1.3.31 `template<typename T, typename... Args> dyn_mat<typename T::Scalar> qpp::dirsum (const T & head, const Args &... tail)`

Direct sum.

See also

[qpp::dirsumpow\(\)](#)

Parameters

<i>head</i>	Eigen expression
<i>tail</i>	Variadic Eigen expression (zero or more parameters)

Returns

Direct sum of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.32 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::dirsum (const std::vector< Derived > & As)`

Direct sum.

See also

[qpp::dirsumpow\(\)](#)

Parameters

<i>As</i>	std::vector of Eigen expressions
-----------	----------------------------------

Returns

Direct sum of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.33 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::dirsum (const std::initializer_list< Derived > & As)`

Direct sum.

See also

[qpp::dirsumpow\(\)](#)

Parameters

<i>As</i>	std::initializer_list of Eigen expressions, such as { <i>A1</i> , <i>A2</i> , ... , <i>Ak</i> }
-----------	---

Returns

Direct sum of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.34 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::dirsumpow (const Eigen::MatrixBase< Derived > & A, idx n)`

Direct sum power.

See also

[qpp::dirsum\(\)](#)

Parameters

A	Eigen expression
n	Non-negative integer

Returns

Direct sum of A with itself n times $A^{\oplus n}$, as a dynamic matrix over the same scalar field as A

6.1.3.35 `template<typename Derived > internal::IOManipEigen qpp::disp (const Eigen::MatrixBase< Derived > & A, double chop = qpp::chop)`

Eigen expression ostream manipulator.

Parameters

A	Eigen expression
$chop$	Set to zero the elements smaller in absolute value than $chop$

Returns

Instance of `qpp::internal::internal::IOManipEigen`

6.1.3.36 `internal::IOManipEigen qpp::disp (cplx z, double chop = qpp::chop) [inline]`

Complex number ostream manipulator.

Parameters

z	Complex number (or any other type implicitly cast-able to <code>std::complex<double></code>)
$chop$	Set to zero the elements smaller in absolute value than $chop$

Returns

Instance of `qpp::internal::internal::IOManipEigen`

6.1.3.37 `template<typename InputIterator > internal::IOManipRange<InputIterator> qpp::disp (InputIterator first, InputIterator last, const std::string & separator, const std::string & start = " [", const std::string & end = "] ")`

Range ostream manipulator.

Parameters

<i>first</i>	Iterator to the first element of the range
<i>last</i>	Iterator to the last element of the range
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking

Returns

Instance of `qpp::internal::internal::IOManipRange`

6.1.3.38 `template<typename Container > internal::IOManipRange<typename Container::const_iterator> qpp::disp (const Container & c, const std::string & separator, const std::string & start = " [", const std::string & end = "] ")`

Standard container ostream manipulator. The container must support `std::begin()`, `std::end()` and forward iteration.

Parameters

<i>c</i>	Container
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking

Returns

Instance of `qpp::internal::internal::IOManipRange`

6.1.3.39 `template<typename PointerType > internal::IOManipPointer<PointerType> qpp::disp (const PointerType * p, idx n, const std::string & separator, const std::string & start = " [", const std::string & end = "] ")`

C-style pointer ostream manipulator.

Parameters

<i>p</i>	Pointer to the first element
<i>n</i>	Number of elements to be displayed
<i>separator</i>	Separator
<i>start</i>	Left marking
<i>end</i>	Right marking

Returns

Instance of `qpp::internal::internal::IOManipPointer`

6.1.3.40 `template<typename Derived > std::pair<dyn_col_vect < cplx>, cmat> qpp::eig (const Eigen::MatrixBase< Derived > & A)`

Full eigen decomposition.

See also

[qpp::heig\(\)](#)

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Pair of: 1. Eigenvalues of *A*, as a complex dynamic column vector, and 2. Eigenvectors of *A*, as columns of a complex dynamic matrix

6.1.3.41 `template<typename Derived> double qpp::entanglement (const Eigen::MatrixBase< Derived> & A, const std::vector< idx> & dims)`

Entanglement of the bi-partite pure state *A*.

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

See also

[qpp::entropy\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

Returns

Entanglement, with the logarithm in base 2

6.1.3.42 `template<typename Derived> double qpp::entropy (const Eigen::MatrixBase< Derived> & A)`

von-Neumann entropy of the density matrix *A*

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

von-Neumann entropy, with the logarithm in base 2

6.1.3.43 `double qpp::entropy (const std::vector< double> & prob) [inline]`

Shannon entropy of the probability distribution *prob*.

Parameters

<i>prob</i>	Real probability vector
-------------	-------------------------

Returns

Shannon entropy, with the logarithm in base 2

6.1.3.44 `template<typename Derived> dyn_col_vect<cplx> qpp::evals (const Eigen::MatrixBase< Derived> & A)`

Eigenvalues.

See also

[qpp::hevals\(\)](#)

Parameters

A	Eigen expression
-----	------------------

Returns

Eigenvalues of A , as a complex dynamic column vector

6.1.3.45 `template<typename Derived> cmat qpp::evecs (const Eigen::MatrixBase< Derived> & A)`

Eigenvectors.

See also

[qpp::hevecs\(\)](#)

Parameters

A	Eigen expression
-----	------------------

Returns

Eigenvectors of A , as columns of a complex dynamic matrix

6.1.3.46 `template<typename Derived> cmat qpp::expm (const Eigen::MatrixBase< Derived> & A)`

Matrix exponential.

Parameters

A	Eigen expression
-----	------------------

Returns

Matrix exponential of A

6.1.3.47 `std::vector<ubigint> qpp::factors (ubigint n) [inline]`

Prime factor decomposition.

Note

Runs in $\mathcal{O}(\sqrt{n})$ time complexity

Parameters

n	Integer strictly greater than 1
-----	---------------------------------

Returns

Integer vector containing the factors

6.1.3.48 `template<typename Derived> cmat qpp::funm (const Eigen::MatrixBase< Derived> & A, cplx(*) (const cplx &) f)`

Functional calculus $f(A)$

Parameters

A	Eigen expression
f	Pointer-to-function from complex to complex

Returns

$f(A)$

6.1.3.49 `ubigint qpp::gcd (ubigint m , ubigint n) [inline]`

Greatest common divisor of two non-negative integers.

See also

[qpp::lcm\(\)](#)

Parameters

m	Non-negative integer
n	Non-negative integer

Returns

Greatest common divisor of m and n

6.1.3.50 `ubigint qpp::gcd (const std::vector< ubigint> & ns) [inline]`

Greatest common divisor of a list of non-negative integers.

See also

[qpp::lcm\(\)](#)

Parameters

ns	List of non-negative integers
------	-------------------------------

Returns

Greatest common divisor of all numbers in ns

6.1.3.51 `template<typename Derived > double qpp::gconcurrency (const Eigen::MatrixBase< Derived > & A)`

G-concurrency of the bi-partite pure state A .

Note

Both local dimensions must be equal

Uses [qpp::logdet\(\)](#) to avoid overflows

See also

[qpp::logdet\(\)](#)

Parameters

A	Eigen expression
-----	------------------

Returns

G-concurrency

6.1.3.52 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::grams (const std::vector< Derived > & Vs)`

Gram-Schmidt orthogonalization.

Parameters

Vs	<code>std::vector</code> of Eigen expressions as column vectors
------	---

Returns

Gram-Schmidt vectors of Vs as columns of a dynamic matrix over the same scalar field as its arguments

6.1.3.53 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::grams (const std::initializer_list< Derived > & Vs)`

Gram-Schmidt orthogonalization.

Parameters

Vs	<code>std::initializer_list</code> of Eigen expressions as column vectors
------	---

Returns

Gram-Schmidt vectors of Vs as columns of a dynamic matrix over the same scalar field as its arguments

6.1.3.54 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::grams (const Eigen::MatrixBase< Derived > & A)`

Gram-Schmidt orthogonalization.

Parameters

A	Eigen expression, the input vectors are the columns of A
-----	--

Returns

Gram-Schmidt vectors of the columns of A , as columns of a dynamic matrix over the same scalar field as A

6.1.3.55 `template<typename Derived > std::pair<dyn_col_vect < double>, cmat> qpp::heig (const Eigen::MatrixBase< Derived > & A)`

Full eigen decomposition of Hermitian expression.

See also

[qpp::eig\(\)](#)

Parameters

A	Eigen expression
-----	------------------

Returns

Pair of: 1. Eigenvalues of A , as a real dynamic column vector, and 2. Eigenvectors of A , as columns of a complex dynamic matrix

6.1.3.56 `template<typename Derived > dyn_col_vect<double> qpp::hevals (const Eigen::MatrixBase< Derived > & A)`

Hermitian eigenvalues.

See also

[qpp::evals\(\)](#)

Parameters

A	Eigen expression
-----	------------------

Returns

Eigenvalues of Hermitian A , as a real dynamic column vector

6.1.3.57 `template<typename Derived > cmat qpp::hevects (const Eigen::MatrixBase< Derived > & A)`

Hermitian eigenvectors.

See also

[qpp::evects\(\)](#)

Parameters

A	Eigen expression
-----	------------------

Returns

Eigenvectors of Hermitian A , as columns of a complex matrix

6.1.3.58 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::inverse (const Eigen::MatrixBase<Derived> & A)`

Inverse.

Parameters

A	Eigen expression
-----	------------------

Returns

Inverse of A , as a dynamic matrix over the same scalar field as A

6.1.3.59 `std::vector<idx> qpp::invperm (const std::vector< idx > & perm) [inline]`

Inverse permutation.

Parameters

$perm$	Permutation
--------	-------------

Returns

Inverse of the permutation $perm$

6.1.3.60 `template<typename Derived> dyn_col_vect<typename Derived::Scalar> qpp::ip (const Eigen::MatrixBase<Derived> & phi, const Eigen::MatrixBase<Derived> & psi, const std::vector< idx > & subsys, const std::vector< idx > & dims)`

Generalized inner product.

Parameters

phi	Column vector Eigen expression
psi	Column vector Eigen expression
$subsys$	Subsystem indexes over which phi is defined
$dims$	Dimensions of the multi-partite system

Returns

The inner product $\langle \phi_{subsys} | \psi \rangle$, as a scalar or column vector over the remaining Hilbert space

6.1.3.61 `template<typename Derived> dyn_col_vect<typename Derived::Scalar> qpp::ip (const Eigen::MatrixBase<Derived> & phi, const Eigen::MatrixBase<Derived> & psi, const std::vector< idx > & subsys, idx d = 2)`

Generalized inner product.

Parameters

<i>phi</i>	Column vector Eigen expression
<i>psi</i>	Column vector Eigen expression
<i>subsys</i>	Subsystem indexes over which <i>phi</i> is defined
<i>d</i>	Subsystem dimensions

Returns

The inner product $\langle \phi_{subsys} | \psi \rangle$, as a scalar or column vector over the remaining Hilbert space

6.1.3.62 `bool qpp::isprime (ubigint n) [inline]`

Primality test.

Note

Runs in $\mathcal{O}(\sqrt{n})$ time complexity

Parameters

<i>n</i>	Integer strictly greater than 1
----------	---------------------------------

Returns

True if the number is prime, false otherwise

6.1.3.63 `cmat qpp::kraus2choi (const std::vector< cmat > & Ks) [inline]`

Choi matrix.

See also

[qpp::choi2kraus\(\)](#)

Constructs the Choi matrix of the channel specified by the set of Kraus operators *Ks* in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

Note

The superoperator matrix *S* and the Choi matrix *C* are related by $S_{ab,mn} = C_{ma,nb}$

Parameters

<i>Ks</i>	Set of Kraus operators
-----------	------------------------

Returns

Choi matrix

6.1.3.64 `cmat qpp::kraus2super (const std::vector< cmat > & Ks) [inline]`

Superoperator matrix.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators *Ks* in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

Parameters

<i>Ks</i>	Set of Kraus operators
-----------	------------------------

Returns

Superoperator matrix

6.1.3.65 `template<typename T> dyn_mat<typename T::Scalar> qpp::kron (const T & head)`

Kronecker product.

See also

[qpp::kronpow\(\)](#)

Used to stop the recursion for the variadic template version of [qpp::kron\(\)](#)

Parameters

<i>head</i>	Eigen expression
-------------	------------------

Returns

Its argument *head*

6.1.3.66 `template<typename T, typename... Args> dyn_mat<typename T::Scalar> qpp::kron (const T & head, const Args &... tail)`

Kronecker product.

See also

[qpp::kronpow\(\)](#)

Parameters

<i>head</i>	Eigen expression
<i>tail</i>	Variadic Eigen expression (zero or more parameters)

Returns

Kronecker product of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.67 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::kron (const std::vector< Derived > & As)`

Kronecker product.

See also

[qpp::kronpow\(\)](#)

Parameters

<i>As</i>	std::vector of Eigen expressions
-----------	----------------------------------

Returns

Kronecker product of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.68 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::kron (const std::initializer_list<Derived > & As)`

Kronecker product.

See also

[qpp::kronpow\(\)](#)

Parameters

<i>As</i>	std::initializer_list of Eigen expressions, such as { <i>A1</i> , <i>A2</i> , ... , <i>Ak</i> }
-----------	---

Returns

Kronecker product of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.69 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::kronpow (const Eigen::MatrixBase<Derived > & A, idx n)`

Kronecker power.

See also

[qpp::kron\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>n</i>	Non-negative integer

Returns

Kronecker product of *A* with itself *n* times $A^{\otimes n}$, as a dynamic matrix over the same scalar field as *A*

6.1.3.70 `ubigint qpp::lcm (ubigint m, ubigint n) [inline]`

Least common multiple of two positive integers.

See also

[qpp::gcd\(\)](#)

Parameters

m	Positive integer
n	Positive integer

Returns

Least common multiple of m and n

6.1.3.71 `ubigint qpp::lcm (const std::vector< ubigint > & ns) [inline]`

Least common multiple of a list of positive integers.

See also

[qpp::gcd\(\)](#)

Parameters

ns	List of positive integers
------	---------------------------

Returns

Least common multiple of all numbers in ns

6.1.3.72 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::load (const std::string & fname)`

Loads Eigen matrix from a binary file (internal format) in double precision.

See also

[qpp::save\(\)](#)

The template parameter cannot be automatically deduced and must be explicitly provided, depending on the scalar field of the matrix that is being loaded.

Example:

```
// loads a previously saved Eigen dynamic complex matrix from "input.bin"
auto mat = load<cmat>("input.bin");
```

Parameters

A	Eigen expression
$fname$	Output file name

6.1.3.73 `template<typename Derived> Derived qpp::loadMATLABmatrix (const std::string & mat_file, const std::string & var_name)`

Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.

See also

[qpp::saveMATLABmatrix\(\)](#)

This is the generic version that always throws `qpp::Exception::Type::UNDEFINED_TYPE`. It is specialized only for `qpp::dmat` and `qpp::cmat` (the only matrix types that can be loaded)

6.1.3.74 `template<> dmat qpp::loadMATLABmatrix (const std::string & mat_file, const std::string & var_name)`
`[inline]`

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))

See also

[qpp::saveMATLABmatrix\(\)](#)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen dynamic double matrix
// from the MATLAB file "input.mat"
auto mat = loadMATLABmatrix<dmat>("input.mat");
```

Note

If *var_name* is a complex matrix, only the real part is loaded

Parameters

<i>mat_file</i>	MATALB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be loaded

Returns

Eigen double dynamic matrix ([qpp::dmat](#))

6.1.3.75 `template<> cmat qpp::loadMATLABmatrix (const std::string & mat_file, const std::string & var_name)`
`[inline]`

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))

See also

[qpp::saveMATLABmatrix\(\)](#)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen dynamic complex matrix
// from the MATLAB file "input.mat"
auto mat = loadMATLABmatrix<cmat>("input.mat");
```

Parameters

<i>mat_file</i>	MATALB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be loaded

Returns

Eigen complex dynamic matrix ([qpp::cmat](#))

6.1.3.76 `template<typename Derived > Derived::Scalar qpp::logdet (const Eigen::MatrixBase< Derived > & A)`

Logarithm of the determinant.

Useful when the determinant overflows/underflows

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Logarithm of the determinant of A , as a scalar over the same scalar field as A

6.1.3.77 `template<typename Derived> cmat qpp::logm (const Eigen::MatrixBase< Derived> & A)`

Matrix logarithm.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Matrix logarithm of A

6.1.3.78 `template<typename Derived> double qpp::lognegativity (const Eigen::MatrixBase< Derived> & A, const std::vector< idx> & dims)`

Logarithmic negativity of the bi-partite mixed state A .

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

Returns

Logarithmic negativity, with the logarithm in base 2

6.1.3.79 `std::vector<double> qpp::marginalX (const dmat & probXY) [inline]`

Marginal distribution.

Parameters

<i>probXY</i>	Real matrix representing the joint probability distribution of X and Y in lexicographical order (X labels the rows, Y labels the columns)
---------------	--

Returns

Real vector consisting of the marginal distribution of X

6.1.3.80 `std::vector<double> qpp::marginalY (const dmat & probXY) [inline]`

Marginal distribution.

Parameters

<i>probXY</i>	Real matrix representing the joint probability distribution of X and Y in lexicographical order (X labels the rows, Y labels the columns)
---------------	--

Returns

Real vector consisting of the marginal distribution of Y

6.1.3.81 `template<typename Derived> std::tuple<idx, std::vector<double>, std::vector<cmat>> qpp::measure (const Eigen::MatrixBase< Derived> & A, const std::vector< cmat> & Ks)`

Measures the state A using the set of Kraus operators Ks .

Parameters

A	Eigen expression
Ks	Set of Kraus operators

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.82 `template<typename Derived> std::tuple<idx, std::vector<double>, std::vector<cmat>> qpp::measure (const Eigen::MatrixBase< Derived> & A, const std::initializer_list< cmat> & Ks)`

Measures the state A using the set of Kraus operators Ks .

Parameters

A	Eigen expression
Ks	Set of Kraus operators

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.83 `template<typename Derived> std::tuple<idx, std::vector<double>, std::vector<cmat>> qpp::measure (const Eigen::MatrixBase< Derived> & A, const cmat & U)`

Measures the state A in the orthonormal basis specified by the unitary matrix U .

Parameters

A	Eigen expression
U	Unitary matrix whose columns represent the measurement basis vectors

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.84 `template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const std::vector< cmat > & Ks, const std::vector< idx > & subsys, const std::vector< idx > & dims)`

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
<i>dims</i>	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.85 `template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const std::initializer_list< cmat > & Ks, const std::vector< idx > & subsys, const std::vector< idx > & dims)`

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
<i>dims</i>	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.86 `template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const std::vector< cmat > & Ks, const std::vector< idx > & subsys, idx d = 2)`

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
<i>d</i>	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.87 `template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const std::initializer_list< cmat > & Ks, const std::vector< idx > & subsys, idx d = 2)`

Measures the part *subsys* of the multi-partite state vector or density matrix *A* using the set of Kraus operators *Ks*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>Ks</i>	Set of Kraus operators
<i>subsys</i>	Subsystem indexes that are measured
<i>d</i>	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.88 `template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const cmat & V, const std::vector< idx > & subsys, const std::vector< idx > & dims)`

Measures the part *subsys* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 POVM specified by the matrix *V*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of *V* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>V</i>	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 POVM
<i>subsys</i>	Subsystem indexes that are measured
<i>dims</i>	Dimensions of the multi-partite system

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.89 `template<typename Derived > std::tuple<idx, std::vector<double>, std::vector<cmat> > qpp::measure (const Eigen::MatrixBase< Derived > & A, const cmat & V, const std::vector< idx > & subsys, idx d = 2)`

Measures the part *subsys* of the multi-partite state vector or density matrix *A* in the orthonormal basis or rank-1 POVM specified by the matrix *V*.

See also

[qpp::measure_seq\(\)](#)

Note

The dimension of *V* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Parameters

<i>A</i>	Eigen expression
<i>V</i>	Matrix whose columns represent the measurement basis vectors or the bra parts of the rank-1 POVM
<i>subsys</i>	Subsystem indexes that are measured
<i>d</i>	Subsystem dimensions

Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.90 `template<typename Derived > std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (const Eigen::MatrixBase< Derived > & A, std::vector< idx > subsys, std::vector< idx > dims)`

Sequentially measures the part *subsys* of the multi-partite state vector or density matrix *A* in the computational basis.

See also

[qpp::measure\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes that are measured
<i>dims</i>	Dimensions of the multi-partite system

Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *subsys*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.91 `template<typename Derived > std::tuple<std::vector<idx>, double, cmat> qpp::measure_seq (const Eigen::MatrixBase< Derived > & A, std::vector< idx > subsys, idx d = 2)`

Sequentially measures the part *subsys* of the multi-partite state vector or density matrix *A* in the computational basis.

See also

[qpp::measure\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes that are measured
<i>d</i>	Subsystem dimensions

Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *subsys*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.92 `ket qpp::mket (const std::vector< idx > & mask, const std::vector< idx > & dims) [inline]`

Multi-partite qudit ket.

Constructs the multi-partite qudit ket $|mask\rangle$, where *mask* is a `std::vector` of non-negative integers. Each element in *mask* has to be smaller than the corresponding element in *dims*.

Parameters

<i>mask</i>	std::vector of non-negative integers
<i>dims</i>	Dimensions of the multi-partite system

Returns

Multi-partite qudit state vector, as a complex dynamic column vector

6.1.3.93 `ket qpp::mket (const std::vector< idx > & mask, idx d = 2)` `[inline]`

Multi-partite qudit ket.

Constructs the multi-partite qudit ket $|\text{mask}\rangle$, all subsystem having equal dimension d . $mask$ is a std::vector of non-negative integers, and each element in $mask$ has to be strictly smaller than d .

Parameters

<i>mask</i>	std::vector of non-negative integers
<i>d</i>	Subsystem dimensions

Returns

Multi-partite qudit state vector, as a complex dynamic column vector

6.1.3.94 `ubigint qpp::modpow (ubigint a, ubigint n, ubigint p)` `[inline]`

Integer power modulo p.

Computes $a^n \bmod p$

Parameters

<i>a</i>	Non-negative integer
<i>n</i>	Non-negative integer
<i>p</i>	Strictly positive integer

Returns

$a^n \bmod p$

6.1.3.95 `cmat qpp::mprj (const std::vector< idx > & mask, const std::vector< idx > & dims)` `[inline]`

Projector onto multi-partite qudit ket.

Constructs the projector onto the multi-partite qudit ket $|\text{mask}\rangle$, where $mask$ is a std::vector of non-negative integers. Each element in $mask$ has to be smaller than the corresponding element in $dims$.

Parameters

<i>mask</i>	std::vector of non-negative integers
<i>dims</i>	Dimensions of the multi-partite system

Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

6.1.3.96 `cmat qpp::mprj (const std::vector< idx > & mask, idx d = 2) [inline]`

Projector onto multi-partite qudit ket.

Constructs the projector onto the multi-partite qudit ket $|\text{mask}\rangle$, all subsystem having equal dimension d . mask is a `std::vector` of non-negative integers, and each element in mask has to be strictly smaller than d .

Parameters

<i>mask</i>	std::vector of non-negative integers
<i>d</i>	Subsystem dimensions

Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

6.1.3.97 `idx qpp::multiidx2n (const std::vector< idx > & midx, const std::vector< idx > & dims)` `[inline]`

Multi-index to non-negative integer index.

See also

[qpp::n2multiidx\(\)](#)

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

Parameters

<i>midx</i>	Multi-index
<i>dims</i>	Dimensions of the multi-partite system

Returns

Non-negative integer index

6.1.3.98 `std::vector<idx> qpp::n2multiidx (idx n, const std::vector< idx > & dims)` `[inline]`

Non-negative integer index to multi-index.

See also

[qpp::multiidx2n\(\)](#)

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

Parameters

<i>n</i>	Non-negative integer index
<i>dims</i>	Dimensions of the multi-partite system

Returns

Multi-index of the same size as *dims*

6.1.3.99 `template<typename Derived > double qpp::negativity (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & dims)`

Negativity of the bi-partite mixed state *A*.

Parameters

A	Eigen expression
$dims$	Dimensions of the bi-partite system

Returns

Negativity

6.1.3.100 `template<typename Derived> double qpp::norm (const Eigen::MatrixBase< Derived> & A)`

Frobenius norm.

Parameters

A	Eigen expression
-----	------------------

Returns

Frobenius norm of A

6.1.3.101 `cplx qpp::omega (idx D) [inline]`

D-th root of unity.

Parameters

D	Non-negative integer
-----	----------------------

Returns

D-th root of unity $\exp(2\pi i/D)$

6.1.3.102 `constexpr cplx qpp::operator""_i (unsigned long long int x) [inline], [noexcept]`

User-defined literal for complex $i = \sqrt{-1}$ (integer overload)

Example:

```
auto z = 4_i; // type of z is std::complex<double>
```

6.1.3.103 `constexpr cplx qpp::operator""_i (long double x) [inline], [noexcept]`

User-defined literal for complex $i = \sqrt{-1}$ (real overload)

Example:

```
auto z = 4.5_i; // type of z is std::complex<double>
```

6.1.3.104 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::powm (const Eigen::MatrixBase< Derived> & A, idx n)`

Matrix power.

See also

[qpp::spectralpowm\(\)](#)Explicitly multiplies the matrix A with itself n times. By convention $A^0 = I$.

Parameters

A	Eigen expression
n	Non-negative integer

Returns

Matrix power A^n , as a dynamic matrix over the same scalar field as A

6.1.3.105 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::prj (const Eigen::MatrixBase< Derived > & V)`

Projector.

Normalized projector onto state vector

Parameters

V	Eigen expression
-----	------------------

Returns

Projector onto the state vector V , or the matrix *Zero* if V has norm zero (i.e. smaller than `qpp::eps`), as a dynamic matrix over the same scalar field as A

6.1.3.106 `template<typename Derived > Derived::Scalar qpp::prod (const Eigen::MatrixBase< Derived > & A)`

Element-wise product of A .

Parameters

A	Eigen expression
-----	------------------

Returns

Element-wise product of A , as a scalar over the same scalar field as A

6.1.3.107 `template<typename InputIterator > std::iterator_traits<InputIterator>::value_type qpp::prod (InputIterator first, InputIterator last)`

Element-wise product of an STL-like range.

Parameters

<i>first</i>	Iterator to the first element of the range
<i>last</i>	Iterator to the last element of the range

Returns

Element-wise product of the range, as a scalar over the same scalar field as the range

6.1.3.108 `template<typename Container > Container::value_type qpp::prod (const Container & c)`

Element-wise product of the elements of an STL-like container.

Parameters

<i>c</i>	STL-like container
----------	--------------------

Returns

Element-wise product of the elements of the container, as a scalar over the same scalar field as the container

6.1.3.109 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::ptrace (const Eigen::MatrixBase<Derived> & A, const std::vector< idx > & subsys, const std::vector< idx > & dims)`

Partial trace.

See also

[qpp::ptrace1\(\)](#), [qpp::ptrace2\(\)](#)

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes
<i>dims</i>	Dimensions of the multi-partite system

Returns

Partial trace $Tr_{subsys}(\cdot)$ over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.110 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::ptrace (const Eigen::MatrixBase<Derived> & A, const std::vector< idx > & subsys, idx d = 2)`

Partial trace.

See also

[qpp::ptrace1\(\)](#), [qpp::ptrace2\(\)](#)

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystem indexes
<i>d</i>	Subsystem dimensions

Returns

Partial trace $Tr_{subsys}(\cdot)$ over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as *A*

6.1.3.111 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::ptrace1 (const Eigen::MatrixBase<Derived> & A, const std::vector< idx > & dims)`

Partial trace.

See also

[qpp::ptrace2\(\)](#)

Partial trace over the first subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
$dims$	Dimensions of the bi-partite system (must be a <code>std::vector</code> with 2 elements)

Returns

Partial trace $Tr_A(\cdot)$ over the first subsystem A in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as A

6.1.3.112 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::ptrace2 (const Eigen::MatrixBase<Derived> & A, const std::vector< idx > & dims)`

Partial trace.

See also

[qpp::ptrace1\(\)](#)

Partial trace over the second subsystem of bi-partite state vector or density matrix

Parameters

A	Eigen expression
$dims$	Dimensions of the bi-partite system (must be a <code>std::vector</code> with 2 elements)

Returns

Partial trace $Tr_B(\cdot)$ over the second subsystem B in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field as A

6.1.3.113 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::ptrtranspose (const Eigen::MatrixBase<Derived> & A, const std::vector< idx > & subsys, const std::vector< idx > & dims)`

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

Parameters

A	Eigen expression
$subsys$	Subsystem indexes
$dims$	Dimensions of the multi-partite system

Returns

Partial transpose $(\cdot)^{T_{subsys}}$ over the subsystems $subsys$ in a multi-partite system, as a dynamic matrix over the same scalar field as A

6.1.3.114 `template<typename Derived> dyn_mat<typename Derived::Scalar> qpp::ptrtranspose (const Eigen::MatrixBase<Derived> & A, const std::vector< idx > & subsys, idx d = 2)`

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

Parameters

A	Eigen expression
$subsys$	Subsystem indexes
d	Subsystem dimensions

Returns

Partial transpose $(\cdot)^{T_{subsys}}$ over the subsystems $subsys$ in a multi-partite system, as a dynamic matrix over the same scalar field as A

6.1.3.115 `template<typename Derived > double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & subsysA, const std::vector< idx > & subsysB, const std::vector< idx > & dims)`

Quantum mutual information between 2 subsystems of a composite system.

Parameters

A	Eigen expression
$subsysA$	Indexes of the first subsystem
$subsysB$	Indexes of the second subsystem
$dims$	Dimensions of the multi-partite system

Returns

Mutual information between the 2 subsystems

6.1.3.116 `template<typename Derived > double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & subsysA, const std::vector< idx > & subsysB, idx d = 2)`

Quantum mutual information between 2 subsystems of a composite system.

Parameters

A	Eigen expression
$subsysA$	Indexes of the first subsystem
$subsysB$	Indexes of the second subsystem
d	Subsystem dimensions

Returns

Mutual information between the 2 subsystems

6.1.3.117 `double qpp::rand (double a = 0, double b = 1) [inline]`

Generates a random real number uniformly distributed in the interval [a, b)

Parameters

a	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

Returns

Random real number (double) uniformly distributed in the interval [a, b)

6.1.3.118 `bigint qpp::rand (bigint a = std::numeric_limits<bigint>::min(), bigint b = std::numeric_limits<bigint>::max()) [inline]`

Generates a random big integer uniformly distributed in the interval [a, b].

Parameters

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, belongs to it

Returns

Random big integer uniformly distributed in the interval [a, b]

6.1.3.119 `ubigint qpp::rand (ubigint a = std::numeric_limits<ubigint>::min(), ubigint b = std::numeric_limits<ubigint>::max()) [inline]`

Generates a random non-negative big integer uniformly distributed in the interval [a, b].

Parameters

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, belongs to it

Returns

Random non-negative big integer uniformly distributed in the interval [a, b]

6.1.3.120 `template<typename Derived > Derived qpp::rand (idx rows, idx cols, double a = 0, double b = 1)`

Generates a random matrix with entries uniformly distributed in the interval [a, b)

If complex, then both real and imaginary parts are uniformly distributed in [a, b)

This is the generic version that always throws `qpp::Exception::Type::UNDEFINED_TYPE`. It is specialized only for `qpp::dmat` and `qpp::cmat`

6.1.3.121 `template<> dmat qpp::rand (idx rows, idx cols, double a, double b) [inline]`

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (`qpp::dmat`)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries uniformly distributed in [-1,1)
auto mat = rand<dmat>(3, 3, -1, 1);
```

Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

Returns

Random real matrix

6.1.3.122 `template<> cmat qpp::rand (idx rows, idx cols, double a, double b) [inline]`

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices ([qpp::cmat](#))

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) uniformly distributed in [-1,1)
auto mat = rand<cmat>(3, 3, -1, 1);
```

Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, does not belong to it

Returns

Random complex matrix

6.1.3.123 `cmat qpp::randH (idx D) [inline]`

Generates a random Hermitian matrix.

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Random Hermitian matrix

6.1.3.124 `idx qpp::randidx (idx a = std::numeric_limits<idx>::min(), idx b = std::numeric_limits<idx>::max()) [inline]`

Generates a random index (idx) uniformly distributed in the interval [a, b].

Parameters

<i>a</i>	Beginning of the interval, belongs to it
<i>b</i>	End of the interval, belongs to it

Returns

Random index (idx) uniformly distributed in the interval [a, b]

6.1.3.125 `ket qpp::randket (idx D) [inline]`

Generates a random normalized ket (pure state vector)

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Random normalized ket

6.1.3.126 `std::vector<cmat> qpp::randkraus (idx N, idx D)` `[inline]`

Generates a set of random Kraus operators.

Note

The set of Kraus operators satisfy the closure condition $\sum_i K_i^\dagger K_i = I$

Parameters

<i>N</i>	Number of Kraus operators
<i>D</i>	Dimension of the Hilbert space

Returns

Set of *N* Kraus operators satisfying the closure condition

6.1.3.127 `template<typename Derived > Derived qpp::randn (idx rows, idx cols, double mean = 0, double sigma = 1)`

Generates a random matrix with entries normally distributed in N(mean, sigma)

If complex, then both real and imaginary parts are normally distributed in N(mean, sigma)

This is the generic version that always throws `qpp::Exception::Type::UNDEFINED_TYPE`. It is specialized only for `qpp::dmat` and `qpp::cmat`

6.1.3.128 `template<> dmat qpp::randn (idx rows, idx cols, double mean, double sigma)` `[inline]`

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (`qpp::dmat`)

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXd,
// with entries normally distributed in N(0,2)
auto mat = randn<dmat>(3, 3, 0, 2);
```

Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

Returns

Random real matrix

6.1.3.129 `template<> cmat qpp::randn (idx rows, idx cols, double mean, double sigma) [inline]`

Generates a random complex matrix with entries (both real and imaginary) normally distributed in $N(\text{mean}, \text{sigma})$, specialization for complex matrices ([qpp::cmat](#))

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd,
// with entries (both real and imaginary) normally distributed in N(0,2)
auto mat = randn<cmat>(3, 3, 0, 2);
```

Parameters

<i>rows</i>	Number of rows of the random generated matrix
<i>cols</i>	Number of columns of the random generated matrix
<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

Returns

Random complex matrix

6.1.3.130 `double qpp::randn (double mean = 0, double sigma = 1) [inline]`

Generates a random real number (double) normally distributed in $N(\text{mean}, \text{sigma})$

Parameters

<i>mean</i>	Mean
<i>sigma</i>	Standard deviation

Returns

Random real number normally distributed in $N(\text{mean}, \text{sigma})$

6.1.3.131 `std::vector<idx> qpp::randperm (idx n) [inline]`

Generates a random uniformly distributed permutation.

Uses Knuth shuffle method (as implemented by `std::shuffle`), so that all permutations are equally probable

Parameters

<i>n</i>	Size of the permutation
----------	-------------------------

Returns

Random permutation of size *n*

6.1.3.132 `cmat qpp::randrho (idx D) [inline]`

Generates a random density matrix.

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Random density matrix

6.1.3.133 `cmat qpp::randU (idx D) [inline]`

Generates a random unitary matrix.

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Random unitary

6.1.3.134 `cmat qpp::randV (idx Din, idx Dout) [inline]`

Generates a random isometry matrix.

Parameters

<i>Din</i>	Size of the input Hilbert space
<i>Dout</i>	Size of the output Hilbert space

Returns

Random isometry matrix

6.1.3.135 `template<typename Derived > double qpp::renyi (const Eigen::MatrixBase< Derived > & A, double alpha)`

Renyi- α entropy of the density matrix *A*, for $\alpha \geq 0$.

Note

When $\alpha \rightarrow 1$ the Renyi entropy converges to the von-Neumann entropy, with the logarithm in base 2

Parameters

<i>A</i>	Eigen expression
<i>alpha</i>	Non-negative real number, use qpp::infy for $\alpha = \infty$

Returns

Renyi- α entropy, with the logarithm in base 2

6.1.3.136 `double qpp::renyi (const std::vector< double > & prob, double alpha) [inline]`

Renyi- α entropy of the probability distribution *prob*, for $\alpha \geq 0$.

Note

When $\alpha \rightarrow 1$ the Renyi entropy converges to the Shannon entropy, with the logarithm in base 2

Parameters

<i>prob</i>	Real probability vector
<i>alpha</i>	Non-negative real number, use qpp::infy for $\alpha = \infty$

Returns

Renyi- α entropy, with the logarithm in base 2

6.1.3.137 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::reshape (const Eigen::MatrixBase<Derived > & A, idx rows, idx cols)`

Reshape.

Uses column-major order when reshaping (same as MATLAB)

Parameters

<i>A</i>	Eigen expression
<i>rows</i>	Number of rows of the reshaped matrix
<i>cols</i>	Number of columns of the reshaped matrix

Returns

Reshaped matrix with *rows* rows and *cols* columns, as a dynamic matrix over the same scalar field as *A*

6.1.3.138 `template<typename Derived > std::vector<double> qpp::rho2bloch (const Eigen::MatrixBase<Derived > & A)`

Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix *A*.

See also

[qpp::bloch2rho\(\)](#)

Note

It is implicitly assumed that the density matrix is Hermitian

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

3-dimensional Bloch vector

6.1.3.139 `template<typename Derived > dyn_col_vect<typename Derived::Scalar> qpp::rho2pure (const Eigen::MatrixBase<Derived > & A)`

Finds the pure state representation of a matrix proportional to a projector onto a pure state.

Note

No purity check is done, the input state *A* must have rank one, otherwise the function returns the first non-zero eigenvector of *A*

Parameters

<i>A</i>	Eigen expression, assumed to be proportional to a projector onto a pure state, i.e. <i>A</i> is assumed to have rank one
----------	--

Returns

The unique non-zero eigenvector of *A*, as a dynamic column vector over the same scalar field as *A*

6.1.3.140 `template<typename Derived > void qpp::save (const Eigen::MatrixBase< Derived > & A, const std::string & fname)`

Saves Eigen expression to a binary file (internal format) in double precision.

See also

[qpp::load\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>fname</i>	Output file name

6.1.3.141 `template<typename Derived > void qpp::saveMATLABmatrix (const Eigen::MatrixBase< Derived > & A, const std::string & mat_file, const std::string & var_name, const std::string & mode)`

Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.

See also

[qpp::loadMATLABmatrix\(\)](#)

This is the generic version that always throws [qpp::Exception::Type::UNDEFINED_TYPE](#). It is specialized only for [qpp::dmat](#) and [qpp::cmat](#) (the only matrix types that can be saved)

6.1.3.142 `template<> void qpp::saveMATLABmatrix (const Eigen::MatrixBase< dmat > & A, const std::string & mat_file, const std::string & var_name, const std::string & mode) [inline]`

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))

See also

[qpp::loadMATLABmatrix\(\)](#)

Parameters

<i>A</i>	Eigen expression over the complex field
<i>mat_file</i>	MATLAB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be saved
<i>mode</i>	Saving mode (append, overwrite etc.), see MATLAB <i>matOpen()</i> documentation for details

6.1.3.143 `template<> void qpp::saveMATLABmatrix (const Eigen::MatrixBase< cmat > & A, const std::string & mat_file, const std::string & var_name, const std::string & mode) [inline]`

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))

See also

[qpp::loadMATLABmatrix\(\)](#)

Parameters

<i>A</i>	Eigen expression over the complex field
<i>mat_file</i>	MATLAB .mat file
<i>var_name</i>	Variable name in the .mat file representing the matrix to be saved
<i>mode</i>	Saving mode (append, overwrite etc.), see MATLAB <i>matOpen()</i> documentation for details

6.1.3.144 `template<typename Derived > double qpp::schatten (const Eigen::MatrixBase< Derived > &A, double p)`

Schatten matrix norm.

Parameters

<i>A</i>	Eigen expression
<i>p</i>	Real number, greater or equal to 1, use qpp::infy for $p = \infty$

Returns

Schatten- p matrix norm of A

6.1.3.145 `template<typename Derived > cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`

Schmidt basis on Alice side.

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

Returns

Unitary matrix U whose columns represent the Schmidt basis vectors on Alice side.

6.1.3.146 `template<typename Derived > cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`

Schmidt basis on Bob side.

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

Returns

Unitary matrix V whose columns represent the Schmidt basis vectors on Bob side.

6.1.3.147 `template<typename Derived > dyn_col_vect<double> qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`

Schmidt coefficients of the bi-partite pure state A .

Note

The sum of the squares of the Schmidt coefficients equals 1

See also

[qpp::schmidtprobs\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

Returns

Schmidt coefficients of *A*, as a real dynamic column vector

6.1.3.148 `template<typename Derived > std::vector<double> qpp::schmidtprobs (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & dims)`

Schmidt probabilities of the bi-partite pure state *A*.

Defined as the squares of the Schmidt coefficients. The sum of the Schmidt probabilities equals 1.

See also

[qpp::schmidtcoeffs\(\)](#)

Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of the bi-partite system

Returns

Real vector consisting of the Schmidt probabilities of *A*

6.1.3.149 `template<typename Container > double qpp::sigma (const std::vector< double > & prob, const Container & X)`

Standard deviation.

Parameters

<i>prob</i>	Real probability vector representing the probability distribution of <i>X</i>
<i>X</i>	Random variable values represented by an STL-like container

Returns

Standard deviation of *X*

6.1.3.150 `template<typename Derived > cmat qpp::sinm (const Eigen::MatrixBase< Derived > & A)`

Matrix sin.

Parameters

A	Eigen expression
-----	------------------

Returns

Matrix sine of A

6.1.3.151 `template<typename Derived> cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived> & A, const cplx z)`

Matrix power.

See also

[qpp::powm\(\)](#)

Uses the spectral decomposition of A to compute the matrix power. By convention $A^0 = I$.

Parameters

A	Eigen expression
z	Complex number

Returns

Matrix power A^z

6.1.3.152 `template<typename Derived> cmat qpp::sqrtm (const Eigen::MatrixBase< Derived> & A)`

Matrix square root.

Parameters

A	Eigen expression
-----	------------------

Returns

Matrix square root of A

6.1.3.153 `template<typename Derived> Derived::Scalar qpp::sum (const Eigen::MatrixBase< Derived> & A)`

Element-wise sum of A .

Parameters

A	Eigen expression
-----	------------------

Returns

Element-wise sum of A , as a scalar over the same scalar field as A

6.1.3.154 `template<typename InputIterator> std::iterator_traits<InputIterator>::value_type qpp::sum (InputIterator first, InputIterator last)`

Element-wise sum of an STL-like range.

Parameters

<i>first</i>	Iterator to the first element of the range
<i>last</i>	Iterator to the last element of the range

Returns

Element-wise sum of the range, as a scalar over the same scalar field as the range

6.1.3.155 `template<typename Container > Container::value_type qpp::sum (const Container & c)`

Element-wise sum of the elements of an STL-like container.

Parameters

<i>c</i>	STL-like container
----------	--------------------

Returns

Element-wise sum of the elements of the container, as a scalar over the same scalar field as the container

6.1.3.156 `cmat qpp::super2choi (const cmat & A) [inline]`

Converts superoperator matrix to Choi matrix.

See also

[qpp::choi2super\(\)](#)

Parameters

<i>A</i>	Superoperator matrix
----------	----------------------

Returns

Choi matrix

6.1.3.157 `template<typename Derived > dyn_col_vect<double> qpp::svals (const Eigen::MatrixBase< Derived > & A)`

Singular values.

Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Singular values of *A*, ordered in decreasing order, as a real dynamic column vector

6.1.3.158 `template<typename Derived > std::tuple<cmat, dyn_col_vect < double>, cmat> qpp::svd (const Eigen::MatrixBase< Derived > & A)`

Full singular value decomposition.

Parameters

A	Eigen expression
-----	------------------

Returns

Tuple of: 1. Left singular vectors of A , as columns of a complex dynamic matrix, 2. Singular values of A , ordered in decreasing order, as a real dynamic column vector, and 3. Right singular vectors of A , as columns of a complex dynamic matrix

6.1.3.159 `template<typename Derived > cmat qpp::svdU (const Eigen::MatrixBase< Derived > & A)`

Left singular vectors.

Parameters

A	Eigen expression
-----	------------------

Returns

Complex dynamic matrix, whose columns are the left singular vectors of A

6.1.3.160 `template<typename Derived > cmat qpp::svdV (const Eigen::MatrixBase< Derived > & A)`

Right singular vectors.

Parameters

A	Eigen expression
-----	------------------

Returns

Complex dynamic matrix, whose columns are the right singular vectors of A

6.1.3.161 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::syspermute (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & perm, const std::vector< idx > & dims)`

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit $perm[i]$ is permuted to the location i .

Parameters

A	Eigen expression
$perm$	Permutation
$dims$	Dimensions of the multi-partite system

Returns

Permuted system, as a dynamic matrix over the same scalar field as A

6.1.3.162 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::syspermute (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & perm, idx d = 2)`

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit $perm[i]$ is permuted to the location i .

Parameters

A	Eigen expression
$perm$	Permutation
d	Subsystem dimensions

Returns

Permuted system, as a dynamic matrix over the same scalar field as A

6.1.3.163 `template<typename Derived > Derived::Scalar qpp::trace (const Eigen::MatrixBase< Derived > & A)`

Trace.

Parameters

A	Eigen expression
-----	------------------

Returns

Trace of A , as a scalar over the same scalar field as A

6.1.3.164 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::transpose (const Eigen::MatrixBase< Derived > & A)`

Transpose.

Parameters

A	Eigen expression
-----	------------------

Returns

Transpose of A , as a dynamic matrix over the same scalar field as A

6.1.3.165 `template<typename Derived > double qpp::tsallis (const Eigen::MatrixBase< Derived > & A, double q)`

Tsallis- q entropy of the density matrix A , for $q \geq 0$.

Note

When $q \rightarrow 1$ the Tsallis entropy converges to the von-Neumann entropy, with the logarithm in base e

Parameters

A	Eigen expression
q	Non-negative real number

Returns

Tsallis- q entropy

6.1.3.166 `double qpp::tsallis (const std::vector< double > & prob, double q) [inline]`

Tsallis- q entropy of the probability distribution $prob$, for $q \geq 0$.

Note

When $q \rightarrow 1$ the Tsallis entropy converges to the Shannon entropy, with the logarithm in base e

Parameters

<i>prob</i>	Real probability vector
<i>q</i>	Non-negative real number

Returns

Tsallis- q entropy

6.1.3.167 `std::vector<double> qpp::uniform (idx N) [inline]`

Uniform probability distribution vector.

Parameters

N	Size of the alphabet
-----	----------------------

Returns

Real vector consisting of a uniform distribution of size N

6.1.3.168 `template<typename Container > double qpp::var (const std::vector< double > & prob, const Container & X)`

Variance.

Parameters

<i>prob</i>	Real probability vector representing the probability distribution of X
X	Random variable values represented by an STL-like container

Returns

Variance of X

6.1.3.169 `std::vector<int> qpp::x2contfrac (double x , idx n , idx cut = 1e5) [inline]`

Simple continued fraction expansion.

See also

[qpp::contfrac2x\(\)](#)

Parameters

x	Real number
n	Number of terms in the expansion
<i>cut</i>	Stop the expansion when the next term is greater than <i>cut</i>

Returns

Integer vector containing the simple continued fraction expansion of x . If there are m less than n terms in the expansion, a shorter vector with m components is returned.

6.1.4 Variable Documentation

6.1.4.1 `constexpr double qpp::chop = 1e-10`

Used in [qpp::disp\(\)](#) for setting to zero numbers that have their absolute value smaller than [qpp::chop](#).

6.1.4.2 `constexpr double qpp::ee = 2.718281828459045235360287471352662497`

Base of natural logarithm, e .

6.1.4.3 `constexpr double qpp::eps = 1e-12`

Used to decide whether a number or expression in double precision is zero or not.

Example:

```
if(std::abs(x) < qpp::eps) // x is zero
```

6.1.4.4 `constexpr double qpp::infy = std::numeric_limits<double>::infinity()`

Used to denote infinity in double precision.

6.1.4.5 `constexpr idx qpp::maxn = 64`

Maximum number of allowed qu(d)its (subsystems)

Used internally to allocate arrays on the stack (for speed reasons)

6.1.4.6 `constexpr double qpp::pi = 3.141592653589793238462643383279502884`

π

6.2 qpp::experimental Namespace Reference

Experimental/test functions/classes, do not use or modify.

6.2.1 Detailed Description

Experimental/test functions/classes, do not use or modify.

6.3 qpp::internal Namespace Reference

Internal utility functions, do not use/modify.

Classes

- class [IOManipEigen](#)
- class [IOManipPointer](#)
- class [IOManipRange](#)
- class [Singleton](#)

[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

Functions

- void [_n2multiidx](#) (idx n, idx numdims, const idx *dims, idx *result) noexcept
- idx [_multiidx2n](#) (const idx *midx, idx numdims, const idx *dims) noexcept
- template<typename Derived >
bool [_check_square_mat](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [_check_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [_check_rvector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [_check_cvector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename T >
bool [_check_nonzero_size](#) (const T &x) noexcept
- template<typename T1 , typename T2 >
bool [_check_matching_sizes](#) (const T1 &lhs, const T2 &rhs) noexcept
- bool [_check_dims](#) (const std::vector< idx > &dims)
- template<typename Derived >
bool [_check_dims_match_mat](#) (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [_check_dims_match_cvect](#) (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &V)
- template<typename Derived >
bool [_check_dims_match_rvect](#) (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &V)
- bool [_check_eq_dims](#) (const std::vector< idx > &dims, idx dim) noexcept
- bool [_check_subsys_match_dims](#) (const std::vector< idx > &subsys, const std::vector< idx > &dims)
- template<typename Derived >
bool [_check_qubit_matrix](#) (const Eigen::MatrixBase< Derived > &A) noexcept
- template<typename Derived >
bool [_check_qubit_cvector](#) (const Eigen::MatrixBase< Derived > &V) noexcept
- template<typename Derived >
bool [_check_qubit_rvector](#) (const Eigen::MatrixBase< Derived > &V) noexcept
- template<typename Derived >
bool [_check_qubit_vector](#) (const Eigen::MatrixBase< Derived > &V) noexcept
- bool [_check_perm](#) (const std::vector< idx > &perm)
- template<typename Derived1 , typename Derived2 >
[dyn_mat](#)< typename Derived1::Scalar > [_kron2](#) (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename Derived1 , typename Derived2 >
[dyn_mat](#)< typename Derived1::Scalar > [_dirsum2](#) (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename T >
void [variadic_vector_emplace](#) (std::vector< T > &)
- template<typename T , typename First , typename... Args>
void [variadic_vector_emplace](#) (std::vector< T > &v, First &&first, Args &&...args)

6.3.1 Detailed Description

Internal utility functions, do not use/modify.

6.3.2 Function Documentation

6.3.2.1 template<typename Derived > bool qpp::internal::_check_cvector (const Eigen::MatrixBase< Derived > & A)

6.3.2.2 bool qpp::internal::_check_dims (const std::vector< idx > & dims) [inline]

- 6.3.2.3 `template<typename Derived > bool qpp::internal::_check_dims_match_cvect (const std::vector< idx > & dims, const Eigen::MatrixBase< Derived > & V)`
- 6.3.2.4 `template<typename Derived > bool qpp::internal::_check_dims_match_mat (const std::vector< idx > & dims, const Eigen::MatrixBase< Derived > & A)`
- 6.3.2.5 `template<typename Derived > bool qpp::internal::_check_dims_match_rvect (const std::vector< idx > & dims, const Eigen::MatrixBase< Derived > & V)`
- 6.3.2.6 `bool qpp::internal::_check_eq_dims (const std::vector< idx > & dims, idx dim) [inline], [noexcept]`
- 6.3.2.7 `template<typename T1, typename T2 > bool qpp::internal::_check_matching_sizes (const T1 & lhs, const T2 & rhs) [noexcept]`
- 6.3.2.8 `template<typename T > bool qpp::internal::_check_nonzero_size (const T & x) [noexcept]`
- 6.3.2.9 `bool qpp::internal::_check_perm (const std::vector< idx > & perm) [inline]`
- 6.3.2.10 `template<typename Derived > bool qpp::internal::_check_qubit_cvector (const Eigen::MatrixBase< Derived > & V) [noexcept]`
- 6.3.2.11 `template<typename Derived > bool qpp::internal::_check_qubit_matrix (const Eigen::MatrixBase< Derived > & A) [noexcept]`
- 6.3.2.12 `template<typename Derived > bool qpp::internal::_check_qubit_rvector (const Eigen::MatrixBase< Derived > & V) [noexcept]`
- 6.3.2.13 `template<typename Derived > bool qpp::internal::_check_qubit_vector (const Eigen::MatrixBase< Derived > & V) [noexcept]`
- 6.3.2.14 `template<typename Derived > bool qpp::internal::_check_rvector (const Eigen::MatrixBase< Derived > & A)`
- 6.3.2.15 `template<typename Derived > bool qpp::internal::_check_square_mat (const Eigen::MatrixBase< Derived > & A)`
- 6.3.2.16 `bool qpp::internal::_check_subsys_match_dims (const std::vector< idx > & subsys, const std::vector< idx > & dims) [inline]`
- 6.3.2.17 `template<typename Derived > bool qpp::internal::_check_vector (const Eigen::MatrixBase< Derived > & A)`
- 6.3.2.18 `template<typename Derived1, typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::internal::_dirsum2 (const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B)`
- 6.3.2.19 `template<typename Derived1, typename Derived2 > dyn_mat<typename Derived1::Scalar> qpp::internal::_kron2 (const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B)`
- 6.3.2.20 `idx qpp::internal::_multiidx2n (const idx * midx, idx numdims, const idx * dims) [inline], [noexcept]`
- 6.3.2.21 `void qpp::internal::_n2multiidx (idx n, idx numdims, const idx * dims, idx * result) [inline], [noexcept]`
- 6.3.2.22 `template<typename T > void qpp::internal::variadic_vector_emplace (std::vector< T > &)`
- 6.3.2.23 `template<typename T, typename First, typename... Args> void qpp::internal::variadic_vector_emplace (std::vector< T > & v, First && first, Args &&... args)`

Chapter 7

Class Documentation

7.1 qpp::Codes Class Reference

const Singleton class that defines quantum error correcting codes

```
#include <classes/codes.h>
```

Inheritance diagram for qpp::Codes:



Collaboration diagram for qpp::Codes:



Public Types

- enum `Type` { `Type::FIVE_QUBIT` = 1, `Type::SEVEN_QUBIT_STEANE`, `Type::NINE_QUBIT_SHOR` }
Code types, add more codes here if needed.

Public Member Functions

- `ket codeword` (`Type` type, `idx` i) const
Returns the codeword of the specified code type.

Private Member Functions

- `Codes` ()
Default constructor.
- `~Codes` ()=default
Default destructor.

Friends

- class `internal::Singleton< const Codes >`

Additional Inherited Members

7.1.1 Detailed Description

const Singleton class that defines quantum error correcting codes

7.1.2 Member Enumeration Documentation

7.1.2.1 enum `qpp::Codes::Type` [strong]

Code types, add more codes here if needed.

See also

`qpp::Codes::codeword()`

Enumerator

`FIVE_QUBIT` [[5,1,3]] qubit code
`SEVEN_QUBIT_STEANE` [[7,1,3]] Steane qubit code
`NINE_QUBIT_SHOR` [[9,1,3]] Shor qubit code

7.1.3 Constructor & Destructor Documentation

7.1.3.1 `qpp::Codes::Codes ()` [inline],[private]

Default constructor.

7.1.3.2 `qpp::Codes::~~Codes ()` [private],[default]

Default destructor.

7.1.4 Member Function Documentation

7.1.4.1 `ket qpp::Codes::codeword (Type type, idx i) const` `[inline]`

Returns the codeword of the specified code type.

See also

[qpp::Codes::Type](#)

Parameters

<i>type</i>	Code type
<i>i</i>	Codeword index

Returns

i-th codeword of the code *type*

7.1.5 Friends And Related Function Documentation

7.1.5.1 `friend class internal::Singleton< const Codes >` `[friend]`

The documentation for this class was generated from the following file:

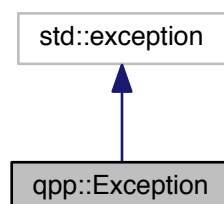
- [classes/codes.h](#)

7.2 qpp::Exception Class Reference

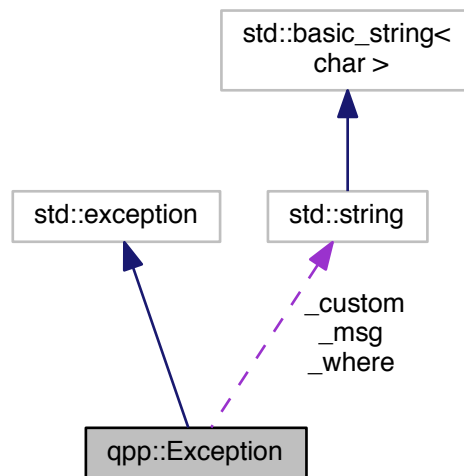
Generates custom exceptions, used when validating function parameters.

```
#include <classes/exception.h>
```

Inheritance diagram for qpp::Exception:



Collaboration diagram for qpp::Exception:



Public Types

- enum `Type` {
`Type::UNKNOWN_EXCEPTION = 1`, `Type::ZERO_SIZE`, `Type::MATRIX_NOT_SQUARE`, `Type::MATRIX_NOT_CVECTOR`,
`Type::MATRIX_NOT_RVECTOR`, `Type::MATRIX_NOT_VECTOR`, `Type::MATRIX_NOT_SQUARE_OR_CVECTOR`, `Type::MATRIX_NOT_SQUARE_OR_RVECTOR`,
`Type::MATRIX_NOT_SQUARE_OR_VECTOR`, `Type::MATRIX_MISMATCH_SUBSYS`, `Type::DIMS_INVALID`, `Type::DIMS_NOT_EQUAL`,
`Type::DIMS_MISMATCH_MATRIX`, `Type::DIMS_MISMATCH_CVECTOR`, `Type::DIMS_MISMATCH_RVECTOR`, `Type::DIMS_MISMATCH_VECTOR`,
`Type::SUBSYS_MISMATCH_DIMS`, `Type::PERM_INVALID`, `Type::PERM_MISMATCH_DIMS`, `Type::NOT_QUBIT_MATRIX`,
`Type::NOT_QUBIT_CVECTOR`, `Type::NOT_QUBIT_RVECTOR`, `Type::NOT_QUBIT_VECTOR`, `Type::NOT_QUBIT_SUBSYS`,
`Type::NOT_BIPARTITE`, `Type::NO_CODEWORD`, `Type::OUT_OF_RANGE`, `Type::TYPE_MISMATCH`,
`Type::SIZE_MISMATCH`, `Type::UNDEFINED_TYPE`, `Type::CUSTOM_EXCEPTION` }

Exception types, add more here if needed.

Public Member Functions

- `Exception` (const std::string &where, const `Type` &type)
Constructs an exception.
- `Exception` (const std::string &where, const std::string &custom)
Constructs an exception.
- virtual const char * `what` () const noexcept override
Overrides std::exception::what()

Private Member Functions

- void [_construct_exception_msg](#) ()
Constructs the exception description from its type.

Private Attributes

- std::string [_where](#)
- std::string [_msg](#)
- Type [_type](#)
- std::string [_custom](#)

7.2.1 Detailed Description

Generates custom exceptions, used when validating function parameters.

Customize this class if more exceptions are needed

7.2.2 Member Enumeration Documentation

7.2.2.1 enum qpp::Exception::Type [strong]

[Exception](#) types, add more here if needed.

See also

[qpp::Exception::_construct_exception_msg\(\)](#)

Enumerator

- UNKNOWN_EXCEPTION** Unknown exception
- ZERO_SIZE** Zero sized object, e.g. empty Eigen::Matrix or std::vector<> with no elements
- MATRIX_NOT_SQUARE** Eigen::Matrix is not square
- MATRIX_NOT_CVECTOR** Eigen::Matrix is not a column vector
- MATRIX_NOT_RVECTOR** Eigen::Matrix is not a row vector
- MATRIX_NOT_VECTOR** Eigen::Matrix is not a row/column vector
- MATRIX_NOT_SQUARE_OR_CVECTOR** Eigen::Matrix is not square nor a column vector
- MATRIX_NOT_SQUARE_OR_RVECTOR** Eigen::Matrix is not square nor a row vector
- MATRIX_NOT_SQUARE_OR_VECTOR** Eigen::Matrix is not square nor a row/column vector
- MATRIX_MISMATCH_SUBSYS** Matrix size mismatch subsystem sizes (e.g. in [qpp::apply\(\)](#))
- DIMS_INVALID** std::vector<idx> of dimensions has zero size or contains zeros
- DIMS_NOT_EQUAL** Local/global dimensions are not equal
- DIMS_MISMATCH_MATRIX** Product of the elements of std::vector<idx> of dimensions is not equal to the number of rows of Eigen::Matrix (assumed to be a square matrix)
- DIMS_MISMATCH_CVECTOR** Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of Eigen::Matrix (assumed to be a column vector)
- DIMS_MISMATCH_RVECTOR** Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of Eigen::Matrix (assumed to be a row vector)
- DIMS_MISMATCH_VECTOR** Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of Eigen::Matrix (assumed to be a row/column vector)
- SUBSYS_MISMATCH_DIMS** std::vector<idx> of subsystem labels has duplicates, or has entries that are larger than the size of the std::vector<idx> of dimensions

PERM_INVALID `std::vector<idx>` does not represent a valid permutation

PERM_MISMATCH_DIMS Size of the `std::vector<idx>` representing the permutation is different from the size of the `std::vector<idx>` of dimensions

NOT_QUBIT_MATRIX `Eigen::Matrix` is not 2 x 2

NOT_QUBIT_CVECTOR `Eigen::Matrix` is not 2 x 1

NOT_QUBIT_RVECTOR `Eigen::Matrix` is not 1 x 2

NOT_QUBIT_VECTOR `Eigen::Matrix` is not 1 x 2 nor 2 x 1

NOT_QUBIT_SUBSYS Subsystems are not 2-dimensional

NOT_BIPARTITE `std::vector<idx>` of dimensions has size different from 2

NO_CODEWORD Codeword does not exist, thrown when calling `qpp::Codes::codeword()` with invalid index *i*

OUT_OF_RANGE Parameter out of range

TYPE_MISMATCH Scalar types do not match

SIZE_MISMATCH Sizes do not match

UNDEFINED_TYPE Templated specialization not defined for this type

CUSTOM_EXCEPTION Custom exception, user must provide a custom message

7.2.3 Constructor & Destructor Documentation

7.2.3.1 `qpp::Exception::Exception (const std::string & where, const Type & type)` `[inline]`

Constructs an exception.

Parameters

<i>where</i>	Text representing where the exception occurred
<i>type</i>	Exception type, defined in qpp::Exception::Type

7.2.3.2 `qpp::Exception::Exception (const std::string & where, const std::string & custom)` `[inline]`

Constructs an exception.

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

Parameters

<i>where</i>	Text representing where the exception occurred
<i>custom</i>	Exception description

7.2.4 Member Function Documentation

7.2.4.1 `void qpp::Exception::_construct_exception_msg ()` `[inline]`, `[private]`

Constructs the exception description from its type.

See also

[qpp::Exception::Type](#)

Must modify the code of this function if more exceptions are added

7.2.4.2 `virtual const char* qpp::Exception::what () const` `[inline]`, `[override]`, `[virtual]`, `[noexcept]`

Overrides `std::exception::what()`

Returns

[Exception](#) description

7.2.5 Member Data Documentation

7.2.5.1 `std::string qpp::Exception::_custom` `[private]`

7.2.5.2 `std::string qpp::Exception::_msg` `[private]`

7.2.5.3 `Type qpp::Exception::_type` `[private]`

7.2.5.4 `std::string qpp::Exception::_where` `[private]`

The documentation for this class was generated from the following file:

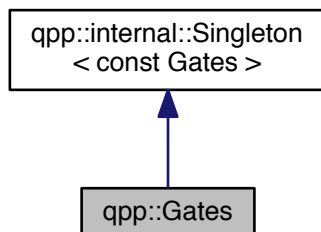
- [classes/exception.h](#)

7.3 qpp::Gates Class Reference

const Singleton class that implements most commonly used gates

```
#include <classes/gates.h>
```

Inheritance diagram for `qpp::Gates`:



Collaboration diagram for `qpp::Gates`:



Public Member Functions

- `cmat Rn` (double theta, const std::vector< double > &n) const
Rotation of theta about the 3-dimensional real unit vector n.
- `cmat Zd` (idx D) const
Generalized Z gate for qudits.
- `cmat Fd` (idx D) const
Fourier transform gate for qudits.
- `cmat Xd` (idx D) const
Generalized X gate for qudits.
- template<typename Derived = Eigen::MatrixXcd>
Derived `Id` (idx D) const
Identity gate.
- template<typename Derived >
`dyn_mat`< typename Derived::Scalar > `CTRL` (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx n, idx d=2) const
Generates the multi-partite multiple-controlled-A gate in matrix form.
- template<typename Derived >
`dyn_mat`< typename Derived::Scalar > `expandout` (const Eigen::MatrixBase< Derived > &A, idx pos, const std::vector< idx > &dims) const
Expands out.

Public Attributes

- `cmat Id2` {cmat::Identity(2, 2)}
Identity gate.
- `cmat H` {cmat::Zero(2, 2)}
Hadamard gate.
- `cmat X` {cmat::Zero(2, 2)}
Pauli Sigma-X gate.
- `cmat Y` {cmat::Zero(2, 2)}
Pauli Sigma-Y gate.
- `cmat Z` {cmat::Zero(2, 2)}
Pauli Sigma-Z gate.
- `cmat S` {cmat::Zero(2, 2)}

- S gate.*
- `cmat T {cmat::Zero(2, 2)}`
- T gate.*
- `cmat CNOT {cmat::Identity(4, 4)}`
- Controlled-NOT control target gate.*
- `cmat CZ {cmat::Identity(4, 4)}`
- Controlled-Phase gate.*
- `cmat CNOTba {cmat::Zero(4, 4)}`
- Controlled-NOT target control gate.*
- `cmat SWAP {cmat::Identity(4, 4)}`
- SWAP gate.*
- `cmat TOF {cmat::Identity(8, 8)}`
- Toffoli gate.*
- `cmat FRED {cmat::Identity(8, 8)}`
- Fredkin gate.*

Private Member Functions

- `Gates ()`
Initializes the gates.
- `~Gates ()=default`
Default destructor.

Friends

- class `internal::Singleton< const Gates >`

Additional Inherited Members

7.3.1 Detailed Description

const Singleton class that implements most commonly used gates

7.3.2 Constructor & Destructor Documentation

7.3.2.1 `qpp::Gates::Gates () [inline], [private]`

Initializes the gates.

7.3.2.2 `qpp::Gates::~Gates () [private], [default]`

Default destructor.

7.3.3 Member Function Documentation

7.3.3.1 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::Gates::CTRL (const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & ctrl, const std::vector< idx > & subsys, idx n, idx d = 2) const [inline]`

Generates the multi-partite multiple-controlled-A gate in matrix form.

See also

[qpp::applyCTRL\(\)](#)

Note

The dimension of the gate A must match the dimension of *subsys*

Parameters

A	Eigen expression
<i>ctrl</i>	Control subsystem indexes
<i>subsys</i>	Subsystem indexes where the gate A is applied
n	Total number of subsystems
d	Subsystem dimensions

Returns

CTRL- A gate, as a matrix over the same scalar field as A

7.3.3.2 `template<typename Derived > dyn_mat<typename Derived::Scalar> qpp::Gates::expandout (const Eigen::MatrixBase< Derived > & A, idx pos, const std::vector< idx > & dims) const [inline]`

Expands out.

See also

[qpp::kron\(\)](#)

Expands out A as a matrix in a multi-partite system. Faster than using [qpp::kron](#)($I, I, \dots, I, A, I, \dots, I$).

Parameters

A	Eigen expression
<i>pos</i>	Position
<i>dims</i>	Dimensions of the multi-partite system

Returns

Tensor product $I \otimes \dots \otimes I \otimes A \otimes I \otimes \dots \otimes I$, with A on position *pos*, as a dynamic matrix over the same scalar field as A

7.3.3.3 `cmat qpp::Gates::Fd (idx D) const [inline]`

Fourier transform gate for qudits.

Note

Defined as $F = \sum_{jk} \exp(2\pi i j k / D) |j\rangle\langle k|$

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Fourier transform gate for qudits

7.3.3.4 `template<typename Derived = Eigen::MatrixXcd> Derived qpp::Gates::Id (idx D) const` `[inline]`

Identity gate.

Note

Can change the return type from complex matrix (default) by explicitly specifying the template parameter

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Identity gate

7.3.3.5 `cmat qpp::Gates::Rn (double theta, const std::vector< double > & n) const` `[inline]`

Rotation of *theta* about the 3-dimensional real unit vector *n*.

Parameters

<i>theta</i>	Rotation angle
<i>n</i>	3-dimensional real unit vector

Returns

Rotation gate

7.3.3.6 `cmat qpp::Gates::Xd (idx D) const` `[inline]`

Generalized X gate for qudits.

Note

Defined as $X = \sum_j |j \oplus 1\rangle \langle j|$

Parameters

<i>D</i>	Dimension of the Hilbert space
----------	--------------------------------

Returns

Generalized X gate for qudits

7.3.3.7 `cmat qpp::Gates::Zd (idx D) const` `[inline]`

Generalized Z gate for qudits.

Note

Defined as $Z = \sum_j \exp(2\pi i j / D) |j\rangle \langle j|$

Parameters

D	Dimension of the Hilbert space
-----	--------------------------------

Returns

Generalized Z gate for qudits

7.3.4 Friends And Related Function Documentation

7.3.4.1 friend class `internal::Singleton< const Gates >` [`friend`]

7.3.5 Member Data Documentation

7.3.5.1 `cmat qpp::Gates::CNOT {cmat::Identity(4, 4)}`

Controlled-NOT control target gate.

7.3.5.2 `cmat qpp::Gates::CNOTba {cmat::Zero(4, 4)}`

Controlled-NOT target control gate.

7.3.5.3 `cmat qpp::Gates::CZ {cmat::Identity(4, 4)}`

Controlled-Phase gate.

7.3.5.4 `cmat qpp::Gates::FRED {cmat::Identity(8, 8)}`

Fredkin gate.

7.3.5.5 `cmat qpp::Gates::H {cmat::Zero(2, 2)}`

Hadamard gate.

7.3.5.6 `cmat qpp::Gates::Id2 {cmat::Identity(2, 2)}`

Identity gate.

7.3.5.7 `cmat qpp::Gates::S {cmat::Zero(2, 2)}`

S gate.

7.3.5.8 `cmat qpp::Gates::SWAP {cmat::Identity(4, 4)}`

SWAP gate.

7.3.5.9 `cmat qpp::Gates::T {cmat::Zero(2, 2)}`

T gate.

7.3.5.10 `cmat qpp::Gates::TOF {cmat::Identity(8, 8)}`

Toffoli gate.

7.3.5.11 `cmat qpp::Gates::X {cmat::Zero(2, 2)}`

Pauli Sigma-X gate.

7.3.5.12 `cmat qpp::Gates::Y {cmat::Zero(2, 2)}`

Pauli Sigma-Y gate.

7.3.5.13 `cmat qpp::Gates::Z {cmat::Zero(2, 2)}`

Pauli Sigma-Z gate.

The documentation for this class was generated from the following file:

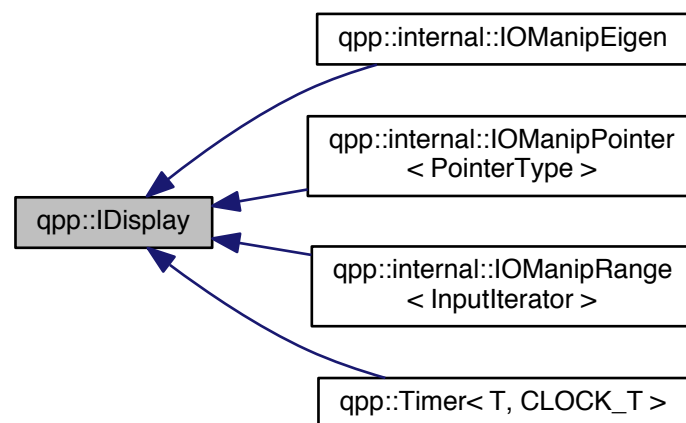
- [classes/gates.h](#)

7.4 qpp::IDisplay Class Reference

Abstract class (interface) that mandates the definition of virtual `std::ostream& display(std::ostream& os) const`.

```
#include <classes/ideisplay.h>
```

Inheritance diagram for `qpp::IDisplay`:



Public Member Functions

- `IDisplay()`=default
Default constructor.
- `IDisplay(const IDisplay &)=default`

Default copy constructor.

- `IDisplay (IDisplay &&)=default`

Default move constructor.

- `IDisplay & operator= (const IDisplay &)=default`

Default copy assignment operator.

- `IDisplay & operator= (IDisplay &&)=default`

Default move assignment operator.

- `virtual ~IDisplay ()=default`

Default virtual destructor.

Private Member Functions

- `virtual std::ostream & display (std::ostream &os) const =0`

Must be overridden by all derived classes.

Friends

- `std::ostream & operator<< (std::ostream &os, const IDisplay &rhs)`

Overloads the extraction operator.

7.4.1 Detailed Description

Abstract class (interface) that mandates the definition of virtual `std::ostream& display(std::ostream& os) const`.

This class defines friend inline `std::ostream& operator<< (std::ostream& os, const qpp::IDisplay& rhs)`. The latter delegates the work to the pure private virtual function `qpp::IDisplay::display()` which has to be overridden by all derived classes.

7.4.2 Constructor & Destructor Documentation

7.4.2.1 `qpp::IDisplay::IDisplay ()` [default]

Default constructor.

7.4.2.2 `qpp::IDisplay::IDisplay (const IDisplay &)` [default]

Default copy constructor.

7.4.2.3 `qpp::IDisplay::IDisplay (IDisplay &&)` [default]

Default move constructor.

7.4.2.4 `virtual qpp::IDisplay::~IDisplay ()` [virtual], [default]

Default virtual destructor.

7.4.3 Member Function Documentation

7.4.3.1 `virtual std::ostream& qpp::IDisplay::display (std::ostream & os) const` `[private], [pure virtual]`

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overridden member function in the derived class. This function is automatically invoked by friend inline `std::ostream& operator<<(std::ostream& os, const IDisplay& rhs)`.

Implemented in `qpp::internal::IOManipEigen`, `qpp::Timer< T, CLOCK_T >`, `qpp::internal::IOManipPointer< PointerType >`, and `qpp::internal::IOManipRange< InputIterator >`.

7.4.3.2 `IDisplay& qpp::IDisplay::operator= (const IDisplay &)` `[default]`

Default copy assignment operator.

7.4.3.3 `IDisplay& qpp::IDisplay::operator= (IDisplay &&)` `[default]`

Default move assignment operator.

7.4.4 Friends And Related Function Documentation

7.4.4.1 `std::ostream& operator<< (std::ostream & os, const IDisplay & rhs)` `[friend]`

Overloads the extraction operator.

Delegates the work to the virtual function `qpp::IDisplay::display()`

The documentation for this class was generated from the following file:

- `classes/idisplay.h`

7.5 qpp::Init Class Reference

const Singleton class that performs additional initializations/cleanups

```
#include <classes/init.h>
```

Inheritance diagram for `qpp::Init`:



Collaboration diagram for `qpp::Init`:



Private Member Functions

- [Init\(\)](#)
Additional initializations.
- [~Init\(\)](#)
Cleanups.

Friends

- class [internal::Singleton< const Init >](#)

Additional Inherited Members

7.5.1 Detailed Description

const Singleton class that performs additional initializations/cleanups

7.5.2 Constructor & Destructor Documentation

7.5.2.1 `qpp::Init::Init()` `[inline]`, `[private]`

Additional initializations.

7.5.2.2 `qpp::Init::~~Init()` `[inline]`, `[private]`

Cleanups.

7.5.3 Friends And Related Function Documentation

7.5.3.1 `friend class internal::Singleton< const Init >` `[friend]`

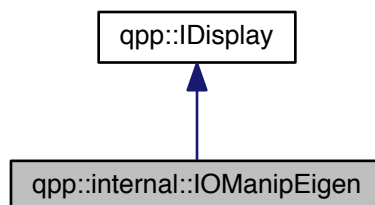
The documentation for this class was generated from the following file:

- [classes/init.h](#)

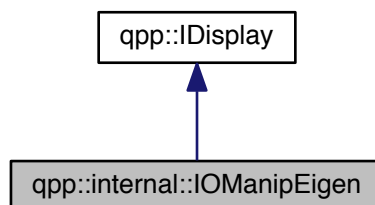
7.6 qpp::internal::IOManipEigen Class Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for qpp::internal::IOManipEigen:



Collaboration diagram for qpp::internal::IOManipEigen:



Public Member Functions

- `template<typename Derived >`
`IOManipEigen` (`const Eigen::MatrixBase< Derived > &A`, `double chop=qpp::chop`)
- `IOManipEigen` (`const cplx z`, `double chop=qpp::chop`)

Private Member Functions

- `std::ostream & display` (`std::ostream &os`) `const` override
Must be overridden by all derived classes.

Private Attributes

- `cmat_A`
- `double _chop`

7.6.1 Constructor & Destructor Documentation

7.6.1.1 `template<typename Derived > qpp::internal::IOManipEigen::IOManipEigen (const Eigen::MatrixBase< Derived > & A, double chop = qpp::chop)` `[inline]`, `[explicit]`

7.6.1.2 `qpp::internal::IOManipEigen::IOManipEigen (const cplx z, double chop = qpp::chop)` `[inline]`, `[explicit]`

7.6.2 Member Function Documentation

7.6.2.1 `std::ostream& qpp::internal::IOManipEigen::display (std::ostream & os) const` `[inline]`, `[override]`, `[private]`, `[virtual]`

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overridden member function in the derived class. This function is automatically invoked by friend inline `std::ostream& operator<<(std::ostream& os, const IDisplay& rhs)`.

Implements [qpp::IDisplay](#).

7.6.3 Member Data Documentation

7.6.3.1 `cmat qpp::internal::IOManipEigen::_A` `[private]`

7.6.3.2 `double qpp::internal::IOManipEigen::_chop` `[private]`

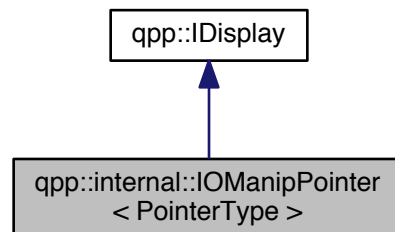
The documentation for this class was generated from the following file:

- [internal/classes/iomanip.h](#)

7.7 `qpp::internal::IOManipPointer< PointerType >` Class Template Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for `qpp::internal::IOManipPointer< PointerType >`:



Collaboration diagram for qpp::internal::IOManipPointer< PointerType >:



Public Member Functions

- `IOManipPointer` (const PointerType *p, idx n, const std::string &separator, const std::string &start="[" , const std::string &end="]")
- `IOManipPointer` (const IOManipPointer &)=default
- `IOManipPointer` & operator= (const IOManipPointer &)=default

Private Member Functions

- `std::ostream & display` (std::ostream &os) const override
Must be overridden by all derived classes.

Private Attributes

- const PointerType * `_p`
- idx `_n`
- std::string `_separator`
- std::string `_start`
- std::string `_end`

7.7.1 Constructor & Destructor Documentation

7.7.1.1 `template<typename PointerType> qpp::internal::IOManipPointer< PointerType >::IOManipPointer (const PointerType * p, idx n, const std::string & separator, const std::string & start = " [" , const std::string & end = "] ") [inline], [explicit]`

7.7.1.2 `template<typename PointerType> qpp::internal::IOManipPointer< PointerType >::IOManipPointer (const IOManipPointer< PointerType > &) [default]`

7.7.2 Member Function Documentation

7.7.2.1 `template<typename PointerType> std::ostream& qpp::internal::IOManipPointer< PointerType >::display (std::ostream & os) const` `[inline], [override], [private], [virtual]`

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overridden member function in the derived class. This function is automatically invoked by friend inline `std::ostream& operator<<(std::ostream& os, const IDisplay& rhs)`.

Implements [qpp::IDisplay](#).

7.7.2.2 `template<typename PointerType> IOManipPointer& qpp::internal::IOManipPointer< PointerType >::operator= (const IOManipPointer< PointerType > &)` `[default]`

7.7.3 Member Data Documentation

7.7.3.1 `template<typename PointerType> std::string qpp::internal::IOManipPointer< PointerType >::_end` `[private]`

7.7.3.2 `template<typename PointerType> idx qpp::internal::IOManipPointer< PointerType >::_n` `[private]`

7.7.3.3 `template<typename PointerType> const PointerType* qpp::internal::IOManipPointer< PointerType >::_p` `[private]`

7.7.3.4 `template<typename PointerType> std::string qpp::internal::IOManipPointer< PointerType >::_separator` `[private]`

7.7.3.5 `template<typename PointerType> std::string qpp::internal::IOManipPointer< PointerType >::_start` `[private]`

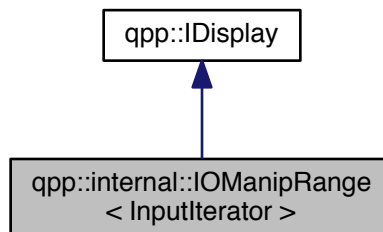
The documentation for this class was generated from the following file:

- [internal/classes/iomanip.h](#)

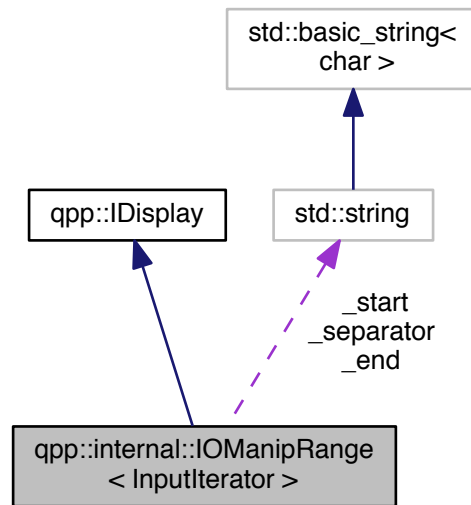
7.8 qpp::internal::IOManipRange< InputIterator > Class Template Reference

```
#include <internal/classes/iomanip.h>
```

Inheritance diagram for `qpp::internal::IOManipRange< InputIterator >`:



Collaboration diagram for qpp::internal::IOManipRange< Inputlterator >:



Public Member Functions

- [IOManipRange](#) (Inputlterator first, Inputlterator last, const std::string &separator, const std::string &start="[, const std::string &end="]")
- [IOManipRange](#) (const [IOManipRange](#) &)=default
- [IOManipRange](#) & [operator=](#) (const [IOManipRange](#) &)=default

Private Member Functions

- std::ostream & [display](#) (std::ostream &os) const override
Must be overridden by all derived classes.

Private Attributes

- Inputlterator [_first](#)
- Inputlterator [_last](#)
- std::string [_separator](#)
- std::string [_start](#)
- std::string [_end](#)

7.8.1 Constructor & Destructor Documentation

7.8.1.1 `template<typename Inputlterator> qpp::internal::IOManipRange< Inputlterator >::IOManipRange (Inputlterator first, Inputlterator last, const std::string & separator, const std::string & start = " [", const std::string & end = "] ") [inline],[explicit]`

7.8.1.2 `template<typename Inputlterator> qpp::internal::IOManipRange< Inputlterator >::IOManipRange (const IOManipRange< Inputlterator > &) [default]`

7.8.2 Member Function Documentation

7.8.2.1 `template<typename InputIterator> std::ostream& qpp::internal::IOManipRange< InputIterator >::display (std::ostream & os) const` `[inline], [override], [private], [virtual]`

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overridden member function in the derived class. This function is automatically invoked by friend inline `std::ostream& operator<<(std::ostream& os, const IDisplay& rhs)`.

Implements [qpp::IDisplay](#).

7.8.2.2 `template<typename InputIterator> IOManipRange& qpp::internal::IOManipRange< InputIterator >::operator= (const IOManipRange< InputIterator > &)` `[default]`

7.8.3 Member Data Documentation

7.8.3.1 `template<typename InputIterator> std::string qpp::internal::IOManipRange< InputIterator >::_end` `[private]`

7.8.3.2 `template<typename InputIterator> InputIterator qpp::internal::IOManipRange< InputIterator >::_first` `[private]`

7.8.3.3 `template<typename InputIterator> InputIterator qpp::internal::IOManipRange< InputIterator >::_last` `[private]`

7.8.3.4 `template<typename InputIterator> std::string qpp::internal::IOManipRange< InputIterator >::_separator` `[private]`

7.8.3.5 `template<typename InputIterator> std::string qpp::internal::IOManipRange< InputIterator >::_start` `[private]`

The documentation for this class was generated from the following file:

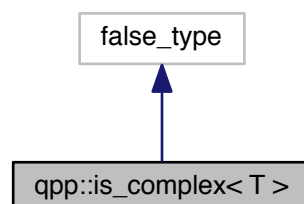
- [internal/classes/iomanip.h](#)

7.9 qpp::is_complex< T > Struct Template Reference

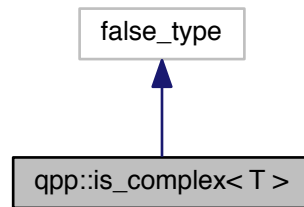
Checks whether the type is a complex type.

```
#include <traits.h>
```

Inheritance diagram for `qpp::is_complex< T >`:



Collaboration diagram for qpp::is_complex< T >:



7.9.1 Detailed Description

```
template<typename T>struct qpp::is_complex< T >
```

Checks whether the type is a complex type.

Provides the member constant *value* which is equal to *true*, if the type is a complex type (i.e. `std::complex< T >`)

The documentation for this struct was generated from the following file:

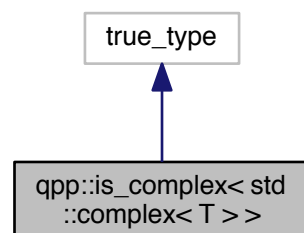
- [traits.h](#)

7.10 qpp::is_complex< std::complex< T > > Struct Template Reference

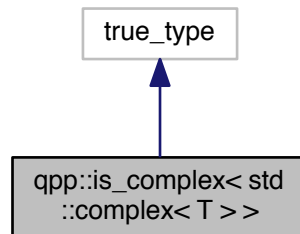
Checks whether the type is a complex number type, specialization for complex types.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_complex< std::complex< T > >:



Collaboration diagram for `qpp::is_complex< std::complex< T > >`:



7.10.1 Detailed Description

```
template<typename T>struct qpp::is_complex< std::complex< T > >
```

Checks whether the type is a complex number type, specialization for complex types.

The documentation for this struct was generated from the following file:

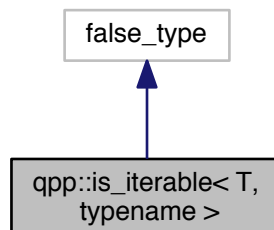
- [traits.h](#)

7.11 `qpp::is_iterable< T, typename >` Struct Template Reference

Checks whether *T* is compatible with an STL-like iterable container.

```
#include <traits.h>
```

Inheritance diagram for `qpp::is_iterable< T, typename >`:



Collaboration diagram for qpp::is_iterable< T, typename >:



7.11.1 Detailed Description

```
template<typename T, typename = void>struct qpp::is_iterable< T, typename >
```

Checks whether *T* is compatible with an STL-like iterable container.

Provides the member constant *value* which is equal to *true*, if *T* is compatible with an iterable container, i.e. provides at least *begin()* and *end()* member functions. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

- [traits.h](#)

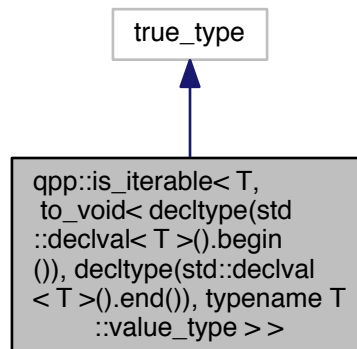
7.12 qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > > Struct Template Reference

Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

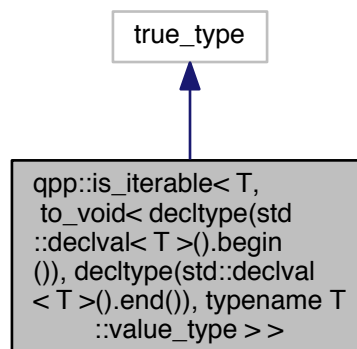
```
#include <traits.h>
```

Inheritance diagram for qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval<

`T >().end()), typename T::value_type > >:`



Collaboration diagram for `qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >:`



7.12.1 Detailed Description

```
template<typename T>struct qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >
```

Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

The documentation for this struct was generated from the following file:

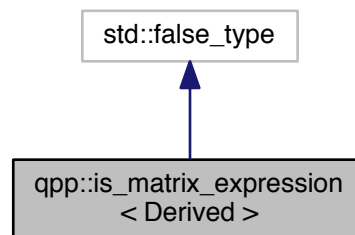
- [traits.h](#)

7.13 qpp::is_matrix_expression< Derived > Struct Template Reference

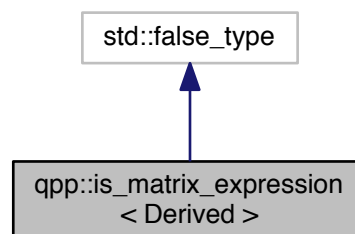
Checks whether the type is an Eigen matrix expression.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_matrix_expression< Derived >:



Collaboration diagram for qpp::is_matrix_expression< Derived >:



7.13.1 Detailed Description

```
template<typename Derived> struct qpp::is_matrix_expression< Derived >
```

Checks whether the type is an Eigen matrix expression.

Provides the member constant *value* which is equal to *true*, if the type is an Eigen matrix expression of type *Eigen↵::MatrixBase<Derived>*. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

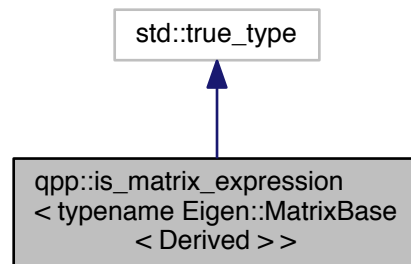
- [traits.h](#)

7.14 qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > > Struct Template Reference

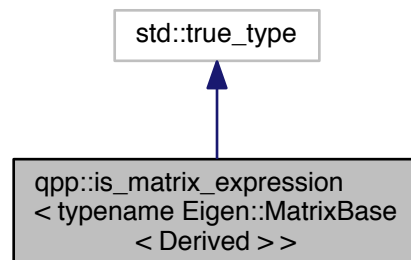
Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.

```
#include <traits.h>
```

Inheritance diagram for qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >:



Collaboration diagram for qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >:



7.14.1 Detailed Description

```
template<typename Derived>struct qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >
```

Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.

The documentation for this struct was generated from the following file:

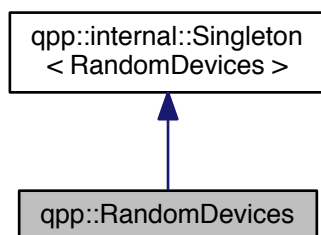
- [traits.h](#)

7.15 qpp::RandomDevices Class Reference

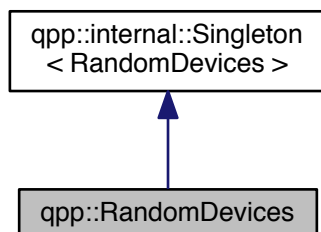
Singleton class that manages the source of randomness in the library.

```
#include <classes/random_devices.h>
```

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



Public Attributes

- [std::mt19937 _rng](#)
Mersenne twister random number generator.

Private Member Functions

- [RandomDevices \(\)](#)
Initializes and seeds the random number generators.
- [~RandomDevices \(\)=default](#)
Default destructor.

Private Attributes

- `std::random_device _rd`
used to seed `std::mt19937_rng`

Friends

- class `internal::Singleton< RandomDevices >`

Additional Inherited Members

7.15.1 Detailed Description

Singleton class that manages the source of randomness in the library.

Consists of a wrapper around an `std::mt19937` Mersenne twister random number generator engine and an `std::random_device` engine. The latter is used to seed the Mersenne twister.

Warning

This class DOES NOT seed the standard C number generator used by `Eigen::Matrix::Random()`, since it is not thread safe. Do not use `Eigen::Matrix::Random()` or functions that depend on the C style random number engine, but use `qpp::rand()` instead!

7.15.2 Constructor & Destructor Documentation

7.15.2.1 `qpp::RandomDevices::RandomDevices () [inline], [private]`

Initializes and seeds the random number generators.

7.15.2.2 `qpp::RandomDevices::~~RandomDevices () [private], [default]`

Default destructor.

7.15.3 Friends And Related Function Documentation

7.15.3.1 `friend class internal::Singleton< RandomDevices > [friend]`

7.15.4 Member Data Documentation

7.15.4.1 `std::random_device qpp::RandomDevices::_rd [private]`

used to seed `std::mt19937_rng`

7.15.4.2 `std::mt19937 qpp::RandomDevices::_rng`

Mersenne twister random number generator.

The documentation for this class was generated from the following file:

- `classes/random_devices.h`

7.16 qpp::internal::Singleton< T > Class Template Reference

[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

```
#include <internal/classes/singleton.h>
```

Static Public Member Functions

- static T & [get_instance](#) () noexcept(std::is_nothrow_constructible< T >::value)
- static thread_local T & [get_thread_local_instance](#) () noexcept(std::is_nothrow_constructible< T >::value)

Protected Member Functions

- [Singleton](#) () noexcept=default
- [Singleton](#) (const [Singleton](#) &)=delete
- [Singleton](#) & [operator=](#) (const [Singleton](#) &)=delete
- virtual [~Singleton](#) ()=default

7.16.1 Detailed Description

```
template<typename T>class qpp::internal::Singleton< T >
```

[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

To implement a singleton, derive your class from [qpp::internal::Singleton](#), make [qpp::internal::Singleton](#) a friend of your class, then declare the constructor and destructor of your class as private. To get an instance, use the static member function [qpp::internal::Singleton::get_instance\(\)](#) ([qpp::internal::Singleton::get_thread_local_instance\(\)](#)), which returns a reference (thread_local reference) to your newly created singleton (thread-safe in C++11).

Example:

```
class MySingleton: public qpp::internal::Singleton<MySingleton>
{
    friend class qpp::internal::Singleton<MySingleton>;
public:
    // Declare all public members here
private:
    MySingleton()
    {
        // Implement the constructor here
    }
    ~MySingleton()
    {
        // Implement the destructor here
    }
};

MySingleton& mySingleton = MySingleton::get_instance(); // Get an instance
thread_local MySingleton& tls = MySingleton::get_thread_local_instance();
// Get a thread_local instance
```

See also

Code of [qpp::Codes](#), [qpp::Gates](#), [qpp::Init](#), [qpp::RandomDevices](#), [qpp::States](#) or [qpp.h](#) for real world examples of usage.

7.16.2 Constructor & Destructor Documentation

7.16.2.1 `template<typename T> qpp::internal::Singleton< T >::Singleton ()` [protected], [default], [noexcept]

7.16.2.2 `template<typename T> qpp::internal::Singleton< T >::Singleton (const Singleton< T > &)` [protected], [delete]

7.16.2.3 `template<typename T> virtual qpp::internal::Singleton< T >::~~Singleton ()` [protected], [virtual], [default]

7.16.3 Member Function Documentation

7.16.3.1 `template<typename T> static T& qpp::internal::Singleton< T >::get_instance ()` [inline], [static], [noexcept]

7.16.3.2 `template<typename T> static thread_local T& qpp::internal::Singleton< T >::get_thread_local_instance ()` [inline], [static], [noexcept]

7.16.3.3 `template<typename T> Singleton& qpp::internal::Singleton< T >::operator= (const Singleton< T > &)` [protected], [delete]

The documentation for this class was generated from the following file:

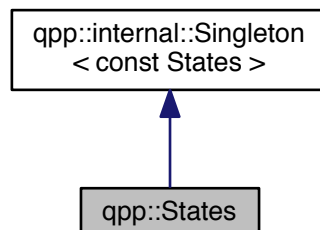
- [internal/classes/singleton.h](#)

7.17 qpp::States Class Reference

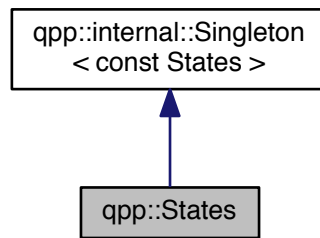
const Singleton class that implements most commonly used states

```
#include <classes/states.h>
```

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



Public Attributes

- **ket x0** {ket::Zero(2)}
Pauli Sigma-X 0-eigenstate $|+\rangle$
- **ket x1** {ket::Zero(2)}
Pauli Sigma-X 1-eigenstate $|-\rangle$
- **ket y0** {ket::Zero(2)}
Pauli Sigma-Y 0-eigenstate $|y+\rangle$
- **ket y1** {ket::Zero(2)}
Pauli Sigma-Y 1-eigenstate $|y-\rangle$
- **ket z0** {ket::Zero(2)}
Pauli Sigma-Z 0-eigenstate $|0\rangle$
- **ket z1** {ket::Zero(2)}
Pauli Sigma-Z 1-eigenstate $|1\rangle$
- **cmat px0** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-X 0-eigenstate $|+\rangle\langle+|$.
- **cmat px1** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-X 1-eigenstate $|-\rangle\langle-|$.
- **cmat py0** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Y 0-eigenstate $|y+\rangle\langle y+|$.
- **cmat py1** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Y 1-eigenstate $|y-\rangle\langle y-|$.
- **cmat pz0** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Z 0-eigenstate $|0\rangle\langle 0|$.
- **cmat pz1** {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Z 1-eigenstate $|1\rangle\langle 1|$.
- **ket b00** {ket::Zero(4)}
Bell-00 state (following the convention in Nielsen and Chuang)
- **ket b01** {ket::Zero(4)}
Bell-01 state (following the convention in Nielsen and Chuang)
- **ket b10** {ket::Zero(4)}
Bell-10 state (following the convention in Nielsen and Chuang)
- **ket b11** {ket::Zero(4)}
Bell-11 state (following the convention in Nielsen and Chuang)
- **cmat pb00** {cmat::Zero(4, 4)}

- Projector onto the Bell-00 state.*
- [cmat pb01](#) {cmat::Zero(4, 4)}
- Projector onto the Bell-01 state.*
- [cmat pb10](#) {cmat::Zero(4, 4)}
- Projector onto the Bell-10 state.*
- [cmat pb11](#) {cmat::Zero(4, 4)}
- Projector onto the Bell-11 state.*
- [ket GHZ](#) {ket::Zero(8)}
- GHZ state.*
- [ket W](#) {ket::Zero(8)}
- W state.*
- [cmat pGHZ](#) {cmat::Zero(8, 8)}
- Projector onto the GHZ state.*
- [cmat pW](#) {cmat::Zero(8, 8)}
- Projector onto the W state.*

Private Member Functions

- [States](#) ()
 - [~States](#) ()=default
- Default destructor.*

Friends

- class [internal::Singleton< const States >](#)

Additional Inherited Members

7.17.1 Detailed Description

const Singleton class that implements most commonly used states

7.17.2 Constructor & Destructor Documentation

7.17.2.1 `qpp::States::States () [inline], [private]`

Initialize the states

7.17.2.2 `qpp::States::~~States () [private], [default]`

Default destructor.

7.17.3 Friends And Related Function Documentation

7.17.3.1 `friend class internal::Singleton< const States > [friend]`

7.17.4 Member Data Documentation

7.17.4.1 `ket qpp::States::b00 {ket::Zero(4)}`

Bell-00 state (following the convention in Nielsen and Chuang)

7.17.4.2 ket qpp::States::b01 {ket::Zero(4)}

Bell-01 state (following the convention in Nielsen and Chuang)

7.17.4.3 ket qpp::States::b10 {ket::Zero(4)}

Bell-10 state (following the convention in Nielsen and Chuang)

7.17.4.4 ket qpp::States::b11 {ket::Zero(4)}

Bell-11 state (following the convention in Nielsen and Chuang)

7.17.4.5 ket qpp::States::GHZ {ket::Zero(8)}

GHZ state.

7.17.4.6 cmat qpp::States::pb00 {cmat::Zero(4, 4)}

Projector onto the Bell-00 state.

7.17.4.7 cmat qpp::States::pb01 {cmat::Zero(4, 4)}

Projector onto the Bell-01 state.

7.17.4.8 cmat qpp::States::pb10 {cmat::Zero(4, 4)}

Projector onto the Bell-10 state.

7.17.4.9 cmat qpp::States::pb11 {cmat::Zero(4, 4)}

Projector onto the Bell-11 state.

7.17.4.10 cmat qpp::States::pGHZ {cmat::Zero(8, 8)}

Projector onto the GHZ state.

7.17.4.11 cmat qpp::States::pW {cmat::Zero(8, 8)}

Projector onto the W state.

7.17.4.12 cmat qpp::States::px0 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-X 0-eigenstate $|+\rangle\langle+|$.

7.17.4.13 cmat qpp::States::px1 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-X 1-eigenstate $|-\rangle\langle-|$.

7.17.4.14 `cmat qpp::States::py0 {cmat::Zero(2, 2)}`

Projector onto the Pauli Sigma-Y 0-eigenstate $|y+\rangle\langle y+|$.

7.17.4.15 `cmat qpp::States::py1 {cmat::Zero(2, 2)}`

Projector onto the Pauli Sigma-Y 1-eigenstate $|y-\rangle\langle y-|$.

7.17.4.16 `cmat qpp::States::pz0 {cmat::Zero(2, 2)}`

Projector onto the Pauli Sigma-Z 0-eigenstate $|0\rangle\langle 0|$.

7.17.4.17 `cmat qpp::States::pz1 {cmat::Zero(2, 2)}`

Projector onto the Pauli Sigma-Z 1-eigenstate $|1\rangle\langle 1|$.

7.17.4.18 `ket qpp::States::W {ket::Zero(8)}`

W state.

7.17.4.19 `ket qpp::States::x0 {ket::Zero(2)}`

Pauli Sigma-X 0-eigenstate $|+\rangle$

7.17.4.20 `ket qpp::States::x1 {ket::Zero(2)}`

Pauli Sigma-X 1-eigenstate $|-\rangle$

7.17.4.21 `ket qpp::States::y0 {ket::Zero(2)}`

Pauli Sigma-Y 0-eigenstate $|y+\rangle$

7.17.4.22 `ket qpp::States::y1 {ket::Zero(2)}`

Pauli Sigma-Y 1-eigenstate $|y-\rangle$

7.17.4.23 `ket qpp::States::z0 {ket::Zero(2)}`

Pauli Sigma-Z 0-eigenstate $|0\rangle$

7.17.4.24 `ket qpp::States::z1 {ket::Zero(2)}`

Pauli Sigma-Z 1-eigenstate $|1\rangle$

The documentation for this class was generated from the following file:

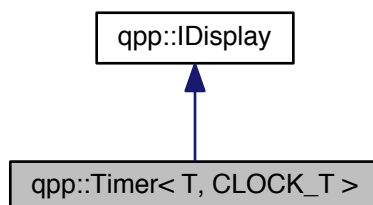
- [classes/states.h](#)

7.18 qpp::Timer< T, CLOCK_T > Class Template Reference

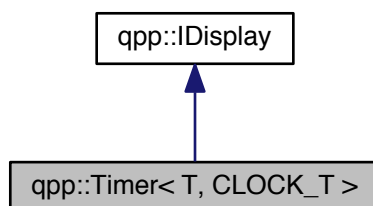
Chronometer.

```
#include <classes/timer.h>
```

Inheritance diagram for qpp::Timer< T, CLOCK_T >:



Collaboration diagram for qpp::Timer< T, CLOCK_T >:



Public Member Functions

- `Timer ()` noexcept
Constructs an instance with the current time as the starting point.
- `void tic ()` noexcept
Resets the chronometer.
- `const Timer & toc ()` noexcept
Stops the chronometer.
- `double tics ()` const noexcept
Time passed in the duration specified by T.
- `template<typename U = T>`
 `U get_duration ()`
Duration specified by U.
- `Timer (const Timer &)=default`
Default copy constructor.
- `Timer (Timer &&)=default`

Default move constructor.

- `Timer & operator= (const Timer &)=default`

Default copy assignment operator.

- `Timer & operator= (Timer &&)=default`

Default move assignment operator.

- `virtual ~Timer ()=default`

Default virtual destructor.

Protected Attributes

- `CLOCK_T::time_point _start`
- `CLOCK_T::time_point _end`

Private Member Functions

- `std::ostream & display (std::ostream &os) const` override
qpp::IDisplay::display() override

7.18.1 Detailed Description

`template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> class qpp::Timer< T, CLOCK_T >`

Chronometer.

Template Parameters

<i>T</i>	Tics duration, default is <code>std::chrono::duration<double, 1></code> i.e. seconds in double precision
<i>CLOCK_T</i>	Clock's type, default is <code>std::chrono::steady_clock</code> , not affected by wall clock changes during runtime

7.18.2 Constructor & Destructor Documentation

7.18.2.1 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> qpp::Timer< T, CLOCK_T >::Timer () [inline], [noexcept]`

Constructs an instance with the current time as the starting point.

7.18.2.2 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> qpp::Timer< T, CLOCK_T >::Timer (const Timer< T, CLOCK_T > &) [default]`

Default copy constructor.

7.18.2.3 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> qpp::Timer< T, CLOCK_T >::Timer (Timer< T, CLOCK_T > &&) [default]`

Default move constructor.

7.18.2.4 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> virtual qpp::Timer< T, CLOCK_T >::~~Timer () [virtual], [default]`

Default virtual destructor.

7.18.3 Member Function Documentation

7.18.3.1 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock>
std::ostream& qpp::Timer< T, CLOCK_T >::display (std::ostream & os) const [inline], [override],
[private], [virtual]`

[qpp::IDisplay::display\(\)](#) override

Parameters

<code>os</code>	Output stream
-----------------	---------------

Returns

Writes to the output stream the number of tics (specified by T) that passed between the instantiation/reset and invocation of [qpp::Timer::toc\(\)](#).

Implements [qpp::IDisplay](#).

7.18.3.2 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock>
template<typename U = T> U qpp::Timer< T, CLOCK_T >::get_duration () [inline]`

Duration specified by U.

Template Parameters

<code>U</code>	Duration, default is T, which defaults to std::chrono::duration<double, 1>, i.e. seconds in double precision
----------------	--

Returns

Duration that passed between the instantiation/reset and invocation of [qpp::Timer::toc\(\)](#)

7.18.3.3 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> Timer&
qpp::Timer< T, CLOCK_T >::operator= (const Timer< T, CLOCK_T > &) [default]`

Default copy assignment operator.

7.18.3.4 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> Timer&
qpp::Timer< T, CLOCK_T >::operator= (Timer< T, CLOCK_T > &&) [default]`

Default move assignment operator.

7.18.3.5 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> void
qpp::Timer< T, CLOCK_T >::tic () [inline], [noexcept]`

Resets the chronometer.

Resets the starting/ending point to the current time

7.18.3.6 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> double
qpp::Timer< T, CLOCK_T >::tics () const [inline], [noexcept]`

Time passed in the duration specified by T.

Returns

Number of tics (specified by T) that passed between the instantiation/reset and invocation of [qpp::Timer::toc\(\)](#)

7.18.3.7 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock> const
Timer& qpp::Timer< T, CLOCK_T >::toc () [inline], [noexcept]`

Stops the chronometer.

Set the current time as the ending point

Returns

Current instance

7.18.4 Member Data Documentation

7.18.4.1 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock>
CLOCK_T::time_point qpp::Timer< T, CLOCK_T >::_end [protected]`

7.18.4.2 `template<typename T = std::chrono::duration<double>, typename CLOCK_T = std::chrono::steady_clock>
CLOCK_T::time_point qpp::Timer< T, CLOCK_T >::_start [protected]`

The documentation for this class was generated from the following file:

- [classes/timer.h](#)

Chapter 8

File Documentation

8.1 classes/codes.h File Reference

Quantum error correcting codes.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::Codes](#)
const Singleton class that defines quantum error correcting codes

Namespaces

- [qpp](#)
Quantum++ main namespace.

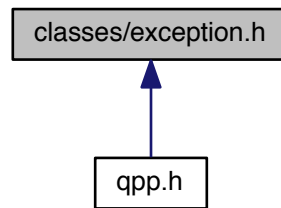
8.1.1 Detailed Description

Quantum error correcting codes.

8.2 classes/exception.h File Reference

Exceptions.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::Exception](#)
Generates custom exceptions, used when validating function parameters.

Namespaces

- [qpp](#)
Quantum++ main namespace.

8.2.1 Detailed Description

Exceptions.

8.3 classes/gates.h File Reference

Quantum gates.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::Gates](#)
const Singleton class that implements most commonly used gates

Namespaces

- [qpp](#)
Quantum++ main namespace.

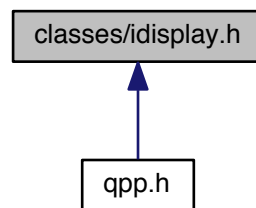
8.3.1 Detailed Description

Quantum gates.

8.4 classes/ideisplay.h File Reference

Display interface via the non-virtual interface (NVI)

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::IDisplay](#)
Abstract class (interface) that mandates the definition of virtual `std::ostream& display(std::ostream& os) const`.

Namespaces

- [qpp](#)
Quantum++ main namespace.

8.4.1 Detailed Description

Display interface via the non-virtual interface (NVI)

8.5 classes/init.h File Reference

Initialization.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::Init](#)
const Singleton class that performs additional initializations/cleanups

Namespaces

- [qpp](#)
Quantum++ main namespace.

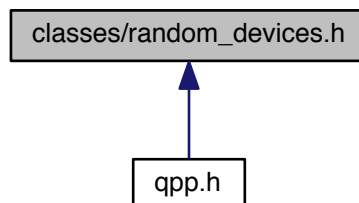
8.5.1 Detailed Description

Initialization.

8.6 classes/random_devices.h File Reference

Random devices.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::RandomDevices](#)

Singleton class that manages the source of randomness in the library.

Namespaces

- [qpp](#)

Quantum++ main namespace.

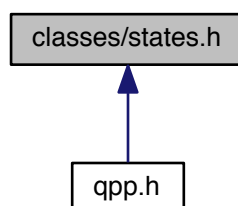
8.6.1 Detailed Description

Random devices.

8.7 classes/states.h File Reference

Quantum states.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::States](#)

const Singleton class that implements most commonly used states

Namespaces

- [qpp](#)

Quantum++ main namespace.

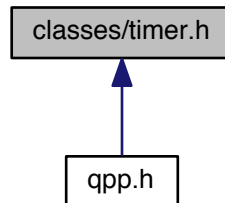
8.7.1 Detailed Description

Quantum states.

8.8 classes/timer.h File Reference

Timing.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::Timer< T, CLOCK_T >](#)
Chronometer.

Namespaces

- [qpp](#)
Quantum++ main namespace.

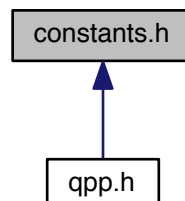
8.8.1 Detailed Description

Timing.

8.9 constants.h File Reference

Constants.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.

Functions

- constexpr cplx [qpp::operator""_i](#) (unsigned long long int x) noexcept
User-defined literal for complex $i = \sqrt{-1}$ (integer overload)
- constexpr cplx [qpp::operator""_i](#) (long double x) noexcept
User-defined literal for complex $i = \sqrt{-1}$ (real overload)
- cplx [qpp::omega](#) (idx D)
D-th root of unity.

Variables

- constexpr double [qpp::chop](#) = 1e-10
Used in [qpp::disp\(\)](#) for setting to zero numbers that have their absolute value smaller than [qpp::chop](#).
- constexpr double [qpp::eps](#) = 1e-12
Used to decide whether a number or expression in double precision is zero or not.
- constexpr idx [qpp::maxn](#) = 64
Maximum number of allowed qu(d)its (subsystems)
- constexpr double [qpp::pi](#) = 3.141592653589793238462643383279502884
 π
- constexpr double [qpp::ee](#) = 2.718281828459045235360287471352662497
Base of natural logarithm, e.
- constexpr double [qpp::infy](#) = std::numeric_limits<double>::infinity()
Used to denote infinity in double precision.

8.9.1 Detailed Description

Constants.

8.10 entanglement.h File Reference

Entanglement functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)

Quantum++ main namespace.

Functions

- `template<typename Derived >
dyn_col_vect< double > qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Schmidt coefficients of the bi-partite pure state A.
- `template<typename Derived >
cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Schmidt basis on Alice side.
- `template<typename Derived >
cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Schmidt basis on Bob side.
- `template<typename Derived >
std::vector< double > qpp::schmidtprobs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Schmidt probabilities of the bi-partite pure state A.
- `template<typename Derived >
double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Entanglement of the bi-partite pure state A.
- `template<typename Derived >
double qpp::gconcurrence (const Eigen::MatrixBase< Derived > &A)`
G-concurrence of the bi-partite pure state A.
- `template<typename Derived >
double qpp::negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Negativity of the bi-partite mixed state A.
- `template<typename Derived >
double qpp::lognegativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Logarithmic negativity of the bi-partite mixed state A.
- `template<typename Derived >
double qpp::concurrence (const Eigen::MatrixBase< Derived > &A)`
Wootters concurrence of the bi-partite qubit mixed state A.

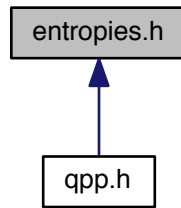
8.10.1 Detailed Description

Entanglement functions.

8.11 entropies.h File Reference

Entropy functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.

Functions

- `template<typename Derived >`
`double qpp::entropy (const Eigen::MatrixBase< Derived > &A)`
von-Neumann entropy of the density matrix A
- `double qpp::entropy (const std::vector< double > &prob)`
Shannon entropy of the probability distribution prob.
- `template<typename Derived >`
`double qpp::renyi (const Eigen::MatrixBase< Derived > &A, double alpha)`
Renyi- α entropy of the density matrix A, for $\alpha \geq 0$.
- `double qpp::renyi (const std::vector< double > &prob, double alpha)`
Renyi- α entropy of the probability distribution prob, for $\alpha \geq 0$.
- `template<typename Derived >`
`double qpp::tsallis (const Eigen::MatrixBase< Derived > &A, double q)`
Tsallis- q entropy of the density matrix A, for $q \geq 0$.
- `double qpp::tsallis (const std::vector< double > &prob, double q)`
Tsallis- q entropy of the probability distribution prob, for $q \geq 0$.
- `template<typename Derived >`
`double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, const std::vector< idx > &dims)`
Quantum mutual information between 2 subsystems of a composite system.
- `template<typename Derived >`
`double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, idx d=2)`
Quantum mutual information between 2 subsystems of a composite system.

8.11.1 Detailed Description

Entropy functions.

8.12 experimental/experimental.h File Reference

Experimental/test functions/classes.

Namespaces

- [qpp](#)
Quantum++ main namespace.
- [qpp::experimental](#)
Experimental/test functions/classes, do not use or modify.

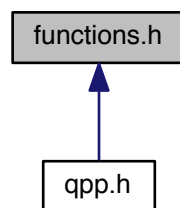
8.12.1 Detailed Description

Experimental/test functions/classes.

8.13 functions.h File Reference

Generic quantum computing functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.

Functions

- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::transpose (const Eigen::MatrixBase< Derived > &A)`
Transpose.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::conjugate (const Eigen::MatrixBase< Derived > &A)`
Complex conjugate.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::adjoint (const Eigen::MatrixBase< Derived > &A)`
Adjoint.

- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::inverse (const Eigen::MatrixBase< Derived > &A)`
Inverse.
- `template<typename Derived >`
`Derived::Scalar qpp::trace (const Eigen::MatrixBase< Derived > &A)`
Trace.
- `template<typename Derived >`
`Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > &A)`
Determinant.
- `template<typename Derived >`
`Derived::Scalar qpp::logdet (const Eigen::MatrixBase< Derived > &A)`
Logarithm of the determinant.
- `template<typename Derived >`
`Derived::Scalar qpp::sum (const Eigen::MatrixBase< Derived > &A)`
Element-wise sum of A.
- `template<typename Derived >`
`Derived::Scalar qpp::prod (const Eigen::MatrixBase< Derived > &A)`
Element-wise product of A.
- `template<typename Derived >`
`double qpp::norm (const Eigen::MatrixBase< Derived > &A)`
Frobenius norm.
- `template<typename Derived >`
`std::pair< dyn_col_vect< cplx >, cmat > qpp::eig (const Eigen::MatrixBase< Derived > &A)`
Full eigen decomposition.
- `template<typename Derived >`
`dyn_col_vect< cplx > qpp::evals (const Eigen::MatrixBase< Derived > &A)`
Eigenvalues.
- `template<typename Derived >`
`cmat qpp::evecs (const Eigen::MatrixBase< Derived > &A)`
Eigenvectors.
- `template<typename Derived >`
`std::pair< dyn_col_vect< double >, cmat > qpp::heig (const Eigen::MatrixBase< Derived > &A)`
Full eigen decomposition of Hermitian expression.
- `template<typename Derived >`
`dyn_col_vect< double > qpp::hevals (const Eigen::MatrixBase< Derived > &A)`
Hermitian eigenvalues.
- `template<typename Derived >`
`cmat qpp::hevecs (const Eigen::MatrixBase< Derived > &A)`
Hermitian eigenvectors.
- `template<typename Derived >`
`std::tuple< cmat, dyn_col_vect< double >, cmat > qpp::svd (const Eigen::MatrixBase< Derived > &A)`
Full singular value decomposition.
- `template<typename Derived >`
`dyn_col_vect< double > qpp::svals (const Eigen::MatrixBase< Derived > &A)`
Singular values.
- `template<typename Derived >`
`cmat qpp::svdU (const Eigen::MatrixBase< Derived > &A)`
Left singular vectors.
- `template<typename Derived >`
`cmat qpp::svdV (const Eigen::MatrixBase< Derived > &A)`
Right singular vectors.
- `template<typename Derived >`
`cmat qpp::funm (const Eigen::MatrixBase< Derived > &A, cplx(*f)(const cplx &))`

- Functional calculus $f(A)$*

 - `template<typename Derived >`
`cmat qpp::sqrtm (const Eigen::MatrixBase< Derived > &A)`
Matrix square root.
 - `template<typename Derived >`
`cmat qpp::absm (const Eigen::MatrixBase< Derived > &A)`
Matrix absolut value.
 - `template<typename Derived >`
`cmat qpp::expm (const Eigen::MatrixBase< Derived > &A)`
Matrix exponential.
 - `template<typename Derived >`
`cmat qpp::logm (const Eigen::MatrixBase< Derived > &A)`
Matrix logarithm.
 - `template<typename Derived >`
`cmat qpp::sinm (const Eigen::MatrixBase< Derived > &A)`
Matrix sin.
 - `template<typename Derived >`
`cmat qpp::cosm (const Eigen::MatrixBase< Derived > &A)`
Matrix cos.
 - `template<typename Derived >`
`cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived > &A, const cplx z)`
Matrix power.
 - `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::powm (const Eigen::MatrixBase< Derived > &A, idx n)`
Matrix power.
 - `template<typename Derived >`
`double qpp::schatten (const Eigen::MatrixBase< Derived > &A, double p)`
Schatten matrix norm.
 - `template<typename OutputScalar , typename Derived >`
`dyn_mat< OutputScalar > qpp::cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const typename Derived::Scalar &))`
Functor.
 - `template<typename T >`
`dyn_mat< typename T::Scalar > qpp::kron (const T &head)`
Kronecker product.
 - `template<typename T , typename... Args>`
`dyn_mat< typename T::Scalar > qpp::kron (const T &head, const Args &...tail)`
Kronecker product.
 - `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::kron (const std::vector< Derived > &As)`
Kronecker product.
 - `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::kron (const std::initializer_list< Derived > &As)`
Kronecker product.
 - `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::kronpow (const Eigen::MatrixBase< Derived > &A, idx n)`
Kronecker power.
 - `template<typename T >`
`dyn_mat< typename T::Scalar > qpp::dirsum (const T &head)`
Direct sum.
 - `template<typename T , typename... Args>`
`dyn_mat< typename T::Scalar > qpp::dirsum (const T &head, const Args &...tail)`
Direct sum.

- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::dirsum (const std::vector< Derived > &As)`
Direct sum.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::dirsum (const std::initializer_list< Derived > &As)`
Direct sum.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::dirsumpow (const Eigen::MatrixBase< Derived > &A, idx n)`
Direct sum power.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::reshape (const Eigen::MatrixBase< Derived > &A, idx rows, idx cols)`
Reshape.
- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > qpp::comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
Commutator.
- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > qpp::anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
Anti-commutator.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::prj (const Eigen::MatrixBase< Derived > &V)`
Projector.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::grams (const std::vector< Derived > &Vs)`
Gram-Schmidt orthogonalization.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::grams (const std::initializer_list< Derived > &Vs)`
Gram-Schmidt orthogonalization.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::grams (const Eigen::MatrixBase< Derived > &A)`
Gram-Schmidt orthogonalization.
- `std::vector< idx > qpp::n2multiidx (idx n, const std::vector< idx > &dims)`
Non-negative integer index to multi-index.
- `idx qpp::multiidx2n (const std::vector< idx > &midx, const std::vector< idx > &dims)`
Multi-index to non-negative integer index.
- `ket qpp::mket (const std::vector< idx > &mask, const std::vector< idx > &dims)`
Multi-partite qudit ket.
- `ket qpp::mket (const std::vector< idx > &mask, idx d=2)`
Multi-partite qudit ket.
- `cmat qpp::mprj (const std::vector< idx > &mask, const std::vector< idx > &dims)`
Projector onto multi-partite qudit ket.
- `cmat qpp::mprj (const std::vector< idx > &mask, idx d=2)`
Projector onto multi-partite qudit ket.
- `template<typename InputIterator >`
`std::vector< double > qpp::abssq (InputIterator first, InputIterator last)`
Computes the absolute values squared of an STL-like range of complex numbers.
- `template<typename Container >`
`std::vector< double > qpp::abssq (const Container &c, typename std::enable_if< is_iterable< Container >::value >::type * = nullptr)`
Computes the absolute values squared of an STL-like container.

- `template<typename Derived >`
`std::vector< double > qpp::abssq (const Eigen::MatrixBase< Derived > &A)`
Computes the absolute values squared of an Eigen expression.
- `template<typename InputIterator >`
`std::iterator_traits< InputIterator >::value_type qpp::sum (InputIterator first, InputIterator last)`
Element-wise sum of an STL-like range.
- `template<typename Container >`
`Container::value_type qpp::sum (const Container &c)`
Element-wise sum of the elements of an STL-like container.
- `template<typename InputIterator >`
`std::iterator_traits< InputIterator >::value_type qpp::prod (InputIterator first, InputIterator last)`
Element-wise product of an STL-like range.
- `template<typename Container >`
`Container::value_type qpp::prod (const Container &c)`
Element-wise product of the elements of an STL-like container.
- `template<typename Derived >`
`dyn_col_vect< typename Derived::Scalar > qpp::rho2pure (const Eigen::MatrixBase< Derived > &A)`
Finds the pure state representation of a matrix proportional to a projector onto a pure state.
- `template<typename T >`
`std::vector< T > qpp::complement (std::vector< T > subsys, idx N)`
Constructs the complement of a subsystem vector.
- `template<typename Derived >`
`std::vector< double > qpp::rho2bloch (const Eigen::MatrixBase< Derived > &A)`
Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix A.
- `cmat qpp::bloch2rho (const std::vector< double > &r)`
Computes the density matrix corresponding to the 3-dimensional real Bloch vector r.

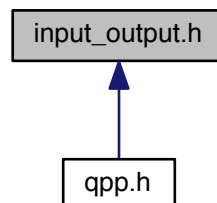
8.13.1 Detailed Description

Generic quantum computing functions.

8.14 input_output.h File Reference

Input/output functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)

Quantum++ main namespace.

Functions

- `template<typename Derived >`
`internal::IOManipEigen qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)`
Eigen expression ostream manipulator.
- `internal::IOManipEigen qpp::disp (cplx z, double chop=qpp::chop)`
Complex number ostream manipulator.
- `template<typename InputIterator >`
`internal::IOManipRange< InputIterator > qpp::disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[" , const std::string &end="]")`
Range ostream manipulator.
- `template<typename Container >`
`internal::IOManipRange< typename Container::const_iterator > qpp::disp (const Container &c, const std::string &separator, const std::string &start="[" , const std::string &end="]")`
Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.
- `template<typename PointerType >`
`internal::IOManipPointer< PointerType > qpp::disp (const PointerType *p, idx n, const std::string &separator, const std::string &start="[" , const std::string &end="]")`
C-style pointer ostream manipulator.
- `template<typename Derived >`
`void qpp::save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)`
Saves Eigen expression to a binary file (internal format) in double precision.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::load (const std::string &fname)`
Loads Eigen matrix from a binary file (internal format) in double precision.

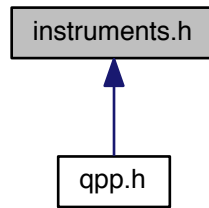
8.14.1 Detailed Description

Input/output functions.

8.15 instruments.h File Reference

Measurement functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.

Functions

- `template<typename Derived >`
`dyn_col_vect< typename Derived::Scalar > qpp::ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, const std::vector< idx > &dims)`
Generalized inner product.
- `template<typename Derived >`
`dyn_col_vect< typename Derived::Scalar > qpp::ip (const Eigen::MatrixBase< Derived > &phi, const Eigen::MatrixBase< Derived > &psi, const std::vector< idx > &subsys, idx d=2)`
Generalized inner product.
- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks)`
Measures the state A using the set of Kraus operators Ks.
- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)`
Measures the state A using the set of Kraus operators Ks.
- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &U)`
Measures the state A in the orthonormal basis specified by the unitary matrix U.
- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)`
Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)`
Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure` (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)
Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure` (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, idx d=2)
Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.
- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure` (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, const std::vector< idx > &dims)
Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- `template<typename Derived >`
`std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure` (const Eigen::MatrixBase< Derived > &A, const cmat &V, const std::vector< idx > &subsys, idx d=2)
Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis or rank-1 POVM specified by the matrix V.
- `template<typename Derived >`
`std::tuple< std::vector< idx >, double, cmat > qpp::measure_seq` (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, std::vector< idx > dims)
Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.
- `template<typename Derived >`
`std::tuple< std::vector< idx >, double, cmat > qpp::measure_seq` (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, idx d=2)
Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.

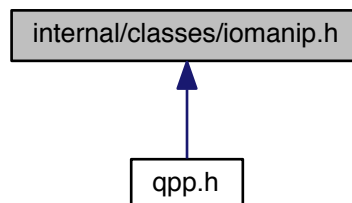
8.15.1 Detailed Description

Measurement functions.

8.16 internal/classes/iomanip.h File Reference

Input/output manipulators.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::internal::IOManipRange< InputIterator >](#)
- class [qpp::internal::IOManipPointer< PointerType >](#)
- class [qpp::internal::IOManipEigen](#)

Namespaces

- [qpp](#)
Quantum++ main namespace.
- [qpp::internal](#)
Internal utility functions, do not use/modify.

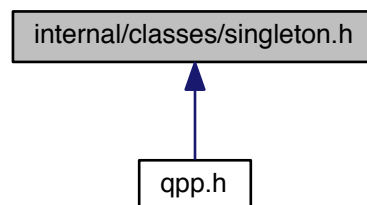
8.16.1 Detailed Description

Input/output manipulators.

8.17 internal/classes/singleton.h File Reference

Singleton pattern via CRTP.

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::internal::Singleton< T >](#)
[Singleton](#) policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

Namespaces

- [qpp](#)
Quantum++ main namespace.
- [qpp::internal](#)
Internal utility functions, do not use/modify.

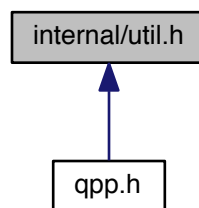
8.17.1 Detailed Description

Singleton pattern via CRTP.

8.18 internal/util.h File Reference

Internal utility functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.
- [qpp::internal](#)
Internal utility functions, do not use/modify.

Functions

- void [qpp::internal::_n2multiidx](#) (idx n, idx numdims, const idx *dims, idx *result) noexcept
- idx [qpp::internal::_multiidx2n](#) (const idx *midx, idx numdims, const idx *dims) noexcept
- template<typename Derived >
bool [qpp::internal::_check_square_mat](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [qpp::internal::_check_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [qpp::internal::_check_rvector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [qpp::internal::_check_cvector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename T >
bool [qpp::internal::_check_nonzero_size](#) (const T &x) noexcept
- template<typename T1 , typename T2 >
bool [qpp::internal::_check_matching_sizes](#) (const T1 &lhs, const T2 &rhs) noexcept
- bool [qpp::internal::_check_dims](#) (const std::vector< idx > &dims)
- template<typename Derived >
bool [qpp::internal::_check_dims_match_mat](#) (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [qpp::internal::_check_dims_match_cvect](#) (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &V)

- `template<typename Derived >`
`bool qpp::internal::_check_dims_match_rvect (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &V)`
- `bool qpp::internal::_check_eq_dims (const std::vector< idx > &dims, idx dim) noexcept`
- `bool qpp::internal::_check_subsys_match_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)`
- `template<typename Derived >`
`bool qpp::internal::_check_qubit_matrix (const Eigen::MatrixBase< Derived > &A) noexcept`
- `template<typename Derived >`
`bool qpp::internal::_check_qubit_cvector (const Eigen::MatrixBase< Derived > &V) noexcept`
- `template<typename Derived >`
`bool qpp::internal::_check_qubit_rvector (const Eigen::MatrixBase< Derived > &V) noexcept`
- `template<typename Derived >`
`bool qpp::internal::_check_qubit_vector (const Eigen::MatrixBase< Derived > &V) noexcept`
- `bool qpp::internal::_check_perm (const std::vector< idx > &perm)`
- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > qpp::internal::_kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > qpp::internal::_dirsum2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
- `template<typename T >`
`void qpp::internal::variadic_vector_emplace (std::vector< T > &)`
- `template<typename T , typename First , typename... Args>`
`void qpp::internal::variadic_vector_emplace (std::vector< T > &v, First &&first, Args &&...args)`

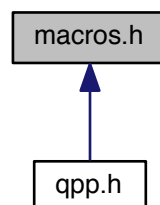
8.18.1 Detailed Description

Internal utility functions.

8.19 macros.h File Reference

Preprocessor macros.

This graph shows which files directly or indirectly include this file:



Macros

- `#define PRINT(x)`
- `#define PRINTLN(x)`

- `#define ERROR(x)`
- `#define ERRORLN(x)`

8.19.1 Detailed Description

Preprocessor macros.

8.19.2 Macro Definition Documentation

8.19.2.1 `#define ERROR(x)`

Prints an error message to `std::cerr`

8.19.2.2 `#define ERRORLN(x)`

Prints an error message to `std::cerr` and adds a new line

8.19.2.3 `#define PRINT(x)`

Prints a message

8.19.2.4 `#define PRINTLN(x)`

Prints a message and adds a new line

8.20 MATLAB/matlab.h File Reference

Input/output interfacing with MATLAB.

```
#include "mat.h"
#include "mex.h"
```

Namespaces

- [qpp](#)
Quantum++ main namespace.

Functions

- `template<typename Derived >`
`Derived qpp::loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`
Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.
- `template<>`
`dmat qpp::loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`
Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))
- `template<>`
`cmat qpp::loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`
Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))

- `template<typename Derived >`
`void qpp::saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`
Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.
- `template<>`
`void qpp::saveMATLABmatrix (const Eigen::MatrixBase< dmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`
Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices ([qpp::dmat](#))
- `template<>`
`void qpp::saveMATLABmatrix (const Eigen::MatrixBase< cmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`
Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices ([qpp::cmat](#))

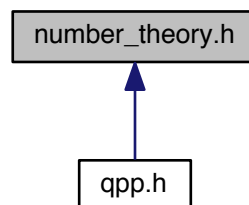
8.20.1 Detailed Description

Input/output interfacing with MATLAB.

8.21 number_theory.h File Reference

Number theory functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.

Functions

- `std::vector< int > qpp::x2contfrac (double x, idx n, idx cut=1e5)`
Simple continued fraction expansion.
- `double qpp::contfrac2x (const std::vector< int > &cf, idx n)`
Real representation of a simple continued fraction.
- `double qpp::contfrac2x (const std::vector< int > &cf)`
Real representation of a simple continued fraction.
- `ubigint qpp::gcd (ubigint m, ubigint n)`

Greatest common divisor of two non-negative integers.

- ubigint [qpp::gcd](#) (const std::vector< ubigint > &ns)

Greatest common divisor of a list of non-negative integers.

- ubigint [qpp::lcm](#) (ubigint m, ubigint n)

Least common multiple of two positive integers.

- ubigint [qpp::lcm](#) (const std::vector< ubigint > &ns)

Least common multiple of a list of positive integers.

- std::vector< idx > [qpp::invperm](#) (const std::vector< idx > &perm)

Inverse permutation.

- std::vector< idx > [qpp::compperm](#) (const std::vector< idx > &perm, const std::vector< idx > &sigma)

Compose permutations.

- std::vector< ubigint > [qpp::factors](#) (ubigint n)

Prime factor decomposition.

- bool [qpp::isprime](#) (ubigint n)

Primality test.

- ubigint [qpp::modpow](#) (ubigint a, ubigint n, ubigint p)

Integer power modulo p.

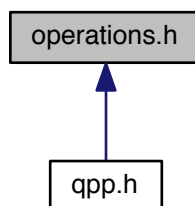
8.21.1 Detailed Description

Number theory functions.

8.22 operations.h File Reference

Quantum operation functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)

Quantum++ main namespace.

Functions

- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state,`
`const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys,`
`const std::vector< idx > &dims)`
Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state,`
`const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys,`
`idx d=2)`
Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.
- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const`
`Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)`
Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- `template<typename Derived1 , typename Derived2 >`
`dyn_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const`
`Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, idx d=2)`
Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.
- `template<typename Derived >`
`cmat qpp::apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks)`
Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.
- `template<typename Derived >`
`cmat qpp::apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< idx > &subsys,`
`const std::vector< idx > &dims)`
Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix rho.
- `template<typename Derived >`
`cmat qpp::apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< idx > &subsys,`
`idx d=2)`
Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix rho.
- `cmat qpp::kraus2super (const std::vector< cmat > &Ks)`
Superoperator matrix.
- `cmat qpp::kraus2choi (const std::vector< cmat > &Ks)`
Choi matrix.
- `std::vector< cmat > qpp::choi2kraus (const cmat &A)`
Orthogonal Kraus operators from Choi matrix.
- `cmat qpp::choi2super (const cmat &A)`
Converts Choi matrix to superoperator matrix.
- `cmat qpp::super2choi (const cmat &A)`
Converts superoperator matrix to Choi matrix.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Partial trace.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)`
Partial trace.
- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys,`
`const std::vector< idx > &dims)`

Partial trace.

- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)`

Partial trace.

- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)`

Partial transpose.

- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsys, idx d=2)`

Partial transpose.

- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, const std::vector< idx > &dims)`

Subsystem permutation.

- `template<typename Derived >`
`dyn_mat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &perm, idx d=2)`

Subsystem permutation.

8.22.1 Detailed Description

Quantum operation functions.

8.23 qpp.h File Reference

Quantum++ main header file, includes all other necessary headers.

```

#include <algorithm>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <ctime>
#include <exception>
#include <fstream>
#include <functional>
#include <initializer_list>
#include <iomanip>
#include <iostream>
#include <iterator>
#include <limits>
#include <numeric>
#include <ostream>
#include <random>
#include <sstream>
#include <stdexcept>
#include <string>
#include <tuple>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "types.h"
#include "classes/exception.h"
#include "constants.h"
#include "traits.h"
#include "classes/ideisplay.h"
#include "internal/util.h"
#include "internal/classes/iomanip.h"
#include "input_output.h"
#include "internal/classes/singleton.h"
#include "classes/init.h"
#include "functions.h"
#include "classes/codes.h"
#include "classes/gates.h"
#include "classes/states.h"
#include "classes/random_devices.h"
#include "statistics.h"
#include "operations.h"
#include "entropies.h"
#include "entanglement.h"
#include "random.h"
#include "classes/timer.h"
#include "instruments.h"
#include "number_theory.h"
#include "macros.h"

```

Namespaces

- [qpp](#)

Quantum++ main namespace.

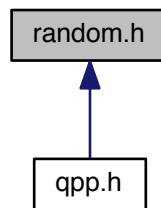
8.23.1 Detailed Description

Quantum++ main header file, includes all other necessary headers.

8.24 random.h File Reference

Randomness-related functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.

Functions

- double [qpp::rand](#) (double a=0, double b=1)
Generates a random real number uniformly distributed in the interval [a, b]
- bigint [qpp::rand](#) (bigint a=std::numeric_limits< bigint >::min(), bigint b=std::numeric_limits< bigint >::max())
Generates a random big integer uniformly distributed in the interval [a, b].
- ubigint [qpp::rand](#) (ubigint a=std::numeric_limits< ubigint >::min(), ubigint b=std::numeric_limits< ubigint >::max())
Generates a random non-negative big integer uniformly distributed in the interval [a, b].
- idx [qpp::randidx](#) (idx a=std::numeric_limits< idx >::min(), idx b=std::numeric_limits< idx >::max())
Generates a random index (idx) uniformly distributed in the interval [a, b].
- template<typename Derived >
Derived [qpp::rand](#) (idx rows, idx cols, double a=0, double b=1)
Generates a random matrix with entries uniformly distributed in the interval [a, b]
- template<>
dmat [qpp::rand](#) (idx rows, idx cols, double a, double b)
Generates a random real matrix with entries uniformly distributed in the interval [a, b], specialization for double matrices ([qpp::dmat](#))
- template<>
cmat [qpp::rand](#) (idx rows, idx cols, double a, double b)
Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b], specialization for complex matrices ([qpp::cmat](#))

- `template<typename Derived >`
`Derived qpp::randn (idx rows, idx cols, double mean=0, double sigma=1)`
Generates a random matrix with entries normally distributed in $N(\text{mean}, \text{sigma})$
- `template<>`
`dmat qpp::randn (idx rows, idx cols, double mean, double sigma)`
Generates a random real matrix with entries normally distributed in $N(\text{mean}, \text{sigma})$, specialization for double matrices (`qpp::dmat`)
- `template<>`
`cmat qpp::randn (idx rows, idx cols, double mean, double sigma)`
Generates a random complex matrix with entries (both real and imaginary) normally distributed in $N(\text{mean}, \text{sigma})$, specialization for complex matrices (`qpp::cmat`)
- `double qpp::randn (double mean=0, double sigma=1)`
Generates a random real number (double) normally distributed in $N(\text{mean}, \text{sigma})$
- `cmat qpp::randU (idx D)`
Generates a random unitary matrix.
- `cmat qpp::randV (idx Din, idx Dout)`
Generates a random isometry matrix.
- `std::vector< cmat > qpp::randkraus (idx N, idx D)`
Generates a set of random Kraus operators.
- `cmat qpp::randH (idx D)`
Generates a random Hermitian matrix.
- `ket qpp::randket (idx D)`
Generates a random normalized ket (pure state vector)
- `cmat qpp::randrho (idx D)`
Generates a random density matrix.
- `std::vector< idx > qpp::randperm (idx n)`
Generates a random uniformly distributed permutation.

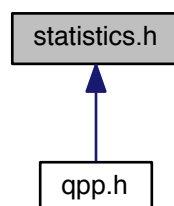
8.24.1 Detailed Description

Randomness-related functions.

8.25 statistics.h File Reference

Statistics functions.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.

Functions

- `std::vector< double > qpp::uniform (idx N)`
Uniform probability distribution vector.
- `std::vector< double > qpp::marginalX (const dmat &probXY)`
Marginal distribution.
- `std::vector< double > qpp::marginalY (const dmat &probXY)`
Marginal distribution.
- `template<typename Container >`
`double qpp::avg (const std::vector< double > &prob, const Container &X)`
Average.
- `template<typename Container >`
`double qpp::cov (const dmat &probXY, const Container &X, const Container &Y)`
Covariance.
- `template<typename Container >`
`double qpp::var (const std::vector< double > &prob, const Container &X)`
Variance.
- `template<typename Container >`
`double qpp::sigma (const std::vector< double > &prob, const Container &X)`
Standard deviation.
- `template<typename Container >`
`double qpp::cor (const dmat &probXY, const Container &X, const Container &Y)`
Correlation.

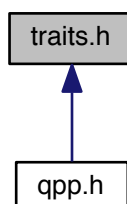
8.25.1 Detailed Description

Statistics functions.

8.26 traits.h File Reference

Type traits.

This graph shows which files directly or indirectly include this file:



Classes

- struct `qpp::is_iterable< T, typename >`
Checks whether *T* is compatible with an STL-like iterable container.
- struct `qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value_type > >`
Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers.
- struct `qpp::is_matrix_expression< Derived >`
Checks whether the type is an Eigen matrix expression.
- struct `qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived > >`
Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.
- struct `qpp::is_complex< T >`
Checks whether the type is a complex type.
- struct `qpp::is_complex< std::complex< T > >`
Checks whether the type is a complex number type, specialization for complex types.

Namespaces

- `qpp`
Quantum++ main namespace.

Typedefs

- `template<typename... >`
using `qpp::to_void` = void
Alias template that implements the proposal for `void_t`.

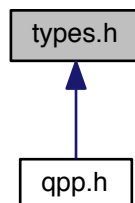
8.26.1 Detailed Description

Type traits.

8.27 types.h File Reference

Type aliases.

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)
Quantum++ main namespace.

Typedefs

- using [qpp::idx](#) = std::size_t
Non-negative integer index.
- using [qpp::bigint](#) = long long int
Big integer.
- using [qpp::ubigint](#) = unsigned long long int
Non-negative big integer.
- using [qpp::cplx](#) = std::complex< double >
Complex number in double precision.
- using [qpp::ket](#) = Eigen::VectorXcd
Complex (double precision) dynamic Eigen column vector.
- using [qpp::bra](#) = Eigen::RowVectorXcd
Complex (double precision) dynamic Eigen row vector.
- using [qpp::cmat](#) = Eigen::MatrixXcd
Complex (double precision) dynamic Eigen matrix.
- using [qpp::dmat](#) = Eigen::MatrixXd
Real (double precision) dynamic Eigen matrix.
- template<typename Scalar >
using [qpp::dyn_mat](#) = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >
Dynamic Eigen matrix over the field specified by Scalar.
- template<typename Scalar >
using [qpp::dyn_col_vect](#) = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >
Dynamic Eigen column vector over the field specified by Scalar.
- template<typename Scalar >
using [qpp::dyn_row_vect](#) = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >
Dynamic Eigen row vector over the field specified by Scalar.

8.27.1 Detailed Description

Type aliases.

Index

- [_A](#)
 - [qpp::internal::IOManipEigen, 100](#)
 - [_check_cvector](#)
 - [qpp::internal, 81](#)
 - [_check_dims](#)
 - [qpp::internal, 81](#)
 - [_check_dims_match_cvect](#)
 - [qpp::internal, 81](#)
 - [_check_dims_match_mat](#)
 - [qpp::internal, 82](#)
 - [_check_dims_match_rvect](#)
 - [qpp::internal, 82](#)
 - [_check_eq_dims](#)
 - [qpp::internal, 82](#)
 - [_check_matching_sizes](#)
 - [qpp::internal, 82](#)
 - [_check_nonzero_size](#)
 - [qpp::internal, 82](#)
 - [_check_perm](#)
 - [qpp::internal, 82](#)
 - [_check_qubit_cvector](#)
 - [qpp::internal, 82](#)
 - [_check_qubit_matrix](#)
 - [qpp::internal, 82](#)
 - [_check_qubit_rvector](#)
 - [qpp::internal, 82](#)
 - [_check_qubit_vector](#)
 - [qpp::internal, 82](#)
 - [_check_rvector](#)
 - [qpp::internal, 82](#)
 - [_check_square_mat](#)
 - [qpp::internal, 82](#)
 - [_check_subsys_match_dims](#)
 - [qpp::internal, 82](#)
 - [_check_vector](#)
 - [qpp::internal, 82](#)
 - [_chop](#)
 - [qpp::internal::IOManipEigen, 100](#)
 - [_construct_exception_msg](#)
 - [qpp::Exception, 88](#)
 - [_custom](#)
 - [qpp::Exception, 89](#)
 - [_dirsum2](#)
 - [qpp::internal, 82](#)
 - [_end](#)
 - [qpp::Timer, 122](#)
 - [qpp::internal::IOManipPointer, 102](#)
 - [qpp::internal::IOManipRange, 104](#)
 - [_first](#)
 - [qpp::internal::IOManipRange, 104](#)
 - [_kron2](#)
 - [qpp::internal, 82](#)
 - [_last](#)
 - [qpp::internal::IOManipRange, 104](#)
 - [_msg](#)
 - [qpp::Exception, 89](#)
 - [_multiidx2n](#)
 - [qpp::internal, 82](#)
 - [_n](#)
 - [qpp::internal::IOManipPointer, 102](#)
 - [_n2multiidx](#)
 - [qpp::internal, 82](#)
 - [_p](#)
 - [qpp::internal::IOManipPointer, 102](#)
 - [_rd](#)
 - [qpp::RandomDevices, 112](#)
 - [_rng](#)
 - [qpp::RandomDevices, 112](#)
 - [_separator](#)
 - [qpp::internal::IOManipPointer, 102](#)
 - [qpp::internal::IOManipRange, 104](#)
 - [_start](#)
 - [qpp::Timer, 122](#)
 - [qpp::internal::IOManipPointer, 102](#)
 - [qpp::internal::IOManipRange, 104](#)
 - [_type](#)
 - [qpp::Exception, 89](#)
 - [_where](#)
 - [qpp::Exception, 89](#)
 - [~Codes](#)
 - [qpp::Codes, 84](#)
 - [~Gates](#)
 - [qpp::Gates, 91](#)
 - [~IDisplay](#)
 - [qpp::IDisplay, 96](#)
 - [~Init](#)
 - [qpp::Init, 98](#)
 - [~RandomDevices](#)
 - [qpp::RandomDevices, 112](#)
 - [~Singleton](#)
 - [qpp::internal::Singleton, 114](#)
 - [~States](#)
 - [qpp::States, 116](#)
 - [~Timer](#)
 - [qpp::Timer, 120](#)
- [absm](#)
 - [qpp, 26](#)
- [abssq](#)

- qpp, 26
- adjoint
 - qpp, 28
- anticomm
 - qpp, 28
- apply
 - qpp, 28–30
- applyCTRL
 - qpp, 30
- avg
 - qpp, 31
- b00
 - qpp::States, 116
- b01
 - qpp::States, 116
- b10
 - qpp::States, 117
- b11
 - qpp::States, 117
- bigint
 - qpp, 25
- bloch2rho
 - qpp, 31
- bra
 - qpp, 25
- CNOT
 - qpp::Gates, 94
- CNOTba
 - qpp::Gates, 94
- CTRL
 - qpp::Gates, 91
- CUSTOM_EXCEPTION
 - qpp::Exception, 88
- CZ
 - qpp::Gates, 94
- choi2kraus
 - qpp, 31
- choi2super
 - qpp, 32
- chop
 - qpp, 79
- classes/codes.h, 123
- classes/exception.h, 123
- classes/gates.h, 124
- classes/ideisplay.h, 125
- classes/init.h, 126
- classes/random_devices.h, 126
- classes/states.h, 127
- classes/timer.h, 128
- cmat
 - qpp, 25
- Codes
 - qpp::Codes, 84
- codeword
 - qpp::Codes, 85
- comm
 - qpp, 32
- complement
 - qpp, 32
- compperm
 - qpp, 33
- concurrency
 - qpp, 33
- conjugate
 - qpp, 33
- constants.h, 128
- contfrac2x
 - qpp, 33, 34
- cor
 - qpp, 34
- cosm
 - qpp, 34
- cov
 - qpp, 34
- cplx
 - qpp, 25
- cwise
 - qpp, 35
- DIMS_INVALID
 - qpp::Exception, 87
- DIMS_MISMATCH_CVECTOR
 - qpp::Exception, 87
- DIMS_MISMATCH_MATRIX
 - qpp::Exception, 87
- DIMS_MISMATCH_RVECTOR
 - qpp::Exception, 87
- DIMS_MISMATCH_VECTOR
 - qpp::Exception, 87
- DIMS_NOT_EQUAL
 - qpp::Exception, 87
- det
 - qpp, 35
- dirsum
 - qpp, 35, 36
- dirsumpow
 - qpp, 36
- disp
 - qpp, 37, 38
- display
 - qpp::IDisplay, 97
 - qpp::Timer, 121
 - qpp::internal::IOManipEigen, 100
 - qpp::internal::IOManipPointer, 102
 - qpp::internal::IOManipRange, 104
- dmat
 - qpp, 25
- dyn_col_vect
 - qpp, 25
- dyn_mat
 - qpp, 25
- dyn_row_vect
 - qpp, 25
- ERROR
 - macros.h, 143

- ERRORLN
 - macros.h, [143](#)
- ee
 - qpp, [79](#)
- eig
 - qpp, [38](#)
- entanglement
 - qpp, [39](#)
- entanglement.h, [129](#)
- entropies.h, [130](#)
- entropy
 - qpp, [39](#)
- eps
 - qpp, [80](#)
- evals
 - qpp, [39](#)
- evects
 - qpp, [40](#)
- Exception
 - qpp::Exception, [88](#)
- expandout
 - qpp::Gates, [92](#)
- experimental/experimental.h, [132](#)
- expm
 - qpp, [40](#)
- FIVE_QUBIT
 - qpp::Codes, [84](#)
- FRED
 - qpp::Gates, [94](#)
- factors
 - qpp, [40](#)
- Fd
 - qpp::Gates, [92](#)
- functions.h, [132](#)
- funm
 - qpp, [41](#)
- GHZ
 - qpp::States, [117](#)
- Gates
 - qpp::Gates, [91](#)
- gcd
 - qpp, [41](#)
- gconcurrency
 - qpp, [41](#)
- get_duration
 - qpp::Timer, [121](#)
- get_instance
 - qpp::internal::Singleton, [114](#)
- get_thread_local_instance
 - qpp::internal::Singleton, [114](#)
- grams
 - qpp, [42](#)
- H
 - qpp::Gates, [94](#)
- heig
 - qpp, [43](#)
- hevals
 - qpp, [43](#)
- hevects
 - qpp, [43](#)
- IDisplay
 - qpp::IDisplay, [96](#)
- IOManipEigen
 - qpp::internal::IOManipEigen, [100](#)
- IOManipPointer
 - qpp::internal::IOManipPointer, [101](#)
- IOManipRange
 - qpp::internal::IOManipRange, [103](#)
- Id
 - qpp::Gates, [93](#)
- Id2
 - qpp::Gates, [94](#)
- idx
 - qpp, [25](#)
- infty
 - qpp, [80](#)
- Init
 - qpp::Init, [98](#)
- input_output.h, [136](#)
- instruments.h, [137](#)
- internal/classes/iomanip.h, [139](#)
- internal/classes/singleton.h, [140](#)
- internal/util.h, [141](#)
- internal::Singleton< const Codes >
 - qpp::Codes, [85](#)
- internal::Singleton< const Gates >
 - qpp::Gates, [94](#)
- internal::Singleton< const Init >
 - qpp::Init, [98](#)
- internal::Singleton< const States >
 - qpp::States, [116](#)
- internal::Singleton< RandomDevices >
 - qpp::RandomDevices, [112](#)
- inverse
 - qpp, [44](#)
- invperm
 - qpp, [44](#)
- ip
 - qpp, [44](#)
- isprime
 - qpp, [45](#)
- ket
 - qpp, [25](#)
- kraus2choi
 - qpp, [45](#)
- kraus2super
 - qpp, [45](#)
- kron
 - qpp, [46](#), [47](#)
- kronpow
 - qpp, [47](#)
- lcm

- qpp, 47, 48
- load
 - qpp, 48
- loadMATLABmatrix
 - qpp, 48, 49
- logdet
 - qpp, 49
- logm
 - qpp, 50
- lognegativity
 - qpp, 50
- MATLAB/matlab.h, 143
- MATRIX_MISMATCH_SUBSYS
 - qpp::Exception, 87
- MATRIX_NOT_CVECTOR
 - qpp::Exception, 87
- MATRIX_NOT_RVECTOR
 - qpp::Exception, 87
- MATRIX_NOT_SQUARE
 - qpp::Exception, 87
- MATRIX_NOT_SQUARE_OR_CVECTOR
 - qpp::Exception, 87
- MATRIX_NOT_SQUARE_OR_RVECTOR
 - qpp::Exception, 87
- MATRIX_NOT_SQUARE_OR_VECTOR
 - qpp::Exception, 87
- MATRIX_NOT_VECTOR
 - qpp::Exception, 87
- macros.h, 142
 - ERROR, 143
 - ERRORLN, 143
 - PRINT, 143
 - PRINTLN, 143
- marginalX
 - qpp, 50
- marginalY
 - qpp, 50
- maxn
 - qpp, 80
- measure
 - qpp, 51–54
- measure_seq
 - qpp, 54, 55
- mket
 - qpp, 55, 56
- modpow
 - qpp, 56
- mprj
 - qpp, 56
- multiidx2n
 - qpp, 58
- n2multiidx
 - qpp, 58
- NINE_QUBIT_SHOR
 - qpp::Codes, 84
- NO_CODEWORD
 - qpp::Exception, 88
- NOT_BIPARTITE
 - qpp::Exception, 88
- NOT_QUBIT_CVECTOR
 - qpp::Exception, 88
- NOT_QUBIT_MATRIX
 - qpp::Exception, 88
- NOT_QUBIT_RVECTOR
 - qpp::Exception, 88
- NOT_QUBIT_SUBSYS
 - qpp::Exception, 88
- NOT_QUBIT_VECTOR
 - qpp::Exception, 88
- negativity
 - qpp, 58
- norm
 - qpp, 59
- number_theory.h, 144
- OUT_OF_RANGE
 - qpp::Exception, 88
- omega
 - qpp, 59
- operations.h, 145
- operator<<
 - qpp::IDisplay, 97
- operator=
 - qpp::IDisplay, 97
 - qpp::Timer, 121
 - qpp::internal::IOManipPointer, 102
 - qpp::internal::IOManipRange, 104
 - qpp::internal::Singleton, 114
- operator""_i
 - qpp, 59
- PERM_INVALID
 - qpp::Exception, 87
- PERM_MISMATCH_DIMS
 - qpp::Exception, 88
- pGHZ
 - qpp::States, 117
- PRINT
 - macros.h, 143
- PRINTLN
 - macros.h, 143
- pW
 - qpp::States, 117
- pb00
 - qpp::States, 117
- pb01
 - qpp::States, 117
- pb10
 - qpp::States, 117
- pb11
 - qpp::States, 117
- pi
 - qpp, 80
- powm
 - qpp, 59
- prj

- qpp, 60
- prod
 - qpp, 60
- ptrace
 - qpp, 61
- ptrace1
 - qpp, 61
- ptrace2
 - qpp, 63
- ptranspose
 - qpp, 63
- px0
 - qpp::States, 117
- px1
 - qpp::States, 117
- py0
 - qpp::States, 117
- py1
 - qpp::States, 118
- pz0
 - qpp::States, 118
- pz1
 - qpp::States, 118
- qmutualinfo
 - qpp, 64
- qpp, 13
 - absm, 26
 - abssq, 26
 - adjoint, 28
 - anticomm, 28
 - apply, 28–30
 - applyCTRL, 30
 - avg, 31
 - bigint, 25
 - bloch2rho, 31
 - bra, 25
 - choi2kraus, 31
 - choi2super, 32
 - chop, 79
 - cmat, 25
 - comm, 32
 - complement, 32
 - comperm, 33
 - concurrence, 33
 - conjugate, 33
 - contfrac2x, 33, 34
 - cor, 34
 - cosm, 34
 - cov, 34
 - cplx, 25
 - cwise, 35
 - det, 35
 - dirsum, 35, 36
 - dirsumpow, 36
 - disp, 37, 38
 - dmat, 25
 - dyn_col_vect, 25
 - dyn_mat, 25
 - dyn_row_vect, 25
 - ee, 79
 - eig, 38
 - entanglement, 39
 - entropy, 39
 - eps, 80
 - evals, 39
 - evects, 40
 - expm, 40
 - factors, 40
 - funm, 41
 - gcd, 41
 - gconcurrency, 41
 - grams, 42
 - heig, 43
 - hevals, 43
 - hevects, 43
 - idx, 25
 - infty, 80
 - inverse, 44
 - invperm, 44
 - ip, 44
 - isprime, 45
 - ket, 25
 - kraus2choi, 45
 - kraus2super, 45
 - kron, 46, 47
 - kronpow, 47
 - lcm, 47, 48
 - load, 48
 - loadMATLABmatrix, 48, 49
 - logdet, 49
 - logm, 50
 - lognegativity, 50
 - marginalX, 50
 - marginalY, 50
 - maxn, 80
 - measure, 51–54
 - measure_seq, 54, 55
 - mket, 55, 56
 - modpow, 56
 - mprj, 56
 - multiidx2n, 58
 - n2multiidx, 58
 - negativity, 58
 - norm, 59
 - omega, 59
 - operator""_i, 59
 - pi, 80
 - powm, 59
 - prj, 60
 - prod, 60
 - ptrace, 61
 - ptrace1, 61
 - ptrace2, 63
 - ptranspose, 63
 - qmutualinfo, 64
 - rand, 64, 66

- randH, [67](#)
- randU, [70](#)
- randV, [70](#)
- randidx, [67](#)
- randket, [67](#)
- randkraus, [68](#)
- randn, [68](#), [69](#)
- randperm, [69](#)
- randrho, [69](#)
- renyi, [70](#)
- reshape, [71](#)
- rho2bloch, [71](#)
- rho2pure, [71](#)
- save, [72](#)
- saveMATLABmatrix, [72](#)
- schatten, [73](#)
- schmidtA, [73](#)
- schmidtB, [73](#)
- schmidtcoeffs, [73](#)
- schmidtprobs, [74](#)
- sigma, [74](#)
- sinm, [74](#)
- spectralpowm, [75](#)
- sqrtn, [75](#)
- sum, [75](#), [76](#)
- super2choi, [76](#)
- svals, [76](#)
- svd, [76](#)
- svdU, [77](#)
- svdV, [77](#)
- syspermute, [77](#)
- to_void, [26](#)
- trace, [78](#)
- transpose, [78](#)
- tsallis, [78](#)
- ubigint, [26](#)
- uniform, [79](#)
- var, [79](#)
- x2confrac, [79](#)
- qpp.h, [147](#)
- qpp::Codes, [83](#)
 - ~Codes, [84](#)
 - Codes, [84](#)
 - codeword, [85](#)
 - FIVE_QUBIT, [84](#)
 - internal::Singleton< const Codes >, [85](#)
 - NINE_QUBIT_SHOR, [84](#)
 - SEVEN_QUBIT_STEANE, [84](#)
 - Type, [84](#)
- qpp::Exception, [85](#)
 - _construct_exception_msg, [88](#)
 - _custom, [89](#)
 - _msg, [89](#)
 - _type, [89](#)
 - _where, [89](#)
 - CUSTOM_EXCEPTION, [88](#)
 - DIMS_INVALID, [87](#)
 - DIMS_MISMATCH_CVECTOR, [87](#)
 - DIMS_MISMATCH_MATRIX, [87](#)
 - DIMS_MISMATCH_RVECTOR, [87](#)
 - DIMS_MISMATCH_VECTOR, [87](#)
 - DIMS_NOT_EQUAL, [87](#)
 - Exception, [88](#)
 - MATRIX_MISMATCH_SUBSYS, [87](#)
 - MATRIX_NOT_CVECTOR, [87](#)
 - MATRIX_NOT_RVECTOR, [87](#)
 - MATRIX_NOT_SQUARE, [87](#)
 - MATRIX_NOT_SQUARE_OR_CVECTOR, [87](#)
 - MATRIX_NOT_SQUARE_OR_RVECTOR, [87](#)
 - MATRIX_NOT_SQUARE_OR_VECTOR, [87](#)
 - MATRIX_NOT_VECTOR, [87](#)
 - NO_CODEWORD, [88](#)
 - NOT_BIPARTITE, [88](#)
 - NOT_QUBIT_CVECTOR, [88](#)
 - NOT_QUBIT_MATRIX, [88](#)
 - NOT_QUBIT_RVECTOR, [88](#)
 - NOT_QUBIT_SUBSYS, [88](#)
 - NOT_QUBIT_VECTOR, [88](#)
 - OUT_OF_RANGE, [88](#)
 - PERM_INVALID, [87](#)
 - PERM_MISMATCH_DIMS, [88](#)
 - SIZE_MISMATCH, [88](#)
 - SUBSYS_MISMATCH_DIMS, [87](#)
 - TYPE_MISMATCH, [88](#)
 - Type, [87](#)
 - UNDEFINED_TYPE, [88](#)
 - UNKNOWN_EXCEPTION, [87](#)
 - what, [88](#)
 - ZERO_SIZE, [87](#)
- qpp::Gates, [89](#)
 - ~Gates, [91](#)
 - CNOT, [94](#)
 - CNOTba, [94](#)
 - CTRL, [91](#)
 - CZ, [94](#)
 - expandout, [92](#)
 - FRED, [94](#)
 - Fd, [92](#)
 - Gates, [91](#)
 - H, [94](#)
 - Id, [93](#)
 - Id2, [94](#)
 - internal::Singleton< const Gates >, [94](#)
 - Rn, [93](#)
 - S, [94](#)
 - SWAP, [94](#)
 - T, [94](#)
 - TOF, [94](#)
 - X, [95](#)
 - Xd, [93](#)
 - Y, [95](#)
 - Z, [95](#)
 - Zd, [93](#)
- qpp::IDisplay, [95](#)
 - ~IDisplay, [96](#)
 - display, [97](#)

- IDisplay, 96
- operator<<, 97
- operator=, 97
- qpp::Init, 97
 - ~Init, 98
 - Init, 98
 - internal::Singleton< const Init >, 98
- qpp::RandomDevices, 111
 - _rd, 112
 - _rng, 112
 - ~RandomDevices, 112
 - internal::Singleton< RandomDevices >, 112
 - RandomDevices, 112
- qpp::States, 114
 - ~States, 116
 - b00, 116
 - b01, 116
 - b10, 117
 - b11, 117
 - GHZ, 117
 - internal::Singleton< const States >, 116
 - pGHZ, 117
 - pW, 117
 - pb00, 117
 - pb01, 117
 - pb10, 117
 - pb11, 117
 - px0, 117
 - px1, 117
 - py0, 117
 - py1, 118
 - pz0, 118
 - pz1, 118
 - States, 116
 - W, 118
 - x0, 118
 - x1, 118
 - y0, 118
 - y1, 118
 - z0, 118
 - z1, 118
- qpp::Timer
 - _end, 122
 - _start, 122
 - ~Timer, 120
 - display, 121
 - get_duration, 121
 - operator=, 121
 - tic, 121
 - tics, 121
 - Timer, 120
 - toc, 122
- qpp::Timer< T, CLOCK_T >, 119
- qpp::experimental, 80
- qpp::internal, 80
 - _check_cvector, 81
 - _check_dims, 81
 - _check_dims_match_cvect, 81
 - _check_dims_match_mat, 82
 - _check_dims_match_rvect, 82
 - _check_eq_dims, 82
 - _check_matching_sizes, 82
 - _check_nonzero_size, 82
 - _check_perm, 82
 - _check_qubit_cvector, 82
 - _check_qubit_matrix, 82
 - _check_qubit_rvector, 82
 - _check_qubit_vector, 82
 - _check_rvector, 82
 - _check_square_mat, 82
 - _check_subsys_match_dims, 82
 - _check_vector, 82
 - _dirsum2, 82
 - _kron2, 82
 - _multiidx2n, 82
 - _n2multiidx, 82
 - variadic_vector_emplace, 82
- qpp::internal::IOManipEigen, 99
 - _A, 100
 - _chop, 100
 - display, 100
 - IOManipEigen, 100
- qpp::internal::IOManipPointer
 - _end, 102
 - _n, 102
 - _p, 102
 - _separator, 102
 - _start, 102
 - display, 102
 - IOManipPointer, 101
 - operator=, 102
- qpp::internal::IOManipPointer< PointerType >, 100
- qpp::internal::IOManipRange
 - _end, 104
 - _first, 104
 - _last, 104
 - _separator, 104
 - _start, 104
 - display, 104
 - IOManipRange, 103
 - operator=, 104
- qpp::internal::IOManipRange< InputIterator >, 102
- qpp::internal::Singleton
 - ~Singleton, 114
 - get_instance, 114
 - get_thread_local_instance, 114
 - operator=, 114
 - Singleton, 114
- qpp::internal::Singleton< T >, 113
- qpp::is_complex< std::complex< T > >, 105
- qpp::is_complex< T >, 104
- qpp::is_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().begin()) >, typename T::value_type > >, 107
- qpp::is_iterable< T, typename >, 106
- qpp::is_matrix_expression< Derived >, 109

qpp::is_matrix_expression< typename Eigen::Matrix<
 Base< Derived > >, 110

 rand
 qpp, 64, 66
 randH
 qpp, 67
 randU
 qpp, 70
 randV
 qpp, 70
 randidx
 qpp, 67
 randket
 qpp, 67
 randkraus
 qpp, 68
 randn
 qpp, 68, 69
 random.h, 149
 RandomDevices
 qpp::RandomDevices, 112
 randperm
 qpp, 69
 randrho
 qpp, 69
 renyi
 qpp, 70
 reshape
 qpp, 71
 rho2bloch
 qpp, 71
 rho2pure
 qpp, 71
 Rn
 qpp::Gates, 93

 S
 qpp::Gates, 94
 SEVEN_QUBIT_STEANE
 qpp::Codes, 84
 SIZE_MISMATCH
 qpp::Exception, 88
 SUBSYS_MISMATCH_DIMS
 qpp::Exception, 87
 SWAP
 qpp::Gates, 94
 save
 qpp, 72
 saveMATLABmatrix
 qpp, 72
 schatten
 qpp, 73
 schmidtA
 qpp, 73
 schmidtB
 qpp, 73
 schmidtcoeffs
 qpp, 73

 schmidtprobs
 qpp, 74
 sigma
 qpp, 74
 Singleton
 qpp::internal::Singleton, 114
 sinm
 qpp, 74
 spectralpowm
 qpp, 75
 sqrtm
 qpp, 75
 States
 qpp::States, 116
 statistics.h, 150
 sum
 qpp, 75, 76
 super2choi
 qpp, 76
 svals
 qpp, 76
 svd
 qpp, 76
 svdU
 qpp, 77
 svdV
 qpp, 77
 syspermute
 qpp, 77

 T
 qpp::Gates, 94
 TOF
 qpp::Gates, 94
 TYPE_MISMATCH
 qpp::Exception, 88
 tic
 qpp::Timer, 121
 tics
 qpp::Timer, 121
 Timer
 qpp::Timer, 120
 to_void
 qpp, 26
 toc
 qpp::Timer, 122
 trace
 qpp, 78
 traits.h, 151
 transpose
 qpp, 78
 tsallis
 qpp, 78
 Type
 qpp::Codes, 84
 qpp::Exception, 87
 types.h, 152

 UNDEFINED_TYPE

- qpp::Exception, 88
- UNKNOWN_EXCEPTION
 - qpp::Exception, 87
- ubigint
 - qpp, 26
- uniform
 - qpp, 79
- var
 - qpp, 79
- variadic_vector_emplace
 - qpp::internal, 82
- W
 - qpp::States, 118
- what
 - qpp::Exception, 88
- X
 - qpp::Gates, 95
- x0
 - qpp::States, 118
- x1
 - qpp::States, 118
- x2contfrac
 - qpp, 79
- Xd
 - qpp::Gates, 93
- Y
 - qpp::Gates, 95
- y0
 - qpp::States, 118
- y1
 - qpp::States, 118
- Z
 - qpp::Gates, 95
- z0
 - qpp::States, 118
- z1
 - qpp::States, 118
- ZERO_SIZE
 - qpp::Exception, 87
- Zd
 - qpp::Gates, 93