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## **Contents**

1	Qua	ntum++														1
2	Nam	espace	Index													5
	2.1	Names	pace List				 	 	 		 	 		 	 	 5
3	Hier	archical	Index													7
	3.1	Class I	Hierarchy				 	 	 		 	 			 	 7
4	Clas	s Index														9
	4.1	Class I	_ist				 	 			 	 			 	 9
5	File	Index														11
•	5.1		t				 	 	 		 	 			 	 11
6	Nam	neenace	Documer	ntatio	nn -											13
U	6.1	•	mespace													13
	0.1		Detailed													
		6.1.1			•											24
		6.1.2	Typedef I													24
			6.1.2.1	_	nt											24
			6.1.2.2													24
			6.1.2.3	cma	at		 	 	 		 	 ٠.	٠.		 	 25
			6.1.2.4	cplx	<b>(</b>		 	 	 		 	 			 	 25
			6.1.2.5	dma	at		 	 	 		 	 			 	 25
			6.1.2.6	dyn	_col_v	vect	 	 	 	 	 	 			 	 25
			6.1.2.7	dyn	_mat		 	 	 	 	 	 			 	 25
			6.1.2.8	dyn	_row_	_vect	 	 	 	 	 	 			 	 25
			6.1.2.9	idx			 	 	 		 	 			 	 25
			6.1.2.10	ket			 	 	 	 	 	 		 	 	 25
			6.1.2.11													25
			6.1.2.12													26
		6.1.3	Function													26
		50	6.1.3.1		sm											26
			6.1.3.2		sq											26
			J. 1. J. Z	abo	~~		 	 	 	 	 	 		 	 	 20

iv CONTENTS

6.1.3.3	abssq	26
6.1.3.4	abssq	26
6.1.3.5	adjoint	27
6.1.3.6	anticomm	28
6.1.3.7	apply	28
6.1.3.8	apply	28
6.1.3.9	apply	29
6.1.3.10	apply	29
6.1.3.11	apply	29
6.1.3.12	applyCTRL	30
6.1.3.13	applyCTRL	30
6.1.3.14	avg	31
6.1.3.15	bloch2rho	31
6.1.3.16	choi2kraus	31
6.1.3.17	choi2super	32
6.1.3.18	comm	32
6.1.3.19	complement	32
6.1.3.20	compperm	33
6.1.3.21	concurrence	34
6.1.3.22	conjugate	34
6.1.3.23	contfrac2x	34
6.1.3.24	contfrac2x	35
6.1.3.25	cor	35
6.1.3.26	cosm	35
6.1.3.27	cov	35
6.1.3.28	cwise	36
6.1.3.29	det	36
6.1.3.30	dirsum	36
6.1.3.31	dirsum	37
6.1.3.32	dirsum	37
6.1.3.33	dirsum	37
6.1.3.34	dirsumpow	38
6.1.3.35	disp	38
6.1.3.36	disp	38
6.1.3.37	disp	38
6.1.3.38	disp	39
6.1.3.39	disp	39
6.1.3.40	eig	39
6.1.3.41	entanglement	40
6.1.3.42	entropy	40

CONTENTS

6.1.3.43	entropy	40
6.1.3.44	evals	41
6.1.3.45	evects	41
6.1.3.46	expm	41
6.1.3.47	factors	41
6.1.3.48	funm	42
6.1.3.49	gcd	42
6.1.3.50	gcd	42
6.1.3.51	gconcurrence	43
6.1.3.52	grams	43
6.1.3.53	grams	43
6.1.3.54	grams	43
6.1.3.55	heig	44
6.1.3.56	hevals	44
6.1.3.57	hevects	44
6.1.3.58	inverse	45
6.1.3.59	invperm	45
6.1.3.60	isprime	45
6.1.3.61	kraus2choi	45
6.1.3.62	kraus2super	46
6.1.3.63	kron	46
6.1.3.64	kron	46
6.1.3.65	kron	47
6.1.3.66	kron	47
6.1.3.67	kronpow	47
6.1.3.68	lcm	48
6.1.3.69	lcm	48
6.1.3.70	load	48
6.1.3.71	loadMATLABmatrix	49
6.1.3.72	loadMATLABmatrix	49
6.1.3.73	loadMATLABmatrix	49
6.1.3.74	logdet	51
6.1.3.75	logm	51
6.1.3.76	lognegativity	51
6.1.3.77	marginalX	51
6.1.3.78	marginalY	52
6.1.3.79	measure	52
6.1.3.80	measure	52
6.1.3.81	measure	52
6.1.3.82	measure	53

vi CONTENTS

6.1.3.83 measu	e	 53
6.1.3.84 measu	e	 54
6.1.3.85 measu	e	 54
6.1.3.86 measu	re	 55
6.1.3.87 measu	re	 55
6.1.3.88 measu	re_seq	 56
6.1.3.89 measu	re_seq	 56
6.1.3.90 mket		 57
6.1.3.91 mket		 57
6.1.3.92 modpo	N	 57
6.1.3.93 mprj		 57
6.1.3.94 mprj		 58
6.1.3.95 multiid	(2n	 58
6.1.3.96 n2mul	idx	 58
6.1.3.97 negati	ity	 59
6.1.3.98 norm		 59
6.1.3.99 omega		 59
6.1.3.100 operat	r"""_i	 59
6.1.3.101 operat	r"""_i	 60
6.1.3.102 powm		 60
6.1.3.103 prj .		 60
6.1.3.104 prod		 60
6.1.3.105 prod		 60
6.1.3.106 prod		 61
6.1.3.107 ptrace		 61
6.1.3.108 ptrace		 61
6.1.3.109 ptrace		 62
6.1.3.110 ptrace	!	 62
6.1.3.111 ptrans	ose	 62
6.1.3.112 ptrans	ose	 63
6.1.3.113 qmutu	linfo	 63
6.1.3.114 qmutu	linfo	 63
6.1.3.115 rand		 64
6.1.3.116 rand		 64
6.1.3.117 rand		 64
6.1.3.118 rand		 64
6.1.3.119 rand		 65
6.1.3.120 rand		 65
6.1.3.121 randH		 65
6.1.3.122 randid		 66

CONTENTS vii

6.1.3.123 randket
6.1.3.124 randkraus
6.1.3.125 randn
6.1.3.126 randn
6.1.3.127 randn
6.1.3.128 randn
6.1.3.129 randperm
6.1.3.130 randrho
6.1.3.131 randU
6.1.3.132 randV
6.1.3.133 renyi
6.1.3.134 renyi
6.1.3.135 reshape
6.1.3.136 rho2bloch
6.1.3.137 rho2pure
6.1.3.138 save
6.1.3.139 saveMATLABmatrix
6.1.3.140 saveMATLABmatrix
6.1.3.141 saveMATLABmatrix
6.1.3.142 schatten
6.1.3.143 schmidtA
6.1.3.144 schmidtB
6.1.3.145 schmidtcoeffs
6.1.3.146 schmidtprobs
6.1.3.147 sigma
6.1.3.148 sinm
6.1.3.149 spectralpowm
6.1.3.150 sqrtm
6.1.3.151 sum
6.1.3.152 sum
6.1.3.153 sum
6.1.3.154 super2choi
6.1.3.155 svals
6.1.3.156 svd
6.1.3.157 svdU
6.1.3.158 svdV
6.1.3.159 syspermute
6.1.3.160 syspermute
6.1.3.161 trace
6.1.3.162 transpose

viii CONTENTS

		6.1.3.163 ts	sallis	78
		6.1.3.164 ts	sallis	78
		6.1.3.165 u	ıniform	78
		6.1.3.166 v	ar	78
		6.1.3.167 x	2contfrac	79
	6.1.4	Variable Do	ocumentation	79
		6.1.4.1 c	hop	79
		6.1.4.2 e	e	79
		6.1.4.3 e	ps	79
		6.1.4.4 ir	nfty	79
		6.1.4.5 m	naxn	79
		6.1.4.6 p	ii	80
6.2	qpp::ex	kperimental N	Namespace Reference	80
	6.2.1	Detailed De	escription	80
6.3	qpp::in	ternal Names	space Reference	80
	6.3.1	Detailed De	escription	81
	6.3.2	Function Do	ocumentation	81
		6.3.2.1 _	check_cvector	81
		6.3.2.2	_check_dims	81
		6.3.2.3	_check_dims_match_cvect	81
		6.3.2.4	_check_dims_match_mat	81
		6.3.2.5	_check_dims_match_rvect	81
		6.3.2.6	_check_eq_dims	81
		6.3.2.7	check_matching_sizes	81
		6.3.2.8	check_nonzero_size	81
		6.3.2.9	_check_perm	81
		6.3.2.10 _	_check_qubit_cvector	81
		6.3.2.11 _	_check_qubit_matrix	81
		6.3.2.12 _	_check_qubit_rvector	82
		6.3.2.13	_check_qubit_vector	82
		6.3.2.14 _	_check_rvector	82
		6.3.2.15 _	check_square_mat	82
		6.3.2.16 _	_check_subsys_match_dims	82
		6.3.2.17 _	check_vector	82
		6.3.2.18 _	_dirsum2	82
		6.3.2.19 _	kron2	82
		6.3.2.20 _	multiidx2n	82
		6.3.2.21 _	n2multiidx	82
		6.3.2.22 v	rariadic_vector_emplace	82
		6.3.2.23 v	rariadic_vector_emplace	82

CONTENTS

7	Clas	s Docu	mentation	83
	7.1	qpp::C	odes Class Reference	83
		7.1.1	Detailed Description	84
		7.1.2	Member Enumeration Documentation	84
			7.1.2.1 Type	84
		7.1.3	Constructor & Destructor Documentation	84
			7.1.3.1 Codes	84
			7.1.3.2 ~Codes	84
		7.1.4	Member Function Documentation	85
			7.1.4.1 codeword	85
		7.1.5	Friends And Related Function Documentation	85
			7.1.5.1 internal::Singleton < const Codes >	85
	7.2	qpp::E	xception Class Reference	85
		7.2.1	Detailed Description	87
		7.2.2	Member Enumeration Documentation	87
			7.2.2.1 Type	87
		7.2.3	Constructor & Destructor Documentation	88
			7.2.3.1 Exception	88
			7.2.3.2 Exception	88
		7.2.4	Member Function Documentation	88
			7.2.4.1 _construct_exception_msg	88
			7.2.4.2 what	89
		7.2.5	Member Data Documentation	89
			7.2.5.1 _custom	89
			7.2.5.2 _msg	89
			7.2.5.3 _type	89
			7.2.5.4 _where	89
	7.3	qpp::G	ates Class Reference	89
		7.3.1	Detailed Description	91
		7.3.2	Constructor & Destructor Documentation	91
			7.3.2.1 Gates	91
			7.3.2.2 ~Gates	91
		7.3.3	Member Function Documentation	91
			7.3.3.1 CTRL	91
			7.3.3.2 expandout	92
			7.3.3.3 Fd	92
			7.3.3.4 ld	93
			7.3.3.5 Rn	93
			7.3.3.6 Xd	93
			7.3.3.7 Zd	93

CONTENTS

	7.3.4	Friends Ar	nd Related Function Documentation	94
		7.3.4.1	internal::Singleton< const Gates >	94
	7.3.5	Member D	Data Documentation	94
		7.3.5.1	CNOT	94
		7.3.5.2	CNOTba	94
		7.3.5.3	CZ	94
		7.3.5.4	FRED	94
		7.3.5.5	H	94
		7.3.5.6	ld2	94
		7.3.5.7	S	94
		7.3.5.8	SWAP	94
		7.3.5.9	T	94
		7.3.5.10	TOF	95
		7.3.5.11	<b>X</b>	95
		7.3.5.12	Y	95
		7.3.5.13	Z	95
7.4	qpp::ID	isplay Clas	s Reference	95
	7.4.1	Detailed D	Description	96
	7.4.2	Constructo	or & Destructor Documentation	96
		7.4.2.1	IDisplay	96
		7.4.2.2	IDisplay	96
		7.4.2.3	IDisplay	96
		7.4.2.4	~IDisplay	96
	7.4.3	Member F	function Documentation	97
		7.4.3.1	display	97
		7.4.3.2	operator=	97
		7.4.3.3	operator=	97
	7.4.4	Friends Ar	nd Related Function Documentation	97
		7.4.4.1	operator <<	97
7.5	qpp::In	it Class Ref	ference	97
	7.5.1	Detailed D	Description	98
	7.5.2	Constructo	or & Destructor Documentation	98
		7.5.2.1	Init	98
		7.5.2.2	~Init	98
	7.5.3	Friends Ar	nd Related Function Documentation	98
		7.5.3.1	internal::Singleton< const Init >	98
7.6	qpp::in	ternal::IOM	anipEigen Class Reference	99
	7.6.1	Constructo	or & Destructor Documentation	100
		7.6.1.1	IOManipEigen	100
		7.6.1.2	IOManipEigen	100

CONTENTS xi

	7.6.2	Member Function Documentation
		7.6.2.1 display
	7.6.3	Member Data Documentation
		7.6.3.1 _A
		7.6.3.2 _chop
7.7	qpp::int	ternal::IOManipPointer< PointerType > Class Template Reference
	7.7.1	Constructor & Destructor Documentation
		7.7.1.1 IOManipPointer
		7.7.1.2 IOManipPointer
	7.7.2	Member Function Documentation
		7.7.2.1 display
		7.7.2.2 operator=
	7.7.3	Member Data Documentation
		7.7.3.1 _end
		7.7.3.2 _n
		7.7.3.3 _p
		7.7.3.4 _separator
		7.7.3.5 _start
7.8	qpp::int	ternal::IOManipRange< InputIterator > Class Template Reference
	7.8.1	Constructor & Destructor Documentation
		7.8.1.1 IOManipRange
	7.8.2	Member Function Documentation
		7.8.2.1 display
	7.8.3	Member Data Documentation
		7.8.3.1 _end
		7.8.3.2 _first
		7.8.3.3 _last
		7.8.3.4 _separator
		7.8.3.5 _start
7.9	qpp::is_	_complex< T > Struct Template Reference
	7.9.1	Detailed Description
7.10	qpp::is_	_complex< std::complex< T >> Struct Template Reference
	7.10.1	Detailed Description
7.11	qpp::is_	_iterable < T, typename > Struct Template Reference
	7.11.1	Detailed Description
7.12		_iterable< T, to_void< decltype(std::declval< T >().begin()), decltype(std::declval< T d()), typename T::value_type >> Struct Template Reference
	7.12.1	Detailed Description
7.13	qpp::is_	_matrix_expression< Derived > Struct Template Reference
	7.13.1	Detailed Description

xii CONTENTS

7.14	qpp::is_	${\tt _matrix\_expression} < {\tt typename\ Eigen::MatrixBase} < {\tt Derived} > > {\tt Struct\ Template\ Reference\ 110} \\$
	7.14.1	Detailed Description
7.15	qpp::Ra	andomDevices Class Reference
	7.15.1	Detailed Description
	7.15.2	Constructor & Destructor Documentation
		7.15.2.1 RandomDevices
		7.15.2.2 ~RandomDevices
	7.15.3	Friends And Related Function Documentation
		$7.15.3.1  internal:: Singleton < Random Devices > \dots \qquad \qquad 112.15.3.1$
	7.15.4	Member Data Documentation
		7.15.4.1 _rd
		7.15.4.2 _rng
7.16	qpp::int	rernal::Singleton< T > Class Template Reference
	7.16.1	Detailed Description
	7.16.2	Constructor & Destructor Documentation
		7.16.2.1 Singleton
		7.16.2.2 Singleton
		7.16.2.3 ~Singleton
	7.16.3	Member Function Documentation
		7.16.3.1 get_instance
		7.16.3.2 get_thread_local_instance
		7.16.3.3 operator=
7.17	qpp::St	ates Class Reference
	7.17.1	Detailed Description
	7.17.2	Constructor & Destructor Documentation
		7.17.2.1 States
		7.17.2.2 ~States
	7.17.3	Friends And Related Function Documentation
		7.17.3.1 internal::Singleton< const States >
	7.17.4	Member Data Documentation
		7.17.4.1 600
		7.17.4.2 b01
		7.17.4.3 b10
		7.17.4.4 b11
		7.17.4.5 GHZ
		7.17.4.6 pb00
		7.17.4.7 pb01
		7.17.4.8 pb10
		7.17.4.9 pb11
		7.17.4.10 pGHZ

CONTENTS xiii

7.17.4.19 px1 7.17.4.14 py0 7.17.4.15 py1 7.17.4.16 pz0 7.17.4.17 pz1 7.17.4.18 W 7.17.4.19 x0 7.17.4.20 x1 7.17.4.22 y1 7.17.4.23 z0 7.17.4.23 z0 7.17.4.24 z1 7.18 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.3 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.2.4 ~Timer 7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation 8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference	7.17.4	.11 pW
7.17.4.14 py0 7.17.4.15 py1 7.17.4.16 pz0 7.17.4.17 pz1 7.17.4.18 W 7.17.4.19 x0 7.17.4.20 x1 7.17.4.21 y0 7.17.4.22 y1 7.17.4.23 z0 7.17.4.24 z1  7.18.1 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.3 Member Function Documentation 7.18.3 display 7.18.3.0 perator= 7.18.3 operator= 7.18.3 operator= 7.18.3 operator= 7.18.3 beconds 7.18.3 tic 7.18.4 seconds 7.18.3 tic 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation 8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference	7.17.4	.12 px0
7.17.4.15 py1 7.17.4.16 pz0 7.17.4.17 pz1 7.17.4.18 W 7.17.4.19 x0 7.17.4.20 x1 7.17.4.21 y0 7.17.4.22 y1 7.17.4.23 z0 7.17.4.24 z1 7.18 qpp:Timer Class Reference 7.18.1 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation 8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference 8.2.1 Detailed Description	7.17.4	.13 px1
7.17.4.16 pz0 7.17.4.17 pz1 7.17.4.18 W 7.17.4.19 x0 7.17.4.20 x1 7.17.4.21 y0 7.17.4.22 y1 7.17.4.23 z0 7.17.4.24 z1  7.18 qpp::Timer Class Reference 7.18.1 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.3 Member Function Documentation 7.18.3 display 7.18.3 operator= 7.18.3 operator= 7.18.3 operator= 7.18.3 operator= 7.18.3 tic 7.18.3 tic 7.18.4 seconds 7.18.5 tic 7.18.5 tic 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation 8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference	7.17.4	.14 py0
7.17.4.17 pz1 7.17.4.18 W 7.17.4.19 x0 7.17.4.20 x1 7.17.4.21 y0 7.17.4.22 y1 7.17.4.22 y1 7.17.4.23 z0 7.17.4.24 z1  7.18 qpp::Timer Class Reference 7.18.1 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.5 tic 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation 8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference	7.17.4	.15 py1
7.17.4.18 W 7.17.4.19 x0 7.17.4.20 x1 7.17.4.21 y0 7.17.4.22 y1 7.17.4.23 z0 7.17.4.24 z1  7.18 qpp::Timer Class Reference 7.18.1 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.2.4 ~Timer 7.18.3.1 display 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation 8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference	7.17.4	.16 pz0
7.17.4.19 x0 7.17.4.20 x1 7.17.4.21 y0 7.17.4.22 y1 7.17.4.23 z0 7.17.4.24 z1  7.18 qpp::Timer Class Reference 7.18.1 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference	7.17.4	.17 pz1
7.17.4.20 x1 7.17.4.21 y0 7.17.4.22 y1 7.17.4.23 z0 7.17.4.24 z1  7.18 qpp::Timer Class Reference 7.18.1 Detailed Description 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.2.4 ~Timer 7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference	7.17.4	.18 W
7.17.4.21 y0 7.17.4.22 y1 7.17.4.23 z0 7.17.4.24 z1  7.18 qpp::Timer Class Reference 7.18.1 Detailed Description 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation  8.1 classes/codes.h File Reference 8.2.1 Detailed Description  8.2 classes/exception.h File Reference 8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.17.4	.19 x0
7.17.4.22 y1 7.17.4.23 z0 7.17.4.24 z1  7.18 qpp::Timer Class Reference 7.18.1 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer  7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc  7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description  8.2 classes/exception.h File Reference 8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.17.4	.20 x1
7.17.4.23 z0 7.17.4.24 z1  7.18 qpp::Timer Class Reference 7.18.1 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.2.4 ~Timer 7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference	7.17.4	.21 y0
7.17.4.24 z1 7.18 qpp::Timer Class Reference 7.18.1 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.2.4 ~Timer 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation 8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference	7.17.4	.22 y1
7.18 qpp::Timer Class Reference 7.18.1 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.2.4 ~Timer 7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation 8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference	7.17.4	.23 z0
7.18.1 Detailed Description 7.18.2 Constructor & Destructor Documentation 7.18.2.1 Timer 7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.4 ~Timer 7.18.3.1 display 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation 8.1 classes/codes.h File Reference 8.1.1 Detailed Description 8.2 classes/exception.h File Reference 8.2.1 Detailed Description 8.3 classes/gates.h File Reference	7.17.4	.24 z1
7.18.2 Constructor & Destructor Documentation  7.18.2.1 Timer  7.18.2.2 Timer  7.18.2.3 Timer  7.18.2.4 ∼Timer  7.18.3 Member Function Documentation  7.18.3.1 display  7.18.3.2 operator=  7.18.3.3 operator=  7.18.3.4 seconds  7.18.3.5 tic  7.18.3.6 toc  7.18.4 Member Data Documentation  7.18.4.1 _end  7.18.4.2 _start   File Documentation  8.1 classes/codes.h File Reference  8.1.1 Detailed Description  8.2 classes/exception.h File Reference  8.2.1 Detailed Description  8.3 classes/gates.h File Reference	qpp::Timer Cl	ss Reference
7.18.2.1 Timer  7.18.2.2 Timer  7.18.2.3 Timer  7.18.2.4 ~Timer  7.18.3 Member Function Documentation  7.18.3.1 display  7.18.3.2 operator=  7.18.3.3 operator=  7.18.3.4 seconds  7.18.3.5 tic  7.18.3.6 toc  7.18.4 Member Data Documentation  7.18.4.1 _end  7.18.4.2 _start   File Documentation  8.1 classes/codes.h File Reference  8.1.1 Detailed Description  8.2 classes/exception.h File Reference  8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.18.1 Detai	ed Description
7.18.2.2 Timer 7.18.2.3 Timer 7.18.2.4 ∼Timer  7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc  7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description  8.2 classes/exception.h File Reference 8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.18.2 Cons	ructor & Destructor Documentation
7.18.2.3 Timer . 7.18.2.4 ~Timer . 7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description  8.2 classes/exception.h File Reference 8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.18.2	.1 Timer
7.18.2.4 ∼Timer  7.18.3 Member Function Documentation  7.18.3.1 display  7.18.3.2 operator=  7.18.3.3 operator=  7.18.3.4 seconds  7.18.3.5 tic  7.18.3.6 toc  7.18.4 Member Data Documentation  7.18.4.1 _end  7.18.4.2 _start   File Documentation  8.1 classes/codes.h File Reference  8.1.1 Detailed Description  8.2 classes/exception.h File Reference  8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.18.2	.2 Timer
7.18.3 Member Function Documentation 7.18.3.1 display 7.18.3.2 operator=. 7.18.3.3 operator=. 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description  8.2 classes/exception.h File Reference 8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.18.2	.3 Timer
7.18.3.1 display 7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description  8.2 classes/exception.h File Reference 8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.18.2	.4 ~Timer
7.18.3.2 operator= 7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic. 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start.  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description  8.2 classes/exception.h File Reference 8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.18.3 Memb	er Function Documentation
7.18.3.3 operator= 7.18.3.4 seconds 7.18.3.5 tic 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description  8.2 classes/exception.h File Reference 8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.18.0	.1 display
7.18.3.4 seconds 7.18.3.5 tic. 7.18.3.6 toc 7.18.4 Member Data Documentation 7.18.4.1 _end 7.18.4.2 _start.  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description  8.2 classes/exception.h File Reference 8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.18.3	.2 operator=
7.18.3.5 tic	7.18.0	.3 operator=
7.18.3.6 toc  7.18.4 Member Data Documentation  7.18.4.1 _end  7.18.4.2 _start   File Documentation  8.1 classes/codes.h File Reference  8.1.1 Detailed Description  8.2 classes/exception.h File Reference  8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.18.0	.4 seconds
7.18.4 Member Data Documentation	7.18.0	.5 tic
7.18.4.1 _end 7.18.4.2 _start  File Documentation  8.1 classes/codes.h File Reference 8.1.1 Detailed Description  8.2 classes/exception.h File Reference 8.2.1 Detailed Description  8.3 classes/gates.h File Reference	7.18.0	.6 toc
7.18.4.2 _start	7.18.4 Memb	er Data Documentation
File Documentation  8.1 classes/codes.h File Reference	_	
8.1 classes/codes.h File Reference	7.18.4	.2 _start
8.1.1 Detailed Description	ocumentatio	12
8.2 classes/exception.h File Reference	classes/codes	h File Reference
8.2.1 Detailed Description	8.1.1 Detail	ed Description
8.3 classes/gates.h File Reference	classes/excep	ion.h File Reference
•	8.2.1 Detail	ed Description
9.2.1 Detailed Description	classes/gates	h File Reference
6.3.1 Detailed Description	8.3.1 Detai	ed Description
8.4 classes/idisplay.h File Reference	classes/idispla	y.h File Reference

8

XIV

	8.4.1 Detailed Description	125
8.5	classes/init.h File Reference	126
	8.5.1 Detailed Description	126
8.6	classes/random_devices.h File Reference	126
	8.6.1 Detailed Description	127
8.7	classes/states.h File Reference	127
	8.7.1 Detailed Description	127
8.8	classes/timer.h File Reference	128
	8.8.1 Detailed Description	128
8.9	constants.h File Reference	128
	8.9.1 Detailed Description	129
8.10	entanglement.h File Reference	129
	8.10.1 Detailed Description	130
8.11	entropies.h File Reference	130
	8.11.1 Detailed Description	131
8.12	experimental/test.h File Reference	132
	8.12.1 Detailed Description	132
8.13	functions.h File Reference	132
	8.13.1 Detailed Description	136
8.14	input_output.h File Reference	136
	8.14.1 Detailed Description	137
8.15	instruments.h File Reference	137
	8.15.1 Detailed Description	139
8.16	internal/classes/iomanip.h File Reference	139
	8.16.1 Detailed Description	140
8.17	internal/classes/singleton.h File Reference	140
	8.17.1 Detailed Description	
8.18	internal/util.h File Reference	140
	8.18.1 Detailed Description	142
8.19		142
	8.19.1 Detailed Description	143
8.20	· · · · · · · · · · · · · · ·	143
	8.20.1 Detailed Description	144
8.21	operations.h File Reference	144
	8.21.1 Detailed Description	146
8.22	qpp.h File Reference	146
	8.22.1 Detailed Description	148
8.23	random.h File Reference	148
	and the state of t	149
8.24	statistics.h File Reference	149

CONTENTS	X

Index													153
	8.26.1	Detailed Descr	iption	 		152							
8.26	types.h	File Reference		 		151							
	8.25.1	Detailed Descr	iption	 		151							
8.25	traits.h	File Reference		 		150							
	8.24.1	Detailed Descr	iption	 		150							

### Chapter 1

### Quantum++

Version 0.8.1 - development

Development branch, use it at your own risk!

Switch to the master branch for the latest stable version.

Quantum++ is a C++11 general purpose quantum computing library, composed solely of template header files. It uses the Eigen 3 linear algebra library and, if available, the OpenMP multi-processing library. For additional Eigen 3 documentation see http://eigen.tuxfamily.org/dox/. For a simple Eigen 3 quick AS CII reference see http://eigen.tuxfamily.org/dox/AsciiQuickReference.txt.

Quantum++ is not restricted to qubit systems or specific quantum information processing tasks, being capable of simulating arbitrary quantum processes. The main design factors taken in consideration were the ease of use, high portability, and high performance.

If you are interesting in contributing, please contact me. To contribute, you need to have a decent knowledge of C++ (preferably C++11), including templates and the standard library, a basic knowledge of quantum computing and linear algebra, and some working experience with Eigen 3.

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You should have received a copy of the GNU General Public License along with Quantum++. If not, see http-://www.gnu.org/licenses/.

### **Building instructions**

#### Configuration:

- Compiler: g++ version 4.8 or later (for good C++11 support)
- Eigen 3 library located in \$HOME/eigen
- Quantum++ library located in \$HOME/qpp
- MATLAB compiler include header files: /Applications/MATLAB\_R2014b.app/extern/include
- MATLAB compiler shared library files: /Applications/MATLAB\_R2014b.app/bin/maci64

2 Quantum++

#### Building without a build system

- Example file: \$HOME/qpp/examples/minimal.cpp
- Output executable: \$HOME/qpp/examples/example
- Must run the commands below from inside the directory \$HOME/qpp/examples

### Release version (without ${\tt MATLAB}$ support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -03 -DNDEBUG -DEIGEN_NO_DEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    minimal.cpp -o minimal
```

#### Debug version (without MATLAB support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -g3 -DDEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    minimal.cpp -o minimal
```

#### Release version (with MATLAB support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -03 -DNDEBUG -DEIGEN_NO_DEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    -I/Applications/MATLAB_R2014b.app/extern/include \
    -L/Applications/MATLAB_R2014b.app/bin/maci64 \
    -lmx -lmat minimal.cpp -o minimal
```

#### Debug version (with MATLAB support):

```
g++ -pedantic -std=c++11 -Wall -Wextra -Weffc++ -fopenmp \
    -g3 -DDEBUG \
    -isystem $HOME/eigen -I $HOME/qpp/include \
    -I /Applications/MATLAB_R2014b.app/extern/include \
    -L /Applications/MATLAB_R2014b.app/bin/maci64 \
    -lmx -lmat minimal.cpp -o minimal
```

#### Building using cmake

The current version of the repository has a ./CMakeLists.txt configuration file for building examples using cmake. To build an example using cmake, I recommend an out-of-source build, i.e., from the root of the project (where ./include is located), type

```
mkdir ./build
cd ./build
cmake ..
make
```

The above commands build the relase version (default) executable qpp, from the source file ./examples/minimal.cpp, without MATLAB support (default), inside the directory ./build. To build a different configuration, e.g. debug version with MATLAB support, type from the root of the project

```
cd ./build  \begin{tabular}{ll} $\sf cd ./build \\ $\sf rm -rf * \\ $\sf cmake -DCMAKE\_BUILD\_TYPE=Debug -DWITH\_MATLAB=ON .. \\ $\sf make \\ \end{tabular}
```

#### Or, to disable OpenMP support (enabled by default), type

```
cd ./build
rm -rf *
cmake -DWITH_OPENMP=OFF ..
make
```

To change the name of the example file, the location of the Eigen 3 library or the location of MATLAB installation, edit the ./CMakeLists.txt file. See also ./CMakeLists.txt for additional options. Do not forget to remove everything from the ./build directory before a fresh build!

#### **Additional remarks**

- The C++ compiler must be C++11 compliant.
- If using Windows, I recommend compiling under cygwin via cmake and g++. See also http←://stackoverflow.com/questions/28997206/cygwin-support-for-c11-in-g4-9-2 for a bug related to lack of support for some C++11 math functions, and how to fix it. Quick fix: patch the standard library header file <cmath> using the provided patch./cmath\_cygwin.patch.
- If your compiler does not support OpenMP (as it is the case e.g with clang++), disable OpenMP in your build, as otherwise the linker may not find the gomp library.
- If you run the program on OS X with MATLAB support, make sure that the environment variable DYLD\_L← IBRARY\_PATH is set to point to the MATLAB compiler library location, see the run\_OSX\_MATLAB script. Otherwise, you will get a runtime error like dyld: Library not loaded: @rpath/libmat.← dylib.

```
* I recommend running via a script, as otherwise setting the 
'DYLD_LIBRARY_PATH' globally may interfere with 
[macports] (https://www.macports.org/)' [cmake] (http://www.cmake.org/) 
installation (in case you use [cmake] (http://www.cmake.org/) from 
[macports] (https://www.macports.org/)). If you use a script, 
then the environment variable is local to the script and 
does not interfere with the rest of the system.

* Example of running script, run from inside the directory where 
the executable 'qpp' is located:

#!/bin/sh # Run Quantum++ under OS X with MATLAB support

export DYLD_LIBRARY_PATH=$DYLD_LIBRARY_PATH:"/Applications/MATLAB_R2014b.app/bin/maci64"
./qpp
```

• If you build a debug version with g++ under OS X and use gdb to step inside template functions you may want to add -fno-weak compiler flag. See http://stackoverflow.← com/questions/23330641/gnu-gdb-can-not-step-into-template-functions-os-x-mavericks for more details about this problem.

Quantum++

# Chapter 2

# Namespace Index

### 2.1 Namespace List

Here is a list of all namespaces with brief descriptions:

qpp	
Quantum++ main namespace	13
qpp::experimental	
Experimental/test functions/classes, do not use or modify	80
qpp::internal	
Internal utility functions, do not use/modify	80

6 Namespace Index

# Chapter 3

## **Hierarchical Index**

### 3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

staexception
qpp::Exception
false_type
qpp::is_complex< T >
qpp::is_iterable < T, typename >
qpp::is_matrix_expression< Derived >
qpp::IDisplay
qpp::internal::IOManipEigen
qpp::internal::IOManipPointer< PointerType >
qpp::internal::IOManipRange< InputIterator >
qpp::Timer
$qpp::internal::Singleton < T > \dots \dots$
qpp::internal::Singleton < const Codes >
qpp::Codes
qpp::internal::Singleton < const Gates >
qpp::Gates
$qpp::internal::Singleton < const \ Init > \dots $
qpp::Init
qpp::internal::Singleton < const States >
qpp::States
qpp::internal::Singleton < RandomDevices >
qpp::RandomDevices
true_type
$qpp::is\_complex < std::complex < T >> \ \dots $
$qpp::is\_iterable < \ T, \ to\_void < \ decltype(std::declval < \ T \ > ().begin()), \ decltype(std::declval < \ T \ > ())$
>().end()), typename T::value_type >>
qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived >>

8 **Hierarchical Index** 

# **Chapter 4**

## **Class Index**

### 4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

qpp::Codes	
Const Singleton class that defines quantum error correcting codes	83
qpp::Exception	
Generates custom exceptions, used when validating function parameters	85
qpp::Gates	
Const Singleton class that implements most commonly used gates	89
qpp::IDisplay	
Abstract class (interface) that mandates the definition of virtual std::ostream& display(std↔	
::ostream& os) const	95
qpp::Init	
Const Singleton class that performs additional initializations/cleanups	97
qpp::internal::IOManipEigen	99
qpp::internal::IOManipPointer< PointerType >	100
qpp::internal::IOManipRange< InputIterator >	102
qpp::is_complex< T >	
Checks whether the type is a complex type	104
qpp::is_complex< std::complex< T >>	
Checks whether the type is a complex number type, specialization for complex types	105
qpp::is_iterable< T, typename >	
Checks whether $T$ is compatible with an STL-like iterable container $\dots \dots \dots \dots \dots$	106
$qpp::is\_iterable < T, \ to\_void < \ decltype(std::declval < T > ().begin()), \ decltype(std::declval < T > ().end()), \\$	
typename T::value_type > >	
Checks whether $T$ is compatible with an STL-like iterable container, specialization for STL-like	
iterable containers	107
qpp::is_matrix_expression< Derived >	
Checks whether the type is an Eigen matrix expression	109
qpp::is_matrix_expression< typename Eigen::MatrixBase< Derived >>	
Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expres-	
sions	110
qpp::RandomDevices	
· · · · · · · · · · · · · · · · · · ·	111
qpp::internal::Singleton< T >	
Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously	
recurring template pattern)	113
qpp::States	
Const Singleton class that implements most commonly used states	114
qpp::Timer	
Chronometer	119

10 Class Index

# **Chapter 5**

## File Index

### 5.1 File List

Here is a list of all files with brief descriptions:

constants.h
Constants
entanglement.h
Entanglement functions
entropies.h
Entropy functions
functions.h
Generic quantum computing functions
input_output.h
Input/output functions
instruments.h
Measurement functions
number_theory.h
Number theory functions
operations.h
Quantum operation functions
qpp.h
Quantum++ main header file, includes all other necessary headers
random.h
Randomness-related functions
statistics.h
Statistics functions
traits.h
Type traits
types.h
Type aliases
classes/codes.h
Quantum error correcting codes
classes/exception.h
Exceptions
classes/gates.h
Quantum gates
classes/idisplay.h
Display interface via the non-virtual interface (NVI)
classes/init.h
Initialization
classes/random_devices.h
Random devices

12 File Index

classes/states.h												
Quantum states	 	 										127
classes/timer.h												
Timing	 	 										128
experimental/test.h												
Experimental/test functions/classes	 	 										132
internal/util.h												
Internal utility functions	 	 										140
internal/classes/iomanip.h												
Input/output manipulators	 	 										139
internal/classes/singleton.h												
Singleton pattern via CRTP	 	 										 140
MATLAB/matlab.h												
Input/output interfacing with MATLAB		 				 				 		142

## **Chapter 6**

## **Namespace Documentation**

### 6.1 qpp Namespace Reference

Quantum++ main namespace.

### **Namespaces**

experimental

Experimental/test functions/classes, do not use or modify.

internal

Internal utility functions, do not use/modify.

### Classes

class Codes

const Singleton class that defines quantum error correcting codes

class Exception

Generates custom exceptions, used when validating function parameters.

• class Gates

const Singleton class that implements most commonly used gates

class IDisplay

Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

class Init

const Singleton class that performs additional initializations/cleanups

· struct is\_complex

Checks whether the type is a complex type.

struct is\_complex< std::complex< T >>

Checks whether the type is a complex number type, specialization for complex types.

• struct is\_iterable

Checks whether T is compatible with an STL-like iterable container.

struct is\_iterable< T, to\_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().end()), typename T::value\_type >>

Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

· struct is matrix expression

Checks whether the type is an Eigen matrix expression.

struct is\_matrix\_expression< typename Eigen::MatrixBase< Derived >>

Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.

· class RandomDevices

Singeleton class that manages the source of randomness in the library.

· class States

const Singleton class that implements most commonly used states

· class Timer

Chronometer.

#### **Typedefs**

```
    template < class... >
        using to_void = void
        Alias template that implements the proposal for void_t.
```

• using idx = std::size\_t

Non-negative integer index.

• using bigint = long long int

Big integer.

using ubigint = unsigned long long int

Non-negative big integer.

using cplx = std::complex < double >

Complex number in double precision.

• using ket = Eigen::VectorXcd

Complex (double precision) dynamic Eigen column vector.

using bra = Eigen::RowVectorXcd

Complex (double precision) dynamic Eigen row vector.

• using cmat = Eigen::MatrixXcd

Complex (double precision) dynamic Eigen matrix.

• using dmat = Eigen::MatrixXd

Real (double precision) dynamic Eigen matrix.

• template<typename Scalar >

```
using dyn_mat = Eigen::Matrix < Scalar, Eigen::Dynamic, Eigen::Dynamic >
```

Dynamic Eigen matrix over the field specified by Scalar.

• template<typename Scalar >

```
using dyn_col_vect = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >
```

Dynamic Eigen column vector over the field specified by Scalar.

template<typename Scalar >

```
using dyn_row_vect = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >
```

Dynamic Eigen row vector over the field specified by Scalar.

### **Functions**

constexpr cplx operator"" i (unsigned long long int x) noexcept

User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)

constexpr cplx operator""\_i (long double x) noexcept

User-defined literal for complex  $i = \sqrt{-1}$  (real overload)

• cplx omega (idx D)

D-th root of unity.

• template<typename Derived >

dyn\_col\_vect< double > schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx >
&dims)

Schmidt coefficients of the bi-partite pure state A.

```
• template<typename Derived >
  cmat schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)
     Schmidt basis on Alice side.

    template<typename Derived >

  cmat schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)
     Schmidt basis on Bob side.
• template<typename Derived >
  std::vector< double > schmidtprobs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx >
  &dims)
     Schmidt probabilities of the bi-partite pure state A.

    template<typename Derived >

  double entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)
     Entanglement of the bi-partite pure state A.

    template<typename Derived >

  double gconcurrence (const Eigen::MatrixBase< Derived > &A)
      G-concurrence of the bi-partite pure state A.

    template<typename Derived >

  double negativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)
     Negativity of the bi-partite mixed state A.

    template<typename Derived >

  double lognegativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)
     Logarithmic negativity of the bi-partite mixed state A.
• template<typename Derived >
  double concurrence (const Eigen::MatrixBase< Derived > &A)
      Wootters concurrence of the bi-partite qubit mixed state A.
• template<typename Derived >
  double entropy (const Eigen::MatrixBase< Derived > &A)
      von-Neumann entropy of the density matrix A

    double entropy (const std::vector< double > &prob)

     Shannon entropy of the probability distribution prob.

    template<typename Derived >

  double renyi (const Eigen::MatrixBase< Derived > &A, double alpha)
      Renyi- \alpha entropy of the density matrix A, for \alpha \geq 0.

    double renyi (const std::vector< double > &prob, double alpha)

     Renyi- \alpha entropy of the probability distribution prob, for \alpha \geq 0.

    template < typename Derived >

  double tsallis (const Eigen::MatrixBase< Derived > &A, double q)
      Tsallis- q entropy of the density matrix A, for q \geq 0.

    double tsallis (const std::vector< double > &prob, double q)

      Tsallis- q entropy of the probability distribution prob, for q \geq 0.
• template<typename Derived >
  double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const
  std::vector< idx > &subsysB, const std::vector< idx > &dims)
      Quantum mutual information between 2 subsystems of a composite system.

    template<typename Derived >

  double gmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const
  std::vector < idx > &subsysB, idx d=2)
      Quantum mutual information between 2 subsystems of a composite system.

    template<typename Derived >

  dyn mat< typename Derived::Scalar > transpose (const Eigen::MatrixBase< Derived > &A)
      Transpose.

    template<typename Derived >

  dyn_mat< typename Derived::Scalar > conjugate (const Eigen::MatrixBase< Derived > &A)
```

Left singular vectors.

```
Complex conjugate.
• template<typename Derived >
  dyn_mat< typename Derived::Scalar > adjoint (const Eigen::MatrixBase< Derived > &A)
     Adjoint.

    template<typename Derived >

  dyn_mat< typename Derived::Scalar > inverse (const Eigen::MatrixBase< Derived > &A)
     Inverse.
template<typename Derived >
  Derived::Scalar trace (const Eigen::MatrixBase< Derived > &A)

    template<typename Derived >

  Derived::Scalar det (const Eigen::MatrixBase < Derived > &A)
     Determinant.

    template<typename Derived >

  Derived::Scalar logdet (const Eigen::MatrixBase< Derived > &A)
     Logarithm of the determinant.

    template<typename Derived >

  Derived::Scalar sum (const Eigen::MatrixBase< Derived > &A)
     Element-wise sum of A.

    template<typename Derived >

  Derived::Scalar prod (const Eigen::MatrixBase< Derived > &A)
     Element-wise product of A.

    template<typename Derived >

  double norm (const Eigen::MatrixBase< Derived > &A)
     Frobenius norm.

    template<typename Derived >

  std::pair< dyn_col_vect< cplx >, cmat > eig (const Eigen::MatrixBase< Derived > &A)
     Full eigen decomposition.
template<typename Derived >
  dyn_col_vect< cplx > evals (const Eigen::MatrixBase< Derived > &A)
     Eigenvalues.
• template<typename Derived >
  cmat evects (const Eigen::MatrixBase< Derived > &A)
     Eigenvectors.

    template<typename Derived >

  std::pair< dyn_col_vect< double >, cmat > heig (const Eigen::MatrixBase< Derived > &A)
     Full eigen decomposition of Hermitian expression.

    template<typename Derived >

  dyn_col_vect< double > hevals (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvalues.

    template<typename Derived >

  cmat hevects (const Eigen::MatrixBase< Derived > &A)
     Hermitian eigenvectors.

    template<typename Derived >

  std::tuple< cmat, dyn_col_vect< double >, cmat > svd (const Eigen::MatrixBase< Derived > &A)
     Full singular value decomposition.

    template<typename Derived >

  dyn_col_vect< double > svals (const Eigen::MatrixBase< Derived > &A)
     Singular values.
• template<typename Derived >
  cmat svdU (const Eigen::MatrixBase< Derived > &A)
```

```
• template<typename Derived >
  cmat svdV (const Eigen::MatrixBase< Derived > &A)
     Right singular vectors.

    template<typename Derived >

  cmat funm (const Eigen::MatrixBase< Derived > &A, cplx(*f)(const cplx &))
     Functional calculus f(A)
• template<typename Derived >
  cmat sqrtm (const Eigen::MatrixBase< Derived > &A)
     Matrix square root.

    template<typename Derived >

  cmat absm (const Eigen::MatrixBase< Derived > &A)
     Matrix absolut value.

    template<typename Derived >

  cmat expm (const Eigen::MatrixBase< Derived > &A)
     Matrix exponential.

    template < typename Derived >

  cmat logm (const Eigen::MatrixBase< Derived > &A)
     Matrix logarithm.
• template<typename Derived >
  cmat sinm (const Eigen::MatrixBase< Derived > &A)
     Matrix sin.
template<typename Derived >
  cmat cosm (const Eigen::MatrixBase< Derived > &A)
     Matrix cos.
• template<typename Derived >
  cmat spectralpowm (const Eigen::MatrixBase< Derived > &A, const cplx z)
     Matrix power.
• template<typename Derived >
  dyn mat< typename Derived::Scalar > powm (const Eigen::MatrixBase< Derived > &A, idx n)
     Matrix power.
ullet template<typename Derived >
  double schatten (const Eigen::MatrixBase< Derived > &A, double p)
     Schatten matrix norm.
• template<typename OutputScalar , typename Derived >
  dyn_mat< OutputScalar > cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const type-
  name Derived::Scalar &))
     Functor.

    template<typename T >

  dyn mat< typename T::Scalar > kron (const T &head)
     Kronecker product.
• template<typename T , typename... Args>
  dyn mat< typename T::Scalar > kron (const T &head, const Args &...tail)
     Kronecker product.

    template<typename Derived >

  dyn_mat< typename Derived::Scalar > kron (const std::vector< Derived > &As)
     Kronecker product.
template<typename Derived >
  dyn_mat< typename Derived::Scalar > kron (const std::initializer_list< Derived > &As)
     Kronecker product.
• template<typename Derived >
  dyn_mat< typename Derived::Scalar > kronpow (const Eigen::MatrixBase< Derived > &A, idx n)
     Kronecker power.
```

```
• template<typename T >
  dyn_mat< typename T::Scalar > dirsum (const T &head)
• template<typename T , typename... Args>
  dyn mat< typename T::Scalar > dirsum (const T &head, const Args &...tail)
     Direct sum.

    template<typename Derived >

  dyn_mat< typename Derived::Scalar > dirsum (const std::vector< Derived > &As)
     Direct sum.

    template<typename Derived >

  dyn_mat< typename Derived::Scalar > dirsum (const std::initializer_list< Derived > &As)
      Direct sum.
• template<typename Derived >
  dyn mat< typename Derived::Scalar > dirsumpow (const Eigen::MatrixBase< Derived > &A, idx n)
      Direct sum power.
\bullet \ \ {\it template}{<} {\it typename Derived}>
  dyn_mat< typename Derived::Scalar > reshape (const Eigen::MatrixBase< Derived > &A, idx rows, idx
  cols)
     Reshape.
 template<typename Derived1 , typename Derived2 >
  dyn mat< typename Derived1::Scalar > comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::↔
  MatrixBase< Derived2 > &B)
      Commutator.
ullet template<typename Derived1 , typename Derived2 >
  dyn_mat< typename Derived1::Scalar > anticomm (const Eigen::MatrixBase< Derived1 > &A, const
  Eigen::MatrixBase< Derived2 > &B)
     Anti-commutator.
• template<typename Derived >
  dyn_mat< typename Derived::Scalar > prj (const Eigen::MatrixBase< Derived > &V)
     Projector.

    template<typename Derived >

  dyn_mat< typename Derived::Scalar > grams (const std::vector< Derived > &Vs)
     Gram-Schmidt orthogonalization.

    template<typename Derived >

  dyn mat< typename Derived::Scalar > grams (const std::initializer list< Derived > &Vs)
     Gram-Schmidt orthogonalization.

    template<typename Derived >

  dyn_mat< typename Derived::Scalar > grams (const Eigen::MatrixBase< Derived > &A)
      Gram-Schmidt orthogonalization.

    std::vector< idx > n2multiidx (idx n, const std::vector< idx > &dims)

     Non-negative integer index to multi-index.

    idx multiidx2n (const std::vector < idx > &midx, const std::vector < idx > &dims)

     Multi-index to non-negative integer index.

    ket mket (const std::vector < idx > &mask, const std::vector < idx > &dims)

     Multi-partite qudit ket.

    ket mket (const std::vector< idx > &mask, idx d=2)

     Multi-partite qudit ket.

    cmat mprj (const std::vector < idx > &mask, const std::vector < idx > &dims)

     Projector onto multi-partite qudit ket.

    cmat mprj (const std::vector < idx > &mask, idx d=2)

     Projector onto multi-partite qudit ket.
• template<typename InputIterator >
```

std::vector< double > abssq (InputIterator first, InputIterator last)

Computes the absolute values squared of an STL-like range of complex numbers.

• template<typename Container >

std::vector< double > abssq (const Container &c, typename std::enable\_if< is\_iterable< Container >::value >::type \*=nullptr)

Computes the absolute values squared of an STL-like container.

template<typename Derived >

std::vector< double > abssq (const Eigen::MatrixBase< Derived > &A)

Computes the absolute values squared of an Eigen expression.

template<typename InputIterator >

std::iterator\_traits< InputIterator >::value\_type sum (InputIterator first, InputIterator last)

Element-wise sum of an STL-like range.

template<typename Container >

Container::value\_type sum (const Container &c)

Element-wise sum of the elements of an STL-like container.

template<typename InputIterator >

std::iterator\_traits < InputIterator >::value\_type prod (InputIterator first, InputIterator last)

Element-wise product of an STL-like range.

template<typename Container >

Container::value\_type prod (const Container &c)

Element-wise product of the elements of an STL-like container.

• template<typename Derived >

dyn\_col\_vect< typename Derived::Scalar > rho2pure (const Eigen::MatrixBase< Derived > &A)

Finds the pure state representation of a matrix proportional to a projector onto a pure state.

template<typename T >

std::vector< T > complement (std::vector< T > subsys, idx N)

Constructs the complement of a subsystem vector.

template<typename Derived >

std::vector< double > rho2bloch (const Eigen::MatrixBase< Derived > &A)

Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix A.

cmat bloch2rho (const std::vector< double > &r)

Computes the density matrix corresponding to the 3-dimensional real Bloch vector r.

template<typename Derived >

internal::IOManipEigen disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)

Eigen expression ostream manipulator.

internal::IOManipEigen disp (cplx z, double chop=qpp::chop)

Complex number ostream manipulator.

 $\bullet \ \ \mathsf{template} \mathord{<} \mathsf{typename\ InputIterator} \mathord{>}$ 

internal::IOManipRange < InputIterator > disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")

Range ostream manipulator.

• template<typename Container >

internal::IOManipRange< typename Container::const\_iterator > disp (const Container &c, const std::string &separator, const std::string &start="[", const std::string &end="]")

Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.

• template<typename PointerType >

internal::IOManipPointer< PointerType > disp (const PointerType \*p, idx n, const std::string &separator, const std::string &start="[", const std::string &end="]")

C-style pointer ostream manipulator.

template<typename Derived >

void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

Saves Eigen expression to a binary file (internal format) in double precision.

template<typename Derived >

dyn\_mat< typename Derived::Scalar > load (const std::string &fname)

Loads Eigen matrix from a binary file (internal format) in double precision.

• template<typename Derived >

```
std::tuple < idx, std::vector < double >, std::vector < cmat > > measure (const Eigen::MatrixBase < Derived > &A, const std::vector < cmat > &Ks)
```

Measures the state A using the set of Kraus operators Ks.

• template<typename Derived >

```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks)
```

Measures the state A using the set of Kraus operators Ks.

template<typename Derived >

```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &U)
```

Measures the state A in the orthonormal basis specified by the unitary matrix U.

• template<typename Derived >

```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)
```

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

• template<typename Derived >

std::tuple < idx, std::vector < double >, std::vector < cmat > > measure (const Eigen::MatrixBase < Derived > &A, const std::initializer\_list < cmat > &Ks, const std::vector < idx > &subsys, const std::vector < idx > &dims)

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

template<typename Derived >

```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const idx d=2)
```

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

ullet template<typename Derived >

```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const std::initializer_list< cmat > &Ks, const std::vector< idx > &subsys, const idx d=2)
```

 $\textit{Measures the part subsys of the multi-partite state vector or density matrix A using the set of \textit{Kraus operators Ks}.$ 

template<typename Derived >

```
std::tuple < idx, std::vector < double >, std::vector < cmat > > measure (const Eigen::MatrixBase < Derived > &A, const cmat &U, const std::vector < idx > &subsys, const std::vector < idx > &dims)
```

Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis specified by the unitary matrix U.

template<typename Derived >

```
std::tuple< idx, std::vector< double >, std::vector< cmat > > measure (const Eigen::MatrixBase< Derived > &A, const cmat &U, const std::vector< idx > &subsys, const idx d=2)
```

Measures the part subsys of the multi-partite state vector or density matrix A\ in the orthonormal basis specified by the unitary matrix U.

template<typename Derived >

```
std::tuple< std::vector< idx >, double, cmat > measure_seq (const Eigen::MatrixBase< Derived > &A, std::vector< idx > subsys, std::vector< idx > dims)
```

Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.

 $\bullet \ \ {\sf template}{<} {\sf typename \ Derived} >$ 

```
std::tuple < std::vector < idx >, double, cmat > measure_seq (const Eigen::MatrixBase < Derived > &A, std::vector < idx > subsys, idx d=2)
```

Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.

template<typename Derived >

Derived loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.

template<>

dmat loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices (qpp::dmat)

• template<>

cmat loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

template<typename Derived >

void saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat\_file, const std ::string &var\_name, const std::string &mode)

Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.

template<>

void saveMATLABmatrix (const Eigen::MatrixBase< dmat > &A, const std::string &mat\_file, const std::string &var name, const std::string &mode)

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices (qpp::dmat)

template<>

void saveMATLABmatrix (const Eigen::MatrixBase< cmat > &A, const std::string &mat\_file, const std::string &var name, const std::string &mode)

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

std::vector< int > x2contfrac (double x, idx n, idx cut=1e5)

Simple continued fraction expansion.

double contfrac2x (const std::vector< int > &cf, idx n)

Real representation of a simple continued fraction.

double contfrac2x (const std::vector< int > &cf)

Real representation of a simple continued fraction.

• ubigint gcd (ubigint m, ubigint n)

Greatest common divisor of two non-negative integers.

ubigint gcd (const std::vector< ubigint > &ns)

Greatest common divisor of a list of non-negative integers.

• ubigint lcm (ubigint m, ubigint n)

Least common multiple of two positive integers.

ubigint lcm (const std::vector< ubigint > &ns)

Least common multiple of a list of positive integers.

std::vector< idx > invperm (const std::vector< idx > &perm)

Inverse permutation.

std::vector< idx > compperm (const std::vector< idx > &perm, const std::vector< idx > &sigma)

Compose permutations.

std::vector< ubigint > factors (ubigint n)

Prime factor decomposition.

• bool isprime (ubigint n)

Primality test.

• ubigint modpow (ubigint a, ubigint n, ubigint p)

Integer power modulo p.

• template<typename Derived1 , typename Derived2 >

dyn\_mat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const
Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, const
std::vector< idx > &dims)

Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.

template<typename Derived1 , typename Derived2 >

dyn\_mat< typename Derived1::Scalar > applyCTRL (const Eigen::MatrixBase< Derived1 > &state, const
Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys, idx
d=2)

Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.

template<typename Derived1 , typename Derived2 >

 $\frac{\text{dyn\_mat}<\text{typename Derived1::Scalar}>\text{apply (const Eigen::MatrixBase}<\text{Derived1}>\text{\&state, const Eigen} \\ \text{::MatrixBase}<\text{Derived2}>\text{\&A, const std::vector}<\text{idx}>\text{\&subsys, const std::vector}<\text{idx}>\text{\&dims})}$ 

Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.

• template<typename Derived1 , typename Derived2 >

dyn\_mat< typename Derived1::Scalar > apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen ← ::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, idx d=2)

Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.

template<typename Derived >

cmat apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks)

Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.

• template<typename Derived >

cmat apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector<
idx > &subsys, const std::vector< idx > &dims)

Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix rho.

• template<typename Derived >

cmat apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector<
idx > &subsys, idx d=2)

Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix

cmat kraus2super (const std::vector < cmat > &Ks)

Superoperator matrix.

cmat kraus2choi (const std::vector< cmat > &Ks)

Choi matrix.

std::vector < cmat > choi2kraus (const cmat &A)

Orthogonal Kraus operators from Choi matrix.

cmat choi2super (const cmat &A)

Converts Choi matrix to superoperator matrix.

cmat super2choi (const cmat &A)

Converts superoperator matrix to Choi matrix.

template<typename Derived >

dyn\_mat< typename Derived::Scalar > ptrace1 (const Eigen::MatrixBase< Derived > &A, const std ← ::vector< idx > &dims)

Partial trace.

 $\bullet \ \ {\it template}{<} {\it typename Derived} >$ 

dyn\_mat< typename Derived::Scalar > ptrace2 (const Eigen::MatrixBase< Derived > &A, const std ← ::vector < idx > &dims)

Partial trace.

template<typename Derived >

dyn\_mat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector<
idx > &subsys, const std::vector< idx > &dims)

Partial trace.

• template<typename Derived >

dyn\_mat< typename Derived::Scalar > ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector
idx > &subsys, idx d=2)

Partial trace.

template<typename Derived >

Partial transpose.

template<typename Derived >

dyn\_mat< typename Derived::Scalar > ptranspose (const Eigen::MatrixBase< Derived > &A, const std ← ::vector< idx > &subsys, idx d=2)

Partial transpose.

template<typename Derived >

Subsystem permutation.

• template<typename Derived >

Subsystem permutation.

double rand (double a=0, double b=1)

Generates a random real number uniformly distributed in the interval [a, b)

bigint rand (bigint a=std::numeric\_limits< bigint >::min(), bigint b=std::numeric\_limits< bigint >::max())

Generates a random big integer uniformly distributed in the interval [a, b].

ubigint rand (ubigint a=std::numeric\_limits< ubigint >::min(), ubigint b=std::numeric\_limits< ubigint >←
 ::max())

Generates a random non-negative big integer uniformly distributed in the interval [a, b].

idx randidx (idx a=std::numeric limits < idx >::min(), idx b=std::numeric limits < idx >::max())

Generates a random index (idx) uniformly distributed in the interval [a, b].

• template<typename Derived >

Derived rand (idx rows, idx cols, double a=0, double b=1)

Generates a random matrix with entries uniformly distributed in the interval [a, b)

• template<>

dmat rand (idx rows, idx cols, double a, double b)

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (gpp::dmat)

template<>

cmat rand (idx rows, idx cols, double a, double b)

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)

template<typename Derived >

Derived randn (idx rows, idx cols, double mean=0, double sigma=1)

Generates a random matrix with entries normally distributed in N(mean, sigma)

• template<>

dmat randn (idx rows, idx cols, double mean, double sigma)

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)

• template<>

cmat randn (idx rows, idx cols, double mean, double sigma)

Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)

• double randn (double mean=0, double sigma=1)

Generates a random real number (double) normally distributed in N(mean, sigma)

cmat randU (idx D)

Generates a random unitary matrix.

cmat randV (idx Din, idx Dout)

Generates a random isometry matrix.

std::vector < cmat > randkraus (idx N, idx D)

Generates a set of random Kraus operators.

· cmat randH (idx D)

Generates a random Hermitian matrix.

ket randket (idx D)

Generates a random normalized ket (pure state vector)

cmat randrho (idx D)

Generates a random density matrix.

std::vector< idx > randperm (idx n)

Generates a random uniformly distributed permutation.

std::vector< double > uniform (idx N)

Uniform probability distribution vector.

std::vector< double > marginalX (const dmat &probXY)

Marginal distribution.

std::vector< double > marginalY (const dmat &probXY)

Marginal distribution.

• template<typename Container >

double avg (const std::vector< double > &prob, const Container &X)

Average.

• template<typename Container >

double cov (const dmat &probXY, const Container &X, const Container &Y)

Covariance

• template<typename Container >

double var (const std::vector< double > &prob, const Container &X)

Variance.

• template<typename Container >

double sigma (const std::vector< double > &prob, const Container &X)

Standard deviation.

• template<typename Container >

double cor (const dmat &probXY, const Container &X, const Container &Y)

Correlation.

# **Variables**

• constexpr double chop = 1e-10

Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.

• constexpr double eps = 1e-12

Used to decide whether a number or expression in double precision is zero or not.

constexpr idx maxn = 64

Maximum number of allowed qu(d)its (subsystems)

constexpr double pi = 3.141592653589793238462643383279502884

 $\pi$ 

• constexpr double ee = 2.718281828459045235360287471352662497

Base of natural logarithm, e.

constexpr double infty = std::numeric\_limits<double>::infinity()

Used to denote infinity in double precision.

# 6.1.1 Detailed Description

Quantum++ main namespace.

# 6.1.2 Typedef Documentation

6.1.2.1 using qpp::bigint = typedef long long int

Big integer.

6.1.2.2 using qpp::bra = typedef Eigen::RowVectorXcd

Complex (double precision) dynamic Eigen row vector.

6.1.2.3 using qpp::cmat = typedef Eigen::MatrixXcd

Complex (double precision) dynamic Eigen matrix.

6.1.2.4 using qpp::cplx = typedef std::complex <double>

Complex number in double precision.

6.1.2.5 using qpp::dmat = typedef Eigen::MatrixXd

Real (double precision) dynamic Eigen matrix.

6.1.2.6 template<typename Scalar > using qpp::dyn\_col\_vect = typedef Eigen::Matrix < Scalar, Eigen::Dynamic, 1>

Dynamic Eigen column vector over the field specified by Scalar.

# Example:

```
// type of colvect is Eigen::Matrix<float, Eigen::Dynamic, 1>
auto colvect = dyn_col_vect<float>(2);
```

6.1.2.7 template<typename Scalar > using qpp::dyn\_mat = typedef Eigen::Matrix < Scalar, Eigen::Dynamic, Eigen::Dynamic>

Dynamic Eigen matrix over the field specified by Scalar.

# Example:

```
// type of mat is Eigen::Matrix<float, Eigen::Dynamic, Eigen::Dynamic>
auto mat = dyn_mat<float>(2,3);
```

6.1.2.8 template<typename Scalar > using qpp::dyn\_row\_vect = typedef Eigen::Matrix < Scalar, 1, Eigen::Dynamic >

Dynamic Eigen row vector over the field specified by Scalar.

# Example:

```
// type of rowvect is Eigen::Matrix<float, 1, Eigen::Dynamic>
auto rowvect = dyn_row_vect<float>(3);
```

6.1.2.9 using qpp::idx = typedef std::size\_t

Non-negative integer index.

6.1.2.10 using qpp::ket = typedef Eigen::VectorXcd

Complex (double precision) dynamic Eigen column vector.

6.1.2.11 template < class... > using qpp::to\_void = typedef void

Alias template that implements the proposal for void t.

See also

http://www.open-std.org/jtc1/sc22/wg21/docs/papers/2014/n3911

6.1.2.12 using qpp::ubigint = typedef unsigned long long int

Non-negative big integer.

# 6.1.3 Function Documentation

6.1.3.1 template < typename Derived > cmat qpp::absm ( const Eigen::MatrixBase < Derived > & A )

Matrix absolut value.

**Parameters** 

Α	Eigen expression

#### Returns

Matrix absolut value of A

6.1.3.2 template<typename InputIterator > std::vector<double> qpp::abssq ( InputIterator first, InputIterator last )

Computes the absolute values squared of an STL-like range of complex numbers.

# **Parameters**

first	Iterator to the first element of the range
last	Iterator to the last element of the range

#### Returns

Real vector consisting of the range absolut values squared

6.1.3.3 template<typename Container > std::vector<double> qpp::abssq ( const Container & c, typename std::enable\_if< is\_iterable< Container >::value >::type \* = nullptr )

Computes the absolute values squared of an STL-like container.

### **Parameters**

С	STL-like container

# Returns

Real vector consisting of the container's absolut values squared

6.1.3.4 template < typename Derived > std::vector < double > qpp::abssq ( const Eigen::MatrixBase < Derived > & A )

Computes the absolute values squared of an Eigen expression.

# Parameters

Α	Eigen expression

### Returns

Real vector consisting of the absolut values squared

6.1.3.5 template < typename Derived > dyn\_mat < typename Derived::Scalar > qpp::adjoint ( const Eigen::MatrixBase < Derived > & A )

Adjoint.

A	Eigen expression
/ ·	Ligen expression

#### Returns

Adjoint (Hermitian conjugate) of A, as a dynamic matrix over the same scalar field as A

6.1.3.6 template<typename Derived1 , typename Derived2 > dyn\_mat<typename Derived1::Scalar> qpp::anticomm ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )

Anti-commutator.

#### See also

# qpp::comm()

Anti-commutator  $\{A, B\} = AB + BA$ . Both A and B must be Eigen expressions over the same scalar field.

#### **Parameters**

Α	Eigen expression
В	Eigen expression

#### Returns

Anti-commutator AB + BA, as a dynamic matrix over the same scalar field as A

6.1.3.7 template < typename Derived1 , typename Derived2 >  $dyn_mat < typename Derived1::Scalar > dpp::apply ( const Eigen::MatrixBase < Derived2 > & A, const std::vector < <math>idx > & subsys$ , const std::vector < idx > & dims)

Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.

Note

The dimension of the gate A must match the dimension of subsys

# **Parameters**

state	Eigen expression
Α	Eigen expression
subsys	Subsystem indexes where the gate A is applied
dims	Dimensions of the multi-partite system

#### Returns

Gate A applied to the part subsys of state

6.1.3.8 template < typename Derived1 , typename Derived2 > dyn\_mat < typename Derived1::Scalar > qpp::apply ( const Eigen::MatrixBase < Derived1 > & state, const Eigen::MatrixBase < Derived2 > & A, const std::vector < idx > & subsys, idx d = 2)

Applies the gate A to the part *subsys* of the multi-partite state vector or density matrix *state*.

Note

The dimension of the gate A must match the dimension of subsys

state	Eigen expression
Α	Eigen expression
subsys	Subsystem indexes where the gate A is applied
d	Subsystem dimensions

# Returns

Gate A applied to the part subsys of state

6.1.3.9 template<typename Derived > cmat qpp::apply ( const Eigen::MatrixBase< Derived > & rho, const std::vector< cmat > & Ks )

Applies the channel specified by the set of Kraus operators *Ks* to the density matrix *rho*.

# **Parameters**

rho	Eigen expression
Ks	Set of Kraus operators

#### Returns

Output density matrix after the action of the channel

6.1.3.10 template < typename Derived > cmat qpp::apply ( const Eigen::MatrixBase < Derived > & rho, const std::vector < cmat > & Ks, const std::vector < idx > & subsys, const std::vector < idx > & dims )

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *rho*.

# **Parameters**

rho	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes where the Kraus operators Ks are applied
dims	Dimensions of the multi-partite system

# Returns

Output density matrix after the action of the channel

6.1.3.11 template < typename Derived > cmat qpp::apply ( const Eigen::MatrixBase < Derived > & rho, const std::vector < cmat > & Ks, const std::vector < idx > & subsys, idx d = 2)

Applies the channel specified by the set of Kraus operators *Ks* to the part *subsys* of the multi-partite density matrix *rho* 

# **Parameters**

rho	Eigen expression
Ks	Set of Kraus operators

subsys	Subsystem indexes where the Kraus operators Ks are applied
d	Subsystem dimensions

#### Returns

Output density matrix after the action of the channel

Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.

# See also

```
qpp::Gates::CTRL()
```

#### Note

The dimension of the gate *A* must match the dimension of *subsys*. Also, all control subsystems in *ctrl* must have the same dimension.

#### **Parameters**

state	Eigen expression
Α	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate A is applied
dims	Dimensions of the multi-partite system

# Returns

CTRL-A gate applied to the part subsys of state

6.1.3.13 template<typename Derived1 , typename Derived2 > dyn\_mat<typename Derived1::Scalar> qpp::applyCTRL ( const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector< idx > & ctrl, const std::vector< idx > & subsys, idx d = 2)

Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.

### See also

```
qpp::Gates::CTRL()
```

### Note

The dimension of the gate A must match the dimension of subsys

# **Parameters**

state	Eigen expression

Α	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate A is applied
d	Subsystem dimensions

# Returns

CTRL-A gate applied to the part subsys of state

6.1.3.14 template < typename Container > double qpp::avg ( const std::vector < double > & prob, const Container & X )

Average.

**Parameters** 

prob	Real probability vector representing the probability distribution of <i>X</i>

# Returns

Average of X

6.1.3.15 cmat qpp::bloch2rho ( const std::vector< double > & r ) [inline]

Computes the density matrix corresponding to the 3-dimensional real Bloch vector *r*.

See also

qpp::rho2bloch()

# **Parameters**

r	3-dimensional real vector
---	---------------------------

# Returns

Qubit density matrix

6.1.3.16 std::vector < cmat > qpp::choi2kraus ( const cmat & A ) [inline]

Orthogonal Kraus operators from Choi matrix.

See also

qpp::kraus2choi()

Extracts a set of orthogonal (under Hilbert-Schmidt operator norm) Kraus operators from the Choi matrix A

Note

The Kraus operators satisfy  $Tr(K_i^{\dagger}K_j) = \delta_{ij}$  for all  $i \neq j$ 

Α	Choi matrix
---	-------------

# Returns

Set of orthogonal Kraus operators

6.1.3.17 cmat qpp::choi2super ( const cmat & A ) [inline]

Converts Choi matrix to superoperator matrix.

See also

qpp::super2choi()

# **Parameters**

Α	Choi matrix

#### Returns

Superoperator matrix

6.1.3.18 template < typename Derived1 , typename Derived2 >  $dyn_mat < typename Derived1::Scalar > qpp::comm ( const Eigen::MatrixBase < Derived1 > & A, const Eigen::MatrixBase < Derived2 > & B )$ 

Commutator.

See also

qpp::anticomm()

Commutator [A, B] = AB - BA. Both A and B must be Eigen expressions over the same scalar field.

#### **Parameters**

Α	Eigen expression
В	Eigen expression

# Returns

Commutator AB - BA, as a dynamic matrix over the same scalar field as A

6.1.3.19 template < typename T > std::vector < T > qpp::complement ( std::vector < T > subsys, idx N )

Constructs the complement of a subsystem vector.

### **Parameters**

subsys	Subsystem vector
N	Total number of systems

# Returns

The complement of *subsys* with respect to the set  $\{0, 1, \dots, N-1\}$ 

6.1.3.20 std::vector < idx > qpp::compperm ( const std::vector < idx > & perm, const std::vector < idx > & sigma ) [inline]

Compose permutations.

perm	Permutation
sigma	Permutation

# Returns

Composition of the permutations  $perm \circ sigma = perm(sigma)$ 

6.1.3.21 template < typename Derived > double qpp::concurrence ( const Eigen::MatrixBase < Derived > & A )

Wootters concurrence of the bi-partite qubit mixed state A.

# **Parameters**

Α	Eigen expression

# Returns

Wootters concurrence

6.1.3.22 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::conjugate ( const Eigen::MatrixBase< Derived > & A )

Complex conjugate.

# **Parameters**

71 Light oxpression
---------------------

# Returns

Complex conjugate of A, as a dynamic matrix over the same scalar field as A

6.1.3.23 double qpp::contfrac2x ( const std::vector < int > & cf, idx n ) [inline]

Real representation of a simple continued fraction.

# See also

qpp::x2contfrac()

# **Parameters**

cf	Integer vector containing the simple continued fraction expansion
n	Number of terms considered in the continued fraction expansion. If <i>n</i> is greater than the size
	of <i>cf</i> ,then all terms in <i>cf</i> are considered.

### Returns

Real representation of the simple continued fraction

6.1.3.24 double qpp::contfrac2x ( const std::vector < int > & cf ) [inline]

Real representation of a simple continued fraction.

See also

qpp::x2contfrac()

#### **Parameters**

cf	Integer vector containing the simple continued fraction expansion

# Returns

Real representation of the simple continued fraction

6.1.3.25 template<typename Container > double qpp::cor ( const dmat & probXY, const Container & X, const Container & Y )

# Correlation.

# **Parameters**

probXY	Real matrix representing the joint probability distribution of X and Y in lexicographical order
	(X labels the rows, Y labels the columns)
X	Random variable values represented by an STL-like container
Y	Random variable values represented by an STL-like container

# Returns

Correlation of X and Y

6.1.3.26 template < typename Derived > cmat qpp::cosm ( const Eigen::MatrixBase < Derived > & A )

Matrix cos.

**Parameters** 

Α	Eigen expression

# Returns

Matrix cosine of A

6.1.3.27 template < typename Container > double qpp::cov ( const dmat & probXY, const Container & X, const Container & Y

Covariance.

# **Parameters**

probXY	Real matrix representing the joint probability distribution of X and Y in lexicographical order
	(X labels the rows, Y labels the columns)

X	Random variable values represented by an STL-like container
Y	Random variable values represented by an STL-like container

# Returns

Covariance of X and Y

6.1.3.28 template<typename OutputScalar , typename Derived >  $dyn_mat$ <OutputScalar> qpp::cwise ( const Eigen::MatrixBase< Derived > & A, OutputScalar(\*)(const typename Derived::Scalar &) f )

#### Functor.

#### **Parameters**

Α	Eigen expression
f	Pointer-to-function from scalars of A to OutputScalar

#### Returns

Component-wise f(A), as a dynamic matrix over the  ${\it OutputScalar}$  scalar field

6.1.3.29 template<typename Derived > Derived::Scalar qpp::det ( const Eigen::MatrixBase< Derived > & A )

# Determinant.

**Parameters** 

Α	Eigen expression
---	------------------

# Returns

Determinant of A, as a scalar over the same scalar field as A. Returns  $\pm \infty$  when the determinant overflows/underflows.

6.1.3.30 template<typename T > dyn\_mat<typename T::Scalar> qpp::dirsum ( const T & head )

Direct sum.

# See also

qpp::dirsumpow()

Used to stop the recursion for the variadic template version of qpp::dirsum()

# **Parameters**

head	Eigen expression

# Returns

Its argument head

6.1.3.31 template<typename T , typename... Args> dyn\_mat<typename T::Scalar> qpp::dirsum ( const T & head, const Args &... tail )

Direct sum.

See also

qpp::dirsumpow()

#### **Parameters**

head	Eigen expression
tail	Variadic Eigen expression (zero or more parameters)

#### Returns

Direct sum of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.32 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::dirsum ( const std::vector< Derived > & As )

Direct sum.

See also

qpp::dirsumpow()

#### **Parameters**

As std::vector of Eigen expressions
-------------------------------------

# Returns

Direct sum of all elements in As, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.33 template < typename Derived > dyn\_mat < typename Derived::Scalar > qpp::dirsum ( const std::initializer\_list < Derived > & As )

Direct sum.

See also

qpp::dirsumpow()

# **Parameters**

As	std::initializer list of Eigen expressions, such as {A1, A2,, Ak}

#### Returns

Direct sum of all elements in As, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.34 template < typename Derived > dyn\_mat < typename Derived::Scalar > qpp::dirsumpow ( const Eigen::MatrixBase < Derived > & A, idx n )

Direct sum power.

See also

qpp::dirsum()

#### **Parameters**

Α	Eigen expression
n	Non-negative integer

# Returns

Direct sum of A with itself n times  $A^{\oplus n}$ , as a dynamic matrix over the same scalar field as A

6.1.3.35 template<typename Derived > internal::IOManipEigen qpp::disp ( const Eigen::MatrixBase< Derived > & A, double chop = qpp::chop )

Eigen expression ostream manipulator.

#### **Parameters**

Α	Eigen expression
chop	Set to zero the elements smaller in absolute value than <i>chop</i>

# Returns

Instance of qpp::internal::internal::IOManipEigen

6.1.3.36 internal::IOManipEigen qpp::disp(cplx z, double chop = qpp::chop) [inline]

Complex number ostream manipulator.

#### **Parameters**

Z	Complex number (or any other type implicitly cast-able to std::complex <double>)</double>
chop	Set to zero the elements smaller in absolute value than <i>chop</i>

#### Returns

Instance of qpp::internal::internal::IOManipEigen

6.1.3.37 template < typename InputIterator > internal::IOManipRange < InputIterator > qpp::disp ( InputIterator first, InputIterator last, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] " )

Range ostream manipulator.

**Parameters** 

first	Iterator to the first element of the range
last	Iterator to the last element of the range
separator	Separator
start	Left marking
end	Right marking

# Returns

Instance of qpp::internal::internal::IOManipRange

Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.

#### **Parameters**

С	Container
separator	Separator
start	Left marking
end	Right marking

#### Returns

Instance of qpp::internal::internal::IOManipRange

6.1.3.39 template<typename PointerType > internal::IOManipPointer<PointerType> qpp::disp ( const PointerType \* p, idx n, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] " )

C-style pointer ostream manipulator.

# **Parameters**

р	Pointer to the first element
n	Number of elements to be displayed
separator	Separator
start	Left marking
end	Right marking

# Returns

Instance of qpp::internal::internal::IOManipPointer

Full eigen decomposition.

#### See also

qpp::heig()

Α	Eigen expression
---	------------------

#### Returns

Pair of: 1. Eigenvalues of *A*, as a complex dynamic column vector, and 2. Eigenvectors of *A*, as columns of a complex dynamic matrix

6.1.3.41 template < typename Derived > double qpp::entanglement ( const Eigen::MatrixBase < Derived > & A, const std::vector < idx > & dims )

Entanglement of the bi-partite pure state A.

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

#### See also

qpp::entropy()

#### **Parameters**

Α	Eigen expression
dims	Dimensions of the bi-partite system

# Returns

Entanglement, with the logarithm in base 2

6.1.3.42 template < typename Derived > double qpp::entropy ( const Eigen::MatrixBase < Derived > & A )

von-Neumann entropy of the density matrix A

**Parameters** 

Α	Eigen expression

# Returns

von-Neumann entropy, with the logarithm in base 2

6.1.3.43 double qpp::entropy ( const std::vector < double > & prob ) [inline]

Shannon entropy of the probability distribution prob.

**Parameters** 

prob	Real probability vector

# Returns

Shannon entropy, with the logarithm in base 2

6.1.3.44 template<typename Derived > dyn\_col\_vect<cplx> qpp::evals ( const Eigen::MatrixBase< Derived > & A )

Eigenvalues.

See also

qpp::hevals()

**Parameters** 

```
A | Eigen expression
```

Returns

Eigenvalues of A, as a complex dynamic column vector

6.1.3.45 template<typename Derived > cmat qpp::evects ( const Eigen::MatrixBase< Derived > & A )

Eigenvectors.

See also

qpp::hevects()

**Parameters** 

Α	Eigen expression

Returns

Eigenvectors of A, as columns of a complex dynamic matrix

6.1.3.46 template<typename Derived > cmat qpp::expm ( const Eigen::MatrixBase< Derived > & A )

Matrix exponential.

**Parameters** 

```
A Eigen expression
```

Returns

Matrix exponential of A

**6.1.3.47** std::vector<ubigint> qpp::factors( ubigint n ) [inline]

Prime factor decomposition.

Note

Runs in  $\mathcal{O}(\sqrt{n})$  time complexity

n	Integer strictly greater than 1
---	---------------------------------

# Returns

Integer vector containing the factors

6.1.3.48 template < typename Derived > cmat qpp::funm ( const Eigen::MatrixBase < Derived > & A, cplx(\*)(const cplx &) f

Functional calculus f(A)

#### **Parameters**

Α	Eigen expression
f	Pointer-to-function from complex to complex

# Returns

f(A)

6.1.3.49 ubigint qpp::gcd ( ubigint m, ubigint n ) [inline]

Greatest common divisor of two non-negative integers.

# See also

qpp::lcm()

# **Parameters**

т	Non-negative integer
n	Non-negative integer

# Returns

Greatest common divisor of m and n

6.1.3.50 ubigint qpp::gcd ( const std::vector< ubigint > & ns ) [inline]

Greatest common divisor of a list of non-negative integers.

See also

qpp::lcm()

### **Parameters**

ns	List of non-negative integers

# Returns

Greatest common divisor of all numbers in ns

6.1.3.51 template < typename Derived > double qpp::gconcurrence ( const Eigen::MatrixBase < Derived > & A )

G-concurrence of the bi-partite pure state A.

Note

Both local dimensions must be equal

Uses qpp::logdet() to avoid overflows

See also

qpp::logdet()

#### **Parameters**

A	Eigen expression
---	------------------

# Returns

G-concurrence

6.1.3.52 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::grams ( const std::vector< Derived > & Vs )

Gram-Schmidt orthogonalization.

### **Parameters**

Vs	std::vector of Eigen expressions as column vectors

#### Returns

Gram-Schmidt vectors of Vs as columns of a dynamic matrix over the same scalar field as its arguments

6.1.3.53 template < typename Derived > dyn\_mat < typename Derived::Scalar > qpp::grams ( const std::initializer\_list < Derived > & Vs)

Gram-Schmidt orthogonalization.

#### **Parameters**

Vs	std::initializer_list of Eigen expressions as column vectors

## Returns

Gram-Schmidt vectors of Vs as columns of a dynamic matrix over the same scalar field as its arguments

6.1.3.54 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::grams ( const Eigen::MatrixBase< Derived > & A )

Gram-Schmidt orthogonalization.

A | Eigen expression, the input vectors are the columns of A

Returns

Gram-Schmidt vectors of the columns of A, as columns of a dynamic matrix over the same scalar field as A

6.1.3.55 template<typename Derived > std::pair<dyn\_col\_vect<double>, cmat> qpp::heig ( const Eigen::MatrixBase< Derived > & A )

Full eigen decomposition of Hermitian expression.

See also

qpp::eig()

#### **Parameters**

A Eigen expression

# Returns

Pair of: 1. Eigenvalues of A, as a real dynamic column vector, and 2. Eigenvectors of A, as columns of a complex dynamic matrix

6.1.3.56 template<typename Derived > dyn\_col\_vect<double> qpp::hevals ( const Eigen::MatrixBase< Derived > & A )

Hermitian eigenvalues.

See also

qpp::evals()

# Parameters

A | Eigen expression

Returns

Eigenvalues of Hermitian A, as a real dynamic column vector

6.1.3.57 template<typename Derived > cmat qpp::hevects ( const Eigen::MatrixBase< Derived > & A )

Hermitian eigenvectors.

See also

qpp::evects()

A | Eigen expression

Returns

Eigenvectors of Hermitian A, as columns of a complex matrix

6.1.3.58 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::inverse ( const Eigen::MatrixBase< Derived > & A )

Inverse.

**Parameters** 

A Eigen expression

Returns

Inverse of A, as a dynamic matrix over the same scalar field as A

6.1.3.59 std::vector<idx> qpp::invperm(const std::vector< idx > & perm) [inline]

Inverse permutation.

**Parameters** 

perm Permutation

Returns

Inverse of the permutation perm

**6.1.3.60** bool qpp::isprime ( ubigint *n* ) [inline]

Primality test.

Note

Runs in  $\mathcal{O}(\sqrt{n})$  time complexity

**Parameters** 

n Integer strictly greater than 1

Returns

True if the number is prime, false otherwise

6.1.3.61 cmat qpp::kraus2choi ( const std::vector < cmat > & Ks ) [inline]

Choi matrix.

See also

qpp::choi2kraus()

Constructs the Choi matrix of the channel specified by the set of Kraus operators  $\mathit{Ks}$  in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

Note

The superoperator matrix S and the Choi matrix C are related by  $S_{ab,mn}=C_{ma,nb}$ 

#### **Parameters**

		_
Ks	Set of Kraus operators	1

Returns

Choi matrix

6.1.3.62 cmat qpp::kraus2super ( const std::vector < cmat > & Ks ) [inline]

Superoperator matrix.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators Ks in the standard operator basis  $\{|i\rangle\langle j|\}$  ordered in lexicographical order, i.e.  $|0\rangle\langle 0|$ ,  $|0\rangle\langle 1|$  etc.

#### **Parameters**

Ks	Set of Kraus operators
----	------------------------

Returns

Superoperator matrix

6.1.3.63 template < typename T > dyn\_mat < typename T::Scalar > qpp::kron ( const T & head )

Kronecker product.

See also

qpp::kronpow()

Used to stop the recursion for the variadic template version of qpp::kron()

**Parameters** 

head	Eigen expression

Returns

Its argument head

6.1.3.64 template<typename T , typename... Args> dyn\_mat<typename T::Scalar> qpp::kron ( const T & head, const Args &... tail )

Kronecker product.

See also

qpp::kronpow()

head	Eigen expression
tail	Variadic Eigen expression (zero or more parameters)

# Returns

Kronecker product of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

6.1.3.65 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::kron ( const std::vector< Derived > & As )

Kronecker product.

See also

qpp::kronpow()

#### **Parameters**

As	std::vector of Eigen expressions
----	----------------------------------

# Returns

Kronecker product of all elements in As, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

Kronecker product.

See also

qpp::kronpow()

# **Parameters**

As	std::initializer_list of Eigen expressions, such as {A1, A2, ,Ak}
----	---

# Returns

Kronecker product of all elements in As, evaluated from left to right, as a dynamic matrix over the same scalar field as its arguments

Kronecker power.

See also

qpp::kron()

Α	Eigen expression
n	Non-negative integer

# Returns

Kronecker product of A with itself n times  $A^{\otimes n}$ , as a dynamic matrix over the same scalar field as A

```
6.1.3.68 ubigint qpp::lcm ( ubigint m, ubigint n ) [inline]
```

Least common multiple of two positive integers.

#### See also

qpp::gcd()

#### **Parameters**

m	Positive integer
n	Positive integer

#### Returns

Least common multiple of m and n

```
6.1.3.69 ubigint qpp::lcm ( const std::vector < ubigint > & ns ) [inline]
```

Least common multiple of a list of positive integers.

See also

qpp::gcd()

# **Parameters**

ns	List of positive integers

### Returns

Least common multiple of all numbers in ns

 $6.1.3.70 \quad template < typename \ Derived > \ dyn\_mat < typename \ Derived:: Scalar > \ qpp:: load \ ( \ const \ std:: string \ \& \ \textit{fname} \ )$ 

Loads Eigen matrix from a binary file (internal format) in double precision.

# See also

```
qpp::save()
```

The template parameter cannot be automatically deduced and must be explicitly provided, depending on the scalar field of the matrix that is being loaded.

# Example:

```
// loads a previously saved Eigen dynamic complex matrix from "input.bin"
auto mat = load<cmat>("input.bin");
```

Α	Eigen expression
fname	Output file name

6.1.3.71 template<typename Derived > Derived qpp::loadMATLABmatrix ( const std::string & mat\_file, const std::string & var\_name )

Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.

See also

qpp::saveMATLABmatrix()

This is the generic version that always throws qpp::Exception::Type::UNDEFINED\_TYPE. It is specialized only for qpp::dmat and qpp::cmat (the only matrix types that can be loaded)

```
6.1.3.72 template<> dmat qpp::loadMATLABmatrix ( const std::string & mat_file, const std::string & var_name )
[inline]
```

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices (qpp::dmat)

See also

```
qpp::saveMATLABmatrix()
```

The template parameter cannot be automatically deduced and must be explicitly provided

```
Example:
```

```
// loads a previously saved Eigen dynamic double matrix
// from the MATLAB file "input.mat"
auto mat = loadMATLABmatrix<dmat>("input.mat");
```

Note

If var\_name is a complex matrix, only the real part is loaded

### **Parameters**

mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be loaded

#### Returns

Eigen double dynamic matrix (qpp::dmat)

6.1.3.73 template<> cmat qpp::loadMATLABmatrix ( const std::string & mat\_file, const std::string & var\_name )

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

See also

qpp::saveMATLABmatrix()

The template parameter cannot be automatically deduced and must be explicitly provided

Example:

```
// loads a previously saved Eigen dynamic complex matrix
// from the MATLAB file "input.mat"
auto mat = loadMATLABmatrix<cmat>("input.mat");
```

mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be loaded

# Returns

Eigen complex dynamic matrix (qpp::cmat)

6.1.3.74 template<typename Derived > Derived::Scalar qpp::logdet ( const Eigen::MatrixBase< Derived > & A )

Logarithm of the determinant.

Useful when the determinant overflows/underflows

**Parameters** 

Α	Eigen expression

# Returns

Logarithm of the determinant of A, as a scalar over the same scalar field as A

6.1.3.75 template<typename Derived > cmat qpp::logm ( const Eigen::MatrixBase< Derived > & A )

Matrix logarithm.

# **Parameters**

Α	Eigen expression
---	------------------

# Returns

Matrix logarithm of A

6.1.3.76 template < typename Derived > double qpp::lognegativity ( const Eigen::MatrixBase < Derived > & A, const std::vector < idx > & dims)

Logarithmic negativity of the bi-partite mixed state A.

# **Parameters**

Α	Eigen expression
dims	Dimensions of the bi-partite system

# Returns

Logarithmic negativity, with the logarithm in base 2

6.1.3.77 std::vector<double> qpp::marginalX ( const dmat & probXY ) [inline]

Marginal distribution.

probXY	Real matrix representing the joint probability distribution of X and Y in lexicographical order
	(X labels the rows, Y labels the columns)

#### Returns

Real vector consisting of the marginal distribution of X

6.1.3.78 std::vector<double> qpp::marginalY ( const dmat & probXY ) [inline]

Marginal distribution.

#### **Parameters**

probXY	Real matrix representing the joint probability distribution of X and Y in lexicographical order
	(X labels the rows, Y labels the columns)

#### Returns

Real vector consisting of the marginal distribution of Y

6.1.3.79 template < typename Derived > std::tuple < idx, std::vector < double >, std::vector < cmat > > qpp::measure ( const Eigen::MatrixBase < Derived > & A, const std::vector < cmat > & Ks)

Measures the state A using the set of Kraus operators Ks.

# **Parameters**

Α	Eigen expression
Ks	Set of Kraus operators

# Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.80 template < typename Derived > std::tuple < idx, std::vector < double >, std::vector < cmat > > qpp::measure ( const Eigen::MatrixBase < Derived > & A, const std::initializer\_list < cmat > & Ks)

Measures the state A using the set of Kraus operators Ks.

# **Parameters**

Α	Eigen expression
Ks	Set of Kraus operators

# Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.81 template<typename Derived > std::tuple<idx, std::vector < double>, std::vector<cmat> > qpp::measure ( const Eigen::MatrixBase< Derived > & A, const cmat & U )

Measures the state A in the orthonormal basis specified by the unitary matrix *U*.

Α	Eigen expression
U	Unitary matrix whose columns represent the measurement basis vectors

#### Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.82 template < typename Derived > std::tuple < idx, std::vector < double >, std::vector < cmat > > qpp::measure ( const Eigen::MatrixBase < Derived > & A, const std::vector < cmat > & Ks, const std::vector < idx > & subsys, const std::vector < idx > & dims )

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

# See also

qpp::measure\_seq()

#### Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

#### **Parameters**

Α	Eigen expression
Ks	Set of Kraus operators
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

# Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.83 template < typename Derived > std::tuple < idx, std::vector < double >, std::vector < cmat > > qpp::measure ( const Eigen::MatrixBase < Derived > & A, const std::initializer\_list < cmat > & Ks, const std::vector < idx > & subsys, const std::vector < idx > & dims )

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

#### See also

qpp::measure\_seq()

## Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Α	Eigen expression
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system
Ks	Set of Kraus operators

#### Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.84 template<typename Derived > std::tuple<idx, std::vector< double>, std::vector<cmat> > qpp::measure ( const Eigen::MatrixBase< Derived > & A, const std::vector< cmat > & Ks, const std::vector< idx > & subsys, const idx d = 2)

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

#### See also

qpp::measure\_seq()

#### Note

The dimension of all *Ks* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

#### **Parameters**

,	A Eigen expression
subsy	Subsystem indexes that are measured
	d Subsystem dimensions
K	Set of Kraus operators

### Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.85 template < typename Derived > std::tuple < idx, std::vector < double >, std::vector < cmat > > qpp::measure ( const Eigen::MatrixBase < Derived > & A, const std::initializer\_list < cmat > & Ks, const std::vector < idx > & subsys, const idx d = 2)

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

# See also

qpp::measure\_seq()

# Note

The dimension of all Ks must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Α	Eigen expression
subsys	Subsystem indexes that are measured
d	Subsystem dimensions
Ks	Set of Kraus operators

#### Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

6.1.3.86 template < typename Derived > std::tuple < idx, std::vector < double >, std::vector < cmat > > qpp::measure ( const Eigen::MatrixBase < Derived > & A, const cmat & U, const std::vector < idx > & subsys, const std::vector < idx > & dims )

Measures the part *subsys* of the multi-partite state vector or density matrix *A* in the orthonormal basis specified by the unitary matrix *U*.

#### See also

qpp::measure\_seq()

#### Note

The dimension of *U* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

# **Parameters**

Α	Eigen expression
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system
U	Unitary matrix whose columns represent the measurement basis vectors

# Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

Measures the part *subsys* of the multi-partite state vector or density matrix A\ in the orthonormal basis specified by the unitary matrix U.

#### See also

qpp::measure\_seq()

### Note

The dimension of *U* must match the dimension of *subsys*. The measurement is destructive, i.e. the measured subsystems are traced away.

Α	Eigen expression
subsys	Subsystem indexes that are measured
d	Subsystem dimensions
U	Unitary matrix whose columns represent the measurement basis vectors

# Returns

Tuple of: 1. Result of the measurement, 2. Vector of outcome probabilities, and 3. Vector of post-measurement normalized states

```
6.1.3.88 template < typename Derived > std::tuple < std::vector < idx > , double, cmat > qpp::measure_seq ( const Eigen::MatrixBase < Derived > & A, std::vector < idx > subsys, std::vector < idx > dims)
```

Sequentially measures the part *subsys* of the multi-partite state vector or density matrix *A* in the computational basis.

#### See also

qpp::measure()

#### **Parameters**

Α	Eigen expression
subsys	Subsystem indexes that are measured
dims	Dimensions of the multi-partite system

# Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *subsys*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

```
6.1.3.89 template<typename Derived > std::tuple<std::vector < idx>, double, cmat> qpp::measure_seq ( const Eigen::MatrixBase< Derived > & A, std::vector< idx> subsys, idx d = 2 )
```

Sequentially measures the part *subsys* of the multi-partite state vector or density matrix *A* in the computational basis.

### See also

qpp::measure()

# **Parameters**

Α	Eigen expression
subsys	Subsystem indexes that are measured
d	Subsystem dimensions

# Returns

Tuple of: 1. Vector of outcome results of the measurement (ordered in increasing order with respect to *subsys*, i.e. first measurement result corresponds to the subsystem with the smallest index), 2. Outcome probability, and 3. Post-measurement normalized state

6.1.3.90 ket qpp::mket ( const std::vector < idx > & mask, const std::vector < idx > & dims ) [inline]

Multi-partite qudit ket.

Constructs the multi-partite qudit ket  $|\text{mask}\rangle$ , where mask is a std::vector of non-negative integers. Each element in mask has to be smaller than the corresponding element in dims.

#### Parameters 4 8 1

mask	std::vector of non-negative integers
dims	Dimensions of the multi-partite system

#### Returns

Multi-partite qudit state vector, as a complex dynamic column vector

6.1.3.91 ket qpp::mket ( const std::vector < idx > & mask, idx d=2 ) [inline]

Multi-partite qudit ket.

Constructs the multi-partite qudit ket  $|mask\rangle$ , all subsystem having equal dimension *d. mask* is a std::vector of non-negative integers, and each element in *mask* has to be strictly smaller than *d*.

## **Parameters**

mask	std::vector of non-negative integers
d	Subsystem dimensions

## Returns

Multi-partite qudit state vector, as a complex dynamic column vector

6.1.3.92 **ubigint qpp::modpow ( ubigint** *a***, ubigint** *n***, ubigint** *p* **)** [inline]

Integer power modulo p.

Computes  $a^n \mod p$ 

#### **Parameters**

а	Non-negative integer
n	Non-negative integer
р	Strictly positive integer

## Returns

 $a^n \bmod p$ 

6.1.3.93 cmat qpp::mprj ( const std::vector < idx > & mask, const std::vector < idx > & dims ) [inline]

Projector onto multi-partite qudit ket.

Constructs the projector onto the multi-partite qudit ket  $|mask\rangle$ , where mask is a std::vector of non-negative integers. Each element in mask has to be smaller than the corresponding element in dims.

mask	std::vector of non-negative integers
dims	Dimensions of the multi-partite system

## Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

6.1.3.94 cmat qpp::mprj (const std::vector < idx > & mask, idx d = 2) [inline]

Projector onto multi-partite qudit ket.

Constructs the projector onto the multi-partite qudit ket  $|mask\rangle$ , all subsystem having equal dimension d. mask is a std::vector of non-negative integers, and each element in mask has to be strictly smaller than d.

#### **Parameters**

mask	std::vector of non-negative integers
d	Subsystem dimensions

## Returns

Projector onto multi-partite qudit state vector, as a complex dynamic matrix

6.1.3.95 idx qpp::multiidx2n(const std::vector < idx > & midx, const std::vector < idx > & dims) [inline]

Multi-index to non-negative integer index.

## See also

qpp::n2multiidx()

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

## **Parameters**

midx	Multi-index
dims	Dimensions of the multi-partite system

#### Returns

Non-negative integer index

6.1.3.96 std::vector<idx> qpp::n2multiidx( idx n, const std::vector< idx > & dims ) [inline]

Non-negative integer index to multi-index.

## See also

qpp::multiidx2n()

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

n	Non-negative integer index
dims	Dimensions of the multi-partite system

## Returns

Multi-index of the same size as dims

6.1.3.97 template < typename Derived > double qpp::negativity ( const Eigen::MatrixBase < Derived > & A, const std::vector < idx > & dims )

Negativity of the bi-partite mixed state A.

#### **Parameters**

Α	Eigen expression
dims	Dimensions of the bi-partite system

## Returns

Negativity

6.1.3.98 template < typename Derived > double qpp::norm ( const Eigen::MatrixBase < Derived > & A )

Frobenius norm.

**Parameters** 

Α	Eigen expression

## Returns

Frobenius norm of A

6.1.3.99 cplx qpp::omega ( idx D ) [inline]

D-th root of unity.

**Parameters** 

D	Non-negative integer

## Returns

D-th root of unity  $\exp(2\pi i/D)$ 

**6.1.3.100** constexpr cplx qpp::operator""\_i ( unsigned long long int x ) [inline], [noexcept]

User-defined literal for complex  $i=\sqrt{-1}$  (integer overload)

Example:

```
auto z = 4_i; // type of z is std::complex<double>
```

**6.1.3.101** constexpr cplx qpp::operator""\_i ( long double x ) [inline], [noexcept]

User-defined literal for complex  $i = \sqrt{-1}$  (real overload)

Example:

```
auto z = 4.5_i; // type of z is std::complex<double>
```

6.1.3.102 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::powm ( const Eigen::MatrixBase < Derived > & A, idx n)

Matrix power.

See also

qpp::spectralpowm()

Explicitly multiplies the matrix A with itself n times. By convention  $A^0 = I$ .

#### **Parameters**

A	Eigen expression
n	Non-negative integer

#### Returns

Matrix power  $A^n$ , as a dynamic matrix over the same scalar field as A

6.1.3.103 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::prj ( const Eigen::MatrixBase < Derived > & V )

Projector.

Normalized projector onto state vector

**Parameters** 

V   Eigen expression
----------------------

## Returns

Projector onto the state vector V, or the matrix Zero if V has norm zero (i.e. smaller than qpp::eps), as a dynamic matrix over the same scalar field as A

6.1.3.104 template<typename Derived > Derived::Scalar qpp::prod ( const Eigen::MatrixBase< Derived > & A )

Element-wise product of A.

**Parameters** 

Α	Eigen expression

## Returns

Element-wise product of A, as a scalar over the same scalar field as A

6.1.3.105 template<typename InputIterator > std::iterator\_traits<InputIterator>::value\_type qpp::prod ( InputIterator first, InputIterator last )

Element-wise product of an STL-like range.

first	Iterator to the first element of the range
last	Iterator to the last element of the range

## Returns

Element-wise product of the range, as a scalar over the same scalar field as the range

6.1.3.106 template < typename Container > Container::value\_type qpp::prod ( const Container & c )

Element-wise product of the elements of an STL-like container.

#### **Parameters**

С	STL-like container

#### Returns

Element-wise product of the elements of the container, as a scalar over the same scalar field as the container

6.1.3.107 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::ptrace ( const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & subsys, const std::vector< idx > & dims )

Partial trace.

#### See also

qpp::ptrace1(), qpp::ptrace2()

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

#### **Parameters**

Α	Eigen expression
subsys	Subsystem indexes
dims	Dimensions of the multi-partite system

#### Returns

Partial trace  $Tr_{subsys}(\cdot)$  over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as A

6.1.3.108 template<typename Derived >  $dyn_mat$ <typename Derived::Scalar> qpp::ptrace ( const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & subsys, idx d = 2 )

Partial trace.

## See also

qpp::ptrace1(), qpp::ptrace2()

Partial trace of the multi-partite state vector or density matrix over a list of subsystems

Α	Eigen expression
subsys	Subsystem indexes
d	Subsystem dimensions

## Returns

Partial trace  $Tr_{subsys}(\cdot)$  over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as A

6.1.3.109 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::ptrace1 ( const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & dims )

Partial trace.

See also

qpp::ptrace2()

Partial trace over the first subsystem of bi-partite state vector or density matrix

#### **Parameters**

Α	Eigen expression
dims	Dimensions of the bi-partite system (must be a std::vector with 2 elements)

#### Returns

Partial trace  $Tr_A(\cdot)$  over the first subsystem A in a bi-partite system  $A\otimes B$ , as a dynamic matrix over the same scalar field as A

6.1.3.110 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::ptrace2 ( const Eigen::MatrixBase< Derived > & A, const std::vector < idx > & dims )

Partial trace.

See also

qpp::ptrace1()

Partial trace over the second subsystem of bi-partite state vector or density matrix

#### **Parameters**

Α	Eigen expression
dims	Dimensions of the bi-partite system (must be a std::vector with 2 elements)

#### Returns

Partial trace  $Tr_B(\cdot)$  over the second subsystem B in a bi-partite system  $A\otimes B$ , as a dynamic matrix over the same scalar field as A

6.1.3.111 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::ptranspose ( const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & subsys, const std::vector< idx > & dims )

Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

	Α	Eigen expression
s	ubsys	Subsystem indexes
	dims	Dimensions of the multi-partite system

#### Returns

Partial transpose  $(\cdot)^{T_{subsys}}$  over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as A

6.1.3.112 template < typename Derived >  $dyn_mat < typename Derived::Scalar > qpp::ptranspose ( const Eigen::MatrixBase < Derived > & A, const std::vector < idx > & subsys, idx d = 2 )$ 

#### Partial transpose.

Partial transpose of the multi-partite state vector or density matrix over a list of subsystems

#### **Parameters**

Α	Eigen expression
subsys	Subsystem indexes
d	Subsystem dimensions

#### Returns

Partial transpose  $(\cdot)^{T_{subsys}}$  over the subsytems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field as A

6.1.3.113 template<typename Derived > double qpp::qmutualinfo ( const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & subsysA, const std::vector< idx > & subsysB, const std::vector< idx > & dims )

Quantum mutual information between 2 subsystems of a composite system.

## Parameters

Α	Eigen expression
subsysA	Indexes of the first subsystem
subsysB	Indexes of the second subsystem
dims	Dimensions of the multi-partite system

## Returns

Mutual information between the 2 subsystems

6.1.3.114 template<typename Derived > double qpp::qmutualinfo ( const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & subsysA, const std::vector< idx > & subsysB, idx d = 2 )

Quantum mutual information between 2 subsystems of a composite system.

#### **Parameters**

A Eigen expression
--------------------

subsysA	Indexes of the first subsystem
subsysB	Indexes of the second subsystem
d	Subsystem dimensions

#### Returns

Mutual information between the 2 subsystems

```
6.1.3.115 double qpp::rand ( double a = 0, double b = 1 ) [inline]
```

Generates a random real number uniformly distributed in the interval [a, b)

#### **Parameters**

а	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

#### Returns

Random real number (double) uniformly distributed in the interval [a, b)

Generates a random big integer uniformly distributed in the interval [a, b].

#### **Parameters**

а	Beginning of the interval, belongs to it
b	End of the interval, belongs to it

## Returns

Random big integer uniformly distributed in the interval [a, b]

Generates a random non-negative big integer uniformly distributed in the interval [a, b].

#### **Parameters**

а	Beginning of the interval, belongs to it
b	End of the interval, belongs to it

## Returns

Random non-negative big integer uniformly distributed in the interval [a, b]

6.1.3.118 template < typename Derived > Derived qpp::rand ( idx rows, idx cols, double a = 0, double b = 1 )

Generates a random matrix with entries uniformly distributed in the interval [a, b)

If complex, then both real and imaginary parts are uniformly distributed in [a, b)

This is the generic version that always throws qpp::Exception::Type::UNDEFINED\_TYPE. It is specialized only for qpp::dmat and qpp::cmat

```
6.1.3.119 template <> dmat qpp::rand ( idx rows, idx cols, double a, double b ) [inline]
```

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)

The template parameter cannot be automatically deduced and must be explicitly provided

#### Example:

```
// generates a 3 x 3 random Eigen::MatrixXd, // with entries uniformly distributed in [-1,1) auto mat = rand<dmat>(3, 3, -1, 1);
```

#### **Parameters**

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
а	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

#### Returns

Random real matrix

```
6.1.3.120 template <> cmat qpp::rand ( idx rows, idx cols, double a, double b ) [inline]
```

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)

The template parameter cannot be automatically deduced and must be explicitly provided

## Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd, 
// with entries (both real and imaginary) uniformly distributed in [-1,1) auto mat = rand<cmat>(3, 3, -1, 1);
```

#### **Parameters**

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
а	Beginning of the interval, belongs to it
b	End of the interval, does not belong to it

## Returns

Random complex matrix

```
6.1.3.121 cmat qpp::randH(idx D) [inline]
```

Generates a random Hermitian matrix.

## **Parameters**

D	Dimension of the Hilbert space

## Returns

Random Hermitian matrix

Generates a random index (idx) uniformly distributed in the interval [a, b].

а	Beginning of the interval, belongs to it
b	End of the interval, belongs to it

#### Returns

Random index (idx) uniformly distributed in the interval [a, b]

```
6.1.3.123 ket qpp::randket(idx D) [inline]
```

Generates a random normalized ket (pure state vector)

## **Parameters**

D Dimension of the Hilbert space
----------------------------------

#### Returns

Random normalized ket

```
6.1.3.124 std::vector<cmat> qpp::randkraus(idx N, idx D) [inline]
```

Generates a set of random Kraus operators.

Note

The set of Kraus operators satisfy the closure condition  $\sum_i K_i^\dagger K_i = I$ 

## **Parameters**

_		
	N	Number of Kraus operators
	D	Dimension of the Hilbert space

## Returns

Set of N Kraus operators satisfying the closure condition

```
6.1.3.125 template < typename Derived > Derived qpp::randn ( idx rows, idx cols, double mean = 0, double sigma = 1 )
```

Generates a random matrix with entries normally distributed in N(mean, sigma)

If complex, then both real and imaginary parts are normally distributed in N(mean, sigma)

This is the generic version that always throws qpp::Exception::Type::UNDEFINED\_TYPE. It is specialized only for qpp::dmat and qpp::cmat

```
6.1.3.126 template <> dmat qpp::randn ( idx rows, idx cols, double mean, double sigma ) [inline]
```

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)

The template parameter cannot be automatically deduced and must be explicitly provided

## Example:

```
// generates a 3 x 3 random Eigen::MatrixXd, 
// with entries normally distributed in N(0,2) auto mat = randn<dmat>(3, 3, 0, 2);
```

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
mean	Mean
sigma	Standard deviation

#### Returns

Random real matrix

```
6.1.3.127 template <> cmat qpp::randn ( idx rows, idx cols, double mean, double sigma ) [inline]
```

Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)

The template parameter cannot be automatically deduced and must be explicitly provided

#### Example:

```
// generates a 3 x 3 random Eigen::MatrixXcd, // with entries (both real and imaginary) normally distributed in N(0,2) auto mat = randn<cmat>(3, 3, 0, 2);
```

#### **Parameters**

rows	Number of rows of the random generated matrix
cols	Number of columns of the random generated matrix
mean	Mean
sigma	Standard deviation

## Returns

Random complex matrix

```
6.1.3.128 double qpp::randn ( double mean = 0, double sigma = 1 ) [inline]
```

Generates a random real number (double) normally distributed in N(mean, sigma)

## **Parameters**

mean	Mean
sigma	Standard deviation

## Returns

Random real number normally distributed in N(mean, sigma)

```
6.1.3.129 std::vector<idx> qpp::randperm(idx n) [inline]
```

Generates a random uniformly distributed permutation.

Uses Knuth shuffle method (as implemented by std::shuffle), so that all permutations are equally probable

n	Size of the permutation
---	-------------------------

## Returns

Random permutation of size n

6.1.3.130 cmat qpp::randrho(idx D) [inline]

Generates a random density matrix.

**Parameters** 

D Dimension of the Hilbert space

## Returns

Random density matrix

6.1.3.131 cmat qpp::randU(idx D) [inline]

Generates a random unitary matrix.

**Parameters** 

	Dimension of the Hilbert space
--	--------------------------------

## Returns

Random unitary

6.1.3.132 cmat qpp::randV (idx Din, idx Dout) [inline]

Generates a random isometry matrix.

## **Parameters**

Din	Size of the input Hilbert space
Dout	Size of the output Hilbert space

## Returns

Random isometry matrix

6.1.3.133 template < typename Derived > double qpp::renyi ( const Eigen::MatrixBase < Derived > & A, double alpha )

Renyi-  $\alpha$  entropy of the density matrix  ${\it A}$ , for  $\alpha \geq 0$ .

Note

When  $\alpha \to 1$  the Renyi entropy converges to the von-Neumann entropy, with the logarithm in base 2

Α	Eigen expression
alpha	Non-negative real number, use qpp::infty for $\alpha = \infty$

## Returns

Renyi-  $\alpha$  entropy, with the logarithm in base 2

6.1.3.134 double qpp::renyi ( const std::vector < double > & prob, double alpha ) [inline]

Renyi-  $\alpha$  entropy of the probability distribution *prob*, for  $\alpha \geq 0$ .

Note

When  $\alpha \to 1$  the Renyi entropy converges to the Shannon entropy, with the logarithm in base 2

#### **Parameters**

prob	Real probability vector
alpha	Non-negative real number, use qpp::infty for $\alpha=\infty$

#### Returns

Renyi-  $\alpha$  entropy, with the logarithm in base 2

6.1.3.135 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::reshape ( const Eigen::MatrixBase< Derived > & A, idx rows, idx cols )

## Reshape.

Uses column-major order when reshaping (same as MATLAB)

#### **Parameters**

Α	Eigen expression
rows	Number of rows of the reshaped matrix
cols	Number of columns of the reshaped matrix

## Returns

Reshaped matrix with rows rows and cols columns, as a dynamic matrix over the same scalar field as A

6.1.3.136 template<typename Derived > std::vector<double> qpp::rho2bloch ( const Eigen::MatrixBase< Derived > & A )

Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix A.

#### See also

qpp::bloch2rho()

#### Note

It is implicitly assumed that the density matrix is Hermitian

Α	Eigen expression

#### Returns

3-dimensional Bloch vector

6.1.3.137 template<typename Derived > dyn\_col\_vect<typename Derived::Scalar> qpp::rho2pure ( const Eigen::MatrixBase< Derived > & A )

Finds the pure state representation of a matrix proportional to a projector onto a pure state.

#### Note

No purity check is done, the input state *A* must have rank one, otherwise the function returns the first non-zero eigenvector of *A* 

#### **Parameters**

Α	Eigen expression, assumed to be proportional to a projector onto a pure state, i.e. A is
	assumed to have rank one

#### Returns

The unique non-zero eigenvector of A, as a dynamic column vector over the same scalar field as A

6.1.3.138 template < typename Derived > void qpp::save ( const Eigen::MatrixBase < Derived > & A, const std::string & fname )

Saves Eigen expression to a binary file (internal format) in double precision.

#### See also

qpp::load()

## Parameters

Α	Eigen expression
fname	Output file name

6.1.3.139 template<typename Derived > void qpp::saveMATLABmatrix ( const Eigen::MatrixBase< Derived > & A, const std::string & mat\_file, const std::string & var\_name, const std::string & mode )

Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.

#### See also

qpp::loadMATLABmatrix()

This is the generic version that always throws qpp::Exception::Type::UNDEFINED\_TYPE. It is specialized only for qpp::dmat and qpp::cmat (the only matrix types that can be saved)

6.1.3.140 template <> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase < dmat > & A, const std::string & mat\_file, const std::string & var\_name, const std::string & mode ) [inline]

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices (qpp::dmat)

#### See also

qpp::loadMATLABmatrix()

#### **Parameters**

Α	Eigen expression over the complex field
mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be saved
mode	Saving mode (append, overwrite etc.), see MATLAB <i>matOpen()</i> documentation for details

6.1.3.141 template <> void qpp::saveMATLABmatrix ( const Eigen::MatrixBase < cmat > & A, const std::string & mat\_file, const std::string & var\_name, const std::string & mode ) [inline]

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

## See also

qpp::loadMATLABmatrix()

## **Parameters**

Α	Eigen expression over the complex field
mat_file	MATALB .mat file
var_name	Variable name in the .mat file representing the matrix to be saved
mode	Saving mode (append, overwrite etc.), see MATLAB matOpen() documentation for details

6.1.3.142 template < typename Derived > double qpp::schatten ( const Eigen::MatrixBase < Derived > & A, double p )

Schatten matrix norm.

## **Parameters**

Α	Eigen expression
р	Real number, greater or equal to 1, use qpp::infty for $p=\infty$

## Returns

Schatten-p matrix norm of A

6.1.3.143 template < typename Derived > cmat qpp::schmidtA ( const Eigen::MatrixBase < Derived > & A, const std::vector < idx > & dims )

Schmidt basis on Alice side.

**Parameters** 

Α	Eigen expression
dims	Dimensions of the bi-partite system

#### Returns

Unitary matrix U whose columns represent the Schmidt basis vectors on Alice side.

6.1.3.144 template < typename Derived > cmat qpp::schmidtB ( const Eigen::MatrixBase < Derived > & A, const std::vector < idx > & dims )

Schmidt basis on Bob side.

## **Parameters**

Α	Eigen expression
dims	Dimensions of the bi-partite system

#### Returns

Unitary matrix  ${\cal V}$  whose columns represent the Schmidt basis vectors on Bob side.

6.1.3.145 template < typename Derived > dyn\_col\_vect < double > qpp::schmidtcoeffs ( const Eigen::MatrixBase < Derived > & A, const std::vector < idx > & dims )

Schmidt coefficients of the bi-partite pure state A.

Note

The sum of the squares of the Schmidt coefficients equals 1

## See also

qpp::schmidtprobs()

#### **Parameters**

Α	Eigen expression
dims	Dimensions of the bi-partite system

## Returns

Schmidt coefficients of A, as a real dynamic column vector

6.1.3.146 template < typename Derived > std::vector < double > qpp::schmidtprobs ( const Eigen::MatrixBase < Derived > & A, const std::vector < idx > & dims )

Schmidt probabilities of the bi-partite pure state A.

Defined as the squares of the Schmidt coefficients. The sum of the Schmidt probabilities equals 1.

#### See also

qpp::schmidtcoeffs()

Α	Eigen expression
dims	Dimensions of the bi-partite system

## Returns

Real vector consisting of the Schmidt probabilites of A

6.1.3.147 template<typename Container > double qpp::sigma ( const std::vector< double > & prob, const Container & X )

Standard deviation.

## **Parameters**

prob	Real probability vector representing the probability distribution of X
X	Random variable values represented by an STL-like container

#### Returns

Standard deviation of X

6.1.3.148 template < typename Derived > cmat qpp::sinm ( const Eigen::MatrixBase < Derived > & A )

Matrix sin.

**Parameters** 

Α	Eigen expression
---	------------------

## Returns

Matrix sine of A

6.1.3.149 template < typename Derived > cmat qpp::spectralpowm ( const Eigen::MatrixBase < Derived > & A, const cplx z )

Matrix power.

See also

qpp::powm()

Uses the spectral decomposition of A to compute the matrix power. By convention  $A^0=I$ .

## **Parameters**

Α	Eigen expression
Z	Complex number

## Returns

Matrix power  $A^z$ 

6.1.3.150 template<typename Derived > cmat qpp::sqrtm ( const Eigen::MatrixBase< Derived > & A )

Matrix square root.

Α	Eigen expression
---	------------------

## Returns

Matrix square root of A

6.1.3.151 template < typename Derived > Derived::Scalar qpp::sum ( const Eigen::MatrixBase < Derived > & A )

Element-wise sum of A.

**Parameters** 

Α	Eigen expression
---	------------------

## Returns

Element-wise sum of A, as a scalar over the same scalar field as A

6.1.3.152 template<typename InputIterator > std::iterator\_traits<InputIterator>::value\_type qpp::sum ( InputIterator *first*, InputIterator *last* )

Element-wise sum of an STL-like range.

## **Parameters**

first	Iterator to the first element of the range
last	Iterator to the last element of the range

## Returns

Element-wise sum of the range, as a scalar over the same scalar field as the range

6.1.3.153 template<typename Container > Container::value\_type qpp::sum ( const Container & c )

Element-wise sum of the elements of an STL-like container.

**Parameters** 

С	STL-like container

## Returns

Element-wise sum of the elements of the container, as a scalar over the same scalar field as the container

6.1.3.154 cmat qpp::super2choi( const cmat & A ) [inline]

Converts superoperator matrix to Choi matrix.

## See also

qpp::choi2super()

A Superoperator matrix

Returns

Choi matrix

6.1.3.155 template<typename Derived > dyn\_col\_vect<double> qpp::svals ( const Eigen::MatrixBase< Derived > & A )

Singular values.

**Parameters** 

A Eigen expression

## Returns

Singular values of A, ordered in decreasing order, as a real dynamic column vector

6.1.3.156 template < typename Derived > std::tuple < cmat, dyn\_col\_vect < double >, cmat > qpp::svd ( const Eigen::MatrixBase < Derived > & A )

Full singular value decomposition.

**Parameters** 

A Eigen expression

## Returns

Tuple of: 1. Left sigular vectors of A, as columns of a complex dynamic matrix, 2. Singular values of A, ordered in decreasing order, as a real dynamic column vector, and 3. Right singular vectors of A, as columns of a complex dynamic matrix

 $\textbf{6.1.3.157} \quad \textbf{template} < \textbf{typename Derived} > \textbf{cmat qpp::svdU ( const Eigen::MatrixBase} < \textbf{Derived} > \textbf{\& A )}$ 

Left singular vectors.

**Parameters** 

A Eigen expression

## Returns

Complex dynamic matrix, whose columns are the left singular vectors of A

6.1.3.158 template<typename Derived > cmat qpp::svdV ( const Eigen::MatrixBase< Derived > & A )

Right singular vectors.

Α	Eigen expression
---	------------------

#### Returns

Complex dynamic matrix, whose columns are the right singular vectors of A

6.1.3.159 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::syspermute ( const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & perm, const std::vector< idx > & dims )

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit *perm[i]* is permuted to the location *i*.

#### **Parameters**

Α	Eigen expression
perm	Permutation
dims	Dimensions of the multi-partite system

#### Returns

Permuted system, as a dynamic matrix over the same scalar field as A

6.1.3.160 template<typename Derived >  $dyn_mat$ <typename Derived::Scalar> qpp::syspermute ( const Eigen::MatrixBase< Derived > & A, const std::vector< idx > & perm, idx d = 2 )

Subsystem permutation.

Permutes the subsystems of a state vector or density matrix. The qubit perm[i] is permuted to the location i.

#### **Parameters**

Α	Eigen expression
perm	Permutation
d	Subsystem dimensions

## Returns

Permuted system, as a dynamic matrix over the same scalar field as A

6.1.3.161 template<typename Derived > Derived::Scalar qpp::trace ( const Eigen::MatrixBase< Derived > & A )

#### Trace.

#### **Parameters**

Α	Eigen expression

#### Returns

Trace of A, as a scalar over the same scalar field as A

6.1.3.162 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::transpose ( const Eigen::MatrixBase< Derived > & A )

Transpose.

Α	Eigen expression
---	------------------

## Returns

Transpose of A, as a dynamic matrix over the same scalar field as A

6.1.3.163 template < typename Derived > double qpp::tsallis ( const Eigen::MatrixBase < Derived > & A, double q )

Tsallis- q entropy of the density matrix A, for  $q \geq 0$ .

Note

When  $q \to 1$  the Tsallis entropy converges to the von-Neumann entropy, with the logarithm in base e

#### **Parameters**

Α	Eigen expression
q	Non-negative real number

#### Returns

Tsallis- q entropy

6.1.3.164 double qpp::tsallis ( const std::vector < double > & prob, double q ) [inline]

Tsallis- q entropy of the probability distribution *prob*, for  $q \ge 0$ .

Note

When  $q \to 1$  the Tsallis entropy converges to the Shannon entropy, with the logarithm in base e

## **Parameters**

prob	Real probability vector
q	Non-negative real number

## Returns

Tsallis- q entropy

6.1.3.165 std::vector<double> qpp::uniform(idx N) [inline]

Uniform probability distribution vector.

## Parameters

N	Size of the alphabet

## Returns

Real vector consisting of a uniform distribution of size N

6.1.3.166 template < typename Container > double qpp::var ( const std::vector < double > & prob, const Container & X )

Variance.

	prob	Real probability vector representing the probability distribution of X
ſ	X	Random variable values represented by an STL-like container

## Returns

Variance of X

6.1.3.167 std::vector<int> qpp::x2contfrac ( double x, idx n, idx cut = 1e5 ) [inline]

Simple continued fraction expansion.

#### See also

qpp::contfrac2x()

#### **Parameters**

X	Real number
n	Number of terms in the expansion
cut	Stop the expansion when the next term is greater than <i>cut</i>

#### Returns

Integer vector containing the simple continued fraction expansion of x. If there are m less than n terms in the expansion, a shorter vector with m components is returned.

## 6.1.4 Variable Documentation

6.1.4.1 constexpr double qpp::chop = 1e-10

Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.

6.1.4.2 constexpr double qpp::ee = 2.718281828459045235360287471352662497

Base of natural logarithm, e.

6.1.4.3 constexpr double qpp::eps = 1e-12

Used to decide whether a number or expression in double precision is zero or not.

## Example:

```
if(std::abs(x) < qpp::eps) // x is zero</pre>
```

6.1.4.4 constexpr double qpp::infty = std::numeric\_limits < double >::infinity()

Used to denote infinity in double precision.

6.1.4.5 constexpr idx qpp::maxn = 64

Maximum number of allowed qu(d)its (subsystems)

Used internally to allocate arrays on the stack (for speed reasons)

6.1.4.6 constexpr double qpp::pi = 3.141592653589793238462643383279502884

 $\pi$ 

# 6.2 qpp::experimental Namespace Reference

Experimental/test functions/classes, do not use or modify.

## 6.2.1 Detailed Description

Experimental/test functions/classes, do not use or modify.

## 6.3 qpp::internal Namespace Reference

Internal utility functions, do not use/modify.

#### Classes

- class IOManipEigen
- class IOManipPointer
- · class IOManipRange
- class Singleton

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

## **Functions**

- void \_n2multiidx (idx n, idx numdims, const idx \*dims, idx \*result) noexcept
- idx \_multiidx2n (const idx \*midx, idx numdims, const idx \*dims) noexcept
- $\bullet \ \ \text{template}{<} \text{typename Derived}>$

bool \_check\_square\_mat (const Eigen::MatrixBase< Derived > &A)

 $\bullet \ \ \mathsf{template}{<}\mathsf{typename} \ \mathsf{Derived}>$ 

 $bool\_check\_vector~(const~Eigen::MatrixBase < Derived > \&A)$ 

template<typename Derived >

 $bool\_check\_rvector~(const~Eigen::MatrixBase < Derived > \&A)$ 

template<typename Derived >

 ${\tt bool\_check\_cvector} \ ({\tt const} \ {\tt Eigen::MatrixBase} < {\tt Derived} > \& {\tt A})$ 

• template<typename T >

bool \_check\_nonzero\_size (const T &x) noexcept

• template<typename T1 , typename T2 >

bool \_check\_matching\_sizes (const T1 &lhs, const T2 &rhs) noexcept

- bool check dims (const std::vector< idx > &dims)
- template<typename Derived >

bool \_check\_dims\_match\_mat (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)

• template<typename Derived >

bool <u>\_check\_dims\_match\_cvect</u> (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &V)

• template<typename Derived >

 $bool\_check\_dims\_match\_rvect \ (const\ std::vector < idx > \&dims,\ const\ Eigen::MatrixBase < Derived > \&V)$ 

- bool check eq dims (const std::vector < idx > &dims, idx dim) noexcept
- bool \_check\_subsys\_match\_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)

- template < typename Derived >
   bool \_check\_qubit\_matrix (const Eigen::MatrixBase < Derived > &A) noexcept
- template<typename Derived >
   bool \_check\_qubit\_cvector (const Eigen::MatrixBase< Derived > &V) noexcept
- template<typename Derived >
   bool \_check\_qubit\_rvector (const Eigen::MatrixBase< Derived > &V) noexcept
- template<typename Derived >
   bool \_check\_qubit\_vector (const Eigen::MatrixBase< Derived > &V) noexcept
- bool <u>\_check\_perm</u> (const std::vector< idx > &perm)
- template<typename Derived1 , typename Derived2 >
   dyn\_mat< typename Derived1::Scalar > \_kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen
   ::MatrixBase< Derived2 > &B)
- template<typename Derived1 , typename Derived2 >
   dyn\_mat< typename Derived1::Scalar > \_dirsum2 (const Eigen::MatrixBase< Derived1 > &A, const
   Eigen::MatrixBase< Derived2 > &B)
- template<typename T >
   void variadic\_vector\_emplace (std::vector< T > &)
- template<typename T, typename First, typename... Args>
   void variadic\_vector\_emplace (std::vector< T > &v, First &&first, Args &&...args)

## 6.3.1 Detailed Description

Internal utility functions, do not use/modify.

#### 6.3.2 Function Documentation

- 6.3.2.1 template < typename Derived > bool qpp::internal::\_check\_cvector ( const Eigen::MatrixBase < Derived > & A )
- **6.3.2.2** bool qpp::internal::\_check\_dims ( const std::vector < idx > & dims ) [inline]
- 6.3.2.3 template<typename Derived > bool qpp::internal::\_check\_dims\_match\_cvect ( const std::vector< idx > & dims, const Eigen::MatrixBase< Derived > & V )
- $6.3.2.4 \quad template < typename \ Derived > bool \ qpp::internal::\_check\_dims\_match\_mat \ ( \ const \ std::vector < idx > \& \ dims, \ const \ Eigen::MatrixBase < Derived > \& \ A \ )$
- 6.3.2.5 template<typename Derived > bool qpp::internal::\_check\_dims\_match\_rvect ( const std::vector< idx > & dims, const Eigen::MatrixBase< Derived > & V )
- 6.3.2.6 bool qpp::internal::\_check\_eq\_dims ( const std::vector < idx > & dims, idx dim ) [inline], [noexcept]
- 6.3.2.7 template<typename T1 , typename T2 > bool qpp::internal::\_check\_matching\_sizes ( const T1 & *lhs*, const T2 & *rhs* ) [noexcept]
- **6.3.2.8** template < typename T > bool qpp::internal::\_check\_nonzero\_size( const T & x ) [noexcept]
- 6.3.2.9 bool gpp::internal:: check perm ( const std::vector < idx > & perm ) [inline]
- $\textbf{6.3.2.11} \quad \textbf{template} < \textbf{typename Derived} > \textbf{bool qpp::internal::\_check\_qubit\_matrix} \ \textbf{( const Eigen::MatrixBase} < \textbf{Derived} > \textbf{\& A )} \\ \textbf{[ noexcept]}$

- $\textbf{6.3.2.13} \quad \textbf{template} < \textbf{typename Derived} > \textbf{bool qpp::internal::\_check\_qubit\_vector} \ ( \ \textbf{const Eigen::MatrixBase} < \textbf{Derived} > \textbf{\& V } \ ) \\ \text{[noexcept]}$
- 6.3.2.14 template < typename Derived > bool qpp::internal::\_check\_rvector ( const Eigen::MatrixBase < Derived > & A )
- 6.3.2.15 template<typename Derived > bool qpp::internal::\_check\_square\_mat ( const Eigen::MatrixBase< Derived > & A )
- 6.3.2.16 bool qpp::internal::\_check\_subsys\_match\_dims ( const std::vector < idx > & subsys, const std::vector < idx > & dims ) [inline]
- 6.3.2.17 template<typename Derived > bool qpp::internal::\_check\_vector ( const Eigen::MatrixBase< Derived > & A )
- 6.3.2.18 template<typename Derived1 , typename Derived2 > dyn\_mat<typename Derived1::Scalar> qpp::internal::\_dirsum2 ( const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B )
- 6.3.2.20 idx qpp::internal::\_multiidx2n ( const idx \* midx, idx numdims, const idx \* dims ) [inline], [noexcept]
- 6.3.2.21 void qpp::internal::\_n2multiidx ( idx n, idx n numdims, const idx \* dims, idx \* result ) [inline], [noexcept]
- 6.3.2.22 template < typename T > void qpp::internal::variadic\_vector\_emplace ( std::vector < T > & )
- 6.3.2.23 template < typename T , typename First , typename... Args > void qpp::internal::variadic\_vector\_emplace ( std::vector < T > & v, First && first, Args &&... args )

# **Chapter 7**

# **Class Documentation**

# 7.1 qpp::Codes Class Reference

const Singleton class that defines quantum error correcting codes

#include <classes/codes.h>

Inheritance diagram for qpp::Codes:



Collaboration diagram for qpp::Codes:



84 Class Documentation

## **Public Types**

enum Type { Type::FIVE\_QUBIT = 1, Type::SEVEN\_QUBIT\_STEANE, Type::NINE\_QUBIT\_SHOR }
 Code types, add more codes here if needed.

## **Public Member Functions**

ket codeword (Type type, idx i) const
 Returns the codeword of the specified code type.

## **Private Member Functions**

• Codes ()

Default constructor.

Codes ()=default

Default destructor.

## **Friends**

class internal::Singleton < const Codes >

## **Additional Inherited Members**

# 7.1.1 Detailed Description

const Singleton class that defines quantum error correcting codes

## 7.1.2 Member Enumeration Documentation

```
7.1.2.1 enum qpp::Codes::Type [strong]
```

Code types, add more codes here if needed.

See also

```
qpp::Codes::codeword()
```

## Enumerator

```
FIVE_QUBIT [[5,1,3]] qubit code
SEVEN_QUBIT_STEANE [[7,1,3]] Steane qubit code
NINE_QUBIT_SHOR [[9,1,3]] Shor qubit code
```

## 7.1.3 Constructor & Destructor Documentation

```
7.1.3.1 qpp::Codes::Codes( ) [inline],[private]
```

Default constructor.

```
7.1.3.2 qpp::Codes::~Codes() [private], [default]
```

Default destructor.

## 7.1.4 Member Function Documentation

7.1.4.1 ket qpp::Codes::codeword ( Type type, idx i ) const [inline]

Returns the codeword of the specified code type.

See also

qpp::Codes::Type

## **Parameters**

type	Code type
i	Codeword index

#### Returns

i-th codeword of the code type

## 7.1.5 Friends And Related Function Documentation

**7.1.5.1 friend class internal::Singleton**< **const Codes**> [friend]

The documentation for this class was generated from the following file:

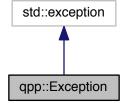
· classes/codes.h

# 7.2 qpp::Exception Class Reference

Generates custom exceptions, used when validating function parameters.

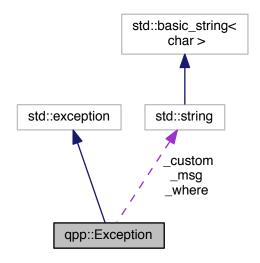
#include <classes/exception.h>

Inheritance diagram for qpp::Exception:



86 Class Documentation

Collaboration diagram for qpp::Exception:



## **Public Types**

enum Type {

Type::UNKNOWN\_EXCEPTION = 1, Type::ZERO\_SIZE, Type::MATRIX\_NOT\_SQUARE, Type::MATRIX\_← NOT\_CVECTOR,

Type::MATRIX\_NOT\_RVECTOR, Type::MATRIX\_NOT\_VECTOR, Type::MATRIX\_NOT\_SQUARE\_OR\_C↔ VECTOR, Type::MATRIX\_NOT\_SQUARE\_OR\_RVECTOR,

Type::MATRIX\_NOT\_SQUARE\_OR\_VECTOR, Type::MATRIX\_MISMATCH\_SUBSYS, Type::DIMS\_INVA← LID, Type::DIMS\_NOT\_EQUAL,

Type::DIMS\_MISMATCH\_MATRIX, Type::DIMS\_MISMATCH\_CVECTOR, Type::DIMS\_MISMATCH\_RVE← CTOR, Type::DIMS\_MISMATCH\_VECTOR,

Type::SUBSYS\_MISMATCH\_DIMS, Type::PERM\_INVALID, Type::PERM\_MISMATCH\_DIMS, Type::NOT ← QUBIT\_MATRIX,

Type::NOT\_QUBIT\_CVECTOR, Type::NOT\_QUBIT\_RVECTOR, Type::NOT\_QUBIT\_VECTOR, Type::NO $\leftarrow$  T\_QUBIT\_SUBSYS,

Type::NOT\_BIPARTITE, Type::NO\_CODEWORD, Type::OUT\_OF\_RANGE, Type::TYPE\_MISMATCH, Type::SIZE\_MISMATCH, Type::UNDEFINED\_TYPE, Type::CUSTOM\_EXCEPTION }

Exception types, add more here if needed.

# **Public Member Functions**

• Exception (const std::string &where, const Type &type)

Constructs an exception.

• Exception (const std::string &where, const std::string &custom)

Constructs an exception.

virtual const char \* what () const noexceptoverride

Overrides std::exception::what()

#### **Private Member Functions**

· void construct exception msg ()

Constructs the exception description from its type.

## **Private Attributes**

- · std::string \_where
- std::string \_msg
- Type \_type
- std::string \_custom

## 7.2.1 Detailed Description

Generates custom exceptions, used when validating function parameters.

Customize this class if more exceptions are needed

#### 7.2.2 Member Enumeration Documentation

**7.2.2.1** enum qpp::Exception::Type [strong]

Exception types, add more here if needed.

See also

qpp::Exception:: construct exception msg()

#### Enumerator

UNKNOWN\_EXCEPTION Unknown exception

**ZERO\_SIZE** Zero sized object, e.g. empty Eigen::Matrix or std::vector<> with no elements

MATRIX\_NOT\_SQUARE Eigen::Matrix is not square

MATRIX\_NOT\_CVECTOR Eigen::Matrix is not a column vector

MATRIX\_NOT\_RVECTOR Eigen::Matrix is not a row vector

MATRIX\_NOT\_VECTOR Eigen::Matrix is not a row/column vector

MATRIX\_NOT\_SQUARE\_OR\_CVECTOR Eigen::Matrix is not square nor a column vector

MATRIX\_NOT\_SQUARE\_OR\_RVECTOR Eigen::Matrix is not square nor a row vector

**MATRIX\_NOT\_SQUARE\_OR\_VECTOR** Eigen::Matrix is not square nor a row/column vector

MATRIX\_MISMATCH\_SUBSYS Matrix size mismatch subsystem sizes (e.g. in qpp::apply())

**DIMS\_INVALID** std::vector<idx> of dimensions has zero size or contains zeros

DIMS\_NOT\_EQUAL Local/global dimensions are not equal

**DIMS\_MISMATCH\_MATRIX** Product of the elements of std::vector<idx> of dimensions is not equal to the number of rows of Eigen::Matrix (assumed to be a square matrix)

**DIMS\_MISMATCH\_CVECTOR** Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of Eigen::Matrix (assumed to be a column vector)

**DIMS\_MISMATCH\_RVECTOR** Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of Eigen::Matrix (assumed to be a row vector)

**DIMS\_MISMATCH\_VECTOR** Product of the elements of std::vector<idx> of dimensions is not equal to the number of elements of Eigen::Matrix (assumed to be a row/column vector)

**SUBSYS\_MISMATCH\_DIMS** std::vector<idx> of subsystem labels has duplicates, or has entries that are larger than the size of the std::vector<idx> of dimensions

88 Class Documentation

**PERM\_INVALID** std::vector<idx> does note represent a valid permutation

**PERM\_MISMATCH\_DIMS** Size of the std::vector<idx> representing the permutation is different from the size of the std::vector<idx> of dimensions

NOT\_QUBIT\_MATRIX Eigen::Matrix is not 2 x 2

NOT\_QUBIT\_CVECTOR Eigen::Matrix is not 2 x 1

NOT\_QUBIT\_RVECTOR Eigen::Matrix is not 1 x 2

NOT\_QUBIT\_VECTOR Eigen::Matrix is not 1 x 2 nor 2 x 1

NOT\_QUBIT\_SUBSYS Subsystems are not 2-dimensional

NOT\_BIPARTITE std::vector<idx> of dimensions has size different from 2

**NO\_CODEWORD** Codeword does not exist, thrown when calling qpp::Codes::codeword() with invalid index i

OUT\_OF\_RANGE Parameter out of range

TYPE\_MISMATCH Scalar types do not match

SIZE MISMATCH Sizes do not match

UNDEFINED\_TYPE Templated specialization not defined for this type

CUSTOM\_EXCEPTION Custom exception, user must provide a custom message

#### 7.2.3 Constructor & Destructor Documentation

7.2.3.1 qpp::Exception::Exception (const std::string & where, const Type & type ) [inline]

Constructs an exception.

#### **Parameters**

where	Text representing where the exception occured
type	Exception type, defined in qpp::Exception::Type

7.2.3.2 qpp::Exception::Exception ( const std::string & where, const std::string & custom ) [inline]

Constructs an exception.

This is an overloaded member function, provided for convenience. It differs from the above function only in what argument(s) it accepts.

#### **Parameters**

where	Text representing where the exception occured
custom	Exception description

## 7.2.4 Member Function Documentation

7.2.4.1 void qpp::Exception::\_construct\_exception\_msg( ) [inline], [private]

Constructs the exception description from its type.

See also

qpp::Exception::Type

Must modify the code of this function if more exceptions are added

7.2.4.2 virtual const char\* qpp::Exception::what( ) const [inline], [override], [virtual], [noexcept]

Overrides std::exception::what()

#### Returns

**Exception** description

## 7.2.5 Member Data Documentation

```
7.2.5.1 std::string qpp::Exception::_custom [private]
```

**7.2.5.2 std::string qpp::Exception::\_msg** [private]

7.2.5.3 Type qpp::Exception::\_type [private]

**7.2.5.4 std::string qpp::Exception::\_where** [private]

The documentation for this class was generated from the following file:

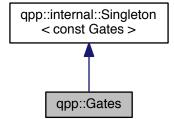
· classes/exception.h

# 7.3 qpp::Gates Class Reference

const Singleton class that implements most commonly used gates

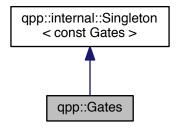
#include <classes/gates.h>

Inheritance diagram for qpp::Gates:



90 Class Documentation

Collaboration diagram for qpp::Gates:



#### **Public Member Functions**

• cmat Rn (double theta, const std::vector< double > &n) const

Rotation of theta about the 3-dimensional real unit vector n.

• cmat Zd (idx D) const

Generalized Z gate for gudits.

• cmat Fd (idx D) const

Fourier transform gate for qudits.

• cmat Xd (idx D) const

Generalized X gate for qudits.

• template<typename Derived = Eigen::MatrixXcd>

Derived Id (idx D) const

Identity gate.

• template<typename Derived >

dyn\_mat< typename Derived::Scalar > CTRL (const Eigen::MatrixBase< Derived > &A, const std::vector<
idx > &ctrl, const std::vector< idx > &subsys, idx n, idx d=2) const

Generates the multi-partite multiple-controlled-A gate in matrix form.

• template<typename Derived >

dyn\_mat< typename Derived::Scalar > expandout (const Eigen::MatrixBase< Derived > &A, idx pos, const
std::vector< idx > &dims) const

Expands out.

## **Public Attributes**

• cmat Id2 {cmat::Identity(2, 2)}

Identity gate.

cmat H {cmat::Zero(2, 2)}

Hadamard gate.

cmat X {cmat::Zero(2, 2)}

Pauli Sigma-X gate.

cmat Y {cmat::Zero(2, 2)}

Pauli Sigma-Y gate.

cmat Z {cmat::Zero(2, 2)}

Pauli Sigma-Z gate.

• cmat S {cmat::Zero(2, 2)}

```
S gate.

cmat T {cmat::Zero(2, 2)}
T gate.

cmat CNOT {cmat::Identity(4, 4)}
Controlled-NOT control target gate.

cmat CZ {cmat::Identity(4, 4)}
Controlled-Phase gate.

cmat CNOTba {cmat::Zero(4, 4)}
Controlled-NOT target control gate.

cmat SWAP {cmat::Identity(4, 4)}
SWAP gate.

cmat TOF {cmat::Identity(8, 8)}
Toffoli gate.
```

• cmat FRED {cmat::Identity(8, 8)}

## **Private Member Functions**

Fredkin gate.

• Gates ()

Initializes the gates.

∼Gates ()=default

Default destructor.

## **Friends**

class internal::Singleton < const Gates >

## **Additional Inherited Members**

## 7.3.1 Detailed Description

Default destructor.

const Singleton class that implements most commonly used gates

## 7.3.2 Constructor & Destructor Documentation

```
7.3.2.1 qpp::Gates::Gates( ) [inline],[private]
Initializes the gates.
7.3.2.2 qpp::Gates::~Gates( ) [private],[default]
```

## 7.3.3 Member Function Documentation

7.3.3.1 template < typename Derived > dyn\_mat < typename Derived::Scalar > qpp::Gates::CTRL ( const Eigen::MatrixBase < Derived > & A, const std::vector < idx > & ctrl, const std::vector < idx > & subsys, idx n, idx d = 2) const [inline]

Generates the multi-partite multiple-controlled-A gate in matrix form.

92 Class Documentation

#### See also

qpp::applyCTRL()

Note

The dimension of the gate A must match the dimension of subsys

#### **Parameters**

Α	Eigen expression
ctrl	Control subsystem indexes
subsys	Subsystem indexes where the gate A is applied
n	Total number of subsystems
d	Subsystem dimensions

#### Returns

CTRL-A gate, as a matrix over the same scalar field as A

7.3.3.2 template<typename Derived > dyn\_mat<typename Derived::Scalar> qpp::Gates::expandout ( const Eigen::MatrixBase< Derived > & A, idx pos, const std::vector< idx > & dims ) const [inline]

Expands out.

See also

qpp::kron()

Expands out A as a matrix in a multi-partite system. Faster than using qpp::kron(I, I, ..., I, A, I, ..., I).

## **Parameters**

Α	Eigen expression
pos	Position
dims	Dimensions of the multi-partite system

## Returns

Tensor product  $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$ , with A on position pos, as a dynamic matrix over the same scalar field as A

7.3.3.3 cmat qpp::Gates::Fd(idx D)const [inline]

Fourier transform gate for qudits.

Note

Defined as  $F = \sum_{jk} \exp(2\pi i j k/D) |j\rangle\langle k|$ 

**Parameters** 

D	Dimension of the Hilbert space

Returns

Fourier transform gate for qudits

7.3.3.4 template < typename Derived = Eigen::MatrixXcd > Derived qpp::Gates::Id ( idx D ) const [inline]

Identity gate.

Note

Can change the return type from complex matrix (default) by explicitly specifying the template parameter

#### **Parameters**

D	Dimension of the Hilbert space

Returns

Identity gate

7.3.3.5 cmat qpp::Gates::Rn ( double theta, const std::vector< double > & n ) const [inline]

Rotation of *theta* about the 3-dimensional real unit vector *n*.

#### **Parameters**

theta	Rotation angle
n	3-dimensional real unit vector

#### Returns

Rotation gate

7.3.3.6 cmat qpp::Gates::Xd (idx D) const [inline]

Generalized X gate for qudits.

Note

Defined as 
$$X = \sum_j |j \oplus 1\rangle\langle j|$$

#### **Parameters**

D	Dimension of the Hilbert space

Returns

Generalized X gate for qudits

7.3.3.7 cmat qpp::Gates::Zd(idx D) const [inline]

Generalized Z gate for qudits.

Note

Defined as  $Z = \sum_{j} \exp(2\pi i j/D) |j\rangle\langle j|$ 

**Parameters** 

D Dimension of the Hilbert space

Returns

Generalized Z gate for qudits

7.3.4 Friends And Related Function Documentation

**7.3.4.1** friend class internal::Singleton < const Gates > [friend]

7.3.5 Member Data Documentation

7.3.5.1 cmat qpp::Gates::CNOT {cmat::Identity(4, 4)}

Controlled-NOT control target gate.

7.3.5.2 cmat qpp::Gates::CNOTba {cmat::Zero(4, 4)}

Controlled-NOT target control gate.

7.3.5.3 cmat qpp::Gates::CZ {cmat::Identity(4, 4)}

Controlled-Phase gate.

7.3.5.4 cmat qpp::Gates::FRED {cmat::Identity(8, 8)}

Fredkin gate.

7.3.5.5 cmat qpp::Gates::H {cmat::Zero(2, 2)}

Hadamard gate.

7.3.5.6 cmat qpp::Gates::ld2 {cmat::Identity(2, 2)}

Identity gate.

7.3.5.7 cmat qpp::Gates::S {cmat::Zero(2, 2)}

S gate.

7.3.5.8 cmat qpp::Gates::SWAP {cmat::Identity(4, 4)}

SWAP gate.

7.3.5.9 cmat qpp::Gates::T {cmat::Zero(2, 2)}

T gate.

7.3.5.10 cmat qpp::Gates::TOF {cmat::Identity(8, 8)}

Toffoli gate.

7.3.5.11 cmat qpp::Gates::X {cmat::Zero(2, 2)}

Pauli Sigma-X gate.

7.3.5.12 cmat qpp::Gates::Y {cmat::Zero(2, 2)}

Pauli Sigma-Y gate.

7.3.5.13 cmat qpp::Gates::Z {cmat::Zero(2, 2)}

Pauli Sigma-Z gate.

The documentation for this class was generated from the following file:

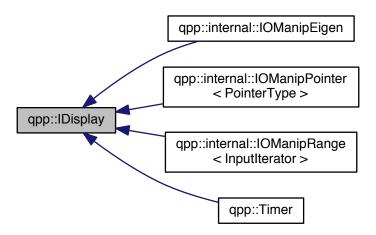
· classes/gates.h

## 7.4 qpp::IDisplay Class Reference

Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

#include <classes/idisplay.h>

Inheritance diagram for qpp::IDisplay:



## **Public Member Functions**

- IDisplay ()=default
   Default constructor.
- IDisplay (const IDisplay &)=default

Default copy constructor.

• IDisplay (IDisplay &&)=default

Default move constructor.

• IDisplay & operator= (const IDisplay &)=default

Default copy assignment operator.

• IDisplay & operator= (IDisplay &&)=default

Default move assignment operator.

virtual ∼IDisplay ()=default

Default virtual destructor.

#### **Private Member Functions**

virtual std::ostream & display (std::ostream &os) const =0
 Must be overridden by all derived classes.

#### **Friends**

std::ostream & operator<< (std::ostream &os, const IDisplay &rhs)</li>
 Overloads the extraction operator.

#### 7.4.1 Detailed Description

Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

This class defines friend inline std::ostream& operator<< (std::ostream& os, const qpp::IDisplay& rhs). The latter delegates the work to the pure private virtual function qpp::IDisplay::display() which has to be overridden by all derived classes.

#### 7.4.2 Constructor & Destructor Documentation

```
7.4.2.1 qpp::IDisplay::IDisplay( ) [default]

Default constructor.
```

7.4.2.2 qpp::IDisplay::IDisplay ( const IDisplay & ) [default]

Default copy constructor.

7.4.2.3 qpp::IDisplay::IDisplay ( IDisplay && ) [default]

Default move constructor.

7.4.2.4 virtual qpp::IDisplay::~IDisplay( ) [virtual], [default]

Default virtual destructor.

#### 7.4.3 Member Function Documentation

7.4.3.1 virtual std::ostream& qpp::IDisplay::display( std::ostream & os ) const [private], [pure virtual]

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs).

Implemented in qpp::internal::IOManipEigen, qpp::Timer, qpp::internal::IOManipPointer< PointerType >, and qpp::internal::IOManipRange< InputIterator >.

7.4.3.2 IDisplay& qpp::IDisplay::operator=( const IDisplay & ) [default]

Default copy assignment operator.

7.4.3.3 IDisplay& qpp::IDisplay::operator=(IDisplay && ) [default]

Default move assignment operator.

#### 7.4.4 Friends And Related Function Documentation

7.4.4.1 std::ostream& operator<< ( std::ostream & os, const IDisplay & rhs ) [friend]

Overloads the extraction operator.

Delegates the work to the virtual function <a href="mailto:qpp::IDisplay::display">qpp::IDisplay::display()</a>

The documentation for this class was generated from the following file:

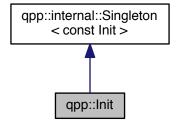
· classes/idisplay.h

## 7.5 qpp::Init Class Reference

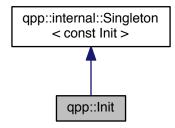
const Singleton class that performs additional initializations/cleanups

#include <classes/init.h>

Inheritance diagram for qpp::Init:



Collaboration diagram for qpp::Init:



#### **Private Member Functions**

• Init ()

Additional initializations.

• ∼Init ()

Cleanups.

#### **Friends**

class internal::Singleton < const Init >

## **Additional Inherited Members**

## 7.5.1 Detailed Description

const Singleton class that performs additional initializations/cleanups

#### 7.5.2 Constructor & Destructor Documentation

```
7.5.2.1 qpp::Init::Init( ) [inline],[private]
```

Additional initializations.

```
7.5.2.2 qpp::Init::\simInit( ) [inline],[private]
```

Cleanups.

### 7.5.3 Friends And Related Function Documentation

**7.5.3.1** friend class internal::Singleton < const lnit > [friend]

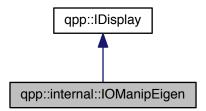
The documentation for this class was generated from the following file:

· classes/init.h

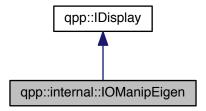
## 7.6 qpp::internal::IOManipEigen Class Reference

#include <internal/classes/iomanip.h>

Inheritance diagram for qpp::internal::IOManipEigen:



Collaboration diagram for qpp::internal::IOManipEigen:



#### **Public Member Functions**

- template<typename Derived >
   IOManipEigen (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)
- IOManipEigen (const cplx z, double chop=qpp::chop)

## **Private Member Functions**

std::ostream & display (std::ostream &os) const override
 Must be overridden by all derived classes.

#### **Private Attributes**

- cmat \_A
- double <u>\_chop</u>

#### 7.6.1 Constructor & Destructor Documentation

- 7.6.1.1 template<typename Derived > qpp::internal::IOManipEigen::IOManipEigen ( const Eigen::MatrixBase< Derived > & A, double chop = qpp::chop ) [inline], [explicit]
- 7.6.1.2 qpp::internal::IOManipEigen::IOManipEigen ( const cplx z, double chop = qpp::chop ) [inline], [explicit]

#### 7.6.2 Member Function Documentation

**7.6.2.1** std::ostream& qpp::internal::IOManipEigen::display ( std::ostream & os ) const [inline], [override], [private], [virtual]

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs). Implements qpp::IDisplay.

#### 7.6.3 Member Data Documentation

- 7.6.3.1 cmat qpp::internal::IOManipEigen::\_A [private]
- **7.6.3.2** double qpp::internal::IOManipEigen::\_chop [private]

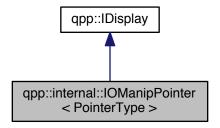
The documentation for this class was generated from the following file:

• internal/classes/iomanip.h

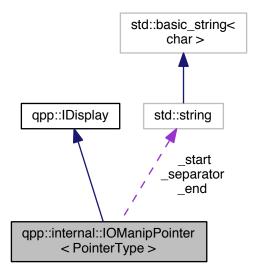
## 7.7 qpp::internal::IOManipPointer < PointerType > Class Template Reference

#include <internal/classes/iomanip.h>

Inheritance diagram for qpp::internal::IOManipPointer< PointerType >:



Collaboration diagram for qpp::internal::IOManipPointer< PointerType >:



#### **Public Member Functions**

- IOManipPointer (const PointerType \*p, const idx n, const std::string &separator, const std::string &start="[", const std::string &end="]")
- IOManipPointer (const IOManipPointer &)=default
- IOManipPointer & operator= (const IOManipPointer &)=default

#### **Private Member Functions**

std::ostream & display (std::ostream &os) const override
 Must be overridden by all derived classes.

#### **Private Attributes**

- const PointerType \* \_p
- idx \_n
- · std::string \_separator
- std::string \_start
- std::string \_end

## 7.7.1 Constructor & Destructor Documentation

- 7.7.1.1 template < typename PointerType > qpp::internal::IOManipPointer < PointerType >::IOManipPointer ( const PointerType \* p, const idx n, const std::string & separator, const std::string & start = " [ ", const std::string & end = " ] " ) [inline], [explicit]
- 7.7.1.2 template<typename PointerType> qpp::internal::IOManipPointer< PointerType>::IOManipPointer( const IOManipPointer<< PointerType> & ) [default]

#### 7.7.2 Member Function Documentation

7.7.2.1 template<typename PointerType> std::ostream& qpp::internal::IOManipPointer< PointerType >::display ( std::ostream & os ) const [inline], [override], [private], [virtual]

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs). Implements qpp::IDisplay.

- 7.7.2.2 template<typename PointerType> IOManipPointer& qpp::internal::IOManipPointer< PointerType
  >::operator=( const IOManipPointer< PointerType > & ) [default]
- 7.7.3 Member Data Documentation
- 7.7.3.1 template<typename PointerType> std::string qpp::internal::IOManipPointer< PointerType>::\_end [private]
- 7.7.3.2 template<typename PointerType>idx qpp::internal::IOManipPointer< PointerType>::\_n [private]
- 7.7.3.3 template<typename PointerType> const PointerType\* qpp::internal::IOManipPointer< PointerType >::\_p [private]
- 7.7.3.4 template<typename PointerType> std::string qpp::internal::IOManipPointer< PointerType>::\_separator [private]
- 7.7.3.5 template<typename PointerType> std::string qpp::internal::IOManipPointer< PointerType >::\_start [private]

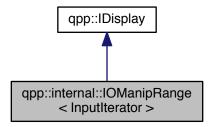
The documentation for this class was generated from the following file:

• internal/classes/iomanip.h

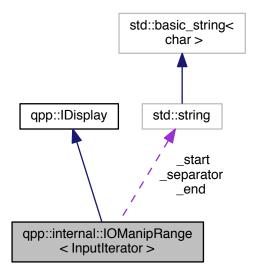
## 7.8 qpp::internal::IOManipRange < InputIterator > Class Template Reference

#include <internal/classes/iomanip.h>

Inheritance diagram for qpp::internal::IOManipRange< InputIterator >:



Collaboration diagram for qpp::internal::IOManipRange< InputIterator >:



#### **Public Member Functions**

• IOManipRange (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")

#### **Private Member Functions**

std::ostream & display (std::ostream &os) const override
 Must be overridden by all derived classes.

#### **Private Attributes**

- · InputIterator \_first
- · InputIterator \_last
- std::string \_separator
- · std::string \_start
- std::string \_end

## 7.8.1 Constructor & Destructor Documentation

#### 7.8.2 Member Function Documentation

7.8.2.1 template<typename InputIterator> std::ostream& qpp::internal::IOManipRange< InputIterator >::display ( std::ostream & os ) const [inline], [override], [private], [virtual]

Must be overridden by all derived classes.

The actual stream extraction processing is performed by the overriden member function in the derived class. This function is automatically invoked by friend inline std::ostream& operator<<(std::ostream& os, const IDisplay& rhs). Implements qpp::IDisplay.

#### 7.8.3 Member Data Documentation

- **7.8.3.1** template<typename InputIterator> std::string qpp::internal::IOManipRange< InputIterator >::\_end [private]
- **7.8.3.2** template<typename InputIterator > InputIterator qpp::internal::IOManipRange< InputIterator >::\_first [private]
- 7.8.3.3 template<typename InputIterator> InputIterator qpp::internal::IOManipRange< InputIterator>::\_last [private]
- **7.8.3.4 template**<typename InputIterator> std::string qpp::internal::IOManipRange< InputIterator >::\_separator [private]
- **7.8.3.5 template**<typename InputIterator> std::string qpp::internal::IOManipRange< InputIterator >::\_start [private]

The documentation for this class was generated from the following file:

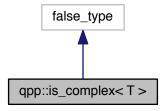
• internal/classes/iomanip.h

## 7.9 qpp::is\_complex< T > Struct Template Reference

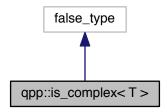
Checks whether the type is a complex type.

#include <traits.h>

Inheritance diagram for qpp::is\_complex< T >:



Collaboration diagram for qpp::is\_complex< T >:



## 7.9.1 Detailed Description

template<typename T>struct qpp::is\_complex< T>

Checks whether the type is a complex type.

Provides the member constant *value* which is equal to *true*, if the type is a complex type (i.e. *std::complex<T>*)

The documentation for this struct was generated from the following file:

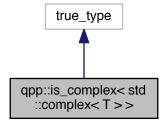
· traits.h

## 7.10 qpp::is\_complex< std::complex< T > > Struct Template Reference

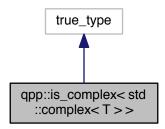
Checks whether the type is a complex number type, specialization for complex types.

#include <traits.h>

Inheritance diagram for qpp::is\_complex< std::complex< T > >:



Collaboration diagram for qpp::is\_complex< std::complex< T > >:



#### 7.10.1 Detailed Description

 $template < typename \ T > struct \ qpp::is\_complex < std::complex < T > >$ 

Checks whether the type is a complex number type, specialization for complex types.

The documentation for this struct was generated from the following file:

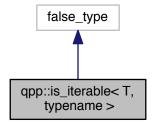
· traits.h

## 7.11 qpp::is\_iterable < T, typename > Struct Template Reference

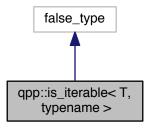
Checks whether *T* is compatible with an STL-like iterable container.

#include <traits.h>

Inheritance diagram for qpp::is\_iterable < T, typename >:



Collaboration diagram for qpp::is\_iterable < T, typename >:



## 7.11.1 Detailed Description

template<typename T, typename = void>struct qpp::is\_iterable< T, typename >

Checks whether T is compatible with an STL-like iterable container.

Provides the member constant *value* which is equal to *true*, if *T* is compatible with an iterable container, i.e. provides at least *begin()* and *end()* member functions. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

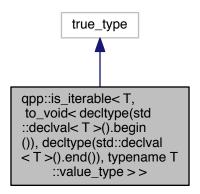
· traits.h

Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

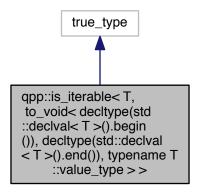
#include <traits.h>

 $Inheritance\ diagram\ for\ qpp:: is\_iterable < T,\ to\_void < \ decltype(std::declval < T > ().begin()),\ decltype(std::decltyp$ 

T >().end()), typename T::value\_type > >:



Collaboration diagram for qpp::is\_iterable< T, to\_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().begin()), typename T::value\_type > >:



#### 7.12.1 Detailed Description

 $template < typename \ T > struct \ qpp::is\_iterable < \ T, \ to\_void < \ decltype(std::declval < \ T > ().begin()), \ decltype(std::declval < \ T > ().end()), \ typename \ T::value\_type > >$ 

Checks whether *T* is compatible with an STL-like iterable container, specialization for STL-like iterable containers. The documentation for this struct was generated from the following file:

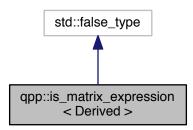
• traits.h

## 7.13 qpp::is\_matrix\_expression < Derived > Struct Template Reference

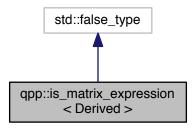
Checks whether the type is an Eigen matrix expression.

#include <traits.h>

Inheritance diagram for qpp::is\_matrix\_expression< Derived >:



Collaboration diagram for qpp::is\_matrix\_expression< Derived >:



#### 7.13.1 Detailed Description

 $template {<} typename \ Derived {>} struct \ qpp::is\_matrix\_expression {<} \ Derived {>}$ 

Checks whether the type is an Eigen matrix expression.

Provides the member constant *value* which is equal to *true*, if the type is an Eigen matrix expression of type *Eigen ∷MatrixBase Oerived >*. Otherwise, *value* is equal to *false*.

The documentation for this struct was generated from the following file:

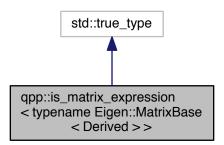
• traits.h

# 7.14 qpp::is\_matrix\_expression< typename Eigen::MatrixBase< Derived >> Struct Template Reference

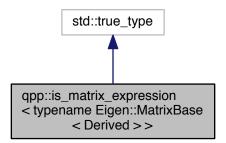
Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.

#include <traits.h>

Inheritance diagram for qpp::is\_matrix\_expression< typename Eigen::MatrixBase< Derived >>:



Collaboration diagram for qpp::is\_matrix\_expression< typename Eigen::MatrixBase< Derived >>:



#### 7.14.1 Detailed Description

 $template < typename\ Derived > struct\ qpp::is\_matrix\_expression < \ typename\ Eigen::MatrixBase < Derived > >$ 

 ${\it Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.}$ 

The documentation for this struct was generated from the following file:

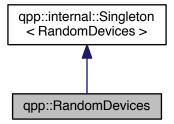
· traits.h

## 7.15 qpp::RandomDevices Class Reference

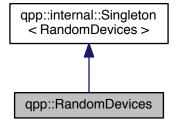
Singeleton class that manages the source of randomness in the library.

#include <classes/random\_devices.h>

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



#### **Public Attributes**

std::mt19937 \_rng

Mersenne twister random number generator.

## **Private Member Functions**

• RandomDevices ()

Initializes and seeds the random number generators.

∼RandomDevices ()=default

Default destructor.

#### **Private Attributes**

```
    std::random_device _rd
    used to seed std::mt19937 _rng
```

#### **Friends**

class internal::Singleton < RandomDevices >

#### **Additional Inherited Members**

## 7.15.1 Detailed Description

Singeleton class that manages the source of randomness in the library.

Consists of a wrapper around an std::mt19937 Mersenne twister random number generator engine and an std⇔ ::random\_device engine. The latter is used to seed the Mersenne twister.

#### Warning

This class DOES NOT seed the standard C number generator used by Eigen::Matrix::Random(), since it is not thread safe. Do not use Eigen::Matrix::Random() or functions that depend on the C style random number engine, but use <a href="mailto:qpp::rand()">qpp::rand()</a> instead!

#### 7.15.2 Constructor & Destructor Documentation

```
7.15.2.1 qpp::RandomDevices::RandomDevices() [inline], [private]
```

Initializes and seeds the random number generators.

```
7.15.2.2 qpp::RandomDevices::~RandomDevices() [private], [default]
```

Default destructor.

#### 7.15.3 Friends And Related Function Documentation

```
7.15.3.1 friend class internal::Singleton < RandomDevices > [friend]
```

#### 7.15.4 Member Data Documentation

```
7.15.4.1 std::random_device qpp::RandomDevices::_rd [private]
```

used to seed std::mt19937 rng

7.15.4.2 std::mt19937 qpp::RandomDevices::\_rng

Mersenne twister random number generator.

The documentation for this class was generated from the following file:

• classes/random\_devices.h

## 7.16 qpp::internal::Singleton < T > Class Template Reference

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

```
#include <internal/classes/singleton.h>
```

#### **Static Public Member Functions**

- static T & get\_instance () noexcept(std::is\_nothrow\_constructible < T >::value)
- static thread\_local T & get\_thread\_local\_instance () noexcept(std::is\_nothrow\_constructible < T >::value)

#### **Protected Member Functions**

- Singleton () noexcept=default
- Singleton (const Singleton &)=delete
- Singleton & operator= (const Singleton &)=delete
- virtual ∼Singleton ()=default

## 7.16.1 Detailed Description

template<typename T>class qpp::internal::Singleton< T>

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

To implement a singleton, derive your class from qpp::internal::Singleton, make qpp::internal::Singleton a friend of your class, then declare the constructor and destructor of your class as private. To get an instance, use the static member function qpp::internal::Singleton::get\_instance() (qpp::internal::Singleton::get\_thread\_local\_cinstance()), which returns a reference (thread\_local reference) to your newly created singleton (thread-safe in C++11).

## Example:

#### See also

Code of qpp::Codes, qpp::Gates, qpp::Init, qpp::RandomDevices, qpp::States or qpp.h for real world examples of usage.

#### 7.16.2 Constructor & Destructor Documentation

```
7.16.2.1 template<typename T> qpp::internal::Singleton< T>::Singleton( ) [protected], [default], [noexcept]
```

7.16.2.3 template virtual qpp::internal::Singleton< T>::
$$\sim$$
Singleton( ) [protected], [virtual], [default]

#### 7.16.3 Member Function Documentation

The documentation for this class was generated from the following file:

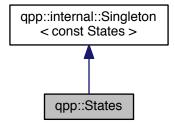
• internal/classes/singleton.h

## 7.17 qpp::States Class Reference

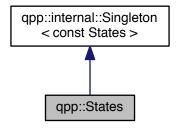
const Singleton class that implements most commonly used states

```
#include <classes/states.h>
```

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



#### **Public Attributes**

```
    ket x0 {ket::Zero(2)}
```

Pauli Sigma-X 0-eigenstate |+>

ket x1 {ket::Zero(2)}

Pauli Sigma-X 1-eigenstate |->

ket y0 {ket::Zero(2)}

Pauli Sigma-Y 0-eigenstate | y+>

ket y1 {ket::Zero(2)}

Pauli Sigma-Y 1-eigenstate | y->

ket z0 {ket::Zero(2)}

Pauli Sigma-Z 0-eigenstate | 0>

ket z1 {ket::Zero(2)}

Pauli Sigma-Z 1-eigenstate | 1>

cmat px0 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-X 0-eigenstate |+><+|.

• cmat px1 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-X 1-eigenstate |-><-|.

• cmat py0 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-Y 0-eigenstate  $|y+\rangle < y+|$ .

cmat py1 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-Y 1-eigenstate |y->< y-|.

• cmat pz0 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-Z 0-eigenstate |0><0|.

cmat pz1 {cmat::Zero(2, 2)}

Projector onto the Pauli Sigma-Z 1-eigenstate | 1><1|.

ket b00 {ket::Zero(4)}

Bell-00 state (following the convention in Nielsen and Chuang)

ket b01 {ket::Zero(4)}

Bell-01 state (following the convention in Nielsen and Chuang)

ket b10 {ket::Zero(4)}

Bell-10 state (following the convention in Nielsen and Chuang)

ket b11 {ket::Zero(4)}

Bell-11 state (following the convention in Nielsen and Chuang)

cmat pb00 {cmat::Zero(4, 4)}

Projector onto the Bell-00 state.

cmat pb01 {cmat::Zero(4, 4)}

Projector onto the Bell-01 state.

cmat pb10 {cmat::Zero(4, 4)}

Projector onto the Bell-10 state.

cmat pb11 {cmat::Zero(4, 4)}

Projector onto the Bell-11 state.

ket GHZ {ket::Zero(8)}

GHZ state.

ket W {ket::Zero(8)}

W state.

cmat pGHZ {cmat::Zero(8, 8)}

Projector onto the GHZ state.

cmat pW {cmat::Zero(8, 8)}

Projector onto the W state.

## **Private Member Functions**

- States ()
- ∼States ()=default

Default destructor.

#### **Friends**

class internal::Singleton < const States >

## **Additional Inherited Members**

#### 7.17.1 Detailed Description

const Singleton class that implements most commonly used states

#### 7.17.2 Constructor & Destructor Documentation

```
7.17.2.1 qpp::States::States( ) [inline],[private]
```

Initialize the states

```
7.17.2.2 qpp::States::~States() [private], [default]
```

Default destructor.

## 7.17.3 Friends And Related Function Documentation

**7.17.3.1** friend class internal::Singleton < const States > [friend]

#### 7.17.4 Member Data Documentation

7.17.4.1 ket qpp::States::b00 {ket::Zero(4)}

Bell-00 state (following the convention in Nielsen and Chuang)

```
7.17.4.2 ket qpp::States::b01 {ket::Zero(4)}
Bell-01 state (following the convention in Nielsen and Chuang)
7.17.4.3 ket qpp::States::b10 {ket::Zero(4)}
Bell-10 state (following the convention in Nielsen and Chuang)
7.17.4.4 ket qpp::States::b11 {ket::Zero(4)}
Bell-11 state (following the convention in Nielsen and Chuang)
7.17.4.5 ket qpp::States::GHZ {ket::Zero(8)}
GHZ state.
7.17.4.6 cmat qpp::States::pb00 {cmat::Zero(4, 4)}
Projector onto the Bell-00 state.
7.17.4.7 cmat qpp::States::pb01 {cmat::Zero(4, 4)}
Projector onto the Bell-01 state.
7.17.4.8 cmat qpp::States::pb10 {cmat::Zero(4, 4)}
Projector onto the Bell-10 state.
7.17.4.9 cmat qpp::States::pb11 {cmat::Zero(4, 4)}
Projector onto the Bell-11 state.
7.17.4.10 cmat qpp::States::pGHZ {cmat::Zero(8, 8)}
Projector onto the GHZ state.
7.17.4.11 cmat qpp::States::pW {cmat::Zero(8, 8)}
Projector onto the W state.
7.17.4.12 cmat qpp::States::px0 {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-X 0-eigenstate |+><+|.
7.17.4.13 cmat qpp::States::px1 {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-X 1-eigenstate |-><-|.
```

```
7.17.4.14 cmat qpp::States::py0 {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Y 0-eigenstate |y+><y+|.
7.17.4.15 cmat qpp::States::py1 {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Y 1-eigenstate |y-><y-|.
7.17.4.16 cmat qpp::States::pz0 {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Z 0-eigenstate |0><0|.
7.17.4.17 cmat qpp::States::pz1 {cmat::Zero(2, 2)}
Projector onto the Pauli Sigma-Z 1-eigenstate |1><1|.
7.17.4.18 ket qpp::States::W {ket::Zero(8)}
W state.
7.17.4.19 ket qpp::States::x0 {ket::Zero(2)}
Pauli Sigma-X 0-eigenstate |+>
7.17.4.20 ket qpp::States::x1 {ket::Zero(2)}
Pauli Sigma-X 1-eigenstate |->
7.17.4.21 ket qpp::States::y0 {ket::Zero(2)}
Pauli Sigma-Y 0-eigenstate |y+>
7.17.4.22 ket qpp::States::y1 {ket::Zero(2)}
Pauli Sigma-Y 1-eigenstate |y->
7.17.4.23 ket qpp::States::z0 {ket::Zero(2)}
Pauli Sigma-Z 0-eigenstate |0>
7.17.4.24 ket qpp::States::z1 {ket::Zero(2)}
Pauli Sigma-Z 1-eigenstate |1>
The documentation for this class was generated from the following file:
```

classes/states.h

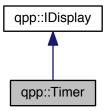
Generated on Sun May 17 2015 21:16:47 for Quantum++ by Doxygen

## 7.18 qpp::Timer Class Reference

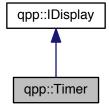
Chronometer.

#include <classes/timer.h>

Inheritance diagram for qpp::Timer:



Collaboration diagram for qpp::Timer:



#### **Public Member Functions**

• Timer () noexcept

Constructs an instance with the current time as the starting point.

• void tic () noexcept

Resets the chronometer.

• const Timer & toc () noexcept

Stops the chronometer.

· double seconds () const noexcept

Time passed in seconds.

• Timer (const Timer &)=default

Default copy constructor.

• Timer (Timer &&)=default

Default move constructor.

• Timer & operator= (const Timer &)=default

Default copy assignment operator.

• Timer & operator= (Timer &&)=default

Default move assignment operator.

virtual ∼Timer ()=default

Default virtual destructor.

#### **Protected Attributes**

```
• std::chrono::steady_clock::time_point _start
```

```
• std::chrono::steady_clock::time_point _end
```

#### **Private Member Functions**

 std::ostream & display (std::ostream &os) const override *qpp::IDisplay::display() override*

#### 7.18.1 Detailed Description

Chronometer.

Uses a std::chrono::steady\_clock. It is not affected by wall clock changes during runtime.

#### 7.18.2 Constructor & Destructor Documentation

```
7.18.2.1 qpp::Timer::Timer() [inline], [noexcept]
```

Constructs an instance with the current time as the starting point.

```
7.18.2.2 qpp::Timer::Timer(const Timer & ) [default]
```

Default copy constructor.

```
7.18.2.3 qpp::Timer::Timer(Timer && ) [default]
```

Default move constructor.

```
7.18.2.4 virtual qpp::Timer:: \sim Timer( ) [virtual], [default]
```

Default virtual destructor.

#### 7.18.3 Member Function Documentation

qpp::IDisplay::display() override

**Parameters** 

os	Output stream

#### Returns

Writes to the output stream the number of seconds that passed between the instantiation/reset and invocation of qpp::Timer::toc().

Implements qpp::IDisplay.

```
7.18.3.2 Timer& qpp::Timer::operator=( const Timer & ) [default]
```

Default copy assignment operator.

```
7.18.3.3 Timer& qpp::Timer::operator=( Timer && ) [default]
```

Default move assignment operator.

```
7.18.3.4 double qpp::Timer::seconds ( ) const [inline], [noexcept]
```

Time passed in seconds.

#### Returns

Number of seconds that passed between the instantiation/reset and invocation of qpp::Timer::toc()

```
7.18.3.5 void qpp::Timer::tic( ) [inline], [noexcept]
```

Resets the chronometer.

Resets the starting/ending point to the current time

```
7.18.3.6 const Timer& qpp::Timer::toc() [inline], [noexcept]
```

Stops the chronometer.

Set the current time as the ending point

Returns

Current instance

#### 7.18.4 Member Data Documentation

```
7.18.4.1 std::chrono::steady_clock::time_point qpp::Timer::_end [protected]
```

```
7.18.4.2 std::chrono::steady_clock::time_point qpp::Timer::_start [protected]
```

The documentation for this class was generated from the following file:

· classes/timer.h

## **Chapter 8**

## **File Documentation**

## 8.1 classes/codes.h File Reference

Quantum error correcting codes.

This graph shows which files directly or indirectly include this file:



## Classes

• class qpp::Codes

const Singleton class that defines quantum error correcting codes

## **Namespaces**

• qpp

Quantum++ main namespace.

## 8.1.1 Detailed Description

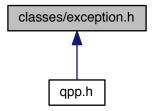
Quantum error correcting codes.

## 8.2 classes/exception.h File Reference

Exceptions.

124 File Documentation

This graph shows which files directly or indirectly include this file:



#### **Classes**

• class qpp::Exception

Generates custom exceptions, used when validating function parameters.

## **Namespaces**

• qpp

Quantum++ main namespace.

## 8.2.1 Detailed Description

Exceptions.

## 8.3 classes/gates.h File Reference

Quantum gates.

This graph shows which files directly or indirectly include this file:



#### Classes

class qpp::Gates

const Singleton class that implements most commonly used gates

#### **Namespaces**

qpp

Quantum++ main namespace.

## 8.3.1 Detailed Description

Quantum gates.

## 8.4 classes/idisplay.h File Reference

Display interface via the non-virtual interface (NVI)

This graph shows which files directly or indirectly include this file:



## Classes

· class qpp::IDisplay

Abstract class (interface) that mandates the definition of virtual std::ostream& display(std::ostream& os) const.

## **Namespaces**

• qpp

Quantum++ main namespace.

## 8.4.1 Detailed Description

Display interface via the non-virtual interface (NVI)

126 File Documentation

## 8.5 classes/init.h File Reference

Initialization.

This graph shows which files directly or indirectly include this file:



#### Classes

• class qpp::Init

const Singleton class that performs additional initializations/cleanups

## **Namespaces**

• qpp

Quantum++ main namespace.

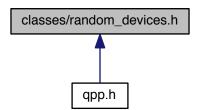
## 8.5.1 Detailed Description

Initialization.

## 8.6 classes/random\_devices.h File Reference

Random devices.

This graph shows which files directly or indirectly include this file:



## **Classes**

• class qpp::RandomDevices

Singeleton class that manages the source of randomness in the library.

## **Namespaces**

qpp

Quantum++ main namespace.

## 8.6.1 Detailed Description

Random devices.

## 8.7 classes/states.h File Reference

Quantum states.

This graph shows which files directly or indirectly include this file:



## Classes

• class qpp::States

const Singleton class that implements most commonly used states

## **Namespaces**

• qpp

Quantum++ main namespace.

## 8.7.1 Detailed Description

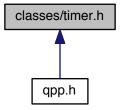
Quantum states.

128 File Documentation

## 8.8 classes/timer.h File Reference

Timing.

This graph shows which files directly or indirectly include this file:



#### Classes

• class qpp::Timer Chronometer.

## **Namespaces**

• qpp

Quantum++ main namespace.

## 8.8.1 Detailed Description

Timing.

## 8.9 constants.h File Reference

Constants.

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

qpp

Quantum++ main namespace.

#### **Functions**

• constexpr cplx qpp::operator""\_i (unsigned long long int x) noexcept

User-defined literal for complex  $i = \sqrt{-1}$  (integer overload)

• constexpr cplx qpp::operator""\_i (long double x) noexcept

User-defined literal for complex  $i = \sqrt{-1}$  (real overload)

• cplx qpp::omega (idx D)

D-th root of unity.

#### **Variables**

• constexpr double qpp::chop = 1e-10

Used in qpp::disp() for setting to zero numbers that have their absolute value smaller than qpp::chop.

• constexpr double qpp::eps = 1e-12

Used to decide whether a number or expression in double precision is zero or not.

constexpr idx qpp::maxn = 64

Maximum number of allowed qu(d)its (subsystems)

• constexpr double qpp::pi = 3.141592653589793238462643383279502884

 $\pi$ 

• constexpr double qpp::ee = 2.718281828459045235360287471352662497

Base of natural logarithm, e.

• constexpr double qpp::infty = std::numeric\_limits<double>::infinity()

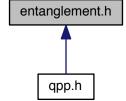
Used to denote infinity in double precision.

## 8.9.1 Detailed Description

Constants.

## 8.10 entanglement.h File Reference

Entanglement functions.



## **Namespaces**

• qpp

Quantum++ main namespace.

#### **Functions**

template<typename Derived >
 dyn\_col\_vect< double > qpp::schmidtcoeffs (const Eigen::MatrixBase< Derived > &A, const std::vector<
 idx > &dims)

Schmidt coefficients of the bi-partite pure state A.

template<typename Derived >
 cmat qpp::schmidtA (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

template<typename Derived >
 cmat qpp::schmidtB (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

Schmidt basis on Bob side.

Schmidt basis on Alice side.

template<typename Derived >
 std::vector< double > qpp::schmidtprobs (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

Schmidt probabilities of the bi-partite pure state A.

template < typename Derived >
 double qpp::entanglement (const Eigen::MatrixBase < Derived > &A, const std::vector < idx > &dims)
 Entanglement of the bi-partite pure state A.

template<typename Derived >
 double qpp::gconcurrence (const Eigen::MatrixBase< Derived > &A)

G-concurrence of the bi-partite pure state A.

template < typename Derived >
 double qpp::negativity (const Eigen::MatrixBase < Derived > &A, const std::vector < idx > &dims)
 Negativity of the bi-partite mixed state A.

template<typename Derived >
 double qpp::lognegativity (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &dims)

template<typename Derived >
 double qpp::concurrence (const Eigen::MatrixBase< Derived > &A)

Wootters concurrence of the bi-partite qubit mixed state A.

Logarithmic negativity of the bi-partite mixed state A.

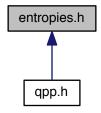
## 8.10.1 Detailed Description

Entanglement functions.

## 8.11 entropies.h File Reference

Entropy functions.

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

• qpp

Quantum++ main namespace.

#### **Functions**

template<typename Derived >
 double qpp::entropy (const Eigen::MatrixBase< Derived > &A)

von-Neumann entropy of the density matrix A

double qpp::entropy (const std::vector< double > &prob)

Shannon entropy of the probability distribution prob.

• template<typename Derived >

double <a href="mailto:qpp::renyi">qpp::renyi</a> (const Eigen::MatrixBase< Derived > &A, double alpha)

Renyi-  $\alpha$  entropy of the density matrix A, for  $\alpha \geq 0$ .

double qpp::renyi (const std::vector< double > &prob, double alpha)

Renyi-  $\alpha$  entropy of the probability distribution prob, for  $\alpha \geq 0$ .

• template<typename Derived >

double qpp::tsallis (const Eigen::MatrixBase< Derived > &A, double q)

Tsallis- q entropy of the density matrix A, for  $q \geq 0$ .

double qpp::tsallis (const std::vector< double > &prob, double q)

Tsallis- q entropy of the probability distribution prob, for  $q \geq 0$ .

• template<typename Derived >

double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< idx > &subsysA, const std::vector< idx > &subsysB, const std::vector< idx > &dims)

Quantum mutual information between 2 subsystems of a composite system.

 $\bullet \ \ {\it template}{<} {\it typename Derived}>$ 

double qpp::qmutualinfo (const Eigen::MatrixBase < Derived > &A, const std::vector < idx > &subsysA, const std::vector < idx > &subsysB, idx d=2)

Quantum mutual information between 2 subsystems of a composite system.

### 8.11.1 Detailed Description

Entropy functions.

# 8.12 experimental/test.h File Reference

Experimental/test functions/classes.

#### **Namespaces**

• qpp

Quantum++ main namespace.

• qpp::experimental

Experimental/test functions/classes, do not use or modify.

## 8.12.1 Detailed Description

Experimental/test functions/classes.

## 8.13 functions.h File Reference

Generic quantum computing functions.

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

• qpp

Quantum++ main namespace.

#### **Functions**

- template<typename Derived >
   dyn\_mat< typename Derived::Scalar > qpp::transpose (const Eigen::MatrixBase< Derived > &A)
   Transpose.
- template<typename Derived >
   dyn\_mat< typename Derived::Scalar > qpp::conjugate (const Eigen::MatrixBase< Derived > &A)
   Complex conjugate.
- template<typename Derived >
   dyn\_mat< typename Derived::Scalar > qpp::adjoint (const Eigen::MatrixBase< Derived > &A)
   Adjoint.

```
• template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::inverse (const Eigen::MatrixBase< Derived > &A)

    template<typename Derived >

  Derived::Scalar qpp::trace (const Eigen::MatrixBase < Derived > &A)
      Trace
• template<typename Derived >
  Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > &A)
      Determinant.
\bullet \ \ {\it template}{<} {\it typename Derived} >
  Derived::Scalar <a href="mailto:qpp::logdet">qpp::logdet</a> (const Eigen::MatrixBase</a> Derived > &A)
      Logarithm of the determinant.

    template<typename Derived >

  Derived::Scalar <a href="mailto:qpp::sum">qpp::sum</a> (const Eigen::MatrixBase</a> Derived > &A)
      Element-wise sum of A.
• template<typename Derived >
  Derived::Scalar <a href="mailto:open:prod">open:prod</a> (const Eigen::MatrixBase</a> Derived > &A)
      Element-wise product of A.

    template<typename Derived >

  double <a href="mailto:qpp::norm">qpp::norm</a> (const Eigen::MatrixBase< Derived > &A)
      Frobenius norm.

    template<typename Derived >

  std::pair< dyn_col_vect< cplx >, cmat > qpp::eig (const Eigen::MatrixBase< Derived > &A)
      Full eigen decomposition.
\bullet \ \ {\it template}{<} {\it typename Derived} >
  dyn_col_vect< cplx > qpp::evals (const Eigen::MatrixBase< Derived > &A)
      Eigenvalues.

    template<typename Derived >

  cmat qpp::evects (const Eigen::MatrixBase< Derived > &A)
      Eigenvectors.

    template<typename Derived >

  std::pair< dyn_col_vect< double >, cmat > qpp::heig (const Eigen::MatrixBase< Derived > &A)
      Full eigen decomposition of Hermitian expression.

    template<typename Derived >

  dyn_col_vect< double > qpp::hevals (const Eigen::MatrixBase< Derived > &A)
      Hermitian eigenvalues.

    template<typename Derived >

  cmat qpp::hevects (const Eigen::MatrixBase< Derived > &A)
      Hermitian eigenvectors.

    template<typename Derived >

  std::tuple< cmat, dyn col vect< double >, cmat > qpp::svd (const Eigen::MatrixBase< Derived > &A)
      Full singular value decomposition.
• template<typename Derived >
  dyn_col_vect< double > qpp::svals (const Eigen::MatrixBase< Derived > &A)
      Singular values.

    template<typename Derived >

  cmat qpp::svdU (const Eigen::MatrixBase< Derived > &A)
      Left singular vectors.

    template<typename Derived >

  cmat qpp::svdV (const Eigen::MatrixBase< Derived > &A)
      Right singular vectors.

    template<typename Derived >

  cmat qpp::funm (const Eigen::MatrixBase< Derived > &A, cplx(*f)(const cplx &))
```

```
Functional calculus f(A)
• template<typename Derived >
  cmat qpp::sqrtm (const Eigen::MatrixBase< Derived > &A)
     Matrix square root.

    template<typename Derived >

  cmat qpp::absm (const Eigen::MatrixBase< Derived > &A)
     Matrix absolut value.
template<typename Derived >
  cmat qpp::expm (const Eigen::MatrixBase< Derived > &A)
     Matrix exponential.

    template<typename Derived >

  cmat qpp::logm (const Eigen::MatrixBase< Derived > &A)
     Matrix logarithm.

    template<typename Derived >

  cmat qpp::sinm (const Eigen::MatrixBase< Derived > &A)
     Matrix sin.
• template<typename Derived >
  cmat qpp::cosm (const Eigen::MatrixBase< Derived > &A)
     Matrix cos.

    template<typename Derived >

  cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived > &A, const cplx z)
     Matrix power.

    template<typename Derived >

  dyn mat< typename Derived::Scalar > qpp::powm (const Eigen::MatrixBase< Derived > &A, idx n)
     Matrix power.
• template<typename Derived >
  double qpp::schatten (const Eigen::MatrixBase< Derived > &A, double p)
     Schatten matrix norm.
• template<typename OutputScalar , typename Derived >
  dyn_mat< OutputScalar > qpp::cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const
  typename Derived::Scalar &))
     Functor.
• template<typename T >
  dyn_mat< typename T::Scalar > qpp::kron (const T &head)
     Kronecker product.
• template<typename T , typename... Args>
  dyn_mat< typename T::Scalar > qpp::kron (const T &head, const Args &...tail)
     Kronecker product.

    template<typename Derived >

  dyn_mat< typename Derived::Scalar > qpp::kron (const std::vector< Derived > &As)
     Kronecker product.

    template<typename Derived >

  dyn_mat< typename Derived::Scalar > qpp::kron (const std::initializer_list< Derived > &As)
     Kronecker product.
• template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::kronpow (const Eigen::MatrixBase< Derived > &A, idx n)
     Kronecker power.
• template<typename T >
  dyn_mat< typename T::Scalar > qpp::dirsum (const T &head)
     Direct sum.
• template<typename T , typename... Args>
  dyn_mat< typename T::Scalar > qpp::dirsum (const T &head, const Args &...tail)
     Direct sum.
```

```
• template<typename Derived >
  dyn mat< typename Derived::Scalar > qpp::dirsum (const std::vector< Derived > &As)

    template < typename Derived >

  dyn_mat< typename Derived::Scalar > qpp::dirsum (const std::initializer_list< Derived > &As)

    template<typename Derived >

  dyn mat< typename Derived::Scalar > qpp::dirsumpow (const Eigen::MatrixBase< Derived > &A, idx n)
     Direct sum power.

    template<typename Derived >

  dyn_mat< typename Derived::Scalar > qpp::reshape (const Eigen::MatrixBase< Derived > &A, idx rows,
  idx cols)
     Reshape.

    template<typename Derived1 , typename Derived2 >

  dyn_mat< typename Derived1::Scalar > qpp::comm (const Eigen::MatrixBase< Derived1 > &A, const
  Eigen::MatrixBase< Derived2 > &B)
     Commutator.

    template<typename Derived1 , typename Derived2 >

  dyn_mat< typename Derived1::Scalar > qpp::anticomm (const Eigen::MatrixBase< Derived1 > &A, const
  Eigen::MatrixBase< Derived2 > &B)
     Anti-commutator.

    template<typename Derived >

  dyn mat< typename Derived::Scalar > qpp::prj (const Eigen::MatrixBase< Derived > &V)
     Projector.

    template<typename Derived >

  dyn_mat< typename Derived::Scalar > qpp::grams (const std::vector< Derived > &Vs)
     Gram-Schmidt orthogonalization.
• template<typename Derived >
  dyn_mat< typename Derived::Scalar > qpp::grams (const std::initializer_list< Derived > &Vs)
     Gram-Schmidt orthogonalization.
template<typename Derived >
  dyn mat< typename Derived::Scalar > qpp::grams (const Eigen::MatrixBase< Derived > &A)
     Gram-Schmidt orthogonalization.

    std::vector< idx > qpp::n2multiidx (idx n, const std::vector< idx > &dims)

     Non-negative integer index to multi-index.

    idx qpp::multiidx2n (const std::vector< idx > &midx, const std::vector< idx > &dims)

     Multi-index to non-negative integer index.

    ket qpp::mket (const std::vector< idx > &mask, const std::vector< idx > &dims)

     Multi-partite qudit ket.

    ket qpp::mket (const std::vector< idx > &mask, idx d=2)

     Multi-partite qudit ket.

    cmat qpp::mprj (const std::vector < idx > &mask, const std::vector < idx > &dims)

     Projector onto multi-partite qudit ket.

    cmat qpp::mprj (const std::vector< idx > &mask, idx d=2)

     Projector onto multi-partite qudit ket.
• template<typename InputIterator >
  std::vector< double > qpp::abssq (InputIterator first, InputIterator last)
     Computes the absolute values squared of an STL-like range of complex numbers.

    template<typename Container >

  std::vector< double > qpp::abssq (const Container &c, typename std::enable_if< is_iterable< Container
  >::value >::type *=nullptr)
```

Computes the absolute values squared of an STL-like container.

template < typename Derived >
 std::vector < double > qpp::abssq (const Eigen::MatrixBase < Derived > &A)

Computes the absolute values squared of an Eigen expression.

• template<typename InputIterator >

std::iterator traits < InputIterator >::value type qpp::sum (InputIterator first, InputIterator last)

Element-wise sum of an STL-like range.

• template<typename Container >

Container::value\_type <a href="mailto:qpp::sum">qpp::sum</a> (const Container &c)

Element-wise sum of the elements of an STL-like container.

template<typename InputIterator >

std::iterator\_traits< InputIterator >::value\_type qpp::prod (InputIterator first, InputIterator last)

Element-wise product of an STL-like range.

template<typename Container >

Container::value\_type <a href="mailto:qpp::prod">qpp::prod</a> (const Container &c)

Element-wise product of the elements of an STL-like container.

• template<typename Derived >

dyn\_col\_vect< typename Derived::Scalar > qpp::rho2pure (const Eigen::MatrixBase< Derived > &A)

Finds the pure state representation of a matrix proportional to a projector onto a pure state.

• template<typename T >

std::vector< T > qpp::complement (std::vector< T > subsys, idx N)

Constructs the complement of a subsystem vector.

• template<typename Derived >

std::vector< double > qpp::rho2bloch (const Eigen::MatrixBase< Derived > &A)

Computes the 3-dimensional real Bloch vector corresponding to the qubit density matrix A.

cmat qpp::bloch2rho (const std::vector< double > &r)

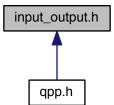
Computes the density matrix corresponding to the 3-dimensional real Bloch vector r.

#### 8.13.1 Detailed Description

Generic quantum computing functions.

## 8.14 input\_output.h File Reference

Input/output functions.



#### **Namespaces**

qpp

Quantum++ main namespace.

#### **Functions**

template<typename Derived >
 internal::IOManipEigen qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=qpp::chop)

Eigen expression ostream manipulator.

internal::IOManipEigen qpp::disp (cplx z, double chop=qpp::chop)

Complex number ostream manipulator.

template<typename InputIterator >
 internal::IOManipRange< InputIterator > qpp::disp (InputIterator first, InputIterator last, const std::string &separator, const std::string &start="[", const std::string &end="]")

Range ostream manipulator.

template<typename Container >
 internal::IOManipRange< typename Container::const\_iterator > qpp::disp (const Container &c, const std
 ::string &separator, const std::string &start="[", const std::string &end="]")

Standard container ostream manipulator. The container must support std::begin(), std::end() and forward iteration.

template<typename PointerType >
 internal::IOManipPointer< PointerType > qpp::disp (const PointerType \*p, idx n, const std::string &separator, const std::string &start="[", const std::string &end="]")

C-style pointer ostream manipulator.

template<typename Derived >
 void qpp::save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)

Saves Eigen expression to a binary file (internal format) in double precision.

 template < typename Derived > dyn\_mat < typename Derived::Scalar > qpp::load (const std::string &fname)

Loads Eigen matrix from a binary file (internal format) in double precision.

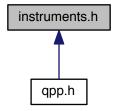
#### 8.14.1 Detailed Description

Input/output functions.

#### 8.15 instruments.h File Reference

Measurement functions.

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

• qpp

Quantum++ main namespace.

#### **Functions**

template<typename Derived >
 std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase
 Derived > &A, const std::vector< cmat > &Ks)

Measures the state A using the set of Kraus operators Ks.

template<typename Derived >

std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer list< cmat > &Ks)

Measures the state A using the set of Kraus operators Ks.

template<typename Derived >

std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &U)

Measures the state A in the orthonormal basis specified by the unitary matrix U.

 $\bullet \ \ {\it template}{<} {\it typename Derived}>$ 

std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

• template<typename Derived >

 $std::tuple < idx, \ std::vector < double >, \ std::vector < cmat > > qpp::measure \ (const \ Eigen::MatrixBase < Derived > &A, \ const \ std::initializer_list < cmat > &Ks, \ const \ std::vector < idx > &subsys, \ const \ std::vector < idx > &dims)\\$ 

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

template<typename Derived >

std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const idx d=2)

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

template<typename Derived >

std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const std::initializer list< cmat > &Ks, const std::vector< idx > &subsys, const idx d=2)

Measures the part subsys of the multi-partite state vector or density matrix A using the set of Kraus operators Ks.

template<typename Derived >

std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &U, const std::vector< idx > &subsys, const std::vector< idx > &dims)

Measures the part subsys of the multi-partite state vector or density matrix A in the orthonormal basis specified by the unitary matrix U.

• template<typename Derived >

std::tuple< idx, std::vector< double >, std::vector< cmat > > qpp::measure (const Eigen::MatrixBase< Derived > &A, const cmat &U, const std::vector< idx > &subsys, const idx d=2)

Measures the part subsys of the multi-partite state vector or density matrix A\ in the orthonormal basis specified by the unitary matrix U.

• template<typename Derived >

std::tuple < std::vector < idx >, double, cmat > qpp::measure\_seq (const Eigen::MatrixBase < Derived > &A, std::vector < idx > subsys, std::vector < idx > dims)

Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.

ullet template<typename Derived >

std::tuple < std::vector < idx >, double, cmat > qpp::measure\_seq (const Eigen::MatrixBase < Derived > &A, std::vector < idx > subsys, idx d=2)

Sequentially measures the part subsys of the multi-partite state vector or density matrix A in the computational basis.

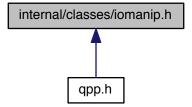
#### 8.15.1 Detailed Description

Measurement functions.

## 8.16 internal/classes/iomanip.h File Reference

Input/output manipulators.

This graph shows which files directly or indirectly include this file:



#### **Classes**

- class qpp::internal::IOManipRange< InputIterator >
- class qpp::internal::IOManipPointer< PointerType >
- class qpp::internal::IOManipEigen

#### **Namespaces**

qpp

Quantum++ main namespace.

· qpp::internal

Internal utility functions, do not use/modify.

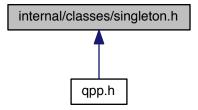
## 8.16.1 Detailed Description

Input/output manipulators.

# 8.17 internal/classes/singleton.h File Reference

Singleton pattern via CRTP.

This graph shows which files directly or indirectly include this file:



## Classes

class qpp::internal::Singleton< T >

Singleton policy class, used internally to implement the singleton pattern via CRTP (Curiously recurring template pattern)

## **Namespaces**

• qpp

Quantum++ main namespace.

· qpp::internal

Internal utility functions, do not use/modify.

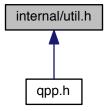
## 8.17.1 Detailed Description

Singleton pattern via CRTP.

## 8.18 internal/util.h File Reference

Internal utility functions.

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

• qpp

Quantum++ main namespace.

qpp::internal

Internal utility functions, do not use/modify.

#### **Functions**

- void qpp::internal:: n2multiidx (idx n, idx numdims, const idx \*dims, idx \*result) noexcept
- idx qpp::internal::\_multiidx2n (const idx \*midx, idx numdims, const idx \*dims) noexcept
- template<typename Derived >
   bool qpp::internal::\_check\_square\_mat (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_vector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_rvector (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_cvector (const Eigen::MatrixBase< Derived > &A)
- template<typename T >
   bool qpp::internal::\_check\_nonzero\_size (const T &x) noexcept
- template < typename T1, typename T2 >
   bool qpp::internal::\_check\_matching\_sizes (const T1 & lhs, const T2 & rhs) noexcept
- bool qpp::internal::\_check\_dims (const std::vector< idx > &dims)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_mat (const std::vector< idx > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_cvect (const std::vector< idx > &dims, const Eigen::MatrixBase
   Derived > &V)
- template<typename Derived >
   bool qpp::internal::\_check\_dims\_match\_rvect (const std::vector< idx > &dims, const Eigen::MatrixBase
   Derived > &V)
- bool qpp::internal:: check eq dims (const std::vector< idx > &dims, idx dim) noexcept
- bool qpp::internal::\_check\_subsys\_match\_dims (const std::vector< idx > &subsys, const std::vector< idx > &dims)
- template < typename Derived >
   bool qpp::internal::\_check\_qubit\_matrix (const Eigen::MatrixBase < Derived > &A) noexcept

```
    template<typename Derived >
        bool qpp::internal::_check_qubit_cvector (const Eigen::MatrixBase< Derived > &V) noexcept
```

template<typename Derived >
 bool qpp::internal::\_check\_qubit\_rvector (const Eigen::MatrixBase< Derived > &V) noexcept

template<typename Derived >
 bool qpp::internal::\_check\_qubit\_vector (const Eigen::MatrixBase< Derived > &V) noexcept

- bool qpp::internal::\_check\_perm (const std::vector< idx > &perm)
- template<typename Derived1, typename Derived2 >
   dyn\_mat< typename Derived1::Scalar > qpp::internal::\_kron2 (const Eigen::MatrixBase< Derived1 > &A,
   const Eigen::MatrixBase< Derived2 > &B)
- template<typename Derived1, typename Derived2 >
   dyn\_mat< typename Derived1::Scalar > qpp::internal::\_dirsum2 (const Eigen::MatrixBase< Derived1 > &A,
   const Eigen::MatrixBase< Derived2 > &B)
- $\begin{tabular}{ll} & \textbf{template}$< typename T>$ \\ & \textbf{void qpp::internal::variadic\_vector\_emplace (std::vector< T> \&)} \\ \end{tabular}$
- template<typename T, typename First, typename... Args>
   void qpp::internal::variadic\_vector\_emplace (std::vector< T > &v, First &&first, Args &&...args)

#### 8.18.1 Detailed Description

Internal utility functions.

#### 8.19 MATLAB/matlab.h File Reference

Input/output interfacing with MATLAB.

```
#include "mat.h"
#include "mex.h"
```

#### **Namespaces**

qpp

Quantum++ main namespace.

#### **Functions**

template<typename Derived >
 Derived qpp::loadMATLABmatrix (const std::string &mat\_file, const std::string &var\_name)
 Loads an Eigen dynamic matrix from a MATLAB .mat file, generic version.

template<>

dmat gpp::loadMATLABmatrix (const std::string &mat file, const std::string &var name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for double matrices (qpp::dmat)

template<>

cmat gpp::loadMATLABmatrix (const std::string &mat file, const std::string &var name)

Loads an Eigen dynamic matrix from a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

 $\bullet \ \ {\it template}{<} {\it typename Derived}>$ 

void qpp::saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat\_file, const std::string &var\_name, const std::string &mode)

Saves an Eigen dynamic matrix to a MATLAB .mat file, generic version.

template<>

void qpp::saveMATLABmatrix (const Eigen::MatrixBase< dmat > &A, const std::string &mat\_file, const std ::string &var\_name, const std::string &mode) Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for double matrices (qpp::dmat)

• template<>

Saves an Eigen dynamic matrix to a MATLAB .mat file, specialization for complex matrices (qpp::cmat)

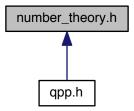
### 8.19.1 Detailed Description

Input/output interfacing with MATLAB.

## 8.20 number\_theory.h File Reference

Number theory functions.

This graph shows which files directly or indirectly include this file:



## **Namespaces**

• qpp

Quantum++ main namespace.

#### **Functions**

- std::vector< int > qpp::x2contfrac (double x, idx n, idx cut=1e5)
  - Simple continued fraction expansion.
- double qpp::contfrac2x (const std::vector< int > &cf, idx n)

Real representation of a simple continued fraction.

double qpp::contfrac2x (const std::vector< int > &cf)

Real representation of a simple continued fraction.

• ubigint qpp::gcd (ubigint m, ubigint n)

Greatest common divisor of two non-negative integers.

ubigint qpp::gcd (const std::vector< ubigint > &ns)

Greatest common divisor of a list of non-negative integers.

• ubigint qpp::lcm (ubigint m, ubigint n)

Least common multiple of two positive integers.

ubigint qpp::lcm (const std::vector< ubigint > &ns)

Least common multiple of a list of positive integers.

std::vector< idx > qpp::invperm (const std::vector< idx > &perm)
 Inverse permutation.

std::vector< idx > qpp::compperm (const std::vector< idx > &perm, const std::vector< idx > &sigma)
 Compose permutations.

std::vector< ubigint > qpp::factors (ubigint n)

Prime factor decomposition.

bool qpp::isprime (ubigint n)

Primality test.

• ubigint qpp::modpow (ubigint a, ubigint n, ubigint p)

Integer power modulo p.

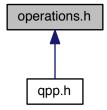
#### 8.20.1 Detailed Description

Number theory functions.

## 8.21 operations.h File Reference

Quantum operation functions.

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

• qpp

Quantum++ main namespace.

#### **Functions**

template<typename Derived1, typename Derived2 >
 dyn\_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state,
 const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys,
 const std::vector< idx > &dims)

Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.

template<typename Derived1 , typename Derived2 >
 dyn\_mat< typename Derived1::Scalar > qpp::applyCTRL (const Eigen::MatrixBase< Derived1 > &state,
 const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &ctrl, const std::vector< idx > &subsys,
 idx d=2)

Applies the controlled-gate A to the part subsys of the multi-partite state vector or density matrix state.

• template<typename Derived1 , typename Derived2 >

dyn\_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, const std::vector< idx > &dims)

Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.

• template<typename Derived1 , typename Derived2 >

dyn\_mat< typename Derived1::Scalar > qpp::apply (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< idx > &subsys, idx d=2)

Applies the gate A to the part subsys of the multi-partite state vector or density matrix state.

template<typename Derived >

cmat qpp::apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks)

Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.

template<typename Derived >

cmat qpp::apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< idx > &subsys, const std::vector< idx > &dims)

Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix rho.

template<typename Derived >

cmat qpp::apply (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std ::vector< idx > &subsys, idx d=2)

Applies the channel specified by the set of Kraus operators Ks to the part subsys of the multi-partite density matrix rho

cmat qpp::kraus2super (const std::vector < cmat > &Ks)

Superoperator matrix.

cmat qpp::kraus2choi (const std::vector< cmat > &Ks)

Choi matrix.

std::vector< cmat > qpp::choi2kraus (const cmat &A)

Orthogonal Kraus operators from Choi matrix.

cmat qpp::choi2super (const cmat &A)

Converts Choi matrix to superoperator matrix.

• cmat qpp::super2choi (const cmat &A)

Converts superoperator matrix to Choi matrix.

template<typename Derived >

dyn\_mat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std ← ::vector< idx > &dims)

Partial trace.

 $\bullet \ \ \text{template}{<} \text{typename Derived} >$ 

 $\label{lem:dyn_mat} $$ dyn_mat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std $$ ::vector < idx > &dims)$$ 

Partial trace.

template<typename Derived >

Partial trace.

 $\bullet \ \ {\it template}{<} {\it typename Derived} >$ 

dyn\_mat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std↔ ::vector< idx > &subsys, idx d=2)

Partial trace.

• template<typename Derived >

 $dyn_mat < typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase < Derived > &A, const std::vector < idx > &subsys, const std::vector < idx > &dims)$ 

Partial transpose.

<ul> <li>template<typename derived="">         dyn_mat&lt; typename Derived::Scalar &gt; qpp::ptranspose (const Eigen::MatrixBase&lt; Derived &gt; &amp;A, const std::vector&lt; idx &gt; &amp;subsys, idx d=2)</typename></li> </ul>
Partial transpose.
<ul> <li>template<typename derived="">         dyn_mat&lt; typename Derived::Scalar &gt; qpp::syspermute (const Eigen::MatrixBase&lt; Derived &gt; &amp;A, const std::vector&lt; idx &gt; &amp;perm, const std::vector&lt; idx &gt; &amp;dims)</typename></li> </ul>
Subsystem permutation.
<ul> <li>template<typename derived="">         dyn_mat&lt; typename Derived::Scalar &gt; qpp::syspermute (const Eigen::MatrixBase&lt; Derived &gt; &amp;A, const std::vector&lt; idx &gt; &amp;perm, idx d=2)</typename></li> </ul>
Subsystem permutation.
8.21.1 Detailed Description
Quantum operation functions.
8.22 qpp.h File Reference

Quantum++ main header file, includes all other necessary headers.

```
#include <algorithm>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <ctime>
#include <exception>
#include <fstream>
#include <functional>
#include <initializer_list>
#include <iomanip>
#include <iostream>
#include <iterator>
#include <limits>
#include <numeric>
#include <ostream>
#include <random>
#include <sstream>
#include <stdexcept>
#include <string>
#include <tuple>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "types.h"
#include "classes/exception.h"
#include "constants.h"
#include "traits.h"
#include "classes/idisplay.h"
#include "internal/util.h"
#include "internal/classes/iomanip.h"
#include "input_output.h"
#include "internal/classes/singleton.h"
#include "classes/init.h"
#include "functions.h"
#include "classes/codes.h"
#include "classes/gates.h"
#include "classes/states.h"
#include "classes/random_devices.h"
#include "statistics.h"
#include "operations.h"
#include "entropies.h"
#include "entanglement.h"
#include "random.h"
#include "classes/timer.h"
#include "instruments.h"
#include "number_theory.h"
```

#### **Namespaces**

dbb

Quantum++ main namespace.

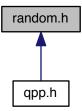
## 8.22.1 Detailed Description

Quantum++ main header file, includes all other necessary headers.

#### 8.23 random.h File Reference

Randomness-related functions.

This graph shows which files directly or indirectly include this file:



#### **Namespaces**

• qpp

Quantum++ main namespace.

## **Functions**

double <a href="mailto:qpp::rand">qpp::rand</a> (double a=0, double b=1)

Generates a random real number uniformly distributed in the interval [a, b)

- bigint qpp::rand (bigint a=std::numeric\_limits< bigint >::min(), bigint b=std::numeric\_limits< bigint >::max())

  Generates a random big integer uniformly distributed in the interval [a, b].
- ubigint qpp::rand (ubigint a=std::numeric\_limits< ubigint >::min(), ubigint b=std::numeric\_limits< ubigint >↔ ::max())

Generates a random non-negative big integer uniformly distributed in the interval [a, b].

idx qpp::randidx (idx a=std::numeric\_limits < idx >::min(), idx b=std::numeric\_limits < idx >::max())

Generates a random index (idx) uniformly distributed in the interval [a, b].

• template<typename Derived >

Derived qpp::rand (idx rows, idx cols, double a=0, double b=1)

Generates a random matrix with entries uniformly distributed in the interval [a, b)

template<>

dmat qpp::rand (idx rows, idx cols, double a, double b)

Generates a random real matrix with entries uniformly distributed in the interval [a, b), specialization for double matrices (qpp::dmat)

template<>

cmat qpp::rand (idx rows, idx cols, double a, double b)

Generates a random complex matrix with entries (both real and imaginary) uniformly distributed in the interval [a, b), specialization for complex matrices (qpp::cmat)

• template<typename Derived >

Derived qpp::randn (idx rows, idx cols, double mean=0, double sigma=1)

Generates a random matrix with entries normally distributed in N(mean, sigma)

template<>

dmat qpp::randn (idx rows, idx cols, double mean, double sigma)

Generates a random real matrix with entries normally distributed in N(mean, sigma), specialization for double matrices (qpp::dmat)

• template<>

cmat gpp::randn (idx rows, idx cols, double mean, double sigma)

Generates a random complex matrix with entries (both real and imaginary) normally distributed in N(mean, sigma), specialization for complex matrices (qpp::cmat)

• double <a href="mailto:qpp::randn">qpp::randn</a> (double mean=0, double sigma=1)

Generates a random real number (double) normally distributed in N(mean, sigma)

cmat qpp::randU (idx D)

Generates a random unitary matrix.

• cmat qpp::randV (idx Din, idx Dout)

Generates a random isometry matrix.

std::vector< cmat > qpp::randkraus (idx N, idx D)

Generates a set of random Kraus operators.

cmat qpp::randH (idx D)

Generates a random Hermitian matrix.

ket qpp::randket (idx D)

Generates a random normalized ket (pure state vector)

cmat qpp::randrho (idx D)

Generates a random density matrix.

std::vector< idx > qpp::randperm (idx n)

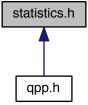
Generates a random uniformly distributed permutation.

#### 8.23.1 Detailed Description

Randomness-related functions.

#### 8.24 statistics.h File Reference

Statistics functions.



#### **Namespaces**

• qpp

Quantum++ main namespace.

#### **Functions**

```
- std::vector< double > qpp::uniform (idx N)
```

Uniform probability distribution vector.

std::vector< double > qpp::marginalX (const dmat &probXY)

Marginal distribution.

std::vector< double > qpp::marginalY (const dmat &probXY)

Marginal distribution.

template<typename Container >

double qpp::avg (const std::vector< double > &prob, const Container &X)

Average

• template<typename Container >

double qpp::cov (const dmat &probXY, const Container &X, const Container &Y)

Covariance.

• template<typename Container >

double qpp::var (const std::vector< double > &prob, const Container &X)

Variance.

• template<typename Container >

double qpp::sigma (const std::vector< double > &prob, const Container &X)

Standard deviation.

• template<typename Container >

double <a href="mailto:qpp::cor">qpp::cor</a> (const dmat &probXY, const Container &X, const Container &Y)

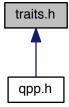
Correlation.

#### 8.24.1 Detailed Description

Statistics functions.

## 8.25 traits.h File Reference

Type traits.



#### Classes

struct qpp::is\_iterable < T, typename >

Checks whether T is compatible with an STL-like iterable container.

struct qpp::is\_iterable< T, to\_void< decltype(std::declval< T >().begin()), decltype(std::declval< T >().← end()), typename T::value\_type >>

Checks whether T is compatible with an STL-like iterable container, specialization for STL-like iterable containers.

struct qpp::is\_matrix\_expression< Derived >

Checks whether the type is an Eigen matrix expression.

struct qpp::is\_matrix\_expression< typename Eigen::MatrixBase< Derived >>

Checks whether the type is an Eigen matrix expression, specialization for Eigen matrix expressions.

struct qpp::is\_complex< T >

Checks whether the type is a complex type.

struct qpp::is\_complex< std::complex< T >>

Checks whether the type is a complex number type, specialization for complex types.

#### **Namespaces**

• qpp

Quantum++ main namespace.

## **Typedefs**

template < class... > using qpp::to\_void = void

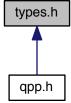
Alias template that implements the proposal for void\_t.

#### 8.25.1 Detailed Description

Type traits.

## 8.26 types.h File Reference

Type aliases.



#### **Namespaces**

• qpp

Quantum++ main namespace.

#### **Typedefs**

```
• using qpp::idx = std::size_t
```

Non-negative integer index.

• using qpp::bigint = long long int

Big integer.

• using qpp::ubigint = unsigned long long int

Non-negative big integer.

• using qpp::cplx = std::complex< double >

Complex number in double precision.

using qpp::ket = Eigen::VectorXcd

Complex (double precision) dynamic Eigen column vector.

• using qpp::bra = Eigen::RowVectorXcd

Complex (double precision) dynamic Eigen row vector.

• using qpp::cmat = Eigen::MatrixXcd

Complex (double precision) dynamic Eigen matrix.

• using qpp::dmat = Eigen::MatrixXd

Real (double precision) dynamic Eigen matrix.

• template<typename Scalar >

```
using qpp::dyn_mat = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >
```

Dynamic Eigen matrix over the field specified by Scalar.

• template<typename Scalar >

```
using qpp::dyn_col_vect = Eigen::Matrix< Scalar, Eigen::Dynamic, 1 >
```

Dynamic Eigen column vector over the field specified by Scalar.

• template<typename Scalar >

```
using <a href="mailto:qpp::dyn_row_vect">qpp::dyn_row_vect</a> = Eigen::Matrix< Scalar, 1, Eigen::Dynamic >
```

Dynamic Eigen row vector over the field specified by Scalar.

## 8.26.1 Detailed Description

Type aliases.

# Index

_A	qpp::internal::IOManipRange, 104
qpp::internal::IOManipEigen, 100	_kron2
_check_cvector	qpp::internal, 82
qpp::internal, 81	_last
_check_dims	qpp::internal::IOManipRange, 104
qpp::internal, 81	_msg
_check_dims_match_cvect	qpp::Exception, 89
qpp::internal, 81	_multiidx2n
_check_dims_match_mat	qpp::internal, 82
qpp::internal, 81	_n
_check_dims_match_rvect	qpp::internal::IOManipPointer, 102
qpp::internal, 81	_n2multiidx
_check_eq_dims	qpp::internal, 82
qpp::internal, 81	_p
_check_matching_sizes	qpp::internal::IOManipPointer, 102
qpp::internal, 81	_rd
_check_nonzero_size	qpp::RandomDevices, 112
qpp::internal, 81	_rng
_check_perm	qpp::RandomDevices, 112
qpp::internal, 81	_separator
_check_qubit_cvector	qpp::internal::IOManipPointer, 102
qpp::internal, 81	qpp::internal::IOManipRange, 104
_check_qubit_matrix	_start
qpp::internal, 81	qpp::Timer, 121
_check_qubit_rvector	qpp::internal::IOManipPointer, 102
qpp::internal, 81	qpp::internal::IOManipRange, 104
_check_qubit_vector	_type
qpp::internal, 82	qpp::Exception, 89
_check_rvector	_where
qpp::internal, 82	qpp::Exception, 89
_check_square_mat	~Codes
qpp::internal, 82	qpp::Codes, 84
_check_subsys_match_dims	~Gates
qpp::internal, 82	qpp::Gates, 91
_check_vector	~IDisplay
qpp::internal, 82	qpp::IDisplay, 96 ∼Init
_chop	
qpp::internal::IOManipEigen, 100	qpp::Init, 98 ∼RandomDevices
_construct_exception_msg	qpp::RandomDevices, 112
qpp::Exception, 88	~Singleton
custom	qpp::internal::Singleton, 114
qpp::Exception, 89	~States
_dirsum2	qpp::States, 116
qpp::internal, 82	~Timer
_end	qpp::Timer, 120
qpp::Timer, 121	App. Timor, TEO
qpp::internal::IOManipPointer, 102	absm
qpp::internal::IOManipRange, 104	qpp, 26
first	abssq

qpp, 26	complement
adjoint	qpp, 32
qpp, 26	compperm
anticomm	qpp, 32
qpp, 28	concurrence
apply	qpp, 34
qpp, 28, 29	conjugate
applyCTRL	qpp, 34
qpp, 30	constants.h, 128
avg	contfrac2x
qpp, 31	qpp, 34
-11-17 -	cor
b00	qpp, 35
qpp::States, 116	cosm
b01	qpp, 35
qpp::States, 116	COV
b10	qpp, 35
qpp::States, 117	cplx
b11	•
qpp::States, 117	qpp, 25 cwise
bigint	
qpp, 24	qpp, 36
bloch2rho	DIMS INVALID
qpp, 31	qpp::Exception, 87
bra	DIMS MISMATCH CVECTOR
	qpp::Exception, 87
qpp, 24	DIMS MISMATCH MATRIX
CNOT	<del>-</del>
qpp::Gates, 94	qpp::Exception, 87
CNOTba	DIMS_MISMATCH_RVECTOR
qpp::Gates, 94	qpp::Exception, 87
CTRL	DIMS_MISMATCH_VECTOR
	qpp::Exception, 87
qpp::Gates, 91	DIMS_NOT_EQUAL
CUSTOM_EXCEPTION	qpp::Exception, 87
qpp::Exception, 88	det
CZ	qpp, 36
qpp::Gates, 94	dirsum
choi2kraus	qpp, 36, 37
qpp, 31	dirsumpow
choi2super	qpp, <mark>37</mark>
qpp, 32	disp
chop	qpp, 38, 39
qpp, 79	display
classes/codes.h, 123	qpp::IDisplay, 97
classes/exception.h, 123	qpp::Timer, 120
classes/gates.h, 124	qpp::internal::IOManipEigen, 100
classes/idisplay.h, 125	qpp::internal::IOManipPointer, 102
classes/init.h, 126	qpp::internal::IOManipRange, 103
classes/random_devices.h, 126	dmat
classes/states.h, 127	qpp, 25
classes/timer.h, 128	dyn_col_vect
cmat	qpp, 25
qpp, 24	dyn_mat
Codes	qpp, 25
qpp::Codes, 84	dyn_row_vect
codeword	qpp, 25
qpp::Codes, 85	4KK,
comm	ee
qpp, 32	qpp, 79
	-II- I- / -

	ID: 1 00
eig	qpp::IDisplay, 96
qpp, 39	IOManipEigen
entanglement	qpp::internal::IOManipEigen, 100
qpp, 40	IOManipPointer
entanglement.h, 129	qpp::internal::IOManipPointer, 101
entropies.h, 130	IOManipRange
entropy	qpp::internal::IOManipRange, 103
qpp, 40	Id
eps	qpp::Gates, 93
·	Id2
qpp, 79	
evals	qpp::Gates, 94
qpp, 40	idx
evects	qpp, 25
qpp, 41	infty
Exception	qpp, 79
qpp::Exception, 88	Init
expandout	qpp::Init, 98
qpp::Gates, 92	input_output.h, 136
experimental/test.h, 132	instruments.h, 137
expm	internal/classes/iomanip.h, 139
·	internal/classes/singleton.h, 140
qpp, 41	internal/util.h, 140
FIVE QUBIT	
<del>_</del>	internal::Singleton< const Codes >
qpp::Codes, 84	qpp::Codes, 85
FRED	internal::Singleton< const Gates >
qpp::Gates, 94	qpp::Gates, 94
factors	internal::Singleton $<$ const Init $>$
qpp, 41	qpp::Init, 98
Fd	internal::Singleton< const States >
qpp::Gates, 92	qpp::States, 116
functions.h, 132	internal::Singleton< RandomDevices >
funm	qpp::RandomDevices, 112
	inverse
qpp, 42	
GHZ	qpp, 45
	invperm
qpp::States, 117	qpp, 45
Gates	isprime
qpp::Gates, 91	qpp, 45
gcd	
qpp, 42	ket
gconcurrence	qpp, 25
qpp, 42	kraus2choi
get_instance	qpp, 45
qpp::internal::Singleton, 114	kraus2super
get_thread_local_instance	qpp, 46
qpp::internal::Singleton, 114	kron
grams	qpp, 46, 47
qpp, 43	kronpow
	qpp, 47
Н	
qpp::Gates, 94	lcm
heig	qpp, 48
qpp, 44	load
hevals	qpp, 48
qpp, 44	loadMATLABmatrix
hevects	qpp, 49
qpp, 44	logdet
אווי י י	qpp, 51
IDisplay	logm
i Diopia,	.~g

qpp, 51	qpp, 59
lognegativity	norm
qpp, 51	qpp, 59
MATIAR/ HILL 440	number_theory.h, 143
MATLAB/matlab.h, 142	0.17.05.541105
MATRIX_MISMATCH_SUBSYS	OUT_OF_RANGE
qpp::Exception, 87	qpp::Exception, 88
MATRIX_NOT_CVECTOR	omega
qpp::Exception, 87	qpp, <del>5</del> 9
MATRIX_NOT_RVECTOR	operations.h, 144
qpp::Exception, 87	operator<<
MATRIX_NOT_SQUARE	qpp::IDisplay, 97
qpp::Exception, 87	operator=
MATRIX_NOT_SQUARE_OR_CVECTOR	qpp::IDisplay, 97
qpp::Exception, 87	qpp::Timer, 121
MATRIX_NOT_SQUARE_OR_RVECTOR	qpp::internal::IOManipPointer, 102
qpp::Exception, 87	qpp::internal::Singleton, 114
MATRIX_NOT_SQUARE_OR_VECTOR	operator"" i
	• –
qpp::Exception, 87	qpp, 59
MATRIX_NOT_VECTOR	PERM INVALID
qpp::Exception, 87	<del>_</del>
marginalX	qpp::Exception, 87
qpp, 51	PERM_MISMATCH_DIMS
marginalY	qpp::Exception, 88
qpp, <mark>52</mark>	pGHZ
maxn	qpp::States, 117
qpp, 79	pW
measure	qpp::States, 117
qpp, 52–55	pb00
measure_seq	qpp::States, 117
qpp, 56	pb01
mket	qpp::States, 117
gpp, 56, 57	pb10
modpow	qpp::States, 117
qpp, 57	pb11
mprj	qpp::States, 117
	pi
qpp, 57, 58 multiidx2n	qpp, 79
	powm
qpp, 58	•
n2multiidx	qpp, 60
	prj
qpp, 58	qpp, 60
NINE_QUBIT_SHOR	prod
qpp::Codes, 84	qpp, 60, 61
NO_CODEWORD	ptrace
qpp::Exception, 88	qpp, 61
NOT_BIPARTITE	ptrace1
qpp::Exception, 88	qpp, 62
NOT_QUBIT_CVECTOR	ptrace2
qpp::Exception, 88	qpp, 62
NOT_QUBIT_MATRIX	ptranspose
qpp::Exception, 88	qpp, 62, 63
NOT QUBIT RVECTOR	px0
qpp::Exception, 88	qpp::States, 117
NOT QUBIT SUBSYS	px1
qpp::Exception, 88	qpp::States, 117
NOT QUBIT VECTOR	py0
qpp::Exception, 88	qpp::States, 117
negativity	py1

qpp::States, 118	infty, 79
pz0	inverse, 45
qpp::States, 118	invperm, 45
pz1	isprime, 45
qpp::States, 118	ket, 25
	kraus2choi, 45
qmutualinfo	kraus2super, 46
qpp, 63	kron, 46, 47
qpp, 13	kronpow, 47
absm, 26	lcm, 48
abssq, 26	load, 48
adjoint, 26	loadMATLABmatrix, 49
anticomm, 28	logdet, 51
apply, 28, 29	logm, 51
applyCTRL, 30	lognegativity, 51
avg, 31	marginalX, 51
bigint, 24	marginalY, 52
bloch2rho, 31	maxn, 79
bra, 24	measure, 52–55
choi2kraus, 31	measure seg, 56
choi2super, 32	mket, 56, 57
chop, 79	modpow, 57
cmat, 24	mprj, 57, 58
comm, 32	multiidx2n, 58
complement, 32	n2multiidx, 58
compperm, 32	negativity, 59
concurrence, 34	
conjugate, 34	norm, 59
contfrac2x, 34	omega, 59
cor, 35	operator""_i, 59
cosm, 35	pi, 79
cov, 35	powm, 60
cplx, 25	prj, 60
cwise, 36	prod, 60, 61
det, 36	ptrace, 61
dirsum, 36, 37	ptrace1, 62
dirsumpow, 37	ptrace2, 62
disp, 38, 39	ptranspose, 62, 63
dmat, 25	qmutualinfo, 63
dyn_col_vect, 25	rand, 64, 65
dyn_mat, 25	randH, 65
dyn_row_vect, 25	randU, 69
ee, 79	randV, 69
eig, 39	randidx, 65
entanglement, 40	randket, 67
entropy, 40	randkraus, 67
eps, 79	randn, 67, 68
evals, 40	randperm, 68
evects, 41	randrho, 69
expm, 41	renyi, 69, 70
factors, 41	reshape, 70
funm, 42	rho2bloch, 70
gcd, 42	rho2pure, 71
gconcurrence, 42	save, 71
grams, 43	saveMATLABmatrix, 71, 72
heig, 44	schatten, 72
hevals, 44	schmidtA, 72
hevects, 44	schmidtB, 73
idx, 25	schmidtcoeffs, 73

schmidtprobs, 73	NOT_QUBIT_VECTOR, 88
sigma, 74	OUT_OF_RANGE, 88
sinm, 74	PERM_INVALID, 87
spectralpowm, 74	PERM_MISMATCH_DIMS, 88
sqrtm, 74	SIZE MISMATCH, 88
•	SUBSYS_MISMATCH_DIMS, 87
sum, 75	
super2choi, 75	TYPE_MISMATCH, 88
svals, 76	Type, 87
svd, 76	UNDEFINED_TYPE, 88
svdU, 76	UNKNOWN_EXCEPTION, 87
svdV, 76	what, 88
syspermute, 77	ZERO_SIZE, 87
to_void, 25	qpp::Gates, 89
trace, 77	$\sim$ Gates, 91
transpose, 77	CNOT, 94
tsallis, 78	CNOTba, 94
ubigint, 25	CTRL, 91
-	CZ, 94
uniform, 78	•
var, 78	expandout, 92
x2contfrac, 79	FRED, 94
qpp.h, 146	Fd, 92
qpp::Codes, 83	Gates, 91
$\sim$ Codes, 84	H, 94
Codes, 84	ld, 93
codeword, 85	ld2, 94
FIVE_QUBIT, 84	internal::Singleton< const Gates >, 94
internal::Singleton< const Codes >, 85	Rn, 93
NINE_QUBIT_SHOR, 84	S, 94
SEVEN_QUBIT_STEANE, 84	SWAP, 94
Type, 84	T, 94
qpp::Exception, 85	TOF, 94
_construct_exception_msg, 88	X, 95
_custom, 89	Xd, 93
_msg, 89	Y, 95
_type, 89	Z, 95
_where, 89	Zd, 93
CUSTOM EXCEPTION, 88	qpp::IDisplay, 95
DIMS_INVALID, 87	∼IDisplay, 96
DIMS MISMATCH CVECTOR, 87	display, 97
DIMS_MISMATCH_MATRIX, 87	IDisplay, 96
DIMS MISMATCH RVECTOR, 87	operator<<, 97
DIMS_MISMATCH_VECTOR, 87	operator=, 97
DIMS_NOT_EQUAL, 87	qpp::Init, 97
Exception, 88	~Init, 98
MATRIX_MISMATCH_SUBSYS, 87	Init, 98
MATRIX_NOT_CVECTOR, 87	internal::Singleton< const Init >, 98
MATRIX_NOT_RVECTOR, 87	qpp::RandomDevices, 111
MATRIX_NOT_SQUARE, 87	_rd, 112
MATRIX_NOT_SQUARE_OR_CVECTOR, 87	_rng, 112
MATRIX_NOT_SQUARE_OR_RVECTOR, 87	$\sim$ RandomDevices, 112
MATRIX NOT SQUARE OR VECTOR, 87	internal::Singleton < RandomDevices >, 112
MATRIX_NOT_VECTOR, 87	RandomDevices, 112
NO_CODEWORD, 88	qpp::States, 114
NOT BIPARTITE, 88	~States, 116
<del>-</del>	
NOT_QUBIT_CVECTOR, 88	b00, 116
NOT_QUBIT_MATRIX, 88	b01, 116
NOT_QUBIT_RVECTOR, 88	b10, 117
NOT_QUBIT_SUBSYS, 88	b11, 117

GHZ, 117	_chop, 100
internal::Singleton< const States >, 116	display, 100
pGHZ, 117	IOManipEigen, 100
pW, 117	qpp::internal::IOManipPointer
pb00, 117	_end, 102
pb01, 117	_n, 102
pb10, 117	_p, 102
pb11, 117	_separator, 102
px0, 117	_start, 102
px1, 117	display, 102
py0, 117	IOManipPointer, 101
py1, 118	operator=, 102
pz0, 118	qpp::internal::IOManipPointer< PointerType >, 100
pz1, 118	qpp::internal::IOManipRange
States, 116	_end, 104
W, 118	_first, 104
x0, 118	_last, 104
x1, 118	_separator, 104
y0, 118	_start, 104
y1, 118	display, 103
z0, 118	IOManipRange, 103
z1, 118	qpp::internal::IOManipRange< InputIterator >, 102
qpp::Timer, 119	qpp::internal::Singleton
_end, 121	∼Singleton, 114
_start, 121	get_instance, 114
$\sim$ Timer, 120	get_thread_local_instance, 114
display, 120	operator=, 114
operator=, 121	Singleton, 114
seconds, 121	qpp::internal::Singleton< T >, 113
tic, 121	qpp::is_complex< std::complex< T >>, 105
Timer, 120	qpp::is_complex < T >, 104
toc, 121	qpp::is_iterable< T, to_void< decltype(std::declval< T
qpp::experimental, 80	>().begin()), decltype(std::declval< T >().←
qpp::internal, 80	end()), typename T::value_type >>, 107
_check_cvector, 81	qpp::is_iterable< T, typename >, 106
_check_dims, 81	<pre>qpp::is_matrix_expression&lt; Derived &gt;, 109 qpp::is_matrix_expression&lt; typename Eigen::Matrix←</pre>
_check_dims_match_cvect, 81	Base< Derived > >, 110
_check_dims_match_mat, 81	base Derived > >, 110
_check_dims_match_rvect, 81	rand
_check_eq_dims, 81	qpp, 64, 65
_check_matching_sizes, 81	randH
_check_nonzero_size, 81	qpp, 65
_check_perm, 81	randU
_check_qubit_cvector, 81	qpp, 69
_check_qubit_matrix, 81	randV
_check_qubit_rvector, 81	qpp, 69
_check_qubit_vector, 82	randidx
_check_rvector, 82	qpp, 65
_check_square_mat, 82	randket
_check_subsys_match_dims, 82	qpp, 67
_check_vector, 82	randkraus
_dirsum2, 82	qpp, 67
_kron2, 82	randn
_multiidx2n, 82	qpp, 67, 68
_n2multiidx, 82	random.h, 148
variadic_vector_emplace, 82	RandomDevices
qpp::internal::IOManipEigen, 99	qpp::RandomDevices, 112
_A, 100	randperm

qpp, 68	
9pp, •••	svd
randrho	qpp, <mark>76</mark>
qpp, 69	svdU
renyi	qpp, 76
qpp, 69, 70	svdV
reshape	qpp, <mark>76</mark>
qpp, 70	syspermute
rho2bloch	qpp, 77
	qpp, 77
qpp, 70	_
rho2pure	Т
qpp, 71	qpp::Gates, 94
Rn	TOF
qpp::Gates, 93	qpp::Gates, 94
qppautoo, oo	TYPE MISMATCH
S	<del>_</del>
	qpp::Exception, 88
qpp::Gates, 94	tic
SEVEN_QUBIT_STEANE	qpp::Timer, 121
qpp::Codes, 84	Timer
SIZE MISMATCH	-
qpp::Exception, 88	qpp::Timer, 120
	to_void
SUBSYS_MISMATCH_DIMS	qpp, 25
qpp::Exception, 87	toc
SWAP	qpp::Timer, 121
qpp::Gates, 94	
	trace
save	qpp, <b>77</b>
qpp, 71	traits.h, 150
saveMATLABmatrix	transpose
qpp, 71, 72	
schatten	qpp, 77
	tsallis
qpp, 72	qpp, <mark>78</mark>
schmidtA	Туре
qpp, 72	qpp::Codes, 84
schmidtB	
· · · · · · · · · · · · · · · · · · ·	
ann 73	qpp::Exception, 87
qpp, 73	types.h, 151
schmidtcoeffs	
	types.h, 151
schmidtcoeffs qpp, 73	types.h, 151 UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs qpp, 73	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs qpp, 73 seconds	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs qpp, 73	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs qpp, 73 seconds	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs qpp, 73 seconds qpp::Timer, 121 sigma	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs qpp, 73 seconds qpp::Timer, 121 sigma qpp, 74	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs qpp, 73 seconds qpp::Timer, 121 sigma qpp, 74 Singleton	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs qpp, 73 seconds qpp::Timer, 121 sigma qpp, 74 Singleton qpp::internal::Singleton, 114	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs qpp, 73 seconds qpp::Timer, 121 sigma qpp, 74 Singleton	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs qpp, 73 seconds qpp::Timer, 121 sigma qpp, 74 Singleton qpp::internal::Singleton, 114	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs qpp, 73 schmidtprobs qpp, 73 seconds qpp::Timer, 121 sigma qpp, 74 Singleton qpp::internal::Singleton, 114 sinm qpp, 74	types.h, 151  UNDEFINED_TYPE
schmidtcoeffs	types.h, 151  UNDEFINED_TYPE

```
qpp::States, 118
x2contfrac
    qpp, 79
Xd
    qpp::Gates, 93
Υ
    qpp::Gates, 95
y0
    qpp::States, 118
у1
    qpp::States, 118
Ζ
    qpp::Gates, 95
z0
    qpp::States, 118
z1
    qpp::States, 118
ZERO_SIZE
    qpp::Exception, 87
Zd
    qpp::Gates, 93
```