

quantum++

0.1

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Chapter 1

quantum++ - A C++11 quantum computing library

Version

0.1

Author

Vlad Gheorghiu

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A simple example:

```
#include "qpp.h"

// #include "matlab.h" // support for MATLAB

using namespace std;
using namespace qpp;

cplx pow3(const cplx& z) // a test function
{
    return std::pow(z, 3);
}

int main()
{
    cout << "Starting qpp..." << endl;
    // output format
    // cout << std::scientific;
    cout << std::fixed; // use fixed format for nice formatting
    cout << std::setprecision(4); // only for fixed or scientific modes

    // TESTING
    // testing channel and Gates::apply
    cout << endl << "Testing channel(...) and Gates::apply(...)." << endl;
    cmat rho = randrho(16);
    cmat K = kron(gt.Id2, gt.X, gt.Y, gt.Z);
    vector<std::size_t> p = randperm(4); // permutation
    cout << "Permutation: ";
    displn(p, " ", " ");
    vector<std::size_t> invp = invperm(p); // inverse permutation
    cout << "Inverse permutation: ";
    displn(invp, " ", " ");
    cmat r1 = channel(rho, { K }, p, { 2, 2, 2, 2 });
    cmat r2 = syspermute(channel(syspermute(rho, p, { 2, 2, 2, 2 })), { K },
        { 0,
            1, 2, 3 }, { 2, 2, 2, 2 }, invp, { 2, 2, 2, 2 });
    cout << norm(r1 - r2) << endl << endl;

    r1 = gt.apply(rho, K, p, { 2, 2, 2, 2 });
    r2 = syspermute(
        gt.apply(syspermute(rho, p, { 2, 2, 2, 2 })), K, { 0, 1, 2, 3 }, { 2,
            2, 2, 2 }, invp, { 2, 2, 2, 2 });
    cout << norm(r1 - r2) << endl << endl;
```

```

displn(channel(prj(mket( { 0, 1 })), { gt.CNOTab, { 1, 0 }, { 2, 2 } }));
cout << endl;
displn(gt.apply(mket( { 0, 0 }), gt.CNOTab, { 0, 1 }, { 2, 2 }));

// quantum teleportation
cout << endl << "Qudit teleportation." << endl;
ket psi = randket(2); // a random state;
cout << "|psi><psi|:" << endl;
displn(prj(psi));
cmat telecircuit = expandout(gt.H, { 0 }, { 2, 2, 2 })
    gt.CTRL(gt.X, { 0 }, { 1 }, 3);
ket psiin = kron(psi, st.b00); // input state
ket psiout = telecircuit * psiin; // output state before measurement
// measure Alice's qubits, measurement results are 1 0
psiout = kron(prj(st.z1), prj(st.z0), gt.Id2) * psiout;
// apply correction
psiout = expandout(powm(gt.Z, 1) * powm(gt.X, 0), { 2 }, { 2, 2, 2 })
    psiout;
// not necessary to normalize, prj() takes care of it below
cmat rhoout = ptrace(prj(psiout), { 0, 1 }, { 2, 2, 2 });
cout << endl << "Teleported state:" << endl;
displn(rhoout);
cout << "Difference in norm: " << norm(prj(psi) - rhoout) << endl;

// qudit measurements
cout << endl << "Qudit measurements." << endl;
cout << "Initially in state |0><0|." << endl;
ket zd0(3);
zd0 << 1, 0, 0;
Qudit q(prj(zd0));
cout << "Measuring Z operator non-destructively. Results:" << endl;
cout << q.measure() << endl;
cout << q.measure() << endl;
cout << q.measure() << endl;
cout << "Measuring X operator non-destructively. Results:" << endl;
cout << q.measure(gt.Xd(3)) << endl;
cout << q.measure(gt.Xd(3)) << endl;
cout << q.measure(gt.Xd(3)) << endl;
// von Neumann projective measurement
cout << "Measuring X operator destructively (collapse). Results:" << endl;
cout << q.measure(gt.Xd(3), true) << endl;
cout << q.measure(gt.Xd(3)) << endl;
cout << q.measure(gt.Xd(3)) << endl;
cout << "Finally measuring Z operator destructively. Results:" << endl;
cout << q.measure(true) << endl;
cout << q.measure() << endl;
cout << q.measure() << endl;
cout << "Final state of qudit:" << endl;
displn(q.getRho());

// Bell state generator
cout << endl << "Bell state generator: " << endl;
cmat circuit;
circuit = gt.CTRL(gt.X, { 0 }, { 1 }, 2) * expandout(gt.
    H, 0, { 2, 2 });
cmat input = kron(st.z0, st.z0);
cmat output = circuit * input;
cout << "Circuit matrix representation: " << endl;
displn(circuit);
cout << endl << "Output (|Bell_0> state) of the circuit on |00>: " << endl;
displn(output);

// 3-qubit repetition code
cout << endl << "3-qubit repetition code: " << endl;
cmat rep;
rep = gt.CTRL(gt.X, { 0 }, { 2 }, 3) * gt.CTRL(gt.X, { 0 }, { 1 }, 3);
input = kron(st.z1, st.z0, st.z0);
output = rep * input;
cout << "Circuit acting on |000> produces |111>. Check: " << endl;
displn(output);

// functor test
cout << endl << "Functor z^3 acting on:" << endl;
cmat a(2, 2);
a << 1, 2, 3, 4;
displn(a);
cout << "Result (with lambda):" << endl;
// functor z^3 componentwise, specify OutputScalar and Derived for lambdas
displn(cwise<cplx, cmat>(a, [](const cplx& z)->cplx
    { return z*z*z; }));
cout << "Result (with proper function):" << endl;
// automatic type deduction for proper functions
displn(cwise(a, &pow3));

// Gram-Schmidt
cout << endl << "Gram-Schmidt on matrix:" << endl;

```

```

cmat A(3, 3);
A << 1, 1, 0, 0, 2, 0, 0, 0, 0;
displn(A);
cmat Ags = grams(A);
cout << endl << "Result:" << endl;
displn(Ags);
cout << endl << "Projector is:" << endl;
displn(Ags * adjoint(Ags));

// spectral decomposition test
cout << endl << "Spectral decomposition tests." << endl;
std::size_t D = 4;
cmat rH = randH(D);
dmat evalsH = hevals(rH);
cmat evecsH = hevects(rH);
cmat spec = cmat::Zero(D, D);
for (std::size_t i = 0; i < D; i++)
    spec += evalsH(i) * prj((cmat) evecsH.col(i));
cout << "Original matrix: " << endl;
displn(rH);
cout << endl << "Reconstructed from spectral decomposition: " << endl;
displn(spec);
cout << "Difference in norm: " << norm(spec - rH) << endl;

// channel tests
cout << endl << "Channel tests." << endl;
std::size_t nk = 10, d = 2; // nk Kraus on d-dimensional system
cout << "Generating a random channel with " << nk
    << " Kraus operators on a " << d << " dimensional space..." << endl;
std::vector<cmat> Ks = randkraus(nk, d);

cmat rho_in = randrho(d); // input state
cmat rho_out = channel(rho_in, Ks); // output state

cout << "Computing its Choi matrix..." << endl;
cmat choim = choi(Ks);
cout << "Choi matrix:" << endl;
displn(choim);
cout << endl << "The eigenvalues of the Choi matrix are: " << endl;
displn(transpose(hevals(choim)));
cout << endl << "Their sum is: " << sum(hevals(choim)) << endl;
std::vector<cmat> Kperps = choi2kraus(choim);
cout << endl << "The Kraus rank of the channel is: " << Kperps.size()
    << endl;
cmat rho_out1 = channel(rho_in, Kperps);
cout << endl << "Difference in norm on output states: "
    << norm(rho_out1 - rho_out) << endl;
cout << endl << "Superoperator matrix:" << endl;
cmat smat = super(Ks);
displn(smat);
cout << endl << "The eigenvalues of the superoperator matrix are: " << endl;
cmat evalsupop = evals(smat);
displn(transpose(evalsupop));
cout << endl << "Their absolute values are: " << endl;
for (std::size_t i = 0; i < (std::size_t) evalsupop.size(); i++)
    cout << std::abs((cplx) evalsupop(i)) << " ";
cout << endl << endl << "Difference in norm for superoperator action: ";
cmat rho_out2 = transpose(
    (cmat) reshape(smat * reshape(transpose(rho_in), d * d, 1), d, d));
cout << norm(rho_out - rho_out2) << endl;

// statistics tests
cout << endl << "Statistics tests." << endl;
std::vector<cplx> ampl = { 1. + 1_i, 1. - 1_i };
cmat va(1, 4);
va << 0.1, 1, 1. + 1_i, 1. + 2_i;
DiscreteDistributionAbsSquare dc(va);
cout << "The probabilities are: ";
displn(dc.probabilities(), " ", "{", " }");

// // TIMING tests
cout << endl << "Timing tests..." << endl;
std::size_t n = 12; // number of qubits
std::size_t N = std::pow(2, n);
vector<std::size_t> dims(n, 2); // local dimensions
cout << "n = " << n << " qubits, matrix size " << N << " x " << N << "."
    << endl;

// matrix initialization
cout << endl << "Matrix initialization timing." << endl;
// start the timer, automatic tic() in the constructor
Timer t, total;
cmat randcmat = cmat::Random(N, N);
t.toc(); // read the time
cout << "Took " << t << " seconds." << endl;

// lazy matrix product

```

```

cout << endl << "Lazy matrix product timing." << endl;
t.tic();
auto lazyprod = randcmat * randcmat; // lazyprod has type GenMatProduct
t.toc(); // read the time
cout << "Took " << t << " seconds." << endl;

// ptrace1 timing
cout << endl << "ptrace1 timing." << endl;
t.tic(); // reset the chronometer
// trace away half of the qubits
ptrace1(randcmat,
        { (std::size_t) std::sqrt(N), (std::size_t) std::sqrt(N) });
t.toc(); // read the time
cout << "Took " << t << " seconds." << endl;

// ptrace2 timing
cout << endl << "ptrace2 timing." << endl;
t.tic(); // reset the chronometer
// trace away half of the qubits
ptrace2(randcmat,
        { (std::size_t) std::sqrt(N), (std::size_t) std::sqrt(N) });
t.toc(); // read the time
cout << "Took " << t << " seconds." << endl;

// ptrace
cout << endl << "ptrace timing." << endl;
vector<std::size_t> subsys_ptrace = { 0 };
cout << "Subsystem(s): ";
displn(subsys_ptrace, " ", "");
t.tic();
ptrace(randcmat, subsys_ptrace, dims);
t.toc();
cout << "Took " << t << " seconds." << endl;

// ptranspose
cout << endl << "ptranspose timing." << endl;
vector<std::size_t> subsys_ptranspose; // partially transpose n-1 subsystems
for (std::size_t i = 0; i < n - 1; i++)
    subsys_ptranspose.push_back(i);
cout << "Subsystem(s): ";
displn(subsys_ptranspose, " ", "");
t.tic();
ptranspose(randcmat, subsys_ptranspose, dims);
t.toc();
cout << "Took " << t << " seconds." << endl;

// syspermute
cout << endl << "syspermute timing." << endl;
vector<std::size_t> perm; // left-shift all subsystems by 1
for (std::size_t i = 0; i < n; i++)
    perm.push_back((i + 1) % n);
cout << "Subsystem(s): ";
displn(perm, " ", "");
t.tic();
syspermute(randcmat, perm, dims);
t.toc();
cout << "Took " << t << " seconds." << endl;

// // matrix product
// cout << endl << "Matrix product timing." << endl;
// t.tic(); // reset the chronometer
// cmat prodmat = randcmat * randcmat; // explicit cmat now
// t.toc(); // read the time
// cout << "Took " << t << " seconds." << endl;

// END TIMING
total.toc(); // read the total running time
cout << endl << "Total time: " << total.seconds() << " seconds.";
cout << endl << "Exiting qpp..." << endl;
}

```


Chapter 2

Namespace Index

2.1 Namespace List

Here is a list of all namespaces with brief descriptions:

qpp	13
qpp::internal	73

Chapter 3

Hierarchical Index

3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

qpp::DiscreteDistribution	77
qpp::DiscreteDistributionAbsSquare	78
exception	
qpp::Exception	79
qpp::NormalDistribution	88
qpp::Qudit	89
qpp::Singleton< T >	92
qpp::Gates	82
qpp::RandomDevices	91
qpp::Singleton< const Gates >	92
qpp::Singleton< const States >	92
qpp::States	93
qpp::Singleton< RandomDevices >	92
qpp::Timer	96
qpp::UniformIntDistribution	97
qpp::UniformRealDistribution	97

Chapter 4

Class Index

4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

qpp::DiscreteDistribution	77
qpp::DiscreteDistributionAbsSquare	78
qpp::Exception	79
qpp::Gates	82
qpp::NormalDistribution	88
qpp::Qudit	89
qpp::RandomDevices	91
qpp::Singleton< T >	92
qpp::States	93
qpp::Timer	96
qpp::UniformIntDistribution	97
qpp::UniformRealDistribution	97

Chapter 5

File Index

5.1 File List

Here is a list of all files with brief descriptions:

include/channels.h	99
include/constants.h	104
include/entanglement.h	105
include/entropies.h	106
include/functions.h	107
include/internal.h	110
include/io.h	111
include/matlab.h	112
include/qpp.h	113
include/random.h	114
include/types.h	115
include/classes/exception.h	100
include/classes/gates.h	100
include/classes/qudit.h	101
include/classes/randevs.h	101
include/classes/singleton.h	102
include/classes/stat.h	103
include/classes/states.h	103
include/classes/timer.h	104

Chapter 6

Namespace Documentation

6.1 qpp Namespace Reference

Namespaces

- [internal](#)

Classes

- class [DiscreteDistribution](#)
- class [DiscreteDistributionAbsSquare](#)
- class [Exception](#)
- class [Gates](#)
- class [NormalDistribution](#)
- class [Qudit](#)
- class [RandomDevices](#)
- class [Singleton](#)
- class [States](#)
- class [Timer](#)
- class [UniformIntDistribution](#)
- class [UniformRealDistribution](#)

Typedefs

- using [cplx](#) = std::complex< double >
Complex number in double precision.
- using [cmat](#) = Eigen::MatrixXcd
Complex (double precision) dynamic Eigen matrix.
- using [dmat](#) = Eigen::MatrixXd
Real (double precision) dynamic Eigen matrix.
- using [ket](#) = Eigen::Matrix< [cplx](#), Eigen::Dynamic, 1 >
Complex (double precision) dynamic Eigen column matrix.
- using [bra](#) = Eigen::Matrix< [cplx](#), 1, Eigen::Dynamic >
Complex (double precision) dynamic Eigen row matrix.
- template<typename Scalar >
using [DynMat](#) = Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >
Dynamic Eigen matrix over the field specified by Scalar.

Functions

- `cmat super` (const std::vector< `cmat` > &Ks)
Superoperator matrix representation.
- `cmat choi` (const std::vector< `cmat` > &Ks)
Choi matrix representation.
- `std::vector< cmat > choi2kraus` (const `cmat` &A)
Extracts orthogonal Kraus operators from Choi matrix.
- `template<typename Derived >`
`cmat channel` (const Eigen::MatrixBase< Derived > &rho, const std::vector< `cmat` > &Ks)
Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.
- `template<typename Derived >`
`cmat channel` (const Eigen::MatrixBase< Derived > &rho, const std::vector< `cmat` > &Ks, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)
Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.
- `constexpr std::complex< double > operator""_i` (unsigned long long int x)
User-defined literal for complex $i = \sqrt{-1}$ (integer overload)
- `constexpr std::complex< double > operator""_i` (long double x)
User-defined literal for complex $i = \sqrt{-1}$ (real overload)
- `std::complex< double > omega` (std::size_t D)
D-th root of unity.
- `template<typename Derived >`
`cmat schmidtcoeff` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)
Schmidt coefficients of the bi-partite pure state A.
- `template<typename Derived >`
`cmat schmidtU` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)
Schmidt basis on Alice's side.
- `template<typename Derived >`
`cmat schmidtV` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)
Schmidt basis on Bob's side.
- `template<typename Derived >`
`cmat schmidtprob` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)
Schmidt probabilities of the bi-partite pure state A.
- `template<typename Derived >`
`double entanglement` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)
Entanglement of the bi-partite pure state A.
- `template<typename Derived >`
`double gconcurrence` (const Eigen::MatrixBase< Derived > &A)
G-concurrence of the bi-partite pure state A.
- `template<typename Derived >`
`double shannon` (const Eigen::MatrixBase< Derived > &A)
Shannon/von-Neumann entropy of the probability distribution/density matrix A.
- `template<typename Derived >`
`double renyi` (const double alpha, const Eigen::MatrixBase< Derived > &A)
Renyi- α entropy of the probability distribution/density matrix A.
- `template<typename Derived >`
`double renyi_inf` (const Eigen::MatrixBase< Derived > &A)
Renyi- ∞ entropy (min entropy) of the probability distribution/density matrix A.
- `template<typename Derived >`
`double tsallis` (const double alpha, const Eigen::MatrixBase< Derived > &A)
Tsallis- α entropy of the probability distribution/density matrix A.

- `template<typename Derived >`
`double qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys,`
`const std::vector< std::size_t > &dims)`
Quantum mutual information between 2 subsystems of a composite system.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > transpose (const Eigen::MatrixBase< Derived > &A)`
Transpose.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > conjugate (const Eigen::MatrixBase< Derived > &A)`
Complex conjugate.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > adjoint (const Eigen::MatrixBase< Derived > &A)`
Adjoint.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > inverse (const Eigen::MatrixBase< Derived > &A)`
Inverse.
- `template<typename Derived >`
`Derived::Scalar trace (const Eigen::MatrixBase< Derived > &A)`
Trace.
- `template<typename Derived >`
`Derived::Scalar det (const Eigen::MatrixBase< Derived > &A)`
Determinant.
- `template<typename Derived >`
`Derived::Scalar logdet (const Eigen::MatrixBase< Derived > &A)`
Logarithm of the determinant.
- `template<typename Derived >`
`Derived::Scalar sum (const Eigen::MatrixBase< Derived > &A)`
Element-wise sum.
- `template<typename Derived >`
`double norm (const Eigen::MatrixBase< Derived > &A)`
Trace norm.
- `template<typename Derived >`
`cmat evals (const Eigen::MatrixBase< Derived > &A)`
Eigenvalues.
- `template<typename Derived >`
`cmat evecs (const Eigen::MatrixBase< Derived > &A)`
Eigenvectors.
- `template<typename Derived >`
`dmat hevals (const Eigen::MatrixBase< Derived > &A)`
Hermitian eigenvalues.
- `template<typename Derived >`
`cmat hevecs (const Eigen::MatrixBase< Derived > &A)`
Hermitian eigenvectors.
- `template<typename Derived >`
`cmat funm (const Eigen::MatrixBase< Derived > &A, cplx(*f)(const cplx &))`
Functional calculus $f(A)$
- `template<typename Derived >`
`cmat sqrtm (const Eigen::MatrixBase< Derived > &A)`
Matrix square root.
- `template<typename Derived >`
`cmat absm (const Eigen::MatrixBase< Derived > &A)`
Matrix absolut value.

- `template<typename Derived >`
`cmat expm` (const Eigen::MatrixBase< Derived > &A)
Matrix exponential.
- `template<typename Derived >`
`cmat logm` (const Eigen::MatrixBase< Derived > &A)
Matrix logarithm.
- `template<typename Derived >`
`cmat sinm` (const Eigen::MatrixBase< Derived > &A)
Matrix sin.
- `template<typename Derived >`
`cmat cosm` (const Eigen::MatrixBase< Derived > &A)
Matrix cos.
- `template<typename Derived >`
`cmat spectralpowm` (const Eigen::MatrixBase< Derived > &A, const `cplx` z)
Matrix power.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > powm` (const Eigen::MatrixBase< Derived > &A, std::size_t n)
Matrix power.
- `template<typename OutputScalar , typename Derived >`
`DynMat< OutputScalar > cwise` (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const typename Derived::Scalar &))
Functor.
- `template<typename T >`
`DynMat< typename T::Scalar > kron` (const T &head)
Kronecker product (variadic overload)
- `template<typename T , typename... Args>`
`DynMat< typename T::Scalar > kron` (const T &head, const Args &...tail)
Kronecker product (variadic overload)
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > kron` (const std::vector< Derived > &As)
Kronecker product (std::vector overload)
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > kron` (const std::initializer_list< Derived > &As)
Kronecker product (std::initializer_list overload)
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > kronpow` (const Eigen::MatrixBase< Derived > &A, std::size_t n)
Kronecker power.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > reshape` (const Eigen::MatrixBase< Derived > &A, std::size_t rows, std::size_t cols)
Reshape.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > syspermute` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &perm, const std::vector< std::size_t > &dims)
System permutation.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > ptrace1` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)
Partial trace.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > ptrace2` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)
Partial trace.

- `template<typename Derived >`
`DynMat< typename Derived::Scalar > ptrace` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)
Partial trace.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > ptranspose` (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)
Partial transpose.
- `template<typename Derived1 , typename Derived2 >`
`DynMat< typename Derived1::Scalar > comm` (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
Commutator.
- `template<typename Derived1 , typename Derived2 >`
`DynMat< typename Derived1::Scalar > anticomm` (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
Anti-commutator.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > prj` (const Eigen::MatrixBase< Derived > &V)
Projector.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > expandout` (const Eigen::MatrixBase< Derived > &A, std::size_t pos, const std::vector< std::size_t > &dims)
Expand out.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > grams` (const std::vector< Derived > &Vs)
Gram-Schmidt orthogonalization (std::vector overload)
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > grams` (const std::initializer_list< Derived > &Vs)
Gram-Schmidt orthogonalization (std::initializer_list overload)
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > grams` (const Eigen::MatrixBase< Derived > &A)
Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)
- `std::vector< std::size_t > n2multiidx` (std::size_t n, const std::vector< std::size_t > &dims)
Non-negative integer index to multi-index.
- `std::size_t multiidx2n` (const std::vector< std::size_t > &midx, const std::vector< std::size_t > &dims)
Multi-index to non-negative integer index.
- `ket mket` (const std::vector< std::size_t > &mask)
Multi-partite qubit ket.
- `ket mket` (const std::vector< std::size_t > &mask, const std::vector< std::size_t > &dims)
Multi-partite qudit ket (different dimensions overload)
- `ket mket` (const std::vector< std::size_t > &mask, std::size_t d)
Multi-partite qudit ket (same dimensions overload)
- `std::vector< std::size_t > invperm` (const std::vector< std::size_t > &perm)
Inverse permutation.
- `std::vector< std::size_t > compperm` (const std::vector< std::size_t > &perm, const std::vector< std::size_t > &sigma)
Compose permutations.
- `template<typename T >`
`void disp` (const T &x, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)
- `template<typename T >`
`void displn` (const T &x, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)

- `template<typename T >`
`void disp (const T *x, const std::size_t n, const std::string &separator, const std::string &start="["`, const std::string &end="]", std::ostream &os=std::cout)
- `template<typename T >`
`void displn (const T *x, const std::size_t n, const std::string &separator, const std::string &start="["`, const std::string &end="]", std::ostream &os=std::cout)
- `template<typename Derived >`
`void disp (const Eigen::MatrixBase< Derived > &A, double chop=chop, std::ostream &os=std::cout)`
- `template<typename Derived >`
`void displn (const Eigen::MatrixBase< Derived > &A, double chop=chop, std::ostream &os=std::cout)`
- `void disp (const cplx c, double chop=chop, std::ostream &os=std::cout)`
- `void displn (const cplx c, double chop=chop, std::ostream &os=std::cout)`
- `template<typename Derived >`
`void save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)`
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > load (const std::string &fname)`
- `template<typename Derived >`
`Derived loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`
- `template<>`
`dmat loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`
- `template<>`
`cmat loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`
- `template<typename Derived >`
`void saveMATLABmatrix (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`
- `template<>`
`void saveMATLABmatrix (const Eigen::MatrixBase< dmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`
- `template<>`
`void saveMATLABmatrix (const Eigen::MatrixBase< cmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)`
- `template<typename Derived >`
`Derived rand (std::size_t rows, std::size_t cols, double a=0, double b=1)`
- `template<>`
`dmat rand (std::size_t rows, std::size_t cols, double a, double b)`
- `template<>`
`cmat rand (std::size_t rows, std::size_t cols, double a, double b)`
- `double rand (double a=0, double b=1)`
- `long long randint (long long a, long long b)`
- `template<typename Derived >`
`Derived randn (std::size_t rows, std::size_t cols, double mean=0, double sigma=1)`
- `template<>`
`dmat randn (std::size_t rows, std::size_t cols, double mean, double sigma)`
- `template<>`
`cmat randn (std::size_t rows, std::size_t cols, double mean, double sigma)`
- `double randn (double mean=0, double sigma=1)`
- `cmat randU (std::size_t D)`
- `cmat randV (std::size_t Din, std::size_t Dout)`
- `std::vector< cmat > randkraus (std::size_t n, std::size_t D)`
- `cmat randH (std::size_t D)`
- `ket randket (std::size_t D)`
- `cmat randrho (std::size_t D)`
- `std::vector< std::size_t > randperm (std::size_t n)`

Variables

- constexpr double `chop` = 1e-10
Used in `qpp::disp()` and `qpp::displn()` for setting to zero numbers that have their absolute value smaller than `qpp::ct←::chop`.
- constexpr double `eps` = 1e-12
Used to decide whether a number or expression in double precision is zero or not.
- constexpr std::size_t `maxn` = 64
Maximum number of qubits.
- constexpr double `pi` = 3.141592653589793238462643383279502884
 π
- constexpr double `ee` = 2.718281828459045235360287471352662497
Base of natural logarithm, e .
- `RandomDevices` & `rdevs` = `RandomDevices::get_instance()`
`qpp::RandomDevices` Singleton
- const `Gates` & `gt` = `Gates::get_instance()`
`qpp::Gates` const Singleton
- const `States` & `st` = `States::get_instance()`
`qpp::States` const Singleton

6.1.1 Typedef Documentation

6.1.1.1 using `qpp::bra` = typedef `Eigen::Matrix<cplx, 1, Eigen::Dynamic>`

Complex (double precision) dynamic Eigen row matrix.

6.1.1.2 using `qpp::cmat` = typedef `Eigen::MatrixXcd`

Complex (double precision) dynamic Eigen matrix.

6.1.1.3 using `qpp::cplx` = typedef `std::complex<double>`

Complex number in double precision.

6.1.1.4 using `qpp::dmat` = typedef `Eigen::MatrixXd`

Real (double precision) dynamic Eigen matrix.

6.1.1.5 template<typename `Scalar`> using `qpp::DynMat` = typedef `Eigen::Matrix<Scalar, Eigen::Dynamic, Eigen::Dynamic>`

Dynamic Eigen matrix over the field specified by *Scalar*.

Example:

```
auto mat = DynMat<float>(2,3); // type of mat is Eigen::Matrix<float, Eigen::Dynamic, Eigen::Dynamic>
```

6.1.1.6 using `qpp::ket` = typedef `Eigen::Matrix<cplx, Eigen::Dynamic, 1>`

Complex (double precision) dynamic Eigen column matrix.

6.1.2 Function Documentation

6.1.2.1 `template<typename Derived > cmat qpp::absm (const Eigen::MatrixBase< Derived > & A)`

Matrix absolut value.

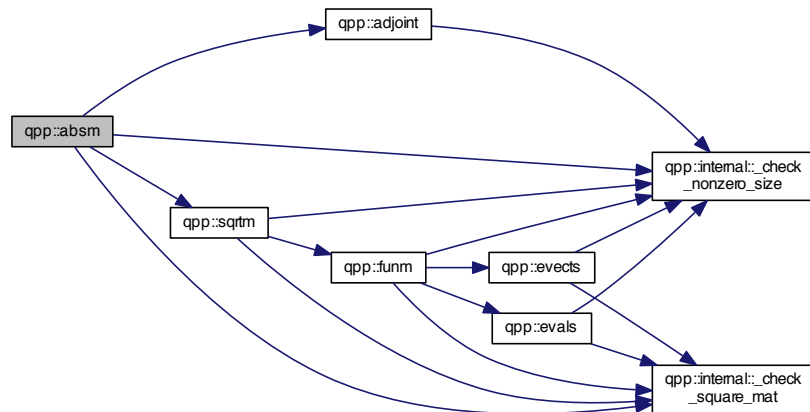
Parameters

A	Eigen expression
-----	------------------

Returns

Matrix absolut value of A , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.2 `template<typename Derived > DynMat<typename Derived::Scalar> qpp::adjoint (const Eigen::MatrixBase<Derived > & A)`

Adjoint.

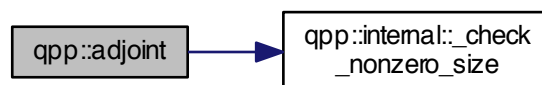
Parameters

A	Eigen expression
-----	------------------

Returns

Adjoint (Hermitian conjugate) of A , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.3 `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::anticomm (const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B)`

Anti-commutator.

Anti-commutator $\{A, B\} = AB + BA$

Both A and B must be Eigen expressions over the same scalar field

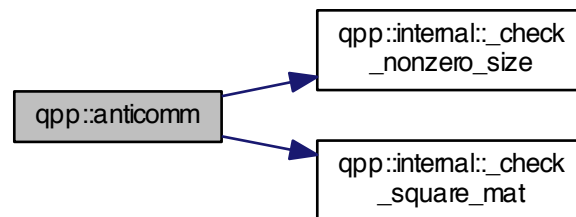
Parameters

A	Eigen expression
B	Eigen expression

Returns

Anti-commutator $AB + BA$, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.4 `template<typename Derived > cmat qpp::channel (const Eigen::MatrixBase< Derived > & rho, const std::vector< cmat > & Ks)`

Applies the channel specified by the set of Kraus operators Ks to the density matrix ρ .

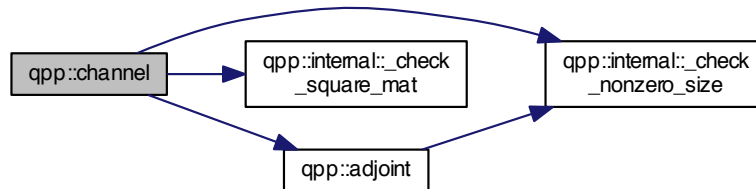
Parameters

ρ	Eigen expression
Ks	std::vector of Eigen expressions representing the set of Kraus operators

Returns

Output density matrix, as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.5 `template<typename Derived> cmat qpp::channel (const Eigen::MatrixBase< Derived> & rho, const std::vector< cmat> & Ks, const std::vector< std::size_t> & subsys, const std::vector< std::size_t> & dims)`

Applies the channel specified by the set of Kraus operators *Ks* to the part of the density matrix *rho* specified by *subsys*.

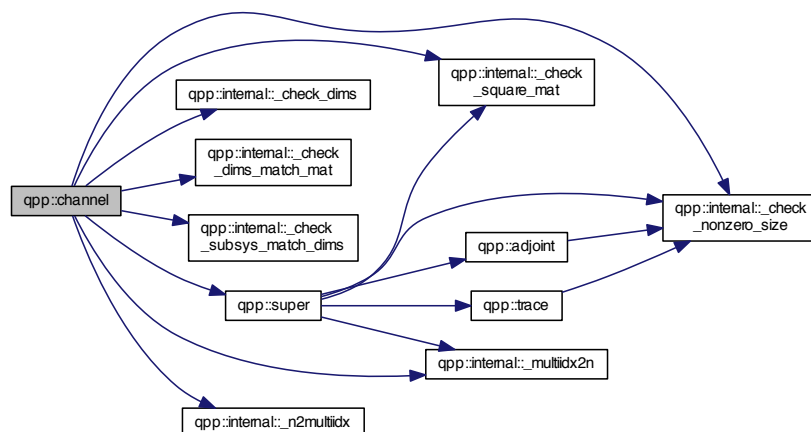
Parameters

<i>rho</i>	Eigen expression
<i>Ks</i>	std::vector of Eigen expressions representing the set of Kraus operators
<i>subsys</i>	Subsystems' indexes
<i>dims</i>	Dimensions of the multi-partite system

Returns

Output density matrix, as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.6 `cmat qpp::choi (const std::vector< cmat > & Ks)`

Choi matrix representation.

Constructs the Choi matrix of the channel specified by the set of Kraus operators K_s in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

Note

the superoperator matrix S and the Choi matrix C are related by $S_{ab,mn} = C_{ma,nb}$

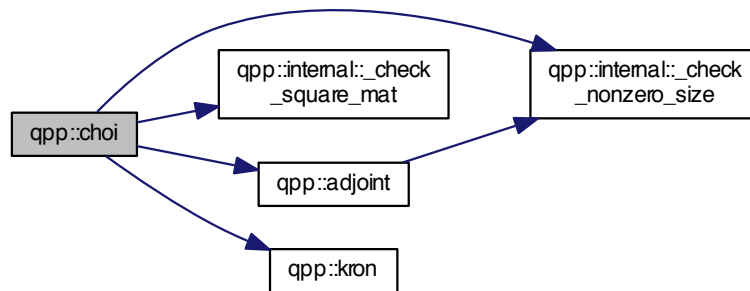
Parameters

K_s	<code>std::vector</code> of Eigen expressions representing the set of Kraus operators
-------	---

Returns

Choi matrix representation, as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.7 `std::vector<cmat> qpp::choi2kraus (const cmat & A)`

Extracts orthogonal Kraus operators from Choi matrix.

Extracts a set of orthogonal (under Hilbert-Schmidt operator norm) Kraus operators from the Choi representation A of the channel

Note

The Kraus operators satisfy $Tr(K_i^\dagger K_j) = \delta_{ij}$ for all $i \neq j$

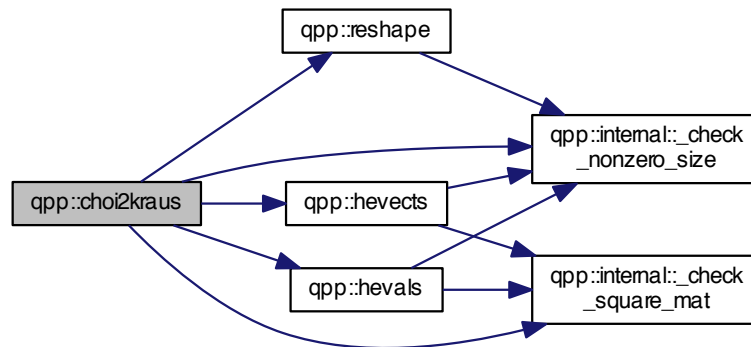
Parameters

A	Choi matrix
-----	-------------

Returns

std::vector of dynamic matrices over the complex field representing the set of Kraus operators

Here is the call graph for this function:



6.1.2.8 `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::comm (const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B)`

Commutator.

Commutator $[A, B] = AB - BA$

Both A and B must be Eigen expressions over the same scalar field

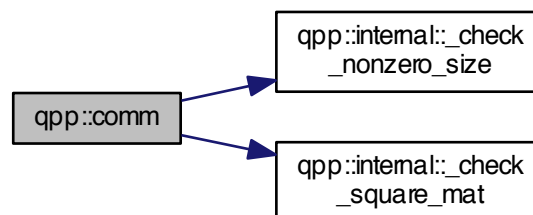
Parameters

A	Eigen expression
B	Eigen expression

Returns

Commutator $AB - BA$, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.9 `std::vector<std::size_t> qpp::compperm (const std::vector< std::size_t > & perm, const std::vector< std::size_t > & sigma)`

Compose permutations.

Parameters

<i>perm</i>	Permutation
<i>sigma</i>	Permutation

Returns

Composition of the permutations $perm \circ sigma = perm(sigma)$

Here is the call graph for this function:



6.1.2.10 `template<typename Derived > DynMat<typename Derived::Scalar> qpp::conjugate (const Eigen::MatrixBase< Derived > & A)`

Complex conjugate.

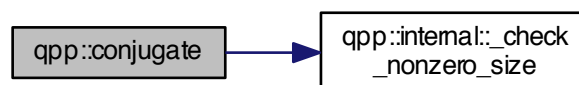
Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Complex conjugate of *A*, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.11 `template<typename Derived > cmat qpp::cosm (const Eigen::MatrixBase< Derived > & A)`

Matrix cos.

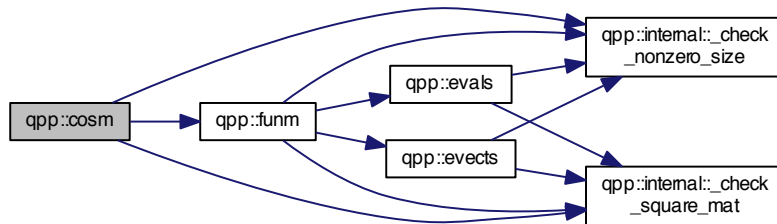
Parameters

A	Eigen expression
-----	------------------

Returns

Matrix cosine of A , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.12 `template<typename OutputScalar , typename Derived > DynMat<OutputScalar> qpp::cwise (const Eigen::MatrixBase< Derived > & A, OutputScalar*)(const typename Derived::Scalar &) f)`

Functor.

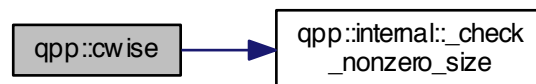
Parameters

A	Eigen expression
f	Pointer-to-function from scalars of A to <i>OutputScalar</i>

Returns

Component-wise $f(A)$, as a dynamic matrix over the *OutputScalar* scalar field

Here is the call graph for this function:



6.1.2.13 `template<typename Derived > Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > & A)`

Determinant.

Parameters

A	Eigen expression
-----	------------------

Returns

Determinant of A , as a dynamic matrix over the same scalar field
 Returns $\pm\infty$ when the determinant overflows/underflows

Here is the call graph for this function:



6.1.2.14 `template<typename T> void qpp::disp (const T & x, const std::string & separator, const std::string & start = " [", const std::string & end = "] ", std::ostream & os = std::cout)`

6.1.2.15 `template<typename T> void qpp::disp (const T * x, const std::size_t n, const std::string & separator, const std::string & start = " [", const std::string & end = "] ", std::ostream & os = std::cout)`

6.1.2.16 `template<typename Derived> void qpp::disp (const Eigen::MatrixBase< Derived> & A, double chop = chop, std::ostream & os = std::cout)`

6.1.2.17 `void qpp::disp (const cplx c, double chop = chop, std::ostream & os = std::cout)`

Here is the call graph for this function:



6.1.2.18 `template<typename T> void qpp::displn (const T & x, const std::string & separator, const std::string & start = " [", const std::string & end = "]" , std::ostream & os = std::cout)`

Here is the call graph for this function:



6.1.2.19 `template<typename T> void qpp::displn (const T * x, const std::size_t n, const std::string & separator, const std::string & start = " [", const std::string & end = "]" , std::ostream & os = std::cout)`

Here is the call graph for this function:



6.1.2.20 `template<typename Derived> void qpp::displn (const Eigen::MatrixBase< Derived > & A, double chop = chop, std::ostream & os = std::cout)`

Here is the call graph for this function:



6.1.2.21 `void qpp::displn (const cplx c, double chop = chop, std::ostream & os = std::cout)`

Here is the call graph for this function:



6.1.2.22 `template<typename Derived > double qpp::entanglement (const Eigen::MatrixBase< Derived > & A, const std::vector< std::size_t > & dims)`

Entanglement of the bi-partite pure state *A*.

Note

Defined as the von-Neumann entropy of the reduced density matrix of one of the subsystems

See also

[qpp::shannon\(\)](#)

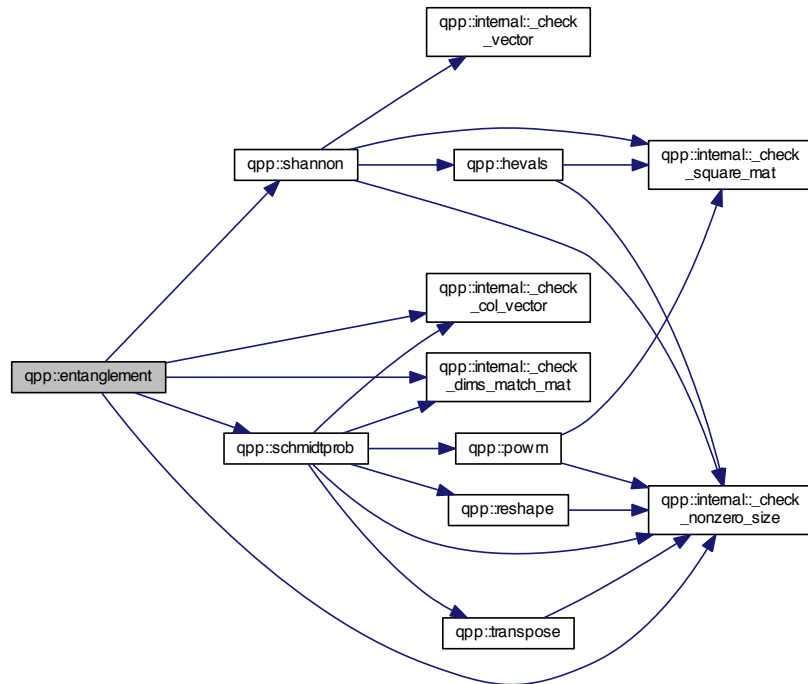
Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Subsystems' dimensions

Returns

Entanglement, with the logarithm in base 2

Here is the call graph for this function:



6.1.2.23 `template<typename Derived> cmat qpp::evals (const Eigen::MatrixBase< Derived> & A)`

Eigenvalues.

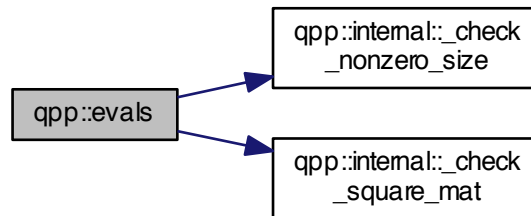
Parameters

A	Eigen expression
---	------------------

Returns

Eigenvalues of A , as a diagonal dynamic matrix over the complex field, with the eigenvalues on the diagonal

Here is the call graph for this function:



6.1.2.24 `template<typename Derived> cmat qpp::evecs (const Eigen::MatrixBase< Derived > & A)`

Eigenvectors.

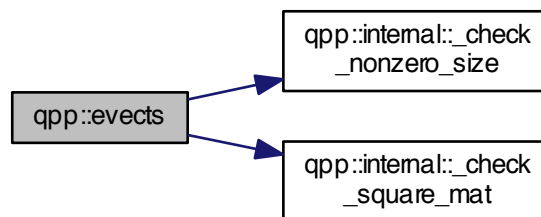
Parameters

A	Eigen expression
-----	------------------

Returns

Eigenvectors of A , as columns of a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.25 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::expandout (const Eigen::MatrixBase< Derived > & A, std::size_t pos, const std::vector< std::size_t > & dims)`

Expand out.

Expand out A as a matrix in a multi-partite system

Faster than using `qpp::kron(I, I, ..., I, A, I, ..., I)`

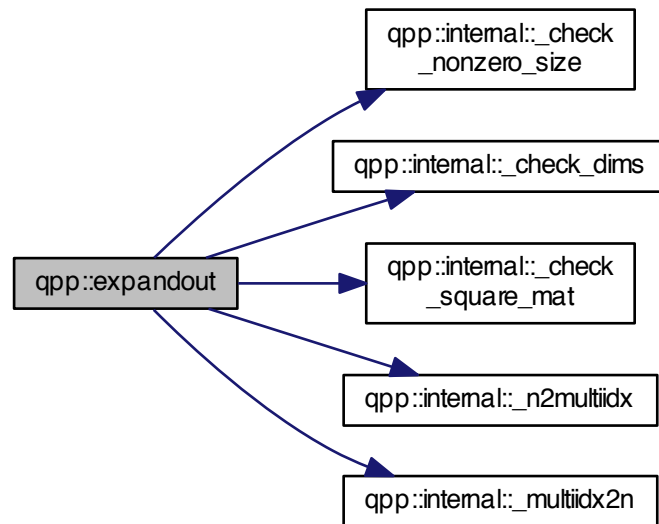
Parameters

<i>A</i>	Eigen expression
<i>pos</i>	Position
<i>dims</i>	Dimensions of the multi-partite system

Returns

Tensor product $I \otimes \cdots \otimes I \otimes A \otimes I \otimes \cdots \otimes I$, with A on position pos , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.26 `template<typename Derived> cmat qpp::expm (const Eigen::MatrixBase< Derived> & A)`

Matrix exponential.

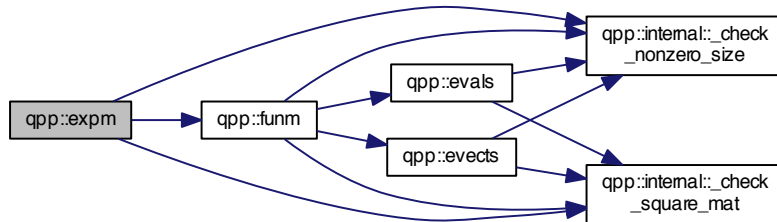
Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Matrix exponential of A , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.27 `template<typename Derived> cmat qpp::funm (const Eigen::MatrixBase< Derived> & A, cplx(*) (const cplx &) f)`

Functional calculus $f(A)$

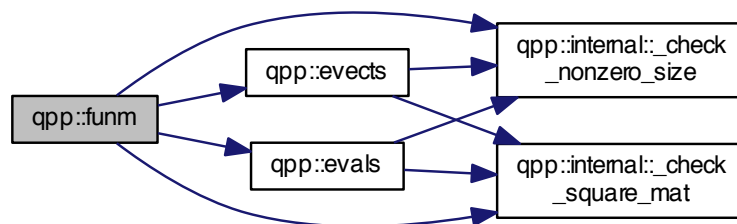
Parameters

A	Eigen expression
f	Pointer-to-function from complex to complex

Returns

$f(A)$, as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.28 `template<typename Derived> double qpp::gconcurrence (const Eigen::MatrixBase< Derived> & A)`

G-concurrence of the bi-partite pure state A .

Note

Uses [qpp::logdet\(\)](#) to avoid overflows

See also

[qpp::logdet\(\)](#)

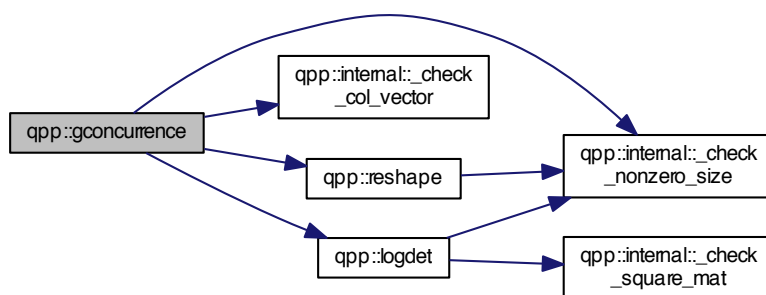
Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Subsystems' dimensions

Returns

G-concurrence

Here is the call graph for this function:



6.1.2.29 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::grams (const std::vector< Derived > & Vs)`

Gram-Schmidt orthogonalization (std::vector overload)

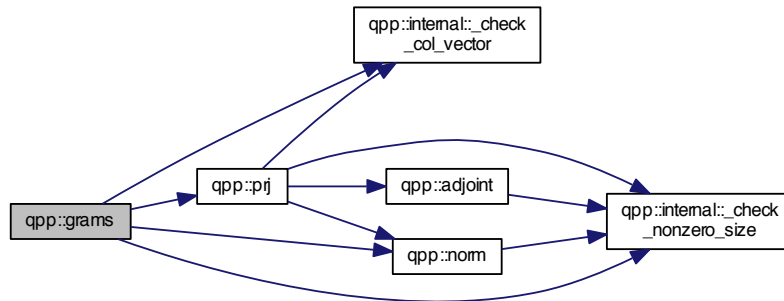
Parameters

<i>Vs</i>	std::vector of Eigen expressions as column vectors
-----------	--

Returns

Gram-Schmidt vectors of V s as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.30 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::grams (const std::initializer_list<Derived> & Vs)`

Gram-Schmidt orthogonalization (std::initializer_list overload)

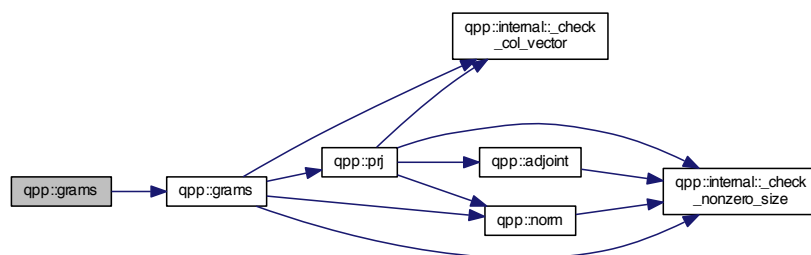
Parameters

V s	std::initializer_list of Eigen expressions as column vectors
-------	--

Returns

Gram-Schmidt vectors of V s as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.31 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::grams (const Eigen::MatrixBase<Derived> & A)`

Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)

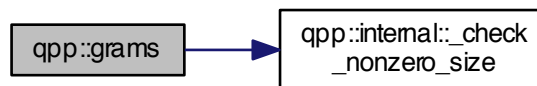
Parameters

A	Eigen expression, the input vectors are the columns of A
-----	--

Returns

Gram-Schmidt vectors of the columns of A , as columns of a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.32 `template<typename Derived> dmat qpp::hevals (const Eigen::MatrixBase< Derived> & A)`

Hermitian eigenvalues.

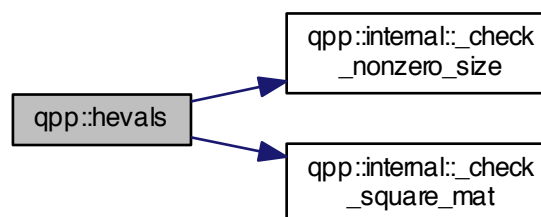
Parameters

A	Eigen expression
-----	------------------

Returns

Eigenvalues of Hermitian A , as a diagonal dynamic matrix over the real field, with eigenvalues on the diagonal

Here is the call graph for this function:



6.1.2.33 `template<typename Derived> cmat qpp::hevects (const Eigen::MatrixBase< Derived> & A)`

Hermitian eigenvectors.

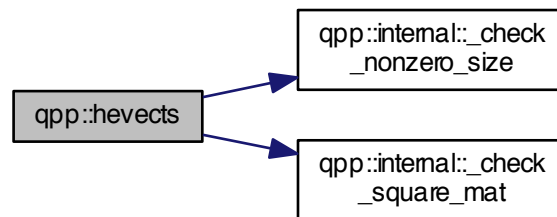
Parameters

A	Eigen expression
-----	------------------

Returns

Eigenvectors of Hermitian A , as columns of a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.34 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::inverse (const Eigen::MatrixBase<Derived> & A)`

Inverse.

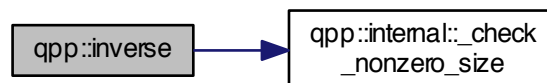
Parameters

A	Eigen expression
-----	------------------

Returns

Inverse of A , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.35 `std::vector<std::size_t> qpp::invperm (const std::vector< std::size_t > & perm)`

Inverse permutation.

Parameters

<i>perm</i>	Permutation
-------------	-------------

Returns

Inverse of the permutation *perm*

Here is the call graph for this function:



6.1.2.36 `template<typename T > DynMat<typename T::Scalar> qpp::kron (const T & head)`

Kronecker product (variadic overload)

Used to stop the recursion for the variadic template version of [qpp::kron\(\)](#)

Parameters

<i>head</i>	Eigen expression
-------------	------------------

Returns

Its argument *head*

6.1.2.37 `template<typename T , typename... Args> DynMat<typename T::Scalar> qpp::kron (const T & head, const Args &... tail)`

Kronecker product (variadic overload)

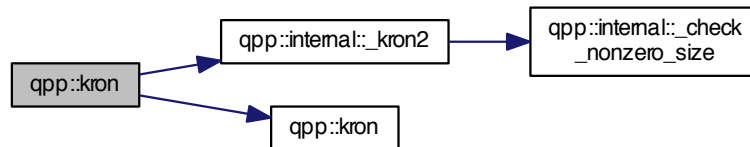
Parameters

<i>head</i>	Eigen expression
<i>tail</i>	Variadic Eigen expression (zero or more parameters)

Returns

Kronecker product of all input parameters, evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.38 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::kron (const std::vector< Derived> & As)`

Kronecker product (std::vector overload)

Parameters

As	std::vector of Eigen expressions
-----------	----------------------------------

Returns

Kronecker product of all elements in As, evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.39 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::kron (const std::initializer_list< Derived> & As)`

Kronecker product (std::initializer_list overload)

Parameters

<i>As</i>	std::initializer_list of Eigen expressions, such as {A1, A2, ... ,Ak}
-----------	---

Returns

Kronecker product of all elements in *As*, evaluated from left to right, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.40 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::kronpow (const Eigen::MatrixBase<Derived> & A, std::size_t n)`

Kronecker power.

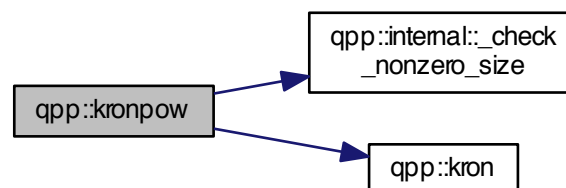
Parameters

<i>A</i>	Eigen expression
<i>n</i>	Non-negative integer

Returns

Kronecker product of *A* with itself *n* times $A^{\otimes n}$, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.41 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::load (const std::string & fname)`

6.1.2.42 `template<typename Derived> Derived qpp::loadMATLABmatrix (const std::string & mat_file, const std::string & var_name)`

6.1.2.43 `template<> dmat qpp::loadMATLABmatrix (const std::string & mat_file, const std::string & var_name)`

6.1.2.44 `template<> cmat qpp::loadMATLABmatrix (const std::string & mat_file, const std::string & var_name)`

6.1.2.45 `template<typename Derived > Derived::Scalar qpp::logdet (const Eigen::MatrixBase< Derived > & A)`

Logarithm of the determinant.

Especially useful when the determinant overflows/underflows

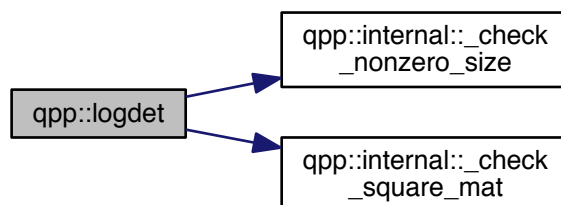
Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Logarithm of the determinant of *A*, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.46 `template<typename Derived > cmat qpp::logm (const Eigen::MatrixBase< Derived > & A)`

Matrix logarithm.

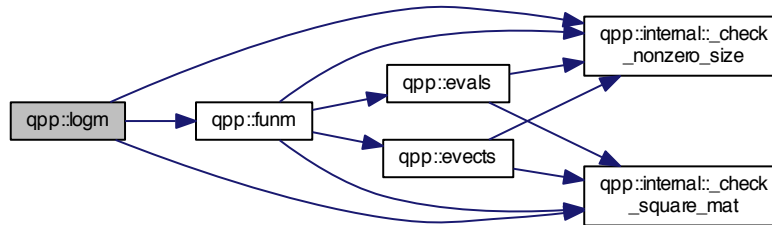
Parameters

<i>A</i>	Eigen expression
----------	------------------

Returns

Matrix logarithm of A , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.47 ket qpp::mket (const std::vector< std::size_t > & mask)

Multi-partite qubit ket.

Constructs the multi-partite qubit ket $|mask\rangle$, where *mask* is a std::vector of 0's and 1's

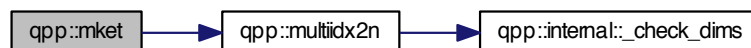
Parameters

<i>mask</i>	std::vector of 0's and 1's
-------------	----------------------------

Returns

Multi-partite qubit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



6.1.2.48 ket qpp::mket (const std::vector< std::size_t > & mask, const std::vector< std::size_t > & dims)

Multi-partite qudit ket (different dimensions overload)

Constructs the multi-partite qudit ket $|mask\rangle$, where *mask* is a std::vector of non-negative integers
Each element in *mask* has to be smaller than the corresponding element in *dims*

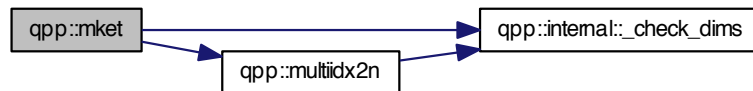
Parameters

<i>mask</i>	std::vector of non-negative integers
<i>dims</i>	Dimensions of the multi-partite system

Returns

Multi-partite qudit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



6.1.2.49 ket qpp::mket (const std::vector< std::size_t > & mask, std::size_t d)

Multi-partite qudit ket (same dimensions overload)

Constructs the multi-partite qudit ket $|\text{mask}\rangle$ in a multi-partite system, all subsystem having equal dimension d . mask is a std::vector of non-negative integers, and each element in mask has to be strictly smaller than d .

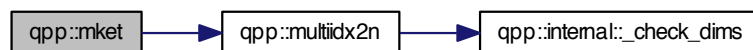
Parameters

<i>mask</i>	std::vector of non-negative integers
<i>d</i>	Subsystems' dimension

Returns

Multi-partite qudit state vector, as a dynamic column vector over the complex field

Here is the call graph for this function:



6.1.2.50 std::size_t qpp::multiidx2n (const std::vector< std::size_t > & midx, const std::vector< std::size_t > & dims)

Multi-index to non-negative integer index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

Parameters

<i>midx</i>	Multi-index
<i>dims</i>	Dimensions of the multi-partite system

Returns

Non-negative integer index

Here is the call graph for this function:



6.1.2.51 `std::vector<std::size_t> qpp::n2multiidx (std::size_t n, const std::vector< std::size_t > & dims)`

Non-negative integer index to multi-index.

Uses standard lexicographical order, i.e. 00...0, 00...1 etc.

Parameters

<i>n</i>	Non-negative integer index
<i>dims</i>	Dimensions of the multi-partite system

Returns

Multi-index of the same size as *dims*

Here is the call graph for this function:



6.1.2.52 `template<typename Derived > double qpp::norm (const Eigen::MatrixBase< Derived > & A)`

Trace norm.

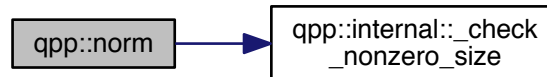
Parameters

A	Eigen expression
-----	------------------

Returns

Trace norm (Frobenius norm) of A , as a real number

Here is the call graph for this function:

6.1.2.53 `std::complex<double> qpp::omega (std::size_t D)`

D-th root of unity.

Parameters

D	Non-negative integer
-----	----------------------

Returns

D-th root of unity $\exp(2\pi i/D)$

6.1.2.54 `constexpr std::complex<double> qpp::operator""_i (unsigned long long int x)`

User-defined literal for complex $i = \sqrt{-1}$ (integer overload)

Example:

```
auto z = 4_i; // type of z is std::complex<double>
```

6.1.2.55 `constexpr std::complex<double> qpp::operator""_i (long double x)`

User-defined literal for complex $i = \sqrt{-1}$ (real overload)

Example:

```
auto z = 4.5_i; // type of z is std::complex<double>
```

6.1.2.56 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::powm (const Eigen::MatrixBase<Derived> & A, std::size_t n)`

Matrix power.

Explicitly multiplies the matrix A with itself n times

By convention $A^0 = I$

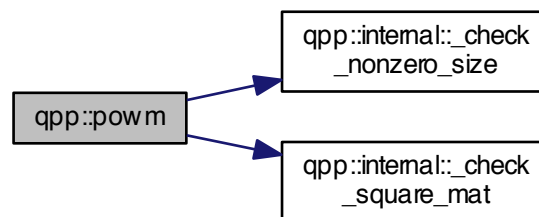
Parameters

A	Eigen expression
n	Non-negative integer

Returns

Matrix power A^n , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.57 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::prj (const Eigen::MatrixBase< Derived> & V)`

Projector.

Normalized projector onto state vector

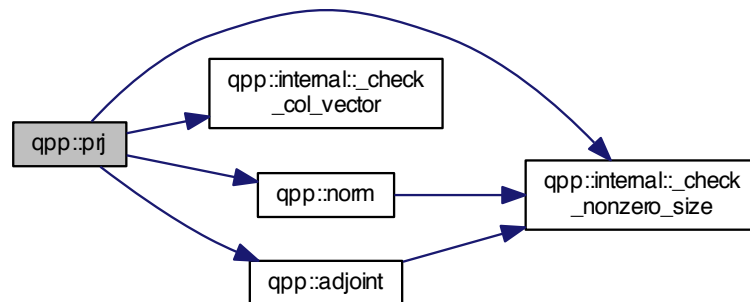
Parameters

V	Eigen expression
-----	------------------

Returns

Projector onto the state vector V , or the matrix $Zero$ if V has norm zero (i.e. smaller than `qpp::eps`), as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.58 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::ptrace (const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & subsys, const std::vector< std::size_t > & dims)`

Partial trace.

Partial trace of the multi-partite density matrix over a list of subsystems

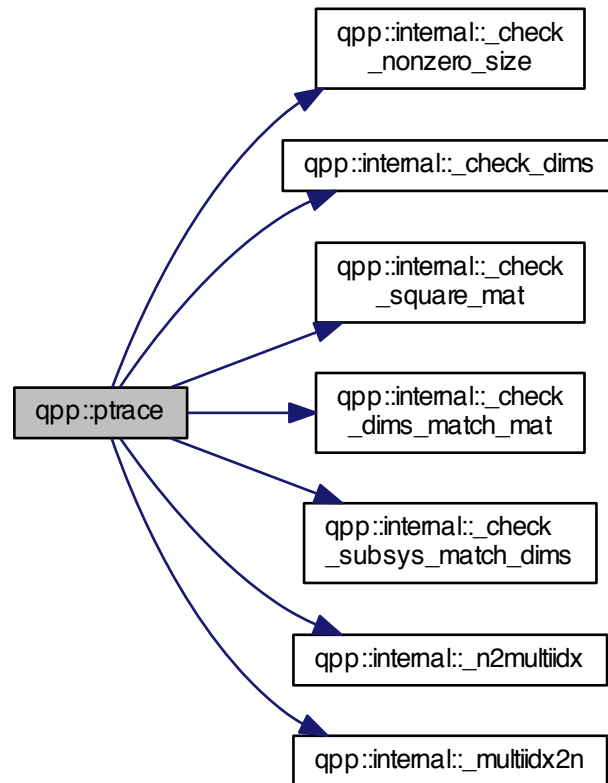
Parameters

A	Eigen expression
$subsys$	Subsystems' indexes
$dims$	Dimensions of the multi-partite system

Returns

Partial trace $Tr_{subsys}(\cdot)$ over the subsystems $subsys$ in a multi-partite system, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.59 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::ptrace1 (const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & dims)`

Partial trace.

Partial trace of density matrix over the first subsystem in a bi-partite system

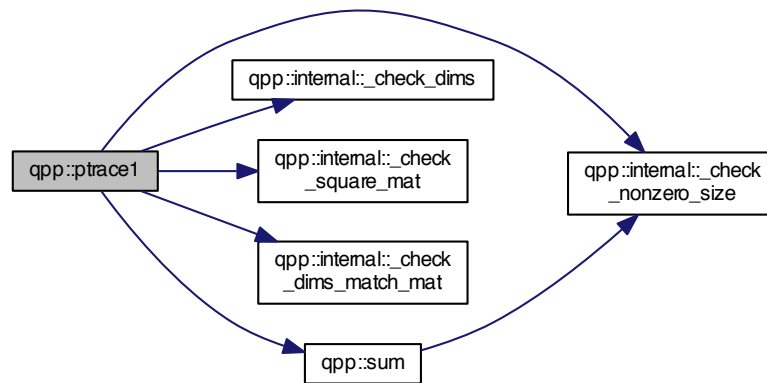
Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Dimensions of bi-partite system (must be a <code>std::vector</code> with 2 elements)

Returns

Partial trace $Tr_A(\cdot)$ over the first subsystem A in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.60 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::ptrace2 (const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & dims)`

Partial trace.

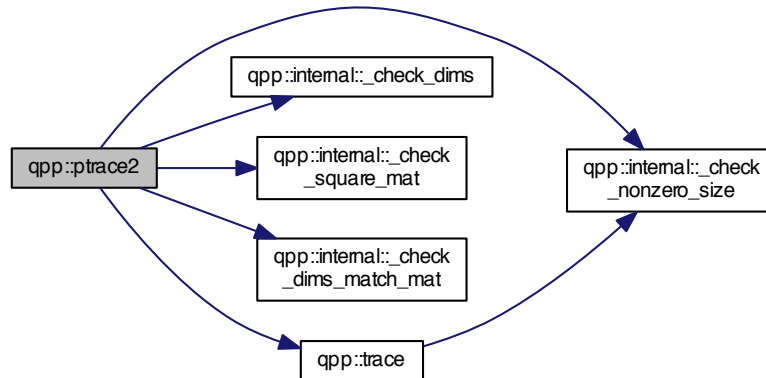
Parameters

A	Eigen expression
$dims$	Dimensions of bi-partite system (must be a <code>std::vector</code> with 2 elements)

Returns

Partial trace $Tr_B(\cdot)$ over the second subsystem B in a bi-partite system $A \otimes B$, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.61 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::ptranspose (const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & subsys, const std::vector< std::size_t > & dims)`

Partial transpose.

Partial transpose of the multi-partite density matrix over a list of subsystems

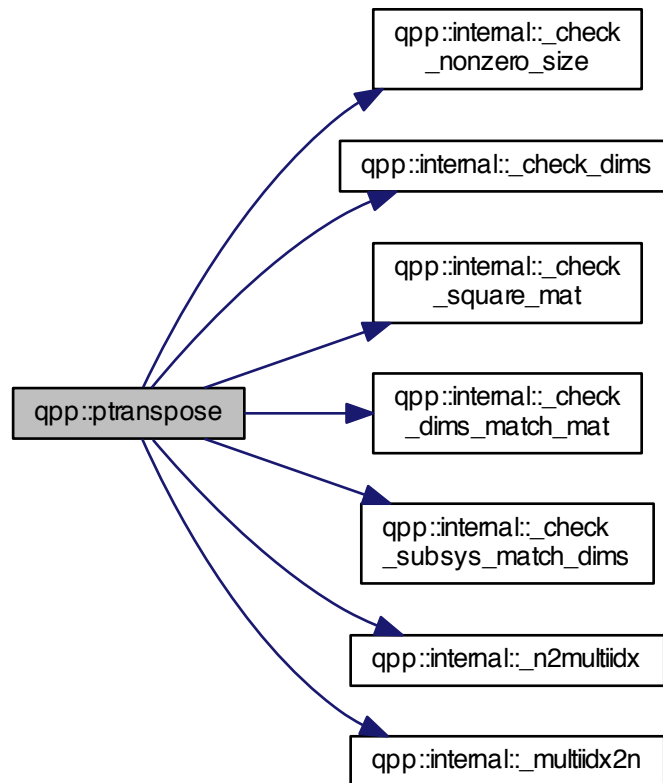
Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystems' indexes
<i>dims</i>	Dimensions of the multi-partite system

Returns

Partial transpose $(\cdot)^{T_{subsys}}$ over the subsystems *subsys* in a multi-partite system, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.62 `template<typename Derived> double qpp::qmutualinfo (const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & subsys, const std::vector< std::size_t> & dims)`

Quantum mutual information between 2 subsystems of a composite system.

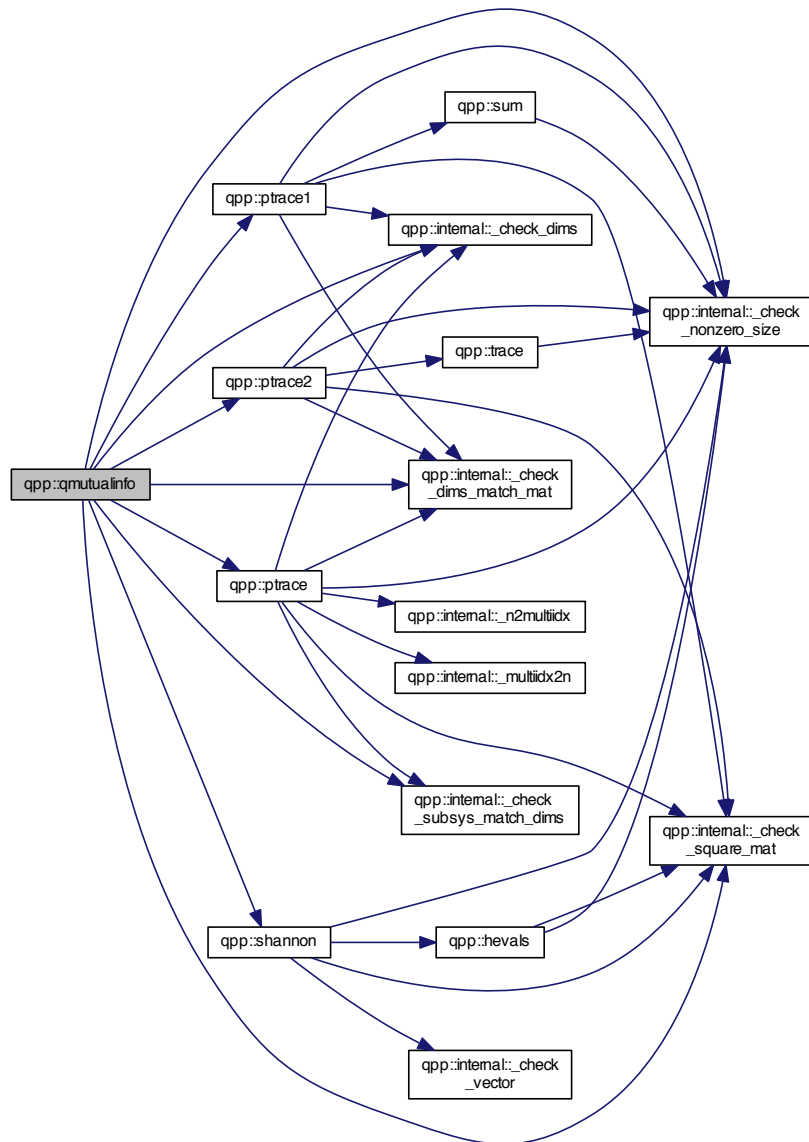
Parameters

<i>A</i>	Eigen expression
<i>subsys</i>	Subsystems' indexes
<i>dims</i>	Subsystems' dimensions

Returns

Mutual information between the 2 subsystems

Here is the call graph for this function:



6.1.2.63 `template<typename Derived> Derived qpp::rand (std::size_t rows, std::size_t cols, double a = 0, double b = 1)`

6.1.2.64 `template<> dmat qpp::rand (std::size_t rows, std::size_t cols, double a, double b)`

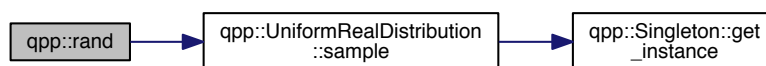
6.1.2.65 `template<> cmat qpp::rand (std::size_t rows, std::size_t cols, double a, double b)`

Here is the call graph for this function:



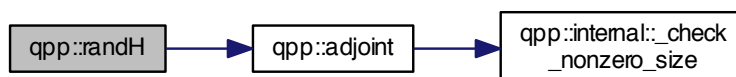
6.1.2.66 `double qpp::rand (double a = 0, double b = 1)`

Here is the call graph for this function:



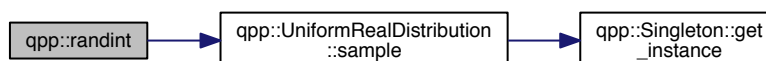
6.1.2.67 `cmat qpp::randH (std::size_t D)`

Here is the call graph for this function:



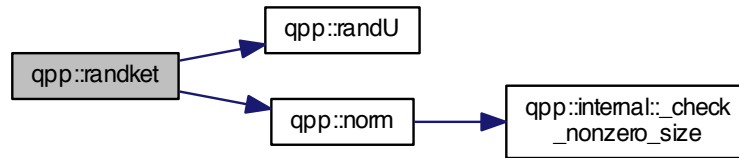
6.1.2.68 `long long qpp::randint (long long a, long long b)`

Here is the call graph for this function:



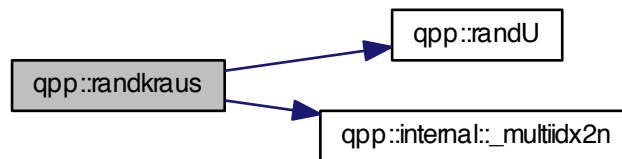
6.1.2.69 ket qpp::randket (std::size_t *D*)

Here is the call graph for this function:



6.1.2.70 std::vector<cmat> qpp::randkraus (std::size_t *n*, std::size_t *D*)

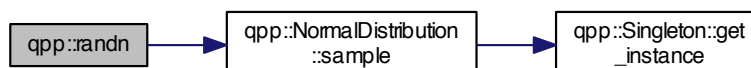
Here is the call graph for this function:



6.1.2.71 template<typename Derived > Derived qpp::randn (std::size_t *rows*, std::size_t *cols*, double *mean* = 0, double *sigma* = 1)

6.1.2.72 template<> dmat qpp::randn (std::size_t *rows*, std::size_t *cols*, double *mean*, double *sigma*)

Here is the call graph for this function:



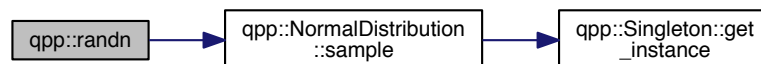
6.1.2.73 `template<> cmat qpp::randn (std::size_t rows, std::size_t cols, double mean, double sigma)`

Here is the call graph for this function:



6.1.2.74 `double qpp::randn (double mean = 0, double sigma = 1)`

Here is the call graph for this function:



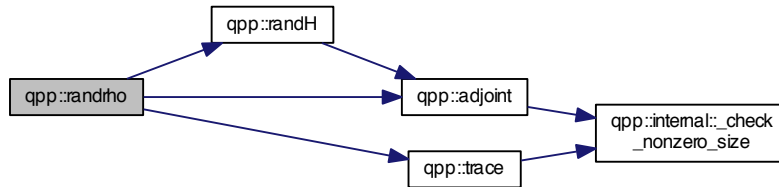
6.1.2.75 `std::vector<std::size_t> qpp::randperm (std::size_t n)`

Here is the call graph for this function:



6.1.2.76 `cmat qpp::randrho (std::size_t D)`

Here is the call graph for this function:



6.1.2.77 `cmat qpp::randU (std::size_t D)`

6.1.2.78 `cmat qpp::randV (std::size_t Din, std::size_t Dout)`

Here is the call graph for this function:



6.1.2.79 `template<typename Derived> double qpp::renyi (const double alpha, const Eigen::MatrixBase< Derived > & A)`

Renyi- α entropy of the probability distribution/density matrix A .

Note

$$\alpha \geq 0$$

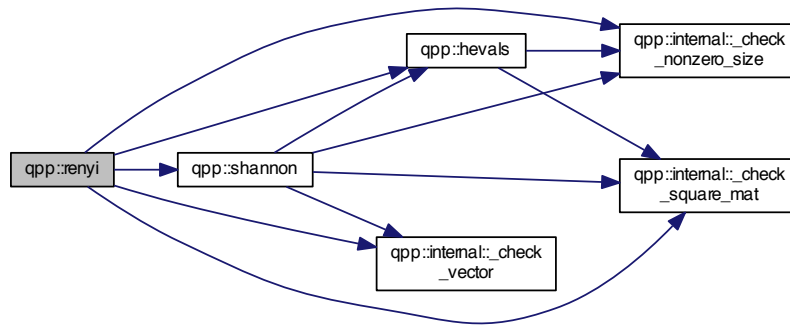
Parameters

A	Eigen expression, representing a probability distribution (dynamic column vector) or a density matrix (dynamic matrix over the complex field)
-----	---

Returns

Renyi- α entropy, with the logarithm in base 2

Here is the call graph for this function:



6.1.2.80 `template<typename Derived> double qpp::renyi_inf (const Eigen::MatrixBase< Derived> & A)`

Renyi- ∞ entropy (min entropy) of the probability distribution/density matrix A .

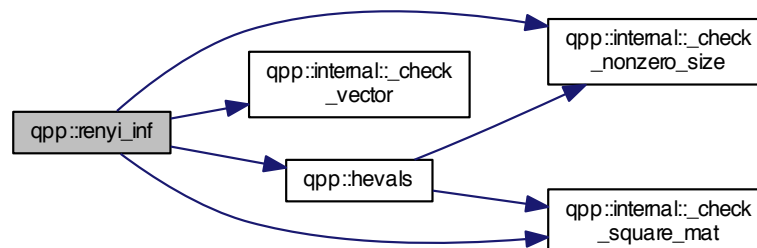
Parameters

A	Eigen expression, representing a probability distribution (dynamic column vector) or a density matrix (dynamic matrix over the complex field)
-----	---

Returns

Renyi- ∞ entropy, with the logarithm in base 2

Here is the call graph for this function:



6.1.2.81 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::reshape (const Eigen::MatrixBase< Derived> & A, std::size_t rows, std::size_t cols)`

Reshape.

Uses column-major order when reshaping (same as MATLAB)

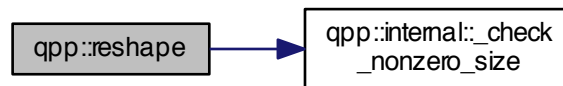
Parameters

<i>A</i>	Eigen expression
<i>rows</i>	Number of rows of the reshaped matrix
<i>cols</i>	Number of columns of the reshaped matrix

Returns

Reshaped matrix with *rows* rows and *cols* columns, as a dynamic matrix over the same scalar field

Here is the call graph for this function:

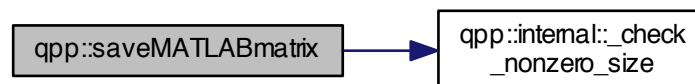


6.1.2.82 `template<typename Derived> void qpp::save (const Eigen::MatrixBase< Derived> & A, const std::string & fname)`

6.1.2.83 `template<typename Derived> void qpp::saveMATLABmatrix (const Eigen::MatrixBase< Derived> & A, const std::string & mat_file, const std::string & var_name, const std::string & mode)`

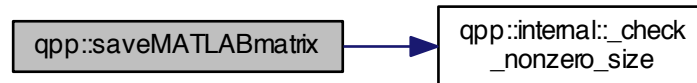
6.1.2.84 `template<> void qpp::saveMATLABmatrix (const Eigen::MatrixBase< dmat> & A, const std::string & mat_file, const std::string & var_name, const std::string & mode)`

Here is the call graph for this function:



6.1.2.85 `template<> void qpp::saveMATLABmatrix (const Eigen::MatrixBase< cmat > & A, const std::string & mat_file, const std::string & var_name, const std::string & mode)`

Here is the call graph for this function:



6.1.2.86 `template<typename Derived > cmat qpp::schmidtcoeff (const Eigen::MatrixBase< Derived > & A, const std::vector< std::size_t > & dims)`

Schmidt coefficients of the bi-partite pure state A .

Note

The sum of the squares of the Schmidt coefficients equals 1

See also

[`qpp::schmidtprob\(\)`](#)

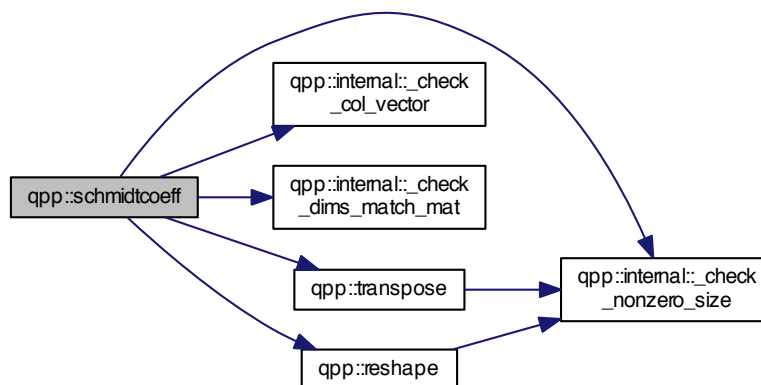
Parameters

A	Eigen expression
$dims$	Subsystems' dimensions

Returns

Schmidt coefficients of A , as a dynamic matrix over the complex field, with the Schmidt coefficients on the diagonal

Here is the call graph for this function:



6.1.2.87 `template<typename Derived> cmat qpp::schmidtprob (const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & dims)`

Schmidt probabilities of the bi-partite pure state A .

Note

Defined as the squares of the Schmidt coefficients
The sum of the Schmidt probabilities equals 1

See also

[qpp::schmidtcoeff\(\)](#)

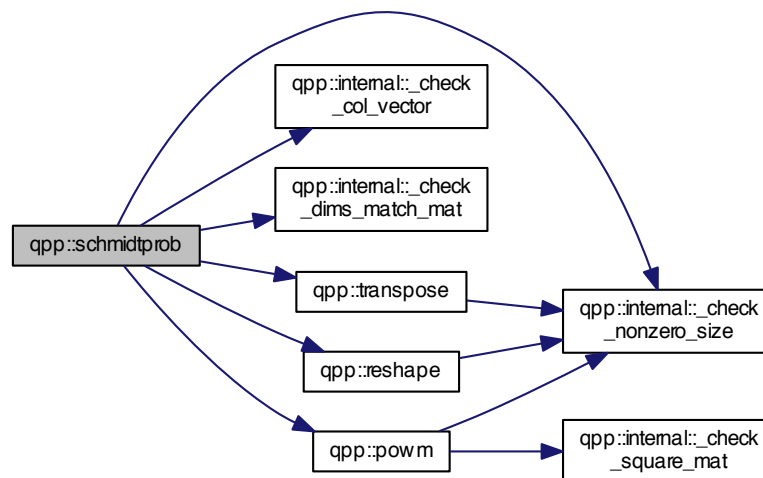
Parameters

A	Eigen expression
$dims$	Subsystems' dimensions

Returns

Schmidt probabilities of A , as a dynamic matrix over the complex field, with the Schmidt probabilities on the diagonal

Here is the call graph for this function:



6.1.2.88 `template<typename Derived> cmat qpp::schmidtU (const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & dims)`

Schmidt basis on Alice's side.

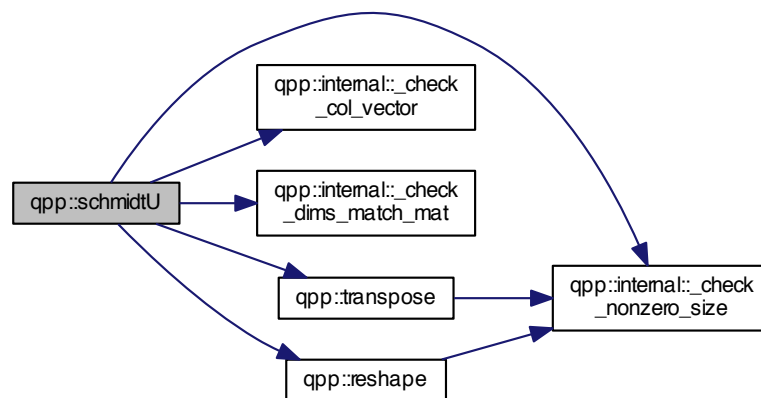
Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Subsystems' dimensions

Returns

Unitary matrix U representing the Schmidt basis on Alice's side, as a dynamic matrix over the complex field, acting on the computational basis as $U|j\rangle = |\bar{j}\rangle$ (Schmidt vector)

Here is the call graph for this function:



6.1.2.89 `template<typename Derived> cmat qpp::schmidtV (const Eigen::MatrixBase< Derived> & A, const std::vector< std::size_t> & dims)`

Schmidt basis on Bob's side.

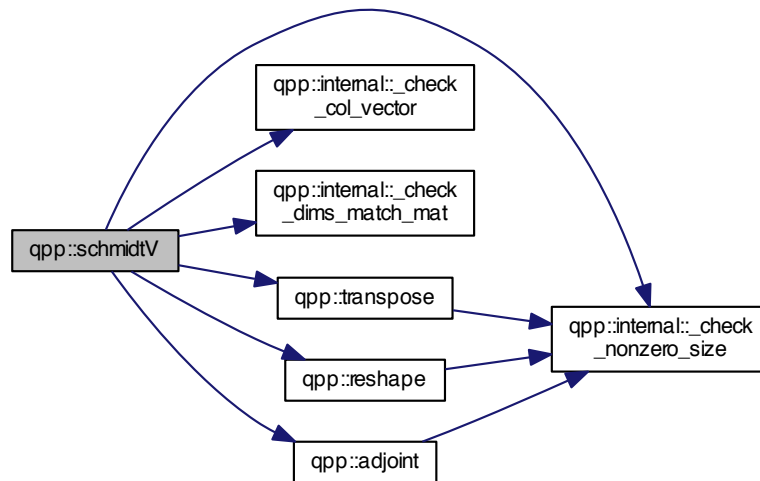
Parameters

<i>A</i>	Eigen expression
<i>dims</i>	Subsystems' dimensions

Returns

Unitary matrix V representing the Schmidt basis on Bob's side, as a dynamic matrix over the complex field, acting on the computational basis as $V|j\rangle = |\bar{j}\rangle$ (Schmidt vector)

Here is the call graph for this function:



6.1.2.90 `template<typename Derived> double qpp::shannon (const Eigen::MatrixBase< Derived > & A)`

Shannon/von-Neumann entropy of the probability distribution/density matrix A .

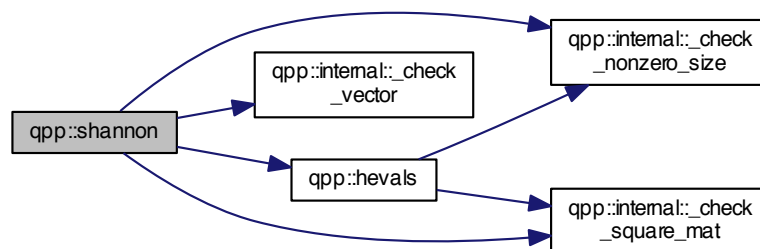
Parameters

A	Eigen expression, representing a probability distribution (dynamic column vector) or a density matrix (dynamic matrix over the complex field)
-----	---

Returns

Shannon/von-Neumann entropy, with the logarithm in base 2

Here is the call graph for this function:



6.1.2.91 `template<typename Derived> cmat qpp::sinm (const Eigen::MatrixBase< Derived> & A)`

Matrix sin.

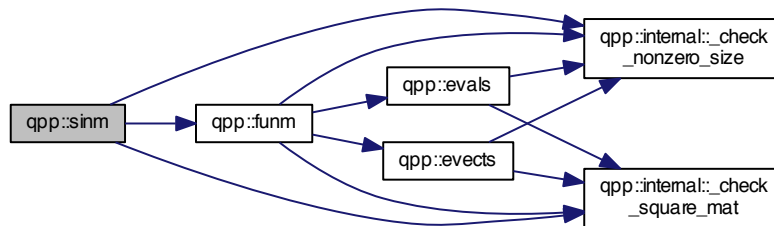
Parameters

<code>A</code>	Eigen expression
----------------	------------------

Returns

Matrix sine of A , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.92 `template<typename Derived> cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived> & A, const cplx z)`

Matrix power.

Uses the spectral decomposition of A to compute the matrix power

By convention $A^0 = I$

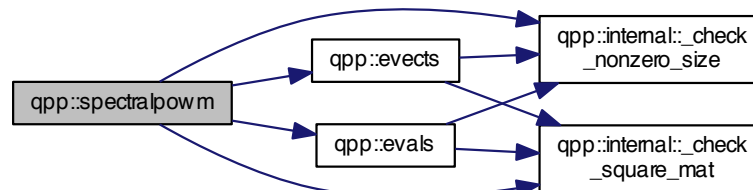
Parameters

<code>A</code>	Eigen expression
<code>z</code>	Complex number

Returns

Matrix power A^z , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.93 `template<typename Derived > cmat qpp::sqrtm (const Eigen::MatrixBase< Derived > & A)`

Matrix square root.

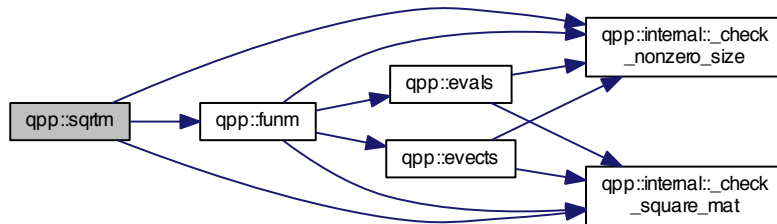
Parameters

A	Eigen expression
-----	------------------

Returns

Matrix square root of A , as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.94 `template<typename Derived > Derived::Scalar qpp::sum (const Eigen::MatrixBase< Derived > & A)`

Element-wise sum.

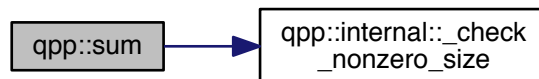
Parameters

A	Eigen expression
-----	------------------

Returns

Element-wise sum of A , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.95 `cmat qpp::super (const std::vector< cmat > & Ks)`

Superoperator matrix representation.

Constructs the superoperator matrix of the channel specified by the set of Kraus operators K_s in the standard operator basis $\{|i\rangle\langle j|\}$ ordered in lexicographical order, i.e. $|0\rangle\langle 0|$, $|0\rangle\langle 1|$ etc.

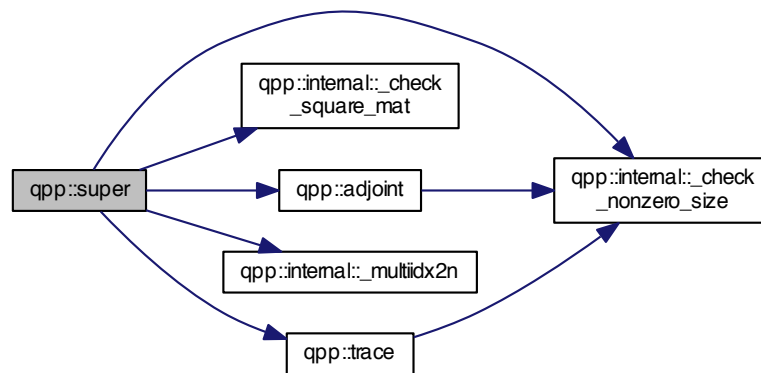
Parameters

<i>Ks</i>	std::vector of Eigen expressions representing the set of Kraus operators
-----------	--

Returns

Superoperator matrix representation, as a dynamic matrix over the complex field

Here is the call graph for this function:



6.1.2.96 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::syspermute (const Eigen::MatrixBase<Derived> & A, const std::vector< std::size_t > & perm, const std::vector< std::size_t > & dims)`

System permutation.

Permutes the subsystems in a state vector or density matrix

The qubit *perm*[*i*] is permuted to the location *i*

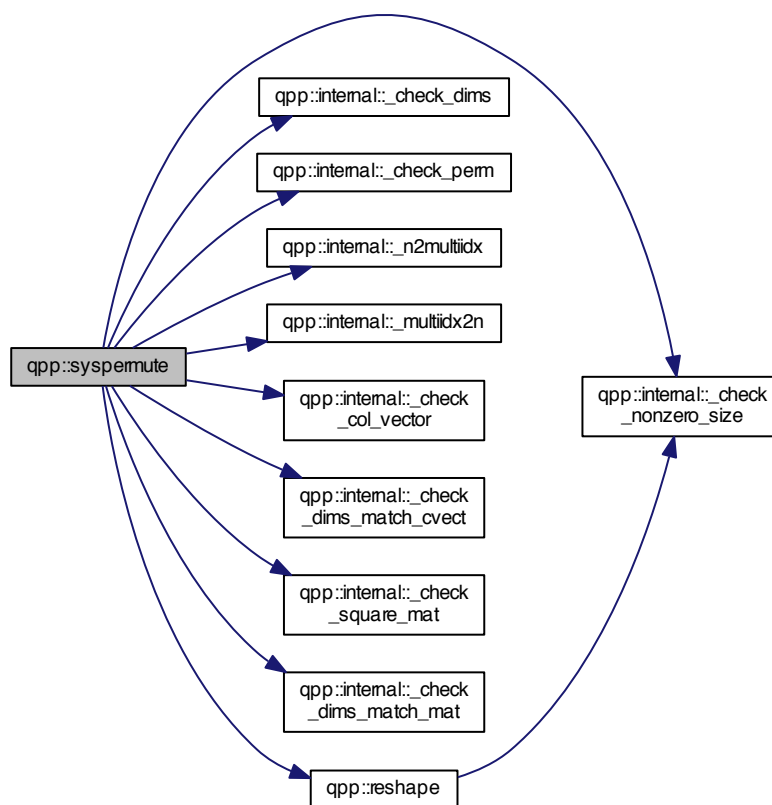
Parameters

<i>A</i>	Eigen expression
<i>perm</i>	Permutation
<i>dims</i>	Subsystems' dimensions

Returns

Permuted system, as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.97 `template<typename Derived> Derived::Scalar qpp::trace (const Eigen::MatrixBase< Derived> & A)`

Trace.

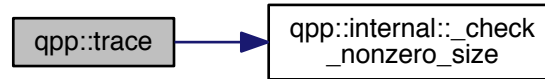
Parameters

A	Eigen expression
---	------------------

Returns

Trace of A , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.98 `template<typename Derived> DynMat<typename Derived::Scalar> qpp::transpose (const Eigen::MatrixBase<Derived> & A)`

Transpose.

Parameters

A	Eigen expression
-----	------------------

Returns

Transpose of A , as a dynamic matrix over the same scalar field

Here is the call graph for this function:



6.1.2.99 `template<typename Derived> double qpp::tsallis (const double alpha, const Eigen::MatrixBase<Derived> & A)`

Tsallis- α entropy of the probability distribution/density matrix A .

Note

$\alpha \geq 0$ When $\alpha \rightarrow 1$ the Tsallis entropy converges to the Shannon/von-Neumann entropy, with the logarithm in base e

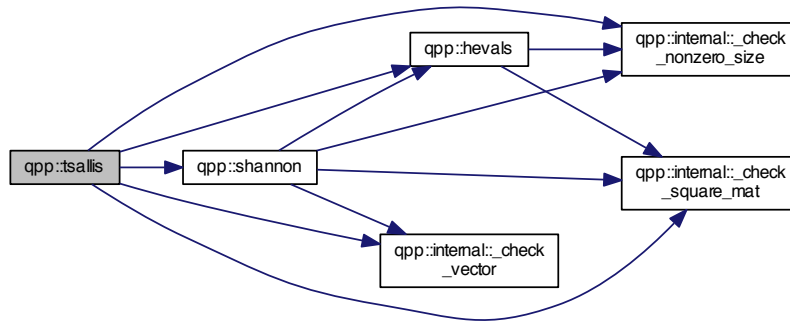
Parameters

A	Eigen expression, representing a probability distribution (dynamic column vector) or a density matrix (dynamic matrix over the complex field)
---	---

Returns

Renyi- α entropy, with the logarithm in base 2

Here is the call graph for this function:



6.1.3 Variable Documentation

6.1.3.1 constexpr double qpp::chop = 1e-10

Used in [qpp::disp\(\)](#) and [qpp::displn\(\)](#) for setting to zero numbers that have their absolute value smaller than $qpp::ct::chop$.

6.1.3.2 constexpr double qpp::ee = 2.718281828459045235360287471352662497

Base of natural logarithm, e .

6.1.3.3 constexpr double qpp::eps = 1e-12

Used to decide whether a number or expression in double precision is zero or not.

Example:

```
if(std::abs(x) < qpp::ct::eps) // x is zero
```

6.1.3.4 const Gates& qpp::gt = Gates::get_instance()

[qpp::Gates](#) const [Singleton](#)

Initializes the gates, see the class [qpp::Gates](#)

6.1.3.5 constexpr std::size_t qpp::maxn = 64

Maximum number of qubits.

Used internally to statically allocate arrays (for speed reasons)

6.1.3.6 constexpr double qpp::pi = 3.141592653589793238462643383279502884

π

6.1.3.7 RandomDevices& qpp::rdevs = RandomDevices::get_instance()

[qpp::RandomDevices](#) Singleton

Initializes the random devices, see the class [qpp::RandomDevices](#)

6.1.3.8 const States& qpp::st = States::get_instance()

[qpp::States](#) const Singleton

Initializes the states, see the class [qpp::States](#)

6.2 qpp::internal Namespace Reference

Functions

- void [_n2multiidx](#) (std::size_t n, std::size_t numdims, const std::size_t *dims, std::size_t *result)
- std::size_t [_multiidx2n](#) (const std::size_t *midx, std::size_t numdims, const std::size_t *dims)
- template<typename Derived >
bool [_check_square_mat](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [_check_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [_check_row_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [_check_col_vector](#) (const Eigen::MatrixBase< Derived > &A)
- template<typename T >
bool [_check_nonzero_size](#) (const T &x)
- bool [_check_dims](#) (const std::vector< std::size_t > &dims)
- template<typename Derived >
bool [_check_dims_match_mat](#) (const std::vector< std::size_t > &dims, const Eigen::MatrixBase< Derived > &A)
- template<typename Derived >
bool [_check_dims_match_cvect](#) (const std::vector< std::size_t > &dims, const Eigen::MatrixBase< Derived > &V)
- template<typename Derived >
bool [_check_dims_match_rvect](#) (const std::vector< std::size_t > &dims, const Eigen::MatrixBase< Derived > &V)
- bool [_check_eq_dims](#) (const std::vector< std::size_t > &dims, std::size_t dim)
- bool [_check_subsys_match_dims](#) (const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)
- bool [_check_perm](#) (const std::vector< std::size_t > &perm)
- template<typename Derived1 , typename Derived2 >
[DynMat](#)< typename Derived1::Scalar > [_kron2](#) (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)
- template<typename T >
void [variadic_vector_emplace](#) (std::vector< T > &)
- template<typename T , typename First , typename... Args>
void [variadic_vector_emplace](#) (std::vector< T > &v, First &&first, Args &&...args)

6.2.1 Detailed Description

Internal functions, do not modify or use them directly

6.2.2 Function Documentation

6.2.2.1 `template<typename Derived > bool qpp::internal::_check_col_vector (const Eigen::MatrixBase< Derived > & A)`

6.2.2.2 `bool qpp::internal::_check_dims (const std::vector< std::size_t > & dims)`

6.2.2.3 `template<typename Derived > bool qpp::internal::_check_dims_match_cvect (const std::vector< std::size_t > & dims, const Eigen::MatrixBase< Derived > & V)`

6.2.2.4 `template<typename Derived > bool qpp::internal::_check_dims_match_mat (const std::vector< std::size_t > & dims, const Eigen::MatrixBase< Derived > & A)`

6.2.2.5 `template<typename Derived > bool qpp::internal::_check_dims_match_rvect (const std::vector< std::size_t > & dims, const Eigen::MatrixBase< Derived > & V)`

6.2.2.6 `bool qpp::internal::_check_eq_dims (const std::vector< std::size_t > & dims, std::size_t dim)`

6.2.2.7 `template<typename T > bool qpp::internal::_check_nonzero_size (const T & x)`

6.2.2.8 `bool qpp::internal::_check_perm (const std::vector< std::size_t > & perm)`

6.2.2.9 `template<typename Derived > bool qpp::internal::_check_row_vector (const Eigen::MatrixBase< Derived > & A)`

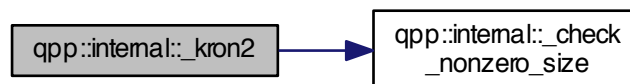
6.2.2.10 `template<typename Derived > bool qpp::internal::_check_square_mat (const Eigen::MatrixBase< Derived > & A)`

6.2.2.11 `bool qpp::internal::_check_subsys_match_dims (const std::vector< std::size_t > & subsys, const std::vector< std::size_t > & dims)`

6.2.2.12 `template<typename Derived > bool qpp::internal::_check_vector (const Eigen::MatrixBase< Derived > & A)`

6.2.2.13 `template<typename Derived1, typename Derived2 > DynMat<typename Derived1::Scalar> qpp::internal::_kron2 (const Eigen::MatrixBase< Derived1 > & A, const Eigen::MatrixBase< Derived2 > & B)`

Here is the call graph for this function:



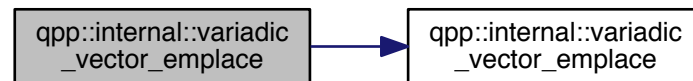
6.2.2.14 `std::size_t qpp::internal::_multiidx2n (const std::size_t * midx, std::size_t numdims, const std::size_t * dims)`

6.2.2.15 `void qpp::internal::_n2multiidx (std::size_t n, std::size_t numdims, const std::size_t * dims, std::size_t * result)`

6.2.2.16 `template<typename T> void qpp::internal::variadic_vector_emplace (std::vector< T> &)`

6.2.2.17 `template<typename T, typename First, typename... Args> void qpp::internal::variadic_vector_emplace (std::vector< T> & v, First && first, Args &&... args)`

Here is the call graph for this function:



Chapter 7

Class Documentation

7.1 qpp::DiscreteDistribution Class Reference

```
#include <stat.h>
```

Public Member Functions

- `template<typename InputIterator >`
`DiscreteDistribution` (InputIterator first, InputIterator last)
- `DiscreteDistribution` (std::initializer_list< double > weights)
- `DiscreteDistribution` (std::vector< double > weights)
- `std::size_t sample` ()
- `std::vector< double > probabilities` () const

Protected Attributes

- `std::discrete_distribution`
< std::size_t > `_d`

7.1.1 Constructor & Destructor Documentation

7.1.1.1 `template<typename InputIterator > qpp::DiscreteDistribution::DiscreteDistribution (InputIterator first, InputIterator last)` [inline]

7.1.1.2 `qpp::DiscreteDistribution::DiscreteDistribution (std::initializer_list< double > weights)` [inline]

7.1.1.3 `qpp::DiscreteDistribution::DiscreteDistribution (std::vector< double > weights)` [inline]

7.1.2 Member Function Documentation

7.1.2.1 `std::vector<double> qpp::DiscreteDistribution::probabilities () const` [inline]

7.1.2.2 `std::size_t qpp::DiscreteDistribution::sample ()` `[inline]`

Here is the call graph for this function:



7.1.3 Member Data Documentation

7.1.3.1 `std::discrete_distribution<std::size_t> qpp::DiscreteDistribution::_d` `[protected]`

The documentation for this class was generated from the following file:

- `include/classes/stat.h`

7.2 `qpp::DiscreteDistributionAbsSquare` Class Reference

```
#include <stat.h>
```

Public Member Functions

- `template<typename InputIterator >`
`DiscreteDistributionAbsSquare` (`InputIterator first`, `InputIterator last`)
- `DiscreteDistributionAbsSquare` (`std::initializer_list< cplx > amplitudes`)
- `DiscreteDistributionAbsSquare` (`std::vector< cplx > amplitudes`)
- `template<typename Derived >`
`DiscreteDistributionAbsSquare` (`const Eigen::MatrixBase< Derived > &V`)
- `std::size_t sample ()`
- `std::vector< double > probabilities () const`

Protected Member Functions

- `template<typename InputIterator >`
`std::vector< double > cplx2weights` (`InputIterator first`, `InputIterator last`) `const`

Protected Attributes

- `std::discrete_distribution`
`< std::size_t > _d`

7.2.1 Constructor & Destructor Documentation

7.2.1.1 `template<typename InputIterator > qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare (InputIterator first, InputIterator last) [inline]`

7.2.1.2 `qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare (std::initializer_list< cplx > amplitudes) [inline]`

7.2.1.3 `qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare (std::vector< cplx > amplitudes) [inline]`

7.2.1.4 `template<typename Derived > qpp::DiscreteDistributionAbsSquare::DiscreteDistributionAbsSquare (const Eigen::MatrixBase< Derived > & V) [inline]`

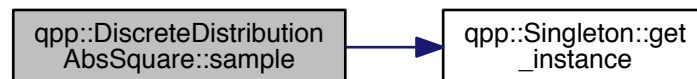
7.2.2 Member Function Documentation

7.2.2.1 `template<typename InputIterator > std::vector<double> qpp::DiscreteDistributionAbsSquare::cplx2weights (InputIterator first, InputIterator last) const [inline], [protected]`

7.2.2.2 `std::vector<double> qpp::DiscreteDistributionAbsSquare::probabilities () const [inline]`

7.2.2.3 `std::size_t qpp::DiscreteDistributionAbsSquare::sample () [inline]`

Here is the call graph for this function:



7.2.3 Member Data Documentation

7.2.3.1 `std::discrete_distribution<std::size_t> qpp::DiscreteDistributionAbsSquare::_d [protected]`

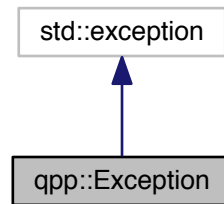
The documentation for this class was generated from the following file:

- [include/classes/stat.h](#)

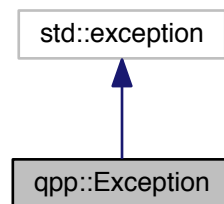
7.3 qpp::Exception Class Reference

```
#include <exception.h>
```

Inheritance diagram for qpp::Exception:



Collaboration diagram for qpp::Exception:



Public Types

- enum `Type` {
`Type::UNKNOWN_EXCEPTION = 1`, `Type::ZERO_SIZE`, `Type::MATRIX_NOT_SQUARE`, `Type::MATRIX_NOT_CVECTOR`,
`Type::MATRIX_NOT_RVECTOR`, `Type::MATRIX_NOT_VECTOR`, `Type::MATRIX_NOT_SQUARE_OR_CVECTOR`,
`Type::MATRIX_NOT_SQUARE_OR_RVECTOR`, `Type::MATRIX_NOT_SQUARE_OR_VECTOR`, `Type::DIMS_INVALID`, `Type::DIMS_NOT_EQUAL`, `Type::DIMS_MISMATCH_MATRIX`,
`Type::DIMS_MISMATCH_CVECTOR`, `Type::DIMS_MISMATCH_RVECTOR`, `Type::DIMS_MISMATCH_VECTOR`,
`Type::SUBSYS_MISMATCH_DIMS`, `Type::PERM_INVALID`, `Type::NOT_QUBIT_GATE`, `Type::NOT_QUBIT_SUBSYS`, `Type::NOT_BIPARTITE`,
`Type::OUT_OF_RANGE`, `Type::TYPE_MISMATCH`, `Type::UNDEFINED_TYPE`, `Type::CUSTOM_EXCEPTION` }

Public Member Functions

- `Exception` (const std::string &where, const `Type` &type)
- `Exception` (const std::string &where, const std::string &custom)
- virtual const char * `what` () const noexcept override

Private Member Functions

- `std::string _construct_exception_msg ()`

Private Attributes

- `std::string _where`
- `std::string _msg`
- `Type _type`
- `std::string _custom`

7.3.1 Member Enumeration Documentation

7.3.1.1 enum `qpp::Exception::Type` [strong]

Enumerator

- UNKNOWN_EXCEPTION** Unknown exception
- ZERO_SIZE** Zero sized object, e.g. empty `Eigen::Matrix` or `std::vector` with no elements
- MATRIX_NOT_SQUARE** `Eigen::Matrix` is not square
- MATRIX_NOT_CVECTOR** `Eigen::Matrix` is not a column vector
- MATRIX_NOT_RVECTOR** `Eigen::Matrix` is not a row vector
- MATRIX_NOT_VECTOR** `Eigen::Matrix` is not a row/column vector
- MATRIX_NOT_SQUARE_OR_CVECTOR** `Eigen::Matrix` is not square nor a column vector
- MATRIX_NOT_SQUARE_OR_RVECTOR** `Eigen::Matrix` is not square nor a row vector
- MATRIX_NOT_SQUARE_OR_VECTOR** `Eigen::Matrix` is not square nor a row/column vector
- DIMS_INVALID** `std::vector<std::size_t>` representing the dimensions has zero size or contains zeros
- DIMS_NOT_EQUAL** `std::vector<std::size_t>` representing the dimensions contains non-equal elements
- DIMS_MISMATCH_MATRIX** Product of the dimensions' `std::vector<std::size_t>` is not equal to the number of rows of `Eigen::Matrix` (assumed to be square)
- DIMS_MISMATCH_CVECTOR** Product of the dimensions' `std::vector<std::size_t>` is not equal to the number of cols of `Eigen::Matrix` (assumed to be a column vector)
- DIMS_MISMATCH_RVECTOR** Product of the dimensions' `std::vector<std::size_t>` is not equal to the number of cols of `Eigen::Matrix` (assumed to be a row vector)
- DIMS_MISMATCH_VECTOR** Product of the dimensions' `std::vector<std::size_t>` is not equal to the number of cols of `Eigen::Matrix` (assumed to be a row/column vector)
- SUBSYS_MISMATCH_DIMS** `std::vector<std::size_t>` representing the subsystems' labels has duplicates, or has entries that are larger than the size of the `std::vector<std::size_t>` representing the dimensions
- PERM_INVALID** Invalid `std::vector<std::size_t>` permutation
- NOT_QUBIT_GATE** `Eigen::Matrix` is not 2 x 2
- NOT_QUBIT_SUBSYS** Subsystems are not 2-dimensional
- NOT_BIPARTITE** `std::vector<std::size_t>` representing the dimensions has size different from 2
- OUT_OF_RANGE** Parameter out of range
- TYPE_MISMATCH** Types do not match (i.e. `Matrix<double>` vs `Matrix<cplx>`)
- UNDEFINED_TYPE** Templated function not defined for this type
- CUSTOM_EXCEPTION** Custom exception, user must provide a custom message

7.3.2 Constructor & Destructor Documentation

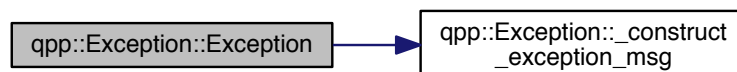
7.3.2.1 `qpp::Exception::Exception (const std::string & where, const Type & type)` `[inline]`

Here is the call graph for this function:



7.3.2.2 `qpp::Exception::Exception (const std::string & where, const std::string & custom)` `[inline]`

Here is the call graph for this function:



7.3.3 Member Function Documentation

7.3.3.1 `std::string qpp::Exception::_construct_exception_msg ()` `[inline]`, `[private]`

7.3.3.2 `virtual const char* qpp::Exception::what () const` `[inline]`, `[override]`, `[virtual]`, `[noexcept]`

7.3.4 Member Data Documentation

7.3.4.1 `std::string qpp::Exception::_custom` `[private]`

7.3.4.2 `std::string qpp::Exception::_msg` `[private]`

7.3.4.3 `Type qpp::Exception::_type` `[private]`

7.3.4.4 `std::string qpp::Exception::_where` `[private]`

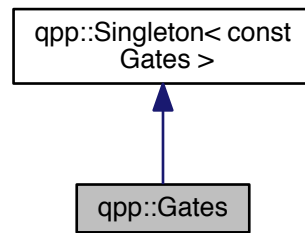
The documentation for this class was generated from the following file:

- [include/classes/exception.h](#)

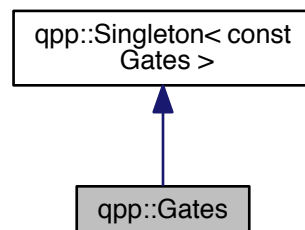
7.4 `qpp::Gates` Class Reference

```
#include <gates.h>
```

Inheritance diagram for qpp::Gates:



Collaboration diagram for qpp::Gates:



Public Member Functions

- [cmat Rn](#) (double theta, std::vector< double > n) const
- [cmat Zd](#) (std::size_t D) const
- [cmat Fd](#) (std::size_t D) const
- [cmat Xd](#) (std::size_t D) const
- template<typename Derived = Eigen::MatrixXcd>
Derived [ld](#) (std::size_t D) const
- template<typename Derived1 , typename Derived2 >
[DynMat](#)< typename Derived1::Scalar > [applyCTRL](#) (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size_t > &ctrl, const std::vector< std::size_t > &subsys, std::size_t n, std::size_t d=2) const
- template<typename Derived1 , typename Derived2 >
[DynMat](#)< typename Derived1::Scalar > [apply](#) (const Eigen::MatrixBase< Derived1 > &state, const Eigen::MatrixBase< Derived2 > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims) const
- template<typename Derived >
[DynMat](#)< typename Derived::Scalar > [CTRL](#) (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &ctrl, const std::vector< std::size_t > &subsys, std::size_t n, std::size_t d=2) const

Public Attributes

- [cmat Id2](#) { cmat::Identity(2, 2) }
- [cmat H](#) { cmat::Zero(2, 2) }
- [cmat X](#) { cmat::Zero(2, 2) }
- [cmat Y](#) { cmat::Zero(2, 2) }
- [cmat Z](#) { cmat::Zero(2, 2) }
- [cmat S](#) { cmat::Zero(2, 2) }
- [cmat T](#) { cmat::Zero(2, 2) }
- [cmat CNOTab](#) { cmat::Identity(4, 4) }
- [cmat CZ](#) { cmat::Identity(4, 4) }
- [cmat CNOTba](#) { cmat::Zero(4, 4) }
- [cmat SWAP](#) { cmat::Identity(4, 4) }
- [cmat TOF](#) { cmat::Identity(8, 8) }
- [cmat FRED](#) { cmat::Identity(8, 8) }

Private Member Functions

- [Gates](#) ()

Friends

- class [Singleton](#)< const [Gates](#) >

Additional Inherited Members

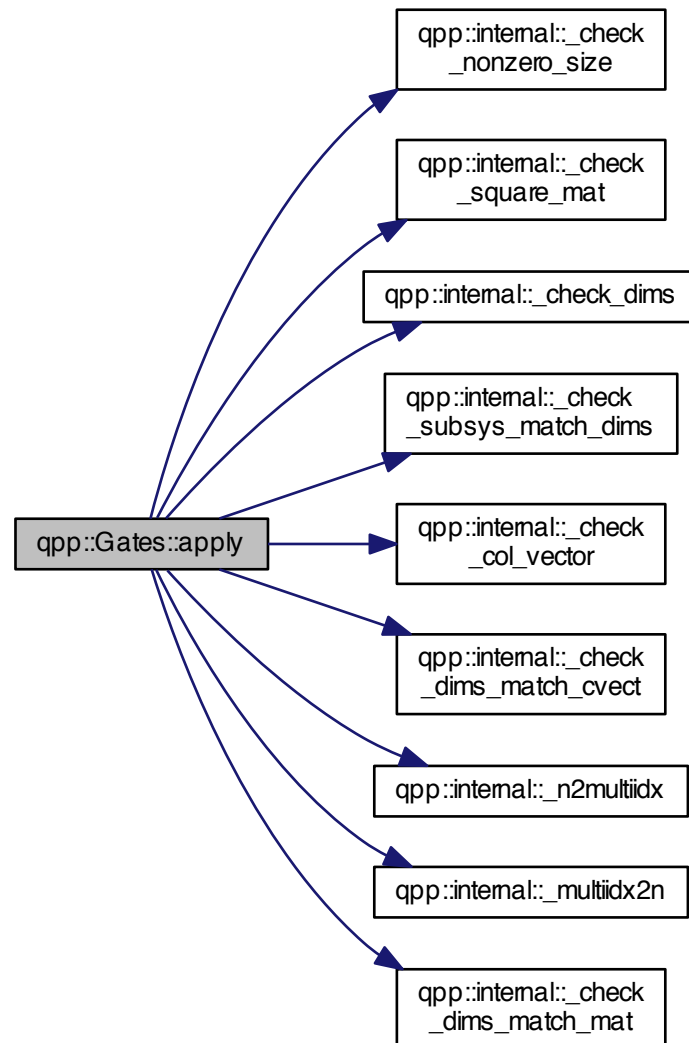
7.4.1 Constructor & Destructor Documentation

7.4.1.1 `qpp::Gates::Gates () [inline], [private]`

7.4.2 Member Function Documentation

7.4.2.1 `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::Gates::apply
(const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector<
std::size_t > & subsys, const std::vector< std::size_t > & dims) const [inline]`

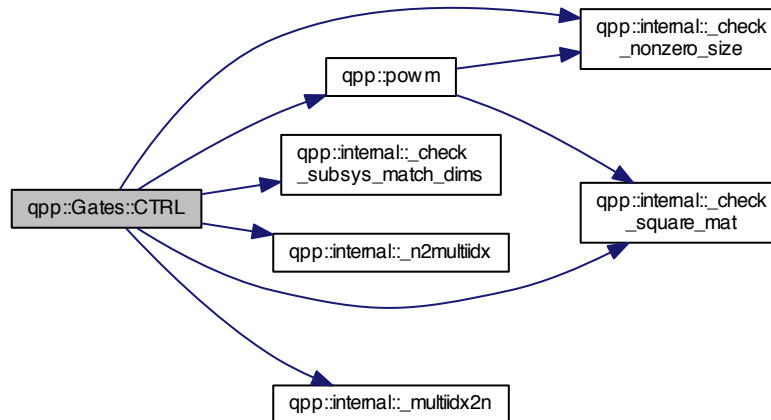
Here is the call graph for this function:



7.4.2.2 `template<typename Derived1 , typename Derived2 > DynMat<typename Derived1::Scalar> qpp::Gates::applyCTRL
(const Eigen::MatrixBase< Derived1 > & state, const Eigen::MatrixBase< Derived2 > & A, const std::vector<
std::size_t > & ctrl, const std::vector< std::size_t > & subsys, std::size_t n, std::size_t d=2) const [inline]`

7.4.2.3 `template<typename Derived > DynMat<typename Derived::Scalar> qpp::Gates::CTRL (const Eigen::MatrixBase<Derived > & A, const std::vector< std::size_t > & ctrl, const std::vector< std::size_t > & subsys, std::size_t n, std::size_t d = 2) const [inline]`

Here is the call graph for this function:



7.4.2.4 `cmat qpp::Gates::Fd (std::size_t D) const [inline]`

Here is the call graph for this function:



7.4.2.5 `template<typename Derived = Eigen::MatrixXcd> Derived qpp::Gates::Id (std::size_t D) const [inline]`

7.4.2.6 `cmat qpp::Gates::Rn (double theta, std::vector< double > n) const [inline]`

7.4.2.7 `cmat qpp::Gates::Xd (std::size_t D) const [inline]`

Here is the call graph for this function:



7.4.2.8 `cmat qpp::Gates::Zd (std::size_t D) const [inline]`

Here is the call graph for this function:



7.4.3 Friends And Related Function Documentation

7.4.3.1 `friend class Singleton< const Gates > [friend]`

7.4.4 Member Data Documentation

7.4.4.1 `cmat qpp::Gates::CNOTab { cmat::Identity(4, 4) }`

7.4.4.2 `cmat qpp::Gates::CNOTba { cmat::Zero(4, 4) }`

7.4.4.3 `cmat qpp::Gates::CZ { cmat::Identity(4, 4) }`

7.4.4.4 `cmat qpp::Gates::FRED { cmat::Identity(8, 8) }`

7.4.4.5 `cmat qpp::Gates::H { cmat::Zero(2, 2) }`

7.4.4.6 `cmat qpp::Gates::Id2 { cmat::Identity(2, 2) }`

7.4.4.7 `cmat qpp::Gates::S { cmat::Zero(2, 2) }`

7.4.4.8 `cmat qpp::Gates::SWAP { cmat::Identity(4, 4) }`

7.4.4.9 `cmat qpp::Gates::T { cmat::Zero(2, 2) }`

7.4.4.10 `cmat qpp::Gates::TOF { cmat::Identity(8, 8) }`

7.4.4.11 `cmat qpp::Gates::X { cmat::Zero(2, 2) }`

7.4.4.12 `cmat qpp::Gates::Y { cmat::Zero(2, 2) }`

7.4.4.13 `cmat qpp::Gates::Z { cmat::Zero(2, 2) }`

The documentation for this class was generated from the following file:

- [include/classes/gates.h](#)

7.5 qpp::NormalDistribution Class Reference

```
#include <stat.h>
```

Public Member Functions

- [NormalDistribution](#) (double mean=0, double sigma=1)
- double [sample](#) ()

Protected Attributes

- `std::normal_distribution _d`

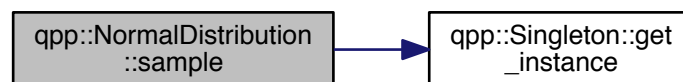
7.5.1 Constructor & Destructor Documentation

7.5.1.1 `qpp::NormalDistribution::NormalDistribution (double mean = 0, double sigma = 1)` `[inline]`

7.5.2 Member Function Documentation

7.5.2.1 `double qpp::NormalDistribution::sample ()` `[inline]`

Here is the call graph for this function:



7.5.3 Member Data Documentation

7.5.3.1 `std::normal_distribution qpp::NormalDistribution::_d` `[protected]`

The documentation for this class was generated from the following file:

- [include/classes/stat.h](#)

7.6 qpp::Qudit Class Reference

```
#include <qudit.h>
```

Public Member Functions

- [Qudit](#) (const [cmat](#) &rho=[States::get_instance\(\)](#).pz0)
- [std::size_t measure](#) (const [cmat](#) &U, bool destructive=false)
- [std::size_t measure](#) (bool destructive=false)
- [cmat getRho](#) () const
- [std::size_t getD](#) () const

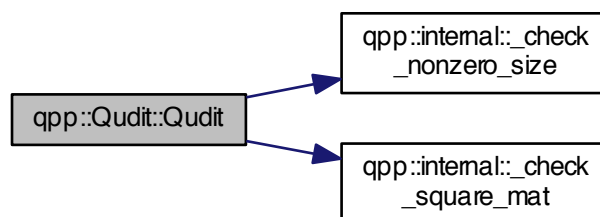
Private Attributes

- [cmat _rho](#)
- [std::size_t _D](#)

7.6.1 Constructor & Destructor Documentation

7.6.1.1 `qpp::Qudit::Qudit (const cmat & rho = States::get_instance() .pz0) [inline]`

Here is the call graph for this function:



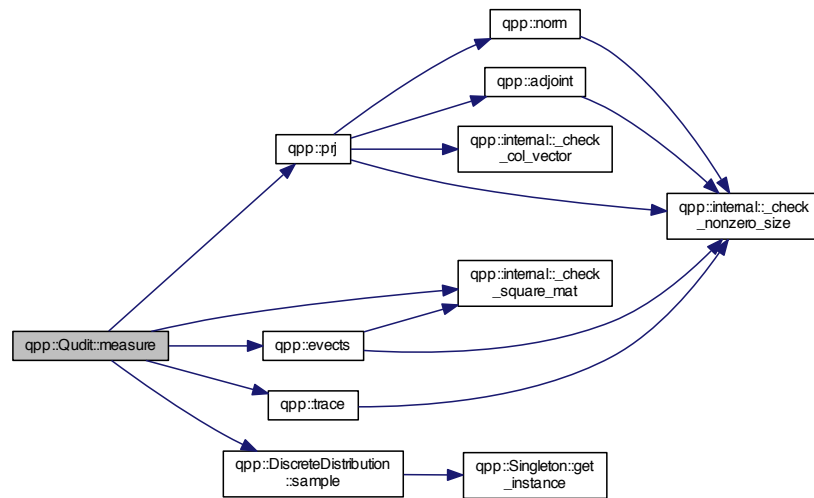
7.6.2 Member Function Documentation

7.6.2.1 `std::size_t qpp::Qudit::getD () const [inline]`

7.6.2.2 `cmat qpp::Qudit::getRho () const [inline]`

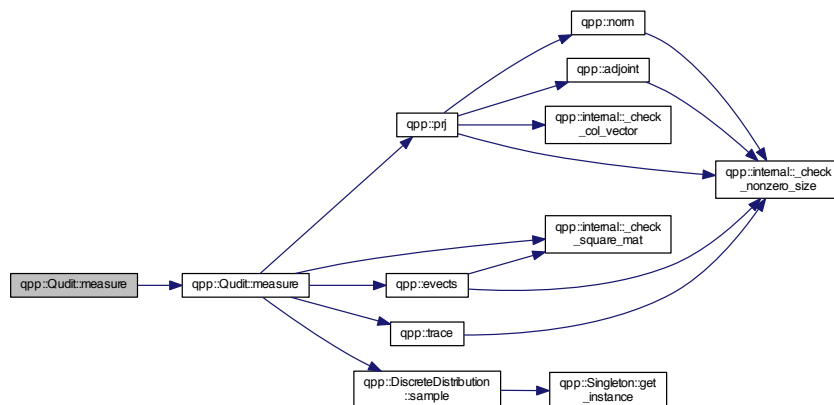
7.6.2.3 `std::size_t qpp::Qudit::measure (const cmat & U, bool destructive = false) [inline]`

Here is the call graph for this function:



7.6.2.4 `std::size_t qpp::Qudit::measure (bool destructive = false) [inline]`

Here is the call graph for this function:



7.6.3 Member Data Documentation

7.6.3.1 `std::size_t qpp::Qudit::_D [private]`

7.6.3.2 `cmat qpp::Qudit::_rho [private]`

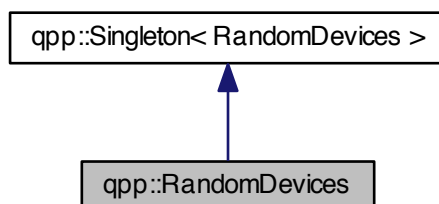
The documentation for this class was generated from the following file:

- [include/classes/qudit.h](#)

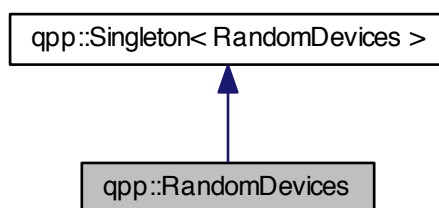
7.7 qpp::RandomDevices Class Reference

```
#include <randevs.h>
```

Inheritance diagram for qpp::RandomDevices:



Collaboration diagram for qpp::RandomDevices:



Public Attributes

- `std::mt19937 _rng`

Private Member Functions

- `RandomDevices ()`

Private Attributes

- `std::random_device _rd`

Friends

- class `Singleton< RandomDevices >`

Additional Inherited Members

7.7.1 Constructor & Destructor Documentation

7.7.1.1 `qpp::RandomDevices::RandomDevices ()` `[inline],[private]`

7.7.2 Friends And Related Function Documentation

7.7.2.1 `friend class Singleton< RandomDevices >` `[friend]`

7.7.3 Member Data Documentation

7.7.3.1 `std::random_device qpp::RandomDevices::_rd` `[private]`

7.7.3.2 `std::mt19937 qpp::RandomDevices::_rng`

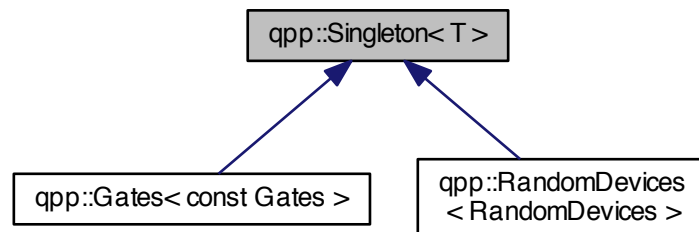
The documentation for this class was generated from the following file:

- `include/classes/randevs.h`

7.8 `qpp::Singleton< T >` Class Template Reference

```
#include <singleton.h>
```

Inheritance diagram for `qpp::Singleton< T >`:



Static Public Member Functions

- static `T & get_instance ()`

Protected Member Functions

- `Singleton ()=default`
- virtual `~Singleton ()`
- `Singleton (const Singleton &)=delete`
- `Singleton & operator= (const Singleton &)=delete`

7.8.1 Constructor & Destructor Documentation

7.8.1.1 `template<typename T> qpp::Singleton< T >::Singleton ()` [protected],[default]

7.8.1.2 `template<typename T> virtual qpp::Singleton< T >::~~Singleton ()` [inline],[protected],[virtual]

7.8.1.3 `template<typename T> qpp::Singleton< T >::Singleton (const Singleton< T > &)` [protected],[delete]

7.8.2 Member Function Documentation

7.8.2.1 `template<typename T> static T& qpp::Singleton< T >::get_instance ()` [inline],[static]

7.8.2.2 `template<typename T> Singleton& qpp::Singleton< T >::operator= (const Singleton< T > &)` [protected],[delete]

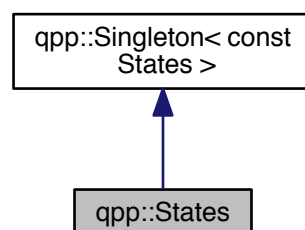
The documentation for this class was generated from the following file:

- [include/classes/singleton.h](#)

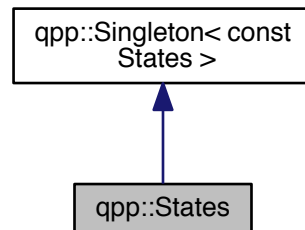
7.9 qpp::States Class Reference

```
#include <states.h>
```

Inheritance diagram for qpp::States:



Collaboration diagram for qpp::States:



Public Attributes

- [ket x0](#) { ket::Zero(2) }
- [ket x1](#) { ket::Zero(2) }
- [ket y0](#) { ket::Zero(2) }
- [ket y1](#) { ket::Zero(2) }
- [ket z0](#) { ket::Zero(2) }
- [ket z1](#) { ket::Zero(2) }
- [cmat px0](#) { cmat::Zero(2, 2) }
- [cmat px1](#) { cmat::Zero(2, 2) }
- [cmat py0](#) { cmat::Zero(2, 2) }
- [cmat py1](#) { cmat::Zero(2, 2) }
- [cmat pz0](#) { cmat::Zero(2, 2) }
- [cmat pz1](#) { cmat::Zero(2, 2) }
- [ket b00](#) { ket::Zero(4) }
- [ket b01](#) { ket::Zero(4) }
- [ket b10](#) { ket::Zero(4) }
- [ket b11](#) { ket::Zero(4) }
- [cmat pb00](#) { cmat::Zero(4, 4) }
- [cmat pb01](#) { cmat::Zero(4, 4) }
- [cmat pb10](#) { cmat::Zero(4, 4) }
- [cmat pb11](#) { cmat::Zero(4, 4) }
- [ket GHZ](#) { ket::Zero(8) }
- [ket W](#) { ket::Zero(8) }
- [cmat pGHZ](#) { cmat::Zero(8, 8) }
- [cmat pW](#) { cmat::Zero(8, 8) }

Private Member Functions

- [States](#) ()

Friends

- class [Singleton< const States >](#)

Additional Inherited Members

7.9.1 Constructor & Destructor Documentation

7.9.1.1 `qpp::States::States () [inline], [private]`

7.9.2 Friends And Related Function Documentation

7.9.2.1 `friend class Singleton< const States > [friend]`

7.9.3 Member Data Documentation

7.9.3.1 `ket qpp::States::b00 { ket::Zero(4) }`

7.9.3.2 `ket qpp::States::b01 { ket::Zero(4) }`

7.9.3.3 `ket qpp::States::b10 { ket::Zero(4) }`

7.9.3.4 `ket qpp::States::b11 { ket::Zero(4) }`

7.9.3.5 `ket qpp::States::GHZ { ket::Zero(8) }`

7.9.3.6 `cmat qpp::States::pb00 { cmat::Zero(4, 4) }`

7.9.3.7 `cmat qpp::States::pb01 { cmat::Zero(4, 4) }`

7.9.3.8 `cmat qpp::States::pb10 { cmat::Zero(4, 4) }`

7.9.3.9 `cmat qpp::States::pb11 { cmat::Zero(4, 4) }`

7.9.3.10 `cmat qpp::States::pGHZ { cmat::Zero(8, 8) }`

7.9.3.11 `cmat qpp::States::pW { cmat::Zero(8, 8) }`

7.9.3.12 `cmat qpp::States::px0 { cmat::Zero(2, 2) }`

7.9.3.13 `cmat qpp::States::px1 { cmat::Zero(2, 2) }`

7.9.3.14 `cmat qpp::States::py0 { cmat::Zero(2, 2) }`

7.9.3.15 `cmat qpp::States::py1 { cmat::Zero(2, 2) }`

7.9.3.16 `cmat qpp::States::pz0 { cmat::Zero(2, 2) }`

7.9.3.17 `cmat qpp::States::pz1 { cmat::Zero(2, 2) }`

7.9.3.18 `ket qpp::States::W { ket::Zero(8) }`

7.9.3.19 `ket qpp::States::x0 { ket::Zero(2) }`

7.9.3.20 `ket qpp::States::x1 { ket::Zero(2) }`

7.9.3.21 `ket qpp::States::y0 { ket::Zero(2) }`

7.9.3.22 `ket qpp::States::y1 { ket::Zero(2) }`

7.9.3.23 `ket qpp::States::z0 { ket::Zero(2) }`

7.9.3.24 `ket qpp::States::z1 { ket::Zero(2) }`

The documentation for this class was generated from the following file:

- [include/classes/states.h](#)

7.10 qpp::Timer Class Reference

```
#include <timer.h>
```

Public Member Functions

- [Timer](#) ()
- void [tic](#) ()
- void [toc](#) ()
- double [seconds](#) () const

Protected Attributes

- `std::chrono::steady_clock::time_point` [_start](#)
- `std::chrono::steady_clock::time_point` [_end](#)

Friends

- `std::ostream & operator<< (std::ostream &os, const Timer &rhs)`

7.10.1 Constructor & Destructor Documentation

7.10.1.1 `qpp::Timer::Timer ()` [[inline](#)]

7.10.2 Member Function Documentation

7.10.2.1 `double qpp::Timer::seconds ()` const [[inline](#)]

7.10.2.2 `void qpp::Timer::tic ()` [[inline](#)]

7.10.2.3 `void qpp::Timer::toc ()` [[inline](#)]

7.10.3 Friends And Related Function Documentation

7.10.3.1 `std::ostream& operator<< (std::ostream & os, const Timer & rhs)` [[friend](#)]

7.10.4 Member Data Documentation

7.10.4.1 `std::chrono::steady_clock::time_point` `qpp::Timer::_end` [[protected](#)]

7.10.4.2 `std::chrono::steady_clock::time_point` `qpp::Timer::_start` [[protected](#)]

The documentation for this class was generated from the following file:

- [include/classes/timer.h](#)

7.11 qpp::UniformIntDistribution Class Reference

```
#include <stat.h>
```

Public Member Functions

- [UniformIntDistribution](#) (int a=0, int b=1)
- int [sample](#) ()

Protected Attributes

- std::uniform_int_distribution [_d](#)

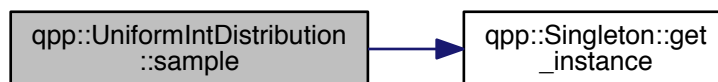
7.11.1 Constructor & Destructor Documentation

7.11.1.1 `qpp::UniformIntDistribution::UniformIntDistribution (int a = 0, int b = 1)` `[inline]`

7.11.2 Member Function Documentation

7.11.2.1 `int qpp::UniformIntDistribution::sample ()` `[inline]`

Here is the call graph for this function:



7.11.3 Member Data Documentation

7.11.3.1 `std::uniform_int_distribution qpp::UniformIntDistribution::_d` `[protected]`

The documentation for this class was generated from the following file:

- include/classes/[stat.h](#)

7.12 qpp::UniformRealDistribution Class Reference

```
#include <stat.h>
```

Public Member Functions

- [UniformRealDistribution](#) (double a=0, double b=1)
- double [sample](#) ()

Protected Attributes

- `std::uniform_real_distribution _d`

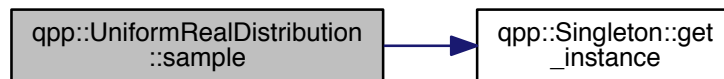
7.12.1 Constructor & Destructor Documentation

7.12.1.1 `qpp::UniformRealDistribution::UniformRealDistribution (double a = 0, double b = 1)` `[inline]`

7.12.2 Member Function Documentation

7.12.2.1 `double qpp::UniformRealDistribution::sample ()` `[inline]`

Here is the call graph for this function:



7.12.3 Member Data Documentation

7.12.3.1 `std::uniform_real_distribution qpp::UniformRealDistribution::_d` `[protected]`

The documentation for this class was generated from the following file:

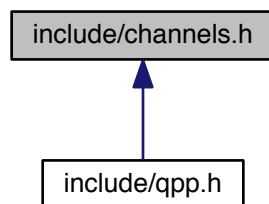
- `include/classes/stat.h`

Chapter 8

File Documentation

8.1 include/channels.h File Reference

This graph shows which files directly or indirectly include this file:



Namespaces

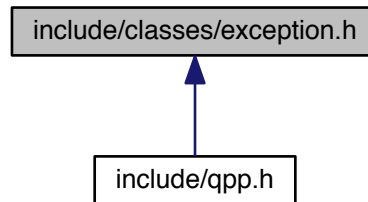
- [qpp](#)

Functions

- `cmat qpp::super (const std::vector< cmat > &Ks)`
Superoperator matrix representation.
- `cmat qpp::choi (const std::vector< cmat > &Ks)`
Choi matrix representation.
- `std::vector< cmat > qpp::choi2kraus (const cmat &A)`
Extracts orthogonal Kraus operators from Choi matrix.
- `template<typename Derived >`
`cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks)`
Applies the channel specified by the set of Kraus operators Ks to the density matrix rho.
- `template<typename Derived >`
`cmat qpp::channel (const Eigen::MatrixBase< Derived > &rho, const std::vector< cmat > &Ks, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`
Applies the channel specified by the set of Kraus operators Ks to the part of the density matrix rho specified by subsys.

8.2 include/classes/exception.h File Reference

This graph shows which files directly or indirectly include this file:



Classes

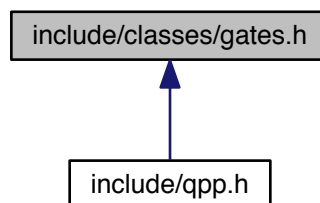
- class [qpp::Exception](#)

Namespaces

- [qpp](#)

8.3 include/classes/gates.h File Reference

This graph shows which files directly or indirectly include this file:



Classes

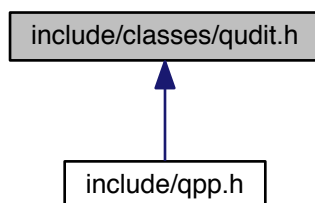
- class [qpp::Gates](#)

Namespaces

- [qpp](#)

8.4 include/classes/qudit.h File Reference

This graph shows which files directly or indirectly include this file:



Classes

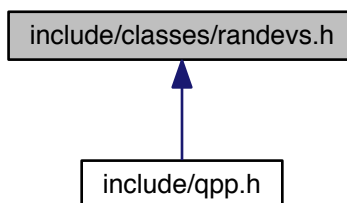
- class [qpp::Qudit](#)

Namespaces

- [qpp](#)

8.5 include/classes/randevs.h File Reference

This graph shows which files directly or indirectly include this file:



Classes

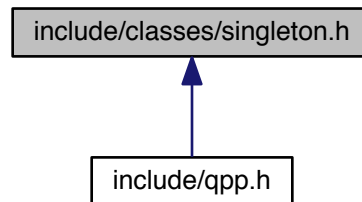
- class [qpp::RandomDevices](#)

Namespaces

- [qpp](#)

8.6 include/classes/singleton.h File Reference

This graph shows which files directly or indirectly include this file:



Classes

- class [qpp::Singleton< T >](#)

Namespaces

- [qpp](#)

Macros

- [#define CLASS_SINGLETON\(Foo\)](#)
- [#define CLASS_CONST_SINGLETON\(Foo\)](#)

8.6.1 Macro Definition Documentation

8.6.1.1 [#define CLASS_CONST_SINGLETON\(Foo \)](#)

Value:

```

class Foo: public Singleton<const Foo>\
{
    friend class Singleton<const Foo>;
}
  
```

8.6.1.2 [#define CLASS_SINGLETON\(Foo \)](#)

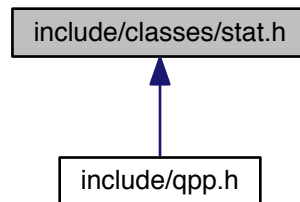
Value:

```

class Foo: public Singleton<Foo>\
{
    friend class Singleton<Foo>;
}
  
```

8.7 include/classes/stat.h File Reference

This graph shows which files directly or indirectly include this file:



Classes

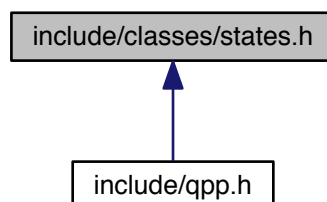
- class [qpp::NormalDistribution](#)
- class [qpp::UniformRealDistribution](#)
- class [qpp::UniformIntDistribution](#)
- class [qpp::DiscreteDistribution](#)
- class [qpp::DiscreteDistributionAbsSquare](#)

Namespaces

- [qpp](#)

8.8 include/classes/states.h File Reference

This graph shows which files directly or indirectly include this file:



Classes

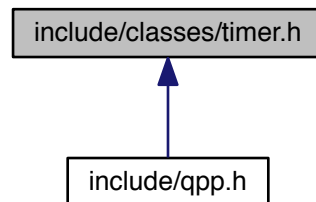
- class [qpp::States](#)

Namespaces

- [qpp](#)

8.9 include/classes/timer.h File Reference

This graph shows which files directly or indirectly include this file:



Classes

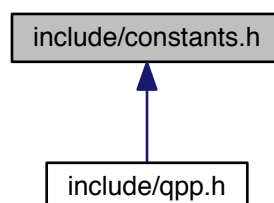
- class [qpp::Timer](#)

Namespaces

- [qpp](#)

8.10 include/constants.h File Reference

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)

Functions

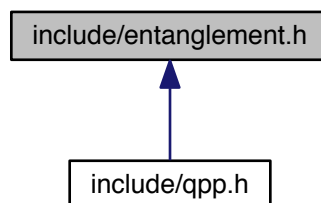
- constexpr std::complex< double > [qpp::operator""_i](#) (unsigned long long int x)
User-defined literal for complex $i = \sqrt{-1}$ (integer overload)
- constexpr std::complex< double > [qpp::operator""_i](#) (long double x)
User-defined literal for complex $i = \sqrt{-1}$ (real overload)
- std::complex< double > [qpp::omega](#) (std::size_t D)
D-th root of unity.

Variables

- constexpr double [qpp::chop](#) = 1e-10
Used in [qpp::disp\(\)](#) and [qpp::displn\(\)](#) for setting to zero numbers that have their absolute value smaller than [qpp::ct->::chop](#).
- constexpr double [qpp::eps](#) = 1e-12
Used to decide whether a number or expression in double precision is zero or not.
- constexpr std::size_t [qpp::maxn](#) = 64
Maximum number of qubits.
- constexpr double [qpp::pi](#) = 3.141592653589793238462643383279502884
 π
- constexpr double [qpp::ee](#) = 2.718281828459045235360287471352662497
Base of natural logarithm, e .

8.11 include/entanglement.h File Reference

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)

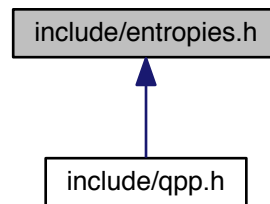
Functions

- template<typename Derived >
cmat [qpp::schmidtcoeff](#) (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)
Schmidt coefficients of the bi-partite pure state A.

- `template<typename Derived >`
`cmat qpp::schmidtU (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`
Schmidt basis on Alice's side.
- `template<typename Derived >`
`cmat qpp::schmidtV (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`
Schmidt basis on Bob's side.
- `template<typename Derived >`
`cmat qpp::schmidtprob (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`
Schmidt probabilities of the bi-partite pure state A.
- `template<typename Derived >`
`double qpp::entanglement (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`
Entanglement of the bi-partite pure state A.
- `template<typename Derived >`
`double qpp::gconcurrence (const Eigen::MatrixBase< Derived > &A)`
G-concurrence of the bi-partite pure state A.

8.12 include/entropies.h File Reference

This graph shows which files directly or indirectly include this file:



Namespaces

- `qpp`

Functions

- `template<typename Derived >`
`double qpp::shannon (const Eigen::MatrixBase< Derived > &A)`
Shannon/von-Neumann entropy of the probability distribution/density matrix A.
- `template<typename Derived >`
`double qpp::renyi (const double alpha, const Eigen::MatrixBase< Derived > &A)`
Renyi- α entropy of the probability distribution/density matrix A.
- `template<typename Derived >`
`double qpp::renyi_inf (const Eigen::MatrixBase< Derived > &A)`
Renyi- ∞ entropy (min entropy) of the probability distribution/density matrix A.
- `template<typename Derived >`
`double qpp::tsallis (const double alpha, const Eigen::MatrixBase< Derived > &A)`

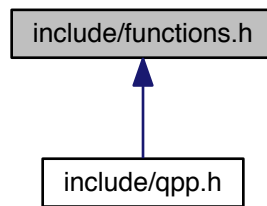
Tsallis- α entropy of the probability distribution/density matrix A .

- `template<typename Derived >`
`double qpp::qmutualinfo (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys,`
`const std::vector< std::size_t > &dims)`

Quantum mutual information between 2 subsystems of a composite system.

8.13 include/functions.h File Reference

This graph shows which files directly or indirectly include this file:



Namespaces

- `qpp`

Functions

- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::transpose (const Eigen::MatrixBase< Derived > &A)`
Transpose.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::conjugate (const Eigen::MatrixBase< Derived > &A)`
Complex conjugate.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::adjoint (const Eigen::MatrixBase< Derived > &A)`
Adjoint.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::inverse (const Eigen::MatrixBase< Derived > &A)`
Inverse.
- `template<typename Derived >`
`Derived::Scalar qpp::trace (const Eigen::MatrixBase< Derived > &A)`
Trace.
- `template<typename Derived >`
`Derived::Scalar qpp::det (const Eigen::MatrixBase< Derived > &A)`
Determinant.
- `template<typename Derived >`
`Derived::Scalar qpp::logdet (const Eigen::MatrixBase< Derived > &A)`
Logarithm of the determinant.

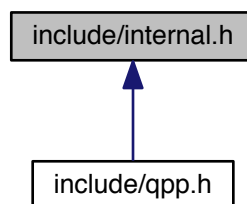
- `template<typename Derived >`
`Derived::Scalar qpp::sum (const Eigen::MatrixBase< Derived > &A)`
Element-wise sum.
- `template<typename Derived >`
`double qpp::norm (const Eigen::MatrixBase< Derived > &A)`
Trace norm.
- `template<typename Derived >`
`cmat qpp::evals (const Eigen::MatrixBase< Derived > &A)`
Eigenvalues.
- `template<typename Derived >`
`cmat qpp::evects (const Eigen::MatrixBase< Derived > &A)`
Eigenvectors.
- `template<typename Derived >`
`dmat qpp::hevals (const Eigen::MatrixBase< Derived > &A)`
Hermitian eigenvalues.
- `template<typename Derived >`
`cmat qpp::hevects (const Eigen::MatrixBase< Derived > &A)`
Hermitian eigenvectors.
- `template<typename Derived >`
`cmat qpp::funm (const Eigen::MatrixBase< Derived > &A, cplx(*f)(const cplx &))`
Functional calculus $f(A)$
- `template<typename Derived >`
`cmat qpp::sqrtm (const Eigen::MatrixBase< Derived > &A)`
Matrix square root.
- `template<typename Derived >`
`cmat qpp::absm (const Eigen::MatrixBase< Derived > &A)`
Matrix absolut value.
- `template<typename Derived >`
`cmat qpp::expm (const Eigen::MatrixBase< Derived > &A)`
Matrix exponential.
- `template<typename Derived >`
`cmat qpp::logm (const Eigen::MatrixBase< Derived > &A)`
Matrix logarithm.
- `template<typename Derived >`
`cmat qpp::sinm (const Eigen::MatrixBase< Derived > &A)`
Matrix sin.
- `template<typename Derived >`
`cmat qpp::cosm (const Eigen::MatrixBase< Derived > &A)`
Matrix cos.
- `template<typename Derived >`
`cmat qpp::spectralpowm (const Eigen::MatrixBase< Derived > &A, const cplx z)`
Matrix power.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::powm (const Eigen::MatrixBase< Derived > &A, std::size_t n)`
Matrix power.
- `template<typename OutputScalar, typename Derived >`
`DynMat< OutputScalar > qpp::cwise (const Eigen::MatrixBase< Derived > &A, OutputScalar(*f)(const type-
name Derived::Scalar &))`
Functor.
- `template<typename T >`
`DynMat< typename T::Scalar > qpp::kron (const T &head)`
Kronecker product (variadic overload)

- `template<typename T, typename... Args>`
`DynMat< typename T::Scalar > qpp::kron (const T &head, const Args &...tail)`
Kronecker product (variadic overload)
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::kron (const std::vector< Derived > &As)`
Kronecker product (std::vector overload)
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::kron (const std::initializer_list< Derived > &As)`
Kronecker product (std::initializer_list overload)
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::kronpow (const Eigen::MatrixBase< Derived > &A, std::size_t n)`
Kronecker power.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::reshape (const Eigen::MatrixBase< Derived > &A, std::size_t rows, std::size_t cols)`
Reshape.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::syspermute (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &perm, const std::vector< std::size_t > &dims)`
System permutation.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::ptrace1 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`
Partial trace.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::ptrace2 (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &dims)`
Partial trace.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::ptrace (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`
Partial trace.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::ptranspose (const Eigen::MatrixBase< Derived > &A, const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`
Partial transpose.
- `template<typename Derived1, typename Derived2 >`
`DynMat< typename Derived1::Scalar > qpp::comm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
Commutator.
- `template<typename Derived1, typename Derived2 >`
`DynMat< typename Derived1::Scalar > qpp::anticomm (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
Anti-commutator.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::prj (const Eigen::MatrixBase< Derived > &V)`
Projector.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::expandout (const Eigen::MatrixBase< Derived > &A, std::size_t pos, const std::vector< std::size_t > &dims)`
Expand out.
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::grams (const std::vector< Derived > &Vs)`

- Gram-Schmidt orthogonalization (std::vector overload)*
 - `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::grams (const std::initializer_list< Derived > &Vs)`
Gram-Schmidt orthogonalization (std::initializer_list overload)
 - `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::grams (const Eigen::MatrixBase< Derived > &A)`
Gram-Schmidt orthogonalization (Eigen expression (matrix) overload)
 - `std::vector< std::size_t > qpp::n2multiidx (std::size_t n, const std::vector< std::size_t > &dims)`
Non-negative integer index to multi-index.
 - `std::size_t qpp::multiidx2n (const std::vector< std::size_t > &midx, const std::vector< std::size_t > &dims)`
Multi-index to non-negative integer index.
 - `ket qpp::mket (const std::vector< std::size_t > &mask)`
Multi-partite qubit ket.
 - `ket qpp::mket (const std::vector< std::size_t > &mask, const std::vector< std::size_t > &dims)`
Multi-partite qudit ket (different dimensions overload)
 - `ket qpp::mket (const std::vector< std::size_t > &mask, std::size_t d)`
Multi-partite qudit ket (same dimensions overload)
 - `std::vector< std::size_t > qpp::invperm (const std::vector< std::size_t > &perm)`
Inverse permutation.
 - `std::vector< std::size_t > qpp::compperm (const std::vector< std::size_t > &perm, const std::vector< std::size_t > &sigma)`
Compose permutations.

8.14 include/internal.h File Reference

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp::internal](#)
- [qpp](#)

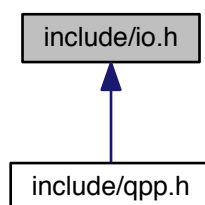
Functions

- `void qpp::internal::_n2multiidx (std::size_t n, std::size_t numdims, const std::size_t *dims, std::size_t *result)`
- `std::size_t qpp::internal::_multiidx2n (const std::size_t *midx, std::size_t numdims, const std::size_t *dims)`

- `template<typename Derived >`
`bool qpp::internal::_check_square_mat (const Eigen::MatrixBase< Derived > &A)`
- `template<typename Derived >`
`bool qpp::internal::_check_vector (const Eigen::MatrixBase< Derived > &A)`
- `template<typename Derived >`
`bool qpp::internal::_check_row_vector (const Eigen::MatrixBase< Derived > &A)`
- `template<typename Derived >`
`bool qpp::internal::_check_col_vector (const Eigen::MatrixBase< Derived > &A)`
- `template<typename T >`
`bool qpp::internal::_check_nonzero_size (const T &x)`
- `bool qpp::internal::_check_dims (const std::vector< std::size_t > &dims)`
- `template<typename Derived >`
`bool qpp::internal::_check_dims_match_mat (const std::vector< std::size_t > &dims, const Eigen::MatrixBase< Derived > &A)`
- `template<typename Derived >`
`bool qpp::internal::_check_dims_match_cvect (const std::vector< std::size_t > &dims, const Eigen::MatrixBase< Derived > &V)`
- `template<typename Derived >`
`bool qpp::internal::_check_dims_match_rvect (const std::vector< std::size_t > &dims, const Eigen::MatrixBase< Derived > &V)`
- `bool qpp::internal::_check_eq_dims (const std::vector< std::size_t > &dims, std::size_t dim)`
- `bool qpp::internal::_check_subsys_match_dims (const std::vector< std::size_t > &subsys, const std::vector< std::size_t > &dims)`
- `bool qpp::internal::_check_perm (const std::vector< std::size_t > &perm)`
- `template<typename Derived1 , typename Derived2 >`
`DynMat< typename Derived1::Scalar > qpp::internal::_kron2 (const Eigen::MatrixBase< Derived1 > &A, const Eigen::MatrixBase< Derived2 > &B)`
- `template<typename T >`
`void qpp::internal::variadic_vector_emplace (std::vector< T > &)`
- `template<typename T , typename First , typename... Args>`
`void qpp::internal::variadic_vector_emplace (std::vector< T > &v, First &&first, Args &&...args)`

8.15 include/io.h File Reference

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)

Functions

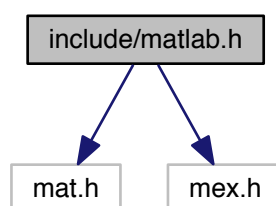
- `template<typename T >`
`void qpp::disp (const T &x, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)`
- `template<typename T >`
`void qpp::displn (const T &x, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)`
- `template<typename T >`
`void qpp::disp (const T *x, const std::size_t n, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)`
- `template<typename T >`
`void qpp::displn (const T *x, const std::size_t n, const std::string &separator, const std::string &start="[" , const std::string &end="]", std::ostream &os=std::cout)`
- `template<typename Derived >`
`void qpp::disp (const Eigen::MatrixBase< Derived > &A, double chop=chop, std::ostream &os=std::cout)`
- `template<typename Derived >`
`void qpp::displn (const Eigen::MatrixBase< Derived > &A, double chop=chop, std::ostream &os=std::cout)`
- `void qpp::disp (const cplx c, double chop=chop, std::ostream &os=std::cout)`
- `void qpp::displn (const cplx c, double chop=chop, std::ostream &os=std::cout)`
- `template<typename Derived >`
`void qpp::save (const Eigen::MatrixBase< Derived > &A, const std::string &fname)`
- `template<typename Derived >`
`DynMat< typename Derived::Scalar > qpp::load (const std::string &fname)`

8.16 include/matlab.h File Reference

```
#include "mat.h"
```

```
#include "mex.h"
```

Include dependency graph for matlab.h:



Namespaces

- [qpp](#)

Functions

- `template<typename Derived >`
`Derived qpp::loadMATLABmatrix (const std::string &mat_file, const std::string &var_name)`

- `template<>`
`dmat qpp::loadMATLABmatrix` (const std::string &mat_file, const std::string &var_name)
- `template<>`
`cmatrix qpp::loadMATLABmatrix` (const std::string &mat_file, const std::string &var_name)
- `template<typename Derived >`
`void qpp::saveMATLABmatrix` (const Eigen::MatrixBase< Derived > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)
- `template<>`
`void qpp::saveMATLABmatrix` (const Eigen::MatrixBase< dmat > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)
- `template<>`
`void qpp::saveMATLABmatrix` (const Eigen::MatrixBase< cmatrix > &A, const std::string &mat_file, const std::string &var_name, const std::string &mode)

8.17 include/qpp.h File Reference

```
#include <algorithm>
#include <chrono>
#include <cmath>
#include <complex>
#include <cstdlib>
#include <cstring>
#include <exception>
#include <fstream>
#include <functional>
#include <iomanip>
#include <iostream>
#include <iterator>
#include <numeric>
#include <ostream>
#include <random>
#include <stdexcept>
#include <string>
#include <type_traits>
#include <utility>
#include <vector>
#include <Eigen/Dense>
#include <Eigen/SVD>
#include "constants.h"
#include "types.h"
#include "classes/exception.h"
#include "classes/singleton.h"
#include "classes/states.h"
#include "classes/randevs.h"
#include "internal.h"
#include "functions.h"
#include "classes/gates.h"
#include "classes/stat.h"
#include "entropies.h"
#include "entanglement.h"
#include "channels.h"
#include "io.h"
#include "random.h"
#include "classes/qudit.h"
#include "classes/timer.h"
```

Include dependency graph for qpp.h:



Namespaces

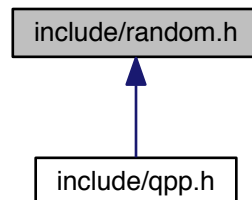
- [qpp](#)

Variables

- RandomDevices & [qpp::rdevs](#) = RandomDevices::get_instance()
[qpp::RandomDevices](#) *Singleton*
- const Gates & [qpp::gt](#) = Gates::get_instance()
[qpp::Gates](#) *const Singleton*
- const States & [qpp::st](#) = States::get_instance()
[qpp::States](#) *const Singleton*

8.18 include/random.h File Reference

This graph shows which files directly or indirectly include this file:



Namespaces

- [qpp](#)

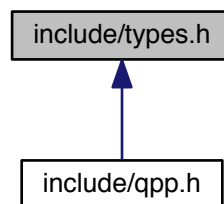
Functions

- template<typename Derived >
 Derived [qpp::rand](#) (std::size_t rows, std::size_t cols, double a=0, double b=1)
- template<>
 dmat [qpp::rand](#) (std::size_t rows, std::size_t cols, double a, double b)
- template<>
 cmat [qpp::rand](#) (std::size_t rows, std::size_t cols, double a, double b)
- double [qpp::rand](#) (double a=0, double b=1)
- long long [qpp::randint](#) (long long a, long long b)

- `template<typename Derived >`
Derived `qpp::randn` (`std::size_t` rows, `std::size_t` cols, double mean=0, double sigma=1)
- `template<>`
`dmat qpp::randn` (`std::size_t` rows, `std::size_t` cols, double mean, double sigma)
- `template<>`
`cmat qpp::randn` (`std::size_t` rows, `std::size_t` cols, double mean, double sigma)
- double `qpp::randn` (double mean=0, double sigma=1)
- `cmat qpp::randU` (`std::size_t` D)
- `cmat qpp::randV` (`std::size_t` Din, `std::size_t` Dout)
- `std::vector< cmat > qpp::randkraus` (`std::size_t` n, `std::size_t` D)
- `cmat qpp::randH` (`std::size_t` D)
- ket `qpp::randket` (`std::size_t` D)
- `cmat qpp::randrho` (`std::size_t` D)
- `std::vector< std::size_t > qpp::randperm` (`std::size_t` n)

8.19 include/types.h File Reference

This graph shows which files directly or indirectly include this file:



Namespaces

- `qpp`

Typedefs

- using `qpp::cplx` = `std::complex< double >`
Complex number in double precision.
- using `qpp::cmat` = `Eigen::MatrixXcd`
Complex (double precision) dynamic Eigen matrix.
- using `qpp::dmat` = `Eigen::MatrixXd`
Real (double precision) dynamic Eigen matrix.
- using `qpp::ket` = `Eigen::Matrix< cplx, Eigen::Dynamic, 1 >`
Complex (double precision) dynamic Eigen column matrix.
- using `qpp::bra` = `Eigen::Matrix< cplx, 1, Eigen::Dynamic >`
Complex (double precision) dynamic Eigen row matrix.
- `template<typename Scalar >`
using `qpp::DynMat` = `Eigen::Matrix< Scalar, Eigen::Dynamic, Eigen::Dynamic >`
Dynamic Eigen matrix over the field specified by Scalar.

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