



CS4379: Parallel and Concurrent Programming

CS5379: Parallel Processing

Lecture 19

Dr. Yong Chen

Associate Professor

Computer Science Department

Texas Tech University



Lecture Video

- Please view the lecture video either from Teams or from the below link:
- <https://texastechuniversity.sharepoint.com/sites/CS4379-CS5379/Shared%20Documents/General/Lecture19.mp4>



Course Info

- **Lecture Time:** TR, 12:30-1:50
- **Lecture Location:** ECE 217
- **Sessions:** CS4379-001, CS4379-002, CS5379-001, CS5379-D01
- **Instructor:** Yong Chen, Ph.D., Associate Professor
- **Email:** yong.chen@ttu.edu
- **Phone:** 806-834-0284
- **Office:** Engineering Center 315
- **Office Hours:** 2-4 p.m. on Wed., or by appointment
- **TA:** Mr. Ghazanfar Ali, Ghazanfar.Ali@ttu.edu
- **TA Office hours:** Tue. and Fri., 2-3 p.m., or by appointment
- **TA Office:** EC 201 A
- **More info:**
 - <http://www.myweb.ttu.edu/yonchen>
 - <http://discl.cs.ttu.edu>; <http://cac.ttu.edu/>; <http://nsfcac.org>

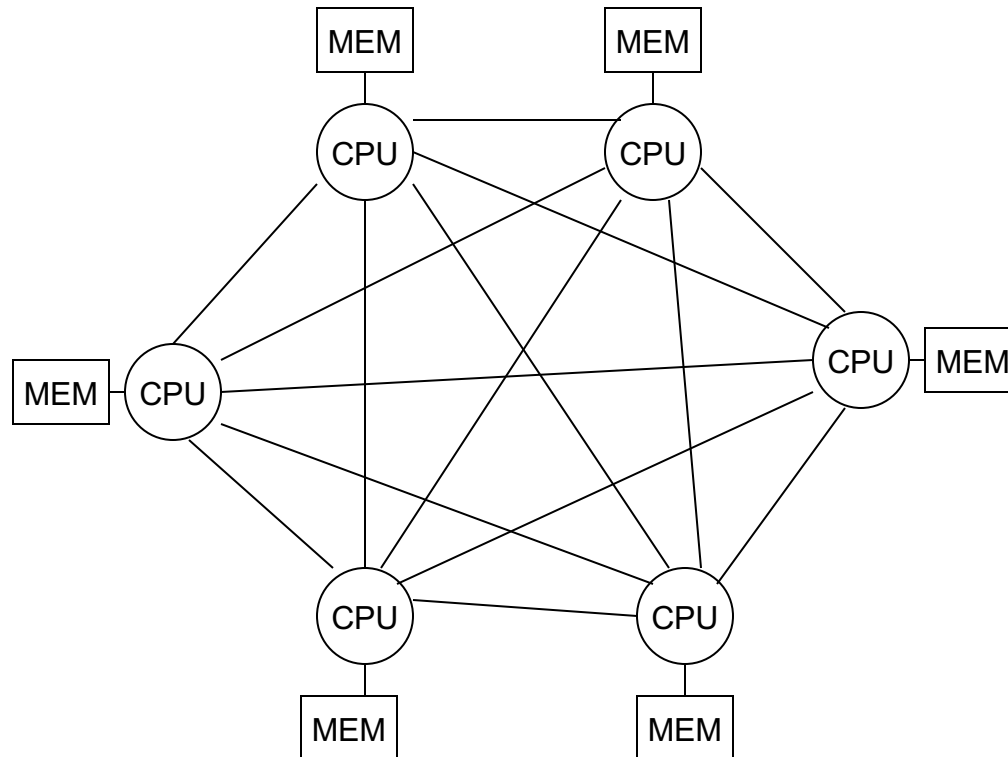


Outline

- Questions?
- Distributed-address-space architectures and message passing cost
- Basic communication operations
- One-to-all broadcast and All-to-One Reduction

Distributed-Address-Space Parallel Computers

- Each processor has its own local address space (“shared nothing”, no global/shared address space)
- Easy to scale up, most large-scale parallel computers, clusters
- Processors share/exchange data via explicit message passing





Message Passing Costs

- Communication is a major overhead in programming distributed-address-space machines

- The cost of communication is dependent on a variety of features
 - ❑ Programming model semantics
 - ❑ Network topology (e.g. 2-D mesh/torus, 3-D mesh/torus, hypercube, etc.; sometimes customized for supercomputers)
 - ❑ Data handling and routing
 - ❑ Associated software protocols



Message Passing Costs

- The total time to transfer a message over a network comprises of the following:
 - ❑ *Startup time (t_s)*: Time spent at sending and receiving nodes (adding header, trailer, executing the routing algorithm, etc.).
 - ❑ *Per-hop time (t_h)*: This time is a function of number of hops and includes factors such as switch latencies, network delays, etc.
 - ❑ *Per-word transfer time (t_w)*: This time includes all overheads that are determined by the length (or size) of the message. This includes bandwidth of links, buffering overheads, etc.



Store-and-Forward Routing

- A message traversing multiple hops is **completely received at an intermediate hop** before being forwarded to the next hop.

- The **total communication cost** for a message of size m words to traverse l communication links is

$$t_{comm} = t_s + (mt_w + t_h)l.$$

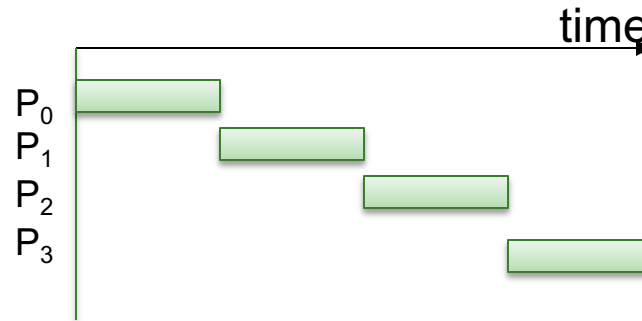
- In most platforms, t_h is small and the above expression can be approximated by

$$t_{comm} = t_s + mlt_w.$$

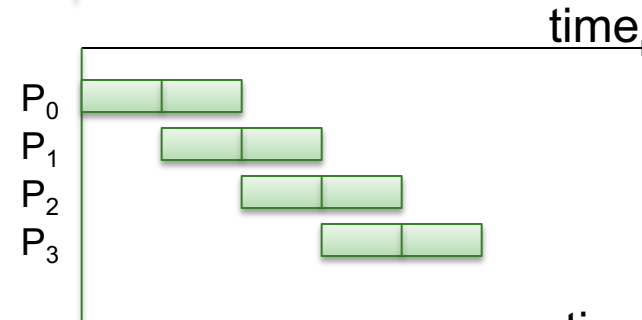


Packet Routing

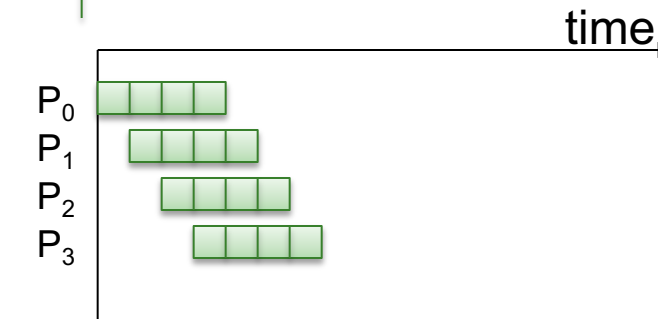
- Store-and-forward makes poor use of communication resources.
- Packet routing breaks messages into packets and pipelines them through the network.



(1) A single message sent over a store-and-forward network



(2) The same message broken into two parts and send over the network



(3) The same message broken into four parts and sent over the network



Cut-Through Routing

- Takes the concept of packet routing to an extreme by further dividing messages into basic units called flits (flow control digits).
- The total communication time for cut-through routing is approximated by:

$$t_{comm} = t_s + t_h l + t_w m.$$



Implications of Message Passing Cost Model

- To optimize the cost of message transfers
- **Communicate in bulk**
 - Instead of sending small messages and paying a startup cost t_s for each, we want to **aggregate small messages into a single large message** and amortize the startup latency across a larger message
 - This is because on typical platforms such as clusters and message-passing machines, the value of t_s is much larger than those of t_h or t_w .
- **Minimize the volume of data**
 - To reduce the overhead paid in terms of per-word transfer time t_w , it is desirable to reduce the volume of data transferred as much as possible.
- **Minimize the distance of data transfer**
 - Minimize the number of hops / that a message must traverse



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- One-to-all broadcast and All-to-One Reduction



Basic Communication Operations: Introduction

- Many communications in distributed-address-space machines occur in **well-defined patterns involving a group of processes**
- Efficient implementations of these operations can improve performance, reduce development effort and cost, and improve software quality
- Efficient implementations **must leverage underlying architecture**. For this reason, we refer to specific architectures here.
- We select a descriptive set of architectures to illustrate the process of algorithm design



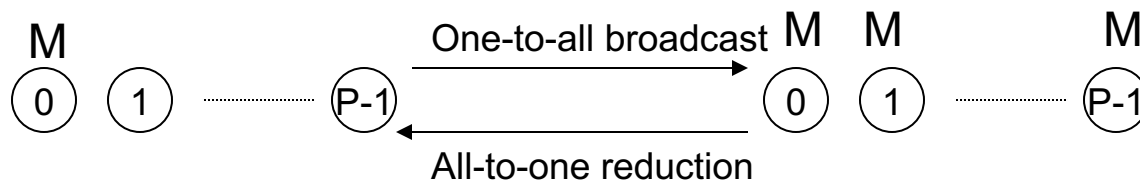
Basic Communication Operations: Introduction

- Group communication operations can be built using point-to-point messaging primitives
- Will use message passing cost model to analyze the cost
 - Store-and-Forward Routing $t_{comm} = t_s + (mt_w + t_h)l$.
 - Cut-Through Routing $t_{comm} = t_s + t_hl + t_wm$.



One-to-all Broadcast/All-to-one Reduction

- Algorithms often require a processor to send identical data to all other processors
- Called a **one-to-all broadcast** or **singlenode broadcast**
- At the start of a singlenode broadcast, one processor has m words of data that needs to be sent, at the end there are p copies of this data, one on each processor
- **All-to-one reduction** or **singlenode reduction (dual)**: at the start of singlenode reduction each process has m words of data, the reduction combines all the data from processors using an associative operator to produce m words at the receiver
- Naïve singlenode broadcast or reduction using $p-1$ steps

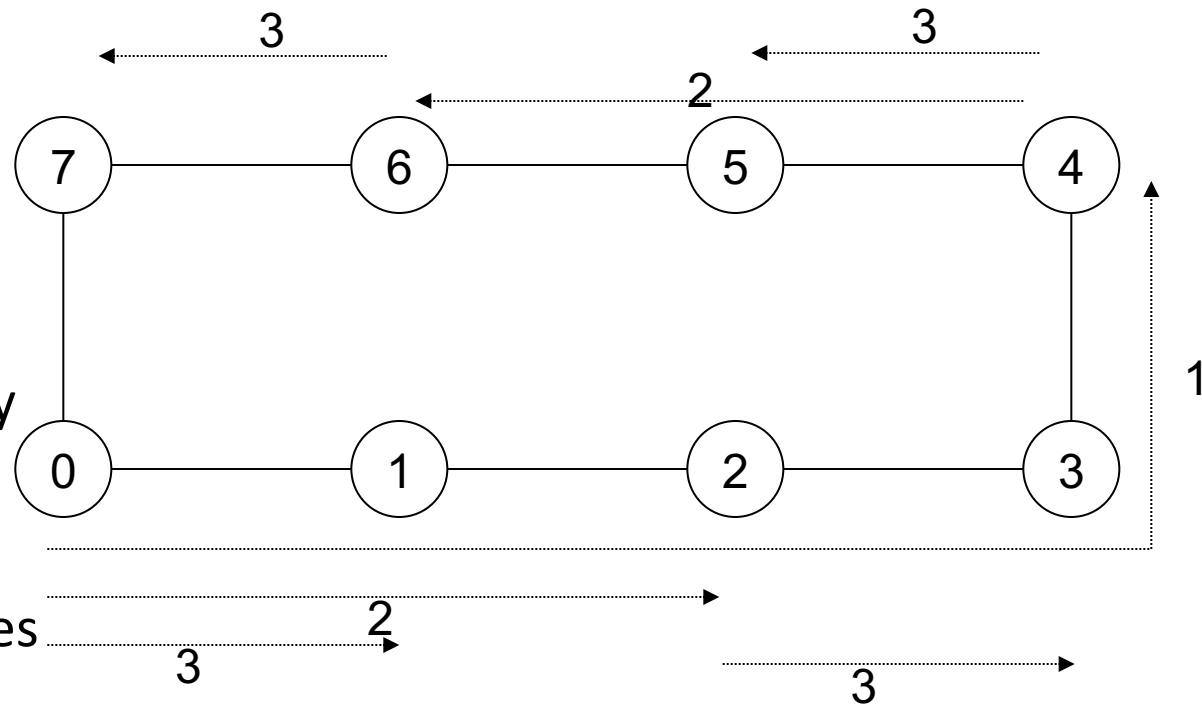




One-to-all Broadcast: CT Routing on Ring

- Use **recursive doubling**:

source sends a msg to a
selected process, and
both processes can
continue simultaneously
send msg



- Continue till all processes
receive data



One-to-all Broadcast: CT Routing on Ring

- Steps needed?
 - in $\log p$ steps

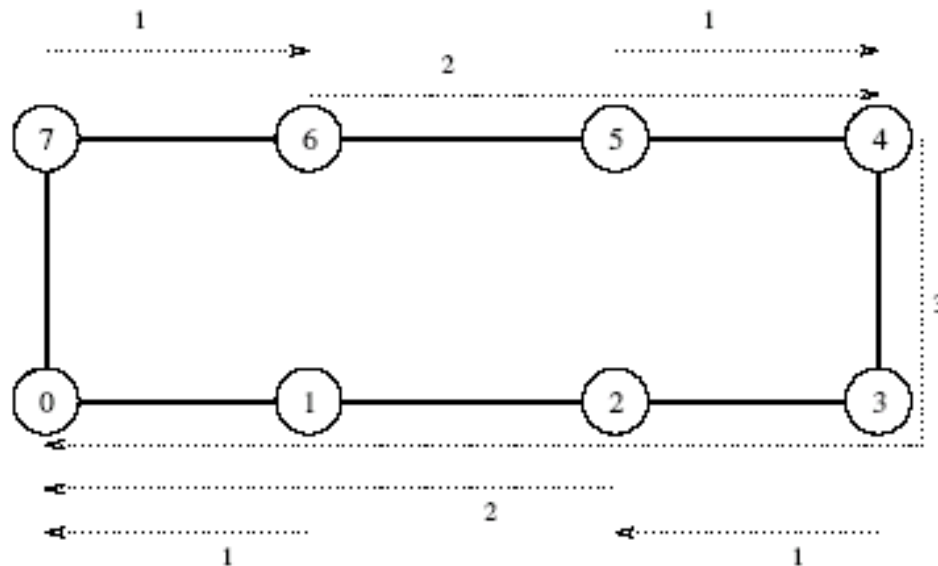
- In step i , message is sent to processor at a distance $\frac{p}{2^i}$
- All messages flow in the same direction
- Cost?

$$t_s \log(p) + t_w m \log(p) + t_h (p - 1)$$



All-to-One Reduction: CT Routing on Ring

- Reduction can be performed in an identical fashion by inverting the process

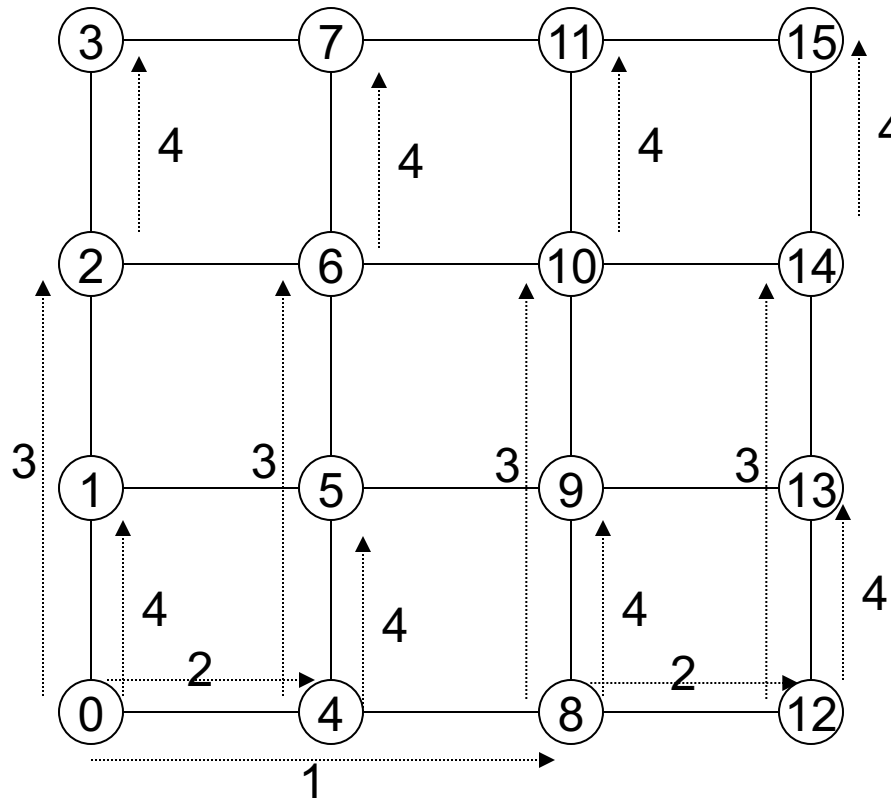


Reduction on an eight-node ring with node 0 as the destination of the reduction.



One-to-all Broadcast: CT Routing on 2d Torus

- Apply ring algorithm for the processor row of sender
- Now use ring algorithm for all processor column





One-to-all Broadcast: CT Routing on 2d Torus

- Steps?

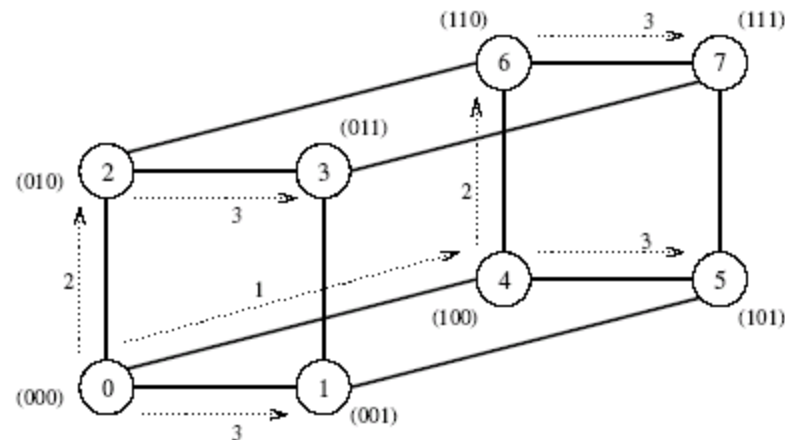
$$2\log(\sqrt{p}) = \log p$$

- Cost:?

$$(t_s + t_w m) \log(p) + 2t_h (\sqrt{p} - 1)$$

Broadcast and Reduction on a Hypercube

- A hypercube with 2^d nodes can be regarded as a d -dimensional mesh with two nodes in each dimension.
- The mesh algorithm can be generalized to a hypercube and the operation is carried out in $d (= \log p)$ steps.



One-to-all broadcast on a three-dimensional hypercube. The binary representations of node labels are shown in parentheses.



Broadcast and Reduction on a Hypercube

- Steps?

$$\log p$$

- Cost:?

$$(t_s + t_w m + t_h) \log p$$



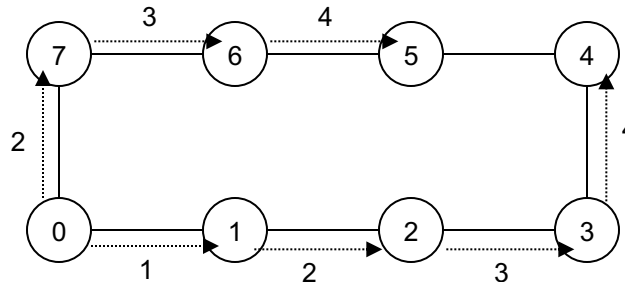
Broadcast and Reduction: **SF Routing on Ring**

- Steps?

$$\left\lceil \frac{p}{2} \right\rceil$$

- Cost?

$$(t_s + mt_w + t_h) \left\lceil \frac{p}{2} \right\rceil \quad \text{Or} \quad (t_s + t_w m) \left\lceil \frac{p}{2} \right\rceil \text{ if we ignore } t_h$$





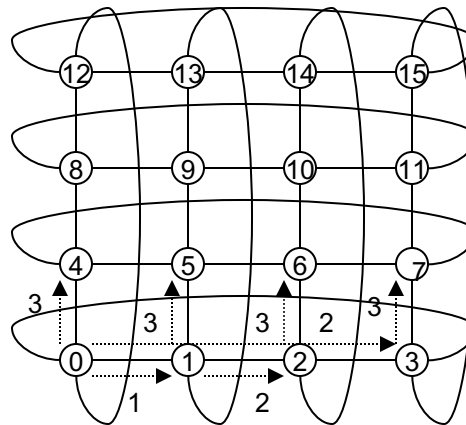
Broadcast and Reduction: **SF Routing on 2d Torus**

- Each row or column of the torus can be regarded as a ring
- Using ring method for the row to which the sending processor belongs; then use ring method for every column

- Steps? $2 \left\lceil \frac{\sqrt{p}}{2} \right\rceil$

- Cost?

$$2(t_s + mt_w + t_h) \left\lceil \frac{\sqrt{p}}{2} \right\rceil$$

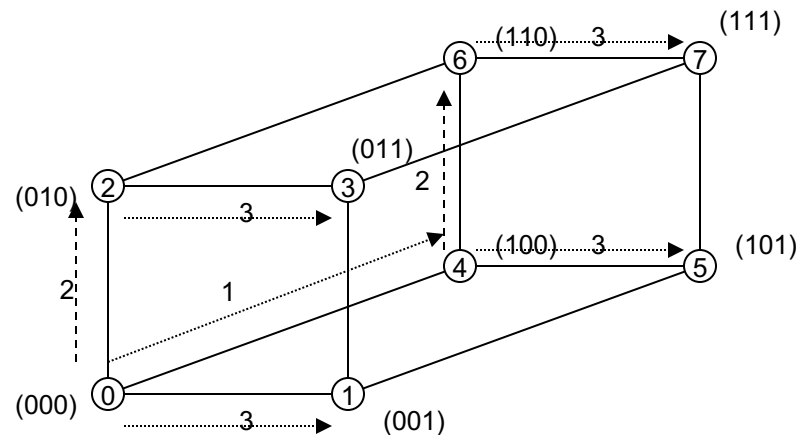




Broadcast and Reduction: SF Routing on Hypercube

- Takes $\log(p)$ steps for a p processor hypercube
- In the i th step, all processors that have the message transmit it to the neighboring processor that differs in the i th most significant bit
- Cost?

$$(t_s + mt_w + t_h)\log(p)$$



Reference book has pseudo-code/algorithm description



Readings

- Reference book ITPC – Chapter 2, 2.5.1; Chapter 4, 4.1
- Reference book has algorithm descriptions
 - One-to-all broadcast/All-to-one reduction on various architectures



Questions?

Questions/Suggestions/Comments are always welcome!

Write me: yong.chen@ttu.edu

Call me: 806-834-0284

See me: ENGCTR 315

If you write me an email for this class, please start the email subject with [CS4379] or [CS5379].