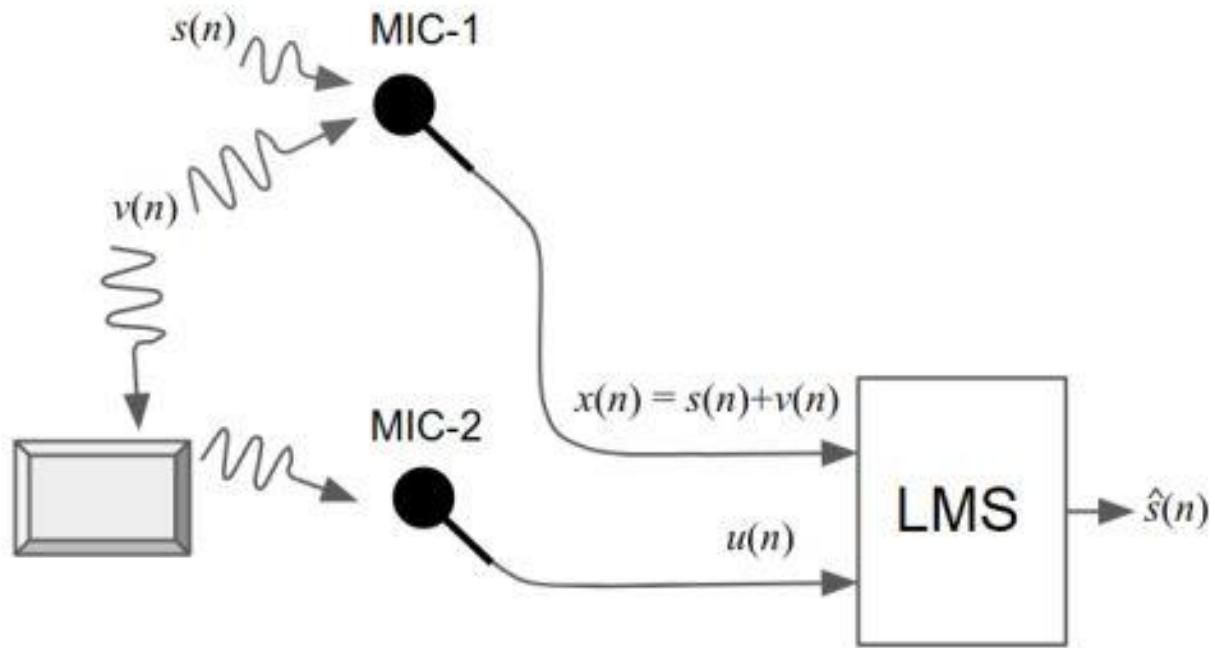
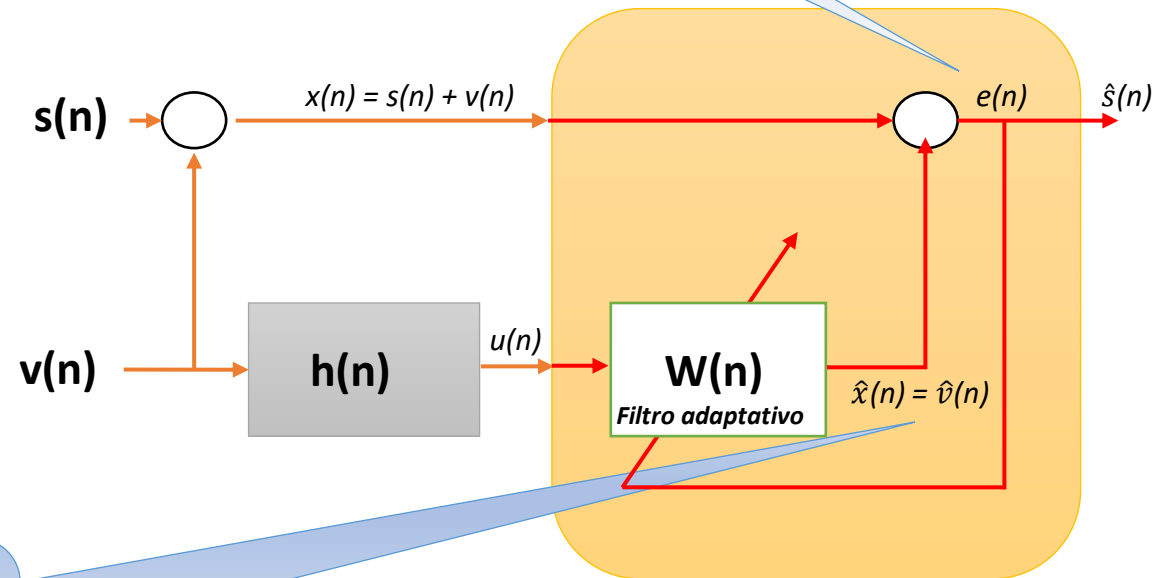


• Problema 1



El error es $x(n) - \hat{v}(n) = \hat{s}(n)$ de esa "resto" el ruido a mi señal estimando el ruido



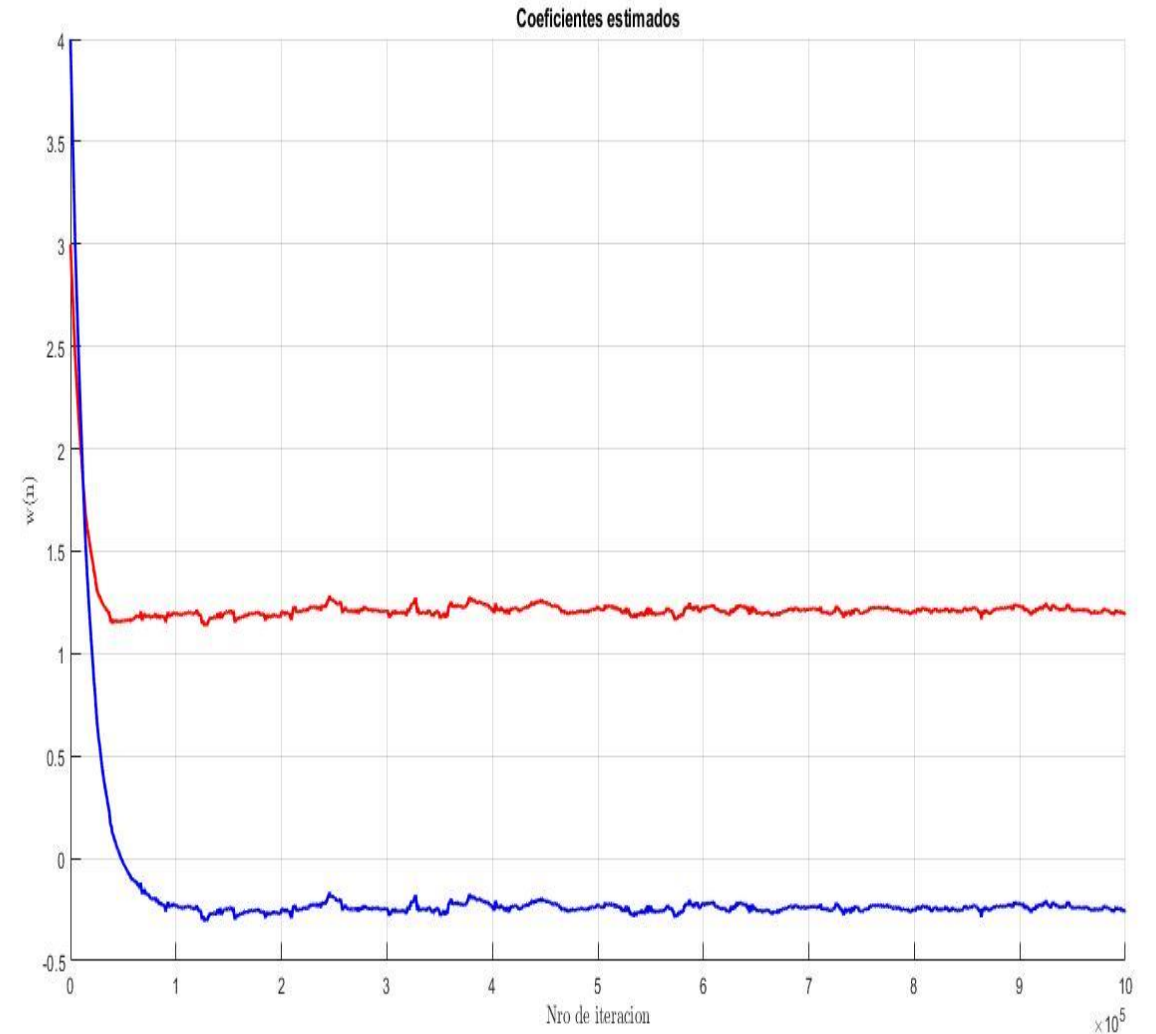
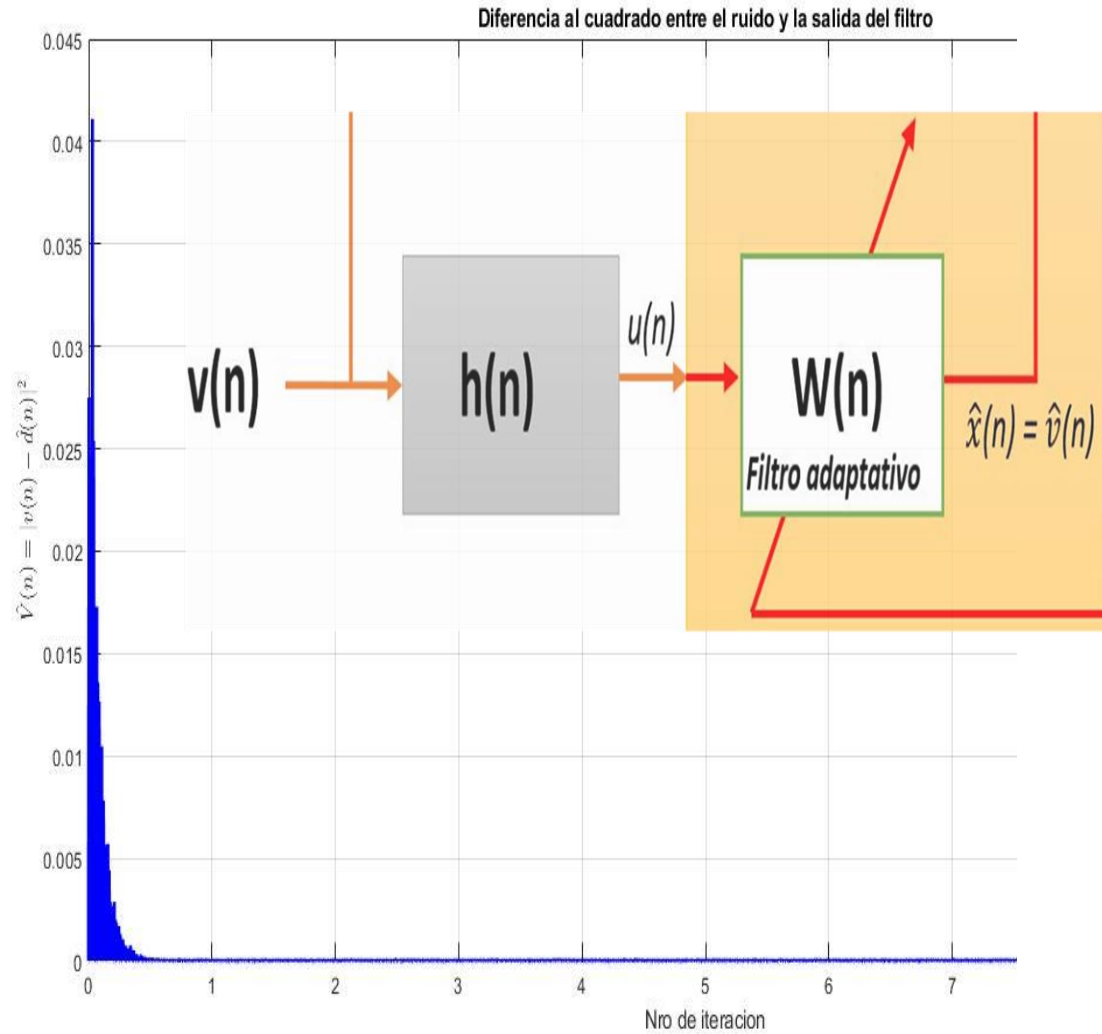
$u(n)$ es ruido captado del ambiente, correlacionado con $v(n)$, estimo el ruido $v(n)$ con $u(n)$.

$$x(n) = s(n) + v(n)$$

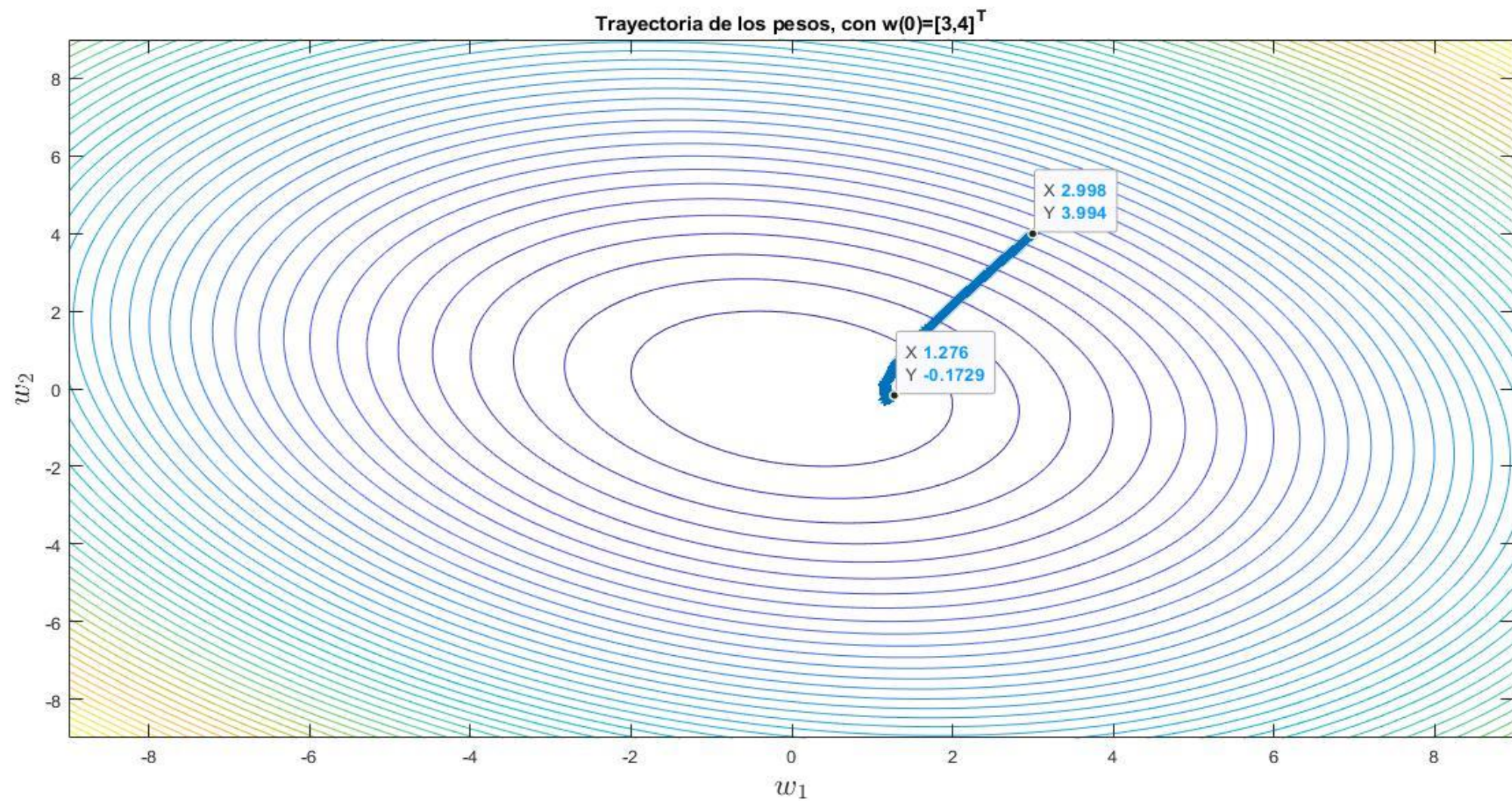
$$\begin{aligned} V &= E[|v(n) - \hat{x}(n)|^2] = E[|v(n) - w^* \cdot u(n)|^2] = \\ &= E[(v(n) - w^* \cdot u(n)) (v(n) - w^* \cdot u(n))^*] = \\ &= E[v(n)v(n)^* - w^* \cdot u(n) v(n) - v(n) u(n)^* w(n) + w^* \cdot u(n) u(n)^* w(n)] = \\ V &= \sigma_v^2 - w^* R_{u,v} - R_{v,u} w + w^* R_u w \end{aligned}$$

$$\begin{aligned} J &= E[|x(n) - \hat{v}(n)|^2] = E[x(n)x(n)^* - x(n)\hat{v}(n)^* - \hat{v}(n)x(n)^* + \hat{v}(n)\hat{v}(n)^*] = \\ &= E[(s(n) + v(n))(s(n) + v(n))^* - (s(n) + v(n))\hat{v}(n)^* - \hat{v}(n)(s(n) + v(n))^* + \\ &\quad \hat{v}(n)\hat{v}(n)^*] = \\ &= E[s(n)s(n)^* + v(n)v(n)^* - s(n)\hat{v}(n) - v(n)\hat{v}(n) - \hat{v}(n)s(n) - \hat{v}(n)v(n)^* + \\ &\quad \hat{v}(n)\hat{v}(n)^*] = \underbrace{\hat{v}(n) = w(n)^* u(n) \text{ y } s(n) \text{ descorrelacionado con } u(n)}_{\text{}} \\ &= E[s(n)s(n)^* + v(n)v(n)^* - \cancel{s(n)w(n)^* u(n)} - v(n)w(n)^* u(n) - \cancel{w(n)^* u(n)s(n)} - \\ &\quad \cancel{w(n)^* u(n)v(n)^*} + w(n)^* u(n) (w(n)^* u(n))^*] = \\ &= E[s(n)s(n)^* + v(n)v(n)^* - v(n)w(n)^* u(n) - w(n)^* u(n)v(n)^* + w(n)^* u(n)u(n)^* w(n)] \\ &= \\ J &= \sigma_s^2 + \sigma_v^2 - R_{v,u} w(n) - w(n)^* R_{u,v} + w(n)^* R_u w(n) = \sigma_s^2 + V \end{aligned}$$

• Problema 2: Filtrado, $\mu = 0.5$, $M = 2$, $W(0) = [3, 4]^T$



• Problema 2

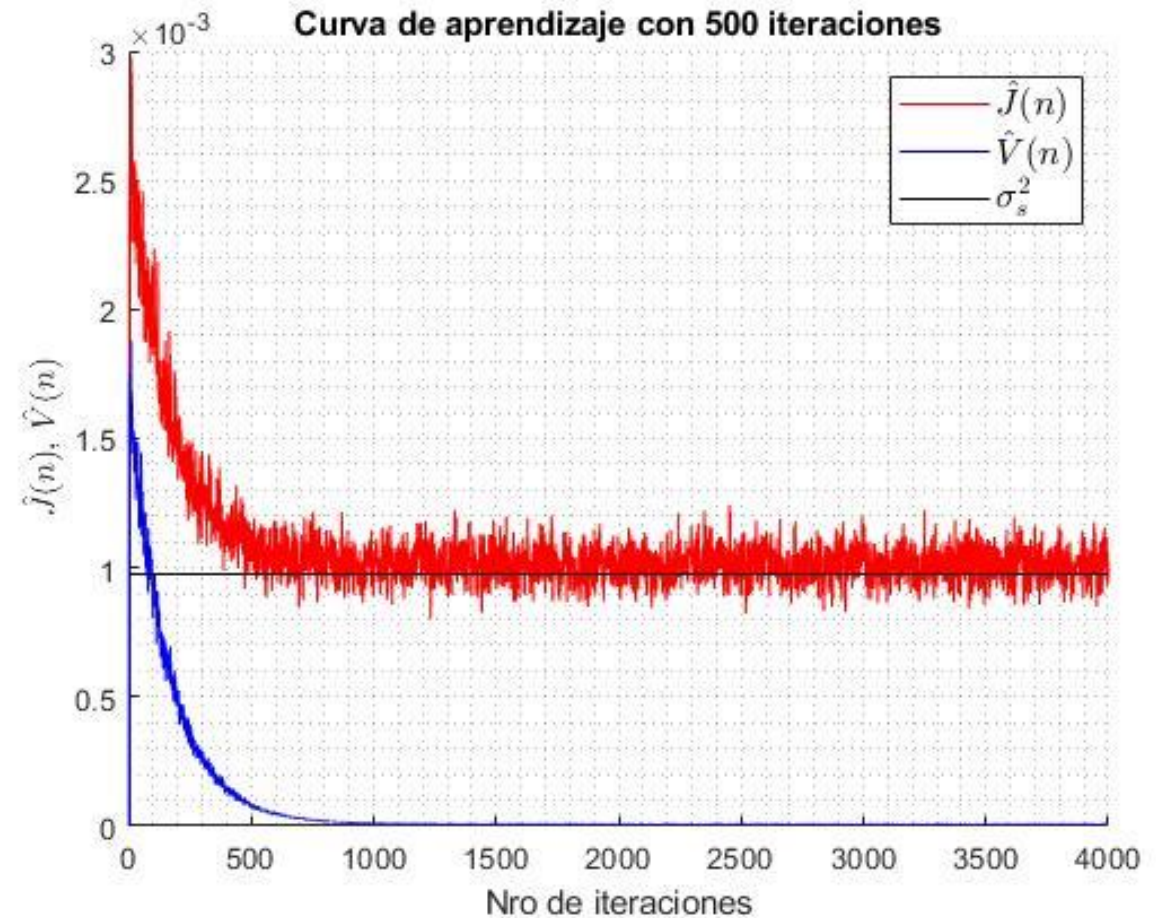


- Problema 3

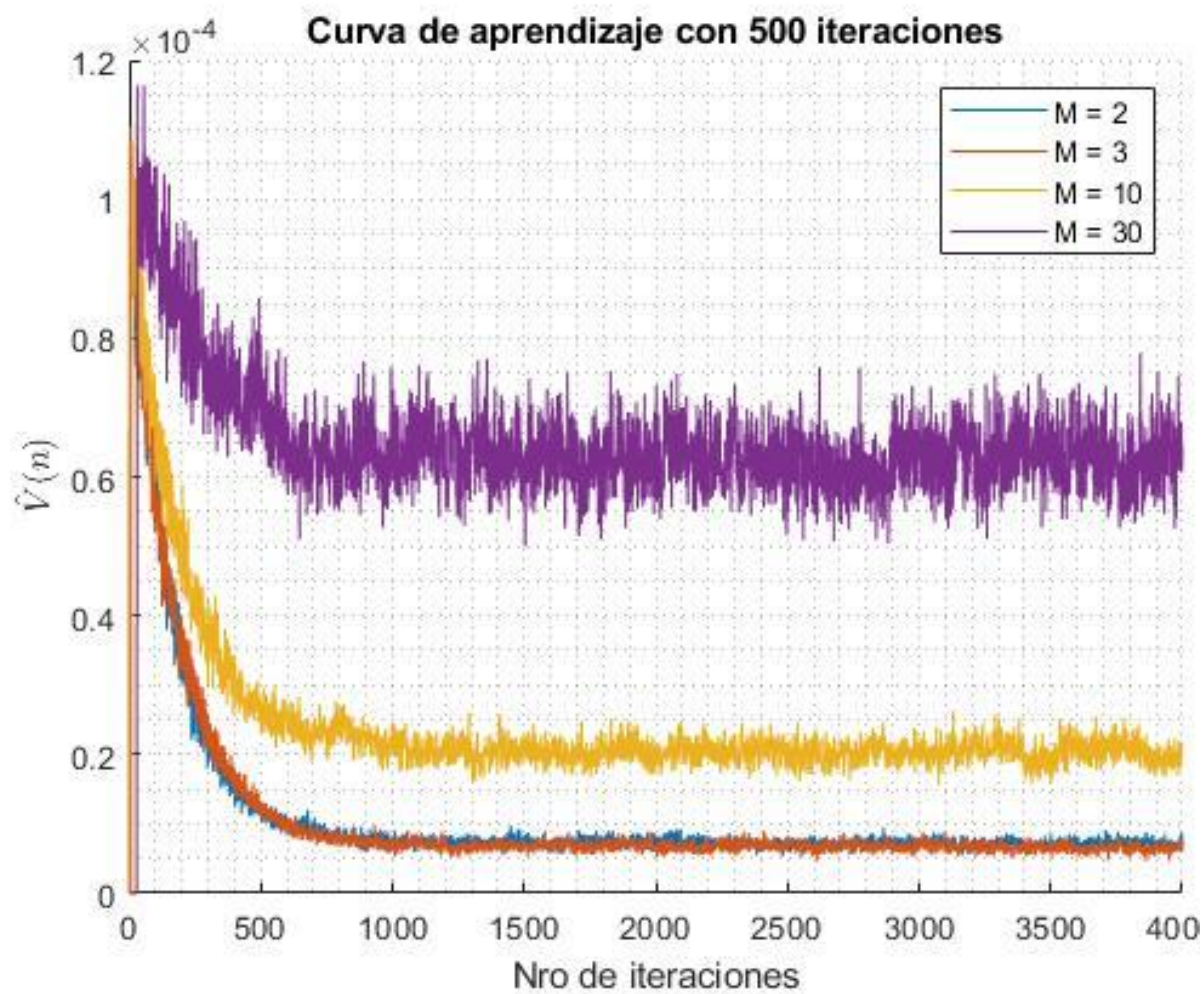
$$SNR_{dB} = 10 \log \left(\frac{\sigma_s^2}{\sigma_v^2} \right) = 10$$
$$\mathbf{h} = [0.8, 0.2, -0.01]$$

$$J = \sigma_s^2 + V$$

LMS: $\mu = 40, M = 2,$
 $\mathbf{W}(0) = [3, 4]^T$



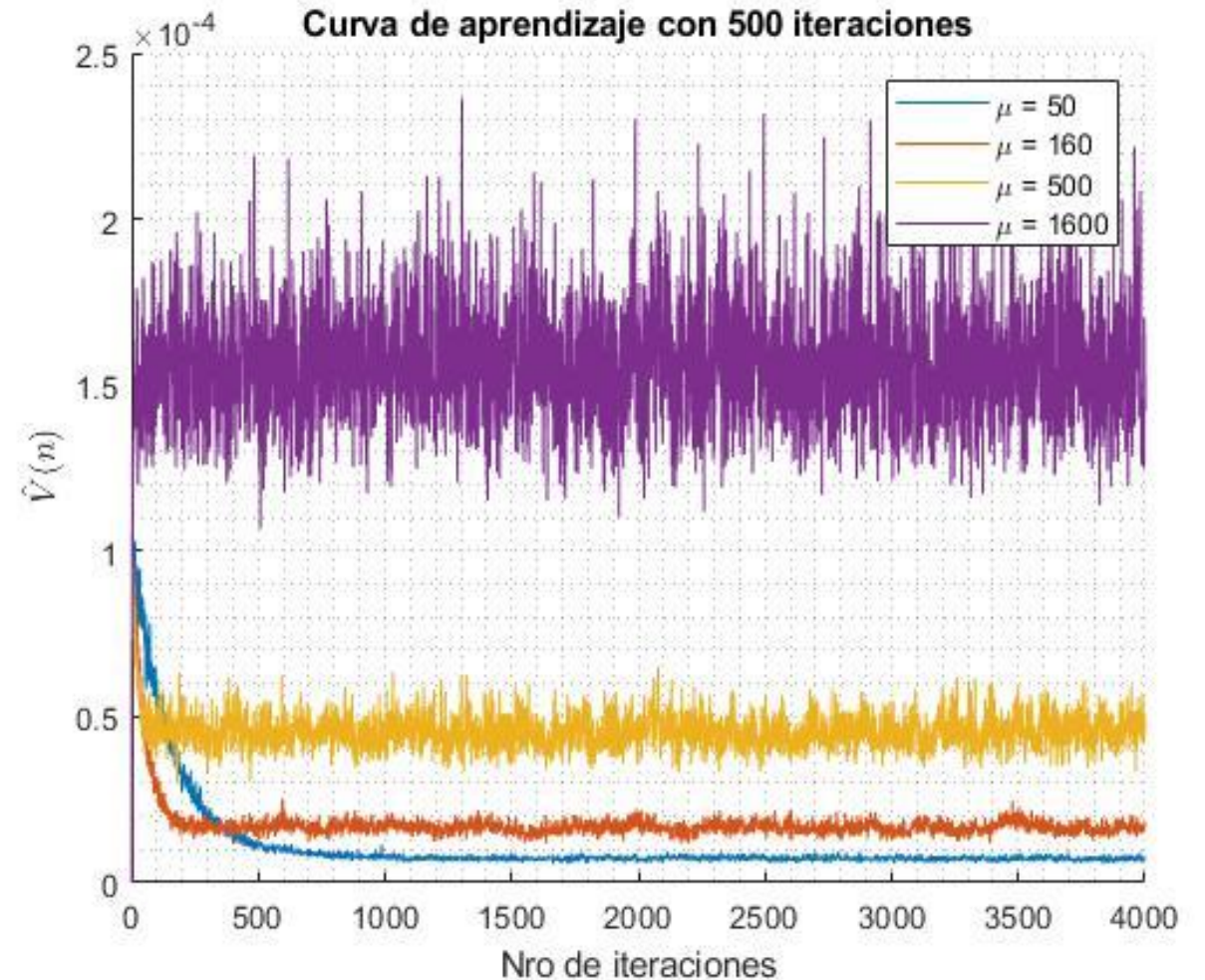
Curva de aprendizaje con 500 iteraciones



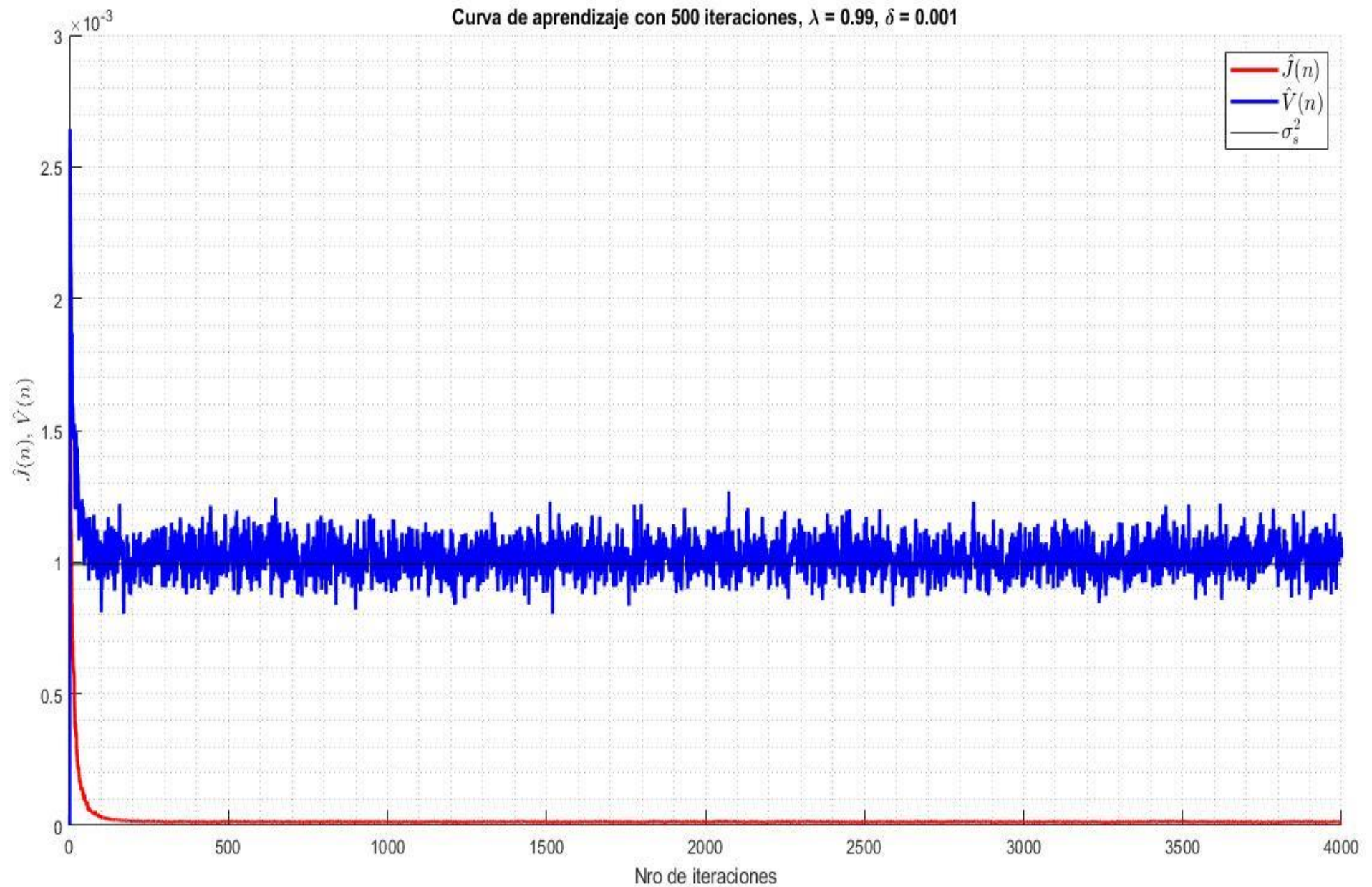
LMS : $\mu = 50$ parametrización con M
 $W(0) = 0$

• Problema 3

LMS : $M = 50$ parametrización con μ
 $W(0) = 0$

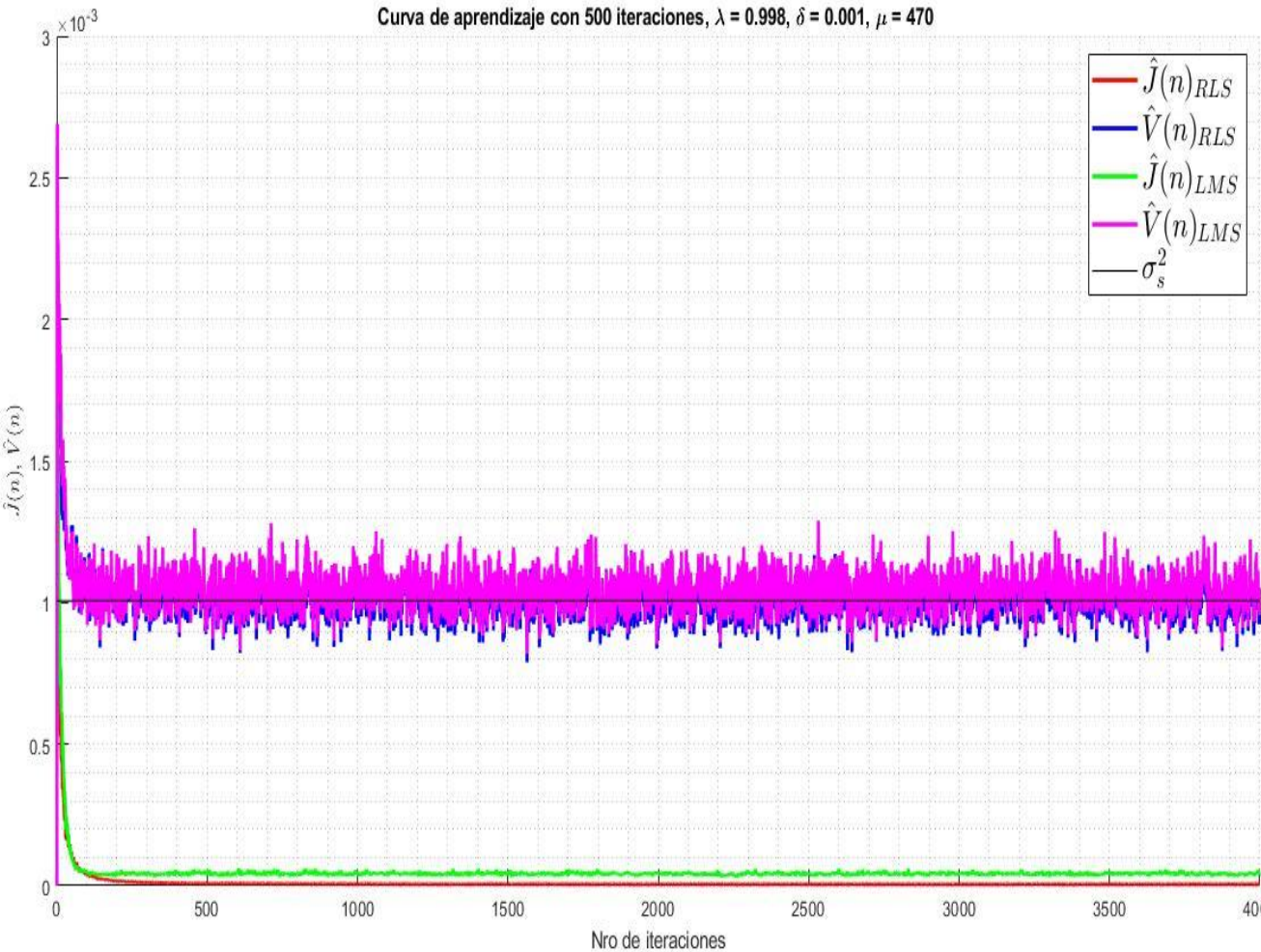


- Problema 4: RLS, $M = 2$, $W(0) = [3, 4]^T$



• Problema 4

RLS y LMS : $\lambda = 0,998$. Modificando μ para tener la potencias $\hat{v}(n)$ en $n \rightarrow \infty$ tiendan a lo mismo
 $\mu = 27$



RLS y LMS : $\lambda = 0,998$. Modificando μ para tener la misma pendiente inicial de las potencial de error.
 $\mu = 470$

