

# MATH 240 - Coordinate Systems

## Terminology

Coordinates of  $v$

- The coordinates of  $v$  relative to  $B$  are the weights  $c_1, c_2, \dots, c_n$  such that  $v = c_1b_1 + c_2b_2 + \dots + c_nb_n$

Coordinate vector relative to  $B$

- The column in  $\mathbb{R}^n$  built of these weights

A vector space  $V$  and a basis  $B$  that contains  $n$  vectors

Then every vector in the vector space can be expressed uniquely as a linear combination  $v = c_1b_1 + \dots + c_nb_n$ .

So, the only information we need to describe  $v$  are the weights  $(c_1, \dots, c_n)$  that can be seen as a vector in  $\mathbb{R}^n$

## The coordinate mapping

Let  $B$  be a basis for a vector space  $V$ . The coordinate mapping or coordinate transformation given by  $B$  is the mapping

$V \rightarrow \mathbb{R}^n$

given by the rule

$V \rightarrow [v]_B$