

MATH 240 - Rank of a matrix

Definition Let A be a matrix. The rank of A is $\text{rank}A = \dim \text{Col}A$

Proposition If two matrices are row equivalent, then they have the same row space.

Theorem Let A be a matrix. $\text{rank}A = \dim \text{Col}A = \dim \text{Row}A$

If A is an $m \times n$ matrix then $\text{rank}A = \dim \text{Col}A = \dim \text{Row}A \leq \min(m, n)$

Theorem *the rank-nullity theorem.* Let A be an $m \times n$ matrix. Then $\text{rank}A + \dim \text{Nul}A = n$