

# PHIL 105 - Consequences of Bayes Theorem

Cataxia Scorga (made up disease)

Life expectancy: 6-8 months

Testing for CS.

I test positive for CS.

1. does the result confirm CS.
2. I want to quit my job and take up base jumping if and only if my odds of having CS are at least 2 to 3.
3. Should I quit my job?

2 mistakes in testing

- 1.

False Negative:

Sometimes a sick person gets a healthy error result

Say  $P(\text{NegativeResult}|\text{CS}) = 0.1$

Say  $P(\text{PositiveResult}|\text{CS}) = 0.9$

This is the sensitivity of the test (90% sensitive)

- 2.

False Positive:

$P(\text{PositiveResult}|\text{Not CS}) = 0.03$

This is a very *specific* test.

We need  $P(\text{CS})$

Say  $P(\text{CS}) = 0.01$

$P(\text{CS} | \text{Negative result}) = (.1 * 0.01) / [(0.1 * 0.1) + (0.97 * 0.99)]$

$P(\text{CS} | \text{Negative result}) = 0.001$

A metal detector that always beeps is perfectly sensitive.

A metal detector that never beeps is perfectly specific.

Consider prior probabilities

Confirming evidence:

- more likely if hypothesis true
- less likely if hypothesis false

keep updating