

**UNIVERSITÀ DEGLI STUDI DELL'INSUBRIA**  
**Dipartimento di Scienze Teoriche e Applicate**  
**Corso di Laurea in Informatica**  
**Insegnamento di Progettazione del Software**  
**Prof. Sandro Morasca**

**ESERCIZI SU TESTING E ANALISI DEL SOFTWARE**

For each of the following methods

- determine all Definition-Use-Annulment expressions
- build (if possible) three sets of test data in such a way as to cover
  - all statements, but not all branches
  - all branches, but not all conditions
  - all conditions

**EXERCISE 1**

```
public static int factorial( int n )
{
    int f = 1;

    for(int i = 1; i <=n; i++)
    {
        f = f*i;
    }
    return f;
}
```

**EXERCISE 2**

```
public static int fibonacci( int threshold )
{
    int first = 0, second = 1;

    while ( second < threshold )
    {
        int sum = first + second;
        first = second;
        second = sum;
    }
    return first;
}
```

### EXERCISE 3

```
public static boolean isSorted( int [] array )
{
    int i = 0;
    boolean check = true;
    while( i < array.length-1 )
    {
        if( array[i] > array[i+1] )
        {
            check = false;
        }
        i++;
    }
    return check;
}
```

### EXERCISE 4

```
public static boolean isSorted( int [] array )
{
    for(int i = 0; i < array.length-1; i++)
    {
        if( array[i] > array[i+1] )
        {
            return false;
        }
    }
    return true;
}
```

### EXERCISE 5

```
public static void sort( int array[] ) {
    int i, j, temp;
    for(i = 1; i < array.length; i++) {
        for(j = 0; j < array.length-i; j++) {
            if(array[j] > array[j+1]) {
                temp = array[j];
                array[j] = array[j+1];
                array[j+1] = temp;
            }
        }
    }
}
```

### EXERCISE 6

```
public static int makeNotDecreasing( int number )
{
    int previousDigit = 9;
```

```

    int powerOfTen = 1;
    int result = 0;

    while( number != 0 )
    {
        int currentDigit = number % 10;
        if( currentDigit >= previousDigit )
        {
            currentDigit = previousDigit;
        }

        result = result + currentDigit*powerOfTen;
        powerOfTen = powerOfTen*10;
        previousDigit = currentDigit;
        number = number/10;
    }

    return result;
}

```

## EXERCISE 7

```

public static boolean isIncreasing( int number )
{
    int previousDigit = 9;

    while( number != 0 )
    {
        int currentDigit = number % 10;
        if( currentDigit > previousDigit )
        {
            return false;
        }
        previousDigit = currentDigit;
        number = number/10;
    }

    return true;
}

```

## EXERCISE 8

```

public static int method( int x, int y, int z )
{
    int a = 2;

    if( a < x && a > y )
    {
        x = x - a;
        z = x + y;

        while ( a + y < x )
        {

```

```
    a = z + y;  
  }  
}  
return( ++a );  
}
```

## EXERCISE 9

```
public static int arrayProducts( int array[] )
{
    int product = 1;
    for( int i = 0; i < (array.length+1)/2; i++ )
    {
        int currentSum = array[i]+array[array.length-1-i];
        if( currentSum != 0 && currentSum%4 != 1 )
        {
            product *= currentSum;
        }
    }
    return product;
}
```

## EXERCISE 10 (Final Exam 2021-12-20)

```
/*
 * Metodo che conta il numero di elementi nella prima metà di 'array'
 * il cui valore è maggiore della media degli elementi
 * di 'array' incrementata di 'upperDistance'
 */
public static int outlierCount( double array[], double upperDistance )
{
    double avg = 0;
    int nOutliers = 0;
    for(int i = 0; i < array.length; i++)
    {
        avg += array[i];
    }
    avg /= array.length;
    for(int j = 0; j < array.length/2; j++)
    {
        if( array[j] > avg + upperDistance )
        {
            nOutliers++;
        }
    }
    return nOutliers;
}
```

### EXERCISE 11 (Exam 2022-01-10)

```
/*
 * Metodo che trova il secondo valore più grande in 'array'
 */
public static int secondToMax( int array[] )
{
    int max = array[0];
    if( array.length == 1 )
    {
        return max;
    }

    int secondMax = array[1];
    if( secondMax > max )
    {
        max = array[1];
        secondMax = array[0];
    }
    for(int i = 2; i < array.length; i++)
    {
        if( array[i] > secondMax )
        {
            if( array[i] > max )
            {
                secondMax = max;
                max = array[i];
            }
            else
            {
                secondMax = array[i];
            }
        }
    }
    return secondMax;
}
```

## EXERCISE 12 (Exam 2022-01-31)

```
/*
 * Metodo che conta il numero di elementi (firstHalf) nella prima metà
 * di 'array' il cui valore è divisibile per l'elemento
 * simmetrico nella seconda metà
 * e il numero di elementi (secondHalf) nella seconda metà di 'array'
 * il cui valore è divisibile per l'elemento simmetrico nella prima
 * e restituisce secondHalf se firstHalf > secondHalf oppure
 * secondHalf - firstHalf
 */
public static int divisiblePairs( int array[] )
{
    int firstHalf = 0;
    int secondHalf = 0;
    for(int i = 0; i < array.length/2; i++)
    {
        if( array[i]%array[array.length-1-i] == 0 )
        {
            firstHalf++;
        }
        else if( array[array.length-1-i]%array[i] == 0 )
        {
            secondHalf++;
        }
    }
    return secondHalf - firstHalf;
}
```



### EXERCISE 13 (Exam 2022-02-16)

```
/*
 * Metodo che conta i numeri pari positivi contenuti in 'array'
 * fino alla posizione 'index'
 */
public static int method( int[] array, int index )
{
    int ret=0;

    if( index>=array.length )
    {
        return ret;
    }
    else
    {
        int i=0;
        while( i<=index )
        {
            if( array[i] > 0 & array[i]%2==0 )
            {
                ret++;
            }
            i++;
        }
        return ret;
    }
}
```

## EXERCISE 14 (Mid-term Exam 2022-11-09)

```
/*
 * Mid-term Exam 2022-11-09
 * Metodo che calcola una somma pesata degli elementi positivi in 'array'.
 * Se un elemento è seguito da un elemento di valore minore, l'elemento viene
 * moltiplicato per un peso e sommato. Il peso viene poi aggiornato.
Altrimenti
 * l'elemento viene sottratto e il peso viene aggiornato.
 */
public static int sumIncreasingDecreasingWithWeights( int[] array )
{
    int sum=0;
    int weight = 1;

    for(int i = 0; i < array.length-1; i++)
    {
        if( array[i] > array[i+1] && array[i] > 0)
        {
            sum = sum + weight*array[i];
            weight = weight+array[i+1];
        }
        else
        {
            sum = sum - array[i];
            weight = weight+array[i];
        }
    }

    return sum;
}
```

## EXERCISE 15 (Mid-term Exam 2022-11-09)

```
/*
 * Mid-term Exam 2022-11-09
 * Metodo che scambia un elemento di 'array' se il suo prodotto
 * con l'elemento simmetrico a partire dal fondo è negativo e conta
 * il numero di scambi avvenuti.
 * Il metodo esamina gli elementi di 'array' solo fino al
 * primo elemento nullo incontrato.
 */
public static int swapNegativeProducts( int array[] )
{
    int count = 0;
    int i = 0;
    while( i < array.length/2 & array[i] != 0 )
    {
        if( array[i]*array[array.length-1-i] < 0 )
        {
            int temp = array[i];
            array[i] = array[array.length-1-i];
            array[array.length-1-i] = temp;
            count++;
        }
        i++;
    }
    return count;
}
```

*Please note that black-box test data are shown in some of the solutions for illustration completeness. Black-box test data generation is NOT a part of the written exam exercises, though it may be the topic for questions.*

## EXERCISE 1: SOLUTION

Definition-Use-Annulment expressions

n: duu\*  
 f: d(ud)\*u  
 i: du(uudu)\*

*White-box test data*

Input	n	Coverage
A	10	All statements and branches and conditions covered

Sets of inputs

- 1) all statements, but not all branches: impossible
- 2) all branches, but not all conditions: impossible
- 3) all statements and all branches and all conditions: {A}

*Black-box test data and goals*

Input	n	Goals
A	10	Regular case. Exactly n = 10 loop iterations.
B	1	Boundary case. Exactly n = 1 loop iteration.
C	0	Boundary case. Exactly n = 0 loop iterations
D	-1	???

## EXERCISE 2: SOLUTION

### Definition-Use-Annulment expressions

```
threshold: duu*  
first: d(ud)*u  
second: du(uudu)*  
sum: (du)*
```

### White-box test data

Input	n	Coverage
A	10	All statements and branches and conditions covered

### Sets of inputs

- 1) all statements, but not all branches: impossible
- 2) all branches, but not all conditions: impossible
- 3) all statements and all branches and all conditions: {A}

### Black-box test data and goals

Input	threshold	Goals
A	10	Regular case. Exactly $n = ?$ loop iterations?
B	1	Boundary case. Exactly $n = 0$ loop iteration.
C	0	Boundary case. Exactly $n = 0$ loop iterations.
D	2	Exactly $n = 1$ loop iteration.
E	13	Case in which threshold is a Fibonacci number.
D	-1	????

### EXERCISE 3: SOLUTION

#### Definition-Use-Annulment expressions

```
array: du(uuu)*  
i: du(uuudu)*  
check: d((d+ε))*u <=> dd*u
```

#### White-box test data

Input	array	Coverage
A	{5,1}	All statements covered
B	{1,5,3}	"if-else" branch covered

#### Sets of inputs

- 1) all statements, but not all branches: {A}
- 2) all branches, but not all conditions: impossible
- 3) all statements and all branches and all conditions: {B}

#### Black-box test data and goals

Try several cases:

- perfectly sorted array
- unsorted array
- pairs of equal values
- array sorted except for the last pair
- array sorted except for the first pair
- ...

## EXERCISE 4: SOLUTION

### Definition-Use-Annulment expressions

array: du(uuu) \*  
i: du(uuudu) \*

### White-box test data

Input	array	Coverage
A	{1}	return true; covered
B	{1,5,3}	All conditions and, therefore, all branches and, therefore, all statements of the for loop covered

### Sets of inputs

- 1) all statements, but not all branches: impossible (there is no way to execute the i++ statement in the for loop heading without executing the "if-else" branch)
- 2) all branches, but not all conditions: impossible
- 3) all statements and all branches and all conditions: {A,B}

### Black-box test data and goals

Try several cases:

- perfectly sorted array
- unsorted array
- pairs of equal values
- array sorted except for the last pair
- array sorted except for the first pair
- ...

## EXERCISE 5: SOLUTION

### Definition-Use-Annulment expressions

```
array: du(u(uu(uudd+ε)u)*u)*  
i:   adu(uu*udu)*  
j:   a(du(uu(uuuu+ε)udu)*)*  
temp: a(((du+ε))*)*
```

### White-box test data

Input	array	Coverage
A	{5,1}	All statements covered
B	{1,5,3}	All branches covered

### Sets of inputs

- 1) all statements, but not all branches: {A}
- 2) all branches, but not all conditions: impossible
- 3) all statements and all branches and all conditions: {B}

### Black-box test data and goals

Try several cases:

- perfectly sorted array
- unsorted array
- pairs of equal values
- array sorted except for the last pair
- array sorted except for the first pair
- ...



## EXERCISE 6: SOLUTION

### Definition-Use-Annulment expressions

```
number: du(uudu)*
previousDigit: d(u(u+ε)d)*
powerOfTen: d(uud)*
result: d(ud)*u
currentDigit: (du(d+ε)uu)*
```

### White-box test data

Input	Number	Coverage
A	9	All statements covered
B	53	All branches covered

### Sets of inputs

- 1) all statements, but not all branches: {A}
- 2) all branches, but not all conditions: impossible
- 3) all statements and all branches and all conditions: {B}

### Black-box test data and goals

Try several cases:

- totally "decreasing" number
- totally "increasing" number
- number in which all digits are the same
- number with only one digit
- number 9
- number 0
- ...
- how about negative numbers?

## EXERCISE 7: SOLUTION

### Definition-Use-Annulment expressions

```
number: du(uudu)*(ε+u)
previousDigit: d(ud)*(ε+u)
currentDigit: (duu)*(ε+du)
```

### White-box test data

Input	Number	Coverage
A	345	All statements covered, except <code>return false;</code>
B	543	All statements covered, except <code>return true;</code>

### Sets of inputs

- 1) all statements, but not all branches: impossible
- 2) all branches, but not all conditions: impossible
- 3) all statements and all branches and all conditions: {A,B}

### Black-box test data and goals

Try several cases:

- totally "decreasing" number
- totally "increasing" number
- number in which all digits are the same
- number with only one digit
- number 9
- number 0
- ...
- how about negative numbers?

## EXERCISE 8: SOLUTION

### Definition-Use-Annulment expressions

Without taking into account lazy evaluation (considering `&&` and `||` as if they were `&` and `|` instead)

```
x: du (uduuu*+ε)
y: du (uu (uu) *+ε)
z: d (du*+ε)
a: duu (uu (du) *+ε) udu
```

### Taking into account lazy evaluation

```
x: du (uduuu*+ε)
y: d (ε+u (uu (uu) *+ε) )
z: d (du*+ε)
a: du (ε+u (uu (du) *+ε) ) udu
```

### White-box test data

Input	x	y	z	Coverage
A	5	0	0	All statements covered
B	0	0	0	"else" branch covered
C	5	3	0	a < y made false

### Sets of inputs

- 1) all statements, but not all branches: {A}
- 2) all branches, but not all conditions: {A,B}
- 3) all statements and all branches and all conditions: {A,B,C}

### Black-box test data and goals

They should be based on the meaning of the method.

## EXERCISE 9: SOLUTION

### Definition-Use-Annulment expressions

Without taking into account lazy evaluation (considering `&&` and `||` as if they were `&` and `|` instead)

```
array: du(uuuu)*
product: d((ud+ε))*u <=> d(ud)*u
i: du(uuudu)*
currentSum: (duu(u+ε))*
```

### Taking into account lazy evaluation

```
array: du(uuuu)*
product: d((ud+ε))*u <=> d(ud)*u
i: du(uuudu)*
currentSum: (du(ε+u(u+ε)))*
```

### White-box test data

Input	array	Coverage
A	{5,2}	All statements covered
B	{5,3,6,2}	"else" branch covered
C	{5,3,-1,1,6,2}	currentSum != 0 made false

### Sets of inputs

- 1) all statements, but not all branches: {A}
- 2) all branches, but not all conditions: {B}
- 3) all statements and all branches and all conditions: {C}

### Black-box test data and goals

Try several cases:

- array with an even number of elements
- array with an odd number of elements
- array with only one element
- array with only zero sums
- array with only sums of the kind  $4n+1$
- array with only even sums
- array with only sums divisible by 4
- ...
- how about negative numbers?



## EXERCISE 10: SOLUTION

### Definition-Use-Annulment expressions

`array`:  $\text{du}(\text{uu}) * \text{uu}(\text{uu}) *$   
`upperDistance`:  $\text{du} *$   
`avg`:  $\text{d}(\text{ud}) * \text{udu} *$   
`nOutliers`:  $\text{d}((\text{ud} + \epsilon)) * \text{u} \Leftrightarrow \text{d}(\text{ud}) * \text{u}$   
`i`:  $\text{du}(\text{uudu}) *$   
`j`:  $\text{du}(\text{uudu}) *$

### White-box test data

Input	<code>array</code>	<code>upperDistance</code>	Coverage
A	{7,6,2,1}	1	All statements covered
B	{7,1,2,6}	1	All branches and conditions covered

### Sets of inputs

- 1) all statements, but not all branches: {A}
- 2) all branches, but not all conditions: impossible
- 3) all statements and all branches and all conditions: {B}

## EXERCISE 11: SOLUTION

### Definition-Use-Annulment expressions

`array`:  $\text{duu}(\varepsilon + u(uu + \varepsilon)u(u(uu + \varepsilon)u)*)$   
`max`:  $\text{d}(u + u(u + \varepsilon)((u(u\text{d} + \varepsilon) + \varepsilon))*) \iff \text{d}(u + u(u + \varepsilon)(u(u\text{d} + \varepsilon))*)$   
`secondMax`:  $\varepsilon + \text{du}(\text{d} + \varepsilon)(u(\text{d} + \varepsilon)) * u$   
`i`:  $\varepsilon + \text{du}(u(uu + \varepsilon)u\text{du}) *$

### White-box test data

Input	<code>array</code>	Coverage
A	{1}	All statements covered down to <b>return</b> <code>max</code> ;
B	{4,10,6,14}	All statements covered (except <b>return</b> <code>max</code> ;). Covered implicit "else" branch in <b>if</b> ( <code>array.length == 1</code> ); covered then branch in <b>if</b> ( <code>secondMax &gt; max</code> ); covered then branch in <b>if</b> ( <code>array[i] &gt; secondMax</code> ); covered both branches in <b>if</b> ( <code>array[i] &gt; max</code> )
C	{10,4,2}	Covered implicit "else" branch in <b>if</b> ( <code>secondMax &gt; max</code> ); covered implicit "else" branch in <b>if</b> ( <code>array[i] &gt; secondMax</code> )

### Sets of inputs

- 1) all statements, but not all branches: {A, B}
- 2) all branches, but not all conditions: impossible
- 3) all statements and all branches and all conditions: {A, B, C}

## EXERCISE 12: SOLUTION

### Definition-Use-Annulment expressions

```
array: du(uuu(ε+uuu)u)*  
firstHalf: d((ud+ε))*u <==> d(ud)*u  
secondHalf: d((ε+(ud+ε)))*u <==> d(ud)*u  
i: du(uu(ε+uu)udu)*
```

### White-box test data

Input	array	Coverage
A	{8,3,6,4}	All statements covered; implicit "else" branch in <b>else if</b> ( array[array.length-1-i]%array[i] == 0 ) not covered
B	{8,3,5,7,6,4}	All branches covered.

### Sets of inputs

- 1) all statements, but not all branches: {A}
- 2) all branches, but not all conditions: impossible
- 3) all statements and all branches and all conditions: {B}



### EXERCISE 13: SOLUTION

#### Definition-Use-Annulment expressions

```
array:      du (ε + (uu) *)
index:      du (ε + (u u*))
ret:        d (u + ( (ud + ε) * u))
i:          ε + (du (uuudu) *)
```

#### White-box test data

Input	array	index	Coverage
A	{2,4}	5	Copro il primo then
B	{2,4}	1	Copro il then dentro while, ma non l'else implicito
C	{2,3}	1	Copro l'else implicito nel while
D	{2,3,-1, 2}	3	Copro tutte le condizioni dell'if interno al while, sia come unione delle 2 componenti che come single component logiche

#### Sets of inputs

- 1) all statements, but not all branches: {A, B}
- 2) all branches, but not all conditions: {A, C} (copro il then e l'else dell'if interno, ma non  $\text{array}[i] < 0$ )
- 3) all statements and all branches and all conditions: {A, D}

## EXERCISE 14: SOLUTION

### Definition-Use-Annulment expressions

Without taking into account lazy evaluation (considering && and || as if they were & and | instead)

```
array: du(uuu(uu+uu)u)* ⇔ du(uuuuuu)*
sum: d((ud+ud))*u ⇔ d(ud+ud)*u ⇔ d(ud)*u
weight: d((uud+ud))* ⇔ d(uud+ud)*
i: du(uuu(uu+uu)udu)* ⇔ du(uuuuuudu)*
```

### Taking into account lazy evaluation

```
array: du(uu(u(uu+uu)+ε(uu)))* ⇔ du(uu(u(uu)+ε(uu)))* ⇔ du(uu(u+ε)uu)*
sum: d((ud+ud))*u ⇔ d(ud+ud)*u ⇔ d(ud)*u
weight: d((uud+ud))* ⇔ d(uud+ud)*
i: du(uu(u(uu+uu)+ε(uu))udu)* ⇔ du(uu(u(uu)+ε(uu))udu)* ⇔ du(uu(u+ε)uuudu)*
```

### White-box test data

Input	array	Coverage
A	{1,3,2}	While loop executed twice: <ul style="list-style-type: none"><li>- when comparing array[0] and array [1] the else branch is covered</li><li>- when comparing array[1] and array [2] the else branch is covered</li></ul>
B	{-1,-2}	Condition array[0] > array [1] is true, but condition array[0] > 0 is false
C	{-1,1}	Condition array[0] > array [1] is false and condition array[0] > 0 is false

### Sets of inputs

- 1) all statements, but not all branches: impossible
- 2) all branches, but not all conditions: {A} (all branches are covered, but condition array[i] > 0 is always true)
- 3) all statements and all branches and all conditions: {A,B,C}

## EXERCISE 15: SOLUTION

### Definition-Use-Annulment expressions

```
array: duu(uuu(uuudud+ε)uu)*  
count: d(ud)*u  
i: duu(uu(uuuu+ε)uduu)*  
temp: ((du))* ⇔ (du)*
```

### White-box test data

Input	array	Coverage
A	{1,-1}	While loop is executed once and then branch is executed
B	{1,2,3,-1}	While loop executed twice - the first time the then branch is executed - the second time the "implicit else" branch is executed
C	{1,0,3,-1}	The second time the while loop predicate is evaluated, - condition $1 < \text{array.length}/2$ is true - condition $\text{array}[0] \neq 0$ is false
D	{1,3,0,-1}	The third time the while loop predicate is evaluated, - condition $1 < \text{array.length}/2$ is false - condition $\text{array}[0] \neq 0$ is false

### Sets of inputs

- 1) all statements, but not all branches: {A} ("implicit else" branch not covered)
- 2) all branches, but not all conditions: {B} (condition  $\text{array}[i] \neq 0$  is never false)
- 3) all statements and all branches and all conditions: {B,C,D}