

#### **STATISTICAL ERROR**

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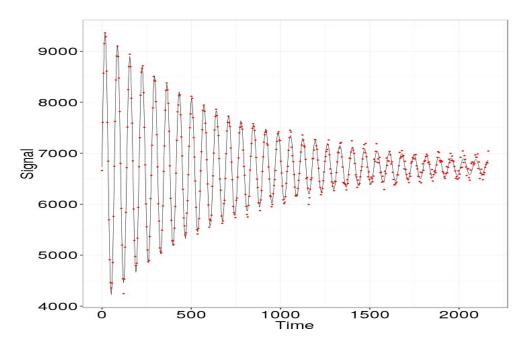
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## **Problem statement**

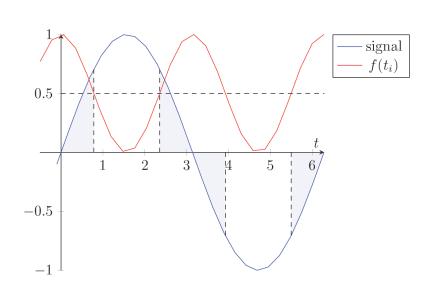
$$N(t) = N_0 \cdot (1 + P \cdot e^{-t/\tau_d} \cdot \sin(\omega \cdot t + \varphi))$$

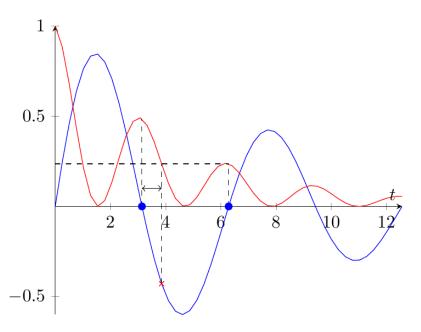
$$\sigma^{2}[\hat{\omega}] = \frac{\sigma^{2}[\varepsilon]}{\sum_{i} f(t_{i}) \cdot \sigma_{w}^{2}[t]}$$





# **Two aspects**







#### Goals

- Under what conditions sampling modulation is beneficial
- How much modulation makes sense
- At what point measurement is no longer reasonable

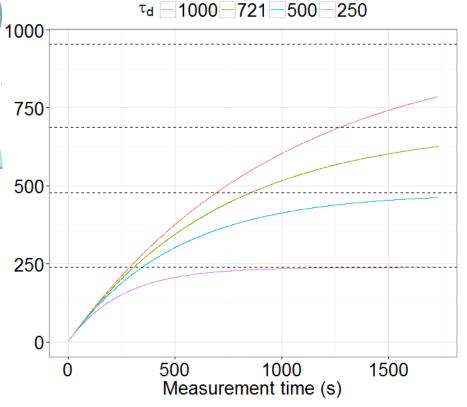


## **Spread**

$$\sum f(t_i) = n_{\varepsilon/zc} \cdot x_{01} \left( \frac{\exp(-\frac{\pi}{\omega \tau_d} n_{zc}) - 1}{\exp(-\frac{\pi}{\omega \tau_d}) - 1} \right)$$

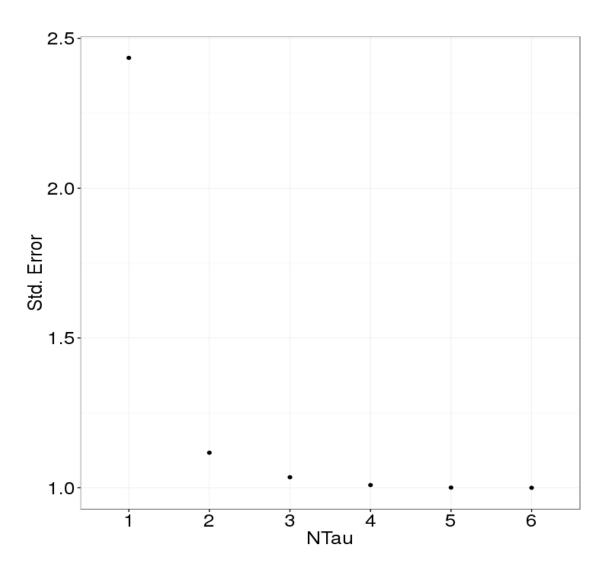
$$t(z) = \tau_d \cdot \ln(\frac{1}{1-z})$$

FI limit (%)	Reached (×τ <sub>d</sub> )	SNR@3% error
95	3.0	1.7
90	2.3	3.3
70	1.2	10.0
50	0.7	16.5



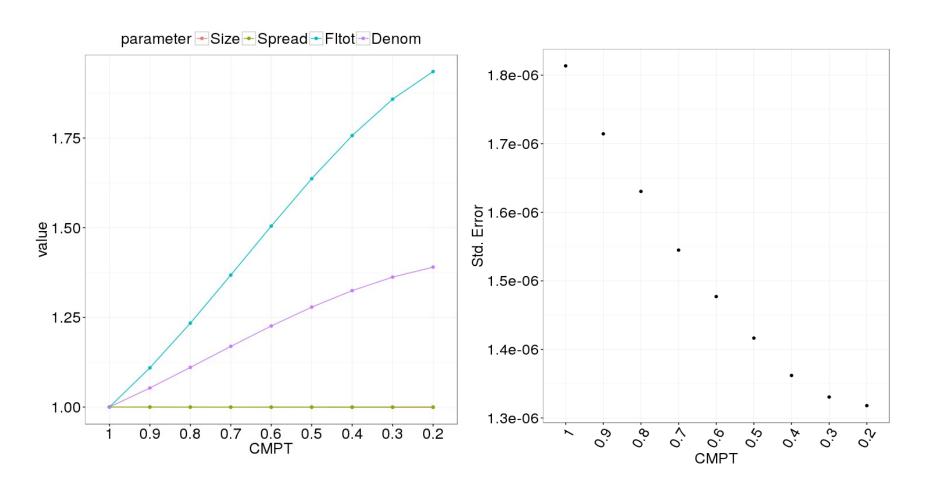


## **Simulation**





## **Modulation: Beam lifetime doesn't matter**





### **Modulation: Beam lifetime does matter**

