Modeling of spin-orbital dynamics in a storage ring

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**Abstract**. Two distinct storage ring designs have been proposed for the deuteron Electric Dipole Moment (dEDM) search experiment: a Frozen Spin, and a Quasi-Frozen Spin ring. The FS-ring allows for the most accurate measurement, but the continuous fulfilment of the FS condition is unrealizable. The QFS design relaxes the condition to only hold on average, at a slight cost of precision. [1] The goal of the present work is to investigate which design is preferable for the attainment of the target precision. This task requires one to model the spin-orbital dynamics of the beam in both rings.

1. The Frozen and Quasi-frozen Spin concepts

There exist two design approaches to the problem of measuring the deuteron Electric Dipole Moment (dEDM) inside a storage ring: the Frozen Spin (FS) lattice, and the Quasi-Frozen Spin (QFS) lattice.

In the FS ring design, the spin of a beam particle is aligned with its momentum at any point in time; this allows the maximization of the useful signal, but requires that the energy of the particle be its so-called “magic energy” – a condition that cannot be fulfilled exactly for an ensemble of particles. The QFS design does not require the continuous fulfillment of the Frozen Spin condition; the cost for this is a slight (on the order of percents) degradation of the EDM signal.

In order to decide which design solution is preferable for the attainment of the target accuracy (upped bound on the dEDM at 10-24 e·cm) one has to model the spin-orbital dynamics of the beam inside both lattices. The present work deals with some problems that are inherent in this enterprise.

1. Experiment systematics

In the original BNL proposal, a longitudinally polarized beam is injected in the storage ring, and the EDM is measured by the growth, over a long period, of its vertical polarization component. [2] The spin dynamics of a particle put into an electro-magnetic field are determined by the Thomas-Bargmann-Michel-Telegdi equation:

(1)

where is the anomalous magnetic moment, g the gyromagnetic ratio, the first two terms are due to the Magnetic Dipole Moment (MDM), and the last two to the EDM.

As is readily observed from the above equation, the presence of a parasitic horizontal magnetic, or vertical electric, field caused by the imprecision of accelerator element positioning (specifically, tilts about the optical axis), induces a faking MDM signal in the measurement plane. To solve this problem, a CW/CCW procedure was proposed in Jülich. [3] The idea behind this method is to estimate the net MDM+EDM spin precession frequency when the beam in injected into the ring counter-/clockwise, and then add the results. Since the magnetic field is reversed going from the CW to CCW case, the MDM frequency changes sign, and hence cancels in addition. One requirement of this method, though, is that the MDM frequency must be much higher than the one caused by the EDM; the sensitivity of MDM precession to the element positioning inaccuracy has to be analyzed by simulation.

Another problem encountered in the EDM search is the finite spin coherence time (SCT). Because the beam particles are injected into the ring at different energies and positions, and hence have different orbit lengths, their spins precess at different frequencies; due to this fact the net beam polarization vector dissipates over time. By Taylor-expanding the expressions for the spin tune in the electric and magnetic fields around the value of the reference particle, we arrive at: [3]

(2)

where G6 is a function of G and , is the synchrotron oscillation amplitude of the particle, is the second-order momentum compaction factor, the slip factor, the synchrotron oscillation frequency, and is the orbit lengthening due to betatron motion. The first term in (2) is averaged out as a result of synchrotron oscillation; the orbit-lengthening-related decoherence effect is mitigated by the introduction of sextupole fields.

3.

## A subsection

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References

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2. Anastassopoulos D et al. 2008 *AGS Proposal: Search for a permanent electric dipole moment of the deuteron nucleus at the 10 −29 e · cm level.*
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