

EJEMPLO 1. CREDITOS

Historia crédito. BAD: Moroso, no moroso

X_1, \dots, X_4 LOAN, MORTDUE, CLAGE, CLNO

~~Test de Igualdad de Medias~~

| | Statistics | F | df1 | df2 | Pr |
|------------------------|------------|----------|-----|-----|----|
| Wilks Lambda | 0.377179 | 55.73007 | 4 | 135 | 0 |
| Pillai Trace | 0.622821 | 55.73007 | 4 | 135 | 0 |
| Hotelling-Lawley Trace | 1.651261 | 55.73007 | 4 | 135 | 0 |
| Roy Greatest Root | 1.651261 | 55.73007 | 4 | 135 | 0 |

~~Test de Mardia de Multinormalidad por grupos~~

grupos: Moroso

| | | | | |
|------------|-----------|------------|-----------|------------|
| kappa1 | pvalsim | kappa2 | pvalkurt | n |
| 16.4509769 | 0.6882819 | -1.5057794 | 0.1321238 | 55.0000000 |

grupos: No moroso

| | | | | |
|-------------|------------|-------------|------------|-------------|
| kappa1 | pvalsim | kappa2 | pvalkurt | n |
| 26.18812374 | 0.15968824 | -1.83298187 | 0.06680527 | 85.00000000 |

DISCRIMINANTE LINEAL

Call:

lda(BAD ~ LOAN + MORTDUE + CLAGE + CLNO, data = credit1)

Prior probabilities of groups:

Moroso No moroso

0.3928571 0.6071429

Group means:

| | LOAN | MORTDUE | CLAGE | CLNO |
|-----------|----------|----------|----------|----------|
| Moroso | 13774.55 | 50982.20 | 142.0774 | 19.65455 |
| No moroso | 17929.41 | 62384.15 | 258.6129 | 19.58824 |

Coefficients of linear discriminants (ES LO QUE EN CLASE SE LLAMO
FUNCION DE CLASIFICACION.):

| | LD1 |
|---------|---------------|
| LOAN | 5.563021e-05 |
| MORTDUE | 1.832424e-05 |
| CLAGE | 1.859608e-02 |
| CLNO | -7.712388e-02 |

Predicción

| | Pred1 | |
|-----------|--------|-----------|
| | Moroso | No moroso |
| Moroso | 45 | 10 |
| No moroso | 0 | 85 |

~~Test de Homogeneidad de Variancias~~

| | Statistic | df | Pr |
|-------|-----------|----|--------------|
| Box.M | 47.88681 | 10 | 6.509141e-07 |
| adj.M | 46.29599 | 10 | 1.267556e-06 |

DISCRIMINANTE CUADRATICO

Call:

```
qda(BAD ~ LOAN + MORTDUE + CLAGE + CLNO, data = credit1)
```

Prior probabilities of groups:

Moroso No moroso

0.3928571 0.6071429

Group means:

| | LOAN | MORTDUE | CLAGE | CLNO |
|-----------|----------|----------|----------|----------|
| Moroso | 13774.55 | 50982.20 | 142.0774 | 19.65455 |
| No moroso | 17929.41 | 62384.15 | 258.6129 | 19.58824 |

Predicción

| | pred2 | |
|-----------|--------|-----------|
| | Moroso | No moroso |
| Moroso | 46 | 9 |
| No moroso | 0 | 85 |

DISCRIMINANTE LOGISTICO

Coefficients:

| | Estimate | Std. Error | z value | Pr(> z) | |
|-------------|------------|------------|---------|----------|-----|
| (Intercept) | -1.076e+01 | 2.484e+00 | -4.334 | 1.47e-05 | *** |
| LOAN | 1.453e-04 | 6.420e-05 | 2.262 | 0.02367 | * |
| MORTDUE | 5.992e-05 | 1.826e-05 | 3.281 | 0.00103 | ** |
| CLAGE | 4.634e-02 | 9.145e-03 | 5.067 | 4.04e-07 | *** |
| CLNO | -2.369e-01 | 7.499e-02 | -3.160 | 0.00158 | ** |

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 187.603 on 139 degrees of freedom
Residual deviance: 68.497 on 135 degrees of freedom
AIC: 78.497
Number of Fisher Scoring iterations: 7

Predicción

| | pred3 | |
|-----------|-------|----|
| | 0 | 1 |
| Moroso | 47 | 8 |
| No moroso | 2 | 83 |

EJEMPLO INVEST (YA USADO EN CLUSTER)

Grupo: el país tiene o no tiene Grado Inversor

X₁, X₂, X₃, X₄, X₅... INDICE PAIS, DEUDA/PBI, PBIPERCAPITA, INFLACION, CRECIMIENTOPBI

~~Test de Igualdad de Medias~~

| | Statistics | F | df1 | df2 | Pr |
|------------------------|------------|----------|-----|-----|--------------|
| Wilks Lambda | 0.3962623 | 16.97704 | 7 | 78 | 1.971756e-13 |
| Pillai Trace | 0.6037377 | 16.97704 | 7 | 78 | 1.971756e-13 |
| Hotelling-Lawley Trace | 1.5235808 | 16.97704 | 7 | 78 | 1.971756e-13 |
| Roy Greatest Root | 1.5235808 | 16.97704 | 7 | 78 | 1.971756e-13 |

~~Test de Homogeneidad de Variancias~~

| | Statistic | df | Pr |
|-------|-----------|----|----|
| Box.M | 388.5175 | 28 | 0 |
| adj.M | 352.2176 | 28 | 0 |

~~Test de Mardia de Multinormalidad por grupos~~

grupos: 0

| kappa1 | pvalsim | kappa2 | pvalkurt | n |
|--------------|--------------|--------------|--------------|----|
| 2.307879e+02 | 1.221245e-15 | 5.909363e+00 | 3.434339e-09 | 34 |

grupos: 1

| kappa1 | pvalsim | kappa2 | pvalkurt | n |
|--------------|--------------|---------------|--------------|----|
| 1.852117e+02 | 1.371679e-09 | -4.400827e-01 | 6.598772e-01 | 52 |

LOGISTICO

Coefficients:

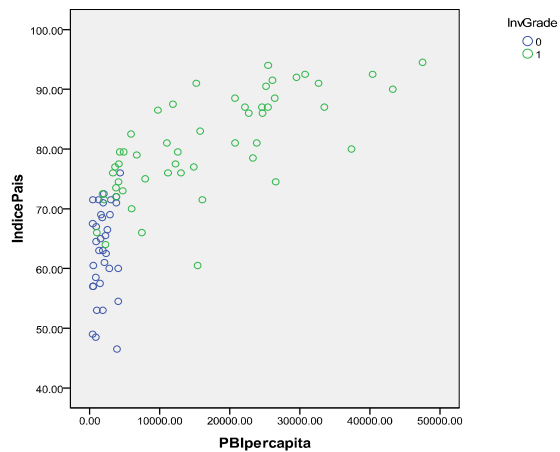
| | Estimate | Std. Error | z value | Pr(> z) |
|--------------|------------|------------|---------|----------|
| (Intercept) | -1.368e+01 | 9.035e+00 | -1.514 | 0.1301 |
| IndicePais | 1.857e-01 | 1.353e-01 | 1.372 | 0.1700 |
| DPBI | -3.234e-02 | 2.470e-02 | -1.309 | 0.1904 |
| PBIpercapita | 1.080e-03 | 5.522e-04 | 1.956 | 0.0504 . |
| Inflacion | -4.277e-01 | 2.318e-01 | -1.845 | 0.0650 . |
| CrecimPBI | 2.441e-01 | 3.045e-01 | 0.802 | 0.4227 |

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 115.426 on 85 degrees of freedom
Residual deviance: 23.771 on 80 degrees of freedom
AIC: 35.771

Number of Fisher Scoring iterations: 10



SALIDA CON MENOS VARIABLES

| | Estimate | Std. Error | z value | Pr(> z) | |
|--------------|------------|------------|---------|----------|----|
| (Intercept) | -1.806e+01 | 6.477e+00 | -2.788 | 0.00531 | ** |
| IndicePais | 2.235e-01 | 9.395e-02 | 2.379 | 0.01738 | * |
| PIBpercapita | 6.607e-04 | 2.897e-04 | 2.280 | 0.02258 | * |

Null deviance: 115.426 on 85 degrees of freedom
 Residual deviance: 34.503 on 83 degrees of freedom
 AIC: 40.503

Predicción

| | InvGrade | |
|-------|----------|------|
| SCOR1 | 0 | 1 |
| 0 | 0.89 | 0.12 |
| 1 | 0.06 | 0.94 |

EJEMPLO BAJO PESO DEL Niño AL NACER

Se desea explicar el bajo peso de los niños al nacer.

PESO: 1, SI TIENE BAJO PESO, 0 SI NO

Se tienen características de las madres: edad (AGE), peso (LWT), cantidad de visitas al médico (FTV), fuma (SMOKE), historia de hipertensión (HT), molestias uterinas (UI)

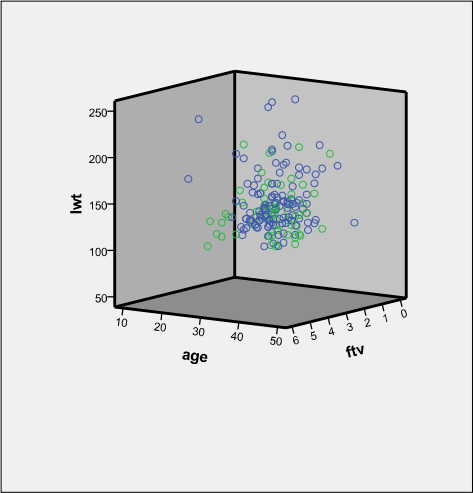
Test para discriminante lineal con 3 variables, edad, peso y cantidad de visitas

testes(peso[,c(2,3,9)], peso[,1])

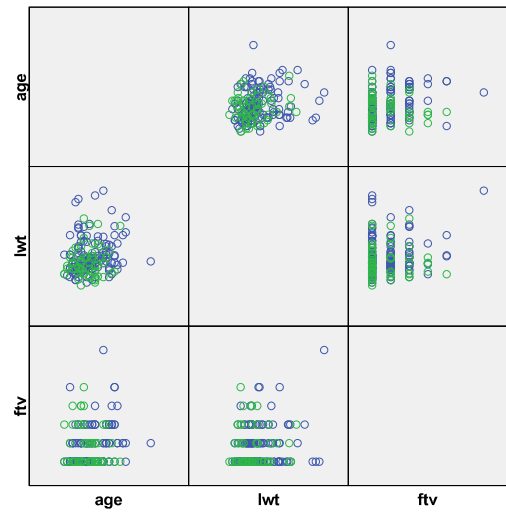
~~Test de Igualdad de Medias~~

| | Statistics | F | df1 | df2 | Pr |
|------------------------|------------|---------|-----|-----|------------|
| Wilks' Lambda | 0.96264931 | 2.39266 | 3 | 185 | 0.06997377 |
| Pillai's Trace | 0.03735069 | 2.39266 | 3 | 185 | 0.06997377 |
| Hotelling-Lawley Trace | 0.03879990 | 2.39266 | 3 | 185 | 0.06997377 |
| Roy's Greatest Root | 0.03879990 | 2.39266 | 3 | 185 | 0.06997377 |

No existe evidencia de que el vector de medias de los 2 grupos sea diferente. Esto lo podemos ver gráficamente



low
0
1



low
0
1

DISCRIMINANTE LOGISTICO CON TODAS LAS VARIABLES

Coefficients:

| | Estimate | Std. Error | z value | Pr(> z) |
|-------------|-----------|------------|---------|------------|
| (Intercept) | 0.480623 | 1.196888 | 0.402 | 0.68801 |
| age | -0.029549 | 0.037031 | -0.798 | 0.42489 |
| lwt | -0.015424 | 0.006919 | -2.229 | 0.02580 * |
| race2 | 1.272260 | 0.527357 | 2.413 | 0.01584 * |
| race3 | 0.880496 | 0.440778 | 1.998 | 0.04576 * |
| smoke | 0.938846 | 0.402147 | 2.335 | 0.01957 * |
| ptl | 0.543337 | 0.345403 | 1.573 | 0.11571 |
| ht | 1.863303 | 0.697533 | 2.671 | 0.00756 ** |
| ui | 0.767648 | 0.459318 | 1.671 | 0.09467 . |
| ftv | 0.065302 | 0.172394 | 0.379 | 0.70484 |

Predicción

| | SCOR1 | |
|-----|-----------|-----------|
| low | 0 | 1 |
| 0 | 0.9000000 | 0.1000000 |
| 1 | 0.6101695 | 0.3898305 |

Otra salida

Coefficients:

| | Estimate | Std. Error | z value | Pr(> z) |
|-------------|-----------|------------|---------|------------|
| (Intercept) | 0.056276 | 0.937853 | 0.060 | 0.95215 |
| lwt | -0.016732 | 0.006803 | -2.459 | 0.01392 * |
| race2 | 1.324562 | 0.521464 | 2.540 | 0.01108 * |
| race3 | 0.926197 | 0.430386 | 2.152 | 0.03140 * |
| smoke | 1.035831 | 0.392558 | 2.639 | 0.00832 ** |
| ht | 1.871416 | 0.690902 | 2.709 | 0.00676 ** |
| ui | 0.904974 | 0.447553 | 2.022 | 0.04317 * |

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 234.67 on 188 degrees of freedom
Residual deviance: 204.22 on 182 degrees of freedom
AIC: 218.22

Number of Fisher Scoring iterations: 4

Clasificación (punto corte 0.5)

| | SCOR2 |
|-----|---------------------|
| low | 0 1 |
| 0 | 0.9000000 0.1000000 |
| 1 | 0.6440678 0.3559322 |

Clasificación (punto corte 0.33)

| | SCOR3 | |
|-----|-----------|-----------|
| low | 0 | 1 |
| 0 | 0.7538462 | 0.2461538 |
| 1 | 0.4237288 | 0.5762712 |

EJEMPLO VINO

Se tienen 3 grupos (3 cepas distintas de vino) y la concentración de 13 productos químicos diferentes (reflejado en 13 variables).

~~Test de Igualdad de Medias~~

| Statistics | F | df1 | df2 | Pr |
|------------------------|-------------|-----------|--------|----|
| Wilks Lambda | 0.01934091 | 77.61987 | 26 326 | 0 |
| Pillai Trace | 1.70582080 | 73.15128 | 26 328 | 0 |
| Hotelling-Lawley Trace | 13.21020848 | 82.30976 | 26 324 | 0 |
| Roy Greatest Root | 9.08173944 | 114.56964 | 13 164 | 0 |

~~Test de Mardia de Multinormalidad por grupos~~

```
grupos: 1
      kappa1      pvalsim      kappa2      pvalkurt      n
489.2834848    0.1290062   -1.4231165    0.1547024     59
```

```
-----
grupos: 2
      kappa1      pvalsim      kappa2      pvalkurt      n
7.121859e+02 1.205702e-13 3.441382e+00 5.787517e-04    71
```

```
-----
grupos: 3
      kappa1      pvalsim      kappa2      pvalkurt      n
429.8665311    0.7958293   -1.5723031    0.1158803     48
```

Coefficients of linear discriminants (FUNCIONES DE CLASIFICACION VISTAS EN CLASE)

| | LD1 | LD2 |
|-----|--------------|---------------|
| V2 | -0.403399781 | 0.8717930699 |
| V3 | 0.165254596 | 0.3053797325 |
| V4 | -0.369075256 | 2.3458497486 |
| V5 | 0.154797889 | -0.1463807654 |
| V6 | -0.002163496 | -0.0004627565 |
| V7 | 0.618052068 | -0.0322128171 |
| V8 | -1.661191235 | -0.4919980543 |
| V9 | -1.495818440 | -1.6309537953 |
| V10 | 0.134092628 | -0.3070875776 |
| V11 | 0.355055710 | 0.2532306865 |
| V12 | -0.818036073 | -1.5156344987 |
| V13 | -1.157559376 | 0.0511839665 |
| V14 | -0.002691206 | 0.0028529846 |

Predicción

| obs | pred1w | | |
|-----|--------|----|----|
| | 1 | 2 | 3 |
| 1 | 59 | 0 | 0 |
| 2 | 0 | 71 | 0 |
| 3 | 0 | 0 | 48 |

Clasificación cross validation

| | pred1wC | | |
|---|---------|----|----|
| | 1 | 2 | 3 |
| 1 | 59 | 0 | 0 |
| 2 | 1 | 69 | 1 |
| 3 | 0 | 0 | 48 |

~~Test de Homogeneidad de Variancias~~

| | Statistic | df | Pr |
|-------|-----------|-----|----|
| Box.M | 764.8065 | 182 | 0 |
| adj.M | 684.2031 | 182 | 0 |

Clasificación con funciones cuadráticas

| | pred2w | | |
|---|--------|----|----|
| | 1 | 2 | 3 |
| 1 | 59 | 0 | 0 |
| 2 | 1 | 70 | 0 |
| 3 | 0 | 0 | 48 |

OTRO EJEMPLO PRESTAMOS

~~Test de Igualdad de Medias~~

| | Statistics | F | df1 | df2 | Pr |
|------------------------|------------|----------|-----|-----|----|
| Wilks Lambda | 0.7124707 | 39.89543 | 7 | 692 | 0 |
| Pillai Trace | 0.2875293 | 39.89543 | 7 | 692 | 0 |
| Hotelling-Lawley Trace | 0.4035665 | 39.89543 | 7 | 692 | 0 |
| Roy Greatest Root | 0.4035665 | 39.89543 | 7 | 692 | 0 |

~~Test de Homogeneidad de Variancias~~

| | Statistic | df | Pr |
|-------|-----------|----|----|
| Box.M | 563.2906 | 28 | 0 |
| adj.M | 554.9823 | 28 | 0 |

~~Test de Mardia de Multinormalidad por grupos~~

grupos: No

| kappa1 | pvalsim | kappa2 | pvalkurt | n |
|------------|---------|----------|----------|-----|
| 3254.15537 | 0.00000 | 58.19759 | 0.00000 | 517 |

grupos: Yes

| kappa1 | pvalsim | kappa2 | pvalkurt | n |
|------------|---------|----------|----------|-----|
| 3996.04829 | 0.00000 | 93.13884 | 0.00000 | 183 |