Análisis de Correspondencias Múltiples

Ejemplo 1 - TE

Biblioteca

Para desarrollar el Análisis de Correspondencias Múltiples (ACM) puede utilizarse la biblioteca FactoMineR como anteriormente.

- > library(FactoMineR)
- > #library(help=FactoMineR)
- > #?MCA

Datos - Ejemplo de FactoMineR

Se cargan los datos tea que están en la misma librería.

```
> data(tea)
> # str(tea); head(tea)
```

Los datos provienen de un cuestionario sobre el TÉ, aplicado a 300 encuestados, con 18 preguntas acerca de como lo toman, 12 preguntas acerca de su percepción y 4 con preguntas personales.

Se dispone de un data.frame con 300 filas una por cada encuestados y 36 columnas por cada una de las diferentes preguntas:

```
breakfast Factor w/ 2 levels: breakfast, Not.breakfast
tea.time Factor w/ 2 levels: Not.tea time, tea time
evening Factor w/ 2 levels: evening, Not.evening
lunch Factor w/ 2 levels: lunch, Not.lunch
dinner Factor w/ 2 levels: dinner, Not.dinner
always Factor w/ 2 levels: always, Not.always
```

```
work Factor w/ 2 levels: Not.work, work
 tearoom Factor w/ 2 levels: Not.tearoom, tearoom
 friends Factor w/ 2 levels: friends, Not.friends
 resto Factor w/ 2 levels: Not.resto, resto
 pub Factor w/ 2 levels: Not.pub, pub
 Tea Factor w/ 3 levels: black, Earl Grey, green
 How Factor w/ 4 levels: alone, lemon, milk, other
 sugar Factor w/ 2 levels: No.sugar, sugar
 how Factor w/3 levels: tea bag, tea bag+unpackaged, unpackaged
 where Factor w/3 levels: chain store, chain store+tea shop, tea shop
 price Factor w/6 levels: p_branded, p_cheap, p_private label, p_unknown,
     p_upscale, p_variable
   La variable continua age es considerada suplementaria y en el ejemplo se
plantean las siguientes variables como suplementarias cualitativas:
 sex Factor w/ 2 levels F,M
 SPC Factor w/7 levels employee, middle, non-worker, other worker, se-
     nior, student, workman
 Sport Factor w/ 2 levels Not.sportsman, sportsman
 age_Q Factor w/ 5 levels 15-24,25-34, 35-44, 45-59, mas60
 frequency Factor w/ 4 levels 1/day,1 to 2/week, +2/day, 3 to 6/week
 escape.exoticism Factor w/2 levels escape-exoticism, Not.escape-exoticism
 spirituality Factor w/ 2 levels Not.spirituality, spirituality
 healthy Factor w/ 2 levels healthy, Not.healthy
 diuretic Factor w/ 2 levels diuretic, Not.diuretic
 friendliness Factor w/ 2 levels friendliness, Not.friendliness
```

home Factor w/ 2 levels: home, Not.home

iron.absorptionFactor w/ 2 levels iron absorption,Not.iron absorption
feminine Factor w/ 2 levels feminine, Not.feminine
sophisticated Factor w/ 2 levels Not.sophisticated, sophisticated

slimming Factor w/ 2 levels No.slimming, slimming

exciting Factor w/ 2 levels exciting, No.exciting

relaxing Factor w/ 2 levels No.relaxing, relaxing

effect.on.health Factor w/ 2 levels effect on health, No.effect on health

breakfast tea.time evening lunch breakfast :144 Not.tea.time:131 evening :103 lunch : 44 Not.breakfast:156 tea.time :169 Not.evening:197 Not.lunch:256

dinner always home work dinner: 21 always: 103 home: 291 Not.work: 213 Not.dinner: 279 Not.always: 197 Not.home: 9 work: 87

tearoom friends pub resto Not.tearoom:242 friends :196 Not.resto:221 Not.pub:237 tearoom : 58 Not.friends:104 resto : 79 pub : 63

Tea How sugar how black : 74 alone:195 No.sugar:155 tea bag :170 Earl Grey:193 lemon: 33 sugar :145 tea bag+unpackaged: 94 : 33 milk : 63 unpackaged green

other: 9

where price chain store :192 p_branded : 95 chain store+tea shop: 78 p_cheap : 7 tea shop : 30 p_private label: 21

p_unknown : 12
p_upscale : 53
p_variable :112

age

Min. 1st Qu. Median Mean 3rd Qu. Max. 15.00 23.00 32.00 37.05 48.00 90.00

SPC Sport frequency age_Q sex F:178 employee :59 Not.sportsman:121 15-24:92 1/day : 95 1 to 2/week: 44 M:122 middle :40 sportsman :179 25-34:69 non-worker :64 35-44:40 +2/day :127 other worker:20 45-59:61 3 to 6/week: 34

senior :35 +60 :38

student :70
workman :12

escape.exoticism spirituality healthy escape-exoticism :142 Not.spirituality:206 healthy :210 Not.escape-exoticism:158 spirituality : 94 Not.healthy: 90

diuretic friendliness iron.absorption diuretic :174 friendliness :242 iron absorption : 31

Not.diuretic:126 Not.friendliness: 58 Not.iron absorption:269

feminine sophisticated slimming exciting feminine :129 Not.sophisticated: 85 No.slimming:255 exciting :116 Not.feminine:171 sophisticated :215 slimming : 45 No.exciting:184

relaxing effect.on.health

No.relaxing:113 effect on health : 66 relaxing :187 No.effect on health:234

\mathbf{ACM}

Se utilizan las primeras 18 preguntas como variables acivas, la siguiente (age) como variable suplementarias cualitativa y las últimas como variables suplementarias categóricas.

La función que realiza el ACM en FactoMineR es:

```
MCA(X, ncp = 5, ind.sup = NULL, quanti.sup = NULL,quali.sup = NULL,
graph = TRUE, level.ventil = 0, axes = c(1,2), row.w = NULL,
method="Indicator", na.method="NA", tab.disj=NULL)
```

Los principales argumentos son:

- X data frame de $I \times J$ individuos por variables categóricas
- ncp numero de dimensiones que se mantienen en los resultados
- ind.sup; quanti.sup; quali.sup vectores son los indices de individuos y variables suplementarias
- graph parámetro lógico.

```
res.mca <- MCA(tea[,1:18],graph=FALSE)</pre>
```

Call:

.ess_weave(Sweave, "/home/andres/Desktop/multivar2015/ACM/acm_lab/ejemplo1.Rnw")

Eigenvalues

	Dim.1	Dim.2	Dim.3	$\mathtt{Dim.4}$	Dim.5	Dim.6	Dim.7
Variance	0.148	0.122	0.090	0.078	0.074	0.071	0.068
% of var.	9.885	8.103	6.001	5.204	4.917	4.759	4.522
Cumulative % of var.	9.885	17.988	23.989	29.192	34.109	38.868	43.390
	Dim.8	Dim.9	Dim.10	Dim.11	Dim.12	Dim.13	Dim.14
Variance	0.065	0.062	0.059	0.057	0.054	0.052	0.049
% of var.	4.355	4.123	3.902	3.805	3.628	3.462	3.250
Cumulative % of var.	47.745	51.867	55.769	59.574	63.202	66.664	69.914
	Dim.15	Dim.16	Dim.17	Dim.18	Dim.19	Dim.20	Dim.21
Variance	0.048	0.047	0.046	0.040	0.038	0.037	0.036
% of var.	3.221	3.127	3.037	2.683	2.541	2.438	2.378
Cumulative % of var.	73.135	76.262	79.298	81.982	84.523	86.961	89.339
	Dim.22	Dim.23	Dim.24	Dim.25	Dim.26	Dim.27	

```
Variance
                        0.035
                                0.031
                                        0.029
                                                 0.027
                                                         0.021
                                                                  0.017
% of var.
                        2.323
                                2.055
                                         1.915
                                                 1.821
                                                         1.407
                                                                  1.139
                                                97.454
Cumulative % of var.
                      91.662
                               93.717
                                       95.633
                                                        98.861 100.000
Categories (the 10 first)
                 Dim.1
                           ctr
                                 cos2 v.test
                                                 Dim.2
                                                          ctr
                                                                 cos2 v.test
                 0.166
breakfast
                        0.495
                                0.025
                                       2.756 | -0.166
                                                        0.607
                                                                0.026 -2.764 |
Not.breakfast | -0.153
                                                 0.154
                                                        0.560
                        0.457
                                0.025 - 2.756
                                                                0.026
                                                                       2.764 \mid
Not.tea time
              1 - 0.498
                         4.053
                                0.192 -7.578 |
                                                 0.093
                                                        0.174
                                                               0.007
                                                                       1.423 l
                                       7.578 | -0.072
tea time
                 0.386
                        3.142
                                0.192
                                                        0.135
                                                               0.007 -1.423 |
                 0.319
                         1.307
                                0.053
                                       3.985 | -0.058
                                                        0.053
                                                                0.002 - 0.728
evening
Not.evening
              | -0.167
                        0.683
                                0.053 -3.985 |
                                                 0.030
                                                        0.028
                                                               0.002 0.728 |
lunch
                 0.659
                        2.385
                                0.075
                                       4.722 | -0.390
                                                        1.018
                                                                0.026 - 2.793
Not.lunch
                                0.075 -4.722 |
                                                 0.067
              -0.113
                        0.410
                                                        0.175
                                                               0.026
                                                                       2.793 |
               -0.661
                                0.033 -3.136 |
dinner
                         1.146
                                                 0.796
                                                        2.025
                                                                0.048
                                                                       3.774
Not.dinner
                 0.050
                         0.086
                                0.033 3.136 | -0.060
                                                        0.152
                                                               0.048 -3.774 |
                               cos2 v.test
               Dim.3
                         ctr
breakfast
              -0.483
                      6.900
                              0.215 -8.017 |
Not.breakfast
               0.445
                       6.369
                              0.215
                                     8.017 |
                                     4.027 I
Not.tea time
               0.265
                       1.886
                              0.054
tea time
              -0.205
                       1.462
                              0.054 -4.027
evening
               0.451
                       4.312
                              0.106
                                    5.640 l
              -0.236
                       2.254
                              0.106 -5.640 |
Not.evening
                       0.822
lunch
               0.301
                              0.016 2.160
Not.lunch
              -0.052
                      0.141
                              0.016 -2.160
                       1.235
dinner
               0.535
                              0.022
                                    2.537
Not.dinner
              -0.040
                      0.093
                              0.022 -2.537 |
Categorical variables (eta2)
                Dim.1 Dim.2 Dim.3
breakfast
              | 0.025 0.026 0.215 |
tea.time
               | 0.192 0.007 0.054 |
evening
              | 0.053 0.002 0.106 |
               | 0.075 0.026 0.016 |
lunch
               0.033 0.048 0.022 |
dinner
always
              | 0.045 0.001 0.101 |
               0.005 0.000 0.134 |
home
work
              | 0.112 0.043 0.005 |
               | 0.372 0.022 0.008 |
tearoom
```

| 0.243 0.015 0.103 |

friends

La función devuelve una lista:

- eig eigenvalues, %de variancia y acumulada
- var resultados para las variables activas
- var\$coord coordenadas de las categorías
- var\$cos2 cos2 para las categorías
- var\$contrib contribuciones de las categorías
- ind resultados para los individuos
- ...sup resultados para las variables suplementarias

```
plot(x, axes = c(1, 2), choix=c("ind","var","quanti.sup"), xlim = NULL, ylim = N
invisible = c("none","ind","var","ind.sup","quali.sup","quanti.sup"),col.ind = "
```

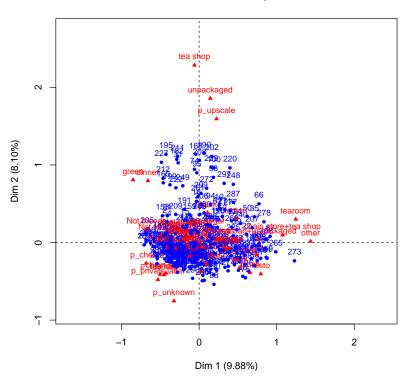
Los argumentos mas importantes son:

- x objeto de clase MCA
- axes vector de los 2 componentes a graficar
- choix "ind", "var", "quanti.sup" . . .
- xlim; ylim; invisible; col.ind; col.var; col.quali.sup...

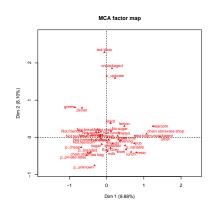
Los gráficos disponibles de forma inmediata son:

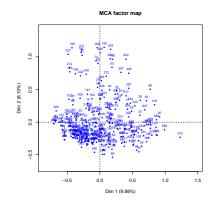
- El del plano principal con la representación simultánea de individuos y modalidades de las variables.
 - > pdf('ej1_varind.pdf');plot(res.mca,cex=0.8);graphics.off()

MCA factor map



- Alternativamente pueden graficarse por separado, usando el argumento invisible= para no desplegar algunos de los elementos
 - > pdf('ej1_ind.pdf');plot(res.mca,invisible=c("var"),cex=0.7)
 - > pdf('ej1_var.pdf');plot(res.mca,invisible=c("ind"),cex=0.8)
 - > graphics.off()





- Si la ejecución de la función MCA fué realizada con elementos suplementarios, estos también pueden graficarse.
- Por defecto se grafica el plano principal, pero con el argumento axes pueden graficarse otros planos: plot(res.mca,axes=c(1,3))
- Se pueden controlar muchos parámetros gráficos, por ejemplo, límites, colores, etiquetas, títulos, etc: ?plot.MCA

Adicionalmente, como ayudas a la interpretación pueden utilizarse:

- Al igual que con otras técnicas/objetos del package: dimdesc(res.mca)
- plotellipses(res.mca,keepvar=1:4)