Compatition Coach Toolkit

This is a collection of lists, formulas and terms that Mathletes frequently use to solve problems like those found in this handbook. There are many others we could have included, but we hope you find this collection useful.

Fraction	Decimal	Percent
1/2	0.5	50
1/3	0.3	$33.\overline{3}$
1/4	0.25	25
1/5	0.2	20
1/6	$0.1\overline{6}$	$16.\overline{6}$
1/8	0.125	12.5
1/9	0.1	11. 1
1/10	0.1	10
1/11	0.09	9.09
1/12	$0.08\bar{3}$	8.3

Fraction	Decimal	Percent
1/2	0.5	50
1/3	0.3	33.3
1/4	0.25	25
1/5	0.2	20
1/6	0.16	16.6
1/8	0.125	12.5
1/9	0.1	11. 1
1/10	0.1	10
1/11	0.09	9.09
1/12	0.083	8.3

n	n²	n³
1	1	1
2	4	8
3	9	27
4	16	64
5	25	125
6	36	216
7	49	343
8	64	512
9	81	729
10	100	1000
11	121	1331
12	144	1728
13	169	2197
14	196	2744
15	225	3375

Common Arithmetic Series		
$1 + 2 + 3 + 4 + \dots + n = \frac{n(n+1)}{2}$		
$1 + 3 + 5 + 7 + \cdots + (2n - 1) = n^2$		
$2 + 4 + 6 + 8 + \dots + 2n = n^2 + n$		

Combinations & Permutations		
$_{n}C_{r}=\frac{n!}{r!(n-r)!}$	$_{n}P_{r}=\frac{n!}{(n-r)!}$	

Prime Numbers		
2	43	
3	47	
5	53	
7	59	
11	61	
13	67	
17	71	
19	73	
23	79	
29	83	
31	89	
37	97	
41		

Geometric Mean $\frac{a}{x} = \frac{x}{b}$ and $x = \sqrt{ab}$

2: units digit is 0, 2, 4, 6 or 8 3: sum of digits is divisible by 3 4: two-digit number formed by tens and units digits is divisible by 4 5: units digit is 0 or 5

Divisibility Rules

- 6: number is divisible by both 2 and 3 8: three-digit number formed by hundreds, tens and units digits is divisible by 8
- 9: sum of digits is divisible by 9
- 10: units digit is 0

Equation of a Line

Standard Form

Ax + By = C

Slope-Intercept Form

$$y = mx + b$$

m = slope

b = y-intercept

Point-Slope Form

$$y - y_1 = m(x - x_1)$$

m = slope

 (x_1, y_1) = point on the line

Distance Traveled

Distance = Rate × Time

Quadratic Formula

For $ax^2 + bx + c = 0$, where $a \neq 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Pythagorean Triples

(3, 4, 5)

(5, 12, 13)

(7, 24, 25)

(8, 15, 17)

(9, 40, 41)

(12, 35, 37)

Difference of Squares

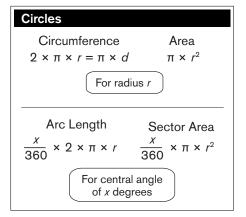
$$a^2 - b^2 = (a + b)(a - b)$$

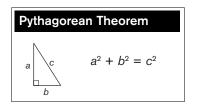
Sum and Difference of Cubes

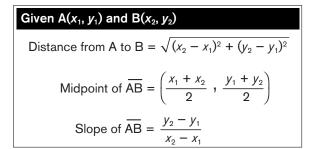
$$a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

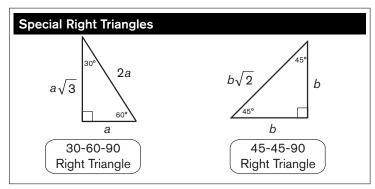
$$a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

MATHCOUNTS 2018-2019 46









Area of Polygons		
Square	side length s	S^2
Rectangle	length /, width w	/×w
Parallelogram	base b, height h	b × h
Trapezoid	bases b_1 , b_2 , height h	$\frac{1}{2}(b_1+b_2)\times h$
Rhombus	diagonals d_1 , d_2	$\frac{1}{2} \times d_1 \times d_2$
Triangle	base b, height h	$\frac{1}{2} \times b \times h$
Triangle	semi-perimeter <i>s</i> , side lengths <i>a</i> , <i>b</i> , <i>c</i>	$\sqrt{s(s-a)(s-b)(s-c)}$
Equilateral Triangle	side length s	$\frac{s^2\sqrt{3}}{4}$

Polygon Angles	(n sides)	
Sum of the interior angle measures:		
180	$0 \times (n-2)$	
Central angle meas	sure of a regular polygon:	
360		
	n	
Interior angle meas	ure of a regular polygon:	
$180 \times (n-2)$	or 180 – 360	
n	n 100 –	

Solid	Dimensions	Surface Area	Volume
Cube	side length s	$6 \times s^2$	s^3
Rectangular Prism	length <i>I</i> , width <i>w</i> , height <i>h</i>	$2\times(l\times w+w\times h+l\times h)$	$l \times w \times h$
Circular Cylinder	base radius <i>r</i> , height <i>h</i>	$2 \times \pi \times r \times h + 2 \times \pi \times r^2$	$\pi \times r^2 \times h$
Circular Cone	base radius <i>r</i> , height <i>h</i>	$\pi \times r^2 + \pi \times r \times \sqrt{r^2 + h^2}$	$\frac{1}{3} \times \pi \times r^2 \times h$
Sphere	radius <i>r</i>	$4 \times \pi \times r^2$	$\frac{4}{3}\times \pi \times r^3$
Pyramid	base area <i>B</i> , height <i>h</i>		$\frac{1}{3} \times B \times h$

MATHCOUNTS 2018-2019 47