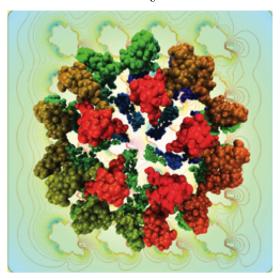
# Reference Manual

Poisson Boltzmann Analytical Model (PB-AM)



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For more information, please visit  $\mbox{http://thglab.berkeley.edu}$  Cover Illustration: An exploded view of a Brome Mosaic Virus capsid composed of T=1 particles (PDB: 1YC6), represented as collections of overlapping spheres, is shown. PB-SAM is a new semi-analytical approach to efficiently solve the linearized Poisson? Boltzmann equation using multipole formalisms for overlapping spheres. The background shows the potential profile for an array of 601YC6 monomers computed using this method.

#### **Recommended Citations:**

When citing PB-AM in the literature, the following citation should be used

I. Lotan and T. Head-Gordon (2006). An analytical electrostatic model for salt screened interactions between multiple proteins J. Chem. Theory Comput 2, 541-555.

When citing PB-SAM in the literature, the following citations should be used

- 1. E.-H. Yap and T. Head-Gordon (2010). New and efficient Poisson-Boltzmann solver for interaction of multiple proteins J. Chem. Theory Comput. (Journal cover) 6, 2214-2224.
- 2. E.-H. Yap and T. Head-Gordon (2013). Calculating the bimolecular rate of protein?protein association with interacting crowders. J. Chem. Theory Comput. 9(5), 2481-2489.
- 3. O. N. Demerdash, E.-H. Yap and T. Head-Gordon (2014). Advanced potential energy surfaces for condensed phase simulation. Ann. Rev. Phys. Chem. 65, 149-174.

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## Chapter 1

#### Introduction

The Poisson-Boltzmann Analytical Model solves the linearized Poisson-Boltzmann Equation (PBE) for systems hitherto not possible using traditional PBE solvers. This manual describes the method and its associated suite of programs. The PBE software suite is licensed as a collection of freely available program under a GPL license.

#### 1.1 PB-AM

The first general analytical solution for computing the screened electrostatic interaction between large numbers of macromolecules of arbitrarily complex charge distributions, assuming they are well described by spherical low dielectric cavities in a higher dielectric medium in the presence of a Debye-Hückel treatment of salt. The method exploits multipole expansion theory for the screened Coulomb potential such that it can describe direct charge-charge interactions and all higher-order cavity polarization effects between low dielectric spherical cavities containing their charges, while treating these higher order terms correctly at all separation distances. The analytical solution is general to arbitrary numbers of macromolecules, is efficient to compute, provides for the first time the ability to provide new benchmarks for other numerical solutions to the linearized Poisson-Boltzmann equation. A number of utilities are described below that use PB-AM results.

### 1.2 Physical Calculations

The PB-AM results allow for fast calculation of physically important quantities. Specifically this program can calculate the energy of, and the force and torque applied to each molecule. These results may be written into a file or printed to the terminal.

### 1.3 Brownian Dynamics

This package also implements dynamics simulations using the Brownian protocol developed by Ermak and McCammon<sup>1</sup>. At each time step, the translation and rotation due to the applied force and torque, respectively, are calculated and added to random components of motion. The user can specify spatial and temporal termination conditions for the simulation and write the trajectory to specified files.

#### 1.4 Electrostatics

<sup>&</sup>lt;sup>1</sup>Ermak, D. L.; McCammon, J. A. J. Chem. Phys. 1978, 69, 1352–1360.

## Chapter 2

## Theory

#### 2.1 PB-AM formulation

PB-AM is an analytical solution to the linearized Poisson-Boltzmann equations for multiple spherical objects of arbitrary charge distribution in an ionic solution. The linearized Poisson-Boltzmann equation is given as:

$$\nabla[\epsilon(r)\nabla\phi(r)] - \epsilon(r)\kappa^2\phi(r) = 4\pi\rho(r)$$

$$\phi_{out}^{(i)} = \phi_{out}^{(i)}\Big|_{r=a_i}$$

$$\epsilon_s \frac{\partial\phi_{out}^{(i)}}{\partial r} = \epsilon_s \frac{\partial\phi_{out}^{(i)}}{\partial r}\Big|_{r=a_i}$$

Exploiting fast-multipole methods, this boundary value problem can be reduced to the following system of linear equations.

$$A = \Gamma \cdot (\Delta \cdot T \cdot A + E)$$

A(i) represents the effective multipole expansion of the charge distributions of molecule (i). E(i) is the free charge distribution of molecule (i).  $\Gamma$  is a dielectric boundary-crossing operator,  $\Delta$  a cavity polarization operator,  $\Gamma$  an operator that transforms the multipole expansion to a local coordinate frame. More details on the method are available in Lotan, Head-Gordon (2006).

#### 2.1.1 Physical Calculations

From the above formulation, computation of the interaction energies  $(\Omega^{(i)})$  is given as follows:

$$\Omega^{(i)} = \frac{1}{\epsilon_s} \langle T \cdot A^{(i)}, A^{(i)} \rangle$$

Where  $\langle M, N \rangle$  denotes the inner product. When energy is computed, forces follow as:

$$\mathbf{F}^{(i)} = \nabla_i \Omega^{(i)} = \frac{1}{\epsilon_s} [\langle \nabla_i \, T \cdot A^{(i)}, A^{(i)} \rangle + \langle T \cdot A^{(i)}, \nabla_i \, A^{(i)} \rangle]$$

The method to calculate the torque  $\tau^{(i)}$  on molecule is outside the scope of this manual, but is discussed extensively in Lotan, Head-Gordon (2006).

#### 2.1.2 Brownian Dynamics

Brownian dynamics simulations are implemented by treating each molecule as a Brownian particle experiencing a conservative force  $\mathbf{F}^{(i)}$  and torque  $\boldsymbol{\tau}^{(i)}$ , as well as friction and random force due to the solvent. The translation  $\Delta r_i$  and rotation  $\Delta \theta_i$  for a time step  $\Delta t$  are then given by

$$\Delta r^{(i)} = \frac{D_{i,trans}\Delta t}{k_B T} \mathbf{F}^{(i)} + \mathbf{S}_i(\Delta t)$$

$$\Delta \theta^{(i)} = \frac{D_{i,rot}\Delta t}{k_B T} \boldsymbol{\tau}^{(i)} + \boldsymbol{\Theta}_i(\Delta t)$$

where  $D_{i,trans}$  and  $D_{i,rot}$  are the translation and rotational diffusion coefficients for molecule i, respectively and  $\mathbf{S}_i(\Delta t)$  and  $\mathbf{\Theta}_i(\Delta t)$  are the stochastic components of translation and rotation, respectively, which have the following properties:

$$\langle \mathbf{S}_i \rangle = 0, \qquad \langle \mathbf{S}_i^2 \rangle = 2D_{i,trans} \Delta t$$

$$\langle \mathbf{\Theta}_i \rangle = 0, \qquad \langle \mathbf{\Theta}_i^2 \rangle = 2D_{i,rot} \Delta t$$

### 2.1.3 Electrostatics

## Chapter 3

#### Use

#### 3.1 Installation

To install this program, first download the source code from the GitHub repository:

```
$ git clone https://github.com/davas301/pb_solvers.git
```

Then navigate to the directory pb\_solvers/pbam. From here, make a build and bin directory, use CMake to create a make file and then make the program. This is done as follows:

- \$ cd pb\_solvers/pbam
- \$ mkdir build bin
- \$ cd build
- \$ cmake ..
- \$ make install

An executable named pbam will now be in pb\_solvers/bin.

## 3.2 Input Information

#### Input Files

The program executable requires an input file as a command line parameter. The input file contains the various arguments and parameters that one may wish to set when running the program. Each line of the input file contains a keyword followed by a variable number of whitespace-delimited parameters, e.g.:

```
keyword1 param1 param2
keyword2 param1 param2 param3
```

Each keyword is described in the table below, along with its associated parameters.

Keyword	Parameters	Description
runname	<name></name>	<name> is desired internal name of this run.</name>
pqr	<fpath></fpath>	Provide input PQR file at <fpath>.</fpath>
xyz	<fpath></fpath>	Provide input XYZ file at <fpath>.</fpath>
salt	<con></con>	Set salt concentration in the system to <con>.</con>
$\operatorname{temp}$	<t></t>	Set system temperature to <t></t>
idiel	<pre><ival></ival></pre>	Set the interior dielectric constant to <ival>.</ival>
sdiel	<sval></sval>	Set the interior dielectric constant to <sval>.</sval>
$\operatorname{pbc}$	<pre><boxlength></boxlength></pre>	Set size of periodic box to <boxlength>.</boxlength>
$\operatorname{random}$	<seed></seed>	Seed the internal random number generator with <seed>.</seed>
attypes	<numtypes></numtypes>	Set the number of different atom types to <numtypes>.</numtypes>
type	<pre><idx> <ct> <movetype> <dtr> <drot></drot></dtr></movetype></ct></idx></pre>	Set attributes of an atom type, where <idx> is the integer id of this type, which can be 1 to <numtypes> (above). <ct> is the number of atoms of this type in the system and <movetype> describes the way this type is allowed to move in a dynamics run (move, rot, or stat). If <movetype> is move, then a translational diffusion coefficient <dtr> and a rotational diffusional coefficient <drot> are required. If <movetype> is rot then just <drot> is required.</drot></movetype></drot></dtr></movetype></movetype></ct></numtypes></idx>
runtype electrostatics	<gridpts></gridpts>	Will run electrostatics calculations. <gridpts> is an optional integer describing the number of evenly spaced points in each dimension to perform calculations on.</gridpts>
$\mathrm{d}\mathbf{x}$	<fname></fname>	For electrostatics. Will write the results of electrostatics calculations for every 3D grid point to <fname>.</fname>
$\operatorname{gridct}$	<ct></ct>	For electrostatics. <ct> is the number of 2D grids to output.</ct>
grid2d	<idx> <fname> <axis> <val></val></axis></fname></idx>	For electrostatics. Set attributes of a grid output where <idx> is the integer id of this grid, which can be 1 to <ct> (above). Will write output of calculations for a cross section along <a href="mailto:axis">axis</a> (x, y, or z) at <value>.</value></ct></idx>
runtype dynamics		Will perform a brownian dynamics run.
termet	<ct></ct>	Set number of termination conditions to $\langle ct \rangle$ .
termcombine	<andor></andor>	Set how termination conditions will be combined. <andor> should be and or or. Default is or.</andor>
term	<pre><idx> <type> <val> <mols></mols></val></type></idx></pre>	Set attributes of a termination condition where <idx> is the integer id of this condition, which can be 1 to <ct> (above). <type> can be time, contact, x&lt;=, y&lt;=, z&lt;=, or r&lt;= (or the &gt;= equivalents of these), <val> is the value where the simulation will terminate and <mols> is a whitespace-delimited list of molecular indices that this condition applies to (contact requires 2, time requires 0, and all else require 1).</mols></val></type></ct></idx>

#### System inputs

All the options above require a PQR file name. A PQR file can be generated from a PDB file using the PDB2PQR program, available as a web server or for download at:

```
http://nbcr-222.ucsd.edu/pdb2pqr_1.9.0/
http://www.poissonboltzmann.org/docs/pdb2pqr-installation/
```

It may also be formatted manually. The general format of a PQR file is as follows, and is whitespace-delimited:

recName serial atName resName chainID resNum X Y Z charge rad

Parameter	Description
recName	A string that should either be ATOM or HETATM.
serial	An integer that provides the atom index
atName	A string that provides the atom name.
resName	A string that provides the residue name.
chainID	An optional string that provides the chain ID of the atom.
residueNumber	An integer that provides the residue index.
X Y Z	Three floats that provide the atomic coordinates.
charge	A float that provides the atomic charge (in electrons).
Rad	A float that provides the atomic radius (in Å).