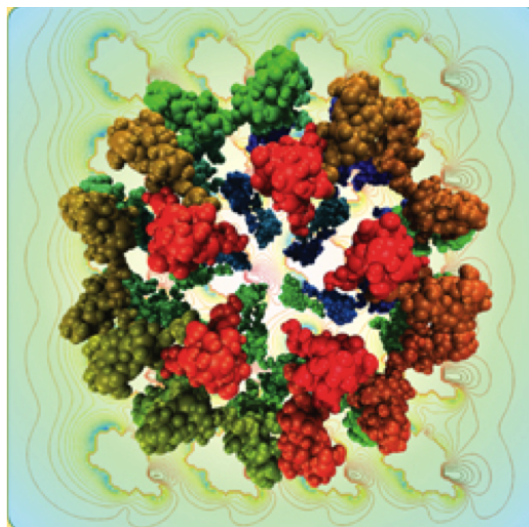


Reference Manual
Poisson Boltzmann Analytical Model (PB-AM)
and
Poisson-Boltzmann Semi-analytical Model (PB-SAM)



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For more information, please visit <http://thglab.berkeley.edu>

Cover Illustration: An exploded view of a Brome Mosaic Virus capsid composed of $T = 1$ particles (PDB: 1YC6), represented as collections of overlapping spheres, is shown. PB-SAM is a new semi-analytical approach to efficiently solve the linearized Poisson-Boltzmann equation using multipole formalisms for overlapping spheres. The background shows the potential profile for an array of 601YC6 monomers computed using this method.

Recommended Citations:

When citing PB-AM in the literature, the following citation should be used

I. Lotan and T. Head-Gordon (2006). An analytical electrostatic model for salt screened interactions between multiple proteins J. Chem. Theory Comput 2, 541-555.

When citing PB-SAM in the literature, the following citations should be used

1. E.-H. Yap and T. Head-Gordon (2010). New and efficient Poisson-Boltzmann solver for interaction of multiple proteins J. Chem. Theory Comput. (Journal cover) 6, 2214-2224.
2. E.-H. Yap and T. Head-Gordon (2013). Calculating the bimolecular rate of protein-protein association with interacting crowders. J. Chem. Theory Comput. 9(5), 2481-2489.
3. O. N. Demerdash, E.-H. Yap and T. Head-Gordon (2014). Advanced potential energy surfaces for condensed phase simulation. Ann. Rev. Phys. Chem. 65, 149-174.

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Chapter 1

Introduction

The Poisson-Boltzmann Analytical Model solves the linearized Poisson-Boltzmann Equation (PBE) for systems hitherto not possible using traditional PBE solvers. This manual describes the method and its associated suite of programs. The PBE software suite is licensed as a collection of freely available program under a GPL license.

1.1 PB-AM

The first general analytical solution for computing the screened electrostatic interaction between large numbers of macromolecules of arbitrarily complex charge distributions, assuming they are well described by spherical low dielectric cavities in a higher dielectric medium in the presence of a Debye-Hckel treatment of salt. The method exploits multipole expansion theory for the screened Coulomb potential such that it can describe direct charge-charge interactions and all higher-order cavity polarization effects between low dielectric spherical cavities containing their charges, while treating these higher order terms correctly at all separation distances. The analytical solution is general to arbitrary numbers of macromolecules, is efficient to compute, provides for the first time the ability to provide new benchmarks for other numerical solutions to the linearized Poisson-Boltzmann equation. A number of utilities are described below that use PB-AM results.

1.2 Brownian Dynamics

1.3 Electrostatics

Chapter 2

Poisson-Boltzmann Analytical Model (PB-AM)

2.1 The Model

2.1.1 PB-AM formulation

PB-AM is an analytical solution to the linearized Poisson-Boltzmann equations for multiple spherical objects of arbitrary charge distribution in an ionic solution. The linearized Poisson-Boltzmann equation is given as:

$$\nabla[\epsilon(r)\nabla\phi(r)] - \epsilon(r)\kappa^2\phi(r) = 4\pi\rho(r)$$

$$\phi_{out}^{(i)} = \phi_{out}^{(i)} \Big|_{r=a_i}$$

$$\epsilon_s \frac{\partial \phi_{out}^{(i)}}{\partial r} = \epsilon_s \frac{\partial \phi_{out}^{(i)}}{\partial r} \Big|_{r=a_i}$$

Exploiting fast-multipole methods, this boundary value problem can be reduced to the following system of linear equations.

$$A = \Gamma \cdot (\Delta \cdot T \cdot A + E)$$

$A(i)$ represents the effective multipole expansion of the charge distributions of molecule (i). $E(i)$ is the free charge distribution of molecule (i). Γ is a dielectric boundary-crossing operator, Δ a cavity polarization operator, T an operator that transforms the multipole expansion to a local coordinate frame. More details on the method are available in Lotan, Head-Gordon (2006).

From this formulation, computation of the interaction energies ($\Omega^{(i)}$) is given as follows:

$$\Omega^{(i)} = \frac{1}{\epsilon_s} \langle T \cdot A^{(i)}, A^{(i)} \rangle$$

Where $\langle M, N \rangle$ denotes the inner product. When energy is computed, forces follow as:

$$F_i = \nabla_i \Omega^{(i)} = \frac{1}{\epsilon_s} [\langle \nabla_i T \cdot A^{(i)}, A^{(i)} \rangle + \langle T \cdot A^{(i)}, \nabla_i A^{(i)} \rangle]$$

2.2 Installation

2.2.1 PB-AM Installation

TODO

2.2.2 PB-AM: Example input files and input file information

Program option

The program executable requires an input file as a command line parameter. The input file contains the various arguments and parameters that one may wish to set when running the program. Each line of the input file contains a keyword followed by a variable number of whitespace-delimited parameters, e.g.:

```
keyword1    param1    param2
keyword2    param1    param2    param3
```

Each keyword is described in the table below, along with its associated parameters.

Keyword	Parameters	Description
runname	<name>	<name> is desired internal name of this run.
pqr	<fpath>	Provide input PQR file at <fpath>.
xyz	<fpath>	Provide input XYZ file at <fpath>.
salt	<con>	Set salt concentration in the system to <con>.
temp	<T>	Set system temperature to <T>
idiel	<ival>	Set the interior dielectric constant to <ival>.
sdiel	<sval>	Set the interior dielectric constant to <sval>.
pbc	<boxlength>	Set size of periodic box to <boxlength>.
random	<seed>	Seed the internal random number generator with <seed>.
attypes	<numtypes>	Set the number of different atom types to <numtypes>.
type	<idx> <ct> <movetype> <dtr> <drot>	Set attributes of an atom type, where <idx> is the integer id of this type, which can be 1 to <numtypes> (above). <ct> is the number of atoms of this type in the system and <movetype> describes the way this type is allowed to move in a dynamics run (move , rot , or stat). If <movetype> is move , then a translational diffusion coefficient <dtr> and a rotational diffusional coefficient <drot> are required. If <movetype> is rot then just <drot> is required.
runtype electrostatics	<gridpts>	Will run electrostatics calculations. <gridpts> is an optional integer describing the number of evenly spaced points in each dimension to perform calculations on.
dx	<fname>	For electrostatics. Will write the results of electrostatics calculations for every 3D grid point to <fname>.
gridct	<ct>	For electrostatics. <ct> is the number of 2D grids to output.
grid2d	<idx> <fname> <axis> <val>	For electrostatics. Set attributes of a grid output where <idx> is the integer id of this grid, which can be 1 to <ct> (above). Will write output of calculations for a cross section along <axis> (x, y, or z) at <value>.
runtype dynamics		Will perform a brownian dynamics run.

System inputs

From the single mpe executable, multiple types of calculations can be performed. Generally, all the programs require a computation flag, and a PDB or PQR file name. If a PDB file is chosen the input is read and atoms are assigned partial charges according to the file charges.OPLS, located in each of the test directories. A PQR file can be generated from the online site or the software can be downloaded:

<http://nbc-222.ucsd.edu/pdb2pqr.1.9.0/>

<http://www.poissonboltzmann.org/docs/pdb2pqr-installation/>

It may also be formatted manually. The general format of a PQR file is as follows, and is whitespace-delimited:

recName serial atName resName chainID resNum X Y Z charge rad

Delimiter	Description
recName	A string that should either be ATOM or HETATM.
serial	An integer that provides the atom index
atName	A string that provides the atom name.
resName	A string that provides the residue name.
chainID	An optional string that provides the chain ID of the atom.
residueNumber	An integer that provides the residue index.
X Y Z	Three floats that provide the atomic coordinates.
charge	A float that provides the atomic charge (in electrons).
Rad	A float that provides the atomic radius (in Å).