



A Comparison of Neuroimaging Software and a Spatial Confidence Sets Method for inference on Task-fMRI data

by

Alexander Bowring

St Catherine's College

Submitted to the University of Oxford

for the degree of

Doctor of Philosophy

Nuffield Department of Population Health

October 2019



Contents

Acknowledgments	iv
Declarations	v
Abstract	vi
1 Introduction	1
2 Background	7
2.1 The Study of Brain Function	8
2.2 Blood Oxygenation Level Dependant (BOLD) Functional Magnetic Resonance Imagery (fMRI)	10
2.2.1 Physiology of the BOLD response	11
2.3 Task-based functional Magnetic Resonance Imagery (t-fMRI)	12
2.4 Overview of Analysis Pipeline	14
2.5 Preprocessing	15
2.5.1 Brain Extraction	15
2.5.2 Distortion Correction	16
2.5.3 Slice timing Correction	16
2.5.4 Realignment	17
2.5.5 Coregistration	18
2.5.6 Spatial Normalization	18
2.5.7 Spatial Smoothing	18
2.5.8 Temporal Filtering	19
2.5.9 Grand Mean Scaling	20
2.6 Modelling of t-fMRI data with the General Linear Model	20
2.6.1 The GLM Set-up	21
2.6.2 Estimating the Parameters with Ordinary Least Squares (OLS)	21
2.6.3 Prewitthing	22
2.6.4 Estimating the Variance	23

2.6.5	Inference with Null-Hypothesis Significance Testing	23
2.6.6	First-Level (Subject-Level) Analysis	24
2.6.7	Second-Level (Group-Level) Analysis	25
2.6.8	Solving the Second-Level GLM with Homoscedastic Errors . .	28
2.6.9	Solving the Second-Level GLM with Heteroscedastic Errors . .	28
2.7	The Multiple Comparisons Problem	29
2.7.1	Random Field Theory for Voxelwise FWE Correction	31
2.7.2	Permutation Testing for Voxelwise FWE Correction	32
2.8	Conclusion	34
3	Exploring the Impact of Analysis Software on Task-fMRI Results	35
3.1	Data and Analysis Methods	35
3.1.1	Study Description and Data Source	35
3.1.2	Data Analyses	36
3.1.3	Comparison Methods	45
3.1.4	Permutation Test Methods	47
3.1.5	Scripting of Analyses and Figures	48
3.2	Results	49
3.2.1	Cross-Software Variability for Parametric Inference	49
3.2.2	Cross-Software Variability for Nonparametric Inference . . .	61
3.2.3	Intra-Software Variability, Parametric vs Nonparametric . . .	62
3.3	Discussion	65
3.3.1	Limitations	67
3.4	Conclusion	69
4	Spatial Confidence Sets for Task-fMRI Inference	71
4.1	Introduction	71
4.2	Theory	71
4.2.1	Overview	71
4.2.2	The Wild Bootstrap Method for Computation of k	74
4.2.3	Approximating the Boundary on a Discrete Lattice	75
4.2.4	Assessment of Continuous Coverage on a Discrete Lattice . .	76
4.3	Method	79
4.3.1	Simulations	79
4.3.2	Implementation of Contour Inference	79
4.3.3	2D Simulations	79
4.3.4	3D Simulations	79
4.3.5	Application to Human Connectome Project Data	79

4.4	Results	79
4.4.1	2D Simulations	79
4.4.2	3D Simulations	79
4.4.3	Human Connectome Project	79
4.5	Discussion	79
4.5.1	Limitations	79
4.6	Conclusion	79
4.7	Toolbox	79
5	Contour Inference for Cohen's d	80
5.1	Theory	80
5.1.1	Transforming the Residual Field	80
5.2	Method	80
5.2.1	2D Simulations	80
5.2.2	3D Simulations	80
5.2.3	Application to UK Biobank Data	80
5.3	Results	80
5.3.1	2D Simulations	80
5.3.2	3D Simulations	80
5.3.3	UK Biobank Data	80
5.3.4	Comparison to Traditional Inference Procedures	80
5.4	Discussion	80
5.4.1	Limitations	80
5.5	Conclusion	80
6	Conclusion and Future Work	81

Acknowledgments

Declarations

I, Alexander Bowring, hereby declare that except where specific reference is made to the work of others, the content of this dissertation is original and has not been submitted in whole or in part for consideration for any other degree or qualification in these, or any other Universities. This dissertation is the result of my own work and includes nothing which is the outcome of work done in collaboration, except where specifically indicated in the text.

- The work presented in Chapter 3 has been published in the *Human Brain Mapping* journal (Bowring et al., 2019). This work was presented at the *Organization for Human Brain Mapping* (OHBM) Annual Meetings in 2017 and 2018. At the OHBM 2018 Annual Meeting, this work was the recipient of an oral presentation and a Merit Abstract Award.
- The work presented in Chapter 4 has been published in the *NeuroImage* journal (Bowring et al., 2018). This work was presented at the OHBM Annual Meeting in 2017, where it was the recipient of an oral presentation.
- The work presented in Chapter 5 is based on a pre-printed manuscript.

Alexander Bowring
September 2019

Abstract

Over the last three decades, Functional Magnetic Resonance Imaging (fMRI) has rapidly progressed to become the primary tool for human brain mapping. Recently however, considerable attention within the field has been directed towards data-sharing and open science initiatives. This has been driven by a growing apprehension about the reproducibility of findings within the neuroimaging literature, amid concerns that current inference procedures are often misused or misinterpreted such that the overall scientific conclusions become distorted. One aspect specific to neuroimaging pinpointed as a cause for poor reproducibility is the high flexibility of a typical fMRI workflow. In the first part of this thesis, we investigate how the choice of software package used to conduct a statistical analysis can influence the group-level results of a task-fMRI study. We use publicly shared data from three published task-fMRI studies, and reanalyze each study within the three main neuroimaging software packages, AFNI, FSL and SPM, using parametric and nonparametric inference. All information on how to process, analyze, and model each dataset we obtain from the publications. We use a variety of quantitative and qualitative comparison methods to gauge the scale of variability in our results and assess fundamental differences between each software package. While qualitatively we find broad similarities between packages, we also discover marked differences, such as Dice similarity coefficient values ranging from 0.000 to 0.743 in comparisons of thresholded statistic maps between software. We discuss the challenges involved in our replication attempt, while also utilizing open science tools in an effort to make our own research reproducible. In the second part of this thesis, we extend a contour inference method initially proposed by [Sommerfeld, Sain, and Schwartzman \(2018\)](#) SSS to develop spatial confidence sets (CSs) on clusters found in thresholded blood-oxygen-level dependent (BOLD) effect size maps. While traditional inferences based on hypothesis testing indicate where the null, i.e. an effect size of zero, can be rejected, the CSs give statements about where effect sizes exceed a *positive* threshold analogous to confidence intervals simultaneously across the entire brain. We make advancements to theoretical aspects and implementation of contour inference to improve the method's finite-sample performance. We extend the wild bootstrap theory presented in SSS, proposing a method based on the t-bootstrap, and recommend that the bootstrapped residuals are multiplied by Rademacher variables instead of Gaussian variables. We also develop a linear interpolation method for computing the topological boundary over which the bootstrap is applied. Notably, we demonstrate that

the framework used in SSS for assessing simulations manifests considerable positive bias in the simulation results, and propose our own novel construction to solve this issue. In the final part of this thesis, we make further theoretical developments to contour inference so that the method can operate on the Cohen's d and partial R^2 effect sizes commonly reported at the end of a neuroimaging study. For the second and third parts of this thesis, we carry out intensive Monte Carlo simulations on synthetic 3D data to investigate the accuracy of contour inference on signals representative of fMRI activation clusters. We also demonstrate the method on two 'big' fMRI datasets, obtaining confidence sets to localize activation in functional data from the Human Connectome Project and UK Biobank.

CHAPTER 1

Introduction

Since its inception at the end of the twentieth century, functional Magnetic Resonance Imaging (fMRI) has experienced a meteoric rise to become the primary tool for human brain mapping. While many forms of the technique exist, introduction of the particular method based on the Blood Oxygenization Level Dependant (BOLD) effect has ultimately been the catalyst in elevating fMRI to such stature within the neuroimaging community. Taking advantage of the magnetic properties of oxygen-rich red blood cells, BOLD fMRI measures changes in blood oxygenization alongside cerebral blood flow and volume as a proxy to identify brain areas where elevated neuronal activity has occurred in response to a stimulus. While the relationship between the BOLD effect and neuronal activity is complex and remains controversial, it is the unique attributes of BOLD fMRI – in particular, its capacity for non-invasive recording of signals across the entire brain at a high spatial resolution – that set the technique apart from other scanning methods.

However, BOLD fMRI is also a *noisy* process. The MR signals researchers set out to measure during a scanning session are corrupted by artefacts from both the imaging hardware and the physiology of the participant. Examples of scanner noise include inhomogeneities of the magnetic field that can cause spatial distortion or blurring in the MR image, and scanner drift characterized by temporal degradation of the signal. Physiological noise induced by subject motion, respiration, and heart-beat exacerbate the problem.

Because of the low signal-to-noise, researchers must apply a series of statistical techniques to find meaning in the data. This usually entails carrying out a number of preprocessing, modelling and analysis steps that together constitute the fMRI processing pipeline. The fundamental objectives of preprocessing are to standardize brain locations across participants, to apply methods ensuring that the data conform to statistical assumptions required for analysis, and to reduce the influence of the

aforementioned noise artefacts present in the data. This is achieved by conducting a number of steps, including slice-timing correction, motion correction, normalization, registration of the functional data to an anatomical template, and spatial smoothing.

For task-based fMRI, a mass-univariate approach is utilized to model the data. During the scanning session, functional data are acquired in the form of voxels – cubic intensity units that partition the brain comparable to the way in which pixels partition a computer screen. Each voxel's time-series is considered independently within the general linear model framework as a combination of signal components. To evaluate the effect of an experimental task condition relative to a baseline condition, hypothesis testing is performed at each voxel to compute a statistical parametric map of t -statistic values. Here, the behaviour of the signal under the null hypothesis of no activation is estimated using either a parametric approach, appealing to the body of mathematics known as Random Field Theory, or a nonparametric approach, where permutation methods are applied to estimate the null-distribution directly from the data. Finally, the statistical parametric map is thresholded to localize brain function.

While we have provided a brief overview of the fMRI analysis pipeline, it is notable that there is not a general consensus as to how each particular analysis step should be carried out. Consequently, researchers have the freedom to make many choices during an analysis, such as how much smoothing is applied to the data, or how the hemodynamic response of blood flow to active neuronal tissues is modelled. However, this ‘methodological plurality’ comes with a drawback. While conceptually similar, two different analysis pipelines applied on the same dataset may not produce the same scientific results, and mathematical modelling has shown that the high analytic flexibility associated with fMRI can potentially distort the final scientific findings of an investigation ([Ioannidis, 2005](#)). The problem is, with so many statistically valid methodological strategies available, if you try them all you are likely to find *something*. Combined with further issues such as p -hacking and publication bias – where there has been evidence to suggest that studies finding a significant effect are disproportionately represented in the fMRI literature ([David et al., 2013; Ioannidis et al., 2014](#)) – these conditions have created the perfect storm: In recent years, many attempts to replicate the results of published fMRI studies have been unsuccessful, in what has been deemed as an ongoing reproducibility crisis within the field ([Poldrack et al., 2017; Gorgolewski and Poldrack, 2016; Open Science Collaboration, 2015](#)).

The degree to which varying methodological decisions can lead to discrepancies in observed results has been investigated extensively. Choices for each individual procedure in the analysis pipeline (for example, head-motion regression ([Lund et al., 2005](#)), temporal filtering ([Skudlarski et al., 1999](#)), and autocorrelation correc-

tion (Woolrich et al., 2001) alongside the order in which these procedures are conducted (Carp, 2013) can all deeply influence the final determined areas of brain activation. In perhaps the most comprehensive of such studies (Carp, 2012), a single publicly available fMRI dataset was analyzed using over 6,000 unique analysis pipelines, generating 34,560 unique thresholded activation images. These results displayed a substantial degree of flexibility in both the sizes and locations of significant activation.

Alongside issues concerned with the flexibility of the analysis workflow, the statistical procedures carried out for fMRI inference have also come under intense scrutiny. Because statistical tests are conducted at each brain voxel independently, the *p*-values used to threshold the statistical parametric map are corrected to account for the large number of simultaneous comparisons being carried out and limit the expected number of voxels falsely declared as significant. This is almost always done using a false discovery rate correction procedure (Benjamini and Hochberg, 1995) or a Bonferroni correction to limit the family-wise error rate of making at least one significant finding.

The importance of such statistical correction methods were made prominent within the neuroimaging community using a humorous example, where one author identified significant activation in the brain of a dead salmon after applying inference with uncorrected *p*-values (Bennett et al., 2009). However, in recent times they have been a source of major controversy. In 2016, a shocking paper by Eklund, Nichols, and Knutsson (2016) discovered that many fMRI software packages were incorrectly carrying out the multiple-correction procedures for clusterwise inference, inflating the false-positive rate to up to 70%. In a damning blow to the field, the implications of this study brought into question the validity of thousands of published fMRI results.

While the relevant software packages have now been patched, deeper conceptual problems have been raised regarding the fMRI approach to inference. Specifically, there is a considerable amount of information that is not captured when applying inference using cluster-size. In this setting, a significant *p*-value only indicates that a cluster is larger than expected by chance, and although a significant cluster may have a large spatial extent, since we can only infer that at least one voxel in the cluster has statistically significant signal, spatial specificity is low (Woo et al., 2014). In addition, this method does not provide a measure of the spatial variation of significant clusters. For illustration, imagine that a single fMRI study is repeated using two varying cohorts of participants; whereas we would expect moderate differences in the size and shape of clusters within each cohort's group-level thresholded map, current statistical results do not characterize this variability.

A more pressing issue stems from an age-old paradox caused by the fallacy of the null hypothesis (Rozeboom, 1960). The paradox is that while the statistical models used for fMRI conventionally assume mean-zero noise, in reality all sources of noise will *never* completely cancel. Therefore, improvements in experimental design will eventually lead to statistically significant results, and the null-hypothesis will, eventually, *always* be rejected (Meehl, 1967). The recent availability of ambitious, large-sample studies (e.g Human Connectome Project (HCP), N = 1,200; UK Biobank, N = 30,000 and counting) have exemplified this problem. Analysis of high-quality fMRI data acquired under optimal noise conditions has been shown to display almost universal activation across the entire brain after hypothesis testing, even with stringent correction (Gonzalez-Castillo et al., 2012). For these reasons, there is an increased urgency for methods that can provide meaningful inference to interpret all significant effects.

In this work, we make contributions in two thematic areas currently challenging the field of task-based fMRI: Firstly, the need for further transparency to the degree in which the body of work comprising the fMRI literature is reproducible. Secondly, the need for further statistical methods to improve current inference practices carried out within the field. To end this section, we summarize our main contributions before providing an outline of the organisation of this dissertation:

1. While we have already discussed a number of studies exploring how decisions made at each stage of the analysis pipeline can influence the final scientific results of an fMRI investigation, for all of these studies the fundamental decision of which analysis software package the pipeline was conducted through remained constant. This is despite a vast array of analysis packages that are used throughout the neuroimaging literature, the most popular of which are AFNI, FSL and SPM. Motivated by this, in Chapter 2 we comprehensively assess how each of these software packages can impact analysis results by reanalyzing three published task-fMRI neuroimaging studies and quantifying several aspects of variability between the three package's group-level statistical maps. Our findings suggest that exceedingly weak effects may not generalise across software. We are unaware of any comparable exercise in the literature.
2. In carrying out this software comparison exercise, we implement a range of quantitative methods for the novel application of comparing fMRI statistical maps. These include Dice statistic comparisons, for assessing differences in the determined regions of activation between the three software's thresholded statistical maps, Bland-Altman plots, for assessing differences between the magni-

tude of the t -static values in the unthresholded maps, Euler Characteristics, for assessing differences in the topological properties of each software's activation profile, and Neurosynth analyses, for assessing differences in the anatomical regions associated to each software's activation pattern. We believe these methods are generalizable and hope they may benefit any further comparison of neuroimaging results.

3. In Chapter 3, we develop an inference method originally proposed for application on geospatial data in [Sommerfeld, Sain, and Schwartzman \(2018\)](#) SSS to create spatial confidence sets on clusters found in fMRI percentage BOLD effect size maps. While currently used hypothesis testing methods indicate where the null, i.e. an effect size of zero, can be rejected, this form of inference allows for statements about anatomical regions where effect sizes have exceeded, and fallen short of, a *non-zero* threshold, such as areas where a BOLD change of 2.0% has occurred.
4. In developing the inference method proposed by SSS, we make theoretical advancements that improve the performance of the confidence sets, particularly for 3D data with moderate sample sizes. We also find that the methods used to assess the empirical coverage for simulations presented in SSS are positively biased. We develop our own weighted-interpolation method for assessing empirical coverage, and on using this method, our simulation results validate the asymptotical mathematical theory set out in SSS.
5. In Chapter 4, we make further theoretical advancements to the confidence sets for application on the Cohen's d and partial R^2 effect sizes.

This dissertation is organized into five chapters: Chapter 2 is dedicated to presenting the context of this work and providing background on the current methodological procedures carried out for analysis of task-fMRI data, with a particular emphasis on the statistical inference methods relevant to this thesis. In Chapter 3, we assess the analytic variability of group-level task-fMRI results under the choice of software package through which the analysis is conducted. We reanalyze three published task-fMRI studies whose data has been made publicly available, attempting to replicate the original analysis procedure within each software package. We then make a number of comparisons to assess the similarity of our results. In Chapter 4, we develop the inference method originally proposed in SSS to create spatial confidence sets on clusters found in fMRI percentage BOLD effect size maps. We summarize the theory in SSS before detailing our proposed modifications. We then carry

out intensive Monte Carlo simulations to investigate the accuracy of the confidence sets on synthetic 3D signals representative of clusters found in fMRI effect size maps. Furthermore, we illustrate the method by computing confidence sets on 80 subject's percentage BOLD data from the Human Connectome Project working memory task. In Chapter 5 we make further theoretical developments to the inference method for application on the Cohen's d and partial R^2 effect sizes commonly used in a task-fMRI study. Finally, in Chapter 6 we conclude this dissertation and provide further discussion of possibilities for future work.

CHAPTER 2

Background

In this chapter, we provide the context that forms the basis of our research. We begin by presenting a broad overview of the study of brain function, before narrowing down to the specific field of task-based functional Magnetic Resonance Imaging (t-fMRI) that will be the main focus of study in this thesis. Here, we describe each of the preprocessing and modelling components of a typical t-fMRI analysis pipeline. Finally, we give an in-depth discussion of the state-of-the-art procedures used for subject- and group-level t-fMRI inference that are of particular relevance to the remaining chapters of this work.

2.1 The Study of Brain Function

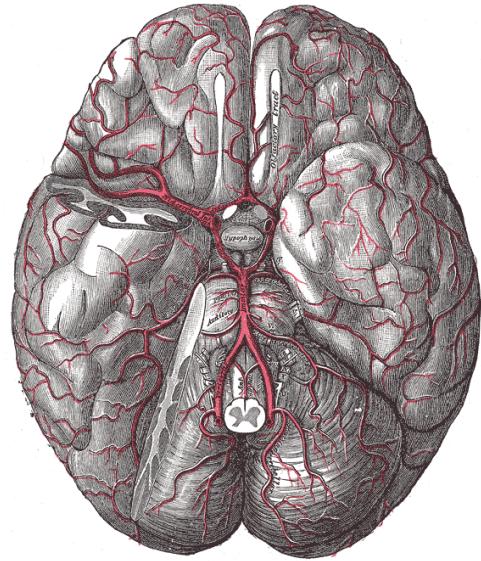


Figure 2.1: An illustration showing the arteries at the base of the human brain. Reprinted from [Anatomy \(1918\)](#).

The human brain, the central organ of the human nervous system, has been described as one of the most complex structures in the known universe. Made up of approximately 86 billion neurons ([Azevedo et al., 2009](#)), where neuronal interaction occurs continuously via trillions of synaptic networks to form intricate and dynamic neural networks, the myriad of processes taking place inside the brain at any given time make the study of brain function an intimidating challenge. Nonetheless, our understanding of this organ has come along way from our ancient Egyptian ancestors, who believed that the heart was the source of human intelligence, and for whom the practice of drilling a hole into the skull was regarded as a solution to cure a headache ([Adelman and Others, 1987; Mohamed, 2014](#)).

Remarkably, much of this progress has come in the last century alone. A number of key developments within this time-frame include: Confirmation of the neuron doctrine, the concept that the nervous system is a collection of discrete individual cells, postulated by Santiago Ramon y Cajal at the end of the 19th century and demonstrated in the 1950s thanks to the development of electron microscopy ([López-Muñoz et al., 2006](#)); the first evidence of neuroplasticity, the ability for the brain's structure to change during an individual's lifetime ([Diamond et al., 1964; Bennett et al., 1964](#)); and the emergence of neuroimaging techniques such as electroencephalography (EEG), positron emission tomography (PET), and magnetic resonance

imaging (MRI). The tools of this scientific endeavour are now translating into concrete advancements influencing a wide variety of aspects concerned with population health. Neuroscience research is beginning to find applications in the clinical setting to advance our understanding of neurodevelopmental and neurodegenerative disorders and generate novel therapies to treat and prevent such diseases. Brain imaging has been used to localize the source of neurological impairment for diseases such as epilepsy ([Stacey and Litt, 2008](#)), and neuroengineering techniques based on our capability to stimulate neural circuits are implemented to treat Parkinson's disease ([Kalia et al., 2013](#)) and dystonia ([Fox and Alterman, 2015](#)). Structural- and functional-MRI are being explored to determine biomarkers for diagnosis of Alzheimer's disease *prior* to symptom onset ([Sperling et al., 2014](#); [McEvoy et al., 2009](#)), alongside providing information about the role of different brain regions in human behaviour that can contribute to an improved prognosis and patient response to therapy ([Matthews et al., 2006](#)).

Modern neuroscience can be dissected into many major branches, each sub-field taking a specific slant to studying the nervous system. It is therefore perhaps unsurprising that in isolation, the phrase 'the study of brain function' is rather vague. Brain function can manifest itself in ways that can be observed using a variety of different measurements, whether that be with a molecular, chemical, structural, or functional approach ([Hargreaves and Klimas, 2012](#)). Different modalities of MRI are employed to evaluate specific properties that ultimately characterize whichever approach is taken. For instance, looking at brain function from an anatomical perspective, voxel-based morphometry (VBM) could be used to measure differences in local concentrations of brain tissue, to assess changes in grey matter volume ([Mechelli et al., 2005](#)). Additionally, one could apply diffusion tensor imaging (DTI) to instead map white matter tractography in the brain ([Alexander et al., 2007](#); [Soares et al., 2013](#)). From a functional outlook, resting state fMRI (rs-fMRI) determines that spatially remote brain areas are functionally connected when each region's BOLD response is temporally correlated in the absence of an explicit task ([Lee et al., 2013](#)). On the other hand, task-based fMRI (t-fMRI) measures spatio-temporal changes in the BOLD signal between task-stimulated and control states to find brain regions that are activated in the presence of a stimulus ([Glover, 2011](#)).

Each imaging method and modality does not live inside a vacuum, and recent work within the field has provided further insight of the interdependence between different approaches to examining brain function. One example of this is in the study of resting state networks, which explores how distinct sets of brain regions can reveal temporally correlated activation patterns when the brain is at rest.

While resting state networks have been most widely investigated using rs-fMRI techniques (e.g. [Smith et al., 2009](#); [Lee et al., 2012](#); [Moussa et al., 2012](#)), more recently, the same correlation patterns have been independently detected using EEG and MEG ([Brookes et al., 2011](#); [Fomina et al., 2015](#)). This work not only demonstrates how utilization of numerous tools can further our understanding of resting state mechanisms, but also suggests a direct relationship between the electro-physiological signals recorded with MEG and the BOLD fluctuations associated to fMRI. Similarly, other recent efforts have shown that the functional response to a cognitive task measured with t-fMRI may be able to be predicted by connectivity features from the same individual's brain at rest ([Parker Jones et al., 2017](#); [Tavor et al., 2016](#)). This research signals towards an innate functional signature that defines our behaviour, while also providing potential clinical solutions to obtain t-fMRI data from patients who are unable to perform the specific task of interest.

In the context of this thesis, we will study brain function from a functional perspective, primarily focussed on task-based fMRI.

2.2 Blood Oxygenation Level Dependant (BOLD) Functional Magnetic Resonance Imagery (fMRI)

Whereas structural MRI is concerned with the anatomy of the brain, functional MRI (fMRI) measures dynamic changes in blood flow in order to ultimately make inference on neuronal activation. This is possible due to the intrinsic relationship between local neuronal activity and subsequent changes in cerebral blood flow (CBF), a biological phenomenon known as neurovascular coupling. An increased supply of oxygen is carried by haemoglobin in red blood cells to provide energy to active neurons, and it is the magnetic properties of the haemoglobin that MRI takes advantage of. Specifically, as deoxygenated haemoglobin is more magnetic (paramagnetic) than oxygenated haemoglobin, MRI uses haemoglobin as an endogenous contrast agent from which to source the signal. Neurovascular coupling induces inhomogeneities in the local magnetic field due to a decreased concentration of deoxygenated haemoglobin, that lead to a detectable change in the MR signal.

The complete chain of events linking neuronal activity to a change in MRI signal is referred to as the Blood Oxygenation Level Dependant (BOLD) effect, and this type of imaging is known as BOLD fMRI. Proof of concept of the BOLD effect was first provided in [Ogawa, Lee, Kay, and Tank \(1990\)](#), and the first use of BOLD fMRI for human brain mapping was carried out in 1992 ([Bandettini et al., 1992](#); [Kwong et al., 1992](#); [Ogawa et al., 1992](#)), leading to a large uptake of the method that has

continued to this day. Alternative approaches to functional imaging exist, the most popular of which is functional Arterial Spin Labelling (fASL), that uses magnetically labelled arterial blood water to quantify changes in CSF. While fASL can offer some advantages over fMRI, and changes in CSF measured with this technique are more closely tied to neuronal activation than the BOLD signal, fASL suffers from a much lower signal-to-noise ratio that has consequently made fMRI the preferred imaging modality of choice.

2.2.1 Physiology of the BOLD response

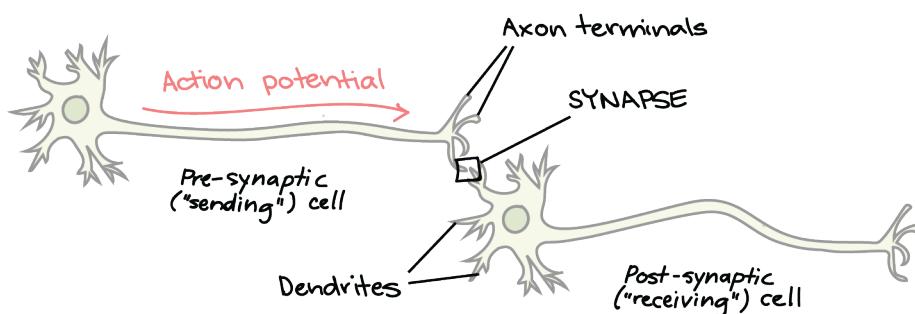


Figure 2.2: A schematic of the interaction between neurons. Image reused from Khan Academy¹ (CC BY-NC-SA 3.0 US).

Neuronal interaction transpires via a system of electrical and chemical activity. To send out information, an individual neuron – the pre-synaptic cell – emits an electrical signal known as an action potential, for the purpose of stimulating another target neuron – the post-synaptic cell. The action potential travels along the axon of the sending cell, and is transmitted to the receiving cell at the synapse. Information is delivered from the output branches (or, *axon terminals*) of the sending cell across the synapse to the input branches (or, *dendrites*) of the receiving cell, involving the release of chemical *neurotransmitters* alongside a number of other cellular processes. This may stimulate or inhibit the firing of action potentials at the target cell to communicate with other neurons, eventually leading to a configuration of neurons collectively processing and responding to information.

The electrical and chemical processes involved in neuronal activation require energy, which drives the neurovascular coupling. Blood vessels that flow into the capillaries pervading the neuronal tissue dilate and the rate of CBF increases to regulate a greater supply of oxygen and nutrients to localized regions of active neurons. Overall, the increases in CBF and cerebral blood volume (CBV) are many orders of

¹All Khan Academy content is available for free at www.khanacademy.org.

magnitude greater than the increases in oxygen extraction (CMRO_2) caused by the neuronal activation. Thus, there is an overall net increase of oxygenated haemoglobin, and an increase in the BOLD signal. The expected BOLD response generated from a brief stimulus is characterized quantitatively by the Hemodynamic Response Function (HRF), encompassing the individual changes in CBF, CBV and CMRO_2 induced by neuronal stimulation.

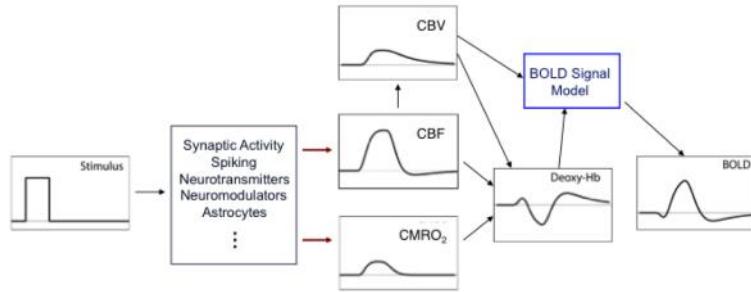


Figure 2.3: The current BOLD signal model. In the presence of a stimulus, changes in biological parameters such as CBF, CBV and CMRO_2 influence the final observed BOLD response. Reprinted from [Buxton \(2012\)](#), with permission from Elsevier.

2.3 Task-based functional Magnetic Resonance Imagery (t-fMRI)

The ultimate goal of a task-based functional Magnetic Resonance Imagery (t-fMRI) experiment is to understand the brain regions that are responsive to a particular task or stimulus the researcher has chosen to investigate. Explicitly, the researcher seeks to detect brain areas whose BOLD time series data is correlated to the task the participant is instructed to perform in the scanner. Researchers can choose from a wide range of possible tasks to explore how the brain processes in a variety of circumstances. For example, a cognitive task may be chosen to gain insight into how the brain processes decision-making or recognition, while a physiological task may be used to see how the brain reacts to a stimulus intended to cause pain or arousal, or how the brain functions when participants are told to hold their breath. In general, the experimenter is only limited in choice of task by the constraints that the task must be able to be conducted within the scanner, and that the task should not involve any sort of head movement which could corrupt the signal.

The MR signal measured in the scanner is noisy, and the haemodynamic response induced by a stimulus only causes fractional changes in the BOLD response, typically of around one percent. Therefore, in order to increase the signal-to-noise ratio (SNR) of the BOLD signal participants repeat the task several times in the scan-

ner. The type of task used, alongside the timings for which the participant is instructed to perform the task inside the scanner, are together known as the *task paradigm* or *experimental design*. Many different task conditions can be investigated within one task paradigm, however, it is fundamental that at least two conditions are included. This is because BOLD data are not quantitative, insofar that we are unable to interpret the level of neuronal activity from the absolute magnitude of the BOLD response alone. Instead, neuronal activity is inferred by using *contrasts* to measure the difference in the MR signal between two conditions. Commonly, the BOLD response to a task condition is contrasted with a *baseline* condition, where the participant is at rest within the scanner. However, it is equally acceptable to contrast two separate task conditions depending on the aims of the investigation.

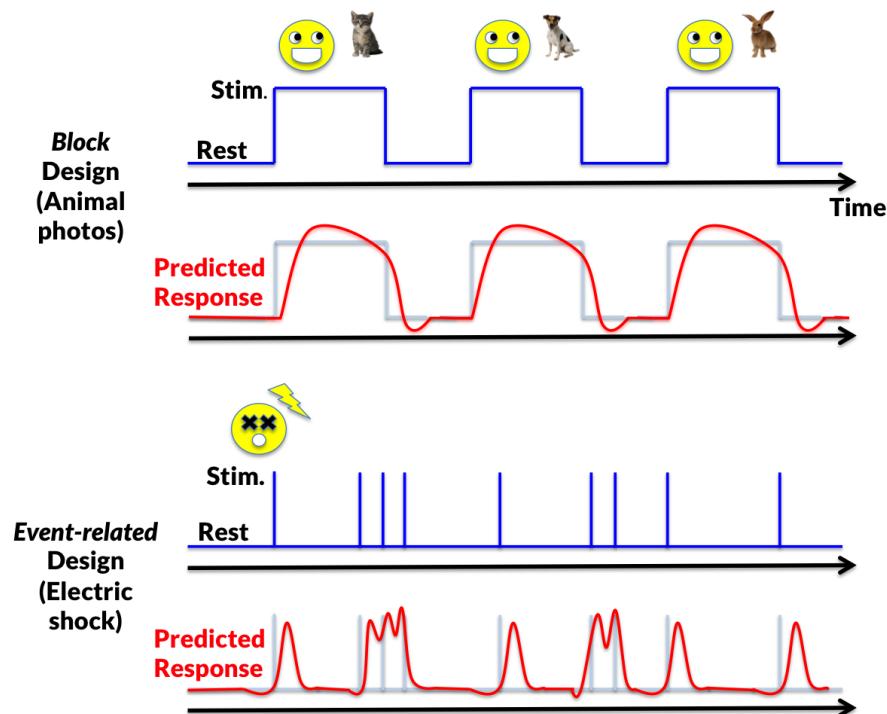


Figure 2.4: The stimulus onset timings (blue) and expected response (red) for a task paradigm using a block design, where participants look at animal photos (top half), and a task paradigm using an event-related design, where participants are given a mild electric shock (bottom half).

An experimental design where the task condition is carried out for an extended period of time is said to have a *block design* (or *boxcar design*). One example of this could be a task paradigm where the participant is instructed to look at an animal photo for five seconds in each task repetition. Alternatively, in an *event-related* design

the task or stimulus takes the form of a discrete, rapid event, such as a study where the participant experiences a mild electric shock. A graphical representation of each of these task paradigms is shown in Figure 2.4, showing the *onset timing function* along with the anticipated response for both types of stimuli. While block designs have greater statistical power, with a relatively larger BOLD response, the researcher has more control with respect to how the stimuli are delivered in an event-related design.

2.4 Overview of Analysis Pipeline

To analyse voxelwise t-fMRI BOLD data, a series of analysis steps are performed on the data in succession. Together, the complete chain of analysis procedures carried out is known as the analysis *pipeline*. Researchers have great flexibility as to how the analysis pipeline is comprised, with various options and adjustable parameters for each individual analysis step, as well as choices as to the order in which certain procedures are conducted. Nevertheless, a standard analysis pipeline of t-fMRI data can be partitioned into three main stages: preprocessing, modelling, and statistical inference. In the upcoming sections we will describe the individual processing steps that are usually carried out in each of these analysis stages, while here we provide a brief overview.

The main goals of preprocessing are to reduce the severity of noise artefacts present in the raw BOLD fMRI data, and to prepare the data for statistical analysis. At the modelling stage, a mass-univariate approach is adopted, whereby each voxel's functional time series data is considered independently as an instance of the general linear model (GLM) framework. Within the GLM, the contrasts discussed in the previous section are formulated to statistically test the main hypotheses investigated within the study. At the inference stage, a *statistical parametric map* is generated containing statistic values at each voxel for each contrast of interest. For *subject-level* inference, a participant's statistical parametric map is thresholded to display only voxels showing statistically significant results. This type of inference may be of interest in a clinical setting, particularly to aid in the diagnosis of a patient, however in a research study there is usually a greater emphasis placed on finding results that generalize across the larger population. In this case, each participant's statistic map is entered into a second-level model for *group-level* inference, and a thresholded map is computed to localize effects that were consistent across all individuals in the study.

In practice, the analysis pipeline is usually carried out within a neuroimaging *software package*. Various software packages are available, many of which are freely distributed on the internet. The three most popular packages are AFNI ([Cox, 1996](#)),

FSL ([Jenkinson et al., 2012](#)), and SPM ([Penny et al., 2011](#)). While there are several differences as to how each software package operates, most packages follow the same fundamental principles to implement the three main stages of the analysis pipeline.

2.5 Preprocessing

In this section, we present each of the analysis steps that are typically conducted within a t-fMRI preprocessing pipeline: brain extraction, distortion correction, slice-timing correction, realignment, coregistration, spatial normalization, spatial smoothing, temporal filtering and intensity normalization. These procedures are carried out to compensate for artefacts present in the data, and to ensure that the data satisfy the assumptions used for modelling and inference.

2.5.1 Brain Extraction

Brain extraction is commonly the first procedure carried out in the analysis pipeline, with the purpose of removing the skull and any other non-brain tissue from a participant's anatomical image. Since the purpose of the analysis is to infer areas of activation *within* the brain, conceptually it is sensible to remove any external structures that are not of interest. However, brain extraction also has a more important role in improving the outcome of subsequent steps in the preprocessing pipeline. In the upcoming sections we describe *coregistration*, where the subject's functional data is spatially realigned to the anatomical image, as well as *spatial normalization*, where each participant's data is registered to a standard space. Brain extraction helps to increase the robustness of both of these registration methods, since differences in non-brain structures can sidetrack the registration algorithms causing an inaccurate alignment of the respective images.

In SPM, brain extraction is carried out by first applying a *segmentation* to the anatomical image, in order to generate probability maps of the gray and white matter tissue in the structural scan. The grey and white matter probability maps are summed and thresholded, creating a binary map containing the brain regions to be included in the analysis. Finally, the anatomical scan is masked with the binary map to remove any non-brain structures. AFNI and FSL both use variants of the Brain Extraction Tool ([Smith, 2002](#)) algorithm, implementing an adaptive model that evolves to fit the brain's surface in order to segment brain and non-brain tissue types.

2.5.2 Distortion Correction

Distortion correction is applied to account for signal loss and geometric distortions in the functional data that can manifest due to spatial inhomogeneities in the main static magnetic field during the acquisition. These inhomogeneities arise due to the different magnetic susceptibility properties of each tissue type in the brain, and the most severely affected regions are those close to air-filled sinuses, such as the temporal or frontal lobe. If not corrected, signal dropout and distortion can cause failure in the registration of the functional data to the non-distorted anatomical image.

While it is not possible to recover regions of signal loss, field distortions can be rectified with the use of a *field map*. A field map is obtained as part of the acquisition to estimate the intensity of the static magnetic field. The analysis software uses the field map to calculate the magnitude of the geometric distortions, and then applies spatial transformations to unwarped the functional data. The field map is also used to de-weight areas of substantial signal dropout during the registration, and if the signal loss is particularly severe, ignore these locations in the analysis of the data.

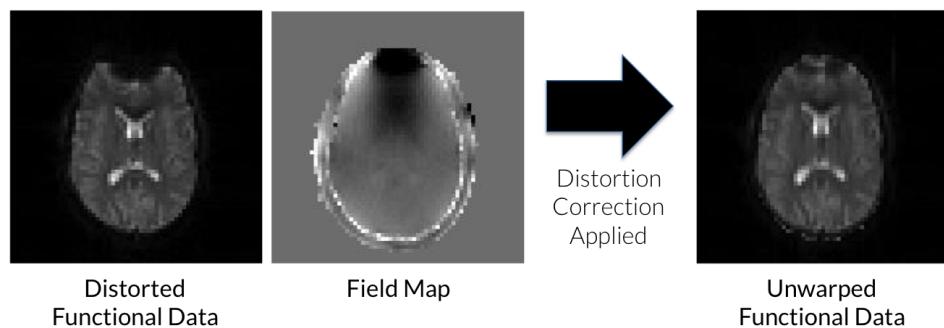


Figure 2.5: Distortion correction applied to functional data with the use of a field map. While lost signal can not be recovered, the correction has vastly improved distorted regions in the frontal lobe. Functional data and field map images reprinted from the *fMRI Graduate Programme* lecture notes¹, with the kind permission of Mark Jenkinson.

2.5.3 Slice timing Correction

While the statistical modelling of fMRI data assumes that the signal is measured over the entire brain simultaneously, in reality functional imaging is usually carried out on a slice-by-slice basis, creating a single 3D volume as a combination of multiple 2D slices. Slices are acquired sequentially from top-to-bottom or bottom-to-top, or by using an interleaved sequence where all odd-numbered slices are collected first, followed by the even slices. Because of this, the BOLD signal is sampled at different

¹<https://fsl.fmrib.ox.ac.uk/fslcourse/>

points of the HRF. This can create the illusion that the signal peaks earlier for slices that are collected later in the acquisition, even though the underlying response is identical.

Slice timing correction uses temporal interpolation methods to artificially obtain an intensity estimate at each brain voxel at a single time point, shifting the data to recreate the image as if all measurements were obtained collectively. The reference time point is commonly chosen to be halfway through the scanning procedure, and in this case the timings from all slices are corrected to match-up with the timings of the volume collected midway in the acquisition, which acts as the reference slice. The time series data from each voxel is temporally shifted to line-up with the signal response from the reference slice, and the voxel's data between the acquisition time points of the reference slice are re-estimated with interpolation. Commonly, this is done using either sinc or spline interpolation.

It is debatable whether slice timing correction should be conducted before or after realignment, and some practitioners have suggested that slice timing correction should be excluded from the analysis pipeline altogether. One alternative to slice timing correction is to account for timing differences at the modelling stage of the analysis. FSL recommend that temporal derivatives are incorporated as extra regressors into the GLM, effectively making the model flexible to temporal shifts in the signal response.

2.5.4 Realignment

While a participant is told to remain as still as possible in the scanner, over the course of the acquisition some head movement is inevitable. This is particularly problematic in fMRI, as it can corrupt the functional data in numerous ways. If left uncorrected, head movement may cause a voxel's time series data to contain signal from two different tissue types, and if the voxel is located at the edge of the brain, may lead to a loss of signal altogether. Additionally, the change in signal intensity induced by head motion can be many orders of magnitude greater than the BOLD effect. Therefore, if head motion is elicited by the task the participant performs in the scanner, this can lead to false activations in the statistical results that invalidate the analysis.

Realignment (or *motion correction*) of the functional data is performed to remove any substantial movement throughout the time series. To do this, each volume in the time series is spatially transformed to match a reference volume, usually chosen as the first volume of the data or an average image of all the scans. Specifically, a rigid-body transformation of translations and rotations is applied to superimpose each volume onto the reference image. The transformation is determined to opti-

mize a cost function that quantifies the goodness of alignment between the images, e.g. a least squares (used by default in SPM) or normalised correlation (used by default in FSL) cost function. Finally, the transformed data are spatially interpolated to obtain estimates of the signal response on the same voxel grid as the reference image, usually with spline interpolation.

2.5.5 Coregistration

In order to carry out group analyses, corresponding voxels between each participant's functional data should contain information from the same physical anatomical location. However, prior to normalizing data *between* subjects, *coregistration* is conducted to align a participant's functional time series data with their own anatomical image. Similar to realignment, coregistration is achieved via a rigid-body transformation chosen to minimize an appropriate cost function. However, to account for differences between the blurry, distorted functional data and the high-resolution structural image, scalings are also included as parameters of the rigid-body transformation, and a mutual information cost function is commonly used.

2.5.6 Spatial Normalization

The goal of *spatial normalization* (or *intersubject registration*) is to warp all participants functional time series data into a universal coordinate space, integrating the data between subjects to facilitate for group analyses. To remove structural variability between subjects, each participant's data is spatially transformed onto a standard template brain image. The most commonly used templates are the MNI152 images, created by the Montreal Neurological Institute by combining structural data from 152 healthy adults. The transformation is computed on a participant's structural image; the anatomy is registered to the template with a series of linear and non-linear transformations, permitting for local deformations to change the size and shape of the subject's structural image for a better alignment with the brain standard. Finally, the functional data are warped to standard space by concatenating the transformation from functional to structural space computed during coregistration with this transformation from structural to standard space.

2.5.7 Spatial Smoothing

Prior to statistical analyses, *spatial smoothing* is conducted on the functional data. Although this step may seem unsound, as any smoothing will effectively reduce some of the spatial resolution of the fMRI data, the reasons for spatial smoothing are twofold.

First and foremost, the main reason for smoothing is to improve the SNR of the data by filtering out high-frequency regions. Intuitively, this works because averaging should reduce the intensity of noisy areas, while leaving the underlying functional signal of interest relatively unaffected. The second reason for smoothing is as a prerequisite for statistical analysis. Specifically, the Gaussian random field theory used for parametric inference is adaptive in how it corrects for the multiple comparison problem dependant on the smoothness of the data. However, a minimum amount of smoothing is required to obtain accurate control over the false discovery rate of activations in the thresholded statistical results.

In practise, the functional data are convolved with a three-dimensional Gaussian filter, and the amount of smoothing applied is proportional to the full width at half maximum (FWHM) of the kernel function. A suitable degree of smoothing is conditional on many factors, such as the quality of the data, the statistical power required, and the expected size of the final activation clusters. A typical smoothing kernel FWHM is between 6 and 10mm³, although the preprocessing pipelines for recent high-quality, large-sample fMRI datasets have used a lesser degree of smoothing (e.g. 5mm FWHM for the UK Biobank, 4mm FWHM for the Human Connectome Project).

2.5.8 Temporal Filtering

Temporal filtering is another processing step that aims to increase the SNR of the functional data, by taking advantage of the fact that the BOLD signals fMRI sets out to measure generally have a consistent frequency range. Temporal filtering suppresses or removes frequencies outside of this range, implicitly eliminating any artefactual signals present in the data while leaving the neuronal signals of interest untouched.

A well-known source of noise is slow drifts that occur due to imperfections in the scanning hardware. As components of the scanner heat up, this can induce a gradual change in the MR signal resulting in low-frequency trends of less than 0.01 Hz in the data. The expected frequency of the BOLD signal response to a task stimulus is around 0.2Hz. Therefore, a *high-pass filter* can be applied, removing all frequencies below a set threshold to attenuate scanner-related drifts. Other forms of noise are caused by physiological effects such as respiratory and cardiac cycles. These artefacts have a frequency range higher than the expected BOLD response (respiratory frequencies are \sim 0.3hz, cardiac frequencies \sim 1.0hz), although they may also manifest in the data as lower frequencies due to the effects of *aliasing*. A *low-pass filter* may be used to cut off higher frequencies and subdue artefacts such as physiological noise. While a high-pass filter is commonly included as part of the preprocessing pipeline, low-pass filters are more controversial as they can cultivate autocorrelation

in the signal, violating the assumption of temporal independence made for statistical inference.

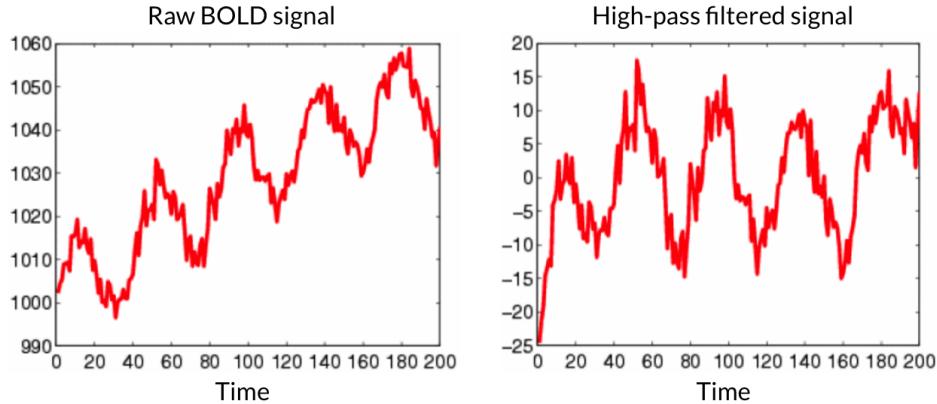


Figure 2.6: Showing the effect of high-pass filtering on one voxel's BOLD time-series data. The high-pass filter has removed the slow drift seen in the raw BOLD signal on the left. Figure adapted from *fMRI Graduate Programme* lecture notes, with the kind permission of Mark Jenkinson.

2.5.9 Grand Mean Scaling

As touched on in [2.3](#), BOLD t-fMRI data are not quantitative. Because of this, the fMRI scanner assigns arbitrary units to the signal intensities during the acquisition, and data can be scaled differently across scanning sessions. *Grand mean scaling* (or *intensity normalization*) is applied to rescale each individual's functional time series to increase the interpretability of the data across the group of participants. This is done by multiplying the functional time series (across all voxels and time points) by a constant so that the mean intensity takes a fixed value of, for example, 100. While grand mean scaling will not affect the statistical inference results, normalizing the data facilitates for comparability of the regression coefficient maps (i.e. *beta* maps) obtained for each task condition at the modelling stage of analysis.

2.6 Modelling of t-fMRI data with the General Linear Model

The *General Linear Model* (GLM) is the most widely used approach to modelling BOLD t-fMRI time series data, and a crucial part of any neuroimaging analysis. The GLM generalises a broad class of models that estimate the observed response as a linear combination of experimental and confounding variables. A key strength of this framework is its flexibility, allowing for analyses of data both within and between

individuals, and providing a foundation for which experimental hypotheses can be assessed with a variety of statistical tests, using either parametric or nonparametric statistics. In this section we provide an overview of the GLM in the context of brain imaging, before describing some of the most commonly used statistical tests performed within the GLM for analysing fMRI data.

2.6.1 The GLM Set-up

To analyse voxelwise t-fMRI data, each voxel's time series is independently modelled within the GLM. This is commonly referred to as a *mass-univariate* analysis – the ‘mass’ term specifies that the same analysis is performed many times, and ‘univariate’ indicates that each analysis is performed separately at every brain voxel (as opposed to *multivariate*, which considers many locations as part of one analysis).

Mathematically, for a compact domain $S \subset \mathcal{R}^D$ (in fMRI, $D = 3$ and S is the brain mask), the GLM at location (or brain voxel) $s \in S$ is expressed as

$$\mathbf{Y}(s) = \mathbf{X}\boldsymbol{\beta}(s) + \boldsymbol{\epsilon}(s), \quad (2.1)$$

where $\mathbf{Y}(s)$ is an $N \times 1$ vector of observations at s , \mathbf{X} is an $N \times p$ design matrix containing explanatory variables linking the observations in $\mathbf{Y}(s)$ to the effect sizes in $\boldsymbol{\beta}(s)$, $\boldsymbol{\beta}(s)$ is an $p \times 1$ vector of the unknown parameters, and $\boldsymbol{\epsilon}(s)$ is an $N \times 1$ vector of error terms. It is assumed that the errors are independently distributed conditional on \mathbf{X} by a Gaussian distribution with mean zero.

The aim of the regression is to find parameter estimates $\hat{\boldsymbol{\beta}}(s)$ that best fit the model to the data. The goodness of fit is determined by a method of *least squares*, depending on additional constraints added to the model. The parameter estimates are then used at the inference stage to test hypotheses about the data expressed in terms of the unknown parameters contained in $\boldsymbol{\beta}(s)$.

2.6.2 Estimating the Parameters with Ordinary Least Squares (OLS)

OLS is used to solve 2.1 with the assumption that the errors are *spherical*, which means that there is no autocorrelation and that each error term has constant variance. Combined with the normality assumption stated in the previous section, this means

$$\boldsymbol{\epsilon}(s) \mid \mathbf{X} \sim \mathcal{N}(0, \sigma^2(s)\mathbf{I}_N), \quad (2.2)$$

where \mathbf{I}_N is the $N \times N$ identity matrix. OLS solves the GLM by minimizing the *sum of squares* cost function S given by

$$S(\boldsymbol{\beta}(s)) = \|\mathbf{Y}(s) - \mathbf{X}\boldsymbol{\beta}(s)\|^2 = \sum_{i=1}^N |Y_i(s) - \sum_{j=1}^p X_{ij}\beta_j(s)|^2. \quad (2.3)$$

This gives the OLS estimates

$$\hat{\boldsymbol{\beta}}(s) = \arg \min_{\boldsymbol{\beta}} S(\boldsymbol{\beta}(s)) = (\mathbf{X}^\top \mathbf{X})^{-1} \mathbf{X}^\top \mathbf{Y}(s). \quad (2.4)$$

By the Gauss-Markov Theorem, it can be shown that the OLS estimates are the Best Linear Unbiased Estimates (BLUE) of $\boldsymbol{\beta}(s)$ providing all the assumptions are satisfied.

2.6.3 Prewitening

The key assumption of OLS is that the errors are spherical, however, this is often violated for fMRI data. As discussed in 2.5.8, functional data are characterized by slow drifts which induce temporal autocorrelation in the MR signal. While high-pass filtering can be applied in an attempt to remove the majority of low frequency components, another strategy is to estimate the autocorrelation directly and then remove it by *prewhitening* the data. This can be more efficient than filtering for event-related designs (Woolrich et al., 2001).

If the data are correlated, the error terms have marginal distribution

$$\epsilon(s) \mid \mathbf{X} \sim \mathcal{N}(0, \sigma^2(s) \mathbf{V}(s)), \quad (2.5)$$

where $\mathbf{V}(s)$ is the correlation matrix. Since $\mathbf{V}(s)$ is symmetric and positive-definite, $\mathbf{V}(s)$ satisfies the assumptions for the Cholesky decomposition, which means there exists a lower triangular matrix $\mathbf{K}(s)$ such that $\mathbf{V}^{-1}(s) = \mathbf{K}^\top(s) \mathbf{K}(s)$. Providing that $\mathbf{K}(s)$ can be accurately determined, the idea is to update the model by multiplying both sides of the GLM by $\mathbf{K}(s)$ so that the error terms are spherical. Denoting $\mathbf{Y}^*(s) = \mathbf{K}(s)\mathbf{Y}(s)$, and defining $\mathbf{X}^*(s)$ and $\epsilon^*(s)$ similarly, then for the updated GLM

$$\mathbf{Y}^*(s) = \mathbf{X}^*(s) + \epsilon^*(s), \quad (2.6)$$

the conditional covariance of $\epsilon^*(s)$ is

$$\text{Cov}(\epsilon^*(s) \mid \mathbf{X}) = \mathbf{K}(s) \text{Cov}(\epsilon(s) \mid \mathbf{X}) \mathbf{K}^\top(s) = \sigma^2(s) \mathbf{I}_N. \quad (2.7)$$

Therefore, the sphericity assumption is satisfied for the updated model, and OLS can

be applied to obtain the BLUE of $\beta(s)$.

2.6.4 Estimating the Variance

For statistical inference, the variance of the errors $\sigma^2(s)$ needs to be estimated. This can be done using the OLS estimates. The *fitted values* given by the OLS estimates are $\hat{Y}(s) = \mathbf{X}\hat{\beta}(s)$. The differences between the observed data points and the fitted values are known as the *residuals*, denoted by $\hat{\epsilon}(s) = \mathbf{Y}(s) - \hat{Y}(s)$. The variance of the errors is estimated as the sum of squares of the residuals divided by the *degrees of freedom* of the model

$$\hat{\sigma}^2(s) = \frac{\hat{\epsilon}^\top(s)\hat{\epsilon}(s)}{N-p}; \quad (2.8)$$

The degrees of freedom are $N - p$, since there are N observations $Y_1(s), \dots, Y_N(s)$, and p parameters $\beta_1(s), \dots, \beta_p(s)$ to estimate.

2.6.5 Inference with Null-Hypothesis Significance Testing

The pay off from obtaining the parameter estimates using OLS is that it enables us to statistically test hypotheses about the unknown effect sizes. This form of inference is known as *Null-Hypothesis Significance Testing* (NHST). Hypotheses are expressed using a contrast vector c to define a linear combination of the parameters. The null hypothesis is always expressed in the form $H_0 : c^\top\beta(s) = 0$, although this covers a wide variety of tests. For example, in a GLM with two parameters, $\beta(s) = (\beta_1(s), \beta_2(s))$, the contrast $c = (1, 0)$ would lead to the null hypothesis $H_0 : \beta_1(s) = 0$, establishing a test to determine if the first parameter $\beta_1(s)$ is significantly different from zero. However, one could also test for significant differences between the two parameters by choosing the contrast vector $c = (1, -1)$ to form the null hypothesis $H_0 : \beta_1(s) = \beta_2(s)$.

If the sphericity assumption is satisfied, then the distribution of $c^\top\hat{\beta}(s)$ is

$$c^\top\hat{\beta}(s) \sim \mathcal{N}(c^\top\beta(s), \hat{\sigma}^2(s)c^\top(\mathbf{X}^\top\mathbf{X})^{-1}c). \quad (2.9)$$

Therefore, hypotheses about a contrast of the model parameters $c^\top\hat{\beta}(s)$ can be assessed with a t -test, using the knowledge that

$$\frac{c^\top\hat{\beta}(s) - c^\top\beta(s)}{\sqrt{\hat{\sigma}^2(s)c^\top(\mathbf{X}^\top\mathbf{X})^{-1}c}} \sim t_{N-p}, \quad (2.10)$$

where t_{N-p} is a Student's t -distribution with $N - p$ degrees of freedom. In practice,

the hypothesis $H_0 : \mathbf{c}^\top \boldsymbol{\beta}(s) = 0$ is tested by computing the t -statistic

$$T(s) = \frac{\mathbf{c}^\top \hat{\boldsymbol{\beta}}(s)}{\sqrt{\hat{\sigma}^2(s) \mathbf{c}^\top (\mathbf{X}^\top \mathbf{X})^{-1} \mathbf{c}}} \quad (2.11)$$

and then obtaining a p -value by comparing $T(s)$ to a t -distribution with $N - p$ degrees of freedom. For a one-sided hypothesis test where the alternative hypothesis is given by $H_A : \mathbf{c}^\top \boldsymbol{\beta}(s) > 0$, the p -value is computed as $p = \Pr(t_{N-p} \geq t)$. In fMRI, the *statistical parametric map* (or *unthresholded statistic map*) is an image containing the p -values computed at every voxel. A p -value is said to be *statistically significant* when $p < \alpha$, where α is a predetermined *significance level* set according to inference standards appropriate for the study (typically for fMRI, α is set at 5% before correction for multiple-comparisons). In this case, the conclusion of the test is that there is sufficient evidence to reject the null hypothesis in favour of the alternative. Thus, for the null $H_0 : \mathbf{c}^\top \boldsymbol{\beta}(s) = 0$, a statistically significant p -value would suggest a non-zero effect size at location s . A *thresholded statistic map* is obtained by masking the statistical parametric map to show only voxels with a statistically significant p -value.

In addition to testing a single contrast, one may also wish to test multiple contrasts at once. For example, in the two-parameter GLM described above, the null hypothesis $H_0 : \beta_1(s) = \beta_2(s) = 0$ could be chosen to test for a significant effect size in either of the parameters. In this case, the contrast \mathbf{c} is given as a matrix

$$\mathbf{c} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \quad (2.12)$$

where each row corresponds to each of the hypotheses being tested (for this example, $\beta_1(s) = 0$ and $\beta_2(s) = 0$ respectively). This time, inference is carried out using an *F-test*. The *F-statistic* is computed as

$$F(s) = (\mathbf{c}^\top \hat{\boldsymbol{\beta}}(s))^\top [r \mathbf{c}^\top \widehat{\text{Cov}}(\hat{\boldsymbol{\beta}}(s)) \mathbf{c}]^{-1} (\mathbf{c}^\top \hat{\boldsymbol{\beta}}(s)), \quad (2.13)$$

where r is the rank of \mathbf{c} , and a p -value is obtained by comparing $F(s)$ to an *F*-distribution with r numerator and $N - p$ denominator degrees of freedom.

2.6.6 First-Level (Subject-Level) Analysis

In a *first-level* (or *subject-level*) analysis, the GLM set-up in 2.6.1 is used to analyze and test hypotheses related to the t-fMRI data obtained from an individual in a single scanning session.

At each brain voxel s , the $N \times 1$ observations vector $\mathbf{Y}(s)$ contains the BOLD

signal response data recorded by the scanner across all N sampled time-points during the session. The columns of the design matrix $\mathbf{X}(s)$ comprise of task-related and nuisance regressors to model the response in $\mathbf{Y}(s)$. The number of task-related regressors is dependent on the task paradigm and the statistical hypotheses the researcher wishes to test. For example, in the animal photo paradigm described at the end of 2.3, to test for activations when the participant was looking at any of the animal photos, a single regressor could be used to model the change in BOLD signal attributable to a photo being displayed. However, if instead the researcher wanted to test for changes in activation when the participant looked at photos of dogs compared to photos of cats, then multiple regressors would need to be used for pictures of each animal type.

The predicted response of each task-related regressor is estimated by convolution of the onset timing function for the stimulus with a HRF. Figure 2.7 shows how the predicted response is obtained for the block design used in the animal photo task. There are a variety of ways to model the HRF: by default FSL and SPM use a single canonical HRF, however alternative methods include use of a basis set of smooth functions (Friston et al., 1998) or a more flexible *finite impulse response* basis set (Goutte et al., 2000). For each task-related condition, temporal derivatives may be included as an additional regressor to account for differences between the actual and modelled HRF. See Lindquist et al. (2009) for a comparison of different HRF models.

The time series of motion-related parameters (e.g. translations and rotations) used for realignment are commonly added to the GLM as nuisance regressors to compensate for any left-over motion artefacts in the signal after preprocessing. Further nuisance regressors may include cardiac and respiratory recordings to account for fluctuations in the BOLD signal caused by changes in heart rate and breathing patterns during the scan.

To remove temporal autocorrelation in the BOLD signal the data are whitened (as in 2.6.3), after which unbiased estimators of the parameters in $\beta(s)$ can be computed via OLS (as in 2.6.2). Finally, changes in neuronal activity between the task conditions is tested by contrasting the task-related regressors with an appropriate contrast vector c under the null hypothesis $H_0 : c^T \beta(s) = 0$, using the NHST procedure described in 2.6.5.

2.6.7 Second-Level (Group-Level) Analysis

The contrast parameter estimates obtained for each individual during the first-level analysis are combined in a *second-level* (or *group-level*) analysis to test whether results

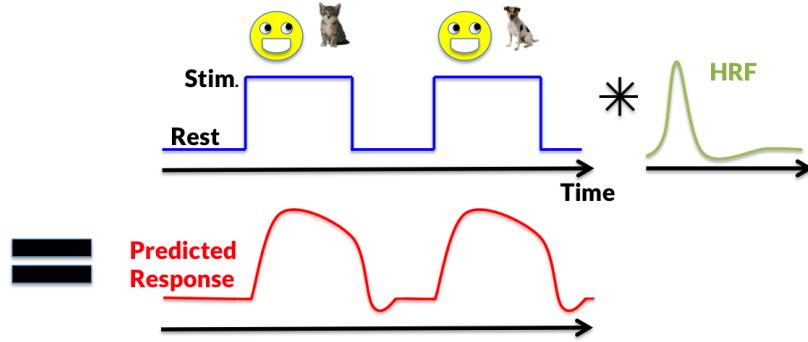


Figure 2.7: Showing how the predicted response for the animal photo task in Figure 2.4 is created by convolution of the onset timing function with the HRF.

can be generalized to the larger population. The second-level model aims to account for variation in quantity estimates within each individual's data, as well as variability *between* the participants stemming from biological differences between each subject. This is fundamental from a research perspective as it means that conclusions drawn from a second-level analysis can relate to the whole population from which the participants came from, rather than just the specific cohort of individuals involved in the study. In this section, we will describe a simplified second-level model for a one-sample *t*-test used to test for a consistent response in a first-level contrast effect across all individuals. However, within the GLM framework it is also possible to conduct a *between-groups* analysis with a *two-sample t-test* to assess activation differences between two distinct groups (e.g. a group of patients and a group of controls), and to incorporate other design types such as a *paired t-test* or *one-way analysis of variance*.

For the GLM set-up in 2.6.1, in a group-level analysis N represents the total number of participants in the study cohort. Theoretically, for a pre-specified contrast, the $N \times 1$ observations vector $\mathbf{Y}(s)$ contains each subject's first-level contrast effect, i.e. $\mathbf{Y}(s) = \mathbf{c}^\top \boldsymbol{\beta}(s) = [c^\top \beta_1(s), \dots, c^\top \beta_N(s)]^\top$. This gives the instance of the GLM

$$\mathbf{c}^\top \boldsymbol{\beta}(s) = \mathbf{X} \boldsymbol{\beta}_G(s) + \epsilon(s), \quad (2.14)$$

where the group-level parameters are notated with $\boldsymbol{\beta}_G(s)$ to distinguish from the subject-level parameters $\boldsymbol{\beta}(s)$. For a one-sample *t*-test the first column of the design matrix \mathbf{X} is an intercept where all elements are set equal to 1. Other columns of the design are covariates to be considered for the analysis, such as the age of each participant or a score to describe each individual's performance in the task carried out dur-

ing the scanning session. For simplicity we will assume no covariates are included, so $\mathbf{X}(s)$ is a column vector of 1's. $\epsilon(s)$ is the vector of group-level errors terms, assumed to have distribution

$$\epsilon(s) \sim \mathcal{N}(0, \sigma_G^2(s) \mathbf{I}_N), \quad (2.15)$$

where $\sigma_G^2(s)$ is the between-subject variance for the group.

Of course, in any practical analysis scenario the true subject-level contrast effects $\mathbf{c}^\top \beta(s)$ are unknown, and therefore the contrast estimates obtained in the first-level analyses $\mathbf{c}^\top \hat{\beta}(s)$ must be used instead. This leads to the GLM formulation

$$\mathbf{c}^\top \hat{\beta}(s) = \mathbf{X}\beta_G(s) + \epsilon^*(s), \quad (2.16)$$

where the errors $\epsilon^*(s)$ must now account for within-subject variation caused by estimating each participant's parameter effect size as well as the between-subject variance. Rearranging 2.14 and 2.16,

$$\epsilon^*(s) = \mathbf{c}^\top \beta(s) - \mathbf{c}^\top \hat{\beta}(s) + \epsilon(s), \quad (2.17)$$

and therefore

$$\begin{aligned} \text{Cov}(\epsilon^*(s)) &= \text{Cov}(\mathbf{c}^\top \hat{\beta}(s)) + \sigma_G^2(s) \mathbf{I}_N \\ &= \underbrace{\begin{pmatrix} \sigma_1^2(s) & 0 & 0 \\ 0 & \ddots & 0 \\ 0 & 0 & \sigma_N^2(s) \end{pmatrix}}_{\text{within-subject variance}} + \underbrace{\sigma_G^2(s) \mathbf{I}_N}_{\text{between-subject variance}}, \end{aligned} \quad (2.18)$$

where $\sigma_i^2(s)$ is the within-subject variance for the i th subject.

From this point on, two approaches are frequently used in the fMRI literature. The first approach assumes that the within-subject variances are equal across individuals so that the errors are *homoscedastic*, meaning that each error term also has equal variance. The second approach relaxes this assumption, allowing the within-subject variances to differ between individuals. In this case, the variance of the error terms also differ, meaning that the error terms are *heteroscedastic*.

2.6.8 Solving the Second-Level GLM with Homoscedastic Errors

Assuming that the within-subject variance terms are equal, $\sigma_1^2(s) = \dots = \sigma_N^2(s)$, 2.18 reduces to

$$\text{Cov}(\epsilon^*(s)) = (\sigma_S^2(s) + \sigma_G^2(s))\mathbf{I}_N \quad (2.19)$$

where $\sigma_S^2(s)$ is the common within-subject variance. Since this means the errors are spherical, the group-level effect estimates can be obtained using OLS as described in 2.6.2. For the one-sample t -test where \mathbf{X} is a column vector with all elements equal to one, this leads to the parameter estimates

$$\hat{\beta}_G(s) = \frac{1}{N} \sum_{i=1}^N \hat{\beta}_i(s). \quad (2.20)$$

2.6.9 Solving the Second-Level GLM with Heteroscedastic Errors

Assuming that the within-subject variance terms are not equal, then the errors are heteroscedastic, and thus the sphericity assumption required for OLS is violated. In this case, a *weighted least square* (WLS) approach is used to solve the GLM instead. Conceptually, the idea of WLS is to de-weight the most variable subject-level parameter estimates contained in $\mathbf{c}^\top \hat{\beta}(s)$. In practice, this is done by constructing a weight matrix $\mathbf{W}(s)$ equal to the inverse of the covariance matrix of the observations. In the context of the second-level analysis, 2.18 leads to the weight matrix

$$\mathbf{W}(s) = \begin{pmatrix} (\sigma_1^2(s) + \sigma_G^2(s))^{-1} & 0 & 0 \\ 0 & \ddots & 0 \\ 0 & 0 & (\sigma_N^2(s) + \sigma_G^2(s))^{-1} \end{pmatrix}. \quad (2.21)$$

The WLS parameter estimates are then computed as

$$\hat{\beta}_{WLS}(s) = (\mathbf{X}^\top \mathbf{W}(s) \mathbf{X})^{-1} \mathbf{X}^\top \mathbf{W}(s) \mathbf{c}^\top \hat{\beta}(s), \quad (2.22)$$

which for the one-sample t -test example reduces to

$$\hat{\beta}_{WLS}(s) = \left(\sum_{i=1}^N \frac{1}{\sigma_i^2(s) + \sigma_G^2(s)} \right)^{-1} \sum_{j=1}^N \frac{\mathbf{c}^\top \hat{\beta}_j(s)}{\sigma_j^2(s) + \sigma_G^2(s)}. \quad (2.23)$$

In the WLS approach to solving the GLM, the weight matrix $\mathbf{W}(s)$ effectively applies a whitening transformation to the data. In fact, it can be advantageous to simplify WLS using a similar procedure as described for Prewhitening in 2.6.3. Using

the same notation as 2.6.3, the error terms in the group-level GLM can be whitened using the diagonal matrix $\mathbf{K}(s)$ where $K_{ii}(s) = \sqrt{W_{ii}(s)}$. The updated model

$$\mathbf{K}(s)\mathbf{c}^\top\hat{\boldsymbol{\beta}}(s) = \mathbf{K}(s)\mathbf{X}\boldsymbol{\beta}_G(s) + \mathbf{K}(s)\boldsymbol{\epsilon}^*(s) \quad (2.24)$$

satisfies the sphericity assumption, and can therefore be solved using OLS. The parameter estimates obtained with this method are equivalent to solving the original model directly with WLS.

In this presentation, we have assumed that the within- and between-subject variance components are known, when in practise they must be estimated. Usually, the within-subject variance estimates obtained from the first-level analyses are also used in the group-level model. There are many proposed methods for estimating the between-subject variance, several of which use an iterative procedure based on OLS or residual maximum likelihood estimates. For more, see (Searle et al., 2009; Woolrich et al., 2004; Worsley et al., 2000).

2.7 The Multiple Comparisons Problem

A fundamental issue with the mass-univariate approach for fMRI inference is the *multiple comparisons problem*. Because the GLM is applied at each voxel independently, across the entire brain mask this means thousands of statistical tests are performed simultaneously. The significance level for each test can be described as the probability of wrongly determining a ‘discovery’ when the null-hypothesis of no activation is in fact true. In statistical terms, this is the probability of making a *type I error*. The problem is, while a significance level of 5% may be appropriate for one test, as more inferences are carried out the probability of an erroneous inference also increases. To highlight this point, if 100 tests are performed independently, each with a significance level of 5%, then the probability of at least one false discovery is 99.4%. In the context of fMRI, where a typical brain mask contains over 100,000 voxels, this problem is especially severe – if the voxelwise significance level of 5% is not corrected, we can expect over 5,000 brain voxels to falsely be determined as active in the thresholded statistical results.

In the task-fMRI literature, two different approaches are commonly used to correct for the multiple comparisons problem. The *false discovery rate* (FDR) procedure corrects the significance level to control the expected proportion of type I errors across all detected voxels in the thresholded statistical results. For example, if a 0.05 FDR procedure is applied for subject-level inference on 20 subjects data, in any individual’s thresholded statistic image we expect 5% of activations to be false-

positives. The second approach is to employ a *familywise error* (FWE) correction, used to control the expected frequency that *any* type I errors are made across the whole brain. This is clearly a more stringent form of correction – in the 20-subject example, using a 0.05 FWE procedure we expect only one individual’s thresholded image to contain any false-positives.

In making a choice between FDR or FWE correction there is a trade-off. While FDR is more statistically powerful than FWE, the drawback is a greater risk of false activations. This has lead to criticism concerning the spatial specificity of FDR-corrected results; particularly, since the location of false activations in an FDR-thresholded map are unknown, it is not possible to say with certainty that any given voxel is activated. On the other hand, FWE correction has also come under fire for being too conservative.

Multiple comparison correction procedures are carried out in fMRI at either the voxelwise or clusterwise level. Voxelwise inference is intuitive, once a corrected threshold has been determined via the FDR or FWE procedure, the thresholded statistical results are computed as all voxels whose *t*-statistic value exceeds the corrected threshold. Clusterwise inference involves a two-step procedure. First, a primary voxelwise threshold c is chosen, usually in correspondence with an uncorrected significance level such as $\alpha = 0.005$. Thresholding the statistic map at c creates groups of contiguous voxels above c , or ‘clusters’. For this reason, c is commonly referred to as the *cluster-forming threshold*. Subsequently, a *cluster-extent threshold* k is determined based on the distribution of cluster sizes obtained under the null-hypothesis of no activation. The final thresholded results are computed as all suprathreshold clusters with a spatial extent larger than k .

FDR and FWE correction procedures can be applied for both voxelwise and clusterwise inference, with the key difference that voxelwise corrections are based on the sampling distribution of voxel intensities under the null-hypothesis of no signal, while clusterwise corrections use the sampling distribution of cluster size. In the remainder of this section, we consider two methods for obtaining FWE-corrected results at the voxelwise level. First, we present how the body of mathematics called *Random Field Theory* (RFT) is used to treat FWE correction with a parametric approach. Then, we show how FWE correction may also be obtained with permutation methods that make weaker assumptions about the data. While we will not consider FDR here, for more information a reader may refer to [Benjamini and Hochberg \(1995\)](#) where the method was originally proposed, or [Genovese, Lazar, and Nichols \(2002\)](#) for a presentation of FDR in the context of functional neuroimaging.

2.7.1 Random Field Theory for Voxelwise FWE Correction

Voxelwise FWE control is established using an intrinsic relationship linking the probability of making a false discovery with the distribution of the maximum t -statistic over the brain. For a threshold c ,

$$P(\text{Reject } H_0 | H_0 \text{ true}) = P\left(\max_{s \in S} T(s) > c\right) \quad (2.25)$$

where $T(s)$ is the t -statistic map given in 2.11 and H_0 is the null hypothesis of no activation.

The intuition of RFT is that under the *global null* of no signal *anywhere*, $T(s)$ can be modelled by a stationary continuous Gaussian random field $Z(s)$ of mean zero and unit variance over the same domain S . Note that this imposes assumptions that the data are stationary and that the discretely sampled statistic image $T(s)$ is sufficiently smooth enough to be approximated by a continuous random field. It is because of the latter that spatial smoothing of the data must be carried out during preprocessing. Supposing that the model is valid, then the right-hand side of 2.25 is approximated by $P\left(\max_{s \in S} Z(s) > c\right)$. Remarkably, this probability can be obtained with use of the *Euler characteristic* (EC), a measure originating from algebraic topology that provides information about a shape's fundamental structure, regardless of ways in which the shape is distorted or deformed.

For a threshold c , defining the *excursion set* A_c as the set of voxels where the random field exceeds c , i.e. $A_c = \{s \in S : Z(s) > c\}$, the EC χ_c can be characterized as counting the number of clusters minus the number of 'handles' plus the number of 'holes' in A_c . If c is chosen large enough then we expect the handles and holes to disappear, so the EC provides an approximation of the number of clusters. This relates back to the maximum distribution because if $\max_{s \in S} Z(s) > c$, then clearly there must be at least one suprathreshold cluster in the excursion. Putting all this information together,

$$\begin{aligned} P\left(\max_{s \in S} T(s) > c\right) &\approx P\left(\max_{s \in S} Z(s) > c\right) \\ &\approx P(\chi_c > 0). \end{aligned} \quad (2.26)$$

Finally, further increasing of the threshold c will result in fewer voxels contained in the excursion set until χ_c will almost certainly take the value of 1 (if the excursion set is made up of one suprathreshold cluster) or 0 (if the excursion set is

empty). In this case,

$$P(\chi_c > 0) = \mathbb{E}(\chi_c). \quad (2.27)$$

In practice, with a parametric approach the FWE-corrected p -value is always approximated using the expectation of the EC. When $S \subset \mathcal{R}^3$, e.g. S is the brain mask in a neuroimaging application, the expected EC has the closed-form solution

$$\mathbb{E}(\chi_c) \approx \lambda(S)|\Lambda|^{\frac{1}{2}}(c^2 - 1)\exp(-c^2/2)/(2\pi)^2, \quad (2.28)$$

where $\lambda(S)$ is the Lebesgue measure (i.e. the volume) of the brain mask, and $|\Lambda|$ is the determinant of the covariance matrix of the gradient of $Z(s)$,

$$|\Lambda| = \left| \text{Cov}\left(\left[\frac{\partial}{\partial x}Z(s), \frac{\partial}{\partial y}Z(s), \frac{\partial}{\partial z}Z(s)\right]\right) \right|. \quad (2.29)$$

Essentially, $|\Lambda|$ provides a measure of the smoothness of the random field $Z(s)$; for a less smooth process $Z(s)$, the determinant is larger.

2.7.2 Permutation Testing for Voxelwise FWE Correction

In the previous section, we showed that the crux of estimating the FWE-corrected p -value is to approximate the maximum distribution of $T(s)$. We demonstrated how this was carried out with a parametric approach by assuming that under the global null, $T(s)$ can be modelled by a Gaussian random field. However, this imposed strong assumptions on the data which in practice are seldom fulfilled. In particular, it has been shown that RFT estimates of the FWE p -value are conservative unless the data are extremely smooth with high degrees of freedom. To remediate these problems, nonparametric methods have been proposed as an alternative.

The principle idea of permutation testing for FWE correction is that if the global null hypothesis is true, and there is really no signal anywhere, then the labels of each observation are arbitrary and the data is *exchangeable*. Therefore, the maximum distribution of $T(s)$ under the global null can be constructed empirically by creating a large number of surrogate realizations of the data, where on each realization the data labels are permuted randomly and the maximum value is obtained from the corresponding statistic map.

In the first-level analysis model described in 2.6.6, where the observations are fMRI time-series data from one individual, permutation testing is usually inappropriate; due to temporal correlation in the data, the exchangeability assumption is violated. However, permutation testing is perfectly viable for the group-level model

in 2.6.7, where the observations are first-level *contrast of parameter estimates* (cope) maps $c^\top \hat{\beta}_1(s), \dots, c^\top \hat{\beta}_N(s)$ obtained from each individual in the cohort.

In a two-sample t -test, where cope maps are obtained from two groups, e.g. a group of patients and a group of controls, permutation testing is conducted by exchanging the labels between the patients and controls. For a one-sample t -test, where there are no group labels to swap, the principle of exchangability is replaced by an assumption of symmetry; if the null hypothesis $H_0 : c^\top \beta(s) = 0$ is true, then it should not matter if a change of sign is applied to all readings in any individual contrast image. In this case, a permutation test is carried out where each surrogate realization is established by randomly multiplying each individual contrast image $c^\top \hat{\beta}_i(s)$ by 1 or -1. Clearly, the assumption of symmetry for the noise distribution is much weaker than Gaussianity required for RFT with the parametric approach.

In full, the voxelwise FWE-corrected p -value for a second-level one-sample t -test is obtained via permutation test using the following algorithm:

1. Let P be a large number of permutations that will be carried out for the permutation test. A larger P will provide a more precise approximation of the empirical null distribution, commonly $P = 10,000$ is used.
2. Create surrogate observations of the data $c^\top \hat{\beta}_1^*(s), \dots, c^\top \hat{\beta}_N^*(s)$, where each $c^\top \hat{\beta}_j^*(s)$ is obtained by multiplying $c^\top \hat{\beta}_j(s)$ randomly by either 1 or -1. Specifically, $c^\top \hat{\beta}_j^*(s) = r_j c^\top \hat{\beta}_j(s)$, where the r_j are independent and identically distributed Rademacher variables (that is, $r_j = 1$ or -1 , each with probability $1/2$).
3. Obtain the group-level statistic map $T^*(s)$ for the surrogate data, and compute the maximal statistic value across the image $t^* = \max_{s \in S} T^*(s)$.
4. Repeat steps 2 and 3 P times, to create an empirical distribution t_1^*, \dots, t_P^* of the maximal statistic.
5. Assuming that t_1^*, \dots, t_P^* are ordered from smallest to largest (otherwise, rearrange the labelling so this is true), for a desired FWE rate of α , choose $c = t_{\lceil(1-\alpha)P\rceil}^*$, where $\lceil(1-\alpha)P\rceil$ is the smallest integer greater than $(1-\alpha)P$.
6. With this construction, it can be shown that c is the corrected p -value for a voxelwise FWE rate of α .

2.8 Conclusion

In this section, we provided the background that will form the basis of our research. We started with a general discussion of what it means to study brain function, before providing an overview of the biological phenomena behind the BOLD effect measured in a functional MRI study. In the rest of this section we gave an in-depth overview of task fMRI, which will be the main field of investigation in this thesis. We described the fundamental preprocessing steps carried out in a t-fMRI analysis, as well as the most common methods used to model subject- and group-level fMRI data within the general linear model. Finally, we described the multiple comparison problem for task fMRI inference, and then demonstrated how a parametric and nonparametric approach can be used to control the voxelwise familywise error rate in the thresholded statistic result maps computed at the end of a t-fMRI analysis.

CHAPTER 3

Exploring the Impact of Analysis Software on Task-fMRI Results

3.1 Data and Analysis Methods

3.1.1 Study Description and Data Source

We selected three t-fMRI studies for reanalysis from the publicly accessible OpenfMRI data repository: ds000001 (Revision: 2.0.4; ([Schonberg et al., 2012](#))), ds000109 (Revision 2.0.2; ([Moran et al., 2012](#))), and ds000120 (Revision 1.0.0; ([Padmanabhan et al., 2011](#))). Each of the datasets have been organized in compliance with the Brain Imaging Data Structure (BIDS, RRID:SCR_016124; ([Gorgolewski et al., 2016](#)))). These datasets were chosen following an extensive selection procedure (carried out between May 2016-November 2016), whereby we vetted the associated publication for each dataset stored in the repository. We sought studies with simple analysis pipelines and clearly reported regions of brain activation that would be easily comparable to our own results. Exclusion criteria included the use of custom software, activations defined using small volume correction, and application of more intricate methods such as region of interest and robust regression analysis, which we believed could be impractical to implement across all analysis software. A full description of the paradigm for each of our chosen studies is included in the respective publication; here we give a brief overview.

For the ds000001 study, 16 healthy adult subjects participated in a balloon analog risk task over three scanning sessions. On each trial, subjects were presented with a simulated balloon, and offered a monetary reward to ‘pump’ the balloon. With each successive pump the money would accumulate, and at each stage of the trial subjects had a choice of whether they wished to pump again or cash-out. After a certain number of pumps, which varied between trials, the balloon exploded. If subjects had cashed-out before this point they were rewarded with all the money they had

earned during the trial, however if the balloon exploded all money accumulated was lost. Three different coloured ‘reward’ balloons were used between trials, each having a different explosion probability, as well as a gray ‘control’ balloon, which had no monetary value and would disappear from the screen after a predetermined number of pumps. Here we reproduce the result contrasting the parametrically modulated activations of pumps of the reward balloons versus pumps of the control balloon, corresponding to Figure 3 and Table 2 in the original paper.

The ds000109 study investigated the ability of people from different age-groups to understand the mental state of others. A total of 48 subjects were scanned, although 43 had acceptable data for the false belief task – 29 younger adults and 14 older adults. In this task participants listened to either a ‘false belief’ or ‘false photo’ story. A false belief story would entail an object being moved from one place to another, with certain characters witnessing the change in location while others were unaware. False photo stories were similar except involved some physical representation, such as a photo of an object in a location from which it had been subsequently removed. The task had a block design where stories were represented for ten seconds, after which participants had to answer a question about one of the character’s perceptions of the location of the object. We reproduce the contrast map of false belief versus false photo activations for the young adults, corresponding to Figure 5a and Table 3 from the original publication.

Finally, the ds000120 study explored reward processing across different age groups. fMRI results were reported on 30 subjects, with 10 participants belonging to each of the three age groups (children, adolescents and adults). Participants took part in an antisaccade task where a visual stimulus was presented in each trial and subjects were instructed to quickly fixate their gaze on the side of the screen opposite to the stimulus. Prior to a trial, subjects were given a visual cue to signal whether or not they had the potential to win a monetary reward based on their upcoming performance (a ‘reward’ or ‘neutral’ trial). We reproduce the main effect of time activation map – an F -statistic for any non-zero coefficients in the sine HRF basis – corresponding to Figure 3 and Table 1 in the original publication.

3.1.2 Data Analyses

All data analyses were conducted using AFNI (version AFNI_18.1.09), FSL (version 5.0.10), and SPM (version SPM12, v6906). Computation was performed on a cluster comprised of 12 Dell PowerEdge servers (6 R410, 12 core 2.40GHz processors, 6 R420, 12 core 2.80GHz processors) running CentOS 7.3.

Pipeline

A full decomposition of the pipelines implemented within the three packages for each study is presented in Table 3.1. Here, we give a brief description of the procedures.

In AFNI, preprocessing and subject-level analyses were conducted using the @SSwarper program and afni_proc.py. For ds000001 and ds000109, we used the 3dMEMA program to perform a one-sample *t*-test, while for ds000120 we used the 3dMVM program at the second level to conduct a mixed-effects analysis, generating an *F*-statistic for the main effect of time.

In FSL, analyses were carried out using the FMRI Expert Analysis Tool (FEAT, v6.00). For each analysis, at the first level a separate .fsf file was created for each scanning session. Runs were then combined as part of a second level fixed-effects model, yielding results which were subsequently inputted into a group analysis.

In SPM, preprocessing, subject- and group-level analyses were conducted by selecting the relevant modules within SPM’s Batch Editor. In particular, subject-level and group-level analyses were conducted using the Specify 1st-level and Specify 2nd-level modules respectively.

Once analyses were complete, the results for each software package were exported as NIDM-Results packs (FSL and SPM only, ([Maumet et al., 2016](#))) and uploaded to a public collection on the NeuroVault (RRID:SCR_003806, ([Gorgolewski et al., 2015](#)) online data repository.

Common Processing Steps

A number of processing steps for each package were included in all of our analyses, regardless of whether they had been implemented in the original study. While this meant deviating from an exact replication of the original pipeline, these processing steps were either fundamental to ensure that the results from each software package could be compared objectively, or steps that are widely accepted as best practices within the community. In this section we describe these steps.

Successful coregistration of the functional data to the structural brain images, and subsequently, registration to the MNI template, was of paramount importance to us for fair comparability of the results. During our first attempt at analysing the ds000001 dataset we discovered that seven subjects had essential orientation information missing from the NIfTI header fields of their functional and structural data. As the source DICOM files were no longer available, the original position matrices for this dataset were unable to be retrieved. This caused coregistration to fail for several subjects across all three software packages in our initial analysis of this data.

Table 3.1: Software Processing Steps. Implementation of each of the processing steps (ds000001, ds000109, ds000120) within AFNI, FSL and SPM.

	Processing Step	AFNI	FSL	SPM
Preprocessing	Script	@SSWarper ² afni_proc.py	FEAT First-level analysis	Batch (multiple modules)
	Slice-timing¹	-tshift_opts_ts -tpattern	Pre-stats: Slice timing correction	Slice Timing
	Realignment/Motion Correction	-volreg_align_e2a	Pre-stats: Motion correction: MCFLIRT	Realign: Estimate and Reslice
	Segmentation	<i>Not applied</i>	<i>Not applied</i>	Segment
Brain Extraction (Anatomical)		-copy_anat [@SSWarper result] -anat_has_skull no	bet (<i>command line</i>)	Image Calculator ³
	Brain Extraction (Functional)	<i>Not applied</i>	Pre-stats: BET brain extraction	<i>Not applied</i>
Intrasubject Coregistration		-align_opts_aea -giant_move -check_flip	Registration: Normal search, BBR	Coregister: Estimate
	Intersubject Registration	-tlrc_base -volreg_tlrc_warp -tlrc_NL_warp -tlrc_NL_warped_dsets [@SSWarper result]	Registration: Nonlinear, Warp resolution 10mm	Normalise: Write
Analysis Voxel Size		-volreg_warp_dxzy (overriding default determined from functional images)	determined by anatomical template voxel sizes	Normalise: Write: Writing Options: Voxel Sizes
	Smoothing	-blur_size	Pre-stats: Spatial smoothing FWHM (mm)	Smooth
First-level	Script	afni_proc.py	FEAT First-level analysis	Specify 1st-level
	Model Specification	-regress_stim_times -regress_stim_labels -regress_basis_multi -regress_stim_types	Stats: Full model setup: EVs	fMRI model specification

Table 3.1 (continued)

Processing Step		AFNI	FSL	SPM
Inclusion of 6 Motion Parameters		<i>Implicitly added with 'regress' block</i>	Stats: Standard Motion Parameters	fMRI model specification: Data & Design: Multiple regressors: Realignment Param file
Model Estimation		<i>Nothing to specify</i>	<i>Nothing to specify</i>	Model estimation
Contrasts		-regress_3dD_stop -regress_reml_exec -regress_opts_3dD -gltsym	Stats: Full model setup: Contrasts	Contrast Manager
Second-level	Script	3dMEMA 3dMVM ¹	Feat Higher-level analysis	Specify 2nd-level
	Model Specification	3dMEMA -set -missing_data 0 3dMVM ¹ -dataTable	Stats: Full model setup: EVs	Factorial design Specification: One-sample T-test Full factorial
	Model Estimation	<i>Nothing to specify</i>	<i>Nothing to specify</i>	Model estimation
	Contrasts	<i>Nothing to specify</i>	Stats: Full model setup: Contrasts	Contrast Manager
Second-level Inference		3dMask_Tool (<i>Obtain group-mask</i>) 3dClustSim 3dClust 3dCalc (<i>Binarizing cluster masks and masking t-stat</i>) 3dTcat (<i>Obtaining one image in a 4D volume</i>)	Post-stats	Results Report
Results sharing	NIDM-Results export	<i>Not available</i>	nidmfsl	Results Report
	NeuroVault upload	<i>Upload all statistic images</i>	<i>Upload of 'group.gfeat.nidm.zip'</i>	<i>Upload of 'spm_****.nidm.zip'</i>

¹ ds000120 only.² The @SSWarper program was ran on each subject prior to afni_proc.py for brain extraction of the anatomical image, and to apply the nonlinear warp of the anatomy to MNI space.³ Image calculator was used to create bain mask from gray matter, white matter and CSF images; see text.

We rectified the issue by manually setting the origins of the functional and structural data. OpenfMRI released a revision (Revision: 2.0.4) of our amended dataset which we used for the analysis. Further to this, we also set a number of common preprocessing steps within each package to be applied in all our analyses.

Firstly, brain extraction was conducted on the structural image in all software. We did this to improve registration and segmentation. In AFNI, brain extraction was carried out using 3dskullstrip, that was called implicitly from within the @SSwarper program. The skull-stripped anatomical volume obtained here was inputted into our afni_proc.py scripts where further preprocessing and first-level analyses were carried out. In FSL, brain extraction was performed on both the functional and structural data. The Brain Extraction Tool (BET; ([Smith, 2002](#))) was applied to each structural image from the command line before preprocessing, and to the functional data with the BET option within the Pre-stats module of FEAT. In SPM, brain extraction was implemented via the segmented structural images. Gray matter, white matter and CSF images were summed and binarised at 0.5 to create a brain mask, which was applied to the bias corrected structural image using the Image Calculator module.

Coregistration of the functional data to the anatomy was carried out for the most part using the default settings in each software. In AFNI, alignment of the data was conducted using the align_epi_anat.py program called implicitly from the align block within the afni_proc.py scripts. We included the -volreg_align_e2a option within our scripts to specify alignment of the functional data onto the anatomy, as by default AFNI conducts the inverse transformation of anatomy onto functional. Further to this, we also added the -align_opts_aea program to all of our scripts with the -giant_move and -check_flip options to allow for larger transformations between the images. In FSL, coregistration was carried out within FEAT using the default linear registration methods with a Boundary-Based Registration (BBR) cost function. The default methods were also applied within SPM's Coregister: Estimate module, using a normalised mutual information cost function.

Registration of the structural and functional data to the anatomical template was executed using each packages nonlinear settings. In AFNI, nonlinear registration of the anatomical data to the MNI template was conducted as part of the @SSwarper program ran prior to the afni_proc.py script. The warps computed by @SSwarper were passed to afni_proc.py using the -tlrc_NL_warpred_dsets option, and applied to the functional data within the tlrc block using the -volreg_tlrc_warp option. By default, the resampled functional data in MNI space has voxel size determined from the raw 4D data; we forced 2mm cubic voxels with the -volreg_warp_dxxy option for compatibility with FSL and SPM's 2mm default. In FSL, registration to the MNI

template was conducted using FMRIB’s Nonlinear Image Registration Tool (FNIRT; ([Andersson et al., 2007](#))), controlling the degrees of freedom of the transformation with a warp resolution of 10mm. In SPM, the nonlinear deformations to MNI space were obtained as part of the Segment module and then applied to the structural and functional data within the Normalise: Write module.

As a form of quality control, we created mean and standard deviation images of the subject-level MNI-transformed anatomical and mean functional images. Alongside the subject-level data, these images were assessed to check that registration to MNI space had been successful. When intersubject registration failed remedial steps were taken within each software; these are described in the software implementation parts of the following study-specific analysis sections.

Across all software packages six motion regressors were included in the analysis design matrix to regress out motion-related fluctuations in the BOLD signal. Use of six or more derived motion regressors is commonly recommended as good practice, and we chose to use just six regressors as this could be easily implemented across software.

Finally, we note that each software package uses a different default connectivity criterion for determining significant clusters: 6-connectivity for AFNI, 18-connectivity for SPM, and 28-connectivity for FSL. Since these settings are not typically modified we have kept these defaults in all of our analyses to reflect standard practices carried out within each software.

We now describe the task-specific analysis procedures for each of the three studies as carried out in the original publications, and how these methods were implemented within each package. While we decided to keep the above steps of the analysis pipelines fixed, for all remaining procedures we attempted to remain true to the original study. Any further deviations necessitated are discussed in the software implementation sections. Notably, apart from the addition of six motion regressors, all of our common steps relate to preprocessing, and hence for first- and group-level analysis we attempt to exactly replicate the original study.

ds000001 Analyses

In the publication associated with the ds000001 study all preprocessing and analysis was conducted within FSL (version 4.1.6). Data on all 16 subjects were available to us on OpenfMRI. In the original preprocessing, the first two volumes of the functional data were discarded and the highpass-filter was set to a sigma of 50.0s. Motion correction was conducted using MCFLIRT and brain extraction of the functional data was applied with BET, after which FSL’s standard three-step registration procedure

was carried out to align the functional images to the structural scan. Spatial normalization was implemented with FMRIB’s Linear Image Registration Tool (FLIRT; ([Jenkinson et al., 2002](#))), and data were smoothed using a 5mm full-width-half-maximum (FWHM) Gaussian kernel. At the run level, each of the events were convolved using a canonical double-gamma HRF; FEAT’s (then newly available) outlier de-weighting was used. Subject-level analysis of the functional data were conducted using a GLM within FEAT, where a selection of the regressors were orthogonalized. The three scanning sessions for each participant were carried out separately and then combined together at the second level. A pair of one-sided t -tests were conducted at the group-level to test for positive and negative effects separately. For each test, clusterwise inference was performed using an uncorrected cluster-forming threshold of $p < 0.01$, FWE-corrected clusterwise threshold of $p < 0.05$ using Gaussian random field theory.

We opted to not use outlier de-weighting on the basis that such methods were impractical to implement across all software packages.

AFNI Implementation

Using our default procedure for the AFNI analysis, we found that coregistration of the functional scans onto the anatomy failed for four subjects. To remedy this issue, for this study we modified our afni_proc.py scripts: Within the -align_opts_aea module, the ‘-ginormous move’ option was added to align the centers of the functional and anatomical volumes, and the ‘-cost lpc+ZZ’ option was used to apply a weighted combination of cost functionals. Both of these changes are recommended for data with little structural detail. Following these modifications all coregistrations were successful.

To replicate the orthogonalization methods from the original study, a separate orthogonalization script was ran for each subject prior to the first-level analyses. Within this script, the (un-orthogonalized) regressors were generated by passing the event timing files to 3dDeconvolve, after which the 3dTproject command was used to obtain the desired projections. The orthogonalized regressor files outputted from this script were then entered into afni_proc.py to replicate the original subject-level analysis model.

Trials were convolved with a single gamma HRF using either the BLOCK or dmBLOCK option within the -regress_basis_multi module, determined by whether the event file had fixed or variable duration times respectively. The -regress_stim_types option was added to our afni_proc.py script to specify event files for regressors which had been parametrically modulated in the original study, and identify the orthogonal-

ized regressors.

At the group level, we performed a mixed-effects analysis using 3dMEMA. The critical cluster size threshold was determined by Monte Carlo simulation with the 3dClustSim program.

FSL Implementation

Implementation in FSL closely followed the original procedure described above, with the exception that nonlinear registration was used to transform the data to standard space.

SPM Implementation

Implementation in SPM closely followed the pipeline outlined in [3.1](#).

ds000109 Analyses

The original preprocessing and statistical analysis for the ds000109 study was carried out using SPM8. Data were shared on 36 of the 40 subjects, 21 of which were young adult subjects that had fMRI data compatible for our reanalysis. First, functional data were realigned and unwarped to correct for head motion and geometric distortions. After transforming the data into a standardized space, the normalized data were smoothed with an 8mm FWHM Gaussian kernel. Further to this, custom software was applied to exclude functional volumes where head motion had exceeded a certain limit, however this process was omitted from our pipelines since this feature was not available in any of the software packages. The preprocessed data were entered into a GLM for first level analysis where trials were modeled using a block design and convolved using SPM's canonical HRF. Each participant's contrast images were then entered into a one-sample group analysis using clusterwise inference, cluster-forming threshold of $p < 0.005$, 5% level FWE using random field theory; in their analysis, this amounted to a critical cluster size threshold of 56 voxels.

AFNI Implementation

Intersubject registration to the MNI atlas failed for one subject, for which part of the frontal lobe was missing. We addressed this by revising this study's AFNI pipeline to use the -pad_base 60 option within the -tlrc_opts_at module included in afni_proc.py. This gave extra padding to the MNI template so that no part of the functional image was lost during the alignment.

The HRF was modelled with SPM's canonical HRF using the SPMG1 option for each event within the -regress_basis_multi option and passing the duration of the regressor as an argument to the function.

At the group level, we performed a mixed-effects analysis using 3dMEMA. *p*-values were determined by Monte Carlo simulations with 3dClustSim.

FSL Implementation

To recreate the original HRF model in FSL, we chose the Double-Gamma HRF from the convolution options within FEAT.

SPM Implementation

Implementation in SPM closely followed the original procedure described above.

ds000120 Analyses

A multi-software analysis procedure was used for the ds000120 study, where data were preprocessed with FSL and then analysed using AFNI. fMRI data were shared on OpenfMRI for 26 of the original 30 subjects, and 17 had data available on the task of interest. This was the only study that applied slice-timing correction, adjusting the functional data for an interleaved slice acquisition. Functional scans were re-aligned to the middle volume, and following brain extraction with BET, registered to the structural scan in Talairach space using FLIRT and FNIRT. Data were high-pass filtered with a sigma value of 30.0s and smoothed with a 5mm FWHM Gaussian kernel. Like the previous study, further methods were used to remove functional volumes with excessive motion which have been left out from our analyses due to discordance across software. Subject-level analysis was conducted within AFNI. To allow for flexible modelling of the response to the saccade task, this study used a HRF basis consisting of eight sine functions with a post-stimulus window length of 24.0s. At the group level, subjects were entered into a mixed-effect model, with subjects as a random factor, trial type (reward, neutral) and time as within-group factors, and age group (child, adolescent, adult) as a between-group factor. Clusterwise inference was used on the main effect of time activation map ($F_{8,142}$ statistic), cluster-forming threshold of $p < 0.001$, controlling FWE at the 5% level, obtained with Monte Carlo methods. This computed critical cluster size threshold was 23 voxels.

For our replication exercise we only consider the main effect of time. This analysis is based on the corresponding time effect contrasts for each subject and requires a simpler model, with one random effect (subject) and one fixed effect (time).

AFNI Implementation

Slice timing was conducted using the -tshift_opts_ts program within afni_proc.py with the -tpattern option applied to specify an interleaved slice acquisition.

The sine basis set used for the HRF was modelled using the -regress_basis_multi module with the SIN option.

At the group level, a mixed-effect analysis was carried out with the 3dMVM program. Following this, 3dClustSim was used to obtain the cluster extent corresponding to the original study threshold. In our analysis we found the cluster size threshold to be 48 voxels.

FSL Implementation

The repeated-measures design used in the group-level analysis of the original study was not feasible to implement for parametric inference in FSL, and as such, we did not attempt an FSL reanalysis for this study. (The FEAT manual does describes “Repeated Measure” examples, but these are based on a restrictive assumption of compound symmetry; here this would entail assuming that all $8 \times 7 / 2 = 28$ correlations among the basis regression coefficients are equal.)

SPM Implementation

Slice timing was conducted using the Slice Timing module within the Batch Editor of SPM.

Although an exact equivalent of the original HRF model was not possible in SPM, we chose the closest equivalent using the Fourier basis set with an order of 4, leading to a total of 9 basis functions fit to each of the reward and neutral conditions for each of the three runs. A set of 9 first level contrasts computed the average Fourier coefficients over conditions and runs.

To reproduce the group-level analysis in SPM, a full factorial design was chosen within the ‘Factorial design specification’ module of the Batch Editor, with a time factor (9 levels) and adding age-group to the model using two covariates (adolescent vs child, adult vs child); the main effect of time was tested with an *F*-contrast.

3.1.3 Comparison Methods

We applied three separate quantitative methods to measure the similarity between the group results obtained within each software package for each of the three studies.

Firstly, Bland-Altman plots comparing the unthresholded group statistic maps were created for each pairwise combination of software packages. These plotted the difference between the statistic values (*y*-axis) against the mean statistic value (*x*-axis) for all voxels lying inside the intersection of the two software's analysis masks. The plots provide an assessment of the level of agreement between two software packages about the magnitude of the statistic value observed at each voxel. If two software packages were in perfect agreement, all points on the bland-altman plot would lie on the *x*-axis, since the difference between the statistic values at each voxel would be zero. The degree of disagreement is therefore evaluated by the perpendicular distance of points from the *x*-axis; for example, for a "AFNI-FSL" Bland-Altman plot, points above *x*-axis are where AFNI's statistic is larger than FSL's. With the difference plotted against the average, general patterns of disagreement can be discerned.

In addition to this, we also created Bland-Altman plots to compare percentage BOLD change maps (for ds000120, partial R^2 maps) between software. For each package, an appropriate normalization of the group-level beta maps was conducted to convert to percentage BOLD change units. Due to differences in how each package scales the data, a different normalization was required for each of the three packages. For ds000120, the partial R^2 maps were computed via a transformation of the group-level F -statistic images. We provide full details on how each of these procedures were carried out in the **CHANGE? appendix (Appendix 1. for percent BOLD change, Appendix 2. for partial R^2)**. In all of our Bland-Altman comparisons, we excluded white matter and cerebral spinal fluid voxels according to the MNI tissue probability maps thresholded at 0.5.

We also computed the Dice similarity coefficient for each pairwise combination of the group-level thresholded statistic maps. The coefficient is calculated as the cardinality of the intersection of the thresholded maps divided by the average of the cardinality of each thresholded map. While Bland-Altman is interested in the similarity between statistic values, Dice measures the overlap of voxels as a means to assess the spatial similarity of activated clusters. The coefficient takes a value between zero and one, where one indicates complete congruence between the size and location of clusters in both thresholded maps, while zero indicates no agreement. Dice coefficients were computed over the intersection of the pair of analysis masks, to assess only regions where activation could occur in both packages. We also calculated the percentage of 'spill over' activation, i.e. the percentage of activation in one software's thresholded statistic map that fell outside of the analysis mask of the other software.

A particular concern we had was that a pair of statistic images could in essence

be very similar, but differ by a scale factor over all voxels. Another possibility was that one software could have greater sensitivity for voxels where signal was present, causing differences between images only for relatively higher statistical values. Both of these features would not be identifiable using our previous comparison methods. To address this, we computed the Euler Characteristic (EC) for each software's group t -statistic map (F -statistic for ds000120), thresholded using t -values between -6 to 6 (0 to 6 for ds000120; increasing with an increment of 0.2). Alongside the EC, we also computed the number of clusters in the statistic images using the same thresholds. As touched on in 2.7.1, for a given threshold t , the EC calculates the number of clusters minus the numbers of 'handles' plus the number of 'holes' in the thresholded image. For large t , we expect the handles and holes to disappear, and therefore the EC provides an approximation of the number of clusters in an image. For smaller t , we expect our thresholded image to be one connected cluster with many holes and handles (like Swiss cheese) - it is in this situation where the EC is clearly more informative about differences between images than the cluster count alone. Over all t , the EC curve provides a signature of an entire statistic image, and provides a means to assess whether only superficial scaling differences are responsible for disparities between a pair of images.

For a qualitative assessment of whether similar activation patterns were displayed between packages, a NeuroSynth (RRID:SCR_006798, <http://neurosynth.org>) association analysis was conducted on each software's unthresholded statistic maps. These analyses performed a cognitive decoding of the unthresholded statistic image with images in the NeuroSynth database, to find the words or phrases most strongly associated with the activation patterns found in the statistic map.

Finally, we visually compared the corresponding slices of each software's thresholded statistic map to those presented in the publication figure we had attempted to recreate. Ensuring we had found activation in approximately the same regions as the original publication gave us an indication that we had successfully replicated the study's analysis pipeline.

3.1.4 Permutation Test Methods

For ds000001 and ds000109, in parallel to our replication analyses we computed an additional set of group-level results applying nonparametric permutation test inference procedures available within each software package (a one-sample repeated measures permutation test needed for ds000120 was not available in AFNI). The first level contrast maps obtained from our initial replications for each subject were entered into a group-level one-sample t -test where clusterwise inference was con-

ducted using the same cluster-forming thresholds, and then 5% level FWE corrected thresholds were computed by permutation, using 10,000 permutations.

AFNI Implementation

In AFNI, permutation inference was carried out using the 3dttest++ module with the -ClustSim option. By applying this option, permutation generated noise realisations which 3dClustSim used to generate cluster-threshold tables. Significant clusters in the group-activation map were found with 3dclust, using a critical cluster size threshold extracted from the 3dClustSim output.

FSL Implementation

Permutation test inference was conducted in FSL using randomise version 2.9 ([Winkler et al., 2016](#)). This outputted a ‘corrp’ image which was then used to mask the raw *t*-statistic image to show significant voxels for the appropriate thresholds.

SPM Implementation

The Statistical nonParametric Mapping (SnPM, version SnPM13; RRID:SCR_002092; ([Nichols and Holmes, 2002](#))) toolbox was used to carry out permutation tests in SPM. The “MultiSub: One Sample T test on diffs/contrasts”, Compute and Inference modules within SnPM were applied to obtain the final group-level activation maps.

Each of the comparison methods described in the previous section were also applied to our permutation results to assess cross-software differences for nonparametric inference methods. In addition, we also generated intra-software Bland-Altman plots and Dice coefficients to understand differences between the parametric and nonparametric methods applied within each package.

These methods were excluded for ds000120, since it was not possible to conduct permutation inference for an *F*-test within AFNI, and parametric inference was unfeasible in FSL for this study as discussed in the previous section.

3.1.5 Scripting of Analyses and Figures

AFNI and FSL scripts were written in Python 2.7.14 and SPM scripts were written in Matlab R2016b. Scripts were made generalizable, such that the only study-specific differences for each of the analyses in a software package were the raw data and working directory inputs, subject- and group-level analysis templates (as well as a run-level template for FSL), and a unique conditions structure necessary for creating the onset files for the specified study. For each analysis package, a script was

written to extract the stimulus timings from the raw data to create event files that were compatible within the software. Subject-level analysis templates were batch scripts created for each study containing all processing steps of the subject analysis pipeline for the respective software, with holding variables used where subject- or run-specific inputs were required. The main script would take the template as an input, and cycling through each of the subjects, replace the holding variables with appropriate pathnames to create distinct batch scripts for each subject. These were then executed to obtain subject-level results for all participants in the study.

A Python Jupyter Notebook ([Kluyver et al., 2016](#)) was created for each of the three studies. Each notebook harvests our results data from NeuroVault and applies the variety of methods discussed in the previous section using NiBabel 2.2.0 ([Brett et al., 2017](#)), NumPy 1.13.3 ([Walt et al., 2011](#)) and Pandas 0.20.3 ([McKinney and Others, 2010](#)) packages. Figures were created using Matplotlib 2.1.0 ([Hunter, 2007](#)) and Nilearn 0.4.0 ([Abraham et al., 2014](#)).

3.2 Results

All scripts and results are available through our Open Science Framework (OSF; ([Erin D. Foster, 2017](#))) Project at <https://osf.io/U2Q4Y/> ([Bowring et al., 2018a](#)), and group-level statistic maps used to create the figures in this section are available on NeuroVault: <https://neurovault.org/collections/4110/>, <https://neurovault.org/collections/4099/>, <https://neurovault.org/collections/4100/>, for ds0000001, ds000109 and ds000120 respectively. All analysis scripts, results reports, and notebooks for each study are available through Zenodo ([Nielsen and Smith, 2014](#)) at <https://doi.org/10.5281/zenodo.1203654> ([Bowring et al., 2018b](#)).

Registration of each subject's functional data onto the anatomy was visually assessed. The mean and standard deviation images of the MNI structural and (mean) functional data (**FIG S1**, note that axial slices are slightly different between software due to different bounding boxes of the images) substantiate that registration was successful in all packages across the three studies.

3.2.1 Cross-Software Variability for Parametric Inference

While qualitatively similar, variability in t -statistic values and locations of significant activation was substantial between software packages across all three studies.

Comparisons of the thresholded results with the published findings are shown in Figure 3.1, with further multi-slice comparisons across software in Figure 3.2 (also in Figs. S2, S4, and S6). The ds000001 study described positive activation in the

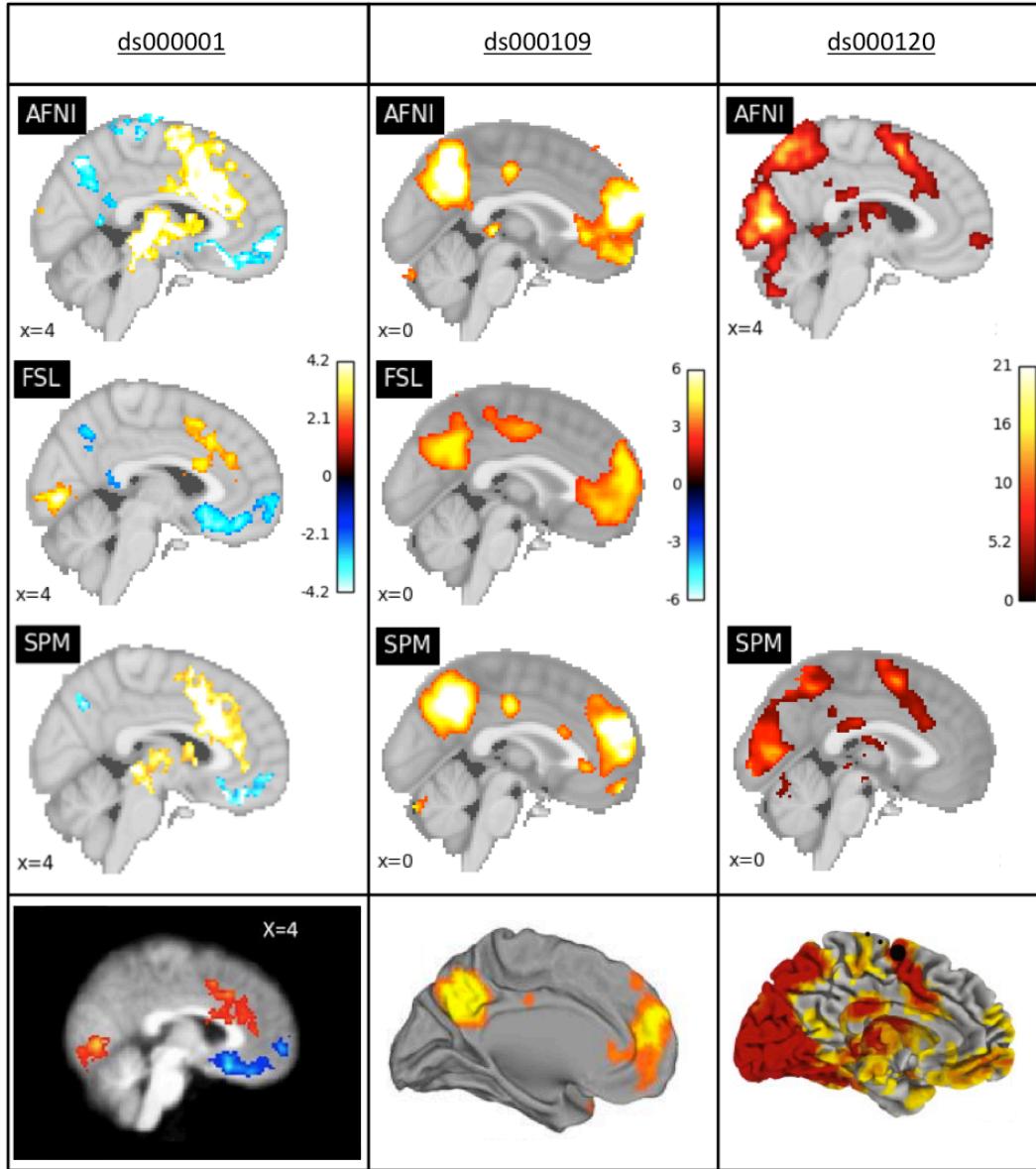


Figure 3.1: Comparison of the thresholded statistic maps from our reanalysis with the main figures from each of the three publications. Left: For ds000001 data, thresholded t -statistic images contrasting the parametric modulation of pumps of reward balloons versus the parametric modulation of the control balloon; beneath, a sagittal slice taken from Fig. 3 in [Schonberg et al. \(2012\)](#). Middle: For ds000109, thresholded t -statistic maps of the false belief versus false photo contrast; beneath, a midsagittal render from [Moran et al. \(2012\)](#). Right: For ds000120, thresholded F -statistic images of the main effect of time contrast; beneath, a midsagittal render from Fig. 3 in [Padmanabhan et al. \(2011\)](#). Note that for ds000109 and ds000120 the publication's figures are renderings onto the cortical surface while our results are slice views. While each major activation area found in the original study exists in the re-analyses, there is substantial variation between each reanalysis.

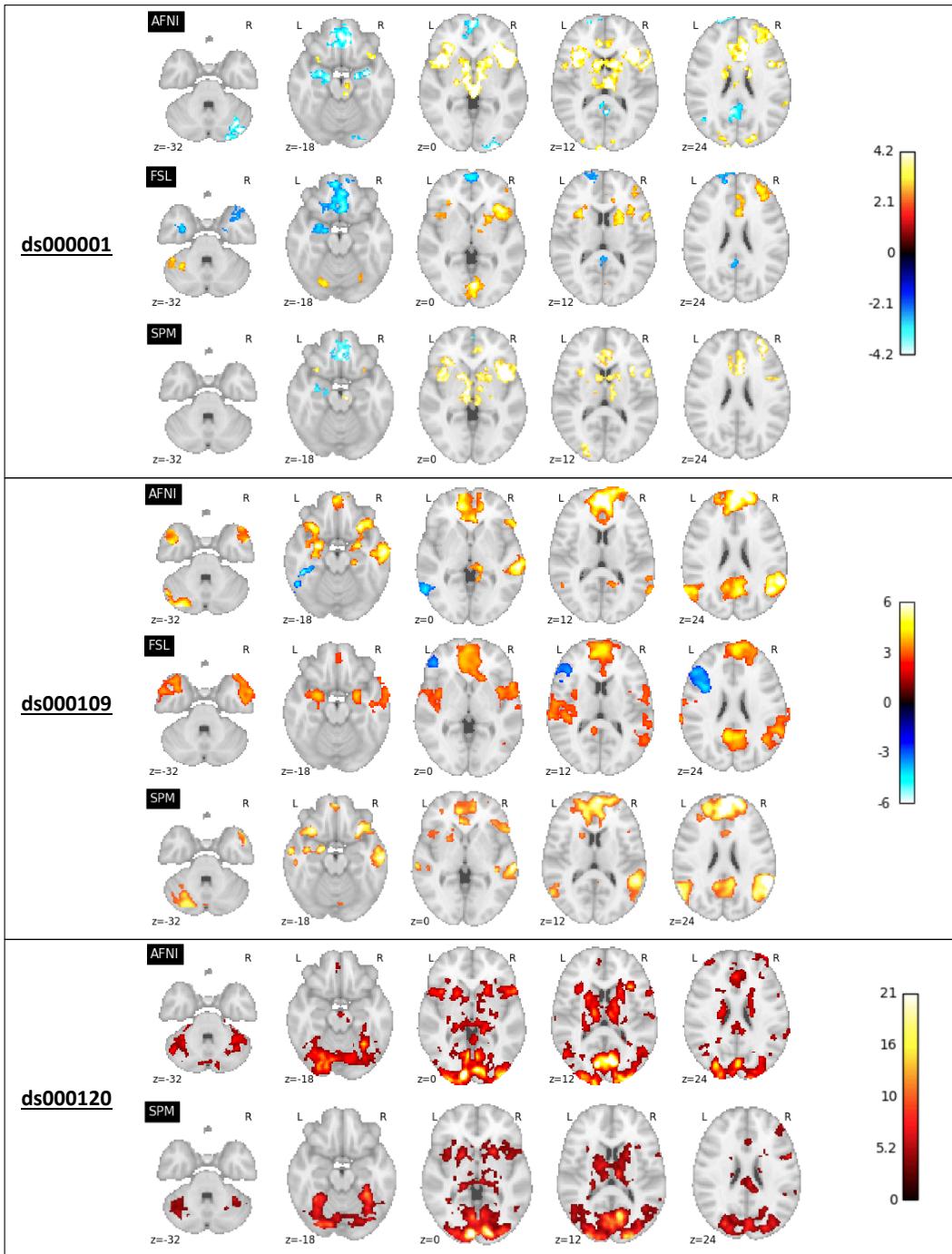


Figure 3.2: Comparison of the thresholded statistic maps from our reanalysis displayed as a series of axial slices. Top: ds000001's thresholded t -statistic maps contrasting parametric modulations of the reward balloons versus pumps of the control balloons. Middle: ds000109's thresholded t -statistic maps of the false belief versus false photo contrast. Bottom: ds000120's thresholded F -statistic maps of the main effect of time contrast. This figure complements the single slice views shown in Fig. 3.1.

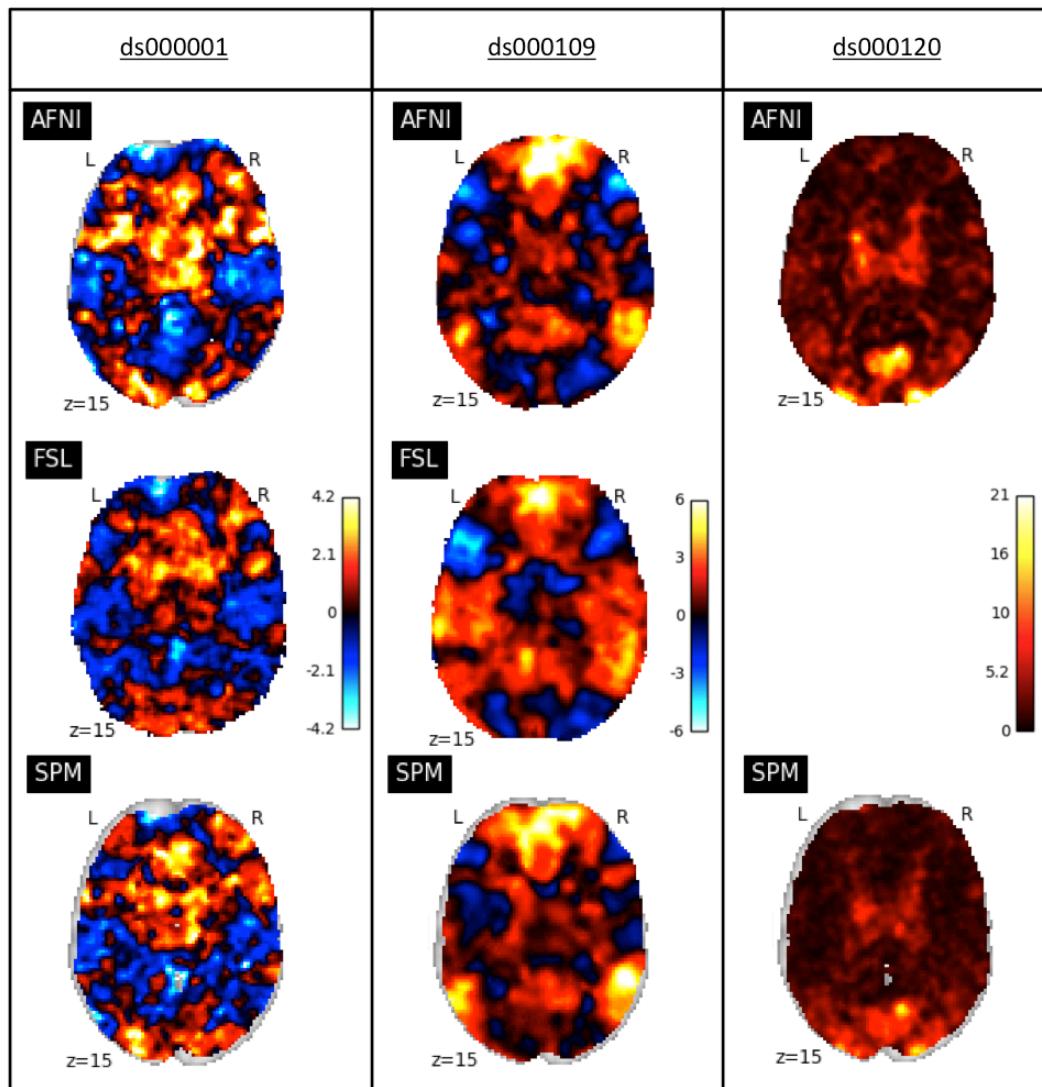


Figure 3.3: Comparison of the unthresholded statistic maps from our reanalysis of the three studies within each software package. Left: ds000001's unthresholded t -statistic maps of the parametric modulation of pumps of reward balloons versus the parametric modulation of the control balloon contrast. Middle: ds000109's unthresholded t -statistic maps of the false belief versus false photo contrast. Right: ds000120's unthresholded F -statistic maps of the main effect of time contrast. While areas of strong activation are somewhat consistent across all three sets of reanalyses, there is substantial variation in non-extreme values.

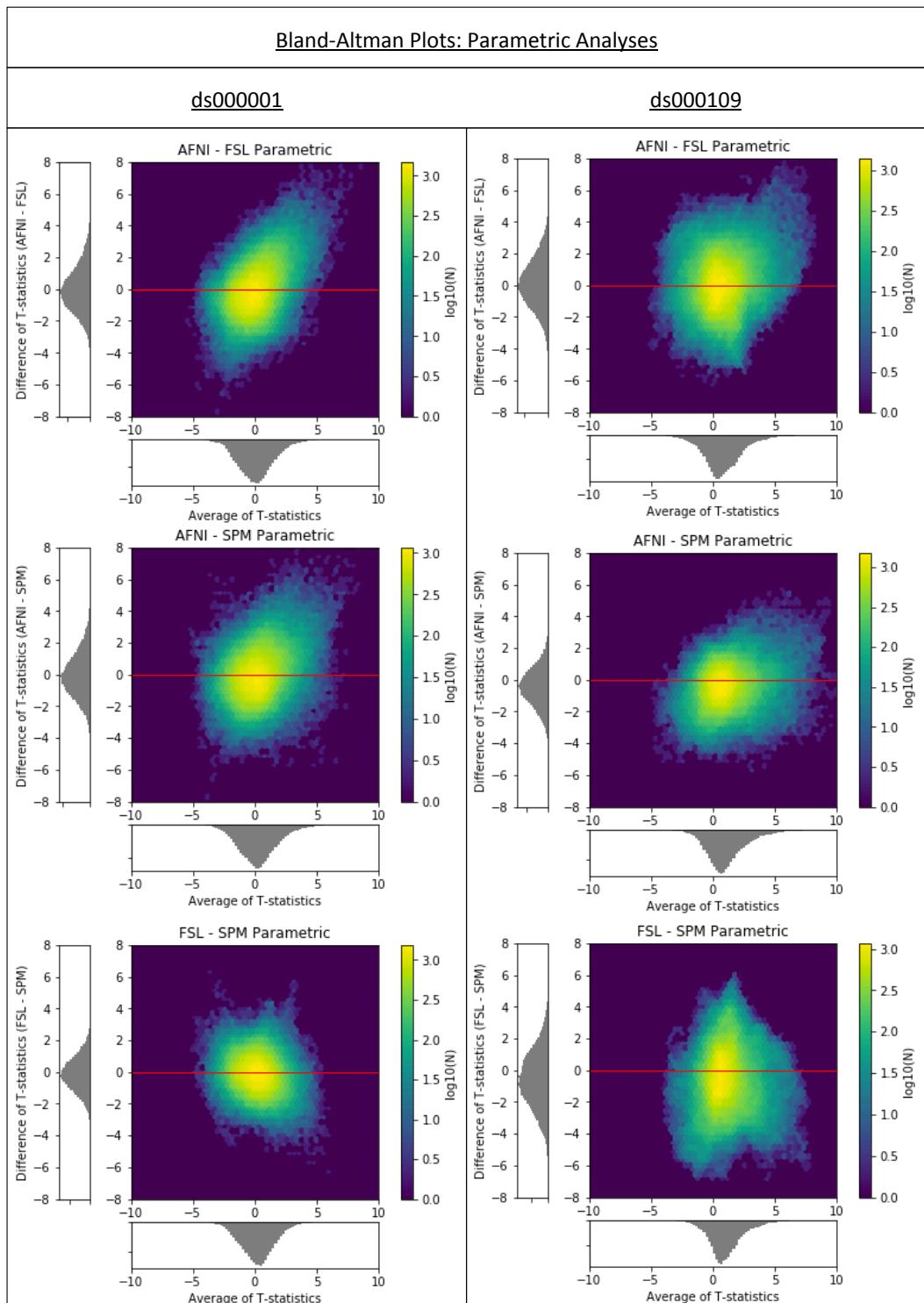


Figure 3.4: Cross-software Bland-Altman 2D histograms comparing the unthresholded group-level t -statistic maps computed as part our reanalyses of the ds000001 and ds000109 studies within AFNI, FSL, and SPM. Left; Comparisons for ds000001's balloon analog risk task, t -statistic images contrasting the parametric modulation of pumps of the reward balloons versus parametric modulation of pumps of the control balloon. Right; Comparisons for ds000109's false belief task, t -statistic images contrasting the false belief versus false photo conditions. Density images show the relationship between the average t -statistic value (abscissa) and difference of t -statistic values (ordinate) at corresponding voxels in the unthresholded t -statistic images for each pairwise combination of software packages. While there is no particular pattern of bias, as the t -statistic differences are centered about zero, there is remarkable range, with differences exceeding ± 4 in all comparisons.

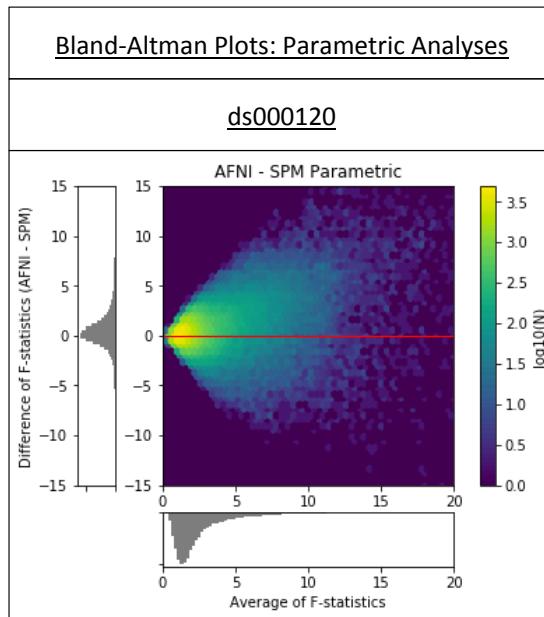


Figure 3.5: Cross-software Bland-Altman 2D histogram comparing the unthresholded main effect of time F -statistic maps computed in AFNI and SPM for reanalyses of the ds000120 study. The differences are generally centered about zero, with a trend of large F -statistics for AFNI. The funnel-like pattern is a consequence of the F -statistic taking on only positive values.

bilateral anterior insula, dorsal anterior cingulate cortex (ACC), and right dorsolateral prefrontal cortex, and negative activation in the ventromedial prefrontal cortex and bilateral medial temporal lobe. In our reanalysis (Fig. 3.1, left) all three software found activation in these set of regions, with the exception that decreases in the medial temporal lobe were unilateral in FSL and SPM (left only). FSL also detected a visual response that neither AFNI or SPM picked up on (Fig. 3.1, left, and Fig. 3.2, top, $z = 0$ slice).

The ds000109 study reported activations in the bilateral temporoparietal junction (TPJ), precuneus, anterior superior temporal sulcus (aSTS), and dorsal medial prefrontal cortex (dmPFC). Similar activations from our reanalyses are seen in Figure 3.1, middle, although FSL only found activation in the right TPJ and aSTS. Further comparisons shown in Figure 3.2, middle, highlight disagreement in the results: AFNI and FSL detected significant deactivations in distinct brain regions (inferior temporal gyrus for AFNI, inferior frontal gyrus for FSL), while SPM did not determine any significant deactivation. FSL also found a positive response in the superior temporal gyrus (STG) where AFNI and SPM did not (Fig. 3.2, middle, $z = 0$ and $z = 12$ slices).

The original ds000120 study found extensive activations for the main effect

of time – the frontal, supplementary, posterior parietal cortex, basal ganglia, pre-frontal cortex, ventral striatum and orbitofrontal cortex all showed significant activation. Our reanalyses (Fig. 3.1, right) are consistent with these findings, with the exception that neither AFNI or SPM exhibited orbitofrontal (OFC) activation (though, the SPM analysis mask had poor OFC coverage). AFNI’s F -statistic values look to be generally larger than SPM here (Fig. 3.2, bottom, $z = 0$ and $z = 12$ slices). The unthresholded statistic maps from our reanalyses (Figs. 3.3, S7, S9 and S11) also show that while extreme values display moderate agreement, there are considerable differences across the brain in each given study.

NeuroSynth association analyses conducted on the unthresholded t -statistic maps (Table 3.2) show that the most strongly related term to the activation patterns displayed across all three sets of results was the same: ‘anterior insula’ for each software’s ds000001 map, ‘medial prefrontal’ for ds000109, and ‘visual’ for ds000120. Phrases related to the task paradigm used in each study (‘goal’ for ds000001, ‘theory mind’ for ds000109, ‘visual’ for ds000120) were found across all software’s activation patterns, alongside a range of common anatomical terms.

Figure 3.4 compares statistic values across packages using Bland-Altman plots (rendered as 2D histograms) for ds000001 and ds000109. The distribution of the pairwise differences in t -statistics (y-axes) is generally centered about zero, indicating no particular bias, however there is substantial variation here, with t -statistic differences exceeding 4.0 in magnitude. Pairwise correlations ranged from 0.429 to 0.747 for inter-software comparisons (3.3). The Bland-Altman plots comparing percentage BOLD change maps (Fig. S13) are more conclusive, showing a clear trend for SPM to report larger effect estimates than the other two packages. Figure 3.5 presents the Bland-Altman plot comparing unthresholded F -statistic images for ds000120, which has a very different appearance due to F -statistics being non-negative. The corresponding Bland-Altman plot comparing partial R^2 values (Fig. S14) for this study is similar in shape. Broadly speaking, while there are no gross differences in sensitivity, there is a slight tendency for AFNI’s extreme statistics to exceed FSL’s and SPM’s, and SPM’s to exceed FSL’s, most evident in ds000109.

Spatial localization of significant activation in the thresholded t -statistic images also varied across software packages. Figure 3.6 shows the Dice coefficients for all pairs of analyses (parametric results are presented in first 3 rows of larger triangles). For ds000001, the average value of Dice coefficients comparing locations of activations across reanalyses is 0.379. These values improve for ds000109, where the mean Dice coefficient for positive activations is 0.512. Here, AFNI and FSL were the only software packages to report significant negative clusters for the ds000109

Table 3.2: Neurosynth Analyses. The Neurosynth analysis terms most strongly associated (via Pearson correlation) to each software's group-level statistic map across the three studies. Non-anatomical terms are shown in bold.

	AFNI		FSL		SPM	
	Neurosynth Analysis	Pearson Corr.	Neurosynth Analysis	Pearson Corr.	Neurosynth Analysis	Pearson Corr.
ds000001	Anterior insula	0.359	Anterior insula	0.240	Anterior insula	0.322
	Insula	0.276	Task	0.233	Anterior	0.245
	Anterior	0.243	Tasks	0.203	Insula	0.240
	Insula anterior	0.233	Parietal	0.190	Goal	0.229
	Thalamus	0.221	Goal	0.188	Task	0.225
	Goal	0.211	Working memory	0.184	Insula anterior	0.214
	Pain	0.198	Working	0.181	Thalamus	0.201
	Supplementary	0.197	Basal ganglia	0.173	Acc	0.199
	Premotor	0.196	Ganglia	0.172	Anterior cingulate	0.196
	Anterior cingulate	0.192	Basal	0.169	Ganglia	0.188
	Medial prefrontal	0.422	Medial prefrontal	0.355	Medial prefrontal	0.361
	Medial	0.381	Medial	0.309	Theory mind	0.331
ds000109	Default	0.366	Default	0.301	Default	0.329
	Theory mind	0.348	Posterior cingulate	0.299	Precuneus	0.314
	Default mode	0.341	Default mode	0.290	Default mode	0.310
	Precuneus	0.334	Social	0.282	Medial	0.301
	Posterior cingulate	0.327	Cingulate	0.275	Mind	0.296
	Social	0.322	Theory mind	0.270	Prefrontal	0.294
	Mind	0.311	Resting	0.261	Mind tom	0.289
	Mind tom	0.287	Precuneus	0.259	Posterior cingulate	0.287
	Visual	0.377			Visual	0.481
	v1	0.317			Occipital	0.367
	Occipital	0.293			v1	0.340
	Eye	0.261			Visual cortex	0.267
ds000120	Eye movements	0.252			Spatial	0.248
	Visual cortex	0.243			Spl	0.245
	Early visual	0.241			Eye	0.242
	Spatial	0.232			Early visual	0.238
	Task	0.229			Lingual	0.238
	Parietal	0.222			Intraparietal	0.237

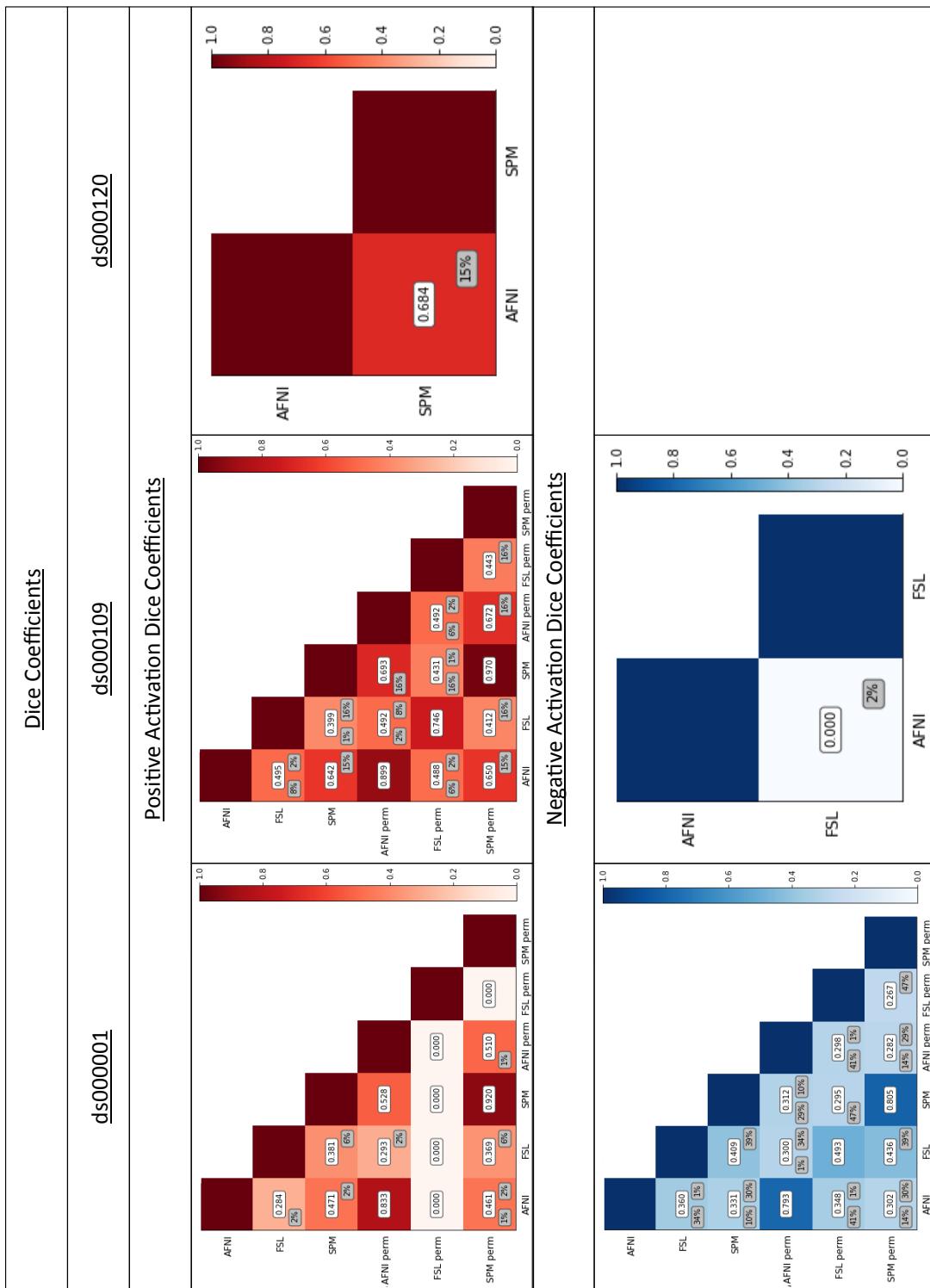


Figure 3.6: Cross-software Bland-Altman 2D histogram comparing the unthresholded main effect of time F -statistic maps computed in AFNI and SPM for reanalyses of the ds000120 study. The differences are generally centered about zero, with a trend of large F -statistics for AFNI. The funnel-like pattern is a consequence of the F -statistic taking on only positive values.

Table 3.3: Summary of test statistics mean differences and correlations for each pair of test statistic images. Mean differences correspond to the y-axes of the Bland-Altman plots displayed in Figures 3.4, 3.4, 3.9 and 3.10. Each mean difference is the first item minus second; for example, AFNI versus FSL mean difference is AFNI-FSL. Correlation is the Pearson's r between the test statistic values for the pair compared. Intersoftware differences are greater than intrasoftware.

Software	Inference Type	ds000001		ds000109		ds000120	
		Mean Difference	Pearson Corr.	Mean Difference	Pearson Corr.	Mean Difference	Pearson Corr.
AFNI vs. FSL	Parametric	0.009	0.616	0.035	0.585		
	Nonparametric	0.271	0.577	0.006	0.573		
AFNI vs. SPM	Parametric	0.061	0.614	-0.490	0.747	0.415	0.748
	Nonparametric	-0.096	0.628	-0.445	0.787	n\ a	n\ a
FSL vs. SPM	Parametric	-0.047	0.684	-0.529	0.429		
	Nonparametric	-0.479	0.720	-0.439	0.438		
AFNI	Para. vs Nonp.	0.155	0.984	-0.048	0.981		
FSL	Para. vs Nonp.	0.382	0.844	-0.064	0.946		
SPM	Para. vs Nonp.	0.000	1.000	0.000	1.000		

study. Strikingly, these activations were found in completely different anatomical regions for each package, witnessed by the negative activation AFNI/FSL dice coefficient of 0. Finally, the AFNI/SPM Dice coefficient for the thresholded *F*-statistic images obtained for ds000120 is 0.684; it is notable that across all studies, the AFNI/SPM dice coefficients are consistently the largest.

Spill over values, given by the grey values beneath the dice coefficients in Figure 3.6, are generally largest for SPM comparisons. They are particularly prominent in the negative activation plot for ds000001, where there is at least 30% spill over for all parametric pairwise comparisons, the largest being 39% for SPM/FSL. Recalling that these values are the percentage of activation which occurred within one package that was outside the other package's analysis mask, this is likely due to the fact SPM consistently had the smallest analysis mask out of the three packages, while FSL had the largest. In our ds000001 reanalyses, SPM's group-level analysis mask was made up of 175269 voxels, while AFNI's had 198295 voxels and 251517 for FSL. For ds000109, SPM's group-level mask contained 178461 voxels compared to AFNI's 212721 and FSL's 236889. Finally, for ds000120, SPM had 174059 voxels to AFNI's 208340. (Note FSL's mask image has slightly but consistently more non-zero voxels than in its statistical result images).

Further evidence of spatial variability is also exhibited by the Euler Characteristic (EC) plots for the parametric analyses presented in Figure 3.7, top (and supple-

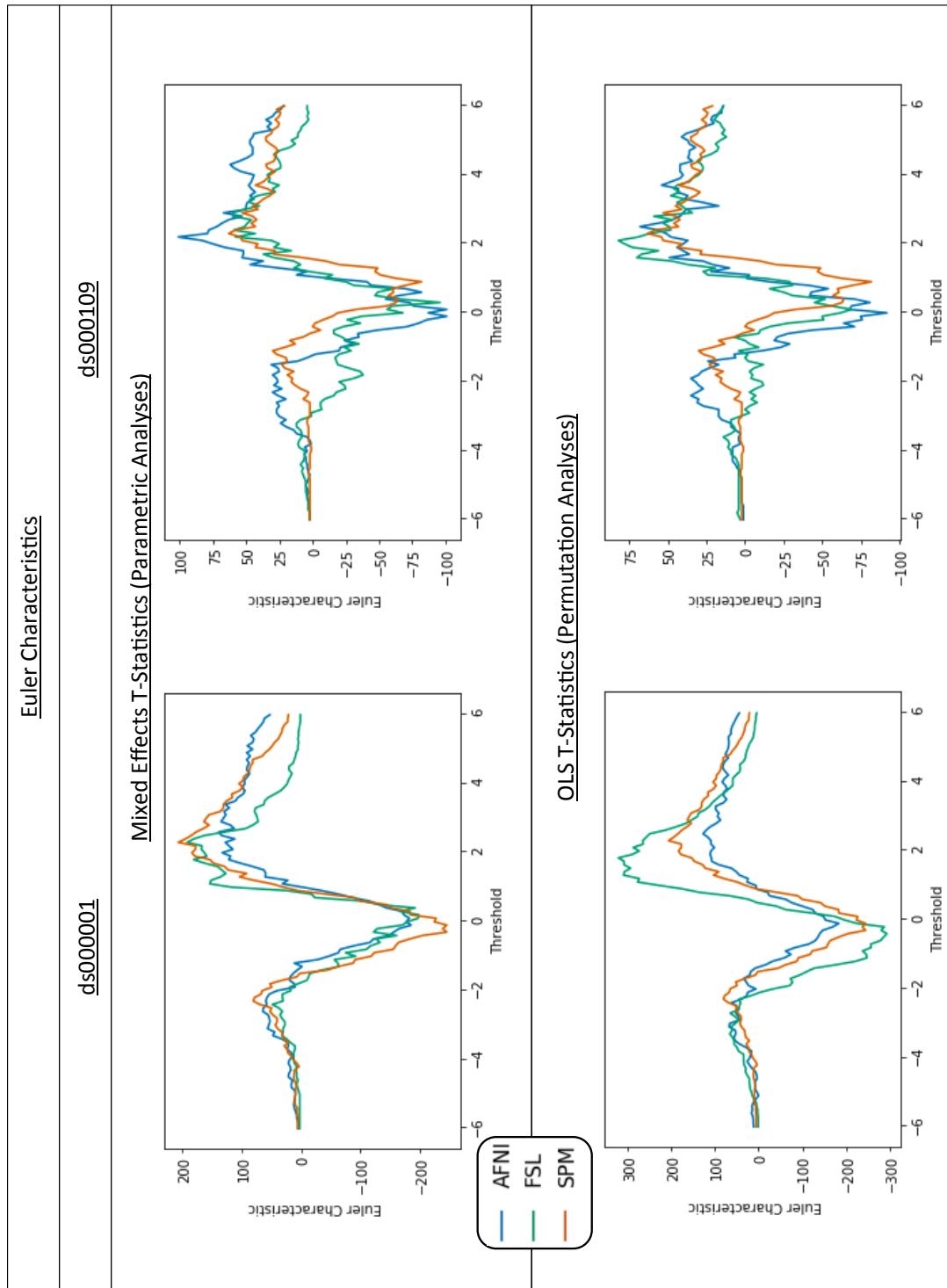


Figure 3.7: Euler characteristic (EC) plots for ds000001 and ds000109. On top, comparisons of the Euler characteristic computed for each software's t -statistic map from our reanalyses using a range of t -value thresholds between -6 and 6. Below, comparisons of the ECs calculated using the same thresholds on the corresponding t -statistic images for permutation inference within each package. For each t -value the EC summarises the topology of the thresholded image, and the curves provide a signature of the structure of the entire image. For extreme thresholds the EC approximates the number of clusters, allowing a simple interpretation of the curves: For example, for ds000001 parametric analyses, FSL clearly has the fewest clusters for positive thresholds.

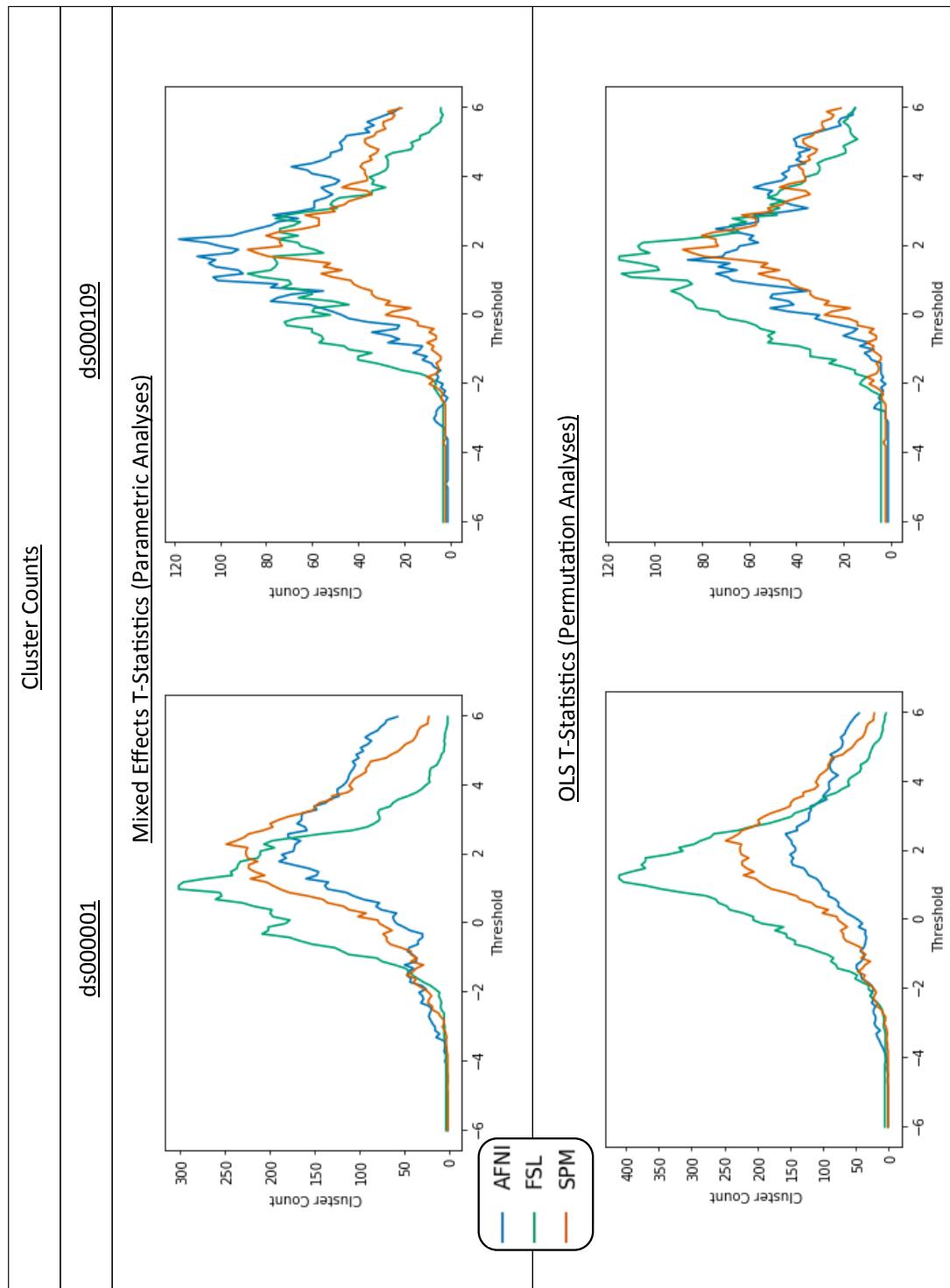


Figure 3.8: Cluster count plots for ds000001 and ds000109. On top, comparisons of the number of cluster found in each software's t -statistic map from our reanalyses using a range of t -value thresholds between -6 and 6. Below, comparisons of the cluster counts calculated using the same thresholds on the corresponding t -statistic images for permutation inference within each package.

mentary Fig. S12 for ds000120), complemented by the cluster count plots in Figure 3.8, top. We note that because the EC plots were created by thresholding each software's statistic map at a fixed range of t -values (without the computation of p -values), differences between the parametric and nonparametric EC curves are due to the different first level models used in each case (mixed-effects for parametric, OLS for nonparametric), and not due to the actual parametric and nonparametric inference procedures used to obtain p -values. Since the EC counts the number of clusters minus the number of 'handles' plus the numbers of 'holes' in an image, for large thresholds we expect the EC to closely approximate the number of clusters of significant activation present in the equivalent thresholded map. This is confirmed by Figures 3.7 and 3.8, both figures showing that across the two studies FSL had a smaller number of activated clusters at larger thresholds. For ds000001, the peak cluster count value (Fig. 3.8, top left) occurs at a lower threshold for FSL. This plot suggests that in general FSL's t -statistic values were more liberal here – the initial rise of the FSL curve signifies the t -statistic image breaking up into clusters at lower thresholds than AFNI and SPM, and then as the clusters begin to get 'thresholded out' this causes the FSL curve to dip below the other two packages. The EC plots highlight overall topological differences in the statistic maps: If the images were the same up to an image-wide monotonic transformation, this would be revealed by the EC curves having the same general shape but with some portions shifted or compressed. In this sense, the distinct shapes seen in portions of the curves (e.g. for ds000109, negative thresholds) suggest differences in the topologies of each software's activation pattern.

3.2.2 Cross-Software Variability for Nonparametric Inference

Consistent with the parametric inference results, activation localization and statistic values varied greatly between packages for the permutation test results computed for ds000001 and ds000109.

Before reviewing statistic map comparisons, we stress that the goal of these nonparametric analyses is to obtain FWE-corrected cluster p -values with weaker assumptions. Thus the permutation test unthresholded statistic maps are not "nonparametric" maps, but rather usual one-sample t -test maps that form the basis of permutation analyses. While SPM's parametric analysis uses the same one-sample t -test, AFNI's and FSL's parametric models use a mixed-effects model and weighted least squares. Hence all comparisons of the nonparametric test statistic values (in contrast to thresholded maps) do not convey information about nonparametric inference per se, but compare different preprocessing and first level modelling from the three packages while holding the second level model constant.

Quantitative assessment with Dice coefficients are shown in Figure 3.6 ("perm" vs "perm" cells) and - in accordance with the parametric results - are generally poor. Like the parametric analyses, AFNI/SPM Dice values are altogether better than the other comparisons. For ds000001, FSL's nonparametric method found no significant clusters, and thus all Dice coefficients connected to this analysis are zero. However, note that the significant regions found in the other parametric and nonparametric results for this study mostly comprise of a single activation cluster spanning the lateral and medial frontal cortex, insular cortex, basal ganglia, and brainstem - an extensive and irregularly-shaped cluster that could easily become disconnected and thus lose significance. As before, ds000109 Dice values are also generally better than ds000001.

The nonparametric Bland-Altman plots (Fig. 3.9) show substantial spread qualitatively similar to the parametric ones (Fig. 3.4), and correlations between statistics maps are similar for nonparametric in congruence with the parametric comparisons (Table 2). EC curves (Fig. 3.7, bottom) again exhibit considerable topological variation between software packages. Notably, while AFNI and SPMs EC curves are relatively similar across choice of inference method, FSL permutation inference determined substantially more clusters than parametric for low positive thresholds in both studies (Figs. 3.7 and 3.8, bottom).

3.2.3 Intra-Software Variability, Parametric vs Nonparametric

Comparisons of parametric and permutation test inference results within each package hold all preprocessing and first level modelling constant, only varying the second level model and inference procedure. The level of agreement between the two inferences *within* each package varied greatly across software. Before making comparisons, we note that since SPM's parametric and nonparametric inference share the same group level model, the unthresholded statistic images produced using each inference model are identical here.

The thresholded statistic maps are generally similar within each of the software packages (ds000001: Fig. S2 vs Fig. S3; ds000109: Fig. S4 vs S5), with the exception of FSL's nonparametric inference 'decreases-only' finding for ds000001. Unthresholded maps are notably more similar for ds000109 (Fig. S9 vs S10) than for ds000001 (Fig. S7 vs Fig. S8), again noting that SPM's pairs of maps here are identical.

Bland-Altman plots (Fig. 3.10) reveal much greater levels of parametric-nonparametric agreement, with AFNI displaying greater agreement than FSL. For FSL, we selectively investigated voxels that differed by the greatest amount, and often found indi-

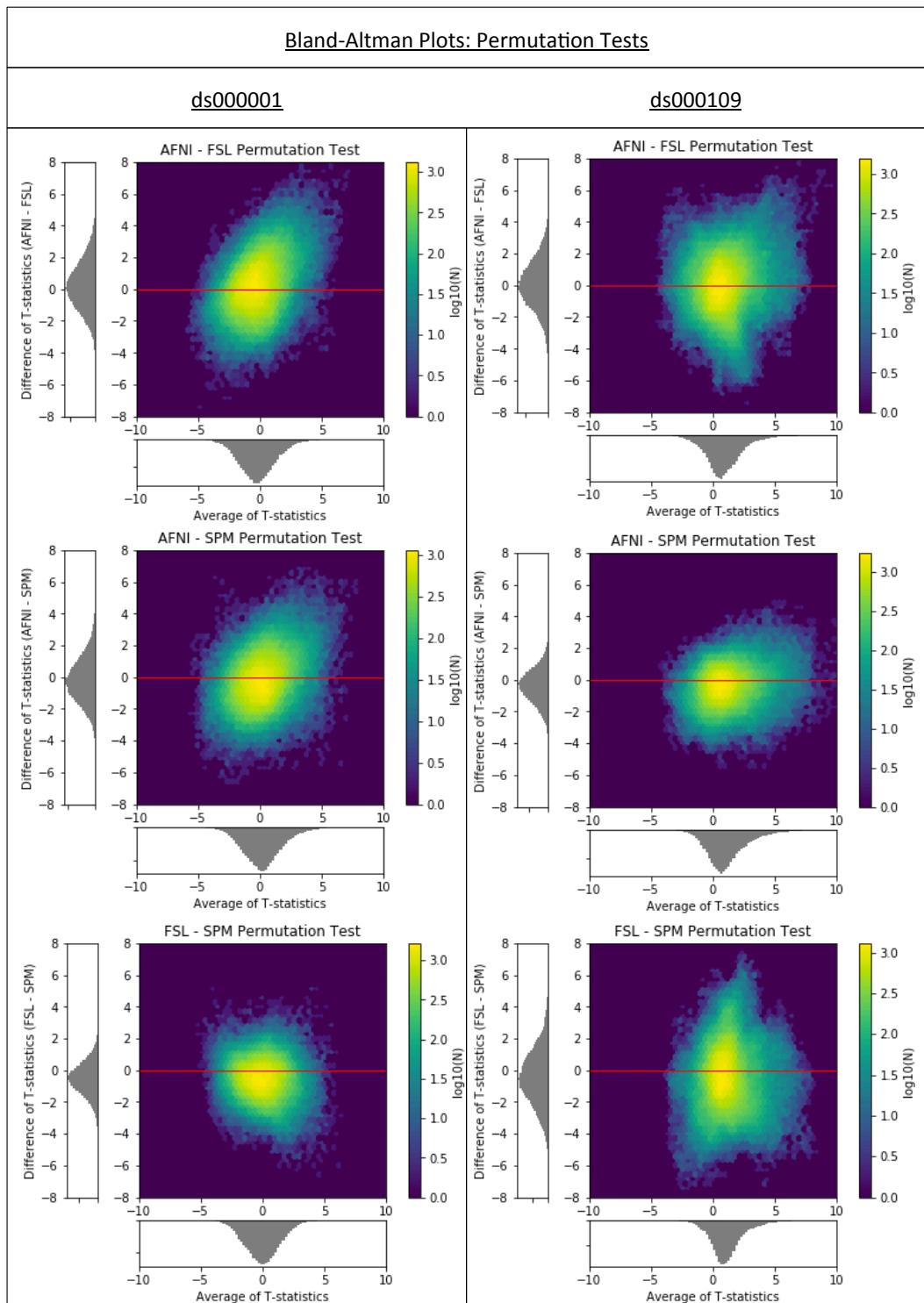


Figure 3.9: Cross-software Bland-Altman 2D histograms for the ds000001 and ds000109 studies comparing the unthresholded group-level t -statistic maps computed using permutation inference methods within AFNI, FSL, and SPM. Similar to the results obtained using parametric inferences in Figure 3.4, all of the densities indicate large differences in the size of activations determined within each package.

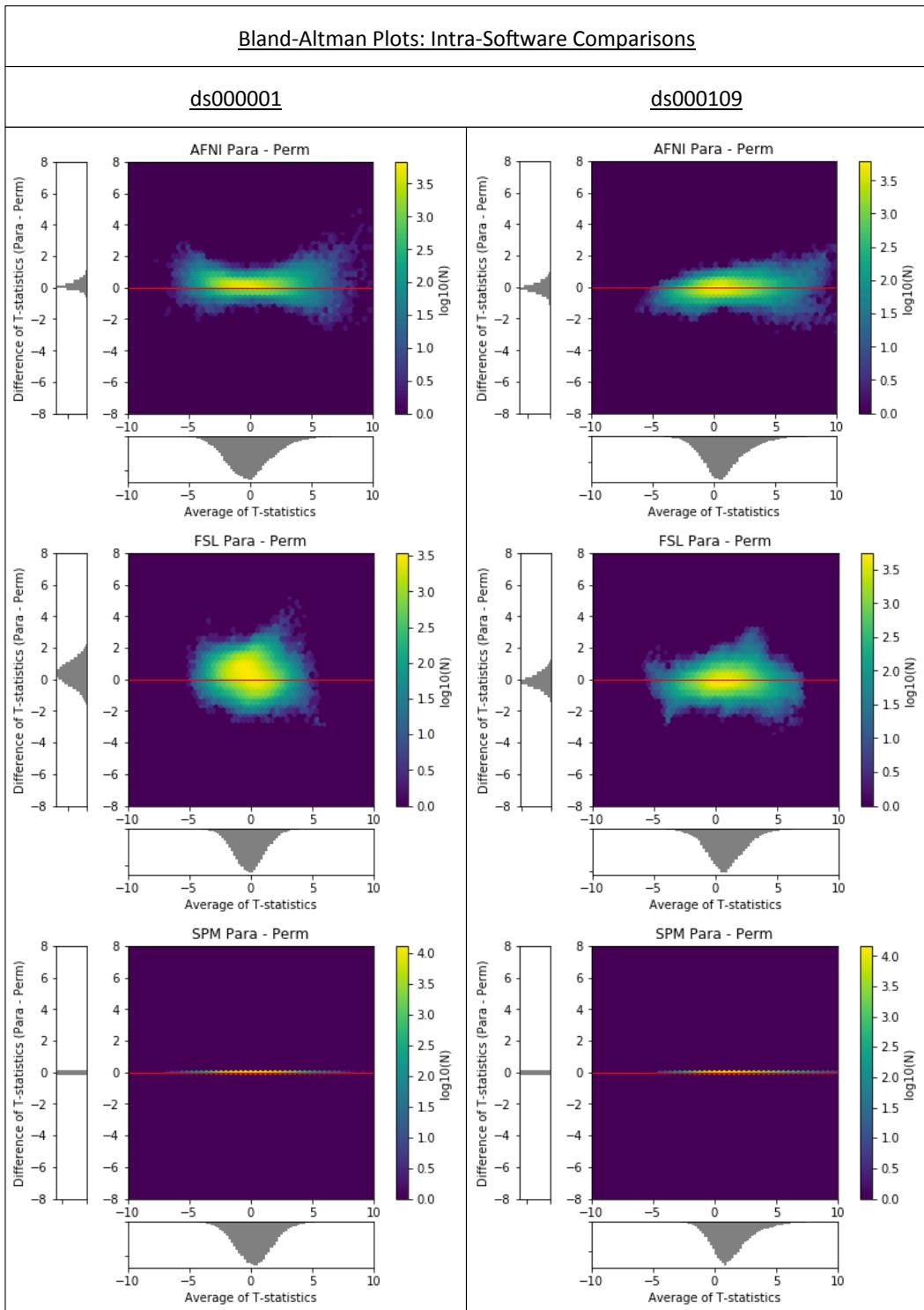


Figure 3.10: Intrasoftware Bland-Altman 2D histograms for the ds000001 and ds000109 studies comparing the unthresholded group-level t -statistic maps computed for parametric and nonparametric inference methods in AFNI, FSL and SPM. Each comparison here uses the same preprocessed data, varying only the second level statistical model. SPM's parametric and nonparametric both use the same (unweighted) one-sample t -test, and thus show no differences. AFNI and FSL's parametric models use iterative estimation of between subject variance and weighted least squares and thus show some differences, but still smaller than between-software comparisons

vidual subjects responsible: A single subject with a large observation can drive a conventional one-sample t -test, but when that same subject also has large intrasubject variance FSL’s mixed effect model downweights that subject leading to a substantially different t -test. For ds000109, the increased difference in AFNI’s values for larger statistic values could also reflect a similar downweighting procedure within the software.

The Dice coefficients comparing the thresholded permutation test and parametric inferences are generally the best of any (Fig. 3.9, 3-element lower diagonal). In general the origin of parametric-nonparametric differences are parametric inference finding a slightly larger number of clusters significant.

3.3 Discussion

Our results have displayed extensive differences in the results between the analysis pipelines of the three software packages. The low Dice values and differences in Euler characteristics (Figs. 3.6 and 3.7) are particularly salient, showing heterogeneity in the sizes and shapes of clusters determined across packages, indicating a strong dependence on software in terms of the anatomical regions covered by the activation. While some authors have pointed out the limitations of interpreting differences in the set of voxels that make up a significant activation when using clusterwise inference (which makes assessments based on topological properties of statistical maps) ([Chumbley and Friston, 2009](#)), we see merit in the use of quantitative measurements such as Dice due to the ultimate application of statistical maps to infer on precise areas of the brain active during a task. While a deeper analysis on the differences between topological aspects of images across software would be valuable, there are inherent difficulties in this approach, such as identifying corresponding features between maps when the number and size of activations reported are variable across software.

It is notable that the level of variation in our analysis results also fluctuated across the datasets we analysed. This is highlighted in our Dice comparisons, where the ds000001 Dice coefficients are considerably smaller than ds000109 for both the inter and intra-software comparisons. The relatively poor performance of ds000001 may be due to the smaller sample size for this study (16 vs 21 for d000109), as well as the particular inference method used. For ds000001, group-level inference was conducted using a cluster-forming threshold of $p < 0.01$ uncorrected. A recent study ([Eklund et al., 2016](#)) found that parametric inference for a one-sample t -test at this threshold in AFNI, FSL and SPM resulted in false-positive rates far exceeding the

nominal level – severely for cluster-forming threshold $p < 0.01$, modestly for $p < 0.001$ – while nonparametric permutation performed closer to the expected 5% FWE level. The results obtained here for ds000001 are consistent with these findings: across all three software packages, the thresholded images produced from permutation test inference display fewer significant clusters than the corresponding parametric maps. While the cluster-defining threshold $p < 0.005$ applied in the ds000109 study was not analysed in Eklund et al., consistency between packages using parametric and nonparametric inference was greater for this study.

Notably, while all packages are purportedly using the same MNI atlas space, an appreciable amount of activation detected by AFNI and FSL fell outside of SPM's analysis mask (shown by the 'spill over' values displayed in gray, Fig. 3.6). Considerable differences in mask sizes are likely to have been a major factor for the disparities in activation and low dice coefficients seen across packages. For effects close to the edge of the brain, a larger analysis mask allows for a larger cluster volume, which can ultimately be the difference as to whether a cluster is determined as significantly active or not. This may explain why only FSL – which had the largest analysis mask – found an auditory response in the ds000109 study, or why Dice coefficients are generally worse for negative activations than positive in our ds000001 renanalyses, where positive clusters were on-the-whole reported in more central anatomical regions. Another possible reason for poor Dice values here is that the size and number of clusters determined for negative activations was smaller than that of positive activations. Since Dice and spill-over values are proportional measurements, this means they will have been more susceptible to differences in cluster and mask size for the negative activations relative to the positive. Disagreement in atlas space may have contributed to the lack of structure in the Bland-Altman plots, however no gross misalignment between packages was evident (Fig. S1). While far from perfect, the ds000120 AFNI and SPM thresholded results have the best Dice similarity score, likely due to the use of a very strong main effect as an outcome of interest.

Qualitative comparison of the results provide some optimism, with certain patterns of activation found across all packages. For example, the ds000001 parametric analyses were unanimous in determining significant activation in the anterior insula. While there is greater discordance over the precise location of activation within the anterior insular region, as well as the precise statistic values here, altogether our results align. This may substantiate that the strongest effects are robust across packages, supported by our own comparisons of the unthresholded maps that showed moderate agreement between software packages in areas with strong signal (many of these anatomical regions were identified across all three package's Neu-

roSynth association analyses) but greater disagreement elsewhere, ds000109 and ds000120 displaying more consistency than ds000001. However, in making these qualitative comparisons, what has become most transparent is the importance for researchers to – at the very least – share their final statistical maps. The reasons for this are exhibited most clearly by our ds000109 analyses; the visual slice comparison of our replications of the main figure from the original study in Figure 3.1, shown alongside the publication figure itself, look remarkably similar and could lead to the conclusion that each package’s results highly agree. It is only when analysing these results over the whole brain that we discover broad differences in these activation patterns, e.g. positive activation identified in the auditory cortex in FSL that was not reported by AFNI and SPM, and significant deactivation determined only by AFNI and FSL.

At the start of our investigations, we selected a common set of preprocessing steps to be applied within each software package across all studies regardless of whether they had been used in the original analysis. This was to maximise the comparability of the results while being consistent with best practices within the community. However, several complications arose during our analyses. For ds000001, orientation information was missing from seven of the subject’s structural and functional scans. Because the source DICOM files were no longer available, it was not possible to retrieve the original position matrices. As a consequence of this, the structural and functional images were misaligned, resulting in suboptimal coregistration during our analyses. Additionally, a bug in the event-files induced during data conversion to the BIDS standard had resulted in some of the event timings being lost. Thanks to the cooperation of BIDS and OpenfMRI these problems were solved; a revised dataset (Revision: 2.0.4) was uploaded to OpenfMRI and used in our analysis.

Future efforts would be strengthened by additional sharing of analysis scripts and statistic maps, enabling confirmation of analyses that follow original procedures and permitting more quantitative comparison of statistic maps. We have made all of our analysis scripts available and statistic maps available, and we hope more researchers join this trend to advance openness in neuroimaging science.

3.3.1 Limitations

This study has mainly focused on comparing statistic maps, since these are the images studied to make judgements about localisation and determine the neuroscientific interpretation of results. However, by comparing the statistic maps obtained at the end of the pipeline, we have only assessed the net accumulation of differences across the entire analysis procedure. To illuminate the specific steps that contribute

most to this variation, further in-depth assessment of software differences at each stage of the analysis pipeline will be required. One recent example of this was a study that investigated differences in the pre-whitening procedures conducted in AFNI, FSL and SPM, by employing an analysis pipeline that used a single software package to carry out all other stages of processing ([Olszowy et al., 2019](#)). Further work could consider the factorial expansion of all possible combinations of preprocessing, first level modelling, and second level modelling, akin to previous efforts in assessing reproducibility over a number of pipelines ([Strother et al., 2002](#)).

Due to the restrictive requirements of this investigation – the necessity for published task-based fMRI data using analysis methods compatible in AFNI, FSL, and SPM – the three studies analysed here were found to be the only datasets hosted on OpenfMRI suited to the aims of our investigation. Of the datasets that were not used, the most common reasons for exclusion were that no publication was associated to the data, that the sample size of the study was too small, or that custom software or region of interest analysis had been used as part of the analysis pipeline which was not feasible across the three software packages. Nevertheless, a greater sample of studies will need to be replicated across the packages to gain a more comprehensive understanding of the variability between software and validate the results found here. With increasing access to population neuroimaging studies, where thousands of fMRI subject data are available, a future study could test for non-zero software-related variation by splitting a large dataset (e.g. UK Biobank ([Alfaro-Almagro et al., 2018](#)), $N > 10,000$) into smaller subsets to generate an extensive collection of replication analyses across the three packages. This may allow for the creation of a null-distribution from which differences between software results could be assessed in terms of statistical significance and confidence intervals, expanding on the raw concrete differences between t -statistic maps highlighted in this effort. As simulation techniques become more advanced, there is also the potential for creation of synthetic subject-level fMRI data as a ground truth to which each software package's results could be compared ([Ellis et al., 2019](#)).

Of the datasets we did use, subject data were missing from both the ds000109 and ds000120 datasets. For ds000109, while 29 young adults were scanned for the false belief task, only 21 were present in the dataset; for ds000120, we analysed 17 subjects instead of 30 used in the original study. These analyses therefore should not be compared like-for-like with the published results, and have substantially less statistical power than the original studies. Overall, our sample sizes for the three datasets analysed (ds000001, ds000109, ds000120) are 16, 21, and 17 respectively. While small, these sample sizes are fairly representative of a typical functional neu-

roimaging study over the past two decades – between 1995 and 2015, the median sample size of an fMRI study increased steadily from 8 to 22 (Poldrack et al., 2017). This increase has continued, and a review of 2017 publications found a median sample size of 33 (Yeung, 2018). Hence while our datasets are important for judging previous work, a future comparison exercise with larger datasets would be a valuable addition to the literature.

We have kept many parameters fixed in our analyses, such as the use of non-linear registration for all software packages, and the addition of motion regressors in all our design matrices. How changes in these variables influence the analysis results warrants further investigation; for example, while we decided to fix a 2mm cubic voxel size in all packages (since this is the default in FSL, SPM), a recent study found that alterations in this parameter can significantly impact statistical inference (Mueller et al., 2017). There are also many areas of the parameter space we have not explored, such as the inclusion of analyses that use small volume corrections, more stringent cluster-forming thresholds (Eklund et al., 2016; Woo et al., 2014), and two-tailed testing (Chen et al., 2018).

3.4 Conclusion

Across all three of the studies reanalysed here we have discovered considerable differences between the AFNI, FSL, and SPM results. The scale of these differences has been highlighted by each of the quantitative metrics applied to compare the group-level statistic maps: Dice coefficients were commonly less than 50% for cross-software comparisons, Bland-Altman plots showed that differences between reported t -statistic values were as large as 4 for a considerable quantity of voxels, and Euler Characteristic curves displayed a divergence in the number of clusters being reported in each software - even at large thresholds.

In reporting these comparisons, we are not making any statements as to which software package is better or worse. Without a gold standard to compare against no such claims can be made, and we believe further development of well-validated pipelines by multiple groups can encourage innovation and ultimately benefit the field. Rather, we feel that the key contribution of our work is the quantitative measurement of inter-software differences on common datasets. Our finding that exceedingly weak effects may not generalise across packages – evidenced across all three of our analyses – is the primary take-home message of this work. While larger effects were found to be more robust – demonstrated by the similar Neurosynth association analysis results that suggest some alignment in the final qualitative conclu-

sions that can be drawn from all three software's statistical maps – we stress that our analyses have been conducted under particularly favourable conditions: The use of studies with a strong, primary effect and extensive efforts made to harmonise the three analyses. Because of this, at best our results present an optimistic view of inter-software disparities. To better understand the underlying differences between software, further work on quantification of pipeline-related variation is needed, which in the long-term will hopefully lead to harmonisation in software implementation to reduce these differences. Another line of work would be the creation of integrative intra-study, ensemble learning techniques to integrate inconsistent findings. An additional contribution with this effort is to provide generalizable measures and metrics to enable software validation, which we hope may benefit any further comprehensive comparison of software packages.

CHAPTER 4

Spatial Confidence Sets for Task-fMRI Inference

4.1 Introduction

4.2 Theory

4.2.1 Overview

A comprehensive treatment of the original method, including proofs, can be found in SSS. Here we develop the method specifically for the general linear model (GLM) and describe our own enhancements to the method. While the method can be performed for subject-level inference, we will motivate the method in the context of a group-level analysis, describing how the method can be applied to subject-level %BOLD estimate maps in order to obtain group-level CSs making confidence statements about %BOLD effect sizes relating to the entire population from which the participants were drawn.

For a compact domain $S \subset \mathbb{R}^D$, e.g. $D = 3$, consider the GLM at location $s \in S$,

$$\mathbf{Y}(s) = \mathbf{X}\boldsymbol{\beta}(s) + \boldsymbol{\epsilon}(s) \quad (4.1)$$

where $\mathbf{Y}(s)$ is an $N \times 1$ vector of observations at s , \mathbf{X} is an $N \times p$ design matrix, $\boldsymbol{\beta}(s)$ is an $p \times 1$ vector of unknown coefficients, and $\boldsymbol{\epsilon}(s)$ an $N \times 1$ vector of mean-zero errors, independent over observations, and with each ϵ_i having common variance $\sigma^2(s)$ and some unspecified spatial correlation. (Throughout we use boldface to indicate a vector- or matrix-valued variable.) In the context of a task-fMRI analysis, $\mathbf{Y}(s)$ is a vector of subject-level %BOLD response estimate maps obtained by applying a first-level GLM to each of the N participants functional data.

For a $p \times 1$ contrast vector \mathbf{w} , we seek to infer regions of the brain where a

contrast of interest $\mathbf{w}^T \boldsymbol{\beta}$ has exceeded a fixed threshold c . Particularly, we are interested in the noise-free, population cluster defined as:

$$\mathcal{A}_c = \{\mathbf{s} \in S : \mathbf{w}^T \boldsymbol{\beta}(\mathbf{s}) \geq c\}. \quad (4.2)$$

Since we are unable to determine this excursion set in practice, our solution is to find spatial CSs: an upper set $\hat{\mathcal{A}}_c^+$ and lower set $\hat{\mathcal{A}}_c^-$ that surround \mathcal{A}_c for a desired confidence level of, for example, 95%. We emphasize that these clusters regard the raw units of the signal. Going forward, we assume that the design matrix \mathbf{X} and contrast \mathbf{w} have been carefully chosen so that $\mathbf{w}^T \hat{\boldsymbol{\beta}}$ has the interpretation of mean %BOLD change across the group. For example, in a one-sample group fMRI model where data \mathbf{Y} have %BOLD units, choosing \mathbf{X} as a column of 1's and $\mathbf{w} = (1)$ would ensure that $\mathbf{w}^T \hat{\boldsymbol{\beta}}$ has units of %BOLD change¹. In this setting, we wish to obtain an upper CS, $\hat{\mathcal{A}}_c^+$, such that we have 95% confidence all voxels contained in this set have a population raw effect size *greater* than, for example, $c = 2.0\%$ BOLD change, and a lower CS, $\hat{\mathcal{A}}_c^-$, such that we have 95% confidence all voxels *outside* of this set have a population raw effect size *less* than 2.0% BOLD change. Moreover, we desire that the 95% confidence statement holds simultaneously across both CSs at once. SSS show that a construction of such CSs is possible within the general linear model framework using the following key result.

Result 1 Consider the general linear model set-up described in (4.1). Let $\hat{\boldsymbol{\beta}}$ denote the ordinary least squares estimator of $\boldsymbol{\beta}$, $\hat{\boldsymbol{\beta}}(\mathbf{s}) = (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{Y}(\mathbf{s})$, and define $v_w^2 = \mathbf{w}^T (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{w}$ to be the normalised variance of the contrast estimate.

Then for a constant k , and for upper and lower CSs defined as

$$\hat{\mathcal{A}}_c^+ := \left\{ \mathbf{s} : \mathbf{w}^T \hat{\boldsymbol{\beta}}(\mathbf{s}) \geq c + k \hat{\sigma}(\mathbf{s}) v_w \right\}, \quad \hat{\mathcal{A}}_c^- := \left\{ \mathbf{s} : \mathbf{w}^T \hat{\boldsymbol{\beta}}(\mathbf{s}) \geq c - k \hat{\sigma}(\mathbf{s}) v_w \right\},$$

the limiting coverage of the CSs is

$$\lim_{n \rightarrow \infty} P \left[\hat{\mathcal{A}}_c^+ \subset \mathcal{A}_c \subset \hat{\mathcal{A}}_c^- \right] = P \left[\sup_{\mathbf{s} \in \partial \mathcal{A}_c} |G(\mathbf{s})| \leq k \right],$$

where $\partial \mathcal{A}_c$ denotes the boundary of \mathcal{A}_c , and G is a smooth Gaussian field on S with mean zero, unit variance, and with the same spatial correlation as each ϵ_i .

Result 1 is subject to continuity of the relevant fields and some basic conditions on

¹For examples of how to set up more complex designs and contrasts, see Figure A.2. in the Appendix A section of (Poldrack et al., 2011).

the increments and moments of the error field ϵ . A list of these assumptions, as well as a proof of Result 1, are itemized in SSS.

A 1D Intuition of the Confidence Sets

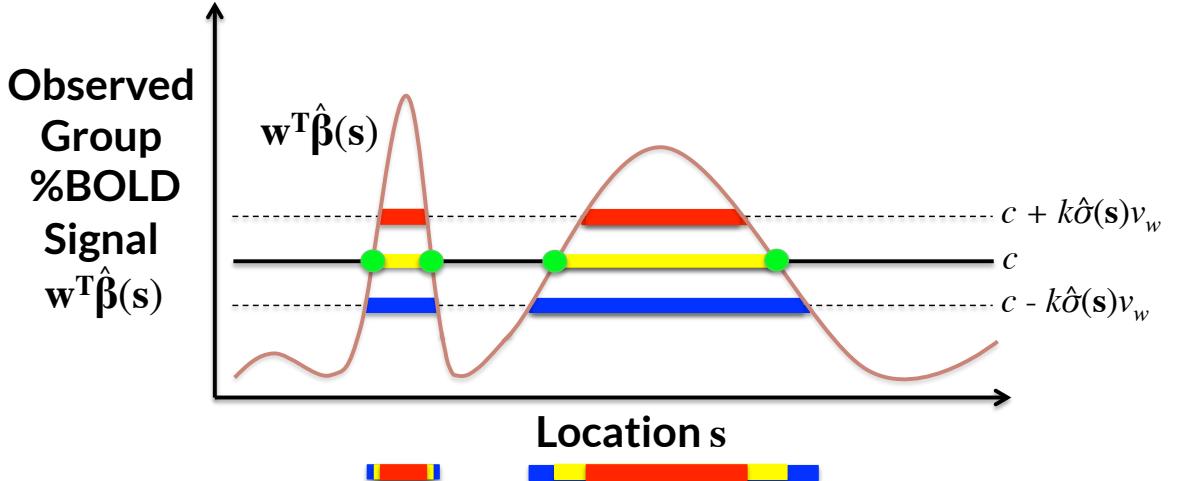


Figure 4.1: A demonstration of how the CSs are computed for a realization of the GLM $Y(s) = X\beta(s) + \epsilon(s)$ in 1 dimension, for each location s . The yellow voxels $\hat{\mathcal{A}}_c$ are obtained by thresholding the observed group contrast map at threshold c ; this is the best guess of \mathcal{A}_c , the set of voxels whose true, noise-free raw effect surpasses c . The red upper CS $\hat{\mathcal{A}}_c^+$ and blue lower CS $\hat{\mathcal{A}}_c^-$ are computed by thresholding the signal at $c + k \hat{\sigma}(s) v_w$ and $c - k \hat{\sigma}(s) v_w$, respectively. We have $(1 - \alpha)100\%$ confidence that $\hat{\mathcal{A}}_c^+ \subset \mathcal{A}_c \subset \hat{\mathcal{A}}_c^-$, i.e. that $\hat{\mathcal{A}}_c^+$ (red) is completely within the true \mathcal{A}_c , and \mathcal{A}_c is completely within $\hat{\mathcal{A}}_c^+$ (blue). We find the critical value k from the $(1 - \alpha)100$ percentile of the maximum distribution of the absolute error process over the estimated boundary $\partial\hat{\mathcal{A}}_c$ (green ●'s) using the Wild t -Bootstrap; $\hat{\sigma}$ is the estimated standard deviation and v_w is the normalised contrast variance.

For a pre-determined confidence level $1 - \alpha$ (e.g. $1 - \alpha = 95\%$), by choosing k such that

$$P \left[\sup_{s \in \partial\hat{\mathcal{A}}_c} |G(s)| \leq k \right] \geq 1 - \alpha, \quad (4.3)$$

Result 1 ensures with asymptotic probability of $1 - \alpha$ that $\hat{\mathcal{A}}_c^-$ contains the true \mathcal{A}_c , and $\hat{\mathcal{A}}_c^+$ is contained within \mathcal{A}_c . In practice, k is determined as the $(1 - \alpha)100$ percentile of the maximum distribution of the asymptotic absolute error process $|G(s)|$ over the true boundary set $\partial\mathcal{A}_c = \{s : w^T \beta(s) = c\}$. The upper CS taken away from the lower CS $(\hat{\mathcal{A}}_c^- \cap (\hat{\mathcal{A}}_c^+)^c)$ can be interpreted analogously to a standard confidence interval: with a confidence of $1 - \alpha$, we can assert the true boundary $\partial\mathcal{A}_c$ lies within this region. Here, we allude to the classical frequentist interpretation of confidence, where stated precisely, there is a probability of $1 - \alpha$ that the region $(\hat{\mathcal{A}}_c^- \cap (\hat{\mathcal{A}}_c^+)^c)$ computed from a future experiment fully encompasses the true set

boundary $\partial\mathcal{A}_c$.

Application of Result 1 presents us with two challenges: that the boundary set $\partial\mathcal{A}_c$ and the critical value k are both unknown. To solve the first problem, SSS propose using $\partial\hat{\mathcal{A}}_c$ as a plug-in estimate of $\partial\mathcal{A}_c$. There remain, however, technicalities as to how the boundary is determined in any non-abstract setting, and in particular in a 3D image. In Section 4.2.3 we propose our own novel method for boundary estimation. Before that, we address the second problem, finding the critical value k via a Wild Bootstrap resampling scheme.

4.2.2 The Wild Bootstrap Method for Computation of k

To apply Result 1, we require knowledge of the tail distribution of the limiting Gaussian field G along the boundary $\partial\mathcal{A}_c$. However, the distribution of this field is unknown, because it is dependent on the unknown spatial correlation of the errors ϵ_i . We can approximate the maximum distribution of G using the Gaussian Wild Bootstrap (Chernozhukov et al., 2013), also known as the Gaussian Multiplier Bootstrap, which multiplies residuals by random values to create surrogate instances of the random errors.

SSS construct G as follows: The standardized residuals,

$$\tilde{\epsilon}(s) = \frac{\mathbf{Y}(s) - \mathbf{X}\hat{\beta}(s)}{\sigma(s)}, \quad (4.4)$$

are multiplied by i.i.d. Gaussian random variables, r_1^*, \dots, r_N^* , summed and scaled,

$$G^*(s) = \frac{1}{\sqrt{N}} \sum_{i=1}^N r_i^* \tilde{\epsilon}_i(s), \quad (4.5)$$

producing a field G^* with approximately the same covariance as each error ϵ_i , where the superscript asterisk (*) indicates these are just one of many bootstrap realizations. With B bootstrap samples G^* , we choose k as the $(1 - \alpha)100$ percentile of the B suprema $\sup_{s \in \partial\hat{\mathcal{A}}_c} |G^*(s)|$ to approximate the LHS of (4.3) and apply Result 1 to obtain the CSs.

Up to this point, we have summarized the Gaussian Wild Bootstrap methodology as proposed in SSS. However, when applying this method to our own simulations, we consistently found that our coverage results fell below the nominal level. This was particularly severe for 3D simulations we conducted using a small sample size ($N = 60$), where our results in some cases suffered from under-coverage 40% or more below the nominal level (see **REFERENCE COMPARISON FIGURE**). Hence we made

two alterations: First, while SSS used Gaussian multipliers, we found improved performance using Rademacher variables, where each r_i takes on 1 or -1 with probability 1/2; others have also reported improved performance with Rademacher variables as well (Davidson and Flachaire, 2008). Second, we implemented a Wild t -Bootstrap (Telschow and Schwartzman, 2019) method, normalizing the bootstrapped residuals $\tilde{\epsilon}_i(\mathbf{s})$ by their standard deviation $\hat{\sigma}^*$. This detail was omitted in the proof of Result 1 provided in SSS, where the true standard deviation was assumed to be known. By taking into account the estimation of the standard deviation via the Wild t -Bootstrap, we found improved performance for moderate sample sizes. The Wild t -Bootstrap version of G is

$$\tilde{G}^*(\mathbf{s}) = \frac{1}{\sqrt{N}} \sum_{i=1}^N r_i^* \frac{\tilde{\epsilon}_i(\mathbf{s})}{\hat{\sigma}^*(\mathbf{s})}, \quad (4.6)$$

where $\hat{\sigma}^*(\mathbf{s})$ is the standard deviation of the present realization of the bootstrapped residuals $r_i^* \tilde{\epsilon}_i(\mathbf{s})$. We then determine k as described above but using \tilde{G}^* instead of G^* . Going forward, we refer to this method as the “Wild t -Bootstrap”, to be contrasted with the original “Gaussian Wild Bootstrap” method proposed in SSS.

With these two alterations we found a dramatic increase in performance for small sample sizes in 3D simulations. Notably, in contrast to the Gaussian Wild Bootstrap, our simulation results presented in Section 4.4 suggest that empirical coverage rates for this modified procedure remain valid, i.e. stay *above* the nominal level.

4.2.3 Approximating the Boundary on a Discrete Lattice

In the previous section, we described the ideal bootstrap procedure used to obtain the maximum distribution of G along the boundary $\partial\mathcal{A}_c$ in order to apply Result 1. However, in any practical application, data will be observed on a discrete grid of lattice points at a fixed resolution. Therefore, a key challenge is how to appropriately approximate the true continuous boundary $\partial\mathcal{A}_c$ from the lattice representation of the data.

In SSS, spline-interpolation was used to estimate a 1D boundary at a resolution greater than their 2D sampled field (SSS, Section 4.1). However, to apply the method to fMRI data we will work with 3D images, and estimating a 2D spline boundary for a 3D field is more involved, requiring careful tuning of the spline basis to accommodate the structure of the 3D signal. Instead, we choose to use a first-order weighted linear interpolation method to approximate the signal values at estimated locations along the true, continuous boundary $\partial\mathcal{A}_c$, providing a method of boundary estimation that is less computationally intensive than spline interpolation.

Consider two adjacent points on the lattice, s_O and s_I , such that s_O lies out-

side of \mathcal{A}_c , while s_I lies inside \mathcal{A}_c . By the definition of \mathcal{A}_c , $w^T \beta(s_O) < c$, and $w^T \beta(s_I) \geq c$. Under the assumption that the component of the signal between s_O and s_I increases linearly, we can find the location s^* between s_O and s_I such that $w^T \beta(s^*) = c$, our estimate of where the true continuous boundary $\partial\mathcal{A}_c$ crosses between s_O and s_I . We can then construct a linear interpolant for the location s^* , using weights

$$m_1 = \frac{w^T \beta(s_I) - c}{w^T \beta(s_I) - w^T \beta(s_O)}, \quad m_2 = \frac{c - w^T \beta(s_O)}{w^T \beta(s_I) - w^T \beta(s_O)}, \quad (4.7)$$

for locations s_O and s_I , respectively. By construction, applying m_1 and m_2 to the contrast image returns the threshold: $m_1 w^T \beta(s_O) + m_2 w^T \beta(s_I) = w^T \beta(s^*) = c$. Applied to standardized residuals $\tilde{\epsilon}(s_O)$ and $\tilde{\epsilon}(s_I)$, we can likewise obtain the residuals at the estimated continuous boundary point $\tilde{\epsilon}(s^*) = m_1 \tilde{\epsilon}(s_O) + m_2 \tilde{\epsilon}(s_I)$.

By repeating this procedure for all adjacent points s_O and s_I that lie on the lattice either side of $\partial\mathcal{A}_c$, we are able to estimate the standardized residual values at locations that should approximately sample the true continuous boundary $\partial\mathcal{A}_c$, and thus we can apply the ideal bootstrap procedure outlined in Section 4.2.2. Of course, in practice we apply this interpolation method on the observed, noisy data, using the plug-in estimated boundary $\partial\hat{\mathcal{A}}_c$.

In the simulation results in Section 4.4, we assess performance of the method when the bootstrap procedure is carried out over the true boundary $\partial\mathcal{A}_c$, and the plug-in estimated boundary $\partial\hat{\mathcal{A}}_c$ that must be used in practice.

4.2.4 Assessment of Continuous Coverage on a Discrete Lattice

In testing the finite-sample validity of our method through simulation, it is imperative that we are able to accurately measure when violations of the subset condition $\hat{\mathcal{A}}_c^+ \subset \mathcal{A}_c \subset \hat{\mathcal{A}}_c^-$ occur. While this may seem a trivial task, as touched on in the previous section, the boundaries of each of these three sets can become ambiguous when data are collected on a discrete lattice.

To illustrate this point, consider the configuration of sets displayed in Fig. 4.2(a). In this instance, suppose the right half of the image corresponds to \mathcal{A}_c (green pixels overlapped by yellow), and yellow pixels belong to $\hat{\mathcal{A}}_c^+$. We wish to determine whether the condition $\hat{\mathcal{A}}_c^+ \subset \mathcal{A}_c$ has been violated or not. One may argue that at the resolution for which the data have been acquired, all pixels that belong to $\hat{\mathcal{A}}_c^+$ also belong to \mathcal{A}_c , and therefore no violation has occurred. However, the example presented in Fig. 4.2(a) has in fact been derived from a 2D simulation conducted at a higher resolution: this 50×50 simulation was obtained by down-sampling a 100×100 grid by dropping every other pixel. Fig. 4.2(a) displays the sets \mathcal{A}_c and $\hat{\mathcal{A}}_c^+$ from the down-

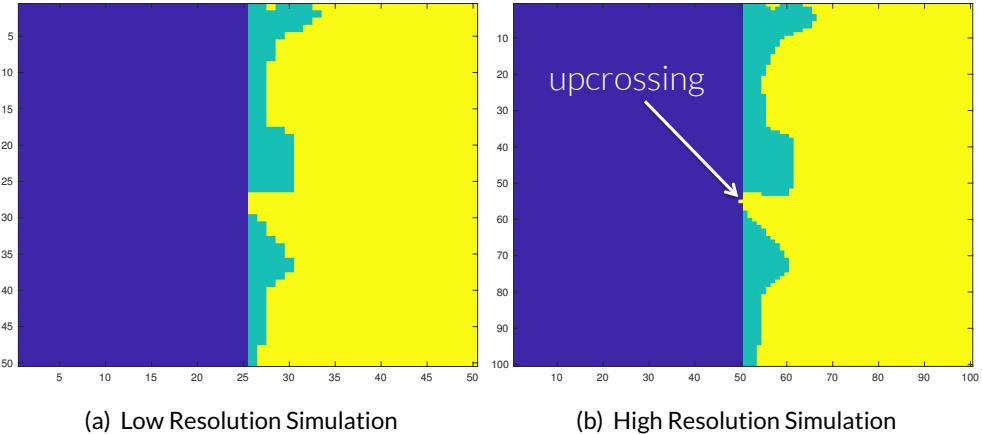


Figure 4.2: Demonstrating the resolution issue for testing the subset condition $\hat{\mathcal{A}}_c^+ \subset \mathcal{A}_c \subset \hat{\mathcal{A}}_c^-$.

Figure 4.2(a): Here \mathcal{A}_c is comprised of the right half of the image (all green and yellow pixels), and $\hat{\mathcal{A}}_c^+$ is shown as yellow pixels. It appears that $\hat{\mathcal{A}}_c^+ \subset \mathcal{A}_c$.

Figure 4.2(b): The same configuration as Fig. 4.2(a) at double the resolution. Here, we have enough detail to see that $\hat{\mathcal{A}}_c^+$ has crossed the boundary $\partial\mathcal{A}_c$ (yellow seeping into blue), and the subset condition $\hat{\mathcal{A}}_c^+ \subset \mathcal{A}_c$ has been violated.

sampled, low resolution simulation, while Fig. 4.2(b) shows the same set of results at the original resolution. In Fig. 4.2(b) we see that there *has* been an upcrossing of the yellow pixels belonging to $\hat{\mathcal{A}}_c^+$ over the boundary of the green, and therefore the subset condition $\hat{\mathcal{A}}_c^+ \subset \mathcal{A}_c$ *has* been violated. From this simulation, it is clear that when we conclude that no violation has occurred in situations like Fig. 4.2(a), our empirical coverage will miss violations and be positively biased. By an analogous argument the same issue occurs when testing violations of $\mathcal{A}_c \subset \hat{\mathcal{A}}_c^-$.

In SSS this direct comparison of the lattice representation of the three sets was used to assess coverage in the simulations. While they observed this phenomenon of missed violations leading to over-coverage, the proposed solution was to sequentially increase the resolution of the data. We instead again make use of interpolation.

Since, in simulation, we know the true continuous mean image and \mathcal{A}_c , following the method described in Section 4.2.3 we can obtain weights m_1 and m_2 to interpolate between points s_O and s_I either side of the true, continuous boundary $\partial\mathcal{A}_c$, in order to find a location s^* that approximately lies on the boundary (if the true mean is linear, it would be exactly on the boundary). To determine if $s^* \in \hat{\mathcal{A}}_c^+$, we

then re-apply the weights m_1 and m_2 and assess whether

$$\mathbf{w}^T \hat{\beta}(s^*) - k \hat{\sigma}(s^*) v_w = m_1 \left(\mathbf{w}^T \hat{\beta}(s_O) - k \hat{\sigma}(s_O) v_w \right) + m_2 \left(\mathbf{w}^T \hat{\beta}(s_I) - k \hat{\sigma}(s_I) v_w \right) \geq c. \quad (4.8)$$

If the inequality holds, then by definition $s^* \in \hat{\mathcal{A}}_c^+$. Otherwise, $s^* \notin \hat{\mathcal{A}}_c^+$, and therefore we can conclude that the subset condition $\hat{\mathcal{A}}_c^+ \subset \mathcal{A}_c$ has been violated. By checking whether $\mathbf{w}^T \hat{\beta}(s^*) + k \hat{\sigma}(s^*) v_w \geq c$, we can similarly test for a violation of $\mathcal{A}_c \subset \hat{\mathcal{A}}_c^-$.

By applying this interpolation scheme to all pairs of lattice points with one point inside, one outside, the lattice representation of the boundary, we have devised a method to more accurately assess violations of the subset condition $\hat{\mathcal{A}}_c^+ \subset \mathcal{A}_c \subset \hat{\mathcal{A}}_c^-$ for configurations similar to 4.2(a). We applied this method for testing the subset condition in our simulations alongside a direct comparison of the lattice representations of the three sets of interest as was done in SSS. The addition of the weighted interpolation method caused a considerable decrease in the empirical coverage results towards the nominal level in all of our 3D simulations. Using the direct comparison of the three sets on its own here essentially determined total empirical coverage ($\hat{\mathcal{A}}_c^+ \subset \mathcal{A}_c \subset \hat{\mathcal{A}}_c^-$ for all simulation runs), even when using small sample sizes and a low nominal coverage level. This is likely to be because the discrete lattice of observed data points is relatively less dense inside the true continuous process for larger, 3D settings, and therefore more violations of the subset condition are missed if only a direct comparison of the lattice representation of the CSs is carried out.

4.3 Method

4.3.1 Simulations

4.3.2 Implementation of Contour Inference

4.3.3 2D Simulations

4.3.4 3D Simulations

4.3.5 Application to Human Connectome Project Data

4.4 Results

4.4.1 2D Simulations

4.4.2 3D Simulations

4.4.3 Human Connectome Project

4.5 Discussion

4.5.1 Limitations

4.6 Conclusion

4.7 Toolbox

CHAPTER 5

Contour Inference for Cohen's d

5.1 Theory

5.1.1 Transforming the Residual Field

5.2 Method

5.2.1 2D Simulations

5.2.2 3D Simulations

5.2.3 Application to UK Biobank Data

5.3 Results

5.3.1 2D Simulations

5.3.2 3D Simulations

5.3.3 UK Biobank Data

5.3.4 Comparison to Traditional Inference Procedures

5.4 Discussion

5.4.1 Limitations

5.5 Conclusion

CHAPTER 6

Conclusion and Future Work

Bibliography

Alexandre Abraham, Fabian Pedregosa, Michael Eickenberg, Philippe Gervais, Andreas Mueller, Jean Kossaifi, Alexandre Gramfort, Bertrand Thirion, and Gaël Varoquaux. Machine learning for neuroimaging with scikit-learn. *Front. Neuroinform.*, 8:14, February 2014.

George Adelman and Others. *Encyclopedia of neuroscience*. Birkhäuser, 1987.

Andrew L Alexander, Jee Eun Lee, Mariana Lazar, and Aaron S Field. Diffusion tensor imaging of the brain. *Neurotherapeutics*, 4(3):316–329, July 2007.

Fidel Alfaro-Almagro, Mark Jenkinson, Neal K Bangerter, Jesper L R Andersson, Ludovica Griffanti, Gwenaëlle Douaud, Stamatiros N Sotiroopoulos, Saad Jbabdi, Moises Hernandez-Fernandez, Emmanuel Vallee, Diego Vidaurre, Matthew Webster, Paul McCarthy, Christopher Rorden, Alessandro Daducci, Daniel C Alexander, Hui Zhang, Iulius Dragonu, Paul M Matthews, Karla L Miller, and Stephen M Smith. Image processing and quality control for the first 10,000 brain imaging datasets from UK biobank. *Neuroimage*, 166:400–424, February 2018.

Grays Anatomy. Gray H. *Barnes & Noble*, 1918.

Jesper L R Andersson, Mark Jenkinson, Stephen Smith, and Others. Non-linear registration, aka spatial normalisation FMRIB technical report TR07JA2. *FMRIB Analysis Group of the University of Oxford*, 2:1–21, 2007.

Frederico A C Azevedo, Ludmila R B Carvalho, Lea T Grinberg, José Marcelo Farfel, Renata E L Ferretti, Renata E P Leite, Wilson Jacob Filho, Roberto Lent, and Suzana Herculano-Houzel. Equal numbers of neuronal and nonneuronal cells make the human brain an isometrically scaled-up primate brain. *J. Comp. Neurol.*, 513(5):532–541, 2009.

P A Bandettini, E C Wong, R S Hinks, R S Tikofsky, and J S Hyde. Time course EPI of human brain function during task activation. *Magn. Reson. Med.*, 25(2):390–397, June 1992.

- Y Benjamini and Y Hochberg. Controlling the false discovery rate: a practical and powerful approach to multiple testing. *J. R. Stat. Soc.*, 1995.
- Craig M Bennett, Michael B Miller, and George L Wolford. Neural correlates of inter-species perspective taking in the post-mortem atlantic salmon: an argument for multiple comparisons correction. *Neuroimage*, 47(Suppl 1):S125, 2009.
- E L Bennett, M C Diamond, D Krech, and M R Rosenzweig. CHEMICAL AND ANATOMICAL PLASTICITY BRAIN. *Science*, 146(3644):610–619, October 1964.
- Alex Bowring, Camille Maumet, and Thomas Nichols. Exploring the impact of analysis software on task fMRI results, 2018a.
- Alexander Bowring, Camille Maumet, and Thomas Nichols. NISoX-BDI/Software_Comparison. Zenodo, March 2018b.
- Matthew Brett, Michael Hanke, Marc-Alexandre Côté, Chris Markiewicz, Satrajit Ghosh, Demian Wassermann, Stephan Gerhard, Eric Larson, Gregory R Lee, Yaroslav Halchenko, Erik Kastman, Cindee M, Félix C Morency, moloney, Ariel Rokem, Michiel Cottaar, Jarrod Millman, jaeilepp, Alexandre Gramfort, Robert D Vincent, Paul McCarthy, Jasper J F van den Bosch, Krish Subramaniam, Nolan Nichols, embaker, markhymers, chaselgrove, Basile, Nikolaas N Oosterhof, and Ian Nimmo-Smith. nipy/nibabel: 2.2.0, 2017.
- Matthew J Brookes, Mark Woolrich, Henry Luckhoo, Darren Price, Joanne R Hale, Mary C Stephenson, Gareth R Barnes, Stephen M Smith, and Peter G Morris. Investigating the electrophysiological basis of resting state networks using magnetoencephalography. *Proc. Natl. Acad. Sci. U. S. A.*, 108(40):16783–16788, October 2011.
- Richard B Buxton. Dynamic models of BOLD contrast. *Neuroimage*, 62(2):953–961, August 2012.
- Joshua Carp. On the plurality of (methodological) worlds: estimating the analytic flexibility of fMRI experiments. *Front. Neurosci.*, 6:149, October 2012.
- Joshua Carp. Optimizing the order of operations for movement scrubbing: Comment on power et al. *Neuroimage*, 76:436–438, August 2013.
- Gang Chen, Robert W Cox, Daniel R Glen, Justin K Rajendra, Richard C Reynolds, and Paul A Taylor. A tail of two sides: Artificially doubled false positive rates in neuroimaging due to the sidedness choice with t-tests. *Hum. Brain Mapp.*, September 2018.

- Victor Chernozhukov, Denis Chetverikov, and Kengo Kato. Gaussian approximations and multiplier bootstrap for maxima of sums of high-dimensional random vectors, 2013.
- Justin R Chumbley and Karl J Friston. False discovery rate revisited: FDR and topological inference using gaussian random fields. *Neuroimage*, 44(1):62–70, January 2009.
- R W Cox. AFNI: software for analysis and visualization of functional magnetic resonance neuroimages. *Comput. Biomed. Res.*, 29(3):162–173, June 1996.
- Sean P David, Jennifer J Ware, Isabella M Chu, Pooja D Loftus, Paolo Fusar-Poli, Joaquim Radua, Marcus R Munafò, and John P A Ioannidis. Potential reporting bias in fMRI studies of the brain. *PLoS One*, 8(7):e70104, July 2013.
- Russell Davidson and Emmanuel Flachaire. The wild bootstrap, tamed at last. *J. Econom.*, 146(1):162–169, September 2008.
- M C Diamond, D Krech, and M R Rosenzweig. THE EFFECTS OF AN ENRICHED ENVIRONMENT ON THE HISTOLOGY OF THE RAT CEREBRAL CORTEX. *J. Comp. Neurol.*, 123:111–120, August 1964.
- Anders Eklund, Thomas E Nichols, and Hans Knutsson. Cluster failure: Why fMRI inferences for spatial extent have inflated false-positive rates. *Proc. Natl. Acad. Sci. U. S. A.*, 113(28):7900–7905, July 2016.
- Cameron Ellis, Christopher Baldassano, Anna C Schapiro, Ming Bo Cai, and Jonathan D Cohen. Facilitating open-science with realistic fMRI simulation: validation and application. January 2019.
- Ariel Deardorff Erin D. Foster. Open science framework (OSF). *J. Med. Libr. Assoc.*, 105(2):203, April 2017.
- Tatiana Fomina, Matthias Hohmann, Bernhard Scholkopf, and Moritz Grosse-Wentrup. Identification of the default mode network with electroencephalography. *Conf. Proc. IEEE Eng. Med. Biol. Soc.*, 2015:7566–7569, 2015.
- Michael D Fox and Ron L Alterman. Brain stimulation for torsion dystonia. *JAMA Neurol.*, 72(6):713–719, June 2015.
- K J Friston, P Fletcher, O Josephs, A Holmes, M D Rugg, and R Turner. Event-related fMRI: characterizing differential responses. *Neuroimage*, 7(1):30–40, January 1998.

- Christopher R Genovese, Nicole A Lazar, and Thomas Nichols. Thresholding of statistical maps in functional neuroimaging using the false discovery rate. *Neuroimage*, 15(4):870–878, April 2002.
- Gary H Glover. Overview of functional magnetic resonance imaging. *Neurosurg. Clin. N. Am.*, 22(2):133–9, vii, April 2011.
- Javier Gonzalez-Castillo, Ziad S Saad, Daniel A Handwerker, Souheil J Inati, Noah Brenowitz, and Peter A Bandettini. Whole-brain, time-locked activation with simple tasks revealed using massive averaging and model-free analysis. *Proc. Natl. Acad. Sci. U. S. A.*, 109(14):5487–5492, April 2012.
- Krzysztof J Gorgolewski and Russell A Poldrack. A practical guide for improving transparency and reproducibility in neuroimaging research. *PLoS Biol.*, 14(7): e1002506, July 2016.
- Krzysztof J Gorgolewski, Gael Varoquaux, Gabriel Rivera, Yannick Schwarz, Satrajit S Ghosh, Camille Maumet, Vanessa V Sochat, Thomas E Nichols, Russell A Poldrack, Jean-Baptiste Poline, Tal Yarkoni, and Daniel S Margulies. NeuroVault.org: a web-based repository for collecting and sharing unthresholded statistical maps of the human brain. *Front. Neuroinform.*, 9:8, April 2015.
- Krzysztof J Gorgolewski, Tibor Auer, Vince D Calhoun, R Cameron Craddock, Samir Das, Eugene P Duff, Guillaume Flandin, Satrajit S Ghosh, Tristan Glatard, Yaroslav O Halchenko, Daniel A Handwerker, Michael Hanke, David Keator, Xiangrui Li, Zachary Michael, Camille Maumet, B Nolan Nichols, Thomas E Nichols, John Pellman, Jean-Baptiste Poline, Ariel Rokem, Gunnar Schaefer, Vanessa Sochat, William Triplett, Jessica A Turner, Gaël Varoquaux, and Russell A Poldrack. The brain imaging data structure, a format for organizing and describing outputs of neuroimaging experiments. *Sci Data*, 3:160044, June 2016.
- C Goutte, F A Nielsen, and K H Hansen. Modeling the hemodynamic response in fMRI using smooth FIR filters. *IEEE Trans. Med. Imaging*, 19(12):1188–1201, December 2000.
- Richard J Hargreaves and Michael Klimas. Imaging in drug development. In *Principles of Clinical Pharmacology*, pages 327–341. Elsevier, 2012.
- John D Hunter. Matplotlib: A 2D graphics environment. *Comput. Sci. Eng.*, 9(3):90–95, May 2007.

- John P A Ioannidis. Why most published research findings are false. *PLoS Med.*, 2(8): e124, August 2005.
- John P A Ioannidis, Marcus R Munafò, Paolo Fusar-Poli, Brian A Nosek, and Sean P David. Publication and other reporting biases in cognitive sciences: detection, prevalence, and prevention. *Trends Cogn. Sci.*, 18(5):235–241, May 2014.
- Mark Jenkinson, Peter Bannister, Michael Brady, and Stephen Smith. Improved optimization for the robust and accurate linear registration and motion correction of brain images. *Neuroimage*, 17(2):825–841, October 2002.
- Mark Jenkinson, Christian F Beckmann, Timothy E J Behrens, Mark W Woolrich, and Stephen M Smith. FSL. *Neuroimage*, 62(2):782–790, August 2012.
- Suneil K Kalia, Tejas Sankar, and Andres M Lozano. Deep brain stimulation for parkinson's disease and other movement disorders. *Curr. Opin. Neurol.*, 26(4):374–380, August 2013.
- Thomas Kluyver, Benjamin Ragan-Kelley, Fernando Pérez, Brian E Granger, Matthias Bussonnier, Jonathan Frederic, Kyle Kelley, Jessica B Hamrick, Jason Grout, Sylvain Corlay, and Others. Jupyter notebooks-a publishing format for reproducible computational workflows. In *ELPUB*, pages 87–90, 2016.
- K K Kwong, J W Belliveau, D A Chesler, I E Goldberg, R M Weisskoff, B P Poncelet, D N Kennedy, B E Hoppel, M S Cohen, and R Turner. Dynamic magnetic resonance imaging of human brain activity during primary sensory stimulation. *Proc. Natl. Acad. Sci. U. S. A.*, 89(12):5675–5679, June 1992.
- M H Lee, C D Smyser, and J S Shimony. Resting-state fMRI: a review of methods and clinical applications. *AJNR Am. J. Neuroradiol.*, 34(10):1866–1872, October 2013.
- Megan H Lee, Carl D Hacker, Abraham Z Snyder, Maurizio Corbetta, Dongyang Zhang, Eric C Leuthardt, and Joshua S Shimony. Clustering of resting state networks. *PLoS One*, 7(7):e40370, July 2012.
- Martin A Lindquist, Ji Meng Loh, Lauren Y Atlas, and Tor D Wager. Modeling the hemodynamic response function in fMRI: efficiency, bias and mis-modeling. *Neuroimage*, 45(1 Suppl):S187–98, March 2009.
- Francisco López-Muñoz, Jesús Boya, and Cecilio Alamo. Neuron theory, the cornerstone of neuroscience, on the centenary of the nobel prize award to santiago ramón y cajal. *Brain Res. Bull.*, 70(4-6):391–405, October 2006.

- Torben E Lund, Minna D Nørgaard, Egill Rostrup, James B Rowe, and Olaf B Paulson. Motion or activity: their role in intra- and inter-subject variation in fMRI. *Neuroimage*, 26(3):960–964, July 2005.
- Paul M Matthews, Garry D Honey, and Edward T Bullmore. Neuroimaging: Applications of fMRI in translational medicine and clinical practice. *Nat. Rev. Neurosci.*, 7(9):732, 2006.
- Camille Maumet, Tibor Auer, Alexander Bowring, Gang Chen, Samir Das, Guillaume Flandin, Satrajit Ghosh, Tristan Glatard, Krzysztof J Gorgolewski, Karl G Helmer, Mark Jenkinson, David B Keator, B Nolan Nichols, Jean-Baptiste Poline, Richard Reynolds, Vanessa Sochat, Jessica Turner, and Thomas E Nichols. Sharing brain mapping statistical results with the neuroimaging data model. *Sci Data*, 3:160102, December 2016.
- Linda K McEvoy, Christine Fennema-Notestine, J Cooper Roddey, Donald J Hagler, Dominic Holland, David S Karow, Christopher J Pung, James B Brewer, and Anders M Dale. Alzheimer disease: Quantitative structural neuroimaging for detection and prediction of clinical and structural changes in mild cognitive impairment, 2009.
- Wes McKinney and Others. Data structures for statistical computing in python. In *Proceedings of the 9th Python in Science Conference*, volume 445, pages 51–56, 2010.
- Andrea Mechelli, Cathy J Price, Karl J Friston, and John Ashburner. Voxel-Based morphometry of the human brain: Methods and applications. *Curr. Med. Imaging Rev.*, 1(2):105–113, 2005.
- Paul E Meehl. Theory-Testing in psychology and physics: A methodological paradox. *Philos. Sci.*, 34(2):103–115, June 1967.
- W Mohamed. The edwin smith surgical papyrus: Neuroscience in ancient egypt. *IBRO History of Neuroscience*, 2014.
- Joseph M Moran, Eshin Jolly, and Jason P Mitchell. Social-cognitive deficits in normal aging. *J. Neurosci.*, 32(16):5553–5561, April 2012.
- Malaak N Moussa, Matthew R Steen, Paul J Laurienti, and Satoru Hayasaka. Consistency of network modules in resting-state FMRI connectome data. *PLoS One*, 7(8):e44428, August 2012.

- Karsten Mueller, Jörn Lepsien, Harald E Möller, and Gabriele Lohmann. Commentary: Cluster failure: Why fMRI inferences for spatial extent have inflated false-positive rates. *Front. Hum. Neurosci.*, 11:345, June 2017.
- Thomas E Nichols and Andrew P Holmes. Nonparametric permutation tests for functional neuroimaging: a primer with examples. *Hum. Brain Mapp.*, 15(1):1–25, January 2002.
- Lars Holm Nielsen and Tim Smith. Zenodo overview. Zenodo, 2014.
- S Ogawa, T M Lee, A R Kay, and D W Tank. Brain magnetic resonance imaging with contrast dependent on blood oxygenation. *Proc. Natl. Acad. Sci. U. S. A.*, 87(24):9868–9872, December 1990.
- S Ogawa, D W Tank, R Menon, J M Ellermann, S G Kim, H Merkle, and K Ugurbil. Intrinsic signal changes accompanying sensory stimulation: functional brain mapping with magnetic resonance imaging. *Proc. Natl. Acad. Sci. U. S. A.*, 89(13):5951–5955, July 1992.
- Wiktor Olszowy, John Aston, Catarina Rua, and Guy B Williams. Accurate autocorrelation modeling substantially improves fMRI reliability, 2019.
- Open Science Collaboration. Estimating the reproducibility of psychological science. *Science*, 349(6251):aac4716, August 2015.
- Aarthi Padmanabhan, Charles F Geier, Sarah J Ordaz, Theresa Teslovich, and Beatriz Luna. Developmental changes in brain function underlying the influence of reward processing on inhibitory control. *Dev. Cogn. Neurosci.*, 1(4):517–529, October 2011.
- O Parker Jones, N L Voets, J E Adcock, R Stacey, and S Jbabdi. Resting connectivity predicts task activation in pre-surgical populations. *NeuroImage: Clinical*, 13:378–385, January 2017.
- William D Penny, Karl J Friston, John T Ashburner, Stefan J Kiebel, and Thomas E Nichols. *Statistical Parametric Mapping: The Analysis of Functional Brain Images*. Elsevier, April 2011.
- Russell A Poldrack, Jeanette A Mumford, and Thomas E Nichols. *Handbook of Functional MRI Data Analysis*. Cambridge University Press, August 2011.
- Russell A Poldrack, Chris I Baker, Joke Durnez, Krzysztof J Gorgolewski, Paul M Matthews, Marcus R Munafò, Thomas E Nichols, Jean-Baptiste Poline, Edward

- Vul, and Tal Yarkoni. Scanning the horizon: towards transparent and reproducible neuroimaging research. *Nat. Rev. Neurosci.*, 18(2):115–126, February 2017.
- William W Rozeboom. The fallacy of the null-hypothesis significance test. *Psychol. Bull.*, 57(5):416–428, 1960.
- Tom Schonberg, Craig R Fox, Jeanette A Mumford, Eliza Congdon, Christopher Trepel, and Russell A Poldrack. Decreasing ventromedial prefrontal cortex activity during sequential risk-taking: an fMRI investigation of the balloon analog risk task. *Front. Neurosci.*, 6:80, June 2012.
- Shayle R Searle, George Casella, and Charles E McCulloch. *Variance Components*. John Wiley & Sons, September 2009.
- P Skudlarski, R T Constable, and J C Gore. ROC analysis of statistical methods used in functional MRI: individual subjects. *Neuroimage*, 9(3):311–329, March 1999.
- Stephen M Smith. Fast robust automated brain extraction. *Hum. Brain Mapp.*, 17(3):143–155, November 2002.
- Stephen M Smith, Peter T Fox, Karla L Miller, David C Glahn, P Mickle Fox, Clare E Mackay, Nicola Filippini, Kate E Watkins, Roberto Toro, Angela R Laird, and Christian F Beckmann. Correspondence of the brain’s functional architecture during activation and rest. *Proc. Natl. Acad. Sci. U. S. A.*, 106(31):13040–13045, August 2009.
- José M Soares, Paulo Marques, Victor Alves, and Nuno Sousa. A hitchhiker’s guide to diffusion tensor imaging. *Front. Neurosci.*, 7:31, March 2013.
- Max Sommerfeld, Stephan Sain, and Armin Schwartzman. Confidence regions for spatial excursion sets from repeated random field observations, with an application to climate. *J. Am. Stat. Assoc.*, 113(523):1327–1340, July 2018.
- Reisa A Sperling, Dorene M Rentz, Keith A Johnson, Jason Karlawish, Michael Donohue, David P Salmon, and Paul Aisen. The A4 study: stopping AD before symptoms begin? *Sci. Transl. Med.*, 6(228):228fs13, March 2014.
- William C Stacey and Brian Litt. Technology insight: neuroengineering and epilepsy—designing devices for seizure control. *Nat. Clin. Pract. Neurol.*, 4(4):190–201, April 2008.
- Stephen C Strother, Jon Anderson, Lars Kai Hansen, Ulrik Kjems, Rafal Kustra, John Sidtis, Sally Frutiger, Suraj Muley, Stephen LaConte, and David Rottenberg. The

quantitative evaluation of functional neuroimaging experiments: the NPAIRS data analysis framework. *Neuroimage*, 15(4):747–771, April 2002.

I Tavor, O Parker Jones, R B Mars, S M Smith, T E Behrens, and S Jbabdi. Task-free MRI predicts individual differences in brain activity during task performance. *Science*, 352(6282):216–220, April 2016.

Fabian J E Telschow and Armin Schwartzman. Simultaneous confidence bands for functional data using the gaussian kinematic formula. January 2019.

Stéfan van der Walt, S Chris Colbert, and Gaël Varoquaux. The NumPy array: A structure for efficient numerical computation. *Comput. Sci. Eng.*, 13(2):22–30, March 2011.

Anderson M Winkler, Gerard R Ridgway, Gwenaëlle Douaud, Thomas E Nichols, and Stephen M Smith. Faster permutation inference in brain imaging. *Neuroimage*, 141: 502–516, November 2016.

Choong-Wan Woo, Anjali Krishnan, and Tor D Wager. Cluster-extent based thresholding in fMRI analyses: pitfalls and recommendations. *Neuroimage*, 91:412–419, May 2014.

M W Woolrich, B D Ripley, M Brady, and S M Smith. Temporal autocorrelation in univariate linear modeling of FMRI data. *Neuroimage*, 14(6):1370–1386, December 2001.

Mark W Woolrich, Timothy E J Behrens, Christian F Beckmann, Mark Jenkinson, and Stephen M Smith. Multilevel linear modelling for FMRI group analysis using bayesian inference. *Neuroimage*, 21(4):1732–1747, April 2004.

K J Worsley, C Liao, M Grabove, V Petre, B Ha, and A C Evans. A general statistical analysis for fMRI data, 2000.

Andy W K Yeung. An updated survey on statistical thresholding and sample size of fMRI studies. *Front. Hum. Neurosci.*, 12:16, January 2018.