Operations with large numbers

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Introduction

Large numbers are numbers that are significantly larger than those ordinarily used in everyday life, for instance in simple counting or in monetary transactions. The term typically refers to large positive integers, or more generally, large positive real numbers, but it may also be used in other contexts.

Very large numbers often occur in fields such as mathematics, cosmology, cryptography, and statistical mechanics. Sometimes people refer to numbers as being "astronomically large". However, it is easy to mathematically define numbers that are much larger even than those used in astronomy.

Problem statement Advanced assignments

Assignment number 5:

A library for operations with large numbers. The library should provide at least addition, subtraction, multiplication, division and taking the square root.

One Centillion

The largest -illion with a name that is officially considered part of the English language

Pseudocode

$Addition\ function$

```
void adunare_numere_mari (numar_mare numar1, numar_mare numar2, numar_mare suma)
            if \ lungime\_numar1 > lungime\_numar2
                         lungime_mare <- lungime_numar1</pre>
                         lungime_mica <- lungime_numar2
                         numar2[i] \leftarrow 0
            _{
m else}
                         if \ lungime\_numar1 < lungime\_numar2
                                      lungime_mare <- lungime_numar2
lungime_mica <- lungime_numar1
                                       for i <- lungime_mica + 1 to lungime_mare do</pre>
                                                   numar1\left[ \ i \ \right] \ <\!\!- \ 0
                         else
                                      lungime\_mare <- \ lungime\_numar1
                                      lungime_mica <- lungime_numar2</pre>
            suma[0] <- lungime_mare
            \begin{array}{c} \textbf{if} \hspace{0.1cm} (\hspace{0.1cm} \texttt{transport} \hspace{0.1cm} != \hspace{0.1cm} 0\hspace{0.1cm}) \\ \hspace{0.1cm} suma\hspace{0.1cm} [\hspace{0.1cm} \texttt{i}\hspace{0.1cm}] \hspace{0.1cm} <- \hspace{0.1cm} \texttt{transport} \\ \hspace{0.1cm} suma\hspace{0.1cm} [\hspace{0.1cm} 0\hspace{0.1cm}] \hspace{0.1cm} +\!\!\!+ \end{array}
```

$Substraction\ function$

```
void scadere_numere_mari (numar_mare numar1, numar_mare numar2, numar_mare diferenta)
             diferenta [0] <- -1
             \begin{array}{c} \text{if numar1} < \text{numar2} \\ \text{print ERROR} \\ \text{return} \end{array}
             if numar1 = numar2
                           print 0
                           return
             if numar1 > numar2
                          lungime_mare <- lungime_numar1
lungime_mica <- lungime_numar2
                           for i <- lungime_mica + 1 to lungime_mare + 1 do numar2[i] <- 0
                           for i <- 1 to lungime_mare do
                                         i\,f\ numar1\,[\,\,i\,\,]\ <\ numar2\,[\,\,i\,\,]
                                                      if index_scadere = 0
    diferenta[i] <- (numar1[i] + 10) - numar2[i]
    index_scadere <- 1</pre>
                                                      if numar1[i] = numar2[i]
                                                      if index_scadere = 1
diferenta[i] <- 9
index_scadere <- 1
                                                      \begin{array}{ll} \mbox{if index\_scadere} \, = \, 0 \\ \mbox{diferenta} \left[ \, \mbox{i} \, \right] \, < - \, \, 0 \\ \mbox{index\_scadere} \, < - \, \, 0 \end{array}
                                         if numar1[i] > numar2[i]
                                                      if index_scadere = 1
    diferenta[i] <- (numar1[i] - 1) - numar2[i]
    index_scadere <- 0</pre>
                                                       \begin{array}{lll} if & index\_scadere = 0 \\ & diferenta [\,i\,] <- \,\, numarl [\,i\,] \,\, - \,\, numar2 [\,i\,] \\ & index\_scadere <- \,\, 0 \end{array} 
                           for i <- lungime_mare to 1 do
                                         if diferenta[i] = 0
                                                     numar_cifre ++
                                         else
                                                 numar_cifre <- lungime_mare - numar_cifre diferenta[0] <- numar_cifre
```

$Multiplication\ function$

Division function

Square root function

```
void\ radical\_numar\_mare\ (numar\_mare\ valoare\ ,\ numar\_mare\ radical\ )
            for i <- 0 to lungime_numar do
                        inceput[i] <- 0
sfarsit[i] <- 0
                        mijloc[i] <- 0
                        patrat[i] <- 0
                        suma[i] <- 0
auxiliar[i] <- 0
           \begin{array}{ll} \mbox{if valoare} \left[ 0 \right] \; = \; 1 \; \mbox{ and valoare} \left[ 1 \right] \; = \; 0 \\ \mbox{ radical } < \!\! - \; 0 \end{array}
                        return
            e\,l\,s\,e
                        if valoare [0] = 1 and valoare [1] = 1
                                    radical <- 1
                                    return
                        e\,l\,s\,e
                                    \mathtt{inceput} \ <\!\!- \ 1
                                    sfarsit <- valoare
                                    while inceput <= sfarsit
                                                mijloc = (inceput + sfarsit) / 2
                                                patrat = mijloc * mijloc
                                                if \ patrat = valoare \\
                                                            radical = mijloc
                                                            return;
                                                e\,l\,s\,e
                                                             if \ patrat < valoare \\
                                                                         inceput <- mijloc + 1
radical <- mijloc
                                                             else
                                                                         if patrat > valoare
                                                                                     {\tt sfarsit} \ <\!\! - \ {\tt mijloc} \ - \ 1
```

Application design

In order to define and construct functions for the main operations that arise while handling large numbers, a new data type has been introduced: numar_mare

In fact, I used an array with a finite length (1000 memory locations) to store these numbers ----> typedef int numar_mare[1000]

The header "functions.h" contains all the function prototypes:

- void citire_numar_mare (char auxiliar[1000], numar_mare valoare)
- void afisare_numar_mare (numar_mare valoare)
- void initializare_cu_mic (numar_mare valoare_mare, int numar_mic)
- void initializare_cu_mare (numar_mare valoare_initiala, numar_mare valoare_noua)
- int comparare_numere_mari (numar_mare numar1, numar_mare numar2)
- void adunare_numere_mari (numar_mare numar1, numar_mare numar2, numar_mare suma)
- void scadere_numere_mari (numar_mare numar1, numar_mare numar2, numar_mare diferenta)
- void inmultire_scalar (numar_mare valoare, int scalar, numar_mare produs)
- void textttinmultire_numar_mare (numar_mare numar1, numar_mare numar2, numar_mare produs)
- int impartire_la_scalar (numar_mare cat, int scalar)
- void radical_numar_mare (numar_mare valoare, numar_mare radical)

The "functions.c" file will contain all the functions used in order to work with large numbers.

The way in which every function is written and should be analysed is very simple. There are just a few steps:

- 1. The large numbers are saved in an array with a finite dimension. In the first position, array[0], we will save the length of the number and in the positions 1, 2, 3... array[0] every digit of the number. The only thing to keep in mind is that the number will be saved in a reversed order because, in this way, a lot of functions will be easier to implement.
- 2. Every operation, excluding the square root, is implemented in a natural way. As an example, let's say you want to add two large numbers. My code will do that by simulating the exact thing that each one of us does. Putting them one under another and making the sum of their digits, one by one, from the end towards the most significant one. There is also a transport variable that carries a value equal to the last sum of two digits / 10 and adds it to the current sum. In the case of the square root, we use a binary search algorithm and replace the trivial operations with functions that do the same thing, but on large numbers.
- 3. We work with positive values so, for example, if we want to compute the difference of two numbers, we must consider the first number greater than or equal to the second (omitting this aspect will be signaled by an ERROR message).

We are talking about natural numbers that have from 1 to 999 digits (we can change their length by making the array that stands behind the data type greater, but I considered that this dimension was enough for my functions).

Here are all the functions used:

```
1. citire_numar_mare()
void citire_numar_mare(char auxiliar[1000], numar_mare valoare)
auxiliar \rightarrow The number represented as a string valoare \rightarrow The value of the number represented as a vector
This function will get a string and save it as a large number.
2. afisare_numar_mare() void afisare_numar_mare (numar_mare valoare)
valoare -> The value of the number that will be printed
This function will get a large number and print its value.
3. initializare_cu_mic ( ) void initializare_cu_mic (numar_mare valoare_mare, int numar_mic)
valoare_mare -> The large number that will be replaced
             -> The new integer value of the large number
numar_mic
This function will replace the value of the given large number with a scalar value.
Parameters
valoare_initiala ->
                         The large number that will be replaced The new value of the large number
valoare_noua
This function will replace the value of the given large number with the value of a
secondary large number.
```

```
5. comparare_numere_mari ( ) int comparare_numere_mari (numar_mare numar1, numar_mare numar2)
Parameters numar1 \rightarrow The first large number numar2 \rightarrow The second large number
This function will compare the two large numbers.
6. adunare_numere_mari ( )
void adunare_numere_mari (numar_mare numar1, numar_mare numar2, numar_mare suma)
Parameters
numar1 -> The first large number
numar2 -> The second large number
suma -> The resulting sum of the two large numbers
This function will calculate the sum of two large numbers.
7. scadere_numere_mari ( ) void scadere_numere_mari (numar_mare numar1, numar_mare numar2, numar_mare diferenta)
Parameters
numar1 -> The first large number
numar2 -> The second large number
diferenta -> The resulting difference of the two large numbers
This function will calculate the difference of two large numbers.
8. inmultire_scalar ( )
void inmultire_scalar (numar_mare valoare, int scalar, numar_mare produs)
Parameters
valoare -> The value of the large number scalar -> The value of the scalar produs -> The resulting product of the numbers
This function will calculate the product between a large number and a scalar value.
9. inmultire_numar_mare ( ) void inmultire_numar_mare (numar_mare numar1, numar_mare numar2, numar_mare produs)
Parameters \begin{array}{lll} numar1 \ -> \ The & first & large & number \\ numar2 \ -> \ The & second & large & number \\ produs \ -> \ The & resulting & product & of & the & two & large & numbers \\ \end{array}
This function will calculate the product of two large numbers.
10. impartire_la_scalar ( ) int impartire_la_scalar (numar_mare cat, int scalar)
Parameters cat \rightarrow The large dividend (we will also save the resulting quotient in it) scalar \rightarrow The scalar value which we will divide by (the divisor)
This function will divide a large number by a scalar value and return the remainder. The quotient will be saved in the original large number ("cat").
11. radical_numar_mare ( ) void radical_numar_mare (numar_mare valoare, numar_mare radical)
Parameters
radianevers valoare -> The large number value radical -> The floor of the square root of the given number
This function will calculate the floor of the square root of a large number.
```

The "main.c" file will use all of the above functions and incorporate them into a basic application that will provide information about large numbers and a list of possible commands like adding two numbers, extracting the square root, calculating a difference or a product etc.

So, by running the main program, the user will have access to an easy to use and friendly command panel and will be able to get the result of some basic operations that involve large numbers and their manipulation.

```
OPERATII CU NUMERE MARI

Selectati una din optiunile de mai jos tastand numarul acesteia in consola :

8. Ce sunt numerele mari?
1. Compararea a doua numere mari
2. Adunarea a doua numere mari
3. Scaderea a doua numere mari
4. Inmultirea unui numar mare cu un scalar
5. Inmultirea a doua numere mari
6. Impartirea unui numar mare la un scalar
7. Extragerea radicalului dintr-un numar mare

Inserati aici alegerea dumneavoastra : 7

Extragerea radicalului dintr-un numar mare

Inserati de la tastatura un numar mare

---> 998000

Numarul citit a fost salvat!

Partea intreaga a radicalului numarului introdus este:
---> 998

Press any key for exit
```

The command panel generated by the main function

Source code - functions.h

```
typedef int numar_mare[1000];
void citire_numar_mare (char auxiliar[1000], numar_mare valoare);
void afisare_numar_mare (numar_mare valoare);
void initializare_cu_mic (numar_mare valoare_mare, int numar_mare valoare_noua);
void initializare_cu_mare (numar_mare valoare_initiala, numar_mare valoare_noua);
int comparare_numere_mari (numar_mare numar1, numar_mare numar2);
void adunare_numere_mari (numar_mare numar1, numar_mare numar2, numar_mare suma);
void scadere_numere_mari (numar_mare numar1, numar_mare numar2, numar_mare diferenta);
void inmultire_scalar (numar_mare valoare, int scalar, numar_mare produs);
void inmultire_numar_mare (numar_mare numar1, numar_mare numar2, numar_mare produs);
int impartire_la_scalar (numar_mare cat, int scalar);
void radical_numar_mare (numar_mare valoare, numar_mare radical);
```

Source code - main.c

```
# include <stdio.h>
# include <stdlib.h>
# include <math.h>
# include <string.h>
# include "functions.h"
  typedef \ int \ numar\_mare [\,1\,0\,0\,0\,]\,;
  numar_mare X:
  numar_mare Y;
  numar_mare suma;
numar_mare diferenta;
  numar_mare produs;
  numar_mare cat;
numar_mare radical;
  char numar_citit [1000];
  int main ()
                                                int i;
                                              int scalar_dividere;
int numar_mic;
int scalar_produs;
int rest = 0;
                                               int alegere_consola;
int verificare = 0;
                                               char caracter;
                                             printf ("\n\n\n\n\n\n\n");
printf (""");
printf ("""");
printf (""");
printf (""");
printf (""");
                                                if (alegere\_consola == 0)
                                                                                          printf ("\n\n");
printf ("\n\n");
printf ("Numerele mari\n\n");
printf ("Numere intregi pozitive de");
printf ("Numere intregi pozitive de");
printf ("dimensiuni foarte mari.\n");
printf ("Lungimea lor va fi limitata la 999");
printf ("de cifre in accest algoritm.\n\n");
printf ("Observatie : Se va considera valid");
printf ("ca numar mare orice numar cu dimensiunea\n");
printf ("intre 1 si 999 de cifre.\n\n");
printf ("!ATENTIE!\nln cazul unor operatii
precum inmultirea, trebuie luata in considerare");
printf ("\ndimensiunea finala a rezultatului.\n");
printf ("Se recomanda introducerea unor numere de");
printf ("1-500 cifre pentru a fi evitate\n");
printf ("eventualele erori de calcul.\n");
printf ("Daca se doreste lucrul cu numere mai mari.");
printf ("acest lucru se poate face prin\n");
printf ("acest lucru se poate face prin\n");
printf ("marirea lungimii vectorului din spatele");
printf ("tipului de date numere_mari.\n\n\n\n\n");
                                               }
```

```
\begin{array}{ll} \text{if (alegere\_consola == 1)} \\ \{ \end{array}
              if (comparare_numere_mari(X, Y) == 0)
              {
                             printf ("Cele doua numere sunt egale!\n\n");
              }
              else
{
                             if \ (comparare\_numere\_mari(X,\ Y) == 1)
                                           printf \ ("\ Primul\ numar\ este\ mai\ mare\ decat\ al\ doilea! \setminus n \setminus n");
                             }
                             e\,l\,s\,e
                                           if (comparare_numere_mari (X, Y) == 2)
                                                         printf \ ("Al \ doilea \ numar \ este \ mai \ mare \ decat \ primul! \ \ \ ");
                                           }
                            }
              }
              verificare = 1;
}
if (alegere_consola == 2)
              printf ("\n\n");
printf ("Adunarea numerelor mari\n\n");
printf ("Inserati de la tastatura un numar mare\n");
printf ("---> ");
scanf ("%s", numar_citit);
citiro ("mar, mar, (numar, citit));
              citire.numar_mare (numar_citit, X);
printf ("Numarul citit a fost salvat!");
printf ("\n\n\n");
              \label{eq:printf} \begin{array}{lll} printf \ ("Inserati \ de \ la \ tastatura \ inca \ un \ numar \ mare\n"); \\ printf \ ("%s", numar_citit); \\ citire_numar_mare \ (numar_citit, Y); \\ printf \ ("Numarul \ citit \ a \ fost \ salvat!"); \\ printf \ ("\n\n\n"); \end{array}
              \label{eq:printf} \begin{array}{ll} printf \; ("Suma \; celor \; doua \; numere \; este \; : \ \ "); \\ adunare\_numere\_mari \; (X, \; Y, \; suma); \\ printf \; ("---> \; "); \\ afisare\_numar\_mare \; (suma); \\ printf \; ("\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ ); \end{array}
              verificare = 1;
}
if (alegere\_consola == 3)
```

```
\label{eq:printf} \begin{array}{lll} printf \ ("Inserati \ de \ la \ tastatura \ inca \ un \ numar \ mare\n"); \\ printf \ ("%s", numar_citit); \\ citire_numar_mare \ (numar_citit \ , \ Y); \\ printf \ ("Numarul \ citit \ a \ fost \ salvat!"); \\ printf \ ("\n\n\n"); \end{array}
              scadere_numere_mari (X, Y, diferenta);
              printf ("\n");
              if (diferenta[0] != -1)
                            printf ("Diferenta celor doua numere este :\n"); printf ("---> ");
                           afisare_numar_mare (diferenta);
printf ("\n\n\n");
             }
              verificare = 1;
}
if (alegere\_consola == 4)
             printf ("Inserati acum un scalar\n");
printf ("---> ");
scanf ("%d", &scalar_produs);
printf ("\nProdusul celor doua numere este : \n");
printf ("---> ");
inmultire_scalar (X, scalar_produs, produs);
             afisare_numar_mare (produs);
printf ("\n\n");
              verificare = 1;
}
if (alegere_consola == 5)
             \label{eq:printf} \begin{array}{lll} printf \ ("Inserati \ de \ la \ tastatura \ inca \ un \ numar \ mare\n"); \\ printf \ ("----> "); \\ scanf \ ("%s", \ numar_citit); \\ citire_numar_mare \ (numar_citit, \ Y); \\ printf \ ("Numarul \ citit \ a \ fost \ salvat!"); \\ printf \ ("\n\n\n"); \end{array}
              printf ("\nProdusul celor doua numere este :\n"); printf ("---> ");
              inmultire_numar_mare (X, Y, produs);
             afisare_numar_mare (produs); printf ("\n\n");
              verificare = 1;
if (alegere\_consola == 6)
```

```
 \begin{array}{lll} \mbox{citire\_numar\_mare} & (\mbox{numar\_citit} , \ X); \\ \mbox{printf} & (\mbox{"Numarul citit a fost salvat!"}); \\ \mbox{printf} & (\mbox{"} \mbox{"} \mbox{"} \mbox{"} \mbox{"}); \\ \end{array} 
                       printf ("Inserati de la tastatura un scalar\n");
printf ("---> ");
scanf ("%d", &scalar_dividere);
rest = impartire_la_scalar (X, scalar_dividere);
                        if \quad (\ rest \ == \ -1)
                                               \begin{array}{lll} printf & ("\n\n Eroare!\n"); \\ printf & ("\n\n\n"); \\ printf & ("\n\n\n"); \\ \end{array} 
                       }
                       else
{
                                              \label{eq:continuous_printf} \begin{array}{ll} printf \ ("\nCatul impartirii este "); \\ printf \ ("---> "); \\ afisare\_numar\_mare \ (X); \\ printf \ ("\nRestul impartirii este ---> %d", rest); \\ printf \ ("\n\n'n"); \end{array}
                       verificare = 1;
}
printf ("\n\n\n");
printf (" Extragerea radicalului dintr-un numar mare\n\n");
printf (" Inserati de la tastatura un numar mare\n");
printf ("---> ");
scanf ("%s", numar_citit);
citire_numar_mare (numar_citit, X);
printf ("Numarul citit a fost salvat!");
printf ("\n\n");
                       \label{eq:printf} \begin{array}{ll} printf \ ("Partea intreaga a radicalului numarului introdus este:\n"); \\ printf \ ("---> "); \\ radical\_numar\_mare \ (X, radical); \\ afisare\_numar\_mare \ (radical); \\ printf \ ("\n\n\n"); \end{array}
                       verificare = 1;
}
if (verificare == 0)
{
                       printf ("\n"); printf ("---> Numarul introdus nu se regaseste in lista de mai sus.\n"); printf ("---> Inserati una din valorile 0,1,2,3,4,5,6,7."); printf ("\n\n\n");
}
else
{
                      printf ("\n\n\n
printf ("
printf ("
printf ("\n\n\n\n");
                                                                                                                                     *******\n");
Press any key for exit\n");
**********);
}
return 0:
```

Because the space does not allow it, in order to check the full source code (functions.c), visit my GitHub account by checking the hyperlink: Source code for functions

If the hyperlink does not work, you can follow the link: https://github.com/Xerophyt/Functions-for-operations-with-large-numbers/blob/master/JustFunctions.c/functions.c

Experiments and results

In order to test the program, I used a random number generator that takes as an input a length and returns a random value having the corresponding number of digits.

This is the source code:

```
# include <stdlib.h>
# include <stdio.h>
void number_generator (size_t length)
{
        int first_digit;
        srand(time(NULL));
        if (length > 1)
                 first_digit = rand() \% 9 + 1;
                 printf ("%d", first_digit);
                 for (i = 2; i \le length; i ++)
                         printf ("%d", rand() % 10);
        }
        e\,l\,s\,e
        {
                 if (length == 1)
                         printf ("%d", rand() % 10);
        }
}
int main ()
        int length;
        printf ("Inserati numarul de cifre -> ");
        scanf ("%d", &length);
        number_generator (length);
        return 0;
}
```

Here I will insert 10 input sets and the results generated by using the main functions (addition, subtraction, multiplication, dividing and extracting the square root).

For the last operation, we will provide the square root of the first number (we read two numbers in order to use the other functions). In fact, it computes the floor of the square root of the given number because the values that we work with are natural numbers.

The inputs will be all generated using the above number generator function. I will start with small numbers and I will increase their length gradually in order to demonstrate that by saving the numbers in this way, we can operate with any finite number, being it one digit long or 100 digits long.

The algorithms being homogeneous, (the same rules of calculation being applied on smaller numbers, as well as on very large ones) I will try to take decent values because testing the correctness of multiplying two numbers that have more than 100 digits each can take a very long time ($100 \times 100 = 10.000$ intermediary products by hand calculation).

Test 1

Number 1:6 Number 2:4

Sum: 10 Difference: 2 Product: 24 Quotient: 1 Remainder: 2

Floor of square root: 2

Test 2

 $\begin{array}{c} \text{Number 1: } 27 \\ \text{Number 2: } 93 \end{array}$

Sum: 120

Difference: ERROR (first number must be at least equal to the second one)

Product: 2511 Quotient: 0 Remainder: 27

Floor of square root: 5

Test 3

Number 1: 446 Number 2: 59 Sum: 505

Difference: 387 Product: 26314 Quotient: 7 Remainder: 33

Floor of square root: 21

 ${\rm Test}\ 4$

Number 1 : 211 Number 2 : 1381

 $Sum:\,1592$

Difference: ERROR (first number must be at least equal to the second one)

Product: 291391 Quotient: 0 Remainder: 211

Floor of square root: 14

Test 5

Number 1: 2908 Number 2: 1973

Sum: 4881 Difference: 935 Product: 5737484

Quotient: 1 Remainder: 935

Floor of square root: 53

Test 6

Number 1: 91609 Number 2: 900 Sum: 92509

Difference: 90709 Product: 82448100 Quotient: 101 Remainder: 709

Floor of square root: 302

Test 7

Number 1:523002

Number 2 : 0 Sum : 523002 Difference : 523002

Product : 0

Quotient: Error message (dividing by 0) Remainder: Error message (dividing by 0)

Floor of square root: 723

Test 8

Number 1: 1608255 Number 2: 4957 Sum: 1613212

Difference: 1603298 Product: 7972120035

Quotient: 324 Remainder: 2187

Floor of square root: 1268

Test 9

Number 1: 19018809 Number 2: 511176

 $Sum:\,19529985$

Difference: 18507633 Product: 9721958709384

Quotient: 37

Remainder: 105297

Floor of square root: 4361

Test 10

Number 1:9967604506Number 2:103475090

 $\begin{array}{l} {\rm Sum}:\,10071079596\\ {\rm Difference}:\,9864129416 \end{array}$

Product: 1031398773342755540

Quotient: 96

 $Remainder:\,33995866$

Floor of square root: 99837

Conclusions

For me, the implementation of this project has been an opportunity to test my level of preparation and the degree in which I can apply the C language in solving more complex problems.

At the same time, it was a good way to improve my methods of processing and editing documents in LaTeX. I also understood the importance of using Doxygen in order to get a well structured project documentation.

It was an exercise of correct code indentation and function management using makefiles, combined with the use of a gcc compiler for a command prompt application.

I enjoyed developing the source code and analyzing the situations that arose in the process because these have shown me once more the undeniable link that connects mathematics and programming.

I will finish by saying that the process of assembling all the project parts into one application and testing it has represented a very good practice for my long term growth associated to the domain of programming.

References

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