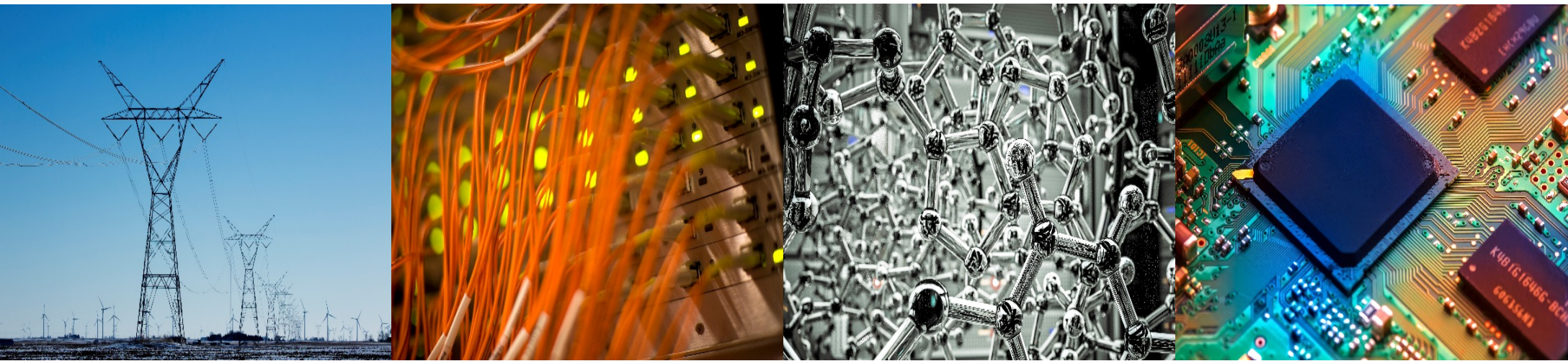


ECE 220 Computer Systems & Programming

Lecture 20 – C to LC-3 Conversion, Recursion with Backtracking

July 15, 2020



I ILLINOIS

Electrical & Computer Engineering

GRAINGER COLLEGE OF ENGINEERING

- MT2 past exam & practice questions posted
- Informal Early Feedback

Stack Built-up and Tear-down

- | | |
|------------------------|----------------------------------------------------------------|
| Caller function | 1. caller built-up (push callee's arguments onto stack) |
| | 2. pass control to callee (invoke function) |
-

- | | |
|------------------------|---------------------------------------------------------------------------------------------------------|
| Callee function | 3. callee built-up (push bookkeeping info and local variables onto stack) |
| | 4. execute function logic |
| | 5. callee tear-down (pop local variables, caller's frame pointer, and return address from stack) |
| | 6. return to caller |
-

- | | |
|------------------------|---------------------------------------------------------------------------------|
| Caller function | 7. caller tear-down (pop callee's return value and arguments from stack) |
|------------------------|---------------------------------------------------------------------------------|

;;convert Factorial function to an LC-3 subroutine

FACTORIAL

;;callee built-up of Factorial(n)'s activation record

;push return value, return address & caller's frame pointer

;push local variable & update frame pointer

;;function logic

;base case skipped here for simplicity

;recursive case

;caller built-up of Factorial(n-1)'s activation record

;push argument n-1 on to RTS

;pass control to Factorial(n-1)

;caller tear-down of Factorial(n-1)'s activation record

;pop return value from Factorial(n-1)

;pop argument from Factorial(n-1)

;calculate $n * \text{Factorial}(n-1)$

;remaining function logic skipped for simplicity

;;callee tear-down of Factorial(n)'s activation record

;pop local variable

;restore caller's frame pointer and return address

;;return to caller

Recursion with Backtracking: n-Queen Problem

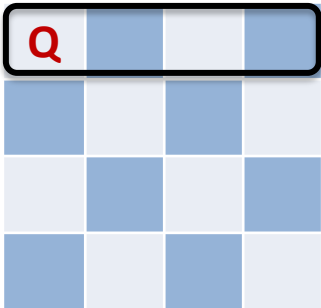
1. Find a safe column (from left to right) to place a queen, starting at row 0;
2. If we find a safe column, make recursive call to place a queen on the next row;
3. If we cannot find one, backtrack by returning from the recursive call to the previous row and find a different column.

	0	1	2	3
0		Q		
1				Q
2	Q			
3			Q	

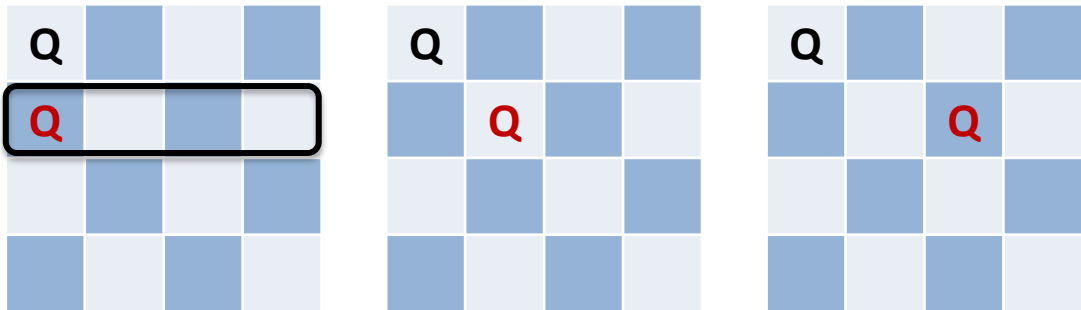
0	1	0	0
0	0	0	1
1	0	0	0
0	0	1	0

Example: 4x4 n-Queen

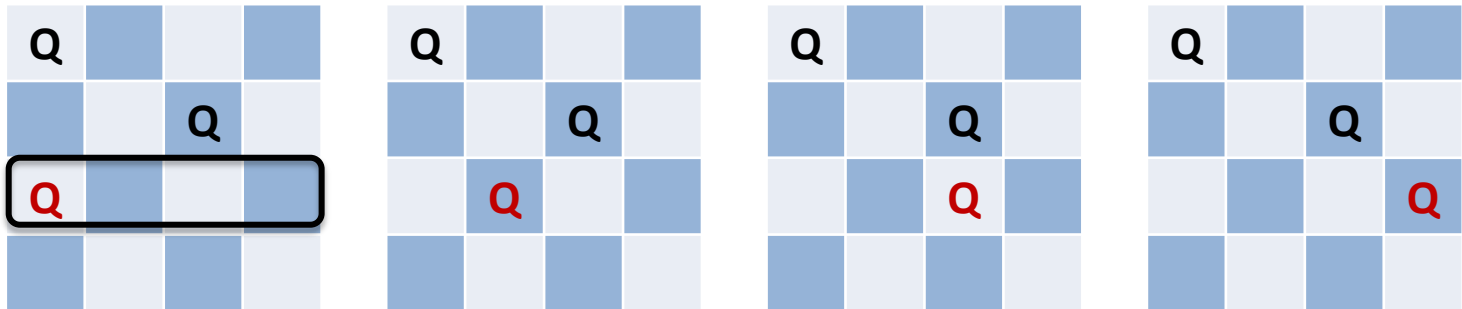
row 0:



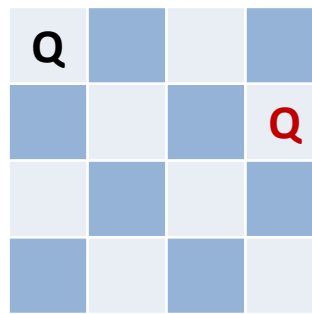
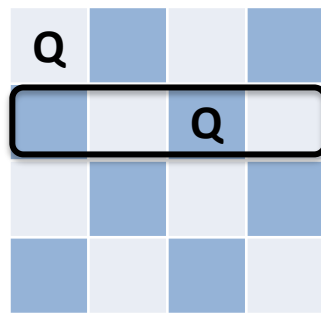
row 1:



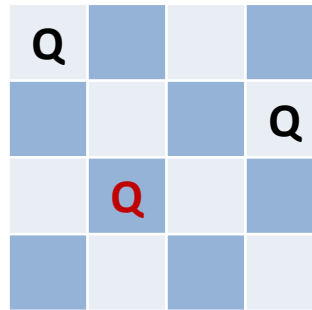
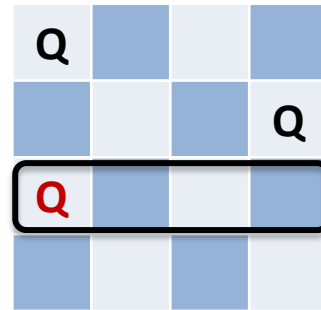
row 2:



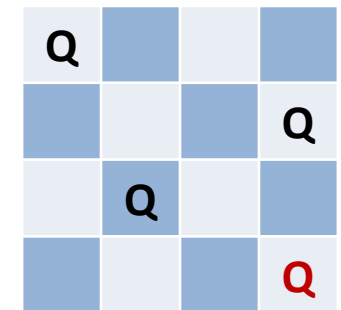
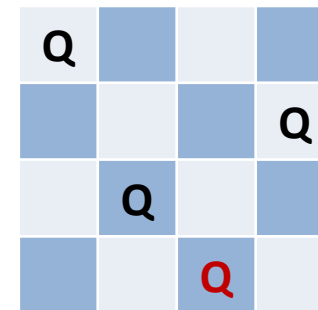
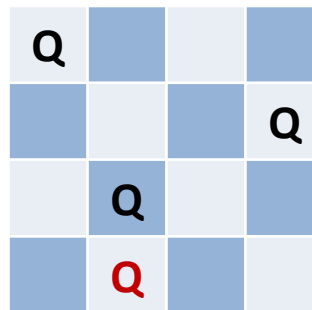
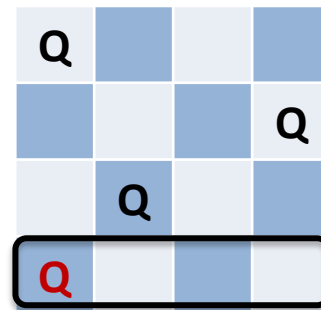
*Backtrack
to row 1 and
make a new
choice:*



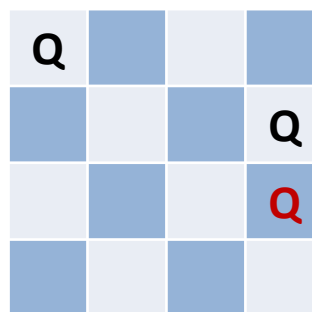
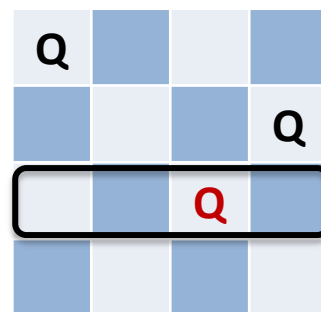
row 2:



row 3:

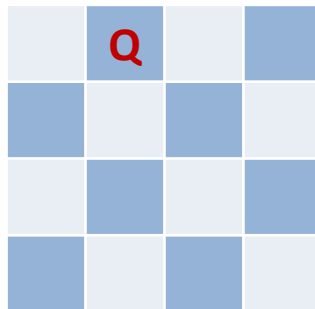
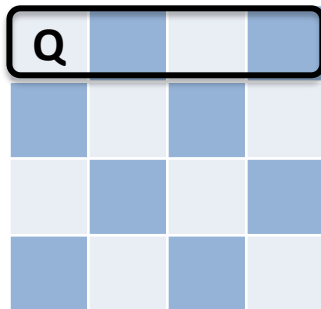


*Backtrack
to row 2 and
make a new
choice:*

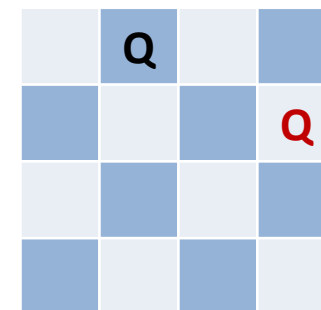
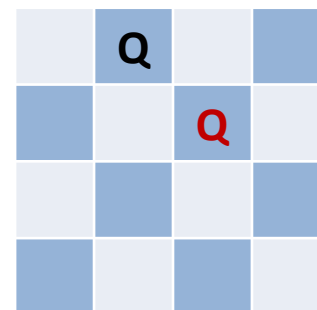
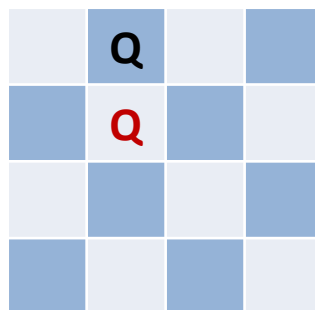
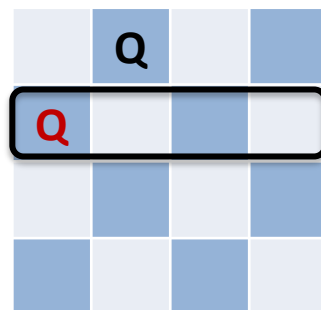


(Backtrack to row 1,
but no columns left)

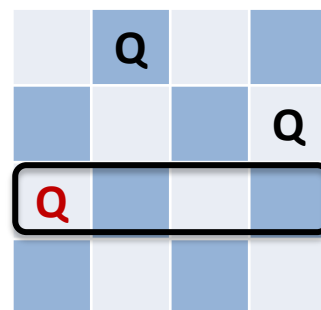
*Backtrack to row 0
and make a new
choice:*



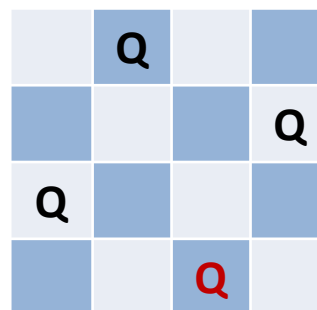
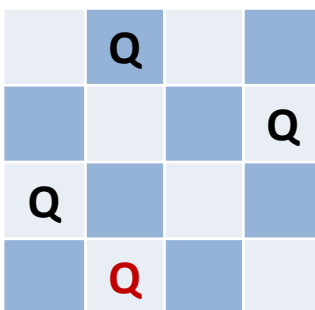
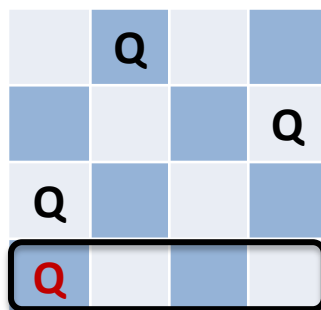
row 1:



row 2:



row 3:



/* isSafe() is a helper function to check whether it's safe to place a queen at board[row][col].

If it's safe, return 1; otherwise, return 0. */

```
int isSafe(int board[N][N], int row, int col){
```

```
}
```


Recursion with Backtracking Template

```
bool solve (configuration conf){
    if (no more choices) /*base case*/
        return (config is goal state);

    for(all available choices){
        try one choice c;
        /*recursively solve after making choice*/
        ok = solve(config with choice c made);
        if (ok)
            return true;
        else
            unmake choice c;
    }

    return false; /*tried all choices and no solution found*/
}
```

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