

State Preparation:

$$|\psi_1\rangle = \sum_{j=0}^{N-1} \sqrt{p_j} |j\rangle ,$$

where  $p_j = \frac{f(X_j)}{C}$ , with  $C$  being the normalizing constant.