

ICPC Team Notebook

typedef unsigned long long uwu

Sorbonne Université

SWERC 2025

A curated reference of algorithms and data structures



November 8, 2025

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1 Number Theory

1.1 Euler totient

Number of ints $\leq n$ coprime to n (c.f. sieve for primes).

```
int phi(int n, vi& primes) {
    int res = n;
    for (int p : primes) {
        if (1LL * p * p > n) break;
        if (n % p == 0) {
            while (n % p == 0) n /= p;
            res -= res / p;
        }
    }
    if (n > 1) res -= res / n;
    return res;
}
```

1.2 Fast exponentiation

$O(\log b)$: fast $a^b \bmod p$.

```
int modular_exp(int a, int b, int p){
    int res = 1;
    while(b > 0){
        if(b & 1) res = (1LL * a * res) % p;
        b = b >> 1;
        a = (1LL * a * a) % p;
    }
    return res;
}
```

1.3 Sieve of Eratosthenes

$O(n \log \log n)$ sieve[i] = 0 if i prime, spf otherwise for fast fact

```
vi sieve(int n){
    vi sieve(n,0);
    for(int i = 2; i*i < n ; i++)
        if(!sieve[i])
            for(int j = i*i ; j <n ; j += i)
                if(!sieve[j]) sieve[j] = i;
    return sieve;
}
```

2 Data Structures

2.1 Fenwick Tree

Point update, prefix and range sum, $O(\log n)$, $O(n)$ build

```
struct Fenwick {
    int n; vector<ll> t; //using long long, int might overflow.
    Fenwick(vector<ll>& a): n(a.size()), t(n+1,0) {
        for(int i = 1; i <=n; i++) { //Builds tree from array in O(n).
            t[i] += a[i-1];
            int p = i+(i&-i);
            if(p<=n) t[p] += t[i];
        }
    }
    void add(int i,long long v){
        for(;i<=n;i+=i&-i) t[i]+=v;
    }
    long long sum(int i){
        long long r=0;
        for(; i>0 ; i -= i&-i) r += t[i];
        return r;
    }
    long long sum(int l,int r){ return sum(r)-sum(l-1); }
};
```

2.2 Union find

Complexity: effectively $O(1)$

```
struct union_find{
    vector<int> rank, parent;
    union_find(int n){
        rank.resize(n, 0); parent.resize(n);
        for (int i = 0; i < n; i++) parent[i] = i;
    }
    int find(int i){
        int root = parent[i];
        if (parent[root] != root) parent[i] = find(root);
        return root;
    }
    void unite(int x, int y) {
        int xRoot = find(x);
        int yRoot = find(y);
        if (xRoot == yRoot) return;
        if (rank[xRoot] < rank[yRoot]) parent[xRoot] = yRoot;
        else if (rank[yRoot] < rank[xRoot]) parent[yRoot] = xRoot;
        else{
            parent[yRoot] = xRoot;
            rank[xRoot]++;
        }
    }
};
```

3 Graph Algorithms

3.1 Max Bipartite Matching

Hopcroft–Karp $O(E\sqrt{V})$ left [0..nL-1], right [0..nR-1] adj from left to right.

```
int nL, nR;
vector<vi>adj;
vi dist, matchL, matchR;
```


};

3.3 Shortest Path

Find shortest paths from src (no negative weights). $O((V+E)\log V)$

```
vi dijkstra(const vector<vector<pii>>& adj, int src) {
    vi dist(adj.size(), INT_MAX);
    priority_queue<pii, vector<pii>, greater<pii> q;
    dist[src] = 0; q.push({0, src});
    while (!q.empty()) {
        auto [d, u] = q.top(); q.pop();
        if (d != dist[u]) continue;
        for (auto [v, w] : adj[u]) {
            if (d+w < dist[v]) {
                dist[v] = d+w;
                q.push({d+w, v});
            }
        }
    }
    return dist;
}
```

$O(VE)$ Shortest Path+neg edges; BFS from nodes with dist $-\infty$ for all neg-cycle reachable.

```
vector<int> bellmanFord(int n, vector<vector<int>>& edges, int src) {
    vector<int> dist(n, INT_MAX);
    dist[src] = 0;
    for (int i = 0; i < n; i++) {
        for (vector<int> edge : edges) {
            int u = edge[0]; int v = edge[1]; int wt = edge[2];
            if (dist[u] != INT_MAX && dist[u] + wt < dist[v]) {
                if (i == n - 1) return {-1};
                dist[v] = dist[u] + wt;
            }
        }
    }
    return dist;
}
```

All-pairs shortest paths (neg edges ok, no neg cycles) $O(V^3)$ $graph[i][i] = 0$, $graph[i][j] = w$ if edge $i \rightarrow j$ else INT_MAX

```
vector<vi> floydWarshall(vector<vi> graph) {
    int V = graph.size();
    auto dist = graph;
    for (int k = 0; k < V; ++k)
        for (int i = 0; i < V; ++i)
            for (int j = 0; j < V; ++j)
                if (dist[i][k] < INT_MAX && dist[k][j] < INT_MAX)
                    dist[i][j] = min(dist[i][j], dist[i][k] + dist[k][j]);
    return dist;
}
```

3.4 TSP

Traveling Salesman Problem $O(n^2 2^n)$

```
int tsp(int n, vvi& dist) {
    int mask_limit = 1 << n;
    vvi dp(mask_limit, vi(n, INT_MAX));
    dp[1][0] = 0;
    for (int mask = 1; mask < mask_limit; mask++) {
        for (int last = 0; last < n; last++) {
            if (dp[mask][last] == INT_MAX) continue;
            for (int next = 0; next < n; next++) {
                if (mask & (1 << next)) continue;
                int new_mask = mask | (1 << next);
                dp[new_mask][next] = min(dp[new_mask][next],
                                         dp[mask][last] + dist[last][next]);
            }
        }
        int ans = INT_MAX;
        for (int last = 1; last < n; last++) {
            if (dp[mask_limit - 1][last] != INT_MAX && dist[last][0] != INT_MAX) {
                ans = min(ans, dp[mask_limit - 1][last] + dist[last][0]);
            }
        }
        return ans;
    }
}
```

3.5 Toposort

TopoSort via DFS $O(V + E)$.

```
void dfs(int u, vector<vi> &adj, vi &vis, vi &res) {
    vis[u] = 1;
    for (int v : adj[u])
        if (!vis[v])
            dfs(v, adj, vis, res);
    res.push_back(u);
}
vi toposort(vector<vi> &adj) {
    int n = adj.size();
    vi vis(n, 0), res;
    for (int i = 1; i < n; i++)
        if (!vis[i]) dfs(i, adj, vis, res);
    reverse(res.begin(), res.end());
    return res;
}
```

4 Arrays

4.1 Inversions

Count pairs where order flips between arrays. $O(n \log n)$

```
ll inversions(vi& a, vi& b) {
    int n = a.size();
    unordered_map<int,int> pos;
    for (int i = 0; i < n; i++) pos[b[i]] = i + 1;
    Fenwick t(n); // C.f. Fenwick tree
    ll inv = 0;
    for (int i = 0; i < n; i++) {
```

```
        inv += i - t.sum(pos[a[i]]);
        t.add(pos[a[i]], 1);
    }
    return inv;
}
```