

$$\begin{aligned}
\vec{a} \times (\vec{b} \times \vec{c}) &= \vec{b}(\vec{a} \cdot \vec{c}) - \vec{c}(\vec{a} \cdot \vec{b}), \\
\vec{a} \cdot (\vec{b} \times \vec{c}) &= \vec{b} \cdot (\vec{c} \times \vec{a}) = \vec{c} \cdot (\vec{a} \times \vec{b}), \\
(\vec{a} \times \vec{b}) \cdot (\vec{c} \times \vec{d}) &= (\vec{a} \cdot \vec{c})(\vec{b} \cdot \vec{d}) - (\vec{a} \cdot \vec{d})(\vec{b} \cdot \vec{c}), \\
\vec{\nabla} \times (\vec{\nabla} \psi) &= 0, \\
\vec{\nabla} \cdot (\vec{\nabla} \times \vec{a}) &= 0, \\
\vec{\nabla} \times (\vec{\nabla} \times \vec{a}) &= \vec{\nabla}(\vec{\nabla} \cdot \vec{a}) - \nabla^2 \vec{a}, \\
\vec{\nabla} \cdot (\psi \vec{a}) &= \vec{a} \cdot \vec{\nabla} \psi + \psi \vec{\nabla} \cdot \vec{a}, \\
\vec{\nabla} \times (\psi \vec{a}) &= \vec{\nabla} \psi \times \vec{a} + \psi \vec{\nabla} \times \vec{a}, \\
\vec{\nabla}(\vec{a} \cdot \vec{b}) &= (\vec{a} \cdot \vec{\nabla}) \vec{b} + (\vec{b} \cdot \vec{\nabla}) \vec{a} + \vec{a} \times (\vec{\nabla} \times \vec{b}) + \vec{b} \times (\vec{\nabla} \times \vec{a}), \\
\vec{\nabla} \cdot (\vec{a} \times \vec{b}) &= \vec{b} \cdot (\vec{\nabla} \times \vec{a}) - \vec{a} \cdot (\vec{\nabla} \times \vec{b}), \\
\vec{\nabla} \times (\vec{a} \times \vec{b}) &= \vec{a}(\vec{\nabla} \cdot \vec{b}) - \vec{b}(\vec{\nabla} \cdot \vec{a}) + (\vec{b} \cdot \vec{\nabla}) \vec{a} - (\vec{a} \cdot \vec{\nabla}) \vec{b}, \\
\vec{\nabla} \cdot \vec{r} &= 3, \\
\vec{\nabla} \times \vec{r} &= 0, \\
\vec{\nabla} \cdot \hat{r} &= 2/r, \\
\vec{\nabla} \times \hat{r} &= 0, \\
\vec{\nabla} r &= \hat{r}, \\
\vec{\nabla} \frac{1}{r} &= -\frac{\hat{r}}{r^2}, \\
\vec{\nabla} \cdot (\hat{r} f(r)) &= \frac{2}{r} f + \frac{df}{dr}, \\
(\vec{a} \cdot \vec{\nabla}) \hat{r} &= \frac{1}{r} [\vec{a} - \hat{r}(\vec{a} \cdot \hat{r})] = \frac{\vec{a}_\perp}{r}, \\
\vec{\nabla}^2 \left( \frac{1}{r} \right) &= -4\pi \delta(\vec{r}), \\
\int_V d^3r \vec{\nabla} \cdot \vec{A} &= \int_S d\vec{S} \cdot \vec{A}, \\
\int_V d^3r \vec{\nabla} \psi &= \int_S \psi d\vec{S}, \\
\int_V d^3r \vec{\nabla} \times \vec{A} &= \int_S d\vec{S} \times \vec{A}, \\
\int_V d^3r (\phi \nabla^2 \psi + \vec{\nabla} \phi \cdot \vec{\nabla} \psi) &= \int_S \phi d\vec{S} \cdot \vec{\nabla} \psi, \\
\int_V d^3r (\phi \nabla^2 \psi - \psi \nabla^2 \phi) &= \int_S (\phi \vec{\nabla} \psi - \psi \vec{\nabla} \phi) \cdot d\vec{S}, \\
\int_S (\vec{\nabla} \times \vec{A}) \cdot d\vec{S} &= \oint d\vec{\ell} \cdot \vec{A}, \\
\int_S d\vec{S} \times \vec{\nabla} \psi &= \oint_C d\vec{\ell} \psi.
\end{aligned}$$

$$\begin{aligned}
\mathcal{L} &= -\frac{1}{4\mu_0}F_{\mu\nu}F^{\mu\nu} - J_\mu A^\mu & x^\mu &= (ct, x, y, z), \\
L &= \frac{1}{\gamma}(-mc^2 - qA_\mu u^\mu) & \partial^\mu &= ((1/c)\partial/\partial t, -\vec{\nabla}) \\
\frac{dp^\mu}{d\tau} &= qF^{\mu\nu}u_\nu & k^\mu &= (\omega/c, \vec{k}), \\
\partial_\mu F^{\mu\nu} &= \mu_0 J^\nu & u^\mu &= (\gamma c, \gamma \vec{v}), \\
\partial_\mu \tilde{F}^{\mu\nu} &= 0 & p^\mu &= (E/c, \vec{p}), \\
\partial_\mu J^\mu &= 0 & A^\mu &= (\phi/c, \vec{A}), \\
(g_{\mu\nu}) &= \text{diag}(1, -1, -1, -1), & J^\mu &= (c\rho, \vec{j}), \\
\vec{\beta} &= \vec{v}/c, & F^{\mu\nu} &= \partial^\mu A^\nu - \partial^\nu A^\mu, \\
\gamma &= 1/\sqrt{1-\beta^2}, & \tilde{F}^{\mu\nu} &= \frac{1}{2}\epsilon^{\mu\nu\alpha\beta}F_{\alpha\beta} \\
x'^\mu &= \Lambda^\mu{}_\nu x^\nu \\
(\Lambda^\mu{}_\nu) &= \begin{pmatrix} \gamma & -\beta\gamma & 0 & 0 \\ -\beta\gamma & \gamma & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix},
\end{aligned}$$

$$\begin{aligned}
\vec{\nabla} \cdot \vec{E} &= \frac{1}{\epsilon_0} \rho, & \vec{\nabla} \cdot \vec{B} &= 0, \\
\vec{\nabla} \times \vec{B} - \frac{1}{c^2} \frac{\partial \vec{E}}{\partial t} &= \mu_0 \vec{j}, & \vec{\nabla} \times \vec{E} + \frac{\partial \vec{B}}{\partial t} &= 0,
\end{aligned}$$

$$\begin{aligned}
\int_{S(V)} \vec{E} \cdot d\vec{A} &= \frac{1}{\epsilon_0} \int_V d^3r \, \rho \\
\frac{d\vec{p}}{dt} &= q(\vec{E} + \vec{v} \times \vec{B}) \\
\vec{E} &= -\vec{\nabla}\phi - \frac{\partial \vec{A}}{\partial t} \\
\vec{B} &= \vec{\nabla} \times \vec{A} \\
p_i &= \int d^3r' \, \rho(\vec{r}') \, r'_i \\
Q_{ij} &= \int d^3r' \, \rho(\vec{r}') \, (3r'_i r'_j - \delta_{ij} r'^2) \\
\phi &= \frac{1}{4\pi\epsilon_0} \left( \frac{Q_{\text{tot}}}{r} + \frac{p_i \hat{r}_i}{r^2} + \frac{1}{2!} Q_{ij} \frac{\hat{r}_i \hat{r}_j}{r^3} + \dots \right) \\
U &= Q_{\text{tot}} \phi(\vec{r}) - p_i E_i(\vec{r}) - \frac{1}{6} Q_{ij} \partial_i E_j + \dots
\end{aligned}$$