

Claim: For set  $S = \{\frac{c}{d} : c \in \mathbb{N} \cup \{0\}, d \in \mathbb{Q}, d \neq 0\}$ ,  $S = \mathbb{Q}$

Proof: Need to show  $\forall s \in S, s \in \mathbb{Q}$

Let  $s \in S \Rightarrow s = \frac{c}{d}$  for  $c \in \mathbb{N} \cup \{0\}, d \in \mathbb{Q}, d \neq 0$

$\Rightarrow d = \frac{a}{b}$  where  $a \in \mathbb{Z}, a \neq 0, b \in \mathbb{Z}, b \neq 0$

1.

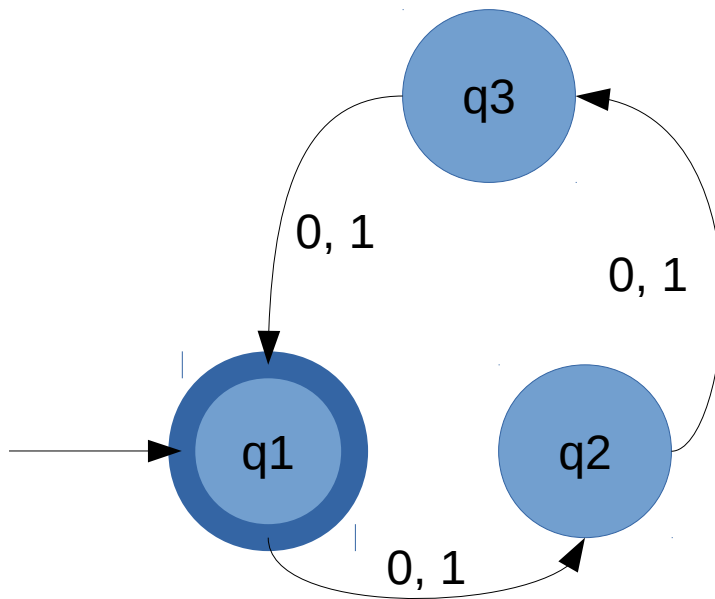
$\Rightarrow s = \frac{c}{\frac{a}{b}}$

$\Rightarrow s = \frac{cb}{a}$

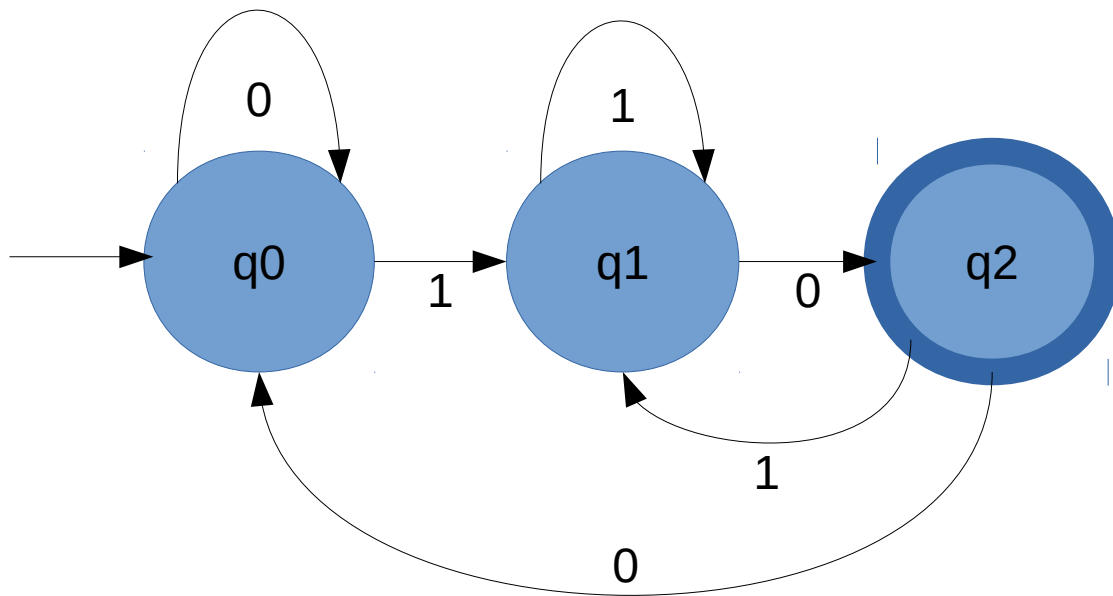
$\Rightarrow s \in \mathbb{Q}$

$\therefore S = \mathbb{Q}$

2.



3.



4.

$\{w : w \text{ starts with sequence } 10\}$