

Claim: For set $S = \{\frac{c}{d} : c \in \mathbb{N} \cup \{0\}, d \in \mathbb{Q}, d \neq 0\}$, $S = \mathbb{Q}$

Proof: Need to show $\forall s \in S, s \in \mathbb{Q}$

Let $s \in S \Rightarrow s = \frac{c}{d}$ for $c \in \mathbb{N} \cup \{0\}, d \in \mathbb{Q}, d \neq 0$

$\Rightarrow d = \frac{a}{b}$ where $a \in \mathbb{Z}, a \neq 0, b \in \mathbb{Z}, b \neq 0$

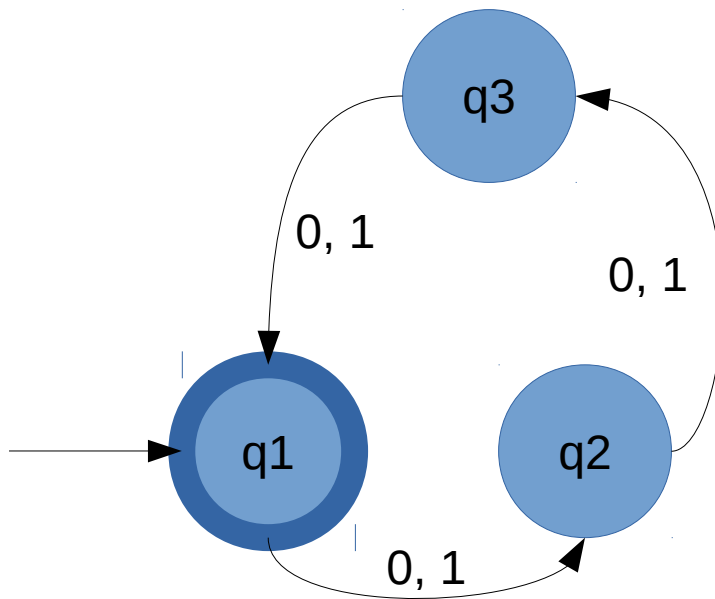
1. $\Rightarrow s = \frac{c}{(\frac{a}{b})}$

$\Rightarrow s = \frac{cb}{a}$

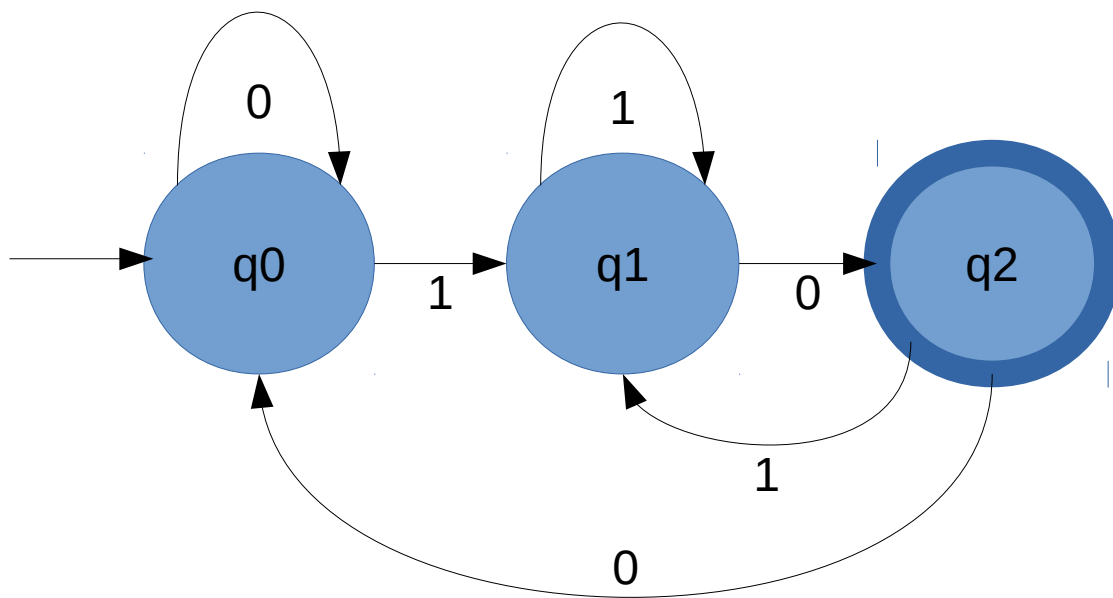
$\Rightarrow s \in \mathbb{Q}$

$\therefore S = \mathbb{Q}$

2.



3.



4.

$\{w : w \text{ starts with sequence } 10\}$