

1. Binary Search Property

Alex
Program

```
function findPoint(x, low, high)
    if low < high
        return false
    mid = (low + high) / 2
    if x[mid] == mid
        return true
    else if x[mid] > mid
        return findPoint(x, low, mid - 1)
    else
        return findPoint(x, mid + 1, high)
```

Time is $O(\log n)$

↳ $O(\log n)$ recursive, $O(1)$ iterative

2. AUB in $O(\log m + \log n)$ time

function kthSmallest(A[1..m], B[1..n], x)

if $x == 0$, return B[1]

if $x == 1$, return A[x]

if $x == 1$, return $\min(A[1], B[1])$

$i = \min(x, x/2)$

$j = x - i$

if $A[i] < B[j]$

return kthSmallest(A[i+1..x], B, x-i)

else

return kthSmallest(A, B[j+1..z], x-i)

complexity is $O(\log m + \log n)$