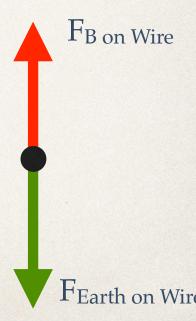
Force on a Current Carrying Wire

* A 2.5 Tesla B-Field goes into the board. A 10g, 1.00m wire carries a current in that magnetic field. Assuming the angle between I and B is 90°, what is the current necessary to make the wire levitate?

$$B = 2.5 \text{ T}$$
 $I = ?$
 $\ell = 1.00 \text{ m}$
 $\theta = 90^{\circ}$
 $F = ?$





$$\sum F = ma! \quad \text{NEWTON'S SECOND LAW!}$$

$$F_{\vec{B}} + (-mg) = 0$$

$$I(B\sin\theta + (-mg) = 0$$

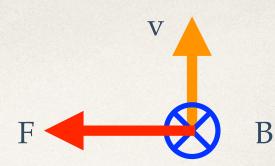
$$I(1.0 \text{ m})(2.5 \text{ T})(1) - (0.01 \text{ kg})(9.8 \frac{m}{s^2}) = 0$$

$$I(2.5 \text{ T} \cdot \text{m}) = (0.098 \text{ N})$$

$$I = 0.039 \text{ Amperes}$$

- * **PURPOSE:** Determine the direction of the force on a charged particle moving with a velocity in a magnetic field.
 - 1. Fingers point in the direction of the velocity of the positively charged particle.
 - 2.Palm points in the direction of the B-Field
 - 3. Thumb points in the direction of the force on the **positively** charged particle*





Derivation:

$$F = I\ell B \sin \theta$$
 but... $I = \frac{q}{t}$
 $F = \frac{q}{t} \ell B \sin \theta$

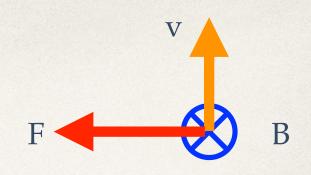
SO,

$$F = q \frac{\ell}{t} B \sin \theta$$

but...
$$\frac{\ell}{t} = v$$

$$F = qvB\sin\theta$$

*Direction of Force is opposite for electron



* A 0.25 Tesla B-Field goes into the board. A proton traveling at 10% of the speed of light* moves perpendicularly through the B-Field, what is the force on the proton?

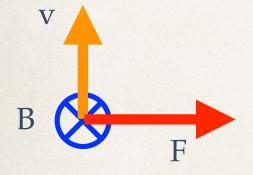
$$F = qvB \sin \theta$$

$$F = (1.6x10^{-19} \text{C})(3.0x10^7 \text{ m/s})(0.25 \text{ T})(1)$$

$$F = 1.2x10^{-12} \text{ N}$$

$$c = 3.00 \times 10^8 \, \text{m/s}$$

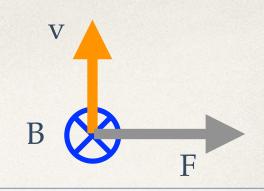
* A 0.25 Tesla B-Field goes into the board. An electron traveling at 10% of the speed of light moves perpendicularly through the B-Field, what is the force on the electron?



$$F = qvB\sin\theta$$

$$F = (1.6x10^{-19})(3.0x10^{7})(0.25)(1)$$

$$F = 1.2x10^{-12} \text{ N}$$



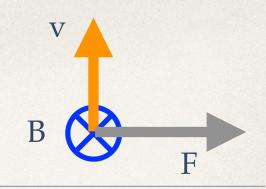
What effect do these forces have on these charged particles?

$$\sum F = ma!$$

$$qvB\sin\theta = m\frac{v^2}{r}$$

$$r = \frac{mv}{qB\sin\theta}$$

| | p ⁺ | e- |
|---|---------------------------|---------------------------|
| F | 1.2x10 ⁻¹² N | 1.2x10 ⁻¹² N |
| m | 1.67x10 ⁻²⁷ Kg | 9.11x10 ⁻³¹ Kg |
| r | | |

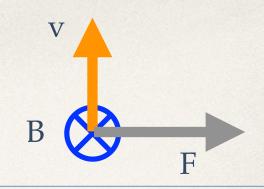


Proton

$$r = \frac{mv}{qB\sin\theta}$$

$$r = \frac{\left(1.67 \times 10^{-27} \, kg\right) \left(3.0 \times 10^7 \, \frac{m}{s}\right)}{\left(1.6 \times 10^{-19}\right) \left(0.25 \, \mathrm{T}\right) \left(1\right)}$$

$$r = 1.25 \text{ m}$$



Electron

$$r = \frac{mv}{qB\sin\theta}$$

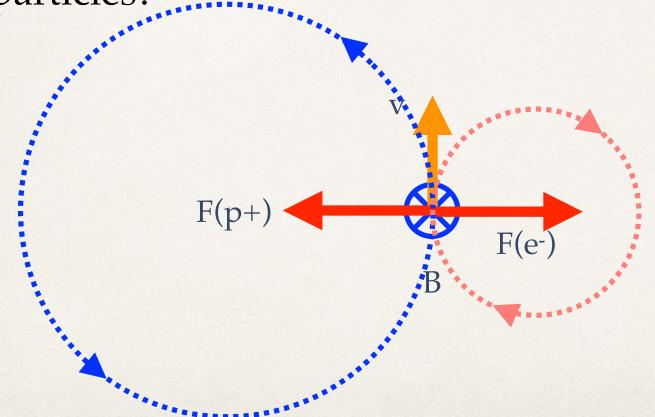
$$r = \frac{\left(9.11x10^{-31}kg\right)\left(3.0x10^{7} \frac{m}{s}\right)}{\left(1.6x10^{-19}\right)\left(0.25 \text{ T}\right)\left(1\right)}$$

$$r = 0.00068 \text{ m}$$

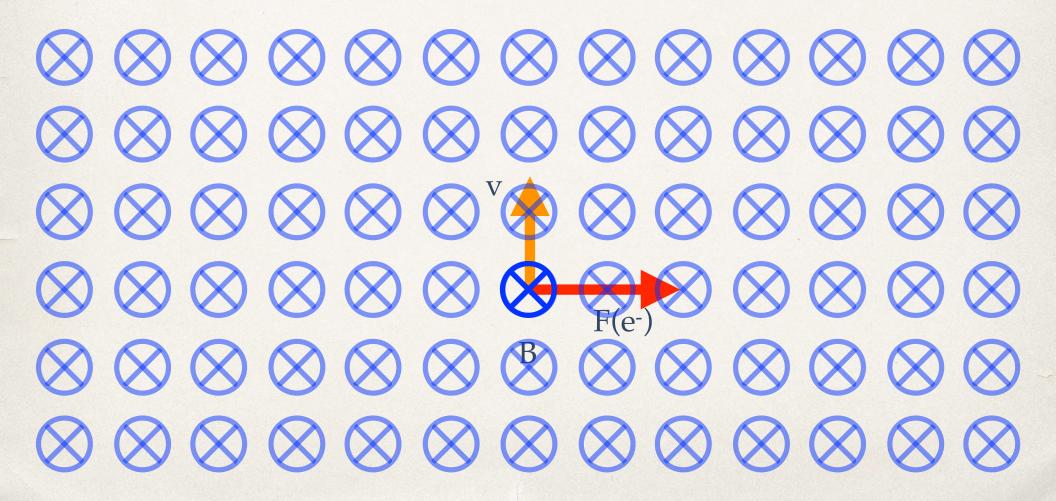
$$r_{p^+} = 2.9225m$$

$$r_{e^{-}} = 0.0016m$$

What effect do these forces have on these charged particles?

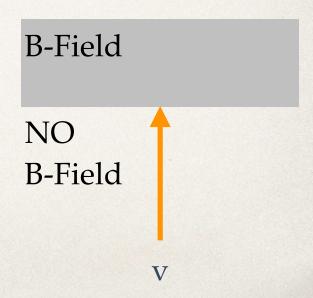


Note: F only occurs in the region where B is present!

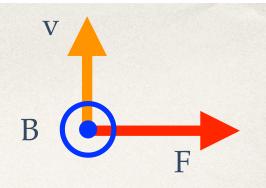


Right Hand Rule #3 - Example

* A protron traveling at 10% of the speed of light enters a region of a 0.17 Tesla B-Field comes out of the board. It moves perpendicularly through the B-Field, what is the force on the proton? What is the path of proton?



RHR#3 - Example



* A protron traveling at 10% of the speed of light enters a region of a 0.17 Tesla B-Field comes out of the board. It moves perpendicularly through the B-Field, what is the force on the proton? What is the path of proton?

$$F = qvB\sin\theta$$
 $F = (1.6x10^{-19})(3.0x10^{7})(0.17)(1)$
 $F = 8.16x10^{-13}$ N

B-Field

NO
B-Field

Hall Effect

What is the effect of charge moving within a conductor?

$$F = qvB\sin\theta$$

$$qE = qvB$$

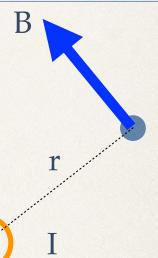
$$E = vB$$
 but...
$$E = \frac{V}{\ell}$$

$$\frac{V}{\ell} = vB$$

$$\boxed{V = B\ell v}$$

Magnetic Field: Straight Wire.

What is the magnitude and direction of the B-Field near a long straight wire?



Magnitude?

$$B = \frac{\mu_o I}{2\pi r}$$



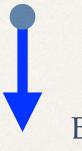
Direction?

RHR #1

Magnetic Field: Straight Wire.

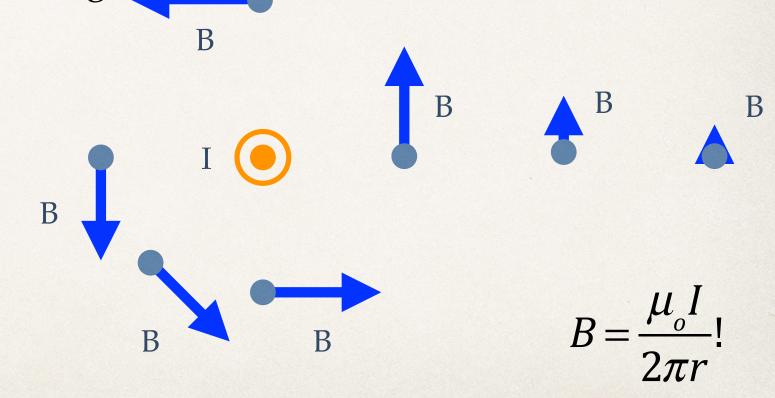
What is the magnitude and direction of the B-Field near a long straight wire?



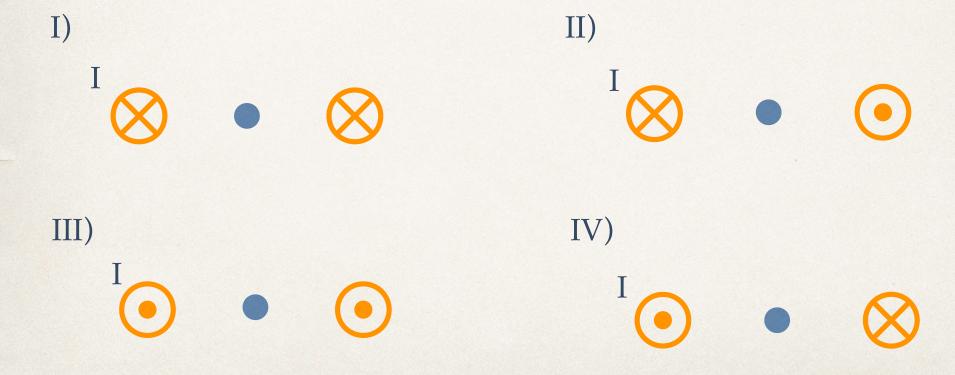


Magnetic Field due to a straight wire.

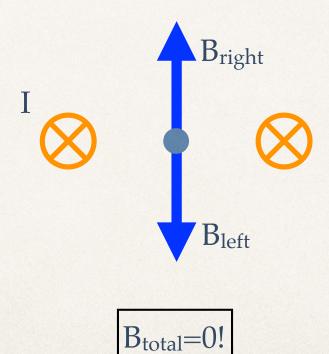
What is the direction of the B-Field at various points near a long straight wire?



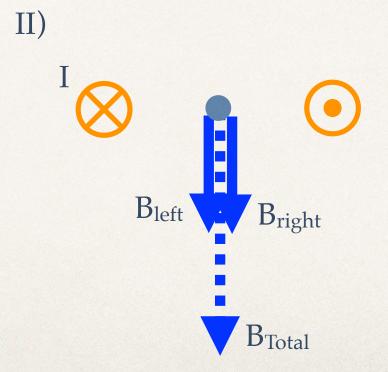
Determine the direction of total magnetic field between two long, parallel wires.

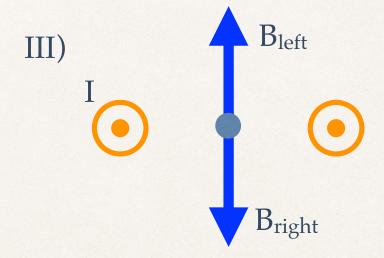


I)

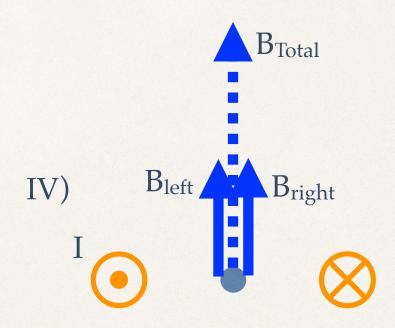


B_{total} = large, downward





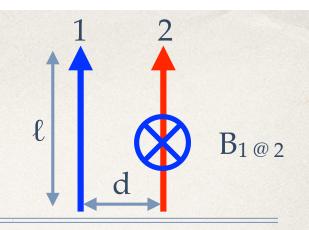
B_{total}=0!



 $B_{total} = large$, upward

Process

- 1. Determine the magnitude and direction of the B-field caused by Wire #1
- 2. **THEN** Determine the force that B-field (from Step #1) applies on to Wire #2.



What is the force on two parallel wires, carrying 2.0 A of current in the same direction, if the wires are 50.0 cm in length and spaced 10.0 cm apart?

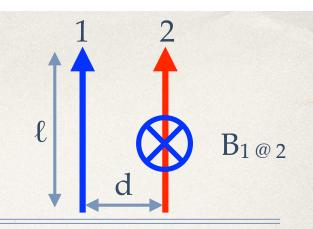
$$\begin{split} I_1 &= 2.0 \text{ A} \\ I_2 &= 2.0 \text{ A} \\ \ell_1 &= 0.50 \text{ m} \\ \ell_2 &= 0.50 \text{ m} \\ d &= 0.1 \text{ m} \\ \mu_o &= 4\pi \text{x} 10^{-7} \end{split}$$

$$B_{1@2} = \frac{\mu_o I_1}{2\pi r}$$
 but $r = d$ in this case!

$$B_{1 @ 2} = \frac{(4\pi x 10^{-7})(2 \text{ A})}{2\pi (0.1 \text{ m})}$$

$$B_{1 @ 2} = 4.0x 10^{-6} \text{ T}$$

$$B_{1 @ 2} = 4.0 \times 10^{-6} \text{ T}$$



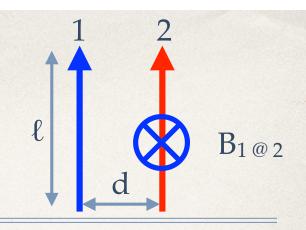
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$$F_{1 \text{ on } 2} = I_2 \ell_2 B_{1 \text{ @ 2}} \sin \theta$$
 but $B_{1 \text{ @ 2}} = \frac{\mu_o I_1}{2\pi r}$

$$F_{1 \text{ on } 2} = I_2 \ell_2 \left(\frac{\mu_o I_1}{2\pi r} \right) \sin \theta$$

$$F_{1 \text{ on } 2} = \left(\frac{\mu_o}{2\pi}\right) \left(\frac{I_1 I_2 \ell_2}{r}\right)$$



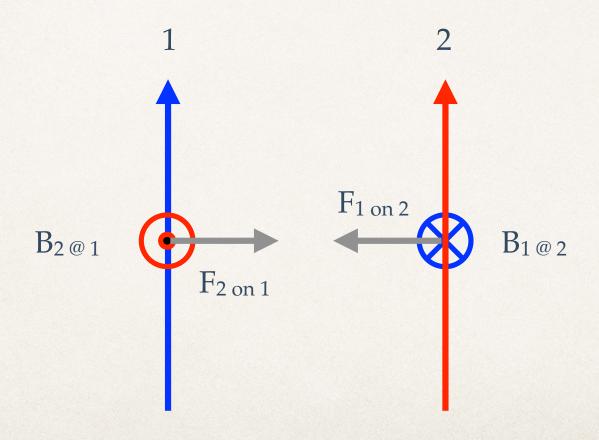
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$$F_{1 \text{ on } 2} = \left(\frac{\mu_o}{2\pi}\right) \left(\frac{I_1 I_2 \ell_2}{r}\right)$$

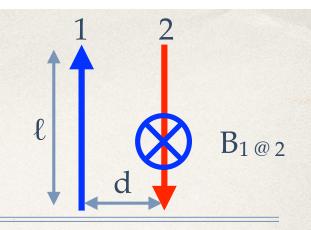
$$|F_{1 \text{ on } 2} = 4.0 \times 10^{-6} N|$$

but, which way?



Group: What is the force on two anti-parallel wires, one carrying $I_1 = 2.0$ A of current and the other carrying $I_2 = 6.5$ A of current, in the opposite direction, if the wires are 1.50 m in length and spaced 0.03 m apart?

- Determine the magnitude and direction of the Force on Wire #2 from Wire #1
- Determine the magnitude and direction of the Force on Wire #1 from Wire #2



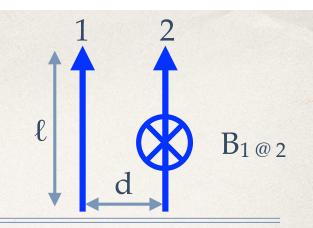
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$$\begin{split} I_1 &= 2.0 \text{ A} \\ I_2 &= 6.5 \text{ A} \\ \ell_1 &= 1.50 \text{ m} \\ \ell_2 &= 1.50 \text{ m} \\ d &= 0.03 \text{ m} \\ \mu_o &= 4\pi \times 10^{-7} \end{split}$$

$$B_{1@2} = \frac{\mu_o I_1}{2\pi r}$$
 but $r = d$ in this case!

$$B_{1@2} = \frac{(4\pi x 10^{-7})(2 \text{ A})}{2\pi (0.03 \text{ m})}$$

$$B_{1 @ 2} = 1.33 \times 10^{-5} \text{ N}$$



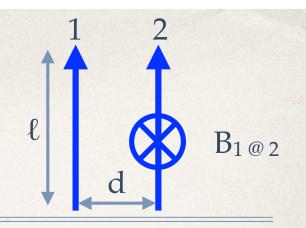
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$$F_{1 \text{ on } 2} = I_{2} \ell_{2} B_{1 \text{ @ 2}} \sin \theta \quad \text{but} \quad B_{1 \text{ @ 2}} = \frac{\mu_{o} I_{1}}{2\pi r}$$

$$F_{1 \text{ on } 2} = I_{2} \ell_{2} \left(\frac{\mu_{o} I_{1}}{2\pi r}\right) \sin \theta$$

$$F_{1 \text{ on } 2} = \left(\frac{\mu_o}{2\pi}\right) \left(\frac{I_1 I_2 \ell_2}{r}\right)$$



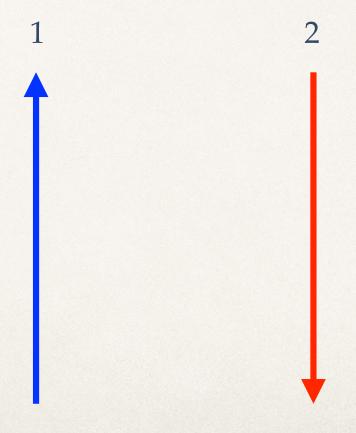
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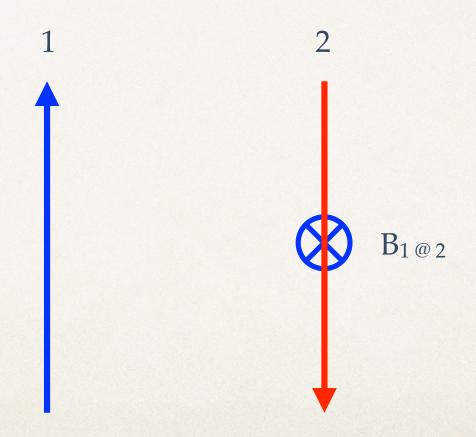
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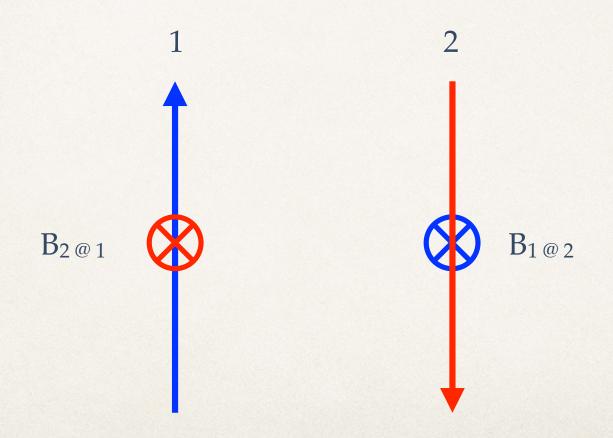
$$F_{1 \text{ on } 2} = \left(\frac{\mu_o}{2\pi}\right) \left(\frac{I_1 I_2 \ell_2}{r}\right)$$

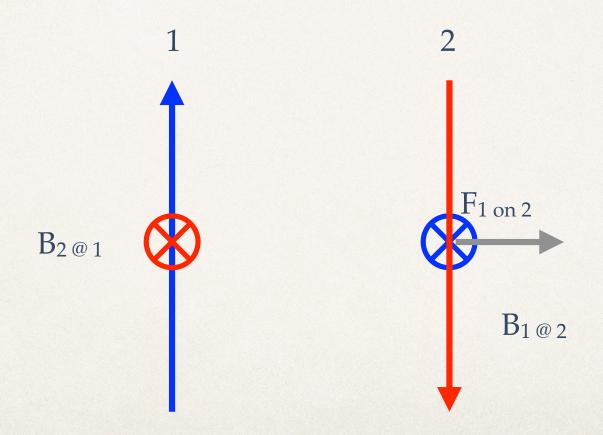
$$F_{1 \text{ on } 2} = 1.33 \times 10^{-4} N$$

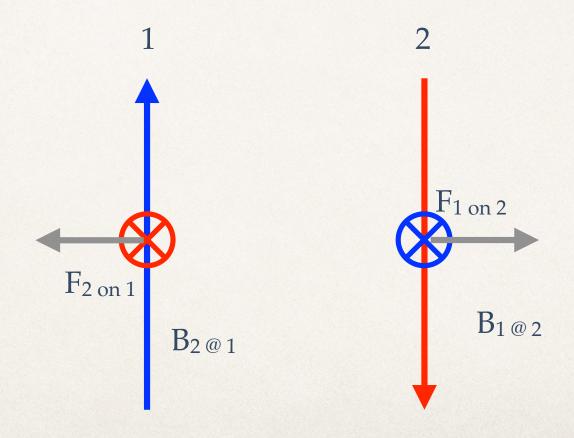
but, which way?





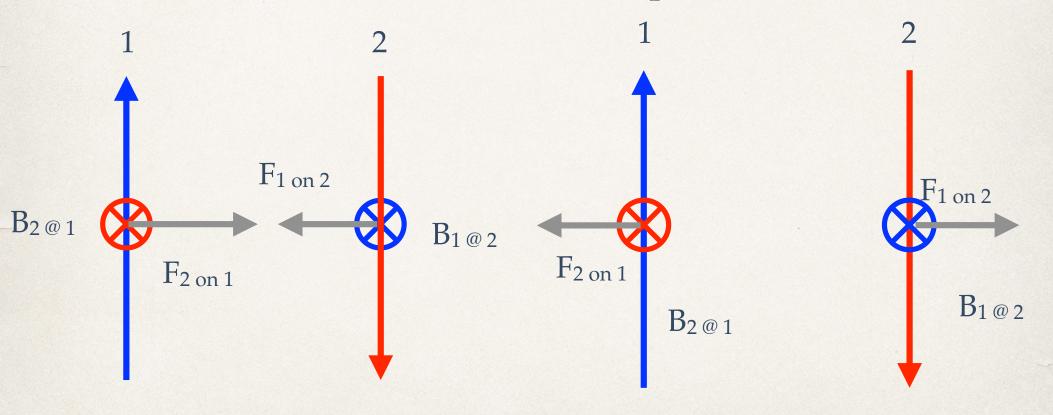




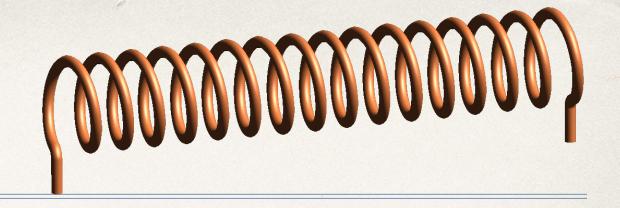


Force: Two Parallel Wires

Which direction is the force on two parallel wires?



Solenoid



What is the magnitude and direction of the magnetic field inside a solenoid that is 10.0 cm long, and 20 coils, and carries a current of 0.75A?

Solenoid

What is the magnitude and direction of the magnetic field inside a solenoid that is 10.0 cm long, and 20 coils, and carries a current of 0.75A?

$$B = \frac{\mu_o NI}{\ell} = \frac{(4\pi x 10^{-7})(20 \text{ Coils})(0.75 \text{ A})}{0.10 \text{ m}}$$

$$B = 0.000188 \text{ T}$$

Solenoid

What is the magnitude and direction of the magnetic field inside a solenoid that is 10.0 cm long, and 20 coils, and carries a current of 0.75A?

If I double the current in a long straight wire, what happens to the strength of the magnetic field produced by that current?

- A. It halves
- B. It remains unchanged
- C. It doubles
- D. None of the above

- * What is the force on a current carrying wire if the angle between the wire and an external magnetic field is 90° (they are perpendicular)?
 - A. The force is zero
 - B. The force varies between zero and a maximum
 - C. The force is a maximum
 - D. The force cannot be determined without the value of the current

- * A wire extends from the floor to the ceiling. You are looking from a top-down prospective. If the current travels from the ceiling to the floor, which way will the magnetic field move?
 - A. Clockwise around the wire
 - B. Counter-Clockwise around the wire
 - C. Uniformly to the right
 - D. Uniformly to the left

What is the maximum force on a 10.0 cm wire carrying a 0.25A current in a 5.0 Tesla magnetic field?

A. 0.00 N

B. 0.13 N

C. 12.5 N

D. More information required

- In the Right-Hand Rule #2, your thumb represents which of the following?
 - A. The direction of force
 - B. The direction of current
 - C. The direction of magnetic field
 - D. The direction of the electric field

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