

PHY 1120 - Dr. Rowley

Chapter 25 - Light: Geometrical Optics

Summer 2020

What do you see?

- ❖ You stand in a windowless room that has no lights of any kind. The room has a chair in the middle of the room and framed pictures on one wall. The door has insulation all the way around so all the cracks are sealed.
- ❖ What do you see?

The Ray Model

- ❖ Light must have a source
- ❖ Light travels as rays, in straight lines, in all directions from the source.
- ❖ Light can be absorbed, reflected, or refracted
- ❖ We can only see objects that produce light or objects that reflect light.

Vanta Black: What's Happening?



Vanta Black

- ❖ Almost (99+%) all light incident on the model coated in Vanta Black is absorbed and almost (< 1%) no light is reflected. So, there is no light available to enter your eye to be detected!

Shadows

- ❖ A light is on the ground 20 m from a tall building. A 1.75 m tall person stands half-way between the light and the building. How tall is her shadow on the building?

Law of Reflection

$$\theta_i = \theta_r$$

- ❖ Always works with reflection
 - ❖ True with both specular and diffuse reflection
- ❖ Angles always measured with respect to the **normal**
 - ❖ a normal is line, perpendicular to the surface, at the point of reflection

Law of Reflection

- ❖ A light ray hits the surface of a planar mirror at an angle of 27° with respect to the surface. Find the angle of reflection and angle of incidence.

$$\theta_i = \theta_r = 63^\circ$$

Reflection

- ❖ What's the speed of light after the reflection?
 - A. Greater than $3.00 \times 10^8 \text{ m/s}$
 - B. Equal to $3.00 \times 10^8 \text{ m/s}$
 - C. Less than $3.00 \times 10^8 \text{ m/s}$
 - D. $-3.00 \times 10^8 \text{ m/s}$ (because of the change in direction)

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Law of Reflection

- ❖ You stand 7.0 m from a wall and hold a laser pointer at a height of 1.6 m. You point it at a mirror on the floor 2.7 m from your feet. Where does the spot appear on the wall?

Index of Refraction

- ❖ Snell's Law describes refraction of light as it passes from one medium to the next.
- ❖ Happens @ the boundary between the surfaces.

$$c = n_1 \cdot v_1$$

$$n_1 \cdot \sin(\theta_1) = n_2 \cdot \sin(\theta_2)$$

1 = incident
2 = refracted

Index of Refraction

$$n_{\text{air}} = 1.00$$

$$n_{\text{water}} = 1.333$$

- ❖ Light passes from **air to water** and has a incident angle of 30° , what is the refracted angle?

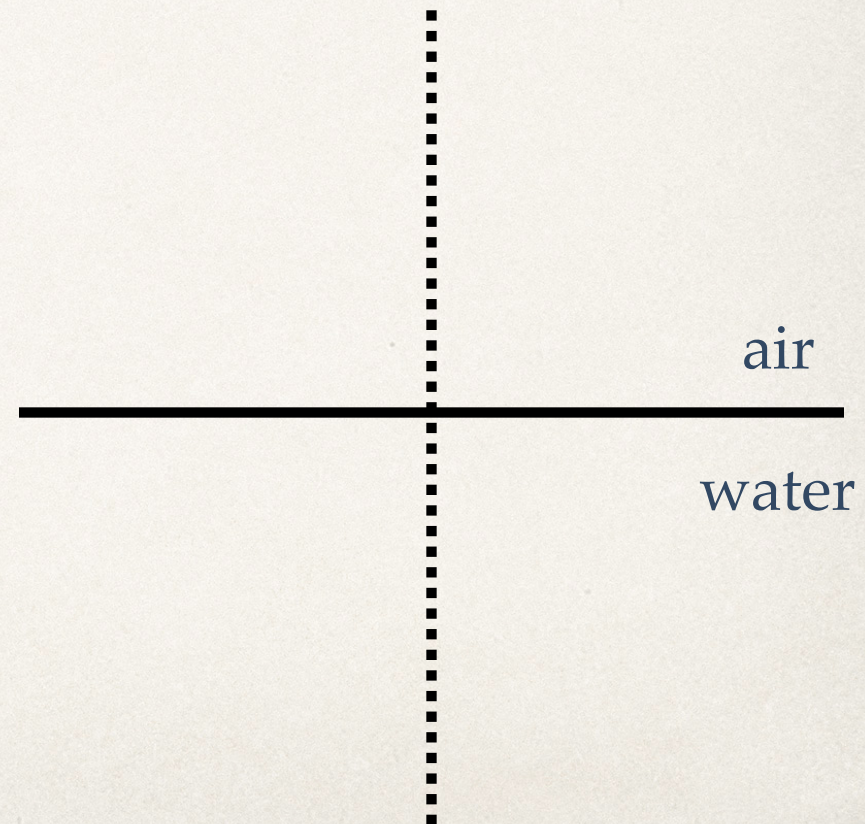
$$n_1 \cdot \sin(\theta_1) = n_2 \cdot \sin(\theta_2)$$

$$1.00 \cdot \sin(30^\circ) = 1.333 \cdot \sin(\theta_2)$$

$$\frac{1.00 \cdot \sin(30^\circ)}{1.333} = \sin(\theta_2)$$

$$\theta_2 = \sin^{-1}(0.3751)$$

$$\boxed{\theta_2 = 22.0^\circ}$$



Index of Refraction

$$n_{\text{air}} = 1.00$$

$$n_{\text{water}} = 1.333$$

- ❖ Light passes from **water to air** and has a incident angle of 30° , what is the refracted angle?

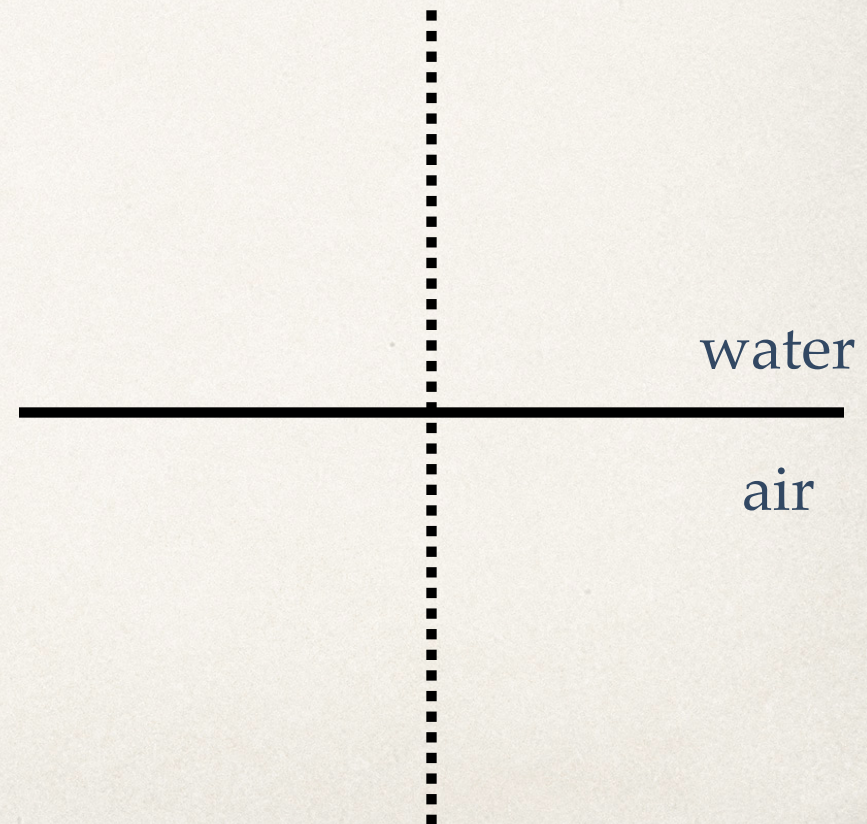
$$n_1 \cdot \sin(\theta_1) = n_2 \cdot \sin(\theta_2)$$

$$1.333 \cdot \sin(30^\circ) = 1.0 \cdot \sin(\theta_2)$$

$$\frac{1.333 \cdot \sin(30^\circ)}{1.0} = \sin(\theta_2)$$

$$\theta_2 = \sin^{-1}(0.6665)$$

$$\boxed{\theta_2 = 41.8^\circ}$$



Index of Refraction

- ❖ How does light behave when passing from low- n to high- n materials?

It bends towards the Normal.

- ❖ How does light behave when passing from high- n to low- n materials

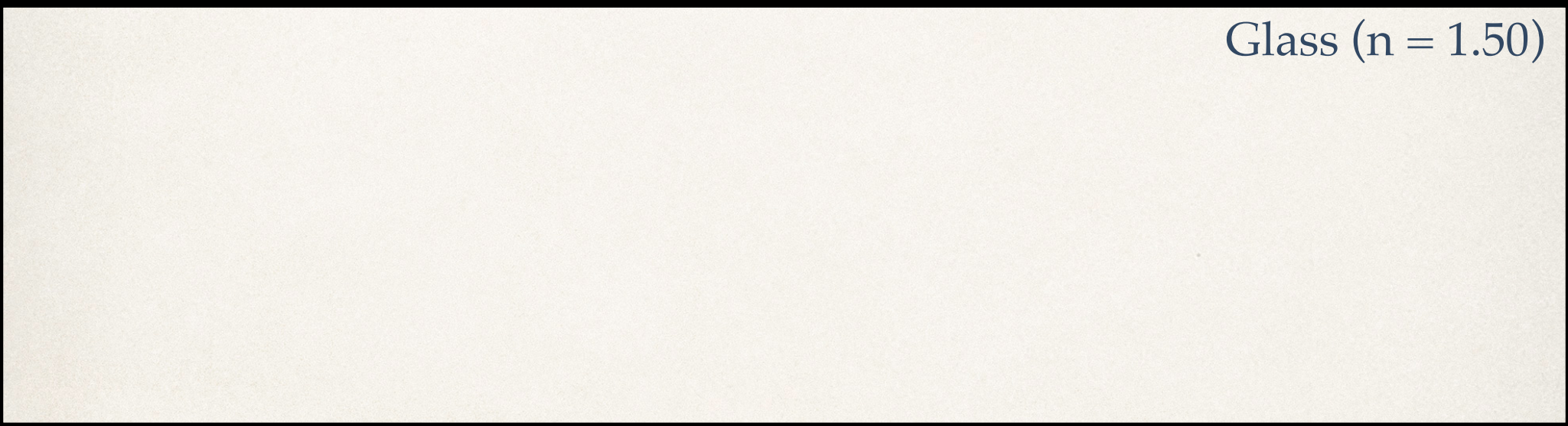
It bends away from the Normal.

Group Problem

- ❖ Find the path of light through the rectangular slab of glass if $\theta_i = 60.0^\circ$

Air ($n = 1.00$)

Glass ($n = 1.50$)



Index of Refraction

Glass ($n = 1.50$)

- ❖ Find the path of light through the rectangular slab of glass if $\theta_i = 60.0^\circ$

$$n_1 \cdot \sin(\theta_1) = n_2 \cdot \sin(\theta_2)$$

$$1.00 \cdot \sin(60^\circ) = 1.5 \cdot \sin(\theta_2)$$

$$\frac{1.00 \cdot \sin(60^\circ)}{1.5} = \sin(\theta_2)$$

$$\theta_2 = \sin^{-1}(0.5774)$$

$$\boxed{\theta_2 = 35.3^\circ}$$

$$n_1 \cdot \sin(\theta_1) = n_2 \cdot \sin(\theta_2)$$

$$1.5 \cdot \sin(35.3^\circ) = 1.0 \cdot \sin(\theta_2)$$

$$\frac{1.5 \cdot \sin(35.3^\circ)}{1.0} = \sin(\theta_2)$$

$$\theta_2 = \sin^{-1}(0.8668)$$

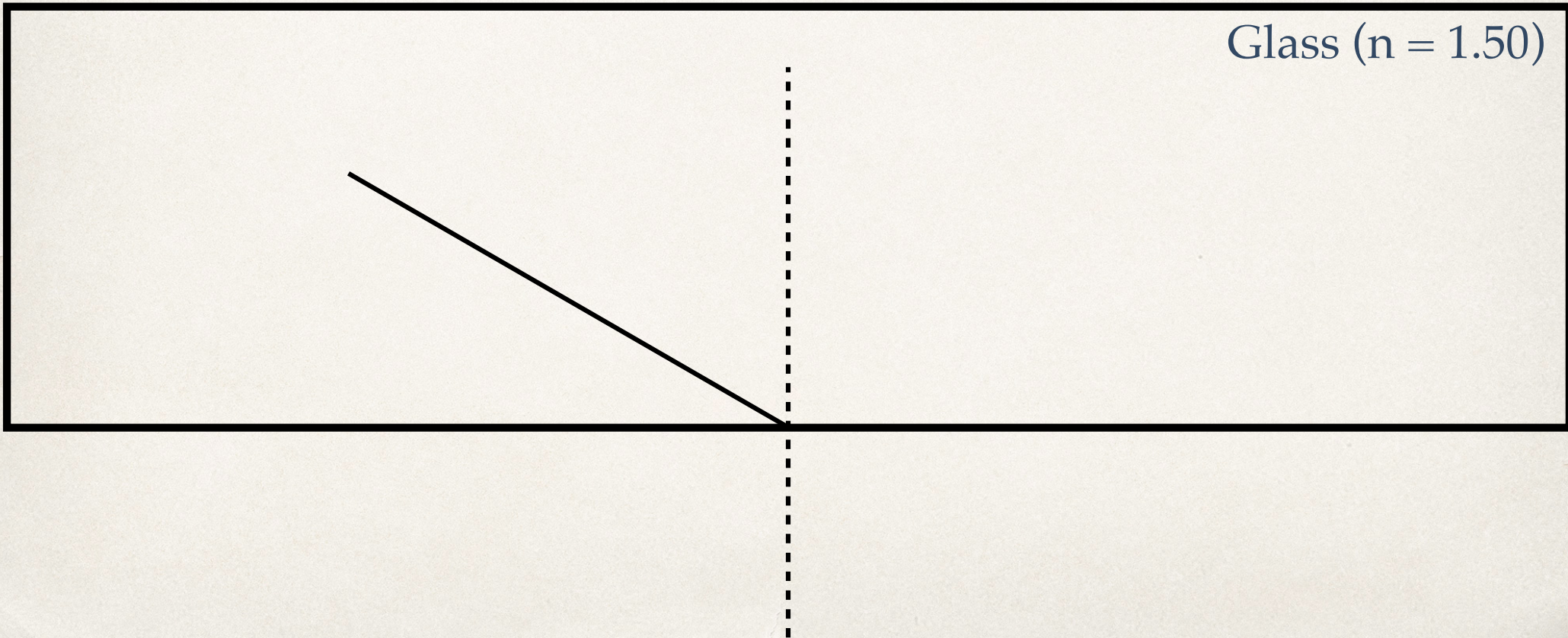
$$\boxed{\theta_2 = 60.0^\circ}$$

Index of Refraction

- ❖ What happens if light hit the Glass-Air boundary at $\theta_i = 60.0^\circ$

Air ($n = 1.00$)

Glass ($n = 1.50$)



Index of Refraction

Glass ($n = 1.50$)

- ❖ Find the path of light through the rectangular slab of glass if $\theta_i = 60.0^\circ$

$$n_1 \cdot \sin(\theta_1) = n_2 \cdot \sin(\theta_2)$$

$$1.5 \cdot \sin(60.0^\circ) = 1.0 \cdot \sin(\theta_2)$$

$$\frac{1.5 \cdot \sin(60.0^\circ)}{1.0} = \sin(\theta_2)$$

$$\theta_2 = \sin^{-1}(1.2990)$$

$$\theta_2 = \text{ERROR???$$

Total Internal Reflection

- ❖ Occurs when θ_2 is equal to, or greater than 90° .
- ❖ Only possible if $n_2 < n_1$
- ❖ Only reflection happens if the incident angle is too large.
- ❖ Critical angle is the angle at which total internal reflection begins.

Critical Angle

- ❖ Occurs when θ_2 is exactly equal to 90° .

$$n_1 \cdot \sin(\theta_1) = n_2 \cdot \sin(\theta_2)$$

$$n_1 \cdot \sin(\theta_1) = n_2 \cdot \sin(90^\circ)$$

$$n_1 \cdot \sin(\theta_1) = n_2$$

$$\theta_1 = \sin^{-1}\left(\frac{n_2}{n_1}\right)$$

$$\boxed{\theta_c = \sin^{-1}\left(\frac{n_2}{n_1}\right)}$$