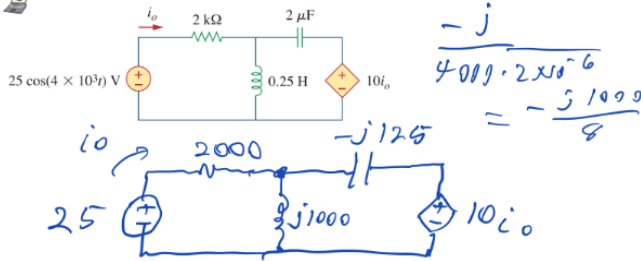


In DC steady state inductors "become" wires, and capacitors "disappear". Super/linked nodes can be made when there is a voltage source between the nodes. To measure current with a multimeter the rods need to be placed together, and voltage one rod on either side of the resistor. Resistors Parallel:  $R_1 \cdot R_2 / R_1 + R_2$ , Series:  $R_1 + R_2$ . Capacitors in s-land are  $1/sC$ , and inductors are  $sL$ . Step response is voltage/s  
Voltage divider formula:  $V_{in}[R_{use}/R_{eq}]$ , Current divider formula:  $I_{in}[R_{eq}/R_{eq}+R_{use}]$   
Phasor:

3. Draw the phasor-domain equivalent circuit for the circuit below.



Thevenin:

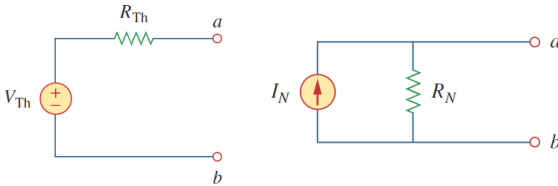


Figure 1: Thevenin equivalent

Figure 2: Norton equivalent

... and we also have the notion of **source transformation** - so that the simple equivalents are completely **interchangeable**.

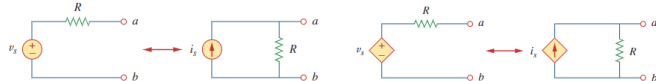
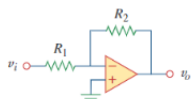


Figure 4.15 Transformation of independent sources.

Figure 4.16 Transformation of dependent sources.

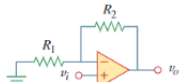
#### Op amp circuit



#### Name/output-input relationship

Inverting amplifier

$$v_o = -\frac{R_2}{R_1} v_i$$



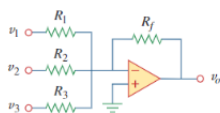
Noninverting amplifier

$$v_o = \left(1 + \frac{R_2}{R_1}\right) v_i$$



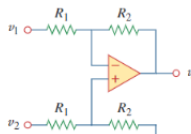
Voltage follower

$$v_o = v_i$$



Summer

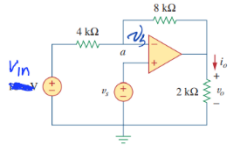
$$v_o = -\left(\frac{R_f}{R_1} v_1 + \frac{R_f}{R_2} v_2 + \frac{R_f}{R_3} v_3\right)$$



Difference amplifier

$$v_o = \frac{R_2}{R_1} (v_2 - v_1)$$

4. Find  $v_o$  = . Do not simplify.



$$\frac{v_s - v_{in}}{4k} + \frac{v_s - v_o}{8k} = 0$$

$$v_o = v_s + \frac{(v_s - v_{in}) \cdot 8k}{4k}$$

$$v_o = 3v_s - 2v_{in}$$

#### Different States:

##### Zero-State Models

t-domain	s-domain	s-domain Impedance
$v(t) = i(t) \cdot R$	$V(s) = I(s) \cdot R$	$Z_R = R$
$v(t) = \frac{1}{C} \int_{t_0}^t i(\tau) d\tau$	$V(s) = \frac{I(s)}{sC}$	$Z_C = \frac{1}{sC}$
$v(t) = L \frac{di(t)}{dt}$	$V(s) = Ls \cdot I(s)$	$Z_L = s \cdot L$

##### Steady-State Impedance Models

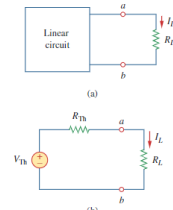
s-domain	Steady State @ $\omega$ R/s	Steady State @ $f$ Hz
$Z_R = R$	$Z_R = R$	$Z_R = R$
$Z_C = \frac{1}{sC}$	$Z_C = \frac{1}{j\omega C}$	$Z_C = \frac{1}{j2\pi f C}$
$Z_L = s \cdot L$	$Z_L = j\omega \cdot L$	$Z_L = j2\pi f \cdot L$

#### Op Amps:

##### Test Load Procedure:

1. With the circuit *in-situ* and energized,
2. Measure the open-circuit voltage, obtain  $V_{Th} = V_{OPEN}$ .
3. Apply a reasonable load  $R_{LOAD}$  within range of the system specs (**NEVER A SHORT!**)
4. Measure the voltage,  $V_{LOAD}$ .
5. We can then find:

$$R_{Th} = -\frac{V_{OPEN} - V_{LOAD}}{I_{OPEN} - I_{LOAD}} = \frac{V_{OPEN} - V_{LOAD}}{I_{LOAD} - 0} = \frac{V_{OPEN} - V_{LOAD}}{V_{LOAD}/R_{LOAD}}$$

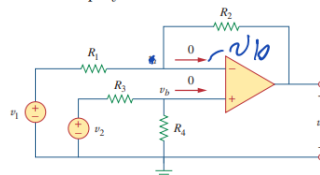


#### Closed-box system<sup>^</sup>

1. Replace *all* independent sources with symbolic representations such as  $V_{in}$  or  $I_{in}$
2. Add a "test-load" resistor  $R_L$  across the specified terminals,  $a - b$ .
3. Use circuit analysis techniques to determine  $V_{a-b}$  in terms of  $V_{in}$  and  $R_L$ .
4. The result will be of the form:  $V_{a-b} = \text{Input}_1 \cdot H_1 + \text{Input}_2 \cdot H_2$  with  $R_L$  in the expressions for the transfer functions.
5. Compute  $V_{a-b}$  as  $R_L \rightarrow \infty$  to obtain  $V_{Th} = V_{a-b}|_{R_L \rightarrow \infty} = \text{Input}_1 \cdot H_1^* + \text{Input}_2 \cdot H_2^*$ .
6. If asked, find  $V_{Th}$  for specific values of  $V_{in}$  or  $I_{in}$ .
7. To find  $R_{Th}$ , select a second reasonable value for  $R_{LOAD}$
8. Compute the voltage,  $V_{LOAD} = V_{a-b}|_{R_L=R_{LOAD}}$ .
9. Then find:

$$R_{Th} = \frac{V_{Th} - V_{LOAD}}{V_{LOAD}/R_{LOAD}}$$

3. Write a node equation you would use to find  $v_o$ . Include any conveniently-labeled voltages. Do not simplify or solve.



$$\frac{(v_o - v_1)}{R_1} + \frac{(v_o - v_2)}{R_2} = 0$$

$$v_o = \frac{v_2 \cdot R_4}{R_3 + R_4}$$

< Open-Box system

## Transiate Responses: S-domain

$$v_{in}(t) \xleftrightarrow{\mathcal{L}} V_{in}(s) \longrightarrow \boxed{H(s)} \longrightarrow V_{in}(s) \cdot H(s) = V_{out}(s) \xleftrightarrow{\mathcal{L}^{-1}} v_{out}(t)$$

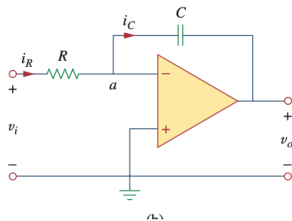
Figure 1: Transient Response Procedure for Zero-State Systems

Note: This is exactly the same procedure as for sinusoidal steady-state except we apply the  $s$ -domain input function to the transfer function  $H(s)$ !

1. Replace all independent sources with symbolic representations such as  $V_{in}(s)$
2. Employ  $s$ -domain impedance models
3. Analyze the circuit using appropriate techniques to find the output:  $V_{out}(s)$ , or whatever output function is dictated by the problem
4. Find the transfer function:  $H(s) = \frac{V_{out}(s)}{V_{in}(s)}$ , or whatever input-output function is dictated by the problem
5. Find the output  $V_{out}(s) = H(s) \cdot V_{in}(s)$ , where  $V_{in}(s) \xleftrightarrow{\mathcal{L}} v_{in}(t)$
6. Find the output  $v_{out}(t) \xleftrightarrow{\mathcal{L}^{-1}} V_{out}(s)$  using the inverse Laplace transform solver  
 $v_{out}(t) = \text{ilaplace}(V_{out}(s))$
7. Plot  $v_{out}(t)$  to observe the response of the system to that input

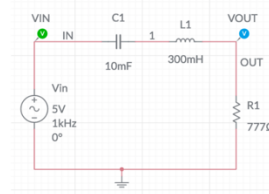
## Misc

3. This circuit is a realization of (choose one): a) High-pass filter, b) Low-pass filter, c) Band-pass filter.



## more phasor/

1. Find the transfer function  $H(s) = \frac{V_{OUT}}{V_{IN}}$ . Do not simplify or compute.



$$H(s) = \frac{777}{777 + 300e^{-3}s + \frac{1}{10e^{-3}s}}$$

2. An analysis of a certain circuit yields transfer function  $H(s) = \frac{V_o}{V_{in}}$ . If

$$V_{in}(t) = 20 \cos(100t + 0.3)$$

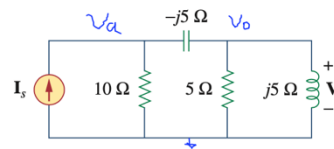
and

$$H(j \cdot 100) = 0.6 \angle 0.2$$

Find  $v_o(t)$  =

$$v_o(t) = 20 \cdot 0.6 \cos(100t + 0.3 + 0.2)$$

4. Write a node equation at  $v_o$ . Do not write any other equations. Do not solve.



$$\frac{v_o}{5} + \frac{v_o}{j5} + \frac{(v_o - v_a)}{-j5} = 0$$

Sorry about the 5's.