

SOLUTION

R Setting	Gain (V/V)			Totals	Averages
	Sample 1	Sample 2	Sample 3		
4	7.8	8.1	7.9	23.80	7.933
3	5.2	6.0	4.3	15.50	5.167
2	4.4	6.9	3.8	15.10	5.033
1	2	1.7	0.8	4.500	1.500
				58.90	4.908

$$\sum_{i=1}^a \sum_{j=1}^n y_{ij}^2 = 359.3$$

$$N = an = 4 \cdot 3 = 12$$

This is actual data from one of Joe Tritschler's audio engineering experiments. Use Analysis of Variance (ANOVA) to test the null hypothesis that the treatment means are equal at the  $\alpha = 0.05$  level of significance. Fill in the ANOVA table.

Source of Variation	Sum of Squares	Degrees of Freedom	Mean Square	$f_0$
Treatments	62.55	3	20.85	21.80
Error	7.65	8	0.9563	-
Total	70.20	11	-	-

(+1)  
everything  
on  
table

$$SS_T = 359.3 - \frac{58.90^2}{12} = 70.20$$

$$d.o.f.(T) = 4 - 1 = 3$$

$$SS_{Tr} = \frac{23.80^2 + 15.50^2 + 15.10^2 + 4.500^2}{3} - \frac{58.90^2}{12} = 62.55$$

$$d.o.f.(Tr) = 4 - 1 = 3$$

$$SS_E = 70.20 - 62.55 = 7.65$$

$$d.o.f.(E) = 4(3-1) = 8$$

$$MS_{Tr} = \frac{62.55}{3} = 20.85$$

$$MS_E = \frac{7.65}{8} = 0.9563$$

$$f_0 = \frac{20.85}{0.9563} = 21.80$$

$$f_{critical} = f_{.05, 3, 8} = 4.07$$

$f \gg f_{critical} \therefore \text{reject } H_0$

(+1)

Use Fisher's Least Significant Difference to determine which, if any, pairs of resistance settings significantly affect attenuation at  $\alpha = 0.05$ .

$$LSD = t_{.025, 8} \sqrt{\frac{2 \cdot 0.9563}{3}} = 2.306 (+)$$

$$= 1.841 (+)$$

$$\begin{aligned} 4 \text{ vs. } 3 &: |7.933 - 5.167| = 2.766 \\ 3 \text{ vs. } 2 &: |5.167 - 5.033| = 0.1340 \\ 2 \text{ vs. } 1 &: |5.033 - 1.500| = 3.533 \end{aligned}$$

< LSD (+)

$$\begin{aligned} 4 \text{ vs. } 2 &: |7.933 - 5.033| = 2.900 \\ 3 \text{ vs. } 1 &: |5.167 - 1.500| = 3.667 \end{aligned}$$

$$4 \text{ vs. } 1: |7.933 - 1.500| = 6.433$$

(+)

(+)

all pairs show significance except 3 vs. 2

(+)