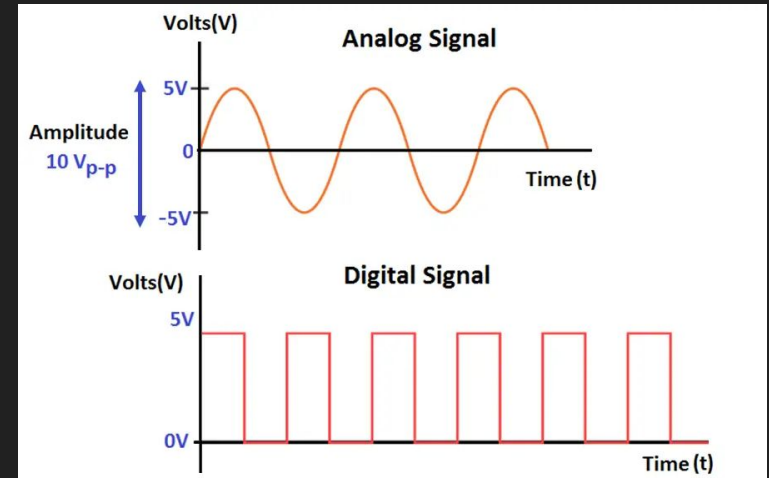
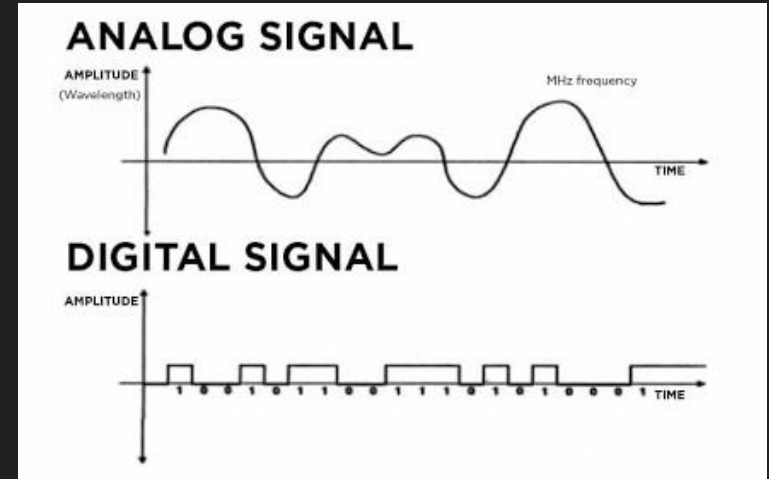


05 - Analog to Digital Converter (ADC)

CEG 4330/6330 - Microprocessor-Based Embedded Systems
Max Gilson

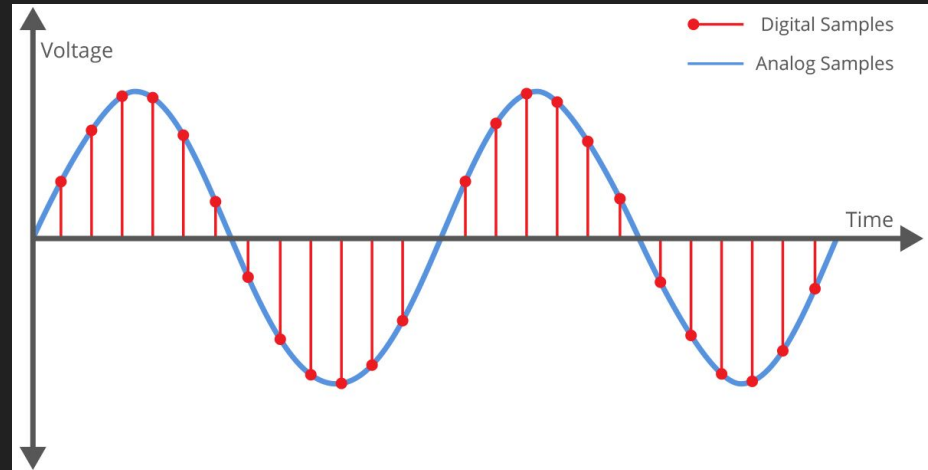
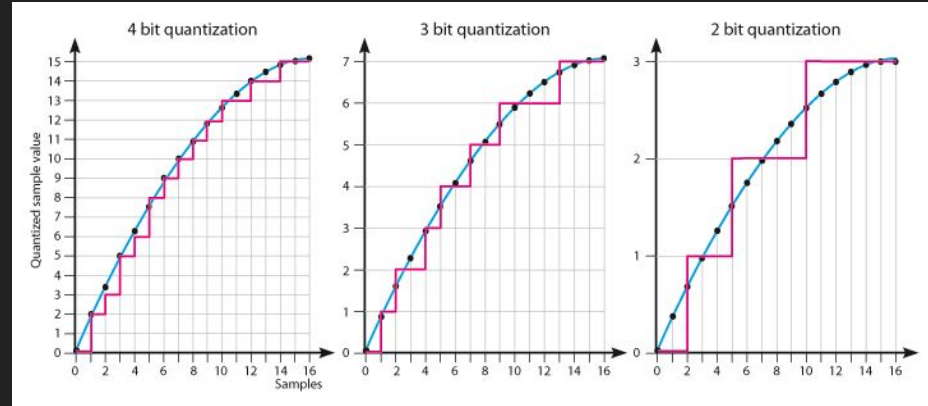
Analog vs Digital

- Digital signals can be HIGH and LOW
 - Arduino HIGH and LOW is 5V and 0V (ground)
- Analog signals are not limited to HIGH and LOW
 - Can be any voltage between HIGH and LOW or even negative



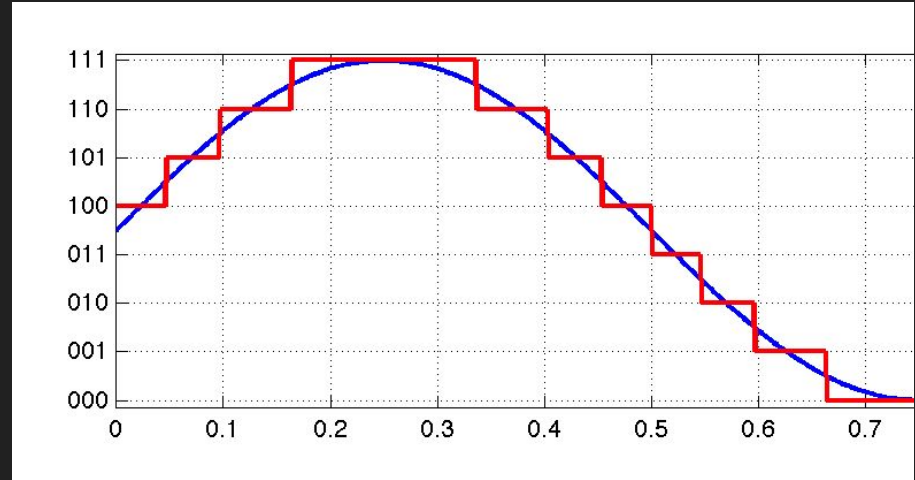
Sampling

- To measure an analog signal with a digital computer, the computer must sample the analog signal periodically
- Each sample is recorded at a frequency and with n-bit quantization
 - Using low frequency or low quantization results in poor signal conversion



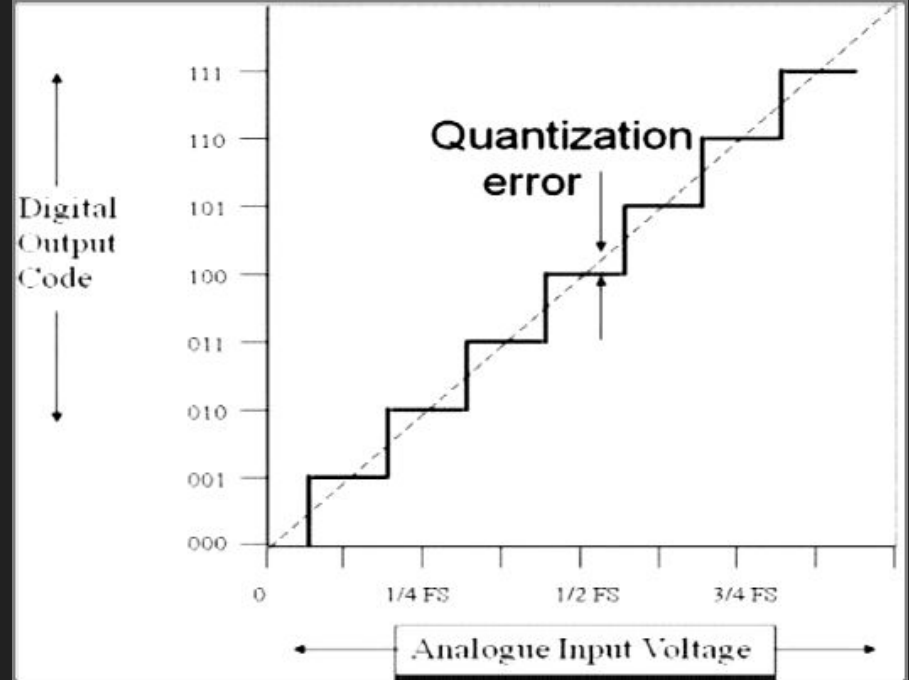
Quantization

- Higher quantization provides higher resolution of digital conversion
- Lower quantization is cheaper but creates a more “chunky” digital conversion
- Sometimes you must make a design trade off for accuracy vs cost



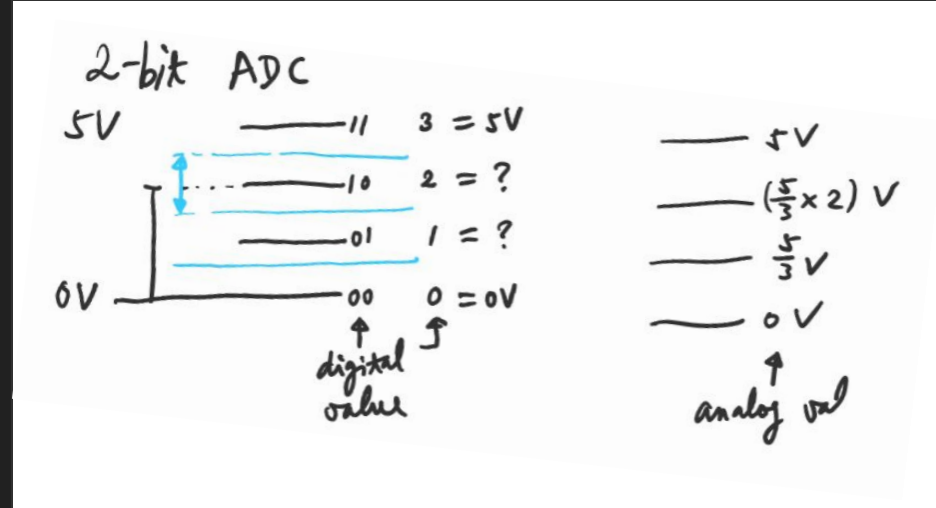
Quantization Error

- Quantization error, is the difference between the actual signal's value and the digital value
- Higher quantization provides less error
- Depends on thresholds between discrete digital values



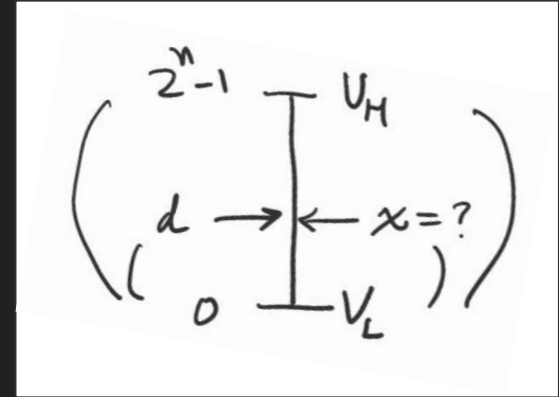
Quantization Mapping

- How do we translate bits into a value?
- Assume 2-bit ADC with 5V maximum:
 - 11: $(5/3) \times 3 = 5.00\text{V}$
 - 10: $(5/3) \times 2 = 3.33\text{V}$
 - 01: $(5/3) \times 1 = 1.67\text{V}$
 - 00: $(5/3) \times 0 = 0.00\text{V}$



Quantization Mapping (cont.)

- For n-bit ADC:
 - $2^n - 1$ = max digital value (integer)
 - 0 = min digital value (integer)
 - V_{max} = max analog value (voltage)
 - V_{min} = min analog value (voltage)



- To calculate the analog value:

where d is the measured ADC integer
and x is the calculated analog value

$$\frac{d}{2^n - 1} = \frac{x - V_{min}}{V_{max} - V_{min}}$$

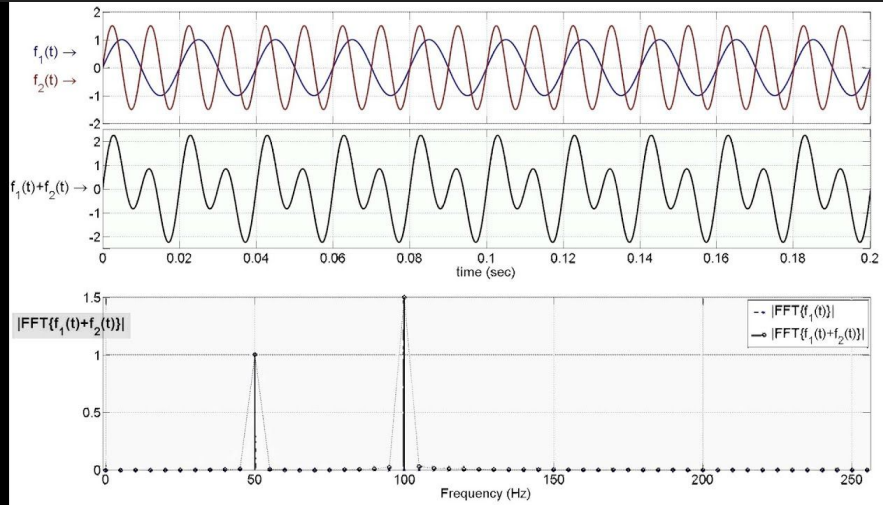
$$x = V_{min} + \frac{V_{max} - V_{min}}{2^n - 1} d$$

Quantization Mapping (cont.)

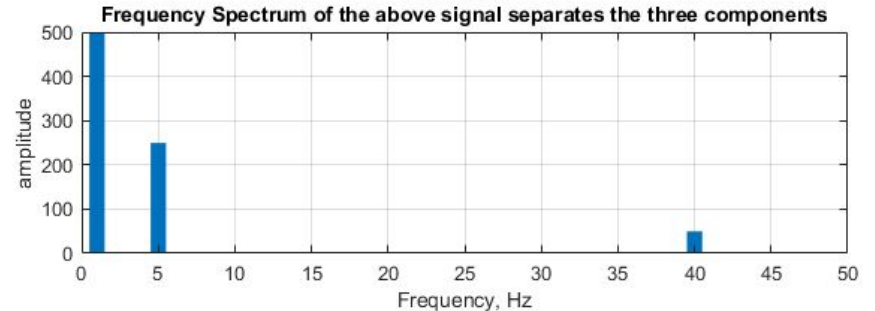
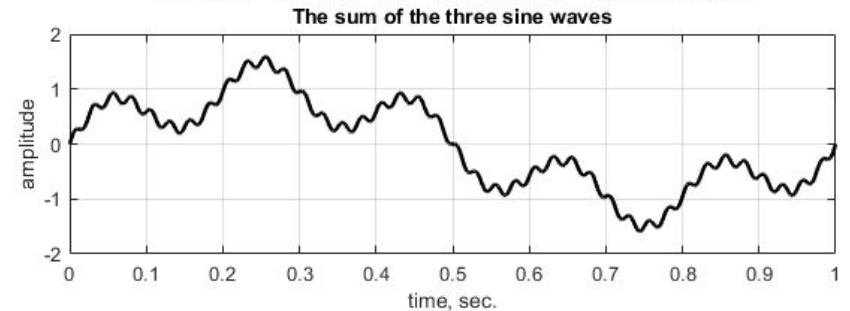
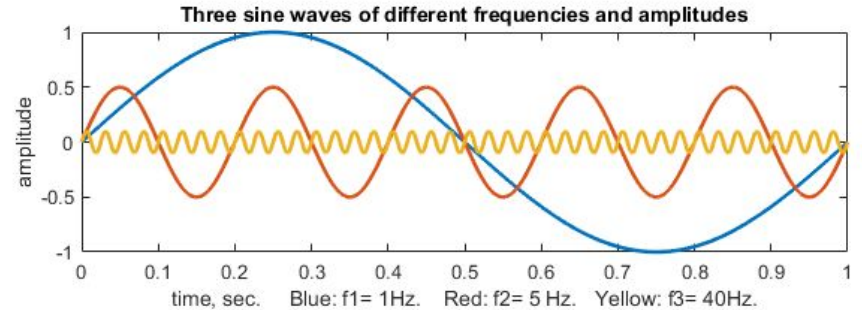
- Arduino `map()` function makes this very easy:
 - `map(value, fromLow, fromHigh, toLow, toHigh)`
 - `value`: the number to map
 - `fromLow`: the lower bound of the value's current range
 - `fromHigh`: the upper bound of the value's current range
 - `toLow`: the lower bound of the value's target range
 - `toHigh`: the upper bound of the value's target range
- Does not provide decimal

Understanding Fast Fourier Transform (FFT)

- Fast Fourier Transform (FFT) is a way of representing a signal in the frequency domain
- It shows magnitudes (or strengths) of frequencies for a given signal
- The x-axis represents frequency
- The y-axis represents magnitude



Understanding Fast Fourier Transform (FFT) (cont.)

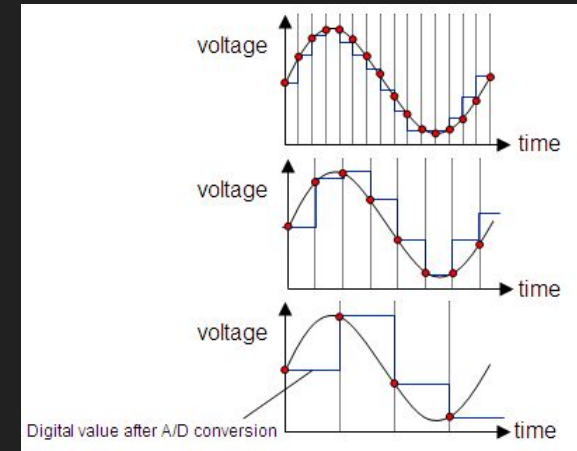
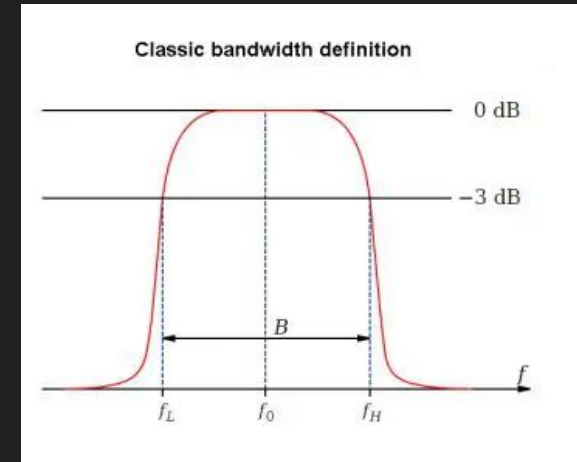


You've Probably Seen FFTs Before!



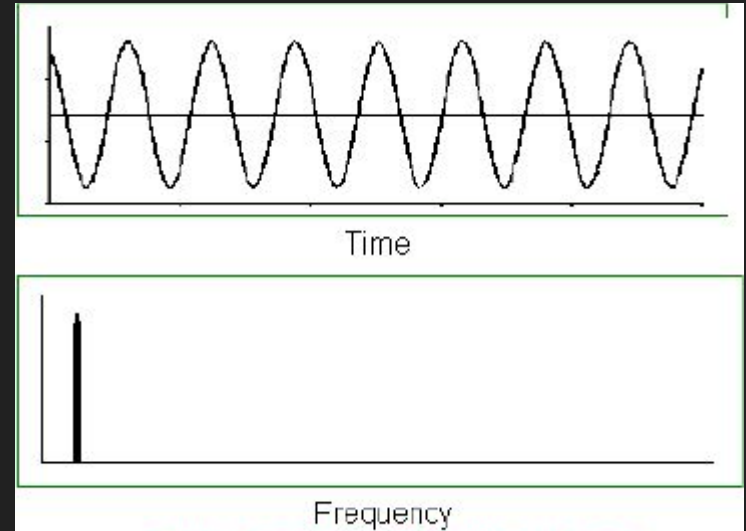
Nyquist Rate and Sampling Rate

- Nyquist Rate = $2B$
 - Where B is the bandwidth of the signal
- Sampling Rate must be greater than Nyquist Rate to fully recover signal
- Example:
 - Bandwidth = 10 KHz
 - Nyquist Rate = 20 KHz
 - Sampling Rate > 20 KHz



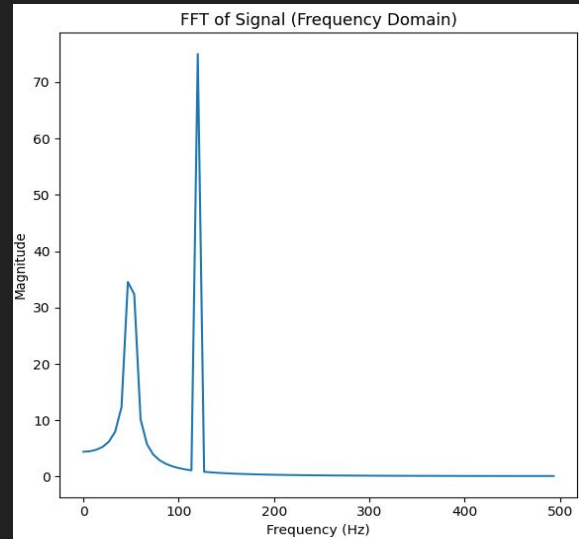
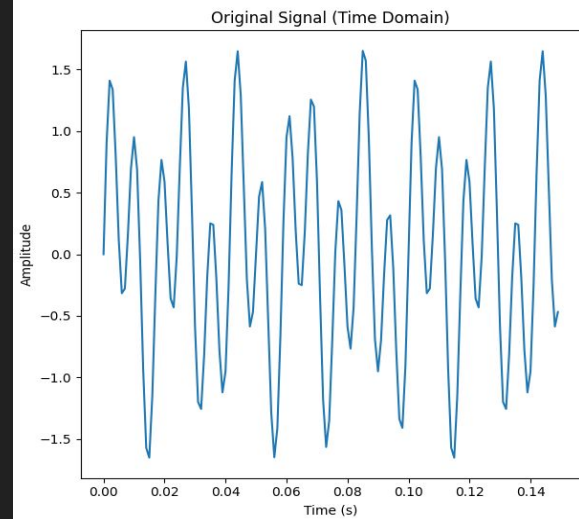
Choosing a Sampling Frequency

- Assume an ideal sine wave at 1 Hz
- Nyquist Rate = 2 Hz
- Sampling Frequency > 2 Hz
- Pick a sampling frequency that fully recovers the signal
 - > 2 Hz minimum
 - 3 Hz
 - 4 Hz
 - 1000 Hz



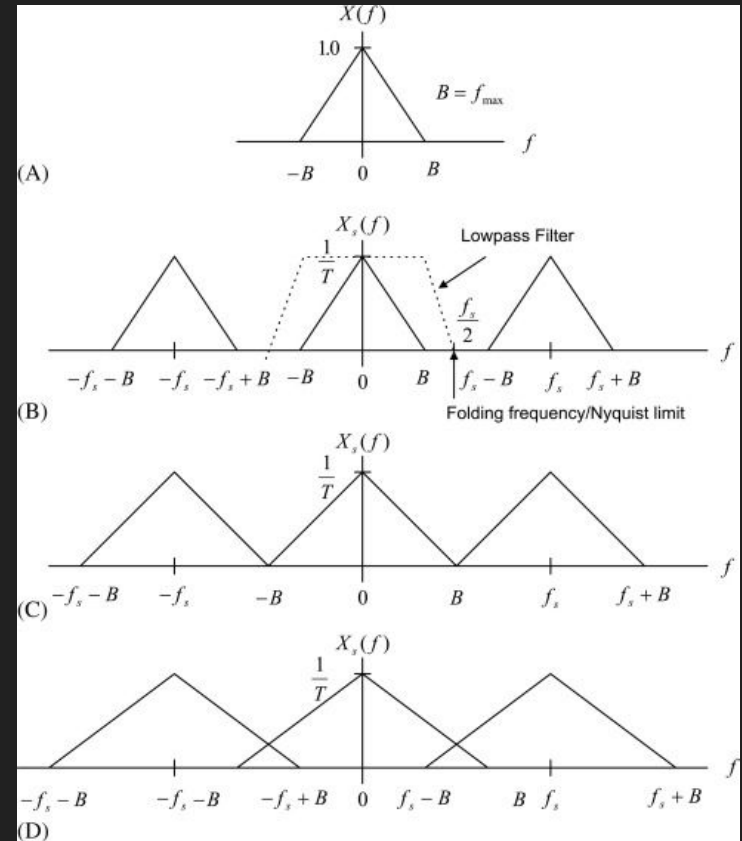
Finding the Bandwidth

- With a signal that has multiple frequency components, we consider the highest significant frequency to be the bandwidth
- First, perform an FFT
- Second, find the highest frequency, select this as B
- Third, select a sampling frequency $> 2B$
- In this example, $B = 120$ Hz and we can select a sampling frequency of > 240 Hz



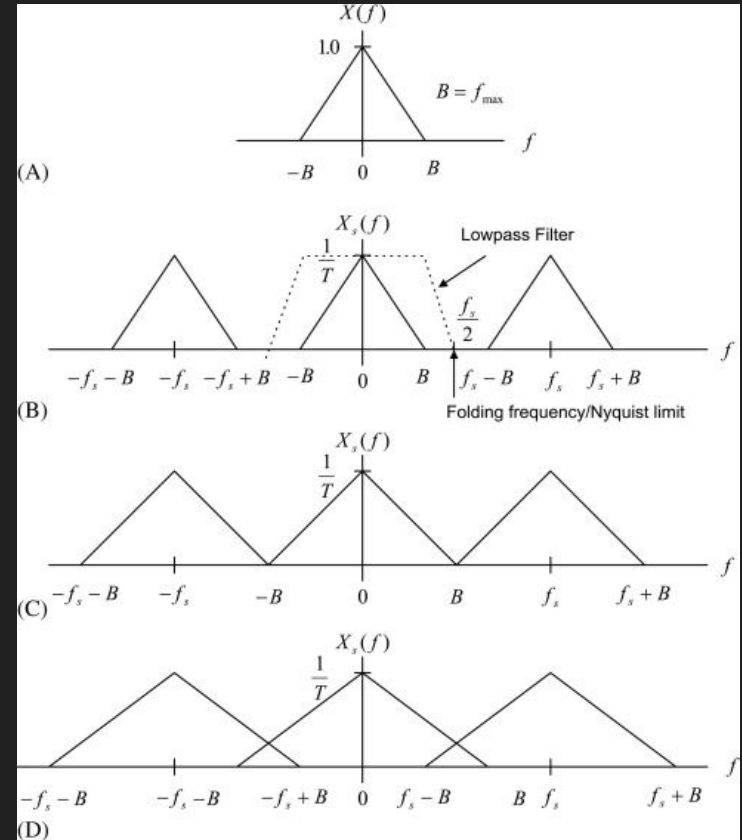
Oversampling vs Undersampling

- A: shows the signals bandwidth in the frequency domain where B is the bandwidth
- B: shows oversampling
 - $f_s > 2B$
- C: sampling at $2B$ Hz
 - $f_s = 2B$
- D: shows undersampling
 - $f_s < 2B$



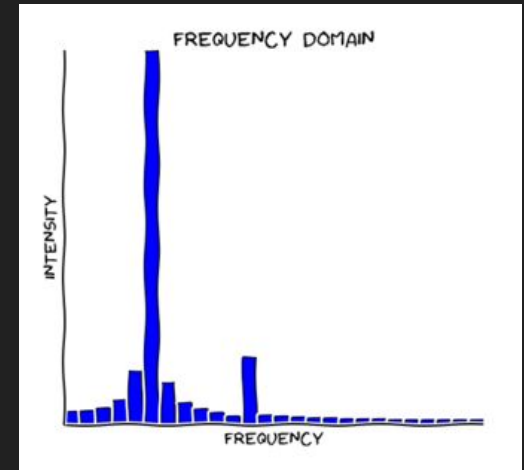
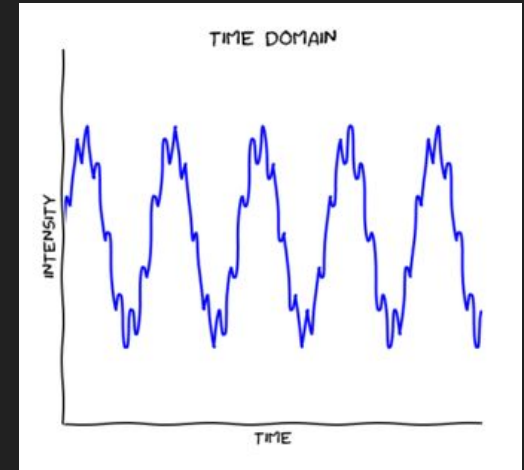
Oversampling vs Undersampling (cont.)

- Just by sampling a signal, frequencies are replicated at $n \cdot f_s$ where $n = 0, 1, 2, \dots$
- Since we have these replicated frequencies, choosing a sampling rate $> 2B$ is required otherwise we'll lose signal clarity



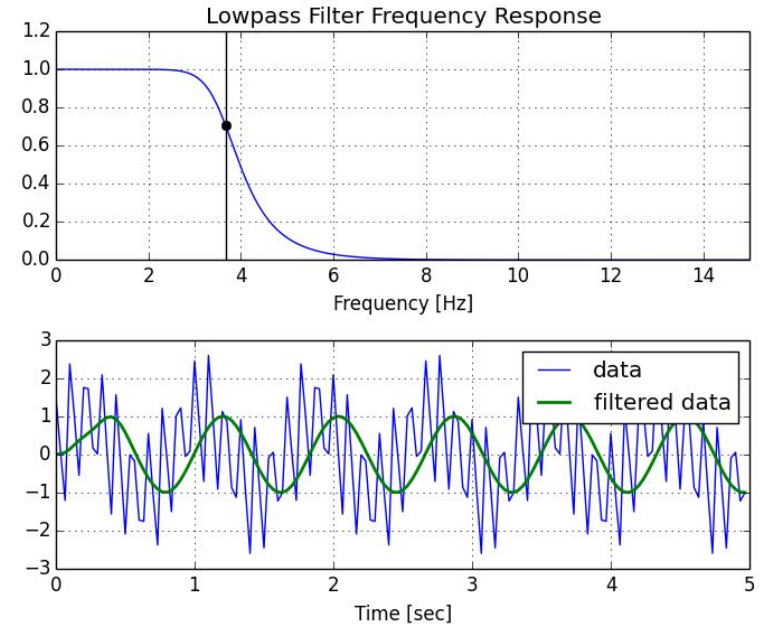
Bandwidth is Never Ideal

- There will always be some amount of noise in your signal
- This noise can be seen in the frequency domain
- To help fight noise, we can use a low pass filter tuned to B frequency to prevent noise during ADC



Low Pass Filters

- Low pass filters only “pass” the low frequencies to the output
- Allows us to “filter” or weaken the higher frequency components before sending to ADC
- This allows us to convert only the data or frequencies that are important (not noise)

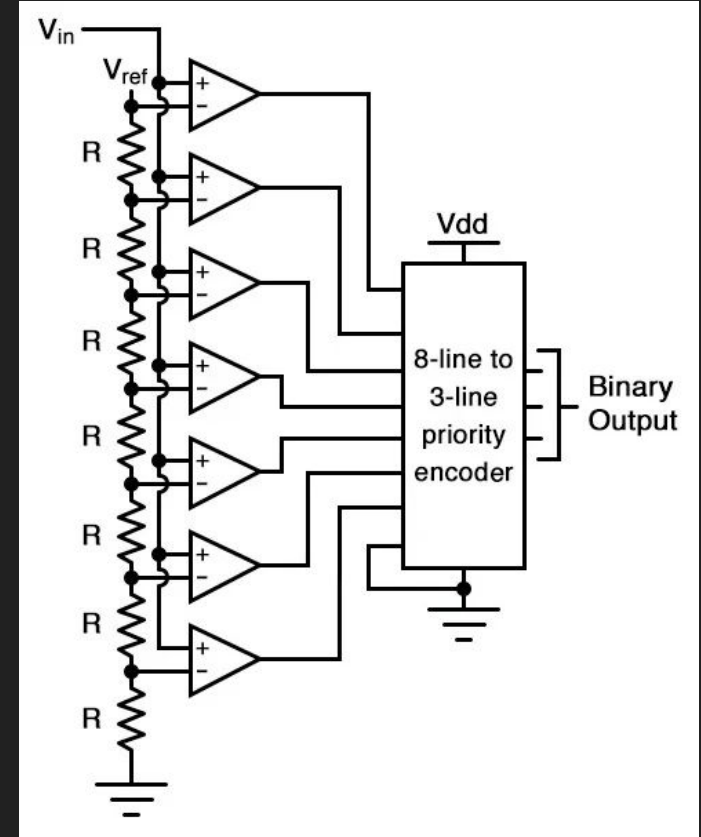


How to Design an ADC

- Comparators:
 - Can use comparators to check each boundary of quantization threshold
 - For $2^{10}-1$ thresholds, 1023 comparators are required
 - Very fast but expensive
- Successive Approximation (used by Arduino):
 - Generate an analog signal iteratively, and compare each iteration to the signal value
 - Check if the value is above or below the current MSB and move to the next value
 - Very slow but cheap

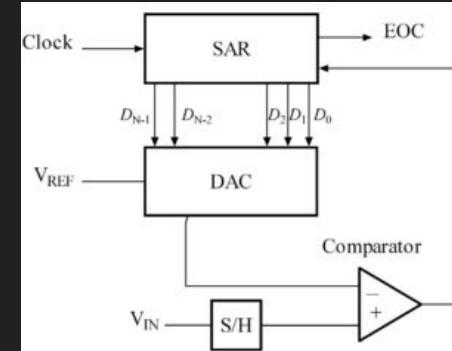
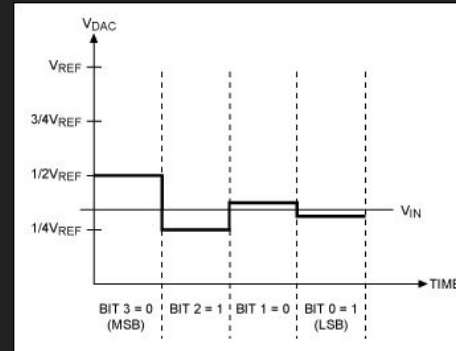
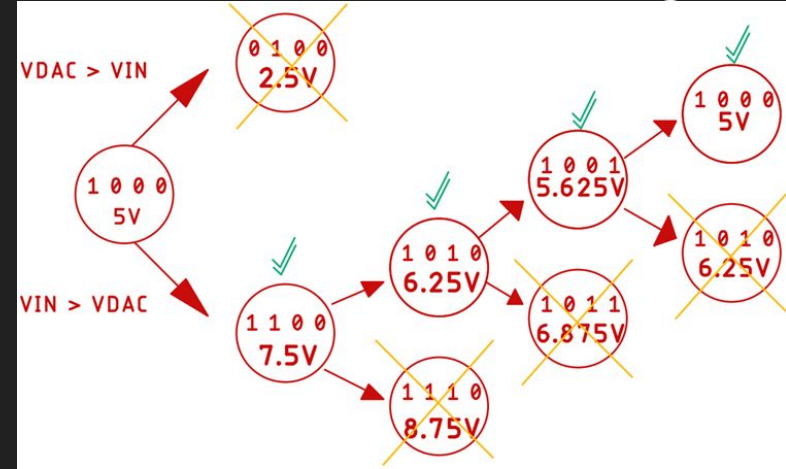
How Comparators Convert to Digital

- Comparators are lined up, and fed different threshold voltages
- The outputs of the comparators are fed into an encoder to convert the threshold values to a digital value
- This requires a lot of hardware but offers great performance
- For $2^{10}-1$ thresholds, 1023 comparators are required



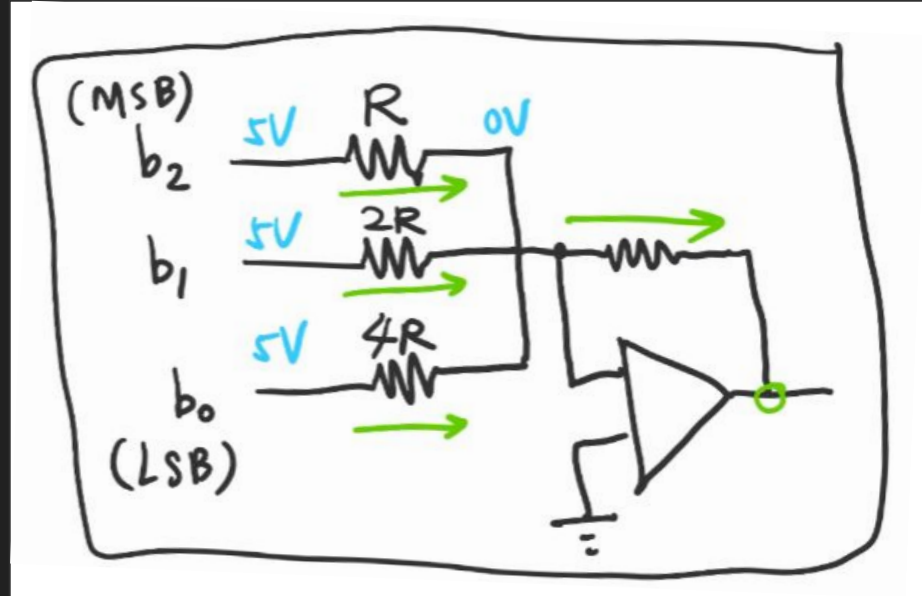
How Successive Approximation Converts to Digital

- Compare the input signal to the digital value if the MSB is set
- If input signal is greater, set the bit and continue with next MSB
- If input signal is less, clear the bit and continue to with next MSB



Designing a DAC for Successive Approximation

- Using an operational amplifier, you can “sum” the bits of a digital output to produce an analog signal that is the sum of weighted currents
- Weighting:
 - Bit 0: 1
 - Bit 1: 2
 - Bit 3: 4
- Very cheap to produce



Arduino ADC

- Arduino UNO:
 - 10-bit ADC
 - 0-5V input
 - 6 analog channels (each shares 1 ADC)
- Uses Successive Approximation

Arduino ADC Sample Code

```
int analogPin = A3; // potentiometer wiper (middle terminal) connected to analog pin 3
                    // outside leads to ground and +5V
int val = 0; // variable to store the value read

void setup() {
  Serial.begin(9600);      // setup serial
}

void loop() {
  val = analogRead(analogPin); // read the input pin
  Serial.println(val);        // debug value
}
```


analogRead() Is Not Always Best

- Sometimes you need to record multiple samples in a row
- Sometimes you need to capture samples very fast
- `analogRead()` is a function, is slow, and only captures 1 value whenever it is called
- Uses polling
 - Notice the while loop!

analogRead() Library Code

```
int analogRead(uint8_t pin)
{
    if (pin >= 14) pin -= 14; // allow for channel or pin numbers

    // set the analog reference (high two bits of ADMUX) and select the
    // channel (low 4 bits). this also sets ADLAR (left-adjust result)
    // to 0 (the default).
    ADMUX = (analog_reference << 6) | (pin & 0x07);

    // without a delay, we seem to read from the wrong channel
    //delay(1);

    // start the conversion
    sbi(ADCSRA, ADSC);

    // ADSC is cleared when the conversion finishes
    while (bit_is_set(ADCSRA, ADSC));

    // ADC macro takes care of reading ADC register.
    // avr-gcc implements the proper reading order: ADCL is read first.
    return ADC;
}
```

ADC Register Control

- ADCSRA
 - Enable ADC
 - Start Conversion
 - Auto Trigger
 - Trigger ADC on a timer or pin
 - Allows you to choose your own sampling frequency
 - Free running is fastest possible frequency
 - ADC Prescaler Select (128 default in init())
 - Conversion takes multiple clock cycles
 - First 25 clock cycles, then 13 clock cycles
 - Default: $125 \text{ Khz} / 13 \text{ avg. cycles} = 9.6 \text{ Khz}$ sampling frequency
 - ADC Interrupt
 - Interrupt enable and interrupt flags

ADC Register Control (cont.)

- ADMUX
 - ADC Reference Selection
 - Select between 5V reference voltage or other
 - Choosing 3.3V reference voltage, gives higher resolution readings from 0V to 3.3V
 - Left Justified
 - Shifts the ADCL bits left into the ADCH
 - Forces the 8 MSB to be in the ADCH register
 - Mostly used in memory constrained situations
 - ADMUX
 - Select analog pin to input into ADC

ADC Interrupt

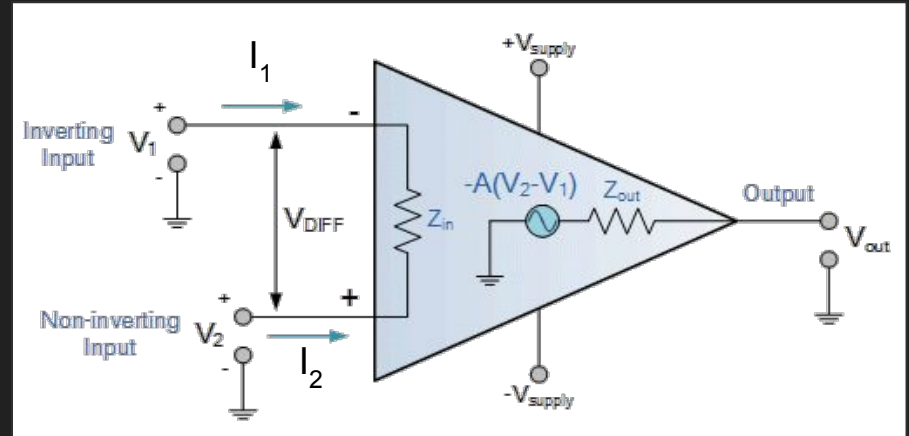
- ADC Conversion Complete Interrupt
 - Use: `ADC_vect`
- Triggers ISR when a conversion on ADC is complete
- Much faster than using `analogRead()`
 - Allows for immediate processing of ADC value after conversion is complete, without waiting for conversion

Signal Conditioning

- Often times, our analog signal is not in a perfect range of 0V to 5V
 - Example: 1S Lipo Battery (same battery in smartphones) has a range of 3.2V to 4.2V
 - 3.2V is 0% battery
 - 4.2V is 100% battery
- Sometimes, the voltage range is too small to be measured in 0V to 5V
 - Example: unprocessed microphone output may be 0.001V to 0.100V
 - This is too small for the Arduino to measure consistently
- Signal conditioning will allow us to convert the sensor's output range to the ADC's input range
 - Amplify and offset voltage

Signal Conditioning using Operational Amplifier

- Operational Amplifier (Op Amp)
 - We can make different circuits:
 - Non-inverting amplifier
 - Inverting amplifier
 - Inverting amplifier with DC offset
- $V_1 = V_2$
- $I_1 = I_2 = 0$
- Ohm's Law:
 - $V = I * R$



Non-Inverting Amplifier

$$V_1 = V_2 = V_{in}$$

$$V_{in} = I_{R2} \cdot R2$$

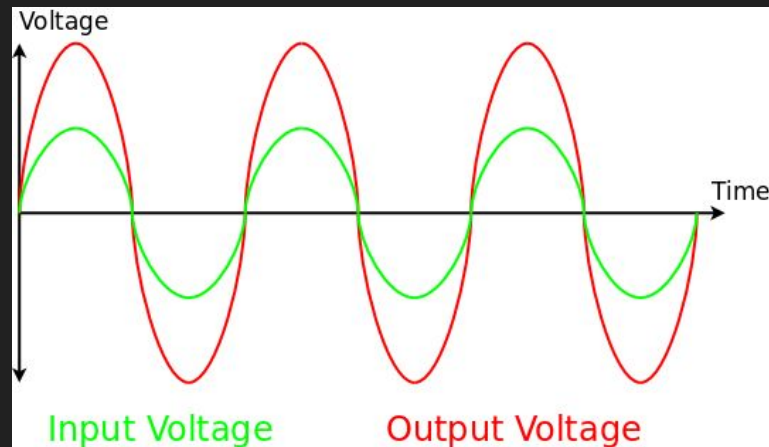
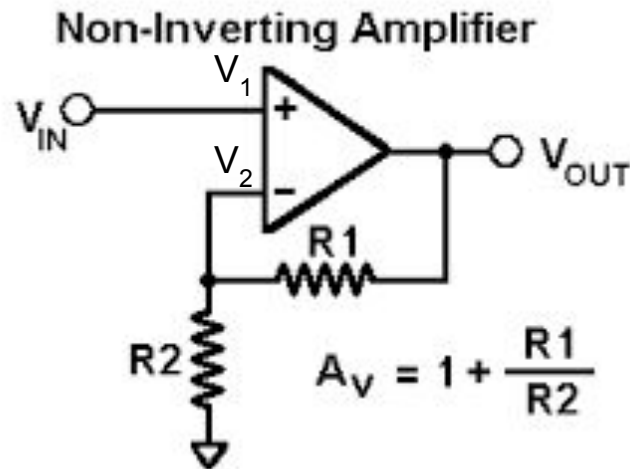
$$I_{R2} = I_{R1} = I$$

$$V_{out} = I \cdot (R1 + R2)$$

$$V_{out} = V_{in} \cdot \frac{R1 + R2}{R2}$$

$$V_{out} = V_{in} \cdot \left(1 + \frac{R1}{R2}\right)$$

$$A_v = 1 + \frac{R1}{R2}$$



Inverting Amplifier

$$V_1 = V_2 = 0$$

$$V_{in} = I_{Ri} \cdot R_i$$

$$I_{Rf} = I_{Ri} = I$$

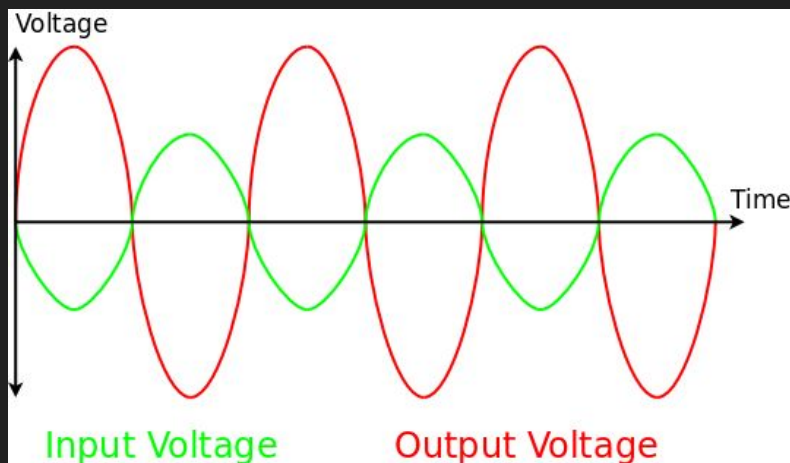
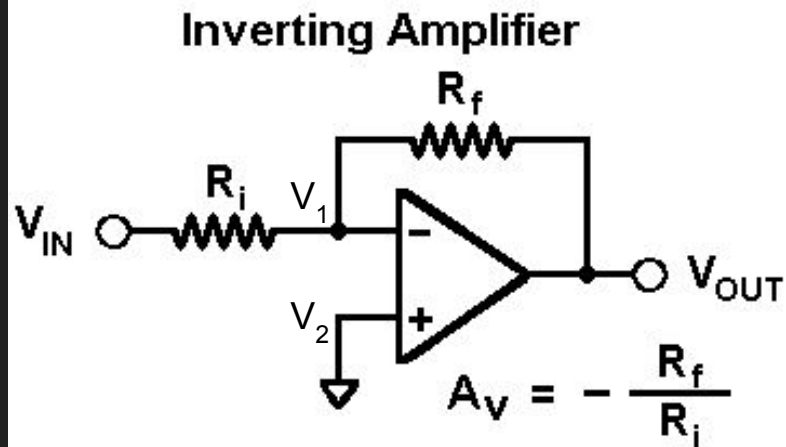
$$V_{Rf} = -V_{out}$$

$$V_{out} = -V_{Rf}$$

$$V_{out} = -(R_f \cdot I)$$

$$V_{out} = -\left(\frac{R_f}{R_i}\right) \cdot V_{in}$$

$$A_v = -\left(\frac{R_f}{R_i}\right)$$



Inverting Amplifier With DC Offset

$$V_1 = V_2 = 0$$

$$V_A = I_{RA} \cdot R_A$$

$$V_B = I_{RB} \cdot R_B$$

$$I_{RA} + I_{RB} = I_{Rf} = I$$

$$V_{Rf} = -V_{out}$$

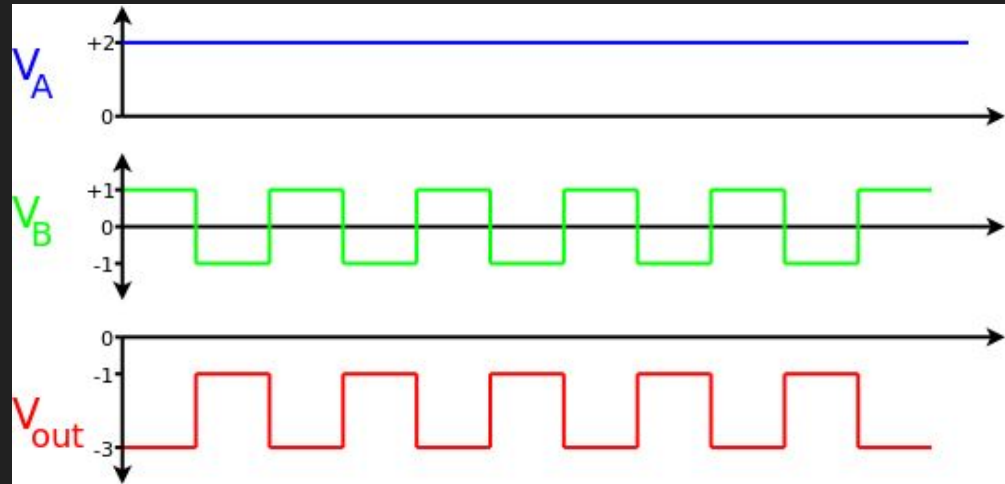
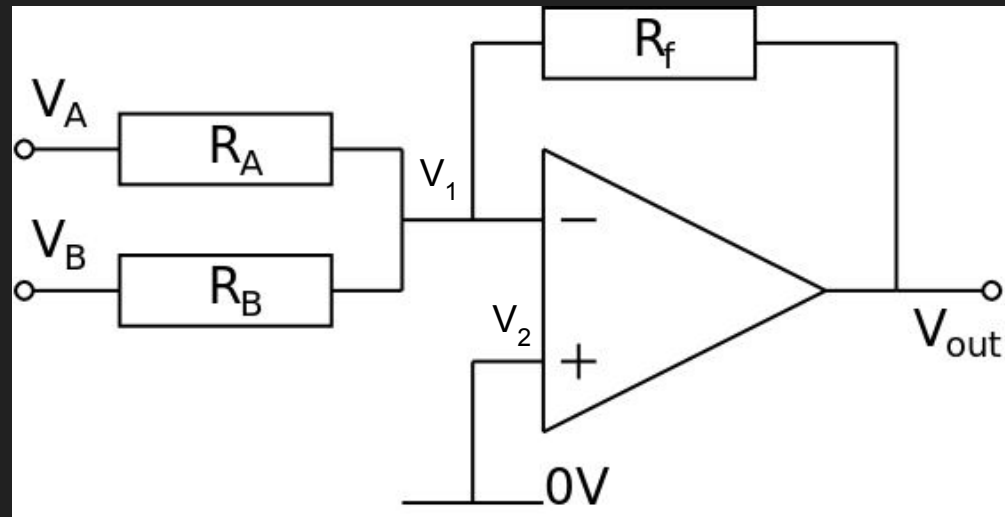
$$V_{out} = -V_{Rf}$$

$$V_{out} = -(R_f \cdot I)$$

$$V_{out} = -(R_f) \cdot (I_{RA} + I_{RB})$$

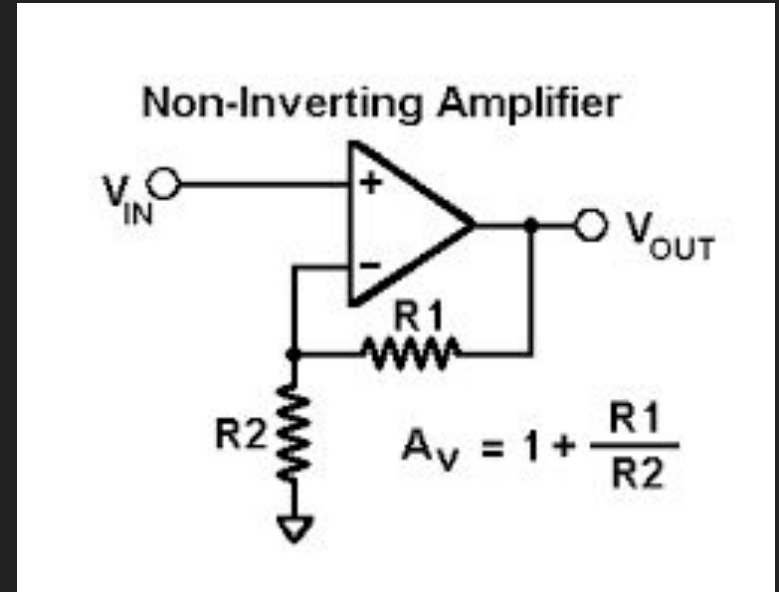
$$V_{out} = -(R_f) \cdot \left(\frac{V_A}{R_A} + \frac{V_B}{R_B} \right)$$

$$V_{out} = -\left(\frac{R_f}{R_A} \right) \cdot V_A + -\left(\frac{R_f}{R_B} \right) \cdot V_B$$



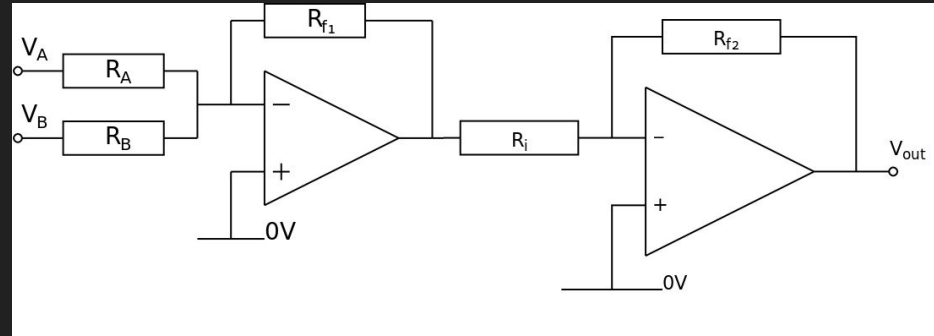
Design Challenge 1

- Given an input signal from 0 mV to 2 mV, create a signal conditioning circuit to measure this signal with the Arduino Uno's 0V to 5V ADC
- Non-inverting amplifier:
- 2500 amplifier gain
- $A_v = \text{gain} = 1 + R1/R2 = 2500$
- $R1/R2 = 2499$
- $R1 = 2,400,000 \Omega = 2,400 \text{ K}\Omega = 2.4 \text{ M}\Omega$
- $R2 = 960 \Omega = 0.960 \text{ K}\Omega$
- $A_v = 1 + (2400000/960) = 2501$



Design Challenge 2

- Given an input signal from -20 mV to 30 mV, create a signal conditioning circuit to measure this signal with the Arduino Uno's 0V to 5V ADC
- Two-stage amplifier:
- 100 amplifier gain
- 2V shift UP after amplifying
- $R_{f1} = R_{f2} = 10\text{ K}\Omega$
- $R_A = R_i = 1\text{ K}\Omega$
- Gain = $10 \times 10 = 100$
- Assume $V_B = 5\text{V}$
 - $R_B = 250\text{ K}\Omega$



Design Challenge 3

- Given an input signal from 10 mV to 20 mV, create a signal conditioning circuit to measure this signal with the Arduino Uno's 0V to 5V ADC
- Two-stage amplifier:
- 500 amplifier gain
- 5V shift DOWN after amplifying
- $R_{f1} = 50\text{ K}\Omega$
- $R_{f2} = 10\text{ K}\Omega$
- $R_A = R_i = 1\text{ K}\Omega$
- $\text{Gain} = 50 \times 10 = 100$
- Assume $V_B = 5\text{V}$
 - $R_B = 10\text{ K}\Omega$

