

**Power Semiconductors Homework Problems**

Summer 2005

Problem 1

- (a) Sketch the symbol and the vertical structure of the IGBT. Briefly state the advantages of the IGBT over the MOSFET for low frequency operation.

[5 marks]

- (b) The IRFPS40N60K power MOSFET (see attached specification sheets on pages 7 to 10) from International Rectifier operates in a boost converter with a dc link voltage  $V_d = 480$  V, and load current  $I_o = 20$  A. The MOSFET is driven by a gate drive IC outputting a square-wave voltage  $v_{GG}$ , of amplitude 0 V to +10 V, in series with an external gate resistance  $R_G = 4.3 \Omega$ . Assume the diode has a 1V forward drop and no reverse recovery.

Useful formula: RC discharge time  $t = -RC \ln \left[ \frac{v_c - (-V_{GG})}{V_{ci} - (-V_{GG})} \right]$

- Determine the following parameters from the data sheet at a junction temperature of 100°C: maximum threshold voltage, minimum forward transconductance, gate-source capacitance, gate-drain capacitance, maximum on-state resistance, maximum gate voltage at the 20 A load current, and maximum conduction drop across MOSFET at 20 A.
- Sketch  $v_{GG}(t)$ ,  $v_{GS}(t)$ ,  $v_{DS}(t)$ , and  $i_D(t)$  during turn-off of the MOSFET. Note the approximate voltage levels on waveforms.
- Calculate the following (a) turn-off delay time  $t_{\text{doff}}$ , (b) voltage rise time  $t_{\text{vr}}$ , and (c) current fall time  $t_{\text{fv}}$  at a junction temperature of 100°C. Sketch the basic switching circuit under analysis in each case.
- Calculate the turn-off energy loss.

[Ans. 5 V, 21 S, 7895 pF, 75 pF, 0.26  $\Omega$ , 6V, 5.2 V, 17.5 ns, 31 ns, 6.2 ns, 0.18 mJ]

[15 marks]

Summer 2004

Problem 2

- (a) Briefly explain reverse recovery in power diodes and sketch the effects of reverse recovery on the turn-on waveforms of the complementary IGBT or MOSFET.

[6 marks]

- (b) The IRFP460 power MOSFET (see attached specification sheets on pages 6 and 7) from International Rectifier operates in a boost converter switching at 20 kHz with a dc link voltage  $V_d = 300$  V, and load current  $I_o = 13$  A. The MOSFET is driven by a gate drive IC outputting a square wave voltage  $v_{GG}$ , of amplitude -5 V to +15 V, in series with an external gate resistance  $R_G = 25 \Omega$ . Assume the diode has a 1V forward drop and no reverse recovery.

Useful formulae: RC discharge time  $t = -RC \ln \left[ \frac{v_c - (-V_{GG})}{V_{ci} - (-V_{GG})} \right]$

- Determine the following parameters from the data sheet at a junction temperature of 80°C: maximum threshold voltage, minimum forward transconductance, gate-source capacitance, gate-drain capacitance, and on-state resistance.
- Sketch  $v_{GG}(t)$ ,  $v_{GS}(t)$ ,  $v_{DS}(t)$ , and  $i_D(t)$  during turn-off of the MOSFET.
- Calculate the following (a) turn-off delay time  $t_{\text{doff}}$ , (b) voltage rise time  $t_{\text{vr}}$ , and (c) current fall time  $t_{\text{fv}}$  at a junction temperature of 80°C. Sketch the switching circuit under analysis in each case.

[Ans. 4 V, 13 S, 3850 pF, 350 pF, 0.43  $\Omega$ , 72.8 ns, 258 ns, 11 ns]

[14 marks]

Summer 2003

Problem 3

An enhancement-mode n-channel vertically diffused power MOSFET operates in a step-up converter switching at 20 kHz, with a dc link voltage  $V_d = 400$  V, and load current  $I_o = 20$  A. The device characteristics are as follows: threshold voltage  $V_{GS(th)} = 4$  V, drain current  $I_D = 20$  A at gate voltage  $V_{GS} = 6$  V, gate-source capacitance  $C_{gs} = 4000$  pF, gate-drain capacitance  $C_{gd} = 400$  pF, and on-state resistance  $R_{DS(on)} = 0.25 \Omega$ . The MOSFET is driven by an ideal voltage-source square wave  $v_{GG}$ , of amplitude 0 V to 15 V, in series with an external gate resistance  $R_G = 25 \Omega$ . Assume the diode has a 1 V forward drop and no reverse recovery.

- (i) Sketch  $v_{GG}(t)$ ,  $v_{GS}(t)$ ,  $v_{DS}(t)$ , and  $i_D(t)$  during turn-on of the MOSFET.

- (ii) Calculate the following times: (a) turn-on delay time  $t_{d(on)}$ , (b) current rise time  $t_{ir}$ , and (c) voltage fall time  $t_{fv}$ . For each of the time durations investigated, sketch the equivalent circuit.

[Ans. 34 ns, 22 ns, 440 ns]

Summer 2002

Problem 4

The IRFP460 power MOSFET from International Rectifier operates in a boost converter switching at 20 kHz with a dc link voltage  $V_d = 400$  V, and load current  $I_o = 20$  A. The MOSFET is driven by a voltage-source square wave  $v_{GG}$ , of amplitude 0 V to 15 V, in series with an external gate resistance  $R_G = 25 \Omega$ . Assume the boost diode has a 1V forward drop and no reverse recovery.

- (a) Sketch  $v_{GG}(t)$ ,  $v_{GS}(t)$ ,  $v_{DS}(t)$ , and  $i_D(t)$  during turn-on of the MOSFET.  
 (b) Determine the following parameters from the data sheet at a junction temperature of 80°C: threshold voltage, forward transconductance, gate-source capacitance, gate-drain capacitance, and on-state resistance.  
 (c) Calculate the following (i) turn-on delay time  $t_{don}$ , (ii) current rise time  $t_{ir}$ , (iii) voltage fall time  $t_{fv}$  and (iv) turn-on energy loss.

[Ans. 4 V, 13 S, 3850 pF, 350 pF, 0.43  $\Omega$ , 33 ns, 15 ns, 363 ns, 1.55 mJ]

Problem 5

An enhancement-mode n-channel vertically diffused power MOSFET operates in a boost converter switching at 20 kHz, with a dc link voltage  $V_d = 300$  V, and load current  $I_o = 10$  A. The device characteristics are as follows: threshold voltage  $V_{GS(th)} = 4$  V, drain current  $I_D = 10$  A at gate voltage  $V_{GS} = 7$  V, gate-source capacitance  $C_{gs} = 1000$  pF, gate-drain capacitance  $C_{ds} = 150$  pF, and on-state resistance  $R_{DS(on)} = 0.5 \Omega$ . The MOSFET is driven by an ideal voltage-source square wave  $v_{GG}$ , of amplitude 0 V to 15 V, in series with an external gate resistance  $R_G = 50 \Omega$ . Assume the diode has a 1V forward drop and no reverse recovery.

- (a) Sketch  $v_{GG}(t)$ ,  $v_{GS}(t)$ ,  $v_{DS}(t)$ ,  $i_D(t)$ ,  $v_{diode}(t)$ , and  $i_{diode}(t)$  during turn-on of the MOSFET.  
 (b) Calculate the following (i) turn-on delay time  $t_{don}$ , (ii) current rise time  $t_{ir}$ , (iii) voltage fall time  $t_{fv}$ .  
 (c) Calculate the following (i) turn-off delay time  $t_{doff}$ , (ii) voltage rise time  $t_{vr}$ , (iii) current fall time  $t_{fv}$ .  
 (d) Calculate the turn-on and turn-off energy losses.  
 (e) Calculate the power dissipation in the MOSFET due to switching and conduction losses.  
 (f) Estimate the MOSFET junction temperature due to turn-on switching loss only, if the MOSFET is bonded to a 70 °C heatsink. The thermal impedance from the heatsink to the junction is  $\theta_{JC} = 0.69$  °C/W.

[Ans. (i) 18 ns (ii) 18 ns (iii) 278 ns, (c) 44 ns (ii) 317 ns (iii) 32 ns (d) 0.46 mJ, 0.53 mJ (e) 15.1 W (f) 100.2 °C]

Summer 2006

Problem 6

- (a) Sketch the symbol and the vertical structure of the MOSFET. Briefly state the advantages of the MOSFET over the IGBT for high-frequency, low-voltage operation.

[5 marks]

- (b) An enhancement-mode n-channel vertically diffused power MOSFET operates in a step-up converter switching at 50 kHz, with a dc link voltage  $V_d = 300$  V, and load current  $I_o = 10$  A. The device characteristics are as follows: threshold voltage  $V_{GS(th)} = 4$  V, drain current  $I_D = 10$  A at gate voltage  $V_{GS} = 7$  V, gate-source capacitance  $C_{gs} = 1000$  pF, gate-drain capacitance  $C_{gd} = 150$  pF, and on-state resistance  $R_{DS(on)} = 0.5 \Omega$ . The MOSFET is driven by a voltage-source square wave  $v_{GG}$ , of amplitude -15 V to +15 V, in series with an external gate resistance  $R_G = 50 \Omega$ . Assume the diode has a 1V forward drop and neglect the reverse recovery.

Useful formulae: RC charge time  $t = -RC \ln \left[ 1 - \frac{v_c - V_{ci}}{V_{GG} - V_{ci}} \right]$  RC discharge time  $t = -RC \ln \left[ \frac{v_c - (-V_{GG})}{V_{ci} - (-V_{GG})} \right]$

- (viii) Sketch  $v_{GG}(t)$ ,  $v_{GS}(t)$ ,  $v_{DS}(t)$ , and  $i_D(t)$  during turn-off of the MOSFET. Note the approximate voltage levels on waveforms.  
 (ix) Calculate the following (i) turn-on delay time  $t_{don}$ , (ii) current rise time  $t_{ir}$ , (iii) voltage fall time  $t_{fv}$ .  
 (x) Calculate the turn-on energy losses.  
 (xi) Estimate the MOSFET junction temperature if the MOSFET is bonded to a 70 °C heatsink. The thermal impedance from the heatsink to the junction is  $\theta_{JC} = 0.5$  °C/W. Assume turn-off energy loss equals the turn-on energy loss, and the conduction loss equals the combined switching loss.

[Ans. 57.7 ns, 18.3 ns, 278 ns, 0.45 mJ, 115 °C]

[15 marks]