

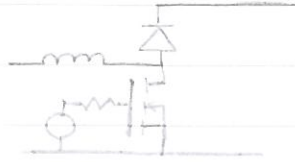
6a)  $V_d = 480V$

$I_o = 20A$

$V_{GS} = 0 \rightarrow 10V$

$R_G = 4.3\Omega$

$V_F = 1V$



i)  $V_{GS(ON) MAX} = 5V$

$g_{FS MIN} = 21S$

$C_{GS} = C_{ISS} - C_{RSS} = 7895 pF$

$C_{GD} = C_{RSS} = 75 pF$

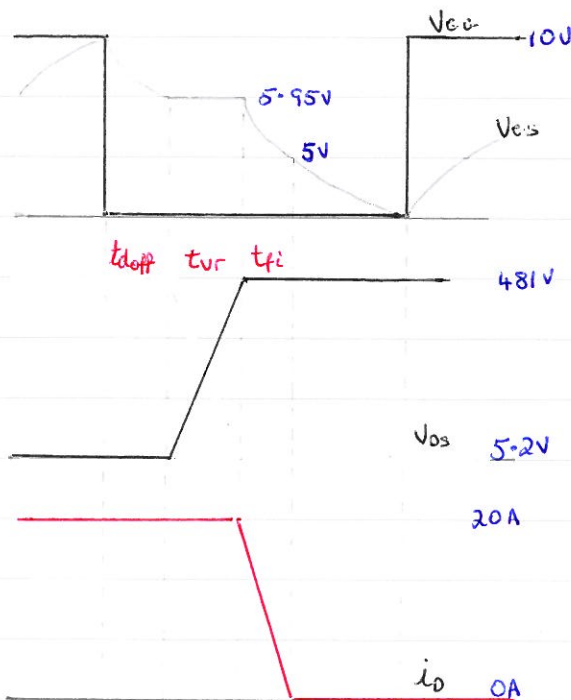
$R_{DS(ON)} @ 100^\circ C = 0.26\Omega$

$V_{GS} @ I_D = 20A = V_{GS(ON) MAX} + \frac{I_D}{g_{FS MIN}}$

$V_{GS MAX} = 5.95V$

$V_{DS MAX} = I_D R_{DS(ON)} = 5.2V$

ii)



iv) Turn-off Energy Loss

$$E_{off} = \frac{1}{2} (V_D + V_F) I_D (t_{vr} + t_{fi}) = 153 \mu J$$

iii)  $t_{doff} = -R_G [C_{GS} + C_{GD}] \ln \left[ \frac{V_{GS} I_D}{V_{GS} - V_{GS(ON) MAX}} \right]$

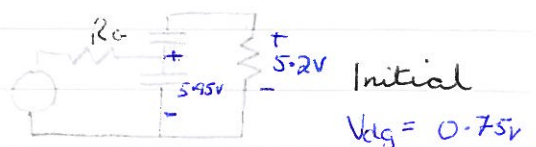
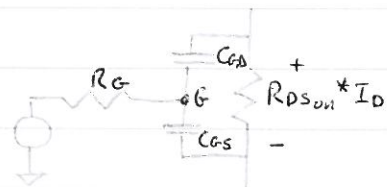
Discharge from 15V  $\rightarrow$  5.95V

$t_{doff} = 17.8 ns$

$t_{vr} = \frac{C_{GS} \Delta V_{GS}}{I_{RG}} \Rightarrow I_{RG} = \frac{V_{GS} I_D}{R_G}$

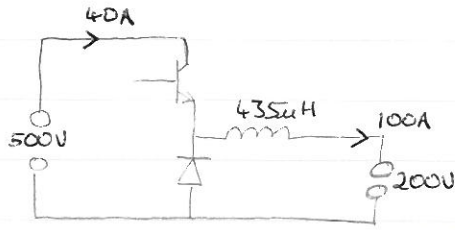
$t_{vr} = 25.79 ns$

$t_{fi} = -R_G [C_{GS} + C_{GD}] \ln \left[ \frac{5}{5.95} \right] = 5.96 ns$



# EE4001 Power Electronics, Drives, Energy Conversion Summer '08

6b)



$$f_{sw} = 10 \text{ kHz} \quad \Delta i_{p-p} = 27.6 \text{ A}$$

$$I_{L \max} = 114 \text{ A}$$

$$I_{L \min} = 86 \text{ A}$$

$$I_{Q \text{ rms}} = 63 \text{ A}$$

$$I_{D \text{ rms}} = 77 \text{ A}$$

$$I_{Q \text{ avg}} = 40 \text{ A}$$

$$I_{D \text{ avg}} = 60 \text{ A}$$

IGBT turn-on @  $I_{L \min}$ , turn-off @  $I_{L \max}$

$$P_{Q \text{ cond}} = V_{CE \text{ on}} I_{Q \text{ avg}} + R_{CE} I_{Q \text{ rms}}^2 = 65 \text{ W}$$

$$P_{Q \text{ (turn-on)}} = f_{sw} E_{on} (.86 \text{ A}) \frac{500}{600} = (10)(12)\left(\frac{5}{6}\right) = 100 \text{ W}$$

$$P_{Q \text{ (turn-off)}} = f_{sw} E_{off} (114 \text{ A}) \frac{500}{600} = 10(17)\left(\frac{5}{6}\right) = 142 \text{ W}$$

$$P_{D \text{ (off)}} = f_{sw} E_{rr} (.86 \text{ A}) \frac{500}{600} = 10(12)\left(\frac{5}{6}\right) = 100 \text{ W}$$

$$P_{D \text{ (cond)}} = V_F I_{D \text{ avg}} + R_F I_{D \text{ rms}}^2 = (0.8 \times 60) + (5.3 \text{ m} \times 77^2) = 79.4 \text{ W}$$

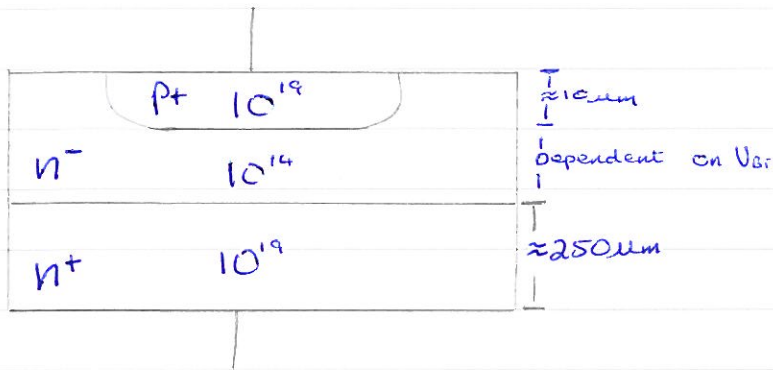
$$P_{Q \text{ (cond)}} = 65 \text{ W}$$

$$P_{Q \text{ (sw)}} = 242 \text{ W}$$

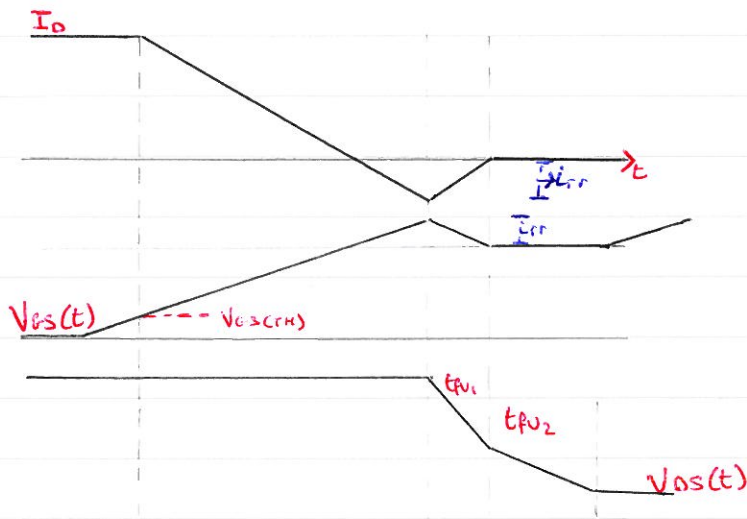
$$P_{D \text{ (cond)}} = 79.4 \text{ W}$$

$$P_{D \text{ (rr)}} = 100 \text{ W}$$

6c)



The  $n^-$  drift region absorbs the depletion layer of the reverse-biased p-n junction. Its width determines the breakdown voltage.



b)

$$f_{sw} = 20 \text{ kHz}$$

$$V_a = 300 \text{ V}$$

$$I_0 = 13 \text{ A}$$

$$V_G \Rightarrow -5 \rightarrow 15 \text{ V}$$

$$R_G = 25 \Omega$$

$$V_f = 1 \text{ V}$$

$$V_{TH \text{ MAX}} = 4 \text{ V}$$

$$g_{fs \text{ MIN}} = 13 \text{ S}$$

$$C_{GS} = C_{LSS} - C_{RSS} = 1850 \text{ pF}$$

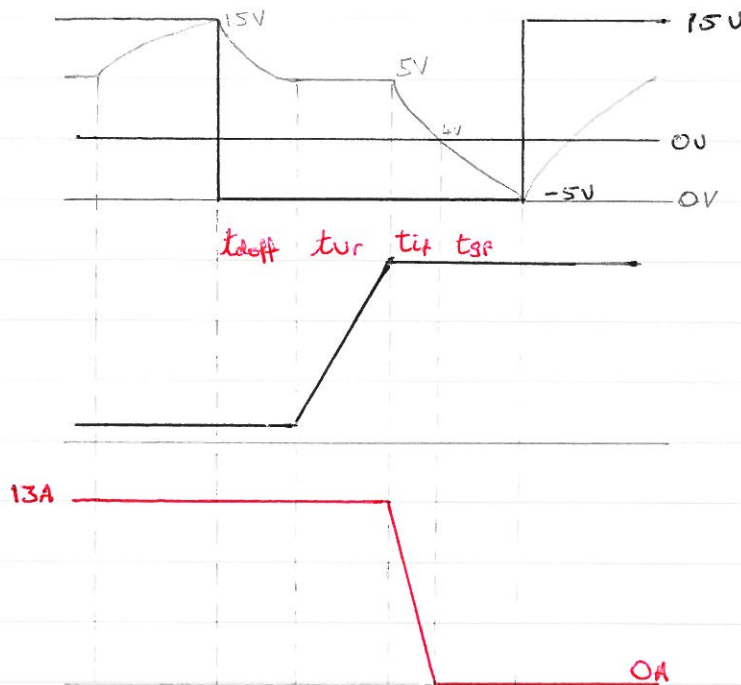
$$C_{GD} = C_{RSS} = 350 \text{ pF}$$

$$R_{DS(on)} @ 80^\circ\text{C} = 1.6 \times 0.27 = 432 \text{ m}\Omega$$

$$V_{GS10} = V_{th} + \frac{I_{DS}}{g_{min}} = 5 \text{ V}$$

$$V_{DSmax} = R_{DS(on)} I_D = 5.6 \text{ V}$$

6. b) ii)

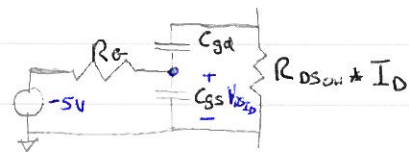


iii)

$$c) t_{doff} = -R_g(C_{gs} + C_{gd}) \ln \left[ \frac{V_{GS_{TH}} - (-V_{GS})}{V_{GS} - (-V_{GS})} \right]$$

$$= -25(4200) \ln \left[ \frac{5+5}{15+5} \right]$$

$$= 72.8 \text{ ns}$$



$$b) t_{ur} = \frac{C_{gd} \Delta V_{gd}}{I_{rg}}$$

$$\Delta V_{gd} = V_{dg} - (V_{ds} - V_{GS_{TH}})$$

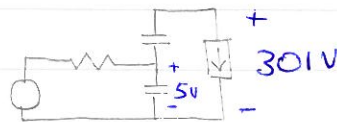
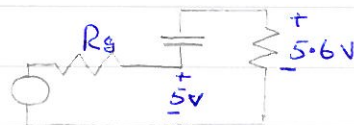
$$= -296 - (-0.6)$$

$$= -295.4 \text{ V}$$

$$I_{rg} = \frac{V_{GS} - V_{GS_{TH}}}{R_g}$$

$$= -0.4 \text{ A}$$

$$t_{ur} = 258 \text{ ns}$$

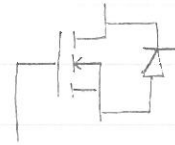
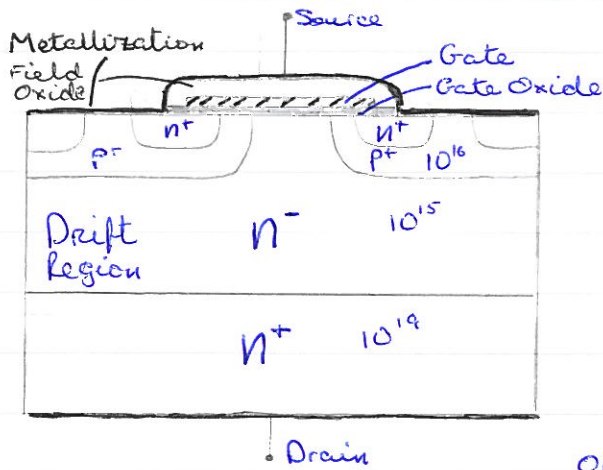


$$c) t_{ti} = -R_g(C_{gs} + C_{gd}) \ln \left[ \frac{V_{GS_{TH}} - (-V_{GS})}{V_{GS} - (-V_{GS})} \right]$$

$$= 11 \text{ ns}$$



5a)

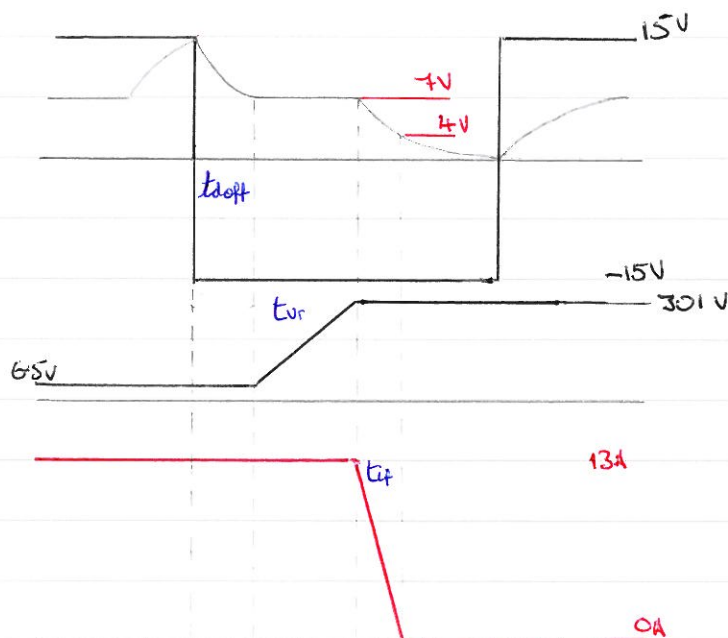


The MOSFET is more suitable for low frequency operation than an IGBT as an IGBT has higher turn-on and turn-off energy losses.

The MOSFET is more suitable at low voltage as the  $C-E$  drop of an IGBT is approximately constant across voltages, while the  $R_{DS(on)}$  of a MOSFET reduces with a breakdown voltage decrease.

b)

$f_{sw} = 50 \text{ kHz}$	$V_{GS} = 7 \text{ V}$	$R_{DS(on)} = 0.5 \Omega$
$V_a = 300 \text{ V}$	$C_{gs} = 1000 \text{ pF}$	$V_{GG} \Rightarrow -15 \text{ V} \rightarrow +15 \text{ V}$
$I_o = 10 \text{ A}$	$C_{gd} = 150 \text{ pF}$	$R_G = 50 \Omega$
$V_f = 1 \text{ V}$	$V_{GS(th)} = 4 \text{ V}$	$V_{DS} = 60.5 \text{ V}$



$$5b) ii) t_{don} = -R_g(C_{gs} + C_{gd}) \ln \left[ 1 - \frac{4}{15} \right]$$

$$= 17.8 \text{ ns}$$

$$t_{ir} = -R_g(C_{gs} + C_{gd}) \ln \left[ 1 - \frac{7-4}{15-4} \right]$$

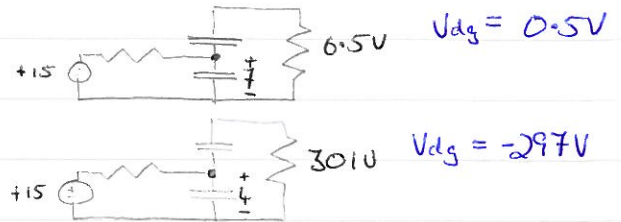
$$= 18.3 \text{ ns}$$

$$t_{vf} = \frac{C_{gd} \Delta V_{dg}}{I_{rg}}$$

$$\Delta V_{dg} = 297.5$$

$$I_{rg} = \frac{V_{dc} - V_{ds}}{R_g} = 0.16 \text{ A}$$

$$t_{vf} = 278.9 \text{ ns}$$



$$iii) E_{on} = \frac{1}{2} (V_{ds} + V_F) I_o (t_{ir} + t_{vf}) + \frac{1}{2} R_{DS(on)} I_o t_{vf}$$

$$= 582 \mu \text{ J}$$

$$iv) T_j = T_{HS} + (\theta_{js} * P_{mos})$$

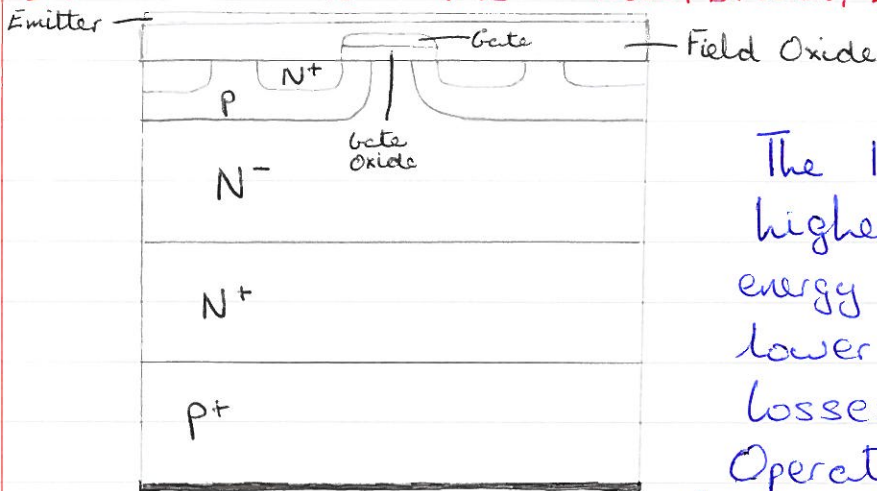
$$P_{mos} = 4 f_{sw} E_{on}$$

$$= 116.4 \text{ W}$$

$$T_j = T_{HS} + (\theta_{j-c} + \theta_{cs}) * P_{mos}$$

$$= 70 + (0.45 + 0.24) * 116.4$$

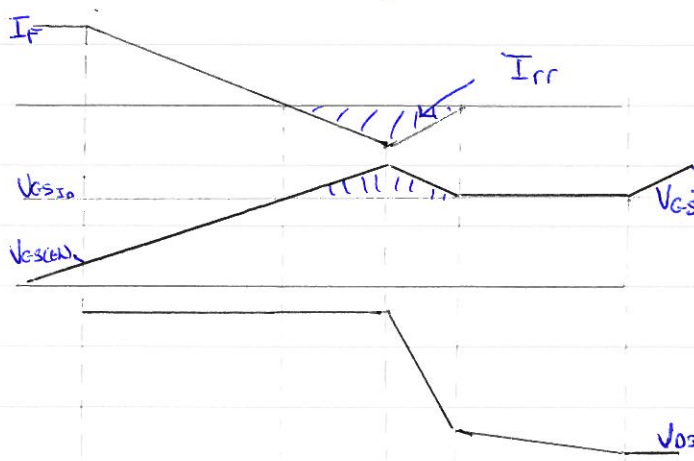
$$= 150.3 \text{ } ^\circ \text{C}$$



The IGBT generally has higher turn-on/turn-off energy losses but lower conduction losses than a MOSFET. Operating at low frequencies reduces the impact of switching  $\eta$  makes conduction the dominant loss.

b) Done, 2008

- 5 a)
- Diode current decays at a rate determined by the turn-on of the complementary IGBT/MOSFET.
- Initially,  $I_F$  drops to zero, but excess carriers remain in the drift region, keeping junction forward biased.
  - This causes  $I_F$  to go negative as excess carriers are swept out.
  - Negative current  $I_F$  decays to zero as the excess carriers are swept out.

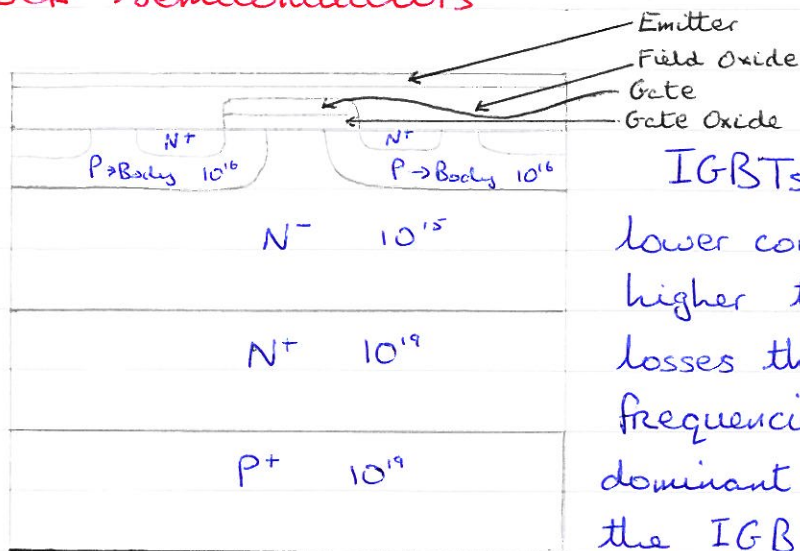




# EE4001 Power Electronics, Drives, Energy Conv.

## Power Semiconductors

1a)



IGBTs typically have lower conduction losses and higher turn-on/turn-off energy losses than MOSFETs. At low frequencies, conduction is the dominant source of loss, making the IGBT the better choice.

b)

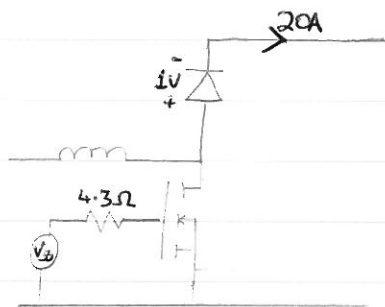
$$V_d = 480V$$

$$I_o = 20A$$

$$V_{GS} = 10V$$

$$R_G = 4.3\Omega$$

$$V_f = 1V$$



i)

$$V_{GS(ON)} Max = 5V$$

$$g_{fs} Min = 21S$$

$$C_{gs} = C_{iss} - C_{rss} = 7895pF$$

$$C_{gd} = C_{rss} = 75pF$$

$$R_{DS(ON)} Max @ 100^\circ C = 0.26\Omega$$

$$V_{GS} @ I_o = 20A = V_{GS(ON)} + \frac{I_o}{g_{fs}}$$

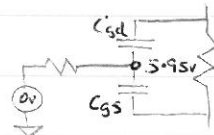
$$V_{GS} @ I_o = 20A = 5.95V$$

$$V_{DS(ON)} = I_o R_{DS(ON)} = 5.2V$$

iii) a)

$$t_{d(off)} = -R_G (C_{gs} + C_{gd}) \ln \left[ \frac{V_{GS} - V_{GS(ON)}}{V_{GS} - V_{GS(ON)}} \right]$$

$$= 17.8ns$$



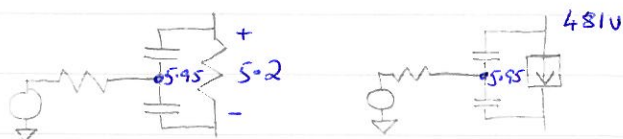
b)

$$t_{ur} = \frac{C_{gd} \Delta V}{I_{rg}}$$

$$\Delta V = -475.8$$

$$I_{rg} = -\frac{5.95}{4.3} = -1.385A$$

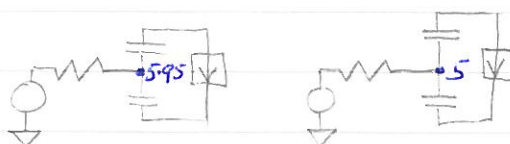
$$t_{ur} = 25.8ns$$



c)

$$t_{if} = -R_G (C_{gs} + C_{gd}) \ln \left[ \frac{5}{5.95} \right]$$

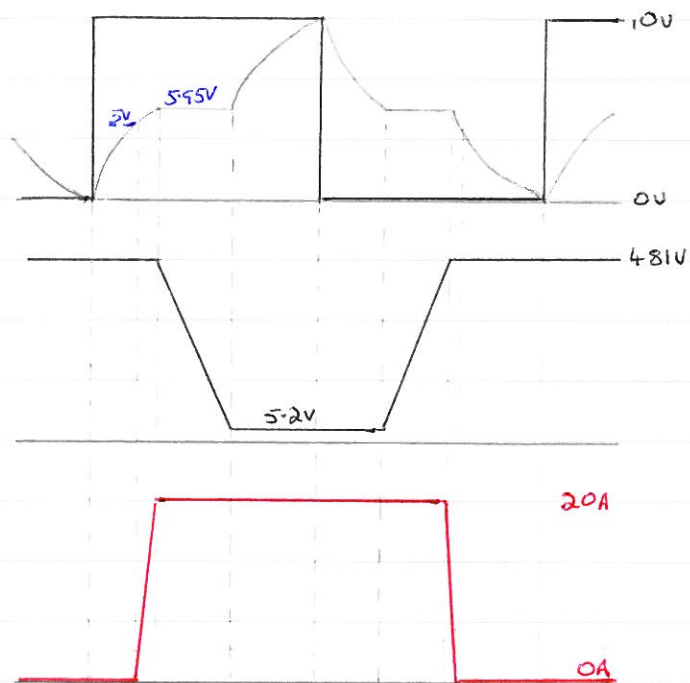
$$= 6ns$$





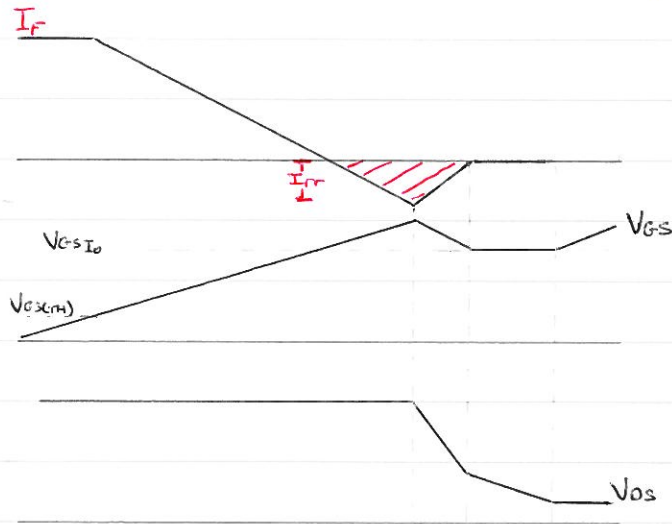
# EE4001 Power Electronics, Drives, Energy Conversion

1b ii)

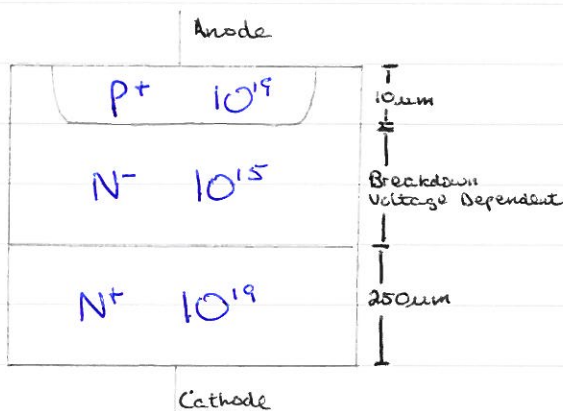


$$\begin{aligned} \text{iv) } E_{\text{off}} &= \frac{1}{2} (V_D + V_F) I_O (t_{\text{vr}} + t_{\text{if}}) \\ &= 153 \mu\text{J} \end{aligned}$$

2. a) The rate of decay of diode current,  $di/dt$ , is determined by the turn-on time of the complementary switch.
- Initially,  $I_F$  drops to zero but excess carriers remain in the drift region, keeping the junction forward biased.
  - $I_F$  goes negative while the excess carriers are swept out.
  - $I_F$  returns to zero when the sweep-out is complete.



b)

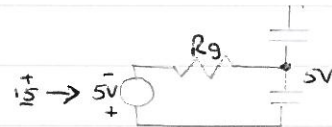


The  $n^-$  drift region absorbs the depletion layer of the reverse-biased p-n junction. Its width determines breakdown voltage.

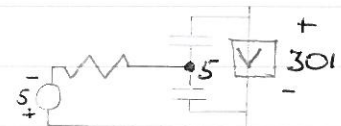
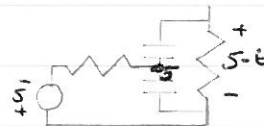
2c)  $f_{sw} = 20 \text{ kHz}$   $R_g = 25 \Omega$   
 $V_{dl} = 300 \text{ V}$   $V_f = 1 \text{ V}$   
 $I_o = 13 \text{ A}$   
 $V_{cc-} = 5 \text{ V}$   
 $V_{cc+} = 15 \text{ V}$

i)  $V_{GS(TH) \text{ Max}} = 4 \text{ V}$   $R_{DS(on)} @ 80^\circ \text{C} = 0.432 \Omega$   
 $g_{fs \text{ Min}} = 13 \text{ S}$   $V_{GS} @ I_o = 13 \text{ A} = 5 \text{ V}$   
 $C_{gs} = 3850 \text{ pF}$   $V_{DS(Cond)} = 5.6 \text{ V}$   
 $C_{gd} = 350 \text{ pF}$

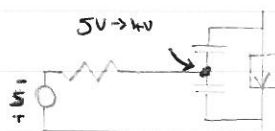
iii)  $t_{d(off)} = -R_g (C_{gs} + C_{gd}) \ln \left[ \frac{5 - (-5)}{15 - (-5)} \right]$   
 $= 72.8 \text{ ns}$



b)  $t_{vr} = \frac{C_{gd} \Delta V_{ds}}{I_{rg}}$   
 $\Delta V_{ds} = +295.4$   
 $I_{rg} = \frac{V_{gs} - V_{gs}}{r_s} = 0.4 \text{ A}$   
 $t_{vr} = 258 \text{ ns}$



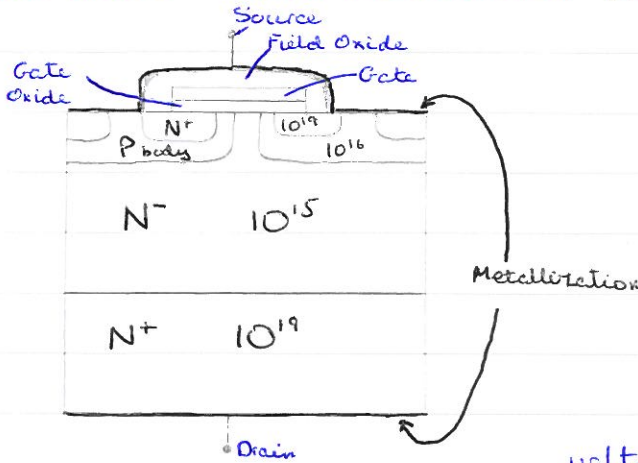
c)  $t_{fv} = -R_g (C_{gs} + C_{gd}) \ln \left[ \frac{9}{10} \right]$   
 $t_{fv} = 11 \text{ ns}$





# EE4001 Power Electronics, Drives, Energy Conv. Semi-C. Problem

6a)



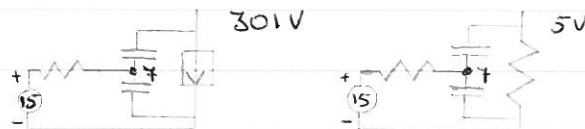
MOSFETs typically have lower turn-on/turn-off energies than IGBTs, resulting in lower switching losses. Conduction losses are essentially fixed in an IGBT over a wide voltage range, while the losses in a MOSFET reduce with voltage.

$V_d = 300V$        $C_{gs} = 1000pF$        $V_{oc+} = 15V$   
 $I_o = 10A$        $C_{gd} = 150pF$        $R_g = 50\Omega$   
 $V_{GS(th)} = 4V$        $R_{DS(on)} = 0.5\Omega$        $V_f = 1V$   
 $V_{GSIo} = 7V$        $V_{oc-} = -15V$

ii)  $t_{don} = -R_g (C_{gs} + C_{gd}) \ln \left[ 1 - \frac{V_{GSth}}{V_{oc-}} \right]$   
 $= 17.8ns$

b)  $t_{ir} = -R_g (C_{gs} + C_{gd}) \ln \left[ 1 - \frac{7-4}{15-4} \right]$   
 $= 18.3ns$

c)  $t_{fv} = \frac{C_{dg} \Delta V_{dg}}{I_{rg}}$   
 $\Delta V_{dg} = 296V$   
 $I_{rg} = \frac{V_{oc-} - V_{GS}}{R_g} = 0.16A$   
 $t_{fv} = 277.5ns$

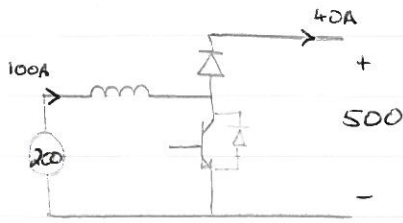


iii)  $E_{on} = \frac{1}{2} (V_d + V_f) I_o (t_{of} + t_{ir}) + \frac{1}{2} R_{DS(on)} I_o^2 t_{fv}$   
 $= 452\mu J$

iv)  $T_j = T_H + (\Theta P_{mos})$   
 Assumed:  $P_{mos} = 4 E_{on} f_{sw}$   
 $T_j = 70 + 45.2$   
 $T_j = 115.2^\circ$

# EE4001 Power Electronics, Drives, Energy Conv. Semi-C Problems

7.



$$I_{L\min} = 86A$$

$$I_{Qrms} = 77A$$

$$I_{L\max} = 114A$$

$$I_{Qavg} = 60A$$

$$I_{Drms} = 63.4A$$

$$I_{Davg} = 40A$$

Switch turn-on / Diode turn-off @  $I_{L\min}$   
Switch turn-off @  $I_{L\max}$

$$\begin{aligned} i) P_{Q(Con)} &= V_{CEon} I_{Qavg} + R_{CE} I_{Qrms}^2 \\ &= 97W \end{aligned}$$

$$\begin{aligned} ii) P_{D(Con)} &= V_f I_{Davg} + r_f I_{Drms}^2 \\ &= 53W \end{aligned}$$

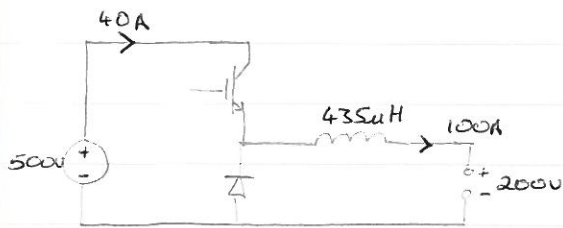
$$\begin{aligned} iii) P_{a(Con)} &= f_{sw} E_{on}(86A) \frac{500}{600} \\ &= 10(12)\left(\frac{5}{6}\right) \\ &= 100W \end{aligned}$$

$$\begin{aligned} iv) P_{a(off)} &= f_{sw} E_{off}(114A) \frac{500}{600} \\ &= 10(17)\frac{5}{6} \\ &= 142W \end{aligned}$$

$$\begin{aligned} v) P_{D(off)} &= f_{sw} E_{rr}(86A) \frac{500}{600} \\ &= 10(12)\frac{5}{6} \\ &= 100W \end{aligned}$$

# EE4001 Power Electronics, Drives, Energy Conv. Semi-C Problems

8.



$$\begin{aligned} I_{Lmin} &= 86A & I_{Qrms} &= 63.4A \\ I_{Lmax} &= 114A & I_{Qavg} &= 40A \\ I_{Drms} &= 77A & I_{DAvg} &= 60A \end{aligned}$$

Turn-on @  $I_{Lmin}$ , turn-off @  $I_{Lmax}$

$$\begin{aligned} i) P_{Qcond} &= V_{CEon} I_{Qavg} + R_{CE} I_{Qrms}^2 \\ &= (0.9 \times 40) + (7.3m \times 63.4^2) \\ &= 65W \end{aligned}$$

$$\begin{aligned} ii) P_{Dcond} &= V_f I_{DAvg} + r_f I_{Drms}^2 \\ &= 79.4W \end{aligned}$$

$$\begin{aligned} iii) P_{Qon} &= f_{sw} E_{on} (86A) \frac{500}{600} \\ &= 100W \end{aligned}$$

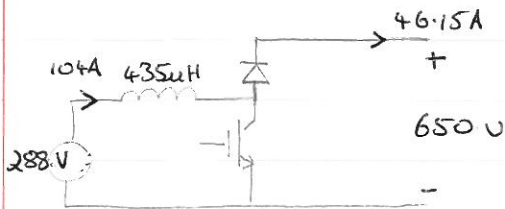
$$\begin{aligned} iv) P_{Qoff} &= f_{sw} E_{off} (114A) \frac{500}{600} \\ &= 146W \end{aligned}$$

$$\begin{aligned} v) P_{Doff} &= f_{sw} E_{rr} (86A) \frac{500}{600} \\ &= 100W \end{aligned}$$



# EE4001 Power Electronics, Drives, Energy Conversion Semi-C.Probs

9.



$$I_{Lmin} = 71.45A$$

$$I_{Lmax} = 136.95A$$

$$I_{Qrms} = 79A$$

$$I_{Drms} = 70.5A$$

$$I_{Qavg} = 58A$$

$$I_{DAvg} = 46.2A$$

$$i) P_{Qcond} = V_{CEon} I_{Qavg} + R_{CE} I_{Qrms}^2$$

$$= (0.9 \times 58) + (7.3m \times 79^2)$$

$$= 97.76W$$

$$ii) P_{Qon} = f_{sw} E_{on} (71.45A) \frac{650}{600}$$

$$= 10(10) \frac{650}{600}$$

$$= 108W$$

$$iii) P_{Qoff} = f_{sw} E_{off} (136.95A) \frac{650}{600}$$

$$= 10(18) \frac{650}{600}$$

$$= 195W$$

$$iv) P_{Dcond} = V_f I_{DAvg} + r_f I_{Drms}^2$$

$$= 63.3W$$

$$v) P_{Doff} = f_{sw} E_{rr} (71.45) \frac{650}{600}$$

$$= 10(9) \frac{650}{600}$$

$$= 97.5W$$