

Control Engineering Summer '08

4 bii) The poles of the discrete time process are given by:

$$\det(zI - A_d) = 0$$

$$\begin{bmatrix} z & 0 & 0 \\ 0 & z & 0 \\ 0 & 0 & z \end{bmatrix} - \begin{bmatrix} 1 & 0 & 0 \\ T & 1 & 0 \\ 0 & T & 1 \end{bmatrix} = \begin{bmatrix} z-1 & 0 & 0 \\ -T & z-1 & 0 \\ 0 & -T & z-1 \end{bmatrix}$$

$$\det = (z-1)[(z-1)(z-1) - 0] + 0[+T^2 - 0] + 0[0 + T(z-1)]$$

$$= (z-1)(z-1)(z-1)$$

Q.E.D.