

9. Derive the torque-speed characteristic equation for a dc machine.

$$\begin{aligned}
 V &= E + I_a R_a & \Rightarrow & V = k\Phi \omega + \frac{T}{k\Phi} R_a \\
 E &= k\Phi \omega \\
 T &= k\Phi I_a & \Rightarrow & \omega = \frac{V}{k\Phi} - \frac{R_a}{(k\Phi)^2} T
 \end{aligned}$$

10. A permanent magnet dc motor has the following parameters: $R_a = 0.25 \Omega$, $k = 0.5$ in MKS units. Calculate the speed in rpm at an applied voltage of 100 V and torque of 10 Nm.

$$\begin{aligned}
 I &= \frac{T}{k} = \frac{10}{0.5} = 20 \text{ A} \\
 E &= V - I_a R_a \\
 &= 100 - 20 \times 0.25 \text{ V} \\
 &= 95 \text{ V} \\
 \Rightarrow \omega &= \frac{E}{k} = \frac{95}{0.5} \text{ rad s}^{-1} \\
 &= 190 \text{ rad s}^{-1} \\
 \Rightarrow N &= \frac{\omega}{2\pi} \times 60 = 1814 \text{ rpm}
 \end{aligned}$$

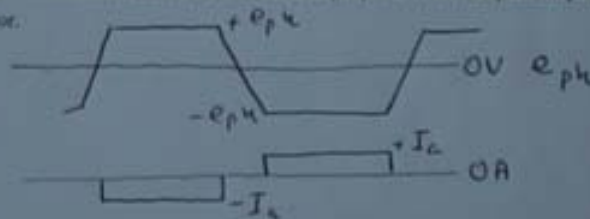
11. How can armature reaction be compensated to minimize its effects?

Use a compound machine;

12. A permanent-magnet dc motor is known to have an armature resistance of 1Ω . When operated at no load from a dc source of 50 V, it is observed to operate at a speed of 1200 rpm and to draw 1 A. Find the motor constant.

$$\begin{aligned}
 E &= V - I_a R_a \\
 &= 50 - 1 \times 1 \text{ V} \\
 &= 49 \text{ V} \\
 k_E &= \frac{E}{\omega} = \frac{E}{N} \cdot \frac{60}{2\pi} = \frac{49}{1200} \cdot \frac{60}{2\pi} = 0.39 \frac{\text{V}}{\text{rad s}}
 \end{aligned}$$

13. Sketch together the induced emf and phase current in regenerative mode for a single phase of a three-phase trapezoidal-waveform electronically-commutated motor.



14. An EC dc motor is sourced by a 50 V supply, and pulls 10 A from the source. The phase-phase resistance is 0.5Ω . The output speed is 5000 rpm. What are the output torque and machine efficiency, neglecting core, friction, and windage losses?

$$\begin{aligned}
 E &= V - I_a R_a \\
 &= 50 - 10 \times 0.5 \text{ V} \\
 &= 45 \text{ V} \\
 \Rightarrow EI &= T \omega = 450 \text{ W} \\
 \Rightarrow T &= \frac{EI}{\omega} = \frac{45 \times 10}{5000} \cdot \frac{60}{2\pi} = 0.859 \text{ Nm} \\
 \eta &= \frac{EI}{VI} = \frac{E}{V} = \frac{45}{50} = 90\%
 \end{aligned}$$

Student Name: John Hayes

Student Number: 007

1. Calculate the regenerative energy recoverable when a flywheel of inertia
- 0.06 kgm^2
- slows from 1500 rpm to 750 rpm.

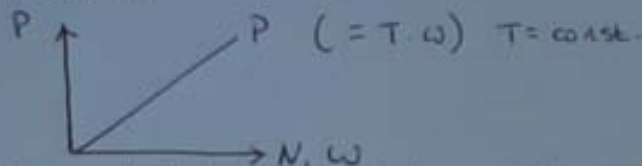
$$E = \frac{1}{2} I (\omega_1^2 - \omega_2^2) \quad \left| \begin{array}{l} \omega_1 = \frac{1500}{60} \cdot 2\pi \text{ rad s}^{-1} = 157.1 \text{ rad s}^{-1} \\ \omega_2 = 78.54 \text{ rad s}^{-1} \end{array} \right.$$

$$\frac{1}{2} \cdot 0.06 (157.1^2 - 78.54^2) = 555 \text{ J}$$

2. If a 1 m diameter windmill generates 500 W of power, what approximate power level might a 10 m windmill develop: (a) 1.5 kW, (b) 5 kW, or (c) 50 kW?

$$P_{\text{wind}} = \frac{1}{2} C_p A v_{\text{wind}}^3 \Rightarrow A \propto r^2 \Rightarrow P(10\text{m}) = 50 \text{ kW}$$

3. Sketch a plot of power vs. speed for a constant-torque load.



4. An electric vehicle has the following attributes: mass
- $M = 500 \text{ kg}$
- , wheel diameter
- $d_w = 1 \text{ m}$
- , gear ratio from rotor to drive axle
- $n = 10$
- , and a nominal gear efficiency of 95%. The vehicle is required to decelerate from 36 to 0 km/hr in 10 s on a flat road surface under calm wind conditions. Neglecting load forces, instantaneously at 18 km/hr calculate the regenerative torque to the electric motor to achieve this braking.

$$F = M \cdot a; \quad a = \frac{\Delta v}{\Delta t} \Rightarrow F = -500 \text{ N}$$

$$a = \frac{(0 - 36000) \text{ m}}{3600 \text{ s}} \cdot \frac{1}{10 \text{ s}} \quad \left| \begin{array}{l} T_{\text{AXLE}} = F r \\ T_{\text{ROTOR}} = \frac{T_{\text{AXLE}}}{n} \cdot \eta = \frac{-250}{10} \cdot 0.95 = -2375 \text{ Nm} \end{array} \right.$$

$$= -1 \text{ m s}^{-2}$$

5. Calculate the regenerative power in horse power for the above condition. (to the motor)

$$P_g = T \cdot \omega$$

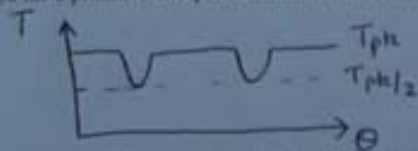
$$\omega_{\text{AXLE}} = \frac{v}{r} = \frac{18000 \text{ m}}{0.5 \text{ m} \cdot 3600 \text{ s}} = 10 \text{ rad s}^{-1} \Rightarrow \omega_{\text{ROTOR}} = n \omega_{\text{AXLE}} = 100 \text{ rad s}^{-1}$$

$$\Rightarrow P_g = T_{\text{ROTOR}} \omega_{\text{ROTOR}} = -2375 \text{ kW} = -3.18 \text{ hp}$$

6. Despite the relatively low service life of dc brushed machines, what are some of the reasons for their common use?

cost; ease of control; low operational useage relative to service life

7. Sketch a plot of torque vs. angle for a primitive two-pole dc motor with an armature winding consisting of 4 coils wave wound.



8. A permanent magnet of length 1 cm is placed in a magnetic circuit with an airgap of 0.2 cm. Assuming a high permeability core and a uniform cross-sectional area, what is the magnet field strength
- H_m
- when the magnet flux density
- B_m
- is 0.3 T?

$$B_m = B_g = 0.3 \text{ T}$$

$$H_m \cdot l_m = -H_g \cdot l_g \quad \left| \begin{array}{l} H_g = \frac{B_g}{\mu_0} \\ \Rightarrow H_m = -\frac{H_g}{l_m} \cdot l_g = -\frac{B_g \cdot l_g}{\mu_0 \cdot l_m} = -\frac{0.3 \text{ T} \cdot 0.2 \text{ cm}}{4\pi \times 10^{-7} \text{ H/m} \cdot 1 \text{ cm}} = -47.77 \text{ kA/m} \end{array} \right.$$