

**OLLSCOIL NA hÉIREANN, CORCAIGH**  
**THE NATIONAL UNIVERSITY OF IRELAND, CORK**

**COLÁISTE NA hOLLSCOILE, CORCAIGH**  
**UNIVERSITY COLLEGE, CORK**

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**AUTUMN EXAMINATIONS, 2006**

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**B. E. (ELECTRICAL)**  
**B.E. (MICROELECTRONIC)**  
**M.ENG.SC. (MICROELECTRONIC)**  
**H.DIP. (MICROELECTRONIC)**

RF IC Design  
EE4011

Professor Dr. U. Schwalke  
Professor P. Murphy  
Dr. K. G. McCarthy

Time allowed: *3 hours*

Answer *five* questions.

All questions carry equal marks.

The use of a Casio fx570w or fx570ms calculator is permitted.

The use of log/statistical tables is allowed.

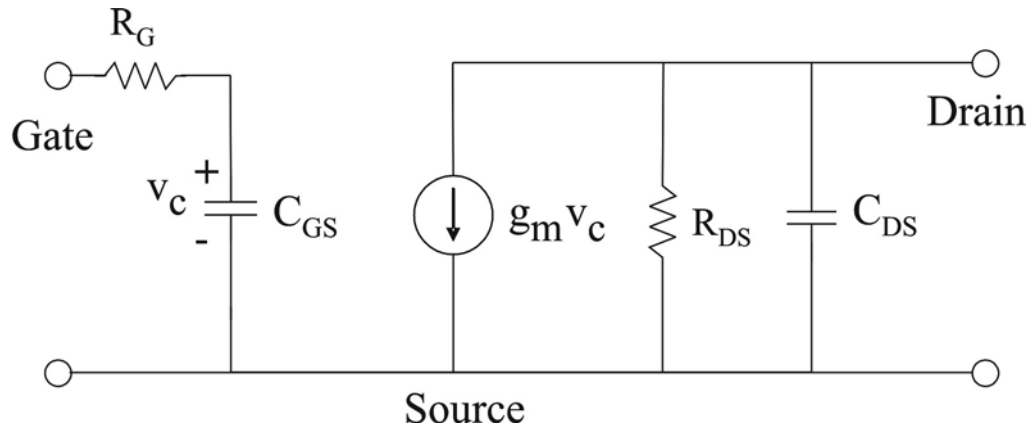
Smith charts are appended to this paper. Detach and use as required.

The following physical constants may be used as appropriate:

Boltzmann's Constant:  $k = 1.38 \times 10^{-23} \text{ J/K}$

Elementary Charge:  $q = 1.602 \times 10^{-19} \text{ C}$

1. (a) The diagram on the next page shows a simplified small-signal model of a GaAs MESFET. If this device is considered to be a two port network with port 1 at the gate, port 2 at the drain and the source grounded, derive expressions for the y-parameters of the device in terms of the circuit elements.



[10 marks]

- (b) Calculate the y-parameters for the device in 1(a) at a frequency of 1.5GHz using the following component values:

$$R_G = 6\Omega, C_{GS} = 0.8\text{pF}, g_m = 0.15\text{S}, R_{DS} = 50\Omega, C_{DS} = 0.3\text{pF}$$

[4 marks]

Note: Express the calculated y-parameters in polar (magnitude and phase) form.

- (c) If the MESFET in 1(a) with component values in 1(b) is measured at 1.5GHz in a non-ideal measurement set-up which has stray capacitances from the signal lines to the ground lines at ports 1 and 2 as shown in the diagram below, determine the measured y-parameters for the full setup including stray capacitances.



[6 marks]

2. (a) Show a small-signal model of a MOS transistor suitable for first-order analysis and from this derive an expression for the cut-off frequency of a MOS transistor. Assume the transistor is biased in saturation and that the current can be approximated by:

$$I_{DS} = \frac{1}{2} \frac{W}{L} \mu C_{OX} (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS})$$

where the symbols have their usual meaning. Also assume that the only capacitance to be considered is the gate-source capacitance.

[10 marks]

- (b) An NMOS transistor is biased in saturation and configured as a common-source two-port amplifier with the input applied to the gate (port 1) and the output taken from the drain (port 2) with the following bias conditions and device parameters:

$$W=10\mu\text{m}, L=0.25\mu\text{m}, T_{\text{ox}}=4\text{nm}, \mu=400\text{cm}^2/\text{Vs}, V_{\text{GS}}=2.5\text{V}, V_{\text{DS}}=2\text{V}, \\ V_{\text{TH}}=0.5\text{V}, \lambda=0.1 \text{ V}^{-1}.$$

Determine:

- (i) The cut-off frequency [2 marks]
  - (ii) The 4 two-port y-parameters at a frequency of 1GHz. [8 marks]
3. (a) Determine an expression for the 1dB compression point (P1dB) of an amplifier whose output  $y(t)$  can be described by the following equation:

$$y(t) = \alpha_1 x(t) + \alpha_3 x^3(t)$$

where the input  $x(t)$  is given by:

$$x(t) = A \cos(\omega t)$$

$A$  is the amplitude of the input waveform and  $\omega$  is the frequency in radians/s. Assume that  $\alpha_1 > 0$  and  $\alpha_3 < 0$ .

[10 marks]

- (b) For the amplifier described in 3(a), determine the input amplitude corresponding to the 1dB compression point if  $\alpha_1 = 10$  and  $\alpha_3 = -0.1$ . [5 marks]
- (c) An RF amplifier is supplied with an input signal power of 0dBm. The output power at the fundamental frequency is 20dBm and the output power at the third harmonic is -10dBm. Determine by graphical means, or otherwise, the input third-order intercept point (input IP3). [5 marks]
4. (a) Describe the principles of operation of a high-frequency balanced amplifier. [5 marks]
- (b) A high-frequency FET has the following S-parameters (at 12 GHz with 50Ω reference);

$$S_{11} = 0.601 \angle 178.5^\circ$$

$$S_{12} = 2.245 \angle -5.7^\circ$$

$$S_{21} = 0.076 \angle -15.9^\circ$$

$$S_{22} = 0.587 \angle -146.4^\circ$$

Check the stability of the device and plot the output 1dB constant gain circle.

[15 marks]

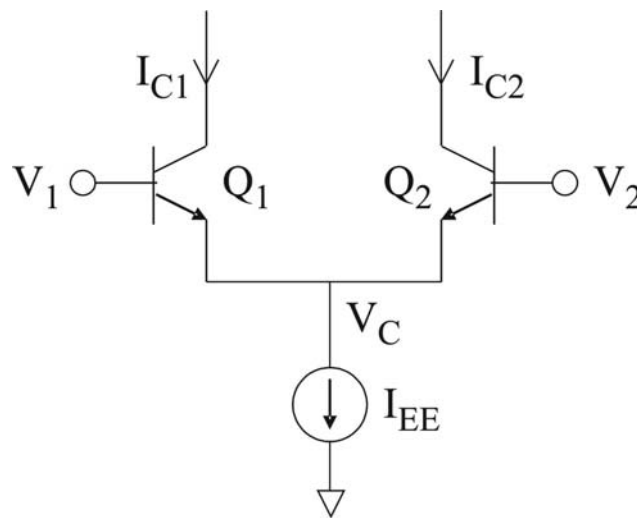
5. (a) Outline the meaning and importance of the “unilateral figure of merit” of a high-frequency amplifier.

[8 marks]

- (b) Discuss the issue of “image frequencies” in RFIC transceiver design and the resulting effects on choice of topology.

[12 marks]

6. (a) The circuit below shows a bipolar common-emitter pair formed using identical transistors  $Q_1$  and  $Q_2$  and a current source  $I_{EE}$ .



Determine an expression for the difference between the collector currents ( $\Delta I_C = I_{C1} - I_{C2}$ ) as a function of the differential input voltage ( $\Delta V = V_1 - V_2$ ).

[12 marks]

- (b) Describe two techniques which can be used to increase the dynamic range of emitter-coupled pairs such as illustrated in 6(a).

[4 marks]

- (c) Illustrate, using a circuit diagram, how emitter coupled pairs such as shown in 6(a) can be combined to form a Gilbert-cell double-balanced mixer for RF applications.

[4 marks]

7. (a) Illustrate a Type II Phase Locked Loop (PLL) based on the Phase-Frequency-Detector/Charge-Pump concept. Assume that the PLL has an integer divider in the feedback path and has an added zero for stability.

[4 marks]

- (b) For the PLL in 7(a) derive expressions for

- (i) the open-loop response

[6 marks]

- (ii) the closed-loop response

[4 marks]

Notes:

1. The “average current” method can be used to determine the transfer function of the PFD/CP combination.

2. The denominator of a second-order system is conveniently written in the following form where the symbols have their usual meaning:

$$s^2 + 2\zeta\omega_n s + \omega_n^2$$

- (c) A Type II PLL has the following parameters:

$$I_P=1\text{mA}, C_P=100\text{pF}, R_P=10\text{k}\Omega, K_{VCO}=100\text{MHz/V}, M=1000$$

Determine:

- (i) The natural frequency

[2 marks]

- (ii) The damping factor

[2 marks]

- (iii) The loop time constant

[2 marks]

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