

**EE4001 Study Questions – ED Chapter 11**

Summer 2004

## Problem 1

- (a) A symmetrical, four-pole, three-phase, star-connected 70 hp induction motor is characterized as follows. The dc phase-to-phase resistance is measured to be  $23.6 \text{ m}\Omega$ . A no-load test with an applied voltage of  $195 \text{ V}$  (line-line),  $200 \text{ Hz}$ , results in a phase current of  $64.7 \text{ A}$ , and a three-phase power of  $1.093 \text{ kW}$ . A locked-rotor test with an applied voltage of  $35.6 \text{ V}$  (line-line),  $200 \text{ Hz}$ , results in a phase current of  $93 \text{ A}$ , and a three-phase power of  $641 \text{ W}$ . Estimate the per-phase equivalent circuit parameters:  $R_S$ ,  $L_{LS}$ ,  $L_M$ ,  $L_{LR}'$ , and  $R_R'$ . Assume that  $L_{LR}' = 0.8 \cdot L_{LS}$  for this class of machine.

[Ans.  $R_S = 11.8 \text{ m}\Omega$ ,  $L_{LS} = 0.097 \text{ mH}$ ,  $L_M = 2.289 \text{ mH}$ ,  $L_{LR}' = 0.078 \text{ mH}$ , and  $R_R' = 12.9 \text{ m}\Omega$ .]

- (b) A four-pole, star-connected induction motor interfaces a mechanical load to the  $400 \text{ V}$  (line-line)  $50 \text{ Hz}$  power grid (via gearing, contactor and breaker). The machine has the following per-phase equivalent circuit parameters:

$$R_S = 20 \text{ m}\Omega, L_{LS} = 0.2 \text{ mH}, L_M = 7.2 \text{ mH}, L_{LR}' = 0.3 \text{ mH}, \text{ and } R_R' = 35 \text{ m}\Omega.$$

At full power, the induction motor requires a per-phase current of  $225 \text{ A}$  at a power factor of  $0.89$  and an overall system efficiency of  $89.7 \%$ . Calculate approximate values for the following: (i) the electrical input power, (ii) the airgap power, (iii) the per-phase magnetizing current, (iv) the per-phase rotor current, (v) the slip, and (vi) the core, friction and windage losses.

Calculate approximate values for the following when the mechanical load drops to  $25 \%$  of its value at full load:

(i) the slip, (ii) the per-phase rotor current, (iii) the per-phase current, and (iv) the power factor.

[Ans.  $138.74 \text{ kW}$ ,  $135.7 \text{ kW}$ ,  $102.6 \text{ A}$ ,  $200.25 \text{ A}$ ,  $3.1 \%$ ,  $7.04 \text{ kW}$ ;  $0.9 \%$ ,  $57.4 \text{ A}$ ,  $117.2 \text{ A}$ ,  $0.488$ ]

Summer 2001

## Problem 2

A symmetrical, four-pole, three-phase, wye-connected induction motor is characterized as follows. The dc phase-to-phase resistance is measured to be  $1.1 \text{ }\Omega$ . A no-load test with an applied voltage of  $208 \text{ V}$  (line-line),  $60 \text{ Hz}$ , results in a phase current of  $6.5 \text{ A}$ , and a three-phase power of  $175 \text{ W}$ . A locked-rotor test with an applied voltage of  $53 \text{ V}$  (line-line),  $60 \text{ Hz}$ , results in a phase current of  $18.2 \text{ A}$ , and a three-phase power of  $900$

W. Estimate the per-phase equivalent circuit parameters:  $R_S$ ,  $L_{LS}$ ,  $L_M$ ,  $L_{LR}'$ , and  $R_R'$ . Assume that  $L_{LR}' = \frac{3}{2} L_{LS}$

for this Class B machine.

[Ans:  $R_S = 0.55 \text{ }\Omega$ ,  $L_{LS} = 1.5 \text{ mH}$ ,  $L_M = 47.4 \text{ mH}$ ,  $L_{LR}' = 2.25 \text{ mH}$ , and  $R_R' = 0.356 \text{ }\Omega$ .]

Summer 2003

## Problem 3

(a) A symmetrical, four-pole, three-phase, star-connected induction motor is characterized as follows. The dc phase-to-phase resistance is measured to be  $3.54 \text{ }\Omega$ . A no-load test with an applied voltage of  $400 \text{ V}$  (line-line),  $50 \text{ Hz}$ , results in a phase current of  $1.8 \text{ A}$ , and a three-phase power of  $120 \text{ W}$ . A locked-rotor test with an applied voltage of  $71 \text{ V}$  (line-line),  $50 \text{ Hz}$ , results in a phase current of  $4 \text{ A}$ , and a three-phase power of  $150 \text{ W}$ .

Estimate the per-phase equivalent circuit parameters:  $R_S$ ,  $L_{LS}$ ,  $L_M$ ,  $L_{LR}'$ , and  $R_R'$ . Assume that  $L_{LR}' = \frac{3}{2} L_{LS}$  for

this Class B machine.

[Ans.  $R_S = 1.77 \text{ }\Omega$ ,  $L_{LS} = 12 \text{ mH}$ ,  $L_M = 395 \text{ mH}$ ,  $L_{LR}' = 19 \text{ mH}$ , and  $R_R' = 1.36 \text{ }\Omega$ ]

(b) A four-pole star-connected induction motor used in an electric vehicle application has the following per-phase equivalent circuit parameters:

$$R_S = 11.8 \text{ m}\Omega, L_{LS} = 0.0972 \text{ mH}, L_M = 2.0 \text{ mH}, L_{LR}' = 0.0772 \text{ mH}, \text{ and } R_R' = 12.9 \text{ m}\Omega.$$

When supplied by a current-controlled inverter outputting  $93 \text{ A}$  at  $200 \text{ Hz}$ , the motor generates an output torque of  $40 \text{ Nm}$  at  $5945 \text{ rpm}$ . Core, friction and windage losses are estimated at  $2.3 \text{ kW}$  at this speed.

Determine approximate values for the input per-phase voltage, power factor, and efficiency at this operating point.

[Ans.  $113.3 \text{ V}$ ,  $0.869$ ,  $89.7 \%$ ]

## Problem 4

The specification table for Westinghouse induction motors is provided as an attachment. Consider the 22 kW, four-pole machine with 400 V (line-line), 50 Hz applied in the delta configuration. What is the slope of the torque/slip curve in its linear region? Estimate the per-phase equivalent circuit parameters:  $L_M$ ,  $R_R'$ ,  $R_S$ ,  $P_{CFW}$ ,  $L_{LS}$ , and  $L_{LR}'$ . Assume that  $L_{LR}' = \frac{3}{2} L_{LS}$  for this class of machine.

[Ans. T/Hz = 245 Nm/Hz,  $L_M = 122$  mH,  $R_R' = 0.44 \Omega$ ,  $R_S = 0.58 \Omega$ ,  $P_{CFW} = 671$  W,  $L_{LS} = 2.9$  mH,  $L_{LR}' = 4.3$  mH]

#### Problem 5

Consider the 75 kW, four-pole machine with 400 V (line-line), 50 Hz applied in the delta configuration. What is the slope of the torque/slip curve in its linear region? Estimate the per-phase equivalent circuit parameters:  $L_M$ ,  $R_R'$ ,  $R_S$ ,  $P_{CFW}$ ,  $L_{LS}$ , and  $L_{LR}'$ . Assume that  $L_{LR}' = \frac{3}{2} L_{LS}$  for this class of machine.

[Ans. T/Hz = 1930 Nm/Hz,  $L_M = 35.6$  mH,  $R_R' = 57$  m $\Omega$ ,  $R_S = 117$  m $\Omega$ ,  $P_{CFW} = 1861$  W,  $L_{LS} = 0.9$  mH,  $L_{LR}' = 1.4$  mH]

#### Summer 2005

##### Problem 6

The specification table for Westinghouse induction motors is provided as an attachment (see page 6). Consider the 110 kW, four-pole machine with 400 V (line-line), 50 Hz applied in the delta configuration. Assume  $R_S = 58.3$  m $\Omega$ .

- Determine the slope of the torque/speed (Nm/Hz) curve in its linear region?
  - Estimate the per-phase equivalent circuit parameters:  $L_M$ ,  $R_R'$ , and  $P_{CFW}$ .
- (b) The four-pole, 22 kW induction motor in the tables is missing the power factor for the 50 % load point. Calculate an approximate value for the power factor based on the information provided at the 100 % load point.
- (c) Given that the four-pole, 22kW motor has  $R_R' = 0.44 \Omega$  and  $R_S = 0.58 \Omega$ , determine the leakage inductances

$L_{LS}$  and  $L_{LR}'$ . Assume that  $L_{LR}' = \frac{3}{2} L_{LS}$  for this class of machine.

[Ans. (a) T/Hz = 2828 Nm/Hz,  $L_M = 24.3$  mH,  $R_R' = 39.3$  m $\Omega$ ,  $P_{CFW} = 3169$  W, (b) PF = 0.7, (c)  $L_{LS} = 2.9$  mH,  $L_{LR}' = 4.3$  mH]

#### Summer 2006

##### Problem 7

- (a) The specification table for Westinghouse induction motors is provided as an attachment (see page 6). Consider the 22 kW, **eight**-pole machine with 400 V (line-line), 50 Hz applied in the delta configuration. Estimate the per-phase equivalent circuit parameters:  $R_R'$ ,  $P_{CFW}$ ,  $L_{LS}$ ,  $L_{LR}'$ , and  $L_M$ . Assume  $R_S = 0.432 \Omega$  and  $L_{LS}$  equals  $L_{LR}'$  for this class of machine.

[Ans.  $R_R' = 0.49 \Omega$ ,  $P_{CFW} = 785$  W,  $L_{LS} = 2.8$  mH,  $L_{LR}' = 2.8$  mH,  $L_M = 73$  mH,]

- (b) A four-pole star-connected induction motor used in an electric vehicle application has the following per-phase equivalent circuit parameters:

$R_S = 11.8$  m $\Omega$ ,  $L_{LS} = 0.0972$  mH,  $L_M = 2.0$  mH,  $L_{LR}' = 0.0772$  mH, and  $R_R' = 12.9$  m $\Omega$ .

When supplied by a current-controlled inverter outputting 93 A at 200 Hz, the motor generates an output torque of 40 Nm at 5945 rpm. Core, friction and windage losses are estimated at 2.3 kW at this speed. Determine approximate values for the input per-phase voltage, power factor, and efficiency at this operating point.

[Ans. 113.3 V, 0.869, 89.7 %]