

EE 4211 Computer Vision

Lecture 2B: Image enhancement (Spatial)

Semester B, 2021-2022

Spatial Domain Topics

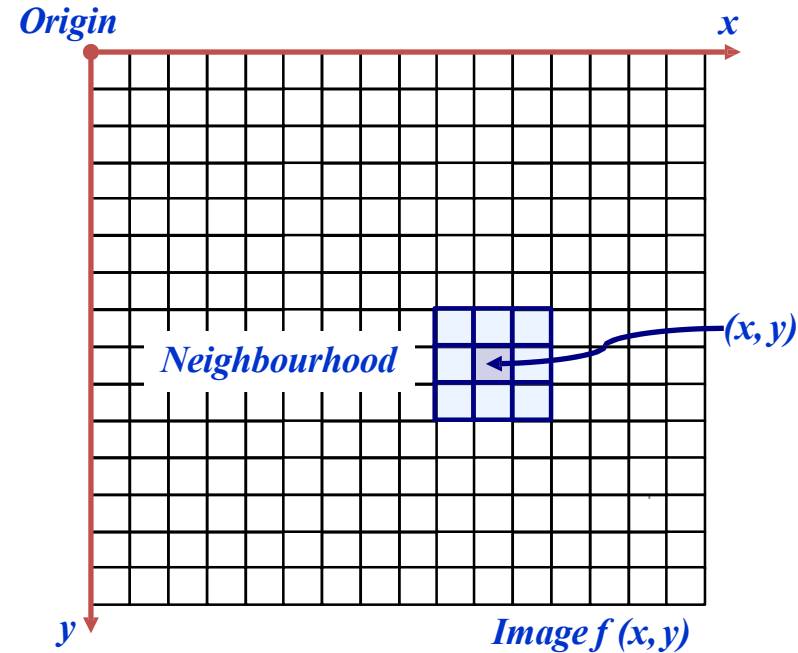
- **Point processing** – Gray values change without any knowledge of its surroundings (Part I)
 - Log, power-law, piecewise linear
 - Histogram Equalization
- **Neighborhood processing (filtering)** – Gray values change depending on the gray values in a small neighborhood of pixels around the given pixel (Part II)
 - Smoothing filters
 - Median filters
 - Sharpening

Spatial Filtering

- Basics of Spatial Filtering
- Smoothing Spatial Filters
 - Averaging filters, Order-Statistics filters
- Sharpening Spatial Filters
 - Laplacian filters, Sobel filter
- Combining Spatial Enhancement Methods

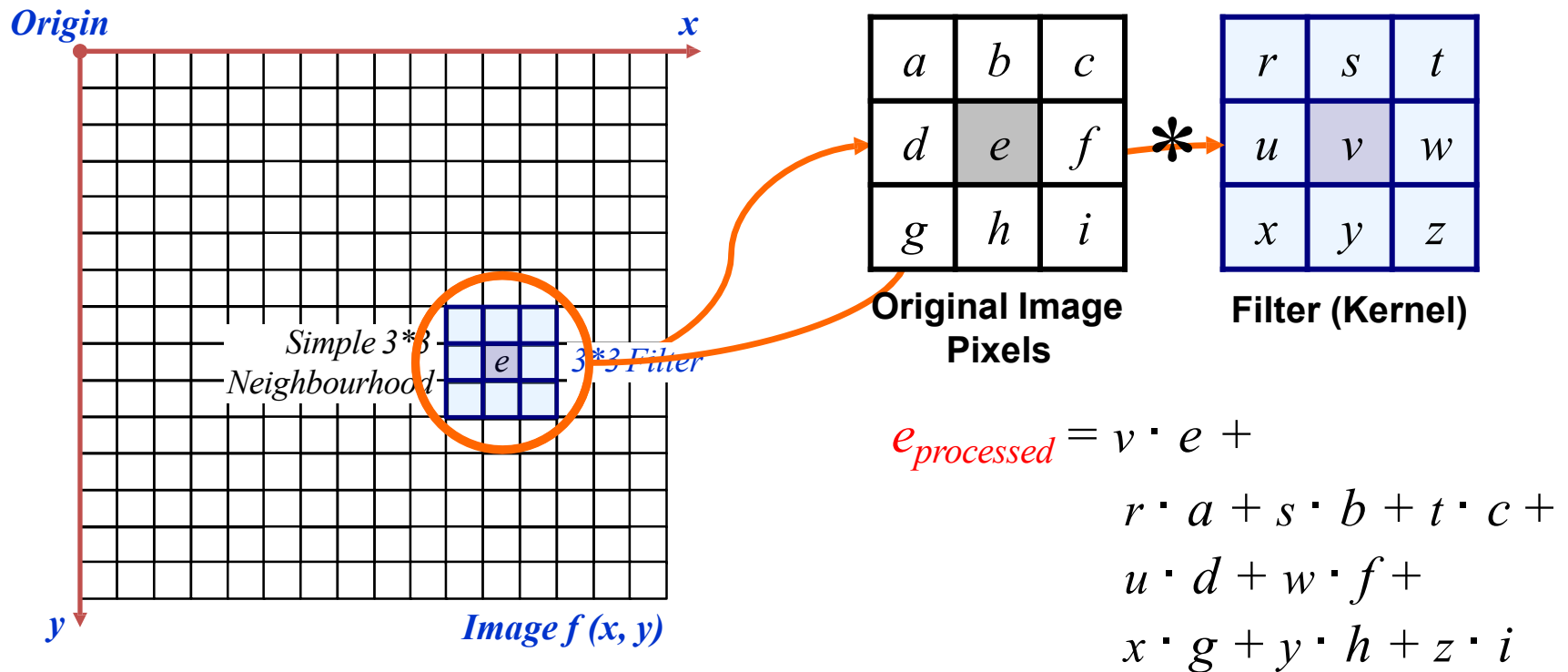
Linear Spatial Filtering

- $g(x,y) = T[f(x,y)]$
 - $f(x,y)$: input image
 - $g(x,y)$: output image
 - T : an operator on f defined over some **neighborhood** of (x,y)
- A spatial filter consists of
 - a neighborhood, and
 - a predefined operation



The Spatial Filtering Process

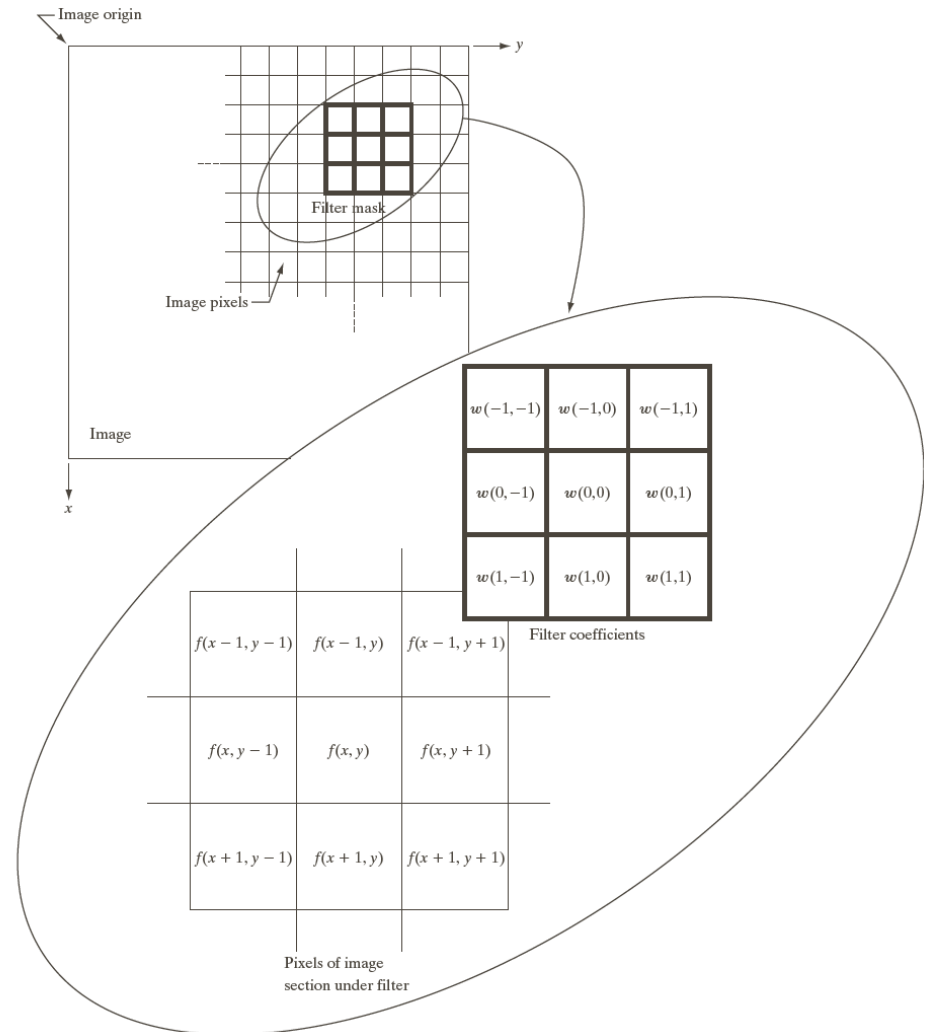
- Repeated for every pixel in the original image to generate the filtered image



Spatial Filtering: Equation Form

- Filtering can be given in equation form by

$$g(x, y) = \sum_{s=-a}^a \sum_{t=-b}^b w(s, t) f(x + s, y + t)$$



Spatial Filtering

- Basics of Spatial Filtering
- **Smoothing Spatial Filters**
 - Averaging filters, Order-Statistics filters
- Sharpening Spatial Filters
 - Laplacian filters, High-boost filters
- Combining Spatial Enhancement Methods

Smoothing Spatial Filters

- Smoothing filters are used for **blurring** and for **noise reduction**
- Blurring is used in preprocessing steps, such as
 - Removal of small details from an image prior to object extraction
 - Bridging of small gaps in lines or curves
- Noise Reduction can be accomplished by blurring with linear or non-linear filters

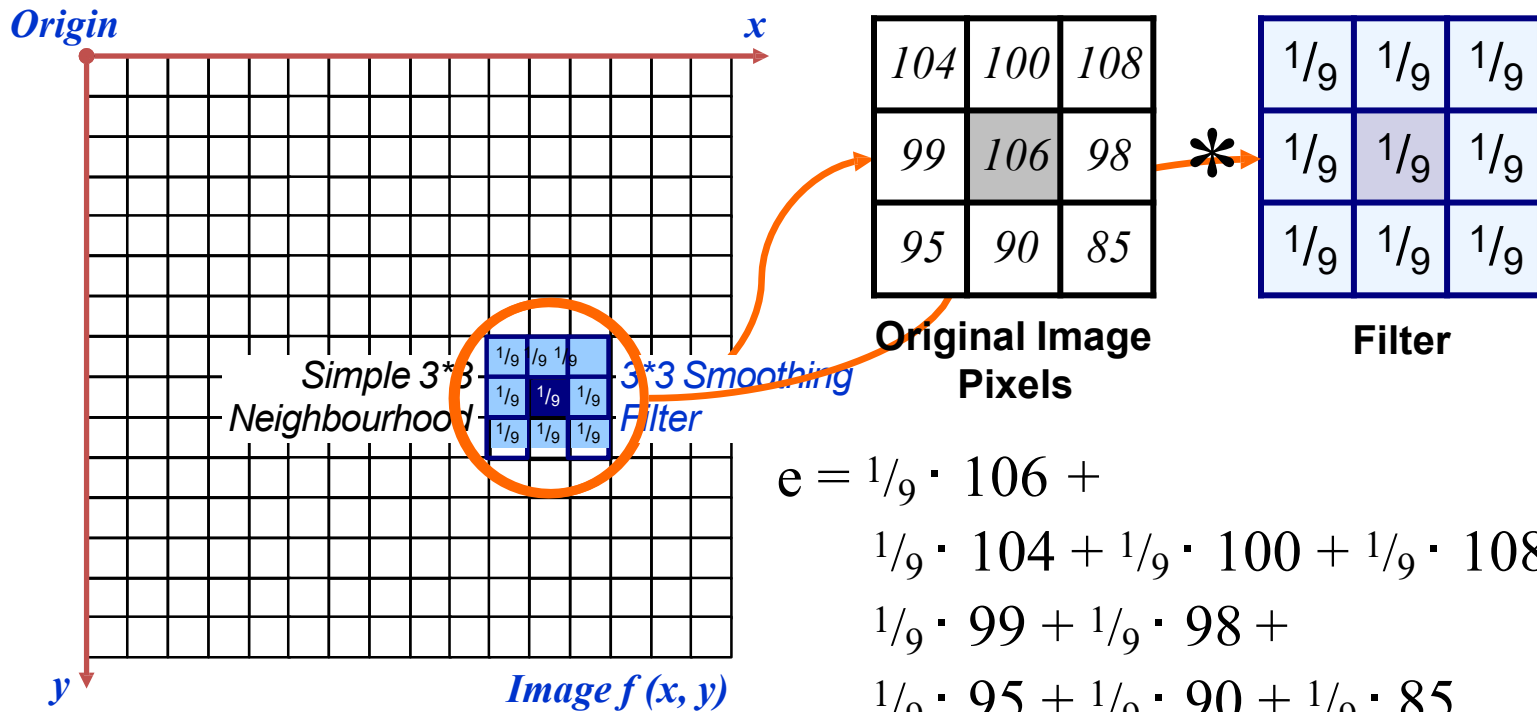
Spatial Smoothing Linear Filters

- Smoothing : One of the simplest spatial filtering operations
- Replace each pixel by the average of pixels in a square window surrounding this pixel
 - Especially useful in removing noise from images
 - Also useful for highlighting gross information

$1/9$	$1/9$	$1/9$
$1/9$	$1/9$	$1/9$
$1/9$	$1/9$	$1/9$

Simple Averaging Filter

Average Filtering Process



Examples

- Original image size 500x500 pixels
- Results of smoothing with averaging filter masks of size $n=3, 5, 9, 15, 35$, respectively



Examples

```
%% avarage filter
clc;
clear;
close all;
f = imread('plate1.tif'); %2B_PP12
w3 = 1/ (3. ^2)*ones (3);
g3 = imfilter (f, w3);
w5 = 1/ (5. ^2)*ones (5);
g5 = imfilter (f, w5);
w9 = 1/ (9. ^2)*ones (9);
g9 = imfilter (f, w9);
w15 = 1/ (15. ^2)*ones (15);
g15 = imfilter (f, w15);
w35 = 1/ (35. ^2)*ones (35);
g35 = imfilter(f, w35);

figure;
subplot(3,2,1);imshow(f);title('Original Image');
subplot(3,2,2);imshow(g3);title('Image with 3*3 filter');
subplot(3,2,3);imshow(g5);title('Image with 5*5 filter');
subplot(3,2,4);imshow(g9);title('Image with 9*9 filter');
subplot(3,2,5);imshow(g15);title('Image with 15*15 filter');
subplot(3,2,6);imshow(g35);title('Image with 35*35 filter');
```

Weighted Smoothing Filters

- Instead of averaging all the pixel values in the window, this filter gives the closer-by pixels higher weighting, and far-away pixels lower weighting.
- Reduce value of coefficients as a function of increasing distance from the origin
- An **attempt to reduce blurring** in the smoothing process

$1/16$	$2/16$	$1/16$
$2/16$	$4/16$	$2/16$
$1/16$	$2/16$	$1/16$

Examples to blur

Original image



Image with smooth



image with weighted

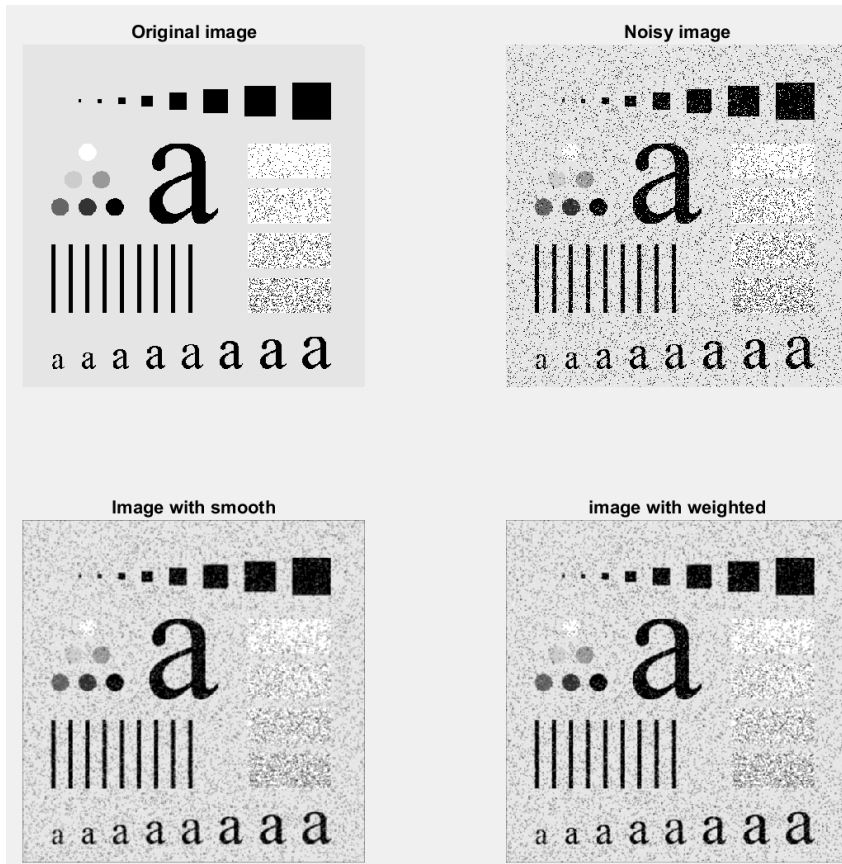


```
%% weighted smooth filter for smooth %2B_PP15
f=imread('lena.bmp');
g5 = 1/ (5. ^2)*ones (5);
w5=1/25*[0,0,1,0,0;0,2,2,2,0;1,2,5,2,1;0,2,2,2,0;0,0,1,0,0];

f_g5=imfilter(f,g5);
f_w5=imfilter(f,w5);
figure;
subplot(1,3,1);imshow(f);title('Original image')
subplot(1,3,2);imshow(uint8(f_g5));title('Image with smooth')
subplot(1,3,3);imshow(uint8(f_w5));title('image with weighted')
```

Examples to remove noise

- By smoothing the original image, we get rid of lots of the finer detail which leaves only the gross features for thresholding



```
%% weighted smooth filter for noise removing %2B_PP16
f=imread('platel.tif');
fn = imnoise(f,'salt & pepper', 0.1);
g3 = 1/ (3. ^2)*ones (3);
w3=1/16*[1,2,1;2,4,2;1,2,1];

f_g3=imfilter(fn,g3);
f_w3=imfilter(fn,w3);
figure;
subplot(2,2,1);imshow(f);title('Original image')
subplot(2,2,2);imshow(fn);title('Noisy image')
subplot(2,2,3);imshow(uint8(f_g3));title('Image with smooth')
subplot(2,2,4);imshow(uint8(f_w3));title('image with weighted')
```

Order-Statistics Filters

- Non-linear filters
- Response is based on ordering (ranking) the pixels contained in the image area encompassed by the filter
- Example:
 - median filter, max filter, min filter

Median Filters

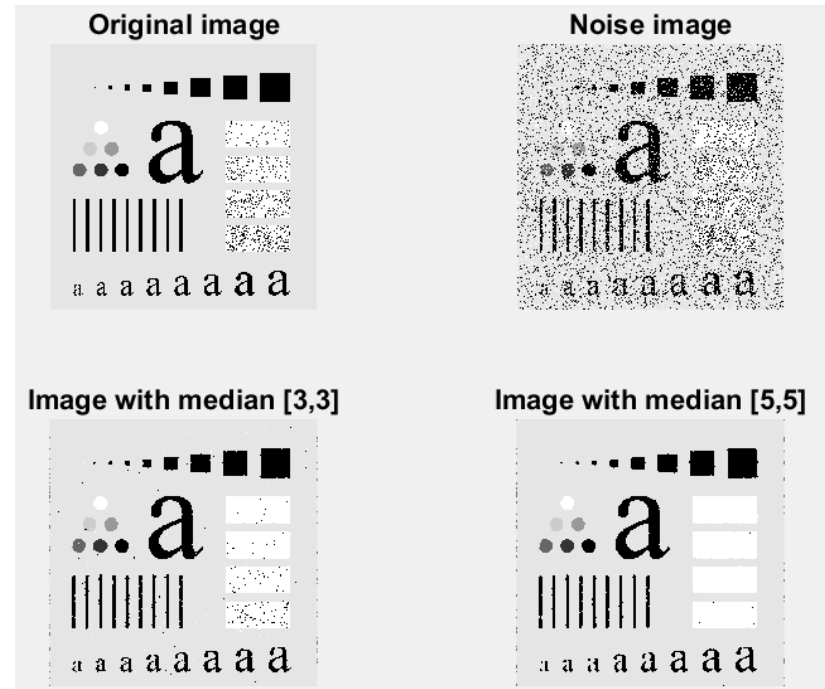
- Obtained by **sorting** all pixels in the analysis window in increasing or decreasing order of amplitudes and **picking the middle value** if the number of pixels is odd, or the average of the two values in middle if the number of pixels is even.

$$g(x, y) = \text{median}\{f(x - n, y - m), (n, m) \in N\}$$

- Popularly used for certain types of random noise (impulse noise, salt and pepper noise)
 - Excellent noise-reduction capabilities
 - Less blurring effect than linear smoothing filters of similar size

2D Median Filtering Example

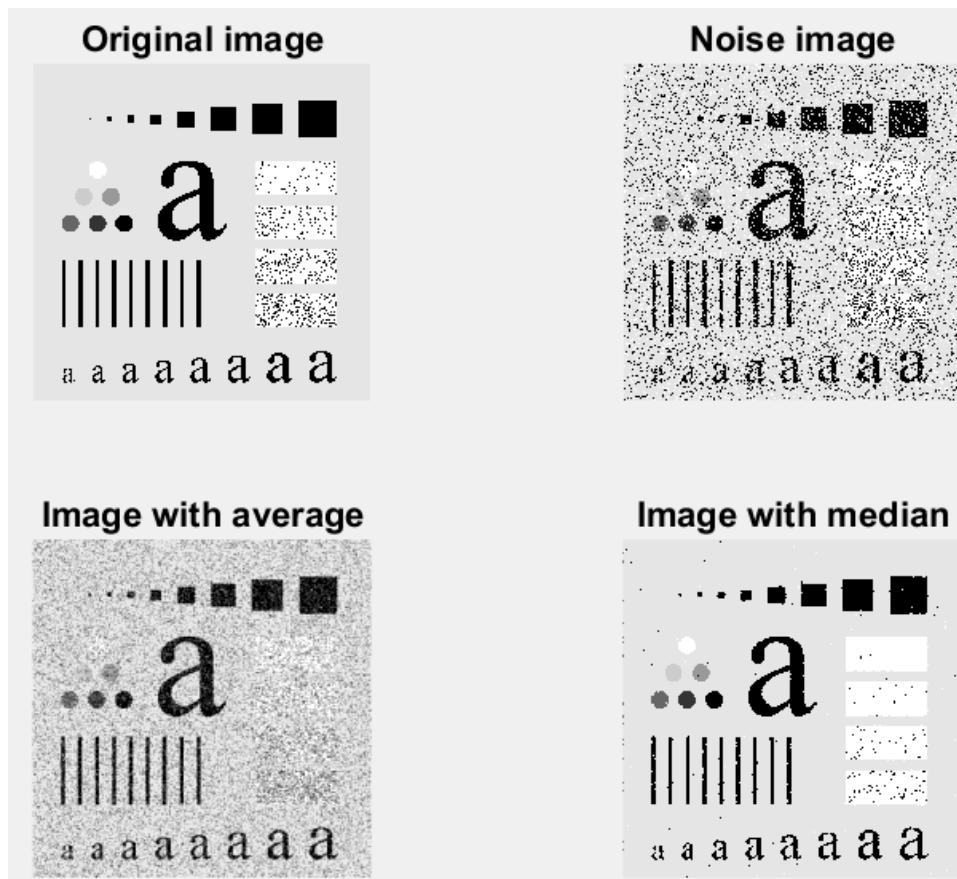
- Filtering is often used to remove noise from images



```
%% median filter %2B_PP19
f = imread('platel.tif');
fn=imnoise(f,'salt & pepper',0.2);
g3 = medfilt2(fn,[3,3]);
g5 = medfilt2(fn,[5,5]);
figure
subplot(2,2,1);imshow(f);title('Original image')
subplot(2,2,2);imshow(fn);title('Noise image')
subplot(2,2,3);imshow(g3);title('Image with median [3,3]')
subplot(2,2,4);imshow(g5);title('Image with median [5,5]')
```

Averaging Filter vs. Median Filter Example

- Filtering is often used to remove noise from images
- Sometimes a median filter works better than an averaging filter



```
%% median filter VS average %2B_PP20
f = imread('platel.tif');
fn=imnoise(f,'salt & pepper',0.2);
w3 = 1/(3.^2)*ones(3);
g3 = imfilter(fn, w3);
g = medfilt2(fn);
figure;
subplot(2,2,1);imshow(f);title('Original image')
subplot(2,2,2);imshow(fn);title('Noise image')
subplot(2,2,3);imshow(g3);title('Image with average')
subplot(2,2,4);imshow(g);title('Image with median')
```

Spatial Filtering

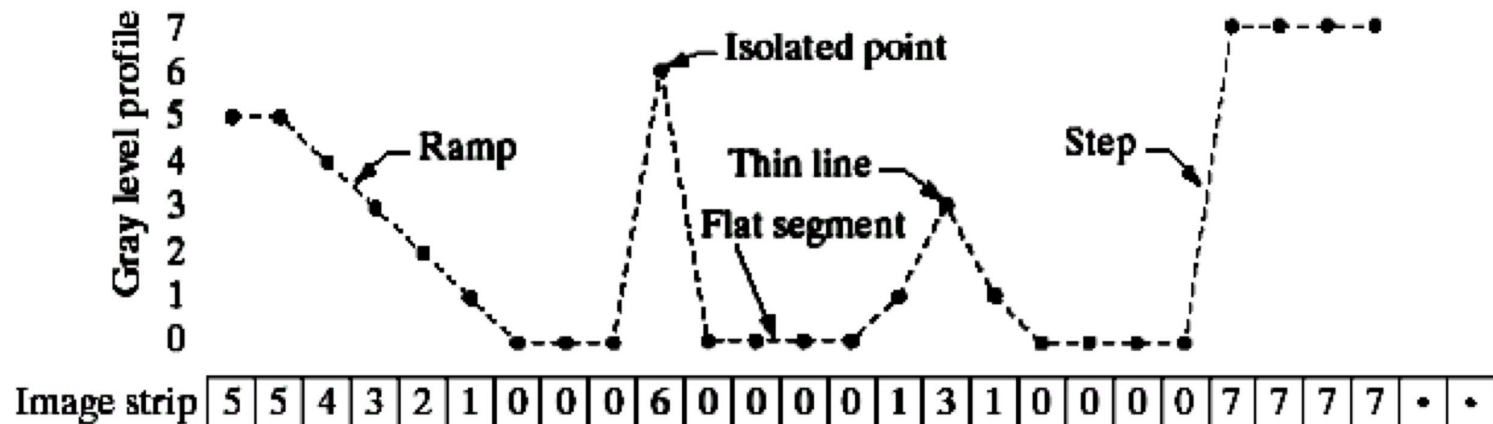
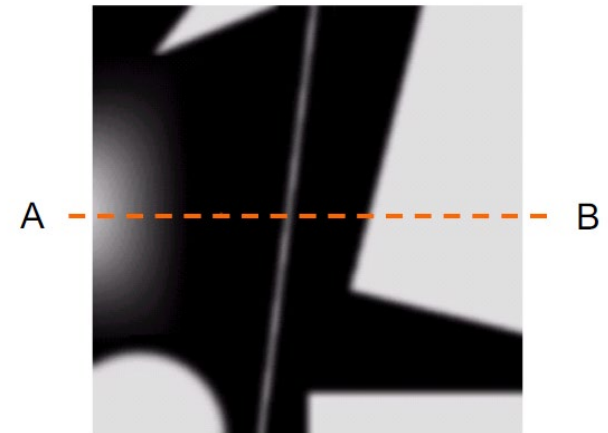
- Basics of Spatial Filtering
- Smoothing Spatial Filters
 - Averaging filters, Order-Statistics filters
- **Sharpening Spatial Filters**
 - Laplacian filters, Sobel filter
- Combining Spatial Enhancement Methods

Sharpening Spatial Filters

- Smoothing filters remove fine detail
- Sharpening spatial filters seek to highlight fine detail
 - Remove blurring from images
 - Highlight edges
- Sharpening filters are based on spatial differentiation

Spatial Differentiation

- Differentiation measures the rate of change of a function
- Let's consider a simple 1 dimensional example



1st Derivative

- The formula for the 1st derivative of a function is as follows:

$$\frac{\partial f}{\partial x} = f(x+1) - f(x)$$

- It's just the difference between subsequent values and measures the rate of change of the function

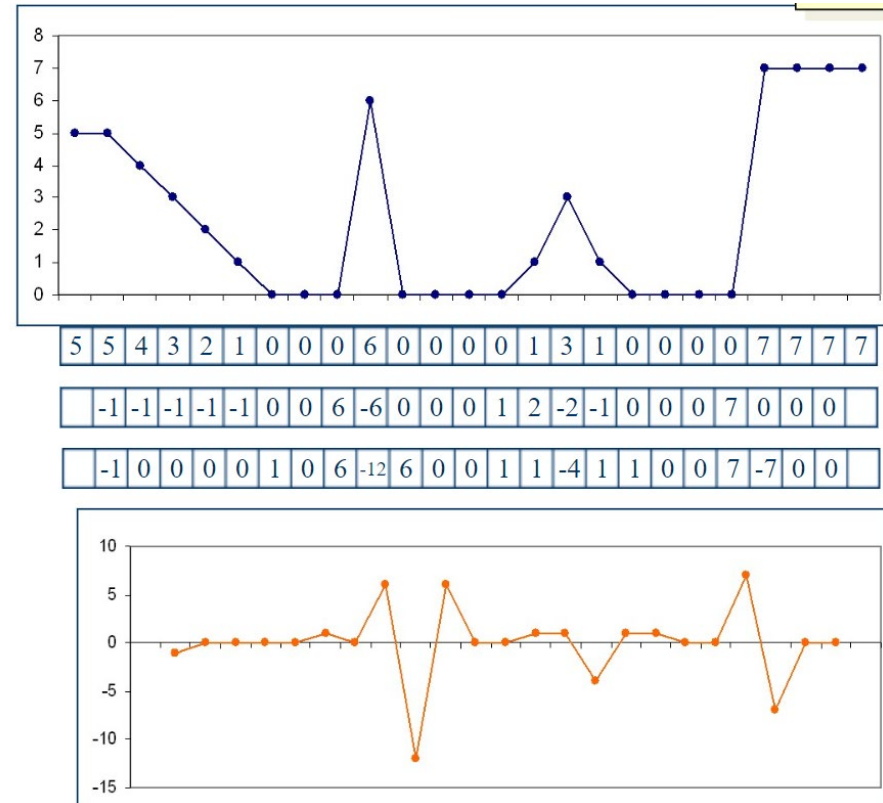
5	5	4	3	2	1	0	0	0	6	0	0	0	0	1	3	1	0	0	0	0	7	7	7	7
	-1	-1	-1	-1	-1	0	0	6	-6	0	0	0	1	2	-2	-1	0	0	0	7	0	0	0	

2nd Derivative

- The derivatives of a function is as follows:

$$\frac{\partial^2 f}{\partial^2 x} = f(x+1) + f(x-1) - 2f(x)$$

- Simply takes into account the values both before and after the current value



Using Second Derivatives for Image Enhancement

- The 2nd derivative is more useful for image enhancement than the 1st derivative
 - Stronger response to fine detail
 - Simple implementation
- The first sharpening filter we will look at is the **Laplacian**
 - Isotropic
 - One of the simplest sharpening filters

The Laplacian

- The Laplacian is defined as follows:

$$\nabla^2 f = \frac{\partial^2 f}{\partial^2 x} + \frac{\partial^2 f}{\partial^2 y}$$

- where the **partial 2nd order derivative** in the x direction is defined as follows:

$$\frac{\partial^2 f}{\partial^2 x} = f(x+1, y) + f(x-1, y) - 2f(x, y)$$

- and in the y direction as follows:

$$\frac{\partial^2 f}{\partial^2 y} = f(x, y+1) + f(x, y-1) - 2f(x, y)$$

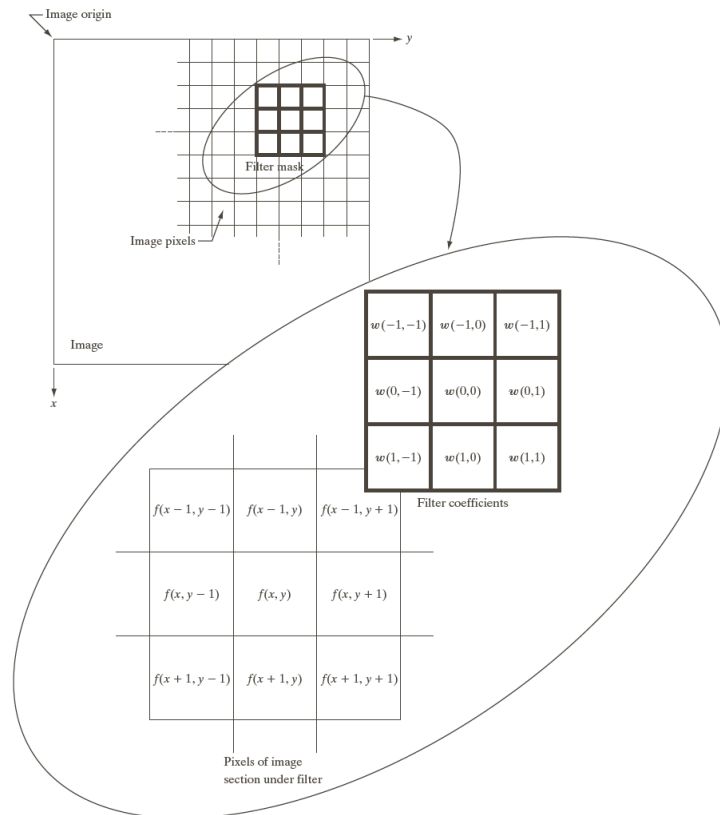
The Laplacian Operator

- So, the Laplacian can be given as follows:

$$\nabla^2 f = [f(x+1, y) + f(x-1, y) + f(x, y+1) + f(x, y-1) - 4f(x, y)]$$

- We can easily build a filter

0	1	0
1	-4	1
0	1	0



Laplacian Mask

- This Laplacian mask is implemented differently by incorporating the diagonal directions. The center value is now -8.

0	1	0
1	-4	1
0	1	0

1	1	1
1	-8	1
1	1	1

The Laplacian Filter Example

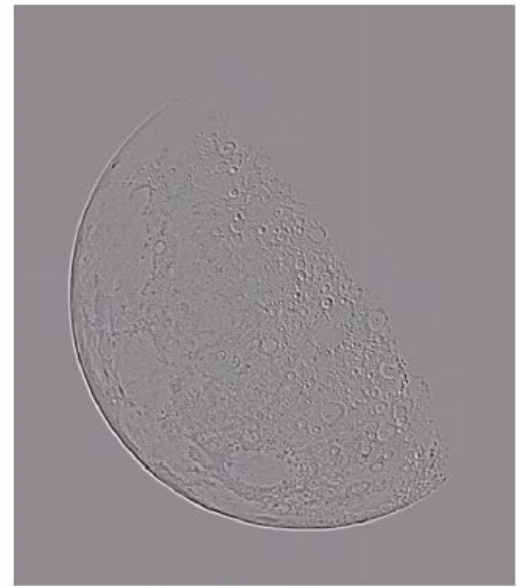
- Applying the Laplacian filter to an image we get a new image that highlights edges and other discontinuities



Original
Image



Laplacian
Filtered Image



Laplacian
Filtered Image
Scaled for Display

But That Is Not Very Enhanced!

- The result of a Laplacian filtering is not an enhanced image
- We have to do more work in order to get our final image
- Subtract the Laplacian result from the original image to generate our final sharpened enhanced image

$$g(x, y) = f(x, y) - \nabla^2 f$$



Laplacian Filtered Image
Scaled for Display

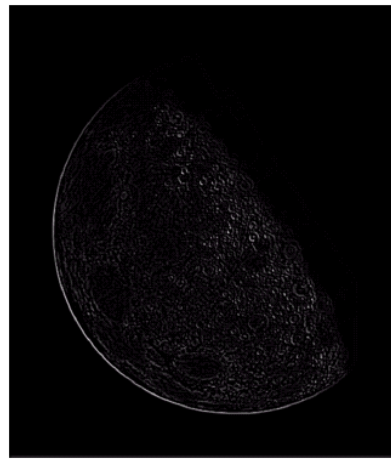
Laplacian Image Enhancement

- In the final sharpened image, edges and fine detail are much more obvious



Original
Image

—



Laplacian
Filtered Image

=



Sharpened
Image

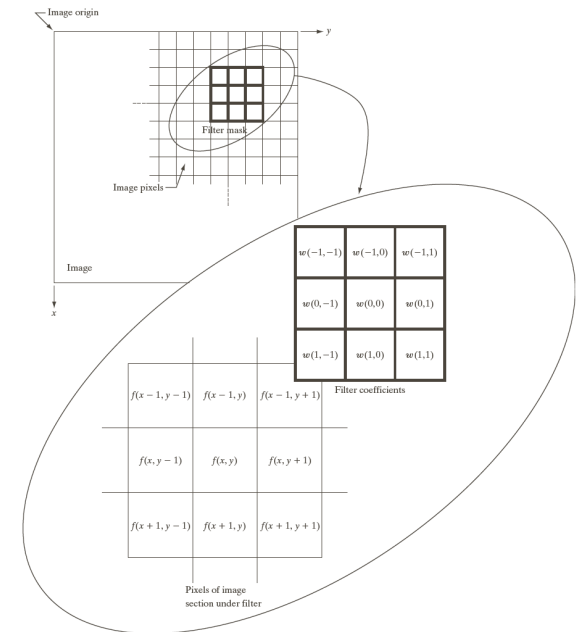
Laplacian Image Enhancement

```
%% laplacian %2B_PP32
f1 = imread('moon.tif');
w4 = fspecial('laplacian', 0);
g1 = imfilter(f1, w4);
f2 = im2double(f1);
g2 = imfilter(f2, w4);
g3 = imsubtract(f2, g2);
g4 = imadd(f2, g2);
figure;
subplot(2,2,1);imshow(f1);
subplot(2,2,2);imshow(g1, [ ]);
subplot(2,2,3);imshow(g2, [ ]);
subplot(2,2,4);imshow(g3);
figure;
subplot(2,1,1);imshow(g3);
subplot(2,1,2);imshow(g4);
```


Simplified Image Enhancement

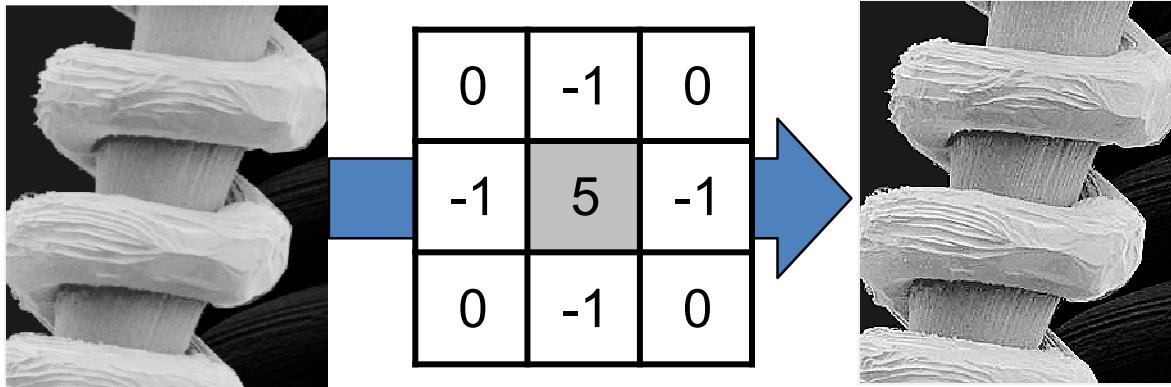
- The entire enhancement can be combined into a single filtering operation

$$\begin{aligned}
 g(x, y) &= f(x, y) - \nabla^2 f \\
 &= f(x, y) - [f(x+1, y) + f(x-1, y) + f(x, y+1) \\
 &\quad + f(x, y-1) - 4f(x, y)] \\
 &= 5f(x, y) - f(x+1, y) - f(x-1, y) \\
 &\quad - f(x, y+1) - f(x, y-1)
 \end{aligned}$$



Simplified Image Enhancement

- This gives us a new filter which does the whole job for us in one step



Variants On The Simple Laplacian

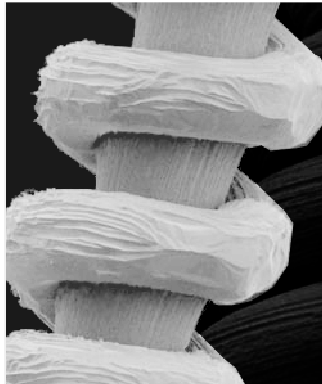
- There are lots of slightly different versions of the Laplacian that can be used:

0	1	0
1	-4	1
0	1	0

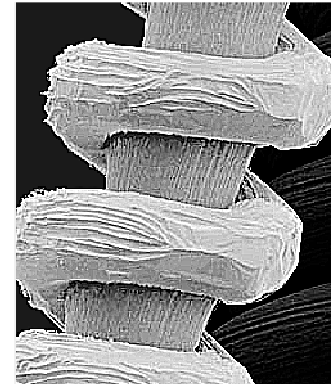
Simple
Laplacian

1	1	1
1	-8	1
1	1	1

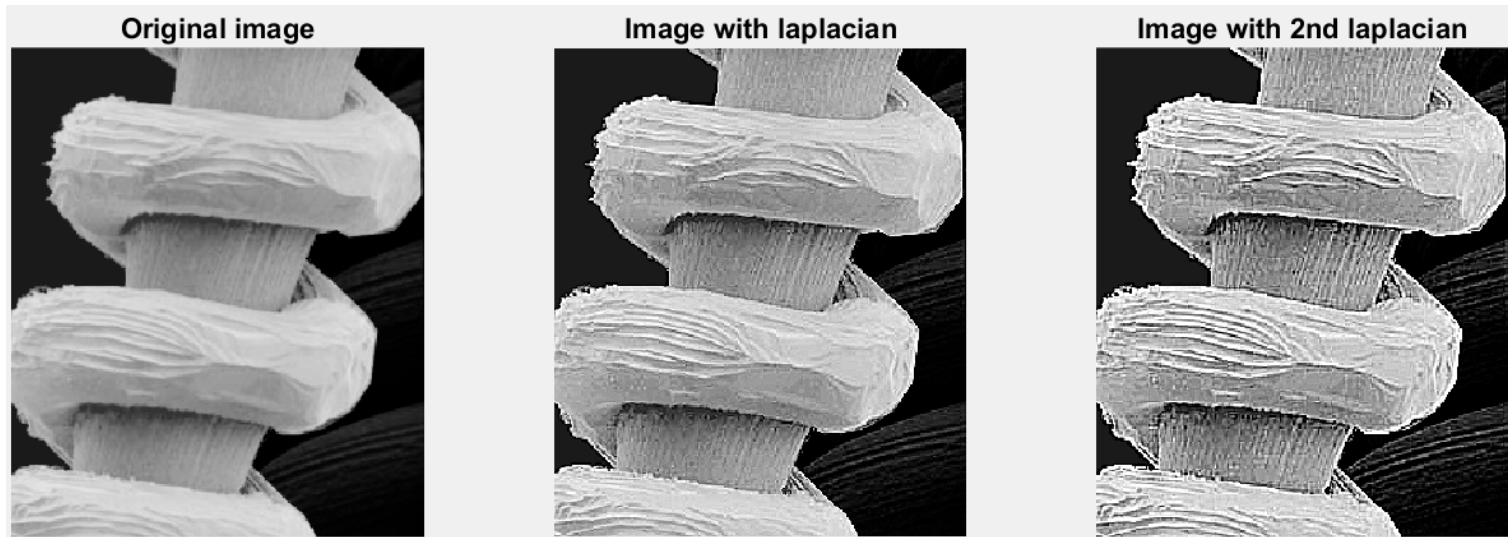
Variant of
Laplacian



-1	-1	-1
-1	9	-1
-1	-1	-1



Comparison of Two Laplacians



```
%% simplified laplacian %2B_PP37
% Laplacian simplification

f1 = imread ('edge.tif');
w5 = [0 -1 0; -1 5 -1; 0 -1 0];
g1 = imfilter (f1, w5);
w9 = [-1 -1 -1; -1 9 -1; -1 -1 -1];
g2 = imfilter (f1, w9);
figure;
subplot(1,3,1);imshow(f1);title('Original image')
subplot(1,3,2);imshow(g1);title('Image with laplacian')
subplot(1,3,3);imshow(g2);title('Image with 2nd laplacian')
```

First Derivatives: Gradient Operator

- First derivatives are implemented using the magnitude of the gradient

$$\nabla f = \begin{bmatrix} G_x \\ G_y \end{bmatrix} = \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \end{bmatrix} \quad \nabla f = \text{mag}(\nabla f) = [G_x^2 + G_y^2]^{\frac{1}{2}}$$
$$= \left[\left(\frac{\partial f}{\partial x} \right)^2 + \left(\frac{\partial f}{\partial y} \right)^2 \right]^{\frac{1}{2}}$$

Approximation:

$$\nabla f \approx |G_x| + |G_y|$$

Gradient Mask

- On the basis of a first-order derivative of a 2-D function $f(x,y)$, the simplest approximation of the gradient mask: 2x2

$$G_x = (z_8 - z_5) \quad \text{and} \quad G_y = (z_6 - z_5)$$

$$\nabla f = [G_x^2 + G_y^2]^{1/2} = [(z_8 - z_5)^2 + (z_6 - z_5)^2]^{1/2}$$

$$\nabla f \approx |z_8 - z_5| + |z_6 - z_5|$$

z_1	z_2	z_3
z_4	z_5	z_6
z_7	z_8	z_9

Gradient Mask

- Roberts 2x2 cross-gradient operators [1965]

$$G_x = (z_9 - z_5) \quad \text{and} \quad G_y = (z_8 - z_6)$$

$$\nabla f = [G_x^2 + G_y^2]^{1/2} = [(z_9 - z_5)^2 + (z_8 - z_6)^2]^{1/2}$$

$$\nabla f \approx |z_9 - z_5| + |z_8 - z_6|$$

z_1	z_2	z_3
z_4	z_5	z_6
z_7	z_8	z_9

-1	0	0	-1
0	1	1	0

Gradient Mask

- Sobel operators, 3x3

$$G_x = (z_7 + 2z_8 + z_9) - (z_1 + 2z_2 + z_3)$$

$$G_y = (z_3 + 2z_6 + z_9) - (z_1 + 2z_4 + z_7)$$

$$\nabla f \approx |G_x| + |G_y|$$

z_1	z_2	z_3
z_4	z_5	z_6
z_7	z_8	z_9

The weight value 2 is to achieve smoothing by giving more important to the center point

-1	-2	-1
0	0	0
1	2	1

-1	0	1
-2	0	2
-1	0	1

Example

Original

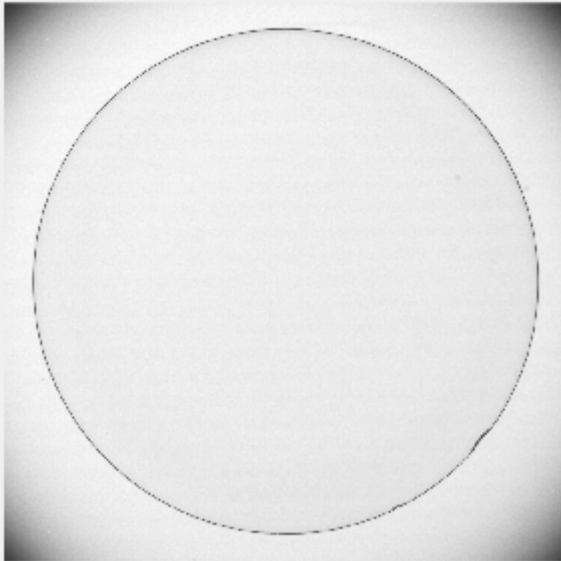
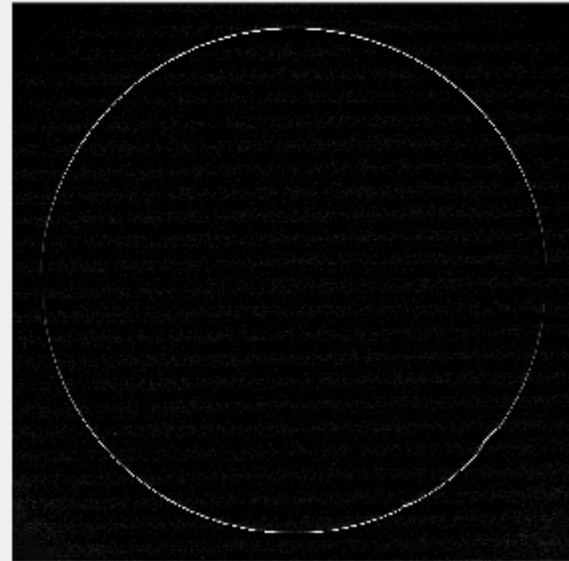


Image with sobel



```
%% sobel transform %2B_PP42
f1 = imread('circle.tif');
w = fspecial('sobel');
g1 = imfilter(f1, w);
figure;
subplot(1,2,1);imshow(f1); title('Original');
subplot(1,2,2);imshow(g1);title('Image with sobel');
```