=)
$$S_{1}(t) = \sum_{R=-\infty}^{\infty} \delta(t-R) = \sum_{R=-\infty}^{\infty} e^{j2\pi Rt} = 1+2\sum_{R=1}^{\infty} C_{s}(2\pi Rt)$$

b)
$$C_o = \frac{A}{2\pi} \int_{-\frac{\pi}{4}}^{\frac{3\pi}{4}} dt = \frac{A}{2}$$
, $\omega_o = \frac{2\pi}{2\pi} = 1$

The given signal XIII is time-shifted version of Ex 3-2) a) in the lecture note

$$X(t) = X_a(t + \frac{\pi}{4})$$
 where FS d_R of $X_a(t)$ is derived as

$$d_{k} = \begin{cases} 0 & \text{for even } R = 2m \\ \frac{A}{j\pi(2m+1)} & \text{for odd } R = 2m+1 \end{cases}$$

Hence, the FS coefficient CR of X(t) is given by

$$C_{k} = e^{jk\frac{\pi}{4}} d_{k} = \frac{A e^{jk\frac{\pi}{4}}}{j2\pi k} \left[1 - e^{-j\pi x}\right] = \frac{A e^{jk\frac{\pi}{4}}}{j2\pi k} \left(1 - (i)^{k}\right)$$

=
$$\begin{cases} 6 & \text{for even } k = 2m \\ \frac{A e^{j k \frac{\pi}{4}}}{j \pi (2m+1)} & \text{for odd } k = 2m+1 \end{cases}$$

$$C_0 = \frac{A}{2}$$

$$C_{k} = \frac{A}{j 2 \pi k} \left[e^{j k \frac{\pi}{4}} - e^{-j k \frac{\pi}{4}} \right] \propto \frac{A e^{-j \frac{\pi}{4}}}{2} \operatorname{Sinc}\left(\frac{R}{2}\right) \text{ are all ok.}$$

Test 2. Salution)

Q1. ()
$$f(sinc^{2}(2Bt)) = \frac{1}{2B} tri\left(\frac{f}{2B}\right)$$

$$\int \left(C_{05}(2xf_{0}t) \operatorname{Sinc}^{2}(2ht) \right) = \frac{1}{4h} \left[\operatorname{tri}\left(\frac{f - f_{0}}{2h}\right) + \operatorname{tri}\left(\frac{f + f_{0}}{2h}\right) \right]$$

Hence
$$f$$
 [4B Sinc²(2Bt) (es (2 π fot)]
= $\left[tri \left(\frac{f-f_0}{2B} \right) + tri \left(\frac{f+f_0}{2B} \right) \right]$

$$\hat{\mathbb{Q}}$$
 2. a) $T_0 = 2$. $\omega_0 = \frac{2\pi}{T_0} = \pi$

$$C_0 = \frac{1}{2} \int_{c}^{2} \cdot \frac{3t}{2} dt = \frac{3}{4} \cdot \frac{t^2}{2} \Big|_{c}^{2} = \frac{3}{2}$$

$$C_{R} = \frac{1}{2} \int_{0}^{2} \frac{3t}{2} e^{-jR\pi t} dt = \frac{3}{4} \int_{0}^{2} t e^{-jR\pi t} dt$$

$$=\frac{3}{4}\left[\left(\frac{t}{-jk\pi}-\frac{1}{(-jk\pi)^2}\right)e^{-jk\pi t}\right]^2$$

$$=\frac{3}{4}\left[\left(\frac{2}{jk\pi}-\frac{1}{(-jk\pi)^2}\right)e^{-j2\pi k}-\left(-\frac{1}{(-jk\pi)^2}\right)\right] \qquad \text{where } e^{-j2\pi k}$$

$$= \frac{3j}{2R\pi} = 0 \qquad a_0 = 2C_0 = 3 \qquad b_R = -2I_m(C_R) = -\frac{3}{R\pi}$$

$$Q_R = 2R_0(C_R) = 0$$

Test 2. Solution)

Q2. a)

$$\mathcal{K}(t) = \frac{3}{2} + \frac{3i}{2\pi} \sum_{R=-c0}^{c0} \frac{1}{R} e^{jR\pi t}$$

$$R \neq 0$$

$$= \frac{3}{2} + \left(-\frac{3}{\pi}\right) \frac{50}{k} \frac{1}{k} S_{M} \left(k\pi t\right) \qquad for \qquad 0 < t < 2$$

$$\frac{3t}{2} - \frac{3}{2} = -\frac{3}{\pi} \sum_{k=1}^{\infty} \frac{1}{k} \operatorname{Sin}(k\pi t) - 0$$

let's assume
$$t=\frac{1}{2}$$
, then (1) becomes

$$\frac{\sum_{k=1}^{\infty} \int_{R} S_{in}\left(\frac{RT}{2}\right) = \frac{T}{4}$$

$$=) 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots = \frac{7}{4}$$

Hence, the sum of the infinite series is 4

(c)
$$P = \frac{1}{2} \int_{c}^{2} |\chi(t)|^{2} dt = \frac{c_{0}}{R = -c_{0}} |C_{R}|^{2}$$

(left-hand) =
$$\frac{1}{2} \cdot \frac{9}{4} \int_{0}^{2} t^{2} dt = \frac{9}{5} \cdot \frac{1}{3} t^{3} \Big|_{0}^{2} = 3$$
.

(Right-hand) =
$$\frac{9}{4} + 2 \times \frac{9}{4\pi^2} = \frac{00}{R=1} \times \frac{1}{R^2}$$
Negative & and Positive & are symmetrice

Test 2. Solution

Q2. C) One to the Parseval's theorem.

$$3 = \frac{9}{4} \left[1 + \frac{2}{\pi^2} \sum_{k=1}^{\infty} \frac{1}{k^2} \right]$$

=) Hence, the sum of the infinite series it

$$\frac{\sum_{k=1}^{\infty}\frac{1}{k^2}-\frac{\chi^2}{6}$$

Q3.
$$\mathcal{X}_{(+)}$$

$$\begin{array}{c}
dx \\
dt
\end{array}$$

$$\frac{1}{\left(\frac{dx}{dt}\right)} = \int_{0}^{1} e^{-j2xft} dt - \int_{2}^{3} e^{-j2xft} dt$$

$$= \frac{1}{j2xf} \left(1 - e^{-j2xf}\right) + \frac{1}{j2xf} \left(e^{-j6xt} - e^{-j4xf}\right)$$

Hence
$$f(\chi(+)) = \frac{1}{4(\pi f)^2} \left[e^{-j2\pi f} - 1 - e^{-j6\pi f} + e^{-j4\pi f} \right]$$

Test 2. Solution)

Q4, a) Since the BW of Cos (15071+), Sin (30071+), Cos(607) are fi=75, f=150, f=300, respectively, The BW of signal X(+) is fm = 300 Hz.

Hence, the Nyquist sampling rate 2 fm = 600 Hz.

$$f(S_{inc^{2}(t)}) = tri(f)$$

$$f(f) = \int_{f(f)}^{f(f)} f(f)$$

368 BW: |H(c)| = 1 and $|H(f_{348})| = \frac{|H(c)|}{\sqrt{2}} = \frac{1}{\sqrt{2}}$

$$f_{3olg} = 1 - \frac{1}{\sqrt{2}} = \frac{\sqrt{2} - 1}{\sqrt{2}}$$

Equivalent BW: $f_{e_f} = \int_0^1 |H(t)|^2 dt = \int_0^1 t^2 dt = \frac{1}{3}$

Hence
$$\int f_3 dg = 1 - \sqrt{\frac{1}{2}}$$
 or $\frac{\sqrt{2}-1}{\sqrt{2}}$

(05. (i)
$$\{(j2xf)^2 + 7(j2xf) + 12\} Y(4) = (j2xf + 2) X(f)$$

$$H(f) = \frac{Y(f)}{X(f)} = \frac{(j2\pi f + 2)}{(j2\pi f)^2 + 7(j2\pi f) + 12} = \frac{(j2\pi f + 2)}{(j2\pi f + 4)(j2\pi f + 3)}$$

$$\int \frac{\alpha_1}{j \, 2\pi f + 4} + \frac{\alpha_2}{j \, 2\pi f + 3} \quad \text{Partial Expansion}$$

$$\lambda_1 = 2, \quad \alpha_2 = -1$$

$$h(t) = \left(2e^{-4t} - e^{-3t}\right) \, U(t)$$

If
b)
$$X(t) = e^{-2t} U(t)$$
, then $X(t) = \frac{1}{j \cdot 2\pi f + 2}$ and

$$Y(f) = H(f) X(f)$$

$$= \frac{j 2\pi f + 2}{(j 2\pi f + 4)(j 2\pi f + 3)} \times \frac{1}{j 2\pi f + 2}$$

$$= \frac{-1}{j 2\pi f + 4} + \frac{1}{j 2\pi f + 3}$$

$$J(t) = \left(-e^{-4t} + e^{-3t}\right) \mathcal{U}(t).$$