

1. Alice and Bob use the Diffie-Hellman key exchange protocol with the common prime  $p = 157$  and generator  $g = 5$ .
  - a) (2 points) Suppose Alice picks her private number as  $a = 64$ . Determine the public message she should send to Bob. Show your steps.
  - b) (2 points) Suppose Bob picks his private number as  $b = 94$ . During the key exchange phase, he received the number calculated in (a). Determine the shared secret key,  $k_{AB}$ . Show your steps.
2. Consider the RSA cryptosystem. Bob has public key ( $N = 37 \times 47$ ,  $e = 25$ ).
  - a) (2 marks) Use extended Euclidean algorithm to determine Bob's private key,  $d$ .
  - b) (2 marks) Alice wants to send the message  $m = 314$  to Bob. She encrypts the message using Bob's public key. What is the value of the ciphertext that Alice sends to Bob?