

Assignment 4

1.

$$p = 157$$

$$g = 5$$

A.

$$5(\bmod 157) = 5$$

$$5^2(\bmod 157) = 25(\bmod 157) = 25$$

$$5^4(\bmod 157) = 25^2(\bmod 157) = 154$$

$$5^8(\bmod 157) = 154^2(\bmod 157) = 9$$

$$5^{16}(\bmod 157) = 9^2(\bmod 157) = 81$$

$$5^{32}(\bmod 157) = 81^2(\bmod 157) = 124$$

$$5^{64}(\bmod 157) = 124^2(\bmod 157) = 147$$

$$a = 64$$

$$y_A = g^a(\bmod p)$$

$$= 5^{64}(\bmod 157)$$

$$= 147$$

B.

$$147(\bmod 157) = 147$$

$$147^2(\bmod 157) = 147^2(\bmod 157) = 100$$

$$147^4(\bmod 157) = 100^2(\bmod 157) = 109$$

$$147^8(\bmod 157) = 109^2(\bmod 157) = 106$$

$$147^{16}(\bmod 157) = 106^2(\bmod 157) = 89$$

$$147^{32}(\bmod 157) = 89^2(\bmod 157) = 71$$

$$147^{64}(\bmod 157) = 71^2(\bmod 157) = 17$$

$$b = 94$$

$$k_{AB} = y_A^b(\bmod p)$$

$$= 147^{94}(\bmod 157)$$

$$= 147^{10111110_b}(\bmod 157)$$

$$= 100 \times 109 \times 106 \times 89 \times 17(\bmod 157)$$

$$= 89$$

2.

$$\begin{aligned} N &= 37 \times 47 \\ &= 1739 \\ e &= 25 \end{aligned}$$

A.

$$\begin{aligned} \phi(N) &= (37 - 1)(47 - 1) \\ &= 1656 \\ ed &\equiv 1 \pmod{\phi(N)} \\ 25d &\equiv 1 \pmod{1656} \end{aligned}$$

1656	25		
1	0	1656	A
0	1	25	B
1	-66	6	$C = A - 66B$
-4	265	1	$D = B - 4C$

$$d = 265$$

B.

$$\begin{aligned} 314 \pmod{1739} &= 314 \\ 314^2 \pmod{1739} &= 1212 \\ 314^4 \pmod{1739} &= 1228 \\ 314^8 \pmod{1739} &= 271 \\ 314^{16} \pmod{1739} &= 403 \end{aligned}$$

$$\begin{aligned} m &= 314 \\ c &= m^e \pmod{N} \\ &= 314^{25} \pmod{1739} \\ &= 314^{11001_b} \pmod{1739} \\ &= 314 \times 271 \times 403 \pmod{1739} \\ &= 1541 \end{aligned}$$