

Modular I/O Reasoning in DimSum

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  let c :=getc();  
  putc(c);  
  return 0;
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$$\{\lambda es, \ulcorner es = [] \urcorner\}$$

echo

$$\{\lambda v, \ulcorner v = 0 \urcorner\}$$

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$$\left\{ \lambda \text{ es}, \lceil \text{es} = [] \rceil * \left\{ \lambda \text{ es}, \lceil \text{es} = [] \rceil \right\} \text{getc} \left\{ \lambda v, \left\{ \lambda \text{ es}, \lceil \text{es} = v \rceil \right\} \text{putc} \{ _ \} \right\} \right\} \\ \text{echo} \\ \left\{ \lambda v, \lceil v = 0 \rceil \right\}$$

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$$\{\lambda es, \ulcorner es = [] \urcorner * \exists v, P\ v * (getc_spec\ P) * (putc_spec\ P)\}$$

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$$\{\lambda \text{ es}, \exists v, \lceil \text{es} = v \rceil * P(v + 1)\} \text{putc} \{\lambda \text{ ret}, P(v + 1)\}$$
$$\{\lambda \text{ es}, \lceil \text{es} = [] \rceil * \exists v, P v\} \text{getc} \{\lambda \text{ ret}, \lceil \text{ret} = v \rceil * P(v + 1)\}$$
$$\{\lambda \text{ es}, \lceil \text{es} = [] \rceil * \exists v, P v * (\text{getc_spec } P) * (\text{putc_spec } P)\}$$

echo

$$\{\lambda v, \lceil v = 0 \rceil\}$$

- Decentralized/language-agnostic multi-language semantics
 - No fixed source
 - No fixed set of languages
 - No fixed memory model
 - No fixed notion of linking
- Program semantics as LTS, interaction via synchronization
 - Reason locally in terms of interaction of two modules
- Notion of semantic linking: \oplus
 - Link semantic components (modules) rather than syntactic
 - Link programs with specifications (abstract program)

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$$\llbracket \text{echo}_{\text{rec}} \oplus \text{getc}_{\text{spec}} \rrbracket \sqsubseteq \llbracket \text{echo}_{\text{spec}} \rrbracket$$

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$\llbracket \text{echo}_{\text{rec}} \oplus \text{getc}_{\text{spec}} \rrbracket$ \preceq $\llbracket \text{echo}_{\text{spec}} \rrbracket$

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TGT Call “echo” es @ $\Pi \{\{\Phi\}\}$

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```
int echo () :=  
  let c := getc();  
  putc(c);  
  return 0;
```

```
int getc (l) :=  
  let _ := read(l);  
  return *l;
```

```
void echo () :=  
  let c := getc();  
  putc(c);  
  echo ();
```

```
global pos = 0;  
read (l, c) :=  
  if (c <= 0) {  
    return 0;  
  } else {  
    l <- *pos;  
    pos <- *pos + 1;  
    ret = read(l + 1, c - 1);  
    return ret + 1;  
  }
```

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```
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TGT Call "getc" es @  $\Pi$ 
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```
PRE  $|-*: es$  POST,  $\exists v, P\ v * \lceil es = [] \rceil *$ 
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$$\llbracket \text{echo}_{\text{rec}} \oplus \text{getc}_{\text{spec}} \rrbracket \preceq \llbracket \text{echo}_{\text{spec}} \rrbracket$$

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Lemma sim_getc fns $\Pi_l \Pi_r$ PL σ_i :

"getc" \hookrightarrow None -*

PL σ_i -*

$\lceil \sigma_i.1 \equiv \text{getc_spec} \rceil$ -*

$\lceil \sigma_i.2 = 0 \rceil$ -*

\square switch_linked_fixed Tgt $\Pi_l \Pi_r$

PRE $|-*: \sigma_l$ POST, $\exists h v \sigma_g, \text{PL } \sigma_g *$

POST (ERCall "getc" \square h) $\sigma_g |-*: \sigma_r \Pi_r'$,

switch_link Tgt Π_r'

Pre $|-*: \sigma_r'$ POST, $\exists h'$

POST (ERReturn (ValNum v) h') $_ \sigma_l |-*: _ \Pi_l'$,

$\lceil \Pi_l' = \Pi_l \rceil * \text{PL } \sigma_r' ==*$

$\exists P, P 0 * \square \text{rec_fn_spec_hoare Tgt } \Pi_l \text{"getc" (getc_fn_spec P)}.$

$$\llbracket \text{echo}_{\text{rec}} \oplus \text{getc}_{\text{spec}} \rrbracket \preceq \llbracket \text{echo}_{\text{spec}} \rrbracket$$

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  "getc"  $\hookrightarrow$  None -*
  PL  $\sigma_i$  -*
   $\ulcorner \sigma_i.1 \equiv \text{getc\_spec} \urcorner$  -*
   $\ulcorner \sigma_i.2 = 0 \urcorner$  -*
   $\square$  switch_linked_fixed Tgt  $\Pi_l$   $\Pi_r$ 
    PRE  $\vdash$   $\sigma_l$  POST,  $\exists$  h v  $\sigma_g$ , PL  $\sigma_g$  *
    POST (ERCall "getc"  $\square$  h)  $\sigma_g \vdash$   $\sigma_r$   $\Pi_r'$ ,
    switch_link Tgt  $\Pi_r'$ 
    Pre  $\vdash$   $\sigma_r'$  POST,  $\exists$  h'
    POST (ERReturn (ValNum v) h')  $\_ \sigma_l \vdash$   $\_ \Pi_l'$ ,
     $\ulcorner \Pi_l' = \Pi_l \urcorner$  * PL  $\sigma_r'$  ==*
     $\exists$  P, P 0 *  $\square$  rec_fn_spec_hoare Tgt  $\Pi_l$  "getc" (getc_fn_spec P).
  
```

$$\llbracket \text{echo}_{\text{rec}} \oplus \text{getc}_{\text{spec}} \rrbracket \preceq \llbracket \text{echo}_{\text{spec}} \rrbracket$$

```

Lemma sim_getc fns  $\Pi_l$   $\Pi_r$  PL  $\sigma_i$  :
  "getc"  $\hookrightarrow$  None -*
  PL  $\sigma_i$  -*
   $\ulcorner \sigma_i.1 \equiv \text{getc\_spec} \urcorner$  -*
   $\ulcorner \sigma_i.2 = 0 \urcorner$  -*
   $\square$  switch_linked_fixed Tgt  $\Pi_l$   $\Pi_r$ 
    PRE  $\mid$  -:  $\sigma_l$  POST,  $\exists$  h v  $\sigma_g$ , PL  $\sigma_g$  *
    POST (ERCall "getc"  $\square$  h)  $\sigma_g$   $\mid$  -:  $\sigma_r$   $\Pi_r'$ ,
    switch_link Tgt  $\Pi_r'$ 
      Pre  $\mid$  -:  $\sigma_r'$  POST,  $\exists$  h'
      POST (ERReturn (ValNum v) h')  $\_$   $\sigma_l$   $\mid$  -:  $\_$   $\Pi_l'$ ,
       $\ulcorner \Pi_l' = \Pi_l \urcorner$  * PL  $\sigma_r'$  ==*
   $\exists$  P, P 0 *  $\square$  rec_fn_spec_hoare Tgt  $\Pi_l$  "getc" (getc_fn_spec P).
  
```

$$\llbracket \text{echo}_{\text{rec}} \oplus \text{getc}_{\text{spec}} \rrbracket \preceq \llbracket \text{echo}_{\text{spec}} \rrbracket$$

```

Lemma sim_getc fns  $\Pi_l$   $\Pi_r$  PL  $\sigma_i$  :
  "getc"  $\hookrightarrow$  None -*
  PL  $\sigma_i$  -*
   $\lceil \sigma_i.1 \equiv \text{getc\_spec} \rceil$  -*
   $\lceil \sigma_i.2 = 0 \rceil$  -*
   $\square$  switch_linked_fixed Tgt  $\Pi_l$   $\Pi_r$ 
    PRE  $|$  -:  $\sigma_l$  POST,  $\exists$  h v  $\sigma_g$ , PL  $\sigma_g$  *
    POST (ERCall "getc"  $\square$  h)  $\sigma_g$   $|$  -:  $\sigma_r$   $\Pi_r'$ ,
    switch_link Tgt  $\Pi_r'$ 
      Pre  $|$  -:  $\sigma_r'$  POST,  $\exists$  h'
      POST (ERReturn (ValNum v) h')  $_$   $\sigma_l$   $|$  -:  $_$   $\Pi_l'$ ,
       $\lceil \Pi_l' = \Pi_l \rceil$  * PL  $\sigma_r'$  ==*
   $\exists$  P, P 0 *  $\square$  rec_fn_spec_hoare Tgt  $\Pi_l$  "getc" (getc_fn_spec P).
  
```

```

Lemma sim_getc fns  $\Pi_l \Pi_r$  PL  $\sigma_i$  :
  "getc"  $\hookrightarrow$  None -*
  PL  $\sigma_i$  -*
   $\lceil \sigma_i.1 \equiv \text{getc\_spec} \rceil$  -*
   $\lceil \sigma_i.2 = 0 \rceil$  -*
   $\square$  switch  $\Pi_l$ 
    PRE |-*:  $\kappa \sigma_0$  POST,  $\exists h v \sigma_g$ , PL  $\sigma_g$  *
    POST Tgt _ _ |*:  $\sigma_{i0} \Pi_i$ ,  $\lceil \sigma_{i0} = \sigma_g \rceil$  *  $\lceil \Pi_i = \Pi_r \rceil$  *
  switch  $\Pi_i$ 
    PRE |-*:  $\kappa' \sigma$  POST0,  $\exists e' : \text{rec\_ev}$ ,  $\lceil \kappa' = \text{Some (Incoming, } e') \rceil$  *
    POST0 Tgt _ _ |*:  $\sigma_r \Pi_r$ ,  $\lceil \sigma_r = \sigma \rceil$  *  $\lceil e' = \text{ERCall "getc" [] } h \rceil$  *
  switch  $\Pi_r$ 
    PRE |-*:  $\kappa_0 \sigma_1$  POST1,  $\exists h'$ ,  $\lceil \kappa_0 = \text{Some (Outgoing, ERReturn } v \ h') \rceil$  *
    POST1 Tgt _ _ |*:  $\sigma_{i1} \Pi_{i0}$ ,  $\lceil \sigma_{i1} = \sigma_0 \rceil$  *
  switch  $\Pi_{i0}$ 
    PRE |-*:  $\kappa'_0 \sigma_2$  POST2,  $\exists e'_0$ ,  $\lceil \kappa'_0 = \text{Some (Incoming, } e'_0) \rceil$  *
    POST2 Tgt _ _ |*:  $\sigma_{r0} \Pi_{r0}$ ,
       $\lceil \sigma_{r0} = \sigma_2 \rceil$  *  $\lceil e'_0 = \text{ERReturn } v \ h' \rceil$  *  $\lceil \Pi_{r0} = \Pi_l \rceil$  * PL  $\sigma_1 ==$ 
   $\exists P, P \ 0$  *  $\square$  rec_fn_spec_hoare Tgt  $\Pi_l$  "getc" (getc_fn_spec P).
  
```

- Lemma for TCallRet
- Keep Π s the same - new lemmas for linking
- Balance between Abstraction and Information
- Balance between Hacking and Thinking