

# PHYS2326

## Lecture #14

Prof. Fabiano Rodrigues

Department of Physics  
The University of Texas at Dallas

# Goals for the lecture

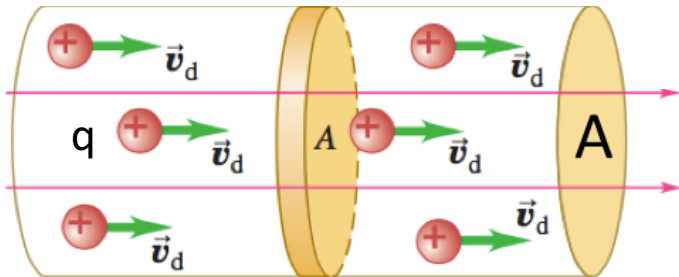
- Review and finish our analysis of Ohm's Law
- Resistors in series and parallel (Sec. 26.1)
- Electric Meters: Voltmeter and Ammeter
- The Electromotive Force (EMF)

Chapter 25 + 26.1

# Charges in Motion

# Electric Current: Definition

- **Electric current ( $I$ )** is the amount of charge flowing through an specific cross section area per unit of time.

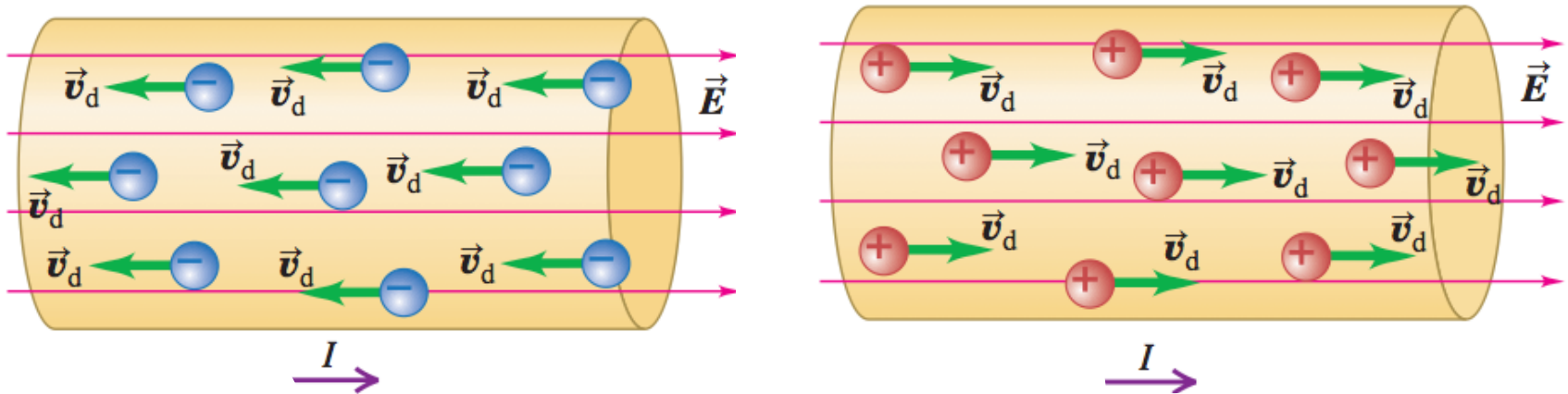


$$I = \frac{dQ}{dt}$$

$$I_{avg} = \frac{\Delta Q}{\Delta t}$$

# Direction of Electric Current

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- **Direction of current:** Convention is that current points in the direction that positive charges would flow.

# Electric Current Density ( $\mathbf{J}$ )

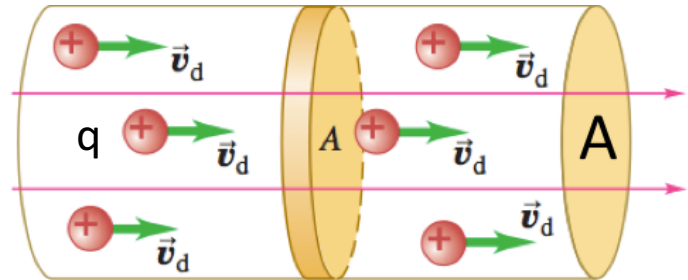
# Electric Current Density (J)

$$J = \frac{I}{A} = |q|nv_d$$

Vector current density:

$$\vec{J} = qn\vec{v}_d$$

$$\text{Units: } C/(m^2s) = A/m^2$$



$A$  = cross - section [ $m^2$ ]

$v_d$  = drift velocity [ $m/s$ ]

$q$  = charge [ $C$ ]

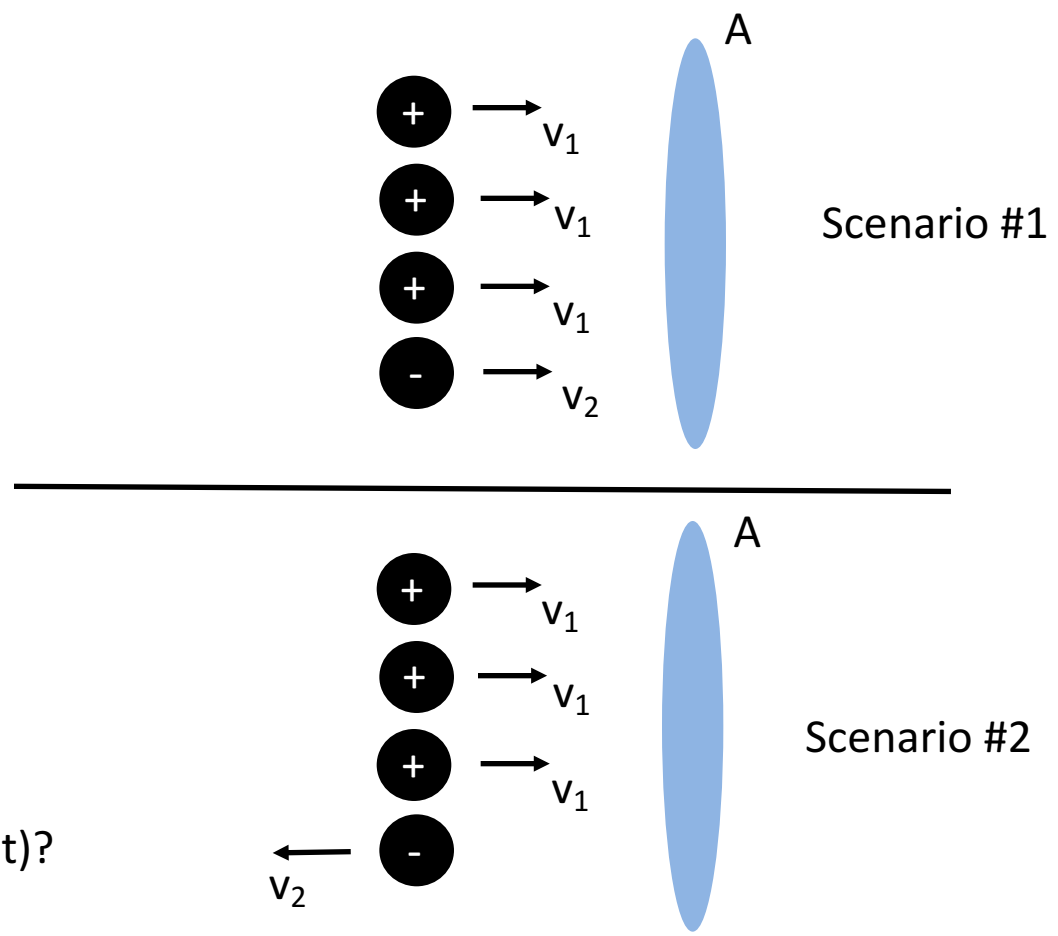
$n$  = volume charge density [ $m^{-3}$ ]



# Analysis: Current

$$\vec{J} = qn\vec{v}_d$$
$$\vec{J} = \sum_{i=1}^N q_i n_i \vec{v}_{d,i}$$

What scenario illustrates a larger current density (or current)?

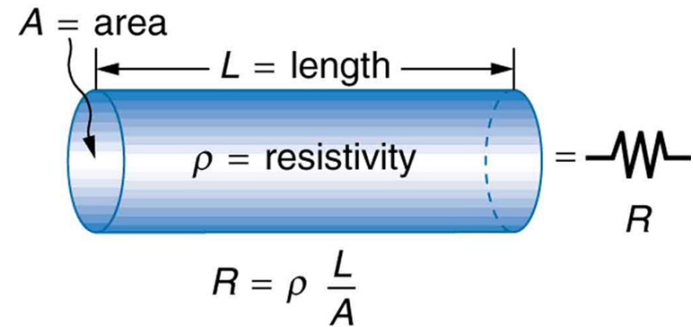


# Ohm's Law: Resistivity and Resistance

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$$\vec{E} = \rho \vec{J}$$

$$V = RI$$



$\rho = \text{resistivity } [\Omega \cdot m \text{ or ohm} \cdot m]$

$$R = \rho \frac{L}{A} = \text{resistance } [\Omega]$$

# Resistors



- **Resistors** are electric circuit devices made with a specific value of resistance.

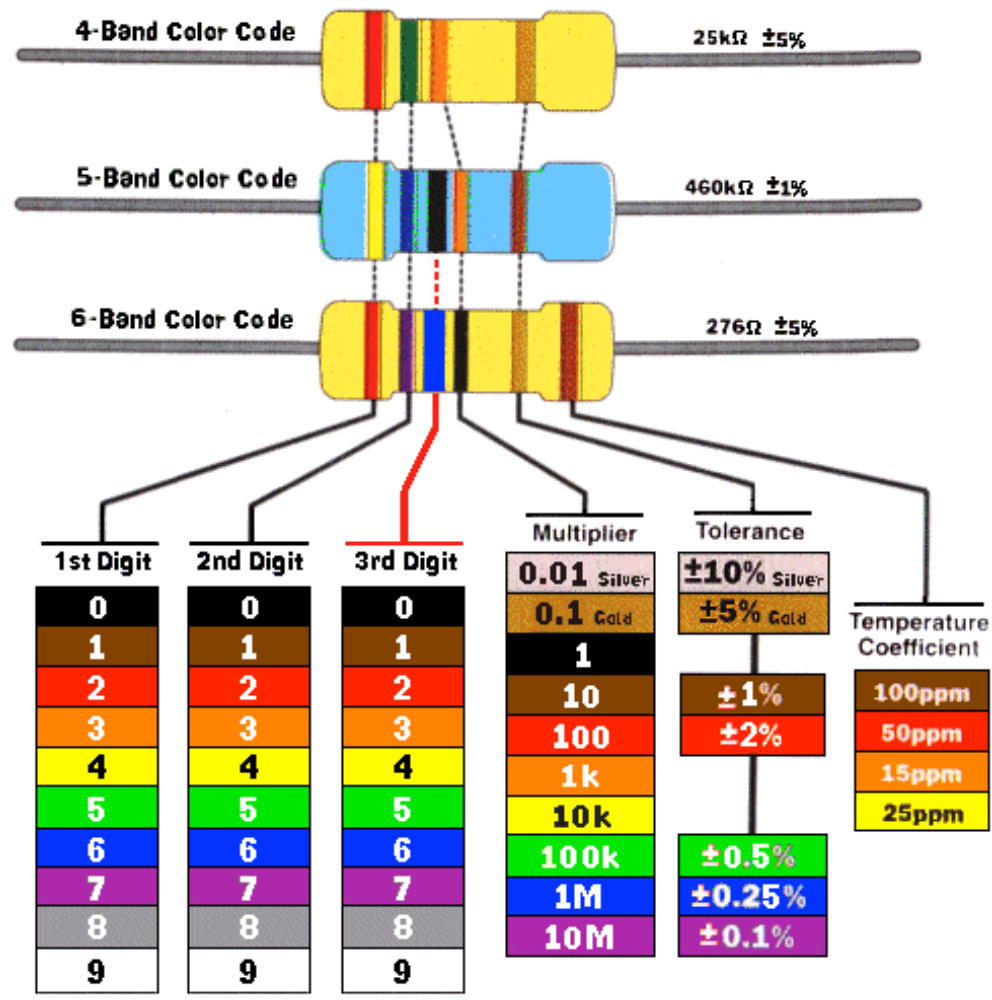
- Symbol:



$$R = \frac{V}{I}$$

- Unit:  $\Omega$  (ohm)

# Resistors



ppm/ $^{\circ}$ C (parts per million per  $^{\circ}$ C)  
 Example: 15 ppm  
 It will not change more than  
 $15 \times 10^{-6} \Omega / ^{\circ}\text{C}$  from value at  $25^{\circ}\text{C}$

**Example:** The current in a wire varies with time according to the relation:

$$I = 55 \text{ A} - (0.65 \text{ A/s}^2)t^2.$$

How many coulombs of charge pass a cross section of the wire in the time interval between  $t=0$  and  $t = 7.5 \text{ s}$  ?

$$I = \frac{dq}{dt}$$

$$|\vec{J}| = \frac{|\vec{E}|}{\rho}$$

$$V = \left( \frac{\rho L}{A} \right) I$$

$$R = \frac{\rho L}{A}$$

$$V = RI$$

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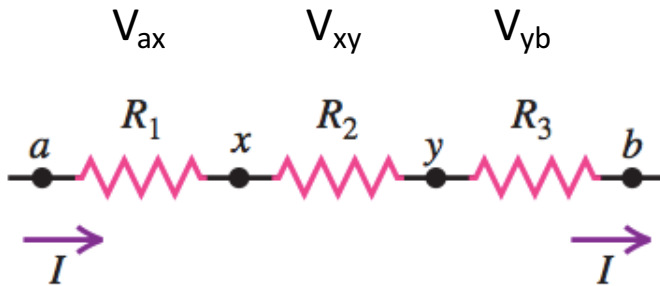
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# Resistors in Series and Parallel

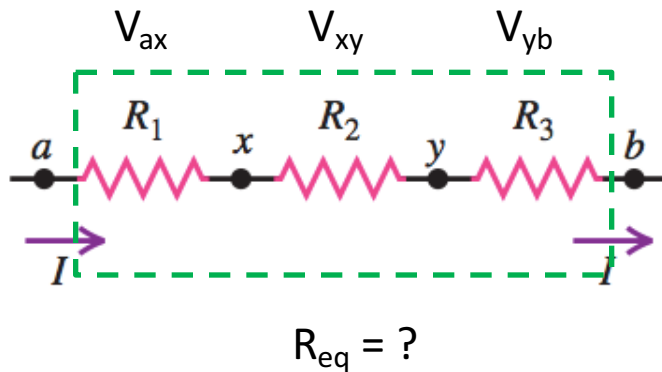
# Resistors in Series

- Resistors share the same current ( $I$ )
- Resistors have distinct potential differences ( $V$ )



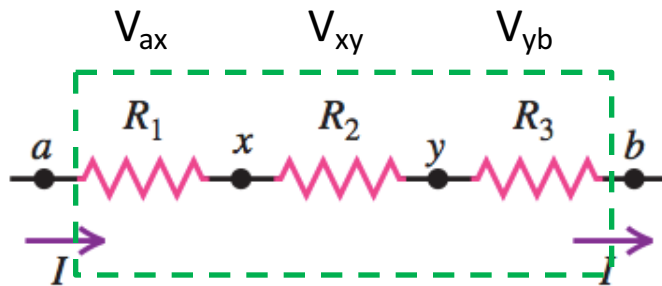
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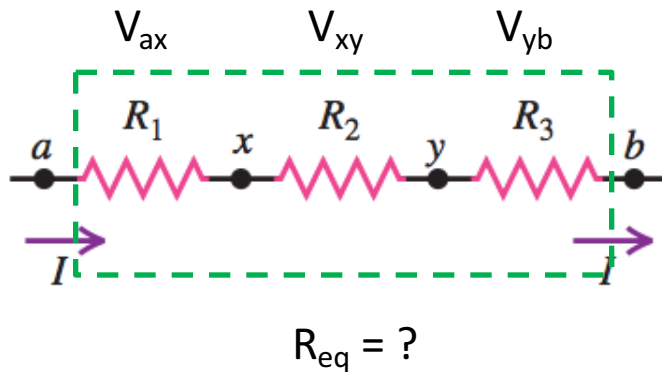
$$R_{eq} = ?$$

$$V_{ab} = V_{ax} + V_{xy} + V_{yb}$$



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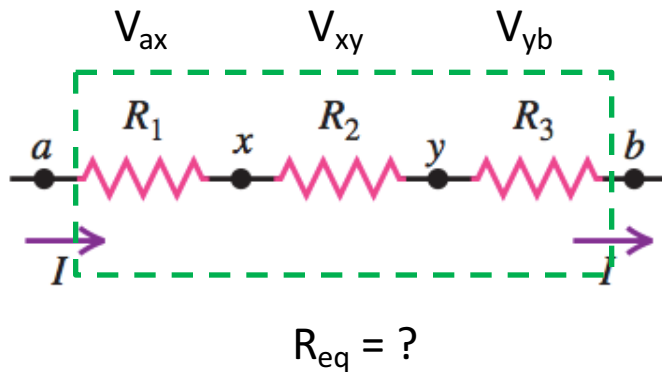


$$V_{ab} = V_{ax} + V_{xy} + V_{yb}$$

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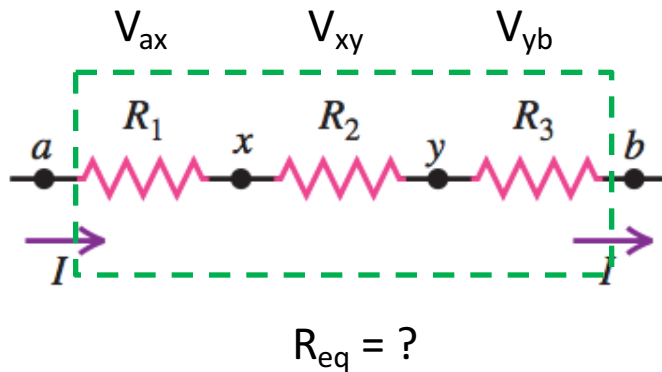
$$V_{ab} = V_{ax} + V_{xy} + V_{yb}$$

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$$\frac{V_{ab}}{I} = R_1 + R_2 + R_3$$

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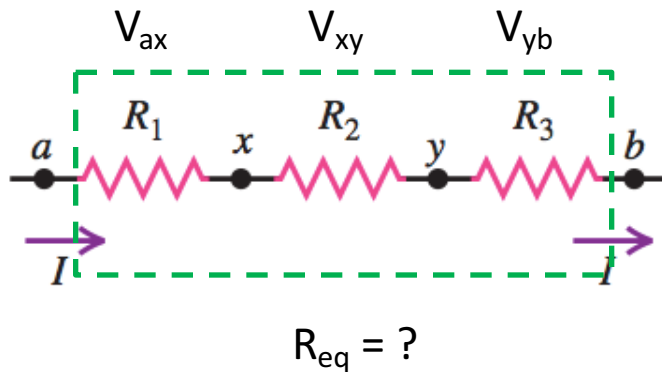
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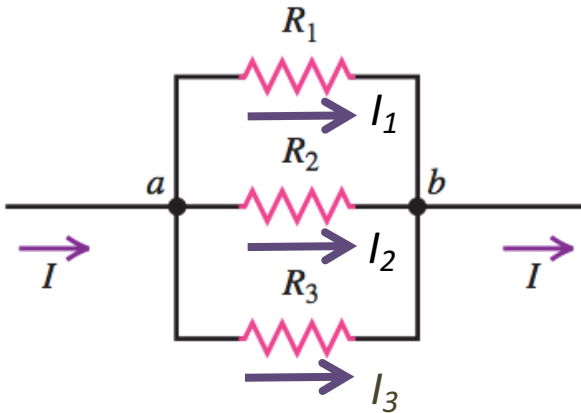
$$R_{eq} = R_1 + R_2 + R_3 + \dots + R_N$$

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$$R_{eq} = \sum_{i=1}^N R_i$$

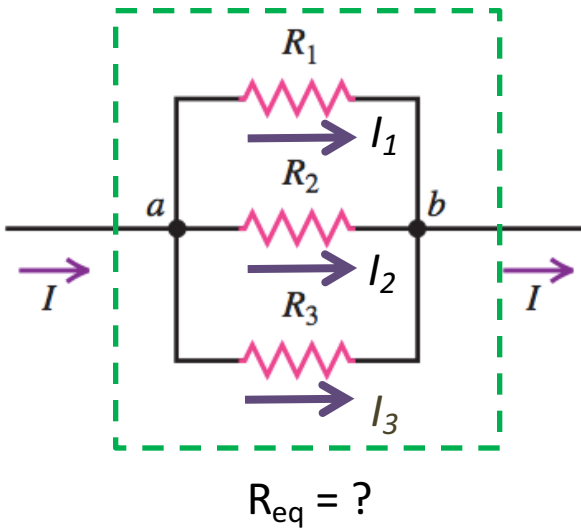
# Resistors in Parallel

- Resistors share the same potential difference ( $V_{ab}$ )
- Resistors have distinct currents ( $I$ )



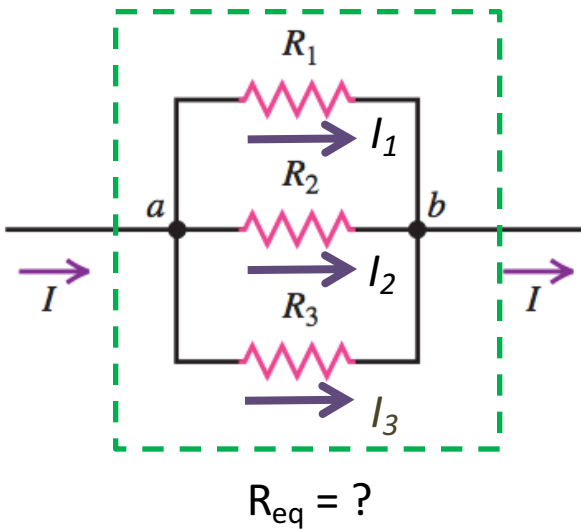
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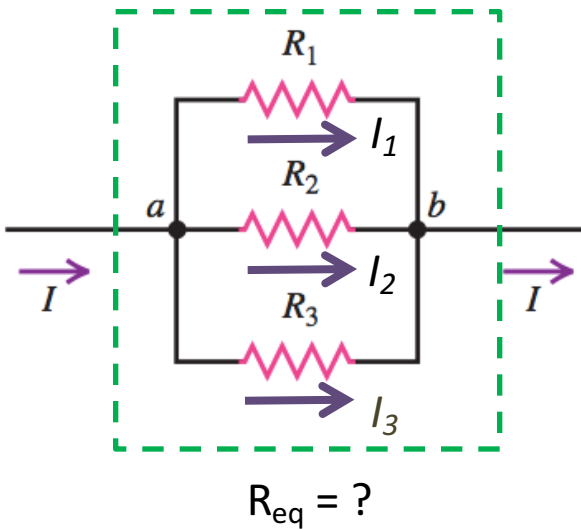
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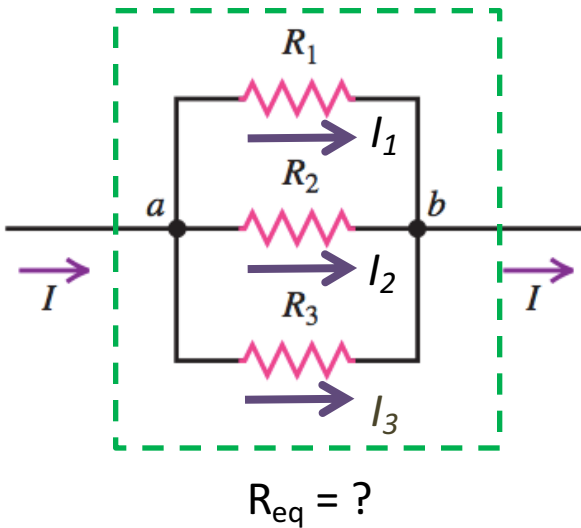
$$I = I_1 + I_2 + I_3$$

$$\frac{V_{ab}}{R_{eq}} = \frac{V_{ab}}{R_1} + \frac{V_{ab}}{R_2} + \frac{V_{ab}}{R_3}$$



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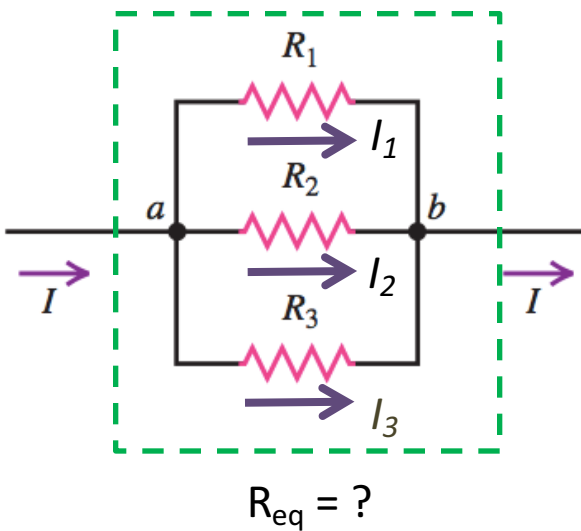
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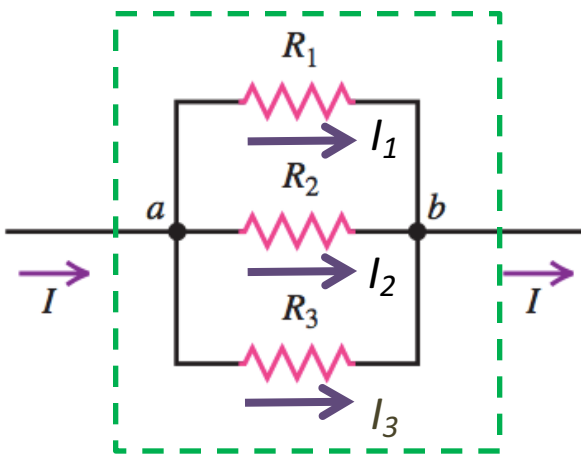
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$$R_{eq} = ?$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$$

$$\frac{1}{R_{eq}} = \sum_{i=1}^N \frac{1}{R_i}$$

$$I = I_1 + I_2 + I_3$$

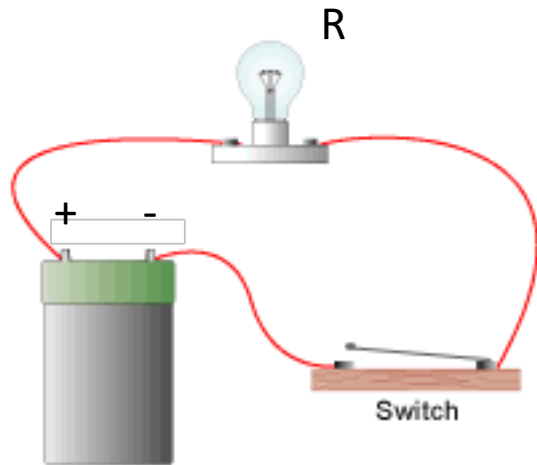
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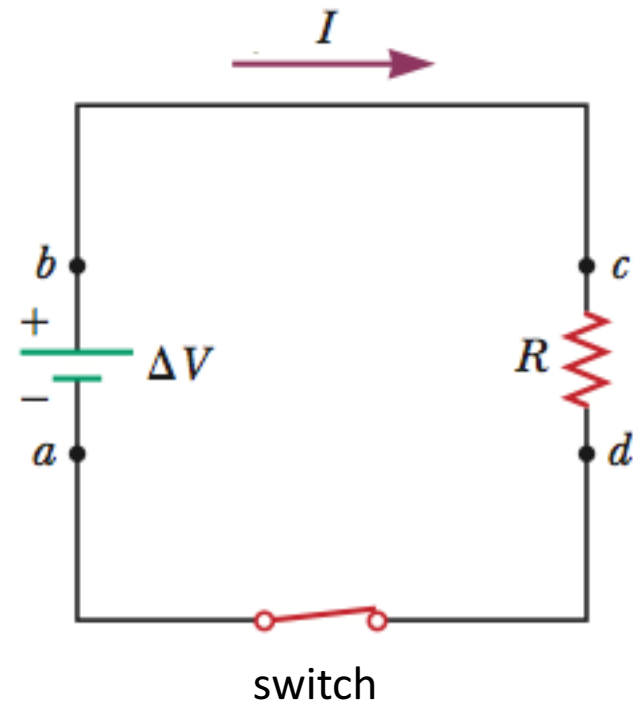
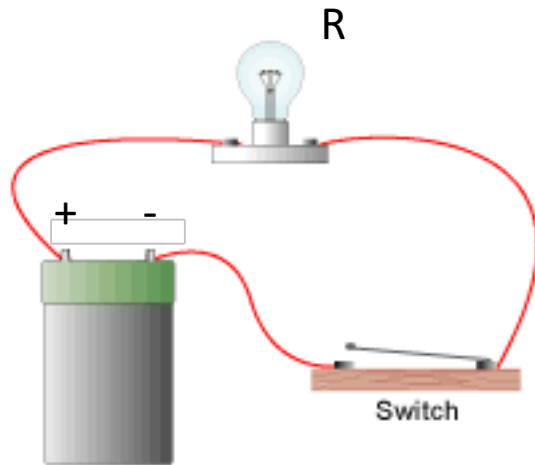
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# Describing Circuits

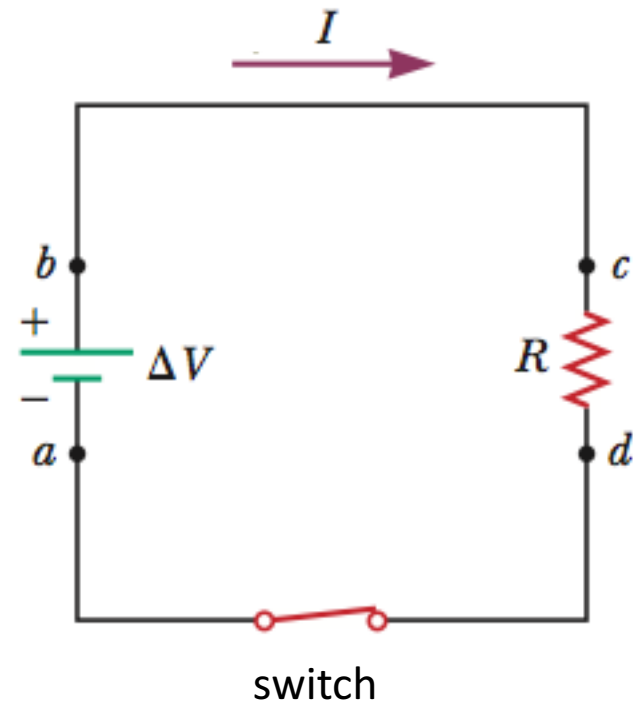
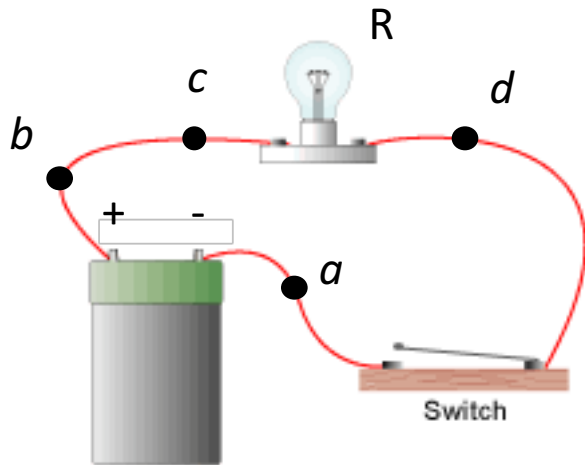
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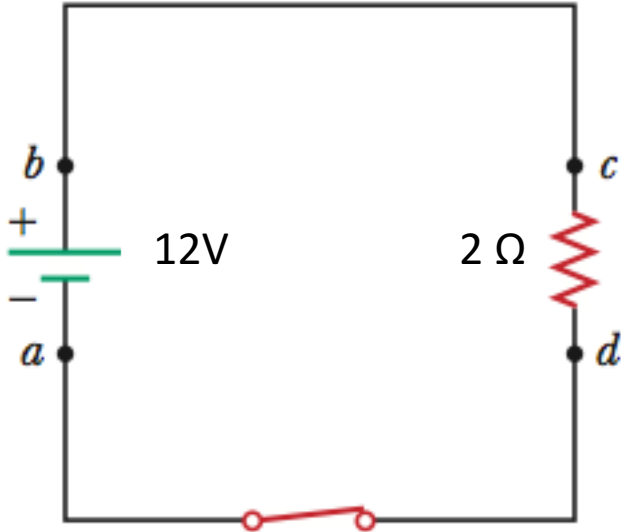
# Describing Circuits



# Example: Ohm's Law

Consider the circuit shown :

(a) What is the direction of the current?

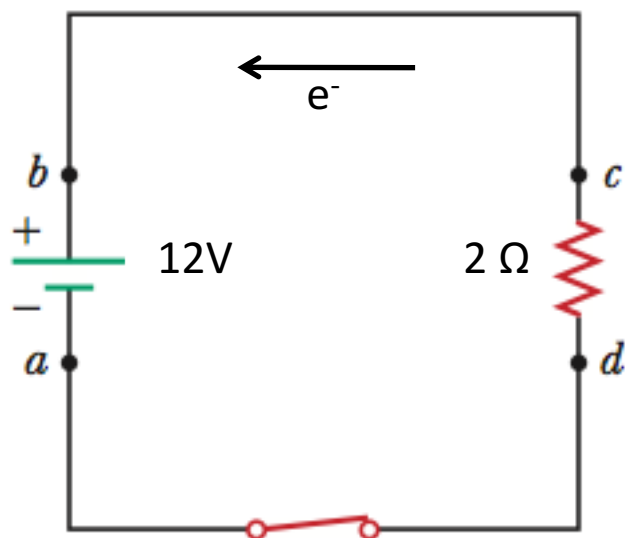




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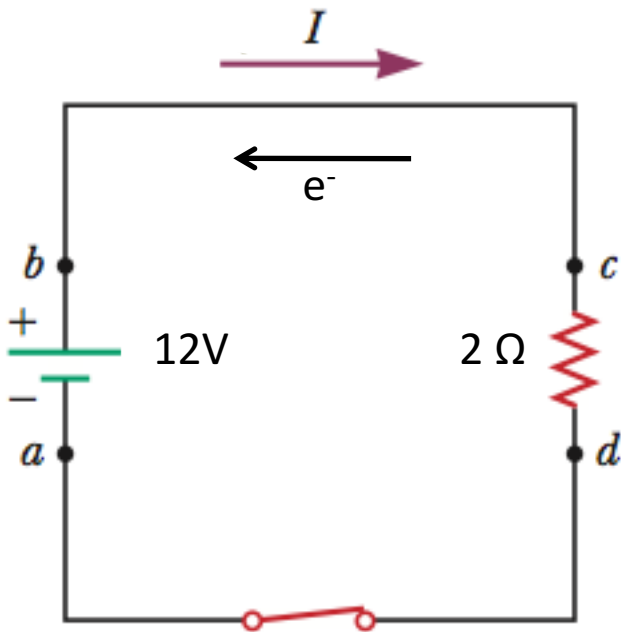
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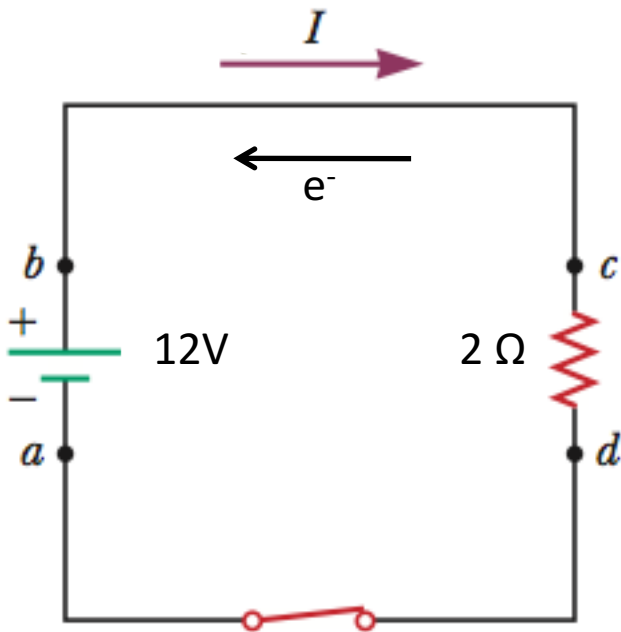


# Example: Ohm's Law

Consider the circuit shown :

(a) What is the direction of the current?

(b)  $V_c > V_d = ?$



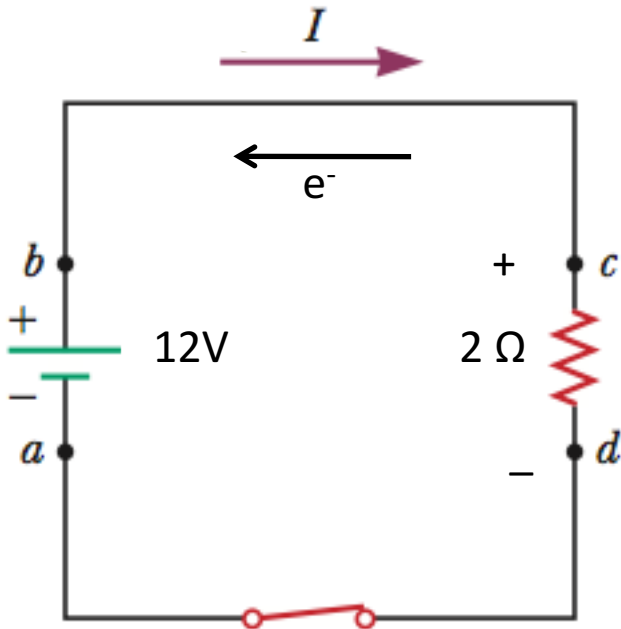
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Consider the circuit shown :

(a) What is the direction of the current?

(b)  $V_c > V_d = ?$

(c) What is the magnitude of the current?



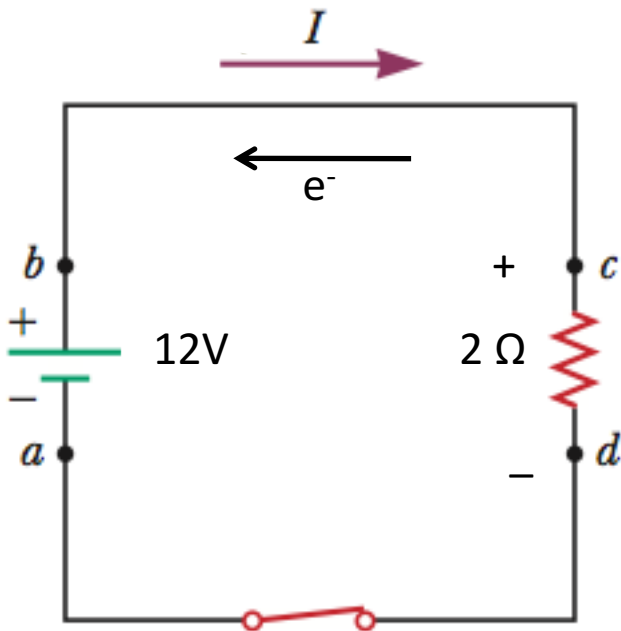
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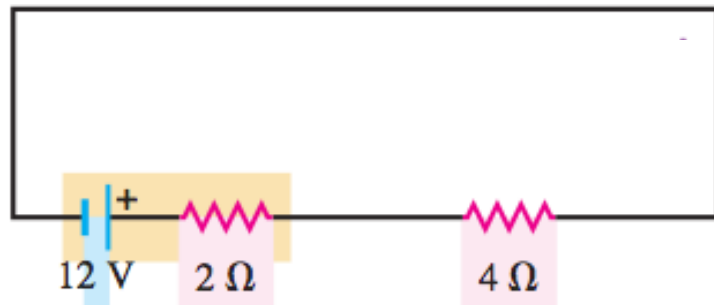
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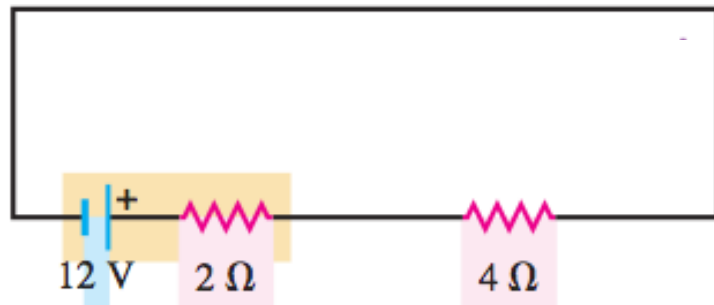
$$I = \frac{\Delta V}{R} = \frac{12V}{2} = 6A$$

# Potential Changes Around a Circuit



$$\Delta V = RI$$

# Potential Changes Around a Circuit

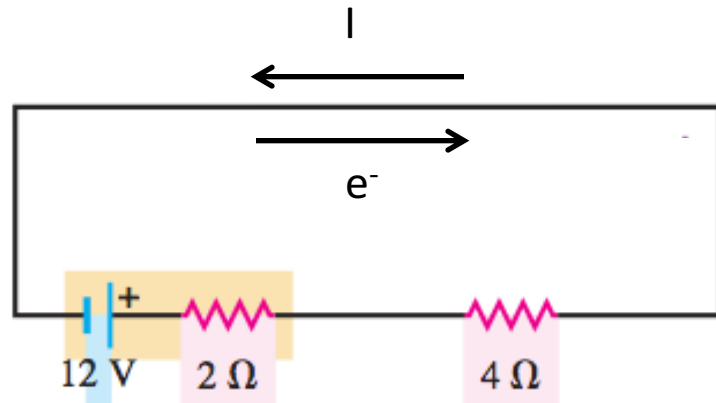


Direction of current?

Clockwise

Counter-clockwise

# Potential Changes Around a Circuit



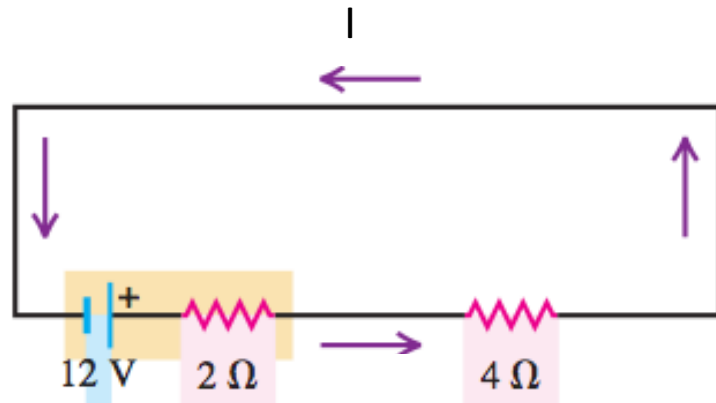
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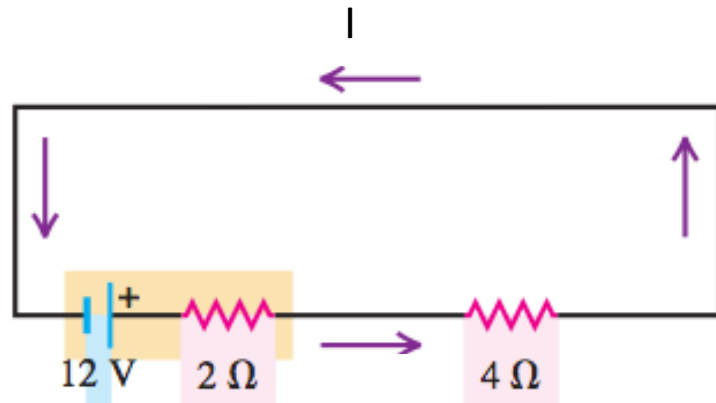


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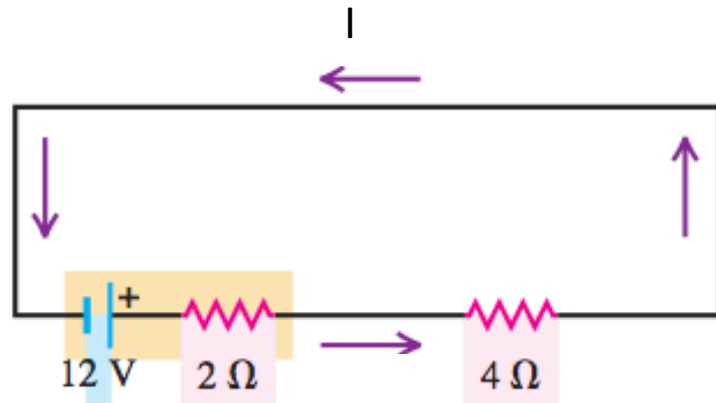
**Counter-clockwise**

# Potential Changes Around a Circuit



Magnitude of current?

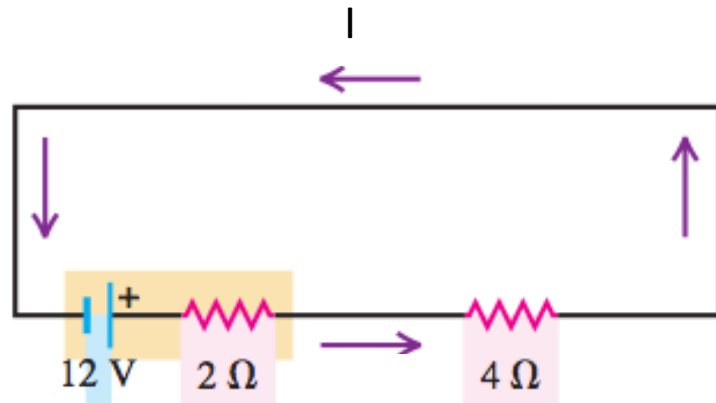
# Potential Changes Around a Circuit



Magnitude of current?

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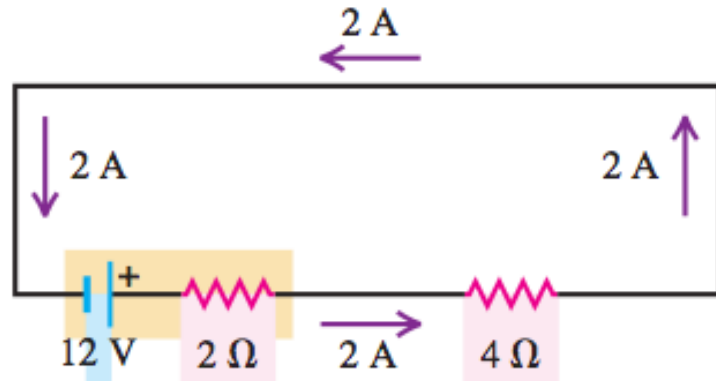


Magnitude of current?

$$\Delta V = RI$$

$$I = \frac{\Delta V}{R} = \frac{12}{2 + 4} = 2 \text{ A}$$

# Potential Changes Around a Circuit

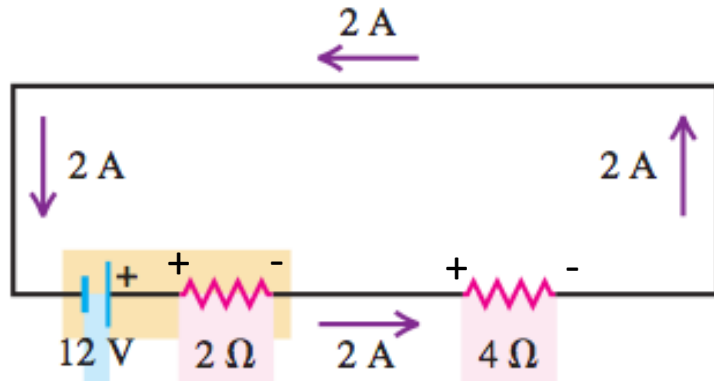


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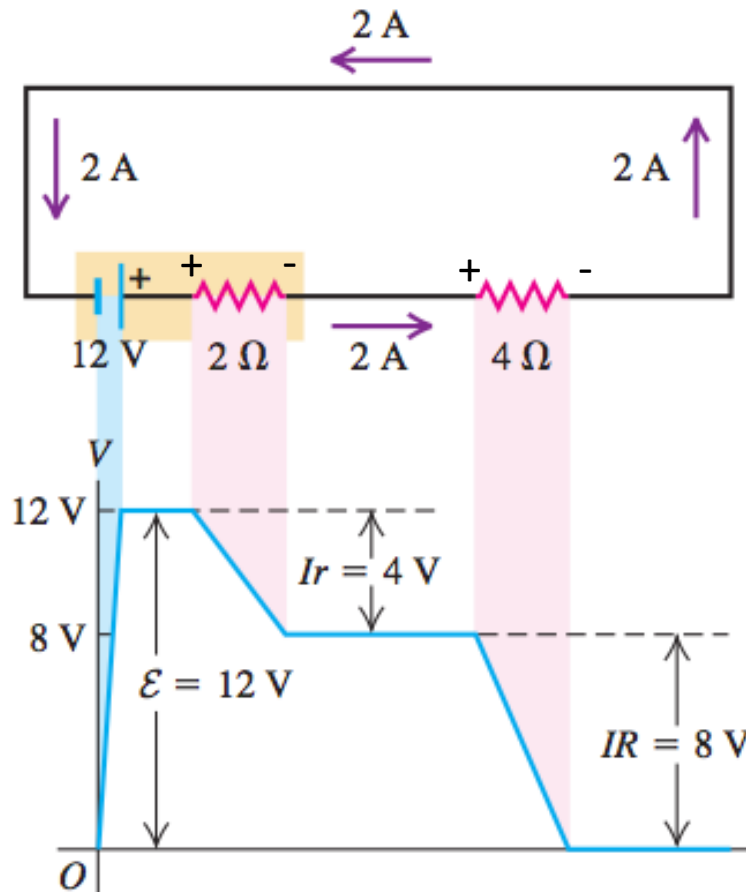


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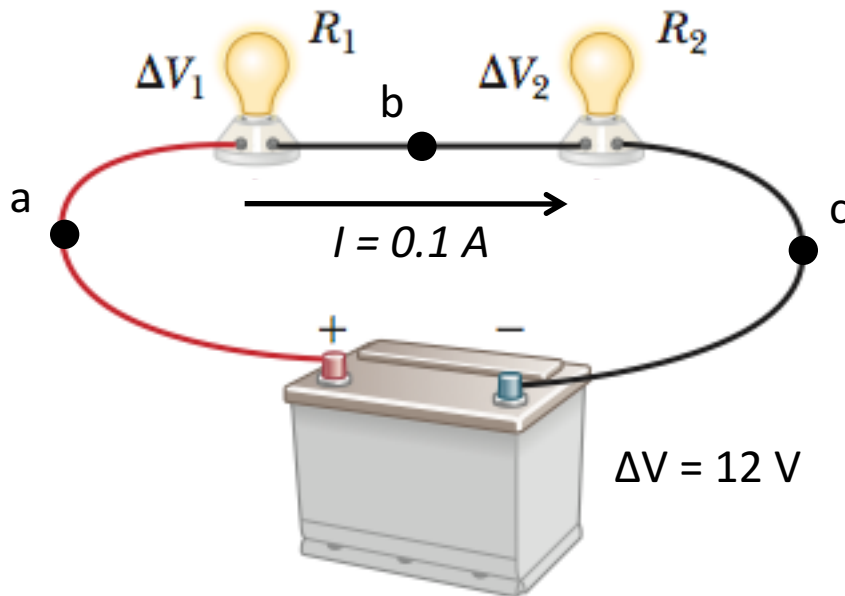


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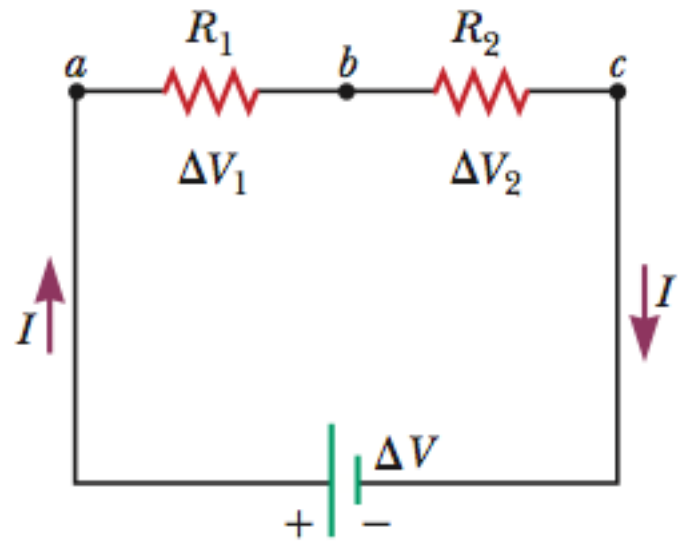
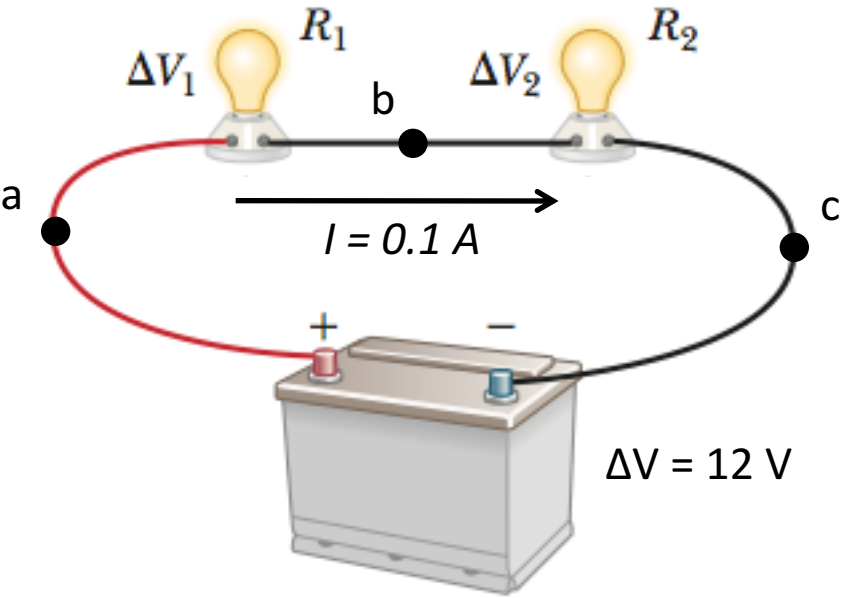
$$I = \frac{\Delta V}{R} = \frac{12}{2 + 4} = 2 \text{ A}$$

**Example:** If a battery provides a potential difference of 12 V, the current is 0.1 A and  $R_1 = 40\ \Omega$  and  $R_2 = 80\ \Omega$ . What potential difference would you measure (a) between points a and b, and (b) between points b and c?

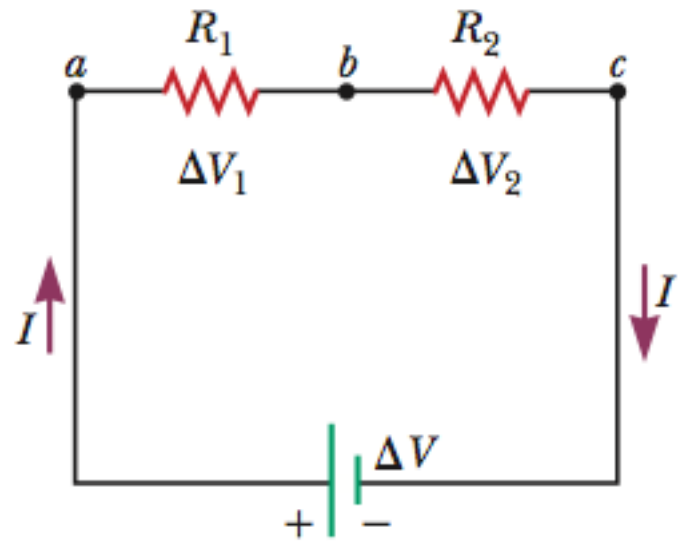
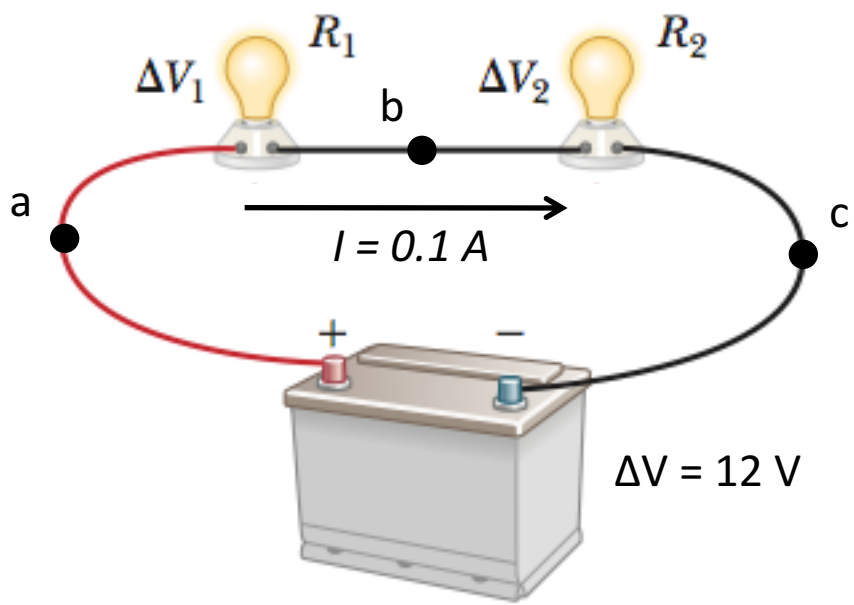




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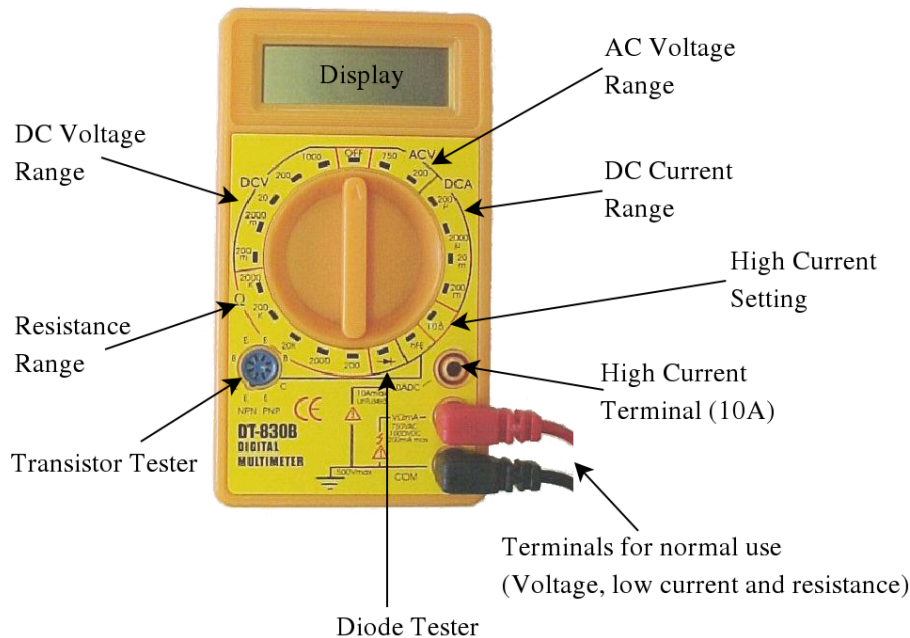
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$$\Delta V = RI$$
$$\Delta V_1 = R_1 I = (40)(0.1) = 4\text{ V}$$
$$\Delta V_2 = R_2 I = (80)(0.1) = 8\text{ V}$$

# Meters

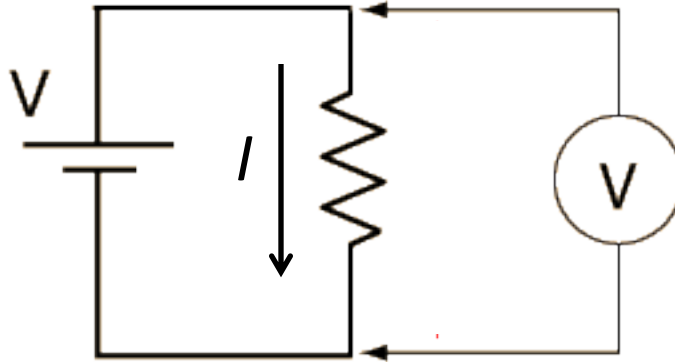
# Meters



- **Voltmeter**: Measures the potential difference between two points in a circuit.

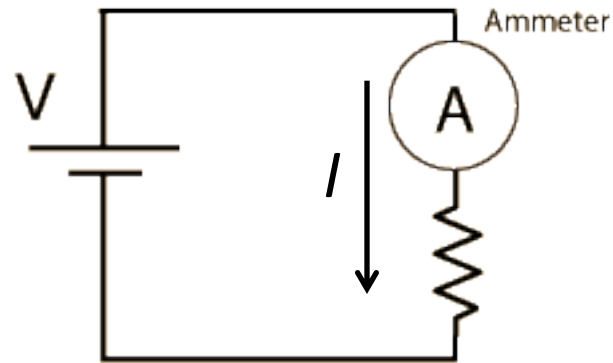
- **Ammeter**: Measures the electric current through a portion of a circuit.

# Voltmeter



- A voltmeter is placed **in parallel** with the circuit element whose voltage is to be measured.
- A voltmeter has **high resistance** so that all the current goes through the circuit element.

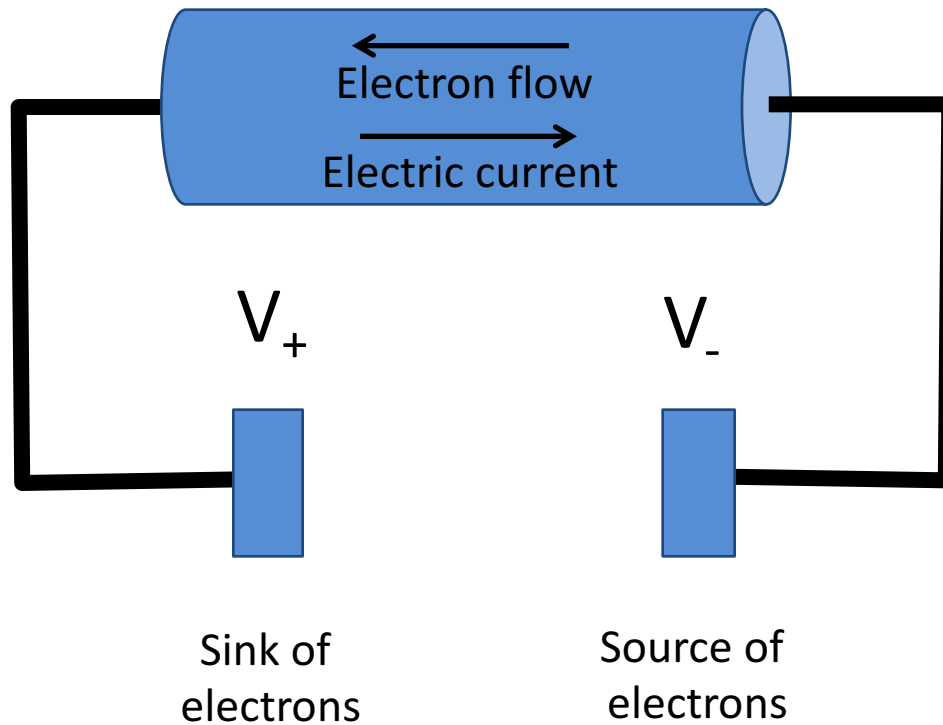
# Ammeter



- Ammeter is placed **in series** with the circuit element whose current going through is to be measured.
- Ammeter has **low resistance** so that it does not affect the current going through element.

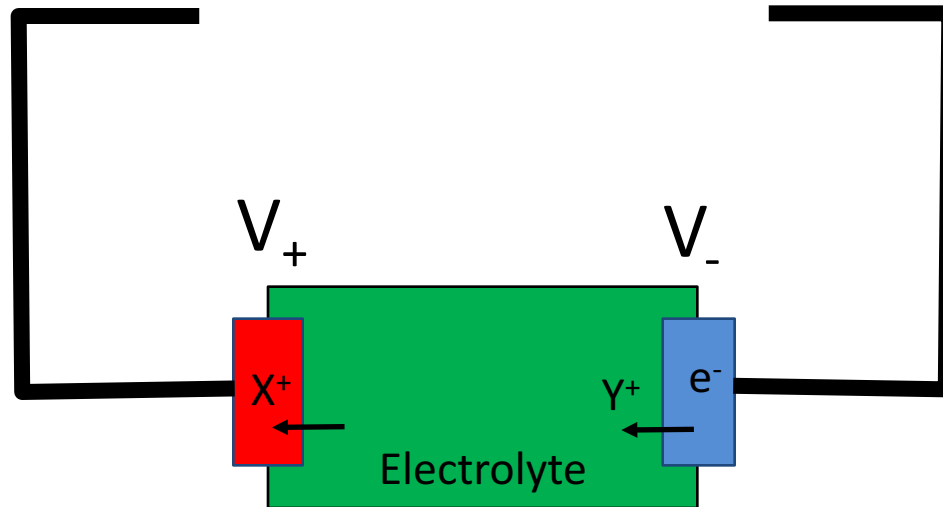
# Electromotive Force

# Electromotive Force





# Electromotive Force



# Electromotive Force

