## **Useful values:**

$$\begin{split} \epsilon_0 &= 8.85 \times 10^{-12} \frac{C^2}{Nm^2} \\ \mu_0 &= 4\pi \times 10^{-7} \frac{Tm}{A} \\ m_e &= 9.11 \times 10^{-31} kg \\ m_p &= 1.67 \times 10^{-27} kg \\ q_e &= e = 1.60 \times 10^{-19} C \\ \rho_{copper} &= 1.72 \times 10^{-8} \, \Omega m \end{split}$$

# **Equations of motion for constant acceleration:**

$$\begin{aligned} v_x &= v_{0x} + a_x \Delta t \\ v_x^2 &= v_{0x}^2 + 2a_x \Delta x \\ \Delta x &= v_{0x} \Delta t + \frac{1}{2} a_x \Delta t \\ \Delta x &= \frac{1}{2} (v_{0x} + v_x) \Delta t \end{aligned}$$

# Ch. 21 - Charge and E-field

$$\vec{F} = \frac{1}{4\pi\epsilon_0} \frac{|q_1||q_2|}{r^2} \hat{r}$$

$$\vec{F} = q\vec{E}$$

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{|q_1|}{r^2} \hat{r}$$

Electric dipole

$$\vec{p} = |q|\vec{d}$$

$$\vec{\tau} = \vec{p} \times \vec{E}$$

$$U = -\vec{p} \cdot \vec{E}$$

Electric field

$$\vec{E} = \frac{1}{4\pi\epsilon_0} \sum_{i=1} \frac{q_i}{r_i^2} \hat{r}_i$$

$$d\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{dq}{r^2} \hat{r}$$

# Ch. 22 - Gauss's Law

$$\Phi_E = \int \vec{E} \cdot d\vec{A}$$
  
Gauss's Law:  
 $\Phi_E = \oint \vec{E} \cdot d\vec{A} = \frac{Q_{encl}}{\epsilon_0}$ 

## Ch. 23 - Electric potential

Electric potential energy:

$$\begin{split} \Delta U &= -W_E \\ W &= \int \vec{F} \cdot d\vec{l} \\ U &= \frac{q_0}{4\pi\epsilon_0} \sum_i \frac{q_i}{r_i} \end{split}$$

Electric potential

$$\begin{split} V &= \frac{U}{q_0} \\ V &= \frac{1}{4\pi\epsilon_0} \sum_{i=1} \frac{q_i}{r_i} \\ \Delta V &= V_b - V_a = -\int\limits_a^b \vec{E} \cdot d\vec{s} \\ \vec{E} &= -\vec{\nabla} V \end{split}$$

# Ch. 24 - Capacitance

Capacitance

$$C = \frac{Q}{V}$$

Parallel-plate capacitor

$$C = \frac{A}{d}\epsilon$$

Cylindrical capacitor

$$C = \frac{2\pi\epsilon L}{\ln\left[\frac{r_b}{r_a}\right]}$$

Spherical capacitor

$$C = \frac{4\pi\epsilon r_a r_b}{r_b - r_a}$$

Capacitor energy

$$U = \frac{1}{2} \frac{Q^{2}}{C} = \frac{1}{2} QV = \frac{1}{2} CV^{2}$$
$$u = \frac{1}{2} E^{2} \epsilon$$

Dielectric constant

$$K = \frac{\epsilon}{\epsilon_0} = \frac{E_0}{E} = \frac{V_0}{V} = \frac{C}{C_0} = \frac{\sigma}{\sigma - \sigma_i}$$

## Ch. 25 - I, R and EMF

$$I = \frac{dQ}{dt} = |q|Anv_D$$

$$J = \frac{I}{A}$$

$$\vec{J} = \frac{\vec{E}}{\rho} = nq\vec{v}_D$$

$$R = \frac{\rho L}{A}$$

$$V = RI$$

$$R = R_0[1 + \alpha(T - T_0)]$$

$$\rho = \rho_0[1 + \alpha(T - T_0)]$$

$$P = \frac{dE}{dt} = VI = RI^2 = V^2/R$$

#### Ch. 26 - DC circuits

**RC Circuits:** 

 $\tau = RC$ 

Charging:

$$q(t) = Q_f(1 - e^{-t/\tau})$$

$$i(t) = I_0 e^{-t/\tau}$$

Discharging:

$$q(t) = Q_0 e^{-t/\tau}$$

$$i(t) = -I_0 e^{-t/\tau}$$

## Ch. 27 - B-Field and Forces

$$\begin{split} \vec{F} &= q\vec{v} \times \vec{B} \\ \vec{F} &= I\vec{l} \times \vec{B} \\ \vec{\mu} &= I\vec{A} \\ \vec{\tau} &= \vec{\mu} \times \vec{B} \\ \Phi_M &= \int \vec{B} \cdot d\vec{A} \end{split}$$

Gauss's Law for Magnetism:

$$\oint \vec{B} \cdot d\vec{A} = 0$$

Charges in magnetic field:

$$R = \frac{mv}{qB}$$

$$\omega = 2\pi f = \frac{v}{R} = \frac{qB}{m}$$

### Ch. 28 - Sources of B-Field

$$\vec{B} = \frac{\mu_0}{4\pi} \frac{q\vec{v} \times \hat{r}}{r^2}$$
$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{Id\vec{l} \times \hat{r}}{r^2}$$

Long wire:

$$B = \frac{\mu_0 I}{2\pi x}$$

Current loop:  

$$B = \frac{\mu_0 I a^2}{2(a^2 + z^2)^{3/2}}$$

Force between parallel conductors:

$$F = \frac{\mu_0 L I_1 I_2}{2\pi r}$$

Ampere's Law:

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I_{encl}$$