

Consider a fair-queuing server where there are three flows, f, g, and h, all with fixed packet sizes of 1000 bits, and the output channel bandwidth is 100 bits/sec.

Assume at real-time 0 packet f,1 arrives.

Then packet g,1 arrives at real-time 6 sec.

Packet h,1 arrives at real-time 9sec,

And finally, packet f,2 arrives at time 19.5

For every packet

a) Show me its F value, i.e. , the fake time of the finishing time of the packet in the fake server.

b) Show me the *real time* of when the packet exits the *real* server.

Part a)

$$F(f,1) = \max(0, V(A(f,1))) + 1000 = 0 + 1000 = 1000$$

$$A(g,1) = 6 \text{ seconds}$$

$$F(g,1) = \max(0, V(A(g,1))) + 1000 = \max(0, V(6)) + 1000$$

Thus, 600 bits were xmitted from A(f,1) to A(g,1). Only f was queued, i.e., 600 rounds.

$$\text{Thus, } V(A(g,1)) = V(6) = 600$$

$$F(g,1) = \max(0, V(A(g,1))) + 1000 = 600 + 1000 = 1600$$

$$A(h,1) = 9$$

$$F(h,1) = \max(0, V(A(h,1))) + 1000 = \max(0, V(9)) + 1000$$

$V(6) = 600$ (from above), what is $V(9)$?

In 3 seconds, server transmits 300 bits, and since both f and g are queued starting at $V(6)$, then 150 rounds occur

I.e., $V(9) = 600 + 150 = 750$. This is true provided neither f nor g finish sending their last bit. Flow f will finish in round 1000 and g in round 1600, so it is true

$$F(h,1) = \max(0, V(A(h,1))) + 1000 = \max(0, V(9)) + 1000 = 1750$$

$$A(f,2) = 19.5$$

$$F(f,2) = \max(F(f,1), V(A(f,2))) + 1000 = \max(1000, \mathbf{V(19.5)}) + 1000$$

What is $V(19.5)$?

$V(9) = 750$, from 9 sec to 19.5 sec we have 10.5 sec, i.e., 1050 bits transmitted. If all f , g , and h are queued, then these are $1050/3 = 350$ rounds. So, the round number would be $750 + 350 = 1100$. Obviously $f,1$ will finish before this, at round $F(f,1) = 1000$, so there is a “change in slope” for V at round 1000.

$V(9) = 750$, $V(x) = 1000$ (when $f,1$ finishes). What is x ? Well, 250 rounds, 3 queued flows gives 750 bits, or 7.5 more seconds, so $x = 9 + 7.5 = 16.5$

$V(16.5) = 1000$ and only g and h remain queued, so the slope of V changes.

Again, what is $V(19.5)$? From 16.5 to 19.5 there are 3 seconds, 300 bits, two queued flows, so 150 rounds. $V(19.5) = V(16.5) + 150 = 1000 + 150 = 1150$. This is PROVIDED neither g nor h finish. Flow g finishes at round 1600, so it is indeed true

$$V(19.5) = 1150.$$

$$\mathbf{F(f,2) = \max(F(f,1), V(A(f,2))) + 1000 = \max(1000, V(19.5)) + 1000 = \max(1000,1150) + 1000 = 1150 + 1000 = 2150}$$

Part b))

$f,1$ is sent first, and finishes at real-time $1000/100 = 10$ seconds.

By time 10, both $g,1$ and $h,1$ have arrived, so the next one to xmit at time 10 is $g,1$, and it exits at time $10 + 1000/100 = 10 + 10 = 20$.

At time 20, $h,1$ remains, and $f,2$ has arrived, $h,1$ has smaller timestamp so it is transmitted. It finishes at time 30

At time 30 $f,2$ is transmitted and ends at time 40.

Fe Ko
Time

$$F_h, 1 \rightarrow 1750$$

$F_{g,1} \rightarrow 16\alpha$

$F_{E1} \rightarrow 1000$

750

650

As it

Ag.1

6

At 1

2

16-5

719.5
AF, 2

regl-tins

$C = 100 \text{ bits/sec}$
 $L = 1000 \text{ bits}$
 $A_{s,1} = 0 \text{ secs}$
 $A_{g,1} = 6 \text{ secs}$
 $A_{h,1} = 9 \text{ secs}$
 $A_{F,2} = 19.5 \text{ sec}$

