# **Neural Sequence Generation**

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  - Open-domain dialogue: context to response
  - Parsing: sentence to linearized trees
  - In general: text to text

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Main difference (and challenge) is that the output space is much larger.

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- Can we reduce it to classification (think logistic regression)?
- Decompose the problem using chain rule of probability

$$p(y \mid x) = p(y_1 \mid x)p(y_2 \mid y_1, x) \dots p(y_m \mid y_{m-1}, \dots, y_1, x)$$
  
=  $\prod_{i=1}^{m} p(y_i \mid y_{< i}, x)$ 

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• We only need to model the next word distribution  $p(y_i \mid y_{< i}, x)$  now.

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We can use an RNN to model  $p(y_i | y_{< i}, x)$ .

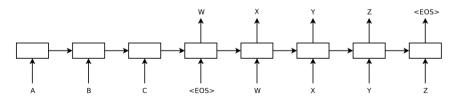


Figure: From Sequence to Sequence Learning with Neural Networks [Sutskever et al., 2014]

### The encoder-decoder architecture

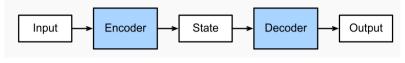


Figure: 10.6.1 from d2l.ai

Model the input (e.g., French) and the output (e.g., English) separately.

#### The encoder-decoder architecture

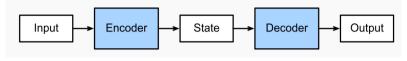


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Model the input (e.g., French) and the output (e.g., English) separately.

• The **encoder** reads the input:

$$\operatorname{Encoder}(x_1,\ldots,x_n)=[h_1,\ldots,h_n]$$

where  $h_i \in \mathbb{R}^d$ 

• The **decoder** writes the output:

$$Decoder(h_1,\ldots,h_n)=[y_1,\ldots,y_m]$$

.

#### RNN encoder-decoder model

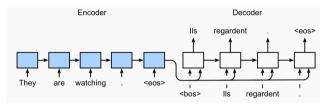


Figure: 10.7.1 from d2l.ai

The encoder embeds the input recurrently and produce a context vector

$$h_t = \text{RNNEncoder}(x_t, h_{t-1}), \quad c = f(h_1, \dots, h_n)$$

 The decoder produce the output state recurrently and map it to a distribution over tokens

$$s_t = \text{RNNDecoder}([y_{t-1}; c], s_{t-1}), \quad p(y_t \mid y_{< t}, c) = \text{softmax}(\text{Linear}(s_t))$$

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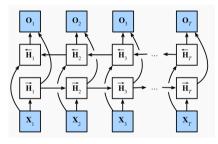


Figure: 10.4.1 from d2l.ai

- Use two RNNs, one encode from left to right, the other from right to left
- Concatenate hidden states from the two RNNs

$$h_t = [\overleftarrow{h_t}; \overrightarrow{h_t}]$$
 $o_t = Wh_t + b$ 

### **Multilayer RNN**

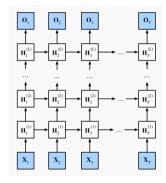


Figure: 10.3.1 from d2l.ai

- Improve model capacity (scaling up)
- Inputs to layer 1 are words
- Inputs to layer I are outputs from layer I-1
- Typically 2–4 layers

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Think the database analogy:

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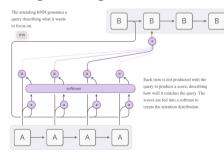
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### **Summary so far**

The outputs of an encoder can be used by linear classifiers for classification, sequence labeling etc.

A decoder is used to generate a sequence of symbols.

#### RNN encoder decoder model:

- Basic unit is an RNN (or its variants like LSTM)
- Make it more expressive: bi-directional, multilayer RNN
- Encoder-decoder attention helps the model learn input-output dependencies more easily
- Bi-directional LSTM is the go-to architecture for NLP tasks until around 2017

### Transformer encoder decoder model

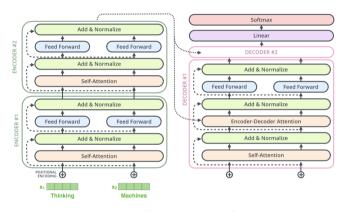


Figure: From illustrated transformer

- Stack the tranformer block (typically 12–24 layers)
- Decoder has an additional encoder-decoder multi-head attention layer

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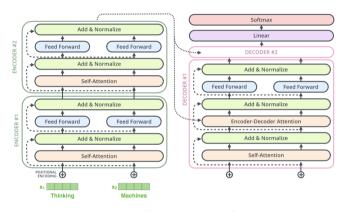


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# **Decoder attention masking**

Recall that the output of self-attention depends on all tokens  $y_1, \dots y_m$ .

But the decoder is supposed to model  $p(y_t \mid y_{< t}, x)$ .

It should not look at the "future"  $(y_{t+1}, \ldots, y_m)!$ 

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How do we fix the decoder self-attention?

- Mathematically, changing the input values and keys suffices.
- Practically, set  $a(s_i, s_j)$  to  $-\inf$  for all j > i and for  $i = 1, \ldots, m$ .
  - The attention matrix is a lower-triangular matrix.

### **Impact on NLP**

- Initially designed for sequential data and obtained SOTA results on MT
- Replaced recurrent models (e.g. LSTM) on many tasks
- Enabled large-scale training which led to pre-trained models such as BERT and GPT-2 (in two weeks)

# **Training**

Maximum likelihood estimation:

$$\max \sum_{(x,y)\in\mathcal{D}} \sum_{j=1}^{m} \log p(y_j \mid y_{< j}, x; \theta)$$

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Option 1: whatever generated by the model

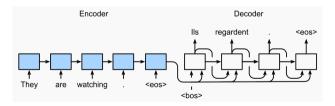


Figure: 10.7.1 from d2l.ai

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Option 2: the groundtruth prefix (teacher forcing)

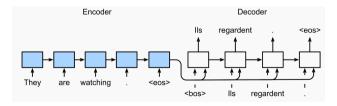


Figure: 10.7.3 from d2l.ai

#### **Inference**

How do we generate sequences given a trained model?

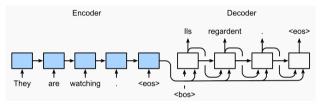


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The encoder-decoder model defines a probability distribution  $p(y \mid x; \theta)$  over sequences.

Which one should we output?

#### Inference

### **Argmax decoding:**

$$\hat{y} = \arg\max_{y \in \mathcal{V}_{\text{out}}^n} p(y \mid x; \theta)$$

- Return the most likely sequence
- But exact search is intractable

#### Inference

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#### Approximate search:

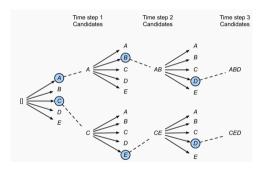
Greedy decoding: return the most likely symbol at each step

$$y_t = \underset{y \in \mathcal{V}_{out}}{\operatorname{arg max}} p(y \mid x, y_{< t}; \theta)$$

### Approximate decoding: beam search

**Beam search**: maintain k (beam size) highest-scored partial solutions at every step

Example: 
$$|\mathcal{V}| = 5, k = 2$$



- At each step, rank symbols by log probability of the partial sequence
- Keep the top-k symbol out of all possible continuations
- Save **backpointer** to the previous state

# Is argmax the right decoding objective?

High likelihood can be correlated with low quality outputs!

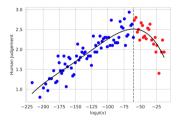


Figure: From the likelihood trap paper by Zhang et al., 2020

In practice, argmax decoding has been observed to lead to

- Repetitive generations, e.g.
   "..., was conducted by researchers from the Universidad Nacional Autonoma de Mexico (UNAM) and the Universidad Nacional Autonoma de Mexico (UNAM/Universidad Nacional Autonoma de Mexico/Universidad Nacional Autonoma..."
- Degraded generations with large beam size in MT

# **Sampling-based decoding**

If we have learned a perfect  $p(y \mid x)$ , shouldn't we just sample from it?

**Sampling** the next word sequentially:

- While output is not EOS
  - Sample next word from  $p(\cdot \mid \text{prefix}, \text{input}; \theta)$
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Standard sampling often produces non-sensical sentences:

They were cattle called Bolivian Cavalleros; they live in a remote desert uninterrupted by town, and they speak huge, beautiful, paradisiacal Bolivian linguistic thing.

Typically we modify the learned distrubtion  $p_{ heta}$  before sampling the next word

# **Tempered sampling**

**Intuition**: concentrate probability mass on highly likely sequences

Scale scores (from the linear layer) before the softmax layer:

$$p(y_t = w \mid y_{< t}, x) \propto \exp(\operatorname{score}(w))$$
  
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- What happends when  $T \to 0$  and  $T \to +\infty$ ?
- Does it change the rank of y according to likelihood?
- Typically we chooose  $T \in (0,1)$ , which makes the distribution more peaky.

# **Truncated sampling**

Another way to focus on high likelihood sequences: truncate the tail of the distribution

#### Top-k sampling:

- Rank all tokens  $w \in \mathcal{V}$  by  $p(y_t = w \mid y_{< t}, x)$
- Only keep the top k of those and renormalize the distribution

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#### Which *k* to choose?

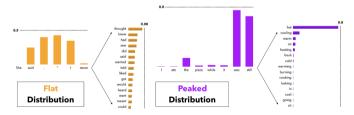


Figure: From the nucleus sampling paper by Holtzman et al., 2020

# **Truncated sampling**

#### Top-p sampling:

- Rank all tokens  $w \in \mathcal{V}$  by  $p(y_t = w \mid y_{< t}, x)$
- Keep only tokens in the top p probability mass and renormalize the distribution
- The corresponding k is dynamic:
  - Start with k=1, increment until the cumulative probability mass is larger than  $\emph{p}$

# **Decoding in practice**

- Can combine different tricks (e.g., temperature + beam search, temperature + top-k)
- Use beam search with small beam size for tasks where there exists a correct answer, e.g. machine translation, summarization
- Use top-k or top-p for open-ended generation, e.g. story generation, chit-chat dialogue, continuation from a prompt
- As models getting better/larger, sampling-based methods tend to work better