Neural Sequence Modeling

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February 7, 2023

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Feature learning

Linear predictor with handcrafted features: $f(x) = w \cdot \phi(x)$.

Can we learn intermediate features?

Feature learning

Linear predictor with handcrafted features: $f(x) = w \cdot \phi(x)$.

Can we learn intermediate features?

Example:

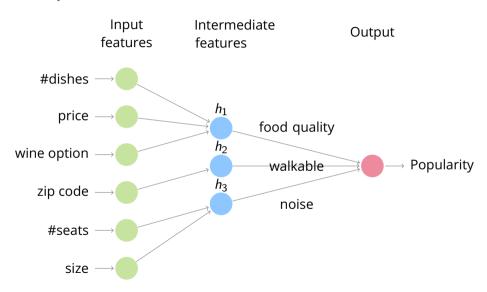
- Predict popularity of restaurants.
- Raw input: #dishes, price, wine option, zip code, #seats, size
- Decompose into subproblems:

```
h_1([\#dishes, price, wine option]) = food quality
```

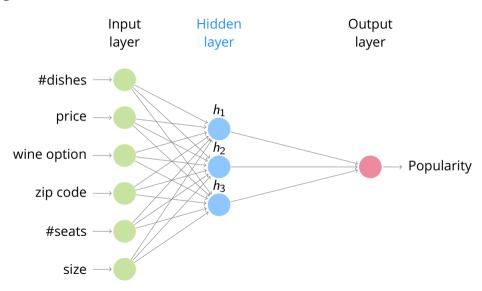
```
h_2([zip code]) = walkable
```

$$h_3([\#seats, size]) = nosie$$

Predefined subproblems



Learning intermediate features



Neural networks

Key idea: automatically learn the intermediate features.

Feature engineering: Manually specify $\phi(x)$ based on domain knowledge and learn the weights:

$$f(x) = \mathbf{w}^T \phi(x).$$

Feature learning: Automatically learn both the features (K hidden units) and the weights:

$$h(x) = [h_1(x), \dots, h_K(x)], \quad f(x) = \mathbf{w}^T h(x)$$

• How should we parametrize h_i 's? Can it be linear?

$$h_i(x) = \sigma(v_i^T x). \tag{1}$$

• σ is the *nonlinear* activation function.

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 - Differentiable approximations: sigmoid functions.
 - E.g., logistic function, hyperbolic tangent function, ReLU

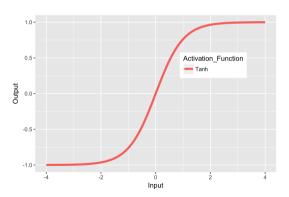
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 - *Differentiable* approximations: sigmoid functions.
 - E.g., logistic function, hyperbolic tangent function, ReLU
- Two-layer neural network (one hidden layer and one output layer) with K
 hidden units:

$$f(x) = \sum_{k=1}^{K} w_k h_k(x) = \sum_{k=1}^{K} w_k \sigma(v_k^T x)$$
 (2)

• The **hyperbolic tangent** is a common activation function:

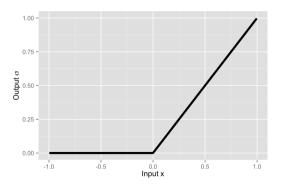
$$\sigma(x) = \tanh(x)$$
.



• More recently, the **rectified linear** (**ReLU**) function has been very popular:

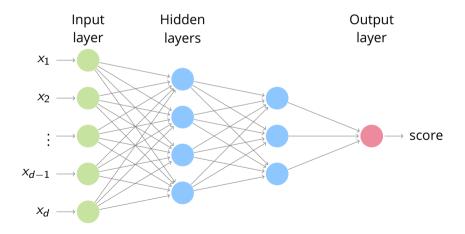
$$\sigma(x)=\max(0,x).$$

- Much faster to calculate, and to calculate its derivatives.
- Work well empirically.



Multilayer perceptron / Feed-forward neural networks

- Wider: more hidden units.
- Deeper: more hidden layers.



Multilayer Perceptron: Standard Recipe

• Each hidden layer takes the output $o \in \mathbb{R}^m$ of previous layer and produces

$$h^{(j)}(o^{(j-1)}) = \sigma\left(W^{(j)}o^{(j-1)} + b^{(j)}\right), \text{ for } j = 2, \dots, L$$

where $W^{(j)} \in \mathbb{R}^{m \times m}$, $b^{(j)} \in \mathbb{R}^m$.

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• The output layer is an *affine* mapping (no activation function):

$$a(o^{(L)}) = W^{(L+1)}o^{(L)} + b^{(L+1)},$$

where $W^{(L+1)} \in \mathbb{R}^{k \times m}$ and $b^{(L+1)} \in \mathbb{R}^k$.

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• The full neural network function is given by the *composition* of layers:

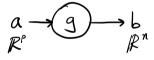
$$f(x) = \left(a \circ h^{(L)} \circ \cdots \circ h^{(1)}\right)(x) \tag{3}$$

Computation graphs

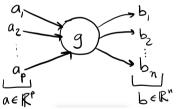
(adpated from David Rosenberg's slides)

Function as a *node* that takes in *inputs* and produces *outputs*.

• Typical computation graph:

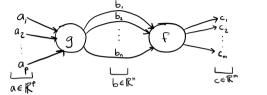


Broken out into components:



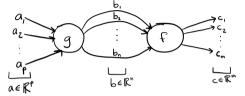
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Compose two functions $g: \mathbb{R}^p \to \mathbb{R}^n$ and $f: \mathbb{R}^n \to \mathbb{R}^m$: c = f(g(a))



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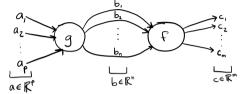
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(adpated from David Rosenberg's slides)

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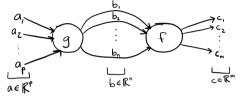


• Derivative: How does change in a_i affect c_i ?

$$\frac{\partial c_i}{\partial a_j} = \sum_{k=1}^n \frac{\partial c_i}{\partial b_k} \frac{\partial b_k}{\partial a_j}$$

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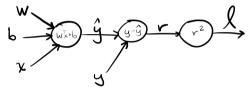


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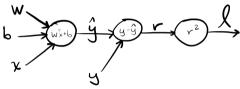
- Visualize the multivariable chain rule:
 - Sum changes induced on all paths from a_i to c_i .
 - Changes on one path is the product of changes on each edge.

(adpated from David Rosenberg's slides)



(What is this graph computing?)

(adpated from David Rosenberg's slides)

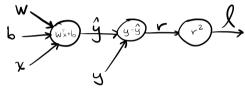


(What is this graph computing?)

$$\frac{\partial \ell}{\partial b} = \frac{\partial \ell}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial b} = (-2r)(1) = -2r$$

$$\frac{\partial \ell}{\partial w_j} = \frac{\partial \ell}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial w_j} = (-2r)x_j = -2rx_j$$

(adpated from David Rosenberg's slides)



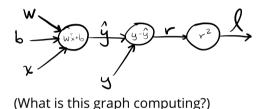
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Computing the derivatives in certain order allows us to save compute!

(adpated from David Rosenberg's slides)



$$\frac{\partial \ell}{\partial r} = 2r$$

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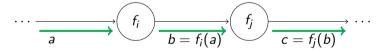
Computing the derivatives in certain order allows us to save compute!

Backpropogation

Backpropogation = chain rule + dynamic programming on a computation graph

Forward pass

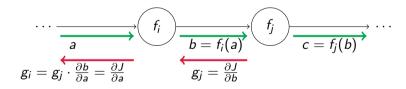
- Topological order: every node appears before its children
- For each node, compute the output given the input (from its parents).



Backpropogation

Backward pass

- **Reverse topological order**: every node appear after its children
- For each node, compute the partial derivative of its output w.r.t. its input, multiplied by the partial derivative from its children (chain rule).



Summary

Key idea in neural nets: feature/representation learning

Building blocks:

- Input layer: raw features (no learnable parameters)
- Hidden layer: perceptron + nonlinear activation function
- Output layer: linear (+ transformation, e.g. softmax)

Optimization:

- Optimize by SGD (implemented by back-propagation)
- Objective is non-convex, may not reach a global minimum

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Overview

Problem setup: given an input sequence, come up with a (neural network) model that outputs a representation of the sequence for downstream tasks (e.g., classification)

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Key challenge: how to model interaction among words?

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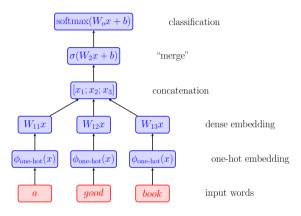
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Key challenge: how to model interaction among words?

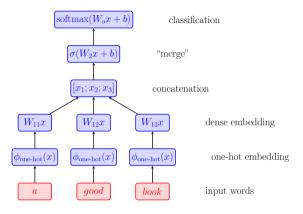
Approach:

- Aggregation / pooling word embeddings
- Recurrence
- Self-attention

Feed-forward neural network for text classification



Feed-forward neural network for text classification





What kind of features can be learned? How to adapt the network to handle sequences with arbitrary length?

Recurrent neural networks

- **Goal**: represent a sequence of symbols of varying lengths
- Idea: combine new symbols with previous symbols recurrently by modeling the temporal dynamics

$$h_t = f(h_{t-1}, x_t)$$

Recurrent neural networks

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$$h_t = f(h_{t-1}, x_t)$$

- Compute the **hidden states** h_t recurrently
 - Output from previous time step is the input to the current time step
 - Apply the same transformation *f* at each time step

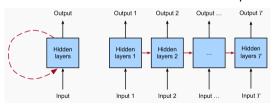
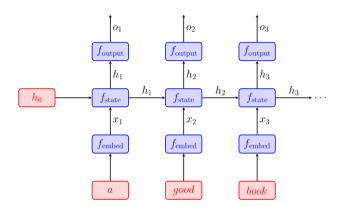
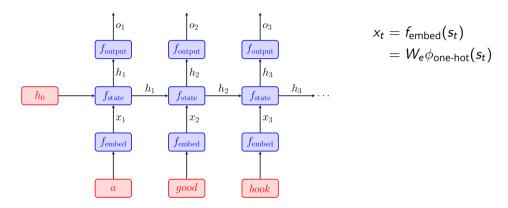
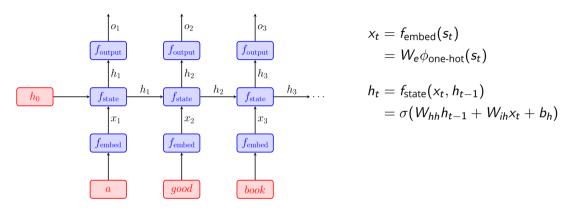
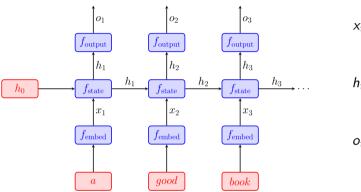


Figure: 9.1 from d2l.ai



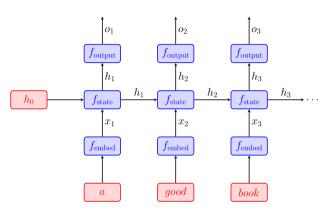






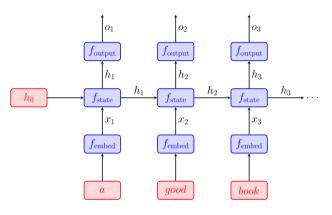
$$egin{aligned} x_t &= f_{\mathsf{embed}}(s_t) \ &= W_e \phi_{\mathsf{one-hot}}(s_t) \end{aligned} \ h_t &= f_{\mathsf{state}}(x_t, h_{t-1}) \ &= \sigma(W_{hh}h_{t-1} + W_{ih}x_t + b_h) \end{aligned} \ o_t &= f_{\mathsf{output}}(h_t) \ &= W_{ho}h_t + b_o \end{aligned}$$

Use o_t 's as features



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Use o_t 's as features



A deep neural network with shared weights in each layer

$$x_{t} = f_{\text{embed}}(s_{t})$$

$$= W_{e}\phi_{\text{one-hot}}(s_{t})$$

$$h_{t} = f_{\text{state}}(x_{t}, h_{t-1})$$

$$= \sigma(W_{hh}h_{t-1} + W_{ih}x_{t} + b_{h})$$

$$o_{t} = f_{\text{output}}(h_{t})$$

$$= W_{ho}h_{t} + b_{o}$$

Which computation can be parallelized?

Backward pass

Given the loss ℓ , compute the gradient with respect to W_{hh} .

$$\frac{\partial \ell}{\partial W_{hh}}$$
 =

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Computation graph of h_t :

Backpropagation through time

Problem with standard backpropagation:

- Gradient involves repeated multiplication of W_{hh}
- Gradient will vanish / explode (depending on the eigenvalues of W_{hh})

Quick fixes:

- Reduce the number of repeated multiplication: truncate after k steps (h_{t-k} has no influence on h_t)
- Limit the norm of the gradient in each step: gradient clipping (can only mitigate explosion)

Long-short term memory (LSTM)

Vanilla RNN: always update the hidden state

Cannot handle long range dependency due to gradient vanishing

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• First successful solution to the gradient vanishing and explosion problem

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First successful solution to the gradient vanishing and explosion problem

Key idea is to use a **gating mechanism**: multiplicative weights that modulate another variable

- How much should a given input affect the state?
- Should the state be reset to 0?
- How much should the state affect the output?

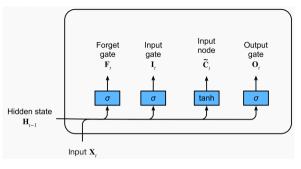


Figure: 10.1.2 from d2l.ai

Update with the new input x_t (same as in vanilla RNN)

$$ilde{c}_t = anh(W_{xc}x_t + W_{hc}h_{t-1} + b_c)$$

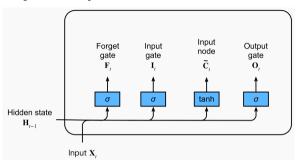


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Update with the new input x_t (same as in vanilla RNN)

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Can we choose between \tilde{c}_t and another state that doesn't update with x_t ?

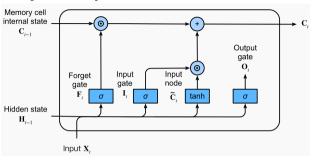


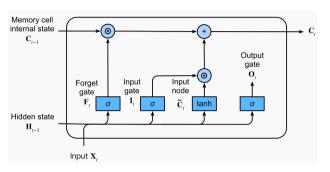
Figure: 10.1.3 from d2l.ai

Choose between \tilde{c}_t (update) and c_{t-1} (no update):

memory cell
$$c_t = i_t \odot \tilde{c}_t + f_t \odot c_{t-1}$$

- f_t : proportion of the old state
- i_t : proportion of the new state • What is a if f = 1 and i = 0?

28/50



Input gate and forget gate:

$$i_t = \operatorname{sigmoid}(W_{xi}x_t + W_{hi}h_{t-1} + b_i),$$

 $f_t = \operatorname{sigmoid}(W_{xf}x_t + W_{hf}h_{t-1} + b_f).$

Each coordinate is between 0 and 1.

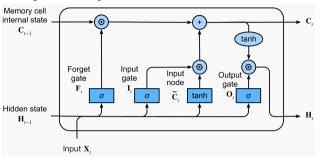


Figure: 10.1.4 from d2l.ai

How much should the memory cell state influence the rest of the network:

$$o_t = \operatorname{sigmoid}(W_{xo}x_t + W_{ho}h_{t-1} + b_o)$$

 $h_t = o_t \odot c_t$

 c_t may accumulate information without impact the network if o_t is close to 0

How does LSTM solve gradient vanishing / explosion?

Intuition: gating allows the network to learn to control how much gradient should vanish.

- Vanilla RNN: gradient depends on repeated multiplication of the same weight matrix
- LSTM: gradient depends on repeated multiplication of some quantity with learned components (values of input and forget gates)
- So the network can learn to reset or update the gradient depending on whether there is long-range dependencies in the data.

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Improve the efficiency of RNN

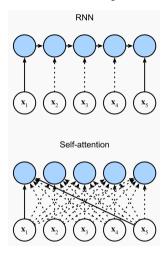


Figure: 11.6.1 from d2l.ai

Recall that our goal is to come up with a good respresentation of a sequence of words.

RNN:

- Past words influence the sentence representation through recurrent update
- Sequential computation O(sequence length), hard to scale

Improve the efficiency of RNN

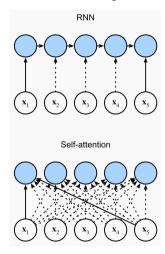


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Can we handle dependency more efficiently?

- Direct interaction between any pair of words in the sequence
- Parallelizable computation

Which word(s) is most related to "time"?

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A database approach:

query	keys	values
	arrow	time
	flies	flies
	like	like
	an	an
time	time	arrow

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• Relatedness should not be hard-coded

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Output should be an aggregation of the values

Model interaction between words using a "soft" database

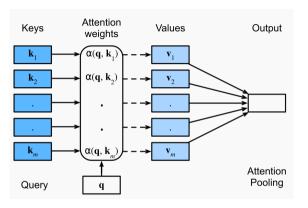


Figure: 11.1.1 from d2l.ai

- **Attention weights** $\alpha(q, k_i)$: how likely is q matched to k_i
- **Attention pooling**: combine v_i 's according to their "relatedness" to the query

Model interaction between words using a "soft" database

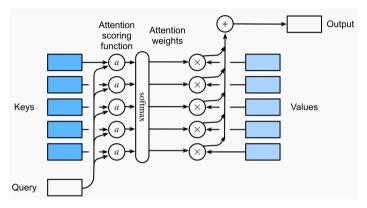


Figure: 11.3.1 from d2l.ai

- Model attention weights as a distribution: $\alpha = \operatorname{softmax}(a(q, k_1), \dots, a(q, k_m))$
- Output a weighted combination of values: $o_i = \sum_{i=1}^m \alpha(q, k_i) v_i$

Self-attention

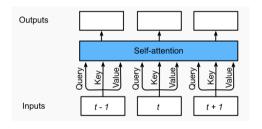
Goal: an efficient model of the interaction among symbols in a sequence

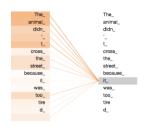
Idea: model the interaction between each pair of words (in parallel)

Self-attention

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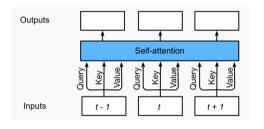


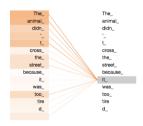
Input: map each symbol to a query, a key, and a value (embeddings)

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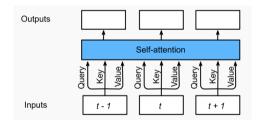


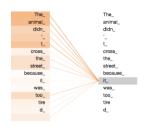
- Input: map each symbol to a query, a key, and a value (embeddings)
- Attend: each word (as a query) interacts with all words (keys)

Self-attention

Goal: an efficient model of the interaction among symbols in a sequence

Idea: model the interaction between each pair of words (in parallel)





- Input: map each symbol to a query, a key, and a value (embeddings)
- Attend: each word (as a query) interacts with all words (keys)
- Output: contextualized representation of each word (weighted sum of values)

Design the function that measures relatedness between queries and keys:

$$\alpha = \operatorname{softmax}(a(q, k))$$

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Dot-product attention

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Scaled dot-product attention

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- \sqrt{d} : dimension of the key vector
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MLP attention

$$a(q, k) = u^T \tanh(W[q; k])$$

Multi-head attention: motivation

Time flies like an arrow

- Each word attends to all other words in the sentence
- Which words should "like" attend to?

Multi-head attention: motivation

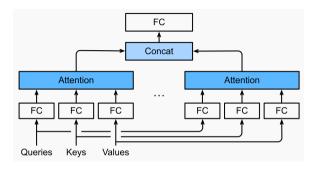
Time flies like an arrow

- Each word attends to all other words in the sentence
- Which words should "like" attend to?
 - Syntax: "flies", "arrow" (a preposition)
 - Semantics: "time", "arrow" (a metaphor)

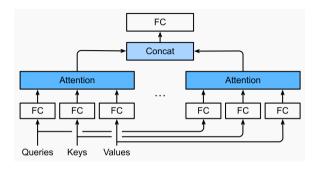
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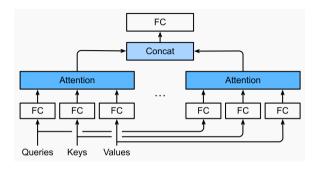
- Each word attends to all other words in the sentence
- Which words should "like" attend to?
 - Syntax: "flies", "arrow" (a preposition)
 - Semantics: "time", "arrow" (a metaphor)
- We want to represent different roles of a word in the sentence: need more than a single embedding
- Instantiation: multiple self-attention modules



• Multiple attention modules: same architecture, different parameters



- Multiple attention modules: same architecture, different parameters
- A **head**: one set of attention outputs



- Multiple attention modules: same architecture, different parameters
- A head: one set of attention outputs
- Concatenate all heads (increased output dimension)
- Linear projection to produce the final output

Matrix representation: input mapping

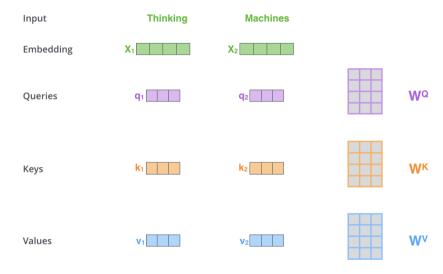


Figure: From The Illustrated Transformer

Matrix representation: attention weights

Scaled dot product attention

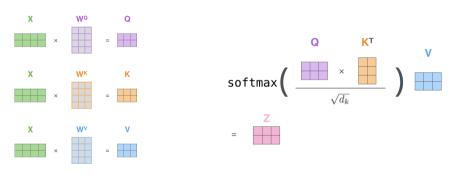


Figure: From The Illustrated Transformer

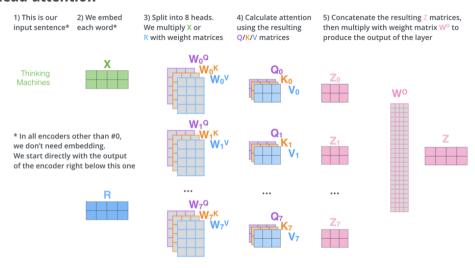


Figure: From The Illustrated Transformer

Summary so far

- Sequence modeling
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Which of these can handle sequences of arbitrary length?

Table of Contents

Neural networks basics

Recurrent neural networks

Self-attention

Tranformer

Overview

- Use self-attention as the core building block
- Vastly increased scalability (model and data size) compared to recurrence-based models
- Initially designed for machine translation (next week)
 - Attention is all you need. Vaswani et al., 2017.
- The backbone of today's large-scale models
- Extended to non-sequential data (e.g., images and molecules)

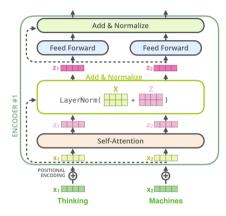


Figure: From The Illustrated Transformer

Multi-head self-attention

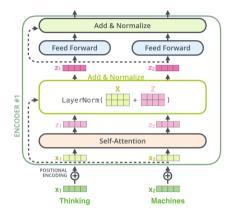


Figure: From The Illustrated Transformer

- Multi-head self-attention
 - Capture dependence among input symbols

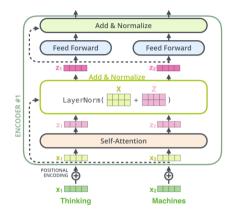


Figure: From The Illustrated Transformer

- Multi-head self-attention
 - Capture dependence among input symbols
- Positional encoding

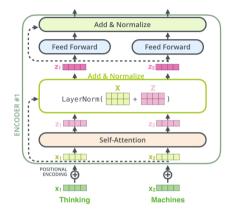


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- Multi-head self-attention
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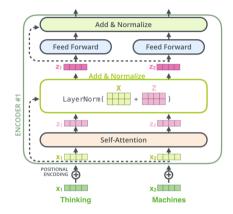


Figure: From The Illustrated Transformer

- Multi-head self-attention
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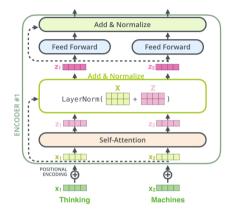
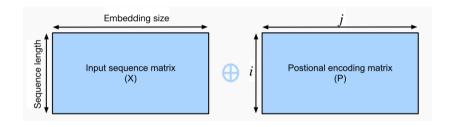


Figure: From The Illustrated Transformer

- Multi-head self-attention
 - Capture dependence among input symbols
- Positional encoding
 - Capture the order of symbols
- Residual connection and layer normalization
 - More efficient and better optimization

Position embedding

Motivation: model word order in the input sequence Solution: add a position embedding to each word



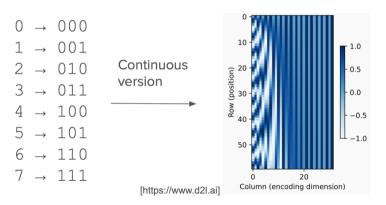
Position embedding:

- Encode absolute and relative positions of a word
- (Same dimension as word embeddings)
- Learned or deterministic

Sinusoidal position embedding

Intuition: binary encoding

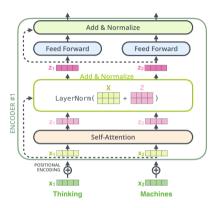
- The frequency of bit flips increases from left to right



Col 1: $sin(w_1t)$ Col 2: $cos(w_1t)$ Col 3: $sin(w_2t)$ Col 4: $cos(w_2t)$

w_i: frequency t: position

Residual connection and layer normalization



- Residual connection: add input to the output of each layer
- Layer normalization: normalize (zero mean, unit variance) over all features for each sample in the batch
- Position-wise feed-forward networks: same mapping for all positions