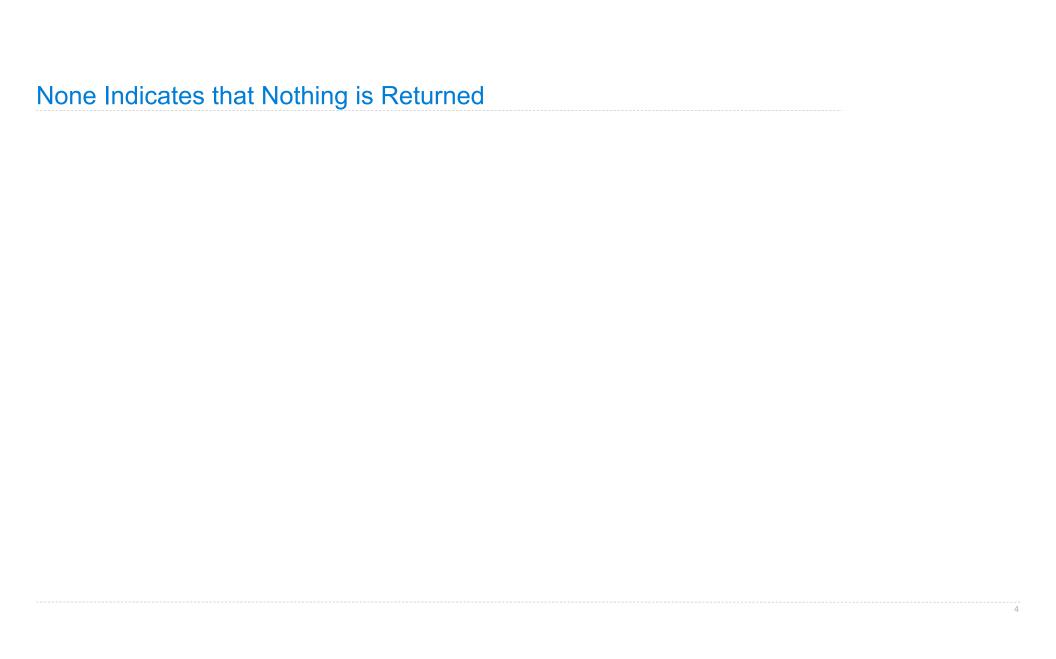




Print and None

(Demo)



| None | Indicates | that | Nothing | is | Returned |
|------|-----------|------|---------|----|----------|
|------|-----------|------|---------|----|----------|

The special value None represents nothing in Python

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Pure Functions
just return values

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abs

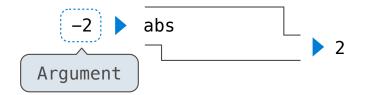
Pure Functions
just return values

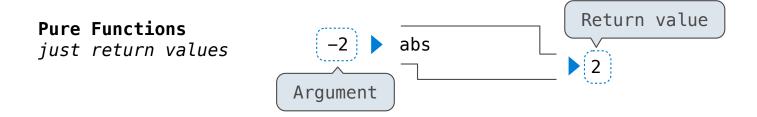


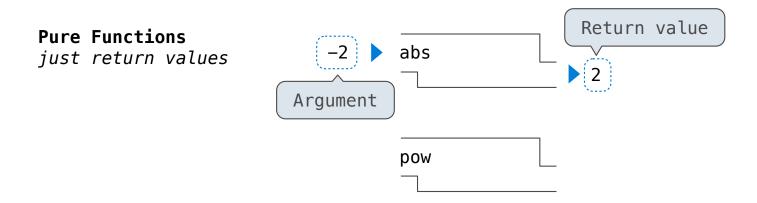
Pure Functions
just return values

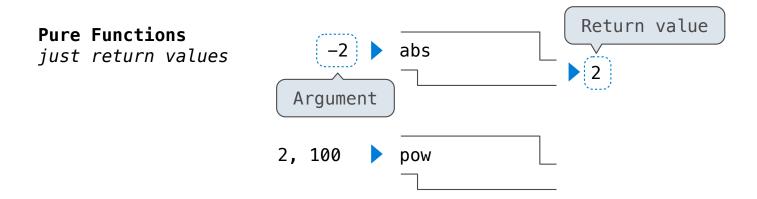


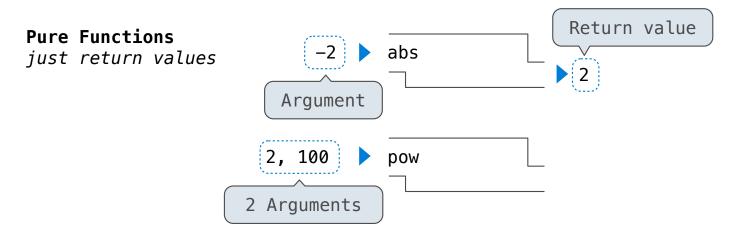
Pure Functions just return values

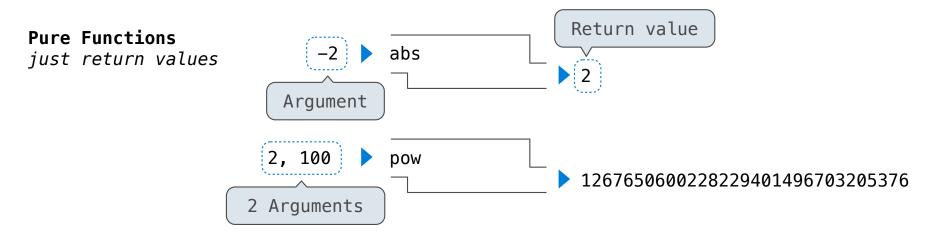


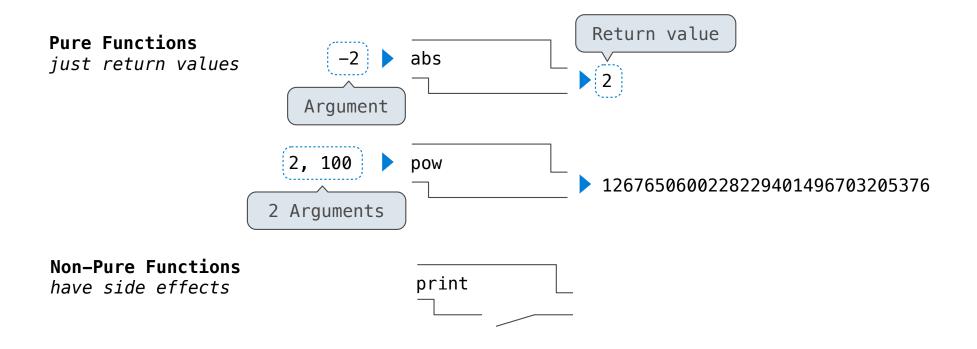


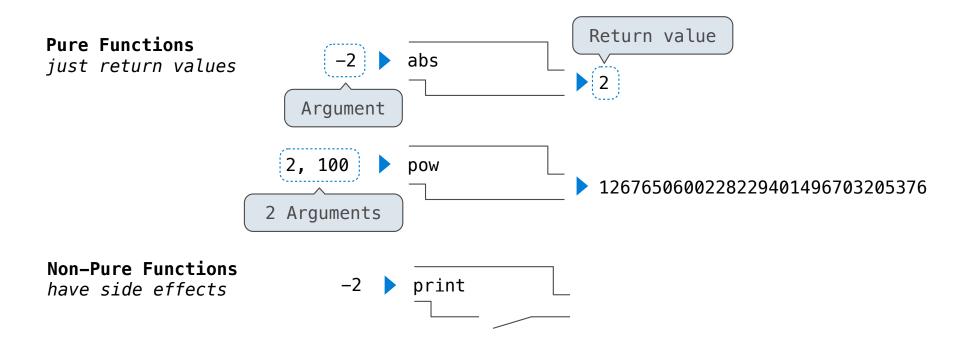


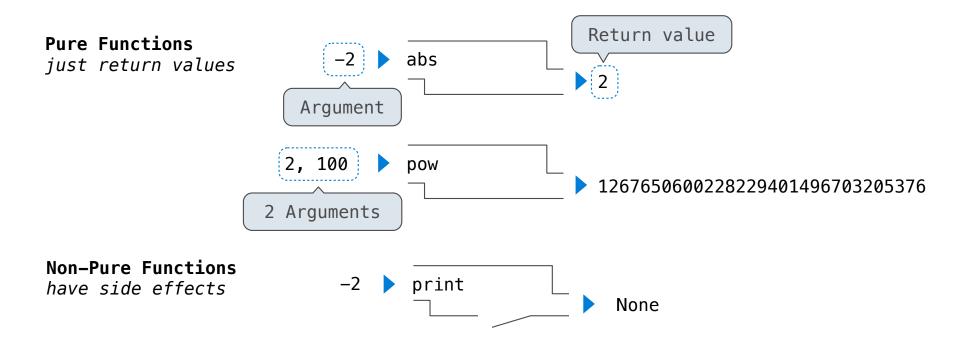


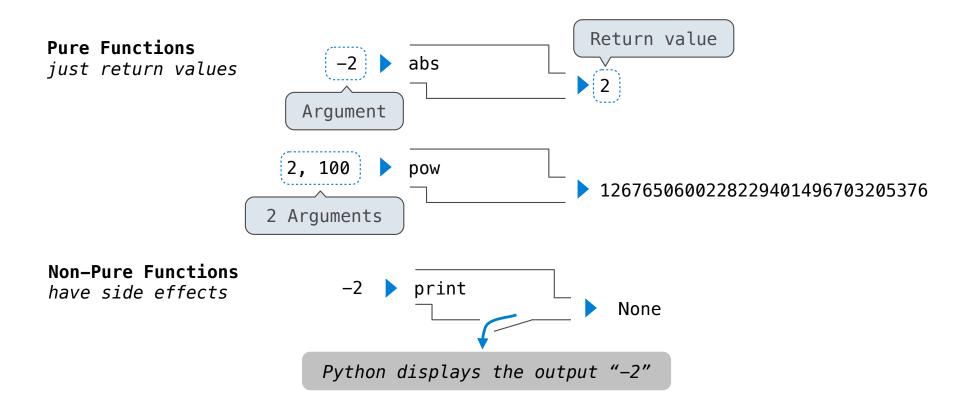


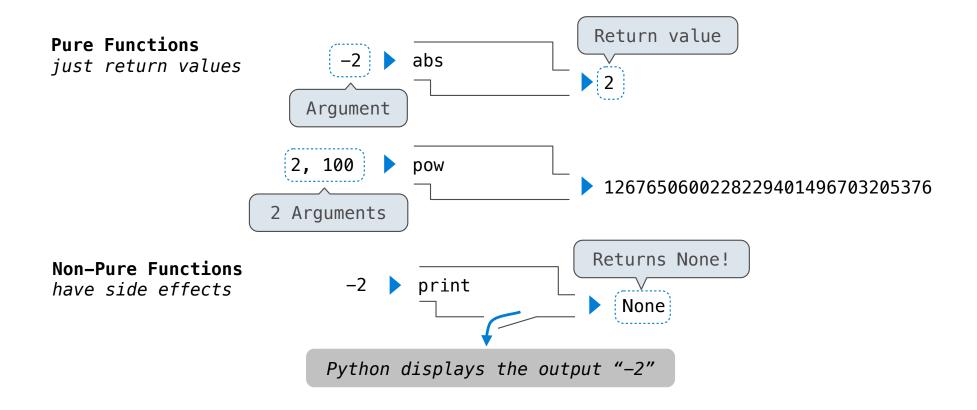


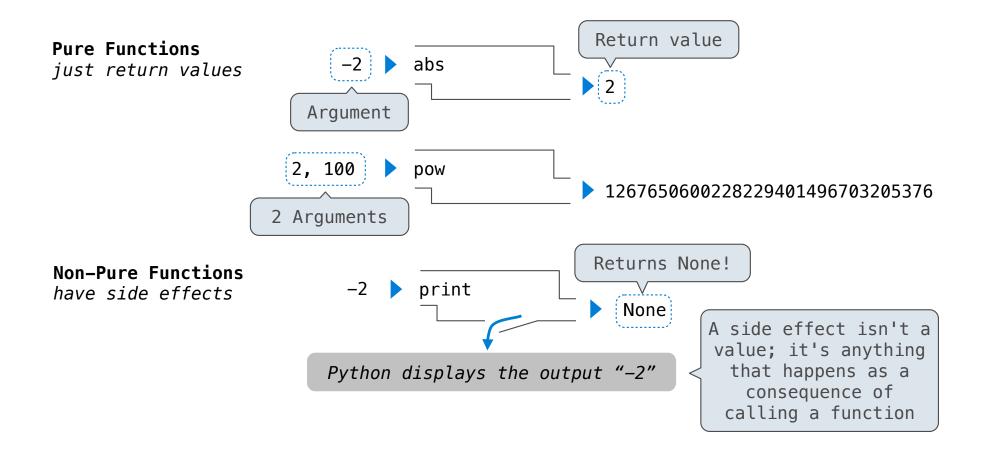












```
>>> print(print(1), print(2))
1
2
None None
```

```
>>> print(print(1), print(2))
1
2
None None
```

print(print(1), print(2))

```
>>> print(print(1), print(2))
1
2
None None
```

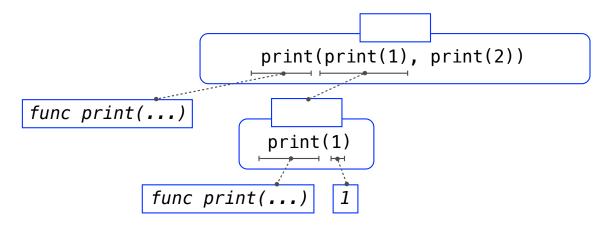
```
print(print(1), print(2))
```

```
>>> print(print(1), print(2))
1
2
None None
```

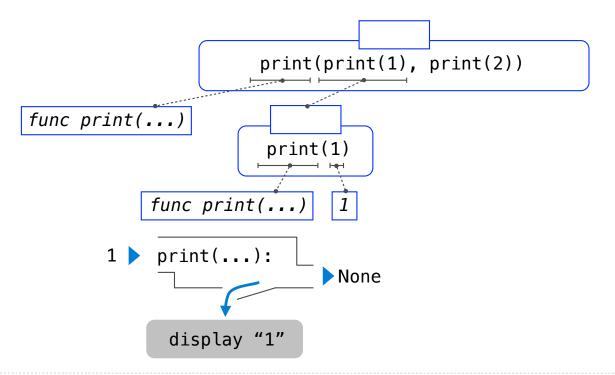
```
print(print(1), print(2))

func print(...)
```

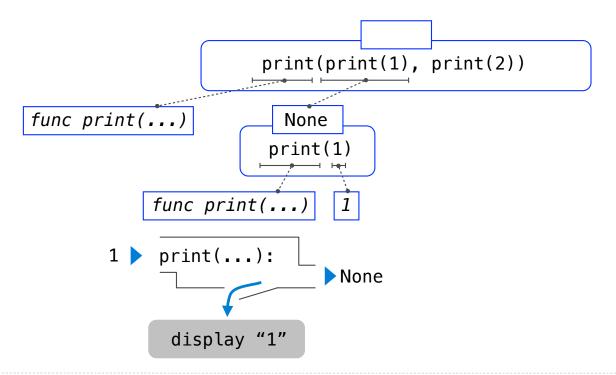
```
>>> print(print(1), print(2))
1
2
None None
```



```
>>> print(print(1), print(2))
1
2
None None
```



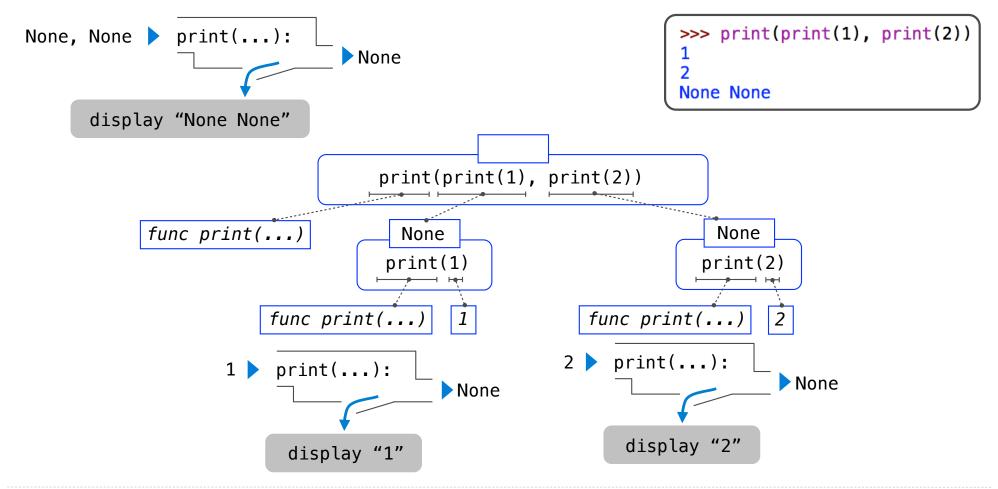
```
>>> print(print(1), print(2))
1
2
None None
```

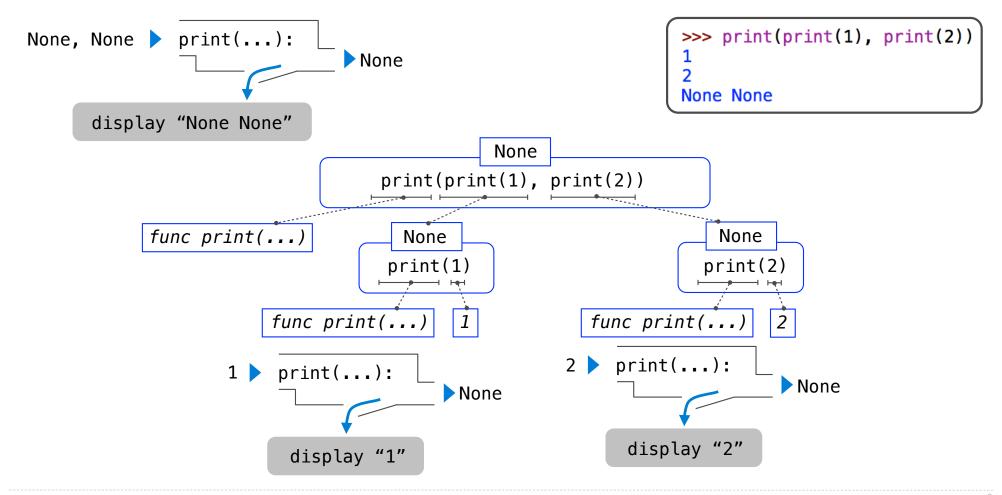


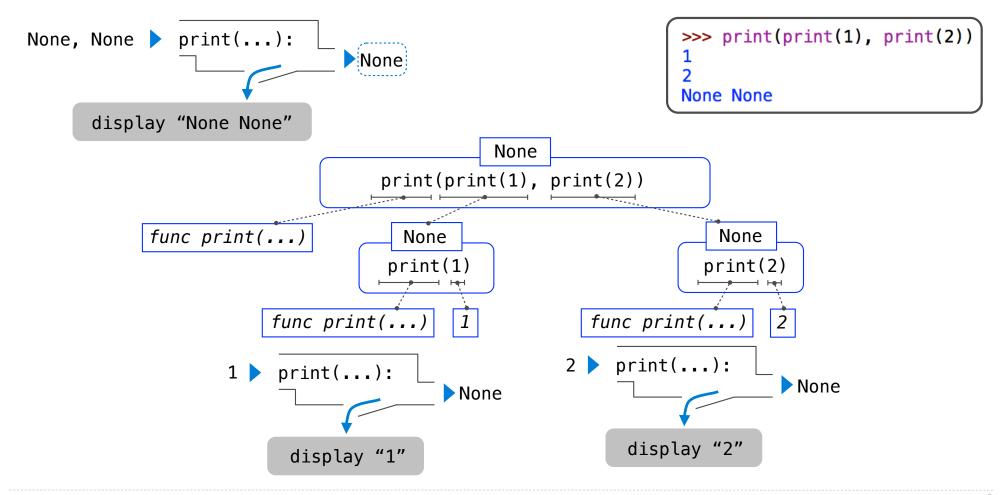
```
>>> print(print(1), print(2))
                                                    None None
                      print(print(1), print(2))
func print(...)
                        None
                                                      print(2)
                       print(1)
           func print(...)
                                           func print(...)
       1 > print(...):
                             None
             display "1"
```

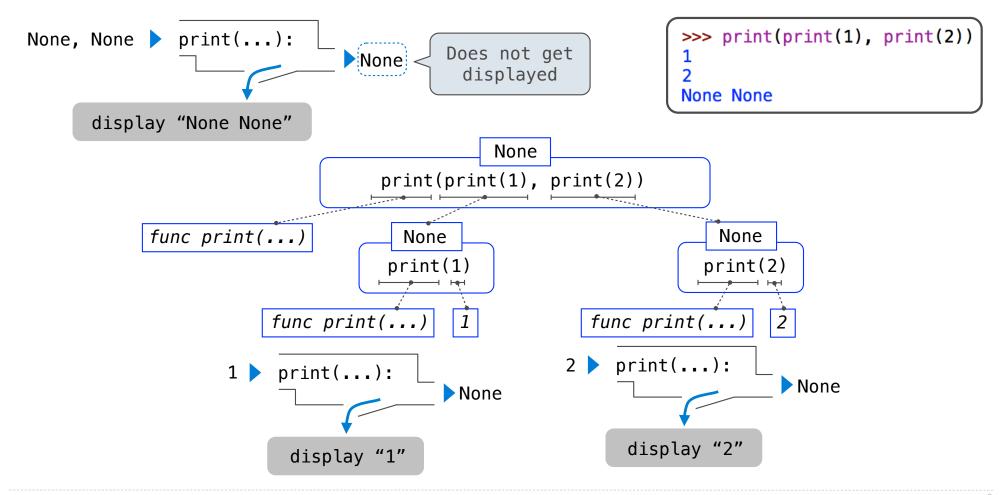
```
>>> print(print(1), print(2))
                                                   None None
                      print(print(1), print(2))
func print(...)
                        None
                                                      print(2)
                       print(1)
           func print(...)
                                           func print(...)
                                             print(...):
       1 > print(...):
                                                             None
                            None
                                              display "2"
             display "1"
```

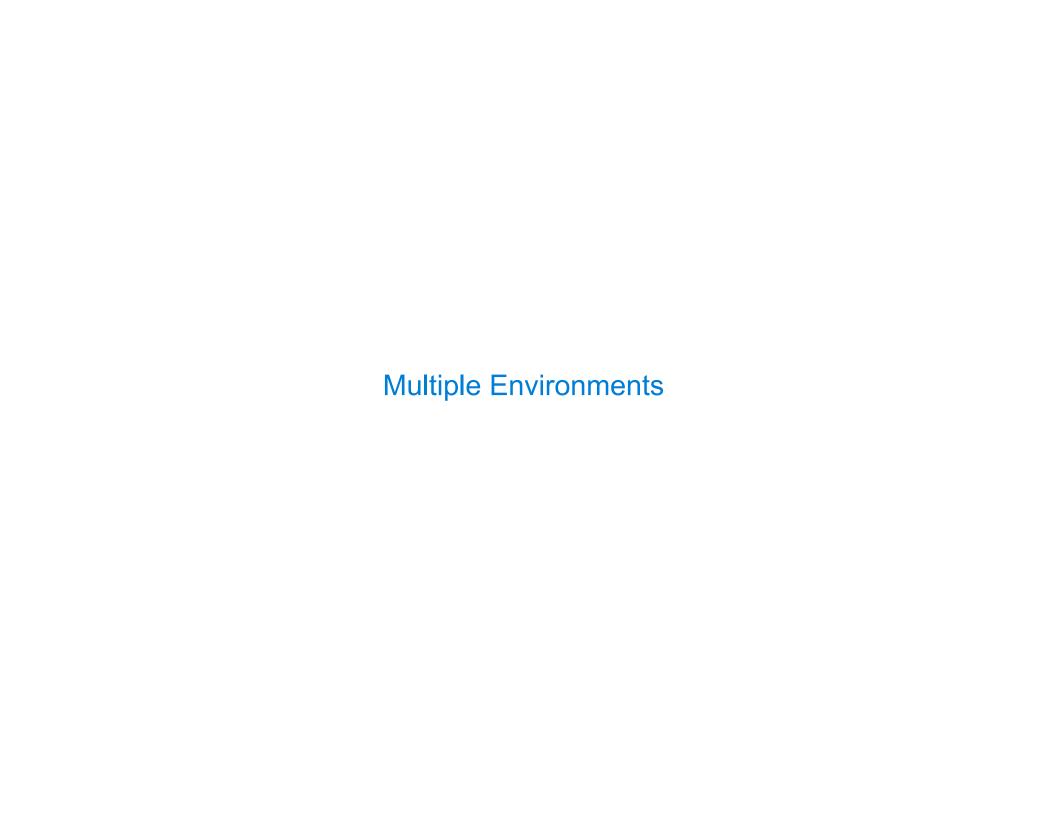
```
>>> print(print(1), print(2))
                                                   None None
                      print(print(1), print(2))
func print(...)
                                                       None
                        None
                       print(1)
                                                      print(2)
           func print(...)
                                           func print(...)
                                             print(...):
       1 > print(...):
                                                             None
                            None
                                              display "2"
             display "1"
```











What happens?

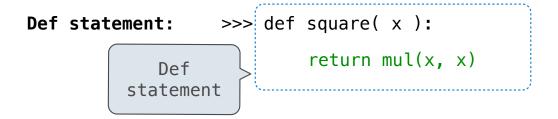
Def statement:

Call expression:

What happens?

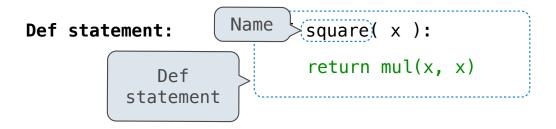
Call expression:

What happens?

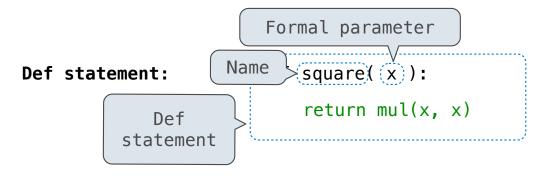


Call expression:

What happens?

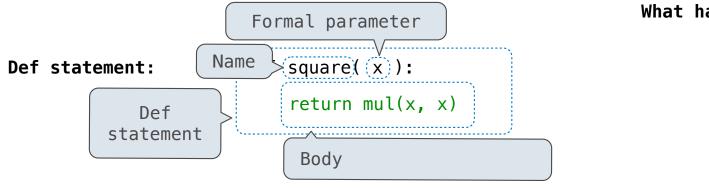


Call expression:



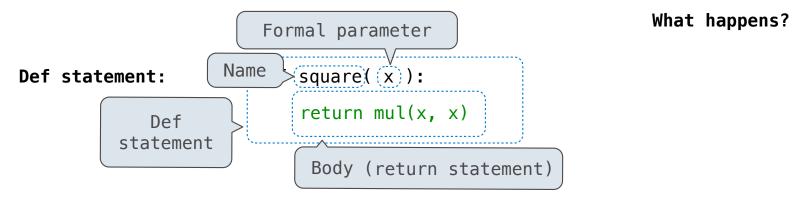
What happens?

Call expression:



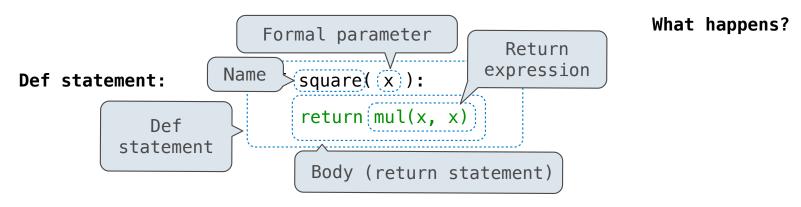
What happens?

Call expression:



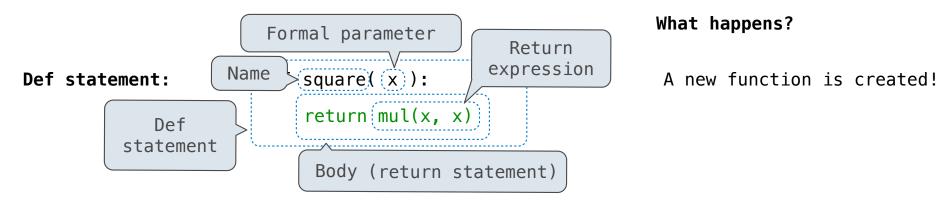
Call expression:

Calling/Applying:



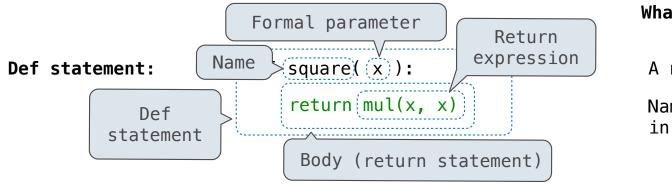
Call expression:

Calling/Applying:



Call expression:

Calling/Applying:

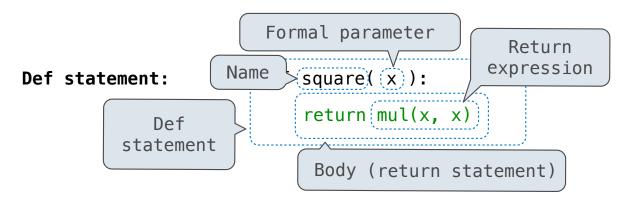


What happens?

A new function is created!

Name bound to that function in the current frame

Call expression:

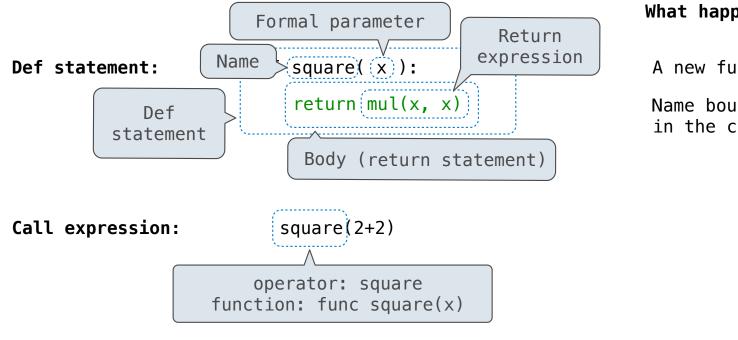


What happens?

A new function is created!

Name bound to that function in the current frame

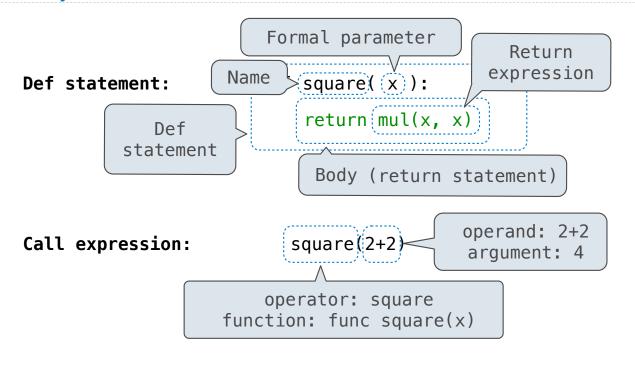
Call expression: square(2+2)



What happens?

A new function is created!

Name bound to that function in the current frame

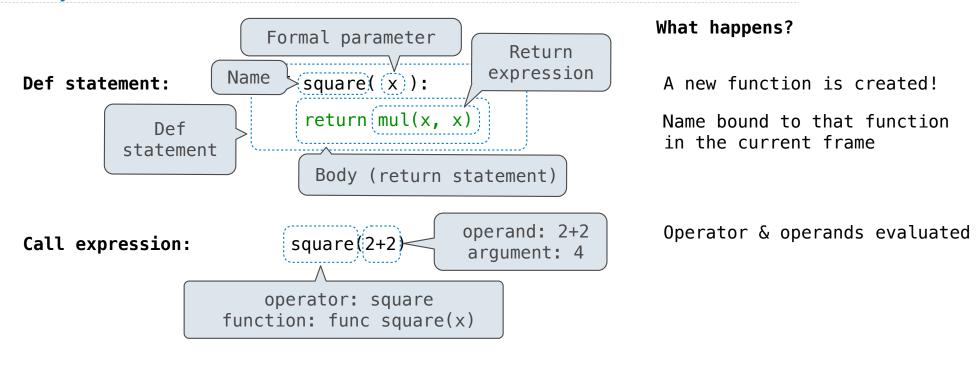


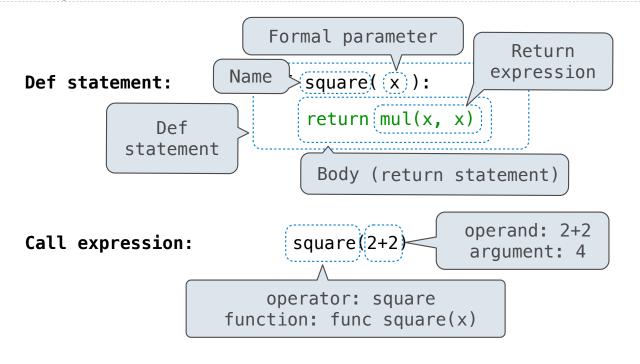
What happens?

A new function is created!

Name bound to that function in the current frame

Calling/Applying:





What happens?

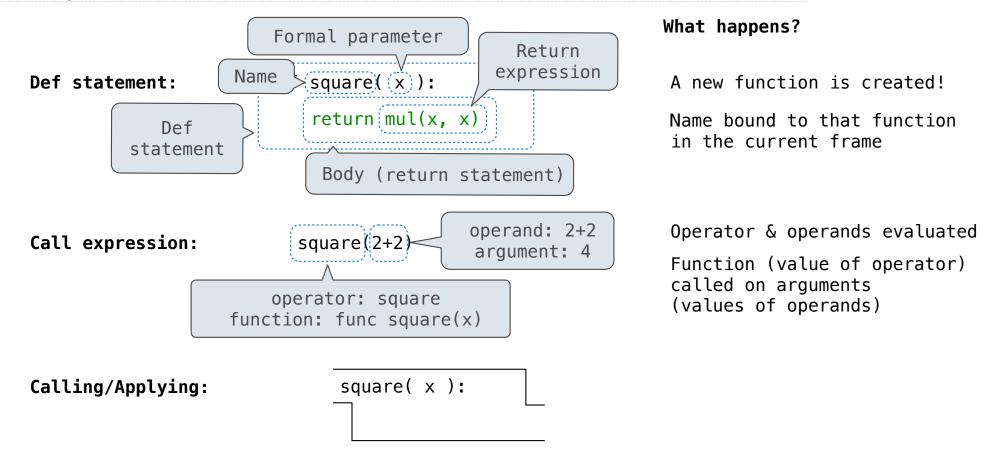
A new function is created!

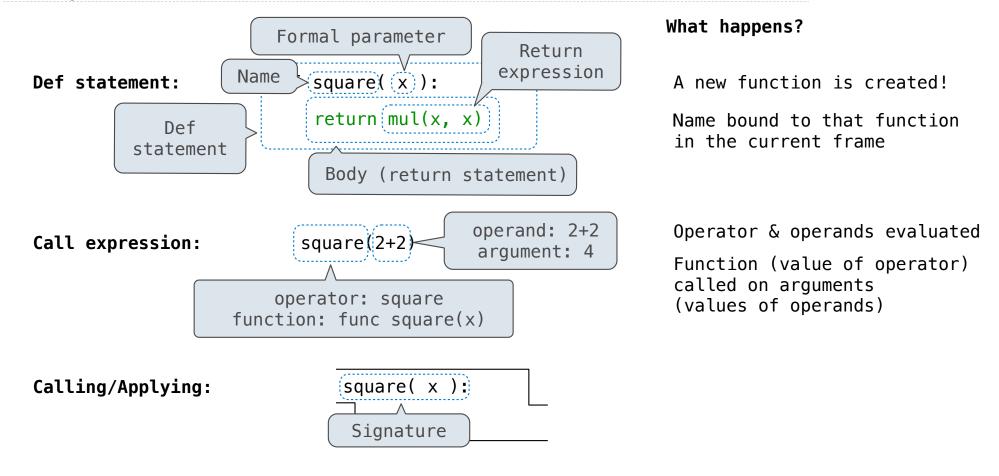
Name bound to that function in the current frame

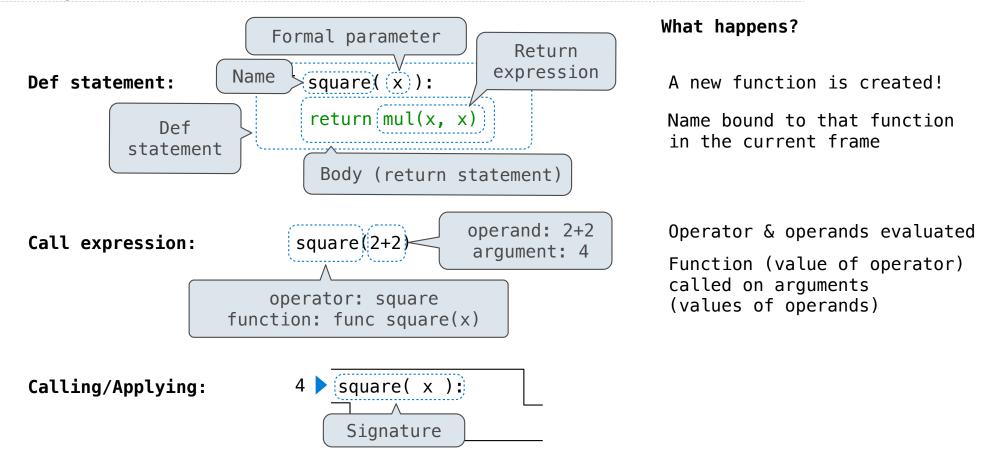
Operator & operands evaluated Function (value of operator) called on arguments

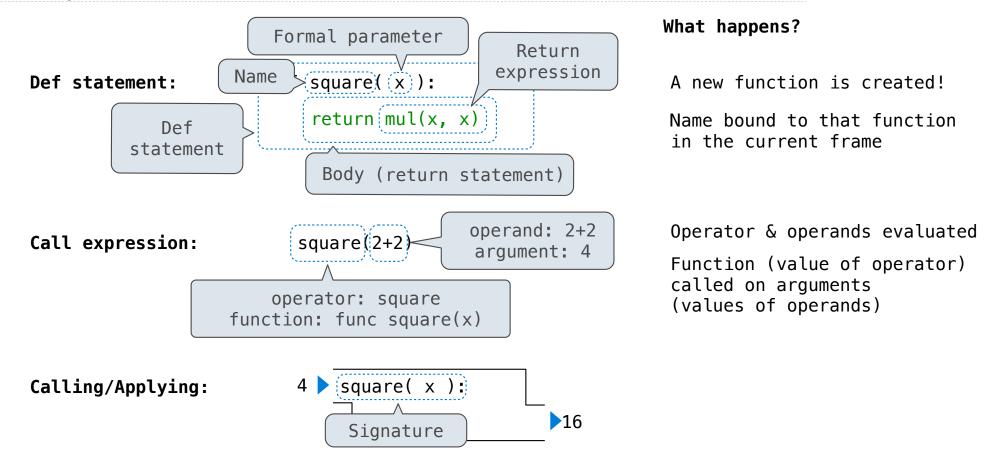
(values of operands)

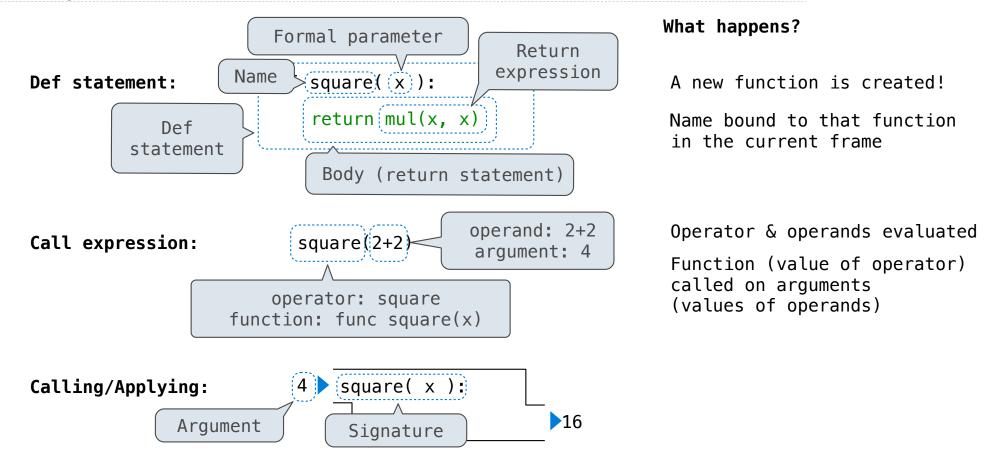
Calling/Applying:

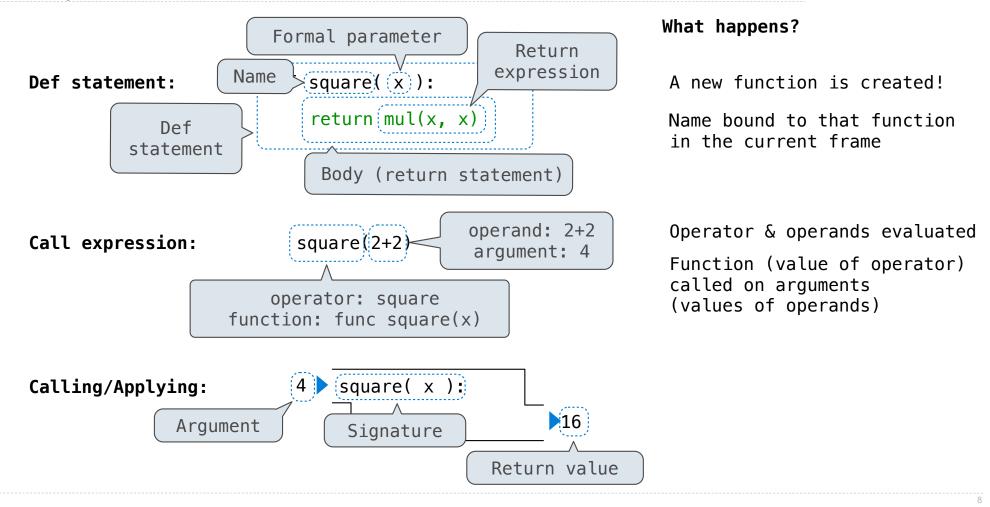


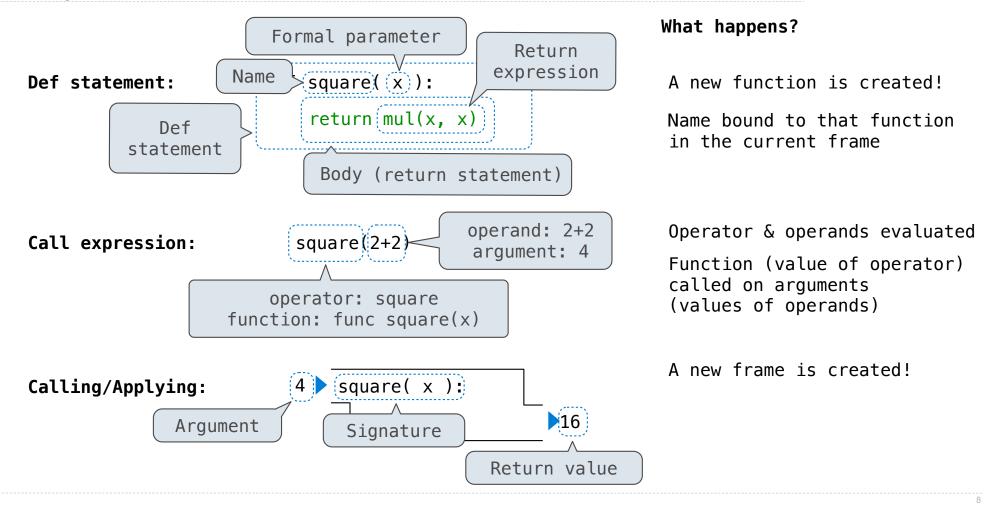


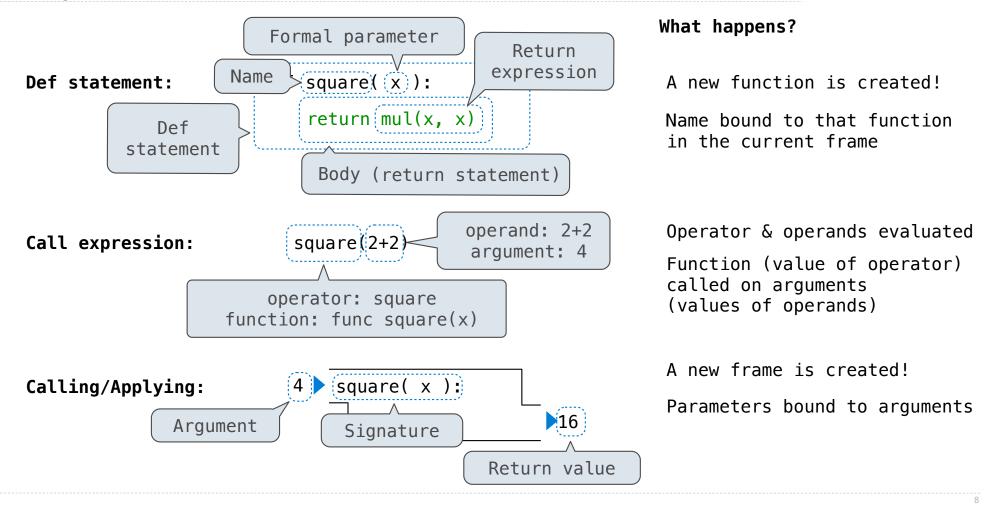


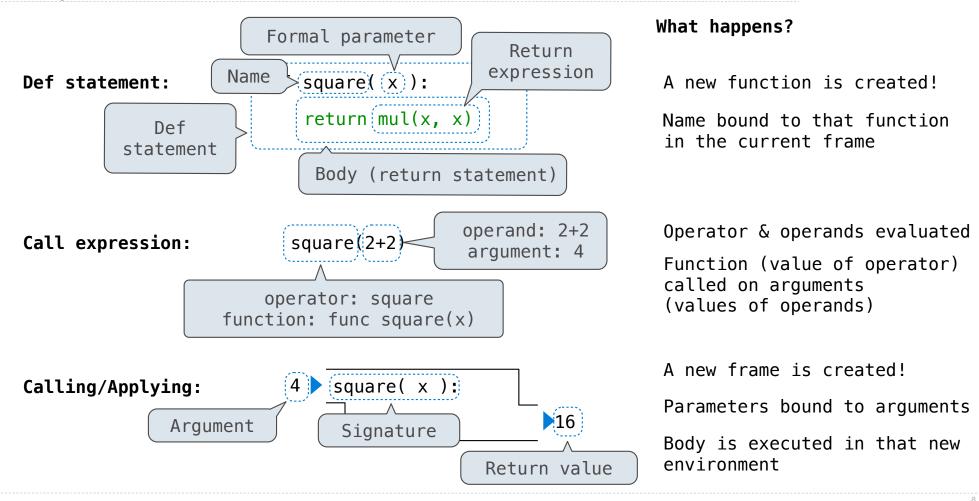


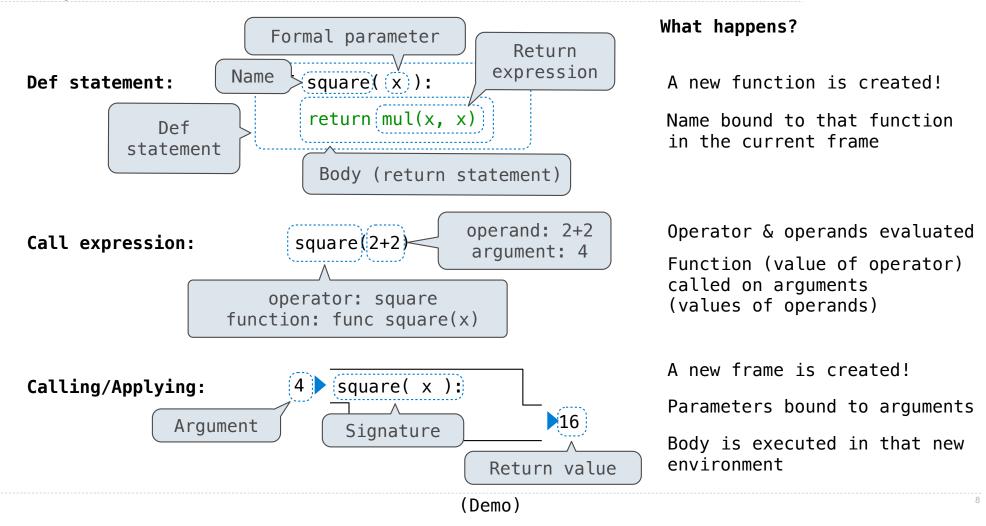












Multiple Environments in One Diagram!

```
1 from operator import mul

→ 2 def square(x):
3    return mul(x, x)

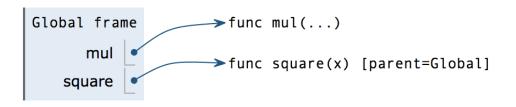
→ 4 square(square(3))
```

Multiple Environments in One Diagram!

```
1 from operator import mul

→ 2 def square(x):
3    return mul(x, x)

→ 4 square(square(3))
```



```
1 from operator import mul

→ 2 def square(x):
3 return mul(x, x)

→ 4 square(square(3))
```

```
Global frame

func mul(...)

mul

func square(x) [parent=Global]

square
```

square(square(3))

orograms.js&py=3&rawInputLstJSON=%5B%5D

```
1 from operator import mul

→ 2 def square(x):
3 return mul(x, x)

→ 4 square(square(3))
```

```
Global frame

func mul(...)

mul

func square(x) [parent=Global]

square
```

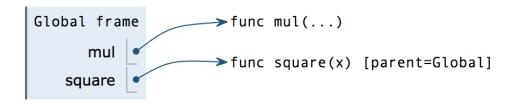
square(square(3))

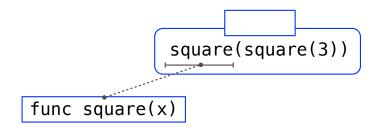
rams.js&py=3&rawInputLstJSON=%5B%5D

```
1 from operator import mul

→ 2 def square(x):
3 return mul(x, x)

→ 4 square(square(3))
```

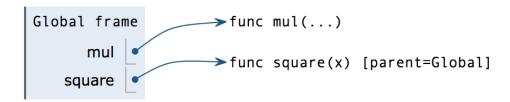


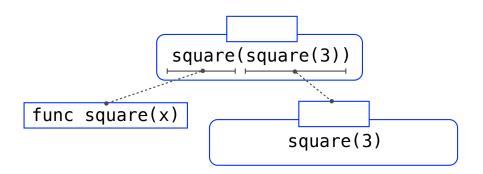


```
1 from operator import mul

→ 2 def square(x):
3 return mul(x, x)

→ 4 square(square(3))
```



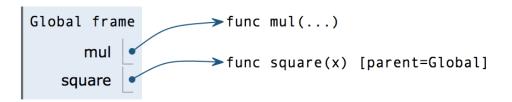


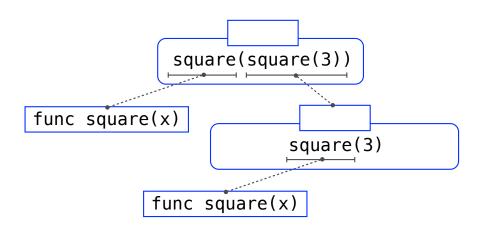
to://orthontutor.com/comoosinoorograms.html@code=fromP2@operator92@imoort%2@mul%akdef%2@suuare%2@sv2993A%akAk2@%2@%2@returm%2@mul%akdef%2@suuare%2@svuare%2@suuare%2@

```
1 from operator import mul

→ 2 def square(x):
3    return mul(x, x)

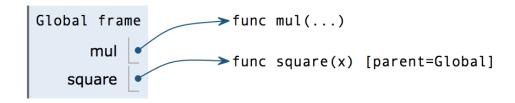
→ 4 square(square(3))
```

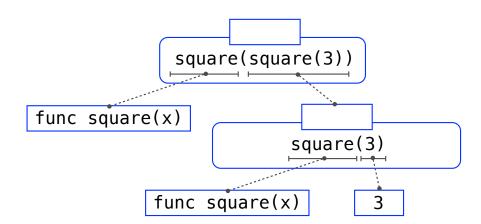




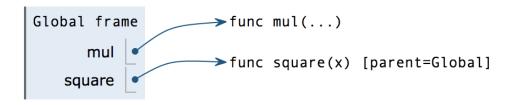
://oythontutor.com/composingerograms.html@code=from%2@operator%2@inmort%2@mul%8Adef%2@square%2&x2%3A%8Ade2@%2@returm%2@mul%2&x.42%%2%8Assquare%2&sq

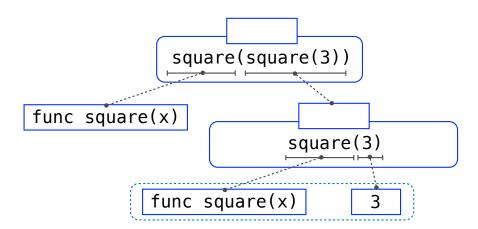
```
1 from operator import mul
→ 2 def square(x):
3    return mul(x, x)
→ 4 square(square(3))
```





```
1 from operator import mul
→ 2 def square(x):
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```





```
1 from operator import mul
→ 2 def square(x):
→ 3 return mul(x, x)
4 square(square(3))
```

```
Global frame

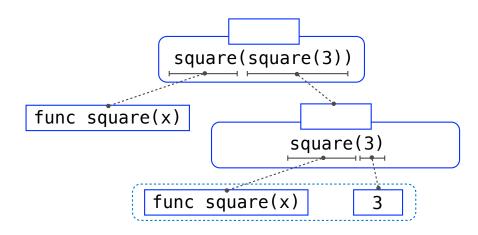
mul

func mul(...)

func square(x) [parent=Global]

f1: square [parent=Global]

x 3
```



```
1 from operator import mul

→ 2 def square(x):
→ 3 return mul(x, x)
4 square(square(3))
```

```
Global frame

mul

mul

square

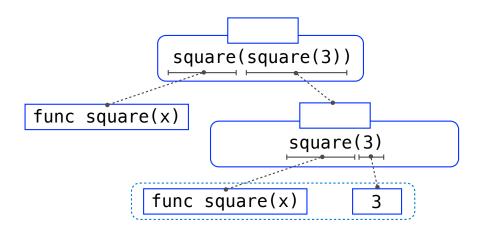
func mul(...)

func square(x) [parent=Global]

x 3

Return
value

yalue
```



```
1 from operator import mul

→ 2 def square(x):

→ 3 return mul(x, x)

4 square(square(3))
```

```
Global frame

mul

mul

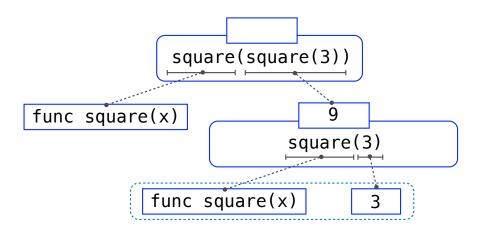
func mul(...)

func square(x) [parent=Global]

f1: square [parent=Global]

x 3

Return
value 9
```



```
1 from operator import mul

→ 2 def square(x):

→ 3 return mul(x, x)

4 square(square(3))
```

```
Global frame

mul
square

func mul(...)

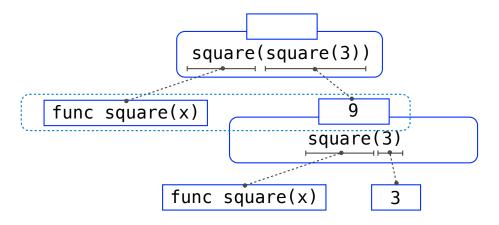
func square(x) [parent=Global]

x 3

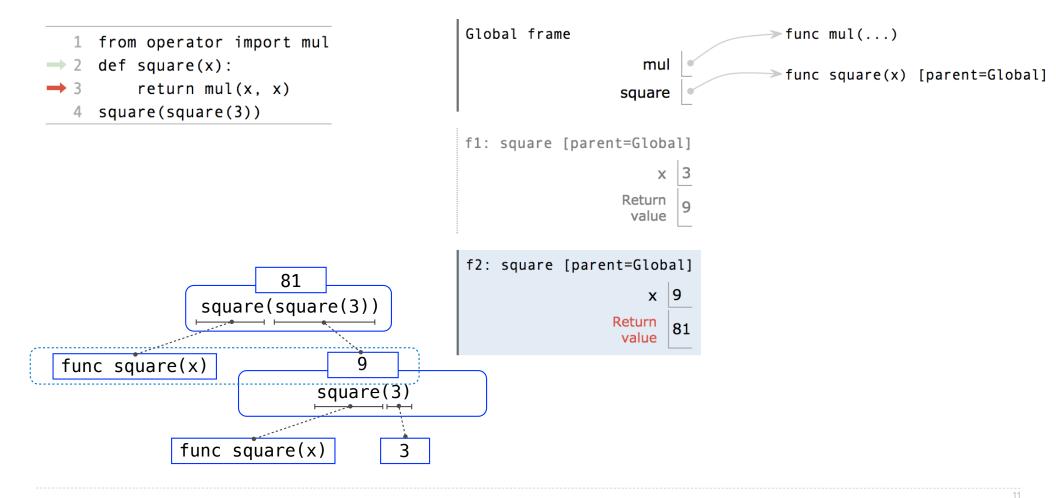
Return
value

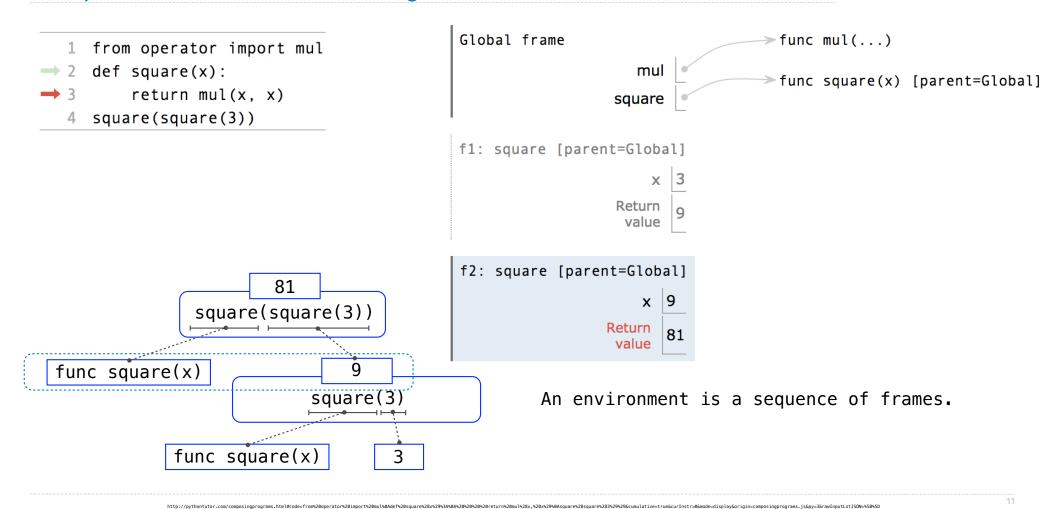
func mul(...)

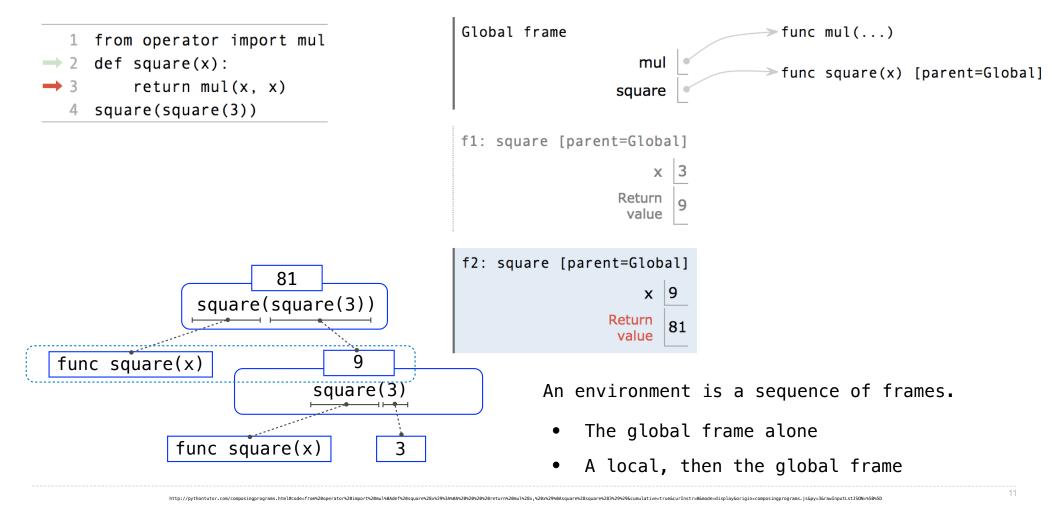
func square(x) [parent=Global]
```

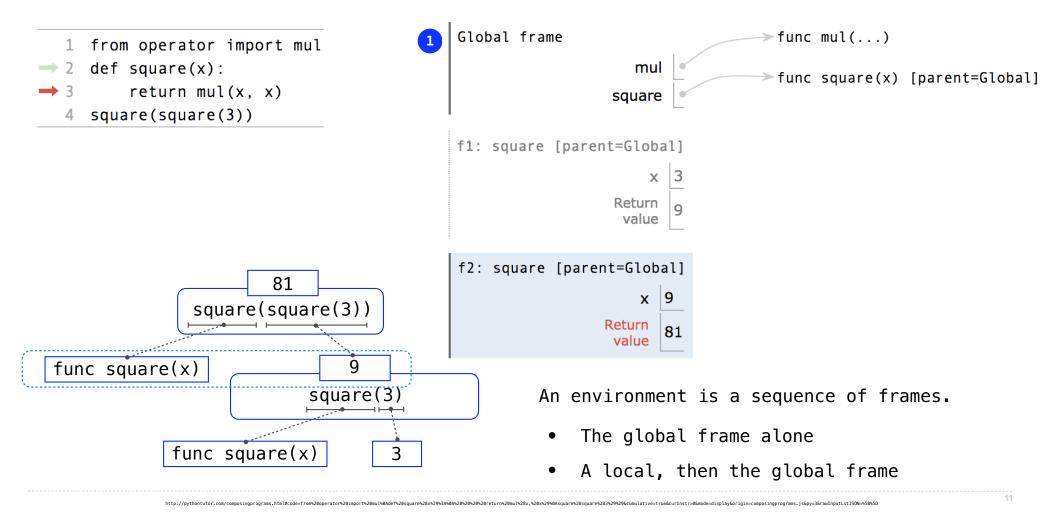


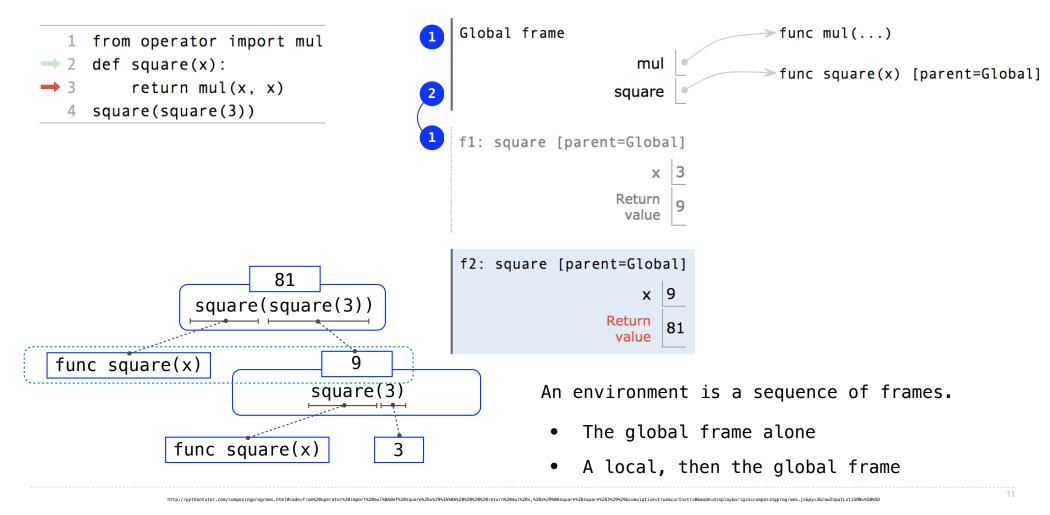
10

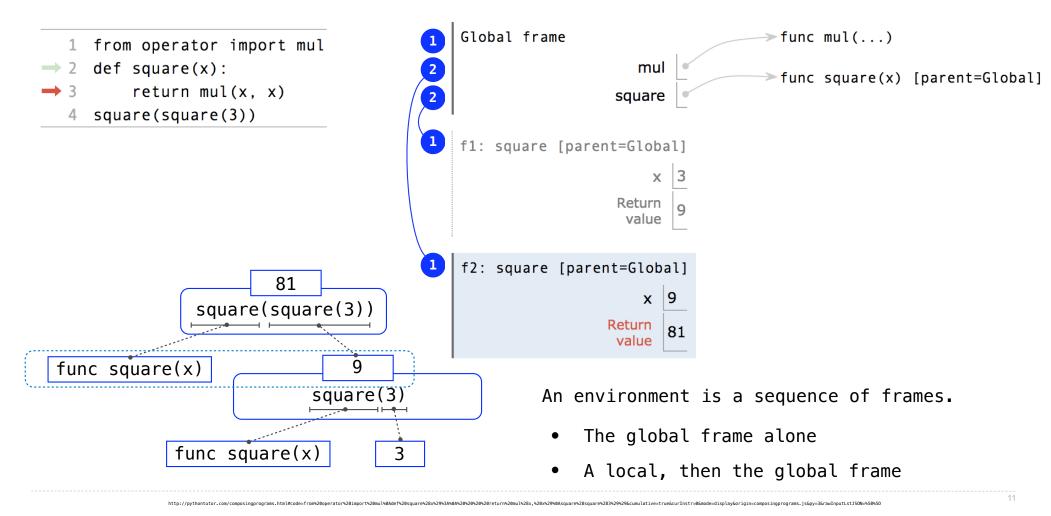






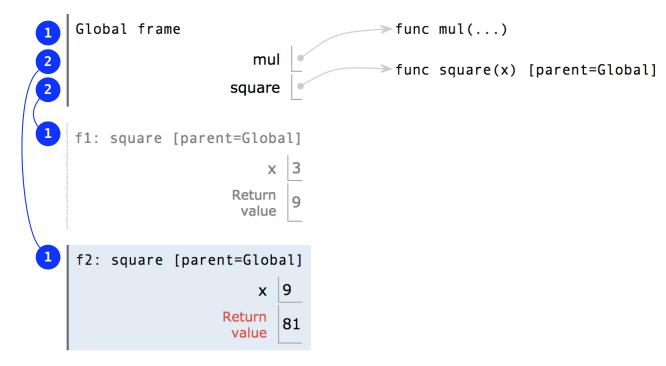






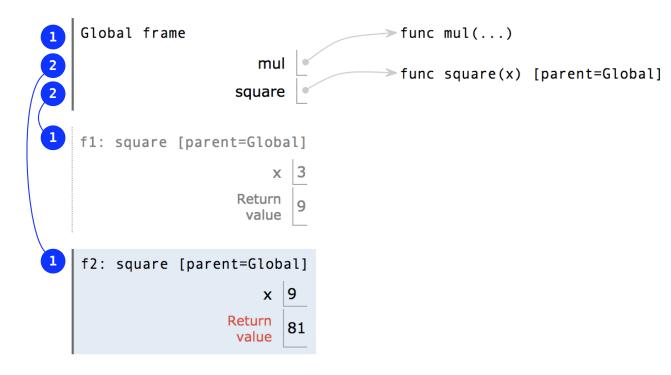
```
1 from operator import mul

→ 2 def square(x):
→ 3 return mul(x, x)
4 square(square(3))
```



- The global frame alone
- A local, then the global frame

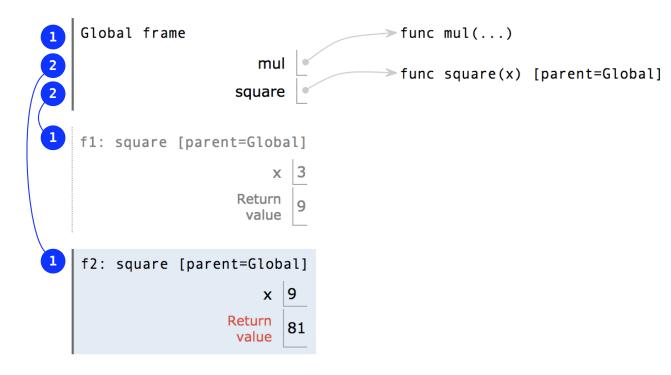
Every expression is evaluated in the context of an environment.



- The global frame alone
- A local, then the global frame

Every expression is evaluated in the context of an environment.

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.



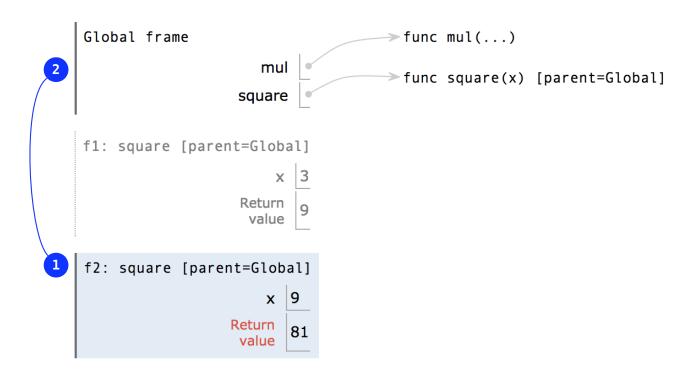
- The global frame alone
- A local, then the global frame

```
1 from operator import mul

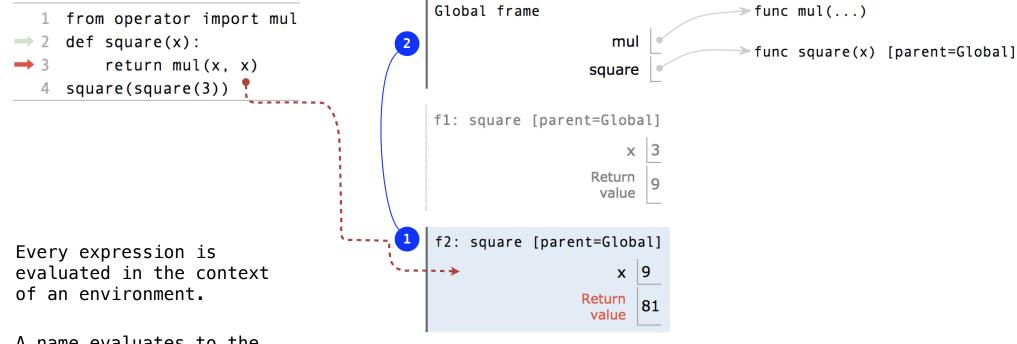
→ 2 def square(x):
→ 3 return mul(x, x)
4 square(square(3))
```

Every expression is evaluated in the context of an environment.

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

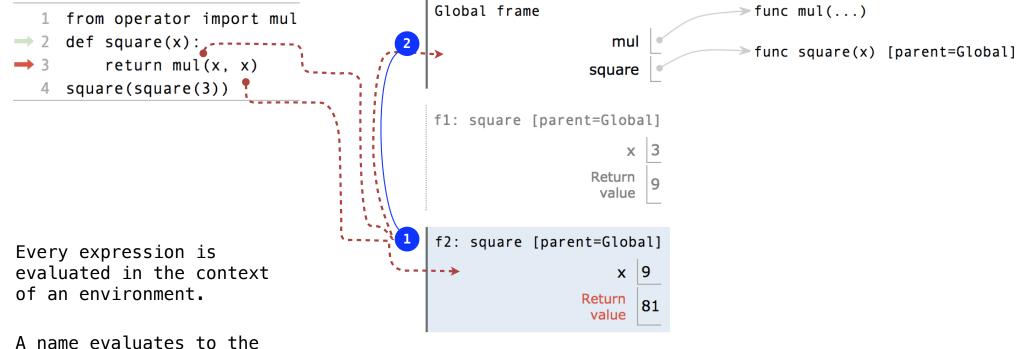


- The global frame alone
- A local, then the global frame



A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

- The global frame alone
- A local, then the global frame



A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

- The global frame alone
- A local, then the global frame

Every expression is evaluated in the context of an environment.

A call expression and the body of the function being called are evaluated in different environments

Every expression is evaluated in the context of an environment.

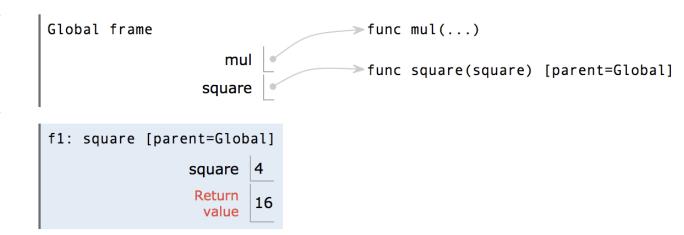
A call expression and the body of the function being called are evaluated in different environments

- 1 from operator import mul
- 2 def square(square):
- 3 return mul(square, square)
- 4 square(4)

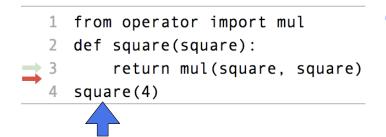
Every expression is evaluated in the context of an environment.

A call expression and the body of the function being called are evaluated in different environments

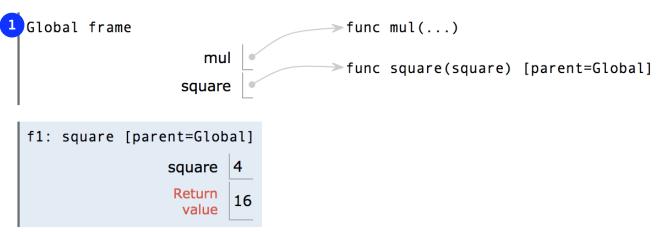
- 1 from operator import mul
 2 def square(square):
 3 return mul(square, square)
 4 square(4)
- Every expression is evaluated in the context of an environment.



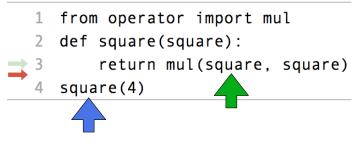
A call expression and the body of the function being called are evaluated in different environments



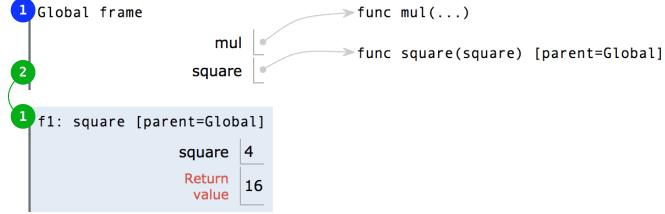
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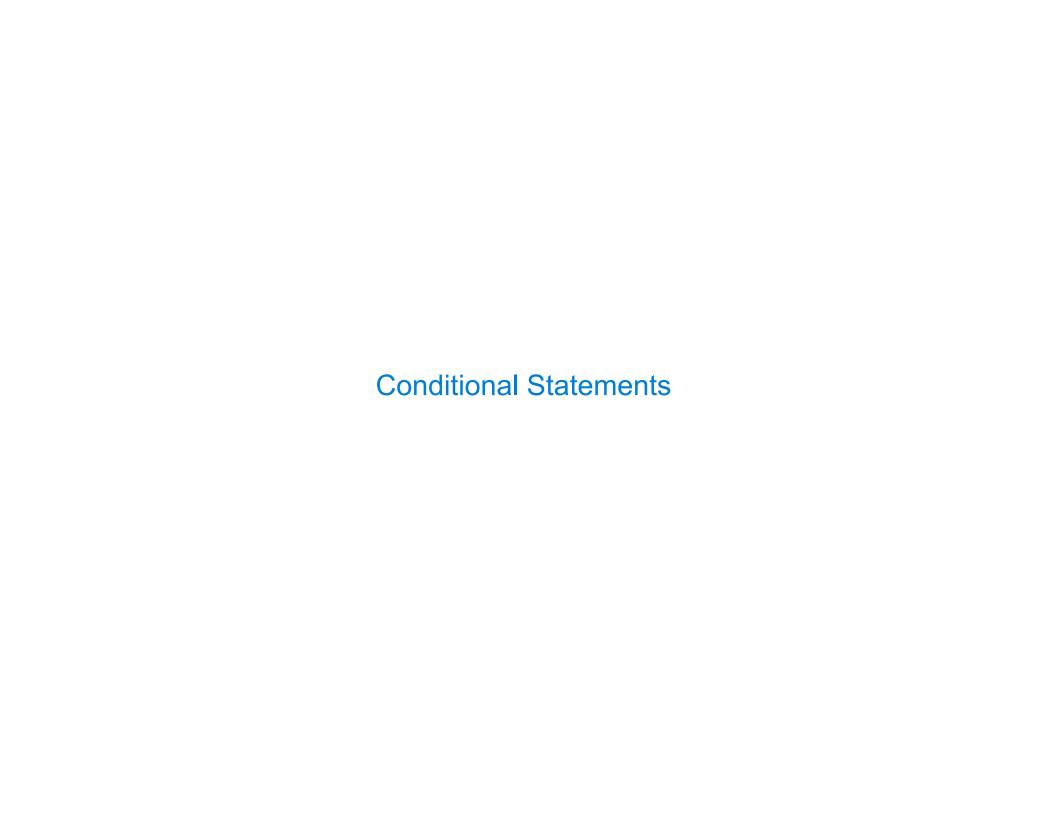
Every expression is evaluated in the context of an environment.



Miscellaneous Python Features

Division
Multiple Return Values
Source Files
Doctests
Default Arguments

(Demo)



A **statement** is executed by the interpreter to perform an action

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Compound statements:

16

A **statement** is executed by the interpreter to perform an action

Compound statements:

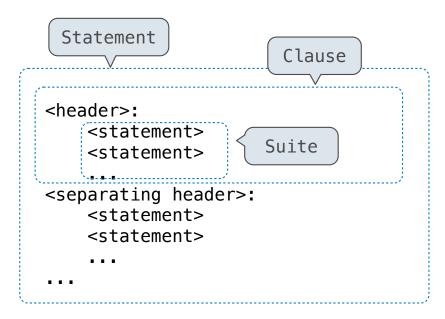
16

A **statement** is executed by the interpreter to perform an action

Compound statements:

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Compound statements:

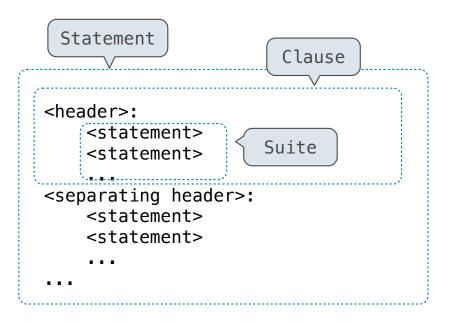


16

Statements

A **statement** is executed by the interpreter to perform an action

Compound statements:

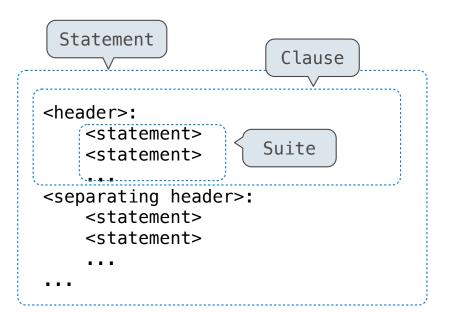


The first header determines a statement's type

Statements

A **statement** is executed by the interpreter to perform an action

Compound statements:



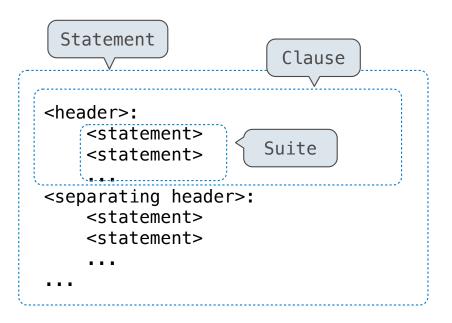
The first header determines a statement's type

The header of a clause "controls" the suite that follows

Statements

A **statement** is executed by the interpreter to perform an action

Compound statements:



The first header determines a statement's type

The header of a clause "controls" the suite that follows

def statements are compound
statements

Compound statements:

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A suite is a sequence of statements

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To "execute" a suite means to execute its sequence of statements, in order

Compound statements:

A suite is a sequence of statements

To "execute" a suite means to execute its sequence of statements, in order

Execution Rule for a sequence of statements:

- Execute the first statement
- Unless directed otherwise, execute the rest

```
def absolute_value(x):
    """Return the absolute value of x."""
    if x < 0:
        return -x
    elif x == 0:
        return 0
    else:
        return x</pre>
```

```
def absolute_value(x):
    """Return the absolute value of x."""

if x < 0:
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elif x == 0:
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18

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Execution Rule for Conditional Statements:

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def absolute_value(x):
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if x < 0:
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```

Execution Rule for Conditional Statements:

Each clause is considered in order.

- 1. Evaluate the header's expression.
- 2. If it is a true value, execute the suite & skip the remaining clauses.

```
def absolute_value(x):
    """Return the absolute value of x."""

if x < 0:
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```

Execution Rule for Conditional Statements:

Syntax Tips:

Each clause is considered in order.

- 1. Evaluate the header's expression.
- 2. If it is a true value, execute the suite & skip the remaining clauses.

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```

Execution Rule for Conditional Statements:

Each clause is considered in order.

- 1. Evaluate the header's expression.
- If it is a true value, execute the suite & skip the remaining clauses.

Syntax Tips:

- 1. Always starts with "if" clause.
- 2. Zero or more "elif" clauses.
- 3. Zero or one "else" clause, always at the end.



George Boole

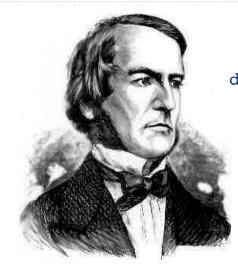
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George Boole

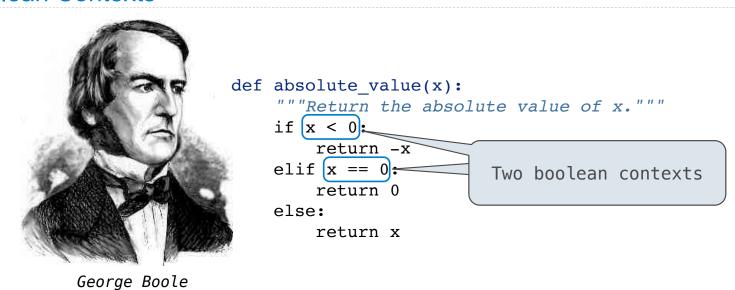
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```

20

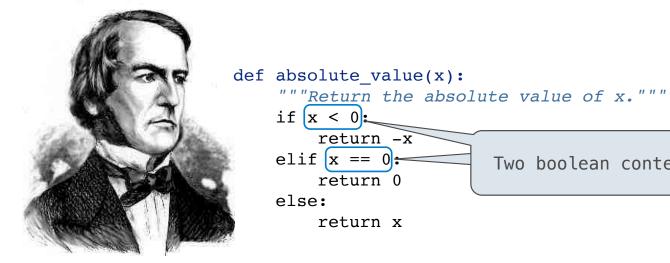


George Boole

```
def absolute_value(x):
    """Return the absolute value of x."""
    if (x < 0):
        return -x
    elif (x == 0):
        return 0
    else:
        return x</pre>
```



False values in Python: False, 0, '', None



George Boole

False values in Python: False, 0, '', None (more to come)

Two boolean contexts

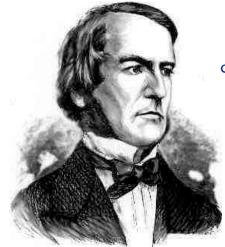


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George Boole

False values in Python: False, 0, '', None (more to come)

True values in Python: Anything else (True)



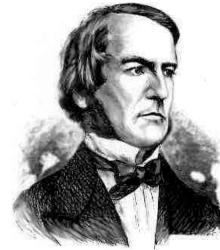
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George Boole

False values in Python: False, 0, '', None (more to come)

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Read Section 1.5.4!



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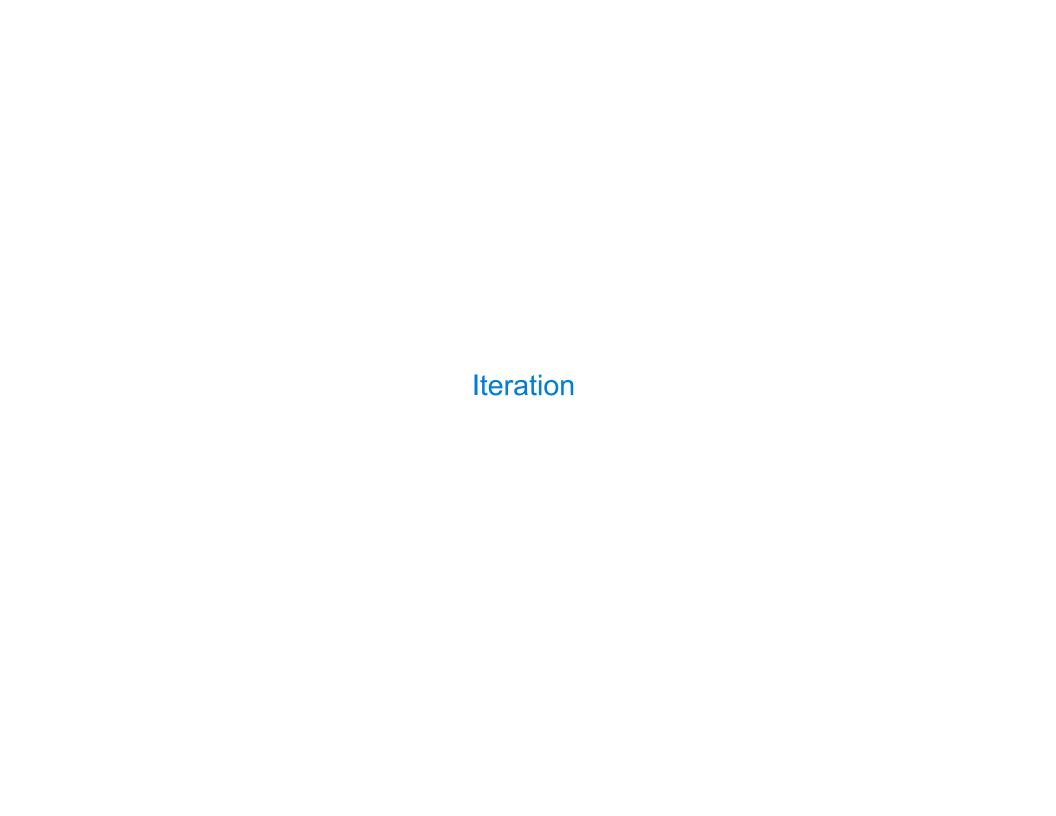
George Boole

False values in Python: False, 0, '', None (more to come)

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Read Section 1.5.4!

(Demo)



(Demo)

(Demo)

```
1 i, total = 0, 0
2 while i < 3:
3         i = i + 1
4         total = total + i</pre>
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George Boole

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(Demo)

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```

```
Global frame
i 0
total 0
```

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George Boole

(Demo)

```
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4         total = total + i</pre>
```

```
Global frame
i 🕱 1
total 0
```

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George Boole

(Demo)

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George Boole

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George Boole

(Demo)

```
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2 while i < 3:
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```

```
Global frame
i 🕱 🛣 2
total 🕱 1
```

- 1. Evaluate the header's expression.
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George Boole

(Demo)

```
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2 while i < 3:
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          total = total + i</pre>
```

```
Global frame

i 🕱 🛣 2

total 🕱 🛣 3
```

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George Boole

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Global frame

i 🗶 🗶 🕱 3

total 🕱 🛣 3
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George Boole

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```
Global frame
i 🕱 🗶 🗶 3
total 🕱 🗶 🗶 6
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George Boole

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total 🕱 🗶 🗶 6
```

Execution Rule for While Statements:

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(Demo)

Example: Prime Factorization

Each positive integer n has a set of prime factors: primes whose product is n

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```
8 = 2 * 2 * 2
9 = 3 * 3
10 = 2 * 5
11 = 11
12 = 2 * 2 * 3
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One approach: Find the smallest prime factor of n, then divide by it

858

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$$858 = 2 * 429 = 2 * 3 * 143$$

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$$858 = 2 * 429 = 2 * 3 * 143 = 2 * 3 * 11 * 13$$

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(Demo)